Support Vector Machine (SVM) Polynomial kernel

Feature space partition ensemble model for replication (FESPAE)

EGG data-based experiments

Article: Lizbeth Naranjo, Carlos J. Perez, Daniel F. Merino (2025). A data ensemble-based approach for detecting vocal disorders using replicated acoustic biomarkers from electroglottography. *Sensing and Bio-Sensing Research Journal*, vol, num, pages.

```
library(tidyverse)
library(e1071)
## change the address where the file will be saved
address = "~/Documents/GitHub/"
setwd("~/Documents/GitHub/")
```

EGG data-based experiments

```
## Comment or uncomment the options: EGG-a, EGG-i, EGG-u
## EGG-a
## datos2 <- read.csv(paste0(address, "a_egg_saarbrucken.csv"),</pre>
                     sep = ";",header=TRUE, dec=",")
## name of the files to save results
## archivo = "FESPAE_crossval_strata_allvar_SVM_poly3_Saarbruken_egg_a"
## EGG-i
datos2 <- read.csv(paste0(address,"i_egg_saarbrucken.csv"),</pre>
                   sep = ";",header=TRUE, dec=",")
## name of the files to save results
archivo = "FESPAE_crossval_strata_allvar_SVM_poly3_Saarbruken_egg_i"
## EGG-u
## datos2 <- read.csv(paste0(address, "u_egg_saarbrucken.csv"),</pre>
                     sep = ";",header=TRUE, dec=",")
##
## name of the files to save results
## archivo = "FESPAE_crossval_strata_allvar_SVM_poly3_Saarbruken_egg_u"
```

dim(datos2)

[1] 675 36

summary(datos2)

```
ID fact
                 status_fact
                                  SEX
                                                   JITTER
Min.
     : 1.0
                Min. :0
                             Min.
                                    :0.0000
                                              Min.
                                                     : 0.12
                                               1st Qu.: 0.48
1st Qu.:169.5
                1st Qu.:0
                             1st Qu.:0.0000
Median :338.0
                Median:1
                             Median :0.0000
                                              Median: 2.54
      :338.0
                                                    : 16.37
Mean
                       :1
                             Mean
                                    :0.4133
                                              Mean
                Mean
3rd Qu.:506.5
                3rd Qu.:2
                             3rd Qu.:1.0000
                                              3rd Qu.: 23.20
Max.
       :675.0
                Max.
                       :2
                             Max.
                                    :1.0000
                                              Max.
                                                      :385.73
   SHIMMER
                       CPP
                                                         FZCF
                                        D2
Min.
       :0.00000
                  Min.
                         :11.69
                                         :-2.000
                                                   Min. :
                                                               3.00
                                  Min.
1st Qu.:0.02000
                  1st Qu.:20.48
                                  1st Qu.: 4.170
                                                   1st Qu.: 11.00
Median :0.03000
                  Median :24.04
                                  Median : 5.160
                                                   Median: 16.00
                                  Mean : 5.487
Mean :0.04761
                  Mean :23.76
                                                   Mean : 42.12
3rd Qu.:0.06000
                  3rd Qu.:27.11
                                  3rd Qu.: 6.300
                                                   3rd Qu.: 23.00
Max.
       :0.32000
                  Max. :35.21
                                  Max.
                                        :22.570
                                                   Max.
                                                         :5280.00
     GNE
                                     HURST
                      HNR
                                                        LZ
       :0.3600
                        :-3.47
                                        :0.1100
                                                        : 21.00
Min.
                 Min.
                                 Min.
                                                  Min.
                                                   1st Qu.: 36.00
1st Qu.:0.6500
                 1st Qu.:18.54
                                 1st Qu.:0.6200
Median : 0.8300
                 Median :22.73
                                 Median :0.8800
                                                  Median: 48.00
Mean
     :0.9723
                 Mean
                       :21.57
                                 Mean
                                        :0.9036
                                                  Mean
                                                        : 59.29
3rd Qu.:1.1500
                 3rd Qu.:25.78
                                 3rd Qu.:1.1700
                                                   3rd Qu.: 71.00
Max.
      :6.6900
                 Max.
                       :33.35
                                 Max.
                                        :1.7800
                                                   Max.
                                                          :357.00
    MFCCO
                       MFCC1
                                          MFCC2
                                                            MFCC3
Min.
       :-2.75000
                   Min.
                          :-33.1300
                                      Min.
                                             :-22.68
                                                        Min.
                                                               :-51.850
                                      1st Qu.: 1.59
1st Qu.:-0.58000
                   1st Qu.: -5.9300
                                                        1st Qu.: -4.685
Median: 0.04000
                   Median : -0.9000
                                      Median : 13.69
                                                        Median: 9.290
                   Mean : -0.9855
Mean : 0.01567
                                      Mean : 12.40
                                                        Mean : 8.217
3rd Qu.: 0.59500
                   3rd Qu.: 4.1400
                                      3rd Qu.: 22.55
                                                        3rd Qu.: 25.480
     : 2.51000
                         : 18.3700
                                                        Max. : 56.000
Max.
                   Max.
                                      Max.
                                            : 41.77
    MFCC4
                      MFCC5
                                        MFCC6
                                                          MFCC7
      :-65.180
                         :-51.930
                                           :-53.77
                                                            :-49.750
\mathtt{Min}.
                  Min.
                                    Min.
                                                     Min.
1st Qu.:-29.390
                  1st Qu.:-18.895
                                    1st Qu.:-23.14
                                                     1st Qu.:-18.130
Median :-11.470
                  Median : -7.340
                                    Median :-11.97
                                                     Median : -7.950
Mean
     :-11.149
                  Mean : -8.123
                                    Mean :-12.41
                                                     Mean : -8.902
3rd Qu.: 4.905
                  3rd Qu.: 1.370
                                    3rd Qu.: -1.29
                                                      3rd Qu.: 1.130
Max.
       : 46.890
                         : 56.520
                                    Max.
                                           : 21.69
                                                      Max.
                                                            : 32.570
                  Max.
    MFCC8
                      MFCC9
                                        MFCC10
                                                           MFCC11
       :-49.410
                         :-47.060
                                    Min.
                                           :-40.290
                                                       Min.
                                                             :-50.030
Min.
                  Min.
1st Qu.:-17.460
                  1st Qu.:-14.730
                                    1st Qu.:-14.505
                                                       1st Qu.:-12.990
Median : -9.870
                  Median : -7.730
                                                       Median : -5.050
                                    Median : -5.940
Mean : -9.593
                  Mean : -6.749
                                    Mean
                                          : -5.744
                                                       Mean
                                                             : -4.704
3rd Qu.: -1.320
                  3rd Qu.: 1.615
                                    3rd Qu.: 2.100
                                                       3rd Qu.: 2.535
      : 36.430
                        : 38.810
                                           : 36.160
Max.
                  Max.
                                    Max.
                                                       Max.
                                                             : 34.840
    MFCC12
                   PERMUTATION
                                       PPE
                                                       SHANNON
       :-33.830
                         :1.160
                                         :0.1800
Min.
                  Min.
                                  Min.
                                                   Min.
                                                          :11.89
1st Qu.:-11.390
                  1st Qu.:1.830
                                  1st Qu.:0.5300
                                                    1st Qu.:12.16
Median : -3.830
                  Median :2.090
                                  Median : 0.5500
                                                   Median :12.20
Mean : -3.119
                  Mean :2.037
                                  Mean :0.5308
                                                   Mean :12.19
```

```
3rd Qu.: 3.700
                 3rd Qu.:2.295
                                 3rd Qu.:0.5700
                                                  3rd Qu.:12.22
Max. : 39.690
                 Max. :2.580
                                 Max.
                                       :0.5700
                                                  Max.
                                                        :12.26
                 energyentropy
                                 spectralcentroid spectralspread
     ZCR
       :0.01000
                 Min. :2.630
                                        :0.0800
                                                  Min. :0.1400
Min.
                                 Min.
1st Qu.:0.03000
                 1st Qu.:3.280
                                 1st Qu.:0.1400
                                                  1st Qu.:0.2000
Median :0.04000
                 Median :3.310
                                 Median :0.1700
                                                  Median :0.2200
Mean :0.04539
                 Mean :3.279
                                 Mean :0.1767
                                                  Mean :0.2285
3rd Qu.:0.05000
                 3rd Qu.:3.320
                                 3rd Qu.:0.2000
                                                  3rd Qu.:0.2500
Max.
       :0.37000
                 Max.
                        :3.320
                                 Max.
                                        :0.4600
                                                  Max.
                                                         :0.3300
spectralentropy
                spectralrolloff
                                      RPDE
                                                       rep
Min.
      :0.0200
                Min.
                       :0.0100
                                 Min.
                                        :0.0100
                                                  Min.
                                                         :1
1st Qu.:0.0900
                1st Qu.:0.0300
                                 1st Qu.:0.2100
                                                  1st Qu.:1
Median :0.1500
                Median :0.0400
                                 Median: 0.3000
                                                  Median:2
Mean
     :0.2261
                Mean
                      :0.0608
                                 Mean :0.3278
                                                  Mean
                                                        :2
3rd Qu.:0.2700
                3rd Qu.:0.0600
                                 3rd Qu.:0.4100
                                                  3rd Qu.:3
Max.
     :2.2500
                Max.
                      :0.7800
                                 Max.
                                       :0.8700
                                                  Max.
                                                        :3
```

head(datos2)

```
ID fact status fact SEX JITTER SHIMMER
                                          CPP
                                                D2 FZCF GNE
                                                              HNR HURST LZ
                   0
                       0
                           0.39
                                   0.02 30.04 3.99
                                                    28 0.54 26.69 1.30 32
1
       1
2
       2
                   0
                       0
                           0.32
                                   0.07 23.02 3.18
                                                    44 0.47 18.56 1.58 33
3
                           0.23
                                   0.03 24.09 4.15
                                                     47 0.45 24.38 1.65 25
       3
                   0
                       0
4
       4
                   0
                           0.34
                                   0.02 32.20 4.02
                                                     29 0.49 26.18 1.29 32
                       0
                           0.36
                                   0.06 30.19 2.36
                                                    51 0.38 22.37 1.64 32
5
       5
                   0
                       0
6
       6
                   0
                           0.61
                                   0.02 33.98 3.58
                                                     26 0.56 26.98 1.23 33
                       0
 MFCC0 MFCC1 MFCC2 MFCC3 MFCC4 MFCC5 MFCC6 MFCC7 MFCC8 MFCC9 MFCC10 MFCC11
1 -0.60 8.90 -1.58 3.69 3.32 1.81 2.48 1.12 0.92 -1.17
                                                             -1.50 -2.00
2 -1.31 0.28 14.18 5.34 10.28
                                5.39 7.45 3.48 4.48 3.93
                                                              2.47
                                                                     1.17
3 -1.46 2.82 17.38
                   7.79 7.49 6.53 4.07 6.27 5.35 4.94
                                                              1.98
                                                                     2.57
4 -0.41 12.20 -2.43 3.14
                          3.31 0.78 0.51 1.39 -0.89 0.35 -0.59 -1.45
                         5.34 6.55 4.36 5.32 3.50 3.83
5 -1.79 9.83 4.12 9.38
                                                               3.43
                                                                     2.45
6 -0.89 8.43 1.50 1.38
                         1.09 1.41 -2.23 1.00 -2.76 -2.13 -4.75 -3.58
 MFCC12 PERMUTATION PPE SHANNON ZCR energyentropy spectralcentroid
1 -3.62
               2.00 0.57
                           12.19 0.02
                                               3.30
                                                               0.12
2 - 0.35
               2.48 0.51
                           12.22 0.01
                                               3.21
                                                                0.13
  0.56
               2.37 0.57
                           12.19 0.01
                                                               0.11
3
                                               3.25
4 -0.88
               1.29 0.55
                           12.16 0.02
                                               3.30
                                                                0.12
5
   2.25
               1.58 0.55
                           12.22 0.01
                                               3.24
                                                               0.10
6 -5.13
               1.31 0.53
                           12.13 0.02
                                               3.30
                                                                0.13
 spectralspread spectralentropy spectralrolloff RPDE rep
           0.18
                           0.11
                                           0.02 0.29
1
           0.22
                           0.07
2
                                           0.02 0.54
                                                       2
3
                           0.02
                                           0.01 0.35
           0.21
                                                      3
4
           0.19
                           0.13
                                           0.03 0.29
                                                      1
5
           0.18
                           0.04
                                           0.01 0.42
                                                      2
6
                                           0.03 0.32
                                                      3
           0.20
                           0.12
```

Re-Scale explanatory variables

```
## Scale the variables
datos2 <- as.data.frame(datos2)</pre>
datos2$STATUS_fact = as.factor(as.numeric(factor(datos2$status_fact)))
table(datos2$STATUS fact)
 1 2 3
225 225 225
datos <- transform(datos2,</pre>
sJITTER= scale(JITTER), sSHIMMER= scale(SHIMMER), sCPP= scale(CPP),
sD2= scale(D2), sFZCF= scale(FZCF), sGNE= scale(GNE),
sHNR= scale(HNR), sHURST= scale(HURST), sLZ= scale(LZ),
sMFCCO= scale(MFCCO),
sMFCC1= scale(MFCC1), sMFCC2= scale(MFCC2), sMFCC3= scale(MFCC3),
sMFCC4= scale(MFCC4), sMFCC5= scale(MFCC5), sMFCC6= scale(MFCC6),
sMFCC7= scale(MFCC7), sMFCC8= scale(MFCC8), sMFCC9= scale(MFCC9),
sMFCC10= scale(MFCC10), sMFCC11= scale(MFCC11), sMFCC12= scale(MFCC12),
sPERMUTATION= scale(PERMUTATION), sPPE= scale(PPE), sSHANNON= scale(SHANNON),
sZCR= scale(ZCR),
senergyentropy= scale(energyentropy), sspectralcentroid= scale(spectralcentroid),
sspectralspread= scale(spectralspread), sspectralentropy= scale(spectralentropy),
sspectralrolloff= scale(spectralrolloff), sRPDE= scale(RPDE))
datos$ID_fact = rep(1:225,each=3)
dim(datos)
```

[1] 675 69

```
## data set
trainc <- datos %>% select(
sJITTER, sSHIMMER, sCPP, sD2, sFZCF,
sGNE, sHNR, sHURST, sLZ, sMFCCO,
sMFCC1, sMFCC2, sMFCC3, sMFCC4, sMFCC5,
sMFCC6, sMFCC7, sMFCC8, sMFCC9, sMFCC10,
sMFCC11, sMFCC12,
sPERMUTATION, sPPE, sSHANNON, sZCR,
senergyentropy, sspectralcentroid, sspectralspread,
sspectralentropy, sspectralrolloff, sRPDE,
STATUS_fact,SEX, rep,ID_fact)
```

Crossvalidation

Subspaces

```
## Function to compute the Mode
Mode <- function(x, na.rm = FALSE) {</pre>
  if(na.rm){
   x = x[!is.na(x)]
   }
 ux <- unique(x)</pre>
  return(ux[which.max(tabulate(match(x, ux)))])
## Partition of subspaces
## The feature space is randomly partitioned into K subspaces with roughly equal sizes
## k = number of predictors
## K = subspaces
KO = 4 ## sub-spaces
k = 32 ## explanatory variables
k2 = round(k/K0)
space = 1:k
subspaces = rep(list(rep(NA,k2)),K0) ## Subspaces
set.seed(12345)
for(j in 1:(KO-1)){
    space1 = sample(space, size=k2, replace=FALSE)
    space = setdiff(space,space1)
    subspaces[[j]] = space1[order(space1)]
}
space1 = space
subspaces[[K0]] = space1[order(space1)]
## 32 features = 1x32, 2x16, 4x8,
subspaces
## [[1]]
## [1] 11 14 16 19 24 26 28 29
## [[2]]
## [1] 2 6 7 10 12 21 30 32
##
## [[3]]
## [1] 1 4 5 9 13 15 27 31
## [[4]]
## [1] 3 8 17 18 20 22 23 25
```

Training and testing data subsets

```
## Select data: 75% training & 25% testing stratified per category
SIM = 100  ## repeat N times the cross-validation process
N = 225 ## sample size
Nfit = 168 ## sample size for training subset
Ntest = 57  ## sample size for testing subset
Ncat = 75  ## sample size per category
Ncatfit = 56 ## training per category
Ncattest = 19 ## testing per category
FIT <- matrix(0,SIM,Nfit) ## training subsets</pre>
TEST <- matrix(0,SIM,Ntest) ## testing subsets</pre>
categoria = trainc %>% filter(rep==1) %>% select(STATUS_fact)
categoria = as.numeric(categoria$STATUS_fact)
id = 1:N
set.seed(12345)
for(si in 1:SIM){
  for(j in 1:3){
    idcat = id[categoria==j] ## stratified per category j
    ran0 = sample(idcat, size=Ncatfit, replace=FALSE)
    FIT[si,(j-1)*Ncatfit+1:Ncatfit] <- sort(ran0)</pre>
    TEST[si,(j-1)*Ncattest+1:Ncattest] <- setdiff(idcat,ran0)</pre>
} }
```

Classification metrics for models predicting nominal outcomes

```
## Functions to compute classification metrics
## Ytrue = true response variable
## Ypred = predicted outcome
## cat = category
## TP = true positive
## TN = true negative
## FP = false positive
## FN = false negative
## Function to compute the precision per class=cat
fn precision class <- function(Ytrue, Ypred, cat){</pre>
  TP = sum(Ypred[Ytrue==cat]==cat)
 FP = sum(Ypred[Ytrue!=cat]==cat)
 precision = TP/(TP+FP)
 return(precision)
## Function to compute the recall per class=cat
fn_recall_class <- function(Ytrue, Ypred, cat){ ## cat==category</pre>
 TP = sum(Ypred[Ytrue==cat]==cat)
 FN = sum(Ypred[Ytrue==cat]!=cat)
 recall = TP/(TP+FN)
 return(recall)
}
## Function to compute the F1-score per class=cat
fn f1score class <- function(Ytrue, Ypred, cat) { ## cat==category</pre>
  TP = sum(Ypred[Ytrue==cat]==cat)
  FP = sum(Ypred[Ytrue!=cat]==cat)
  FN = sum(Ypred[Ytrue==cat]!=cat)
  precision = TP/(TP+FP)
  recall = TP/(TP+FN)
  f1score = 2*(precision*recall)/(precision+recall)
  return(f1score)
}
## To save classification metrics
## Fitxxx: metric for training subset. Testxxx: metric for testing subset
FitAccuracy = TestAccuracy <- array(NA, dim=c(SIM, 1)) ## Accuracy Rate
FitPrecisionClass = TestPrecisionClass <- array(NA, dim=c(SIM, 1, 3)) ## Precision per class
FitRecallClass = TestRecallClass <- array(NA,dim=c(SIM,1,3)) ## Recall per class
FitF1ScoreClass = TestF1ScoreClass <- array(NA, dim=c(SIM, 1, 3)) ## F1-score per class
FitPrecisionMacroAve = TestPrecisionMacroAve <- array(NA,dim=c(SIM,1)) ## Precision Macro Average
FitRecallMacroAve = TestRecallMacroAve <- array(NA, dim=c(SIM,1)) ## Recall Macro Average
FitF1ScoreMacroAve = TestF1ScoreMacroAve <- array(NA, dim=c(SIM, 1)) ## F1-score Macro Average
```

Cross-validation

```
##-----
for(sim in 1:SIM){ ### BEGIN sim
my_fit = FIT[sim,] ## training subset
my_test = TEST[sim,] ## testing subset
## Training data subset
train1 <- trainc %>% filter(ID_fact%in%my_fit, rep==1) ## repetition=1
train2 <- trainc %>% filter(ID_fact%in%my_fit, rep==2) ## repetition=2
train3 <- trainc %>% filter(ID_fact%in%my_fit, rep==3) ## repetition=3
Yc = train1$STATUS_fact ## categorical response variable for training
n = length(Yc)
G = 3 # classes
## Testing data subset
test1 <- trainc %>% filter(ID_fact%in%my_test, rep==1) ## repetition=1
test2 <- trainc %>% filter(ID_fact%in%my_test, rep==2) ## repetition=2
test3 <- trainc %>% filter(ID_fact%in%my_test, rep==3) ## repetition=3
Yc.new = test1$STATUS_fact ## categorical response variable for testing
n.new = length(Yc.new)
## Delete variables which are not used
train1 <- train1 %>% select(-c(rep,ID_fact))
train2 <- train2 %>% select(-c(rep,ID_fact))
train3 <- train3 %>% select(-c(rep,ID_fact))
test1 <- test1 %>% select(-c(rep,ID_fact))
test2 <- test2 %>% select(-c(rep,ID_fact))
test3 <- test3 %>% select(-c(rep,ID_fact))
## Algorithm FESPAE
## Feature space partition ensemble model for replication
##-----
## Algo1: The feature space is randomly partitioned into M subspaces, {$1,$2,...,$M}
KO = 4 ## sub-spaces
k = 32 ## explanatory variables
k2 = round(k/K0)
space = 1:k
subspaces = rep(list(rep(NA,k2)),K0) ## Subspaces
set.seed(12345)
for(j in 1:(KO-1)){
   space1 = sample(space, size=k2, replace=FALSE)
   space = setdiff(space,space1)
   subspaces[[j]] = space1[order(space1)]
space1 = space
```

```
subspaces[[K0]] = space1[order(space1)]
# 32 features = 1x32, 2x16, 4x8,
##-----
## Algo2: for feature subspace m = 1 to M do
pred.vgam = array(NA,dim=c(n,K0,3)) ## 3 repetitions
pred.new.vgam = array(NA,dim=c(n.new,K0,3)) ## 3 repetitions
##-----
## Algo3: for replication j = 1 to J do
## REPLICATION j=1:
for(parti1 in 1:K0){ ## partition of the subspaces
train1_par = train1[,c(subspaces[[parti1]],k+1)]
test1_par = test1[,c(subspaces[[parti1]],k+1)]
## Algo4: Fit a classifier T(xj,z), xj\in Sm, to the training data
mod1 <- tune( "svm", STATUS_fact ~ . ,</pre>
             data = train1_par,
             kernel = "polynomial", degree=3,
             ranges = list(cost=c(0.01,0.1,0.5,1,5,10,20,50)))
## summary(mod1)
mejor_mod1 <- mod1$best.model</pre>
## Algo5: Compute the C response probabilities {\pi^(m,j) {ic}}, for i=1,...,n.
## Predictions
predict1 <- predict(mejor_mod1, newdata = train1_par)</pre>
predict1.new <- predict(mejor_mod1, newdata = test1_par)</pre>
pred.vgam[,parti1,1] = predict1
pred.new.vgam[,parti1,1] = predict1.new
## REPLICATION j=2:
for(parti2 in 1:K0){ ## partition of the subspaces
train2_par = train2[,c(subspaces[[parti2]],k+1)]
test2_par = test2[,c(subspaces[[parti2]],k+1)]
## Algo4: Fit a classifier $T(xj,z)$, $xj\in Sm$, to the training data
mod2 <- tune( "svm", STATUS_fact ~ . ,</pre>
             data = train2_par,
             kernel = "polynomial", degree=3,
             ranges = list(cost=c(0.01,0.1,0.5,1,5,10,20,50)))
## summary(mod2)
mejor_mod2 <- mod2$best.model</pre>
## Algo5: Compute the C response probabilities {\pi^(m,j)_{ic}}, for i=1,...,n.
## Predictions
predict2 <- predict(mejor_mod2, newdata = train2_par)</pre>
predict2.new <- predict(mejor_mod2, newdata = test2_par)</pre>
pred.vgam[,parti2,2] = predict2
pred.new.vgam[,parti2,2] = predict2.new
```

```
}
## REPLICATION j=3:
for(parti3 in 1:K0){ ## partition of the subspaces
train3_par = train3[,c(subspaces[[parti3]],k+1)]
test3_par = test3[,c(subspaces[[parti3]],k+1)]
## Algo4: Fit a classifier T(xj,z), xj \in Sm, to the training data
mod3 <- tune( "svm", STATUS_fact ~ . ,</pre>
            data = train3_par,
            kernel = "polynomial", degree=3,
            ranges = list(cost=c(0.01,0.1,0.5,1,5,10,20,50)) )
## summary(mod3)
mejor_mod3 <- mod3$best.model</pre>
## Algo5: Compute the C response probabilities {\pi^(m,j)_{ic}}, for i=1,...,n.
## Predictions
predict3 <- predict(mejor_mod3, newdata = train3_par)</pre>
predict3.new <- predict(mejor_mod3, newdata = test3_par)</pre>
pred.vgam[,parti3,3] = predict3
pred.new.vgam[,parti3,3] = predict3.new
##-----
## Algo6: End for replication j = 1 to J
## Algo7: End for feature subspace m = 1 to M
##-----
## Algo8: Output: compute the response probabilities $\pi_{ic} = mean({\pi^(m,j)_{ic}})
##-----
## Algo8: Output: compute the response category T*(x,z) = arg max {\pi_{ic}}
pred.vgam_max = array(NA,dim=n)
for(i in 1:n){
 pred.vgam_max[i] = Mode(pred.vgam[i,,])
### Predict new subjects
pred.new.vgam_max = array(NA,dim=n.new)
for(i in 1:n.new){
 pred.new.vgam_max[i] = Mode(pred.new.vgam[i,,])
##-----
## End FESPAE
##-----
## Classification Metrics for models predicting nominal outcomes
## Accuracy Rate
FitAccuracy[sim,] = c(sum(Yc==pred.vgam_max)/n)
TestAccuracy[sim,] = c(sum(Yc.new==pred.new.vgam_max)/n.new)
## Precision
```

```
for(cate in 1:3){
  FitPrecisionClass[sim,1, cate] = fn_precision_class(Yc, pred.vgam_max, cate)
  TestPrecisionClass[sim,1, cate] = fn_precision_class(Yc.new, pred.new.vgam_max, cate)
FitPrecisionMacroAve[sim, 1] = mean(FitPrecisionClass[sim, 1,])
TestPrecisionMacroAve[sim,1] = mean(TestPrecisionClass[sim,1,])
## Recall
for(cate in 1:3){
  FitRecallClass[sim,1, cate] = fn_recall_class(Yc, pred.vgam_max, cate)
  TestRecallClass[sim,1, cate] = fn_recall_class(Yc.new, pred.new.vgam_max, cate)
FitRecallMacroAve[sim, 1] = mean(FitRecallClass[sim, 1,])
TestRecallMacroAve[sim,1] = mean(TestRecallClass[sim,1,])
## F1-Score
for(cate in 1:3){
  FitF1ScoreClass[sim,1, cate] = fn_f1score_class(Yc, pred.vgam_max, cate)
  TestF1ScoreClass[sim,1, cate] = fn_f1score_class(Yc.new, pred.new.vgam_max, cate)
FitF1ScoreMacroAve[sim, 1] = mean(FitF1ScoreClass[sim, 1,])
TestF1ScoreMacroAve[sim,1] = mean(TestF1ScoreClass[sim,1,])
} ## END sim
```

Results

Accuracy Rate

```
columna = c("ensemble")
renglon = c("fit_mean","fit_sd","test_mean","test_sd")
summary(FitAccuracy)
##
         ۷1
## Min. :0.8036
## 1st Qu.:0.8988
## Median :0.9226
## Mean :0.9172
## 3rd Qu.:0.9405
## Max. :0.9762
apply(FitAccuracy,2,"sd")
## [1] 0.0322504
summary(TestAccuracy)
         V1
##
## Min. :0.4737
## 1st Qu.:0.5614
## Median :0.5965
## Mean :0.5986
## 3rd Qu.:0.6491
## Max. :0.7018
apply(TestAccuracy,2,"sd")
## [1] 0.05407553
RESaccuracy <- rbind(apply(FitAccuracy,2,"mean"), apply(FitAccuracy,2,"sd"),</pre>
                    apply(TestAccuracy,2,"mean"),apply(TestAccuracy,2,"sd"))
colnames(RESaccuracy) = columna
rownames(RESaccuracy) = renglon
write.csv(RESaccuracy, file=paste0(archivo,"_accuracy",".csv"))
```

Precision Macro Average

```
summary(FitPrecisionMacroAve)
          V1
##
          :0.8642
## Min.
## 1st Qu.:0.9187
## Median :0.9337
          :0.9310
## Mean
## 3rd Qu.:0.9455
## Max.
          :0.9769
apply(FitPrecisionMacroAve,2,"sd")
## [1] 0.02106619
summary(TestPrecisionMacroAve)
##
          V1
           :0.5153
##
  Min.
  1st Qu.:0.5992
## Median :0.6385
## Mean
         :0.6426
## 3rd Qu.:0.6918
## Max.
          :0.7889
apply(TestPrecisionMacroAve,2,"sd")
## [1] 0.06462288
RESprecision <- rbind(apply(FitPrecisionMacroAve,2,"mean"), apply(FitPrecisionMacroAve,2,"sd"),
                      apply(TestPrecisionMacroAve,2,"mean"),apply(TestPrecisionMacroAve,2,"sd"))
colnames(RESprecision) = columna
rownames(RESprecision) = renglon
write.csv(RESprecision, file=paste0(archivo,"_precision",".csv"))
```

Recall Macro Average

```
summary(FitRecallMacroAve)
          V1
##
## Min.
           :0.8036
## 1st Qu.:0.8988
## Median :0.9226
           :0.9172
## Mean
## 3rd Qu.:0.9405
## Max.
           :0.9762
apply(FitRecallMacroAve,2,"sd")
## [1] 0.0322504
summary(TestRecallMacroAve)
##
          V1
           :0.4737
##
  Min.
  1st Qu.:0.5614
## Median :0.5965
## Mean
          :0.5986
## 3rd Qu.:0.6491
## Max.
           :0.7018
apply(TestRecallMacroAve,2,"sd")
## [1] 0.05407553
RESrecall <- rbind(apply(FitRecallMacroAve,2,"mean"), apply(FitRecallMacroAve,2,"sd"),</pre>
                   apply(TestRecallMacroAve,2,"mean"),apply(TestRecallMacroAve,2,"sd"))
colnames(RESrecall) = columna
rownames(RESrecall) = renglon
write.csv(RESrecall, file=pasteO(archivo,"_recall",".csv"))
```

F1-Score Macro Average

```
summary(FitF1ScoreMacroAve)
         V1
##
## Min.
          :0.8075
## 1st Qu.:0.9012
## Median :0.9239
          :0.9185
## Mean
## 3rd Qu.:0.9408
## Max.
           :0.9762
apply(FitF1ScoreMacroAve,2,"sd")
## [1] 0.03136175
summary(TestF1ScoreMacroAve)
##
          V1
           :0.4050
##
  Min.
## 1st Qu.:0.5413
## Median :0.5747
## Mean
          :0.5821
## 3rd Qu.:0.6258
## Max.
           :0.6925
apply(TestF1ScoreMacroAve,2,"sd")
## [1] 0.05998845
RESf1score <- rbind(apply(FitF1ScoreMacroAve,2,"mean"), apply(FitF1ScoreMacroAve,2,"sd"),
                    apply(TestF1ScoreMacroAve, 2, "mean"), apply(TestF1ScoreMacroAve, 2, "sd"))
colnames(RESf1score) = columna
rownames(RESf1score) = renglon
write.csv(RESf1score, file=paste0(archivo,"_f1score",".csv"))
```