Random Forest (RF)

Replication-based stagewise additive modeling (RSAM)

Simulation-based settings

Article: Lizbeth Naranjo, Carlos J. Perez, Daniel F. Merino (2025). A data ensemble-based approach for detecting vocal disorders using replicated acoustic biomarkers from electroglottography. *Sensing and Bio-Sensing Research Journal*, vol, num, pages.

Data

dim(datos2)

[1] 900 24

summary(datos2)

```
VЗ
                                                                ۷4
       :-2.46818
                           :-2.8869
                                              :-2.3041
                                                                 :-2.23859
Min.
                    \mathtt{Min}.
                                       Min.
                                                          Min.
1st Qu.:-0.64472
                    1st Qu.:-0.4958
                                       1st Qu.:-0.1822
                                                         1st Qu.: 0.05472
Median : 0.02661
                    Median: 0.2384
                                       Median : 0.6347
                                                          Median: 1.09540
Mean
       :-0.01209
                    Mean
                           : 0.2109
                                       Mean
                                              : 0.6358
                                                         Mean
                                                                 : 1.05924
3rd Qu.: 0.60494
                    3rd Qu.: 0.9120
                                       3rd Qu.: 1.3916
                                                          3rd Qu.: 1.98603
Max.
       : 2.62886
                    Max.
                           : 2.9954
                                       Max.
                                              : 4.0518
                                                          Max.
                                                                 : 4.75694
      V5
                                                               ٧8
                         V6
Min.
       :-2.9530
                          :-2.1113
                                             :-3.0853
                                                                :-2.236
                   Min.
                                      Min.
                                                         Min.
1st Qu.: 0.2255
                   1st Qu.: 0.6053
                                      1st Qu.: 0.9834
                                                         1st Qu.: 1.317
Median : 1.2606
                   Median : 1.8159
                                      Median : 2.4098
                                                         Median : 2.774
      : 1.4013
                   Mean
                          : 1.9805
                                             : 2.5094
                                                         Mean
                                                                : 2.689
3rd Qu.: 2.4265
                   3rd Qu.: 3.3161
                                      3rd Qu.: 3.9536
                                                         3rd Qu.: 3.962
Max.
       : 7.2912
                          : 7.2158
                                      Max.
                                             : 8.0646
                                                         Max.
                                                                : 7.362
                   Max.
      V9
                       V10
                                         V11
                                                           V12
       :-2.530
                         :-1.322
                                           :-1.068
                                                             :-0.9634
Min.
                  Min.
                                    Min.
                                                      Min.
1st Qu.: 1.402
                  1st Qu.: 1.986
                                    1st Qu.: 2.123
                                                      1st Qu.: 1.8628
Median : 2.667
                  Median : 3.055
                                    Median : 3.296
                                                      Median: 2.9238
      : 2.573
                                           : 3.388
                                                             : 2.9824
Mean
                  Mean
                         : 3.064
                                   Mean
                                                      Mean
```

```
3rd Qu.: 3.817
               3rd Qu.: 4.127 3rd Qu.: 4.546
                                             3rd Qu.: 4.0124
Max. : 7.988
               Max. : 7.115 Max. : 7.231
                                             Max. : 7.0910
     V13
                   V14
                                   V15
                                                  V16
               Min. :-2.079
Min. :-1.885
                              Min. :-2.269
                                             Min. :-2.1259
1st Qu.: 1.655
               1st Qu.: 1.313
                              1st Qu.: 1.112
                                             1st Qu.: 0.5982
Median : 3.038
               Median : 2.747 Median : 2.537
                                             Median : 1.9031
Mean : 2.805
               Mean : 2.623 Mean : 2.648
                                             Mean : 1.9893
               3rd Qu.: 3.928 3rd Qu.: 4.098
3rd Qu.: 4.087
                                             3rd Qu.: 3.3091
Max. : 6.597
               Max. : 6.704 Max. : 8.223 Max. : 7.2479
     V17
                     V18
                                     V19
                                                     V20
                                       :-3.8817
Min. :-3.18364
                Min. :-2.7850
                                 Min.
                                                Min.
                                                       :-2.7783
                1st Qu.:-0.1074 1st Qu.:-0.1600
                                                1st Qu.:-0.2862
 1st Qu.:-0.01008
Median : 1.08517
                Median: 0.8566 Median: 0.6810
                                                Median: 0.4368
Mean : 1.25594
                Mean : 0.9245 Mean : 0.6666
                                                Mean : 0.3959
3rd Qu.: 2.51669
                 3rd Qu.: 1.9699 3rd Qu.: 1.5111
                                                 3rd Qu.: 1.1143
Max. : 6.44674
                 Max. : 5.6873
                                 Max. : 4.1971
                                               Max. : 4.0928
     V21
                      ID
                                              status
                                    rep
Min. :-2.43443
                Min. : 1.00
                                Min. :1
                                         Min.
                                                : 1
1st Qu.:-0.67873
                1st Qu.: 75.75
                               1st Qu.:1
                                          1st Qu.:1
Median : 0.06097
                                Median :2 Median :2
                Median :150.50
Mean : 0.01474 Mean :150.50
                                Mean :2 Mean :2
3rd Qu.: 0.67792
                 3rd Qu.:225.25
                                3rd Qu.:3
                                           3rd Qu.:3
Max. : 3.26405
                                           Max.
                 Max.
                       :300.00
                                Max. :3
head(datos2)
        V1
                 V2
                           V3
                                    ۷4
                                              V5
                                                        ۷6
                                                                   ۷7
1 1.1541136 1.206173 -0.9686025 0.02312405 2.3165891 -0.3054029 -1.61019789
2 1.1541136 1.485269 -0.4104103 0.86041236 3.4329735 1.0900776 0.06437873
3 1.1541136 1.485269 -0.4104103 0.86041236 3.4329735 0.3691737 -1.37742906
4 \ -0.6443284 \ -1.553137 \ -1.5977095 \ 1.80509752 \ -0.4816474 \ 1.3936230 \ 2.15860994
5 -0.6443284 -1.326381 -1.1441960 2.48536784 0.4253797 2.5274069 3.51915059
8V
            V9
                     V10
                             V11
                                    V12
                                           V13
                                                       V14
1 2.0685608 2.6366958 5.544770 4.434717 4.987851 3.720234 3.668854 3.077667
2 3.4640413 3.7530802 6.102962 4.434717 4.429659 2.603849 2.273374 1.403090
3 1.3013296 0.8694646 3.219346 1.551101 2.987851 2.603849 3.715182 4.286706
4 2.1574187 3.9048461 6.289806 7.142163 6.178932 4.254271 3.944702 2.582941
5 3.2912026 4.8118732 6.743320 7.142163 5.725419 3.347244 2.810918 1.222400
6 0.9714729 1.7189003 3.650347 4.049190 4.178932 3.347244 4.357404 4.315373
       V16
                V17
                         V18
                                  V19
                                           V20
                                                     V21 ID rep status
1
2 -1.7919686 0.4728324 -0.35411707 1.305594 -1.1075336 -0.1784143 2
                                                              1
3 1.0916470 3.3564480 1.80859462 2.747402 -0.3866297 -0.1784143 3
                                                              1
4 0.2449769 2.6747610 0.70607137 1.582024 -2.1536013 -1.0602656 1
                                                              2
                                                                    1
5 -0.8888070 1.7677339 0.02580105 1.128511 -2.3803581 -1.0602656 2
                                                              2
                                                                    2
6 2.2041659 4.8607067 2.34553072 2.674997 -1.6071148 -1.0602656 3
datos2 <- as.data.frame(datos2)</pre>
datos2$ID_fact = as.factor(datos2$ID) ## categorical ID of the subject
datos2$STATUS_fact = as.factor(datos2$status) ## categorical response variable
table(datos2$STATUS_fact)
```

1 2 3

300 300 300

data set

trainc <- datos2 %>% select(-status,-ID)

Crossvalidation

Training and testing data subsets

```
## Select data: 75% training & 25% testing stratified per category
SIM = 100  ## repeat N times the cross-validation process
N = 300 ## sample size
Nfit = 225  ## sample size for training subset
Ntest = 75  ## sample size for testing subset
Ncat = 100  ## sample size per category
Ncatfit = 75 ## training per category
Ncattest = 25  ## testing per category
FIT <- matrix(0,SIM,Nfit) ## training subsets</pre>
TEST <- matrix(0,SIM,Ntest) ## testing subsets</pre>
categoria = trainc %>% filter(rep==1) %>% select(STATUS_fact)
categoria = as.numeric(categoria$STATUS_fact)
id = 1:N
set.seed(12345)
for(si in 1:SIM){
  for(j in 1:3){
    idcat = id[categoria==j] ## stratified per category j
    ran0 = sample(idcat, size=Ncatfit, replace=FALSE)
    FIT[si,(j-1)*Ncatfit+1:Ncatfit] <- sort(ran0)</pre>
    TEST[si,(j-1)*Ncattest+1:Ncattest] <- setdiff(idcat,ran0)</pre>
} }
```

Classification metrics for models predicting nominal outcomes

```
## Functions to compute classification metrics
## Ytrue = true response variable
## Ypred = predicted outcome
## cat = category
## TP = true positive
## TN = true negative
## FP = false positive
## FN = false negative
## Function to compute the precision per class=cat
fn precision class <- function(Ytrue, Ypred, cat){</pre>
  TP = sum(Ypred[Ytrue==cat]==cat)
 FP = sum(Ypred[Ytrue!=cat]==cat)
 precision = TP/(TP+FP)
 return(precision)
## Function to compute the recall per class=cat
fn_recall_class <- function(Ytrue, Ypred, cat){ ## cat==category</pre>
 TP = sum(Ypred[Ytrue==cat]==cat)
 FN = sum(Ypred[Ytrue==cat]!=cat)
 recall = TP/(TP+FN)
 return(recall)
}
## Function to compute the F1-score per class=cat
fn f1score class <- function(Ytrue, Ypred, cat) { ## cat==category</pre>
  TP = sum(Ypred[Ytrue==cat]==cat)
  FP = sum(Ypred[Ytrue!=cat]==cat)
  FN = sum(Ypred[Ytrue==cat]!=cat)
  precision = TP/(TP+FP)
  recall = TP/(TP+FN)
  f1score = 2*(precision*recall)/(precision+recall)
  return(f1score)
}
## To save classification metrics
## Fitxxx: metric for training subset. Testxxx: metric for testing subset
FitAccuracy = TestAccuracy <- array(NA, dim=c(SIM, 4)) ## Accuracy Rate
FitPrecisionClass = TestPrecisionClass <- array(NA, dim=c(SIM, 4, 3)) ## Precision per class
FitRecallClass = TestRecallClass <- array(NA,dim=c(SIM,4,3)) ## Recall per class
FitF1ScoreClass = TestF1ScoreClass <- array(NA, dim=c(SIM, 4,3)) ## F1-score per class
FitPrecisionMacroAve = TestPrecisionMacroAve <- array(NA,dim=c(SIM,4)) ## Precision Macro Average
FitRecallMacroAve = TestRecallMacroAve <- array(NA, dim=c(SIM,4)) ## Recall Macro Average
FitF1ScoreMacroAve = TestF1ScoreMacroAve <- array(NA, dim=c(SIM, 4)) ## F1-score Macro Average
```

Model estimation

```
for(sim in 1:SIM){ ## BEGIN sim
my fit = FIT[sim,] ## training subset
my_test = TEST[sim,] ## testing subset
## Training data subset
train1 <- trainc %>% filter(ID_fact%in%my_fit, rep==1) ## repetition=1
train2 <- trainc %>% filter(ID_fact%in%my_fit, rep==2) ## repetition=2
train3 <- trainc %>% filter(ID_fact%in%my_fit, rep==3) ## repetition=3
Yc = train1$STATUS_fact ## categorical response variable for training
n = length(Yc)
G = 3 # classes
## Testing data subset
test1 <- trainc %>% filter(ID_fact%in%my_test, rep==1) ## repetition=1
test2 <- trainc %>% filter(ID_fact%in%my_test, rep==2) ## repetition=2
test3 <- trainc %>% filter(ID_fact%in%my_test, rep==3) ## repetition=3
Yc.new = test1$STATUS fact ## categorical response variable for testing
n.new = length(Yc.new)
## Delete variables which are not used
train1 <- train1 %>% select(-c(rep,ID_fact,STATUS_fact))
train2 <- train2 %>% select(-c(rep,ID_fact,STATUS_fact))
train3 <- train3 %>% select(-c(rep,ID fact,STATUS fact))
test1 <- test1 %>% select(-c(rep,ID_fact,STATUS_fact))
test2 <- test2 %>% select(-c(rep,ID_fact,STATUS_fact))
test3 <- test3 %>% select(-c(rep,ID_fact,STATUS_fact))
## Algorithm RSAM
## Replication-based stagewise additive modeling
## Algo1: Initialize the observation weights $w_i=1/n$, $i=1,...,n$
wi1 = rep(1/n,n)
## Algo2: BEGIN for replication j=1 to J do:
## REPLICATION j=1:
## Algo3: Fit a classifier T(x_j,z) to the training data using weights $wi$
mod1 <- randomForest(</pre>
 x = train1,
 y = Yc,
 weights = wi1,
 ntree = 500,
 xtest = test1)
## summary(mod1)
```

```
## Predictions
pred1.vgam <- mod1$votes</pre>
pred1 <- apply(pred1.vgam,1,which.max)</pre>
## Algo4: Compute err = \sum_{i=1}^{n} I[Y != I(xj,z)] / \sum_{i=1}^{n
err1 <- (sum(wi1*(Yc!=pred1))) / sum(wi1)</pre>
 ## Algo5: Compute $alpha = log (1-err)/err +log(G-1)$
alp1 \leftarrow log((1-err1)/err1) + log(G-1)
alp1 <- ifelse(is.finite(alp1), alp1, log(G-1))</pre>
## Algo6: Set wi = wi* exp(alpha*I[Y \neq T(xj,z)])
wi2 = wi1*exp(alp1*(Yc!=pred1))
## Algo7: Re-normalize wi
wi2 = c(wi2/sum(wi2))
 ##-----
## REPLICATION j=2:
## Algo3: Fit a classifier T(x_j,z) to the training data using weights wi
mod2 <- randomForest(</pre>
      x = train2,
       y = Yc,
       weights = wi2,
       ntree = 500,
      xtest = test2)
 ## summary(mod2)
 ## Predictions
pred2.vgam <- mod2$votes</pre>
pred2 <- apply(pred2.vgam,1,which.max)</pre>
## Algo4: Compute err = \sum_{i=1}^{n} I[Y != I(xj,z)] / \sum_{i=1}^{n
err2 <- (sum(wi2*(Yc!=pred2))) / sum(wi2)</pre>
## Algo5: Compute $alpha = log (1-err)/err +log(G-1)$
alp2 \leftarrow log((1-err2)/err2) + log(G-1)
alp2 <- ifelse(is.finite(alp2), alp2, log(G-1))</pre>
## Algo6: Set wi = wi* exp(alpha*I[Y \neq T(xj,z)])
wi3 = wi2*exp(alp2*(Yc!=pred2))
## Algo7: Re-normalize wi
wi3 = c(wi3/sum(wi3))
 ##-----
## REPLICATION j=3:
## Algo3: Fit a classifier T(x_j,z) to the training data using weights $wi$
mod3 <- randomForest(</pre>
       x = train3,
       y = Yc,
       weights = wi1,
    ntree = 500,
       xtest = test3)
 ## summary(mod3)
## Predictions
pred3.vgam <- mod3$votes</pre>
for(i in 1:n){ if(is.na(pred3.vgam[i,])){
```

```
pred3.vgam[i,] = 1/3
} }
pred3 <- apply(pred3.vgam,1,which.max)</pre>
## Algo4: Compute err = \sum_{i=1}^{n} I[Y != I(xj,z)] / \sum_{i=1}^{n
err3 <- (sum(wi3*(Yc!=pred3))) / sum(wi3)</pre>
## Algo5: Compute $alpha = log (1-err)/err +log(G-1)$
alp3 \leftarrow log((1-err3)/err3) + log(G-1)
alp3 <- ifelse(is.finite(alp3), alp3, log(G-1))</pre>
## Algo6: Set wi = wi* exp(alpha*I[Y \neq T(xj,z)])
wi4 = wi3*exp(alp3*(Yc!=pred3))
## Algo7: Re-normalize wi
wi4 = c(wi4/sum(wi4))
## Algo8: End for replication j=1 to J
## Algo9: Output T*(x,z) = arg \max_G \sum_{i=1}^{n} alpha*I[T(xj,z)=G]
pred = cbind(pred1,pred2,pred3)
alpha = c(alp1,alp2,alp3)
argclase = matrix(NA,n,3)
clase = rep(NA,n)
for(i in 1:n){
     argclase[i,1] = sum(alpha*(pred[i,]==1))
     argclase[i,2] = sum(alpha*(pred[i,]==2))
     argclase[i,3] = sum(alpha*(pred[i,]==3))
     clase[i] = which(argclase[i,]==max(argclase[i,]))
}
## Predict new subjects for testing subsets
pred1.new.vgam <- mod1$test$votes</pre>
pred2.new.vgam <- mod2$test$votes</pre>
pred3.new.vgam <- mod3$test$votes</pre>
pred1.new <- apply(pred1.new.vgam,1,which.max)</pre>
pred2.new <- apply(pred2.new.vgam,1,which.max)</pre>
pred3.new <- apply(pred3.new.vgam,1,which.max)</pre>
pred.new = cbind(pred1.new,pred2.new,pred3.new)
argclase.new = matrix(NA,n.new,3)
clase.new = rep(NA,n.new)
for(i in 1:n.new){
     argclase.new[i,1] = sum(alpha*(pred.new[i,]==1))
     argclase.new[i,2] = sum(alpha*(pred.new[i,]==2))
     argclase.new[i,3] = sum(alpha*(pred.new[i,]==3))
     clase.new[i] = which(argclase.new[i,]==max(argclase.new[i,]))
## End RSAM
```

```
## Classification Metrics for models predicting nominal outcomes
## Accuracy Rate
FitAccuracy[sim,] = c(sum(Yc==pred1)/n,
                      sum(Yc==pred2)/n,
                      sum(Yc==pred3)/n,
                      sum(Yc==clase)/n)
TestAccuracy[sim,] = c(sum(Yc.new==pred1.new)/n.new,
                       sum(Yc.new==pred2.new)/n.new,
                       sum(Yc.new==pred3.new)/n.new,
                       sum(Yc.new==clase.new)/n.new)
## Precision
for(cate in 1:3){
  FitPrecisionClass[sim,1, cate] = fn_precision_class(Yc, pred1, cate)
  FitPrecisionClass[sim,2, cate] = fn_precision_class(Yc, pred2, cate)
  FitPrecisionClass[sim,3, cate] = fn_precision_class(Yc, pred3, cate)
  FitPrecisionClass[sim,4, cate] = fn_precision_class(Yc, clase, cate)
  TestPrecisionClass[sim,1, cate] = fn_precision_class(Yc.new, pred1.new, cate)
  TestPrecisionClass[sim,2, cate] = fn_precision_class(Yc.new, pred2.new, cate)
  TestPrecisionClass[sim,3, cate] = fn_precision_class(Yc.new, pred3.new, cate)
  TestPrecisionClass[sim,4, cate] = fn_precision_class(Yc.new, clase.new, cate)
}
for(rep in 1:4){
  FitPrecisionMacroAve[sim, rep] = mean(FitPrecisionClass[sim, rep,])
  TestPrecisionMacroAve[sim,rep] = mean(TestPrecisionClass[sim,rep,])
}
## Recall
for(cate in 1:3){
  FitRecallClass[sim,1, cate] = fn_recall_class(Yc, pred1, cate)
  FitRecallClass[sim,2, cate] = fn_recall_class(Yc, pred2, cate)
  FitRecallClass[sim,3, cate] = fn_recall_class(Yc, pred3, cate)
  FitRecallClass[sim,4, cate] = fn_recall_class(Yc, clase, cate)
  TestRecallClass[sim,1, cate] = fn_recall_class(Yc.new, pred1.new, cate)
  TestRecallClass[sim,2, cate] = fn_recall_class(Yc.new, pred2.new, cate)
  TestRecallClass[sim,3, cate] = fn_recall_class(Yc.new, pred3.new, cate)
  TestRecallClass[sim,4, cate] = fn_recall_class(Yc.new, clase.new, cate)
}
for(rep in 1:4){
  FitRecallMacroAve[sim, rep] = mean(FitRecallClass[sim, rep,])
  TestRecallMacroAve[sim,rep] = mean(TestRecallClass[sim,rep,])
}
## F1-Score
for(cate in 1:3){
  FitF1ScoreClass[sim,1, cate] = fn_f1score_class(Yc, pred1, cate)
  FitF1ScoreClass[sim,2, cate] = fn_f1score_class(Yc, pred2, cate)
  FitF1ScoreClass[sim,3, cate] = fn_f1score_class(Yc, pred3, cate)
  FitF1ScoreClass[sim,4, cate] = fn_f1score_class(Yc, clase, cate)
```

Results

Accuracy Rate

```
columna = c("rep1", "rep2", "rep3", "ensemble")
renglon = c("fit_mean","fit_sd","test_mean","test_sd")
summary(FitAccuracy)
##
                         ٧2
                                         VЗ
                                                         ۷4
         V1
                          :0.7600 Min.
                                         :0.7644
                                                          :0.8489
## Min.
         :0.6844
                   Min.
                                                   Min.
## 1st Qu.:0.7111
                   1st Qu.:0.7867
                                   1st Qu.:0.7911
                                                   1st Qu.:0.8756
                   Median :0.8044 Median :0.8089
                                                   Median :0.8844
## Median :0.7289
## Mean :0.7295
                   Mean :0.8031 Mean :0.8074
                                                   Mean :0.8862
## 3rd Qu.:0.7467
                   3rd Qu.:0.8178
                                   3rd Qu.:0.8222
                                                   3rd Qu.:0.8978
## Max. :0.7778
                   Max. :0.8489
                                   Max. :0.8533
                                                   Max. :0.9289
apply(FitAccuracy,2,"sd")
## [1] 0.02242026 0.02075704 0.02116973 0.01649581
summary(TestAccuracy)
##
         ۷1
                         ٧2
                                         ٧3
                                                         ٧4
## Min. :0.5867
                   Min.
                         :0.7467
                                         :0.7200
                                                   Min.
                                                         :0.8267
                                   Min.
## 1st Qu.:0.6933
                  1st Qu.:0.8000 1st Qu.:0.7967
                                                   1st Qu.:0.8800
                   Median :0.8200 Median :0.8267
                                                   Median :0.8933
## Median :0.7200
## Mean :0.7223
                   Mean
                         :0.8224
                                   Mean :0.8241
                                                   Mean :0.8976
## 3rd Qu.:0.7467
                   3rd Qu.:0.8400
                                   3rd Qu.:0.8533
                                                   3rd Qu.:0.9200
## Max. :0.8133
                   Max.
                        :0.9067
                                   Max. :0.9067
                                                   Max.
                                                          :0.9600
apply(TestAccuracy,2,"sd")
## [1] 0.04288392 0.03634873 0.04223583 0.02835592
```

apply(TestAccuracy,2,"mean"),apply(TestAccuracy,2,"sd"))

RESaccuracy <- rbind(apply(FitAccuracy,2,"mean"), apply(FitAccuracy,2,"sd"),

write.csv(RESaccuracy, file=paste0(archivo,"_accuracy",".csv"))

colnames(RESaccuracy) = columna
rownames(RESaccuracy) = renglon

Precision Macro Average

```
summary(FitPrecisionMacroAve)
##
          V1
                           V2
                                             VЗ
                                                              ۷4
##
  Min.
           :0.6847
                     Min.
                            :0.7604
                                      Min.
                                              :0.7642
                                                        Min.
                                                               :0.8529
   1st Qu.:0.7123
                     1st Qu.:0.7903
                                       1st Qu.:0.7937
                                                        1st Qu.:0.8770
   Median :0.7293
                     Median :0.8081
                                      Median :0.8098
                                                        Median :0.8873
## Mean
           :0.7301
                     Mean
                            :0.8059
                                      Mean
                                              :0.8087
                                                        Mean
                                                               :0.8886
   3rd Qu.:0.7473
                     3rd Qu.:0.8206
                                       3rd Qu.:0.8236
                                                        3rd Qu.:0.8999
## Max.
           :0.7801
                            :0.8549
                                              :0.8557
                                                               :0.9312
                     Max.
                                      Max.
                                                        Max.
apply(FitPrecisionMacroAve,2,"sd")
## [1] 0.02249900 0.02148532 0.02157773 0.01670458
summary(TestPrecisionMacroAve)
##
          V1
                           V2
                                             VЗ
                                                              ۷4
##
           :0.5837
                            :0.7463
                                              :0.7188
                                                               :0.8331
   \mathtt{Min}.
                     Min.
                                      Min.
                                                        Min.
   1st Qu.:0.6984
                     1st Qu.:0.8051
                                       1st Qu.:0.8003
                                                        1st Qu.:0.8814
  Median :0.7329
                     Median :0.8284
                                      Median :0.8309
                                                        Median :0.9030
## Mean
           :0.7280
                     Mean
                            :0.8295
                                      Mean
                                              :0.8302
                                                        Mean
                                                               :0.9021
   3rd Qu.:0.7532
                     3rd Qu.:0.8546
                                       3rd Qu.:0.8633
                                                        3rd Qu.:0.9239
##
           :0.8208
                            :0.9188
                                              :0.9130
                                                               :0.9600
  Max.
                     Max.
                                      Max.
                                                        Max.
apply(TestPrecisionMacroAve, 2, "sd")
## [1] 0.04284167 0.03682220 0.04261891 0.02796833
RESprecision <- rbind(apply(FitPrecisionMacroAve,2,"mean"), apply(FitPrecisionMacroAve,2,"sd"),
                      apply(TestPrecisionMacroAve,2,"mean"),apply(TestPrecisionMacroAve,2,"sd"))
colnames(RESprecision) = columna
rownames(RESprecision) = renglon
write.csv(RESprecision, file=paste0(archivo,"_precision",".csv"))
```

Recall Macro Average

summary(FitRecallMacroAve) ## V1 V2 VЗ ۷4 ## $\mathtt{Min}.$:0.6844 Min. :0.7600 Min. :0.7644 Min. :0.8489 1st Qu.:0.7111 1st Qu.:0.7867 1st Qu.:0.7911 1st Qu.:0.8756 Median :0.7289 Median :0.8044 Median :0.8089 Median :0.8844 ## Mean :0.7295 Mean :0.8031 Mean :0.8074 Mean :0.8862 3rd Qu.:0.7467 3rd Qu.:0.8178 3rd Qu.:0.8222 3rd Qu.:0.8978 ## Max. :0.7778 :0.8489 :0.8533 :0.9289 Max. Max. Max. apply(FitRecallMacroAve,2,"sd") ## [1] 0.02242026 0.02075704 0.02116973 0.01649581 summary(TestRecallMacroAve)

```
##
          V1
                           ٧2
                                             VЗ
                                                               ۷4
##
           :0.5867
                             :0.7467
                                              :0.7200
                                                                :0.8267
   Min.
                     Min.
                                       Min.
                                                        Min.
   1st Qu.:0.6933
                     1st Qu.:0.8000
                                       1st Qu.:0.7967
                                                        1st Qu.:0.8800
  Median :0.7200
                     Median :0.8200
                                       Median :0.8267
                                                        Median :0.8933
## Mean
           :0.7223
                     Mean
                            :0.8224
                                       Mean
                                              :0.8241
                                                        Mean
                                                                :0.8976
    3rd Qu.:0.7467
                     3rd Qu.:0.8400
                                       3rd Qu.:0.8533
                                                        3rd Qu.:0.9200
##
           :0.8133
  Max.
                     Max.
                             :0.9067
                                       Max.
                                              :0.9067
                                                        Max.
                                                                :0.9600
apply(TestRecallMacroAve, 2, "sd")
```

[1] 0.04288392 0.03634873 0.04223583 0.02835592

F1-Score Macro Average

summary(FitF1ScoreMacroAve)

```
##
          V1
                            V2
                                              VЗ
                                                                ۷4
##
   \mathtt{Min}.
           :0.6839
                      Min.
                             :0.7567
                                        Min.
                                               :0.7624
                                                          Min.
                                                                 :0.8480
   1st Qu.:0.7113
                      1st Qu.:0.7854
                                        1st Qu.:0.7898
                                                          1st Qu.:0.8752
   Median :0.7287
                      Median :0.8033
                                        Median :0.8084
                                                          Median :0.8844
## Mean
           :0.7293
                      Mean
                             :0.8017
                                        Mean
                                               :0.8068
                                                          Mean
                                                                 :0.8858
    3rd Qu.:0.7465
                      3rd Qu.:0.8165
                                        3rd Qu.:0.8221
                                                          3rd Qu.:0.8976
## Max.
           :0.7775
                             :0.8478
                                               :0.8529
                                                                 :0.9285
                      Max.
                                        Max.
                                                          Max.
apply(FitF1ScoreMacroAve,2,"sd")
```

[1] 0.02233348 0.02091019 0.02122110 0.01662957

summary(TestF1ScoreMacroAve)

```
##
          V1
                           V2
                                             VЗ
                                                               ۷4
##
           :0.5748
                             :0.7406
                                              :0.7156
                                                               :0.8252
   Min.
                     Min.
                                      Min.
                                                        Min.
   1st Qu.:0.6932
                     1st Qu.:0.7965
                                       1st Qu.:0.7934
                                                        1st Qu.:0.8788
  Median :0.7201
                     Median :0.8189
                                       Median :0.8253
                                                        Median :0.8931
## Mean
           :0.7207
                     Mean
                            :0.8210
                                       Mean
                                              :0.8225
                                                        Mean
                                                                :0.8970
   3rd Qu.:0.7474
                     3rd Qu.:0.8400
                                       3rd Qu.:0.8539
                                                        3rd Qu.:0.9197
##
           :0.8121
                             :0.9064
                                              :0.9081
  Max.
                     Max.
                                       Max.
                                                        Max.
                                                                :0.9600
apply(TestF1ScoreMacroAve,2,"sd")
```

[1] 0.04352213 0.03679869 0.04317659 0.02857064