Classification and Regression Trees (CART)

Replication-based stagewise additive modeling (RSAM)

EGG data-based experiments

Article: Lizbeth Naranjo, Carlos J. Perez, Daniel F. Merino (2025). A data ensemble-based approach for detecting vocal disorders using replicated acoustic biomarkers from electroglottography.
Sensing and Bio-Sensing Research Journal, vol, num, pages.

```
library(tidyverse)
library(caret)
library(rpart)
## change the address where the file will be saved
address = "~/Documents/GitHub/"
setwd("~/Documents/GitHub/")
```

EGG data-based experiments

```
## Comment or uncomment the options: EGG-a, EGG-i, EGG-u
```

```
## EGG-a
datos2 <- read.csv(paste0(address,"a_egg_saarbrucken.csv"),
                   sep = ";",header=TRUE, dec=",")

## name of the files to save results
archivo = "RSAM_crossval_strata_allvar_CART_Saarbruken_egg_a"
```

```
## EGG-i
## datos2 <- read.csv(paste0(address,"i_egg_saarbrucken.csv"),
##                    sep = ";",header=TRUE, dec=",")

## name of the files to save results
## archivo = "RSAM_crossval_strata_allvar_CART_Saarbruken_egg_i"
```

```
## EGG-u
## datos2 <- read.csv(paste0(address,"u_egg_saarbrucken.csv"),
##                    sep = ";",header=TRUE, dec=",")

## name of the files to save results
## archivo = "RSAM_crossval_strata_allvar_CART_Saarbruken_egg_u"
```

```
dim(datos2)
```

```
[1] 675  36
```

```
summary(datos2)
```

```
   ID_fact       status_fact      SEX             JITTER
 Min.   :  1.0   Min.   :0    Min.   :0.0000   Min.   :  0.11
 1st Qu.:169.5   1st Qu.:0    1st Qu.:0.0000   1st Qu.:  0.49
 Median :338.0   Median :1    Median :0.0000   Median :  5.52
 Mean   :338.0   Mean   :1    Mean   :0.4133   Mean   : 18.90
 3rd Qu.:506.5   3rd Qu.:2    3rd Qu.:1.0000   3rd Qu.: 25.89
 Max.   :675.0   Max.   :2    Max.   :1.0000   Max.   :281.41
   SHIMMER             CPP              D2              FZCF
 Min.   :0.01000   Min.   :12.26   Min.   : 2.480   Min.   :   2.00
 1st Qu.:0.03000   1st Qu.:21.08   1st Qu.: 4.130   1st Qu.:   5.00
 Median :0.04000   Median :24.60   Median : 5.100   Median :   9.00
 Mean   :0.05887   Mean   :24.26   Mean   : 5.666   Mean   :  45.86
 3rd Qu.:0.08000   3rd Qu.:27.36   3rd Qu.: 6.795   3rd Qu.:  20.00
 Max.   :0.37000   Max.   :35.94   Max.   :27.380   Max.   :5323.00
     GNE              HNR            HURST              LZ
 Min.   :0.3800   Min.   :-4.40   Min.   :0.0400   Min.   : 19.00
 1st Qu.:0.6300   1st Qu.:14.07   1st Qu.:0.4200   1st Qu.: 55.50
 Median :0.7700   Median :18.40   Median :0.6300   Median : 83.00
 Mean   :0.9037   Mean   :17.38   Mean   :0.7015   Mean   : 86.81
 3rd Qu.:1.0000   3rd Qu.:21.66   3rd Qu.:0.9100   3rd Qu.:107.00
 Max.   :4.6300   Max.   :32.35   Max.   :1.7800   Max.   :304.00
    MFCC0             MFCC1             MFCC2             MFCC3
 Min.   :-2.6200   Min.   :-23.850   Min.   :-47.190   Min.   :-49.37
 1st Qu.:-0.5700   1st Qu.:  3.300   1st Qu.:-22.285   1st Qu.:-24.59
 Median : 0.1700   Median :  9.150   Median : -9.750   Median :-15.21
 Mean   : 0.1388   Mean   :  8.767   Mean   : -9.716   Mean   :-14.79
 3rd Qu.: 0.8600   3rd Qu.: 14.980   3rd Qu.:  2.915   3rd Qu.: -4.03
 Max.   : 3.0700   Max.   : 30.920   Max.   : 23.390   Max.   : 19.56
    MFCC4             MFCC5             MFCC6             MFCC7
 Min.   :-61.070   Min.   :-67.210   Min.   :-62.600   Min.   :-39.460
 1st Qu.:-21.130   1st Qu.:-12.535   1st Qu.:-16.040   1st Qu.:-11.790
 Median : -8.770   Median : -2.020   Median : -3.600   Median : -2.960
 Mean   : -9.488   Mean   : -3.153   Mean   : -4.740   Mean   : -3.146
 3rd Qu.:  2.400   3rd Qu.:  7.065   3rd Qu.:  5.175   3rd Qu.:  4.690
 Max.   : 38.080   Max.   : 36.640   Max.   : 46.700   Max.   : 40.120
    MFCC8             MFCC9             MFCC10            MFCC11
 Min.   :-44.230   Min.   :-35.240   Min.   :-41.950   Min.   :-41.300
 1st Qu.:-14.685   1st Qu.:-12.990   1st Qu.:-12.415   1st Qu.:-11.705
 Median : -5.340   Median : -4.580   Median : -4.830   Median : -4.040
 Mean   : -5.353   Mean   : -3.993   Mean   : -4.637   Mean   : -4.130
 3rd Qu.:  2.660   3rd Qu.:  3.420   3rd Qu.:  2.760   3rd Qu.:  2.755
 Max.   : 49.090   Max.   : 49.370   Max.   : 41.220   Max.   : 36.180
    MFCC12          PERMUTATION          PPE             SHANNON
 Min.   :-36.840   Min.   :1.150   Min.   :0.1900   Min.   :11.79
 1st Qu.:-10.890   1st Qu.:1.640   1st Qu.:0.5300   1st Qu.:12.12
 Median : -3.390   Median :1.810   Median :0.5500   Median :12.16
 Mean   : -2.904   Mean   :1.827   Mean   :0.5312   Mean   :12.15
```

```
 3rd Qu.:  3.935   3rd Qu.:1.990   3rd Qu.:0.5700   3rd Qu.:12.19
 Max.   : 31.870   Max.   :2.550   Max.   :0.5700   Max.   :12.26
      ZCR          energyentropy   spectralcentroid spectralspread
 Min.   :0.01000   Min.   :2.540   Min.   :0.0600   Min.   :0.1100
 1st Qu.:0.04000   1st Qu.:3.230   1st Qu.:0.1200   1st Qu.:0.1600
 Median :0.07000   Median :3.300   Median :0.1500   Median :0.1800
 Mean   :0.07056   Mean   :3.248   Mean   :0.1545   Mean   :0.1805
 3rd Qu.:0.09000   3rd Qu.:3.310   3rd Qu.:0.1800   3rd Qu.:0.2000
 Max.   :0.23000   Max.   :3.320   Max.   :0.3200   Max.   :0.2800
 spectralentropy  spectralrolloff       RPDE             rep
 Min.   :0.0100   Min.   :0.0100   Min.   :0.1000   Min.   :1
 1st Qu.:0.1900   1st Qu.:0.0700   1st Qu.:0.2700   1st Qu.:1
 Median :0.6600   Median :0.1100   Median :0.3500   Median :2
 Mean   :0.6867   Mean   :0.1178   Mean   :0.3948   Mean   :2
 3rd Qu.:1.0700   3rd Qu.:0.1600   3rd Qu.:0.4950   3rd Qu.:3
 Max.   :1.9100   Max.   :0.4500   Max.   :0.9100   Max.   :3
```

```
head(datos2)
```

```
  ID_fact status_fact SEX JITTER SHIMMER   CPP   D2 FZCF  GNE   HNR HURST LZ
1       1           0   0   6.76    0.06 28.26 3.71   23 0.67 18.96  1.11 44
2       2           0   0   0.31    0.06 23.32 3.40   48 0.47 17.76  1.58 36
3       3           0   0   0.19    0.04 23.55 3.68   58 0.46 21.86  1.70 24
4       4           0   0   0.45    0.01 33.64 2.96   37 0.42 25.78  1.45 27
5       5           0   0   0.39    0.07 26.95 2.66   50 0.39 21.44  1.63 29
6       6           0   0   0.34    0.04 35.36 3.03   35 0.44 28.32  1.45 28
  MFCC0 MFCC1 MFCC2 MFCC3 MFCC4 MFCC5 MFCC6 MFCC7 MFCC8 MFCC9 MFCC10 MFCC11
1 -0.75 11.11 -0.88 -4.03  4.01 -0.10 -5.14 -4.07 -7.72 -9.94 -12.93 -13.10
2 -1.16 -0.60 12.22  4.06  5.84  3.35  6.71  1.68  2.86  3.01   1.88   1.35
3 -1.70  2.81 15.53  7.78  7.22  8.27  3.33  3.90  4.74  6.15   1.74   2.75
4 -1.00 11.34  5.69  1.20  1.84  8.61 -0.60  4.50  0.59  2.95  -0.09   1.14
5 -1.91 11.97  7.29  7.30  7.14  4.34  6.10  3.49  2.89  2.92   2.73   2.47
6 -1.43  6.93  3.04 11.37  1.89  1.65  3.27  5.75 -0.33  4.49  -1.93   2.00
  MFCC12 PERMUTATION  PPE SHANNON  ZCR energyentropy spectralcentroid
1 -10.64        1.94 0.40   12.18 0.02          3.30             0.12
2   2.93        2.53 0.57   12.20 0.01          3.21             0.13
3   2.26        2.41 0.53   12.16 0.01          3.26             0.12
4  -0.36        1.34 0.55   12.18 0.01          3.28             0.10
5   2.88        1.76 0.57   12.20 0.01          3.23             0.09
6  -1.05        1.38 0.55   12.05 0.01          3.29             0.13
  spectralspread spectralentropy spectralrolloff RPDE rep
1           0.19            0.16            0.04 0.50   1
2           0.23            0.07            0.02 0.57   2
3           0.21            0.06            0.02 0.43   3
4           0.18            0.07            0.03 0.41   1
5           0.16            0.03            0.01 0.47   2
6           0.20            0.09            0.03 0.28   3
```

Re-Scale explanatory variables

```
## Scale the variables
datos2 <- as.data.frame(datos2)
datos2$STATUS_fact = as.factor(as.numeric(factor(datos2$status_fact)))

table(datos2$STATUS_fact)
```

```
  1   2   3
225 225 225
```

```
datos <- transform(datos2,
sJITTER= scale(JITTER), sSHIMMER= scale(SHIMMER), sCPP= scale(CPP),
sD2= scale(D2), sFZCF= scale(FZCF), sGNE= scale(GNE),
sHNR= scale(HNR), sHURST= scale(HURST), sLZ= scale(LZ),
sMFCC0= scale(MFCC0),
sMFCC1= scale(MFCC1), sMFCC2= scale(MFCC2), sMFCC3= scale(MFCC3),
sMFCC4= scale(MFCC4), sMFCC5= scale(MFCC5), sMFCC6= scale(MFCC6),
sMFCC7= scale(MFCC7), sMFCC8= scale(MFCC8), sMFCC9= scale(MFCC9),
sMFCC10= scale(MFCC10), sMFCC11= scale(MFCC11), sMFCC12= scale(MFCC12),
sPERMUTATION= scale(PERMUTATION), sPPE= scale(PPE), sSHANNON= scale(SHANNON),
sZCR= scale(ZCR),
senergyentropy= scale(energyentropy), sspectralcentroid= scale(spectralcentroid),
sspectralspread= scale(spectralspread), sspectralentropy= scale(spectralentropy),
sspectralrolloff= scale(spectralrolloff), sRPDE= scale(RPDE))

datos$ID_fact = rep(1:225,each=3)

dim(datos)
```

```
[1] 675  69
```

```
## data set
trainc <- datos %>% select(
sJITTER, sSHIMMER, sCPP, sD2, sFZCF,
sGNE, sHNR, sHURST, sLZ, sMFCC0,
sMFCC1, sMFCC2, sMFCC3, sMFCC4, sMFCC5,
sMFCC6, sMFCC7, sMFCC8, sMFCC9, sMFCC10,
sMFCC11, sMFCC12,
sPERMUTATION, sPPE, sSHANNON, sZCR,
senergyentropy, sspectralcentroid, sspectralspread,
sspectralentropy, sspectralrolloff, sRPDE,
STATUS_fact,SEX, rep,ID_fact)
```

Crossvalidation

Training and testing data subsets

```
## Select data: 75% training & 25% testing stratified per category
SIM = 100   ## repeat N times the cross-validation process
N = 225   ## sample size
Nfit = 168   ## sample size for training subset
Ntest = 57   ## sample size for testing subset
Ncat = 75   ## sample size per category
Ncatfit = 56   ## training per category
Ncattest = 19   ## testing per category
FIT <- matrix(0,SIM,Nfit)   ## training subsets
TEST <- matrix(0,SIM,Ntest)   ## testing subsets

categoria = trainc %>% filter(rep==1) %>% select(STATUS_fact)
categoria = as.numeric(categoria$STATUS_fact)
id = 1:N
set.seed(12345)
for(si in 1:SIM){
  for(j in 1:3){
    idcat = id[categoria==j]   ## stratified per category j
    ran0 = sample(idcat, size=Ncatfit, replace=FALSE)

    FIT[si,(j-1)*Ncatfit+1:Ncatfit] <- sort(ran0)
    TEST[si,(j-1)*Ncattest+1:Ncattest] <- setdiff(idcat,ran0)
} }
```

Classification metrics for models predicting nominal outcomes

```
## Functions to compute classification metrics
## Ytrue = true response variable
## Ypred = predicted outcome
## cat = category
## TP = true positive
## TN = true negative
## FP = false positive
## FN = false negative

## Function to compute the precision per class=cat
fn_precision_class <- function(Ytrue,Ypred,cat){
  TP = sum(Ypred[Ytrue==cat]==cat)
  FP = sum(Ypred[Ytrue!=cat]==cat)
  precision = TP/(TP+FP)
  return(precision)
}

## Function to compute the recall per class=cat
fn_recall_class <- function(Ytrue,Ypred,cat){ ## cat==category
  TP = sum(Ypred[Ytrue==cat]==cat)
  FN = sum(Ypred[Ytrue==cat]!=cat)
  recall = TP/(TP+FN)
  return(recall)
}

## Function to compute the F1-score per class=cat
fn_f1score_class <- function(Ytrue,Ypred,cat){ ## cat==category
  TP = sum(Ypred[Ytrue==cat]==cat)
  FP = sum(Ypred[Ytrue!=cat]==cat)
  FN = sum(Ypred[Ytrue==cat]!=cat)
  precision = TP/(TP+FP)
  recall = TP/(TP+FN)
  f1score = 2*(precision*recall)/(precision+recall)
  return(f1score)
}

## To save classification metrics
## Fitxxx: metric for training subset. Testxxx: metric for testing subset
FitAccuracy = TestAccuracy <- array(NA,dim=c(SIM,4))  ## Accuracy Rate
FitPrecisionClass = TestPrecisionClass <- array(NA,dim=c(SIM,4,3))  ## Precision per class
FitRecallClass = TestRecallClass <- array(NA,dim=c(SIM,4,3))  ## Recall per class
FitF1ScoreClass = TestF1ScoreClass <- array(NA,dim=c(SIM,4,3))  ## F1-score per class
FitPrecisionMacroAve = TestPrecisionMacroAve <- array(NA,dim=c(SIM,4))  ## Precision Macro Average
FitRecallMacroAve = TestRecallMacroAve <- array(NA,dim=c(SIM,4))  ## Recall Macro Average
FitF1ScoreMacroAve = TestF1ScoreMacroAve <- array(NA,dim=c(SIM,4))  ## F1-score Macro Average
```

Model estimation

```
##-----------------------------------------------------
for(sim in 1:SIM){  ## BEGIN sim
##-----------------------------------------------------
my_fit = FIT[sim,]   ## training subset
my_test = TEST[sim,]   ## testing subset

## Training data subset
train1 <- trainc %>% filter(ID_fact%in%my_fit, rep==1)  ## repetition=1
train2 <- trainc %>% filter(ID_fact%in%my_fit, rep==2)  ## repetition=2
train3 <- trainc %>% filter(ID_fact%in%my_fit, rep==3)  ## repetition=3

Yc = train1$STATUS_fact  ## categorical response variable for training
n = length(Yc)
G = 3 # classes

## Testing data subset
test1 <- trainc %>% filter(ID_fact%in%my_test, rep==1)  ## repetition=1
test2 <- trainc %>% filter(ID_fact%in%my_test, rep==2)  ## repetition=2
test3 <- trainc %>% filter(ID_fact%in%my_test, rep==3)  ## repetition=3

Yc.new = test1$STATUS_fact  ## categorical response variable for testing
n.new = length(Yc.new)

## Delete variables which are not used
train1 <- train1 %>% select(-c(SEX,rep,ID_fact))
train2 <- train2 %>% select(-c(SEX,rep,ID_fact))
train3 <- train3 %>% select(-c(SEX,rep,ID_fact))
test1 <- test1 %>% select(-c(SEX,rep,ID_fact,STATUS_fact))
test2 <- test2 %>% select(-c(SEX,rep,ID_fact,STATUS_fact))
test3 <- test3 %>% select(-c(SEX,rep,ID_fact,STATUS_fact))

##-----------------------------------------------------
## Algorithm RSAM
## Replication-based stagewise additive modeling
##-----------------------------------------------------

## Algo1: Initialize the observation weights $w_i=1/n$, $i=1,...,n$
wi1 = rep(1/n,n)

## Algo2: BEGIN for replication j=1 to J do:

## REPLICATION j=1:
## Algo3: Fit a classifier $T(xj,z)$ to the training data using weights $wi$
mod1 <- rpart( STATUS_fact ~ . ,
               weights = wi1,
               data = train1)
## Predictions
pred1.vgam <- predict(mod1, newdata = train1)
pred1 <- apply(pred1.vgam,1,which.max)

## Algo4: Compute $err = \sum wi I[Y != T(xj,z)] / \sum wi$
```

```
err1 <- (sum(wi1*(Yc!=pred1))) / sum(wi1)
## Algo5: Compute $alpha = log (1-err)/err +log(G-1)$
alp1 <- log((1-err1)/err1) + log(G-1)
#alp1 <- ifelse(is.finite(alp1), alp1, log(G-1))
## Algo6: Set wi = wi* exp(alpha*I[Y \neq T(xj,z)])
wi2 = wi1*exp(alp1*(Yc!=pred1))
## Algo7: Re-normalize wi
wi2 = c(wi2/sum(wi2))

##-------------------------------------------------
## REPLICATION j=2:
## Algo3: Fit a classifier $T(xj,z)$ to the training data using weights $wi$
mod2 <- rpart( STATUS_fact ~ . ,
               weights = wi2,
               data = train2)
#summary(mod2)

### Predictions
pred2.vgam <- predict(mod2, newdata = train2)
pred2 <- apply(pred2.vgam,1,which.max)

## Algo4: Compute $err = \sum wi I[Y != T(xj,z)] / \sum wi$
err2 <- (sum(wi2*(Yc!=pred2))) / sum(wi2)
## Algo5: Compute $alpha = log (1-err)/err +log(G-1)$
alp2 <- log((1-err2)/err2) + log(G-1)
#alp2 <- ifelse(is.finite(alp2), alp2, log(G-1))
## Algo6: Set wi = wi* exp(alpha*I[Y \neq T(xj,z)])
wi3 = wi2*exp(alp2*(Yc!=pred2))
## Algo7: Re-normalize wi
wi3 = c(wi3/sum(wi3))

##-------------------------------------------------
## REPLICATION j=3:
## Algo3: Fit a classifier $T(xj,z)$ to the training data using weights $wi$
mod3 <- rpart( STATUS_fact ~ . ,
               weights = wi3,
               data = train3)
#summary(mod3)

### Predictions
pred3.vgam <- predict(mod3, newdata = train3)
pred3 <- apply(pred3.vgam,1,which.max)

## Algo4: Compute $err = \sum wi I[Y != T(xj,z)] / \sum wi$
err3 <- (sum(wi3*(Yc!=pred3))) / sum(wi3)
## Algo5: Compute $alpha = log (1-err)/err +log(G-1)$
alp3 <- log((1-err3)/err3) + log(G-1)
#alp3 <- ifelse(is.finite(alp3), alp3, log(G-1))
## Algo6: Set wi = wi* exp(alpha*I[Y \neq T(xj,z)])
wi4 = wi3*exp(alp3*(Yc!=pred3))
## Algo7: Re-normalize wi
wi4 = c(wi4/sum(wi4))
```

```
## Algo8: End for replication j=1 to J
##-------------------------------------------------

## Algo9: Output T*(x,z) = arg max_G \sum_j alpha*I[T(xj,z)=G]

pred = cbind(pred1,pred2,pred3)
alpha = c(alp1,alp2,alp3)

argclase = matrix(NA,n,3)
clase = rep(NA,n)
for(i in 1:n){
  argclase[i,1] = sum(alpha*(pred[i,]==1))
  argclase[i,2] = sum(alpha*(pred[i,]==2))
  argclase[i,3] = sum(alpha*(pred[i,]==3))
  clase[i] = which(argclase[i,]==max(argclase[i,]))
}
##-------------------------------------------------
## Predict new subjects for testing subsets

pred1.new.vgam <- predict(mod1, newdata = test1)
pred2.new.vgam <- predict(mod2, newdata = test2)
pred3.new.vgam <- predict(mod3, newdata = test3)
pred1.new <- apply(pred1.new.vgam,1,which.max)
pred2.new <- apply(pred2.new.vgam,1,which.max)
pred3.new <- apply(pred3.new.vgam,1,which.max)

pred.new = cbind(pred1.new,pred2.new,pred3.new)

argclase.new = matrix(NA,n.new,3)
clase.new = rep(NA,n.new)
for(i in 1:n.new){
  argclase.new[i,1] = sum(alpha*(pred.new[i,]==1))
  argclase.new[i,2] = sum(alpha*(pred.new[i,]==2))
  argclase.new[i,3] = sum(alpha*(pred.new[i,]==3))
  clase.new[i] = which(argclase.new[i,]==max(argclase.new[i,]))
}
##-------------------------------------------------
## End RSAM
##-------------------------------------------------
## Classification Metrics for models predicting nominal outcomes

## Accuracy Rate
FitAccuracy[sim,] = c(sum(Yc==pred1)/n,
                      sum(Yc==pred2)/n,
                      sum(Yc==pred3)/n,
                      sum(Yc==clase)/n)

TestAccuracy[sim,] = c(sum(Yc.new==pred1.new)/n.new,
                       sum(Yc.new==pred2.new)/n.new,
                       sum(Yc.new==pred3.new)/n.new,
                       sum(Yc.new==clase.new)/n.new)

## Precision
```

```
for(cate in 1:3){
  FitPrecisionClass[sim,1, cate] = fn_precision_class(Yc, pred1, cate)
  FitPrecisionClass[sim,2, cate] = fn_precision_class(Yc, pred2, cate)
  FitPrecisionClass[sim,3, cate] = fn_precision_class(Yc, pred3, cate)
  FitPrecisionClass[sim,4, cate] = fn_precision_class(Yc, clase, cate)

  TestPrecisionClass[sim,1, cate] = fn_precision_class(Yc.new, pred1.new, cate)
  TestPrecisionClass[sim,2, cate] = fn_precision_class(Yc.new, pred2.new, cate)
  TestPrecisionClass[sim,3, cate] = fn_precision_class(Yc.new, pred3.new, cate)
  TestPrecisionClass[sim,4, cate] = fn_precision_class(Yc.new, clase.new, cate)
}
for(rep in 1:4){
  FitPrecisionMacroAve[sim, rep] = mean(FitPrecisionClass[sim, rep,])
  TestPrecisionMacroAve[sim,rep] = mean(TestPrecisionClass[sim,rep,])
}

## Recall
for(cate in 1:3){
  FitRecallClass[sim,1, cate] = fn_recall_class(Yc, pred1, cate)
  FitRecallClass[sim,2, cate] = fn_recall_class(Yc, pred2, cate)
  FitRecallClass[sim,3, cate] = fn_recall_class(Yc, pred3, cate)
  FitRecallClass[sim,4, cate] = fn_recall_class(Yc, clase, cate)

  TestRecallClass[sim,1, cate] = fn_recall_class(Yc.new, pred1.new, cate)
  TestRecallClass[sim,2, cate] = fn_recall_class(Yc.new, pred2.new, cate)
  TestRecallClass[sim,3, cate] = fn_recall_class(Yc.new, pred3.new, cate)
  TestRecallClass[sim,4, cate] = fn_recall_class(Yc.new, clase.new, cate)
}
for(rep in 1:4){
  FitRecallMacroAve[sim, rep] = mean(FitRecallClass[sim, rep,])
  TestRecallMacroAve[sim,rep] = mean(TestRecallClass[sim,rep,])
}

## F1-Score
for(cate in 1:3){
  FitF1ScoreClass[sim,1, cate]= fn_f1score_class(Yc, pred1, cate)
  FitF1ScoreClass[sim,2, cate]= fn_f1score_class(Yc, pred2, cate)
  FitF1ScoreClass[sim,3, cate]= fn_f1score_class(Yc, pred3, cate)
  FitF1ScoreClass[sim,4, cate]= fn_f1score_class(Yc, clase, cate)

  TestF1ScoreClass[sim,1, cate] = fn_f1score_class(Yc.new, pred1.new, cate)
  TestF1ScoreClass[sim,2, cate] = fn_f1score_class(Yc.new, pred2.new, cate)
  TestF1ScoreClass[sim,3, cate] = fn_f1score_class(Yc.new, pred3.new, cate)
  TestF1ScoreClass[sim,4, cate] = fn_f1score_class(Yc.new, clase.new, cate)
}
for(rep in 1:4){
  FitF1ScoreMacroAve[sim, rep] = mean(FitF1ScoreClass[sim, rep,])
  TestF1ScoreMacroAve[sim,rep] = mean(TestF1ScoreClass[sim,rep,])
}
##------------------------------------------------
}## END sim
##------------------------------------------------
```

Results

Accuracy Rate

```
columna = c("rep1","rep2","rep3","ensemble")
renglon = c("fit_mean","fit_sd","test_mean","test_sd")

summary(FitAccuracy)
```

```
##        V1               V2               V3               V4
##  Min.   :0.6667   Min.   :0.6190   Min.   :0.6310   Min.   :0.8155
##  1st Qu.:0.7321   1st Qu.:0.6726   1st Qu.:0.6830   1st Qu.:0.8631
##  Median :0.7440   Median :0.6905   Median :0.7054   Median :0.8810
##  Mean   :0.7452   Mean   :0.6913   Mean   :0.7042   Mean   :0.8799
##  3rd Qu.:0.7619   3rd Qu.:0.7143   3rd Qu.:0.7262   3rd Qu.:0.8988
##  Max.   :0.8036   Max.   :0.7679   Max.   :0.8036   Max.   :0.9464
```

```
apply(FitAccuracy,2,"sd")
```

```
## [1] 0.02377944 0.03031184 0.03266285 0.02686583
```

```
summary(TestAccuracy)
```

```
##        V1               V2               V3               V4
##  Min.   :0.3684   Min.   :0.3333   Min.   :0.3158   Min.   :0.4035
##  1st Qu.:0.4561   1st Qu.:0.4561   1st Qu.:0.4386   1st Qu.:0.4912
##  Median :0.4912   Median :0.5000   Median :0.4912   Median :0.5263
##  Mean   :0.4958   Mean   :0.4912   Mean   :0.4933   Mean   :0.5339
##  3rd Qu.:0.5263   3rd Qu.:0.5439   3rd Qu.:0.5439   3rd Qu.:0.5789
##  Max.   :0.6842   Max.   :0.6316   Max.   :0.7018   Max.   :0.6842
```

```
apply(TestAccuracy,2,"sd")
```

```
## [1] 0.05998177 0.06233939 0.07775319 0.06225230
```

```
RESaccuracy <- rbind(apply(FitAccuracy,2,"mean"), apply(FitAccuracy,2,"sd"),
                     apply(TestAccuracy,2,"mean"),apply(TestAccuracy,2,"sd"))
colnames(RESaccuracy) = columna
rownames(RESaccuracy) = renglon
write.csv(RESaccuracy, file=paste0(archivo,"_accuracy",".csv"))
```

Precision Macro Average

```
summary(FitPrecisionMacroAve)
```

```
##        V1               V2               V3               V4
##  Min.   :0.6695   Min.   :0.6202   Min.   :0.6493   Min.   :0.8186
##  1st Qu.:0.7372   1st Qu.:0.6871   1st Qu.:0.6968   1st Qu.:0.8702
##  Median :0.7531   Median :0.7019   Median :0.7188   Median :0.8830
##  Mean   :0.7527   Mean   :0.7051   Mean   :0.7173   Mean   :0.8834
##  3rd Qu.:0.7718   3rd Qu.:0.7269   3rd Qu.:0.7373   3rd Qu.:0.8993
##  Max.   :0.8056   Max.   :0.7891   Max.   :0.8238   Max.   :0.9492
```

```
apply(FitPrecisionMacroAve,2,"sd")
```

```
## [1] 0.02453913 0.03095175 0.03297672 0.02585454
```

```
summary(TestPrecisionMacroAve)
```

```
##        V1               V2               V3               V4
##  Min.   :0.3497   Min.   :0.3328   Min.   :0.3075   Min.   :0.3843
##  1st Qu.:0.4620   1st Qu.:0.4512   1st Qu.:0.4493   1st Qu.:0.5044
##  Median :0.5009   Median :0.5077   Median :0.5032   Median :0.5359
##  Mean   :0.5015   Mean   :0.5001   Mean   :0.5016   Mean   :0.5408
##  3rd Qu.:0.5429   3rd Qu.:0.5517   3rd Qu.:0.5499   3rd Qu.:0.5845
##  Max.   :0.7099   Max.   :0.6496   Max.   :0.7145   Max.   :0.7063
```

```
apply(TestPrecisionMacroAve,2,"sd")
```

```
## [1] 0.06404473 0.06727812 0.08421329 0.06766443
```

```
RESprecision <- rbind(apply(FitPrecisionMacroAve,2,"mean"), apply(FitPrecisionMacroAve,2,"sd"),
                      apply(TestPrecisionMacroAve,2,"mean"),apply(TestPrecisionMacroAve,2,"sd"))
colnames(RESprecision) = columna
rownames(RESprecision) = renglon
write.csv(RESprecision, file=paste0(archivo,"_precision",".csv"))
```

Recall Macro Average

```
summary(FitRecallMacroAve)
```

```
##        V1               V2               V3               V4
##  Min.   :0.6667   Min.   :0.6190   Min.   :0.6310   Min.   :0.8155
##  1st Qu.:0.7321   1st Qu.:0.6726   1st Qu.:0.6830   1st Qu.:0.8631
##  Median :0.7440   Median :0.6905   Median :0.7054   Median :0.8810
##  Mean   :0.7452   Mean   :0.6913   Mean   :0.7042   Mean   :0.8799
##  3rd Qu.:0.7619   3rd Qu.:0.7143   3rd Qu.:0.7262   3rd Qu.:0.8988
##  Max.   :0.8036   Max.   :0.7679   Max.   :0.8036   Max.   :0.9464
```

```
apply(FitRecallMacroAve,2,"sd")
```

```
## [1] 0.02377944 0.03031184 0.03266285 0.02686583
```

```
summary(TestRecallMacroAve)
```

```
##        V1               V2               V3               V4
##  Min.   :0.3684   Min.   :0.3333   Min.   :0.3158   Min.   :0.4035
##  1st Qu.:0.4561   1st Qu.:0.4561   1st Qu.:0.4386   1st Qu.:0.4912
##  Median :0.4912   Median :0.5000   Median :0.4912   Median :0.5263
##  Mean   :0.4958   Mean   :0.4912   Mean   :0.4933   Mean   :0.5339
##  3rd Qu.:0.5263   3rd Qu.:0.5439   3rd Qu.:0.5439   3rd Qu.:0.5789
##  Max.   :0.6842   Max.   :0.6316   Max.   :0.7018   Max.   :0.6842
```

```
apply(TestRecallMacroAve,2,"sd")
```

```
## [1] 0.05998177 0.06233939 0.07775319 0.06225230
```

```
RESrecall <- rbind(apply(FitRecallMacroAve,2,"mean"), apply(FitRecallMacroAve,2,"sd"),
                   apply(TestRecallMacroAve,2,"mean"),apply(TestRecallMacroAve,2,"sd"))
colnames(RESrecall) = columna
rownames(RESrecall) = renglon
write.csv(RESrecall, file=paste0(archivo,"_recall",".csv"))
```

F1-Score Macro Average

```
summary(FitF1ScoreMacroAve)
```

```
##        V1               V2               V3               V4
##  Min.   :0.6647   Min.   :0.6174   Min.   :0.6261   Min.   :0.8154
##  1st Qu.:0.7330   1st Qu.:0.6701   1st Qu.:0.6797   1st Qu.:0.8643
##  Median :0.7449   Median :0.6876   Median :0.7010   Median :0.8809
##  Mean   :0.7444   Mean   :0.6879   Mean   :0.7020   Mean   :0.8799
##  3rd Qu.:0.7615   3rd Qu.:0.7129   3rd Qu.:0.7232   3rd Qu.:0.8984
##  Max.   :0.8029   Max.   :0.7651   Max.   :0.8026   Max.   :0.9469
```

```
apply(FitF1ScoreMacroAve,2,"sd")
```

```
## [1] 0.02399778 0.03113582 0.03333325 0.02678693
```

```
summary(TestF1ScoreMacroAve)
```

```
##        V1               V2               V3               V4
##  Min.   :0.3552   Min.   :0.3293   Min.   :0.3165   Min.   :0.3915
##  1st Qu.:0.4531   1st Qu.:0.4418   1st Qu.:0.4352   1st Qu.:0.4917
##  Median :0.4881   Median :0.4903   Median :0.4904   Median :0.5264
##  Mean   :0.4902   Mean   :0.4852   Mean   :0.4882   Mean   :0.5308
##  3rd Qu.:0.5256   3rd Qu.:0.5332   3rd Qu.:0.5347   3rd Qu.:0.5759
##  Max.   :0.6696   Max.   :0.6376   Max.   :0.7041   Max.   :0.6779
##                                    NA's   :1
```

```
apply(TestF1ScoreMacroAve,2,"sd")
```

```
## [1] 0.06066620 0.06384796         NA 0.06278466
```

```
RESf1score <- rbind(apply(FitF1ScoreMacroAve,2,"mean"), apply(FitF1ScoreMacroAve,2,"sd"),
                    apply(TestF1ScoreMacroAve,2,"mean"),apply(TestF1ScoreMacroAve,2,"sd"))
colnames(RESf1score) = columna
rownames(RESf1score) = renglon
write.csv(RESf1score, file=paste0(archivo,"_f1score",".csv"))
```