#### Problem Set 4, 10/11/2017

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# Section 10.10 Problem 1

#### Part a and b: fitting models and evaluating and comparing models

We first try fitting a model with all the variables and no interactions:

	Median	MAD_SD
(Intercept)	-4.0	0.5
income	-0.1	0.1
gender2. female	0.5	0.2
race2. black	-1.9	0.5
race3. asian	0.0	0.8
race4. native american	0.5	0.6
race5. hispanic	0.7	0.4
educ1	0.2	0.1
partyid3_b2. indpendents and apolitical (1966 on)	Ly 1.8	0.3
partyid3_b3. republicans (including leaners)	4.1	0.2
ideo3. moderate ('middle of the road')	0.9	0.4
ideo5. conservative	1.8	0.2

We have a lot of predictors and not all of them helpful, so let us try paring them down. income has an extremely small coefficient compared to its standard deviation. partyid3\_b, in contrast, has large coefficients compared to its standard deviation. gender and educ1 have small coefficients compared to their standard deviations, race has a large coefficient compared to its standard deviation only for black voters, and ideo also has a large coefficient compared to its standard deviation for conservative voters.

Since they have extremely small coefficients compared to their standard deviations, income and educ1 are good candidates for removal from the model:

	Median	MAD_SD
(Intercept)	-3.3	0.3
gender2. female	0.3	0.2

race2. black	-2.0	0.4
race3. asian	0.4	0.7
race4. native american	0.3	0.6
race5. hispanic	0.4	0.4
partyid3_b2. indpendents and apolitical (1966 only	1.7	0.3
partyid3_b3. republicans (including leaners)	4.0	0.2
ideo3. moderate ('middle of the road')	0.6	0.4
ideo5. conservative	1.6	0.2

In this new model, we see that <code>gender</code> has a very low coefficient compared to its standard deviation; therefore we also remove <code>gender</code>. We are left with this model including only important variables:

	Median	MAD_SD
(Intercept)	-3.1	0.2
race2. black	-1.9	0.4
race3. asian	0.3	0.8
race4. native american	0.3	0.6
race5. hispanic	0.4	0.4
partyid3_b2. indpendents and apolitical (1966 only	1.6	0.3
partyid3_b3. republicans (including leaners)	3.9	0.2
ideo3. moderate ('middle of the road')	0.6	0.4
ideo5. conservative	1.6	0.2

Since it has an especially large coefficient compared to its standard deviations, partyid3\_b is a good candidate for including interactions. We try interacting partyid3 b with race:

	Median	MAD_SD
(Intercept)	-3.1	0.2
race2. black	-2.0	0.6
race3. asian	-0.4	1.2
race4. native american	0.4	0.7
race5. hispanic	0.3	0.5
partyid3_b2. indpendents and apolitical (1966 only	1.5	0.3
partyid3_b3. republicans (including leaners)	3.9	0.2
ideo3. moderate ('middle of the road')	0.6	0.4
ideo5. conservative	1.6	0.2
race2. black:partyid3_b2. indpendents and apolitical (1966 only	0.5	1.0
race3. asian:partyid3_b2. indpendents and apolitical (1966 only	1.4	1.6
race4. native american:partyid3_b2. indpendents and apolitical (1966 only	-2.0	1.8
race5. hispanic:partyid3_b2. indpendents and apolitical (1966 only	1.3	1.3
<pre>race2. black:partyid3_b3. republicans (including leaners)</pre>	-0.3	0.9
race3. asian:partyid3_b3. republicans (including leaners)	0.9	1.5
race4. native american:partyid3_b3. republicans (including leaners)	1.6	1.8
race5. hispanic:partyid3_b3. republicans (including leaners)	-0.1	1.1

We also try interacting partyid3\_b with ideo:

	Median	MAD_SD
(Intercept)	-3.3	0.3
race2. black	-2.0	0.4
race3. asian	0.3	0.7
race4. native american	0.3	0.6
race5. hispanic	0.4	0.4
partyid3_b2. indpendents and apolitical (1966 only	1.7	0.6
partyid3_b3. republicans (including leaners)	4.5	0.4
ideo3. moderate ('middle of the road')	0.9	0.6
ideo5. conservative	1.9	0.3
partyid3_b2. indpendents and apolitical (1966 only:ideo3. moderate ('middle of the road')	0.4	0.9
partyid3_b3. republicans (including leaners):ideo3. moderate ('middle of the road')	-1.0	0.7
partyid3_b2. indpendents and apolitical (1966 only:ideo5. conservative	-0.4	0.7
partyid3 b3. republicans (including leaners):ideo5. conservative	-0.7	0.5

In both cases, the coefficients of the interactions are overwhelmed by the standard deviations. Therefore, the simpler model without interactions (presvote\_2party ~ race + partyid3\_b + ideo) seems to be best.

### Part c: importance of input variables

The paragraph below describes the importance of our predictors for the model:

	Median	MAD_SD
(Intercept)	-3.1	0.2
race2. black	-1.9	0.4
race3. asian	0.3	0.8
race4. native american	0.3	0.6
race5. hispanic	0.4	0.4
partyid3_b2. indpendents and apolitical (1966 only	1.6	0.3
partyid3_b3. republicans (including leaners)	3.9	0.2
ideo3. moderate ('middle of the road')	0.6	0.4
ideo5. conservative	1.6	0.2

First we start with the intercept. Here we see that if you were a white, democratic, and liberal person in 1992, you were 86% less likely to vote for Bush than your compatriots (or put another way, only a 14% probability of voting for Bush). If we used the "Divide by 4" rule (as we do from here on out), we achieve a relatively close approximation of 78%.

Of the five racial categories, only black is estimated within a certain degree of confidence. This factor tells us that, regardless of party id or ideological leanings, a black voter is 47% less likely

to vote for a republican than a white voter. Other ethnicity switches do not drastically change the probability, only 7-10% with large error margins.

A white member of a the republican party is 98% more likely to vote republican than if they are a democrat, while a white independent is only 40% more likely to vote for Bush than a white democrat. We can see that party affiliation is a strong predictor of voting. Conservatives are also 40% more likely to vote republican than liberals. Moderates are only 15% more likely to vote republican than liberals.

Overall, party affiliation is the most important predictor of republican voting.

## R Code

```
rm(list=ls())
library(arm)
library(rstanarm)
library(foreign)
# section 10.10 Problem 1
# import and prep data for regression
# data is in the NES folder at http://www.stat.columbia.edu/~gelman/arm/
d = read.dta(file="nes5200 processed voters realideo.dta")
colnames(d)
d = subset(d, year=="1992") #removes all years except 1992
# curate variables
\texttt{d} \\ \texttt{sincome} = \texttt{as.numeric} \\ (\texttt{factor} \\ (\texttt{d}\\ \texttt{sincome}) \\ \texttt{, levels} = \texttt{unique} \\ (\texttt{d}\\ \texttt{sincome}) \\ \texttt{)} \\ \texttt{\#income} \\ \texttt{as numeric} \\ \texttt{rank} \\ \texttt{numeric} \\ \texttt{rank} \\ \texttt{numeric} \\ \texttt{numeric} \\ \texttt{rank} \\ \texttt{numeric} \\ \texttt{numeric} \\ \texttt{rank} \\ \texttt{numeric} \\ \texttt{num
(1-5)
d$gender = as.factor(d$gender) #gender as factor with 2 levels
d$race = as.factor(d$race) #race as factor with 5 levels
deduc1 = as.numeric(factor(d$educ1), levels = unique(d$educ1)) #education as numeric rank
(1-4)
\label{eq:dpartyid3b} \texttt{d}. \texttt{partyid3\_b} = \texttt{as.factor(d}. \texttt{partyid3\_b)} \text{ \#party ID as factor with 3 levels}
d$ideo = as.factor(d$ideo) #political ideaology as factor with 3 levels
# part a - logistic regression predicting support for Bush in 1992 given
# income, sex, ethnicity, education, party ID, and political ideology
# include all variables
fit1=stan glm(presvote 2party~income + gender + race + educ1 + partyid3 b + ideo,
                                       family=binomial(link="logit"), data=d)
print(fit1)
# remove variables with low coefficients compared to standard deviations
fit2=stan glm(presvote 2party~gender + race + partyid3 b + ideo,
                                       family=binomial(link="logit"), data=d)
print(fit2)
# further remove variables with low coefficients compared to standard deviations,
# leaving only important variables
fit3=stan_glm(presvote_2party~race + partyid3_b + ideo,
                                      family=binomial(link="logit"), data=d)
print(fit3)
# try interactions with partyid3 b
fit4=stan_glm(presvote_2party~race + partyid3_b + ideo + partyid3_b:race,
                                       family=binomial(link="logit"), data=d)
print(fit4)
fit5=stan_glm(presvote_2party~race + partyid3_b + ideo + partyid3_b:ideo,
                                       family=binomial(link="logit"), data=d)
print(fit5)
```

```
###Dan's failed attempt to zscore:
d2<-dplyr::select(d,presvote_2party,income,gender,race,educ1,partyid3,ideo)
d2$presvote_2party<-as.numeric(d2$presvote_2party)-2
d2$income<-as.numeric(d2$income)-2
d2$gender<-as.numeric(d2$gender)-2
d2$race<-as.numeric(d2$race)-1
d2$educ1<-as.numeric(d2$partyid3)-2
d2$partyid3<-as.numeric(d2$partyid3)-2
d2$ideo<-as.numeric(d2$ideo)-2

d2$z_income<-(d2$income-mean(d2$income))/(2*sd(d2$income))
d2$z_gender<-(d$gender-mean(d$gender))/(2*sd(d$gender))
d2$z_race<- (d$race-mean(d$race))/(2*sd(d$face))
d2$z_educ1<-(d2$educ1-mean(d2$educ1))/2*sd(d2$educ1)
d2$z_partyid3<-(d2$partyid3-mean(d2$partyid3))/(2*sd(d2$partyid3))
d2$z_ideo<-(d2$ideo-mean(d2$ideo))/(2*sd(d2$ideo))</pre>
```