

# A four-step simulation-based workflow for ecological analysis and science

EM Wolkovich<sup>1\*</sup>, T Jonathan Davies<sup>1,2</sup>, William D Pearse<sup>3,4</sup> & Michael Betancourt<sup>5</sup>

November 1, 2025

<sup>1</sup> Forest and Conservation Sciences, University of British Columbia, Vancouver, BC V6T 1Z4, Canada

<sup>2</sup> Botany, University of British Columbia, Vancouver, BC V6T 1Z4, Canada

<sup>3</sup> Department of Life Sciences, Imperial College London, Ascot SL5 7PY, United Kingdom

<sup>4</sup> Alan Turing Institute, British Library, 96 Euston Road, London NW1 2DB, United Kingdom

<sup>5</sup> Symplectomorphic, LLC, New York, NY 10026, USA

\* mailto: e.wolkovich@ubc.ca

*Keywords:* big data; scientific workflow; data simulation; prediction; null hypothesis testing, machine learning

---

## 1                   Abstract

2                   Ecology is a discipline that has faced increasing challenges as the disconnect between its scientific and statistical methods has become more obvious. Growing demands for useful forecasts  
3                   in an era of intensifying global change had required models that can capture the variability  
4                   and underlying uncertainty of ecological systems and related data. Yet many ecologists are not  
5                   trained in current methods to build the flexible robust models needed to address this challenge.  
6                   Thus, they often rely on a limited set of pre-defined models combined with null hypothesis  
7                   testing or are tempted to adopt new approaches without fully understanding their limitations.  
8                   The result is poor models that lead to incorrect predictions, alongside concerns of a looming  
9                   replication crisis. Here we use show how new advances in workflows can lead to better models  
10                  and enhance training in ecology, an approach that could be followed by other fields facing similar  
11                  challenges. Building on the increasingly computational toolkit of many ecologists, this approach  
12                  leverages simulation to integrate model building and testing for empirical data more fully with  
13                  ecological theory. We argue this approach can fit models that are more robust and better-suited  
14                  to providing new ecological insights and improved predictions, and may provide a blueprint for  
15                  other fields similarly challenged by complex systems, growing datasets and limited training in  
16                  how to best approach them.

18                  *Example & Data:* We provide an example of the full workflow with complete code available at  
19                  <https://github.com/lizzieinvancouver/bayesianflowsexample>. The data used for the example is  
20                  provided and full metadata on it is available via the Knowledge Network for Biocomplexity:  
21                  doi:10.5063/F12J69B2.

22

## Introduction

23

Ecology is a discipline that has followed a trajectory similar to other biological and social science fields in its growing aims, study design and data. Decades ago ecological research usually reported results from simple experiments or observations of one site using frequentist tests associated with null hypothesis testing. Mechanistic models were typically the terrain of theorists, who studied ordinary differential equations (ODE, for example of Lotka Volterra predator-prey dynamics) and rarely compared their models explicitly to empirical data. But in recent decades growing demands have pushed ecological science to work across systems, contribute to policy and provide models to forecast the outcomes of growing anthropogenic pressures (Hák et al., 2016; Lindenmayer and Likens, 2010). These new scales and aims have led many ecologists to try to adapt what they were trained in (e.g., null hypothesis testing using  $F$  and  $t$  tests) to increasingly larger scales, more complex datasets, and to fads in specific approaches (Grace et al., 2025).

35

Yet many commonly used statistical approaches do not align with these new demands. Beyond the reality that most traditional methods are fragile when used beyond the cleaner, simpler experiments these methods assume (e.g. spatial, temporal and phylogenetic correlations often violate independence assumptions), they will usually fail to produce robust, reproducible results. For example, an overly zealous focus on  $p$ -values has led to a replication crises in several fields, where results derived from studies with small sample sizes seem most likely the outcome of noisy data combined with a search for statistical significance through many models (effectively a garden of forking paths, Halsey et al., 2015; Loken and Gelman, 2017). Some model selection approaches, including new machine learning methods, try to avoid this by comparing across models, but may not generalize to provide useful forecasts. This is especially true when forecasts have to adapt to changes in the underlying biology (Boettiger, 2022). This leaves ecology in a predicament shared across other fields—concerns of a looming replication crisis (Filazzola and Cahill Jr, 2021; Fraser et al., 2020) and overly confident forecasts with the potential to erode public trust in science when found not to be accurate (Leroux, 2019; Boettiger, 2022).

49

Many researchers recognize these issues and have turned to methods better designed for forecasting from complex systems and messy data. Machine learning methods, which benefit from large datasets—often with many predictors—fitted to test and training datasets (Breiman, 2001), have revolutionized image classification in ecology and other fields, but are increasingly used to forecast ecological processes (e.g., Zwart et al., 2023). These methods often build complex, opaque ('black-box') models (Cox, 2001; Efron, 2001; Shmueli, 2010), thus providing opaque inference into ecological processes. Unlike many 'black-box' methods, Bayesian inference encourages the fitting of bespoke mechanistic models with interpretable parameters and can thus handle many of the complexities of ecological data (Hobbs and Hilborn, 2006). Long used in select applications in ecology (Muthukumarana et al., 2008; Zheng et al., 2007; Trijoulet et al., 2018; Strinella et al., 2020), Bayesian inference has recently increased in use (Anderson et al., 2021; Pichler and Hartig, 2023), alongside new algorithms (e.g. Hamiltonian Monte Carlo, Hoffman and Gelman, 2014; Betancourt, 2019) that have made fitting and implementing models faster, more robust and—in many ways—easier (Carpenter et al., 2017)

63

Regardless of the approach, fitting larger and more complex models has not dramatically improved forecasts, nor made research more reproducible. Instead, these new approaches have highlighted a fundamental training disconnect that applies from simple to complex models: treating scientific and statistical methods as separate.

67

Merging scientific and statistical training is possible by approaching analyses through specific

---

68 workflows (Betancourt, 2020; Grinsztajn et al., 2021; van de Schoot et al., 2021), which them-  
69 selves are built on a process of how to do not just statistics, but how to do science (Box, 1976).  
70 While these approaches are slowly gaining traction in other fields (e.g., Esfahani et al., 2021;  
71 Schad et al., 2021; Bouman et al., 2024), they are not widely used in ecology or many other fields  
72 today. Such approaches move away from a focus on null hypothesis testing, towards estimating  
73 effect sizes, using models calibrated (see Table 1) and better understood through simulating data  
74 at multiple steps. We argue that potential benefits include not only a better understanding of  
75 models fit to empirical data, but also a better understanding of system dynamics by requiring  
76 explicit consideration of the generative processes underlying observations.

77 Here we outline a simplified—but powerful—workflow that builds on new insights from statistics  
78 (Betancourt, 2020; Gelman et al., 2020; van de Schoot et al., 2021) and the increasingly compu-  
79 tational nature of ecology today. Our aim is to provide an approachable rubric for those new to  
80 fitting complex models or simply those interested in re-considering their current workflow (and  
81 is not intended to be a comprehensive overview; see ‘Next steps’ in the Supplement). Because of  
82 this aim and to maximize interpretability, we illustrate our workflow using examples of simple  
83 models, and suggest additional resources as users build more complex models. Our examples  
84 include several statistical inference methods, though we focus on implementing the workflow  
85 through a Bayesian statistical framework (with an example shown in R and Stan), because this  
86 framework allows integrating bespoke model building more fully with ecological theory and un-  
87 derstanding. We suggest that adopting this workflow approach can help fit models that are  
88 more robust and well-suited to provide new ecological insights—allowing us to refine where to  
89 put resources for better estimates, better models, and better forecasts.

## 90 A four-step workflow

91 Our workflow outlines what we consider the major steps for building bespoke models (Fig. 1).  
92 Several of these steps will be familiar to statistical ecologists, but are often overlooked, whereas  
93 other steps may appear particular to certain methods (e.g. prior predictive checks in Bayesian  
94 analyses), but are actually useful for anyone—using Bayesian models or not—to challenge their  
95 models of how the world works. We find that it is easiest to illustrate and describe this workflow  
96 using a Bayesian framework (see *A brief review of statistical inference using Bayesian approaches*  
97 in the Supplement), but we argue this workflow can be adapted to other approaches (Fig. 2).  
98 Parts of this workflow could be expanded as workflows in themselves, given other aims (see  
99 Supplement: *Which workflow?*).

### 100 Step 1: Develop your model(s)

101 We start the workflow with what can feel like the biggest step—build a model (or potentially,  
102 models) based on your aims (Hilborn and Mangel, 2013). By developing a model designed for  
103 your biological question, data and aims, your statistical workflow naturally becomes a scientific  
104 workflow. You will more clearly see the assumptions and mechanisms in your model, which is  
105 especially valuable given how often our intuition of how models ‘work’ is wrong (Kokko, 2005).  
106 You likely already have a model, though it may be only verbal or conceptual. For this workflow,  
107 however, you’ll need to convert such models into mathematical versions (Servedio et al., 2014).

108 Though it can feel challenging at first, this step is best approached before you collect any data. A  
109 suite of resources for ‘generative’ or ‘narratively generative’ modeling can help (McElreath, 2016;

---

110 Betancourt, 2021b). As you start, ask lots of questions—and push yourself on your answers—  
111 about what you expect and what’s reasonable biologically from your model. As you do this,  
112 you’ll be generating your model—including its priors. Priors are important for Bayesian analysis,  
113 but the basic idea of them—coming up with a distribution of reasonable values for parameters in  
114 your model (see Table 1)—is useful to all analyses (for an example, see discussion of a heuristic  
115 model in the case study for Fig. 2b). Assigning priors generally forces you to think about your  
116 model with regard to your study system, and interrogate what’s probable, possible or actually  
117 unreasonable—and can quickly disabuse users of prejudices regarding priors. For example, you  
118 may not think you have a prior on how sunlight affects plant growth, until you realize your  
119 ‘agnostic prior’ actually allows plants to grow hundreds of meters per day.

120 **Step 2: Check your model on simulated data**

121 Once you have your model and its priors jotted down, you need to formalise it in your preferred  
122 modeling language and check it. As with all code: just because it runs, does not mean it does  
123 what you think it does. The worst errors often still permit code to run.

124 Test data (aka ‘simulated data’, or ‘fake data,’ etc.), and the skills required to generate it, are  
125 central to this workflow. With ‘test data’ you simulate data from your model in such a way  
126 that you can use the resulting data to test if your model code is correct (i.e., you fix values  
127 for your model parameters, then test how well your model recovers them, see the Supplement  
128 for several examples). This is more straightforward when your statistical model is the same as  
129 your generative model, but the basic idea can be adapted to other approaches (see Fig. 2b).  
130 While there’s no guarantee that inferences will always recover the parameter values you set,  
131 even when using the correct model, extreme disagreement is often an indicator that something  
132 is amiss in the implementation of the model. At the same time these simulation studies can  
133 help understand how often a model might lead to the correct inference (see Figs. 2 and S1).  
134 As you do this, you will also be calibrating your model—seeing how accurately and precisely it  
135 estimates parameters and under what conditions.

136 This very basic model checking step is uncommon for many ecologists, but critical in our view. If  
137 you can simulate data from your model, then you can powerfully—and easily—answer questions  
138 related to statistical power (see Fig. 2a and related Supplemental examples), what effect sizes  
139 are reasonable, and—most likely—have new insights into how your model suggests the world  
140 works, all before looking at any real data. Thus, this apparently simple programmatic task  
141 actually encapsulates a far deeper understanding of your model. ‘All models are wrong; some  
142 models are useful,’ becomes much clearer when you have the power to generate data from your  
143 model under any parameter set and sample size you want.

144 You can learn only so much, however, from data simulated from a particular parameter set.  
145 Simulation studies across multiple parameter sets allow you to investigate how robust your  
146 inferential performance might be. Prior predictive checks (Betancourt, 2021a; Winter and De-  
147 paoli, 2023) use the Bayesian prior model to set the scope of such simulations, but the basic idea  
148 of prior predictive checks can be used in any analysis. For these, you draw values from your prior  
149 distribution and then explore how your model performs. Seeing how this influences your result-  
150 ing model output reveals the extent to which your model can capture known variation in your  
151 data, and gives insight into whether your model is capable of distinguishing among competing  
152 hypotheses. If adopting a Bayesian approach, it can also serve as a check on the priors you’re  
153 using (addressing one of the common concerns of those inexperienced with Bayesian models).

---

154           **Step 3: Run your model on your empirical data**

155       The next step is to run the model—you’ve now evaluated, test-run and have ready to go—  
156       on your exciting new empirical data. Check diagnostics so you know it’s running well and  
157       adjust until it is. Which diagnostics to use depends on your exact fitting approach, with many  
158       approaches having a suite of metrics that are well-discussed elsewhere (for Bayesian methods,  
159       this includes a suite of convergence and efficiency metrics Betancourt, 2020; Gelman et al., 2020;  
160       van de Schoot et al., 2021; Gabry et al., 2019).

161       This is the step many ecologists skip straight to, ourselves included. It’s easy to see the appeal:  
162       this is the inference step and where you might gain new ecological insights. Fitting new data  
163       to the model can feel like the moment when you’ll learn something new. But, at least in our  
164       experience, this is not always the case. When we rush to this step, that first model we fit is  
165       often followed by another, and another—perhaps because one does not converge, or the results  
166       of another do not make immediate sense. And with the excitement of getting a model to run  
167       we can get distracted from what we are actually most interested in—the inference into our  
168       ecological system.

169       Following this workflow can make this step much more satisfying. Here the benefits of the  
170       workflow may become especially apparent: using it with Bayesian inference you likely have  
171       estimates in useful units with uncertainty you can understand. You can use this information to  
172       draw new conclusions, design new experiments and more—but this is also a point to stop and  
173       check your model.

174           **Step 4: Check your model on data simulated from your empirical model  
175       output**

176       Once you have your parameter estimates based on your model and new empirical data, it’s  
177       time to remember that your model is wrong (as all models are) and ask how useful it is. You  
178       can do some of this through common model-fit diagnostics, such as  $R^2$ , which compares point  
179       predictions to the observed data. With a Bayesian posterior (see Table 1), however, you have  
180       an added benefit in that you can compare an entire distribution of predictions to the observed  
181       data.

182       This is where simulating from your model can be especially insightful. It will not only indicate  
183       when the model isn’t adequately fitting the data but also can suggest what the problems might  
184       be. Using the parameter estimates from your fitted model to simulate new data (Held et al.,  
185       2010; Gelman et al., 2000; Conn et al., 2018) lets you see how that new world compares to the  
186       observed data. This is most easily done in a Bayesian framework—called posterior retrodictive  
187       checks or posterior predictive checks (Fig. 3)—where your posterior captures your uncertainty  
188       in a useful way, but can be done with estimates of your parameters and their uncertainty from  
189       other inferential frameworks. Exactly how to do this effectively, however, requires care for any  
190       particular framework. Tailoring these checks to the research question and model makes this step  
191       most likely to pick up model mis-specification and provide useful insight for improvement (e.g.,  
192       Mimno et al., 2015).

193       Often here you may find large differences from your empirical data, and can start to generate  
194       hypotheses for why. For example, you may find patterns that suggest missing grouping factors  
195       (e.g. site or biome) through visual posterior retrodictive checks, or you may quickly realize your  
196       model predicts impossible numbers for your biological reality. You may begin to see inadequacies

---

197 in your model, or even potentially your data. This is one of the main benefits of the workflow:  
198 models don't fail silently, they fail with a wealth of context that helps to generate new models  
199 and experiments.

200 **Feedbacks & workflows**

201 A key feature of this workflow is that it can be iterated. If you find that you want to tweak your  
202 model then you return to the beginning, adjust your model, and repeat the rest of the workflow  
203 (Fig. 1). In this way, fitting multiple models is encouraged, but this is distinct from the quest  
204 for a minimum adequate model or one 'best' fit. Feedbacks in this workflow are focused far more  
205 on what is biologically reasonable, and understanding the utility—and limits—of inference from  
206 your data for your model. And there are big benefits to it.

207 **How this workflow changed our science**

208 Before this workflow, not all of us commonly discussed the values that parameters in our model  
209 took—things like the slope and intercept (two common model parameters) were sometimes  
210 reported, but we did not know them as well as we knew whether the *p*-value for the slope was  
211 < 0.05. This changes quickly when you need to build simulated data (Step 2). For example,  
212 when modeling phenological events (observations of biological events on numbered days within  
213 the calendar year: 1-366 days when including leap years) it is not uncommon to find seemingly-  
214 reasonable models generating predictions of events on non-existent calendar days beyond 366.

215 A closer inspection of our parameters also taught us a lot about identifiability and nonidentifiability,  
216 when all parameters in a model can—or cannot—be uniquely identified with infinite  
217 data, and a statistical kin: degeneracy (see Table 1). Degeneracy concerns the kinds of complex  
218 uncertainties that can arise from finite data sets (Gelman and Hill, 2009), and something we  
219 have often found in Steps 2-3 of our workflow. Nonidentifiability and degeneracy can insert  
220 themselves in many ways in ecology, and may lead us to believe we understand our system when  
221 we do not. These were issues we never thought about before using this workflow, but since then  
222 we have realized (especially in steps 1-2) lots of places for nonidentifiability and degeneracies to  
223 live—and we have adjusted how we collect data and interpret results because of it. For example,  
224 we have found fitting both site and species in a model with highly imbalanced data or trying to  
225 estimate interaction terms with low sample sizes (for more details see Gelman and Hill, 2020)  
226 leads to degenerate models, while spatial autocorrelation in environmental data can often lead  
227 to issues of nonidentifiability, but there's often no warning in common statistical packages to  
228 tell us of these problems (see Fig. 2c).

229 **How this workflow intersects with ecological training**

230 This four-step workflow is a simplified version of the current best practices for model fitting  
231 (Betancourt, 2020; van de Schoot et al., 2021), but many of the skills required are not part of  
232 traditional ecological training. Writing out the math behind most statistical models to complete  
233 Steps 1-2 leans on the skillset usually reserved for those working on theory, where coding and  
234 simulating from a model are common tasks. In contrast field, lab and otherwise empirical-data  
235 based ecologists often fit models they could not easily simulate data from. This dichotomy

236 seems short-sighted in our current era of bigger, messier data and a greater diversity of methods  
237 available to handle such data. The increasingly computational toolkit of the modern ecologist  
238 makes it easier to bridge the gap between statistical models used in ecology and the field's  
239 underlying mechanistic theories.

240 We argue training in simulating data as part of an organized workflow could speed progress  
241 in ecology and is possible given the increasingly computational abilities of many ecologists. A  
242 reasonably competent coder could easily simulate data under a complex model that they might  
243 not have the mathematical expertise to solve analytically (e.g., solving for an equilibrium in  
244 an ODE)—if doing so was part of their training and the workflows they regularly use. While  
245 training in frequentist methods often includes memorizing assumptions for a particular test,  
246 or steps specifically designed to test particular assumptions (e.g. normal quantile plots), this  
247 workflow requires no such training. Instead it requires only the skills to identify whatever  
248 the assumptions have been encoded in your models. It thus moves away from some modeling  
249 paradigms in ecology, which focus on fewer underlying assumptions (e.g. random forests, non-  
250 parametric), to building models where the assumptions are transparent and motivated by the  
251 specific domain expertise of researchers.

252 In Bayesian inference advances in developing workflows have come alongside improved algo-  
253 rithms, visualizations (e.g. Betancourt, 2020; van de Schoot et al., 2021; Gabry et al., 2019),  
254 perspectives on priors (Gelman et al., 2014; Gelman and Hill, 2020; Betancourt, 2021a) and  
255 hierarchical approaches that could also improve training. For example, new work shows that  
256 prior predictive checks provide a more powerful and intuitive way to understand how priors  
257 work within a particular Bayesian model (Betancourt, 2021a), compared to past approaches.  
258 Similarly, traditional ecological training in hierarchical models still often refers to grouping fac-  
259 tors (such as species or individual) as ‘random effects,’ which is misleading, imprecise and thus  
260 no longer recommended (Gelman and Hill, 2009). In ecology, it also carries with it many older  
261 ‘rules’ of what is ‘random’ versus ‘fixed,’ including that ‘random effects are things you don’t care  
262 about’ (for example the ‘block’ effect from a randomized block design). Training in retrodictive  
263 checks (Step 4) may reshape these views, as hierarchical effects are (by definition) drawn from  
264 an underlying distribution—meaning they can predict outside of the specific set sampled (for  
265 example, to predict for a new species or individual), whereas the same is not true for most  
266 categorical ‘fixed’ effects.

## 267 How this workflow extends to other fields

268 These new best practices have gained traction at the same time that ecology, alongside many  
269 other fields, has recognized that *p*-values, and null hypothesis testing in general, are easily mis-  
270 leading (Gelman and Geurts, 2017; Ferraro and Shukla, 2020; Filazzola and Cahill Jr, 2021;  
271 Fraser et al., 2020). Small sample sizes alongside a tendency to fit complicated models with  
272 multiple interactions makes ecological research particularly vulnerable to these problems (Gel-  
273 man, 2015). Adding to this, a lack of routine reporting of interpretable effect sizes, fitting of  
274 many models without adequate explanation (or reporting), and poor data and code recording  
275 habits all increase the chance of finding ‘significance’ at a level of  $\leq 0.05$  (Halsey et al., 2015;  
276 Loken and Gelman, 2017).

277 The answer to these problems is not to make *p*-values smaller (Halsey et al., 2015; Colquhoun,  
278 2017), nor is it Bayesian, machine learning or ‘new’ causal inference approaches, despite asser-  
279 tions to the contrary, which echo previous promised revolutions through the introduction of new

---

280 methods (e.g., Mitchell, 1992; Burnham and Anderson, 2004; Byrnes and Dee, 2025). Ecology,  
281 like many fields, has increasingly adopted machine learning methods in hopes they will help  
282 them fit better models, but they can easily lead to poor models that do not match the under-  
283 lying realities of the system (Efron, 2020; Pichler and Hartig, 2023). Similarly ecology readily  
284 took up path analysis, multi-model comparison with AIC, and a suite of other approaches, that  
285 promised better inference, but ultimately led to many papers reporting poor models, and result-  
286 ing policy recommendations based on such models (Petrailis et al., 1996; Leroux, 2019). This  
287 fad approach to statistics is not unique to ecology, but the cure for it is also not yet another  
288 new statistical method.

289 We argue that the answer is training in workflows designed for careful model building, model  
290 fitting and model interrogation informed by underlying theory and understanding of the system  
291 being modeled (Betancourt, 2020; Gelman et al., 2020; van de Schoot et al., 2021)—including  
292 the one we outline here. Our workflow depends strongly on simulating data—for testing your  
293 model (Step 2), and understanding your model results (Step 4)—an area we actively under-train  
294 in many research fields that depend on increasingly complex statistical methods. Simulation  
295 approaches encourage interactive learning, build intuition, and stress exploring a model in its  
296 relevant context. Ecologists, similar to researchers in any domain-specific field, are much better  
297 at thinking about domain-specific scientific problems than statistical ones. Grounding statistical  
298 approaches in theory and domain knowledge will likely bring the best out of statistical modeling.  
299 While this idea is not new, we argue the need for it is especially high, as the line between  
300 estimation and prediction becomes more blurred (Shmueli, 2010). At the same time, however,  
301 computation is increasingly part of a researcher’s toolkit, lowering the barriers for those wishing  
302 to adopt this workflow and improve their statistical inference.

303 *Acknowledgements:* Comments from F. Baumgarten, B. Bolker, D. Loughnan, N. Pates, V.  
304 Rudolf, J. Socolar and V. Van der Meersch improved this manuscript and J. Ngo improved  
305 Figure 1. Thanks to V. Van der Meersch also for helping with Markdown formatting.

---

306                    **References**

307

- 308                    Anderson, S. C., P. R. Elsen, B. B. Hughes, R. K. Tonietto, M. C. Bletz, D. A. Gill, M. A.  
309                    Holgerson, S. E. Kuebbing, C. McDonough MacKenzie, M. H. Meek, et al. 2021. Trends  
310                    in ecology and conservation over eight decades. *Frontiers in Ecology and the Environment*  
311                    19:274–282.
- 312                    Betancourt, M. 2019. The Convergence of Markov Chain Monte Carlo Methods: From the  
313                    Metropolis Method to Hamiltonian Monte Carlo. *Annalen der physik* 531.
- 314                    ———. 2020. Towards A Principled Bayesian Workflow. [https://betanalpha.github.io/assets/case\\_studies/principled\\_bayesian\\_workflow.html](https://betanalpha.github.io/assets/case_studies/principled_bayesian_workflow.html).
- 315                    ———. 2021a. Prior modeling. [https://betanalpha.github.io/assets/case\\_studies/prior\\_modeling.html](https://betanalpha.github.io/assets/case_studies/prior_modeling.html).
- 316                    ———. 2021b. (what's the probabilistic story) modeling glory?  
317                    [https://betanalpha.github.io/assets/case\\_studies/generative\\_modeling.html](https://betanalpha.github.io/assets/case_studies/generative_modeling.html).
- 318                    Boettiger, C. 2022. The forecast trap. *Ecology Letters* 25:1655–1664.
- 319                    Bouman, J. A., A. Hauser, S. L. Grimm, M. Wohlfender, S. Bhatt, E. Semenova, A. Gelman,  
320                    C. L. Althaus, and J. Riou. 2024. Bayesian workflow for time-varying transmission in stratified compartmental infectious disease transmission models. *PLoS computational biology*  
321                    20:e1011575.
- 322                    Box, G. E. 1976. Science and statistics. *Journal of the American Statistical Association* pages  
323                    791–799.
- 324                    Breiman, L. 2001. Statistical modeling: The two cultures (with comments and a rejoinder by  
325                    the author). *Statistical science* 16:199–231.
- 326                    Burnham, K. P., and D. R. Anderson. 2004. Multimodel inference: understanding aic and bic  
327                    in model selection. *Sociological methods & research* 33:261–304.
- 328                    Byrnes, J. E., and L. E. Dee. 2025. Causal inference with observational data and unobserved  
329                    confounding variables. *Ecology Letters* 28:e70023.
- 330                    Carpenter, B., A. Gelman, M. Hoffman, D. Lee, B. Goodrich, M. Betancourt, M. A. Brubaker,  
331                    J. Guo, P. Li, and R. Allen. 2017. Stan: A probabilistic programming language. *Journal of  
332                    Statistical Software* 76:10.18637/jss.v076.i01.
- 333                    Colquhoun, D. 2017. The reproducibility of research and the misinterpretation of p-values.  
334                    Royal Society Open Science 4.
- 335                    Conn, P. B., D. S. Johnson, P. J. Williams, S. R. Melin, and M. B. Hooten. 2018. A guide to  
336                    Bayesian model checking for ecologists. *Ecological Monographs* 88:526–542.
- 337                    Cox, D. R. 2001. Comment on statistical modeling: The two cultures. *Statistical Science*  
338                    16:216–218.
- 339                    Efron, B. 2001. Comment on statistical modeling: The two cultures. *Statistical Science* 16:218–  
340                    219.

- 338 ———. 2020. Prediction, estimation, and attribution. International Statistical Review 88:S28–  
339 S59.

340 Esfahani, A. A., M. Betancourt, Z. Bogorad, S. Böser, N. Buzinsky, R. Cervantes, C. Claessens,  
341 L. De Viveiros, M. Fertl, J. Formaggio, et al. 2021. Bayesian analysis of a future  $\beta$  decay  
342 experiment’s sensitivity to neutrino mass scale and ordering. Physical Review C 103:065501.

343 Ferraro, P. J., and P. Shukla. 2020. Feature—is a replicability crisis on the horizon for environ-  
344 mental and resource economics? Review of Environmental Economics and Policy .

345 Filazzola, A., and J. F. Cahill Jr. 2021. Replication in field ecology: Identifying challenges and  
346 proposing solutions. Methods in Ecology and Evolution 12:1780–1792.

347 Fraser, H., A. Barnett, T. H. Parker, and F. Fidler. 2020. The role of replication studies in  
348 ecology. Ecology and Evolution 10:5197–5207.

349 Gabry, J., D. Simpson, A. Vehtari, M. Betancourt, and A. Gelman. 2019. Visualization in  
350 bayesian workflow. Journal of the Royal Statistical Society Series a-Statistics in Society  
351 182:389–402.

352 Gelman, A. 2015. The connection between varying treatment effects and the crisis of unreplicable  
353 research: A bayesian perspective.

354 Gelman, A., J. B. Carlin, H. S. Stern, D. B. Dunson, A. Vehtari, and D. B. Rubin. 2014.  
355 Bayesian Data Analysis. 3rd ed. CRC Press, New York.

356 Gelman, A., and H. M. Geurts. 2017. The statistical crisis in science: How is it relevant to  
357 clinical neuropsychology? The Clinical Neuropsychologist 31:1000–1014.

358 Gelman, A., Y. Goegebeur, F. Tuerlinckx, and I. Van Mechelen. 2000. Diagnostic checks for  
359 discrete data regression models using posterior predictive simulations. Journal of the Royal  
360 Statistical Society Series C-Applied Statistics 49:247–268.

361 Gelman, A., and J. Hill. 2009. Data Analysis Using Regression and Multilevel/Hierarchical  
362 Models. Cambridge, New York.

363 ———. 2020. Regression and Other Stories. Cambridge University Press.

364 Gelman, A., A. Vehtari, D. Simpson, C. C. Margossian, B. Carpenter, Y. Yao, L. Kennedy,  
365 J. Gabry, P.-C. Bürkner, and M. Modrák. 2020. Bayesian workflow. arXiv.

366 Grace, J. B., N. Huntington-Klein, E. W. Schweiger, M. Martinez, M. J. Osland, L. C. Feher,  
367 G. R. Guntenspergen, and K. M. Thorne. 2025. Causal effects versus causal mechanisms:  
368 Two traditions with different requirements and contributions towards causal understanding.  
369 Ecology letters 28:e70029.

370 Grinsztajn, L., E. Semenova, C. C. Margossian, and J. Riou. 2021. Bayesian workflow for disease  
371 transmission modeling in Stan. Statistics in Medicine 40:6209–6234.

372 Hák, T., S. Janoušková, and B. Moldan. 2016. Sustainable development goals: A need for  
373 relevant indicators. Ecological indicators 60:565–573.

374 Halsey, L. G., D. Curran-Everett, S. L. Vowler, and G. B. Drummond. 2015. The fickle p value  
375 generates irreproducible results. Nature Methods 12:179–185.

- 376 Held, L., B. Schroedle, and H. Rue. 2010. Posterior and Cross-validatory Predictive Checks: A  
377 Comparison of MCMC and INLA. Pages 91–110 in T. Kneib and G. Tutz, eds. Statistical  
378 Modelling and Regression Structures: Festschrift in Honour of Ludwig Fahrmeir.
- 379 Hilborn, R., and M. Mangel. 2013. The ecological detective: confronting models with data  
380 (MPB-28). Princeton University Press.
- 381 Hobbs, N. T., and R. Hilborn. 2006. Alternatives to statistical hypothesis testing in ecology: a  
382 guide to self teaching. Ecological Applications 16:5–19.
- 383 Hoffman, M. D., and A. Gelman. 2014. The No-U-Turn Sampler: Adaptively Setting Path  
384 Lengths in Hamiltonian Monte Carlo. Journal of Machine Learning Research 15:1593–1623.
- 385 Kokko, H. 2005. Useful ways of being wrong. Journal of evolutionary biology 18:1155–1157.
- 386 Leroux, S. J. 2019. On the prevalence of uninformative parameters in statistical models applying  
387 model selection in applied ecology. PloS one 14:e0206711.
- 388 Lindenmayer, D. B., and G. E. Likens. 2010. The science and application of ecological monitoring.  
389 Biological conservation 143:1317–1328.
- 390 Loken, E., and A. Gelman. 2017. Measurement error and the replication crisis. Science 355:584–  
391 585.
- 392 McElreath, R. 2016. Statistical Rethinking, vol. 469 pp. CRC Press, New York.
- 393 Mimno, D., D. M. Blei, and B. E. Engelhardt. 2015. Posterior predictive checks to quantify  
394 lack-of-fit in admixture models of latent population structure. Proceedings of the National  
395 Academy of Sciences 112:E3441–E3450.
- 396 Mitchell, R. J. 1992. Testing evolutionary and ecological hypotheses using path analysis and  
397 structural equation modelling. Functional Ecology pages 123–129.
- 398 Muthukumarana, S., C. J. Schwarz, and T. B. Swartz. 2008. Bayesian analysis of mark-recapture  
399 data with travel time-dependent survival probabilities. Canadian Journal of Statistics 36:5–21.
- 400 Petraitis, P., A. Dunham, and P. Niewiarowski. 1996. Inferring multiple causality: the limita-  
401 tions of path analysis. Functional ecology pages 421–431.
- 402 Pichler, M., and F. Hartig. 2023. Machine learning and deep learning—a review for ecologists.  
403 Methods in Ecology and Evolution 14:994–1016.
- 404 Schad, D. J., M. Betancourt, and S. Vasishth. 2021. Toward a principled Bayesian workflow in  
405 cognitive science. Psychological Methods 26:103–126.
- 406 Servedio, M. R., Y. Brandvain, S. Dhole, C. L. Fitzpatrick, E. E. Goldberg, C. A. Stern,  
407 J. Van Cleve, and D. J. Yeh. 2014. Not just a theory—the utility of mathematical models in  
408 evolutionary biology. PLoS biology 12:e1002017.
- 409 Shmueli, G. 2010. To explain or to predict? Statistical science pages 289–310.
- 410 Strinella, E., D. Scridel, M. Brambilla, C. Schano, and F. Korner-Nievergelt. 2020. Potential  
411 sex-dependent effects of weather on apparent survival of a high-elevation specialist. Scientific  
412 Reports 10:8386.

- 
- 413 Trijoulet, V., S. J. Holmes, and R. M. Cook. 2018. Grey seal predation mortality on three  
414 depleted stocks in the West of Scotland: What are the implications for stock assessments?  
415 Canadian Journal of Fisheries and Aquatic Sciences 75:723–732.
- 416 van de Schoot, R., S. Depaoli, R. King, B. Kramer, K. Maertens, M. C. Tadesse, M. Vanmucci,  
417 A. Gelman, D. Veen, J. Willemse, and C. Yau. 2021. Bayesian statistics and modelling.  
418 Nature Reviews Methods Primers 1.
- 419 Winter, S. D. D., and S. Depaoli. 2023. Illustrating the Value of Prior Predictive Checking for  
420 Bayesian Structural Equation Modeling. Structural Equation Modeling-a multidisciplinary  
421 journal .
- 422 Zheng, C., O. Ovaskainen, M. Saastamoinen, and I. Hanski. 2007. Age-dependent survival  
423 analyzed with Bayesian models of mark-recapture data. Ecology 88:1970–1976.
- 424 Zwart, J. A., S. K. Oliver, W. D. Watkins, J. M. Sadler, A. P. Appling, H. R. Corson-Dosch,  
425 X. Jia, V. Kumar, and J. S. Read. 2023. Near-term forecasts of stream temperature using  
426 deep learning and data assimilation in support of management decisions. JAWRA Journal of  
427 the American Water Resources Association 59:317–337.

---

## Tables & Figures

Table 1: Glossary: We provide below simplified definitions of the major terms we use (many of these terms, such as calibration, may be used differently depending on the particular literature).

<i>Term</i>	<i>Definition</i>
calibration	analyzing how often an estimate is close to the true value over an ensemble of hypothetical observations. An exact calibration would require simulating from the true data generating process which is impossible in practice. We can, however, calibrate to data simulated from the configurations of models we plan use to fit to our data ( <i>Steps 1-2</i> ) so we understand the models better, including their limits given data similar to ours. We emphasize simulations to calibrate model behaviors consistent with our ecological systems and understanding (e.g. working within a limited set of parameter ranges through prior predictive checks). In contrast to this approach, frequentist method are calibrated against all possible behaviors, which is not only impractical for complicated models it's also irrelevant given that the most extreme behaviors are unlikely to manifest in reality.
degeneracy	complex uncertainties that come from a mix of sources, including, non-identified models and cases where the data cannot well inform model parameters. When the data are not informing the parameters that we care about, this highlights a measurement issue. Identifying these problems in simulation studies can highlight when we need a better experimental design (e.g. sampling for more overlapping species across sites, or changing what we measure, etc.).
non-identifiability	when all parameters in a model cannot be uniquely identified with infinite data
prior	an distribution of reasonable values for a parameter based on fundamental biological and ecological understanding, previous research, or other sources
statistical model	Mathematical approximations of the true data generating process labeled with numerical parameters. Evaluating a statistical model on observed data gives a likelihood function that quantifies how compatible different parameters are with the observed data, and hence can be used to ‘fit’ the best parameters. In this article, we often simplify to ‘model.’ See also the Supplement: What’s a model?
posterior	product of the likelihood and prior; that is, a probability distribution that quantifies how compatible different model parameters are with both the observed data and the domain expertise encoded in the prior model.
workflow	a set of steps to achieve a goal, with those steps designed to help organize the process, and ideally make it more systematic

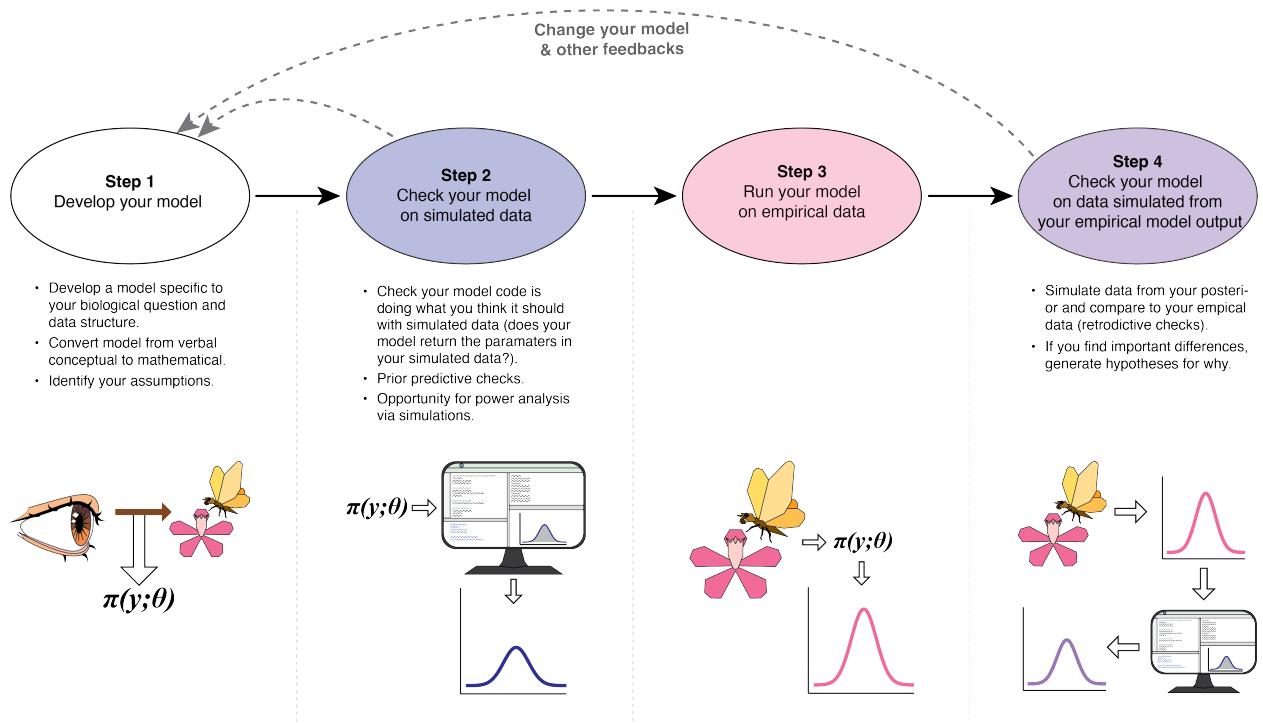


Figure 1: The four-step iterative workflow we outline can help design models for specific ecological questions, data and aims—which makes this a statistical workflow that can naturally become a scientific workflow. It makes the step that many of us focus on—running your model on your empirical data (Step 3)—far more straightforward and insightful by using simulations both before (Step 2) and after (Step 4) it to better understand the model and data together.

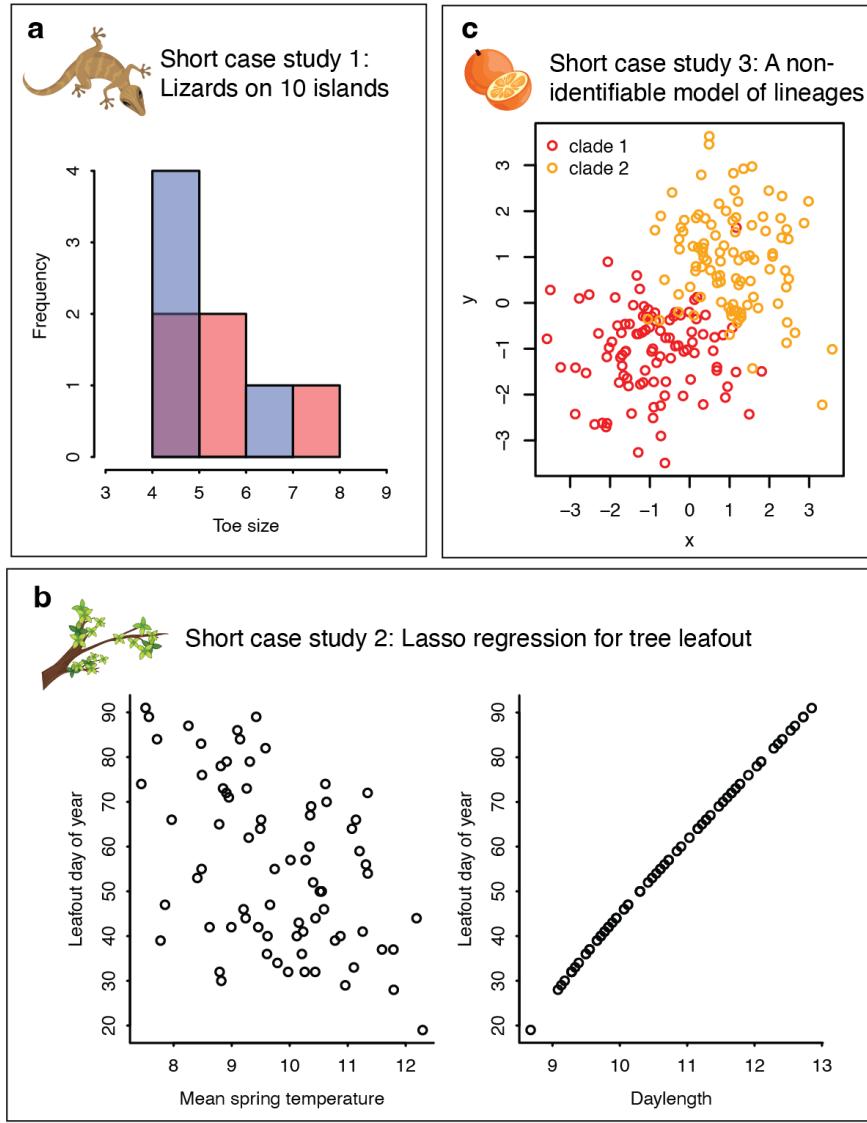


Figure 2: We provide three very simple examples of the first steps of this workflow as Supplements (in PDF from R Markdown files). One example (a) uses ordinary least squares regression considering a natural experiment on lizards on tropical islands, and simulating two different possible sample sizes. The next example (b) uses lasso regression to examine how environmental variables may predict tree leafout. The third example (c) shows several examples of non-identifiability in regression models. See supplements: ‘Is a sample size of five stormy islands enough?’; ‘Identifying predictors of tree leafout’ and ‘Three non-identifiable models, two of which are vital in biology.’

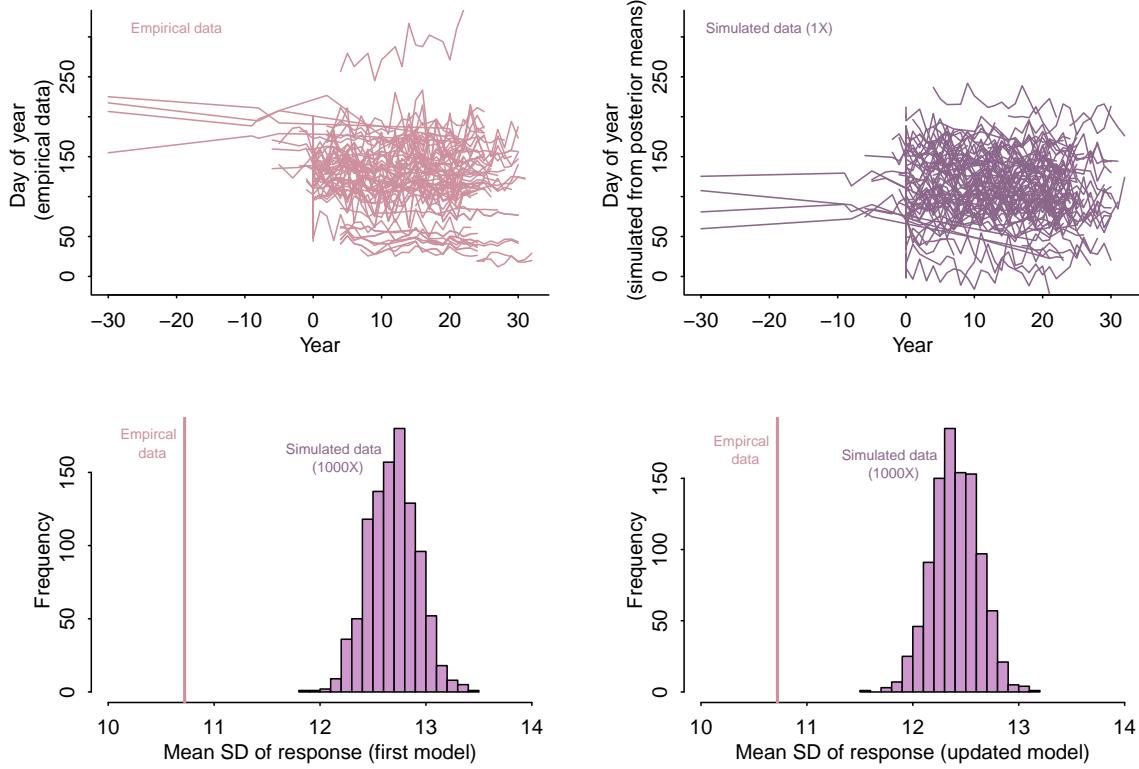


Figure 3: Example of retrodictive checks (Step 4) and feedbacks from time-series data of phenological events over time. The empirical data (top left, pink) looks similar to one simulated dataset (top right, purple), based on existing species number, their respective  $x$  data, and simulating from the parameters for each species, but the spread of the simulated data seems possibly higher. Repeating this retrodictive (or posterior predictive) check 1000 times, and taking the standard deviation (SD) of each simulated dataset, then looking at the resulting histogram confirms this (lower left in purple, empirical data SD in pink). This leads to an updated model, where the same retrodictive check looks slightly closer to the empirical data (lower right), but clearly still could be improved as part of additional feedbacks. These examples are shown in full in ‘Steps 1-4 in a Bayesian framework’ in the Supplement and available at: <https://github.com/lizzieinvancouver/bayesianflowsexample>.