

Unsupervised Anomaly Detection for Intricate KPIs via Adversarial Training of VAE

Wenxiao Chen, Haowen Xu, Zeyan Li, Dan Pei,
Jie Chen, Honglin Qiao, Yang Feng, Zhaogang Wang

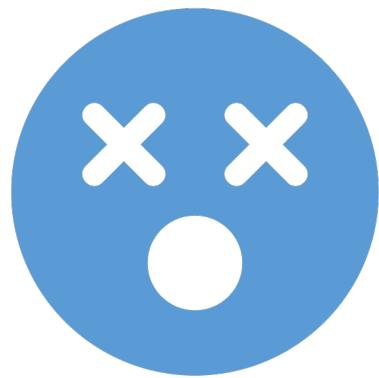


Tsinghua University

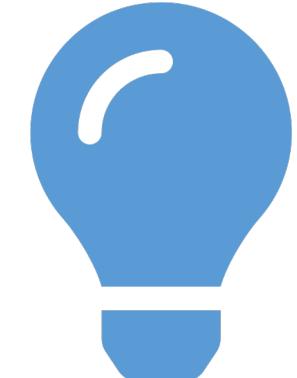




Background



Challenges



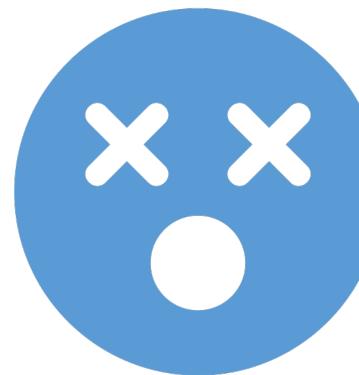
Ideas



Experiments



Background



Challenges



Ideas

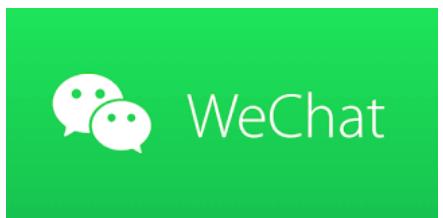


Experiments

Key Performance Indicators



Google



amazon.com



Fig1: Web Applications

Key Performance Indicators

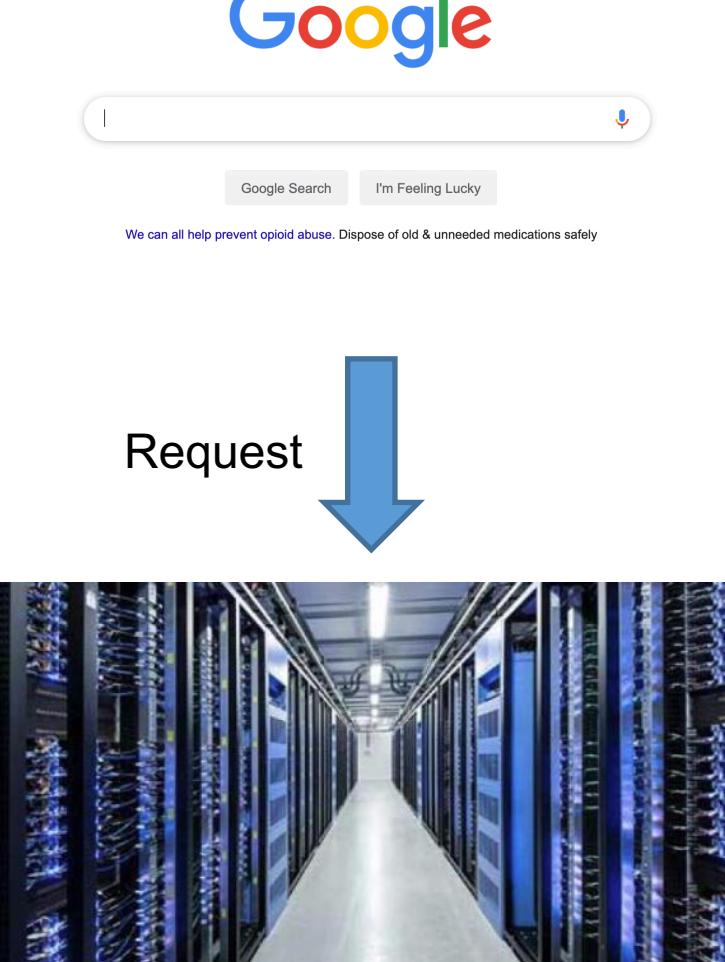


Fig2: From user to server

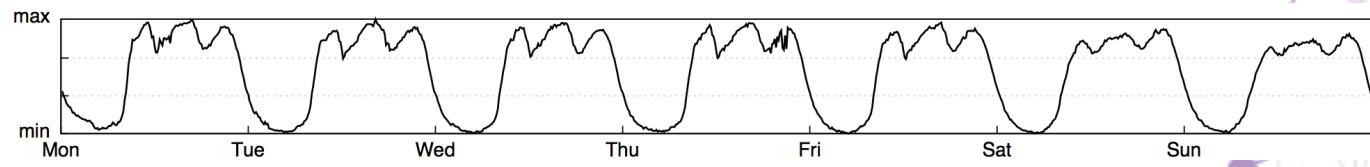


Fig3: Page view



Monitor

It is stable?



Key Performance Indicators

Smooth KPIs: e.g, The respond time of server, and page view

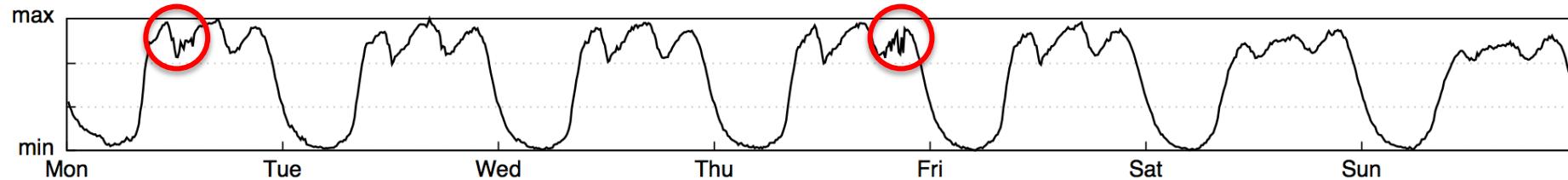


Fig4: An example of Anomalies in page view

Intricate KPIs: e.g, The query per second and transaction per second

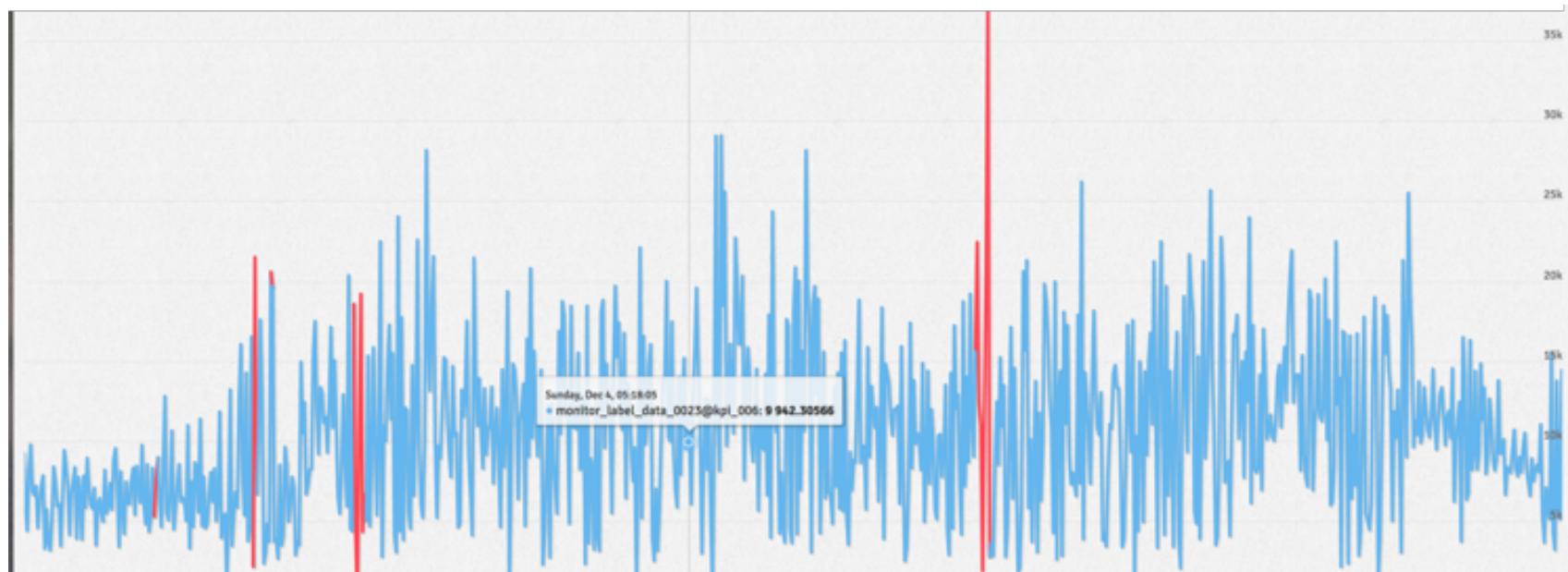


Fig5: An example of Anomalies in database

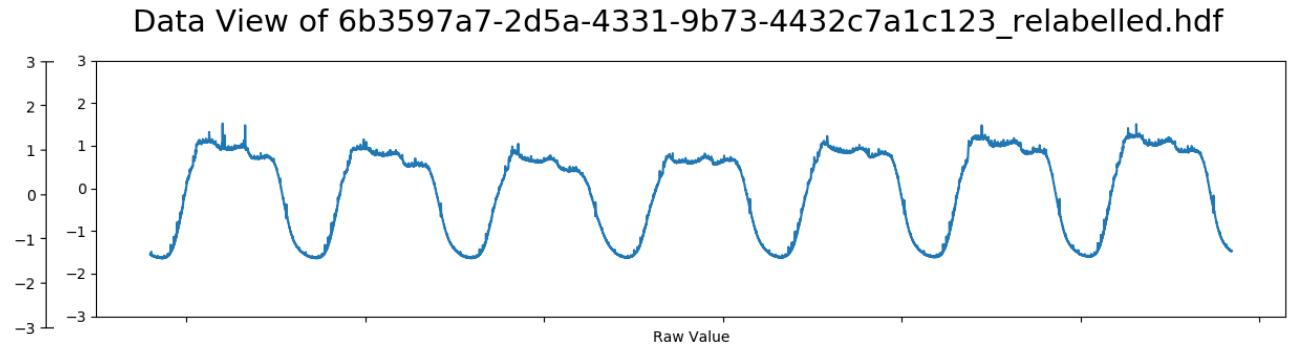
Existing Method

- Statistical
 - Anomaly detectors based on traditional statistical models [INFOCOM2012]
- Supervised
 - Supervised ensemble learning with above detectors – Opprentice[IMC2015]
- Unsupervised
 - Unsupervised anomaly detection based on VAE – Donut [WWW2018]

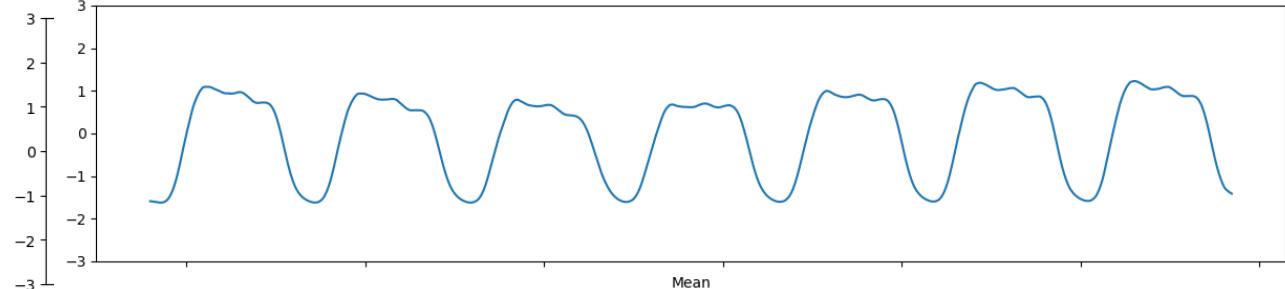
They can only work
on **smooth** KPIs.

Smooth KPIs

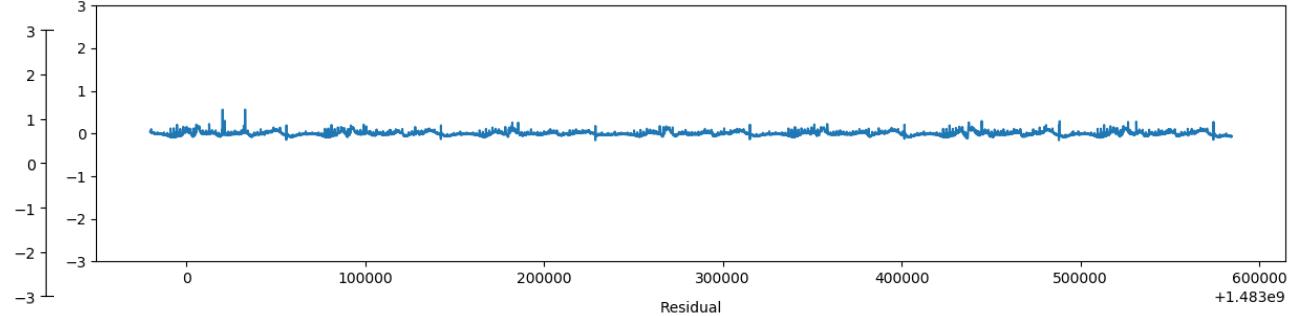
Original data



Smooth Curve



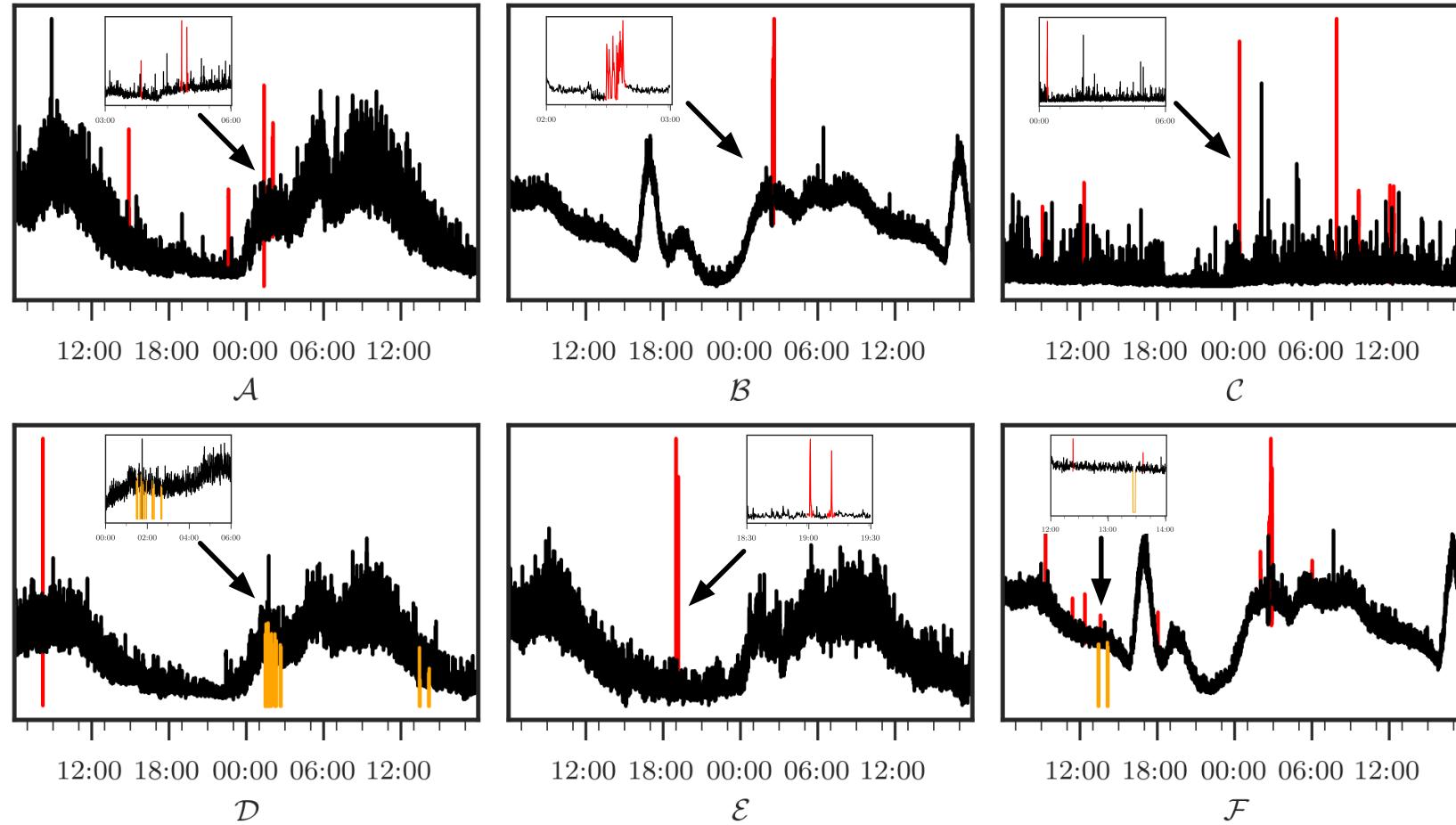
Gaussian Noise



Time of 2016-12-29 10:51:00 to 2017-01-05 10:50:00
Time of 2017-04-02 00:00:00 to 2017-04-08 23:59:50

Fig6: Smooth KPI

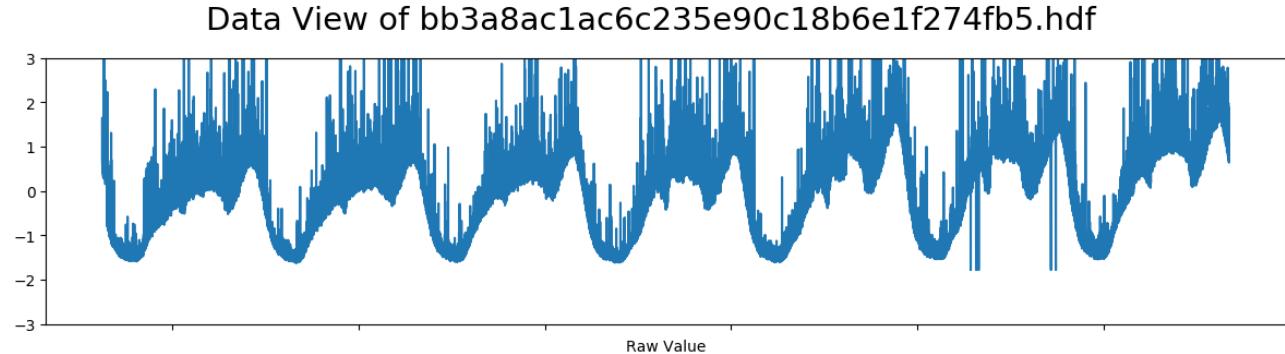
Intricate KPIs



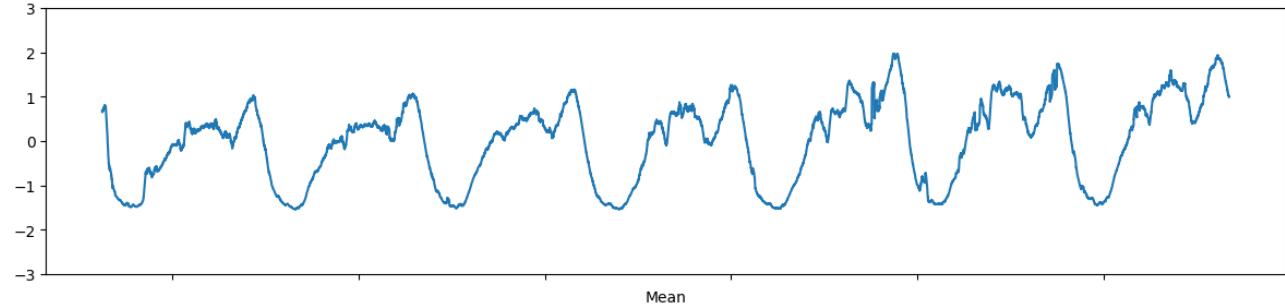
- micro-congestion
- fine granularity
- prevalent and important (e.g, database, server)
- little studied

Intricate KPIs

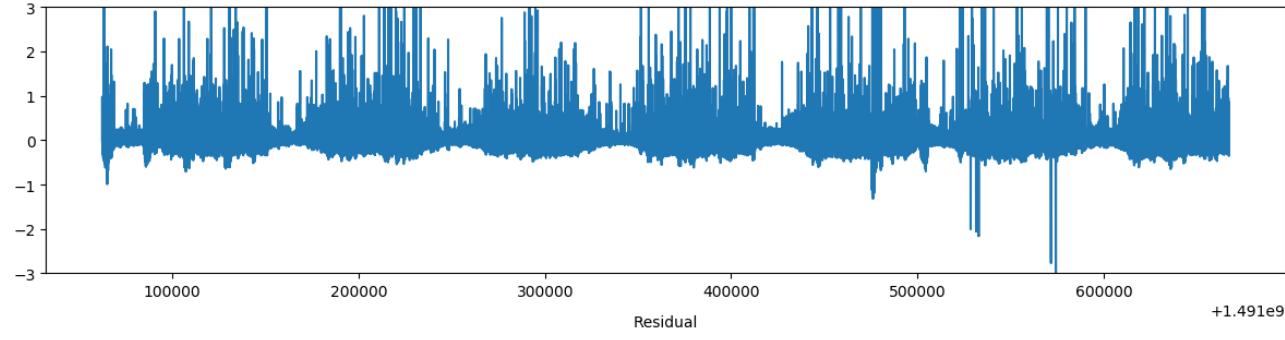
Original data



Smooth Curve



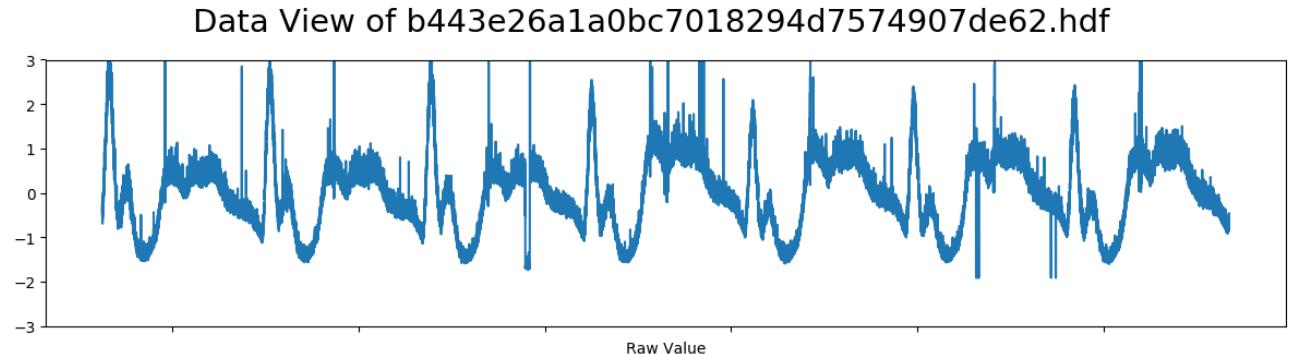
Noise



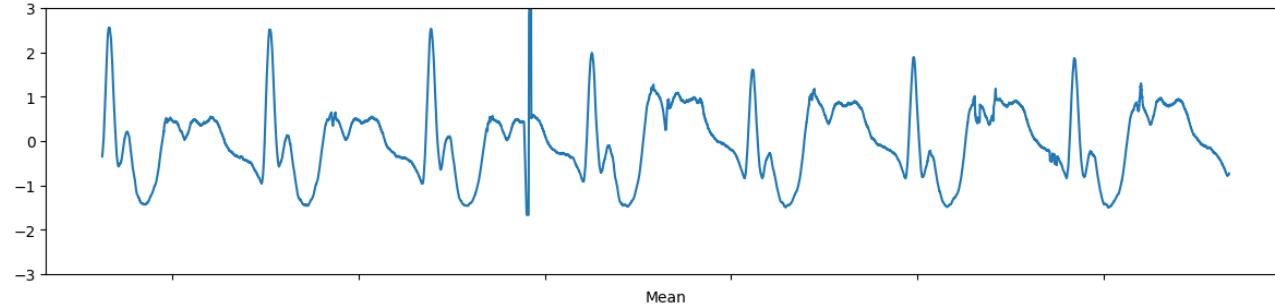
- non-Gaussian noises
- hard to model

Intricate KPIs

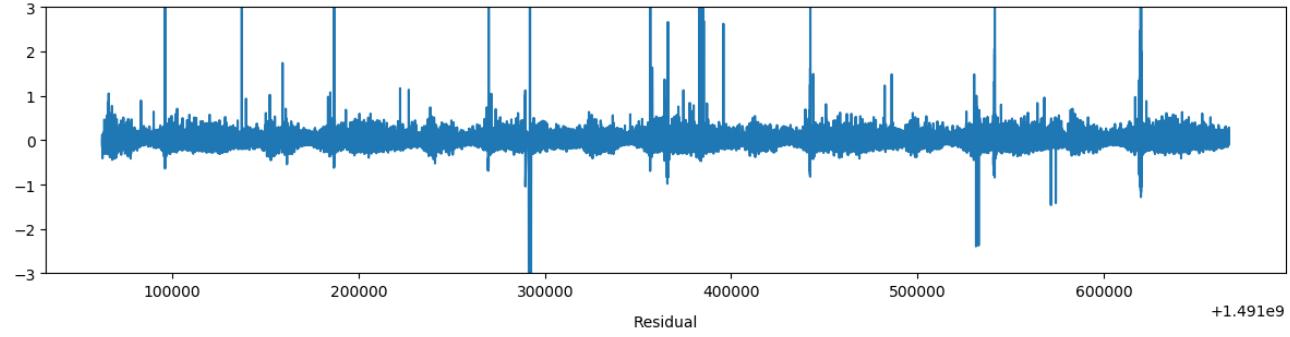
Original data



Smooth Curve



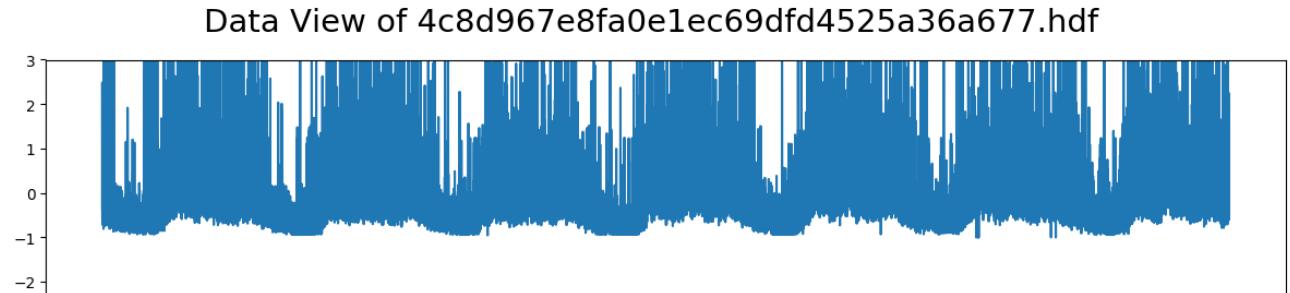
Noise



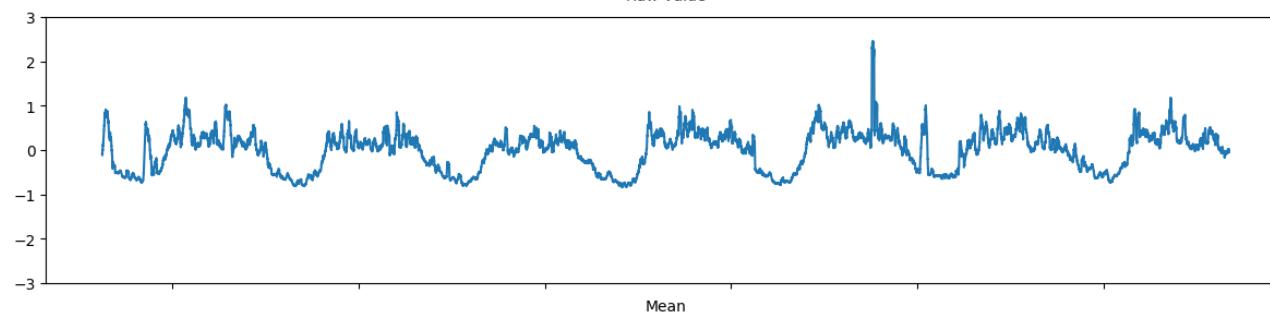
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Intricate KPIs

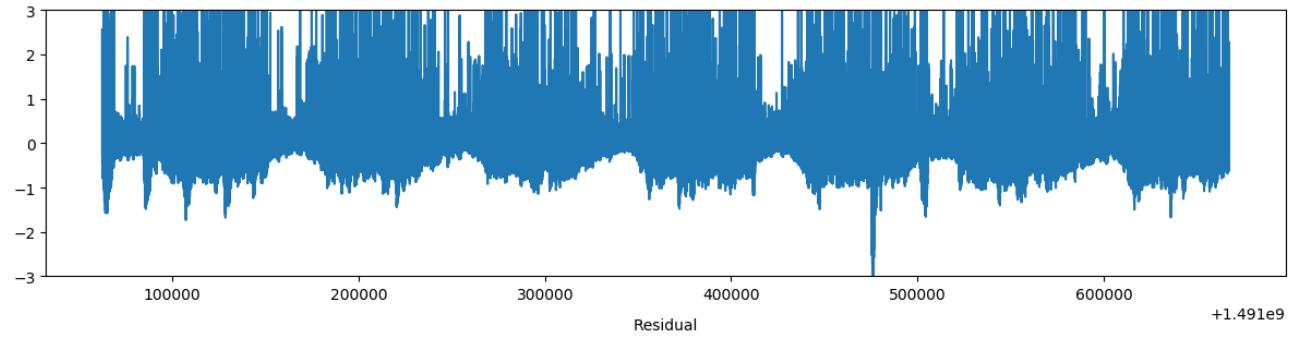
Original data



Smooth Curve



Noise



- non-Gaussian noises
- hard to model

Donut

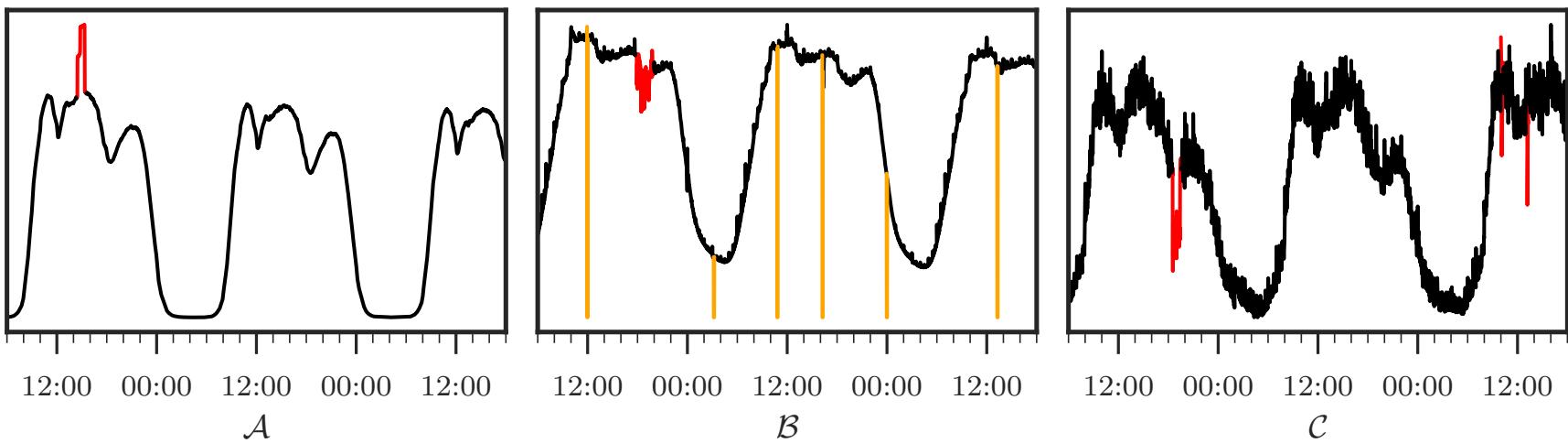


Fig11: The Dataset of Donut

Donut

- A recent future of W data points at time t is called a window at time t. Donut tries to model the distribution of normal windows by VAE(Variational Auto Encoder) and find anomalies by likelihood.
- The training objective of VAE, is the evidence lower bound of likelihood(ELBO).

$$\mathcal{L}_{vae} = \mathbb{E}_{p(\mathbf{x})} \left[\mathbb{E}_{q_{\phi}(\mathbf{z}|\mathbf{x})} [\log p_{\theta}(\mathbf{x}|\mathbf{z})] - \text{KL} [q_{\phi}(\mathbf{z}|\mathbf{x}) \parallel p_{\theta}(\mathbf{z})] \right]$$

- In Donut, $p_{\theta}(\mathbf{x}|\mathbf{z})$ is diagonal multivariate gaussian distribution and it works well on seasonal smooth KPIs.

Donut

- Element-wise posterior:
 - $\ln p_{\theta}(x|z) = \sum_i \ln p_{\theta}(x_i|z)$
- It is useful for smooth KPIs but not for Intricate KPIs.



Out of Expectation

- Donut assumes that the data is seasonal smooth with diagonal gaussian noise but the intricate KPIs are not.
- VAE will only learn the mean and variance locally.

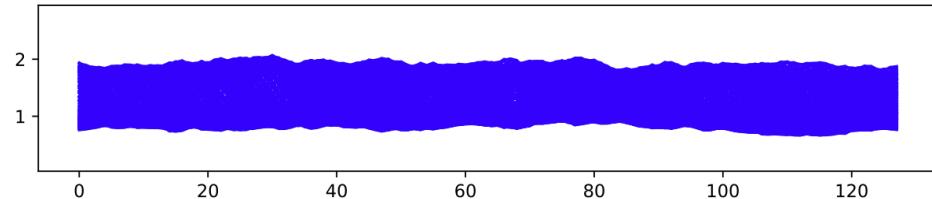


Fig12: Reconstructed element-wise gaussian distribution

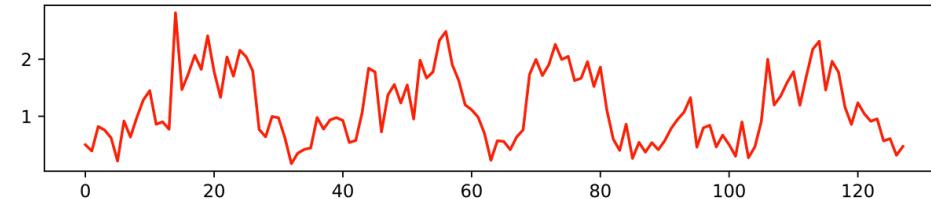


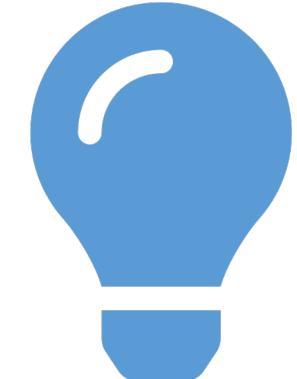
Fig13: Original curve



Background



Challenges



Ideas

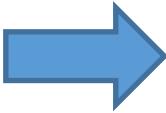


Experiments

Challenges



Dataset is too intricate
for VAE to learn



Element-wise gaussian
posterior is not appropriate



Reconstruction loss is too
hard to learn

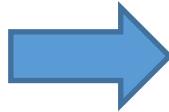


The limit of training method

Challenges



Dataset is too intricate
for VAE to learn



Element-wise gaussian
posterior is not appropriate



Reconstruction loss is too
hard to learn

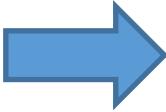


The limit of training method

Challenges



Dataset is too intricate
for VAE to learn



Element-wise gaussian
posterior is not appropriate



Reconstruction loss is too
hard to learn



The limit of training method

Challenges

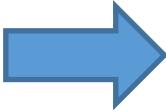
$$\mathcal{L}_{vae} = \mathbb{E}_{p(\mathbf{x})} \left[\mathbb{E}_{q_\phi(\mathbf{z}|\mathbf{x})} [\log p_\theta(\mathbf{x}|\mathbf{z})] - \text{KL} [q_\phi(\mathbf{z}|\mathbf{x}) \parallel p_\theta(\mathbf{z})] \right]$$

- $\mathbb{E}_{p(\mathbf{x})} \left[\mathbb{E}_{q_\phi(\mathbf{z}|\mathbf{x})} [\log p_\theta(\mathbf{x}|\mathbf{z})] \right]$ is called reconstruction loss.
- ELBO is a trade-off and when the reconstruction loss is hard to learn (nearly no gradient from it), our model tends to learn another term.

Challenges



Dataset is too intricate
for VAE to learn



Element-wise gaussian
posterior is not appropriate



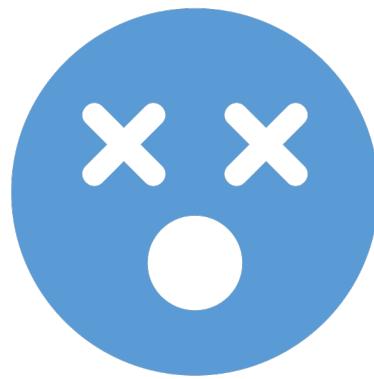
Reconstruction loss is too
hard to learn



The limit of training method



Background



Challenges



Ideas

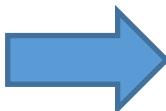


Experiments

Ideas



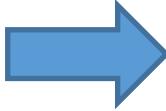
Element-wise gaussian posterior is not appropriate



Choose another posterior which is not element-wise



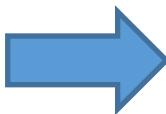
Reconstruction loss is too hard to learn



Relax the constraint of reconstruction loss



The limit of training method



Use adversarial training

Ideas



Choose another posterior
which is not element-wise

- $p_\theta(x|z) = \frac{1}{Z(\lambda)} e^{-\lambda \|x - G(z)\|}$
- $G(z)$ is the generative network and λ is a learnable variable.
- $Z(\lambda)$ can be simply calculated when λ is fixed.
- It is easy to check that it is not element-wise.

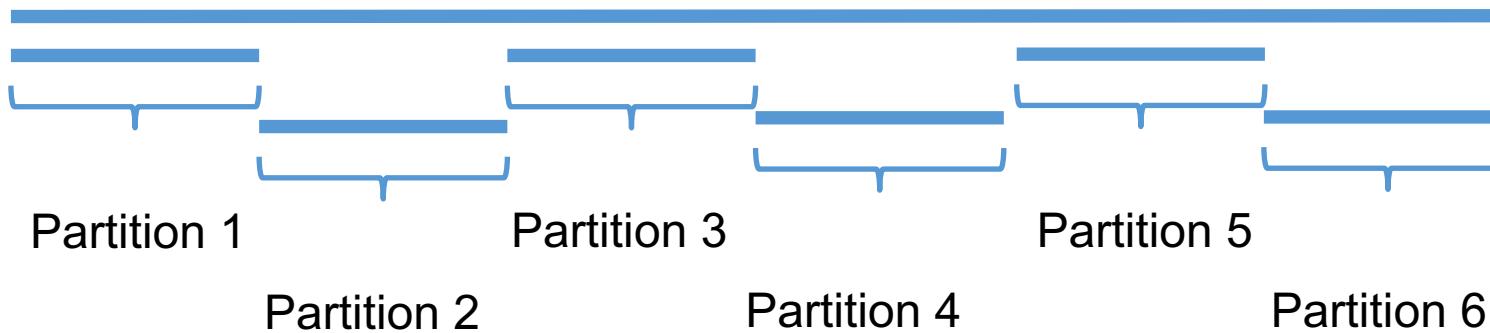


Ideas



Relax the constraint of reconstruction loss

- Introduce a new notion: Partition
- Divide the whole KPI into several partitions, whose length are all L



Throw away
the redundant

Partition and Window

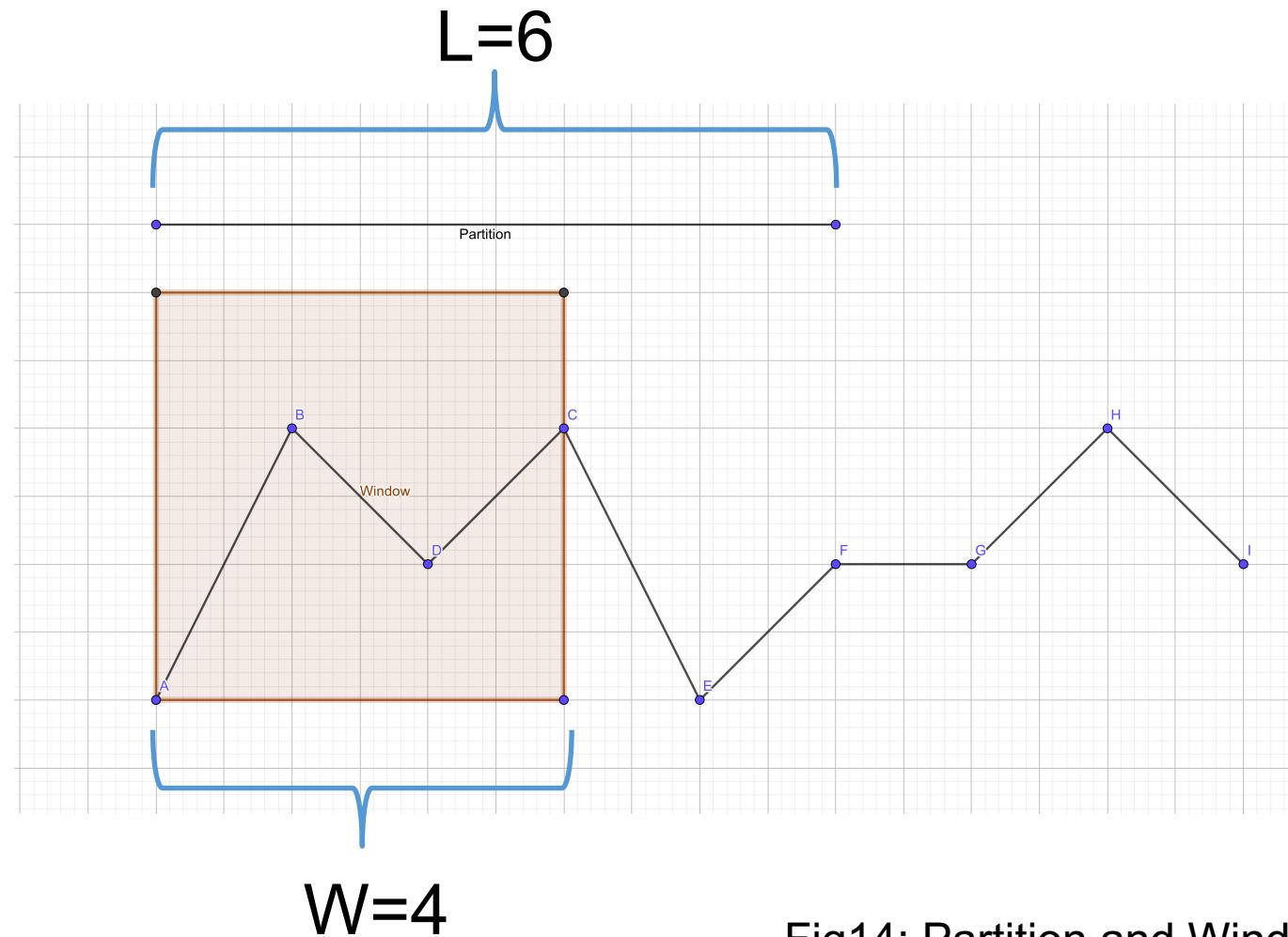


Fig14: Partition and Window

Window 1

Partition and Window

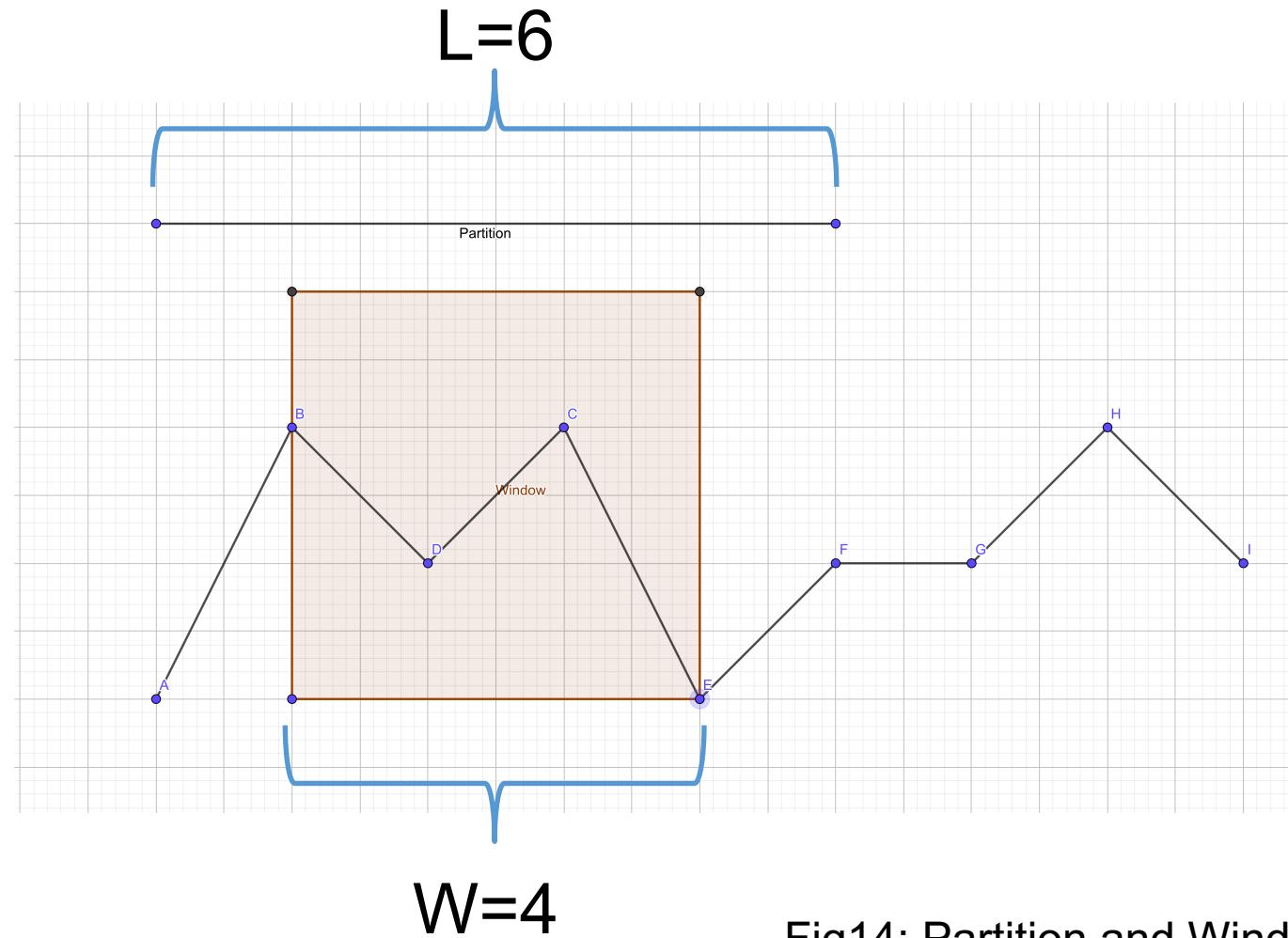
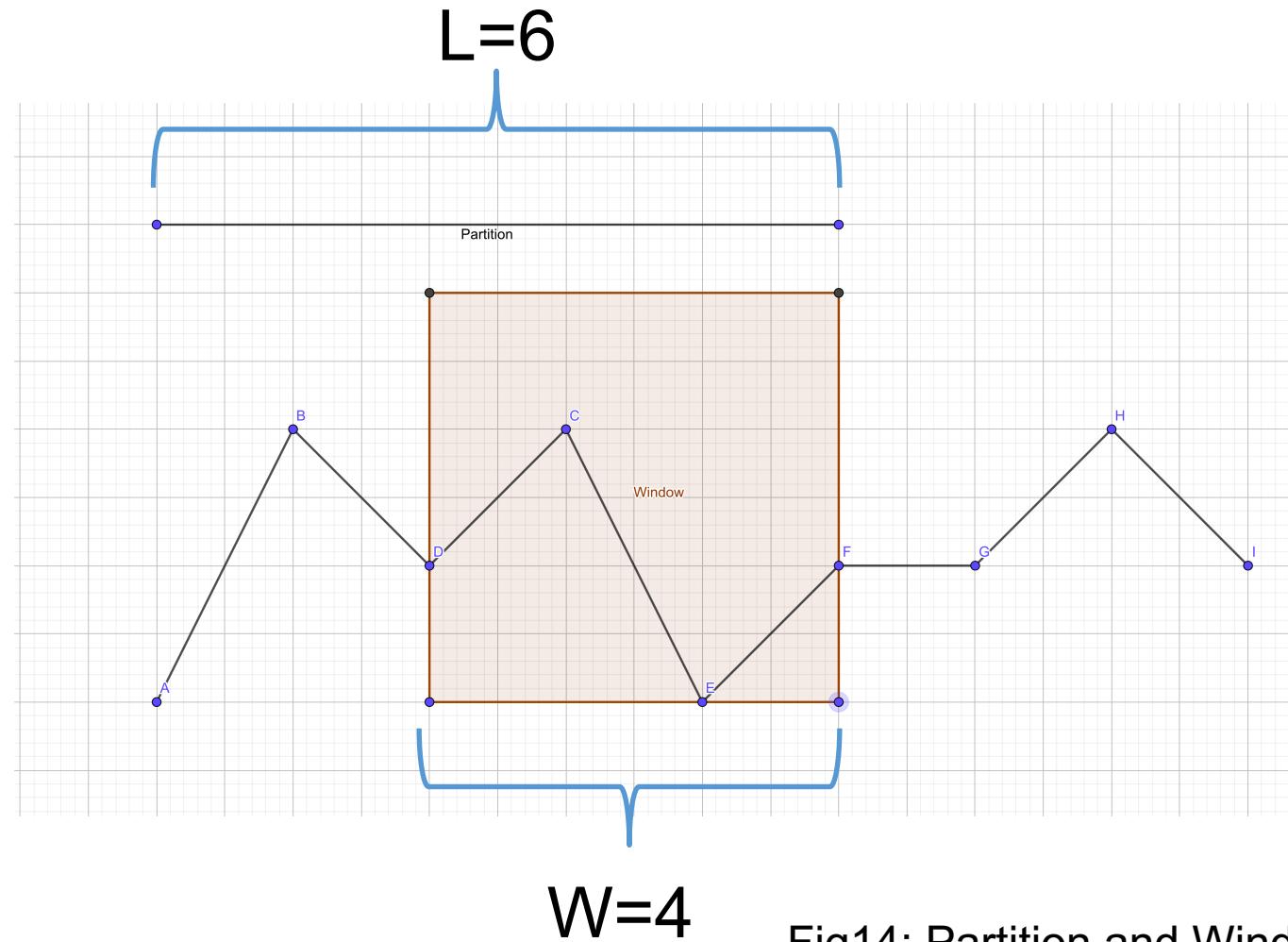


Fig14: Partition and Window

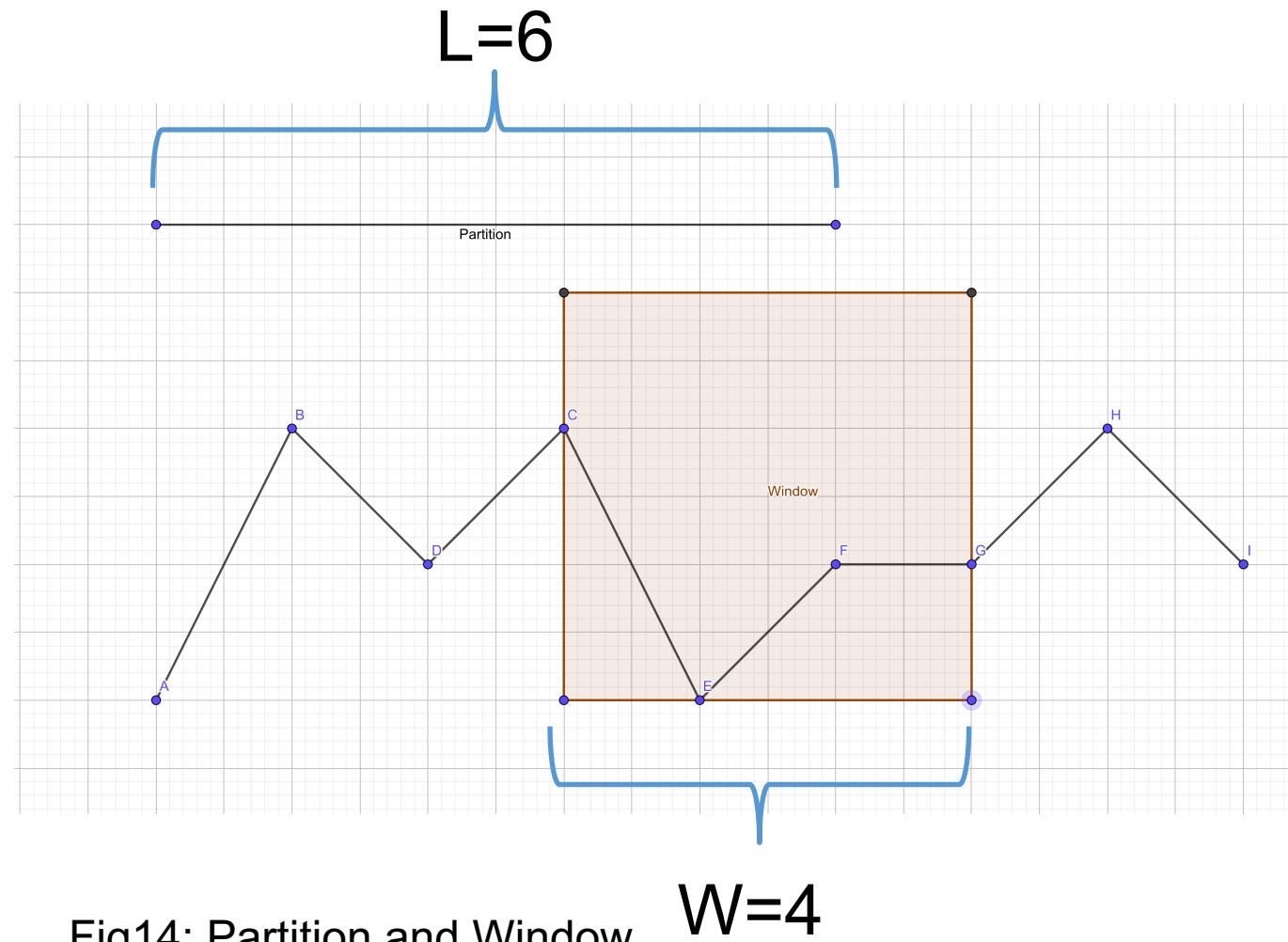
Window 2

Partition and Window



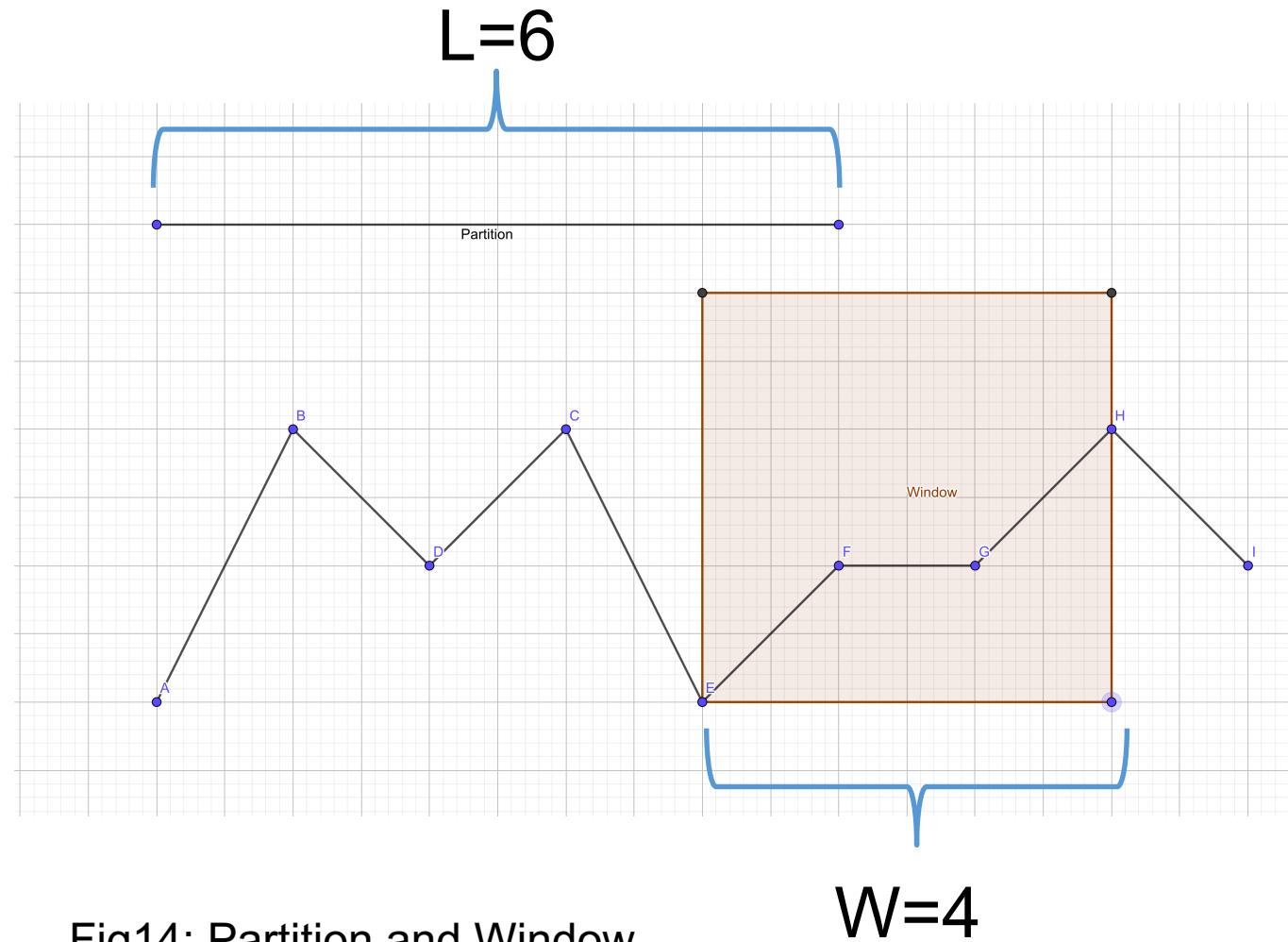
Window 3

Partition and Window



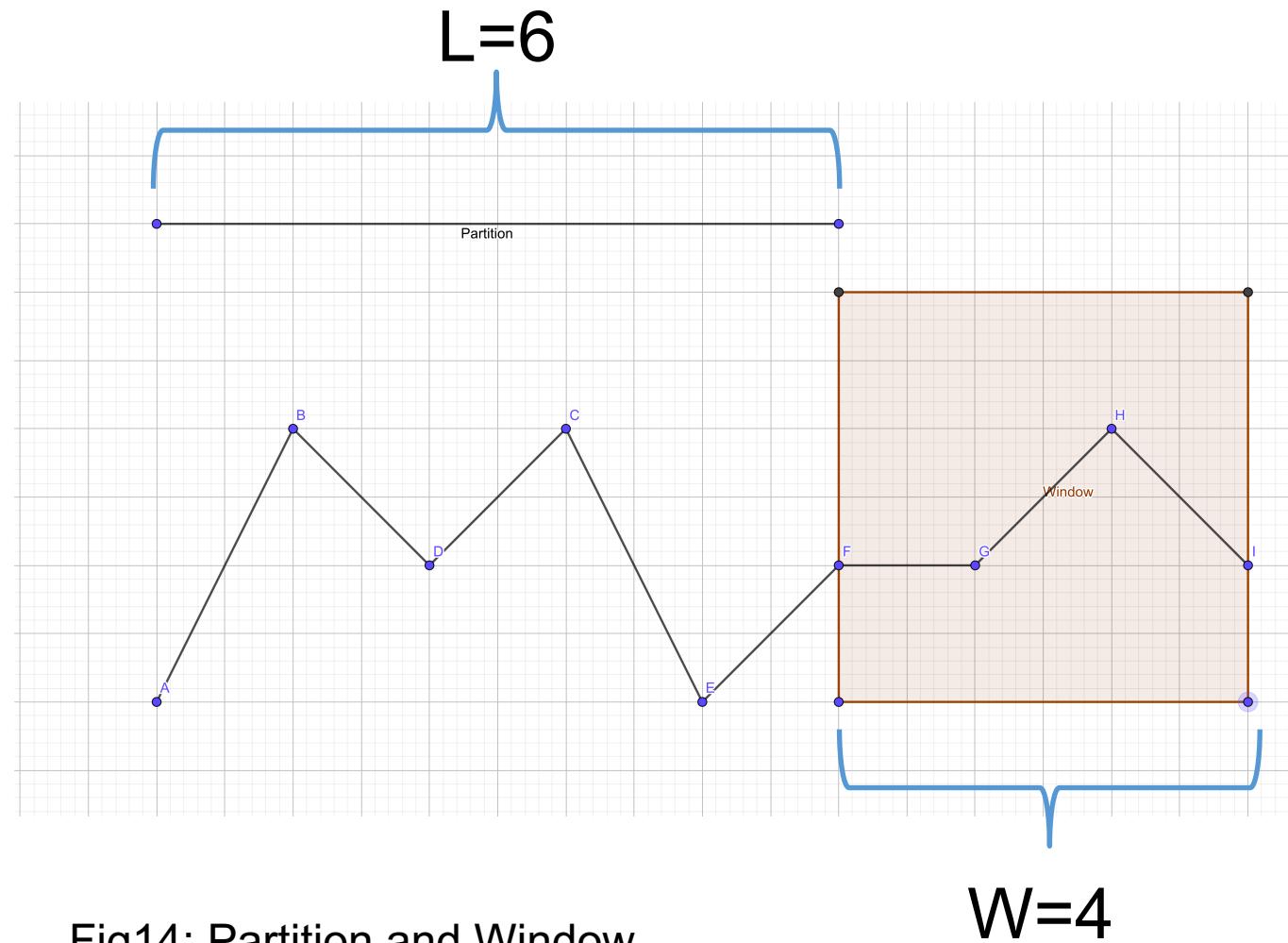
Window 4

Partition and Window



Window 5

Partition and Window

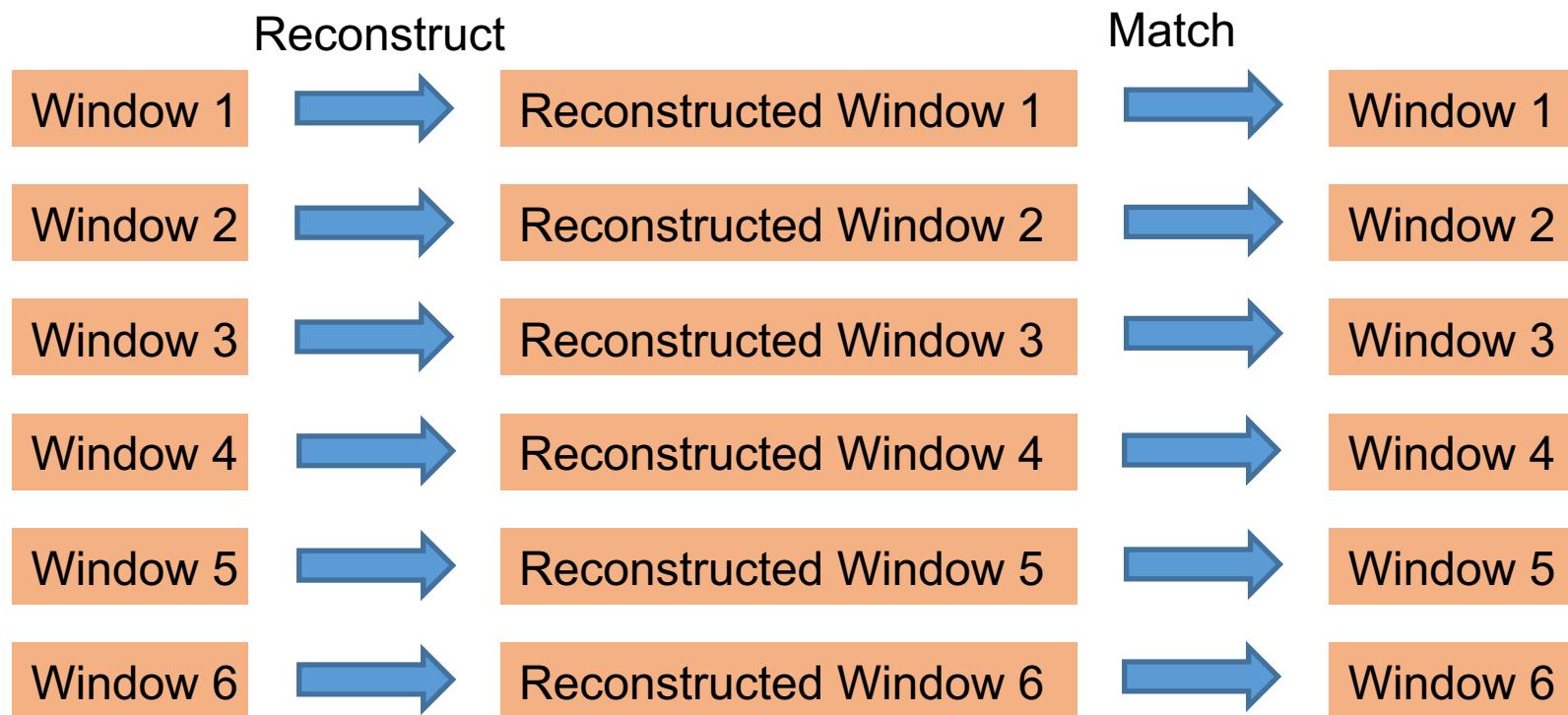


Window 6



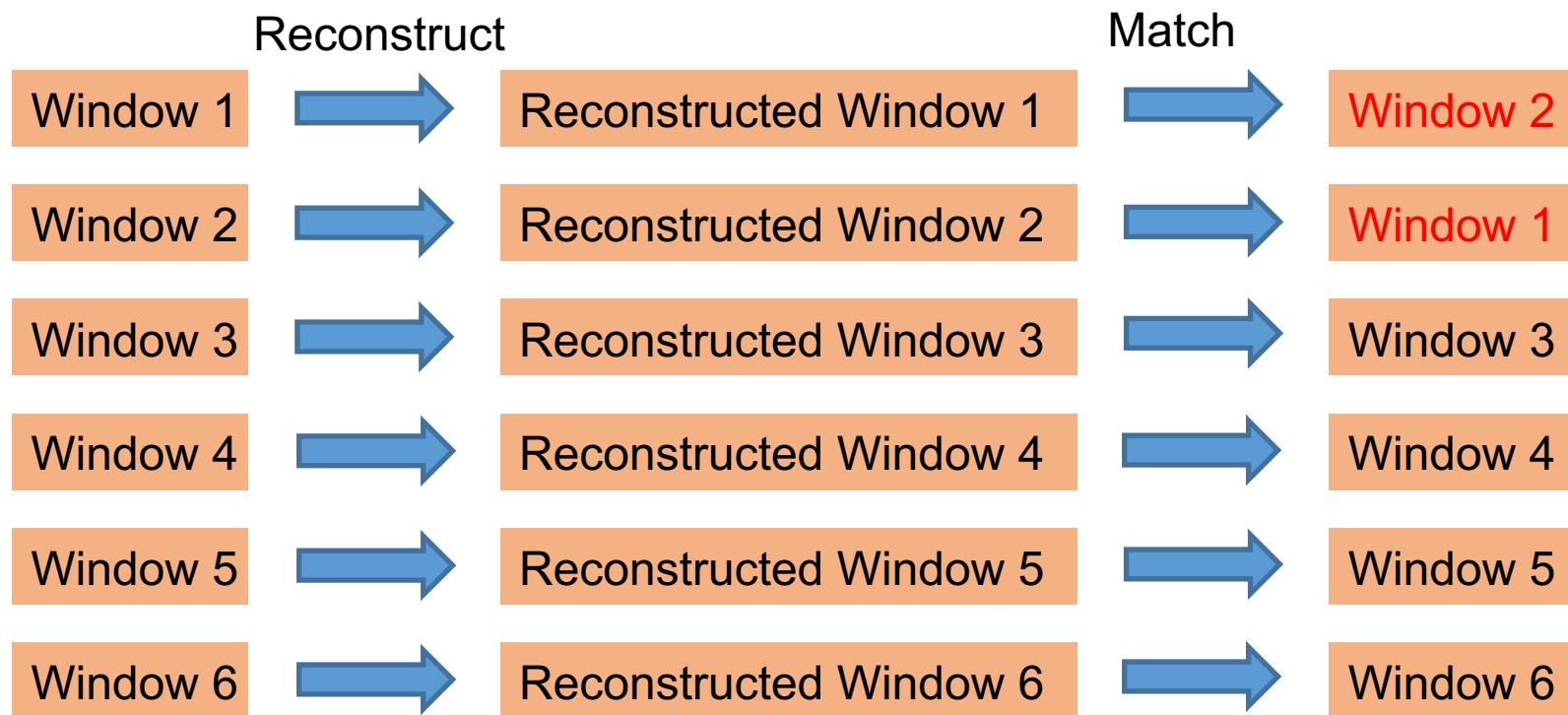
Match

- In a partition, we regard the reconstruction loss as distance between reconstructed window and original window.



Match

- We relax the reconstruction loss by following way: we permit each reconstructed window to **match** one window in this partition and compute the sum of the distance between each pair.



Whole Process

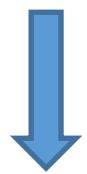
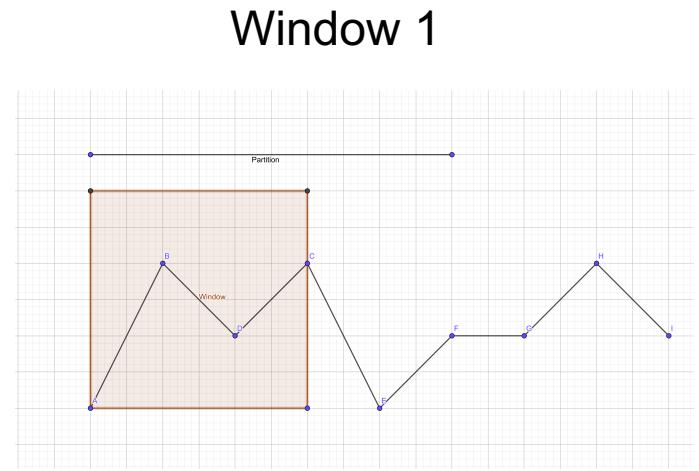
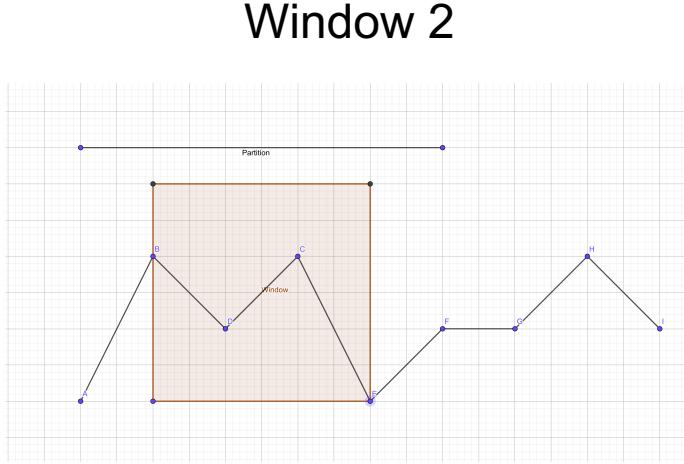
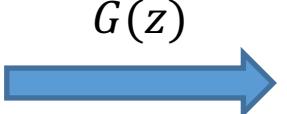
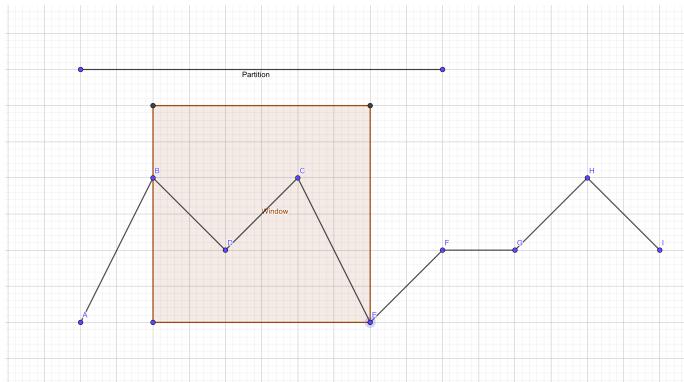

$$q_\varphi(z|x)$$
**Match**

Fig15: Reconstruction and Match

Reconstructed window 1

Relationship

- It is easy to see that **match reconstruction loss** is less than reconstruction loss (just trivial match).
- Reconstruction loss is the special case: $L=1$
- Understand it intuitively: L is our tolerance. We tolerate some errors of reconstruction.



Use adversarial training

- A **generative adversarial network (GAN)** is a class of machine learning systems. Two neural networks contest with each other in a zero-sum game framework.
- It works very well in image generation.

Wasserstein distance

- **Wasserstein distance** used by WGAN[ICML2017].

$$\begin{aligned} W^1[P(\mathbf{x}|w)\|P_G(\mathbf{y}|w)] &= \inf_{\gamma \in \Gamma_w} \int_{\mathcal{X} \times \mathcal{X}} \|\mathbf{x} - \mathbf{y}\| d\gamma(\mathbf{x}, \mathbf{y}) \\ &= \sup_{Lip(f) \leq 1} \left\{ \int_{\mathcal{X}} f(\mathbf{x}) p(\mathbf{x}|w) d\mathbf{x} - \int_{\mathcal{X}} f(\mathbf{y}) p_G(\mathbf{y}|w) d\mathbf{y} \right\} \end{aligned}$$

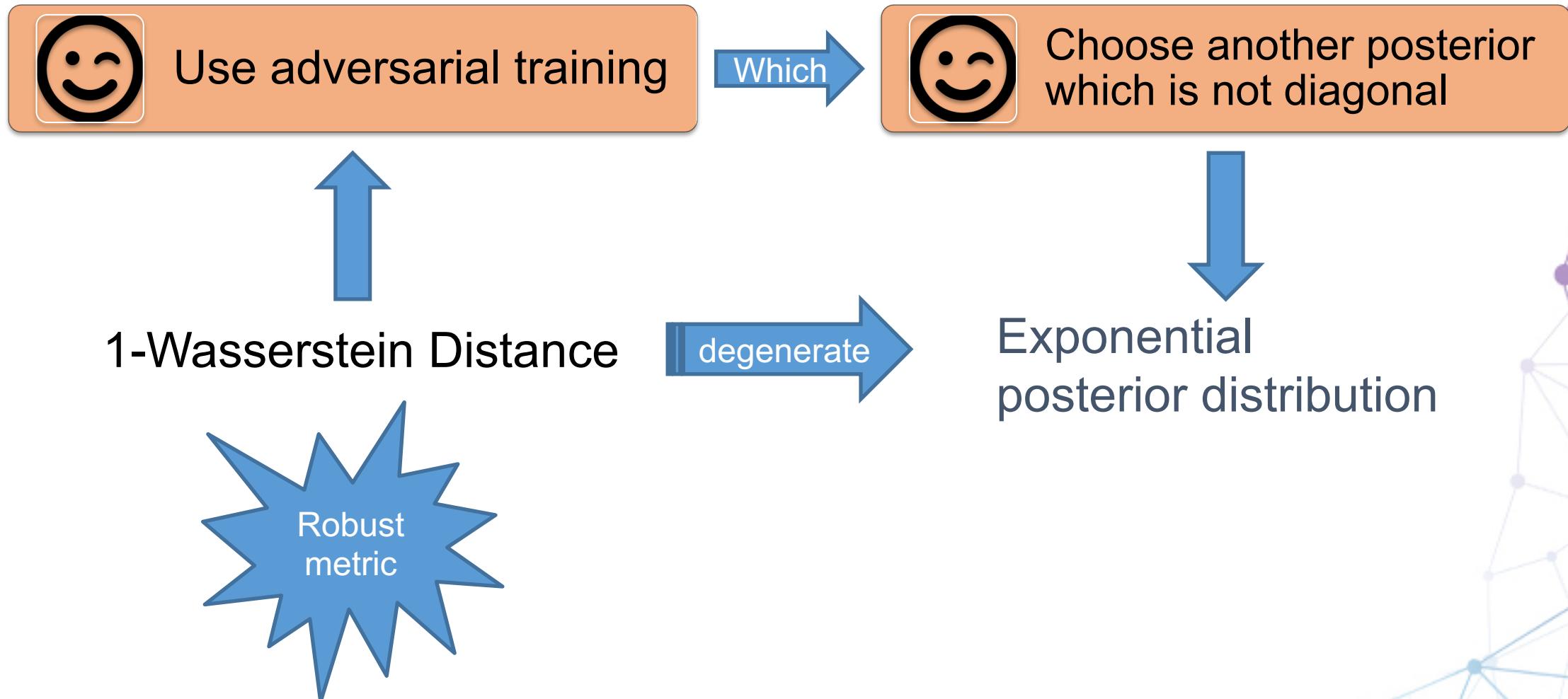
- $P(\mathbf{x}|w)$ is the distribution of windows in Partition ω
- $P_G(\mathbf{y}|w)$ is the distribution of reconstructed windows in Partition ω
- γ represents the matches

Training

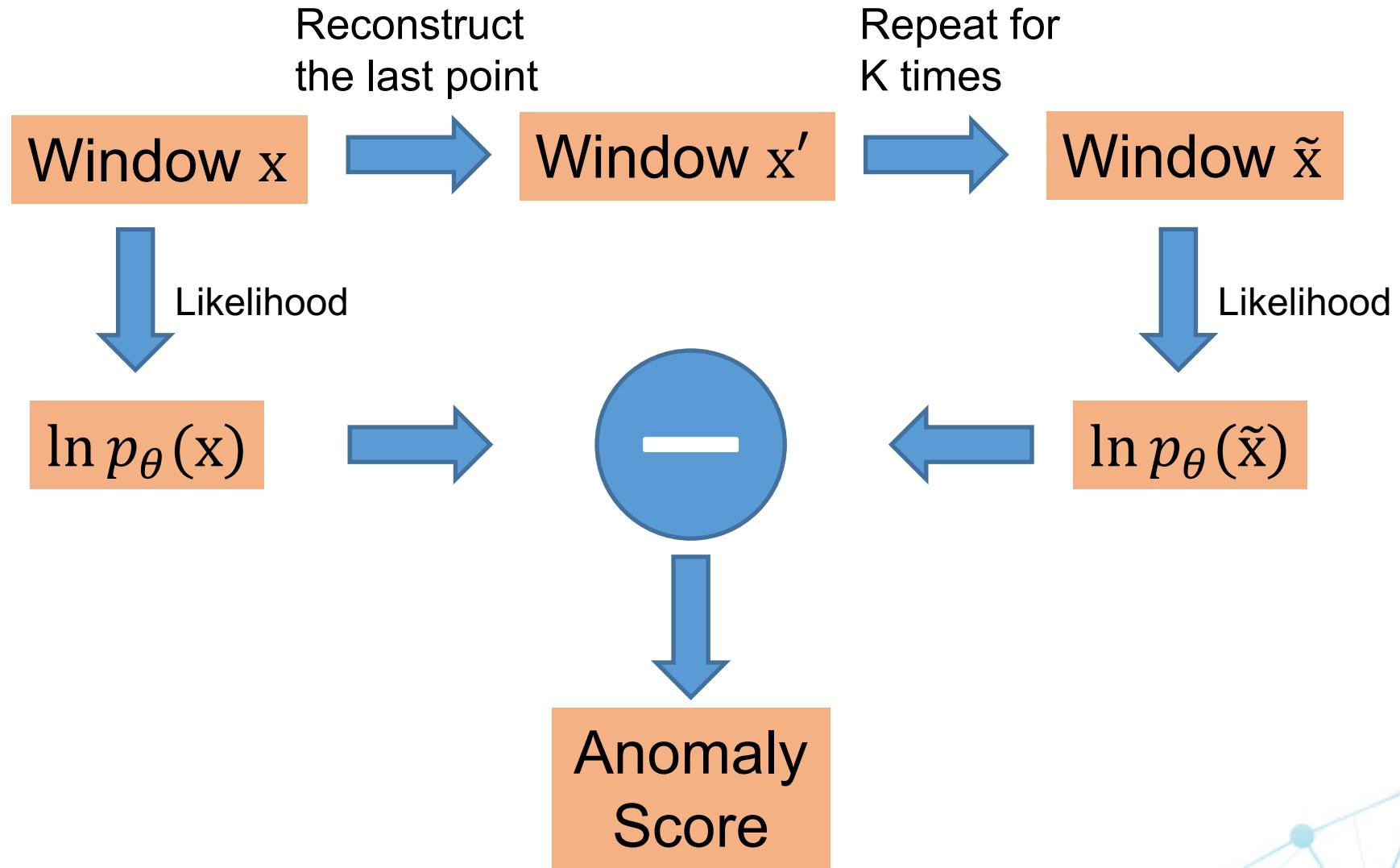
$$\begin{aligned} W^1[P(\mathbf{x}|w)\|P_G(\mathbf{y}|w)] &= \inf_{\gamma \in \Gamma_w} \int_{\mathcal{X} \times \mathcal{X}} \|\mathbf{x} - \mathbf{y}\| d\gamma(\mathbf{x}, \mathbf{y}) \\ &= \sup_{Lip(f) \leq 1} \left\{ \int_{\mathcal{X}} f(\mathbf{x}) p(\mathbf{x}|w) d\mathbf{x} - \int_{\mathcal{X}} f(\mathbf{y}) p_G(\mathbf{y}|w) d\mathbf{y} \right\} \end{aligned}$$

- We train another network $D(\mathbf{x})$ to find the optimal f above, with a penalty on the gradient norm for random samples (WGAN-GP[NIPS2017]).
- Decrease the size of each partition during training.
- We complete an adversarial training algorithm of VAE.

Review

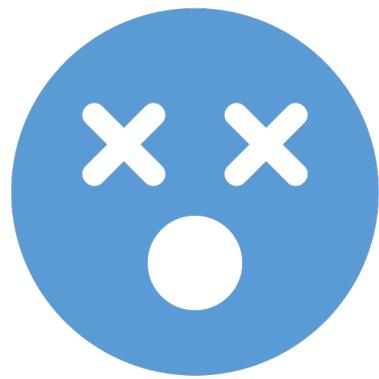


Detection





Background



Challenges



Ideas



Experiments

Experiments

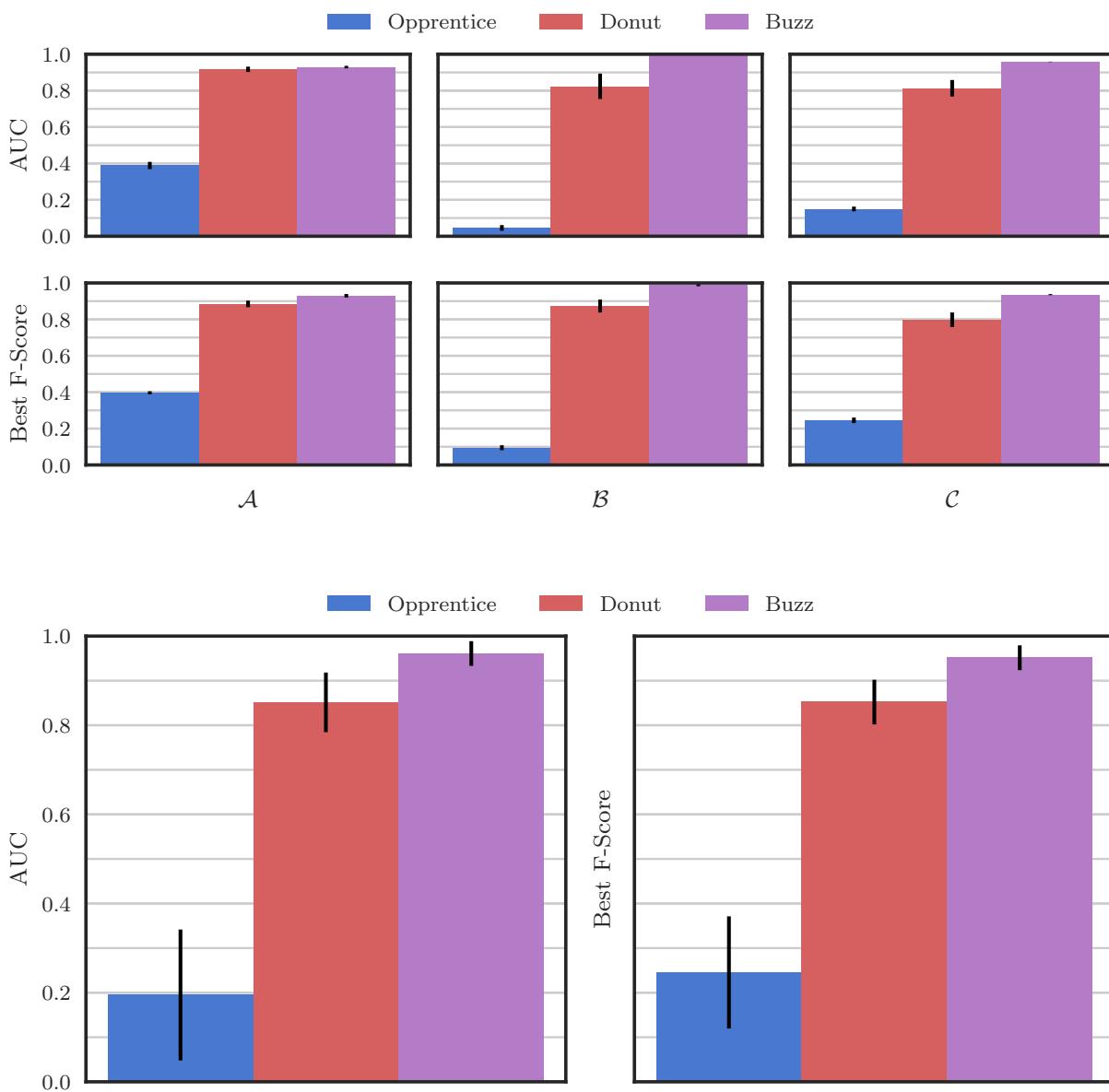


Fig16: Performance

Experiments

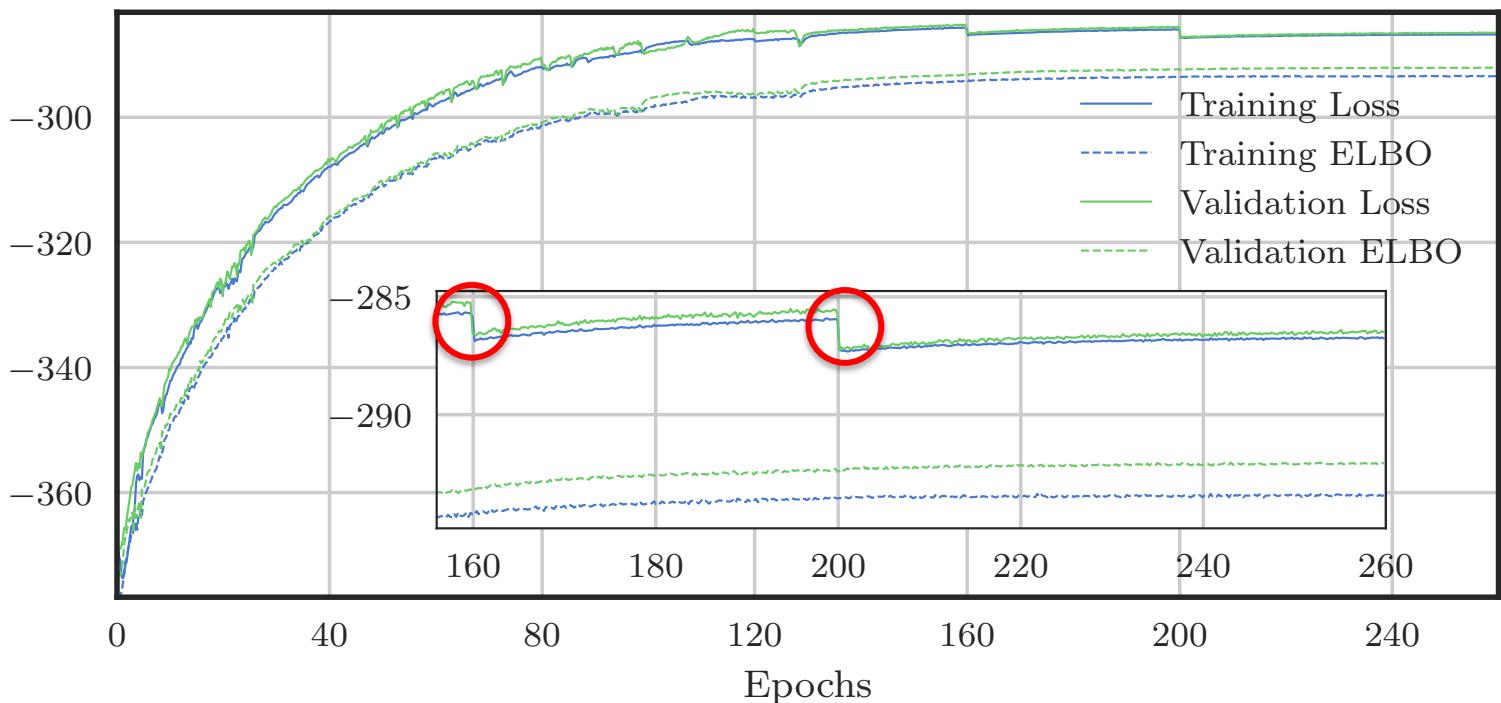


Fig17: Loss and ELBO

The fact that ELBO increases during the training, indicates that our model maximizes the ELBO indeed.

Conclusion

- The first unsupervised anomaly detection algorithm via deep generative model on intricate KPIs
- The first adversarial training method for VAE, based on partitions analysis
- Our deduction build the bridge between VAE and Wasserstein Distance



Thank you

Q&A