

Generalized Boosted Regression Model (GBM)

Feature space partition ensemble model for replication (FESPAE)

EGG data-based experiments

Article: Lizbeth Naranjo, Carlos J. Perez, Daniel F. Merino (2025). A data ensemble-based approach for detecting vocal disorders using replicated acoustic biomarkers from electroglottography. *Sensing and Bio-Sensing Research Journal*, vol, num, pages.

```
library(tidyverse)
library(gbm)
## change the address where the file will be saved
address = "~/Documents/GitHub/"
setwd("~/Documents/GitHub/")
```

EGG data-based experiments

```
## Comment or uncomment the options: EGG-a, EGG-i, EGG-u
```

```
## EGG-a
## datos2 <- read.csv(paste0(address,"a_egg_saarbrucken.csv"),
##                    sep = ";",header=TRUE, dec=",")

## name of the files to save results
## archivo = "FESPAE_crossval_strata_allvar_GBM_Saarbrucken_egg_a"
```

```
## EGG-i
datos2 <- read.csv(paste0(address,"i_egg_saarbrucken.csv"),
                  sep = ";",header=TRUE, dec=",")

## name of the files to save results
archivo = "FESPAE_crossval_strata_allvar_GBM_Saarbrucken_egg_i"
```

```
## EGG-u
## datos2 <- read.csv(paste0(address,"u_egg_saarbrucken.csv"),
##                    sep = ";",header=TRUE, dec=",")

## name of the files to save results
## archivo = "FESPAE_crossval_strata_allvar_GBM_Saarbrucken_egg_u"
```

```
dim(datos2)
```

```
[1] 675 36
```

```
summary(datos2)
```

| ID_fact | status_fact | SEX | JITTER |
|-------------------|------------------|------------------|------------------|
| Min. : 1.0 | Min. :0 | Min. :0.0000 | Min. : 0.12 |
| 1st Qu.:169.5 | 1st Qu.:0 | 1st Qu.:0.0000 | 1st Qu.: 0.48 |
| Median :338.0 | Median :1 | Median :0.0000 | Median : 2.54 |
| Mean :338.0 | Mean :1 | Mean :0.4133 | Mean : 16.37 |
| 3rd Qu.:506.5 | 3rd Qu.:2 | 3rd Qu.:1.0000 | 3rd Qu.: 23.20 |
| Max. :675.0 | Max. :2 | Max. :1.0000 | Max. :385.73 |
| SHIMMER | CPP | D2 | FZCF |
| Min. :0.00000 | Min. :11.69 | Min. : -2.000 | Min. : 3.00 |
| 1st Qu.:0.02000 | 1st Qu.:20.48 | 1st Qu.: 4.170 | 1st Qu.: 11.00 |
| Median :0.03000 | Median :24.04 | Median : 5.160 | Median : 16.00 |
| Mean :0.04761 | Mean :23.76 | Mean : 5.487 | Mean : 42.12 |
| 3rd Qu.:0.06000 | 3rd Qu.:27.11 | 3rd Qu.: 6.300 | 3rd Qu.: 23.00 |
| Max. :0.32000 | Max. :35.21 | Max. :22.570 | Max. :5280.00 |
| GENE | HNHR | HURST | LZ |
| Min. :0.3600 | Min. : -3.47 | Min. :0.1100 | Min. : 21.00 |
| 1st Qu.:0.6500 | 1st Qu.:18.54 | 1st Qu.:0.6200 | 1st Qu.: 36.00 |
| Median :0.8300 | Median :22.73 | Median :0.8800 | Median : 48.00 |
| Mean :0.9723 | Mean :21.57 | Mean :0.9036 | Mean : 59.29 |
| 3rd Qu.:1.1500 | 3rd Qu.:25.78 | 3rd Qu.:1.1700 | 3rd Qu.: 71.00 |
| Max. :6.6900 | Max. :33.35 | Max. :1.7800 | Max. :357.00 |
| MFCC0 | MFCC1 | MFCC2 | MFCC3 |
| Min. : -2.75000 | Min. : -33.1300 | Min. : -22.68 | Min. : -51.850 |
| 1st Qu.: -0.58000 | 1st Qu.: -5.9300 | 1st Qu.: 1.59 | 1st Qu.: -4.685 |
| Median : 0.04000 | Median : -0.9000 | Median : 13.69 | Median : 9.290 |
| Mean : 0.01567 | Mean : -0.9855 | Mean : 12.40 | Mean : 8.217 |
| 3rd Qu.: 0.59500 | 3rd Qu.: 4.1400 | 3rd Qu.: 22.55 | 3rd Qu.: 25.480 |
| Max. : 2.51000 | Max. : 18.3700 | Max. : 41.77 | Max. : 56.000 |
| MFCC4 | MFCC5 | MFCC6 | MFCC7 |
| Min. : -65.180 | Min. : -51.930 | Min. : -53.77 | Min. : -49.750 |
| 1st Qu.: -29.390 | 1st Qu.: -18.895 | 1st Qu.: -23.14 | 1st Qu.: -18.130 |
| Median : -11.470 | Median : -7.340 | Median : -11.97 | Median : -7.950 |
| Mean : -11.149 | Mean : -8.123 | Mean : -12.41 | Mean : -8.902 |
| 3rd Qu.: 4.905 | 3rd Qu.: 1.370 | 3rd Qu.: -1.29 | 3rd Qu.: 1.130 |
| Max. : 46.890 | Max. : 56.520 | Max. : 21.69 | Max. : 32.570 |
| MFCC8 | MFCC9 | MFCC10 | MFCC11 |
| Min. : -49.410 | Min. : -47.060 | Min. : -40.290 | Min. : -50.030 |
| 1st Qu.: -17.460 | 1st Qu.: -14.730 | 1st Qu.: -14.505 | 1st Qu.: -12.990 |
| Median : -9.870 | Median : -7.730 | Median : -5.940 | Median : -5.050 |
| Mean : -9.593 | Mean : -6.749 | Mean : -5.744 | Mean : -4.704 |
| 3rd Qu.: -1.320 | 3rd Qu.: 1.615 | 3rd Qu.: 2.100 | 3rd Qu.: 2.535 |
| Max. : 36.430 | Max. : 38.810 | Max. : 36.160 | Max. : 34.840 |
| MFCC12 | PERMUTATION | PPE | SHANNON |
| Min. : -33.830 | Min. :1.160 | Min. :0.1800 | Min. :11.89 |
| 1st Qu.: -11.390 | 1st Qu.:1.830 | 1st Qu.:0.5300 | 1st Qu.:12.16 |
| Median : -3.830 | Median :2.090 | Median :0.5500 | Median :12.20 |
| Mean : -3.119 | Mean :2.037 | Mean :0.5308 | Mean :12.19 |

| | | | |
|-----------------|-----------------|------------------|----------------|
| 3rd Qu.: 3.700 | 3rd Qu.:2.295 | 3rd Qu.:0.5700 | 3rd Qu.:12.22 |
| Max. : 39.690 | Max. :2.580 | Max. :0.5700 | Max. :12.26 |
| ZCR | energyentropy | spectralcentroid | spectralspread |
| Min. :0.01000 | Min. :2.630 | Min. :0.0800 | Min. :0.1400 |
| 1st Qu.:0.03000 | 1st Qu.:3.280 | 1st Qu.:0.1400 | 1st Qu.:0.2000 |
| Median :0.04000 | Median :3.310 | Median :0.1700 | Median :0.2200 |
| Mean :0.04539 | Mean :3.279 | Mean :0.1767 | Mean :0.2285 |
| 3rd Qu.:0.05000 | 3rd Qu.:3.320 | 3rd Qu.:0.2000 | 3rd Qu.:0.2500 |
| Max. :0.37000 | Max. :3.320 | Max. :0.4600 | Max. :0.3300 |
| spectralentropy | spectralrolloff | RPDE | rep |
| Min. :0.0200 | Min. :0.0100 | Min. :0.0100 | Min. :1 |
| 1st Qu.:0.0900 | 1st Qu.:0.0300 | 1st Qu.:0.2100 | 1st Qu.:1 |
| Median :0.1500 | Median :0.0400 | Median :0.3000 | Median :2 |
| Mean :0.2261 | Mean :0.0608 | Mean :0.3278 | Mean :2 |
| 3rd Qu.:0.2700 | 3rd Qu.:0.0600 | 3rd Qu.:0.4100 | 3rd Qu.:3 |
| Max. :2.2500 | Max. :0.7800 | Max. :0.8700 | Max. :3 |

```
head(datos2)
```

| | ID_fact | status_fact | SEX | JITTER | SHIMMER | CPP | D2 | FZCF | GNE | HNR | HURST | LZ | |
|---|----------------|-----------------|-----------------|---------|---------|---------------|------------------|-------|-------|-------|--------|--------|----|
| 1 | 1 | | 0 | 0 | 0.39 | 0.02 | 30.04 | 3.99 | 28 | 0.54 | 26.69 | 1.30 | 32 |
| 2 | 2 | | 0 | 0 | 0.32 | 0.07 | 23.02 | 3.18 | 44 | 0.47 | 18.56 | 1.58 | 33 |
| 3 | 3 | | 0 | 0 | 0.23 | 0.03 | 24.09 | 4.15 | 47 | 0.45 | 24.38 | 1.65 | 25 |
| 4 | 4 | | 0 | 0 | 0.34 | 0.02 | 32.20 | 4.02 | 29 | 0.49 | 26.18 | 1.29 | 32 |
| 5 | 5 | | 0 | 0 | 0.36 | 0.06 | 30.19 | 2.36 | 51 | 0.38 | 22.37 | 1.64 | 32 |
| 6 | 6 | | 0 | 0 | 0.61 | 0.02 | 33.98 | 3.58 | 26 | 0.56 | 26.98 | 1.23 | 33 |
| | MFCC0 | MFCC1 | MFCC2 | MFCC3 | MFCC4 | MFCC5 | MFCC6 | MFCC7 | MFCC8 | MFCC9 | MFCC10 | MFCC11 | |
| 1 | -0.60 | 8.90 | -1.58 | 3.69 | 3.32 | 1.81 | 2.48 | 1.12 | 0.92 | -1.17 | -1.50 | -2.00 | |
| 2 | -1.31 | 0.28 | 14.18 | 5.34 | 10.28 | 5.39 | 7.45 | 3.48 | 4.48 | 3.93 | 2.47 | 1.17 | |
| 3 | -1.46 | 2.82 | 17.38 | 7.79 | 7.49 | 6.53 | 4.07 | 6.27 | 5.35 | 4.94 | 1.98 | 2.57 | |
| 4 | -0.41 | 12.20 | -2.43 | 3.14 | 3.31 | 0.78 | 0.51 | 1.39 | -0.89 | 0.35 | -0.59 | -1.45 | |
| 5 | -1.79 | 9.83 | 4.12 | 9.38 | 5.34 | 6.55 | 4.36 | 5.32 | 3.50 | 3.83 | 3.43 | 2.45 | |
| 6 | -0.89 | 8.43 | 1.50 | 1.38 | 1.09 | 1.41 | -2.23 | 1.00 | -2.76 | -2.13 | -4.75 | -3.58 | |
| | MFCC12 | PERMUTATION | PPE | SHANNON | ZCR | energyentropy | spectralcentroid | | | | | | |
| 1 | -3.62 | | 2.00 | 0.57 | 12.19 | 0.02 | 3.30 | | | | 0.12 | | |
| 2 | -0.35 | | 2.48 | 0.51 | 12.22 | 0.01 | 3.21 | | | | 0.13 | | |
| 3 | 0.56 | | 2.37 | 0.57 | 12.19 | 0.01 | 3.25 | | | | 0.11 | | |
| 4 | -0.88 | | 1.29 | 0.55 | 12.16 | 0.02 | 3.30 | | | | 0.12 | | |
| 5 | 2.25 | | 1.58 | 0.55 | 12.22 | 0.01 | 3.24 | | | | 0.10 | | |
| 6 | -5.13 | | 1.31 | 0.53 | 12.13 | 0.02 | 3.30 | | | | 0.13 | | |
| | spectralspread | spectralentropy | spectralrolloff | RPDE | rep | | | | | | | | |
| 1 | | 0.18 | | 0.11 | | 0.02 | 0.29 | 1 | | | | | |
| 2 | | 0.22 | | 0.07 | | 0.02 | 0.54 | 2 | | | | | |
| 3 | | 0.21 | | 0.02 | | 0.01 | 0.35 | 3 | | | | | |
| 4 | | 0.19 | | 0.13 | | 0.03 | 0.29 | 1 | | | | | |
| 5 | | 0.18 | | 0.04 | | 0.01 | 0.42 | 2 | | | | | |
| 6 | | 0.20 | | 0.12 | | 0.03 | 0.32 | 3 | | | | | |

Re-Scale explanatory variables

```
## Scale the variables
datos2 <- as.data.frame(datos2)
datos2$STATUS_fact = as.factor(as.numeric(factor(datos2$status_fact)))

table(datos2$STATUS_fact)
```

```
 1    2    3
225 225 225
```

```
datos <- transform(datos2,
  sJITTER= scale(JITTER), sSHIMMER= scale(SHIMMER), sCPP= scale(CPP),
  sD2= scale(D2), sFZCF= scale(FZCF), sGNE= scale(GNE),
  sHNR= scale(HNR), sHURST= scale(HURST), sLZ= scale(LZ),
  sMFCC0= scale(MFCC0),
  sMFCC1= scale(MFCC1), sMFCC2= scale(MFCC2), sMFCC3= scale(MFCC3),
  sMFCC4= scale(MFCC4), sMFCC5= scale(MFCC5), sMFCC6= scale(MFCC6),
  sMFCC7= scale(MFCC7), sMFCC8= scale(MFCC8), sMFCC9= scale(MFCC9),
  sMFCC10= scale(MFCC10), sMFCC11= scale(MFCC11), sMFCC12= scale(MFCC12),
  sPERMUTATION= scale(PERMUTATION), sPPE= scale(PPE), sSHANNON= scale(SHANNON),
  sZCR= scale(ZCR),
  senergyentropy= scale(energyentropy), sspectralcentroid= scale(spectralcentroid),
  sspectralspread= scale(spectralspread), sspectralentropy= scale(spectralentropy),
  sspectralrolloff= scale(spectralrolloff), sRPDE= scale(RPDE))

datos$ID_fact = rep(1:225,each=3)

dim(datos)
```

```
[1] 675  69
```

```
## data set
trainc <- datos %>% select(
  sJITTER, sSHIMMER, sCPP, sD2, sFZCF,
  sGNE, sHNR, sHURST, sLZ, sMFCC0,
  sMFCC1, sMFCC2, sMFCC3, sMFCC4, sMFCC5,
  sMFCC6, sMFCC7, sMFCC8, sMFCC9, sMFCC10,
  sMFCC11, sMFCC12,
  sPERMUTATION, sPPE, sSHANNON, sZCR,
  senergyentropy, sspectralcentroid, sspectralspread,
  sspectralentropy, sspectralrolloff, sRPDE,
  STATUS_fact, SEX, rep, ID_fact)
```

Crossvalidation

Subspaces

```
## Partition of subspaces
## The feature space is randomly partitioned into K subspaces with roughly equal sizes
## k = number of predictors
## K = subspaces

K0 = 4 ## sub-spaces
k = 32 ## explanatory variables
k2 = round(k/K0)
space = 1:k
subspaces = rep(list(rep(NA,k2)),K0) ## Subspaces
set.seed(12345)
for(j in 1:(K0-1)){
  space1 = sample(space, size=k2, replace=FALSE)
  space = setdiff(space,space1)
  subspaces[[j]] = space1[order(space1)]
}
space1 = space
subspaces[[K0]] = space1[order(space1)]
## 32 features = 1x32, 2x16, 4x8,
subspaces
```

```
## [[1]]
## [1] 11 14 16 19 24 26 28 29
##
## [[2]]
## [1] 2 6 7 10 12 21 30 32
##
## [[3]]
## [1] 1 4 5 9 13 15 27 31
##
## [[4]]
## [1] 3 8 17 18 20 22 23 25
```

Training and testing data subsets

```
## Select data: 75% training & 25% testing stratified per category
SIM = 100  ## repeat N times the cross-validation process
N = 225  ## sample size
Nfit = 168  ## sample size for training subset
Ntest = 57  ## sample size for testing subset
Ncat = 75  ## sample size per category
Ncatfit = 56  ## training per category
Ncattest = 19  ## testing per category
FIT <- matrix(0,SIM,Nfit)  ## training subsets
TEST <- matrix(0,SIM,Ntest)  ## testing subsets

categoria = trainc %>% filter(rep==1) %>% select(STATUS_fact)
categoria = as.numeric(categoria$STATUS_fact)
id = 1:N
set.seed(12345)
for(si in 1:SIM){
  for(j in 1:3){
    idcat = id[categoria==j]  ## stratified per category j
    ran0 = sample(idcat, size=Ncatfit, replace=FALSE)

    FIT[si,(j-1)*Ncatfit+1:Ncatfit] <- sort(ran0)
    TEST[si,(j-1)*Ncattest+1:Ncattest] <- setdiff(idcat,ran0)
  }
}
```

Classification metrics for models predicting nominal outcomes

```
## Functions to compute classification metrics
## Ytrue = true response variable
## Ypred = predicted outcome
## cat = category
## TP = true positive
## TN = true negative
## FP = false positive
## FN = false negative

## Function to compute the precision per class=cat
fn_precision_class <- function(Ytrue,Ypred,cat){
  TP = sum(Ypred[Ytrue==cat]==cat)
  FP = sum(Ypred[Ytrue!=cat]==cat)
  precision = TP/(TP+FP)
  return(precision)
}

## Function to compute the recall per class=cat
fn_recall_class <- function(Ytrue,Ypred,cat){ ## cat==category
  TP = sum(Ypred[Ytrue==cat]==cat)
  FN = sum(Ypred[Ytrue==cat]!=cat)
  recall = TP/(TP+FN)
  return(recall)
}

## Function to compute the F1-score per class=cat
fn_f1score_class <- function(Ytrue,Ypred,cat){ ## cat==category
  TP = sum(Ypred[Ytrue==cat]==cat)
  FP = sum(Ypred[Ytrue!=cat]==cat)
  FN = sum(Ypred[Ytrue==cat]!=cat)
  precision = TP/(TP+FP)
  recall = TP/(TP+FN)
  f1score = 2*(precision*recall)/(precision+recall)
  return(f1score)
}

## To save classification metrics
## Fitxxx: metric for training subset. Testxxx: metric for testing subset
FitAccuracy = TestAccuracy <- array(NA,dim=c(SIM,1)) ## Accuracy Rate
FitPrecisionClass = TestPrecisionClass <- array(NA,dim=c(SIM,1,3)) ## Precision per class
FitRecallClass = TestRecallClass <- array(NA,dim=c(SIM,1,3)) ## Recall per class
FitF1ScoreClass = TestF1ScoreClass <- array(NA,dim=c(SIM,1,3)) ## F1-score per class
FitPrecisionMacroAve = TestPrecisionMacroAve <- array(NA,dim=c(SIM,1)) ## Precision Macro Average
FitRecallMacroAve = TestRecallMacroAve <- array(NA,dim=c(SIM,1)) ## Recall Macro Average
FitF1ScoreMacroAve = TestF1ScoreMacroAve <- array(NA,dim=c(SIM,1)) ## F1-score Macro Average
```

Model estimation

```
##-----
for(sim in 1:SIM){ ### BEGIN sim
##-----

my_fit = FIT[sim,]    ## training subset
my_test = TEST[sim,]  ## testing subset

## Training data subset
train1 <- trainc %>% filter(ID_fact%in%my_fit, rep==1) ## repetition=1
train2 <- trainc %>% filter(ID_fact%in%my_fit, rep==2) ## repetition=2
train3 <- trainc %>% filter(ID_fact%in%my_fit, rep==3) ## repetition=3

Yc = train1$STATUS_fact ## categorical response variable for training
n = length(Yc)
G = 3 # classes

## Testing data subset
test1 <- trainc %>% filter(ID_fact%in%my_test, rep==1) ## repetition=1
test2 <- trainc %>% filter(ID_fact%in%my_test, rep==2) ## repetition=2
test3 <- trainc %>% filter(ID_fact%in%my_test, rep==3) ## repetition=3

Yc.new = test1$STATUS_fact ## categorical response variable for testing
n.new = length(Yc.new)

## Delete variables which are not used
train1 <- train1 %>% select(-c(rep,ID_fact))
train2 <- train2 %>% select(-c(rep,ID_fact))
train3 <- train3 %>% select(-c(rep,ID_fact))
test1 <- test1 %>% select(-c(rep,ID_fact))
test2 <- test2 %>% select(-c(rep,ID_fact))
test3 <- test3 %>% select(-c(rep,ID_fact))

##-----
## Algorithm FESPAE
## Feature space partition ensemble model for replication
##-----

## Algo1: The feature space is randomly partitioned into M subspaces, {S1,S2,...,SM}

K0 = 4 ## sub-spaces
k = 32 ## explanatory variables
k2 = round(k/K0)
space = 1:k
subspaces = rep(list(rep(NA,k2)),K0) ## Subspaces
set.seed(12345)
for(j in 1:(K0-1)){
  space1 = sample(space, size=k2, replace=FALSE)
  space = setdiff(space,space1)
  subspaces[[j]] = space1[order(space1)]
}
space1 = space
```



```

subspaces[[K0]] = space1[order(space1)]
# 32 features = 1x32, 2x16, 4x8,

##-----
## Algo2: for feature subspace m = 1 to M do

pred.vgam = array(NA,dim=c(n,G,K0,3)) ## 3 repetitions
pred.new.vgam = array(NA,dim=c(n.new,G,K0,3)) ## 3 repetitions
##-----
## Algo3: for replication j = 1 to J do

## REPLICATION j=1:
for(parti1 in 1:K0){ ## partition of the subspaces
train1_par = train1[,c(subspaces[[parti1]],k+1)]
test1_par = test1[,c(subspaces[[parti1]])]

## Algo4: Fit a classifier  $T(x_j, z)$ ,  $x_j \in S_m$ , to the training data
mod1 <- gbm(
  formula = STATUS_fact ~ . ,
  distribution = "multinomial" ,
  data = train1_par ,
  n.trees = 100 ,
  interaction.depth = 5,
  shrinkage = 0.3,
  bag.fraction = 0.5,
  train.fraction = 1.0,
  n.cores = NULL # will use all cores by default
)
## summary(mod1)

## Algo5: Compute the C response probabilities  $\{\pi^{(m,j)}_{ic}\}$ , for  $i=1, \dots, n$ .
## Predictions
predict1.vgam <- predict(mod1, newdata=train1_par, n.trees=100, "response")
predict1.new.vgam <- predict(mod1, newdata=test1_par, n.trees=100, "response")

pred.vgam[, , parti1, 1] = predict1.vgam
pred.new.vgam[, , parti1, 1] = predict1.new.vgam
}

## REPLICATION j=2:
for(parti2 in 1:K0){ ## partition of the subspaces
train2_par = train2[,c(subspaces[[parti2]],k+1)]
test2_par = test2[,c(subspaces[[parti2]])]

## Algo4: Fit a classifier  $T(x_j, z)$ ,  $x_j \in S_m$ , to the training data
mod2 <- gbm(
  formula = STATUS_fact ~ . ,
  distribution = "multinomial" ,
  data = train2_par ,
  n.trees = 100 ,
  interaction.depth = 5,
  shrinkage = 0.3,
  bag.fraction = 0.5,

```

```

train.fraction = 1.0,
n.cores = NULL # will use all cores by default
)
## summary(mod2)

## Algo5: Compute the C response probabilities  $\{\pi^{(m,j)}_{ic}\}$ , for  $i=1,\dots,n$ .
## Predictions
predict2.vgam <- predict(mod2, newdata=train2_par, n.trees=100, "response")
predict2.new.vgam <- predict(mod2, newdata=test2_par, n.trees=100, "response")

pred.vgam[, , parti2, 2] = predict2.vgam
pred.new.vgam[, , parti2, 2] = predict2.new.vgam
}

## REPLICATION j=3:
for(parti3 in 1:K0){ ## partition of the subspaces
train3_par = train3[,c(subspaces[[parti3]],k+1)]
test3_par = test3[,c(subspaces[[parti3]])]

## Algo4: Fit a classifier  $T(x_j, z)$ ,  $x_j$  in  $S_m$ , to the training data
mod3 <- gbm(
  formula = STATUS_fact ~ . ,
  distribution = "multinomial" ,
  data = train3_par ,
  n.trees = 100 ,
  interaction.depth = 5,
  shrinkage = 0.3,
  bag.fraction = 0.5,
  train.fraction = 1.0,
  n.cores = NULL # will use all cores by default
)
## summary(mod3)

## Algo5: Compute the C response probabilities  $\{\pi^{(m,j)}_{ic}\}$ , for  $i=1,\dots,n$ .
## Predictions
predict3.vgam <- predict(mod3, newdata=train3_par, n.trees=100, "response")
predict3.new.vgam <- predict(mod3, newdata=test3_par, n.trees=100, "response")

pred.vgam[, , parti3, 3] = predict3.vgam
pred.new.vgam[, , parti3, 3] = predict3.new.vgam
}

##-----
## Algo6: End for replication  $j = 1$  to  $J$ 
## Algo7: End for feature subspace  $m = 1$  to  $M$ 
##-----
## Algo8: Output: compute the response probabilities  $\pi_{ic} = \text{mean}(\{\pi^{(m,j)}_{ic}\})$ 

pred.ave.vgam = apply(pred.vgam, c(1,2), mean)

### Predict new subjects
pred.ave.new.vgam = apply(pred.new.vgam, c(1,2), mean)

##-----

```

```

## Algo8: Output: compute the response category  $T^*(x,z) = \arg \max \{\pi_{ic}\}$ 

pred.vgam_max <- apply(pred.ave.vgam, 1, which.max)

### Predict new subjects
pred.new.vgam_max <- apply(pred.ave.new.vgam, 1, which.max)

##-----
## End FESPAE
##-----
## Classification Metrics for models predicting nominal outcomes

## Accuracy Rate
FitAccuracy[sim,] = c(sum(Yc==pred.vgam_max)/n)

TestAccuracy[sim,] = c(sum(Yc.new==pred.new.vgam_max)/n.new)

## Precision
for(cate in 1:3){
  FitPrecisionClass[sim,1, cate] = fn_precision_class(Yc, pred.vgam_max, cate)
  TestPrecisionClass[sim,1, cate] = fn_precision_class(Yc.new, pred.new.vgam_max, cate)
}
FitPrecisionMacroAve[sim, 1] = mean(FitPrecisionClass[sim, 1,])
TestPrecisionMacroAve[sim,1] = mean(TestPrecisionClass[sim,1,])

## Recall
for(cate in 1:3){
  FitRecallClass[sim,1, cate] = fn_recall_class(Yc, pred.vgam_max, cate)
  TestRecallClass[sim,1, cate] = fn_recall_class(Yc.new, pred.new.vgam_max, cate)
}
FitRecallMacroAve[sim, 1] = mean(FitRecallClass[sim, 1,])
TestRecallMacroAve[sim,1] = mean(TestRecallClass[sim,1,])

## F1-Score
for(cate in 1:3){
  FitF1ScoreClass[sim,1, cate]= fn_f1score_class(Yc, pred.vgam_max, cate)
  TestF1ScoreClass[sim,1, cate] = fn_f1score_class(Yc.new, pred.new.vgam_max, cate)
}
FitF1ScoreMacroAve[sim, 1] = mean(FitF1ScoreClass[sim, 1,])
TestF1ScoreMacroAve[sim,1] = mean(TestF1ScoreClass[sim,1,])

##-----
} ## END sim
##-----

```

Results

Accuracy Rate

```
columna = c("ensemble")
renglon = c("fit_mean", "fit_sd", "test_mean", "test_sd")

summary(FitAccuracy)
```

```
##           V1
##  Min.      :1
## 1st Qu.:1
##  Median :1
##   Mean   :1
## 3rd Qu.:1
##   Max.   :1
```

```
apply(FitAccuracy, 2, "sd", na.rm=TRUE)
```

```
## [1] 0
```

```
summary(TestAccuracy)
```

```
##           V1
##  Min.      :0.5088
## 1st Qu.:0.5965
##  Median :0.6316
##   Mean   :0.6333
## 3rd Qu.:0.6667
##   Max.   :0.7544
```

```
apply(TestAccuracy, 2, "sd", na.rm=TRUE)
```

```
## [1] 0.05494361
```

```
RESaccuracy <- rbind(apply(FitAccuracy, 2, "mean", na.rm=TRUE),
                        apply(FitAccuracy, 2, "sd", na.rm=TRUE),
                        apply(TestAccuracy, 2, "mean", na.rm=TRUE),
                        apply(TestAccuracy, 2, "sd", na.rm=TRUE))
colnames(RESaccuracy) = columna
rownames(RESaccuracy) = renglon
write.csv(RESaccuracy, file=paste0(archivo, "_accuracy", ".csv"))
```

Precision Macro Average

```
summary(FitPrecisionMacroAve)
```

```
##          V1
##  Min.    :1
## 1st Qu.:1
##  Median :1
##   Mean  :1
## 3rd Qu.:1
##   Max.  :1
```

```
apply(FitPrecisionMacroAve,2,"sd",na.rm=TRUE)
```

```
## [1] 0
```

```
summary(TestPrecisionMacroAve)
```

```
##          V1
##  Min.    :0.5054
## 1st Qu.:0.6182
##  Median :0.6503
##   Mean  :0.6474
## 3rd Qu.:0.6797
##   Max.  :0.7600
```

```
apply(TestPrecisionMacroAve,2,"sd",na.rm=TRUE)
```

```
## [1] 0.05454588
```

```
RESprecision <- rbind(apply(FitPrecisionMacroAve,2,"mean",na.rm=TRUE),
                        apply(FitPrecisionMacroAve,2,"sd",na.rm=TRUE),
                        apply(TestPrecisionMacroAve,2,"mean",na.rm=TRUE),
                        apply(TestPrecisionMacroAve,2,"sd",na.rm=TRUE))
colnames(RESprecision) = columna
rownames(RESprecision) = renglon
write.csv(RESprecision, file=paste0(archivo,"_precision",".csv"))
```

Recall Macro Average

```
summary(FitRecallMacroAve)
```

```
##          V1
##  Min.    :1
## 1st Qu.:1
##  Median :1
##   Mean  :1
## 3rd Qu.:1
##   Max.  :1
```

```
apply(FitRecallMacroAve,2,"sd",na.rm=TRUE)
```

```
## [1] 0
```

```
summary(TestRecallMacroAve)
```

```
##          V1
##  Min.    :0.5088
## 1st Qu.:0.5965
##  Median :0.6316
##   Mean  :0.6333
## 3rd Qu.:0.6667
##   Max.  :0.7544
```

```
apply(TestRecallMacroAve,2,"sd",na.rm=TRUE)
```

```
## [1] 0.05494361
```

```
RESrecall <- rbind(apply(FitRecallMacroAve,2,"mean",na.rm=TRUE),
                    apply(FitRecallMacroAve,2,"sd",na.rm=TRUE),
                    apply(TestRecallMacroAve,2,"mean",na.rm=TRUE),
                    apply(TestRecallMacroAve,2,"sd",na.rm=TRUE))
colnames(RESrecall) = columna
rownames(RESrecall) = renglon
write.csv(RESrecall, file=paste0(archivo,"_recall",".csv"))
```

F1-Score Macro Average

```
summary(FitF1ScoreMacroAve)
```

```
##          V1
##  Min.    :1
## 1st Qu.:1
##  Median :1
##   Mean  :1
## 3rd Qu.:1
##   Max.  :1
```

```
apply(FitF1ScoreMacroAve,2,"sd",na.rm=TRUE)
```

```
## [1] 0
```

```
summary(TestF1ScoreMacroAve)
```

```
##          V1
##  Min.    :0.5056
## 1st Qu.:0.5953
##  Median :0.6351
##   Mean  :0.6340
## 3rd Qu.:0.6669
##   Max.  :0.7549
```

```
apply(TestF1ScoreMacroAve,2,"sd",na.rm=TRUE)
```

```
## [1] 0.05482649
```

```
RESf1score <- rbind(apply(FitF1ScoreMacroAve,2,"mean",na.rm=TRUE),
                        apply(FitF1ScoreMacroAve,2,"sd",na.rm=TRUE),
                        apply(TestF1ScoreMacroAve,2,"mean",na.rm=TRUE),
                        apply(TestF1ScoreMacroAve,2,"sd",na.rm=TRUE))
colnames(RESf1score) = columna
rownames(RESf1score) = renglon
write.csv(RESf1score, file=paste0(archivo,"_f1score",".csv"))
```