# Multinomial linear regression (MLR)

Replication-based stagewise additive modeling (RSAM)

#### Simulation-based settings

**Article:** Lizbeth Naranjo, Carlos J. Perez, Daniel F. Merino (2025). A data ensemble-based approach for detecting vocal disorders using replicated acoustic biomarkers from electroglottography. *Sensing and Bio-Sensing Research Journal*, vol, num, pages.

#### Data

dim(datos2)

[1] 900 24

#### summary(datos2)

```
VЗ
                                                                 ۷4
       :-2.46818
                           :-2.8869
                                               :-2.3041
                                                                  :-2.23859
Min.
                    \mathtt{Min}.
                                       \mathtt{Min}.
                                                          Min.
                                       1st Qu.:-0.1822
1st Qu.:-0.64472
                    1st Qu.:-0.4958
                                                          1st Qu.: 0.05472
Median : 0.02661
                    Median : 0.2384
                                       Median : 0.6347
                                                          Median: 1.09540
Mean
       :-0.01209
                    Mean
                           : 0.2109
                                       Mean
                                              : 0.6358
                                                          Mean
                                                                 : 1.05924
3rd Qu.: 0.60494
                    3rd Qu.: 0.9120
                                       3rd Qu.: 1.3916
                                                          3rd Qu.: 1.98603
Max.
       : 2.62886
                    Max.
                           : 2.9954
                                       {\tt Max.}
                                               : 4.0518
                                                          Max.
                                                                  : 4.75694
      ۷5
                                                                V8
                         V6
Min.
       :-2.9530
                           :-2.1113
                                             :-3.0853
                                                                 :-2.236
                   Min.
                                      Min.
                                                         Min.
                   1st Qu.: 0.6053
                                      1st Qu.: 0.9834
1st Qu.: 0.2255
                                                         1st Qu.: 1.317
Median : 1.2606
                   Median : 1.8159
                                      Median : 2.4098
                                                         Median : 2.774
Mean
      : 1.4013
                   Mean
                           : 1.9805
                                             : 2.5094
                                                         Mean
                                                                 : 2.689
3rd Qu.: 2.4265
                   3rd Qu.: 3.3161
                                      3rd Qu.: 3.9536
                                                         3rd Qu.: 3.962
Max.
       : 7.2912
                   Max.
                           : 7.2158
                                      Max.
                                              : 8.0646
                                                         Max.
                                                                 : 7.362
      V9
                       V10
                                         V11
                                                           V12
       :-2.530
                         :-1.322
                                           :-1.068
                                                              :-0.9634
Min.
                  Min.
                                    Min.
                                                      Min.
1st Qu.: 1.402
                  1st Qu.: 1.986
                                    1st Qu.: 2.123
                                                      1st Qu.: 1.8628
Median : 2.667
                  Median : 3.055
                                    Median : 3.296
                                                      Median: 2.9238
      : 2.573
                                           : 3.388
                                                             : 2.9824
Mean
                  Mean
                         : 3.064
                                    Mean
                                                      Mean
```

```
3rd Qu.: 3.817
               3rd Qu.: 4.127 3rd Qu.: 4.546
                                             3rd Qu.: 4.0124
Max. : 7.988
               Max. : 7.115 Max. : 7.231
                                             Max. : 7.0910
     V13
                   V14
                                   V15
                                                  V16
               Min. :-2.079
Min. :-1.885
                              Min. :-2.269
                                             Min. :-2.1259
1st Qu.: 1.655
               1st Qu.: 1.313
                              1st Qu.: 1.112
                                             1st Qu.: 0.5982
Median : 3.038
               Median : 2.747 Median : 2.537
                                             Median : 1.9031
Mean : 2.805
               Mean : 2.623 Mean : 2.648
                                             Mean : 1.9893
               3rd Qu.: 3.928 3rd Qu.: 4.098
3rd Qu.: 4.087
                                             3rd Qu.: 3.3091
Max. : 6.597
               Max. : 6.704 Max. : 8.223 Max. : 7.2479
     V17
                     V18
                                     V19
                                                     V20
                                       :-3.8817
Min. :-3.18364
                Min. :-2.7850
                                 Min.
                                                Min.
                                                       :-2.7783
                1st Qu.:-0.1074 1st Qu.:-0.1600
                                                1st Qu.:-0.2862
 1st Qu.:-0.01008
Median : 1.08517
                Median: 0.8566 Median: 0.6810
                                                Median: 0.4368
Mean : 1.25594
                Mean : 0.9245 Mean : 0.6666
                                                Mean : 0.3959
3rd Qu.: 2.51669
                 3rd Qu.: 1.9699 3rd Qu.: 1.5111
                                                 3rd Qu.: 1.1143
Max. : 6.44674
                 Max. : 5.6873
                                 Max. : 4.1971
                                               Max. : 4.0928
     V21
                      ID
                                              status
                                    rep
Min. :-2.43443
                Min. : 1.00
                                Min. :1
                                         Min.
                                                : 1
1st Qu.:-0.67873
                1st Qu.: 75.75
                               1st Qu.:1
                                          1st Qu.:1
Median : 0.06097
                                Median :2 Median :2
                Median :150.50
Mean : 0.01474 Mean :150.50
                                Mean :2 Mean :2
3rd Qu.: 0.67792
                 3rd Qu.:225.25
                                3rd Qu.:3
                                           3rd Qu.:3
Max. : 3.26405
                                           Max.
                 Max.
                       :300.00
                                Max. :3
head(datos2)
        V1
                 V2
                           V3
                                    ۷4
                                              V5
                                                        ۷6
                                                                   ۷7
1 1.1541136 1.206173 -0.9686025 0.02312405 2.3165891 -0.3054029 -1.61019789
2 1.1541136 1.485269 -0.4104103 0.86041236 3.4329735 1.0900776 0.06437873
3 1.1541136 1.485269 -0.4104103 0.86041236 3.4329735 0.3691737 -1.37742906
4 \ -0.6443284 \ -1.553137 \ -1.5977095 \ 1.80509752 \ -0.4816474 \ 1.3936230 \ 2.15860994
5 -0.6443284 -1.326381 -1.1441960 2.48536784 0.4253797 2.5274069 3.51915059
8V
            V9
                     V10
                             V11
                                    V12
                                           V13
                                                       V14
1 2.0685608 2.6366958 5.544770 4.434717 4.987851 3.720234 3.668854 3.077667
2 3.4640413 3.7530802 6.102962 4.434717 4.429659 2.603849 2.273374 1.403090
3 1.3013296 0.8694646 3.219346 1.551101 2.987851 2.603849 3.715182 4.286706
4 2.1574187 3.9048461 6.289806 7.142163 6.178932 4.254271 3.944702 2.582941
5 3.2912026 4.8118732 6.743320 7.142163 5.725419 3.347244 2.810918 1.222400
6 0.9714729 1.7189003 3.650347 4.049190 4.178932 3.347244 4.357404 4.315373
       V16
                V17
                         V18
                                  V19
                                           V20
                                                     V21 ID rep status
1
2 -1.7919686 0.4728324 -0.35411707 1.305594 -1.1075336 -0.1784143 2
                                                              1
3 1.0916470 3.3564480 1.80859462 2.747402 -0.3866297 -0.1784143 3
                                                              1
4 0.2449769 2.6747610 0.70607137 1.582024 -2.1536013 -1.0602656 1
                                                              2
                                                                    1
5 -0.8888070 1.7677339 0.02580105 1.128511 -2.3803581 -1.0602656 2
                                                              2
                                                                    2
6 2.2041659 4.8607067 2.34553072 2.674997 -1.6071148 -1.0602656 3
datos2 <- as.data.frame(datos2)</pre>
datos2$ID_fact = as.factor(datos2$ID) ## categorical ID of the subject
datos2$STATUS_fact = as.factor(datos2$status) ## categorical response variable
table(datos2$STATUS_fact)
```

1 2 3

300 300 300

## ## data set

trainc <- datos2 %>% select(-status,-ID)

## Crossvalidation

## Training and testing data subsets

```
## Select data: 75% training & 25% testing stratified per category
SIM = 100  ## repeat N times the cross-validation process
N = 300 ## sample size
Nfit = 225  ## sample size for training subset
Ntest = 75  ## sample size for testing subset
Ncat = 100  ## sample size per category
Ncatfit = 75 ## training per category
Ncattest = 25  ## testing per category
FIT <- matrix(0,SIM,Nfit) ## training subsets</pre>
TEST <- matrix(0,SIM,Ntest) ## testing subsets</pre>
categoria = trainc %>% filter(rep==1) %>% select(STATUS_fact)
categoria = as.numeric(categoria$STATUS_fact)
id = 1:N
set.seed(12345)
for(si in 1:SIM){
  for(j in 1:3){
    idcat = id[categoria==j] ## stratified per category j
    ran0 = sample(idcat, size=Ncatfit, replace=FALSE)
    FIT[si,(j-1)*Ncatfit+1:Ncatfit] <- sort(ran0)</pre>
    TEST[si,(j-1)*Ncattest+1:Ncattest] <- setdiff(idcat,ran0)</pre>
} }
```

## Classification metrics for models predicting nominal outcomes

```
## Functions to compute classification metrics
## Ytrue = true response variable
## Ypred = predicted outcome
## cat = category
## TP = true positive
## TN = true negative
## FP = false positive
## FN = false negative
## Function to compute the precision per class=cat
fn precision class <- function(Ytrue, Ypred, cat){</pre>
  TP = sum(Ypred[Ytrue==cat]==cat)
 FP = sum(Ypred[Ytrue!=cat]==cat)
 precision = TP/(TP+FP)
 return(precision)
## Function to compute the recall per class=cat
fn_recall_class <- function(Ytrue, Ypred, cat){ ## cat==category</pre>
 TP = sum(Ypred[Ytrue==cat]==cat)
 FN = sum(Ypred[Ytrue==cat]!=cat)
 recall = TP/(TP+FN)
 return(recall)
}
## Function to compute the F1-score per class=cat
fn f1score class <- function(Ytrue, Ypred, cat) { ## cat==category</pre>
  TP = sum(Ypred[Ytrue==cat]==cat)
  FP = sum(Ypred[Ytrue!=cat]==cat)
  FN = sum(Ypred[Ytrue==cat]!=cat)
  precision = TP/(TP+FP)
  recall = TP/(TP+FN)
  f1score = 2*(precision*recall)/(precision+recall)
  return(f1score)
}
## To save classification metrics
## Fitxxx: metric for training subset. Testxxx: metric for testing subset
FitAccuracy = TestAccuracy <- array(NA, dim=c(SIM, 4)) ## Accuracy Rate
FitPrecisionClass = TestPrecisionClass <- array(NA, dim=c(SIM, 4, 3)) ## Precision per class
FitRecallClass = TestRecallClass <- array(NA,dim=c(SIM,4,3)) ## Recall per class
FitF1ScoreClass = TestF1ScoreClass <- array(NA, dim=c(SIM, 4,3)) ## F1-score per class
FitPrecisionMacroAve = TestPrecisionMacroAve <- array(NA,dim=c(SIM,4)) ## Precision Macro Average
FitRecallMacroAve = TestRecallMacroAve <- array(NA, dim=c(SIM,4)) ## Recall Macro Average
FitF1ScoreMacroAve = TestF1ScoreMacroAve <- array(NA, dim=c(SIM, 4)) ## F1-score Macro Average
```

#### Model estimation

```
for(sim in 1:SIM){ ## BEGIN sim
my fit = FIT[sim,] ## training subset
my_test = TEST[sim,] ## testing subset
## Training data subset
train1 <- trainc %>% filter(ID_fact%in%my_fit, rep==1) ## repetition=1
train2 <- trainc %>% filter(ID_fact%in%my_fit, rep==2) ## repetition=2
train3 <- trainc %>% filter(ID_fact%in%my_fit, rep==3) ## repetition=3
Yc = train1$STATUS_fact ## categorical response variable for training
n = length(Yc)
G = 3 # classes
## Testing data subset
test1 <- trainc %>% filter(ID_fact%in%my_test, rep==1) ## repetition=1
test2 <- trainc %>% filter(ID_fact%in%my_test, rep==2) ## repetition=2
test3 <- trainc %>% filter(ID_fact%in%my_test, rep==3) ## repetition=3
Yc.new = test1$STATUS fact ## categorical response variable for testing
n.new = length(Yc.new)
## Delete variables which are not used
train1 <- train1 %>% select(-c(rep,ID_fact))
train2 <- train2 %>% select(-c(rep,ID_fact))
train3 <- train3 %>% select(-c(rep,ID fact))
test1 <- test1 %>% select(-c(rep,ID_fact,STATUS_fact))
test2 <- test2 %>% select(-c(rep,ID_fact,STATUS_fact))
test3 <- test3 %>% select(-c(rep,ID_fact,STATUS_fact))
##-----
## Algorithm RSAM
## Replication-based stagewise additive modeling
## Algo1: Initialize the observation weights $w_i=1/n$, $i=1,...,n$
wi1 = rep(1/n,n)
## Algo2: BEGIN for replication j=1 to J do:
## REPLICATION j=1:
## Algo3: Fit a classifier T(x_j,z) to the training data using weights $wi$
mod1 <- vglm( STATUS_fact ~ . ,</pre>
              weights = wi1,
              multinomial(refLevel=1),
              data = train1)
## Predictions
pred1.vgam <- predict(mod1, newdata = train1, "response")</pre>
pred1 <- apply(pred1.vgam,1,which.max)</pre>
```

```
## Algo4: Compute err = \sum_{i=1}^{n} I[Y != I(xj,z)] / \sum_{i=1}^{n
err1 <- (sum(wi1*(Yc!=pred1))) / sum(wi1)</pre>
## Algo5: Compute $alpha = log (1-err)/err +log(G-1)$
alp1 \leftarrow log((1-err1)/err1) + log(G-1)
alp1 <- ifelse(is.finite(alp1), alp1, log(G-1))</pre>
## Algo6: Set wi = wi* exp(alpha*I[Y \neq T(xj,z)])
wi2 = wi1*exp(alp1*(Yc!=pred1))
## Algo7: Re-normalize wi
wi2 = c(wi2/sum(wi2))
## REPLICATION j=2:
## Algo3: Fit a classifier T(x_j,z) to the training data using weights wi
mod2 <- vglm( STATUS_fact ~ . ,</pre>
                                                                   weights = wi2,
                                                                   multinomial(refLevel=1),
                                                                   data = train2)
## Predictions
pred2.vgam <- predict(mod2, newdata = train2, "response")</pre>
pred2 <- apply(pred2.vgam,1,which.max)</pre>
## Algo4: Compute err = \sum_{i=1}^{n} I[Y != I(xj,z)] / \sum_{i=1}^{n
err2 <- (sum(wi2*(Yc!=pred2))) / sum(wi2)</pre>
## Algo5: Compute \alpha = \log (1-err)/err + \log (G-1)
alp2 \leftarrow log((1-err2)/err2) + log(G-1)
alp2 <- ifelse(is.finite(alp2), alp2, log(G-1))</pre>
## Algo6: Set wi = wi* exp(alpha*I[Y \neq T(xj,z)])
wi3 = wi2*exp(alp2*(Yc!=pred2))
## Algo7: Re-normalize wi
wi3 = c(wi3/sum(wi3))
## REPLICATION j=3:
## Algo3: Fit a classifier T(x_j,z) to the training data using weights wi
mod3 <- vglm( STATUS_fact ~ . ,</pre>
                                                                    weights = wi3,
                                                                   multinomial(refLevel=1),
                                                                   data = train3)
## Predictions
pred3.vgam <- predict(mod3, newdata = train3, "response")</pre>
pred3 <- apply(pred3.vgam,1,which.max)</pre>
## Algo4: Compute err = \sum_{i=1}^{n} I[Y != I(xj,z)] / \sum_{i=1}^{n
err3 <- (sum(wi3*(Yc!=pred3))) / sum(wi3)</pre>
## Algo5: Compute $alpha = log (1-err)/err +log(G-1)$
alp3 \leftarrow log((1-err3)/err3) + log(G-1)
alp3 <- ifelse(is.finite(alp3), alp3, log(G-1))</pre>
## Algo6: Set wi = wi* exp(alpha*I[Y \neq T(xj,z)])
wi4 = wi3*exp(alp3*(Yc!=pred3))
## Algo7: Re-normalize wi
wi4 = c(wi4/sum(wi4))
## Algo8: End for replication j=1 to J
```

```
## Algo9: Output T*(x,z) = arg \max_{G} \sum_{j=1}^{max} alpha*I[T(xj,z)=G]
pred = cbind(pred1,pred2,pred3)
alpha = c(alp1,alp2,alp3)
argclase = matrix(NA,n,3)
clase = rep(NA,n)
for(i in 1:n){
  argclase[i,1] = sum(alpha*(pred[i,]==1))
  argclase[i,2] = sum(alpha*(pred[i,]==2))
  argclase[i,3] = sum(alpha*(pred[i,]==3))
  clase[i] = which(argclase[i,]==max(argclase[i,]))
## Predict new subjects for testing subsets
pred1.new.vgam <- predict(mod1, newdata = test1, "response")</pre>
pred2.new.vgam <- predict(mod2, newdata = test2, "response")</pre>
pred3.new.vgam <- predict(mod3, newdata = test3, "response")</pre>
pred1.new <- apply(pred1.new.vgam,1,which.max)</pre>
pred2.new <- apply(pred2.new.vgam,1,which.max)</pre>
pred3.new <- apply(pred3.new.vgam,1,which.max)</pre>
pred.new = cbind(pred1.new,pred2.new,pred3.new)
argclase.new = matrix(NA,n.new,3)
clase.new = rep(NA,n.new)
for(i in 1:n.new){
  argclase.new[i,1] = sum(alpha*(pred.new[i,]==1))
  argclase.new[i,2] = sum(alpha*(pred.new[i,]==2))
  argclase.new[i,3] = sum(alpha*(pred.new[i,]==3))
  clase.new[i] = which(argclase.new[i,]==max(argclase.new[i,]))
##----
## End RSAM
##-----
## Classification Metrics for models predicting nominal outcomes
## Accuracy Rate
FitAccuracy[sim,] = c(sum(Yc==pred1)/n,
                      sum(Yc==pred2)/n,
                      sum(Yc==pred3)/n,
                      sum(Yc==clase)/n)
TestAccuracy[sim,] = c(sum(Yc.new==pred1.new)/n.new,
                       sum(Yc.new==pred2.new)/n.new,
                       sum(Yc.new==pred3.new)/n.new,
                       sum(Yc.new==clase.new)/n.new)
## Precision
for(cate in 1:3){
```

```
FitPrecisionClass[sim,1, cate] = fn_precision_class(Yc, pred1, cate)
  FitPrecisionClass[sim,2, cate] = fn_precision_class(Yc, pred2, cate)
  FitPrecisionClass[sim,3, cate] = fn_precision_class(Yc, pred3, cate)
  FitPrecisionClass[sim,4, cate] = fn_precision_class(Yc, clase, cate)
  TestPrecisionClass[sim,1, cate] = fn_precision_class(Yc.new, pred1.new, cate)
  TestPrecisionClass[sim,2, cate] = fn_precision_class(Yc.new, pred2.new, cate)
  TestPrecisionClass[sim,3, cate] = fn_precision_class(Yc.new, pred3.new, cate)
  TestPrecisionClass[sim,4, cate] = fn_precision_class(Yc.new, clase.new, cate)
}
for(rep in 1:4){
 FitPrecisionMacroAve[sim, rep] = mean(FitPrecisionClass[sim, rep,])
  TestPrecisionMacroAve[sim,rep] = mean(TestPrecisionClass[sim,rep,])
## Recall
for(cate in 1:3){
  FitRecallClass[sim,1, cate] = fn_recall_class(Yc, pred1, cate)
  FitRecallClass[sim,2, cate] = fn_recall_class(Yc, pred2, cate)
  FitRecallClass[sim,3, cate] = fn_recall_class(Yc, pred3, cate)
  FitRecallClass[sim,4, cate] = fn_recall_class(Yc, clase, cate)
  TestRecallClass[sim,1, cate] = fn_recall_class(Yc.new, pred1.new, cate)
  TestRecallClass[sim,2, cate] = fn_recall_class(Yc.new, pred2.new, cate)
  TestRecallClass[sim,3, cate] = fn_recall_class(Yc.new, pred3.new, cate)
  TestRecallClass[sim,4, cate] = fn_recall_class(Yc.new, clase.new, cate)
for(rep in 1:4){
  FitRecallMacroAve[sim, rep] = mean(FitRecallClass[sim, rep,])
  TestRecallMacroAve[sim,rep] = mean(TestRecallClass[sim,rep,])
}
## F1-Score
for(cate in 1:3){
  FitF1ScoreClass[sim,1, cate] = fn_f1score_class(Yc, pred1, cate)
  FitF1ScoreClass[sim,2, cate] = fn_f1score_class(Yc, pred2, cate)
  FitF1ScoreClass[sim,3, cate] = fn_f1score_class(Yc, pred3, cate)
  FitF1ScoreClass[sim,4, cate] = fn_f1score_class(Yc, clase, cate)
  TestF1ScoreClass[sim,1, cate] = fn_f1score_class(Yc.new, pred1.new, cate)
  TestF1ScoreClass[sim,2, cate] = fn_f1score_class(Yc.new, pred2.new, cate)
  TestF1ScoreClass[sim,3, cate] = fn_f1score_class(Yc.new, pred3.new, cate)
  TestF1ScoreClass[sim,4, cate] = fn_f1score_class(Yc.new, clase.new, cate)
for(rep in 1:4){
 FitF1ScoreMacroAve[sim, rep] = mean(FitF1ScoreClass[sim, rep,])
  TestF1ScoreMacroAve[sim,rep] = mean(TestF1ScoreClass[sim,rep,])
##----
}## END sim
```

## Results

#### **Accuracy Rate**

```
columna = c("rep1", "rep2", "rep3", "ensemble")
renglon = c("fit_mean","fit_sd","test_mean","test_sd")
summary(FitAccuracy)
##
         V1
                         ٧2
                                         VЗ
                                                         ۷4
                         :0.9200 Min.
                                                          :0.9733
## Min.
         :0.8533
                                          :0.8933
                   Min.
                                                    Min.
                   1st Qu.:0.9467
## 1st Qu.:0.9011
                                   1st Qu.:0.9289
                                                    1st Qu.:1.0000
                   Median :0.9600 Median :0.9400
                                                   Median :1.0000
## Median :0.9111
## Mean :0.9146
                   Mean :0.9571 Mean :0.9408
                                                   Mean :0.9996
## 3rd Qu.:0.9289
                   3rd Qu.:0.9689
                                   3rd Qu.:0.9511
                                                    3rd Qu.:1.0000
## Max. :0.9733
                   Max. :1.0000
                                   Max. :0.9956
                                                    Max. :1.0000
apply(FitAccuracy,2,"sd")
## [1] 0.021380979 0.015257690 0.019915071 0.002730256
summary(TestAccuracy)
##
         ۷1
                         ٧2
                                         ٧3
                                                         ٧4
## Min. :0.6800
                         :0.7200 Min.
                                          :0.7333
                                                   Min.
                                                          :0.7867
                   Min.
## 1st Qu.:0.7600
                   1st Qu.:0.8000 1st Qu.:0.8000
                                                    1st Qu.:0.9033
                   Median :0.8267
## Median :0.7867
                                   Median :0.8267
                                                    Median :0.9200
## Mean :0.7845
                         :0.8293 Mean :0.8273
                                                    Mean :0.9171
                   Mean
## 3rd Qu.:0.8133
                   3rd Qu.:0.8533
                                   3rd Qu.:0.8533
                                                    3rd Qu.:0.9333
## Max. :0.8667
                   Max.
                         :0.9200
                                   Max. :0.9333
                                                    Max.
                                                          :0.9733
apply(TestAccuracy,2,"sd")
## [1] 0.04146455 0.03813850 0.04343810 0.03361257
RESaccuracy <- rbind(apply(FitAccuracy,2,"mean"), apply(FitAccuracy,2,"sd"),
                    apply(TestAccuracy,2,"mean"),apply(TestAccuracy,2,"sd"))
colnames(RESaccuracy) = columna
rownames(RESaccuracy) = renglon
write.csv(RESaccuracy, file=paste0(archivo,"_accuracy",".csv"))
```

## Precision Macro Average

```
summary(FitPrecisionMacroAve)
##
          V1
                           V2
                                            VЗ
                                                              ۷4
##
  Min.
           :0.8535
                     Min.
                            :0.9201
                                      Min.
                                             :0.8929
                                                       Min.
                                                               :0.9733
   1st Qu.:0.9012
                     1st Qu.:0.9467
                                      1st Qu.:0.9292
                                                        1st Qu.:1.0000
## Median :0.9115
                     Median :0.9600
                                      Median :0.9400
                                                        Median :1.0000
## Mean
          :0.9148
                     Mean
                            :0.9574
                                      Mean
                                             :0.9411
                                                       Mean
                                                               :0.9996
   3rd Qu.:0.9292
                     3rd Qu.:0.9688
                                      3rd Qu.:0.9514
                                                        3rd Qu.:1.0000
## Max.
           :0.9733
                            :1.0000
                                             :0.9956
                                                               :1.0000
                     Max.
                                      Max.
                                                        Max.
apply(FitPrecisionMacroAve,2,"sd")
## [1] 0.021293506 0.015219898 0.019900229 0.002729435
summary(TestPrecisionMacroAve)
##
          ۷1
                           V2
                                            VЗ
                                                              ۷4
##
           :0.6800
                            :0.7194
                                             :0.7425
                                                               :0.7867
  Min.
                     Min.
                                      Min.
                                                       Min.
   1st Qu.:0.7644
                     1st Qu.:0.8080
                                      1st Qu.:0.8047
                                                        1st Qu.:0.9050
## Median :0.7891
                     Median :0.8345
                                      Median :0.8288
                                                        Median :0.9217
## Mean
           :0.7904
                     Mean
                            :0.8341
                                      Mean
                                             :0.8322
                                                       Mean
                                                               :0.9198
   3rd Qu.:0.8195
                     3rd Qu.:0.8579
                                      3rd Qu.:0.8567
                                                        3rd Qu.:0.9387
##
           :0.8781
                                             :0.9386
## Max.
                     Max.
                            :0.9228
                                      Max.
                                                        Max.
                                                               :0.9753
apply(TestPrecisionMacroAve, 2, "sd")
## [1] 0.04194277 0.03817970 0.04273418 0.03295799
RESprecision <- rbind(apply(FitPrecisionMacroAve,2,"mean"), apply(FitPrecisionMacroAve,2,"sd"),
                      apply(TestPrecisionMacroAve,2,"mean"),apply(TestPrecisionMacroAve,2,"sd"))
colnames(RESprecision) = columna
rownames(RESprecision) = renglon
write.csv(RESprecision, file=paste0(archivo,"_precision",".csv"))
```

## Recall Macro Average

#### summary(FitRecallMacroAve) ## V1 V2 VЗ ۷4 :0.9200 ## $\mathtt{Min}.$ :0.8533 Min. Min. :0.8933 Min. :0.9733 1st Qu.:0.9011 1st Qu.:0.9467 1st Qu.:0.9289 1st Qu.:1.0000 Median :0.9111 Median :0.9600 Median :0.9400 Median :1.0000 ## Mean :0.9146 Mean :0.9571 Mean :0.9408 Mean :0.9996 3rd Qu.:0.9289 3rd Qu.:0.9689 3rd Qu.:0.9511 3rd Qu.:1.0000 ## Max. :0.9733 :1.0000 :0.9956 :1.0000 Max. Max. Max. apply(FitRecallMacroAve, 2, "sd") ## [1] 0.021380979 0.015257690 0.019915071 0.002730256 summary(TestRecallMacroAve) ## V1 V2 VЗ ۷4 ## :0.6800 :0.7200 :0.7333 :0.7867 Min. Min. Min. Min. 1st Qu.:0.7600 1st Qu.:0.8000 1st Qu.:0.8000 1st Qu.:0.9033 Median :0.7867 Median :0.8267 Median :0.8267 Median :0.9200 ## Mean :0.7845 Mean :0.8293 Mean :0.8273 Mean :0.9171

```
apply(TestRecallMacroAve,2,"sd")
```

:0.8667

3rd Qu.:0.8133

##

Max.

**##** [1] 0.04146455 0.03813850 0.04343810 0.03361257

Max.

3rd Qu.:0.8533

:0.9200

3rd Qu.:0.8533

Max.

:0.9333

3rd Qu.:0.9333

:0.9733

Max.

## F1-Score Macro Average

#### summary(FitF1ScoreMacroAve)

```
##
          V1
                           V2
                                             VЗ
                                                              ۷4
                            :0.9197
##
  Min.
           :0.8533
                     Min.
                                      Min.
                                             :0.8930
                                                        Min.
                                                               :0.9732
   1st Qu.:0.9010
                     1st Qu.:0.9466
                                       1st Qu.:0.9285
                                                        1st Qu.:1.0000
  Median :0.9111
                     Median :0.9598
                                      Median :0.9399
                                                        Median :1.0000
                            :0.9571
## Mean
           :0.9146
                     Mean
                                      Mean
                                             :0.9407
                                                        Mean
                                                               :0.9996
   3rd Qu.:0.9289
                     3rd Qu.:0.9688
                                       3rd Qu.:0.9511
                                                        3rd Qu.:1.0000
## Max.
           :0.9733
                            :1.0000
                                              :0.9956
                                                               :1.0000
                     Max.
                                      Max.
                                                        Max.
apply(FitF1ScoreMacroAve,2,"sd")
```

## [1] 0.021376139 0.015285224 0.019947772 0.002739206

#### summary(TestF1ScoreMacroAve)

```
##
          V1
                            V2
                                              VЗ
                                                                ۷4
##
           :0.6800
                             :0.7184
                                              :0.7259
                                                                 :0.7852
   \mathtt{Min}.
                     Min.
                                       Min.
                                                         Min.
   1st Qu.:0.7596
                     1st Qu.:0.8008
                                       1st Qu.:0.7992
                                                         1st Qu.:0.9019
  Median :0.7846
                     Median :0.8273
                                       Median :0.8267
                                                         Median :0.9199
## Mean
           :0.7838
                     Mean
                             :0.8288
                                       Mean
                                              :0.8267
                                                         Mean
                                                                 :0.9169
    3rd Qu.:0.8135
                     3rd Qu.:0.8528
                                       3rd Qu.:0.8530
                                                         3rd Qu.:0.9338
##
           :0.8683
  Max.
                     Max.
                             :0.9180
                                       Max.
                                               :0.9338
                                                         Max.
                                                                 :0.9736
apply(TestF1ScoreMacroAve,2,"sd")
```

#### ## [1] 0.04179340 0.03831716 0.04377716 0.03377795