aneur: comparando stan y cgam

1. Aortic Aneurysm Progression Data

This dataset contains longitudinal measurements of grades of aortic aneurysms, measured by ultrasound examination of the diameter of the aorta.

A data frame containing 4337 rows, with each row corresponding to an ultrasound scan from one of 838 men over 65 years of age.

- ptnum (numeric) Patient identification number
- age (numeric) Recipient age at examination (years)
- diam (numeric) Aortic diameter
- state (numeric) State of aneurysm.

The states represent successive degrees of aneurysm severity, as indicated by the aortic diameter.

- State 1 Aneurysm-free < 30 cm
- State 2 Mild aneurysm 30-44 cm
- State 3 Moderate aneurysm 45-54 cm
- State 4 Severe aneurysm > 55 cm

683 of these men were aneurysm-free at age 65 and were re-screened every two years. The remaining men were aneurysmal at entry and had successive screens with frequency depending on the state of the aneurysm. Severe aneurysms are repaired by surgery.

```
data(aneur)
attach(aneur)
head(aneur)
```

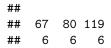
```
age diam state
##
     ptnum
                        29
## 1
         1 60.00000
         1 65.47671
## 3
         1 67.50411
                        29
                               1
         1 70.04384
                        29
                               1
## 5
         1 72.07671
                        29
                               1
         1 74.08767
```

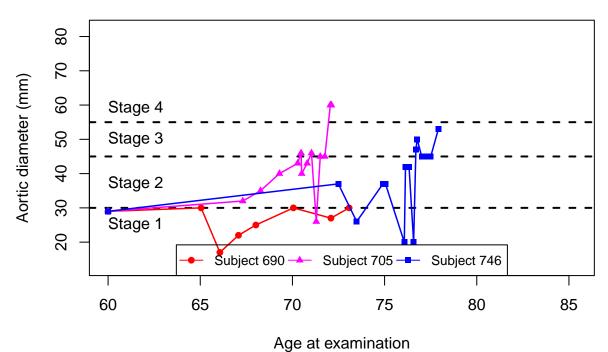
```
tail(aneur)
```

```
##
                   age diam state
        ptnum
## 4332
          838 73.40822
                         43
                                2
          838 73.61644
## 4333
                         43
                                2
## 4334
          838 73.87671
                         42
                                 2
                                 2
## 4335
          838 74.05753
## 4336
          838 74.31507
                         41
                                2
## 4337
          838 74.56712
#help(aneur)
dim(aneur)
## [1] 4337
(N = n_distinct(aneur$ptnum)) # subjects
## [1] 838
(K = max(table(aneur$ptnum))) # times
## [1] 21
table(table(aneur$ptnum))
##
##
     2
         3
             4
                 5
                     6
                         7
                             8
                                 9
                                    10 11 12 14
                                                     15
                                                        16 17 18 19
                                                                          21
## 121 107
           99 96 260 97 12 12
                                      9
                                          5
                                              2
                                                  5
                                                      5
                                                          3
J = 4 # categories
Y_diam = array(NA,dim=c(N,K))
Y_state = array(NA,dim=c(N,K))
X_age = array(NA, dim=c(N,K))
Ki = table(aneur$ptnum)
Ni = c(0, cumsum(Ki))+1
for(i in 1:N){
    aneur_i = aneur[aneur$ptnum==i,]
    for(k in 1:Ki[i]){
        Y_diam[i,k] = aneur_i$diam[k]
        Y_state[i,k] = aneur_i$state[k]
        X_age[i,k] = aneur_i$age[k]
    }
}
(Y_diam[11:18,1:8])
        [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8]
##
## [1,]
          29
               29
                    29
                         29
                               29
                                    29
                                         29
                                              NA
## [2,]
          29
               29
                    29
                               29
                                    29
                                         29
                                              NA
                         29
## [3,]
          29
               29
                    29
                         29
                               29
                                    29
                                              NA
          29
## [4,]
               29
                    NA
                         NA
                              NA
                                   NA
                                         NA
                                              NA
## [5,]
          29
               29
                    29
                         29
                               29
                                    29
                                         29
                                              NA
## [6,]
               29
                    29
                         29
                               29
                                   29
                                         29
          29
                                              NA
## [7,]
          29
               29
                    29
                         29
                              NA
                                   NA
                                         NA
                                              NA
## [8,]
          29
               29
                    34
                         NA
                              NA
                                   NA
                                         NA
                                              NA
```

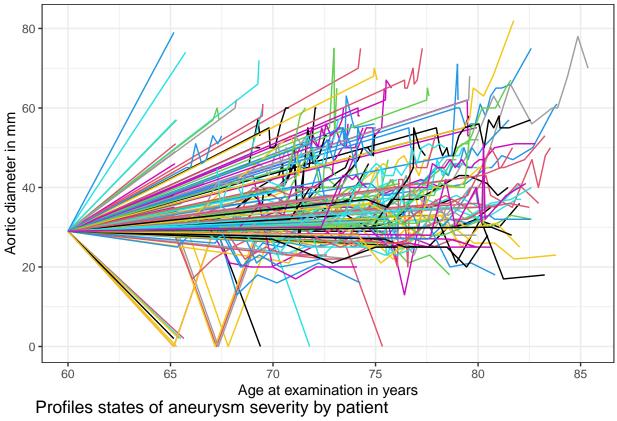
```
(Y_state[11:18,1:8])
        [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8]
##
## [1,]
           1
                1
                     1
                          1
                               1
                                     1
                                              NA
## [2,]
                1
                     1
                          1
                                1
                                     1
                                              NA
           1
## [3,]
           1
                                     1
                                              NA
                1
                     1
                          1
                               1
                                          1
## [4,]
           1
                1
                    NA
                         NA
                              NA
                                    NA
                                         NA
                                              NA
## [5,]
           1
                     1
                          1
                               1
                                    1
                                          1
                                              NA
                1
## [6,]
           1
                     1
                          1
                               1
                                    1
                                              NA
## [7,]
                                              NA
                              NA
           1
                1
                     1
                          1
                                   NA
                                         NA
## [8,]
                     2
                         NA
                              NA
                                   NA
                                              NA
(X_age[11:18,1:8])
##
        [,1]
                 [,2]
                          [,3]
                                    [,4]
                                             [,5]
                                                      [,6]
                                                                [,7] [,8]
## [1,]
          60 65.45205 67.45205 69.92877 72.01096 74.01096 76.00000
## [2,]
         60 65.44932 67.46301 69.92603 71.96986 73.96986 75.92055
## [3,]
         60 65.45753 67.44658 69.92329 71.96712 73.96712 75.91781
## [4,]
        60 65.44384
                            NA
                                     NA
                                               NA
                                                        NA
## [5,]
        60 65.43836 67.42192 69.93699 71.94247 73.94247 75.89315
        60 65.40822 67.40822 70.04932 72.07123 74.06575 76.09041
## [6,]
## [7,]
          60 65.38082 67.38082 70.02192
                                               NA
                                                                       NA
## [8,]
          60 65.47123 67.47123
                                               NA
                                                        NA
                                                                 NA
                                                                       NA
(Ki[11:18])
##
## 11 12 13 14 15 16 17 18
## 7 7 7 2 7 7 4 3
### Considering only data having more than one screen (state>1)
idx2 = c()
for(i in 1:N){
 if( sum(Y_state[i,1:Ki[i]])>Ki[i]){
    idx2 = c(idx2,i)
 }
Y2_{diam} = Y_{diam}[idx2,]
Y2_state = Y_state[idx2,]
X2_age = X_age[idx2,]
N2 = length(idx2)
Ki2 = Ki[idx2]
### Considering only data having more than one screen (diam!=29, or diam<29 & dim>29)
idx3 = c()
for(i in 1:N){
  if( min(Y_diam[i,1:Ki[i]])!=max(Y_diam[i,1:Ki[i]])){
    idx3 = c(idx3,i)
 }
Y3_{diam} = Y_{diam}[idx3,]
```

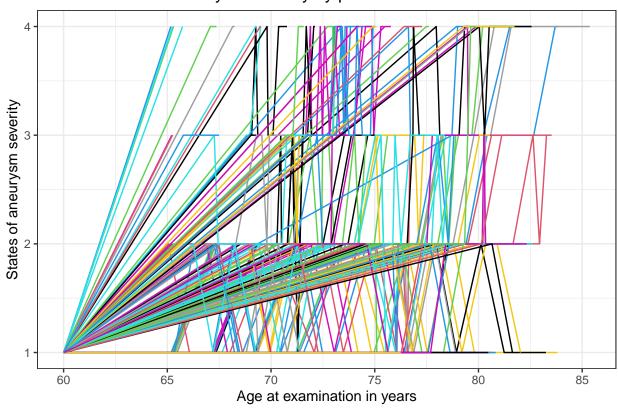
```
Y3_state = Y_state[idx3,]
X3_age = X_age[idx3,]
N3 = length(idx3)
Ki3 = Ki[idx3]
aneur2 = aneur%>%filter(aneur$ptnum%in%idx2)
aneur3 = aneur%>%filter(aneur$ptnum%in%idx3)
### Creo que es mejor trabajar con aneur3
```





Profiles aortic diameter by patient





Profiles aortic diameter by patient Aortic diameter in mm Age at examination in years Profiles states of aneurysm severity by patient States of aneurysm severity

La variable respuesta puede ser continua (''diam'') u ordinal (''state''), y la unica covariable es la edad

Age at examination in years

("age") \

$$diam_{it} = \beta_0 + f_1(age_{it}) + b_{0i} + age_{it} \times b_{1i} + \varepsilon_{it}, \qquad b_i \sim \mathcal{N}(0, \psi), \quad \varepsilon_i \sim \mathcal{N}(0, \Lambda \sigma^2),$$

where f_1 is a non-decreasing smoothing function and $b_{1i} > 0$.

Quiza solo debemos considerar intercepto fijo, pero NO intercepto aleatorio, y SI pendiente aleatorio

$$diam_{it} = \beta_0 + f_1(age_{it}) + age_{it} \times b_{1i} + \varepsilon_{it}, \qquad b_{1i} \sim N(0, \psi), \quad \varepsilon_i \sim N(0, \Lambda\sigma^2),$$

The ordinal response $state_{it}$ is modelled in terms of the cumulative probabilities $P(state_{it} \leq j|b_i)$ by using the proportional odds model,

$$P(state_{it} \le j|b_i) = \eta_{it,j},$$

subject to

$$\eta_{it,i} = \kappa_i + \beta_0 + f_1(age_{it}) + age_{it} \times b_{1i}, \qquad b_{1i} \sim \mathcal{N}(0, \psi),$$

where the constraints are such that f_1 is a non-decreasing smoothing function and $b_{1i} > 0$, and for the breakpoints $\kappa_j < \kappa_{j+1}$ with j = 1, 2.

```
y = aneur3$diam -29
x1 = aneur3$age -60
x2 = aneur3$age -60
id = as.numeric(as.factor(aneur3$ptnum))

n = length(y)
N = n_distinct(id)
Ni = c(0,cumsum(table(id)))+1
k1 = 3 #
k2 = 3 #
knots1 = quantile(x1, c(0.5))
knots2 = quantile(x2, c(0.5))
```

2. Generar la matriz diseño X para los B-splines

Note que f(x) se representa como:

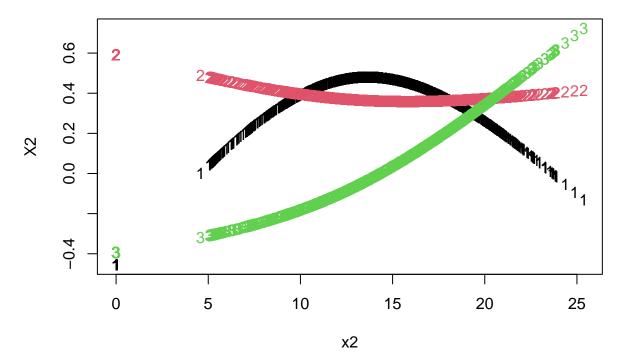
$$\begin{array}{rcl} f(x) & = & f_1(x_1) \\ & = & \sum_{j=1}^{h_1} \beta_{1j} I_{1j}(x) \end{array}$$

para β_{1j} parámetros desconocidos, y para los $I_{1j}(x)$ se utilizar'an I-splines y B-splines.

El número de knots se elige lo suficientemente grande para evitar **over-smoothing**, pero lo suficientemente pequeño para evitar excesivo costo computacional.

El número de $knots\ K$ es considerado a priori.

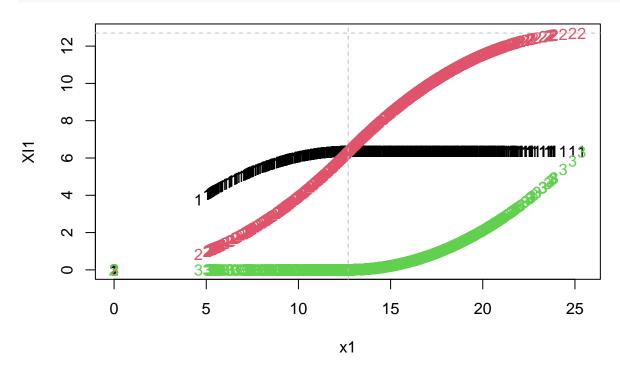
```
# Generate a basis matrix for Natural Cubic Splines
X2 <- ns(x = x2, knots = knots2, intercept = TRUE)
###X2 = (X2-mean(X2))/sd(X2)
matplot(x2, X2)</pre>
```



3. Generar la matriz diseño XI1 para los I-splines

$$\begin{array}{lll} f_1(x_1) & & \displaystyle \sum_{j=1}^{h_1} \beta_{1j} I_{1j}(x_1) \\ \\ I_{1j}(x_1) & = & \displaystyle \int_{x_0}^{x_1} B_{1j}(u) d_u \end{array}$$

```
### ibs: integrated basis splines
### degree = 3 cubic splines
XI1 <- ibs(x1, knots = knots1, degree = 1, intercept = TRUE)
###XI1 = (XI1-mean(XI1))/sd(XI1)
matplot(x1, XI1)
abline(v = knots1, h = knots1, lty = 2, col = "gray")</pre>
```



4. Definir la penalización S1 y S2

La flexibilidad ajustada de f es controlada por K, a través de una penalización cuadrátrica de la forma:

$$\sum_{j} \lambda_{j} \beta^{T} S_{j} \beta$$

donde los S_j son matrices de coeficientes conocidos, y los λ_j son parámetros de suavizamiento estimados.

```
#Este es el código que produce la matriz de diferenciación.
#No es el óptimo, pero funciona.
#"k" es el número de b-splines y
#"d" el orden de la diferenciación.
#Adjunto el artículo donde discutimos esto (página 7).
diffMatrix = function(k, d = 2){
  if( (d<1) || (d %% 1 != 0) )stop("d must be a positive integer value");
  if( (k<1) \mid | (k \% 1 != 0) )stop("k must be a positive integer value");
  if(d >= k)stop("d must be lower than k");
 out = diag(k);
 for(i in 1:d){
   out = diff(out);
 }
 return(out)
(D1 = diffMatrix(k=k1, d=2))
##
        [,1] [,2] [,3]
## [1,]
          1 -2
(D2 = diffMatrix(k=k2, d=2))
        [,1] [,2] [,3]
## [1,]
          1 -2
(S1 = t(D1)\%*\%D1 + diag(1,k1)*10e-4)
          [,1]
               [,2]
                        [,3]
## [1,] 1.001 -2.000 1.000
## [2,] -2.000 4.001 -2.000
## [3,] 1.000 -2.000 1.001
(S2 = t(D2)\%*\%D2 + diag(1,k2)*10e-4)
          [,1]
                 [,2]
                        [,3]
## [1,] 1.001 -2.000 1.000
## [2,] -2.000 4.001 -2.000
## [3,] 1.000 -2.000 1.001
```

8. Spline con restricciones creciente

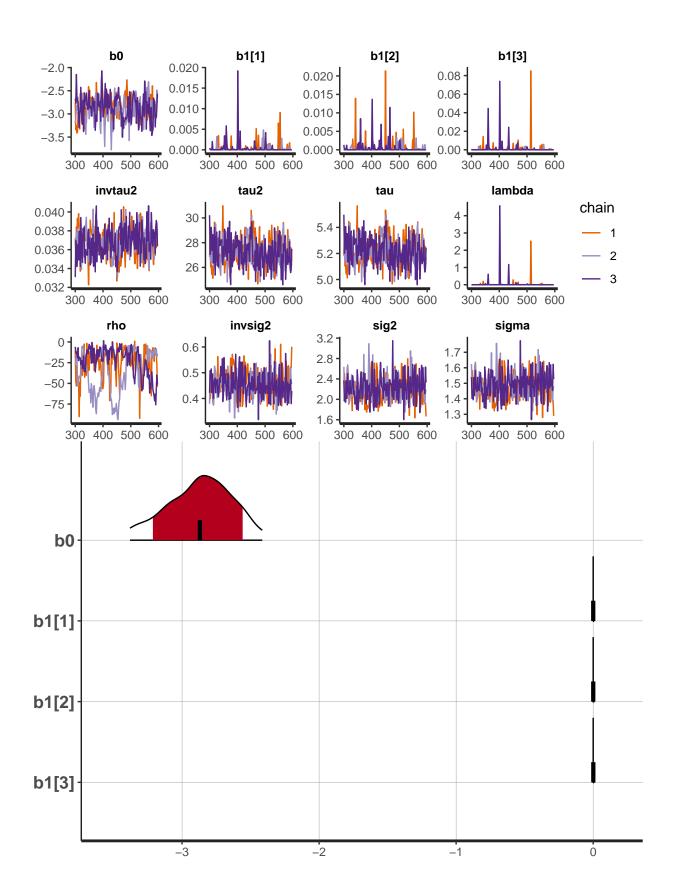
8.2. LME: Spline con restricciones creciente

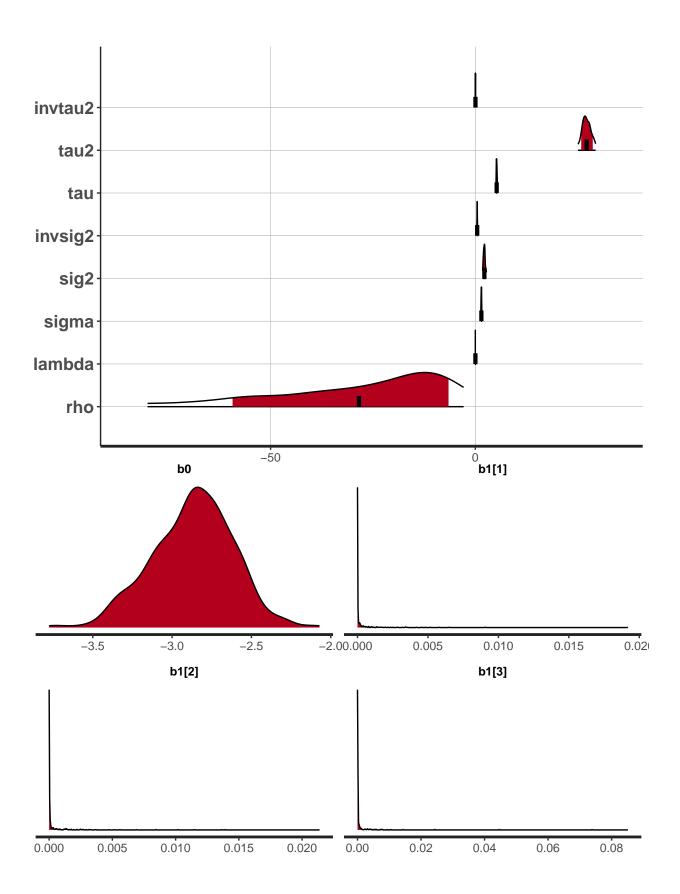
```
datos.lme.add.incr <- list( y = y ,</pre>
                          id = id,
              n = length(y),
              N = N, Ni = Ni,
              k1=k1
              XI1 = XI1,
              x1 = x1
              zero = rep(0,1+k1),
              S1=S1 )
inits.lme.add.incr <- function(){</pre>
  "b0" = rnorm(1,0,0.1),
  "b1" = abs(rnorm(k1,0,0.1)),
  "invtau2" = rgamma(1,1,1) ,
  "lambda" = rgamma(1,1,1) ,
 "invsig2" = rgamma(1,1,1)
param.add = c("b0","b1", "invtau2","tau2","tau", "lambda","rho")
param.lme.add = c("b0","b1", "invtau2","tau2","tau1", "lambda","rho", "invsig2","sig2","sigma")
fit.lme.add.incr.reslope <- stan("jagam_9_aneur_lme_add_incr_reslope.stan",</pre>
            data=datos.lme.add.incr,
            chains=3,warmup=300,iter=600,thin=2,cores=4,
            init= inits.lme.add.incr)
## Running /Library/Frameworks/R.framework/Resources/bin/R CMD SHLIB foo.c
## clang -mmacosx-version-min=10.13 -I"/Library/Frameworks/R.framework/Resources/include" -DNDEBUG
## In file included from <built-in>:1:
## In file included from /Library/Frameworks/R.framework/Versions/4.1/Resources/library/StanHeaders/inc
## In file included from /Library/Frameworks/R.framework/Versions/4.1/Resources/library/RcppEigen/inclu
## In file included from /Library/Frameworks/R.framework/Versions/4.1/Resources/library/RcppEigen/inclu
## /Library/Frameworks/R.framework/Versions/4.1/Resources/library/RcppEigen/include/Eigen/src/Core/util
## namespace Eigen {
## ^
## /Library/Frameworks/R.framework/Versions/4.1/Resources/library/RcppEigen/include/Eigen/src/Core/util
## namespace Eigen {
##
## In file included from <built-in>:1:
## In file included from /Library/Frameworks/R.framework/Versions/4.1/Resources/library/StanHeaders/inc
## In file included from /Library/Frameworks/R.framework/Versions/4.1/Resources/library/RcppEigen/inclu
## /Library/Frameworks/R.framework/Versions/4.1/Resources/library/RcppEigen/include/Eigen/Core:96:10: f
## #include <complex>
           ^~~~~~~
## 3 errors generated.
## make: *** [foo.o] Error 1
```

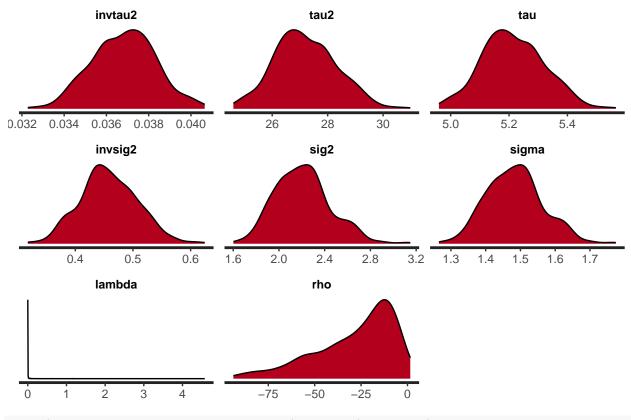
```
print(fit.lme.add.incr.reslope, pars=param.lme.add)
## Inference for Stan model: jagam_9_aneur_lme_add_incr_reslope.
## 3 chains, each with iter=600; warmup=300; thin=2;
## post-warmup draws per chain=150, total post-warmup draws=450.
##
##
                                 2.5%
                                         25%
            mean se_mean
                             sd
                                                 50%
                                                        75% 97.5% n_eff Rhat
## b0
            -2.87
                    0.02 0.25
                                -3.38 -3.04
                                              -2.86
                                                     -2.70 -2.42
                                                                    222 1.01
            0.00
                    0.00 0.00
                                        0.00
                                                                   339 1.01
## b1[1]
                                 0.00
                                               0.00
                                                       0.00 0.00
## b1[2]
            0.00
                    0.00 0.00
                                 0.00
                                        0.00
                                               0.00
                                                       0.00 0.00
                                                                   436 1.00
            0.00
                    0.00 0.01
                                 0.00
                                        0.00
## b1[3]
                                               0.00
                                                       0.00 0.01
                                                                   448 1.01
## invtau2
            0.04
                    0.00 0.00
                                 0.03
                                       0.04
                                               0.04
                                                       0.04 0.04
                                                                    345 1.01
## tau2
            27.19
                    0.06 1.11
                                25.08 26.44 27.08
                                                     27.91 29.29
                                                                   341 1.01
                    0.01 0.11
                                 5.01
                                        5.14
                                                                   342 1.01
## tau
            5.21
                                               5.20
                                                       5.28 5.41
## lambda
            0.02
                    0.01 0.25
                                 0.00
                                        0.00
                                               0.00
                                                       0.00 0.06
                                                                   461 1.00
## rho
           -28.61
                    4.05 21.32 -80.03 -41.43 -22.41 -11.85 -2.76
                                                                    28 1.13
                                 0.37
                                        0.43
                                                                   376 1.01
## invsig2
            0.46
                    0.00 0.05
                                               0.46
                                                       0.49 0.56
## sig2
            2.21
                    0.01 0.25
                                 1.78
                                        2.03
                                               2.19
                                                       2.33 2.71
                                                                    375 1.01
## sigma
            1.48
                    0.00 0.08
                                 1.33
                                        1.42
                                               1.48
                                                       1.53 1.65
                                                                   375 1.01
##
## Samples were drawn using NUTS(diag_e) at Wed Aug 16 11:48:16 2023.
## For each parameter, n_eff is a crude measure of effective sample size,
## and Rhat is the potential scale reduction factor on split chains (at
```

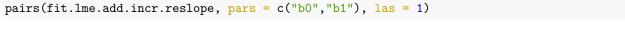
convergence, Rhat=1).

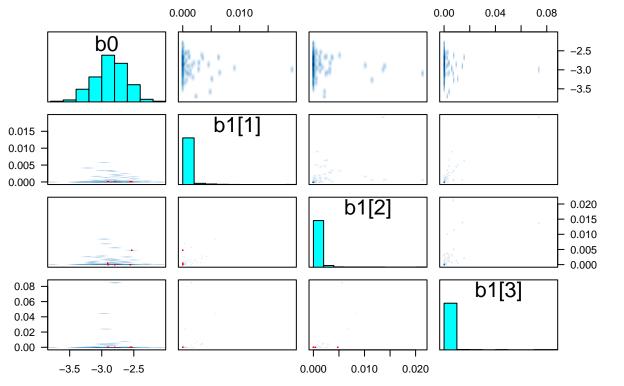
```
stan_trace(fit.lme.add.incr.reslope, pars=param.lme.add)
stan_plot(fit.lme.add.incr.reslope, pars=c("b0","b1"), point_est = "mean", show_density = TRUE)
stan_plot(fit.lme.add.incr.reslope, pars=c("invtau2","tau2","tau2","tau", "invsig2","sig2","sigma", "lambda",
stan_dens(fit.lme.add.incr.reslope, pars=c("b0","b1"))
stan_dens(fit.lme.add.incr.reslope, pars=c("invtau2","tau2","tau2","tau2","sig2","sig2","sigma", "lambda",";
```



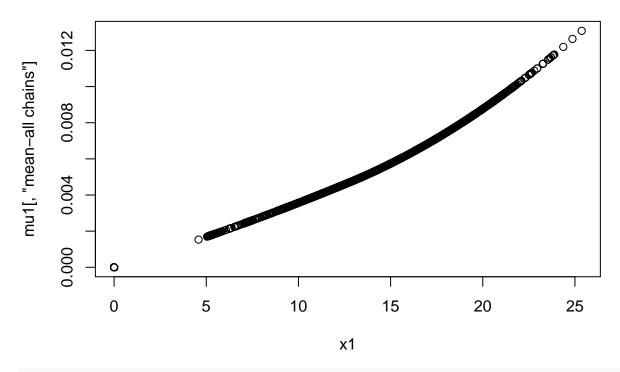




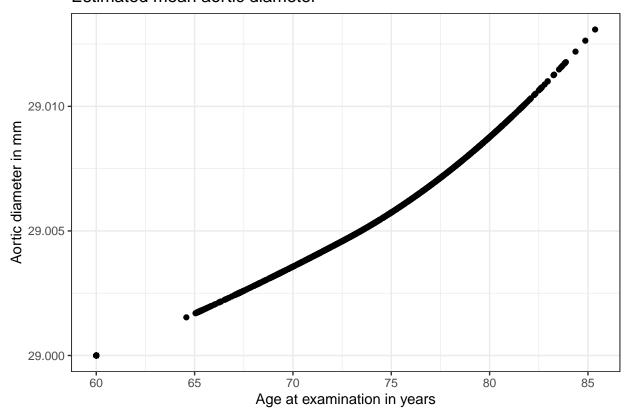




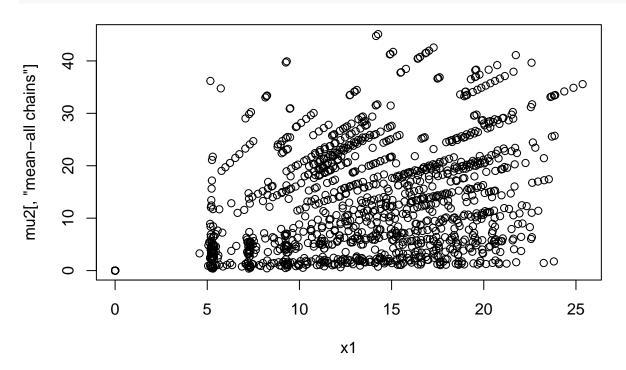
mu1 = get_posterior_mean(fit.lme.add.incr.reslope,"mu1")
plot(x1,mu1[,"mean-all chains"])



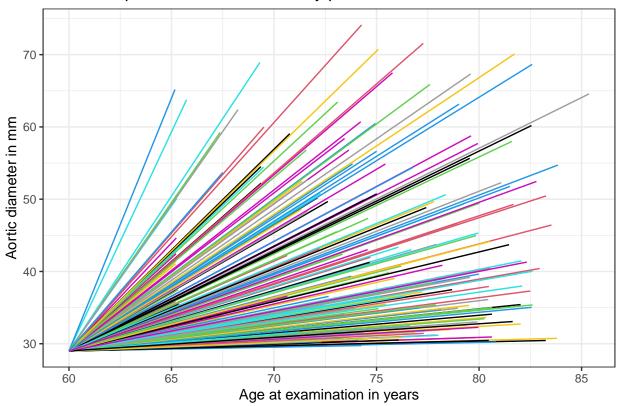
Estimated mean aortic diameter



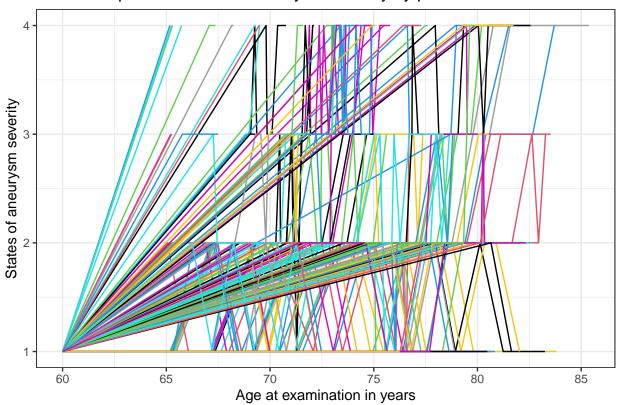
mu2 = get_posterior_mean(fit.lme.add.incr.reslope,"mu2")
plot(x1,mu2[,"mean-all chains"])



Estimated profiles aortic diameter by patient



Estimated profiles states of aneurysm severity by patient



CASES 9.2. LME: Spline con restricciones creciente

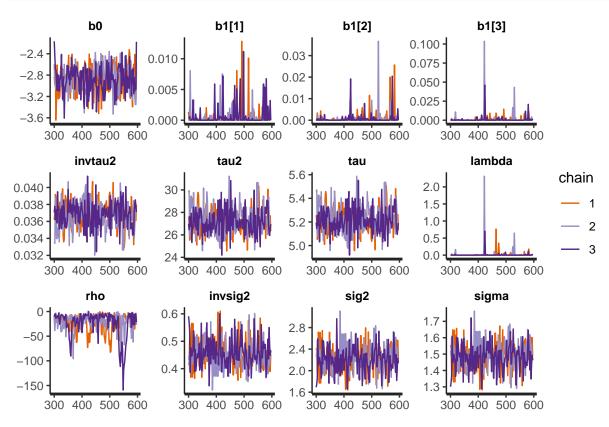
```
idx = names(table(aneur3$ptnum))
id690 = which(aneur3$ptnum==690)
n690 = length(id690)
i690 = which(idx==690)
XI690 = XI1[id690,]
x690 = x1[id690]
id703 = which(aneur3$ptnum==703)
n703 = length(id703)
i703 = which(idx==703)
XI703 = XI1[id703,]
x703 = x1[id703]
id705 = which(aneur3$ptnum==705)
n705 = length(id705)
i705 = which(idx==705)
XI705 = XI1[id705,]
x705 = x1[id705]
id745 = which(aneur3$ptnum==745)
n745 = length(id745)
i745 = which(idx==745)
XI745 = XI1[id745,]
x745 = x1[id745]
id746 = which(aneur3$ptnum==746)
n746 = length(id746)
i746 = which(idx==746)
XI746 = XI1[id746,]
x746 = x1[id746]
id837 = which(aneur3$ptnum==837)
n837 = length(id837)
i837 = which(idx==837)
XI837 = XI1[id837,]
x837 = x1[id837]
datos.lme.add.incr.cases <- list( y = y ,</pre>
                         id = id,
               n = length(y),
               N = N , Ni = Ni,
               k1=k1,
              XI1 = XI1,
              x1 = x1
              zero = rep(0,1+k1),
              S1=S1,
              n690=n690, i690=i690, XI690=XI690, x690=x690,
              n703=n703, i703=i703, XI703=XI703, x703=x703,
              n705=n705, i705=i705, XI705=XI705, x705=x705,
              n745=n745, i745=i745, XI745=XI745, x745=x745,
```

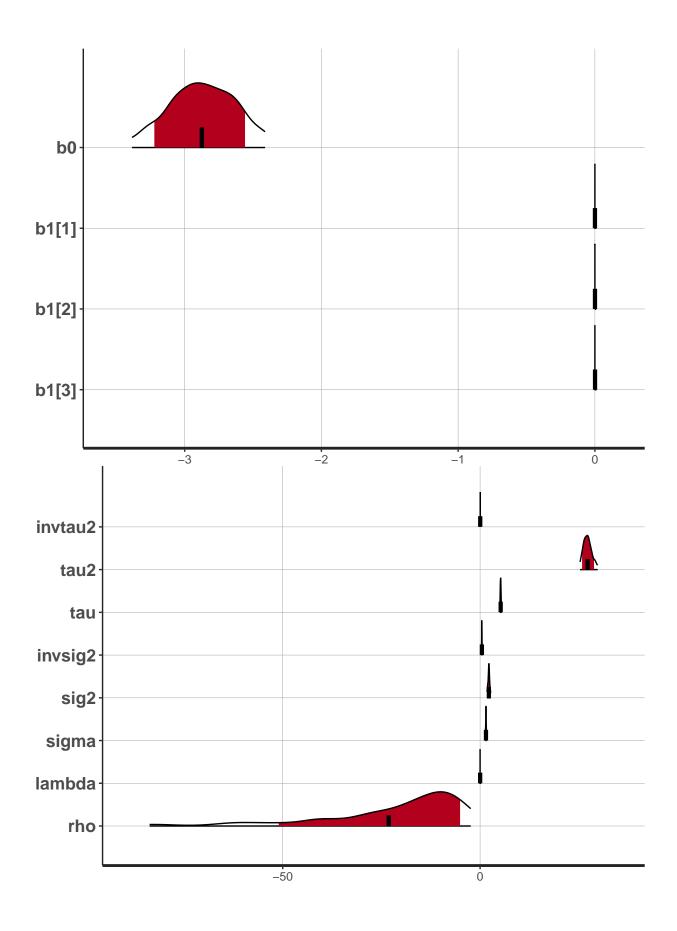
```
n746=n746, i746=i746, XI746=XI746, x746=x746,
              n837=n837, i837=i837, XI837=XI837, x837=x837)
fit.lme.add.incr.reslope.cases <- stan("jagam_9_aneur_lme_add_incr_reslope_cases.stan",
            data=datos.lme.add.incr.cases,
            chains=3,warmup=300,iter=600,thin=2,cores=4,
            init= inits.lme.add.incr)
## Running /Library/Frameworks/R.framework/Resources/bin/R CMD SHLIB foo.c
## clang -mmacosx-version-min=10.13 -I"/Library/Frameworks/R.framework/Resources/include" -DNDEBUG
## In file included from <built-in>:1:
## In file included from /Library/Frameworks/R.framework/Versions/4.1/Resources/library/StanHeaders/inc
## In file included from /Library/Frameworks/R.framework/Versions/4.1/Resources/library/RcppEigen/inclu
## In file included from /Library/Frameworks/R.framework/Versions/4.1/Resources/library/RcppEigen/inclu
## /Library/Frameworks/R.framework/Versions/4.1/Resources/library/RcppEigen/include/Eigen/src/Core/util
## namespace Eigen {
## ^
## /Library/Frameworks/R.framework/Versions/4.1/Resources/library/RcppEigen/include/Eigen/src/Core/util
## namespace Eigen {
##
##
## In file included from <built-in>:1:
## In file included from /Library/Frameworks/R.framework/Versions/4.1/Resources/library/StanHeaders/inc
## In file included from /Library/Frameworks/R.framework/Versions/4.1/Resources/library/RcppEigen/inclu
## /Library/Frameworks/R.framework/Versions/4.1/Resources/library/RcppEigen/include/Eigen/Core:96:10: f
## #include <complex>
            ^~~~~~~~
##
## 3 errors generated.
## make: *** [foo.o] Error 1
print(fit.lme.add.incr.reslope.cases, pars=param.lme.add)
## Inference for Stan model: jagam_9_aneur_lme_add_incr_reslope_cases.
## 3 chains, each with iter=600; warmup=300; thin=2;
## post-warmup draws per chain=150, total post-warmup draws=450.
##
##
                                          25%
            mean se mean
                                  2.5%
                                                 50%
                                                       75% 97.5% n_eff Rhat
                             sd
                                       -3.05
## b0
            -2.88
                     0.01
                           0.25
                                 -3.38
                                               -2.87 - 2.69 - 2.41
                                                                   288 1.01
## b1[1]
             0.00
                     0.00
                           0.00
                                  0.00
                                        0.00
                                                0.00 0.00 0.01
                                                                   461 1.01
             0.00
                     0.00
                          0.00
                                  0.00
                                         0.00
                                                0.00 0.00 0.01
## b1[2]
                                                                   474 1.00
                                  0.00
                                         0.00
## b1[3]
             0.00
                     0.00
                          0.01
                                                0.00 0.00 0.01
                                                                   469 1.00
## invtau2
            0.04
                     0.00 0.00
                                  0.03
                                        0.04
                                                0.04 0.04 0.04
                                                                   353 1.00
                                 25.32 26.44 27.16 27.93 29.79
## tau2
            27.24
                     0.06 1.17
                                                                   352 1.00
## tau
            5.22
                     0.01 0.11
                                  5.03
                                        5.14
                                                5.21 5.28 5.46
                                                                   352 1.00
## lambda
            0.01
                     0.01 0.13
                                  0.00
                                        0.00
                                                0.00 0.00 0.09
                                                                   458 1.00
## rho
           -23.21
                     2.62 21.59 -83.63 -29.16 -16.27 -8.93 -2.38
                                                                    68 1.01
## invsig2
            0.46
                     0.00 0.05
                                  0.37
                                         0.42
                                                0.45 0.48 0.57
                                                                   336 1.00
## sig2
             2.22
                     0.01 0.24
                                  1.75
                                         2.07
                                                2.23 2.36 2.71
                                                                   292 1.00
             1.49
                                  1.32
                                         1.44
                                                1.49 1.54 1.65
                                                                   298 1.00
## sigma
                     0.00 0.08
## Samples were drawn using NUTS(diag_e) at Wed Aug 16 11:50:45 2023.
```

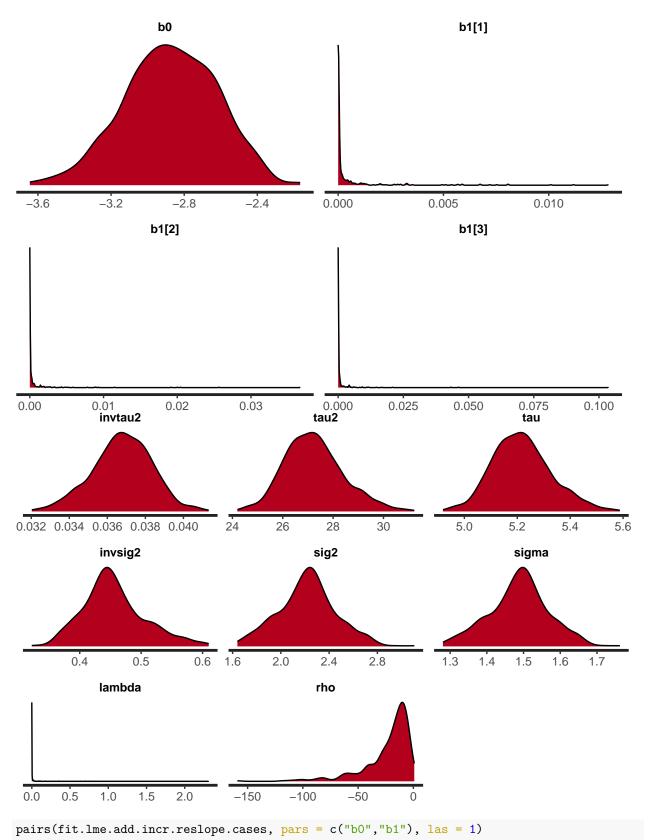
For each parameter, n_eff is a crude measure of effective sample size,

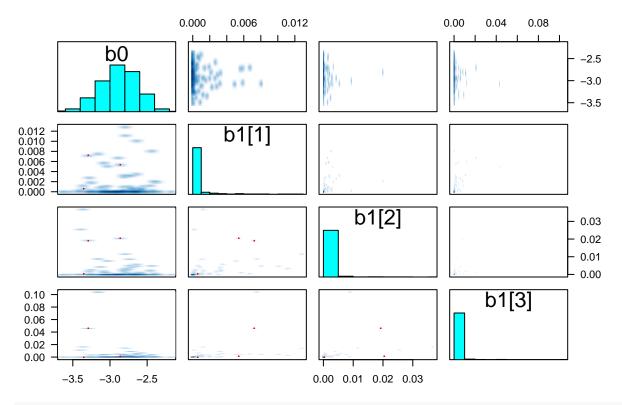
and Rhat is the potential scale reduction factor on split chains (at
convergence, Rhat=1).

```
stan_trace(fit.lme.add.incr.reslope.cases, pars=param.lme.add)
stan_plot(fit.lme.add.incr.reslope.cases, pars=c("b0","b1"), point_est = "mean", show_density = TRUE)
stan_plot(fit.lme.add.incr.reslope.cases, pars=c("invtau2","tau2","tau", "invsig2","sig2","sigma", "latan_dens(fit.lme.add.incr.reslope.cases, pars=c("b0","b1"))
stan_dens(fit.lme.add.incr.reslope.cases, pars=c("invtau2","tau2","tau2","tau", "invsig2","sig2","sigma", "latan_dens(fit.lme.add.incr.reslope.cases, pars=c("invtau2","tau2","tau2","tau2","sig2","sigma", "latan_dens(fit.lme.add.incr.reslope.cases, pars=c("invtau2","tau2","tau2","tau2","sig2","sigma", "latan_dens(fit.lme.add.incr.reslope.cases, pars=c("invtau2","tau2","tau2","tau2","sig2","sigma", "latan_dens(fit.lme.add.incr.reslope.cases, pars=c("invtau2","tau2","tau2","tau2","sig2","sig2","sigma", "latan_dens(fit.lme.add.incr.reslope.cases, pars=c("invtau2","tau2","tau2","tau2","tau2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2","sig2",
```

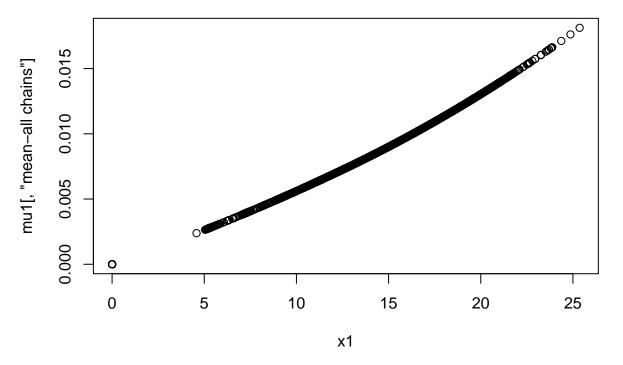




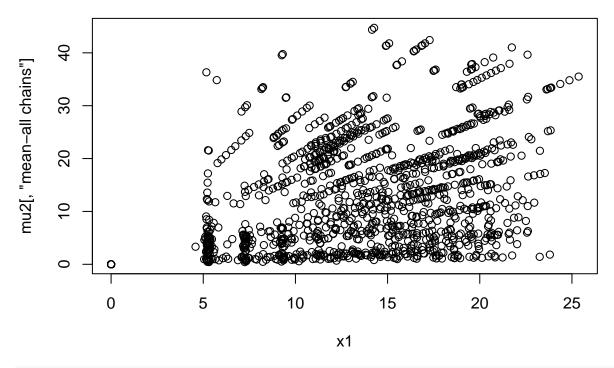




mu1 = get_posterior_mean(fit.lme.add.incr.reslope.cases,"mu1")
plot(x1,mu1[,"mean-all chains"])

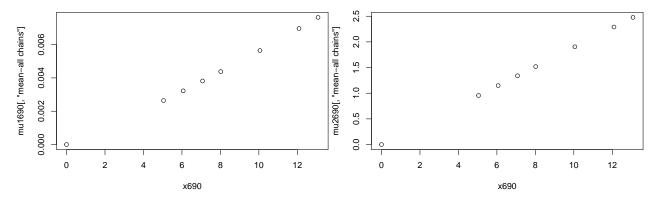


mu2 = get_posterior_mean(fit.lme.add.incr.reslope.cases,"mu2")
plot(x1,mu2[,"mean-all chains"])



```
mu1690 = get_posterior_mean(fit.lme.add.incr.reslope.cases,"mu1690")
mu2690 = get_posterior_mean(fit.lme.add.incr.reslope.cases,"mu2690")

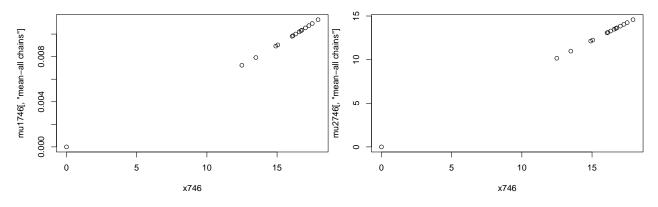
plot(x690,mu1690[,"mean-all chains"])
plot(x690,mu2690[,"mean-all chains"])
```



```
mu1703 = get_posterior_mean(fit.lme.add.incr.reslope.cases,"mu1703")
mu2703 = get_posterior_mean(fit.lme.add.incr.reslope.cases,"mu2703")

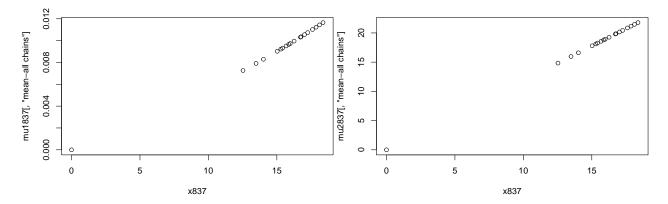
plot(x703,mu1703[,"mean-all chains"])
plot(x703,mu2703[,"mean-all chains"])
```

```
o o opposite opposite
                                                                                                                                                                                         20
mu1703[, "mean-all chains"]
                                                                                                                                                                             mu2703[, "mean-all chains"]
                                                                                                                                                                                         15
                                                                                                                                                                                         10
           0.004
                                                                                                                                                                                         2
           0.000
                                                                                                                                                                                         0
                         0
                                                                 5
                                                                                                       10
                                                                                                                                             15
                                                                                                                                                                                                       0
                                                                                                                                                                                                                                              5
                                                                                                                                                                                                                                                                                     10
                                                                                                                                                                                                                                                                                                                           15
                                                                                                                                                                                                                                                                          x703
                                                                                            x703
mu1705 = get_posterior_mean(fit.lme.add.incr.reslope.cases,"mu1705")
mu2705 = get_posterior_mean(fit.lme.add.incr.reslope.cases,"mu2705")
plot(x705,mu1705[,"mean-all chains"])
plot(x705,mu2705[,"mean-all chains"])
                                                                                                                                                                                                                                                                                                                           0000000
                                                                                                                                                                                         20
           0.006
mu1705[, "mean-all chains"]
                                                                                                                                                                             mu2705[, "mean-all chains"]
                                                                                                                                                                                         15
           0.004
                                                                                                                                                                                         9
           0.002
                                                                                                                                                                                         2
           0.000
                                                                                                                                                                                         0
                         0
                                                 2
                                                                                              6
                                                                                                                      8
                                                                                                                                            10
                                                                                                                                                                  12
                                                                                                                                                                                                       0
                                                                                                                                                                                                                              2
                                                                                                                                                                                                                                                                            6
                                                                                                                                                                                                                                                                                                   8
                                                                                                                                                                                                                                                                                                                          10
                                                                                                                                                                                                                                                                                                                                                12
                                                                                                                                                                                                                                                      4
                                                                                            x705
mu1745 = get_posterior_mean(fit.lme.add.incr.reslope.cases,"mu1745")
mu2745 = get_posterior_mean(fit.lme.add.incr.reslope.cases,"mu2745")
plot(x745,mu1745[,"mean-all chains"])
plot(x745,mu2745[,"mean-all chains"])
                                                                                                                                                                                                                                                                                                                            00000000
                                                                                                                                                                                         20
mu1745[, "mean-all chains"]
                                                                                                                                                                             mu2745[, "mean-all chains"]
           900.0
                                                                                                                                                                                         15
           0.004
                                                                                                                                                                                         10
           0.002
                                                                                                                                                                                         0
                         0
                                                2
                                                                                            6
                                                                                                                  8
                                                                                                                                       10
                                                                                                                                                             12
                                                                                                                                                                                                       0
                                                                                                                                                                                                                             2
                                                                                                                                                                                                                                                                          6
                                                                                                                                                                                                                                                                                               8
                                                                                                                                                                                                                                                                                                                    10
                                                                                                                                                                                                                                                                                                                                          12
                                                                      4
                                                                                            x745
                                                                                                                                                                                                                                                                          x745
mu1746 = get_posterior_mean(fit.lme.add.incr.reslope.cases,"mu1746")
mu2746 = get_posterior_mean(fit.lme.add.incr.reslope.cases,"mu2746")
plot(x746,mu1746[,"mean-all chains"])
plot(x746,mu2746[,"mean-all chains"])
```



```
mu1837 = get_posterior_mean(fit.lme.add.incr.reslope.cases,"mu1837")
mu2837 = get_posterior_mean(fit.lme.add.incr.reslope.cases,"mu2837")

plot(x837,mu1837[,"mean-all chains"])
plot(x837,mu2837[,"mean-all chains"])
```

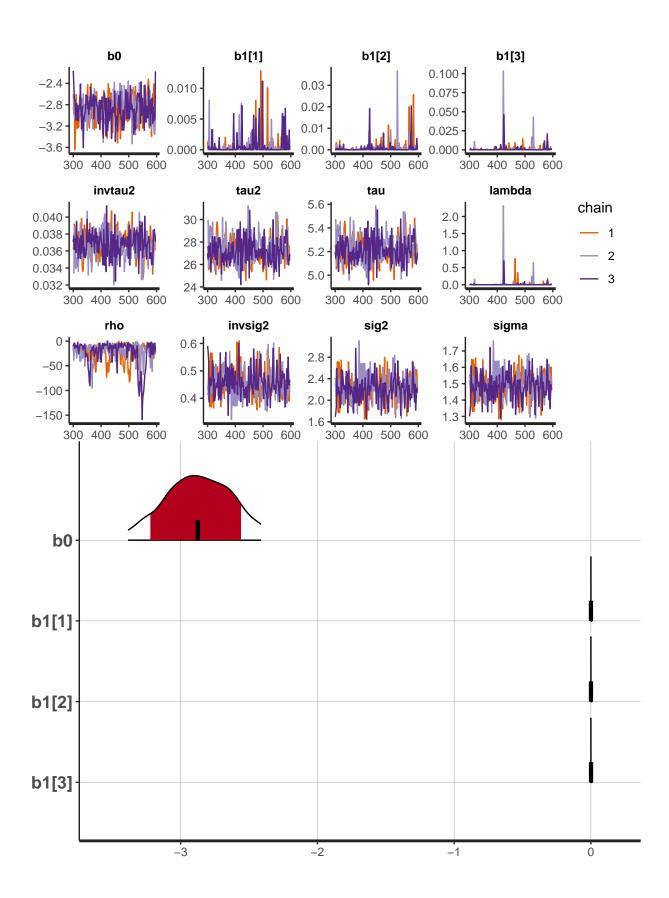


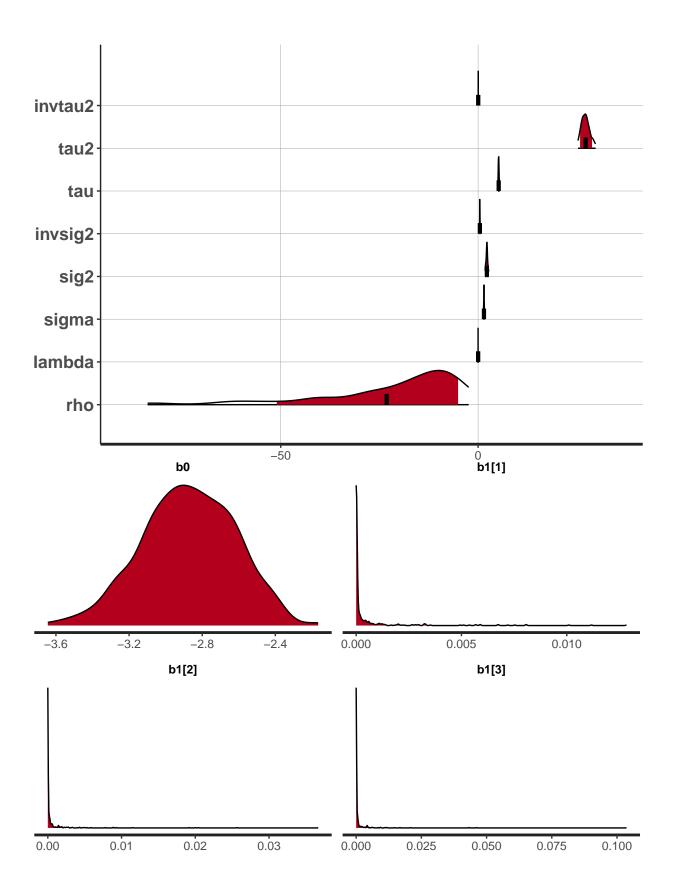
CASES 10.2. LME: Spline con restricciones creciente

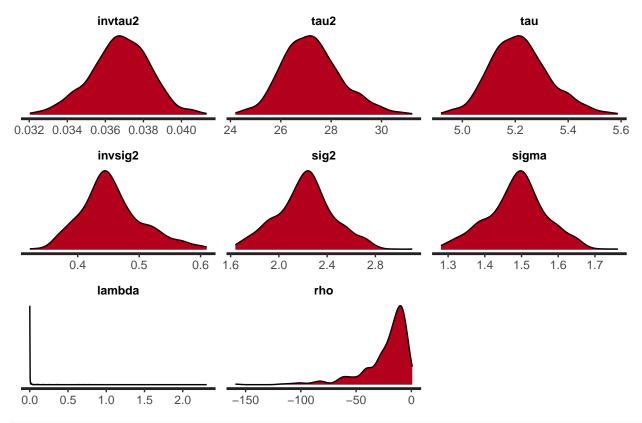
```
idx = names(table(aneur3$ptnum))
id690 = which(aneur3$ptnum==690)
n690 = length(id690)
i690 = which(idx==690)
XI690 = XI1[id690,]
x690 = x1[id690]
id703 = which(aneur3$ptnum==703)
n703 = length(id703)
i703 = which(idx==703)
XI703 = XI1[id703,]
x703 = x1[id703]
id705 = which(aneur3$ptnum==705)
n705 = length(id705)
i705 = which(idx==705)
XI705 = XI1[id705,]
x705 = x1[id705]
id745 = which(aneur3$ptnum==745)
n745 = length(id745)
i745 = which(idx==745)
XI745 = XI1[id745,]
x745 = x1[id745]
id746 = which(aneur3$ptnum==746)
n746 = length(id746)
i746 = which(idx==746)
XI746 = XI1[id746,]
x746 = x1[id746]
id837 = which(aneur3$ptnum==837)
n837 = length(id837)
i837 = which(idx==837)
XI837 = XI1[id837,]
x837 = x1[id837]
datos.lme.add.incr.cases <- list( y = y ,</pre>
                         id = id,
               n = length(y),
               N = N , Ni = Ni,
               k1=k1,
              XI1 = XI1,
              x1 = x1
              zero = rep(0,1+k1),
              S1=S1,
              n690=n690, i690=i690, XI690=XI690, x690=x690,
              n703=n703, i703=i703, XI703=XI703, x703=x703,
              n705=n705, i705=i705, XI705=XI705, x705=x705,
              n745=n745, i745=i745, XI745=XI745, x745=x745,
```

```
n746=n746, i746=i746, XI746=XI746, x746=x746,
              n837=n837, i837=i837, XI837=XI837, x837=x837)
## fit.lme.add.incr.reslope.cases <- stan("jagam_9_aneur_lme_add_incr_reslope_cases_v2.stan",
##
              data=datos.lme.add.incr.cases,
##
               chains=3, warmup=300, iter=600, thin=2, cores=4,
##
               init= inits.lme.add.incr)
print(fit.lme.add.incr.reslope.cases, pars=param.lme.add)
## Inference for Stan model: jagam_9_aneur_lme_add_incr_reslope_cases.
## 3 chains, each with iter=600; warmup=300; thin=2;
## post-warmup draws per chain=150, total post-warmup draws=450.
##
##
                                  2.5%
                                          25%
                                                 50%
                                                       75% 97.5% n eff Rhat
            mean se mean
                             sd
                                -3.38 -3.05 -2.87 -2.69 -2.41
## b0
            -2.88
                    0.01 0.25
                                                                   288 1.01
## b1[1]
            0.00
                    0.00 0.00
                                 0.00
                                        0.00
                                               0.00 0.00 0.01
                                                                   461 1.01
            0.00
                    0.00 0.00
                                 0.00
                                       0.00
                                               0.00 0.00 0.01
## b1[2]
                                                                   474 1.00
## b1[3]
            0.00
                    0.00 0.01
                                 0.00
                                       0.00
                                               0.00 0.00 0.01
                                                                   469 1.00
## invtau2
            0.04
                    0.00 0.00
                                 0.03
                                       0.04
                                               0.04 0.04 0.04
                                                                   353 1.00
## tau2
            27.24
                    0.06 1.17
                                25.32 26.44 27.16 27.93 29.79
                                                                   352 1.00
                                               5.21 5.28 5.46
## tau
            5.22
                    0.01 0.11
                                 5.03
                                       5.14
                                                                   352 1.00
## lambda
            0.01
                    0.01 0.13
                                  0.00
                                        0.00
                                               0.00 0.00 0.09
                                                                   458 1.00
## rho
           -23.21
                    2.62 21.59 -83.63 -29.16 -16.27 -8.93 -2.38
                                                                   68 1.01
            0.46
                    0.00 0.05
                                 0.37
                                        0.42
                                               0.45 0.48 0.57
                                                                   336 1.00
## invsig2
                                        2.07
## sig2
            2.22
                    0.01 0.24
                                  1.75
                                                2.23 2.36 2.71
                                                                   292 1.00
            1.49
                    0.00 0.08
                                 1.32
                                        1.44
                                                1.49 1.54 1.65
                                                                   298 1.00
## sigma
## Samples were drawn using NUTS(diag_e) at Wed Aug 16 11:50:45 2023.
## For each parameter, n_eff is a crude measure of effective sample size,
## and Rhat is the potential scale reduction factor on split chains (at
## convergence, Rhat=1).
stan_trace(fit.lme.add.incr.reslope.cases, pars=param.lme.add)
stan_plot(fit.lme.add.incr.reslope.cases, pars=c("b0","b1"), point_est = "mean", show_density = TRUE)
stan plot(fit.lme.add.incr.reslope.cases, pars=c("invtau2", "tau2", "tau", "invsig2", "sig2", "sigma",
stan_dens(fit.lme.add.incr.reslope.cases, pars=c("b0","b1"))
```

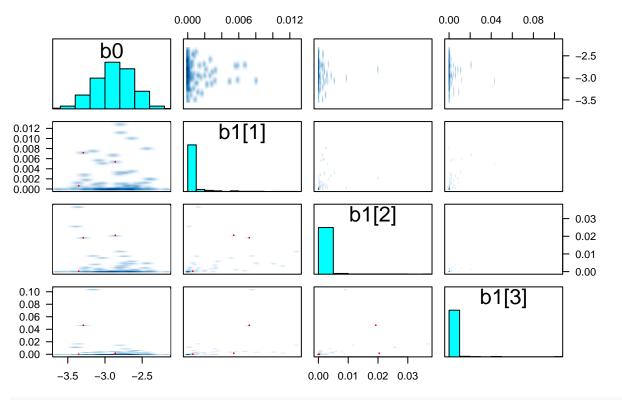
stan_dens(fit.lme.add.incr.reslope.cases, pars=c("invtau2","tau2","tau2", "invsig2", "sig2", "sigma", "lam"



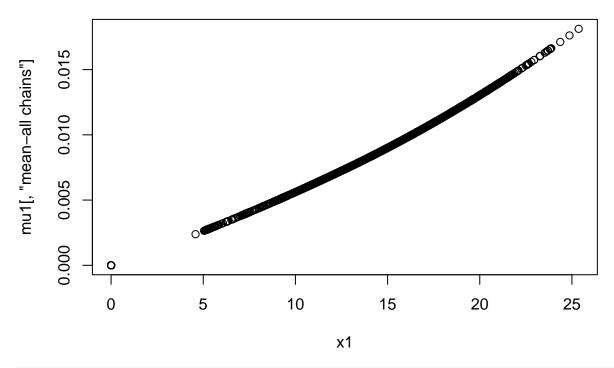




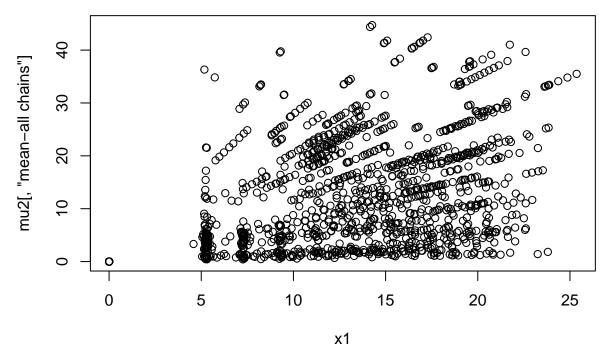
pairs(fit.lme.add.incr.reslope.cases, pars = c("b0","b1"), las = 1)



mu1 = get_posterior_mean(fit.lme.add.incr.reslope.cases,"mu1")
plot(x1,mu1[,"mean-all chains"])



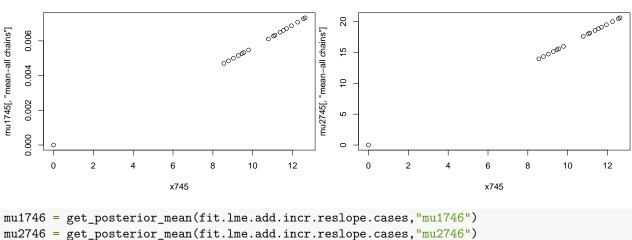
mu2 = get_posterior_mean(fit.lme.add.incr.reslope.cases,"mu2")
plot(x1,mu2[,"mean-all chains"])



```
mu1690 = get_posterior_mean(fit.lme.add.incr.reslope.cases,"mu1690")
mu2690 = get_posterior_mean(fit.lme.add.incr.reslope.cases,"mu2690")

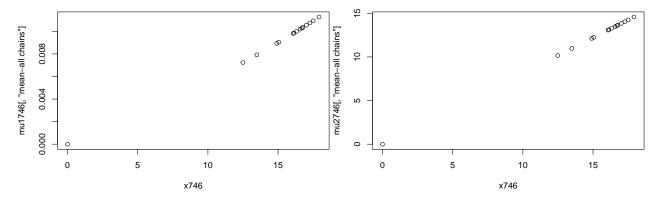
plot(x690,mu1690[,"mean-all chains"])
plot(x690,mu2690[,"mean-all chains"])
```

```
mu1690[, "mean-all chains"]
                                                           mu2690[, "mean-all chains"]
                                                               2.0
                                                                                                        0
                                                               1.5
   0.004
                                                               1.0
   0.002
                                                               0.5
   0.000
                                                               0.0
        0
                2
                                                                    0
                                                                           2
                                                                                                        10
                       4
                                      8
                                            10
                                                   12
                                                                                          6
                                                                                                 8
                                                                                                               12
                               x690
                                                                                          x690
mu1703 = get_posterior_mean(fit.lme.add.incr.reslope.cases,"mu1703")
mu2703 = get_posterior_mean(fit.lme.add.incr.reslope.cases,"mu2703")
plot(x703,mu1703[,"mean-all chains"])
plot(x703,mu2703[,"mean-all chains"])
                                                                                                20
mu1703[, "mean-all chains"]
                                                           mu2703[, "mean-all chains"]
                                                               15
                                                               10
   0.004
                                                               2
   0.000
                                                               0
        0
                      5
                                   10
                                                15
                                                                    0
                                                                                 5
                                                                                                           15
                                                                                              10
                               x703
                                                                                          x703
mu1705 = get_posterior_mean(fit.lme.add.incr.reslope.cases,"mu1705")
mu2705 = get_posterior_mean(fit.lme.add.incr.reslope.cases,"mu2705")
plot(x705,mu1705[,"mean-all chains"])
plot(x705,mu2705[,"mean-all chains"])
                                                                                                           20
   900.0
mu1705[, "mean-all chains"]
                                                           mu2705[, "mean-all chains"]
                                                               15
   0.004
                                                               10
   0.002
                                                               2
   0.000
        0
                2
                                6
                                        8
                                                                            2
                                                                                           6
                                               10
                                                       12
                                                                    0
                                                                                                   8
                                                                                                           10
                                                                                                                  12
                               x705
                                                                                          x705
mu1745 = get_posterior_mean(fit.lme.add.incr.reslope.cases,"mu1745")
mu2745 = get_posterior_mean(fit.lme.add.incr.reslope.cases,"mu2745")
plot(x745,mu1745[,"mean-all chains"])
plot(x745,mu2745[,"mean-all chains"])
```



```
mu1746 = get_posterior_mean(fit.lme.add.incr.reslope.cases,"mu1746")
mu2746 = get_posterior_mean(fit.lme.add.incr.reslope.cases,"mu2746")

plot(x746,mu1746[,"mean-all chains"])
plot(x746,mu2746[,"mean-all chains"])
```



```
mu1837 = get_posterior_mean(fit.lme.add.incr.reslope.cases,"mu1837")
mu2837 = get_posterior_mean(fit.lme.add.incr.reslope.cases,"mu2837")

plot(x837,mu1837[,"mean-all chains"])
plot(x837,mu2837[,"mean-all chains"])
```

