

Classification and Regression Trees (CART)

Feature space partition ensemble model for replication (FESPAE)

Simulation-based settings

Article: Lizbeth Naranjo, Carlos J. Perez, Daniel F. Merino (2025). A data ensemble-based approach for detecting vocal disorders using replicated acoustic biomarkers from electroglottography. *Sensing and Bio-Sensing Research Journal*, vol, num, pages.

Data

```
## read data
datos2 <- read.csv(paste0(address,"data_simulated.csv"),
                  sep = ";",header=TRUE, dec=".")

archivo = "FESPAE_crossval_strata_CART_simula"  ## name of the files to save results
```

```
dim(datos2)
```

```
[1] 900 24
```

```
summary(datos2)
```

V1	V2	V3	V4
Min. : -2.46818	Min. : -2.8869	Min. : -2.3041	Min. : -2.23859
1st Qu.: -0.64472	1st Qu.: -0.4958	1st Qu.: -0.1822	1st Qu.: 0.05472
Median : 0.02661	Median : 0.2384	Median : 0.6347	Median : 1.09540
Mean : -0.01209	Mean : 0.2109	Mean : 0.6358	Mean : 1.05924
3rd Qu.: 0.60494	3rd Qu.: 0.9120	3rd Qu.: 1.3916	3rd Qu.: 1.98603
Max. : 2.62886	Max. : 2.9954	Max. : 4.0518	Max. : 4.75694

V5	V6	V7	V8
Min. : -2.9530	Min. : -2.1113	Min. : -3.0853	Min. : -2.236
1st Qu.: 0.2255	1st Qu.: 0.6053	1st Qu.: 0.9834	1st Qu.: 1.317
Median : 1.2606	Median : 1.8159	Median : 2.4098	Median : 2.774
Mean : 1.4013	Mean : 1.9805	Mean : 2.5094	Mean : 2.689
3rd Qu.: 2.4265	3rd Qu.: 3.3161	3rd Qu.: 3.9536	3rd Qu.: 3.962
Max. : 7.2912	Max. : 7.2158	Max. : 8.0646	Max. : 7.362

V9	V10	V11	V12
Min. : -2.530	Min. : -1.322	Min. : -1.068	Min. : -0.9634
1st Qu.: 1.402	1st Qu.: 1.986	1st Qu.: 2.123	1st Qu.: 1.8628
Median : 2.667	Median : 3.055	Median : 3.296	Median : 2.9238
Mean : 2.573	Mean : 3.064	Mean : 3.388	Mean : 2.9824

3rd Qu.: 3.817	3rd Qu.: 4.127	3rd Qu.: 4.546	3rd Qu.: 4.0124
Max. : 7.988	Max. : 7.115	Max. : 7.231	Max. : 7.0910
V13	V14	V15	V16
Min. :-1.885	Min. :-2.079	Min. :-2.269	Min. :-2.1259
1st Qu.: 1.655	1st Qu.: 1.313	1st Qu.: 1.112	1st Qu.: 0.5982
Median : 3.038	Median : 2.747	Median : 2.537	Median : 1.9031
Mean : 2.805	Mean : 2.623	Mean : 2.648	Mean : 1.9893
3rd Qu.: 4.087	3rd Qu.: 3.928	3rd Qu.: 4.098	3rd Qu.: 3.3091
Max. : 6.597	Max. : 6.704	Max. : 8.223	Max. : 7.2479
V17	V18	V19	V20
Min. :-3.18364	Min. :-2.7850	Min. :-3.8817	Min. :-2.7783
1st Qu.: -0.01008	1st Qu.: -0.1074	1st Qu.: -0.1600	1st Qu.: -0.2862
Median : 1.08517	Median : 0.8566	Median : 0.6810	Median : 0.4368
Mean : 1.25594	Mean : 0.9245	Mean : 0.6666	Mean : 0.3959
3rd Qu.: 2.51669	3rd Qu.: 1.9699	3rd Qu.: 1.5111	3rd Qu.: 1.1143
Max. : 6.44674	Max. : 5.6873	Max. : 4.1971	Max. : 4.0928
V21	ID	rep	status
Min. :-2.43443	Min. : 1.00	Min. :1	Min. :1
1st Qu.: -0.67873	1st Qu.: 75.75	1st Qu.:1	1st Qu.:1
Median : 0.06097	Median :150.50	Median :2	Median :2
Mean : 0.01474	Mean :150.50	Mean :2	Mean :2
3rd Qu.: 0.67792	3rd Qu.:225.25	3rd Qu.:3	3rd Qu.:3
Max. : 3.26405	Max. :300.00	Max. :3	Max. :3

```
head(datos2)
```

	V1	V2	V3	V4	V5	V6	V7		
1	1.1541136	1.206173	-0.9686025	0.02312405	2.3165891	-0.3054029	-1.61019789		
2	1.1541136	1.485269	-0.4104103	0.86041236	3.4329735	1.0900776	0.06437873		
3	1.1541136	1.485269	-0.4104103	0.86041236	3.4329735	0.3691737	-1.37742906		
4	-0.6443284	-1.553137	-1.5977095	1.80509752	-0.4816474	1.3936230	2.15860994		
5	-0.6443284	-1.326381	-1.1441960	2.48536784	0.4253797	2.5274069	3.51915059		
6	-0.6443284	-1.326381	-1.1441960	2.48536784	0.4253797	1.7541637	1.97266414		
	V8	V9	V10	V11	V12	V13	V14	V15	
1	2.0685608	2.6366958	5.544770	4.434717	4.987851	3.720234	3.668854	3.077667	
2	3.4640413	3.7530802	6.102962	4.434717	4.429659	2.603849	2.273374	1.403090	
3	1.3013296	0.8694646	3.219346	1.551101	2.987851	2.603849	3.715182	4.286706	
4	2.1574187	3.9048461	6.289806	7.142163	6.178932	4.254271	3.944702	2.582941	
5	3.2912026	4.8118732	6.743320	7.142163	5.725419	3.347244	2.810918	1.222400	
6	0.9714729	1.7189003	3.650347	4.049190	4.178932	3.347244	4.357404	4.315373	
	V16	V17	V18	V19	V20	V21	ID	rep	status
1	-0.3964881	1.5892168	0.48317124	1.863786	-0.8284375	-0.1784143	1	1	1
2	-1.7919686	0.4728324	-0.35411707	1.305594	-1.1075336	-0.1784143	2	1	2
3	1.0916470	3.3564480	1.80859462	2.747402	-0.3866297	-0.1784143	3	1	3
4	0.2449769	2.6747610	0.70607137	1.582024	-2.1536013	-1.0602656	1	2	1
5	-0.8888070	1.7677339	0.02580105	1.128511	-2.3803581	-1.0602656	2	2	2
6	2.2041659	4.8607067	2.34553072	2.674997	-1.6071148	-1.0602656	3	2	3

```
datos2 <- as.data.frame(datos2)
datos2$ID_fact = as.factor(datos2$ID)    ## categorical ID of the subject
datos2$STATUS_fact = as.factor(datos2$status)    ## categorical response variable
table(datos2$STATUS_fact)
```

```
1  2  3
```

300 300 300

```
## data set  
trainc <- datos2 %>% select(-status,-ID)
```

Crossvalidation

Subspaces

```
## Partition of subspaces
## The feature space is randomly partitioned into K subspaces with roughly equal sizes
## k = number of predictors
## K = subspaces

K0 = 3 ### sub-spaces
k = 21 ### explanatory variable
k2 = round(k/K0)
space = 1:k
subspaces = rep(list(rep(NA,k2)),K0)
set.seed(12345)
for(j in 1:(K0-1)){
  space1 = sample(space, size=k2, replace=FALSE)
  space = setdiff(space,space1)
  subspaces[[j]] = space1[order(space1)]
}
space1 = space
subspaces[[K0]] = space1[order(space1)]
# 21 features = 1x21, 3x7,
subspaces

## [[1]]
## [1]  2  6 11 14 16 18 19
##
## [[2]]
## [1]  1  8  9 10 13 20 21
##
## [[3]]
## [1]  3  4  5  7 12 15 17
```

Training and testing data subsets

```
## Select data: 75% training & 25% testing stratified per category
SIM = 100  ## repeat N times the cross-validation process
N = 300  ## sample size
Nfit = 225  ## sample size for training subset
Ntest = 75  ## sample size for testing subset
Ncat = 100  ## sample size per category
Ncatfit = 75  ## training per category
Ncattest = 25  ## testing per category
FIT <- matrix(0,SIM,Nfit)  ## training subsets
TEST <- matrix(0,SIM,Ntest)  ## testing subsets

categoria = trainc %>% filter(rep==1) %>% select(STATUS_fact)
categoria = as.numeric(categoria$STATUS_fact)
id = 1:N
set.seed(12345)
for(si in 1:SIM){
  for(j in 1:3){
    idcat = id[categoria==j]  ## stratified per category j
    ran0 = sample(idcat, size=Ncatfit, replace=FALSE)

    FIT[si,(j-1)*Ncatfit+1:Ncatfit] <- sort(ran0)
    TEST[si,(j-1)*Ncattest+1:Ncattest] <- setdiff(idcat,ran0)
  }
}
```

Classification metrics for models predicting nominal outcomes

```
## Functions to compute classification metrics
## Ytrue = true response variable
## Ypred = predicted outcome
## cat = category
## TP = true positive
## TN = true negative
## FP = false positive
## FN = false negative

## Function to compute the precision per class=cat
fn_precision_class <- function(Ytrue,Ypred,cat){
  TP = sum(Ypred[Ytrue==cat]==cat)
  FP = sum(Ypred[Ytrue!=cat]==cat)
  precision = TP/(TP+FP)
  return(precision)
}

## Function to compute the recall per class=cat
fn_recall_class <- function(Ytrue,Ypred,cat){ ## cat==category
  TP = sum(Ypred[Ytrue==cat]==cat)
  FN = sum(Ypred[Ytrue==cat]!=cat)
  recall = TP/(TP+FN)
  return(recall)
}

## Function to compute the F1-score per class=cat
fn_f1score_class <- function(Ytrue,Ypred,cat){ ## cat==category
  TP = sum(Ypred[Ytrue==cat]==cat)
  FP = sum(Ypred[Ytrue!=cat]==cat)
  FN = sum(Ypred[Ytrue==cat]!=cat)
  precision = TP/(TP+FP)
  recall = TP/(TP+FN)
  f1score = 2*(precision*recall)/(precision+recall)
  return(f1score)
}

## To save classification metrics
## Fitxxx: metric for training subset. Testxxx: metric for testing subset
FitAccuracy = TestAccuracy <- array(NA,dim=c(SIM,4)) ## Accuracy Rate
FitPrecisionClass = TestPrecisionClass <- array(NA,dim=c(SIM,4,3)) ## Precision per class
FitRecallClass = TestRecallClass <- array(NA,dim=c(SIM,4,3)) ## Recall per class
FitF1ScoreClass = TestF1ScoreClass <- array(NA,dim=c(SIM,4,3)) ## F1-score per class
FitPrecisionMacroAve = TestPrecisionMacroAve <- array(NA,dim=c(SIM,4)) ## Precision Macro Average
FitRecallMacroAve = TestRecallMacroAve <- array(NA,dim=c(SIM,4)) ## Recall Macro Average
FitF1ScoreMacroAve = TestF1ScoreMacroAve <- array(NA,dim=c(SIM,4)) ## F1-score Macro Average
```

Model estimation

```
##-----
for(sim in 1:SIM){ ### BEGIN sim
##-----

my_fit = FIT[sim,]    ## training subset
my_test = TEST[sim,]  ## testing subset

## Training data subset
train1 <- trainc %>% filter(ID_fact%in%my_fit, rep==1) ## repetition=1
train2 <- trainc %>% filter(ID_fact%in%my_fit, rep==2) ## repetition=2
train3 <- trainc %>% filter(ID_fact%in%my_fit, rep==3) ## repetition=3

Yc = train1$STATUS_fact ## categorical response variable for training
n = length(Yc)
G = 3 # classes

## Testing data subset
test1 <- trainc %>% filter(ID_fact%in%my_test, rep==1) ## repetition=1
test2 <- trainc %>% filter(ID_fact%in%my_test, rep==2) ## repetition=2
test3 <- trainc %>% filter(ID_fact%in%my_test, rep==3) ## repetition=3

Yc.new = test1$STATUS_fact ## categorical response variable for testing
n.new = length(Yc.new)

## Delete variables which are not used
train1 <- train1 %>% select(-c(rep,ID_fact))
train2 <- train2 %>% select(-c(rep,ID_fact))
train3 <- train3 %>% select(-c(rep,ID_fact))
test1 <- test1 %>% select(-c(rep,ID_fact))
test2 <- test2 %>% select(-c(rep,ID_fact))
test3 <- test3 %>% select(-c(rep,ID_fact))

##-----
## Algorithm FESPAE
## Feature space partition ensemble model for replication
##-----

## Algo1: The feature space is randomly partitioned into M subspaces, {S1,S2,...,SM}

K0 = 3 ## sub-spaces
k = 21 ## explanatory variables
k2 = round(k/K0)
space = 1:k
subspaces = rep(list(rep(NA,k2)),K0) ## Subspaces
set.seed(12345)
for(j in 1:(K0-1)){
  space1 = sample(space, size=k2, replace=FALSE)
  space = setdiff(space,space1)
  subspaces[[j]] = space1[order(space1)]
}
space1 = space
```

```

subspaces[[K0]] = space1[order(space1)]
# 21 features = 1x21, 3x7,

##-----
## Algo2: for feature subspace m = 1 to M do

pred.vgam = array(NA,dim=c(n,G,K0,3)) ## 3 repetitions
pred.new.vgam = array(NA,dim=c(n.new,G,K0,3)) ## 3 repetitions
##-----
## Algo3: for replication j = 1 to J do

## REPLICATION j=1:
for(parti1 in 1:K0){ ## partition of the subspaces
train1_par = train1[,c(subspaces[[parti1]],k+1)]
test1_par = test1[,c(subspaces[[parti1]],k+1)]

## Algo4: Fit a classifier  $T(x_j, z)$ ,  $x_j \in S_m$ , to the training data
mod1 <- rpart( STATUS_fact ~ . ,
               data = train1_par)
## summary(mod1)

## Algo5: Compute the C response probabilities  $\{\pi^{(m,j)}_{ic}\}$ , for  $i=1, \dots, n$ .
## Predictions
predict1.vgam <- predict(mod1, newdata = train1_par)
predict1.new.vgam <- predict(mod1, newdata = test1_par)

pred.vgam[, , parti1, 1] = predict1.vgam
pred.new.vgam[, , parti1, 1] = predict1.new.vgam
}

## REPLICATION j=2:
for(parti2 in 1:K0){ ## partition of the subspaces
train2_par = train2[,c(subspaces[[parti2]],k+1)]
test2_par = test2[,c(subspaces[[parti2]],k+1)]

## Algo4: Fit a classifier  $T(x_j, z)$ ,  $x_j \in S_m$ , to the training data
mod2 <- rpart( STATUS_fact ~ . ,
               data = train2_par)
## summary(mod2)

## Algo5: Compute the C response probabilities  $\{\pi^{(m,j)}_{ic}\}$ , for  $i=1, \dots, n$ .
## Predictions
predict2.vgam <- predict(mod2, newdata = train2_par)
predict2.new.vgam <- predict(mod2, newdata = test2_par)

pred.vgam[, , parti2, 2] = predict2.vgam
pred.new.vgam[, , parti2, 2] = predict2.new.vgam
}

## REPLICATION j=3:
for(parti3 in 1:K0){ ## partition of the subspaces
train3_par = train3[,c(subspaces[[parti3]],k+1)]
test3_par = test3[,c(subspaces[[parti3]],k+1)]

```



```

## Algo4: Fit a classifier  $T(x_j, z)$ ,  $x_j \in S_m$ , to the training data
mod3 <- rpart( STATUS_fact ~ . ,
              data = train3_par)
## summary(mod3)

## Algo5: Compute the  $C$  response probabilities  $\{\pi^{(m,j)}_{ic}\}$ , for  $i=1, \dots, n$ .
## Predictions
predict3.vgam <- predict(mod3, newdata = train3_par)
predict3.new.vgam <- predict(mod3, newdata = test3_par)

pred.vgam[, , parti3, 3] = predict3.vgam
pred.new.vgam[, , parti3, 3] = predict3.new.vgam
}

##-----
## Algo6: End for replication  $j = 1$  to  $J$ 
## Algo7: End for feature subspace  $m = 1$  to  $M$ 
##-----
## Algo8: Output: compute the response probabilities  $\pi_{ic} = \text{mean}(\{\pi^{(m,j)}_{ic}\})$ 

pred.ave1 = apply(pred.vgam[, , 1], c(1,2), mean)
pred.ave2 = apply(pred.vgam[, , 2], c(1,2), mean)
pred.ave3 = apply(pred.vgam[, , 3], c(1,2), mean)

pred.ave.vgam = apply(pred.vgam, c(1,2), mean)

### Predict new subjects
pred.ave.new1 = apply(pred.new.vgam[, , 1], c(1,2), mean)
pred.ave.new2 = apply(pred.new.vgam[, , 2], c(1,2), mean)
pred.ave.new3 = apply(pred.new.vgam[, , 3], c(1,2), mean)

pred.ave.new.vgam = apply(pred.new.vgam, c(1,2), mean)

##-----
## Algo8: Output: compute the response category  $T^*(x, z) = \arg \max \{\pi_{ic}\}$ 

pred.max1 <- apply(pred.ave1, 1, which.max)
pred.max2 <- apply(pred.ave2, 1, which.max)
pred.max3 <- apply(pred.ave3, 1, which.max)

pred.vgam_max <- apply(pred.ave.vgam, 1, which.max)

### Predict new subjects

pred.new.max1 <- apply(pred.ave.new1, 1, which.max)
pred.new.max2 <- apply(pred.ave.new2, 1, which.max)
pred.new.max3 <- apply(pred.ave.new3, 1, which.max)

pred.new.vgam_max <- apply(pred.ave.new.vgam, 1, which.max)

##-----
## End FESPAE
##-----

```

```

## Classification Metrics for models predicting nominal outcomes

## Accuracy Rate
FitAccuracy[sim,] = c(sum(Yc==pred.max1)/n,
                      sum(Yc==pred.max2)/n,
                      sum(Yc==pred.max3)/n,
                      sum(Yc==pred.vgam_max)/n)

TestAccuracy[sim,] = c(sum(Yc.new==pred.new.max1)/n.new,
                      sum(Yc.new==pred.new.max2)/n.new,
                      sum(Yc.new==pred.new.max3)/n.new,
                      sum(Yc.new==pred.new.vgam_max)/n.new)

## Precision
for(cate in 1:3){
  FitPrecisionClass[sim,1, cate] = fn_precision_class(Yc, pred.max1, cate)
  FitPrecisionClass[sim,2, cate] = fn_precision_class(Yc, pred.max2, cate)
  FitPrecisionClass[sim,3, cate] = fn_precision_class(Yc, pred.max3, cate)
  FitPrecisionClass[sim,4, cate] = fn_precision_class(Yc, pred.vgam_max, cate)

  TestPrecisionClass[sim,1, cate] = fn_precision_class(Yc.new, pred.new.max1, cate)
  TestPrecisionClass[sim,2, cate] = fn_precision_class(Yc.new, pred.new.max2, cate)
  TestPrecisionClass[sim,3, cate] = fn_precision_class(Yc.new, pred.new.max3, cate)
  TestPrecisionClass[sim,4, cate] = fn_precision_class(Yc.new, pred.new.vgam_max, cate)
}
for(rep in 1:4){
  FitPrecisionMacroAve[sim, rep] = mean(FitPrecisionClass[sim, rep,])
  TestPrecisionMacroAve[sim,rep] = mean(TestPrecisionClass[sim,rep,])
}

## Recall
for(cate in 1:3){
  FitRecallClass[sim,1, cate] = fn_recall_class(Yc, pred.max1, cate)
  FitRecallClass[sim,2, cate] = fn_recall_class(Yc, pred.max2, cate)
  FitRecallClass[sim,3, cate] = fn_recall_class(Yc, pred.max3, cate)
  FitRecallClass[sim,4, cate] = fn_recall_class(Yc, pred.vgam_max, cate)

  TestRecallClass[sim,1, cate] = fn_recall_class(Yc.new, pred.new.max1, cate)
  TestRecallClass[sim,2, cate] = fn_recall_class(Yc.new, pred.new.max2, cate)
  TestRecallClass[sim,3, cate] = fn_recall_class(Yc.new, pred.new.max3, cate)
  TestRecallClass[sim,4, cate] = fn_recall_class(Yc.new, pred.new.vgam_max, cate)
}
for(rep in 1:4){
  FitRecallMacroAve[sim, rep] = mean(FitRecallClass[sim, rep,])
  TestRecallMacroAve[sim,rep] = mean(TestRecallClass[sim,rep,])
}

## F1-Score
for(cate in 1:3){
  FitF1ScoreClass[sim,1, cate]= fn_f1score_class(Yc, pred.max1, cate)
  FitF1ScoreClass[sim,2, cate]= fn_f1score_class(Yc, pred.max2, cate)
  FitF1ScoreClass[sim,3, cate]= fn_f1score_class(Yc, pred.max3, cate)
  FitF1ScoreClass[sim,4, cate]= fn_f1score_class(Yc, pred.vgam_max, cate)
}

```

```

TestF1ScoreClass[sim,1, cate] = fn_f1score_class(Yc.new, pred.new.max1, cate)
TestF1ScoreClass[sim,2, cate] = fn_f1score_class(Yc.new, pred.new.max2, cate)
TestF1ScoreClass[sim,3, cate] = fn_f1score_class(Yc.new, pred.new.max3, cate)
TestF1ScoreClass[sim,4, cate] = fn_f1score_class(Yc.new, pred.new.vgam_max, cate)
}
for(rep in 1:4){
  FitF1ScoreMacroAve[sim, rep] = mean(FitF1ScoreClass[sim, rep,])
  TestF1ScoreMacroAve[sim,rep] = mean(TestF1ScoreClass[sim,rep,])
}

##-----
} ## END sim
##-----

```

Results

Accuracy Rate

```
columna = c("rep1","rep2","rep3","ensemble")
renglon = c("fit_mean","fit_sd","test_mean","test_sd")

summary(FitAccuracy)
```

##	V1	V2	V3	V4
## Min.	:0.8400	Min. :0.8756	Min. :0.8622	Min. :0.9778
## 1st Qu.:	0.8756	1st Qu.:0.9011	1st Qu.:0.8878	1st Qu.:0.9867
## Median	:0.8889	Median :0.9111	Median :0.8978	Median :0.9911
## Mean	:0.8870	Mean :0.9102	Mean :0.8995	Mean :0.9906
## 3rd Qu.:	0.8978	3rd Qu.:0.9200	3rd Qu.:0.9111	3rd Qu.:0.9956
## Max.	:0.9244	Max. :0.9422	Max. :0.9467	Max. :1.0000

```
apply(FitAccuracy,2,"sd")
```

```
## [1] 0.016869976 0.015042029 0.016423076 0.006186042
```

```
summary(TestAccuracy)
```

##	V1	V2	V3	V4
## Min.	:0.6133	Min. :0.6800	Min. :0.6800	Min. :0.8667
## 1st Qu.:	0.7033	1st Qu.:0.7600	1st Qu.:0.7600	1st Qu.:0.9200
## Median	:0.7200	Median :0.7867	Median :0.7867	Median :0.9333
## Mean	:0.7251	Mean :0.7916	Mean :0.7844	Mean :0.9292
## 3rd Qu.:	0.7600	3rd Qu.:0.8267	3rd Qu.:0.8133	3rd Qu.:0.9467
## Max.	:0.8267	Max. :0.8667	Max. :0.8800	Max. :0.9867

```
apply(TestAccuracy,2,"sd")
```

```
## [1] 0.04390705 0.04120105 0.04082450 0.02582476
```

```
RESaccuracy <- rbind(apply(FitAccuracy,2,"mean"), apply(FitAccuracy,2,"sd"),
                     apply(TestAccuracy,2,"mean"),apply(TestAccuracy,2,"sd"))
colnames(RESaccuracy) = columna
rownames(RESaccuracy) = renglon
write.csv(RESaccuracy, file=paste0(archivo,"_accuracy",".csv"))
```

Precision Macro Average

```
summary(FitPrecisionMacroAve)
```

##	V1	V2	V3	V4
## Min.	:0.8405	Min. :0.8767	Min. :0.8669	Min. :0.9778
## 1st Qu.:	0.8797	1st Qu.:0.9031	1st Qu.:0.8908	1st Qu.:0.9868
## Median	:0.8898	Median :0.9134	Median :0.9038	Median :0.9912
## Mean	:0.8890	Mean :0.9124	Mean :0.9029	Mean :0.9907
## 3rd Qu.:	0.9007	3rd Qu.:0.9213	3rd Qu.:0.9136	3rd Qu.:0.9956
## Max.	:0.9249	Max. :0.9424	Max. :0.9491	Max. :1.0000

```
apply(FitPrecisionMacroAve,2,"sd")
```

```
## [1] 0.016425429 0.014389452 0.016106290 0.006106091
```

```
summary(TestPrecisionMacroAve)
```

##	V1	V2	V3	V4
## Min.	:0.6106	Min. :0.6928	Min. :0.6921	Min. :0.8726
## 1st Qu.:	0.7092	1st Qu.:0.7644	1st Qu.:0.7635	1st Qu.:0.9196
## Median	:0.7379	Median :0.8011	Median :0.7940	Median :0.9344
## Mean	:0.7332	Mean :0.7978	Mean :0.7902	Mean :0.9319
## 3rd Qu.:	0.7665	3rd Qu.:0.8266	3rd Qu.:0.8169	3rd Qu.:0.9501
## Max.	:0.8295	Max. :0.8717	Max. :0.8878	Max. :0.9872

```
apply(TestPrecisionMacroAve,2,"sd")
```

```
## [1] 0.04429244 0.04103448 0.04124990 0.02513817
```

```
RESprecision <- rbind(apply(FitPrecisionMacroAve,2,"mean"), apply(FitPrecisionMacroAve,2,"sd"),  
                      apply(TestPrecisionMacroAve,2,"mean"), apply(TestPrecisionMacroAve,2,"sd"))  
colnames(RESprecision) = columna  
rownames(RESprecision) = renglon  
write.csv(RESprecision, file=paste0(archivo,"_precision",".csv"))
```

Recall Macro Average

```
summary(FitRecallMacroAve)
```

##	V1	V2	V3	V4
## Min.	:0.8400	Min. :0.8756	Min. :0.8622	Min. :0.9778
## 1st Qu.	:0.8756	1st Qu.:0.9011	1st Qu.:0.8878	1st Qu.:0.9867
## Median	:0.8889	Median :0.9111	Median :0.8978	Median :0.9911
## Mean	:0.8870	Mean :0.9102	Mean :0.8995	Mean :0.9906
## 3rd Qu.	:0.8978	3rd Qu.:0.9200	3rd Qu.:0.9111	3rd Qu.:0.9956
## Max.	:0.9244	Max. :0.9422	Max. :0.9467	Max. :1.0000

```
apply(FitRecallMacroAve,2,"sd")
```

```
## [1] 0.016869976 0.015042029 0.016423076 0.006186042
```

```
summary(TestRecallMacroAve)
```

##	V1	V2	V3	V4
## Min.	:0.6133	Min. :0.6800	Min. :0.6800	Min. :0.8667
## 1st Qu.	:0.7033	1st Qu.:0.7600	1st Qu.:0.7600	1st Qu.:0.9200
## Median	:0.7200	Median :0.7867	Median :0.7867	Median :0.9333
## Mean	:0.7251	Mean :0.7916	Mean :0.7844	Mean :0.9292
## 3rd Qu.	:0.7600	3rd Qu.:0.8267	3rd Qu.:0.8133	3rd Qu.:0.9467
## Max.	:0.8267	Max. :0.8667	Max. :0.8800	Max. :0.9867

```
apply(TestRecallMacroAve,2,"sd")
```

```
## [1] 0.04390705 0.04120105 0.04082450 0.02582476
```

```
RESrecall <- rbind(apply(FitRecallMacroAve,2,"mean"), apply(FitRecallMacroAve,2,"sd"),  
                  apply(TestRecallMacroAve,2,"mean"), apply(TestRecallMacroAve,2,"sd"))  
colnames(RESrecall) = columna  
rownames(RESrecall) = renglon  
write.csv(RESrecall, file=paste0(archivo,"_recall",".csv"))
```

F1-Score Macro Average

```
summary(FitF1ScoreMacroAve)
```

```
##           V1           V2           V3           V4
## Min.      :0.8388   Min.    :0.8742   Min.    :0.8608   Min.    :0.9777
## 1st Qu.:0.8756   1st Qu.:0.8999   1st Qu.:0.8868   1st Qu.:0.9867
## Median :0.8887   Median :0.9107   Median :0.8977   Median :0.9911
## Mean     :0.8869   Mean     :0.9098   Mean     :0.8990   Mean     :0.9906
## 3rd Qu.:0.8979   3rd Qu.:0.9198   3rd Qu.:0.9110   3rd Qu.:0.9956
## Max.     :0.9245   Max.     :0.9419   Max.     :0.9468   Max.     :1.0000
```

```
apply(FitF1ScoreMacroAve,2,"sd")
```

```
## [1] 0.017012734 0.015216776 0.016674836 0.006195713
```

```
summary(TestF1ScoreMacroAve)
```

```
##           V1           V2           V3           V4
## Min.      :0.6051   Min.    :0.6833   Min.    :0.6728   Min.    :0.8622
## 1st Qu.:0.7002   1st Qu.:0.7590   1st Qu.:0.7578   1st Qu.:0.9185
## Median :0.7201   Median :0.7867   Median :0.7852   Median :0.9321
## Mean     :0.7238   Mean     :0.7894   Mean     :0.7815   Mean     :0.9288
## 3rd Qu.:0.7581   3rd Qu.:0.8245   3rd Qu.:0.8098   3rd Qu.:0.9467
## Max.     :0.8266   Max.     :0.8669   Max.     :0.8778   Max.     :0.9867
```

```
apply(TestF1ScoreMacroAve,2,"sd")
```

```
## [1] 0.04454079 0.04192974 0.04223230 0.02610994
```

```
RESf1score <- rbind(apply(FitF1ScoreMacroAve,2,"mean"), apply(FitF1ScoreMacroAve,2,"sd"),
                    apply(TestF1ScoreMacroAve,2,"mean"), apply(TestF1ScoreMacroAve,2,"sd"))
colnames(RESf1score) = columna
rownames(RESf1score) = renglon
write.csv(RESf1score, file=paste0(archivo,"_f1score",".csv"))
```