

# NBA Hackathon Problem 1

Chia-Wei Hsu, Zeyu Li

August 4, 2017

(a)

## Approach 1: Exact answer

```
no_closs <- function(win){
  ans <- choose((win + 1), (82 - win) ) * 0.8^win * 0.2^(82 - win)

  return(ans)
}
### Probability of no 2 consecutive losses
x <- sum(sapply(41:82, no_closs))
x
## [1] 0.05881686
```

The exact probability that the Warriors would never lose consecutive games at any point during an 82-game season is as follows,

$$\sum_{x=41}^{82} \binom{x+1}{82-x} 0.8^x 0.2^{82-x}$$

Above sum is approximately 0.0588169.

## Approach 2: Simulation

Below code chunk is the function that repeats n times of simulating 900 samples of 82-game seasons.

```
season_simulation <- function(n = 1000) {
  # simulate 900 82-game seasons
  sample <- 900
  # create a container for storing experiment outcomes
  container <- matrix(NA, ncol = sample, nrow = n)

  for(j in 1:n){
    for(i in 1:sample){
      # set-up
      sample.space <- c(0,1) # win -- 1; loss -- 0
      theta <- 0.8 # Warriors have 80% chance of winning each game
      N <- 82 # 82 games
```

```

# Similar to biased coin flips
flips <- rbinom(n = N, size = 1, prob = theta)
# next check for consecutive losses (consecutive 0s)
r0 <- rle(flips) # list running lengths
x <- r0$length[r0$values == 0] # count running length of 0s
boo <- sum(x != 1) == 0 # consecutive occurrence of 0 or not;
# FALSE : there are consecutive loss in a simulated 82-game season
# TRUE : there are no consecutive loss in a simulated 82-game season
container[j,i] <- boo
}
}

return(container)
}

```

Repeat the process for 1000 times.

```

# (a)
set.seed(123456789) # set starting point
sim <- season_simulation(n = 1000)
y <- rowSums(sim)/ncol(sim) # Prob(no consecutive losses)
p <- mean(y)
se <- sd(y)/sqrt(900)
p
## [1] 0.05891111
se
## [1] 0.0002582845

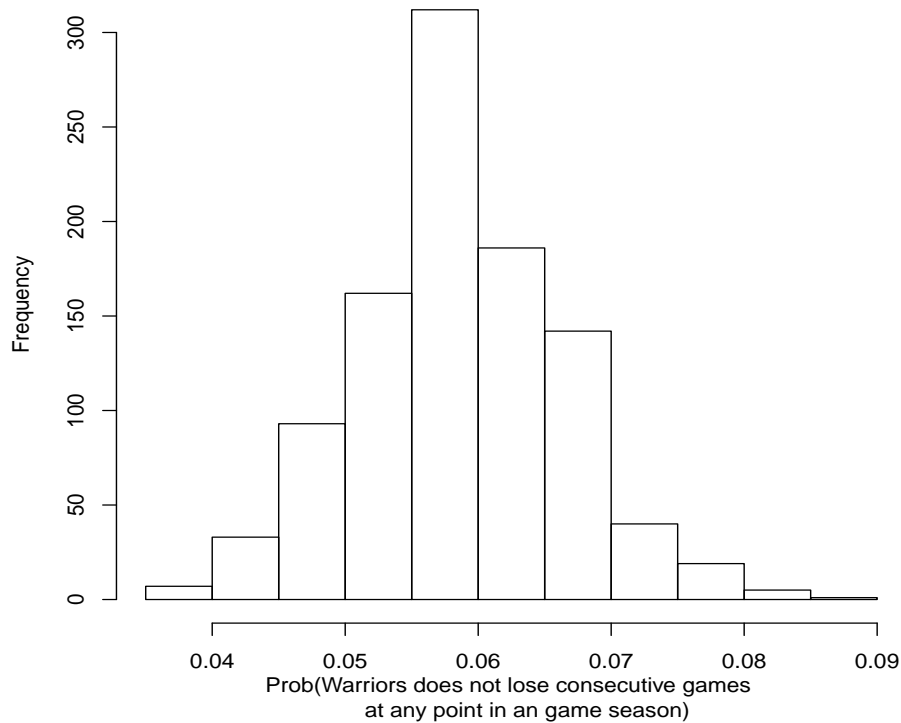
```

```

hist(y,
     main = "Histogram of the simulated probabilities",
     xlab = "Prob(Warriors does not lose consecutive games
             at any point in an game season)")

```

**Histogram of the simulated probabilities**



```
# 95% confidence interval
upp <- p + 1.96 * se
low <- p - 1.96 * se
upp_per <- upp*100
low_per <- low*100
```

(Note: code for simulation see separate attached file). We build a simulator that simulates many 82-game seasons. Each 82-game season is binomially distributed with a success probability of 0.8 ( $p = 0.8$ ) and a failure probability of 0.2 ( $q = 1 - p = 0.2$ ). We draw random samples of size 900 from the binomial distribution and count the number of samples where the Warriors does not lose consecutive games at any point in a given 82-game season. This way we obtain an approximated probability. We repeat this process  $n$  times (we choose  $n$  to be 1000 to ensure that law of large numbers applies). After repeating for 1000 times, we obtain an averaged probability of 0.0589111 and a standard error (variability) of  $2.582845 \times 10^{-4}$ . We are 95% confidence that the true probability lies within the interval (0.0584049, 0.0594173).

**(b)**

The null hypothesis is that the Warriors would never lose consecutive games at any point during an 82-game season, that is  $P(\text{no consecutive losses}) = 100\%$ . From above simulations, we can calculate a 95% confidence interval, which is (5.8404873%, 5.9417349%). Since it does not contain 100%, we reject the null hypothesis.

**(c)**

```

# (c)
# At least game win percentage
least_per <- function(percentage){
  ans <- 0
  for(i in 41 :82){
    ans <- ans + choose((i + 1), (82 - i) ) * percentage^i *
      (1-percentage)^(82-i)
  }
  ans - 0.5
}
z <- uniroot(least_per,c(0,1))
z <- z$root
z_per <- z*100
### At least winning percentage
#0.903776165, this is tested by a lot of numbers to get different answer from
#the uniroot function

```

This question is easy to derive from the exact solution in the form presented in (a). The answer is calculated to be 90.3772241%.