

# Support Vector Machine (SVM) Linear kernel

Feature space partition ensemble model for replication (FESPAE)

EGG data-based experiments

**Article:** Lizbeth Naranjo, Carlos J. Perez, Daniel F. Merino (2025). A data ensemble-based approach for detecting vocal disorders using replicated acoustic biomarkers from electroglottography. *Sensing and Bio-Sensing Research Journal*, vol, num, pages.

```
library(tidyverse)
library(e1071)
## change the address where the file will be saved
address = "~/Documents/GitHub/"
setwd("~/Documents/GitHub/")
```

## EGG data-based experiments

```
## Comment or uncomment the options: EGG-a, EGG-i, EGG-u
```

```
## EGG-a
## datos2 <- read.csv(paste0(address,"a_egg_saarbrucken.csv"),
##                    sep = ";",header=TRUE, dec=",")

## name of the files to save results
## archivo = "FESPAE_crossval_strata_allvar_SVM_linear_Saarbrucken_egg_a"
```

```
## EGG-i
## datos2 <- read.csv(paste0(address,"i_egg_saarbrucken.csv"),
##                    sep = ";",header=TRUE, dec=",")

## name of the files to save results
## archivo = "FESPAE_crossval_strata_allvar_SVM_linear_Saarbrucken_egg_i"
```

```
## EGG-u
datos2 <- read.csv(paste0(address,"u_egg_saarbrucken.csv"),
                  sep = ";",header=TRUE, dec=",")

## name of the files to save results
archivo = "FESPAE_crossval_strata_allvar_SVM_linear_Saarbrucken_egg_u"
```

```
dim(datos2)
```

```
[1] 675 36
```

```
summary(datos2)
```

| ID_fact          | status_fact      | SEX              | JITTER           |
|------------------|------------------|------------------|------------------|
| Min. : 1.0       | Min. :0          | Min. :0.0000     | Min. : 0.00      |
| 1st Qu.:169.5    | 1st Qu.:0        | 1st Qu.:0.0000   | 1st Qu.: 0.45    |
| Median :338.0    | Median :1        | Median :0.0000   | Median : 1.06    |
| Mean :338.0      | Mean :1          | Mean :0.4133     | Mean : 13.84     |
| 3rd Qu.:506.5    | 3rd Qu.:2        | 3rd Qu.:1.0000   | 3rd Qu.: 17.95   |
| Max. :675.0      | Max. :2          | Max. :1.0000     | Max. :273.97     |
| SHIMMER          | CPP              | D2               | FZCF             |
| Min. :0.00000    | Min. :12.04      | Min. : 2.000     | Min. : 5.00      |
| 1st Qu.:0.03000  | 1st Qu.:18.02    | 1st Qu.: 3.625   | 1st Qu.: 11.00   |
| Median :0.05000  | Median :20.86    | Median : 4.410   | Median : 16.00   |
| Mean :0.06012    | Mean :21.36      | Mean : 4.738     | Mean : 42.47     |
| 3rd Qu.:0.08000  | 3rd Qu.:23.95    | 3rd Qu.: 5.445   | 3rd Qu.: 23.00   |
| Max. :0.38000    | Max. :34.19      | Max. :18.380     | Max. :5280.00    |
| GNR              | HNHR             | HURST            | LZ               |
| Min. :0.4100     | Min. : -3.94     | Min. :0.1000     | Min. : 19.0      |
| 1st Qu.:0.6350   | 1st Qu.:20.15    | 1st Qu.:0.6150   | 1st Qu.: 37.0    |
| Median :0.8000   | Median :23.48    | Median :0.8700   | Median : 50.0    |
| Mean :0.9465     | Mean :22.34      | Mean :0.8806     | Mean : 54.2      |
| 3rd Qu.:1.0950   | 3rd Qu.:26.51    | 3rd Qu.:1.1350   | 3rd Qu.: 65.5    |
| Max. :5.0900     | Max. :33.91      | Max. :1.7700     | Max. :279.0      |
| MFCC0            | MFCC1            | MFCC2            | MFCC3            |
| Min. : -2.8800   | Min. : -19.06    | Min. : -30.610   | Min. : -45.920   |
| 1st Qu.: -1.1200 | 1st Qu.: 11.15   | 1st Qu.: -0.635  | 1st Qu.: -21.495 |
| Median : -0.5300 | Median : 18.10   | Median : 10.670  | Median : -7.850  |
| Mean : -0.5224   | Mean : 16.26     | Mean : 9.860     | Mean : -8.324    |
| 3rd Qu.: 0.1200  | 3rd Qu.: 22.50   | 3rd Qu.: 19.775  | 3rd Qu.: 3.180   |
| Max. : 2.0500    | Max. : 32.80     | Max. : 46.420    | Max. : 48.690    |
| MFCC4            | MFCC5            | MFCC6            | MFCC7            |
| Min. : -57.250   | Min. : -43.400   | Min. : -43.040   | Min. : -41.830   |
| 1st Qu.: -20.330 | 1st Qu.: -14.910 | 1st Qu.: -15.365 | 1st Qu.: -16.115 |
| Median : -10.640 | Median : -7.710  | Median : -8.610  | Median : -8.020  |
| Mean : -11.226   | Mean : -7.712    | Mean : -8.940    | Mean : -8.249    |
| 3rd Qu.: -2.105  | 3rd Qu.: 0.945   | 3rd Qu.: -2.035  | 3rd Qu.: -0.215  |
| Max. : 25.070    | Max. : 34.400    | Max. : 26.060    | Max. : 36.600    |
| MFCC8            | MFCC9            | MFCC10           | MFCC11           |
| Min. : -51.090   | Min. : -47.06    | Min. : -39.590   | Min. : -39.150   |
| 1st Qu.: -15.975 | 1st Qu.: -13.44  | 1st Qu.: -12.060 | 1st Qu.: -12.575 |
| Median : -7.810  | Median : -6.26   | Median : -4.420  | Median : -4.380  |
| Mean : -7.906    | Mean : -5.64     | Mean : -4.325    | Mean : -4.466    |
| 3rd Qu.: -0.240  | 3rd Qu.: 1.71    | 3rd Qu.: 2.080   | 3rd Qu.: 2.885   |
| Max. : 36.520    | Max. : 40.73     | Max. : 42.350    | Max. : 35.350    |
| MFCC12           | PERMUTATION      | PPE              | SHANNON          |
| Min. : -37.200   | Min. : 1.110     | Min. : 0.0000    | Min. : 11.92     |
| 1st Qu.: -11.775 | 1st Qu.: 1.440   | 1st Qu.: 0.5300  | 1st Qu.: 12.16   |
| Median : -5.020  | Median : 1.570   | Median : 0.5500  | Median : 12.19   |
| Mean : -4.221    | Mean : 1.642     | Mean : 0.5315    | Mean : 12.18     |

|                 |                 |                  |                |
|-----------------|-----------------|------------------|----------------|
| 3rd Qu.: 2.625  | 3rd Qu.:1.780   | 3rd Qu.:0.5700   | 3rd Qu.:12.21  |
| Max. : 29.550   | Max. :2.580     | Max. :0.5700     | Max. :12.26    |
| ZCR             | energyentropy   | spectralcentroid | spectralspread |
| Min. :0.01000   | Min. :2.500     | Min. :0.0700     | Min. :0.1200   |
| 1st Qu.:0.02000 | 1st Qu.:3.260   | 1st Qu.:0.1100   | 1st Qu.:0.1600 |
| Median :0.03000 | Median :3.310   | Median :0.1200   | Median :0.1800 |
| Mean :0.03846   | Mean :3.269     | Mean :0.1206     | Mean :0.1798   |
| 3rd Qu.:0.05000 | 3rd Qu.:3.320   | 3rd Qu.:0.1300   | 3rd Qu.:0.1900 |
| Max. :0.20000   | Max. :3.320     | Max. :0.3300     | Max. :0.3300   |
| spectralentropy | spectralrolloff | RPDE             | rep            |
| Min. :0.0000    | Min. :0.01000   | Min. :0.0100     | Min. :1        |
| 1st Qu.:0.0500  | 1st Qu.:0.04000 | 1st Qu.:0.2000   | 1st Qu.:1      |
| Median :0.1100  | Median :0.05000 | Median :0.2800   | Median :2      |
| Mean :0.1832    | Mean :0.05613   | Mean :0.3194     | Mean :2        |
| 3rd Qu.:0.2400  | 3rd Qu.:0.07000 | 3rd Qu.:0.3900   | 3rd Qu.:3      |
| Max. :1.6400    | Max. :0.37000   | Max. :0.9000     | Max. :3        |

```
head(datos2)
```

|   | ID_fact        | status_fact     | SEX             | JITTER  | SHIMMER | CPP           | D2               | FZCF  | GNE   | HNR   | HURST  | LZ     |    |
|---|----------------|-----------------|-----------------|---------|---------|---------------|------------------|-------|-------|-------|--------|--------|----|
| 1 | 1              |                 | 0               | 0       | 0.21    | 0.02          | 28.48            | 4.35  | 25    | 0.63  | 27.12  | 1.20   | 32 |
| 2 | 2              |                 | 0               | 0       | 0.43    | 0.06          | 22.18            | 3.23  | 31    | 0.58  | 18.23  | 1.38   | 44 |
| 3 | 3              |                 | 0               | 0       | 0.46    | 0.03          | 24.91            | 5.24  | 27    | 0.60  | 24.93  | 1.30   | 33 |
| 4 | 4              |                 | 0               | 0       | 0.49    | 0.02          | 31.64            | 3.14  | 24    | 0.57  | 25.71  | 1.17   | 34 |
| 5 | 5              |                 | 0               | 0       | 11.39   | 0.09          | 24.74            | 2.16  | 40    | 0.43  | 15.64  | 1.51   | 39 |
| 6 | 6              |                 | 0               | 0       | 0.33    | 0.03          | 29.29            | 3.27  | 33    | 0.47  | 24.57  | 1.40   | 33 |
|   | MFCC0          | MFCC1           | MFCC2           | MFCC3   | MFCC4   | MFCC5         | MFCC6            | MFCC7 | MFCC8 | MFCC9 | MFCC10 | MFCC11 |    |
| 1 | -0.41          | 8.69            | -0.89           | 0.03    | 3.66    | -0.03         | -0.20            | -3.42 | -4.11 | -6.53 | -8.78  | -9.64  |    |
| 2 | -1.47          | 3.10            | 15.86           | 5.73    | 9.91    | 4.40          | 4.72             | 0.60  | 2.27  | -2.16 | -3.27  | -3.26  |    |
| 3 | -0.92          | 7.38            | 11.85           | 2.93    | 2.55    | 2.91          | 3.56             | -1.11 | -1.74 | -4.55 | -4.97  | -7.97  |    |
| 4 | -0.52          | 8.81            | -2.68           | 2.83    | -0.76   | -0.60         | -2.30            | -5.78 | -4.10 | -7.55 | -7.57  | -8.92  |    |
| 5 | -2.06          | 11.23           | 9.58            | 5.36    | 7.67    | 2.17          | 3.94             | 4.12  | 4.38  | 0.62  | 0.97   | 1.00   |    |
| 6 | -1.39          | 14.83           | 3.50            | -2.30   | 9.86    | 2.90          | 1.00             | 6.24  | -1.52 | 1.44  | -0.26  | -1.19  |    |
|   | MFCC12         | PERMUTATION     | PPE             | SHANNON | ZCR     | energyentropy | spectralcentroid |       |       |       |        |        |    |
| 1 | -11.13         |                 | 2.02            | 0.55    | 12.19   | 0.02          | 3.31             |       |       |       | 0.13   |        |    |
| 2 | -3.81          |                 | 2.26            | 0.48    | 12.20   | 0.02          | 3.27             |       |       |       | 0.12   |        |    |
| 3 | -5.99          |                 | 1.99            | 0.55    | 12.21   | 0.02          | 3.30             |       |       |       | 0.12   |        |    |
| 4 | -8.74          |                 | 1.68            | 0.55    | 12.17   | 0.02          | 3.31             |       |       |       | 0.12   |        |    |
| 5 | -0.09          |                 | 1.84            | 0.44    | 12.19   | 0.01          | 3.19             |       |       |       | 0.09   |        |    |
| 6 | -1.26          |                 | 1.64            | 0.53    | 12.17   | 0.01          | 3.28             |       |       |       | 0.11   |        |    |
|   | spectralspread | spectralentropy | spectralrolloff | RPDE    | rep     |               |                  |       |       |       |        |        |    |
| 1 |                | 0.19            |                 | 0.11    |         | 0.02          | 0.21             |       | 1     |       |        |        |    |
| 2 |                | 0.21            |                 | 0.06    |         | 0.02          | 0.50             |       | 2     |       |        |        |    |
| 3 |                | 0.21            |                 | 0.06    |         | 0.02          | 0.32             |       | 3     |       |        |        |    |
| 4 |                | 0.18            |                 | 0.13    |         | 0.03          | 0.32             |       | 1     |       |        |        |    |
| 5 |                | 0.17            |                 | 0.03    |         | 0.01          | 0.58             |       | 2     |       |        |        |    |
| 6 |                | 0.18            |                 | 0.08    |         | 0.02          | 0.37             |       | 3     |       |        |        |    |

## Re-Scale explanatory variables

```
## Scale the variables
datos2 <- as.data.frame(datos2)
datos2$STATUS_fact = as.factor(as.numeric(factor(datos2$status_fact)))

table(datos2$STATUS_fact)
```

```
 1    2    3
225 225 225
```

```
datos <- transform(datos2,
  sJITTER= scale(JITTER), sSHIMMER= scale(SHIMMER), sCPP= scale(CPP),
  sD2= scale(D2), sFZCF= scale(FZCF), sGNE= scale(GNE),
  sHNR= scale(HNR), sHURST= scale(HURST), sLZ= scale(LZ),
  sMFCC0= scale(MFCC0),
  sMFCC1= scale(MFCC1), sMFCC2= scale(MFCC2), sMFCC3= scale(MFCC3),
  sMFCC4= scale(MFCC4), sMFCC5= scale(MFCC5), sMFCC6= scale(MFCC6),
  sMFCC7= scale(MFCC7), sMFCC8= scale(MFCC8), sMFCC9= scale(MFCC9),
  sMFCC10= scale(MFCC10), sMFCC11= scale(MFCC11), sMFCC12= scale(MFCC12),
  sPERMUTATION= scale(PERMUTATION), sPPE= scale(PPE), sSHANNON= scale(SHANNON),
  sZCR= scale(ZCR),
  senergyentropy= scale(energyentropy), sspectralcentroid= scale(spectralcentroid),
  sspectralspread= scale(spectralspread), sspectralentropy= scale(spectralentropy),
  sspectralrolloff= scale(spectralrolloff), sRPDE= scale(RPDE))

datos$ID_fact = rep(1:225,each=3)

dim(datos)
```

```
[1] 675 69
```

```
## data set
trainc <- datos %>% select(
  sJITTER, sSHIMMER, sCPP, sD2, sFZCF,
  sGNE, sHNR, sHURST, sLZ, sMFCC0,
  sMFCC1, sMFCC2, sMFCC3, sMFCC4, sMFCC5,
  sMFCC6, sMFCC7, sMFCC8, sMFCC9, sMFCC10,
  sMFCC11, sMFCC12,
  sPERMUTATION, sPPE, sSHANNON, sZCR,
  senergyentropy, sspectralcentroid, sspectralspread,
  sspectralentropy, sspectralrolloff, sRPDE,
  STATUS_fact, SEX, rep, ID_fact)
```

# Crossvalidation

## Subspaces

```
## Function to compute the Mode
Mode <- function(x, na.rm = FALSE) {
  if(na.rm){
    x = x[!is.na(x)]
  }
  ux <- unique(x)
  return(ux[which.max(tabulate(match(x, ux)))]])
}

## Partition of subspaces
## The feature space is randomly partitioned into K subspaces with roughly equal sizes
## k = number of predictors
## K = subspaces

K0 = 4 ## sub-spaces
k = 32 ## explanatory variables
k2 = round(k/K0)
space = 1:k
subspaces = rep(list(rep(NA,k2)),K0) ## Subspaces
set.seed(12345)
for(j in 1:(K0-1)){
  space1 = sample(space, size=k2, replace=FALSE)
  space = setdiff(space,space1)
  subspaces[[j]] = space1[order(space1)]
}
space1 = space
subspaces[[K0]] = space1[order(space1)]
## 32 features = 1x32, 2x16, 4x8,
subspaces

## [[1]]
## [1] 11 14 16 19 24 26 28 29
##
## [[2]]
## [1] 2 6 7 10 12 21 30 32
##
## [[3]]
## [1] 1 4 5 9 13 15 27 31
##
## [[4]]
## [1] 3 8 17 18 20 22 23 25
```

## Training and testing data subsets

```
## Select data: 75% training & 25% testing stratified per category
SIM = 100  ## repeat N times the cross-validation process
N = 225  ## sample size
Nfit = 168  ## sample size for training subset
Ntest = 57  ## sample size for testing subset
Ncat = 75  ## sample size per category
Ncatfit = 56  ## training per category
Ncattest = 19  ## testing per category
FIT <- matrix(0,SIM,Nfit)  ## training subsets
TEST <- matrix(0,SIM,Ntest)  ## testing subsets

categoria = trainc %>% filter(rep==1) %>% select(STATUS_fact)
categoria = as.numeric(categoria$STATUS_fact)
id = 1:N
set.seed(12345)
for(si in 1:SIM){
  for(j in 1:3){
    idcat = id[categoria==j]  ## stratified per category j
    ran0 = sample(idcat, size=Ncatfit, replace=FALSE)

    FIT[si,(j-1)*Ncatfit+1:Ncatfit] <- sort(ran0)
    TEST[si,(j-1)*Ncattest+1:Ncattest] <- setdiff(idcat,ran0)
  }
}
```

## Classification metrics for models predicting nominal outcomes

```
## Functions to compute classification metrics
## Ytrue = true response variable
## Ypred = predicted outcome
## cat = category
## TP = true positive
## TN = true negative
## FP = false positive
## FN = false negative

## Function to compute the precision per class=cat
fn_precision_class <- function(Ytrue,Ypred,cat){
  TP = sum(Ypred[Ytrue==cat]==cat)
  FP = sum(Ypred[Ytrue!=cat]==cat)
  precision = TP/(TP+FP)
  return(precision)
}

## Function to compute the recall per class=cat
fn_recall_class <- function(Ytrue,Ypred,cat){ ## cat==category
  TP = sum(Ypred[Ytrue==cat]==cat)
  FN = sum(Ypred[Ytrue==cat]!=cat)
  recall = TP/(TP+FN)
  return(recall)
}

## Function to compute the F1-score per class=cat
fn_f1score_class <- function(Ytrue,Ypred,cat){ ## cat==category
  TP = sum(Ypred[Ytrue==cat]==cat)
  FP = sum(Ypred[Ytrue!=cat]==cat)
  FN = sum(Ypred[Ytrue==cat]!=cat)
  precision = TP/(TP+FP)
  recall = TP/(TP+FN)
  f1score = 2*(precision*recall)/(precision+recall)
  return(f1score)
}

## To save classification metrics
## Fitxxx: metric for training subset. Testxxx: metric for testing subset
FitAccuracy = TestAccuracy <- array(NA,dim=c(SIM,1)) ## Accuracy Rate
FitPrecisionClass = TestPrecisionClass <- array(NA,dim=c(SIM,1,3)) ## Precision per class
FitRecallClass = TestRecallClass <- array(NA,dim=c(SIM,1,3)) ## Recall per class
FitF1ScoreClass = TestF1ScoreClass <- array(NA,dim=c(SIM,1,3)) ## F1-score per class
FitPrecisionMacroAve = TestPrecisionMacroAve <- array(NA,dim=c(SIM,1)) ## Precision Macro Average
FitRecallMacroAve = TestRecallMacroAve <- array(NA,dim=c(SIM,1)) ## Recall Macro Average
FitF1ScoreMacroAve = TestF1ScoreMacroAve <- array(NA,dim=c(SIM,1)) ## F1-score Macro Average
```

## Cross-validation

```
##-----
for(sim in 1:SIM){ ### BEGIN sim
##-----

my_fit = FIT[sim,]    ## training subset
my_test = TEST[sim,]  ## testing subset

## Training data subset
train1 <- trainc %>% filter(ID_fact%in%my_fit, rep==1) ## repetition=1
train2 <- trainc %>% filter(ID_fact%in%my_fit, rep==2) ## repetition=2
train3 <- trainc %>% filter(ID_fact%in%my_fit, rep==3) ## repetition=3

Yc = train1$STATUS_fact    ## categorical response variable for training
n = length(Yc)
G = 3 # classes

## Testing data subset
test1 <- trainc %>% filter(ID_fact%in%my_test, rep==1) ## repetition=1
test2 <- trainc %>% filter(ID_fact%in%my_test, rep==2) ## repetition=2
test3 <- trainc %>% filter(ID_fact%in%my_test, rep==3) ## repetition=3

Yc.new = test1$STATUS_fact    ## categorical response variable for testing
n.new = length(Yc.new)

## Delete variables which are not used
train1 <- train1 %>% select(-c(rep,ID_fact))
train2 <- train2 %>% select(-c(rep,ID_fact))
train3 <- train3 %>% select(-c(rep,ID_fact))
test1 <- test1 %>% select(-c(rep,ID_fact))
test2 <- test2 %>% select(-c(rep,ID_fact))
test3 <- test3 %>% select(-c(rep,ID_fact))

##-----
## Algorithm FESPAE
## Feature space partition ensemble model for replication
##-----

## Algo1: The feature space is randomly partitioned into M subspaces, {S1,S2,...,SM}

K0 = 4 ## sub-spaces
k = 32 ## explanatory variables
k2 = round(k/K0)
space = 1:k
subspaces = rep(list(rep(NA,k2)),K0) ## Subspaces
set.seed(12345)
for(j in 1:(K0-1)){
  space1 = sample(space, size=k2, replace=FALSE)
  space = setdiff(space,space1)
  subspaces[[j]] = space1[order(space1)]
}
space1 = space
```



```

subspaces[[K0]] = space1[order(space1)]
# 32 features = 1x32, 2x16, 4x8,

##-----
## Algo2: for feature subspace m = 1 to M do

pred.vgam = array(NA,dim=c(n,K0,3)) ## 3 repetitions
pred.new.vgam = array(NA,dim=c(n.new,K0,3)) ## 3 repetitions
##-----
## Algo3: for replication j = 1 to J do

## REPLICATION j=1:
for(parti1 in 1:K0){ ## partition of the subspaces
train1_par = train1[,c(subspaces[[parti1]],k+1)]
test1_par = test1[,c(subspaces[[parti1]],k+1)]

## Algo4: Fit a classifier  $T(x_j, z)$ ,  $x_j \in S_m$ , to the training data
mod1 <- tune( "svm", STATUS_fact ~ . ,
              data = train1_par,
              kernel = "linear",
              ranges = list(cost=c(0.01,0.1,0.5,1,5,10,20,50)) )
## summary(mod1)
mejor_mod1 <- mod1$best.model

## Algo5: Compute the C response probabilities  $\{\pi^{(m,j)}_{ic}\}$ , for  $i=1, \dots, n$ .
## Predictions
predict1 <- predict(mejor_mod1, newdata = train1_par)
predict1.new <- predict(mejor_mod1, newdata = test1_par)

pred.vgam[,parti1,1] = predict1
pred.new.vgam[,parti1,1] = predict1.new
}

## REPLICATION j=2:
for(parti2 in 1:K0){ ## partition of the subspaces
train2_par = train2[,c(subspaces[[parti2]],k+1)]
test2_par = test2[,c(subspaces[[parti2]],k+1)]

## Algo4: Fit a classifier  $T(x_j, z)$ ,  $x_j \in S_m$ , to the training data
mod2 <- tune( "svm", STATUS_fact ~ . ,
              data = train2_par,
              kernel = "linear",
              ranges = list(cost=c(0.01,0.1,0.5,1,5,10,20,50)) )
## summary(mod2)
mejor_mod2 <- mod2$best.model

## Algo5: Compute the C response probabilities  $\{\pi^{(m,j)}_{ic}\}$ , for  $i=1, \dots, n$ .
## Predictions
predict2 <- predict(mejor_mod2, newdata = train2_par)
predict2.new <- predict(mejor_mod2, newdata = test2_par)

pred.vgam[,parti2,2] = predict2
pred.new.vgam[,parti2,2] = predict2.new

```

```

}

## REPLICATION j=3:
for(parti3 in 1:K0){ ## partition of the subspaces
train3_par = train3[,c(subspaces[[parti3]],k+1)]
test3_par = test3[,c(subspaces[[parti3]],k+1)]

## Algo4: Fit a classifier  $T(x_j, z)$ ,  $x_j \in S_m$ , to the training data
mod3 <- tune( "svm", STATUS_fact ~ . ,
             data = train3_par,
             kernel = "linear",
             ranges = list(cost=c(0.01,0.1,0.5,1,5,10,20,50)) )
## summary(mod3)
mejor_mod3 <- mod3$best.model

## Algo5: Compute the C response probabilities  $\{\pi^{(m,j)}_{ic}\}$ , for  $i=1, \dots, n$ .
## Predictions
predict3 <- predict(mejor_mod3, newdata = train3_par)
predict3.new <- predict(mejor_mod3, newdata = test3_par)

pred.vgam[,parti3,3] = predict3
pred.new.vgam[,parti3,3] = predict3.new
}

##-----
## Algo6: End for replication  $j = 1$  to  $J$ 
## Algo7: End for feature subspace  $m = 1$  to  $M$ 
##-----
## Algo8: Output: compute the response probabilities  $\pi_{ic} = \text{mean}(\{\pi^{(m,j)}_{ic}\})$ 
##-----
## Algo8: Output: compute the response category  $T^*(x, z) = \arg \max \{\pi_{ic}\}$ 

pred.vgam_max = array(NA, dim=n)
for(i in 1:n){
  pred.vgam_max[i] = Mode(pred.vgam[i,,])
}
### Predict new subjects
pred.new.vgam_max = array(NA, dim=n.new)
for(i in 1:n.new){
  pred.new.vgam_max[i] = Mode(pred.new.vgam[i,,])
}

##-----
## End FESPAE
##-----
## Classification Metrics for models predicting nominal outcomes

## Accuracy Rate
FitAccuracy[sim,] = c(sum(Yc==pred.vgam_max)/n)

TestAccuracy[sim,] = c(sum(Yc.new==pred.new.vgam_max)/n.new)

## Precision

```

```

for(cate in 1:3){
  FitPrecisionClass[sim,1, cate] = fn_precision_class(Yc, pred.vgam_max, cate)
  TestPrecisionClass[sim,1, cate] = fn_precision_class(Yc.new, pred.new.vgam_max, cate)
}
FitPrecisionMacroAve[sim, 1] = mean(FitPrecisionClass[sim, 1,])
TestPrecisionMacroAve[sim,1] = mean(TestPrecisionClass[sim,1,])

## Recall
for(cate in 1:3){
  FitRecallClass[sim,1, cate] = fn_recall_class(Yc, pred.vgam_max, cate)
  TestRecallClass[sim,1, cate] = fn_recall_class(Yc.new, pred.new.vgam_max, cate)
}
FitRecallMacroAve[sim, 1] = mean(FitRecallClass[sim, 1,])
TestRecallMacroAve[sim,1] = mean(TestRecallClass[sim,1,])

## F1-Score
for(cate in 1:3){
  FitF1ScoreClass[sim,1, cate]= fn_f1score_class(Yc, pred.vgam_max, cate)
  TestF1ScoreClass[sim,1, cate] = fn_f1score_class(Yc.new, pred.new.vgam_max, cate)
}
FitF1ScoreMacroAve[sim, 1] = mean(FitF1ScoreClass[sim, 1,])
TestF1ScoreMacroAve[sim,1] = mean(TestF1ScoreClass[sim,1,])

##-----
} ## END sim
##-----

```

# Results

## Accuracy Rate

```
columna = c("ensemble")
renglon = c("fit_mean", "fit_sd", "test_mean", "test_sd")

summary(FitAccuracy)
```

```
##           V1
##  Min.      :0.6369
## 1st Qu.:0.6964
##  Median :0.7083
##   Mean   :0.7091
## 3rd Qu.:0.7262
##   Max.   :0.7798
```

```
apply(FitAccuracy, 2, "sd")
```

```
## [1] 0.02348649
```

```
summary(TestAccuracy)
```

```
##           V1
##  Min.      :0.4737
## 1st Qu.:0.5439
##  Median :0.5965
##   Mean   :0.5970
## 3rd Qu.:0.6360
##   Max.   :0.7544
```

```
apply(TestAccuracy, 2, "sd")
```

```
## [1] 0.06110303
```

```
RESaccuracy <- rbind(apply(FitAccuracy, 2, "mean"), apply(FitAccuracy, 2, "sd"),
                     apply(TestAccuracy, 2, "mean"), apply(TestAccuracy, 2, "sd"))
colnames(RESaccuracy) = columna
rownames(RESaccuracy) = renglon
write.csv(RESaccuracy, file=paste0(archivo, "_accuracy", ".csv"))
```

## Precision Macro Average

```
summary(FitPrecisionMacroAve)
```

```
##          V1
##  Min.    :0.6784
## 1st Qu.:0.7177
##  Median :0.7341
##   Mean  :0.7348
## 3rd Qu.:0.7519
##   Max.   :0.8057
```

```
apply(FitPrecisionMacroAve,2,"sd")
```

```
## [1] 0.02485598
```

```
summary(TestPrecisionMacroAve)
```

```
##          V1
##  Min.    :0.4695
## 1st Qu.:0.5767
##  Median :0.6260
##   Mean  :0.6260
## 3rd Qu.:0.6678
##   Max.   :0.7668
```

```
apply(TestPrecisionMacroAve,2,"sd")
```

```
## [1] 0.06321981
```

```
RESprecision <- rbind(apply(FitPrecisionMacroAve,2,"mean"), apply(FitPrecisionMacroAve,2,"sd"),
                      apply(TestPrecisionMacroAve,2,"mean"), apply(TestPrecisionMacroAve,2,"sd"))
colnames(RESprecision) = columna
rownames(RESprecision) = renglon
write.csv(RESprecision, file=paste0(archivo,"_precision",".csv"))
```

## Recall Macro Average

```
summary(FitRecallMacroAve)
```

```
##          V1
##  Min.    :0.6369
## 1st Qu.:0.6964
##  Median :0.7083
##   Mean   :0.7091
## 3rd Qu.:0.7262
##   Max.   :0.7798
```

```
apply(FitRecallMacroAve,2,"sd")
```

```
## [1] 0.02348649
```

```
summary(TestRecallMacroAve)
```

```
##          V1
##  Min.    :0.4737
## 1st Qu.:0.5439
##  Median :0.5965
##   Mean   :0.5970
## 3rd Qu.:0.6360
##   Max.   :0.7544
```

```
apply(TestRecallMacroAve,2,"sd")
```

```
## [1] 0.06110303
```

```
RESrecall <- rbind(apply(FitRecallMacroAve,2,"mean"), apply(FitRecallMacroAve,2,"sd"),
                    apply(TestRecallMacroAve,2,"mean"),apply(TestRecallMacroAve,2,"sd"))
colnames(RESrecall) = columna
rownames(RESrecall) = renglon
write.csv(RESrecall, file=paste0(archivo,"_recall",".csv"))
```

## F1-Score Macro Average

```
summary(FitF1ScoreMacroAve)
```

```
##          V1
##  Min.    :0.6375
## 1st Qu.:0.6949
##  Median :0.7107
##   Mean   :0.7099
## 3rd Qu.:0.7254
##   Max.   :0.7820
```

```
apply(FitF1ScoreMacroAve,2,"sd")
```

```
## [1] 0.02405304
```

```
summary(TestF1ScoreMacroAve)
```

```
##          V1
##  Min.    :0.4672
## 1st Qu.:0.5511
##  Median :0.5926
##   Mean   :0.5961
## 3rd Qu.:0.6362
##   Max.   :0.7566
```

```
apply(TestF1ScoreMacroAve,2,"sd")
```

```
## [1] 0.06236083
```

```
RESf1score <- rbind(apply(FitF1ScoreMacroAve,2,"mean"), apply(FitF1ScoreMacroAve,2,"sd"),
                    apply(TestF1ScoreMacroAve,2,"mean"), apply(TestF1ScoreMacroAve,2,"sd"))
colnames(RESf1score) = columna
rownames(RESf1score) = renglon
write.csv(RESf1score, file=paste0(archivo,"_f1score",".csv"))
```