

# XCPC Template Library

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## 第 1 部分 图论 Graph

### 1.1 connectivity

#### 1.1.1 bcc

edge.cpp

---

```
1  #include <cstdio>
2  #include <iostream>
3  #include <vector>
4  using namespace std;
5  const int N = 5e5 + 10, M = 2e6 + 10;
6  int n, m, head[N], tot = 1;
7  struct edge {
8      int v, nxt;
9      bool is_bridge;
10 } e[M << 1];
11 void add(int u, int v) { e[++tot].v = v, e[tot].nxt = head[u], head[u] =
    tot; }
12 int dfn[N], low[N], Time;
13 void tarjan(int u, int edge) {
14     dfn[u] = low[u] = ++Time;
15     for (int i = head[u]; i; i = e[i].nxt) {
16         int v = e[i].v;
17         if (!dfn[v]) {
18             tarjan(v, i), low[u] = min(low[u], low[v]);
19         } else if (i != (edge ^ 1)) low[u] = min(low[u], dfn[v]);
20         if (dfn[u] < low[v]) e[i].is_bridge = e[i ^ 1].is_bridge = true;
21     }
22 }
23 int dc;
24 bool in_dcc[N];
25 vector<int> DCC[N];
26 void dfs(int u, int dc) {
27     in_dcc[u] = true;
28     DCC[dc].push_back(u);
29     for (int i = head[u]; i; i = e[i].nxt) {
30         int v = e[i].v;
31         if (in_dcc[v] || e[i].is_bridge) continue;
32         dfs(v, dc);
```

```

33     }
34 }
35 int main() {
36     ios::sync_with_stdio(false);
37     cin.tie(0), cout.tie(0);
38     cin >> n >> m;
39     for (int i = 1; i ≤ m; i++) {
40         int u, v;
41         cin >> u >> v;
42         add(u, v);
43         add(v, u);
44     }
45     for (int i = 1; i ≤ n; i++)
46         if (!dfn[i]) tarjan(i, 0);
47     for (int i = 1; i ≤ n; i++)
48         if (!in_dcc[i]) dfs(i, ++dc);
49     cout << dc << "\n";
50     for (int i = 1; i ≤ dc; i++) {
51         cout << DCC[i].size() << " ";
52         for (auto v : DCC[i]) cout << v << " ";
53         cout << "\n";
54     }
55     return 0;
56 }

```

#### point.cpp

---

```

1  #include <cstdio>
2  #include <iostream>
3  #include <vector>
4  using namespace std;
5  const int N = 500005;
6  const int M = 2000005;
7  int n, m, head[N], tot;
8  struct edge {
9     int v, nxt;
10 } e[M << 1];
11 void add(int u, int v) {
12     e[++tot].v = v;
13     e[tot].nxt = head[u];
14     head[u] = tot;
15 }
16 int dfn[N], low[N], Time;
17 vector<int> dcc[N];
18 int cnt, stk[N], top;
19 void tarjan(int u, int rt) {
20     dfn[u] = low[u] = ++Time, stk[++top] = u;
21     if (u == rt && head[u] == 0) {

```

```

22     dcc[++cnt].push_back(u);
23     return;
24 }
25 for (int i = head[u]; i; i = e[i].nxt) {
26     int v = e[i].v;
27     if (!dfn[v]) {
28         tarjan(v, rt);
29         low[u] = min(low[u], low[v]);
30         if (dfn[u] ≤ low[v]) {
31             ++cnt;
32             do { dcc[cnt].push_back(stk[top--]); } while (stk[top + 1] ≠ v
33             );
34             dcc[cnt].push_back(u);
35         } else low[u] = min(low[u], dfn[v]);
36     }
37 }
38 int main() {
39     cin.tie(0)→sync_with_stdio(false);
40     cout.tie(0);
41     cin >> n >> m;
42     for (int i = 1; i ≤ m; i++) {
43         int u, v;
44         cin >> u >> v;
45         if (u = v) continue;
46         add(u, v);
47         add(v, u);
48     }
49     for (int i = 1; i ≤ n; i++)
50         if (!dfn[i]) tarjan(i, i);
51     cout << cnt << "\n";
52     for (int i = 1; i ≤ cnt; i++) {
53         cout << dcc[i].size() << " ";
54         for (auto x : dcc[i]) cout << x << " ";
55         cout << "\n";
56     }
57     return 0;
58 }

```

### 1.1.2 scc

kosaraju.cpp

---

```

1 // g 是原图, g2 是反图
2 #include <bits/stdc++.h>
3 using namespace std;
4 const int N = 1e6 + 5;
5 vector<vector<int>>> g, g2;

```

```

6  vector<int> s;
7  bool vis[N];
8  int sccCnt, n, color[N];
9  void dfs1(int u) {
10     vis[u] = true;
11     for (int v : g[u])
12         if (!vis[v]) dfs1(v);
13     s.push_back(u);
14 }
15 void dfs2(int u) {
16     color[u] = sccCnt;
17     for (int v : g2[u])
18         if (!color[v]) dfs2(v);
19 }
20 void kosaraju() {
21     sccCnt = 0;
22     for (int i = 1; i ≤ n; ++i)
23         if (!vis[i]) dfs1(i);
24     for (int i = n; i ≥ 1; --i)
25         if (!color[s[i]]) {
26             ++sccCnt;
27             dfs2(s[i]);
28         }
29 }

```

#### tarjan.cpp

---

```

1  #include <algorithm>
2  #include <cstdio>
3  #include <cstring>
4  #include <iostream>
5  #include <vector>
6  using namespace std;
7  const int N = 10005, M = 100005;
8  int n, m, head[M], tot;
9  struct edge {
10     int v, nxt;
11 } e[M];
12 void add(int u, int v) {
13     e[++tot].v = v;
14     e[tot].nxt = head[u];
15     head[u] = tot;
16 }
17 int dfn[N], low[N];
18 int stk[N], top, Time;
19 bool ins[N], vis[N];
20 int fa[N], cnt;
21 vector<vector<int>> SCC;

```

```

22 void tarjan(int u) {
23     dfn[u] = ++Time, low[u] = dfn[u], stk[++top] = u, ins[u] = true;
24     for (int i = head[u]; i; i = e[i].nxt) {
25         int v = e[i].v;
26         if (!dfn[v]) {
27             tarjan(v);
28             low[u] = min(low[u], low[v]);
29         } else if (ins[v]) low[u] = min(low[u], dfn[v]);
30     }
31     if (dfn[u] == low[u]) {
32         ++cnt;
33         SCC.push_back(vector<int>());
34         while (stk[top] != u) {
35             SCC[cnt].push_back(stk[top]);
36             fa[stk[top]] = cnt, ins[stk[top]] = false, top--;
37         }
38         SCC[cnt].push_back(stk[top]);
39         fa[stk[top]] = cnt, ins[stk[top]] = false, top--;
40     }
41 }
42 int main() {
43     ios::sync_with_stdio(false);
44     cin.tie(0);
45     cout.tie(0);
46     cin >> n >> m;
47     for (int i = 1; i ≤ m; i++) {
48         int u, v;
49         cin >> u >> v;
50         add(u, v);
51     }
52     SCC.push_back(vector<int>());
53     for (int i = 1; i ≤ n; i++)
54         if (!dfn[i]) tarjan(i);
55     cout << cnt << "\n";
56     for (int i = 1; i ≤ cnt; i++) sort(SCC[i].begin(), SCC[i].end());
57     for (int i = 1; i ≤ n; i++) {
58         if (vis[fa[i]]) continue;
59         else {
60             for (auto x : SCC[fa[i]]) cout << x << " ";
61             cout << "\n";
62             vis[fa[i]] = true;
63         }
64     }
65     return 0;
66 }

```



## 1.2 mst

### 1.2.1 kruscal.cpp

---

```

1  #include <bits/stdc++.h>
2  using namespace std;
3  const int N = 1e6 + 5;
4  struct E {
5      int u, v, w;
6      bool operator<(const E &b) const { return w < b.w; }
7  } Edge[N];
8  int f[N];
9  int getf(int x) { return f[x] = x ? x : f[x] = getf(f[x]); }
10 vector<int> tr[N];
11 int main() {
12     int n, m;
13     cin >> n >> m;
14     for (int i = 1; i ≤ n; i++) f[i] = i;
15     for (int i = 1; i ≤ m; i++) cin >> Edge[i].u >> Edge[i].v >> Edge[i].w;
16     sort(Edge + 1, Edge + 1 + m);
17     for (int i = 1; i ≤ m; i++) {
18         int fu = getf(Edge[i].u), fv = getf(Edge[i].v);
19         if (fu == fv) continue;
20         tr[Edge[i].u].push_back(Edge[i].v);
21         tr[Edge[i].v].push_back(Edge[i].u);
22     }
23     return 0;
24 }

```

### 1.2.2 prim.cpp

---

```

1  #include <cstring>
2  #include <iostream>
3  #include <queue>
4  using namespace std;
5  constexpr int N = 5050, M = 2e5 + 10;
6  struct E {
7      int v, w, x;
8  } e[M * 2];
9  int n, m, h[N], cnte;
10 void adde(int u, int v, int w) { e[++cnte] = E{v, w, h[u]}, h[u] = cnte; }
11 struct S {
12     int u, d;
13 };
14 bool operator<(const S &x, const S &y) { return x.d > y.d; }
15 priority_queue<S> q;
16 int dis[N];

```

```

17  bool vis[N];
18  int res = 0, cnt = 0;
19  void Prim() {
20      memset(dis, 0x3f, sizeof(dis));
21      dis[1] = 0;
22      q.push({1, 0});
23      while (!q.empty()) {
24          if (cnt ≥ n) break;
25          int u = q.top().u, d = q.top().d;
26          q.pop();
27          if (vis[u]) continue;
28          vis[u] = true;
29          ++cnt;
30          res += d;
31          for (int i = h[u]; i; i = e[i].x) {
32              int v = e[i].v, w = e[i].w;
33              if (w < dis[v]) { dis[v] = w, q.push({v, w}); }
34          }
35      }
36  }
37  int main() {
38      cin >> n >> m;
39      for (int i = 1, u, v, w; i ≤ m; ++i) { cin >> u >> v >> w, adde(u, v, w
        ), adde(v, u, w); }
40      Prim();
41      if (cnt == n) cout << res;
42      else cout << "No_MST.";
43      return 0;
44  }

```

## 1.3 shortest-path

### 1.3.1 dijkstra.cpp

---

```

1  struct edge {
2      int v, w;
3  };
4  struct node {
5      int dis, u;
6      bool operator>(const node &a) const { return dis > a.dis; }
7  };
8  vector<edge> e[MAXN];
9  int dis[MAXN], vis[MAXN];
10 priority_queue<node, vector<node>, greater<node>> q;
11 void dijkstra(int n, int s) {
12     memset(dis, 0x3f, (n + 1) * sizeof(int));
13     memset(vis, 0, (n + 1) * sizeof(int));

```

```

14     dis[s] = 0;
15     q.push({0, s});
16     while (!q.empty()) {
17         int u = q.top().u;
18         q.pop();
19         if (vis[u]) continue;
20         vis[u] = 1;
21         for (auto ed : e[u]) {
22             int v = ed.v, w = ed.w;
23             if (dis[v] > dis[u] + w) {
24                 dis[v] = dis[u] + w;
25                 q.push({dis[v], v});
26             }
27         }
28     }
29 }

```

### 1.3.2 spfa.cpp

---

```

1  #include <bits/stdc++.h>
2  using namespace std;
3  const int N = 1e5 + 5;
4  int n, m;
5  vector<pair<int, int>> g[N];
6  inline void add(int u, int v, int w) { g[u].push_back({v, w}); }
7  queue<int> q;
8  int dis[N];
9  bool inq[N];
10 inline void spfa(int s) {
11     memset(dis, 0x3f, sizeof(dis));
12     memset(inq, false, sizeof(inq));
13     inq[s] = true, dis[s] = 0;
14     q.push(s);
15     while (q.size()) {
16         int u = q.front();
17         q.pop(), inq[u] = false;
18         for (auto [v, w] : g[u])
19             if (dis[v] > dis[u] + w) {
20                 dis[v] = dis[u] + w;
21                 if (!inq[v]) q.push(v);
22             }
23     }
24 }
25 int main() {
26     cin >> n >> m;
27     for (int i = 1, u, v, w; i <= m; i++) cin >> u >> v >> w, add(u, v, w),
28         add(v, u, w);
29     spfa(1);

```

```

29     return 0;
30 }

```

## 1.4 tree

### 1.4.1 centroid.cpp

---

```

1  int size[MAXN], weight[MAXN], centroid[2];
2  void GetCentroid(int cur, int fa) {
3      size[cur] = 1, weight[cur] = 0;
4      for (int i = head[cur]; i ≠ -1; i = e[i].nxt) {
5          if (e[i].to ≠ fa) {
6              GetCentroid(e[i].to, cur);
7              size[cur] += size[e[i].to];
8              weight[cur] = max(weight[cur], size[e[i].to]);
9          }
10     }
11     weight[cur] = max(weight[cur], n - size[cur]);
12     if (weight[cur] ≤ n / 2) centroid[centroid[0] ≠ 0] = cur;
13 }

```

### 1.4.2 diameter.cpp

---

```

1  #include <bits/stdc++.h>
2  constexpr int N = 10000 + 10;
3  int n, c, d[N];
4  vector<int> E[N];
5  void dfs(int u, int fa) {
6      for (int v : E[u]) {
7          if (v == fa) continue;
8          d[v] = d[u] + 1;
9          if (d[v] > d[c]) c = v;
10         dfs(v, u);
11     }
12 }
13 int main() {
14     scanf("%d", &n);
15     for (int i = 1; i < n; i++) {
16         int u, v;
17         scanf("%d_%d", &u, &v);
18         E[u].push_back(v), E[v].push_back(u);
19     }
20     dfs(1, 0);
21     d[c] = 0, dfs(c, 0);
22     printf("%d\n", d[c]);
23     return 0;
24 }

```

### 1.4.3 hld.cpp

---

```

1  #include <bits/stdc++.h>
2  using namespace std;
3  const int N = 1e5 + 5;
4  int n;
5  vector<int> g[N];
6  int fa[N], dep[N], siz[N], hson[N], dfn[N], idx, top[N];
7  void hld1(int u, int fath) {
8      fa[u] = fath, dep[u] = dep[fath] + 1, siz[u] = 1;
9      for (int v : g[u]) {
10         if (v == fath) continue;
11         hld1(v, u), siz[u] += siz[v];
12         if (siz[v] > siz[hson[u]]) hson[u] = v;
13     }
14 }
15 void hld2(int u, int nowtp) {
16     top[u] = nowtp, dfn[u] = ++idx;
17     if (hson[u]) hld2(hson[u], nowtp);
18     for (int v : g[u])
19         if (v != fa[u] && v != hson[u]) hld2(v, v);
20 }
21 inline int LCA(int x, int y) {
22     while (top[x] != top[y]) return dep[top[x]] < dep[top[y]] ? y = fa[top[y]] : x = fa[top[x]];
23     return dep[x] < dep[y] ? x : y;
24 }
25 int main() { return 0; }
```

### 1.4.4 virtual-tree.cpp

---

```

1  #include <bits/stdc++.h>
2  using namespace std;
3  const int N = 1e5 + 5;
4  int n, q, m, h[N], s[N], cnt;
5  vector<int> g[N], vt[N];
6  int fa[N], dep[N], siz[N], hson[N], dfn[N], top[N], idx;
7  void hld1(int u, int fath) { ... }
8  void hld2(int u, int fath) { ... }
9  int lca(int u, int v) { ... } // 重链剖分相关内容见 oi-algorithms/graph/tree/hld.cpp
10 bool cmp(int a, int b) { return dfn[a] < dfn[b]; }
11 inline void buildVtree() {
12     sort(h + 1, h + 1 + m, cmp);
13     s[cnt = 1] = 1;
14     for (int i = 1; i ≤ m; i++) s[++cnt] = h[i], s[++cnt] = lca(h[i], h[i + 1]);
15 }
```

```

15     s[++cnt] = h[m];
16     sort(s + 1, s + 1 + cnt, cmp);
17     cnt = unique(s + 1, s + 1 + cnt) - s - 1;
18     for (int i = 1; i ≤ cnt; i++) vt[lca(s[i], s[i + 1])].push_back(s[i +
19         1]);
20     }
21     int main() { return 0; }

```

## 1.5 diff-constraints.cpp

---

```

1  #include <cstring>
2  #include <iostream>
3  #include <queue>
4  using namespace std;
5  struct edge {
6      int v, w, next;
7  } e[40005];
8  int head[10005], vis[10005], tot[10005], cnt;
9  long long ans, dist[10005];
10 queue<int> q;
11 void addedge(int u, int v, int w) { // 加边
12     e[++cnt].v = v;
13     e[cnt].w = w;
14     e[cnt].next = head[u];
15     head[u] = cnt;
16 }
17 int main() {
18     cin.tie(nullptr)->sync_with_stdio(false);
19     int n, m;
20     cin >> n >> m;
21     for (int i = 1; i ≤ m; i++) {
22         int op, x, y, z;
23         cin >> op;
24         if (op == 1) {
25             cin >> x >> y >> z;
26             addedge(y, x, z);
27         } else if (op == 2) {
28             cin >> x >> y >> z;
29             addedge(x, y, -z);
30         } else {
31             cin >> x >> y;
32             addedge(x, y, 0);
33             addedge(y, x, 0);
34         }
35     }
36     for (int i = 1; i ≤ n; i++) addedge(0, i, 0);
37     memset(dist, -0x3f, sizeof(dist));

```

```
38     dist[0] = 0;
39     vis[0] = 1;
40     q.push(0);
41     while (!q.empty()) { // 判负环, 看上面的
42         int cur = q.front();
43         q.pop();
44         vis[cur] = 0;
45         for (int i = head[cur]; i; i = e[i].next)
46             if (dist[cur] + e[i].w > dist[e[i].v]) {
47                 dist[e[i].v] = dist[cur] + e[i].w;
48                 if (!vis[e[i].v]) {
49                     vis[e[i].v] = 1;
50                     q.push(e[i].v);
51                     tot[e[i].v]++;
52                     if (tot[e[i].v] ≥ n) {
53                         cout << "No\n";
54                         return 0;
55                     }
56                 }
57             }
58     }
59     cout << "Yes\n";
60     return 0;
61 }
```

## 第 2 部分 字符串 String

### 2.1 hash

#### 2.1.1 double-valued.cpp

---

```
1  #include <cstring>
2  #include <iostream>
3  using std::string;
4  using ull = unsigned long long;
5  ull base = 131, mod1 = 212370440130137957, mod2 = 1e9 + 7;
6  ull get_hash1(string s) {
7      int len = s.size();
8      ull ans = 0;
9      for (int i = 0; i < len; i++) ans = (ans * base + (ull)s[i]) % mod1;
10     return ans;
11 }
12 ull get_hash2(string s) {
13     int len = s.size();
14     ull ans = 0;
15     for (int i = 0; i < len; i++) ans = (ans * base + (ull)s[i]) % mod2;
16     return ans;
17 }
18 bool cmp(const string s, const string t) {
19     bool f1 = get_hash1(s) != get_hash1(t);
20     bool f2 = get_hash2(s) != get_hash2(t);
21     return f1 || f2;
22 }
23 int main() { return 0; }
```

#### 2.1.2 modular.cpp

---

```
1  #include <cstring>
2  #include <iostream>
3  using std::string;
4  constexpr int M = 1e9 + 7;
5  constexpr int B = 233;
6  using ll = long long;
7  int get_hash(const string &s) {
8     int res = 0;
```



```

9     for (int i = 0; i < s.size(); ++i) { res = ((ll)res * B + s[i]) % M; }
10    return res;
11 }
12 bool cmp(const string &s, const string &t) { return get_hash(s) == get_hash
    (t); }
13 int main() { return 0; }

```

## 2.2 SA

### 2.2.1 DC3.cpp

---

```

1  #include <cstring>
2  #include <iostream>
3  #define f(x) (x / 3) + (x % 3 == 1 ? 0 : cd) // f(x) 表示原串中后缀 x 在新串中
    的位置
4  #define g(x) (x ≥ cd ? (x - cd) * 3 + 2 : x * 3 + 1) // g(x) 表示新串后缀 x
    在原串中的位置
5  using namespace std;
6  const int N = 1e6 + 5;
7  string s;
8  int n, sa[N * 3 + 100], rk[N * 3 + 100], buc[N], x[N], y[N], height[N];
9  void sort(int *rk, int *a, int *b, int n, int Sigma) // rk 表示待排序串, a 表
    示指标集, b 表示排序后的指标顺序
10 {
11     for (int i = 0; i ≤ Sigma; i++) buc[i] = 0;
12     for (int i = 0; i < n; i++) buc[rk[a[i]]]++;
13     for (int i = 1; i ≤ Sigma; i++) buc[i] += buc[i - 1];
14     for (int i = n - 1; i ≥ 0; i--) b[--buc[rk[a[i]]]] = a[i];
15 }
16 bool cmp3(int *r, int x, int y) { return r[x] == r[y] && r[x + 1] == r[y +
    1] && r[x + 2] == r[y + 2]; }
17 bool cmps(int *r, int x, int y) {
18     if (r[x] ≠ r[y]) return r[x] < r[y];
19     if (x % 3 == 1) return buc[x + 1] < buc[y + 1];
20     return !cmps(r, y + 1, x + 1);
21 }
22 void DC3(int *rk, int *sa, int n, int Sigma) {
23     bool h = (n % 3 == 1);
24     if (h) rk[n++] = 0;
25     int *nrk = rk + n + 2, *nsa = sa + n, cb = 0, p; // nrk, nsa 分别表示新的
    rk 和 sa, cb 表示 B 类后缀的数量
26     for (int i = 0; i < n; i++)
27         if (i % 3) x[cb++] = i;
28     rk[n] = rk[n + 1] = 0;
29     sort(rk + 2, x, y, cb, Sigma), sort(rk + 1, y, x, cb, Sigma), sort(rk, x
    , y, cb, Sigma); // 指标顺序存在了 y 中
30     int ca = 0, cd = (n + 1) / 3; // ca 表示 A 类后缀的数量, cd 表示 i % 3 = 1

```

```

    的后缀的数量
31     nrk[f(y[0])] = p = 1;
32     for (int i = 1; i < cb; i++) {
33         if (!cmp3(rk, y[i], y[i - 1])) p++;
34         nrk[f(y[i])] = p;
35     }
36     if (p < cb) DC3(nrk, nsa, cb, p); // 递归求解 B 类后缀
37     else
38         for (int i = 0; i < cb; i++)
39             if (nrk[i]) nsa[nrk[i] - 1] = i;
40     for (int i = 0; i < cb; i++)
41         if (nsa[i] < cd) y[ca++] = 3 * nsa[i];
42     sort(rk, y, x, ca, Sigma);
43     for (int i = 0; i < cb; i++) buc[y[i] = g(nsa[i])] = i; // 利用 buc 存 B
        类后缀的排名
44     buc[n] = -1, p = 0;
45     int i = 0, j = h;
46     while (i < ca && j < cb) {
47         if (cmps(rk, y[j], x[i])) sa[p++] = y[j++];
48         else sa[p++] = x[i++];
49     }
50     while (i < ca) sa[p++] = x[i++];
51     while (j < cb) sa[p++] = y[j++];
52 }
53 int main() {
54     cin.tie(nullptr)->sync_with_stdio(false);
55     cout.tie(nullptr);
56     cin >> s;
57     n = s.length();
58     for (int i = 0; i < n; i++) rk[i] = s[i] - '0' + 1;
59     DC3(rk, sa, n, 75);
60     for (int i = 0; i < n; i++) cout << sa[i] + 1 << ' ';
61     cout << '\n';
62     for (int i = 0; i < n; i++) rk[sa[i]] = i;
63     for (int i = 0, k = 0; i < n; i++) {
64         if (!rk[i]) continue;
65         if (k) --k;
66         while (s[i + k] == s[sa[rk[i] - 1] + k]) ++k;
67         height[rk[i]] = k;
68     }
69     for (int i = 1; i < n; i++) cout << height[i] << ' ';
70     return cout << '\n', 0;
71 }

```

### 2.2.2 SA-IS.cpp

---

```

1  #include <algorithm>
2  #include <cstdio>

```

```

3  using namespace std;
4  const int N = 1e6 + 10;
5  typedef long long ll;
6  template <typename T> inline void gm(T *a, int siz, T *op) { op = a,
    a += siz; }
7  #define pus(x) (a[cur[a[x]]--] = x)
8  #define pul(x) (a[cur[a[x]]++] = x)
9  #define inds(lms)

10     for (int i = 1; i ≤ n; i++) sa[i] = -1;
11     for (int i = 1; i ≤ n; i++) sum[i] = 0;
12     for (int i = 1; i ≤ n; i++) sum[a[i]]++;
13     for (int i = 1; i ≤ n; i++) sum[i] += sum[i - 1];
14     for (int i = 1; i ≤ n; i++) cur[i] = sum[i];
15     for (int i = m; i ≥ 1; i--) pus(lms[i]);
16     for (int i = 1; i ≤ n; i++) cur[i] = sum[i - 1] + 1;
17     for (int i = 1; i ≤ n; i++)
18         if (sa[i] > 1 && !tp[sa[i] - 1]) pul(sa[i] - 1);
19     for (int i = 1; i ≤ n; i++) cur[i] = sum[i];
20     for (int i = n; i ≥ 1; i--)
21         if (sa[i] > 1 && tp[sa[i] - 1]) pus(sa[i] - 1);
22 int sa[N], sum[N], cur[N], rk[N], A_bas[N << 4], *A_t;
23 inline void sais(int n, int *a) {
24     int *tp, *p;
25     gm(A_t, n + 1, tp), gm(A_t, n + 2, p);
26     tp[n] = 1;
27     for (int i = n - 1; i ≥ 1; i--) tp[i] = (a[i] == a[i + 1]) ? tp[i + 1]
        : (a[i] < a[i + 1]);
28     int m = 0;
29     for (int i = 1; i ≤ n; i++) rk[i] = (tp[i] && !tp[i - 1]) ? (p[++m] = i
        , m) : -1;
30     inds(p);
31     int tot = 0, *a1;
32     gm(A_t, m + 1, a1);
33     p[m + 1] = n;
34     for (int i = 1, x, y; i ≤ n; i++)
35         if ((x = rk[sa[i]]) ≠ -1) {
36             if (tot == 0 || p[x + 1] - p[x] ≠ p[y + 1] - p[y]) tot++;

```

```

37         else
38             for (int p1 = p[x], p2 = p[y]; p2 ≤ p[y + 1]; p1++, p2++)
39                 if ((a[p1] << 1 | tp[p1]) ≠ (a[p2] << 1 | tp[p2])) {
40                     tot++;
41                     break;
42                 }
43             a1[y = x] = tot;
44         }
45     if (tot == m)
46         for (int i = 1; i ≤ m; i++) sa[a1[i]] = i;
47     else sais(m, a1);
48     for (int i = 1; i ≤ m; i++) a1[i] = p[sa[i]];
49     inds(a1);
50 }
51 char mde[N];
52 int n;
53 int a[N];
54 int tr[300];
55 char buf[20];
56 int cnt;
57 int main() {
58     A_t = A_bas;
59     scanf("%s", mde + 1);
60     while (mde[n + 1] ≠ '\0') n++;
61     for (int i = 1; i ≤ n; i++) tr[mde[i]] = 1;
62     for (int i = 1; i < 300; i++) tr[i] += tr[i - 1];
63     for (int i = 1; i ≤ n; i++) a[i] = tr[mde[i]] + 1;
64     a[++n] = 1;
65     sais(n, a);
66     for (int i = 2; i ≤ n; i++) {
67         int tmp = sa[i];
68         while (tmp) buf[++cnt] = tmp % 10 + 48, tmp /= 10;
69         while (cnt) putchar(buf[cnt--]);
70         putchar('_');
71     }
72     return 0;
73 }

```

## 2.3 trie

### 2.3.1 persistent-trie.cpp

---

```

1  #include <bits/stdc++.h>
2  using namespace std;
3  const int N = 6e5 + 5, H = 28;
4  int n, m, a[N], s[N], rt[N], ch[N * 33][2], cnt[N * 33], tot;
5  void Insert(int u, int pre, int x) {

```

```

6     for (int i = H; i ≥ 0; i--) {
7         cnt[u] = cnt[pre] + 1;
8         int c = ((x & (1 << i)) ? 1 : 0);
9         if (!ch[u][c]) ch[u][c] = ++tot;
10        ch[u][c ^ 1] = ch[pre][c ^ 1];
11        u = ch[u][c], pre = ch[pre][c];
12    }
13    cnt[u] = cnt[pre] + 1;
14 }
15 int query(int u, int v, int x) {
16     int res = 0;
17     for (int i = H; i ≥ 0; i--) {
18         int c = ((x & (1 << i)) ? 1 : 0);
19         if (cnt[ch[u][!c]] - cnt[ch[v][!c]]) u = ch[u][!c], v = ch[v][!c],
20             res += (1 << i);
21         else u = ch[u][c], v = ch[v][c];
22     }
23     return res;
24 }
25 int main() {
26     cin.tie(nullptr)->sync_with_stdio(false);
27     cout.tie(nullptr);
28     cin >> n >> m;
29     for (int i = 1, x; i ≤ n; i++) cin >> a[i], s[i] = s[i - 1] ^ a[i];
30     for (int i = 1; i ≤ n; i++) rt[i] = ++tot, Insert(rt[i], rt[i - 1], s[i]);
31     char op;
32     for (int l, r, val; m; m--) {
33         cin >> op;
34         if (op == 'A') {
35             n++, cin >> a[n];
36             s[n] = s[n - 1] ^ a[n], rt[n] = ++tot;
37             Insert(rt[n], rt[n - 1], s[n]);
38         }
39         if (op == 'Q') {
40             cin >> l >> r >> val;
41             l--, r--;
42             if (!l) cout << max(s[n] ^ val, query(rt[r], rt[0], s[n] ^ val))
43                 << '\n';
44             else cout << query(rt[r], rt[l - 1], s[n] ^ val) << '\n';
45         }
46     }
47     return 0;
48 }

```

### 2.3.2 trie.cpp

---

```

1 #include <cstring>

```

```

2  #include <iostream>
3  using namespace std;
4  struct trie {
5      int son[100000][26], cnt;
6      bool exist[100000];
7      void insert(char *s, int l) {
8          int p = 0;
9          for (int i = 0; i < l; i++) {
10             int c = s[i] - 'a';
11             if (!son[p][c]) son[p][c] = ++cnt;
12             p = son[p][c];
13         }
14         exist[p] = true;
15     }
16     bool find(char *s, int l) {
17         int p = 0;
18         for (int i = 0; i < l; i++) {
19             int c = s[i] - 'a';
20             if (!son[p][c]) return 0;
21             p = son[p][c];
22         }
23         return exist[p];
24     }
25 };
26 int main() { return 0; }

```

## 2.4 acam.cpp

---

```

1  #include <cstring>
2  #include <iostream>
3  #include <queue>
4  #include <vector>
5  using namespace std;
6  namespace acam {
7      const int SIZ = 2000005;
8      struct node {
9          int ch[26], fail, ans, id;
10         node() { memset(ch, 0, sizeof(ch)), ans = id = 0; }
11         inline int &operator[](const int x) { return x < 26 ? ch[x] : ch[x - 'a']
12             ]; }
13         inline int operator[](const int x) const { return x < 26 ? ch[x] : ch[x
14             - 'a']; }
15     } tr[SIZ];
16     int tot, ans[SIZ], pcnt;
17     vector<int> fail[SIZ];
18     inline void insert(char *s, int &id) {
19         int u = 0;

```

```

18     for (int i = 1; s[i]; i++) {
19         if (!tr[u][i]) tr[u][i] = ++tot;
20         u = tr[u][i];
21     }
22     if (!tr[u].id) tr[u].id = ++pcnt;
23     id = tr[u].id;
24 }
25 inline void build() {
26     queue<int> q;
27     for (int i = 0; i < 26; i++)
28         if (tr[0][i]) q.push(tr[0][i]), fail[0].push_back(tr[0][i]);
29     while (!q.empty()) {
30         int u = q.front();
31         q.pop();
32         for (int i = 0; i < 26; i++) {
33             if (tr[u][i]) {
34                 tr[tr[u][i]].fail = tr[tr[u].fail][i];
35                 fail[tr[tr[u].fail][i]].push_back(tr[u][i]);
36                 q.push(tr[u][i]);
37             } else tr[u][i] = tr[tr[u].fail][i];
38         }
39     }
40 }
41 void query(char *t) {
42     int u = 0;
43     for (int i = 1; t[i]; ++i) u = tr[u][t[i]], tr[u].ans++;
44 }
45 void dfs(int u) {
46     for (int v : fail[u]) {
47         dfs(v);
48         tr[u].ans += tr[v].ans;
49     }
50     ans[tr[u].id] = tr[u].ans;
51 }
52 }; // namespace acam
53 int main() { return 0; }

```

## 2.5 kmp.cpp

---

```

1  #include <cstring>
2  #include <iostream>
3  #include <vector>
4  using namespace std;
5  vector<int> pf(string s) {
6      int n = (int)s.length();
7      vector<int> pi(n);
8      for (int i = 1; i < n; i++) {

```

```

9         int j = pi[i - 1];
10        while (j && s[j] != s[i]) j = pi[j - 1];
11        if (s[i] == s[j]) ++j;
12        pi[i] = j;
13    }
14    return pi;
15 }
16 int main() { return 0; }

```

## 2.6 manacher.cpp

---

```

1  #include <cstring>
2  #include <iostream>
3  using namespace std;
4  const int N = 2.2e7 + 10;
5  inline bool chk(char c) { return c ≥ 'a' && c ≤ 'z'; }
6  int n, f[N];
7  char s[N], c;
8  int main() {
9      s[0] = '~';
10     while (chk(c = getchar())) s[++n] = '|', s[++n] = c;
11     s[++n] = '|';
12     for (int i = 1, maxr = 0, mid = 0; i ≤ n; i++) {
13         if (i < maxr) f[i] = min(f[2 * mid - i], maxr - i);
14         for (int j = i + f[i] + 1; j ≤ n; j++) {
15             if (s[j] == s[2 * i - j]) ++f[i];
16             else break;
17         }
18         if (i + f[i] > maxr) maxr = i + f[i], mid = i;
19     }
20     int ans = 0;
21     for (int i = 1; i ≤ n; i++)
22         if (f[i] > ans) ans = f[i];
23     cout << ans;
24     return 0;
25 }

```

## 2.7 z-func.cpp

---

```

1  #include <cstring>
2  #include <iostream>
3  #include <vector>
4  using namespace std;
5  vector<int> z_function(string s) {
6      int n = (int)s.length();

```



```
7     vector<int> z(n);
8     for (int i = 1, l = 0, r = 0; i < n; i++) {
9         if (i ≤ r && z[i - l] < r - i + 1) z[i] = z[i - l];
10        else {
11            z[i] = r - i + 1;
12            while (i + z[i] < n && s[i + z[i]] == s[z[i]]) ++z[i];
13        }
14        if (i + z[i] - 1 > r) r = i + z[i] - 1, l = i;
15    }
16    return z;
17 }
18 int main() { return 0; }
```

## 第 3 部分 数学 Math

### 3.1 lineral-algebra

#### 3.1.1 mat.cpp

---

```
1  #include <bits/stdc++.h>
2  using namespace std;
3  struct mat {
4      LL a[sz][sz];
5      mat() { memset(a, 0, sizeof a); }
6      mat operator-(const mat &T) const {
7          mat res;
8          for (int i = 0; i < sz; ++i)
9              for (int j = 0; j < sz; ++j) res.a[i][j] = (a[i][j] - T.a[i][j]) %
10                 MOD;
11         return res;
12     }
13     mat operator+(const mat &T) const {
14         mat res;
15         for (int i = 0; i < sz; ++i)
16             for (int j = 0; j < sz; ++j) res.a[i][j] = (a[i][j] + T.a[i][j]) %
17                 MOD;
18         return res;
19     }
20     mat operator*(const mat &T) const {
21         mat res;
22         int r;
23         for (int i = 0; i < sz; ++i)
24             for (int k = 0; k < sz; ++k) {
25                 r = a[i][k];
26                 for (int j = 0; j < sz; ++j) res.a[i][j] += T.a[k][j] * r, res.
27                     a[i][j] %= MOD;
28             }
29         return res;
30     }
31     mat operator^(LL x) const {
32         mat res, bas;
```

```

33         for (int j = 0; j < sz; ++j) bas.a[i][j] = a[i][j] % MOD;
34     while (x) {
35         if (x & 1) res = res * bas;
36         bas = bas * bas;
37         x >>= 1;
38     }
39     return res;
40 }
41 };
42 int main() { return 0; }

```

## 3.2 lineral-programming

### 3.2.1 simplex.cpp

---

```

1  #include <cmath>
2  #include <cstring>
3  #include <iostream>
4  using namespace std;
5  constexpr int M = 10005, N = 1005, INF = 1e9;
6  int n, m;
7  double a[M][N], b[M], c[N], v;
8  void pivot(int l, int e) { // 转轴操作函数
9      b[l] /= a[l][e];
10     for (int j = 1; j ≤ n; j++)
11         if (j ≠ e) a[l][j] /= a[l][e];
12     a[l][e] = 1 / a[l][e];
13
14     for (int i = 1; i ≤ m; i++)
15         if (i ≠ l && fabs(a[i][e]) > 0) {
16             b[i] -= a[i][e] * b[l];
17             for (int j = 1; j ≤ n; j++)
18                 if (j ≠ e) a[i][j] -= a[i][e] * a[l][j];
19             a[i][e] = -a[i][e] * a[l][e];
20         }
21     v += c[e] * b[l];
22     for (int j = 1; j ≤ n; j++)
23         if (j ≠ e) c[j] -= c[e] * a[l][j];
24     c[e] = -c[e] * a[l][e];
25 }
26 double simplex() {
27     while (true) {
28         int e = 0, l = 0;
29         for (e = 1; e ≤ n; e++)
30             if (c[e] > (double)0) break;
31         if (e == n + 1) return v; // 此时v即为最优解
32         double mn = INF;

```

```

33     for (int i = 1; i ≤ m; i++) {
34         if (a[i][e] > (double)0 && mn > b[i] / a[i][e]) {
35             mn = b[i] / a[i][e]; // 找对这个e限制最紧的l
36             l = i;
37         }
38     }
39     if (mn == INF) return INF; // unbounded
40     pivot(l, e); // 转动l,e
41 }
42 }
43 int main() {
44     cin.tie(nullptr)->sync_with_stdio(false);
45     cin >> n >> m;
46     for (int i = 1; i ≤ n; i++) cin >> c[i];
47     for (int i = 1; i ≤ m; i++) {
48         int s, t;
49         cin >> s >> t;
50         for (int j = s; j ≤ t; j++) a[i][j] = 1; // 表示第i种志愿者在j时间可以服
           务
51         cin >> b[i];
52     }
53     cout << (int)(simplex() + 0.5);
54 }

```

### 3.3 number-theory

#### 3.3.1 euler

theorem

get-euler.cpp

---

```

1  #include <cmath>
2  int euler_phi(int n) {
3      int ans = n;
4      for (int i = 2; i * i ≤ n; i++)
5          if (n % i == 0) {
6              ans = ans / i * (i - 1);
7              while (n % i == 0) n /= i;
8          }
9      if (n > 1) ans = ans / n * (n - 1);
10     return ans;
11 }
12 int main() { return 0; }

```

sieve.cpp

---

```

1  #include <bitset>
2  #include <iostream>
3  #include <vector>
4  using std::bitset;
5  using std::vector;
6  const int N = 1e7 + 5;
7  bitset<N> not_prime;
8  int prime[N], pcnt, phi[N];
9  inline void sieve(int n) {
10     phi[1] = 1;
11     for (int i = 2; i ≤ n; i++) {
12         if (!not_prime[i]) prime[++pcnt] = i, phi[i] = i - 1;
13         for (int j = 1; j ≤ pcnt && i * prime[j] ≤ n; j++) {
14             not_prime[i * prime[j]] = true;
15             if (i % prime[j] == 0) {
16                 phi[i * prime[j]] = phi[i] * prime[j];
17                 break;
18             }
19             phi[i * prime[j]] = phi[i] * phi[prime[j]];
20         }
21     }
22 }
23 int main() { return 0; }
```

### 3.3.2 lucas

ex-lucas.cpp

---

```

1  #include <iostream>
2  #include <vector>
3
4  // Extended Euclid.
5  void ex_gcd(int a, int b, int &x, int &y) {
6      if (!b) x = 1, y = 0;
7      else ex_gcd(b, a % b, y, x), y -= a / b * x;
8  }
9
10 // Inverse of a mod m.
11 int inverse(int a, int m) {
12     int x, y;
13     ex_gcd(a, m, x, y);
14     return (x % m + m) % m;
15 }
16
17 // Coefficient in CRT.
18 int crt_coeff(int m_i, int m) {
19     long long mm = m / m_i;
20     mm *= inverse(mm, m_i);
```

```

21     return mm % m;
22 }
23
24 // Binominal Coefficient Calculator Modulo Prime Power.
25 class BinomModPrimePower {
26     int p, a, pa;
27     std::vector<int> f;
28
29     // Obtain multiplicity of p in n!.
30     long long nu(long long n) {
31         long long count = 0;
32         do {
33             n /= p;
34             count += n;
35         } while (n);
36         return count;
37     }
38
39     // Calculate (n!)_p mod pa.
40     long long fact_mod(long long n) {
41         bool neg = p == 2 || pa <= 4;
42         long long res = 1;
43         while (n > 1) {
44             if ((n / pa) & neg) res = pa - res;
45             res = res * f[n % pa] % pa;
46             n /= p;
47         }
48         return res;
49     }
50
51 public:
52     BinomModPrimePower(int p, int a, int pa) : p(p), a(a), pa(pa), f(pa) {
53         // Pretreatment.
54         f[0] = 1;
55         for (int i = 1; i < pa; ++i) { f[i] = i % p ? (long long)f[i - 1] * i
56             % pa : f[i - 1]; }
57     }
58
59     // Calculate Binom(n, k) mod pa.
60     int binomial(long long n, long long k) {
61         long long v = nu(n) - nu(n - k) - nu(k);
62         if (v >= a) return 0;
63         auto res = fact_mod(n - k) * fact_mod(k) % pa;
64         res = fact_mod(n) * inverse(res, pa) % pa;
65         for (; v; --v) res *= p;
66         return res % pa;
67     };
68

```

```

69 // Binominal Coefficient Calculator.
70 class BinomMod {
71     int m;
72     std::vector<BinomModPrimePower> bp;
73     std::vector<long long> crt_m;
74
75 public:
76     BinomMod(int n) : m(n) {
77         // Factorize.
78         for (int p = 2; p * p ≤ n; ++p) {
79             if (n % p == 0) {
80                 int a = 0, pa = 1;
81                 for (; n % p == 0; n /= p, ++a, pa *= p);
82                 bp.emplace_back(p, a, pa);
83                 crt_m.emplace_back(crt_coeff(pa, m));
84             }
85         }
86         if (n > 1) {
87             bp.emplace_back(n, 1, n);
88             crt_m.emplace_back(crt_coeff(n, m));
89         }
90     }
91
92     // Calculate Binom(n, k) mod m.
93     int binomial(long long n, long long k) {
94         long long res = 0;
95         for (size_t i = 0; i ≠ bp.size(); ++i) { res = (bp[i].binomial(n, k)
96             * crt_m[i] + res) % m; }
97         return res;
98     }
99 };
100
101 int main() {
102     int t, m;
103     std::cin >> t >> m;
104     BinomMod bm(m);
105     for (; t; --t) {
106         long long n, k;
107         std::cin >> n >> k;
108         std::cout << bm.binomial(n, k) << '\n';
109     }
110     return 0;
111 }

```

lucas.cpp

---

```

1 long long Lucas(long long n, long long k, long long p) {
2     if (k == 0) return 1;

```

```

3     return (C(n % p, k % p, p) * Lucas(n / p, k / p, p)) % p;
4 }

```

### 3.3.3 mobius

sieve.cpp

---

```

1  #include <bitset>
2  #include <iostream>
3  #include <vector>
4  using std::bitset;
5  using std::vector;
6  using ll = long long;
7  const int N = 1e7 + 5;
8  bitset<N> not_prime;
9  vector<int> pr;
10 int mu[N];
11 inline void sieve(int n) {
12     mu[1] = 1;
13     for (int i = 2; i ≤ n; i++) {
14         if (!not_prime[i]) mu[i] = -1, pr.push_back(i);
15         for (int x : pr) {
16             if (i * x > n) break;
17             not_prime[i * x] = true;
18             if (i % x == 0) break;
19             mu[i * x] = -mu[i];
20         }
21     }
22 }
23 int main() { return 0; }

```

### 3.3.4 prime

millerrabin.cpp

---

```

1  #include <bits/stdc++.h>
2  using namespace std;
3  bool millerRabin(int n) {
4     if (n < 3 || n % 2 == 0) return n == 2;
5     if (n % 3 == 0) return n == 3;
6     int u = n - 1, t = 0;
7     while (u % 2 == 0) u /= 2, ++t;
8     // test_time 为测试次数, 建议设为不小于 8
9     // 的整数以保证正确率, 但也不宜过大, 否则会影响效率
10    for (int i = 0; i < test_time; ++i) {
11        // 0, 1, n-1 可以直接通过测试, a 取值范围 [2, n-2]
12        int a = rand() % (n - 3) + 2, v = quickPow(a, u, n);
13        if (v == 1) continue;

```



```

14     int s;
15     for (s = 0; s < t; ++s) {
16         if (v == n - 1) break; // 得到平凡平方根 n-1, 通过此轮测试
17         v = (long long)v * v % n;
18     }
19     // 如果找到了非平凡平方根, 则会由于无法提前 break; 而运行到 s == t
20     // 如果 Fermat 素性测试无法通过, 则一直运行到 s == t 前 v 都不会等于 -1
21     if (s == t) return 0;
22 }
23 return 1;
24 }
25 int main() { return 0; }

```

### sieve.cpp

---

```

1  #include <bitset>
2  #include <iostream>
3  #include <vector>
4  using std::bitset;
5  using std::vector;
6  const int N = 1e7 + 5;
7  bitset<N> not_prime;
8  vector<int> sieve(int n) {
9      vector<int> prime;
10     for (int i = 2; i ≤ n; i++) {
11         if (!not_prime[i]) prime.emplace_back(i);
12         for (int x : prime) {
13             if (x * i > n) break;
14             not_prime[x * i] = true;
15             if (i % x == 0) break;
16         }
17     }
18     return prime;
19 }
20 int main() { return 0; }

```

### 3.3.5 crt.cpp

---

```

1  #include <iostream>
2  using LL = long long;
3  LL ex_gcd(LL a, LL b, LL &x, LL &y) {
4      if (!b) return x = 1, y = 0, a;
5      LL g = ex_gcd(b, a % b, x, y), t = x;
6      x = y, y = t - (a / b) * y;
7      return g;
8  }
9  LL CRT(int k, LL *a, LL *r) {

```

```

10     LL n = 1, ans = 0;
11     for (int i = 1; i ≤ k; i++) n = n * r[i];
12     for (int i = 1; i ≤ k; i++) {
13         LL m = n / r[i], b, y;
14         ex_gcd(m, r[i], b, y); // b * m mod r[i] = 1
15         ans = (ans + a[i] * m * b % n) % n;
16     }
17     return (ans % n + n) % n;
18 }
19 int main() { return 0; }

```

### 3.3.6 du.cpp

---

```

1  #include <cstdio>
2  #include <iostream>
3  #include <map>
4  #define int long long
5  using namespace std;
6  const int N = 2000005;
7  int p[N], mu[N], sum[N], cnt;
8  bool flg[N];
9  map<int, int> mp;
10 void init(int n) {
11     mu[1] = 1ll;
12     for (int i = 2; i ≤ n; i++) {
13         if (!flg[i]) p[++cnt] = i, mu[i] = -1;
14         for (int j = 1; j ≤ cnt && i * p[j] ≤ n; j++) {
15             flg[i * p[j]] = true;
16             if (i % p[j] == 0) {
17                 mu[i * p[j]] = 0;
18                 break;
19             }
20             mu[i * p[j]] = -mu[i];
21         }
22     }
23     for (int i = 1; i ≤ n; i++) sum[i] = sum[i - 1] + mu[i];
24 }
25 int sum_mu(int n) {
26     if (n < N) return sum[n];
27     if (mp.find(n) ≠ mp.end()) return mp[n];
28     int res = 1ll;
29     for (int i = 2, j; i ≤ n; i = j + 1) {
30         j = n / (n / i);
31         res -= sum_mu(n / i) * (j - i + 1);
32     }
33     return mp[n] = res;
34 }
35 int sum_phi(int n) {

```

```

36     int res = 0ll;
37     for (int i = 1, j; i ≤ n; i = j + 1) {
38         j = n / (n / i);
39         res += (sum_mu(j) - sum_mu(i - 1)) * (n / i) * (n / i);
40     }
41     return (res - 1) / 2 + 1;
42 }
43 signed main() {
44     cin.tie(0)->sync_with_stdio(false);
45     cout.tie(0);
46     init(N - 1);
47     int T, n;
48     cin >> T;
49     while (T--) {
50         cin >> n;
51         cout << sum_phi(n) << " " << sum_mu(n) << "\n";
52     }
53     return 0;
54 }

```

### 3.3.7 exgcd.cpp

---

```

1  #include <iostream>
2  int gcd(int a, int b) { return !b ? a : gcd(b, a % b); }
3  int ex_gcd(int a, int b, int &x, int &y) {
4      if (!b) return x = 1, y = 0, a;
5      int g = ex_gcd(b, a % b, x, y), t = x;
6      x = y, y = t - (a / b) * y;
7      return g;
8  }
9  int main() { return 0; }

```

### 3.3.8 pollard-rho.cpp

---

```

1  #include <algorithm>
2  #include <cstdlib>
3  #include <ctime>
4  #include <iostream>
5  using namespace std;
6  using ll = long long;
7  using ull = unsigned long long;
8  int t;
9  ll max_factor, n;
10 ll gcd(ll a, ll b) {
11     if (b == 0) return a;
12     return gcd(b, a % b);
13 }

```

```

14 ll bmul(ll a, ll b, ll m) { // 快速乘
15     ull c = (ull)a * (ull)b - (ull)((long double)a / m * b + 0.5L) * (ull)m;
16     if (c < (ull)m) return c;
17     return c + m;
18 }
19 ll qpow(ll x, ll p, ll mod) { // 快速幂
20     ll ans = 1;
21     while (p) {
22         if (p & 1) ans = bmul(ans, x, mod);
23         x = bmul(x, x, mod);
24         p >>= 1;
25     }
26     return ans;
27 }
28 bool Miller_Rabin(ll p) { // 判断素数
29     if (p < 2) return false;
30     if (p == 2) return true;
31     if (p == 3) return true;
32     ll d = p - 1, r = 0;
33     while (!(d & 1)) ++r, d >>= 1; // 将d处理为奇数
34     for (ll k = 0; k < 10; ++k) {
35         ll a = rand() % (p - 2) + 2;
36         ll x = qpow(a, d, p);
37         if (x == 1 || x == p - 1) continue;
38         for (int i = 0; i < r - 1; ++i) {
39             x = bmul(x, x, p);
40             if (x == p - 1) break;
41         }
42         if (x != p - 1) return false;
43     }
44     return true;
45 }
46 ll Pollard_Rho(ll x) {
47     ll s = 0, t = 0;
48     ll c = (ll)rand() % (x - 1) + 1;
49     int step = 0, goal = 1;
50     ll val = 1;
51     for (goal = 1;; goal *= 2, s = t, val = 1) { // 倍增优化
52         for (step = 1; step <= goal; ++step) {
53             t = (bmul(t, t, x) + c) % x;
54             val = bmul(val, abs(t - s), x);
55             if ((step % 127) == 0) {
56                 ll d = gcd(val, x);
57                 if (d > 1) return d;
58             }
59         }
60         ll d = gcd(val, x);
61         if (d > 1) return d;
62     }

```

```

63 }
64 void fac(ll x) {
65     if (x ≤ max_factor || x < 2) return;
66     if (Miller_Rabin(x)) { // 如果x为质数
67         max_factor = max(max_factor, x); // 更新答案
68         return;
69     }
70     ll p = x;
71     while (p ≥ x) p = Pollard_Rho(x); // 使用该算法
72     while ((x % p) == 0) x /= p;
73     fac(x), fac(p); // 继续向下分解x和p
74 }
75 int main() {
76     cin >> t;
77     while (t--) {
78         srand((unsigned)time(NULL));
79         max_factor = 0;
80         cin >> n;
81         fac(n);
82         if (max_factor == n) cout << "Prime\n";
83         else cout << max_factor << '\n';
84     }
85     return 0;
86 }

```

### 3.3.9 sqrt-decomposition.cpp

---

```

1 #include <iostream>
2 using ll = long long;
3 ll get_sum(int l, int r) { return r - l + 1; }
4 ll calc(int n) {
5     ll res = 0;
6     for (int l = 1, r = 0; l ≤ n; l = r + 1) {
7         r = n / (n / l);
8         res += get_sum(l, r);
9     }
10    return res;
11 }
12 int main() { return 0; }

```

## 3.4 poly

### 3.4.1 fft

#### divide-and-conquer.cpp

---

```

1 #include <cmath>

```

```

2  #include <cstdio>
3  #define MAXN 4000005
4  using namespace std;
5  int n, m;
6  const double PI = acos(-1.0);
7  struct CP {
8      CP(double xx = 0, double yy = 0) { x = xx, y = yy; }
9      double x, y;
10     CP operator+(const CP &B) const { return CP(x + B.x, y + B.y); }
11     CP operator-(const CP &B) const { return CP(x - B.x, y - B.y); }
12     CP operator*(const CP &B) const { return CP(x * B.x - y * B.y, x * B.y +
        y * B.x); }
13 } f[MAXN], g[MAXN], sav[MAXN];
14 void FFT(CP *f, int limit, int type) {
15     if (limit == 1) return;
16     CP *fl = f, *fr = f + limit / 2;
17     for (int i = 0; i < limit; i++) sav[i] = f[i];
18     for (int i = 0; i < limit / 2; i++) fl[i] = sav[i << 1], fr[i] = sav[i
        << 1 | 1];
19     FFT(fl, limit / 2, type);
20     FFT(fr, limit / 2, type);
21     CP Omega(cos(2.0 * PI / limit), type * sin(2.0 * PI / limit)), w(1, 0);
22     for (int i = 0; i < limit / 2; i++, w = w * Omega)
23         sav[i] = fl[i] + fr[i] * w, sav[i + limit / 2] = fl[i] - fr[i] * w;
24     for (int i = 0; i < limit; i++) f[i] = sav[i];
25 }
26 int main() {
27     scanf("%d%d", &n, &m);
28     for (int i = 0; i ≤ n; i++) scanf("%lf", &f[i].x);
29     for (int i = 0; i ≤ m; i++) scanf("%lf", &g[i].x);
30     m += n, n = 1;
31     while (n ≤ m) n <= 1;
32     FFT(f, n, 1), FFT(g, n, 1);
33     for (int i = 0; i < n; i++) f[i] = f[i] * g[i];
34     FFT(f, n, -1);
35     for (int i = 0; i ≤ m; i++) printf("%d", (int)(f[i].x / n + 0.5));
36     return 0;
37 }

```

#### iteration.cpp

---

```

1  #include <cmath>
2  #include <cstdio>
3  #include <iostream>
4  using namespace std;
5  #define db double
6  int read() {
7     int x = 0, f = 1;

```

```

8      char c = getchar();
9      while (c < '0' || c > '9') f ^= (c == '-'), c = getchar();
10     while (c ≥ '0' && c ≤ '9') x = (x << 1) + (x << 3) + (c ^ 48), c =
        getchar();
11     return f ? x : -x;
12 }
13 void write(int x) {
14     if (x < 0) putchar('-'), x = -x;
15     if (x > 9) write(x / 10);
16     putchar(x % 10 + '0');
17 }
18 const db PI = acos(-1.0);
19 struct CP {
20     db re, im;
21     CP() { re = im = 0; }
22     CP(db x, db y) { re = x, im = y; }
23     CP operator+(const CP &b) const { return CP(re + b.re, im + b.im); }
24     CP operator-(const CP &b) const { return CP(re - b.re, im - b.im); }
25     CP operator*(const CP &b) const { return CP(re * b.re - im * b.im, re *
        b.im + im * b.re); }
26 };
27 #define N 3000005
28 int n, m, rev[N];
29 CP a[N], b[N];
30 inline void init(int n) {
31     int b = log2(n);
32     for (int i = 1; i < n; i++) rev[i] = (rev[i >> 1] >> 1) + ((i & 1) << (b
        - 1));
33 }
34 inline void FFT(CP *a, int n, int op) {
35     for (int i = 0; i < n; i++)
36         if (i < rev[i]) swap(a[i], a[rev[i]]);
37     for (int len = 1; len ≤ (n >> 1); len <= 1) {
38         CP wn = CP(cos(PI / len), sin(PI / len) * op);
39         for (int i = 0; i < n; i += (len << 1)) {
40             CP w = CP(1.0, 0.0);
41             for (int j = 0; j < len; j++, w = w * wn) {
42                 CP a0 = a[i + j], a1 = w * a[i + j + len];
43                 a[i + j] = a0 + a1, a[i + j + len] = a0 - a1;
44             }
45         }
46     }
47 }
48 inline void IFFT(CP *a, int n) {
49     FFT(a, n, -1);
50     for (int i = 0; i < n; i++) a[i].re = a[i].re / n + 0.5;
51 }
52 int main() {
53     n = read(), m = read();

```

```

54     for (int i = 0; i ≤ n; i++) a[i].re = read();
55     for (int i = 0; i ≤ m; i++) b[i].re = read();
56     int len = 1;
57     while (len ≤ n + m) len <= 1;
58     init(len);
59     FFT(a, len, 1), FFT(b, len, 1);
60     for (int i = 0; i < len; i++) a[i] = a[i] * b[i];
61     IFFT(a, len);
62     for (int i = 0; i ≤ n + m; i++) write(a[i].re), putchar(' ');
63     return 0;
64 }

```

### 3.4.2 fwt.cpp

---

```

1  #include <bits/stdc++.h>
2  #include <ext/pb_ds/assoc_container.hpp>
3  #include <ext/pb_ds/hash_policy.hpp>
4  #include <ext/pb_ds/priority_queue.hpp>
5  #include <ext/pb_ds/tree_policy.hpp>
6  #include <ext/pb_ds/trie_policy.hpp>
7  #define fi first
8  #define se second
9  #define mkp make_pair
10 #define pb push_back
11 #define eb emplace_back
12 #define inf 0x3f3f3f3f
13 #define INF 0x3f3f3f3f3f3f3f3f
14 #define gi int, vector<int>, greater<int>
15 #define IOS cin.tie(0)->sync_with_stdio(false), cout.tie(0)
16 #define fo(i, begin, end)
\
17     for (__typeof(end) i = (begin) - ((begin) > (end)); i ≠ (end) - ((begin)
    ) > (end)); i += 1 - 2 * ((begin) > (end)))
18 using namespace std;
19 using namespace __gnu_pbds;
20 using db = double;
21 using ll = long long;
22 using lint = __int128;
23 using pdd = pair<db, db>;
24 using pll = pair<ll, ll>;
25 using pdl = pair<db, ll>;
26 using pdi = pair<db, int>;
27 using pil = pair<int, ll>;
28 using pii = pair<int, int>;
29 using ull = unsigned ll;
30 using uint = unsigned int;
31 inline lint read() {
32     lint x = 0;

```



```

33     bool f = 0;
34     char c = getchar();
35     while (c < '0' || c > '9') f = (c == '-'), c = getchar();
36     while (c ≥ '0' && c ≤ '9') x = (x << 1) + (x << 3) + (c ^ 48), c =
        getchar();
37     return f ? -x : x;
38 }
39 void write(lint x) {
40     if (x < 0) { putchar('-'), x = -x; }
41     if (x > 9) write(x / 10);
42     putchar(x % 10 + '0');
43 }
44 const db eps = 1e-10, PI = acos(-1.0);
45 const ll mod = 998244353, MOD = 1e9 + 7, inv2 = 499122177;
46 const int N = (1 << 17) + 5;
47 const ll Cor[2][2] = {{1, 0}, {1, 1}};
48 const ll ICor[2][2] = {{1, 0}, {mod - 1, 1}};
49 const ll Cand[2][2] = {{1, 1}, {0, 1}};
50 const ll ICand[2][2] = {{1, mod - 1}, {0, 1}};
51 const ll Cxor[2][2] = {{1, 1}, {1, mod - 1}};
52 const ll ICxor[2][2] = {{inv2, inv2}, {inv2, mod - inv2}};
53 inline void FWT(ll *f, const ll c[2][2], int n) {
54     for (int len = 1; len < n; len <= 1)
55         for (int p = 0; p < n; p += len + len)
56             for (int i = p; i < p + len; ++i) {
57                 int tmp = f[i];
58                 f[i] = (c[0][0] * f[i] + c[0][1] * f[i + len]) % mod;
59                 f[i + len] = (c[1][0] * tmp + c[1][1] * f[i + len]) % mod;
60             }
61 }
62 inline void mul(ll *f, ll *g, const ll c[2][2], const ll ic[2][2], int n) {
63     FWT(f, c, n), FWT(g, c, n);
64     fo(i, 0, n) f[i] = (f[i] * g[i]) % mod;
65     FWT(f, ic, n);
66 }
67 int n;
68 ll a[N], b[N], f[N], g[N];
69 inline void work(const ll c[2][2], const ll ic[2][2]) {
70     fo(i, 0, n) f[i] = a[i];
71     fo(i, 0, n) g[i] = b[i];
72     mul(f, g, c, ic, n);
73     fo(i, 0, n) cout << f[i] << '␣';
74     cout << '\n';
75 }
76 int main() {
77     IOS;
78     cin >> n, n = (1 << n);
79     fo(i, 0, n) cin >> a[i];
80     fo(i, 0, n) cin >> b[i];

```

```

81     work(Cor, ICor), work(Cand, ICand), work(Cxor, ICxor);
82     return 0;
83 }

```

### 3.4.3 ntt.cpp

---

```

1  #include <algorithm>
2  #include <bitset>
3  #include <cmath>
4  #include <cstdio>
5  #include <cstdlib>
6  #include <cstring>
7  #include <ctime>
8  #include <iomanip>
9  #include <iostream>
10 #include <map>
11 #include <queue>
12 #include <set>
13 #include <string>
14 #include <vector>
15 using namespace std;
16 int read() {
17     int x = 0, f = 1;
18     char ch = getchar();
19     while (ch < '0' || ch > '9') {
20         if (ch == '-') f = -1;
21         ch = getchar();
22     }
23     while (ch ≤ '9' && ch ≥ '0') {
24         x = 10 * x + ch - '0';
25         ch = getchar();
26     }
27     return x * f;
28 }
29 void print(int x) {
30     if (x < 0) putchar('-'), x = -x;
31     if (x ≥ 10) print(x / 10);
32     putchar(x % 10 + '0');
33 }
34 constexpr int N = 300100, P = 998244353;
35 int qpow(int x, int y) {
36     int res(1);
37     while (y) {
38         if (y & 1) res = 1ll * res * x % P;
39         x = 1ll * x * x % P;
40         y >>= 1;
41     }
42     return res;

```

```

43 }
44 int r[N];
45 void ntt(int *x, int lim, int opt) {
46     int i, j, k, m, gn, g, tmp;
47     for (i = 0; i < lim; ++i)
48         if (r[i] < i) swap(x[i], x[r[i]]);
49     for (m = 2; m ≤ lim; m ≤ 1) {
50         k = m >> 1;
51         gn = qpow(3, (P - 1) / m);
52         for (i = 0; i < lim; i += m) {
53             g = 1;
54             for (j = 0; j < k; ++j, g = 1ll * g * gn % P) {
55                 tmp = 1ll * x[i + j + k] * g % P;
56                 x[i + j + k] = (x[i + j] - tmp + P) % P;
57                 x[i + j] = (x[i + j] + tmp) % P;
58             }
59         }
60     }
61     if (opt == -1) {
62         reverse(x + 1, x + lim);
63         int inv = qpow(lim, P - 2);
64         for (i = 0; i < lim; ++i) x[i] = 1ll * x[i] * inv % P;
65     }
66 }
67 int A[N], B[N], C[N];
68 char a[N], b[N];
69 int main() {
70     int i, lim(1), n;
71     scanf("%s", a);
72     n = strlen(a);
73     for (i = 0; i < n; ++i) A[i] = a[n - i - 1] - '0';
74     while (lim < (n << 1)) lim <= 1;
75     scanf("%s", b);
76     n = strlen(b);
77     for (i = 0; i < n; ++i) B[i] = b[n - i - 1] - '0';
78     while (lim < (n << 1)) lim <= 1;
79     for (i = 0; i < lim; ++i) r[i] = (i & 1) * (lim >> 1) + (r[i >> 1] >> 1)
80         ;
81     ntt(A, lim, 1);
82     ntt(B, lim, 1);
83     for (i = 0; i < lim; ++i) C[i] = 1ll * A[i] * B[i] % P;
84     ntt(C, lim, -1);
85     int len(0);
86     for (i = 0; i < lim; ++i) {
87         if (C[i] ≥ 10) len = i + 1, C[i + 1] += C[i] / 10, C[i] %= 10;
88         if (C[i]) len = max(len, i);
89     }
90     while (C[len] ≥ 10) C[len + 1] += C[len] / 10, C[len] %= 10, len++;
91     for (i = len; ~i; --i) putchar(C[i] + '0');

```

```

91     puts("");
92     return 0;
93 }

```

### 3.5 bignum.cpp

---

```

1  #include <stdio>
2  #include <cstring>
3  constexpr int LEN = 1004;
4  int a[LEN], b[LEN], c[LEN], d[LEN];
5  void clear(int a[]) {
6      for (int i = 0; i < LEN; ++i) a[i] = 0;
7  }
8  void read(int a[]) {
9      static char s[LEN + 1];
10     scanf("%s", s);
11     clear(a);
12     int len = strlen(s);
13     for (int i = 0; i < len; ++i) a[len - i - 1] = s[i] - '0';
14 }
15 void print(int a[]) {
16     int i;
17     for (i = LEN - 1; i ≥ 1; --i)
18         if (a[i] ≠ 0) break;
19     for (; i ≥ 0; --i) putchar(a[i] + '0');
20     putchar('\n');
21 }
22 void add(int a[], int b[], int c[]) {
23     clear(c);
24     for (int i = 0; i < LEN - 1; ++i) {
25         c[i] += a[i] + b[i];
26         if (c[i] ≥ 10) {
27             c[i + 1] += 1;
28             c[i] -= 10;
29         }
30     }
31 }
32 void sub(int a[], int b[], int c[]) {
33     clear(c);
34     for (int i = 0; i < LEN - 1; ++i) {
35         c[i] += a[i] - b[i];
36         if (c[i] < 0) {
37             c[i + 1] -= 1;
38             c[i] += 10;
39         }
40     }
41 }

```

```

42 void mul(int a[], int b[], int c[]) {
43     clear(c);
44     for (int i = 0; i < LEN - 1; ++i) {
45         for (int j = 0; j ≤ i; ++j) c[i] += a[j] * b[i - j];
46         if (c[i] ≥ 10) {
47             c[i + 1] += c[i] / 10;
48             c[i] %= 10;
49         }
50     }
51 }
52 bool greater_eq(int a[], int b[], int last_dg, int len) {
53     if (a[last_dg + len] ≠ 0) return true;
54     for (int i = len - 1; i ≥ 0; --i) {
55         if (a[last_dg + i] > b[i]) return true;
56         if (a[last_dg + i] < b[i]) return false;
57     }
58     return true;
59 }
60 void div(int a[], int b[], int c[], int d[]) {
61     clear(c), clear(d);
62     int la, lb;
63     for (la = LEN - 1; la > 0; --la)
64         if (a[la - 1] ≠ 0) break;
65     for (lb = LEN - 1; lb > 0; --lb)
66         if (b[lb - 1] ≠ 0) break;
67     if (lb == 0) {
68         puts(">_<");
69         return;
70     }
71     for (int i = 0; i < la; ++i) d[i] = a[i];
72     for (int i = la - lb; i ≥ 0; --i) {
73         while (greater_eq(d, b, i, lb)) {
74             for (int j = 0; j < lb; ++j) {
75                 d[i + j] -= b[j];
76                 if (d[i + j] < 0) {
77                     d[i + j + 1] -= 1;
78                     d[i + j] += 10;
79                 }
80             }
81             c[i] += 1;
82         }
83     }
84 }
85 int main() {
86     read(a);
87     char op[4];
88     scanf("%s", op);
89     read(b);
90     switch (op[0]) {

```

```

91     case '+': add(a, b, c), print(c); break;
92     case '-': sub(a, b, c), print(c); break;
93     case '*': mul(a, b, c), print(c); break;
94     case '/': div(a, b, c, d), print(c), print(d); break;
95     default: puts(">_<");
96     }
97     return 0;
98 }

```

### 3.6 binary-exponentiation.cpp

---

```

1  #include <iostream>
2  using ll = long long;
3  inline ll qpow(ll a, ll b, ll mod) {
4      ll res = 1;
5      a %= mod;
6      if (b) {
7          if (b & 1) res = res * a % mod;
8          a = a * a % mod, b >>= 1;
9      }
10     return res % mod;
11 }
12 int main() { return 0; }

```

### 3.7 gauss.cpp

---

```

1  #include <algorithm>
2  #include <cmath>
3  #include <cstdio>
4  #include <iostream>
5  using namespace std;
6  double map[111][111];
7  double ans[111];
8  double eps = 1e-7;
9  int main() {
10     int n;
11     cin >> n;
12     for (int i = 1; i ≤ n; i++)
13         for (int j = 1; j ≤ n + 1; j++) scanf("%lf", &map[i][j]);
14     for (int i = 1; i ≤ n; i++) {
15         int r = i;
16         for (int j = i + 1; j ≤ n; j++)
17             if (fabs(map[r][i]) < fabs(map[j][i])) r = j; //
18             find_the_biggest_number_of_the_first_column (at present)
19         if (fabs(map[r][i]) < eps) {

```

```

19         printf("No Solution");
20         return 0;
21     }
22     if (i != r)
23         swap(map[i], map[r]); // 对换一行或一列,属于找最大当前系数的其中一步。(这
                                样就可以只处理当前行的系数啦!)
24     double div = map[i][i];
25     for (int j = i; j ≤ n + 1; j++) map[i][j] /= div;
26     for (int j = i + 1; j ≤ n; j++) {
27         div = map[j][i];
28         for (int k = i; k ≤ n + 1; k++) map[j][k] -= map[i][k] * div;
29     }
30 }
31 ans[n] = map[n][n + 1];
32 for (int i = n - 1; i ≥ 1; i--) {
33     ans[i] = map[i][n + 1];
34     for (int j = i + 1; j ≤ n; j++) ans[i] -= (map[i][j] * ans[j]);
35 } // 回带操作
36 for (int i = 1; i ≤ n; i++) printf("%.2lf\n", ans[i]);
37 return 0;
38 }

```

### 3.8 quick-pow.cpp

---

```

1  /*
2  可以在  $O(\log n)$  的时间内求出  $a^b \bmod p$  的值。
3
4  不需要任何头文件。
5
6  最初编辑人: 01bit
7  最后修改人: SnowFlavour
8  */
9
10 using ll = long long;
11 ll p;
12 ll qpow(ll x, ll y) {
13     ll z = 1;
14     while (y) {
15         if (y & 1) z = z * x % p;
16         x = x * x % p;
17         y >>= 1;
18     }
19     return z;
20 }

```

## 第 4 部分 数据结构 Data Structure

### 4.1 bst

#### 4.1.1 fhq-treap.cpp

---

```
1  #include <bits/stdc++.h>
2  using namespace std;
3  mt19937 rng(chrono::steady_clock::now().time_since_epoch().count());
4  const int N = 1e5 + 10;
5  int n, rt, L, R, p, cnt;
6  struct node {
7      int ls, rs, val, pri, siz;
8      node() {}
9      node(int _l, int _r, int _v, int _p, int _s) { ls = _l, rs = _r, val =
        _v, pri = _p, siz = _s; }
10 } t[N];
11 void pushup(int u) { t[u].siz = t[t[u].ls].siz + t[t[u].rs].siz + 1; }
12 void newnode(int x) { t[++cnt] = node(0, 0, x, rng(), 1); }
13 void split(int u, int x, int &L, int &R) {
14     if (!u) return L = R = 0, void();
15     if (t[u].val ≤ x) L = u, split(t[u].rs, x, t[u].rs, R);
16     else R = u, split(t[u].ls, x, L, t[u].ls);
17     pushup(u);
18 }
19 int merge(int L, int R) {
20     if (!L || !R) return L | R;
21     if (t[L].pri ≤ t[R].pri) return t[L].rs = merge(t[L].rs, R), pushup(L),
        L;
22     else return t[R].ls = merge(L, t[R].ls), pushup(R), R;
23 }
24 inline void Insert(int x) { newnode(x), split(rt, x, L, R), rt = merge(
    merge(L, cnt), R); }
25 inline void Delete(int x) {
26     split(rt, x - 1, L, R), split(R, x, p, R);
27     p = merge(t[p].ls, t[p].rs), rt = merge(merge(L, p), R);
28 }
29 inline int get_rank(int x) {
30     split(rt, x - 1, L, R);
31     int y = t[L].siz + 1;
32     rt = merge(L, R);
```



```

33     return y;
34 }
35 inline int get_val(int u, int k) {
36     int now = u;
37     while (now) {
38         int x = t[t[now].ls].siz + 1;
39         if (x == k) return t[now].val;
40         if (x < k) now = t[now].rs, k -= x;
41         else now = t[now].ls;
42     }
43 }
44 inline int get_pre(int x) {
45     split(rt, x - 1, L, R);
46     int y = get_val(L, t[L].siz);
47     rt = merge(L, R);
48     return y;
49 }
50 inline int get_nxt(int x) {
51     split(rt, x, L, R);
52     int y = get_val(R, 1);
53     rt = merge(L, R);
54     return y;
55 }
56 signed main() { return 0; }

```

#### 4.1.2 splay.cpp

---

```

1  const int N = 1e5 + 5;
2  int rt, siz[N], ch[N][2], val[N], tot, fa[N], cnt[N];
3  void pushup(int p) { siz[p] = siz[ch[p][0]] + siz[ch[p][1]] + cnt[p]; }
4  bool get(int p) { return p == ch[fa[p]][1]; }
5  void clear(int p) { siz[p] = ch[p][0] = ch[p][1] = val[p] = fa[p] = cnt[p]
    = 0; }
6  void rotate(int p) {
7      int f = fa[p], g = fa[f], chk = get(p);
8      ch[f][chk] = ch[p][chk ^ 1];
9      if (ch[p][chk ^ 1]) fa[ch[p][chk ^ 1]] = f;
10     ch[p][chk ^ 1] = f, fa[f] = p, fa[p] = g;
11     if (g) ch[g][f == ch[g][1]] = p;
12     pushup(f), pushup(p);
13 }
14 void splay(int p) {
15     for (int f = fa[p]; f = fa[p], f; rotate(p))
16         if (fa[f]) rotate(get(p) == get(f) ? f : p);
17     rt = p;
18 }
19 void nw(int k, int fath, int op) { val[++tot] = k, siz[tot] = cnt[tot] = 1,
    fa[tot] = fath, ch[fath][op] = tot; }

```

```

20 void ins(int k) {
21     if (!rt) {
22         val[++tot] = k, cnt[tot]++, rt = tot;
23         return pushup(rt);
24     }
25     int cur = rt, f = 0;
26     while (1) {
27         if (val[cur] == k) {
28             cnt[cur]++;
29             pushup(cur), pushup(f), splay(cur);
30             break;
31         }
32         f = cur, cur = ch[cur][val[cur] < k];
33         if (!cur) {
34             val[++tot] = k;
35             cnt[tot]++, fa[tot] = f, ch[f][val[f] < k] = tot;
36             pushup(tot), pushup(f), splay(tot);
37             break;
38         }
39     }
40 }
41 int rk(int k) {
42     int p = rt, res = 0;
43     while (true) {
44         if (k < val[p]) p = ch[p][0];
45         else {
46             res += siz[ch[p][0]];
47             if (!p) return res + 1;
48             if (val[p] == k) return splay(p), res + 1;
49             res += cnt[p], p = ch[p][1];
50         }
51     }
52 }
53 int prev() {
54     int p = ch[rt][0];
55     if (!p) return p;
56     while (ch[p][1]) p = ch[p][1];
57     return splay(p), p;
58 }
59 int next() {
60     int p = ch[rt][1];
61     if (!p) return p;
62     while (ch[p][0]) p = ch[p][0];
63     return splay(p), p;
64 }
65 void del(int k) {
66     rk(k);
67     if (cnt[rt] > 1) return --cnt[rt], pushup(rt), void();
68     if (!ch[rt][0] && !ch[rt][1]) return clear(rt), rt = 0, void();

```

```

69     if (!ch[rt][0]) {
70         int cur = rt;
71         rt = ch[rt][1], fa[rt] = 0;
72         clear(cur);
73         return;
74     }
75     if (!ch[rt][1]) {
76         int cur = rt;
77         rt = ch[rt][0], fa[rt] = 0;
78         clear(cur);
79         return;
80     }
81     int cur = rt, x = prev();
82     fa[ch[cur][1]] = x, ch[x][1] = ch[cur][1];
83     clear(cur), pushup(rt);
84 }
85 int kth(int k) {
86     int p = rt;
87     while (1) {
88         if (ch[p][0] && k ≤ siz[ch[p][0]]) p = ch[p][0];
89         else {
90             k -= cnt[p] + siz[ch[p][0]];
91             if (k ≤ 0) return splay(p), val[p];
92             p = ch[p][1];
93         }
94     }
95 }

```

## 4.2 dsu

## 4.3 dynamic-tree

### 4.3.1 lct.cpp

---

```

1  #include <bits/stdc++.h>
2  using namespace std;
3  const int N = 3e5 + 5;
4  int n, m, fa[N], ch[N][2], val[N], tag[N], sum[N];
5  inline int get(int p) { return ch[fa[p]][1] == p; }
6  inline bool is_root(int p) { return ch[fa[p]][0] ≠ p && ch[fa[p]][1] ≠ p; }
7  inline void pushup(int p) { sum[p] = sum[ch[p][0]] ^ val[p] ^ sum[ch[p][1]]; }
8  inline void reverse(int p) { swap(ch[p][0], ch[p][1]), tag[p] ^= 1; }
9  inline void pushdown(int p) {
10     if (!tag[p]) return;
11     reverse(ch[p][0]), reverse(ch[p][1]), tag[p] = 0;

```

```

12 }
13 inline void push(int p) {
14     if (!is_root(p)) push(fa[p]);
15     pushdown(p);
16 }
17 inline void rotate(int p) {
18     int f = fa[p], g = fa[f], k = get(p);
19     if (!is_root(f)) ch[g][get(f)] = p;
20     ch[f][k] = ch[p][k ^ 1], fa[ch[p][k ^ 1]] = f;
21     ch[p][k ^ 1] = f, fa[f] = p, fa[p] = g;
22     pushup(f), pushup(p);
23 }
24 void splay(int p) {
25     push(p);
26     for (int f; f = fa[p], !is_root(p); rotate(p))
27         if (!is_root(f)) rotate(get(p) == get(f) ? f : p);
28 }
29 inline void access(int p) {
30     for (int child = 0; p; child = p, p = fa[p]) splay(p), ch[p][1] = child,
31         pushup(p);
32 }
33 inline void makeroot(int p) { access(p), splay(p), reverse(p); }
34 inline void split(int u, int v) { makeroot(u), access(v), splay(v); }
35 inline int findroot(int p) {
36     access(p), splay(p), pushdown(p);
37     while (ch[p][0]) p = ch[p][0], pushdown(p);
38     return splay(p), p;
39 }
40 inline void link(int u, int v) { makeroot(u), fa[u] = v; }
41 inline void cut(int u, int v) {
42     makeroot(u);
43     if (findroot(v) == u && fa[v] == u && !ch[v][0]) fa[v] = ch[u][1] = 0,
44         pushup(u);
45 }
46 int main() {
47     cin.tie(0) -> sync_with_stdio(false);
48     cout.tie(0);
49     cin >> n >> m;
50     for (int i = 1; i ≤ n; i++) cin >> val[i];
51     for (int op, x, y; m--;) {
52         cin >> op >> x >> y;
53         switch (op) {
54             case 0: split(x, y), cout << sum[y] << '\n'; break;
55             case 1:
56                 if (findroot(x) ≠ findroot(y)) link(x, y);
57                 break;
58             case 2: cut(x, y); break;
59             case 3: splay(x), val[x] = y; break;
60         }
61     }
62 }

```

```

59     }
60     return 0;
61 }

```

## 4.4 fenwick

### 4.4.1 fenwick-1.cpp

---

```

1  #include <iostream>
2  using namespace std;
3  const int N = 5e5 + 10;
4  int n, m, a[N];
5  struct BIT {
6      int tr[N];
7      inline int lowbit(int x) { return x & -x; }
8      inline void upd(int x, int c) {
9          while (x ≤ n) tr[x] += c, x += lowbit(x);
10     }
11     inline int que(int x) {
12         int res = 0;
13         while (x) res += tr[x], x -= lowbit(x);
14         return res;
15     }
16 } tree;
17 int main() {
18     ios::sync_with_stdio(false);
19     cin.tie(0);
20     cout.tie(0);
21     cin >> n >> m;
22     for (int i = 1; i ≤ n; i++) cin >> a[i], tree.upd(i, a[i]);
23     while (m--) {
24         int op, x, y;
25         cin >> op >> x >> y;
26         if (op == 1) tree.upd(x, y);
27         else cout << tree.que(y) - tree.que(x - 1) << "\n";
28     }
29     return 0;
30 }

```

### 4.4.2 fenwick-2.cpp

---

```

1  #include <iostream>
2  using namespace std;
3  const int N = 500005;
4  int n, m, a[N], s[N], t[N];
5  inline int lowbit(int s) { return s & -s; }

```

```

6  inline void add(int x, int k) {
7      for (; x ≤ n; x += lowbit(x)) t[x] += k;
8  }
9  inline int query(int x) {
10     int res = 0;
11     for (; x; x -= lowbit(x)) res += t[x];
12     return res;
13 }
14 int main() {
15     ios::sync_with_stdio(false);
16     cin.tie(0);
17     cout.tie(0);
18     cin >> n >> m;
19     for (int i = 1; i ≤ n; i++) cin >> a[i];
20     while (m--) {
21         int op, x, y, k;
22         cin >> op >> x;
23         if (op == 1) {
24             cin >> y >> k;
25             add(x, k);
26             add(y + 1, -k);
27         } else cout << a[x] + query(x) << "\n";
28     }
29     return 0;
30 }

```

## 4.5 segment-tree

### 4.5.1 persistant

persistant-seg1.cpp

---

```

1  #include <cstdio>
2  using namespace std;
3  const int N = 1e6 + 5;
4  int n, m, a[N], tot;
5  int root[N], cnt;
6  struct node {
7     int ls, rs;
8     int val;
9 } tree[N * 30];
10 int build(int pl, int pr) {
11     int rt = tot++;
12     if (pl == pr) {
13         tree[rt].val = a[pl];
14         return rt;
15     }
16     int mid = (pl + pr) >> 1;

```

```

17     tree[rt].ls = build(pl, mid);
18     tree[rt].rs = build(mid + 1, pr);
19     return rt;
20 }
21 int update(int pre, int pl, int pr, int loc, int val) {
22     int rt = tot++;
23     if (pl == pr) {
24         tree[rt].val = val;
25         return rt;
26     }
27     int mid = (pl + pr) >> 1;
28     tree[rt].ls = tree[pre].ls;
29     tree[rt].rs = tree[pre].rs;
30     if (loc ≤ mid) tree[rt].ls = update(tree[pre].ls, pl, mid, loc, val);
31     else tree[rt].rs = update(tree[pre].rs, mid + 1, pr, loc, val);
32     return rt;
33 }
34 int query(int p, int pl, int pr, int loc) {
35     if (pl == pr) return tree[p].val;
36     int mid = (pl + pr) >> 1;
37     if (loc ≤ mid) return query(tree[p].ls, pl, mid, loc);
38     else return query(tree[p].rs, mid + 1, pr, loc);
39 }
40 int main() {
41     scanf("%d%d", &n, &m);
42     for (int i = 1; i ≤ n; i++) scanf("%d", &a[i]);
43     root[cnt++] = build(1, n);
44     while (m--) {
45         int v, op, loc, val;
46         scanf("%d%d%d", &v, &op, &loc);
47         if (op == 1) {
48             scanf("%d", &val);
49             root[cnt++] = update(root[v], 1, n, loc, val);
50         } else {
51             root[cnt++] = root[v];
52             int res = query(root[v], 1, n, loc);
53             printf("%d\n", res);
54         }
55     }
56     return 0;
57 }

```

persistent-seg2.cpp

---

```

1 #include <algorithm>
2 #include <cstdio>
3 #include <iostream>
4 #define endl '\n'

```

```

5  using std::cin;
6  using std::cout;
7  using std::lower_bound;
8  using std::sort;
9  using std::unique;
10 const int N = 2e5 + 5;
11 int n, m, a[N], b[N], size, tot;
12 int root[N], vcnt;
13 struct node {
14     int l, r;
15     int sum;
16 } tree[N * 30];
17 int build(int pl, int pr) {
18     int rt = ++tot;
19     tree[rt].sum = 0;
20     int mid = (pl + pr) >> 1;
21     if (pl < pr) {
22         tree[rt].l = build(pl, mid);
23         tree[rt].r = build(mid + 1, pr);
24     }
25     return rt;
26 }
27 int update(int pre, int pl, int pr, int x) {
28     int rt = ++tot;
29     tree[rt].l = tree[pre].l;
30     tree[rt].r = tree[pre].r;
31     tree[rt].sum = tree[pre].sum + 1;
32     int mid = (pl + pr) >> 1;
33     if (pl < pr) {
34         if (x ≤ mid) tree[rt].l = update(tree[pre].l, pl, mid, x);
35         else tree[rt].r = update(tree[pre].r, mid + 1, pr, x);
36     }
37     return rt;
38 }
39 int query(int u, int v, int pl, int pr, int k) {
40     if (pl == pr) return pl;
41     int x = tree[tree[v].l].sum - tree[tree[u].l].sum;
42     int mid = (pl + pr) >> 1;
43     if (x ≥ k) return query(tree[u].l, tree[v].l, pl, mid, k);
44     else return query(tree[u].r, tree[v].r, mid + 1, pr, k - x);
45 }
46 int main() {
47     cin >> n >> m;
48     for (int i = 1; i ≤ n; i++) {
49         cin >> a[i];
50         b[i] = a[i];
51     }
52     sort(b + 1, b + 1 + n);
53     size = unique(b + 1, b + 1 + n) - (b + 1);

```



```

54     root[0] = build(1, size);
55     for (int i = 1; i ≤ n; i++) {
56         int x = lower_bound(b + 1, b + 1 + size, a[i]) - b;
57         root[i] = update(root[i - 1], 1, size, x);
58     }
59     while (m--) {
60         int l, r, k;
61         cin >> l >> r >> k;
62         int res = query(root[l - 1], root[r], 1, size, k);
63         cout << b[res] << endl;
64     }
65     return 0;
66 }

```

#### 4.5.2 lc-segment.cpp

---

```

1  #include <bits/stdc++.h>
2  using namespace std;
3  using ll = long long;
4  using pdi = pair<double, int>;
5  constexpr int N = 4e4 + 5, M1 = 39989, M2 = 1e9;
6  constexpr double eps = 1e-9;
7  int comp(double a, double b) {
8      if (a - b > eps) return 1;
9      if (b - a > eps) return -1;
10     return 0;
11 }
12 struct LiChaoT {
13     int cnt, t[N << 2];
14     struct line {
15         double k, b;
16         double operator()(int x) { return k * x + b; }
17     } seg[N << 2];
18     void add(int x1, int y1, int x2, int y2) {
19         double k, b;
20         if (x2 == x1) k = 0, b = max(y1, y2);
21         else k = 1.0 * (y2 - y1) / (x2 - x1), b = y1 - x1 * k;
22         seg[++cnt] = {k, b};
23     }
24     void update(int rt, int L, int R, int x) {
25         int &v = t[rt];
26         int mid = (L + R) / 2;
27         if (comp(seg[v](mid), seg[x](mid)) < 0) swap(v, x);
28         if (comp(seg[v](L), seg[x](L)) < 0) update(rt << 1, L, mid, x);
29         if (comp(seg[v](R), seg[x](R)) < 0) update(rt << 1 | 1, mid + 1, R, x);
30     }
31     void insert(int rt, int L, int R, int l, int r, int x) {

```

```

32     if (l ≤ L && R ≤ r) return update(rt, L, R, x);
33     int mid = (L + R) / 2;
34     if (l ≤ mid) insert(rt << 1, L, mid, l, r, x);
35     if (r > mid) insert(rt << 1 | 1, mid + 1, R, l, r, x);
36 }
37 pdi mx(pdi a, pdi b) {
38     int c = comp(a.first, b.first);
39     if (c > 0) return a;
40     if (c < 0) return b;
41     return a.second < b.second ? a : b;
42 }
43 pdi query(int rt, int L, int R, int x) {
44     if (x < L || x > R) return {0, 0};
45     pdi ret = {seg[t[rt]](x), t[rt]};
46     if (L == R) return ret;
47     int mid = (L + R) / 2;
48     return mx(ret, mx(query(rt << 1, L, mid, x), query(rt << 1 | 1, mid +
        1, R, x)));
49 }
50 } t;
51 int main() {
52     cin.tie(nullptr), cout.tie(nullptr);
53     ios::sync_with_stdio(0);
54     int n, last = 0;
55     cin >> n;
56     for (int i = 1; i ≤ n; i++) {
57         int op, k, x, y, xx, yy;
58         cin >> op;
59         if (op == 0) {
60             cin >> k;
61             k = (k + last - 1) % M1 + 1;
62             cout << (last = t.query(1, 0, 40000, k).second) << '\n';
63         } else {
64             cin >> x >> y >> xx >> yy;
65             x = (x + last - 1) % M1 + 1, xx = (xx + last - 1) % M1 + 1;
66             y = (y + last - 1) % M2 + 1, yy = (yy + last - 1) % M2 + 1;
67             t.add(x, y, xx, yy), t.insert(1, 0, 40000, min(x, xx), max(x, xx),
                t.cnt);
68         }
69     }
70     return 0;
71 }

```

### 4.5.3 sgt-1.cpp

---

```

1 #include <iostream>
2 using namespace std;
3 using ll = long long;

```

```

4 namespace segment_tree {
5 #define ls (p << 1)
6 #define rs (p << 1 | 1)
7 #define mid (pl + pr >> 1)
8 const int N = 1e6 + 5;
9 int sum[N], tag[N];
10 inline void up(int p) { sum[p] = sum[ls] + sum[rs]; }
11 inline void spread(int p, int pl, int pr) {
12     if (!tag[p]) return;
13     tag[ls] += tag[p], tag[rs] += tag[p];
14     sum[ls] += tag[p] * (mid - pl + 1), sum[rs] += tag[p] * (pr - mid);
15     tag[p] = 0;
16 }
17 void build(int p, int pl, int pr, int *a) {
18     if (pl == pr) return sum[p] = a[pl], void();
19     build(ls, pl, mid, a), build(rs, mid + 1, pr, a), up(p);
20 }
21 void update(int p, int pl, int pr, int L, int R, int v) {
22     if (L ≤ pl && pr ≤ R) return sum[p] += v, void();
23     spread(p, pl, pr);
24     if (L ≤ mid) update(ls, pl, mid, L, R, v);
25     if (R > mid) update(rs, mid + 1, pr, L, R, v);
26     up(p);
27 }
28 int query(int p, int pl, int pr, int L, int R) {
29     if (L ≤ pl && pr ≤ R) return sum[p];
30     spread(p, pl, pr);
31     int res(0);
32     if (L ≤ mid) res += query(ls, pl, mid, L, R);
33     if (R > mid) res += query(rs, mid + 1, pr, L, R);
34     return res;
35 }
36 }; // namespace segment_tree
37 int main() { return 0; }

```

#### 4.5.4 sgt-2.cpp

---

```

1 #include <cstdio>
2 #include <iostream>
3 #define int long long
4 using namespace std;
5 int n, m, mod, a[101000];
6 struct node {
7     int l, r, sum;
8     int add, mul;
9 } t[401000];
10 void build(int p, int l, int r) {
11     t[p].l = l, t[p].r = r;

```

```

12     t[p].mul = 1, t[p].add = 0;
13     if (l == r) {
14         t[p].sum = a[l];
15         return;
16     }
17     int mid = (l + r) / 2;
18     build(p * 2, l, mid);
19     build(p * 2 + 1, mid + 1, r);
20     t[p].sum = t[p * 2].sum + t[p * 2 + 1].sum;
21 }
22 void push_down(int p) {
23     if (t[p].mul != 1) {
24         t[p * 2].mul *= t[p].mul, t[p * 2].mul %= mod;
25         t[p * 2 + 1].mul *= t[p].mul, t[p * 2 + 1].mul %= mod;
26         t[p * 2].sum *= t[p].mul, t[p * 2].sum %= mod;
27         t[p * 2 + 1].sum *= t[p].mul, t[p * 2 + 1].sum %= mod;
28         t[p * 2].add *= t[p].mul, t[p * 2].add %= mod;
29         t[p * 2 + 1].add *= t[p].mul, t[p * 2 + 1].add %= mod;
30         t[p].mul = 1;
31     }
32     if (t[p].add != 0) {
33         t[p * 2].add += t[p].add, t[p * 2].add %= mod;
34         t[p * 2 + 1].add += t[p].add, t[p * 2 + 1].add %= mod;
35         t[p * 2].sum += t[p].add * (t[p * 2].r - t[p * 2].l + 1), t[p * 2].
            sum %= mod;
36         t[p * 2 + 1].sum += t[p].add * (t[p * 2 + 1].r - t[p * 2 + 1].l + 1),
            t[p * 2 + 1].sum %= mod;
37         t[p].add = 0;
38     }
39 }
40 void mulnum(int p, int dat, int l, int r) {
41     if (l ≤ t[p].l && r ≥ t[p].r) {
42         t[p].mul *= dat, t[p].mul %= mod;
43         t[p].sum *= dat, t[p].sum %= mod;
44         t[p].add *= dat, t[p].add %= mod;
45         return;
46     }
47     push_down(p);
48     int mid = (t[p].l + t[p].r) / 2;
49     if (l ≤ mid) mulnum(p * 2, dat, l, r);
50     if (r > mid) mulnum(p * 2 + 1, dat, l, r);
51     t[p].sum = t[p * 2].sum + t[p * 2 + 1].sum;
52 }
53 void addnum(int p, int dat, int l, int r) {
54     if (l ≤ t[p].l && r ≥ t[p].r) {
55         t[p].add += dat, t[p].add %= mod;
56         t[p].sum += dat * (t[p].r - t[p].l + 1), t[p].sum %= mod;
57         return;
58     }

```

```

59     push_down(p);
60     int mid = (t[p].l + t[p].r) / 2;
61     if (l ≤ mid) addnum(p * 2, dat, l, r);
62     if (r > mid) addnum(p * 2 + 1, dat, l, r);
63     t[p].sum = t[p * 2].sum + t[p * 2 + 1].sum;
64 }
65 int query(int p, int l, int r) {
66     if (l ≤ t[p].l && r ≥ t[p].r) return t[p].sum % mod;
67     push_down(p);
68     int mid = (t[p].l + t[p].r) / 2, val = 0;
69     if (l ≤ mid) val += query(p * 2, l, r);
70     if (r > mid) val += query(p * 2 + 1, l, r);
71     return val % mod;
72 }
73 signed main() {
74     cin >> n >> m >> mod;
75     for (int i = 1; i ≤ n; i++) cin >> a[i];
76     build(1, 1, n);
77     while (m--) {
78         int op, x, y, k;
79         cin >> op >> x >> y;
80         if (op == 1) {
81             cin >> k;
82             mulnum(1, k, x, y);
83         } else if (op == 2) {
84             cin >> k;
85             addnum(1, k, x, y);
86         } else cout << query(1, x, y) << endl;
87     }
88     return 0;
89 }

```

#### 4.5.5 sgt-merge.cpp

---

```

1  #include <cstdio>
2  #include <iostream>
3  using namespace std;
4  const int N = 100005, M = 100000;
5  int n, m, head[N], tot, ans[N];
6  struct edge {
7     int v, nxt;
8 } e[N << 1];
9 inline void add(int u, int v) {
10     e[++tot].v = v;
11     e[tot].nxt = head[u];
12     head[u] = tot;
13 }
14 int fa[N], dep[N], siz[N], hson[N], dfn[N], top[N], Time;

```

```

15 void dfs1(int u, int fath) {
16     fa[u] = fath, dep[u] = dep[fath] + 1, siz[u] = 1;
17     for (int i = head[u]; i; i = e[i].nxt) {
18         int v = e[i].v;
19         if (v == fath) continue;
20         dfs1(v, u);
21         siz[u] += siz[v];
22         if (!hson[u] || siz[v] > siz[hson[u]]) hson[u] = v;
23     }
24 }
25 void dfs2(int u, int tp) {
26     top[u] = tp, dfn[u] = ++Time;
27     if (hson[u]) dfs2(hson[u], tp);
28     for (int i = head[u]; i; i = e[i].nxt)
29         if (e[i].v != fa[u] && e[i].v != hson[u]) dfs2(e[i].v, e[i].v);
30 }
31 inline int LCA(int x, int y) {
32     while (top[x] != top[y]) {
33         if (dep[top[x]] < dep[top[y]]) swap(x, y);
34         x = fa[top[x]];
35     }
36     return dep[x] ≤ dep[y] ? x : y;
37 }
38 int cnt = 0, rt[N];
39 struct node {
40     int mx, id;
41     int ls, rs;
42 } t[N * 100];
43 void pushup(int p) {
44     if (t[t[p].ls].mx ≥ t[t[p].rs].mx) t[p].mx = t[t[p].ls].mx, t[p].id = t[t[p].ls].id;
45     else t[p].mx = t[t[p].rs].mx, t[p].id = t[t[p].rs].id;
46 }
47 void update(int &p, int pl, int pr, int k, int val) {
48     if (!p) p = ++cnt;
49     if (pl == pr) {
50         t[p].mx += val, t[p].id = k;
51         return;
52     }
53     int mid = (pl + pr) >> 1;
54     if (k ≤ mid) update(t[p].ls, pl, mid, k, val);
55     else update(t[p].rs, mid + 1, pr, k, val);
56     pushup(p);
57 }
58 int merge(int &L, int &R, int pl, int pr) {
59     if (!L) return R;
60     if (!R) return L;
61     if (pl == pr) {
62         t[L].mx += t[R].mx;

```

```

63     return L;
64 }
65 int mid = (pl + pr) >> 1;
66 t[L].ls = merge(t[L].ls, t[R].ls, pl, mid);
67 t[L].rs = merge(t[L].rs, t[R].rs, mid + 1, pr);
68 pushup(L);
69 return L;
70 }
71 void dfs(int u) {
72     for (int i = head[u]; i; i = e[i].nxt) {
73         int v = e[i].v;
74         if (v == fa[u]) continue;
75         dfs(v);
76         rt[u] = merge(rt[u], rt[v], 1, M);
77     }
78     ans[u] = t[rt[u]].id;
79     if (!t[rt[u]].mx) ans[u] = 0;
80 }
81 int main() {
82     ios::sync_with_stdio(false);
83     cin.tie(0);
84     cout.tie(0);
85     cin >> n >> m;
86     for (int i = 1; i < n; i++) {
87         int u, v;
88         cin >> u >> v;
89         add(u, v);
90         add(v, u);
91     }
92     dfs1(1, 0);
93     dfs2(1, 1);
94     while (m--) {
95         int l, r, z;
96         cin >> l >> r >> z;
97         update(rt[l], 1, M, z, 1);
98         update(rt[r], 1, M, z, 1);
99         int lca = LCA(l, r);
100         update(rt[lca], 1, M, z, -1);
101         update(rt[fa[lca]], 1, M, z, -1);
102     }
103     dfs(1);
104     for (int i = 1; i ≤ n; i++) cout << ans[i] << "\n";
105     return 0;
106 }

```

#### 4.5.6 sgt-split.cpp

---

```

1 #include <cstdio>

```

```

2  #include <iostream>
3  #define int long long
4  using namespace std;
5  const int N = 2e5 + 5;
6  int n, m, root[N << 2], rcnt = 1, rub[N << 5], cnt, nodecnt;
7  struct treenode {
8      int ls, rs, sum;
9  } tr[N << 5];
10 inline int newnode() { return cnt ? rub[cnt--] : ++nodecnt; }
11 inline void del(int &p) { tr[p].ls = tr[p].rs = tr[p].sum = 0, rub[++cnt] =
    p, p = 0; }
12 inline void push_up(int p) { tr[p].sum = tr[tr[p].ls].sum + tr[tr[p].rs].
    sum; }
13 inline void build(int &p, int pl, int pr) {
14     if (!p) p = newnode();
15     if (pl == pr) return cin >> tr[p].sum, void();
16     int mid = (pl + pr) >> 1;
17     build(tr[p].ls, pl, mid), build(tr[p].rs, mid + 1, pr);
18     push_up(p);
19 }
20 inline void update(int &p, int pl, int pr, int pos, int k) {
21     if (!p) p = newnode();
22     if (pl == pr) return tr[p].sum += k, void();
23     int mid = (pl + pr) >> 1;
24     if (pos ≤ mid) update(tr[p].ls, pl, mid, pos, k);
25     else update(tr[p].rs, mid + 1, pr, pos, k);
26     push_up(p);
27 }
28 inline int merge(int p, int q, int pl, int pr) {
29     if (!p || !q) return p + q;
30     if (pl == pr) return tr[p].sum += tr[q].sum, del(q), p;
31     int mid = (pl + pr) >> 1;
32     tr[p].ls = merge(tr[p].ls, tr[q].ls, pl, mid);
33     tr[p].rs = merge(tr[p].rs, tr[q].rs, mid + 1, pr);
34     return push_up(p), del(q), p;
35 }
36 inline void split(int &p, int &q, int pl, int pr, int L, int R) {
37     if (R < pl || L > pr) return;
38     if (!p) return;
39     if (L ≤ pl && pr ≤ R) return q = p, p = 0, void();
40     int mid = (pl + pr) >> 1;
41     if (!q) q = newnode();
42     if (L ≤ mid) split(tr[p].ls, tr[q].ls, pl, mid, L, R);
43     if (R > mid) split(tr[p].rs, tr[q].rs, mid + 1, pr, L, R);
44     push_up(p), push_up(q);
45 }
46 inline int query(int p, int pl, int pr, int L, int R) {
47     if (!p) return 0;
48     if (L ≤ pl && pr ≤ R) return tr[p].sum;

```



```

49     int mid = (pl + pr) >> 1, res = 0;
50     if (L ≤ mid) res += query(tr[p].ls, pl, mid, L, R);
51     if (R > mid) res += query(tr[p].rs, mid + 1, pr, L, R);
52     return res;
53 }
54 inline int kth(int p, int pl, int pr, int k) {
55     if (pl == pr) return pl;
56     int mid = (pl + pr) >> 1, left = tr[tr[p].ls].sum;
57     if (k ≤ left) return kth(tr[p].ls, pl, mid, k);
58     else return kth(tr[p].rs, mid + 1, pr, k - left);
59 }
60 signed main() {
61     cin.tie(0)->sync_with_stdio(false);
62     cout.tie(0);
63     cin >> n >> m;
64     build(root[1], 1, n);
65     for (int i = 1, op, p, x, y; i ≤ m; i++) {
66         cin >> op >> p >> x;
67         if (op == 0 || op == 2 || op == 3) cin >> y;
68         if (op == 0) split(root[p], root[++rcnt], 1, n, x, y);
69         else if (op == 1) root[p] = merge(root[p], root[x], 1, n);
70         else if (op == 2) update(root[p], 1, n, y, x);
71         else if (op == 3) cout << query(root[p], 1, n, x, y) << "\n";
72         else if (op == 4) {
73             if (tr[root[p]].sum < x) cout << "-1\n";
74             else cout << kth(root[p], 1, n, x) << "\n";
75         }
76     }
77     return 0;
78 }

```

## 4.6 st-table

## 4.7 dsu.cpp

---

```

1  #include <bits/stdc++.h>
2  using namespace std;
3  struct dsu {
4      vector<size_t> pa, size;
5      explicit dsu(size_t size_) : pa(size_), size(size_, 1) { iota(pa.begin(),
6          , pa.end(), 0); }
7      inline size_t find(int x) { return pa[x] == x ? x : pa[x] = find(pa[x]); }
8      void unite(size_t x, size_t y) {
9          x = find(x), y = find(y);
10         if (x == y) return;
11         if (size[x] < size[y]) swap(x, y);

```

```

11     pa[y] = x;
12     size[x] += size[y];
13 }
14 void erase(size_t x) { --size[find(x)], pa[x] = x; }
15 void dsu::move(size_t x, size_t y) {
16     auto fx = find(x), fy = find(y);
17     if (fx == fy) return;
18     pa[x] = fy;
19     --size[fx], ++size[fy];
20 }
21 };

```

## 4.8 st-table.cpp

---

```

1  #include <cmath>
2  #include <cstdio>
3  #include <iostream>
4  using namespace std;
5  int n, m, a[1010000], st[1010000][200];
6  int main() {
7      cin >> n >> m;
8      for (int i = 1; i ≤ n; i++) scanf("%d", a + i), st[i][i] = a[i];
9      for (int j = 1; 1 + (1 << j) ≤ n; j++)
10         for (int i = 1; i + (1 << j) - 1 ≤ n; i++) st[i][j] = max(st[i][j -
11             1], st[i + (1 << j - 1)][j - 1]);
12     while (m--) {
13         int l, r, ans;
14         scanf("%d%d", &l, &r);
15         int t = log2(r - l + 1);
16         ans = max(st[l][t], st[r - (1 << t) + 1][t]);
17         printf("%d\n", ans);
18     }
19     return 0;

```

## 第 5 部分 杂项 Misc

### 5.1 offline

#### 5.1.1 mo

mo-algo.cpp

---

```
1 void move(int pos, int sign) { ... }
2 int unit;
3 struct node {
4     int l, r, id;
5     bool operator<(const node &x) const {
6         return l / unit == x.l / unit ? (r == x.r ? 0 : ((l / unit) & 1) ^ (r
          < x.r)) : l < x.l;
7     }
8 } queries[N];
9 void solve() {
10     unit = int(ceil(pow(n, 0.5)));
11     sort(queries, queries + m);
12     for (int i = 0; i < m; ++i) {
13         const node &q = queries[i];
14         while (l > q.l) move(--l, 1);
15         while (r < q.r) move(++r, 1);
16         while (l < q.l) move(l++, -1);
17         while (r > q.r) move(r--, -1);
18         ans[q.id] = nowAns;
19     }
20 }
```

secondary-offline.cpp

---

```
1 #include <bits/stdc++.h>
2 using namespace std;
3 using ll = long long;
4 inline int rd() {
5     int x = 0, f = 1;
6     char c = getchar();
7     while (c < '0' || c > '9') f ^= (c == '-'), c = getchar();
8     while (c ≥ '0' && c ≤ '9') x = (x << 1) + (x << 3) + (c ^ 48), c =
        getchar();
```

```

9      return f ? x : -x;
10 }
11 inline void wr(ll x) {
12     if (x < 0) putchar('-'), x = -x;
13     if (x > 9) wr(x / 10);
14     putchar(x % 10 + '0');
15 }
16 const int N = 1e5 + 5;
17 int n, m, a[N], b[N], V, tot;
18 int st[N], ed[N], pos[N], B;
19 struct que {
20     int l, r, id;
21     inline bool operator<(const que &b) const { return (l / tot == b.l / tot
22         ) ? r < b.r : l < b.l; }
23 } q[N];
24 ll ans[N];
25 struct ask {
26     int id, op, l, r;
27     ask() { id = op = l = r = 0; }
28     ask(int _id, int _op, int _l, int _r) { id = _id, op = _op, l = _l, r =
29         _r; }
30 };
31 ll tr[N];
32 inline void add(int x, int v) {
33     for (; x ≤ n; x += x & -x) tr[x] += (ll)v;
34 }
35 inline ll qry(int x) {
36     ll res = 0;
37     for (; x; x -= x & -x) res += tr[x];
38     return res;
39 }
40 int le[N], ri[N];
41 ll sl[N], sr[N];
42 vector<ask> v1[N], v2[N];
43 inline void addl(int pos, int op, int l, int r, int id) { v1[pos].push_back
44     (ask(id, op, l, r)); }
45 inline void addr(int pos, int op, int l, int r, int id) { v2[pos].push_back
46     (ask(id, op, l, r)); }
47 ll val[N], tag[N];
48 inline void updl(int x) {
49     if (tag[pos[x]])
50         for (int i = st[pos[x]]; i ≤ ed[pos[x]]; i++) val[i] += tag[pos[x]];
51     tag[pos[x]] = 0;
52     for (int i = st[pos[x]]; i ≤ x; i++) val[i]++;
53     for (int i = 1; i < pos[x]; i++) tag[i]++;
54 }
55 inline void updr(int x) {
56     if (tag[pos[x]])
57         for (int i = st[pos[x]]; i ≤ ed[pos[x]]; i++) val[i] += tag[pos[x]];

```

```

54     tag[pos[x]] = 0;
55     for (int i = x; i ≤ ed[pos[x]]; i++) val[i]++;
56     for (int i = pos[x] + 1; i ≤ B; i++) tag[i]++;
57 }
58 signed main() {
59     n = rd(), m = rd(), tot = 355, sl[0] = sr[n + 1] = 0;
60     for (int i = 1; i ≤ n; i++) b[i] = a[i] = rd();
61     sort(b + 1, b + 1 + n);
62     V = unique(b + 1, b + 1 + n) - (b + 1);
63     for (int i = 1; i ≤ n; i++) a[i] = lower_bound(b + 1, b + 1 + V, a[i])
        - b;
64     for (int i = 1; i ≤ n; i++) le[i] += (i - 1 - qry(a[i])), add(a[i], 1),
        sl[i] = sl[i - 1] + le[i];
65     for (int i = 0; i ≤ n; i++) tr[i] = 0;
66     for (int i = n; i ≥ 1; i--) ri[i] += qry(a[i] - 1), add(a[i], 1), sr[i]
        = sr[i + 1] + ri[i];
67     for (int i = 1; i ≤ m; i++) q[i].l = rd(), q[i].r = rd(), q[i].id = i;
68     sort(q + 1, q + 1 + m);
69     int l = 1, r = 0;
70     for (int i = 1; i ≤ m; i++) {
71         if (r < q[i].r) ans[q[i].id] += sl[q[i].r] - sl[r], addl(l, -1, r +
            1, q[i].r, q[i].id), r = q[i].r;
72         if (r > q[i].r) ans[q[i].id] -= sl[r] - sl[q[i].r], addl(l, 1, q[i].r
            + 1, r, q[i].id), r = q[i].r;
73         if (l < q[i].l) ans[q[i].id] -= sr[l] - sr[q[i].l], addr(r, 1, l, q[i]
            ].l - 1, q[i].id), l = q[i].l;
74         if (l > q[i].l) ans[q[i].id] += sr[q[i].l] - sr[l], addr(r, -1, q[i].
            l, l - 1, q[i].id), l = q[i].l;
75     }
76     B = sqrt(V);
77     for (int i = 1; i ≤ B; i++) st[i] = (i - 1) * B + 1, ed[i] = i * B;
78     if (ed[B] < V) ed[B] = V;
79     for (int i = 1; i ≤ B; i++)
80         for (int j = st[i]; j ≤ ed[i]; j++) pos[j] = i;
81     for (int i = 1; i ≤ n; i++) {
82         for (ask now : v1[i])
83             for (int j = now.l; j ≤ now.r; j++) ans[now.id] += (ll)now.op * (
                tag[pos[a[j] + 1]] + val[a[j] + 1]);
84         updl(a[i]);
85     }
86     for (int i = 0; i ≤ n; i++) tag[i] = val[i] = 0;
87     for (int i = n; i ≥ 1; i--) {
88         for (ask now : v2[i])
89             for (int j = now.l; j ≤ now.r; j++) ans[now.id] += (ll)now.op * (
                tag[pos[a[j] - 1]] + val[a[j] - 1]);
90         updr(a[i]);
91     }
92     for (int i = 1; i ≤ m; i++) ans[q[i].id] += ans[q[i - 1].id];
93     for (int i = 1; i ≤ m; i++) wr(ans[i]), puts("");

```

```

94     return 0;
95 }

```

## 5.2 odt.cpp

---

```

1  #include <algorithm>
2  #include <cstdio>
3  #include <iostream>
4  #include <set>
5  #include <vector>
6  #define int long long
7  using namespace std;
8  const int N = 1e5 + 5, mod = 1e9 + 7;
9  int n, m, seed, vmax, a[N];
10 int rnd() {
11     int ret = seed;
12     seed = (seed * 7 + 13) % mod;
13     return ret;
14 }
15 int qpow(int a, int b, int Mod) {
16     long long res = 1;
17     a %= Mod;
18     while (b) {
19         if (b & 1) res = res * a % Mod;
20         a = a * a % Mod, b >>= 1;
21     }
22     return res;
23 }
24 struct node {
25     int l, r;
26     mutable int v;
27     node(const int &ll, const int &rr, const int &vv) : l(ll), r(rr), v(vv) {}
28     bool operator<(const node &b) const { return l < b.l; }
29 };
30 set<node> st;
31 typedef set<node>::iterator it;
32 it split(int x) {
33     if (x > n) return st.end();
34     it I = st.lower_bound((node){x, 0, 0});
35     if (I != st.end() && I->l == x) return I;
36     I--;
37     if (I->r < x) return st.end();
38     int l = I->l, r = I->r, v = I->v;
39     st.erase(I);
40     st.insert(node(l, x - 1, v));
41     return st.insert(node(x, r, v)).first;

```

```

42 }
43 void assign(int l, int r, int v) {
44     it itr = split(r + 1), itl = split(l);
45     st.erase(itl, itr);
46     st.insert(node(l, r, v));
47 }
48 vector<pair<int, int>> tmp;
49 signed main() {
50     cin.tie(0)->sync_with_stdio(false);
51     cout.tie(0);
52     cin >> n >> m >> seed >> vmax;
53     for (int i = 1; i ≤ n; i++) {
54         a[i] = rnd() % vmax + 1;
55         st.insert(node(i, i, a[i]));
56     }
57     for (int at = 1, op, l, r, x, y, ans; at ≤ m; at++) {
58         op = (rnd() % 4) + 1;
59         l = (rnd() % n) + 1;
60         r = (rnd() % n) + 1;
61         if (l > r) swap(l, r);
62         if (op == 1) {
63             x = rnd() % vmax + 1;
64             it itr = split(r + 1), itl = split(l);
65             for (; itl ≠ itr; ++itl) itl->v += x;
66         } else if (op == 2) {
67             x = rnd() % vmax + 1;
68             assign(l, r, x);
69         } else if (op == 3) {
70             x = rnd() % (r - l + 1) + 1;
71             tmp.clear();
72             it itr = split(r + 1), itl = split(l);
73             for (it I = itl; I ≠ itr; ++I) tmp.push_back({I->v, I->r - I->l +
74                 1});
75             sort(tmp.begin(), tmp.end());
76             ans = -1;
77             for (int i = 0; i < tmp.size(); i++) {
78                 x -= tmp[i].second;
79                 if (x ≤ 0) {
80                     ans = tmp[i].first;
81                     break;
82                 }
83             }
84             cout << ans << '\n';
85         } else {
86             ans = 0;
87             x = rnd() % vmax + 1;
88             y = rnd() % vmax + 1;
89             it itr = split(r + 1), itl = split(l);
90             for (it I = itl; I ≠ itr; ++I) ans = (ans + qpow(I->v, x, y) * (I

```

```
        ->r - I->l + 1) % y) % y;
90      cout << ans << '\n';
91    }
92  }
93  return 0;
94 }
```