

## 第一题

1.

$$\pi_{O.ordno, C.city, A.city}(\sigma_{O.cid=C.cid \wedge O.aid=A.aid \wedge C.city \neq A.city}(C \times A \times O))$$

2.

$$\pi_{C.cname}(C) - \pi_{C.cname}(\sigma_{O.ordyear > 2022 \wedge O.cid=C.cid}(C \times O))$$

3.

$$\pi_{O.aid, C.city}(\pi_{cid, O.aid, O.ordno}(O) \bowtie \pi_{cid, C.city}(C)) \div \pi_{C.city}(C)$$

不用除法的表示为：

$$\text{令 } T := \pi_{cid, O.aid, O.ordno}(O) \bowtie \pi_{cid, C.city}(C)$$

$$\pi_{O.aid}(T) - \pi_{O.aid}(\pi_{cid, O.aid}(T) \times \pi_{city}(C) - \pi_{cid, O.aid, C.city}(T))$$

4.

$$\pi_{A.aid, C.city, C.cname}((C \bowtie \pi_{O.aid, O.cid, O.ordno}(O) \bowtie A)) \div \pi_{C.cname}(\sigma_{city=r\_city}(C))$$

5.

不用除法：

$$D := \pi_{cid, dis}(C)$$

$$\pi_{C.cid}(C) - \pi_{C.cid}(\sigma_{C.dis > D.dis}(\pi_{C.dis, C.cid}(C) \times D))$$

用除法

$$D \div (\pi_{C.dis}(C) - \pi_{C.dis}(\pi_{C.cid, C.dis}(C) \bowtie_{C.dis > D.dis} D)) \text{ (被除数是在找最低的dis)}$$

## 第二题

1.

$$\pi_{sno, sname}((\sigma_{dept='计算机系'}(C) \bowtie L) \bowtie \pi_{sno, sname}(S))$$

2.

$$\pi_{sno, sname}((L \bowtie C - L \bowtie (\sigma_{cname='数据库'}(C))) \bowtie \pi_{sno, sname}(S))$$

3.

$$\pi_{sno, sname}(\sigma_{score \geq 60}((\pi_{sno, cno}(L) \div \pi_{cno}(\sigma_{dept='计算机系' \wedge opt='必修'}(C))) \bowtie L) \bowtie S)$$

4.

$$(\pi_{sno, sname}(S) - \pi_{sno, sname}(\sigma_{opt='必修'}(L \bowtie (\sigma_{grade=2019}(S) \bowtie C)))) \cup (\sigma_{opt='必修' \wedge score < 60}(L \bowtie (\sigma_{grade=2019}(S) \bowtie C)))$$

5.

$$T := \pi_{L.sno, L.cno, L.score}(S \bowtie L)$$

$$\pi_{sno, sname}(S) \bowtie (\pi_{sno}(L) - \pi_{sno}(\sigma_{L.cno=T.cno \wedge L.score < T.score}(\pi_{L.sno, L.cno, L.score}(S \bowtie L) \times T)))$$