

Problem 2 (a)

$N = 4 : H H A A$

$$\mathbb{P}(N = 4) = \underbrace{p_H^2 p_A^2}_{\text{east1 wins 4 games}} + \underbrace{(1 - p_H)^2 (1 - p_A)^2}_{\text{east8 wins 4 games}}$$

$N = 5 : H H A A H$

$$\begin{aligned} \mathbb{P}(N = 5) = & \underbrace{\binom{2}{1} (1 - p_H) p_H^2 p_A^2}_{\text{east1 loses 1 Home}} + \underbrace{\binom{2}{1} (1 - p_A) p_H^3 p_A}_{\text{east1 loses 1 Away}} \\ & + \underbrace{\binom{2}{1} p_H (1 - p_H)^2 (1 - p_A)^2}_{\text{east8 loses 1 Home}} + \underbrace{\binom{2}{1} p_A (1 - p_H)^3 (1 - p_A)}_{\text{east8 loses 1 Away}} \end{aligned}$$

$N = 6 : H H A A H A$

$$\begin{aligned} \mathbb{P}(N = 6) = & \underbrace{\binom{3}{2} (1 - p_H)^2 p_H p_A^3}_{\text{east1 loses 2 Home}} + \underbrace{(1 - p_A)^2 p_H^3 p_A}_{\text{east1 loses 2 Away}} + \underbrace{\binom{3}{1} \binom{2}{1} (1 - p_H) (1 - p_A) p_H^2 p_A^2}_{\text{east1 loses 1 Home 1 Away}} \\ & + \underbrace{\binom{3}{2} p_H^2 (1 - p_H) (1 - p_A)^3}_{\text{east8 loses 2 Home}} + \underbrace{p_A^2 (1 - p_H)^3 (1 - p_A)}_{\text{east8 loses 2 Away}} \\ & + \underbrace{\binom{3}{1} \binom{2}{1} p_H p_A (1 - p_H)^2 (1 - p_A)^2}_{\text{east8 loses 1 Home 1 Away}} \end{aligned}$$

$N = 7 : H H A A H A H$

$$\begin{aligned} \mathbb{P}(N = 7) = & \underbrace{(1 - p_H)^3 p_H p_A^3}_{\text{east1 loses 3 Home}} + \underbrace{(1 - p_A)^3 p_H^4}_{\text{east1 loses 3 Away}} \\ & + \underbrace{\binom{3}{1} \binom{3}{1} (1 - p_H)^2 (1 - p_A) p_H^2 p_A^2}_{\text{east1 loses 2 Home 1 Away}} + \underbrace{\binom{3}{1} \binom{3}{1} (1 - p_H) (1 - p_A)^2 p_H^3 p_A}_{\text{east1 loses 1 Home 2 Away}} \\ & + \underbrace{p_H^3 (1 - p_H) (1 - p_A)^3}_{\text{east8 loses 3 Home}} + \underbrace{p_A^3 (1 - p_H)^4}_{\text{east8 loses 3 Away}} \\ & + \underbrace{\binom{3}{1} \binom{3}{1} p_H^2 p_A (1 - p_H)^2 (1 - p_A)^2}_{\text{east8 loses 2 Home 1 Away}} + \underbrace{\binom{3}{1} \binom{3}{1} p_H p_A^2 (1 - p_H)^3 (1 - p_A)}_{\text{east8 loses 1 Home 2 Away}} \end{aligned}$$