Support Vector Machine (SVM) Radial kernel

Feature space partition ensemble model for replication (FESPAE)

Simulation-based settings

Article: Lizbeth Naranjo, Carlos J. Perez, Daniel F. Merino (2025). A data ensemble-based approach for detecting vocal disorders using replicated acoustic biomarkers from electroglottography. *Sensing and Bio-Sensing Research Journal*, vol, num, pages.

Data

24

[1] 900

```
summary(datos2)
```

```
VЗ
                                                                 ۷4
       :-2.46818
                           :-2.8869
                                               :-2.3041
                                                                  :-2.23859
Min.
                    \mathtt{Min}.
                                       \mathtt{Min}.
                                                          Min.
1st Qu.:-0.64472
                    1st Qu.:-0.4958
                                       1st Qu.:-0.1822
                                                          1st Qu.: 0.05472
Median : 0.02661
                    Median : 0.2384
                                       Median : 0.6347
                                                          Median: 1.09540
Mean
       :-0.01209
                    Mean
                           : 0.2109
                                       Mean
                                              : 0.6358
                                                          Mean
                                                                 : 1.05924
3rd Qu.: 0.60494
                    3rd Qu.: 0.9120
                                       3rd Qu.: 1.3916
                                                          3rd Qu.: 1.98603
Max.
       : 2.62886
                    Max.
                           : 2.9954
                                       {\tt Max.}
                                               : 4.0518
                                                          Max.
                                                                  : 4.75694
      ۷5
                                             ۷7
                                                                V8
                         V6
Min.
       :-2.9530
                           :-2.1113
                                             :-3.0853
                                                                 :-2.236
                   Min.
                                      Min.
                                                         Min.
1st Qu.: 0.2255
                   1st Qu.: 0.6053
                                      1st Qu.: 0.9834
                                                         1st Qu.: 1.317
Median : 1.2606
                   Median : 1.8159
                                      Median : 2.4098
                                                         Median : 2.774
Mean
      : 1.4013
                   Mean
                           : 1.9805
                                      Mean
                                             : 2.5094
                                                         Mean
                                                                 : 2.689
3rd Qu.: 2.4265
                   3rd Qu.: 3.3161
                                      3rd Qu.: 3.9536
                                                         3rd Qu.: 3.962
       : 7.2912
                   Max.
                           : 7.2158
                                      Max.
                                              : 8.0646
                                                         Max.
                                                                 : 7.362
Max.
      V9
                       V10
                                                           V12
                                         V11
       :-2.530
                         :-1.322
                                           :-1.068
                                                              :-0.9634
Min.
                  Min.
                                    Min.
                                                      Min.
1st Qu.: 1.402
                  1st Qu.: 1.986
                                    1st Qu.: 2.123
                                                      1st Qu.: 1.8628
Median : 2.667
                  Median : 3.055
                                    Median : 3.296
                                                      Median: 2.9238
      : 2.573
                                           : 3.388
Mean
                  Mean
                         : 3.064
                                    Mean
                                                      Mean
                                                              : 2.9824
```

```
3rd Qu.: 3.817
               3rd Qu.: 4.127 3rd Qu.: 4.546
                                             3rd Qu.: 4.0124
Max. : 7.988
               Max. : 7.115 Max. : 7.231
                                             Max. : 7.0910
     V13
                   V14
                                   V15
                                                  V16
               Min. :-2.079
Min. :-1.885
                              Min. :-2.269
                                             Min. :-2.1259
1st Qu.: 1.655
               1st Qu.: 1.313
                              1st Qu.: 1.112
                                             1st Qu.: 0.5982
Median : 3.038
               Median : 2.747 Median : 2.537
                                             Median : 1.9031
Mean : 2.805
               Mean : 2.623 Mean : 2.648
                                             Mean : 1.9893
               3rd Qu.: 3.928 3rd Qu.: 4.098
3rd Qu.: 4.087
                                             3rd Qu.: 3.3091
Max. : 6.597
               Max. : 6.704 Max. : 8.223 Max. : 7.2479
     V17
                     V18
                                     V19
                                                     V20
                                       :-3.8817
Min. :-3.18364
                Min. :-2.7850
                                 Min.
                                                Min.
                                                       :-2.7783
                1st Qu.:-0.1074 1st Qu.:-0.1600
                                                1st Qu.:-0.2862
 1st Qu.:-0.01008
Median : 1.08517
                Median: 0.8566 Median: 0.6810
                                                Median: 0.4368
Mean : 1.25594
                Mean : 0.9245 Mean : 0.6666
                                                Mean : 0.3959
3rd Qu.: 2.51669
                 3rd Qu.: 1.9699 3rd Qu.: 1.5111
                                                 3rd Qu.: 1.1143
Max. : 6.44674
                 Max. : 5.6873
                                 Max. : 4.1971
                                               Max. : 4.0928
     V21
                      ID
                                              status
                                    rep
Min. :-2.43443
                Min. : 1.00
                                Min. :1
                                         Min.
                                                : 1
1st Qu.:-0.67873
                1st Qu.: 75.75
                               1st Qu.:1
                                          1st Qu.:1
Median : 0.06097
                                Median :2 Median :2
                Median :150.50
Mean : 0.01474 Mean :150.50
                                Mean :2 Mean :2
3rd Qu.: 0.67792
                 3rd Qu.:225.25
                                3rd Qu.:3
                                           3rd Qu.:3
Max. : 3.26405
                                           Max.
                 Max.
                       :300.00
                                Max. :3
head(datos2)
        V1
                 V2
                           V3
                                    ۷4
                                              V5
                                                        ۷6
                                                                   ۷7
1 1.1541136 1.206173 -0.9686025 0.02312405 2.3165891 -0.3054029 -1.61019789
2 1.1541136 1.485269 -0.4104103 0.86041236 3.4329735 1.0900776 0.06437873
3 1.1541136 1.485269 -0.4104103 0.86041236 3.4329735 0.3691737 -1.37742906
4 \ -0.6443284 \ -1.553137 \ -1.5977095 \ 1.80509752 \ -0.4816474 \ 1.3936230 \ 2.15860994
5 -0.6443284 -1.326381 -1.1441960 2.48536784 0.4253797 2.5274069 3.51915059
8V
            V9
                     V10
                             V11
                                    V12
                                           V13
                                                       V14
1 2.0685608 2.6366958 5.544770 4.434717 4.987851 3.720234 3.668854 3.077667
2 3.4640413 3.7530802 6.102962 4.434717 4.429659 2.603849 2.273374 1.403090
3 1.3013296 0.8694646 3.219346 1.551101 2.987851 2.603849 3.715182 4.286706
4 2.1574187 3.9048461 6.289806 7.142163 6.178932 4.254271 3.944702 2.582941
5 3.2912026 4.8118732 6.743320 7.142163 5.725419 3.347244 2.810918 1.222400
6 0.9714729 1.7189003 3.650347 4.049190 4.178932 3.347244 4.357404 4.315373
       V16
                V17
                         V18
                                  V19
                                           V20
                                                     V21 ID rep status
1
2 -1.7919686 0.4728324 -0.35411707 1.305594 -1.1075336 -0.1784143 2
                                                              1
3 1.0916470 3.3564480 1.80859462 2.747402 -0.3866297 -0.1784143 3
                                                              1
4 0.2449769 2.6747610 0.70607137 1.582024 -2.1536013 -1.0602656 1
                                                              2
                                                                    1
5 -0.8888070 1.7677339 0.02580105 1.128511 -2.3803581 -1.0602656 2
                                                              2
                                                                    2
6 2.2041659 4.8607067 2.34553072 2.674997 -1.6071148 -1.0602656 3
datos2 <- as.data.frame(datos2)</pre>
datos2$ID_fact = as.factor(datos2$ID) ## categorical ID of the subject
datos2$STATUS_fact = as.factor(datos2$status) ## categorical response variable
table(datos2$STATUS_fact)
```

1 2 3

300 300 300

data set

trainc <- datos2 %>% select(-status,-ID)

Crossvalidation

Subspaces

```
## Function to compute the Mode
Mode <- function(x, na.rm = FALSE) {</pre>
  if(na.rm){
   x = x[!is.na(x)]
   }
 ux <- unique(x)</pre>
  return(ux[which.max(tabulate(match(x, ux)))])
## Partition of subspaces
## The feature space is randomly partitioned into K subspaces with roughly equal sizes
## k = number of predictors
## K = subspaces
KO = 3 ### sub-spaces
k = 21 ### explanatory variable
k2 = round(k/K0)
space = 1:k
subspaces = rep(list(rep(NA,k2)),K0)
set.seed(12345)
for(j in 1:(KO-1)){
    space1 = sample(space, size=k2, replace=FALSE)
    space = setdiff(space,space1)
    subspaces[[j]] = space1[order(space1)]
}
space1 = space
subspaces[[K0]] = space1[order(space1)]
# 21 features = 1x21, 3x7,
subspaces
## [[1]]
## [1] 2 6 11 14 16 18 19
## [[2]]
## [1] 1 8 9 10 13 20 21
##
## [[3]]
## [1] 3 4 5 7 12 15 17
```

Training and testing data subsets

```
## Select data: 75% training & 25% testing stratified per category
SIM = 100  ## repeat N times the cross-validation process
N = 300 ## sample size
Nfit = 225 ## sample size for training subset
Ntest = 75  ## sample size for testing subset
Ncat = 100  ## sample size per category
Ncatfit = 75 ## training per category
Ncattest = 25  ## testing per category
FIT <- matrix(0,SIM,Nfit) ## training subsets</pre>
TEST <- matrix(0,SIM,Ntest) ## testing subsets</pre>
categoria = trainc %>% filter(rep==1) %>% select(STATUS_fact)
categoria = as.numeric(categoria$STATUS_fact)
id = 1:N
set.seed(12345)
for(si in 1:SIM){
  for(j in 1:3){
    idcat = id[categoria==j] ## stratified per category j
    ran0 = sample(idcat, size=Ncatfit, replace=FALSE)
    FIT[si,(j-1)*Ncatfit+1:Ncatfit] <- sort(ran0)</pre>
    TEST[si,(j-1)*Ncattest+1:Ncattest] <- setdiff(idcat,ran0)</pre>
} }
```

Classification metrics for models predicting nominal outcomes

```
## Functions to compute classification metrics
## Ytrue = true response variable
## Ypred = predicted outcome
## cat = category
## TP = true positive
## TN = true negative
## FP = false positive
## FN = false negative
## Function to compute the precision per class=cat
fn precision class <- function(Ytrue, Ypred, cat){</pre>
  TP = sum(Ypred[Ytrue==cat]==cat)
 FP = sum(Ypred[Ytrue!=cat]==cat)
 precision = TP/(TP+FP)
 return(precision)
## Function to compute the recall per class=cat
fn_recall_class <- function(Ytrue, Ypred, cat){ ## cat==category</pre>
 TP = sum(Ypred[Ytrue==cat]==cat)
 FN = sum(Ypred[Ytrue==cat]!=cat)
 recall = TP/(TP+FN)
 return(recall)
}
## Function to compute the F1-score per class=cat
fn f1score class <- function(Ytrue, Ypred, cat) { ## cat==category</pre>
  TP = sum(Ypred[Ytrue==cat]==cat)
  FP = sum(Ypred[Ytrue!=cat]==cat)
  FN = sum(Ypred[Ytrue==cat]!=cat)
  precision = TP/(TP+FP)
  recall = TP/(TP+FN)
  f1score = 2*(precision*recall)/(precision+recall)
  return(f1score)
}
## To save classification metrics
## Fitxxx: metric for training subset. Testxxx: metric for testing subset
FitAccuracy = TestAccuracy <- array(NA, dim=c(SIM, 4)) ## Accuracy Rate
FitPrecisionClass = TestPrecisionClass <- array(NA, dim=c(SIM, 4, 3)) ## Precision per class
FitRecallClass = TestRecallClass <- array(NA,dim=c(SIM,4,3)) ## Recall per class
FitF1ScoreClass = TestF1ScoreClass <- array(NA, dim=c(SIM, 4,3)) ## F1-score per class
FitPrecisionMacroAve = TestPrecisionMacroAve <- array(NA,dim=c(SIM,4)) ## Precision Macro Average
FitRecallMacroAve = TestRecallMacroAve <- array(NA, dim=c(SIM,4)) ## Recall Macro Average
FitF1ScoreMacroAve = TestF1ScoreMacroAve <- array(NA, dim=c(SIM, 4)) ## F1-score Macro Average
```

Model estimation

```
##-----
for(sim in 1:SIM){ ### BEGIN sim
my_fit = FIT[sim,] ## training subset
my_test = TEST[sim,] ## testing subset
## Training data subset
train1 <- trainc %>% filter(ID_fact%in%my_fit, rep==1) ## repetition=1
train2 <- trainc %>% filter(ID_fact%in%my_fit, rep==2) ## repetition=2
train3 <- trainc %>% filter(ID_fact%in%my_fit, rep==3) ## repetition=3
Yc = train1$STATUS_fact ## categorical response variable for training
n = length(Yc)
G = 3 # classes
## Testing data subset
test1 <- trainc %>% filter(ID_fact%in%my_test, rep==1) ## repetition=1
test2 <- trainc %>% filter(ID_fact%in%my_test, rep==2) ## repetition=2
test3 <- trainc %>% filter(ID_fact%in%my_test, rep==3) ## repetition=3
Yc.new = test1$STATUS_fact ## categorical response variable for testing
n.new = length(Yc.new)
## Delete variables which are not used
train1 <- train1 %>% select(-c(rep,ID_fact))
train2 <- train2 %>% select(-c(rep,ID_fact))
train3 <- train3 %>% select(-c(rep,ID_fact))
test1 <- test1 %>% select(-c(rep,ID_fact))
test2 <- test2 %>% select(-c(rep,ID_fact))
test3 <- test3 %>% select(-c(rep,ID_fact))
## Algorithm FESPAE
## Feature space partition ensemble model for replication
##-----
## Algo1: The feature space is randomly partitioned into M subspaces, {$1,$2,...,$M}
KO = 3 ## sub-spaces
k = 21 ## explanatory variables
k2 = round(k/K0)
space = 1:k
subspaces = rep(list(rep(NA,k2)),K0) ## Subspaces
set.seed(12345)
for(j in 1:(KO-1)){
   space1 = sample(space, size=k2, replace=FALSE)
   space = setdiff(space,space1)
   subspaces[[j]] = space1[order(space1)]
space1 = space
```

```
subspaces[[K0]] = space1[order(space1)]
# 21 features = 1x21, 3x7,
##-----
## Algo2: for feature subspace m = 1 to M do
pred.vgam = array(NA,dim=c(n,K0,3)) ## 3 repetitions
pred.new.vgam = array(NA,dim=c(n.new,K0,3)) ## 3 repetitions
##-----
## Algo3: for replication j = 1 to J do
## REPLICATION j=1:
for(parti1 in 1:K0){ ## partition of the subspaces
train1_par = train1[,c(subspaces[[parti1]],k+1)]
test1_par = test1[,c(subspaces[[parti1]],k+1)]
## Algo4: Fit a classifier T(xj,z), xj\in Sm, to the training data
mod1 <- tune( "svm", STATUS_fact ~ . ,</pre>
             data = train1_par,
             kernel = "radial",
             ranges = list(cost=c(0.01,0.1,0.5,1,5,10,20,50)))
## summary(mod1)
mejor_mod1 <- mod1$best.model</pre>
## Algo5: Compute the C response probabilities {\pi^(m,j)_{ic}}, for i=1,...,n.
## Predictions
predict1 <- predict(mejor_mod1, newdata = train1_par)</pre>
predict1.new <- predict(mejor_mod1, newdata = test1_par)</pre>
pred.vgam[,parti1,1] = predict1
pred.new.vgam[,parti1,1] = predict1.new
## REPLICATION j=2:
for(parti2 in 1:K0){ ## partition of the subspaces
train2_par = train2[,c(subspaces[[parti2]],k+1)]
test2_par = test2[,c(subspaces[[parti2]],k+1)]
## Algo4: Fit a classifier $T(xj,z)$, $xj\in Sm$, to the training data
mod2 <- tune( "svm", STATUS_fact ~ . ,</pre>
             data = train2_par,
             kernel = "radial",
             ranges = list(cost=c(0.01,0.1,0.5,1,5,10,20,50)) )
## summary(mod2)
mejor_mod2 <- mod2$best.model</pre>
## Algo5: Compute the C response probabilities {\pi^(m,j)_{ic}}, for i=1,...,n.
## Predictions
predict2 <- predict(mejor_mod2, newdata = train2_par)</pre>
predict2.new <- predict(mejor_mod2, newdata = test2_par)</pre>
pred.vgam[,parti2,2] = predict2
pred.new.vgam[,parti2,2] = predict2.new
```

```
}
## REPLICATION j=3:
for(parti3 in 1:K0){ ## partition of the subspaces
train3_par = train3[,c(subspaces[[parti3]],k+1)]
test3_par = test3[,c(subspaces[[parti3]],k+1)]
## Algo4: Fit a classifier T(xj,z), xj \in Sm, to the training data
mod3 <- tune( "svm", STATUS_fact ~ . ,</pre>
              data = train3_par,
              kernel = "radial",
              ranges = list(cost=c(0.01,0.1,0.5,1,5,10,20,50)) )
## summary(mod3)
mejor_mod3 <- mod3$best.model</pre>
## Algo5: Compute the C response probabilities {\pi^(m,j)_{ic}}, for i=1,...,n.
## Predictions
predict3 <- predict(mejor_mod3, newdata = train3_par)</pre>
predict3.new <- predict(mejor_mod3, newdata = test3_par)</pre>
pred.vgam[,parti3,3] = predict3
pred.new.vgam[,parti3,3] = predict3.new
## Algo6: End for replication j = 1 to J
## Algo7: End for feature subspace m = 1 to M
## Algo8: Output: compute the response probabilities $\pi_{ic} = mean({\pi^(m,j)_{ic}})
##-----
## Algo8: Output: compute the response category T*(x,z) = arg \max \{ \neq ic \} \}
pred.max = array(NA, dim=c(n,3))
pred.vgam_max = array(NA,dim=n)
for(i in 1:n){
  for(j in 1:3){
    pred.max[i,j] = Mode(pred.vgam[i,,j])
  pred.vgam_max[i] = Mode(pred.vgam[i,,])
}
### Predict new subjects
pred.new.max = array(NA,dim=c(n.new,3))
pred.new.vgam_max = array(NA,dim=n.new)
for(i in 1:n.new){
  for(j in 1:3){
    pred.new.max[i,j] = Mode(pred.new.vgam[i,,j])
  pred.new.vgam_max[i] = Mode(pred.new.vgam[i,,])
## End FESPAE
```

```
## Classification Metrics for models predicting nominal outcomes
## Accuracy Rate
FitAccuracy[sim,] = c(sum(Yc==pred.max[,1])/n,
                     sum(Yc==pred.max[,2])/n,
                     sum(Yc==pred.max[,3])/n,
                     sum(Yc==pred.vgam max)/n)
TestAccuracy[sim,] = c(sum(Yc.new==pred.new.max[,1])/n.new,
                       sum(Yc.new==pred.new.max[,2])/n.new,
                       sum(Yc.new==pred.new.max[,3])/n.new,
                       sum(Yc.new==pred.new.vgam_max)/n.new)
## Precision
for(cate in 1:3){
  FitPrecisionClass[sim,1, cate] = fn_precision_class(Yc, pred.max[,1], cate)
  FitPrecisionClass[sim,2, cate] = fn_precision_class(Yc, pred.max[,2], cate)
  FitPrecisionClass[sim,3, cate] = fn_precision_class(Yc, pred.max[,3], cate)
  FitPrecisionClass[sim,4, cate] = fn_precision_class(Yc, pred.vgam_max, cate)
  TestPrecisionClass[sim,1, cate] = fn_precision_class(Yc.new, pred.new.max[,1], cate)
  TestPrecisionClass[sim,2, cate] = fn_precision_class(Yc.new, pred.new.max[,2], cate)
  TestPrecisionClass[sim,3, cate] = fn_precision_class(Yc.new, pred.new.max[,3], cate)
  TestPrecisionClass[sim,4, cate] = fn_precision_class(Yc.new, pred.new.vgam_max, cate)
}
for(rep in 1:4){
  FitPrecisionMacroAve[sim, rep] = mean(FitPrecisionClass[sim, rep,])
  TestPrecisionMacroAve[sim,rep] = mean(TestPrecisionClass[sim,rep,])
}
## Recall
for(cate in 1:3){
  FitRecallClass[sim,1, cate] = fn_recall_class(Yc, pred.max[,1], cate)
  FitRecallClass[sim,2, cate] = fn_recall_class(Yc, pred.max[,2], cate)
  FitRecallClass[sim,3, cate] = fn_recall_class(Yc, pred.max[,3], cate)
  FitRecallClass[sim,4, cate] = fn_recall_class(Yc, pred.vgam_max, cate)
  TestRecallClass[sim,1, cate] = fn_recall_class(Yc.new, pred.new.max[,1], cate)
  TestRecallClass[sim,2, cate] = fn_recall_class(Yc.new, pred.new.max[,2], cate)
  TestRecallClass[sim,3, cate] = fn_recall_class(Yc.new, pred.new.max[,3], cate)
  TestRecallClass[sim,4, cate] = fn_recall_class(Yc.new, pred.new.vgam_max, cate)
for(rep in 1:4){
  FitRecallMacroAve[sim, rep] = mean(FitRecallClass[sim, rep,])
  TestRecallMacroAve[sim,rep] = mean(TestRecallClass[sim,rep,])
}
## F1-Score
for(cate in 1:3){
  FitF1ScoreClass[sim,1, cate] = fn_f1score_class(Yc, pred.max[,1], cate)
  FitF1ScoreClass[sim,2, cate] = fn_f1score_class(Yc, pred.max[,2], cate)
  FitF1ScoreClass[sim,3, cate] = fn_f1score_class(Yc, pred.max[,3], cate)
```

Results

Accuracy Rate

```
columna = c("rep1", "rep2", "rep3", "ensemble")
renglon = c("fit_mean","fit_sd","test_mean","test_sd")
summary(FitAccuracy)
##
         V1
                         ٧2
                                          VЗ
                                                          ۷4
                          :0.8267
                                                           :0.9156
## Min.
         :0.8133
                                          :0.7956
                   Min.
                                   Min.
                                                    Min.
## 1st Qu.:0.8489
                   1st Qu.:0.8578 1st Qu.:0.8489
                                                    1st Qu.:0.9556
                   Median :0.8711 Median :0.8667
                                                    Median :0.9644
## Median :0.8578
## Mean :0.8626
                   Mean :0.8712 Mean :0.8665
                                                    Mean :0.9646
## 3rd Qu.:0.8756
                    3rd Qu.:0.8844
                                    3rd Qu.:0.8844
                                                    3rd Qu.:0.9733
## Max. :0.9289
                   Max. :0.9244
                                   Max. :0.9200
                                                    Max. :0.9911
apply(FitAccuracy,2,"sd")
## [1] 0.02161394 0.02167202 0.02266631 0.01354055
summary(TestAccuracy)
##
         ۷1
                         ٧2
                                          ٧3
                                                          ٧4
## Min. :0.6400
                          :0.7200 Min.
                                          :0.6667
                                                    Min.
                                                           :0.8400
                   Min.
## 1st Qu.:0.7067
                   1st Qu.:0.7867
                                   1st Qu.:0.7733
                                                    1st Qu.:0.8800
                   Median :0.8000 Median :0.8000
                                                    Median :0.9067
## Median :0.7467
## Mean :0.7399
                   Mean
                         :0.8040
                                   Mean :0.7975
                                                    Mean :0.9080
## 3rd Qu.:0.7733
                    3rd Qu.:0.8267
                                    3rd Qu.:0.8267
                                                    3rd Qu.:0.9333
## Max.
        :0.8400
                   Max.
                         :0.8800
                                    Max. :0.8800
                                                    Max.
                                                           :0.9733
apply(TestAccuracy,2,"sd")
## [1] 0.04478636 0.03122634 0.03741093 0.03011389
RESaccuracy <- rbind(apply(FitAccuracy,2,"mean"), apply(FitAccuracy,2,"sd"),</pre>
                    apply(TestAccuracy,2,"mean"),apply(TestAccuracy,2,"sd"))
colnames(RESaccuracy) = columna
rownames(RESaccuracy) = renglon
write.csv(RESaccuracy, file=paste0(archivo,"_accuracy",".csv"))
```

Precision Macro Average

```
summary(FitPrecisionMacroAve)
##
          V1
                           V2
                                            VЗ
                                                              ۷4
##
  Min.
           :0.8173
                     Min.
                            :0.8401
                                      Min.
                                             :0.8372
                                                        Min.
                                                               :0.9246
   1st Qu.:0.8503
                     1st Qu.:0.8680
                                      1st Qu.:0.8711
                                                        1st Qu.:0.9585
  Median :0.8623
                     Median :0.8794
                                      Median :0.8852
                                                        Median : 0.9667
## Mean
           :0.8663
                     Mean
                            :0.8795
                                      Mean
                                             :0.8835
                                                        Mean
                                                               :0.9667
   3rd Qu.:0.8811
                     3rd Qu.:0.8919
                                      3rd Qu.:0.8974
                                                        3rd Qu.:0.9748
## Max.
           :0.9291
                            :0.9290
                                             :0.9253
                                                               :0.9913
                     Max.
                                      Max.
                                                        Max.
apply(FitPrecisionMacroAve,2,"sd")
## [1] 0.02064504 0.01908212 0.01743592 0.01204647
summary(TestPrecisionMacroAve)
##
          V1
                           V2
                                            VЗ
                                                              ۷4
##
           :0.6592
                            :0.7213
                                             :0.6991
                                                               :0.8550
  Min.
                     Min.
                                      Min.
                                                        Min.
   1st Qu.:0.7206
                     1st Qu.:0.7999
                                      1st Qu.:0.8053
                                                        1st Qu.:0.8985
  Median :0.7497
                     Median :0.8167
                                      Median :0.8273
                                                        Median :0.9191
## Mean
           :0.7500
                     Mean
                            :0.8161
                                      Mean
                                             :0.8240
                                                        Mean
                                                               :0.9186
   3rd Qu.:0.7880
                     3rd Qu.:0.8376
                                      3rd Qu.:0.8519
                                                        3rd Qu.:0.9387
##
           :0.8446
                            :0.8819
                                             :0.8886
  Max.
                     Max.
                                      Max.
                                                        Max.
                                                               :0.9744
apply(TestPrecisionMacroAve, 2, "sd")
## [1] 0.04371159 0.03146200 0.03491336 0.02480341
RESprecision <- rbind(apply(FitPrecisionMacroAve,2,"mean"), apply(FitPrecisionMacroAve,2,"sd"),
                      apply(TestPrecisionMacroAve,2,"mean"),apply(TestPrecisionMacroAve,2,"sd"))
colnames(RESprecision) = columna
rownames(RESprecision) = renglon
write.csv(RESprecision, file=paste0(archivo,"_precision",".csv"))
```

Recall Macro Average

summary(FitRecallMacroAve) ## V1 V2 VЗ ۷4 ## $\mathtt{Min}.$:0.8133 Min. :0.8267 Min. :0.7956 Min. :0.9156 1st Qu.:0.8489 1st Qu.:0.8578 1st Qu.:0.8489 1st Qu.:0.9556 Median :0.8578 Median :0.8711 Median :0.8667 Median :0.9644 ## Mean :0.8626 Mean :0.8712 Mean :0.8665 Mean :0.9646 3rd Qu.:0.8756 3rd Qu.:0.8844 3rd Qu.:0.8844 3rd Qu.:0.9733 ## Max. :0.9289 :0.9244 :0.9200 :0.9911 Max. Max. Max. apply(FitRecallMacroAve, 2, "sd") ## [1] 0.02161394 0.02167202 0.02266631 0.01354055 summary(TestRecallMacroAve) ## V1 ٧2 VЗ ۷4 ## :0.6400 :0.7200 :0.6667 :0.8400 Min. Min. Min. Min. 1st Qu.:0.7067 1st Qu.:0.7867 1st Qu.:0.7733 1st Qu.:0.8800 Median :0.7467 Median :0.8000 Median :0.8000 Median :0.9067 ## Mean :0.7399 Mean :0.8040 Mean :0.7975 Mean :0.9080 ## 3rd Qu.:0.7733 3rd Qu.:0.8267 3rd Qu.:0.8267 3rd Qu.:0.9333 :0.8400 :0.8800 :0.8800 Max.Max. Max. Max. :0.9733 apply(TestRecallMacroAve, 2, "sd")

```
## [1] 0.04478636 0.03122634 0.03741093 0.03011389
```

```
RESrecall <- rbind(apply(FitRecallMacroAve,2,"mean"), apply(FitRecallMacroAve,2,"sd"),
                   apply(TestRecallMacroAve,2,"mean"),apply(TestRecallMacroAve,2,"sd"))
colnames(RESrecall) = columna
rownames(RESrecall) = renglon
write.csv(RESrecall, file=paste0(archivo,"_recall",".csv"))
```

F1-Score Macro Average

summary(FitF1ScoreMacroAve) ## V1 V2 VЗ ۷4 ## $\mathtt{Min}.$:0.8120 Min. :0.8170 Min. :0.7803 Min. :0.9126 1st Qu.:0.8478 1st Qu.:0.8543 1st Qu.:0.8448 1st Qu.:0.9552 Median :0.8575 Median :0.8690 Median :0.8664 Median : 0.9642 ## Mean :0.8619 Mean :0.8692 Mean :0.8639 Mean :0.9643 3rd Qu.:0.8756 3rd Qu.:0.8834 3rd Qu.:0.8840 3rd Qu.:0.9733 ## Max. :0.9289 :0.9234 :0.9201 :0.9911 Max. Max. Max. apply(FitF1ScoreMacroAve,2,"sd")

[1] 0.02202714 0.02281992 0.02473271 0.01388173

summary(TestF1ScoreMacroAve)

```
##
          V1
                           V2
                                             VЗ
                                                              ۷4
##
           :0.6419
                            :0.7176
                                              :0.6535
                                                               :0.8235
   Min.
                     Min.
                                      Min.
                                                        Min.
   1st Qu.:0.7047
                     1st Qu.:0.7824
                                       1st Qu.:0.7678
                                                        1st Qu.:0.8791
  Median :0.7435
                     Median :0.7992
                                      Median :0.7876
                                                        Median :0.9055
## Mean
           :0.7368
                     Mean
                            :0.8001
                                      Mean
                                              :0.7913
                                                        Mean
                                                               :0.9059
   3rd Qu.:0.7694
                     3rd Qu.:0.8210
                                       3rd Qu.:0.8222
                                                        3rd Qu.:0.9327
##
           :0.8392
                            :0.8790
                                              :0.8821
  Max.
                     Max.
                                      Max.
                                                        Max.
                                                               :0.9730
apply(TestF1ScoreMacroAve,2,"sd")
```

[1] 0.04645286 0.03198242 0.04036869 0.03197485