Multinomial linear regression (MLR)

Replication-based stagewise additive modeling (RSAM)

EGG data-based experiments

Article: Lizbeth Naranjo, Carlos J. Perez, Daniel F. Merino (2025). A data ensemble-based approach for detecting vocal disorders using replicated acoustic biomarkers from electroglottography. *Sensing and Bio-Sensing Research Journal*, vol, num, pages.

```
library(VGAM)
library(VGAM)
## change the address where the file will be saved
address = "~/Documents/GitHub/"
setwd("~/Documents/GitHub/")
```

EGG data-based experiments

```
## Comment or uncomment the options: EGG-a, EGG-i, EGG-u
## EGG-a
## datos2 <- read.csv(paste0(address, "a_egg_saarbrucken.csv"),</pre>
                     sep = ";",header=TRUE, dec=",")
## name of the files to save results
## archivo = "RSAM_crossval_strata_allvar_MLR_Saarbruken_egg_a"
## EGG-i
## datos2 <- read.csv(paste0(address,"i_egg_saarbrucken.csv"),</pre>
                     sep = ";",header=TRUE, dec=",")
##
## name of the files to save results
## archivo = "RSAM_crossval_strata_allvar_MLR_Saarbruken_egg_i"
## EGG-u
datos2 <- read.csv(paste0(address, "u_egg_saarbrucken.csv"),</pre>
                   sep = ";",header=TRUE, dec=",")
## name of the files to save results
archivo = "RSAM_crossval_strata_allvar_MLR_Saarbruken_egg_u"
```

dim(datos2)

[1] 675 36

summary(datos2)

ID_fact	status_fact	SEX	JITTER
Min. : 1.0	_		: 0.00
1st Qu.:169.5			Qu.: 0.45
Median :338.0			an : 1.06
Mean :338.0			: 13.84
3rd Qu.:506.5			Qu.: 17.95
Max. :675.0	3rd Qu.:2 3rd Q Max. :2 Max.		:273.97
SHIMMER	CPP	D2	FZCF
Min. :0.00000			
	1st Qu.:18.02	1st Qu.: 3.625	
Median :0.05000			Median : 16.00
Mean :0.06012		Mean : 4.738	Mean : 42.47
3rd Qu.:0.08000	•	3rd Qu.: 5.445	
Max. :0.38000		Max. :18.380	Max. :5280.00
GNE	HNR	HURST	LZ
Min. :0.4100			Min. : 19.0
1st Qu.:0.6350	1st Qu.:20.15 1	st Qu.:0.6150	1st Qu.: 37.0
Median :0.8000	Median:23.48 M	ledian :0.8700	Median : 50.0
Mean :0.9465		lean :0.8806	Mean : 54.2
3rd Qu.:1.0950	3rd Qu.:26.51 3	rd Qu.:1.1350	3rd Qu.: 65.5
Max. :5.0900	Max. :33.91 M	[ax. :1.7700	Max. :279.0
MFCCO	MFCC1	MFCC2	MFCC3
Min. :-2.8800	Min. :-19.06	Min. :-30.610	Min. :-45.920
1st Qu.:-1.1200			1st Qu.:-21.495
Median :-0.5300	•	Median : 10.670	Median : -7.850
Mean :-0.5224		Mean : 9.860	
3rd Qu.: 0.1200		3rd Qu.: 19.775	
Max. : 2.0500	Max. : 32.80	Max. : 46.420	•
MFCC4	MFCC5	MFCC6	MFCC7
Min. :-57.250		Min. :-43.04	
1st Qu.:-20.330			
Median :-10.640	Median : -7.710	Median : -8.61	
Mean :-11.226		Mean : -8.94	
3rd Qu.: -2.105		3rd Qu.: -2.03	
Max. : 25.070		Max. : 26.06	
MFCC8	MFCC9	MFCC10	MFCC11
Min. :-51.090	Min. :-47.06	Min. :-39.590	
1st Qu.:-15.975		1st Qu.:-12.060	
Median : -7.810	Median : -6.26	Median : -4.420	
Mean : -7.906	Mean : -5.64	Mean : -4.325	
3rd Qu.: -0.240	3rd Qu.: 1.71	3rd Qu.: 2.080	·
Max. : 36.520	Max. : 40.73	Max. : 42.350	
MFCC12	PERMUTATION	PPE	SHANNON
Min. :-37.200		Min. :0.0000	Min. :11.92
1st Qu.:-11.775		1st Qu.:0.5300	1st Qu.:12.16
Median : -5.020		Median :0.5500	Median :12.19
Mean : -4.221	Mean :1.642	Mean :0.5315	Mean :12.18

```
3rd Qu.: 2.625
                 3rd Qu.:1.780
                                 3rd Qu.:0.5700
                                                  3rd Qu.:12.21
Max. : 29.550
                 Max. :2.580
                                 Max.
                                       :0.5700
                                                 Max.
                                                       :12.26
     ZCR
                 energyentropy
                                 spectralcentroid spectralspread
       :0.01000
                 Min. :2.500
                                       :0.0700
                                                 Min. :0.1200
Min.
                                 Min.
1st Qu.:0.02000
                 1st Qu.:3.260
                                 1st Qu.:0.1100
                                                  1st Qu.:0.1600
Median :0.03000
                 Median :3.310
                                 Median :0.1200
                                                 Median :0.1800
Mean :0.03846
                 Mean :3.269
                                 Mean :0.1206
                                                  Mean :0.1798
3rd Qu.:0.05000
                 3rd Qu.:3.320
                                 3rd Qu.:0.1300
                                                  3rd Qu.:0.1900
Max.
       :0.20000
                 Max.
                        :3.320
                                 Max.
                                        :0.3300
                                                  Max.
                                                        :0.3300
spectralentropy
                spectralrolloff
                                       RPDE
                                                        rep
Min.
      :0.0000
                Min.
                       :0.01000
                                  Min.
                                         :0.0100
                                                   Min.
                                                         : 1
1st Qu.:0.0500
                                  1st Qu.:0.2000
                1st Qu.:0.04000
                                                   1st Qu.:1
                                  Median :0.2800
Median :0.1100
                Median :0.05000
                                                   Median :2
Mean
     :0.1832
                Mean
                      :0.05613
                                  Mean
                                        :0.3194
                                                   Mean
                                                        :2
3rd Qu.:0.2400
                3rd Qu.:0.07000
                                  3rd Qu.:0.3900
                                                   3rd Qu.:3
Max.
     :1.6400
                Max.
                      :0.37000
                                  Max.
                                        :0.9000
                                                   Max. :3
```

head(datos2)

```
ID fact status fact SEX JITTER SHIMMER
                                          CPP
                                                D2 FZCF GNE
                                                               HNR HURST LZ
                   0
                       0
                           0.21
                                   0.02 28.48 4.35
                                                     25 0.63 27.12 1.20 32
1
        1
2
        2
                   0
                       0
                           0.43
                                   0.06 22.18 3.23
                                                     31 0.58 18.23 1.38 44
3
                           0.46
                                   0.03 24.91 5.24
        3
                   0
                       0
                                                     27 0.60 24.93 1.30 33
4
        4
                   0
                           0.49
                                   0.02 31.64 3.14
                                                     24 0.57 25.71 1.17 34
                       0
                          11.39
                                   0.09 24.74 2.16
5
        5
                   0
                       0
                                                     40 0.43 15.64 1.51 39
6
                   0
                           0.33
                                   0.03 29.29 3.27
                                                     33 0.47 24.57 1.40 33
 MFCC0 MFCC1 MFCC2 MFCC3 MFCC4 MFCC5 MFCC6 MFCC7 MFCC8 MFCC9 MFCC10 MFCC11
1 - 0.41 - 8.69 - 0.89 - 0.03 - 3.66 - 0.03 - 0.20 - 3.42 - 4.11 - 6.53 - 8.78 - 9.64
        3.10 15.86 5.73 9.91 4.40 4.72 0.60 2.27 -2.16
2 - 1.47
                                                              -3.27
                                                                     -3.26
3 -0.92 7.38 11.85 2.93 2.55 2.91 3.56 -1.11 -1.74 -4.55 -4.97 -7.97
4 -0.52 8.81 -2.68 2.83 -0.76 -0.60 -2.30 -5.78 -4.10 -7.55 -7.57 -8.92
5 -2.06 11.23 9.58 5.36 7.67 2.17 3.94 4.12 4.38 0.62
                                                               0.97
                                                                      1.00
6 -1.39 14.83 3.50 -2.30
                         9.86 2.90 1.00 6.24 -1.52 1.44 -0.26 -1.19
 MFCC12 PERMUTATION PPE SHANNON ZCR energyentropy spectralcentroid
1 -11.13
               2.02 0.55
                           12.19 0.02
                                               3.31
                                                                0.13
2 -3.81
               2.26 0.48
                           12.20 0.02
                                               3.27
                                                                 0.12
3 -5.99
               1.99 0.55
                           12.21 0.02
                                                                0.12
                                               3.30
4 -8.74
               1.68 0.55
                           12.17 0.02
                                               3.31
                                                                 0.12
5 -0.09
               1.84 0.44
                           12.19 0.01
                                               3.19
                                                                0.09
6 -1.26
               1.64 0.53
                           12.17 0.01
                                                3.28
                                                                 0.11
  spectralspread spectralentropy spectralrolloff RPDE rep
           0.19
                           0.11
                                           0.02 0.21
1
            0.21
                           0.06
2
                                           0.02 0.50
3
                           0.06
                                           0.02 0.32
            0.21
                                                       3
4
            0.18
                           0.13
                                           0.03 0.32
5
            0.17
                           0.03
                                           0.01 0.58
6
                           0.08
                                           0.02 0.37
            0.18
                                                       3
```

Re-Scale explanatory variables

```
## Scale the variables
datos2 <- as.data.frame(datos2)</pre>
datos2$STATUS_fact = as.factor(as.numeric(factor(datos2$status_fact)))
table(datos2$STATUS fact)
 1 2 3
225 225 225
datos <- transform(datos2,</pre>
sJITTER= scale(JITTER), sSHIMMER= scale(SHIMMER), sCPP= scale(CPP),
sD2= scale(D2), sFZCF= scale(FZCF), sGNE= scale(GNE),
sHNR= scale(HNR), sHURST= scale(HURST), sLZ= scale(LZ),
sMFCCO= scale(MFCCO),
sMFCC1= scale(MFCC1), sMFCC2= scale(MFCC2), sMFCC3= scale(MFCC3),
sMFCC4= scale(MFCC4), sMFCC5= scale(MFCC5), sMFCC6= scale(MFCC6),
sMFCC7= scale(MFCC7), sMFCC8= scale(MFCC8), sMFCC9= scale(MFCC9),
sMFCC10= scale(MFCC10), sMFCC11= scale(MFCC11), sMFCC12= scale(MFCC12),
sPERMUTATION= scale(PERMUTATION), sPPE= scale(PPE), sSHANNON= scale(SHANNON),
sZCR= scale(ZCR),
senergyentropy= scale(energyentropy), sspectralcentroid= scale(spectralcentroid),
sspectralspread= scale(spectralspread), sspectralentropy= scale(spectralentropy),
sspectralrolloff= scale(spectralrolloff), sRPDE= scale(RPDE))
datos$ID_fact = rep(1:225,each=3)
dim(datos)
```

[1] 675 69

```
## data set
trainc <- datos %>% select(
sJITTER, sSHIMMER, sCPP, sD2, sFZCF,
sGNE, sHNR, sHURST, sLZ, sMFCCO,
sMFCC1, sMFCC2, sMFCC3, sMFCC4, sMFCC5,
sMFCC6, sMFCC7, sMFCC8, sMFCC9, sMFCC10,
sMFCC11, sMFCC12,
sPERMUTATION, sPPE, sSHANNON, sZCR,
senergyentropy, sspectralcentroid, sspectralspread,
sspectralentropy, sspectralrolloff, sRPDE,
STATUS_fact,SEX, rep,ID_fact)
```

Crossvalidation

Training and testing data subsets

```
## Select data: 75% training & 25% testing stratified per category
SIM = 100  ## repeat N times the cross-validation process
N = 225 ## sample size
Nfit = 168  ## sample size for training subset
Ntest = 57  ## sample size for testing subset
Ncat = 75  ## sample size per category
Ncatfit = 56 ## training per category
Ncattest = 19 ## testing per category
FIT <- matrix(0,SIM,Nfit) ## training subsets</pre>
TEST <- matrix(0,SIM,Ntest) ## testing subsets</pre>
categoria = trainc %>% filter(rep==1) %>% select(STATUS_fact)
categoria = as.numeric(categoria$STATUS_fact)
id = 1:N
set.seed(12345)
for(si in 1:SIM){
  for(j in 1:3){
    idcat = id[categoria==j] ## stratified per category j
    ran0 = sample(idcat, size=Ncatfit, replace=FALSE)
    FIT[si,(j-1)*Ncatfit+1:Ncatfit] <- sort(ran0)</pre>
    TEST[si,(j-1)*Ncattest+1:Ncattest] <- setdiff(idcat,ran0)</pre>
} }
```

Classification metrics for models predicting nominal outcomes

```
## Functions to compute classification metrics
## Ytrue = true response variable
## Ypred = predicted outcome
## cat = category
## TP = true positive
## TN = true negative
## FP = false positive
## FN = false negative
## Function to compute the precision per class=cat
fn precision class <- function(Ytrue, Ypred, cat){</pre>
  TP = sum(Ypred[Ytrue==cat]==cat)
 FP = sum(Ypred[Ytrue!=cat]==cat)
 precision = TP/(TP+FP)
 return(precision)
## Function to compute the recall per class=cat
fn_recall_class <- function(Ytrue, Ypred, cat){ ## cat==category</pre>
 TP = sum(Ypred[Ytrue==cat]==cat)
 FN = sum(Ypred[Ytrue==cat]!=cat)
 recall = TP/(TP+FN)
 return(recall)
}
## Function to compute the F1-score per class=cat
fn f1score class <- function(Ytrue, Ypred, cat) { ## cat==category</pre>
  TP = sum(Ypred[Ytrue==cat]==cat)
  FP = sum(Ypred[Ytrue!=cat]==cat)
  FN = sum(Ypred[Ytrue==cat]!=cat)
  precision = TP/(TP+FP)
  recall = TP/(TP+FN)
  f1score = 2*(precision*recall)/(precision+recall)
  return(f1score)
}
## To save classification metrics
## Fitxxx: metric for training subset. Testxxx: metric for testing subset
FitAccuracy = TestAccuracy <- array(NA, dim=c(SIM, 4)) ## Accuracy Rate
FitPrecisionClass = TestPrecisionClass <- array(NA, dim=c(SIM, 4, 3)) ## Precision per class
FitRecallClass = TestRecallClass <- array(NA,dim=c(SIM,4,3)) ## Recall per class
FitF1ScoreClass = TestF1ScoreClass <- array(NA, dim=c(SIM, 4,3)) ## F1-score per class
FitPrecisionMacroAve = TestPrecisionMacroAve <- array(NA,dim=c(SIM,4)) ## Precision Macro Average
FitRecallMacroAve = TestRecallMacroAve <- array(NA, dim=c(SIM,4)) ## Recall Macro Average
FitF1ScoreMacroAve = TestF1ScoreMacroAve <- array(NA, dim=c(SIM, 4)) ## F1-score Macro Average
```

Model estimation

```
for(sim in 1:SIM){ ## BEGIN sim
my fit = FIT[sim,] ## training subset
my_test = TEST[sim,] ## testing subset
## Training data subset
train1 <- trainc %>% filter(ID_fact%in%my_fit, rep==1) ## repetition=1
train2 <- trainc %>% filter(ID_fact%in%my_fit, rep==2) ## repetition=2
train3 <- trainc %>% filter(ID_fact%in%my_fit, rep==3) ## repetition=3
Yc = train1$STATUS_fact ## categorical response variable for training
n = length(Yc)
G = 3 # classes
## Testing data subset
test1 <- trainc %>% filter(ID_fact%in%my_test, rep==1) ## repetition=1
test2 <- trainc %>% filter(ID_fact%in%my_test, rep==2) ## repetition=2
test3 <- trainc %>% filter(ID_fact%in%my_test, rep==3) ## repetition=3
Yc.new = test1$STATUS fact ## categorical response variable for testing
n.new = length(Yc.new)
## Delete variables which are not used
train1 <- train1 %>% select(-c(SEX,rep,ID_fact))
train2 <- train2 %>% select(-c(SEX,rep,ID_fact))
train3 <- train3 %>% select(-c(SEX,rep,ID fact))
test1 <- test1 %>% select(-c(SEX,rep,ID_fact,STATUS_fact))
test2 <- test2 %>% select(-c(SEX,rep,ID_fact,STATUS_fact))
test3 <- test3 %>% select(-c(SEX,rep,ID_fact,STATUS_fact))
## Algorithm RSAM
## Replication-based stagewise additive modeling
##-----
## Algo1: Initialize the observation weights $w_i=1/n$, $i=1,...,n$
wi1 = rep(1/n,n)
## Algo2: BEGIN for replication j=1 to J do:
## REPLICATION j=1:
## Algo3: Fit a classifier T(x_j,z) to the training data using weights $wi$
mod1 <- vglm( STATUS_fact ~ . ,</pre>
             weights = wi1,
             multinomial(refLevel=1),
             data = train1)
## Predictions
pred1.vgam <- predict(mod1, newdata = train1, "response")</pre>
pred1 <- apply(pred1.vgam,1,which.max)</pre>
```

```
## Algo4: Compute err = \sum_{i=1}^{n} I[Y != I(xj,z)] / \sum_{i=1}^{n
err1 <- (sum(wi1*(Yc!=pred1))) / sum(wi1)</pre>
## Algo5: Compute $alpha = log (1-err)/err +log(G-1)$
alp1 \leftarrow log((1-err1)/err1) + log(G-1)
## Algo6: Set wi = wi* exp(alpha*I[Y \neq T(xj,z)])
wi2 = wi1*exp(alp1*(Yc!=pred1))
## Algo7: Re-normalize wi
wi2 = c(wi2/sum(wi2))
## REPLICATION j=2:
## Algo3: Fit a classifier T(x_j,z) to the training data using weights $wi$
mod2 <- vglm( STATUS_fact ~ . ,</pre>
                                                                    weights = wi2,
                                                                    multinomial(refLevel=1),
                                                                    data = train2)
### Predictions
pred2.vgam <- predict(mod2, newdata = train2, "response")</pre>
pred2 <- apply(pred2.vgam,1,which.max)</pre>
## Algo4: Compute err = \sum_{i=1}^{n} I[Y != I(xj,z)] / \sum_{i=1}^{n
err2 <- (sum(wi2*(Yc!=pred2))) / sum(wi2)</pre>
## Algo5: Compute $alpha = log (1-err)/err +log(G-1)$
alp2 \leftarrow log((1-err2)/err2) + log(G-1)
## Algo6: Set wi = wi* exp(alpha*I[Y \neq T(xj,z)])
wi3 = wi2*exp(alp2*(Yc!=pred2))
## Algo7: Re-normalize wi
wi3 = c(wi3/sum(wi3))
##-----
## REPLICATION j=3:
## Algo3: Fit a classifier $T(xj,z)$ to the training data using weights $wi$
mod3 <- vglm( STATUS_fact ~ . ,</pre>
                                                                    weights = wi3,
                                                                    multinomial(refLevel=1),
                                                                    data = train3)
### Predictions
pred3.vgam <- predict(mod3, newdata = train3, "response")</pre>
pred3 <- apply(pred3.vgam,1,which.max)</pre>
## Algo4: Compute err = \sum_{i=1}^{n} I[Y != I(xj,z)] / \sum_{i=1}^{n
err3 <- (sum(wi3*(Yc!=pred3))) / sum(wi3)</pre>
## Algo5: Compute $alpha = log (1-err)/err +log(G-1)$
alp3 \leftarrow log((1-err3)/err3) + log(G-1)
## Algo6: Set wi = wi* exp(alpha*I[Y \neq T(xj,z)])
wi4 = wi3*exp(alp3*(Yc!=pred3))
## Algo7: Re-normalize wi
wi4 = c(wi4/sum(wi4))
## Algo8: End for replication j=1 to J
## Algo9: Output T*(x,z) = arg \max_{G} \sum_{j=1}^{max} alpha*I[T(xj,z)=G]
```

```
pred = cbind(pred1,pred2,pred3)
alpha = c(alp1,alp2,alp3)
argclase = matrix(NA,n,3)
clase = rep(NA,n)
for(i in 1:n){
  argclase[i,1] = sum(alpha*(pred[i,]==1))
  argclase[i,2] = sum(alpha*(pred[i,]==2))
  argclase[i,3] = sum(alpha*(pred[i,]==3))
  clase[i] = which(argclase[i,]==max(argclase[i,]))
## Predict new subjects for testing subsets
pred1.new.vgam <- predict(mod1, newdata = test1, "response")</pre>
pred2.new.vgam <- predict(mod2, newdata = test2, "response")</pre>
pred3.new.vgam <- predict(mod3, newdata = test3, "response")</pre>
pred1.new <- apply(pred1.new.vgam,1,which.max)</pre>
pred2.new <- apply(pred2.new.vgam,1,which.max)</pre>
pred3.new <- apply(pred3.new.vgam,1,which.max)</pre>
pred.new = cbind(pred1.new,pred2.new,pred3.new)
argclase.new = matrix(NA,n.new,3)
clase.new = rep(NA,n.new)
for(i in 1:n.new){
  argclase.new[i,1] = sum(alpha*(pred.new[i,]==1))
  argclase.new[i,2] = sum(alpha*(pred.new[i,]==2))
  argclase.new[i,3] = sum(alpha*(pred.new[i,]==3))
  clase.new[i] = which(argclase.new[i,]==max(argclase.new[i,]))
##----
## End RSAM
## Classification Metrics for models predicting nominal outcomes
## Accuracy Rate
FitAccuracy[sim,] = c(sum(Yc==pred1)/n,
                      sum(Yc==pred2)/n,
                      sum(Yc==pred3)/n,
                      sum(Yc==clase)/n)
TestAccuracy[sim,] = c(sum(Yc.new==pred1.new)/n.new,
                       sum(Yc.new==pred2.new)/n.new,
                       sum(Yc.new==pred3.new)/n.new,
                        sum(Yc.new==clase.new)/n.new)
## Precision
for(cate in 1:3){
  FitPrecisionClass[sim,1, cate] = fn_precision_class(Yc, pred1, cate)
  FitPrecisionClass[sim,2, cate] = fn_precision_class(Yc, pred2, cate)
  FitPrecisionClass[sim,3, cate] = fn_precision_class(Yc, pred3, cate)
  FitPrecisionClass[sim,4, cate] = fn_precision_class(Yc, clase, cate)
```

```
TestPrecisionClass[sim,1, cate] = fn_precision_class(Yc.new, pred1.new, cate)
  TestPrecisionClass[sim,2, cate] = fn_precision_class(Yc.new, pred2.new, cate)
  TestPrecisionClass[sim,3, cate] = fn_precision_class(Yc.new, pred3.new, cate)
  TestPrecisionClass[sim,4, cate] = fn_precision_class(Yc.new, clase.new, cate)
}
for(rep in 1:4){
 FitPrecisionMacroAve[sim, rep] = mean(FitPrecisionClass[sim, rep,])
  TestPrecisionMacroAve[sim,rep] = mean(TestPrecisionClass[sim,rep,])
}
## Recall
for(cate in 1:3){
  FitRecallClass[sim,1, cate] = fn_recall_class(Yc, pred1, cate)
  FitRecallClass[sim,2, cate] = fn_recall_class(Yc, pred2, cate)
  FitRecallClass[sim,3, cate] = fn_recall_class(Yc, pred3, cate)
  FitRecallClass[sim,4, cate] = fn_recall_class(Yc, clase, cate)
  TestRecallClass[sim,1, cate] = fn_recall_class(Yc.new, pred1.new, cate)
  TestRecallClass[sim,2, cate] = fn_recall_class(Yc.new, pred2.new, cate)
  TestRecallClass[sim,3, cate] = fn_recall_class(Yc.new, pred3.new, cate)
  TestRecallClass[sim,4, cate] = fn_recall_class(Yc.new, clase.new, cate)
}
for(rep in 1:4){
  FitRecallMacroAve[sim, rep] = mean(FitRecallClass[sim, rep,])
  TestRecallMacroAve[sim,rep] = mean(TestRecallClass[sim,rep,])
}
## F1-Score
for(cate in 1:3){
  FitF1ScoreClass[sim,1, cate] = fn_f1score_class(Yc, pred1, cate)
  FitF1ScoreClass[sim,2, cate] = fn_f1score_class(Yc, pred2, cate)
  FitF1ScoreClass[sim,3, cate] = fn_f1score_class(Yc, pred3, cate)
  FitF1ScoreClass[sim,4, cate] = fn_f1score_class(Yc, clase, cate)
  TestF1ScoreClass[sim,1, cate] = fn_f1score_class(Yc.new, pred1.new, cate)
  TestF1ScoreClass[sim,2, cate] = fn_f1score_class(Yc.new, pred2.new, cate)
  TestF1ScoreClass[sim,3, cate] = fn_f1score_class(Yc.new, pred3.new, cate)
  TestF1ScoreClass[sim,4, cate] = fn_f1score_class(Yc.new, clase.new, cate)
for(rep in 1:4){
  FitF1ScoreMacroAve[sim, rep] = mean(FitF1ScoreClass[sim, rep,])
  TestF1ScoreMacroAve[sim,rep] = mean(TestF1ScoreClass[sim,rep,])
}
}## END sim
```

Results

Accuracy Rate

```
columna = c("rep1", "rep2", "rep3", "ensemble")
renglon = c("fit_mean","fit_sd","test_mean","test_sd")
summary(FitAccuracy)
##
         ۷1
                         ٧2
                                          VЗ
                                                          ۷4
                          :0.6488
                                                           :0.7976
## Min.
         :0.6905
                                          :0.6964
                   Min.
                                    Min.
                                                    Min.
## 1st Qu.:0.7321
                   1st Qu.:0.7009 1st Qu.:0.7500
                                                    1st Qu.:0.8929
## Median :0.7500
                   Median :0.7202 Median :0.7679
                                                    Median :0.9107
## Mean :0.7514
                   Mean :0.7225 Mean :0.7747
                                                    Mean :0.9127
## 3rd Qu.:0.7738
                    3rd Qu.:0.7396
                                    3rd Qu.:0.7976
                                                    3rd Qu.:0.9345
## Max. :0.8155
                   Max. :0.8095
                                    Max. :0.8750
                                                    Max.
                                                           :1.0000
apply(FitAccuracy,2,"sd")
## [1] 0.02780167 0.03343475 0.03572806 0.03704453
summary(TestAccuracy)
##
         ۷1
                         ٧2
                                          ٧3
                                                          ٧4
## Min. :0.4035
                   Min.
                          :0.3860 Min.
                                          :0.3509
                                                    Min.
                                                           :0.4561
## 1st Qu.:0.5088
                   1st Qu.:0.4561 1st Qu.:0.5088
                                                    1st Qu.:0.5439
                   Median :0.5088 Median :0.5614
                                                    Median :0.5789
## Median :0.5439
## Mean :0.5419
                   Mean
                         :0.5026
                                    Mean :0.5588
                                                    Mean :0.5916
## 3rd Qu.:0.5833
                    3rd Qu.:0.5439
                                    3rd Qu.:0.5965
                                                    3rd Qu.:0.6316
## Max.
        :0.6667
                   Max.
                         :0.6667
                                    Max. :0.7544
                                                    Max.
                                                           :0.7193
apply(TestAccuracy,2,"sd")
## [1] 0.06112542 0.05950065 0.06393360 0.05692129
RESaccuracy <- rbind(apply(FitAccuracy,2,"mean"), apply(FitAccuracy,2,"sd"),</pre>
                    apply(TestAccuracy,2,"mean"),apply(TestAccuracy,2,"sd"))
colnames(RESaccuracy) = columna
rownames(RESaccuracy) = renglon
write.csv(RESaccuracy, file=paste0(archivo,"_accuracy",".csv"))
```

Precision Macro Average

```
summary(FitPrecisionMacroAve)
##
          V1
                           V2
                                            VЗ
                                                              ۷4
                            :0.6447
##
  Min.
           :0.6894
                     Min.
                                      Min.
                                             :0.7078
                                                        Min.
                                                               :0.7991
   1st Qu.:0.7339
                     1st Qu.:0.7002
                                      1st Qu.:0.7581
                                                        1st Qu.:0.8930
  Median :0.7505
                     Median :0.7222
                                      Median :0.7716
                                                        Median : 0.9109
## Mean
           :0.7526
                     Mean
                            :0.7227
                                      Mean
                                             :0.7782
                                                        Mean
                                                               :0.9132
   3rd Qu.:0.7769
                     3rd Qu.:0.7402
                                      3rd Qu.:0.8007
                                                        3rd Qu.:0.9354
## Max.
           :0.8153
                            :0.8090
                                             :0.8746
                                                               :1.0000
                     Max.
                                      Max.
                                                        Max.
apply(FitPrecisionMacroAve,2,"sd")
## [1] 0.02816140 0.03415584 0.03465540 0.03690173
summary(TestPrecisionMacroAve)
##
          V1
                           V2
                                            VЗ
                                                              ۷4
##
           :0.3903
                            :0.3834
                                             :0.3702
                                                               :0.4500
  Min.
                     Min.
                                      Min.
                                                        Min.
   1st Qu.:0.5116
                     1st Qu.:0.4546
                                      1st Qu.:0.5247
                                                        1st Qu.:0.5569
  Median :0.5539
                     Median :0.4996
                                      Median :0.5681
                                                        Median :0.5930
## Mean
           :0.5463
                     Mean
                            :0.5007
                                      Mean
                                             :0.5671
                                                        Mean
                                                               :0.5969
   3rd Qu.:0.5943
                     3rd Qu.:0.5418
                                      3rd Qu.:0.6102
                                                        3rd Qu.:0.6441
##
           :0.6741
                                             :0.7591
                                                               :0.7244
  Max.
                     Max.
                            :0.6854
                                      Max.
                                                        Max.
apply(TestPrecisionMacroAve, 2, "sd")
## [1] 0.06481502 0.06315414 0.06483409 0.05866465
RESprecision <- rbind(apply(FitPrecisionMacroAve,2,"mean"), apply(FitPrecisionMacroAve,2,"sd"),
                      apply(TestPrecisionMacroAve,2,"mean"),apply(TestPrecisionMacroAve,2,"sd"))
colnames(RESprecision) = columna
rownames(RESprecision) = renglon
write.csv(RESprecision, file=paste0(archivo,"_precision",".csv"))
```

Recall Macro Average

summary(FitRecallMacroAve) ## V1 V2 VЗ ۷4 :0.6488 ## $\mathtt{Min}.$:0.6905 Min. Min. :0.6964 Min. :0.7976 1st Qu.:0.7321 1st Qu.:0.7009 1st Qu.:0.7500 1st Qu.:0.8929 Median :0.7500 Median :0.7202 Median :0.7679 Median : 0.9107 ## Mean :0.7514 Mean :0.7225 Mean :0.7747 Mean :0.9127 3rd Qu.:0.7738 3rd Qu.:0.7396 3rd Qu.:0.7976 3rd Qu.:0.9345 ## Max. :0.8155 :0.8095 :0.8750 :1.0000 Max. Max. Max. apply(FitRecallMacroAve,2,"sd") ## [1] 0.02780167 0.03343475 0.03572806 0.03704453 summary(TestRecallMacroAve)

```
##
          V1
                           ٧2
                                             VЗ
                                                               ۷4
##
           :0.4035
                             :0.3860
                                              :0.3509
                                                                :0.4561
   Min.
                     Min.
                                       Min.
                                                        Min.
   1st Qu.:0.5088
                     1st Qu.:0.4561
                                       1st Qu.:0.5088
                                                         1st Qu.:0.5439
  Median :0.5439
                     Median :0.5088
                                       Median :0.5614
                                                         Median :0.5789
## Mean
           :0.5419
                     Mean
                            :0.5026
                                       Mean
                                              :0.5588
                                                        Mean
                                                                :0.5916
    3rd Qu.:0.5833
                     3rd Qu.:0.5439
                                       3rd Qu.:0.5965
                                                         3rd Qu.:0.6316
##
           :0.6667
  Max.
                     Max.
                             :0.6667
                                       Max.
                                              :0.7544
                                                         Max.
                                                                :0.7193
apply(TestRecallMacroAve, 2, "sd")
```

```
## [1] 0.06112542 0.05950065 0.06393360 0.05692129
```

F1-Score Macro Average

summary(FitF1ScoreMacroAve)

```
##
          V1
                            V2
                                              VЗ
                                                                ۷4
                             :0.6447
##
   \mathtt{Min}.
           :0.6892
                      Min.
                                        Min.
                                               :0.7000
                                                          Min.
                                                                 :0.7978
   1st Qu.:0.7327
                      1st Qu.:0.6989
                                        1st Qu.:0.7506
                                                          1st Qu.:0.8928
  Median :0.7495
                      Median :0.7204
                                        Median :0.7684
                                                          Median : 0.9107
## Mean
           :0.7514
                      Mean
                             :0.7211
                                        Mean
                                               :0.7749
                                                          Mean
                                                                 :0.9127
    3rd Qu.:0.7749
                      3rd Qu.:0.7392
                                        3rd Qu.:0.7976
                                                          3rd Qu.:0.9348
## Max.
           :0.8145
                             :0.8087
                                               :0.8747
                                                                 :1.0000
                      Max.
                                        Max.
                                                          Max.
apply(FitF1ScoreMacroAve,2,"sd")
```

[1] 0.02786029 0.03401390 0.03564010 0.03705223

summary(TestF1ScoreMacroAve)

```
##
          V1
                           V2
                                             VЗ
                                                              ۷4
##
           :0.3938
                            :0.3795
                                              :0.3578
                                                               :0.4504
   Min.
                     Min.
                                      Min.
                                                        Min.
   1st Qu.:0.5080
                     1st Qu.:0.4538
                                      1st Qu.:0.5101
                                                        1st Qu.:0.5471
  Median :0.5463
                     Median :0.4929
                                      Median :0.5592
                                                        Median :0.5801
## Mean
           :0.5391
                     Mean
                            :0.4955
                                      Mean
                                              :0.5561
                                                        Mean
                                                               :0.5888
   3rd Qu.:0.5836
                     3rd Qu.:0.5378
                                       3rd Qu.:0.5992
                                                        3rd Qu.:0.6340
##
           :0.6678
                                                               :0.7206
  Max.
                     Max.
                            :0.6611
                                      Max.
                                              :0.7519
                                                        Max.
apply(TestF1ScoreMacroAve,2,"sd")
```

[1] 0.06226287 0.05996349 0.06468090 0.05832062