Supplementary information: A simple explanation for declining temperature sensitivity with warming

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1   A first-hitting-time model of leafout

Our model follows the general understanding of how warm temperatures (forcing) trigger leafout in temperate deciduous trees (Chuine, 2000). We use a first-hitting-time model, which describes the first time a random process hits a threshold, because of its broad applicability and conceptual simplicity. We define leafout day, n_β, as the day, n, that cumulative daily temperature, S^n, hits the threshold, β.

We derive the relationship between daily temperature and leafout in two common scenarios. In the first, we take the average daily temperature up until the leafout date. In the second, we take the average daily temperature over a fixed window, such as March 1st to April 30th. In both cases, we discretize time since, although many biological processes depend continuously on time, research typically measures time in discretized units, such as days, weeks, or months.

1.1   Scenario 1: Using average daily temperature until the leafout date

We use the following notation:

$$n = \text{day since temperatures start to accumulate, } n = 0, 1, ..., N$$

$$X_n = \text{observed temperature on day } n$$

$$S_0^n = \sum_{i=0}^{n} X_i, \text{the cumulative daily temperature from day 0 to day } n$$

$$M_0^n = \frac{S_0^n}{n}, \text{the average daily temperature from day 0 to day } n$$

$$\beta = \text{the threshold of interest, } \beta > 0, \text{ (thermal sum required for leafout)}$$

$$n_\beta = \underset{n}{\text{argmin}}\ S_n > \beta, \text{the first day the cumulative daily temperature passes the threshold}$$

$$\text{(for example, day of year (doy) of leafout).}$$

We model X_n as a Gaussian random walk, $X_n \overset{\text{i.i.d}}{\sim} \text{normal}\,(\alpha_0 + \alpha_1 n, \sigma)$, where $\alpha_0 > 0$ is the average temperature on day $n = 0$, $\alpha_1 > 0$ is the day-over-day increase in average temperatures, and σ is the standard deviation. This model differs from the traditional Gaussian random walk because of the factor n.

This model has two important consequences:

(1) Leafout time is inversely related to average temperature at leafout time.

Under this model, $M_0^{n_\beta}$ and n_β are inversely proportional. To see why, assume for the moment that the cumulative daily temperature hits the threshold exactly on leafout day. That is, $S_0^{n_\beta} = \beta$. Then

$$M_0^{n_\beta} = \frac{S_0^{n_\beta}}{n_\beta} = \frac{\beta}{n_\beta}$$

rearranging yields

$$n_\beta = \frac{\beta}{M_0^{n_\beta}}$$

Many global change biology studies use linear regression to quantify the relationship between n_β and $M_0^{n_\beta}$ (or similar metrics, see Wolkovich et al., 2012; Piao et al., 2017; Keenan et al., 2020, for examples). Regressing n_β on $M_0^{n_\beta}$ finds a best fit line to the inverse curve, $n_\beta = \frac{\beta}{M_0^{n_\beta}}$. The relationship is linearized with the logarithm transformation: $\log(n_\beta) = \log(\beta) - \log(M_0^{n_\beta})$. That is, $\log(n_\beta)$ is linear in log-average daily temperature with slope -1 and intercept $\log(\beta)$.

(2) The variance of the average temperature may decreases as temperatures rise.

Under the model, the mean and variance of M_0^n are $\mathrm{E}(M_0^n|\alpha_0, \alpha_1) = \frac{1}{n}\sum_{i=0}^{n}(\alpha_0 + \alpha_1 i) = \alpha_0 + \alpha_1 \frac{(n+1)}{2}$ and $\mathrm{Var}(M_0^n|\alpha_0, \alpha_1) = \frac{\sigma^2}{n}$.

By the law of total variance,

$$\mathrm{Var}(M_0^n) = \mathrm{E}(\mathrm{Var}(M_0^n|\alpha_0, \alpha_1)) + \mathrm{Var}(\mathrm{E}(M_0^n|\alpha_0, \alpha_1))$$
$$= \frac{\sigma^2}{n} + \mathrm{Var}(\alpha_0 + \alpha_1 \frac{n+1}{2})$$
$$= \frac{\sigma^2}{n} + \mathrm{Var}(\alpha_0) + \frac{(n+1)^2}{4}\mathrm{Var}(\alpha_1) + (n+1)\mathrm{Cov}(\alpha_0, \alpha_1)$$

As temperatures rise and leafout date becomes earlier, the variance of the average temperature will decline—provided the variation in temperatures, σ, is sufficiently small.

1.2 Scenario 2: Using average daily temperature over a fixed window

We slightly modify the notation:

$n =$ day since temperatures start to accumulate, $n = 0, \ldots, a, \ldots, b$

$X_n =$ observed temperature on day n

$S_a^n = \sum_{i=a}^{n} X_i,$ the cumulative daily temperature from day a to day n

$M_a^n = \dfrac{S_a^n}{n-a},$ the average daily temperature from day a to day n

$\beta =$ the threshold of interest, $\beta > 0$, (thermal sum required for leafout)

$n_\beta = \underset{n}{\operatorname{argmin}} \; S_0^n > \beta,$ the first day the cumulative daily temperature passes the threshold

(for example, day of year (doy) of leafout).

As before, we model X_n as a Gaussian random walk, $X_n \overset{\text{i.i.d}}{\sim} \text{normal}\,(\alpha_0 + \alpha_1 n, \sigma)$, where $\alpha_0 > 0$ is the average temperature on day $n = 0$, $\alpha_1 > 0$ is the day-over-day increase in average temperatures, and σ is the standard deviation. We make the additional assumption that $X_n \geq 0$ for all n and $a < n_\beta < b$. That is, the cumulative temperature acquired by the plant always increases.

Note that

$$S_a^b \sim \text{normal}\left(\alpha_0(b-a) + \tfrac{\alpha_1}{2}(b-a)(b+a+1), \sigma\sqrt{b-a}\right)$$

$$M_a^b \sim \text{normal}\left(\alpha_0 + \tfrac{\alpha_1}{2}(b+a+1), \tfrac{\sigma}{\sqrt{b-a}}\right)$$

$$S_n^b - S_a^b \sim \text{normal}\left(\alpha_0(b-a-n) + \tfrac{\alpha_1}{2}((b-n)(b+n+1) - a(a+1)), \sigma\sqrt{b+a-n}\right)$$

so that

$$
\begin{aligned}
Pr\left(n_\beta \leq n \mid M_a^b = m\right) &= Pr\left(n_\beta \leq n \mid S_a^b = (b-a)m\right) \\
&= Pr\left(S_0^n \geq \beta \mid S_a^b = (b-a)m\right) \\
&= Pr\left(S_n^b \leq (b-a)m + S_0^a - \beta\right) \\
&= Pr\left(S_n^b - S_0^a \leq (b-a)m - \beta\right) \\
&= \Phi\left(\frac{(b-a)m - \beta - [\alpha_0(b-a-n) + \tfrac{\alpha_1}{2}((b-n)(b+n+1) - a(a+1))]}{\sigma\sqrt{b+a-n}}\right)
\end{aligned}
$$

The distribution of M_a^b shows that consequence (2) above still holds with this model. Consequence (1) no longer holds directly, but will in many situations where average daily temperature until an event correlates strongly with average daily temperature because the window is chosen based, in part, on the expected hitting time (Figs. S1-S2). We note two additional consequences:

(3) The conditional median is quadratic in n:

$$\frac{1}{2} \overset{\text{set}}{=} Pr\left(n_\beta \leq n \mid M_a^b = m\right)$$

$$\Rightarrow 0 = (b-a)m - \beta - [\alpha_0(b-a-n) + \frac{\alpha_1}{2}((b-n)(b+n+1) - a(a+1))]$$

$$\Rightarrow m = \frac{1}{(a-b)}[-\beta - \alpha_0(b-a-n) - \frac{\alpha_1}{2}((b-n)(b+n+1) - a(a+1))]$$

$$= \frac{1}{(a-b)}[-\beta - \alpha_0(b-a) - \frac{\alpha_1}{2}(b-a)(b+a+1)] + \frac{\alpha_0 + \frac{\alpha_1}{2}}{(a-b)}n + \frac{\frac{\alpha_1}{2}}{(a-b)}n^2$$

$$:= \gamma_0 + \gamma_1 n + \gamma_2 n^2$$

(4) The conditional mean and variance are sums of negative sigmoids, according to the following identities

$$E\left(n_\beta \mid M_a^b = m\right) = \sum_{n=0}^{\infty} Pr\left(n_\beta \geq n \mid M_a^b = m\right)$$

$$E\left(n_\beta^2 \mid M_a^b = m\right) = \sum_{n=0}^{\infty} n\, Pr\left(n_\beta \geq n \mid M_a^b = m\right)$$

1.3 Effect of shifting β on sensitivity

Many biological hypotheses of why plant sensitivities should decline suggest a shifting thermal sum required for leafout, due to declines in over-winter chilling or short photoperiods. However, the first-hitting model suggests that if β (thermal sum for leafout) is changing over time for any reason (increasing or decreasing), the regression coefficient from regressing leafout date on spring-time temperature (commonly referred to as 'sensitivity') should decrease. Using the total law of covariance: sensitivity from changing $\beta = Cov(Y,X)/Var(X)$:

$$Cov(Y,X)/Var(X) = [Cov(E(Y|\beta), E(X)) + E(Cov(Y,X|\beta))]/Var(X)(Cov(Y,X|\beta)/Var(X))$$

[Jonathan, can you work on the text here?] This, however, assumes X and β are independent and $Cov(E(Y|\beta), E(X)) < 0$. The latter is often true because increased mean temperatures (X) lead to earlier leafout dates (Y). The former would be false if mean temperatures (X) are correlated with over-winter chilling, or other covariates that lead to shifts in β. Then, likely $Var(X|\beta) \leq Var(X)$ and then the inequality above could be reversed.

2 Simulations of common hypotheses for declining sensitivity

We extended simulations from our first hitting-time model to examine two common biological hypotheses for declining sensitivities, and to understand how easily discernible biological shifts would be from the shifts always present when using linear models to estimate sensitivities.

First, we simulated the most often cited hypothesis (e.g., Fu et al., 2015; Piao et al., 2017): an increasing thermal sum threshold given declines in over-winter chilling. Experiments in controlled environments show that plants require greater thermal sums to budburst or leafout given lower chilling (e.g., Laube et al., 2014; Flynn and Wolkovich, 2018). Connecting chilling to leafout in observational data, however, is difficult as we know little mechanistically about what temperatures determine chilling (but see Rinne et al., 2011; van der Schoot et al., 2014, for recent developments in lab molecular work), and most models of chilling are based on statistical correlations (Erez and Lavee, 1971; **?**; Luedeling et al., 2009).

Without robust estimates of chilling, teasing out effects of chilling from forcing are likely impossible given identifiability issues. Data for a particular model are non-identifiable when multiple parameter (or parameters) values can be estimated from the same data. In the example of our simulated chilling + forcing model, the same leafout day can be driven by a lower thermal sum (β in our first-hitting time model) when chilling is higher, and higher thermal sums when chilling is lower, making attempts to separate chilling and forcing parameter values both non-identifiable. The model could become identifiable with an accurate covariate predicting chilling of forcing, which underlies efforts to model chilling (CITES) and 'pre-season' length (CITES, and discussed below in 'Methods & results using long-term empirical data from PEP725'), but these efforts are to date mostly based on statistical fits, which cannot easily overcome identifiability without additional information.

We further found that under this model—where the thermal sum (β) increases as over-winter chilling declines—would lead to larger estimated sensitivities given simple linear regression (see Fig. S3), in contrast with the general expectation in the literature that a larger role for chilling would reduce the estimated sensitivity. The actual effect with warming, however, depends on the covariation of X and β (discussed above) and highlights how difficult teasing apart relationships in observational spring phenology may be given correlations across multiple predictors (correlations that are likely exacerbated by climate change). Effects of biological shifts in the drivers of leafout are far more obvious in statistical estimates that include the non-linear nature of plants temperature response compared to linear estimates (see top panel of Fig. S4).

Second, we simulated an alternative hypothesis where warming causes the thermal sum to be reached before a required daylength threshold and plants then leaf out on the first day the daylength threshold is met (CITES). At its extreme this model produces the same leafout day (the day when the required daylength is met) across different temperatures and thus does produce a smaller estimated sensitivity. Estimated sensitivities, however, from a linear model do not necessarily decline depending on exact parameter values. Again this shift appears more obvious from statistical estimates that include the non-linear nature of plants temperature response compared to linear estimates (see Fig. S4).

3 Methods & results using long-term empirical data from PEP725

To examine how estimated sensitivities shift over time, we selected sites of two common European tree species (silver birch, *Betula pendula*, and European beech, *Fagus sylvatica*) that have long-term observational data of leafout, through the Pan European Phenology Project (PEP725, Templ et al., 2018). We selected these two species given that they were best represented for consistent data at the same sites over our study years for an early-leafout (*Betula pendula*) and a late-leafout (*Fagus sylvatica*) species (e.g., *Betula pendula* had 17 sites with leafout data from 1950-1960 and 2000-2010, while the next best option for an early-leafout species, *Alnus glutinosa*, had data for only five sites). We used sites with complete leafout data across both our 10-year (and 20-year) windows to avoid possible confounding effects of shifting sites over time (see Tables S1-S2 for numbers of sites per species x window).

To calculate temperature sensitivities, we used a European-wide gridded climate dataset *(E-OBS, Cornes et al., 2018)* to extract daily minimum and maximum temperature for the grid cells where observations of leafout for these two species were available. Determining the appropriate window over which to estimate a temperature sensitivity for spring plant phenology is an area of active research (CITES). Ideally researchers wish to separate windows over which chilling and forcing apply (if they can be cleanly separated CITES), but this is generally impossible given our limited understanding of the two process in natural systems (CITES). Researchers thus either use a pre-defined spring window (CITES) or use a statistical search to determine window attributes; for example, some use a set period then search for a start date (CITES), while others search for both a start date and window length (CITES). Given the non-identifiability of the simple chilling + forcing model described above ('Simulations of common hypotheses for declining sensitivity'), we do not feel there is sufficient evidence that statistical searches for pre-season windows will select biologically relevant periods related to forcing, and more easily could add additional issues of non-identifiability. Thus, we used pre-determined windows from 1 March to 30 April (60 d; we also present windows of 45 d, from 1 Mar to 15 Apr, and for 31 d, from 15 Mar to 15 Apr for comparison). Our window represents a period b in the spring when forcing is likely the dominant cue, and is similar to many other studies of temperature trees using pre-defined windows (CITES). We then estimated the sensitivity as a simple linear regression leafout day of year versus the mean daily temperature over the window ('slope' in Tables S1-S2), or a simple linear regression using logged versions of these predictors ('log-slope' in Tables S1-S2).

Our estimates of temperature sensitivity from a linear model using untransformed variables show a decline in sensitivity with recent warming for *Betula pendula* over 10 and 20-year windows, but no decline for *Fagus sylvatica*; using logged variables estimates appeared more similar over time or sometimes suggested an increase in sensitivity (see Figs. S6-S7, Tables S1-S2). This shift in estimated sensitivity when regressing with untransformed versus logged variables suggests the declining estimates with untransformed variables may not be caused by changes in the underlying mechanisms of leafout (i.e., reduced winter chilling) and driven instead by using linear regression for a non-linear process. This hypothesis is supported further by large declines in variance of leafout in recent decades.

Shifts in variance provide another hurdle to robust estimates of temperature sensitivity. Previous work has highlighted how shifting temperature variance (over space and/or time) could lead to shifting estimates of temperature sensitivities (Keenan et al., 2020), but our results stress that variance in both leafout and temperature are shifting. If both shift in step, estimates would not be impacted by changes in temperature variance, but our results suggest variance in temperature—for these data—has declined more than variance in leafout, though both have declined substantially in recent decades (Tables S1-S2).

Estimated sensitivities for the empirical data (PEP725) using logged variables are far lower than the value obtained in our simulations (-1). This likely results from a contrast between our simulations—where we can accurately define the temperature plants experience and the temporal window that drives leafout—and our empirical data, where we do not know how measured temperatures translate into the temperatures that plants accumulate and where we have no clear method to define the relevant temporal window (Güsewell et al., 2017).

These results highlight how the acceleration of biological time due to climate change requires researchers to clarify their assumptions. Expecting temperature sensitivity to remain constant as temperatures rise assumes the relationship between response and temperature is proportional. But the underlying biological processes suggest this relationship is seldom proportional, or even linear. In fact, when our model holds, declining sensitivity with rising temperatures should be the null hypothesis of any analysis of temperature sensitivity based on linear regression or similar methods.

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4 Tables

Table S1: Climate and phenology statistics for two species (*Betula pendula, Fagus sylvatica*, across 45 and 47 sites respectively) from the PEP725 data across all sites with continuous data from 1950-1960 and 2000-2010. ST is spring temperature from 1 March to 30 April, ST.leafout is temperature 30 days before leafout, and GDD is growing degree days 30 days before leafout. Slope represents the estimated sensitivity using untransformed leafout and ST, while log-slope represents the estimated sensitivity using log(leafout) and log(ST). We calculated all metrics for for each species x site x 10 year period before taking mean or variance estimates. See also Fig. S6.

years	species	mean (ST)			mean ST.lo	var (ST)			var (lo)	GDD	slope			log-slope		
		31	45	60		31	45	60			31	45	60	31	45	60
1950-1960	*Betula*	6.3	5.2	5.6	7.0	2.0	2.6	3.4	110.5	71.7	3.3	-2.1	-4.3	0.20	-0.09	-0.17
2000-2010	*Betula*	6.1	4.9	6.6	6.8	3.7	2.4	1.2	47.0	64.6	-0.1	0.5	-3.6	0.00	0.02	-0.22
1950-1960	*Fagus*	6.3	5.3	5.6	7.5	1.9	2.6	3.3	71.9	83.8	2.0	-0.9	-2.8	0.12	-0.05	-0.11
2000-2010	*Fagus*	6.2	5.0	6.7	7.7	3.8	2.4	1.2	38.3	86.7	-0.7	1.2	-3.4	-0.03	0.06	-0.20

Table S2: Climate and phenology statistics for two species (*Betula pendula, Fagus sylvatica*, across 17 and 24 sites respectively) from the PEP725 data across all sites with continuous data from 1950-2010. ST is spring temperature from 1 March to 30 April, ST.leafout is temperature 30 days before leafout, and GDD is growing degree days 30 days before leafout. Slope represents the estimated sensitivity using untransformed leafout and ST, while log-slope represents the estimated sensitivity using log(leafout) and log(ST). We calculated all metrics for for each species x site x 20 year period before taking mean or variance estimates. See also Fig. S7.

| years	species	mean (ST)			mean ST.lo	var (ST)			var (lo)	GDD	slope			log-slope		
		31	45	60		31	45	60			31	45	60	31	45	60
1950-1970	*Betula*	6.4	4.9	5.8	7.1	3.7	2.7	2.6	79.9	72.5	1.1	-1.0	-4.3	0.08	-0.03	-0.19
1970-1990	*Betula*	6.4	5.4	5.9	7.2	2.2	2.9	1.3	104.8	72.2	-0.0	-2.0	-6.1	-0.02	-0.07	-0.33
1990-2010	*Betula*	5.8	5.3	6.8	6.7	2.1	2.7	0.9	36.2	60.0	-1.2	0.0	-3.3	-0.07	0.00	-0.21
1950-1970	*Fagus*	6.1	4.7	5.6	7.6	3.8	2.8	2.7	63.4	86.0	1.0	-0.2	-3.1	0.05	0.00	-0.12
1970-1990	*Fagus*	6.2	5.2	5.6	7.5	2.3	3.0	1.3	56.2	81.3	-0.2	-1.3	-2.5	-0.01	-0.04	-0.16
1990-2010	*Fagus*	5.5	5.2	6.7	7.5	2.2	2.8	1.0	32.8	79.9	-0.6	0.1	-2.8	-0.03	0.01	-0.15

5 Figures
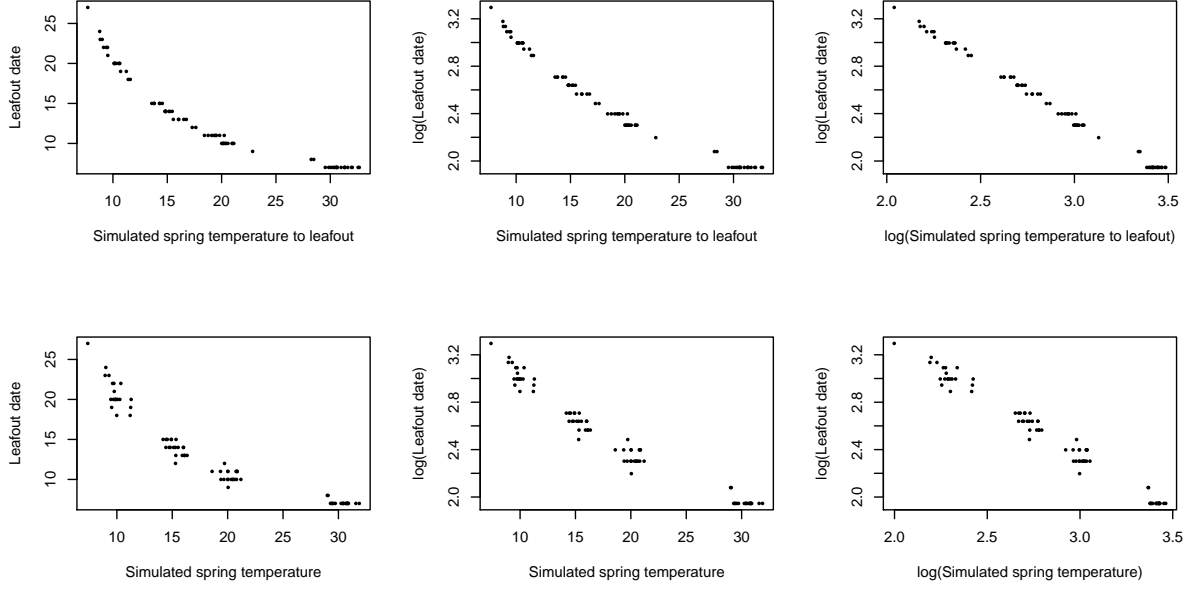
Figure S1: **Simulated leafout as a function of temperature across different temperatures highlights non-linearity of process.** Here we simulated sets of data where leafout constantly occurs at 200 growing degree days (thermal sum of mean daily temperatures with 0°C as base temperature) across mean temperatures of 10, 15, 20 and 30°C (constant SD of 4), we calculated estimated mean temperature until leafout date (top row) or across a fixed window (bottom row, similar to estimates of 'spring temperature'). While within any small temperature range the relationship may appear linear, its non-linear relationship becomes clear across the greater range shown here (left). Taking the log of both leafout and temperature (right) linearizes the relationship.
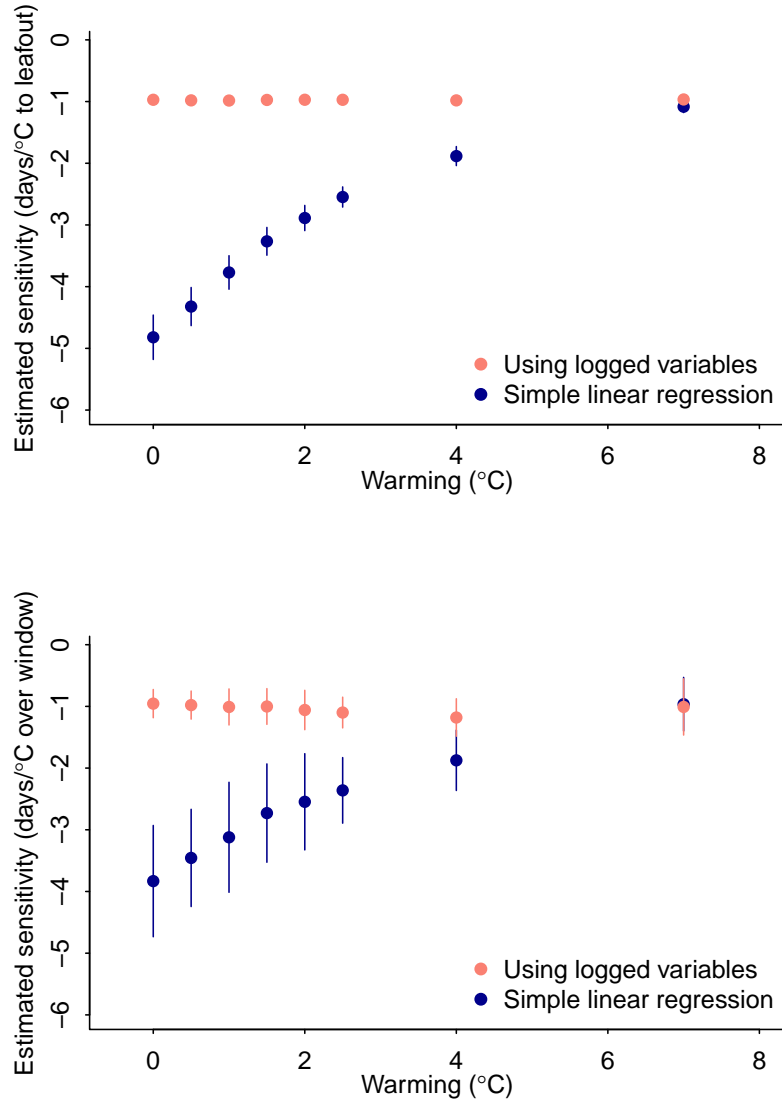
Figure S2: **A simple model generates declining sensitivities with warming.** We show declines in estimated sensitivities with warming from simulations (top: using average temperature until leafout, bottom: using a fixed window) with no underlying change in the biological process when sensitivities were estimated with simple linear regression ("Simple linear regression"). This decline disappears using regression on logged predictor and response variables ("Using logged variables").
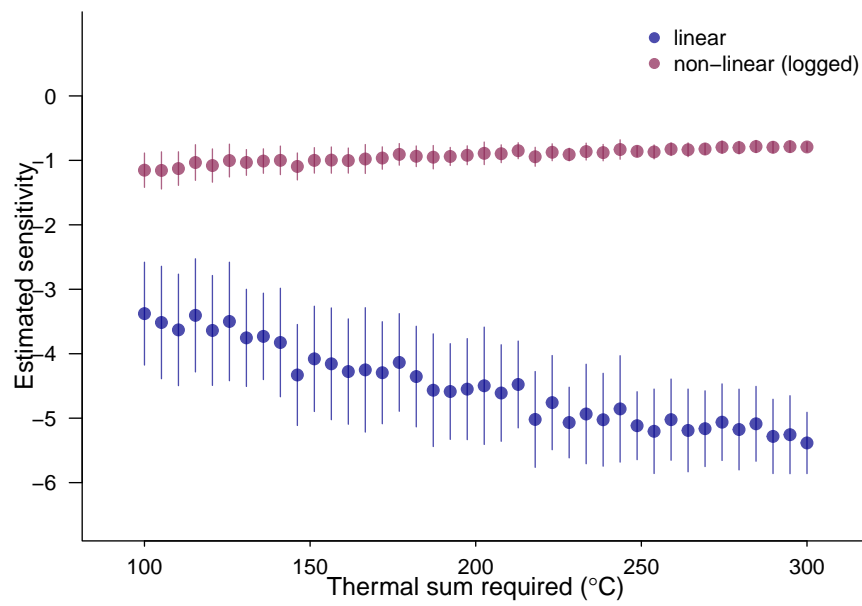
Figure S3: **Simulated leafout as a function of required thermal sum for leafout.** Here we simulated sets of data where leafout occurs at varying thermal sums (sum of mean daily temperatures with 0°C as base temperature).
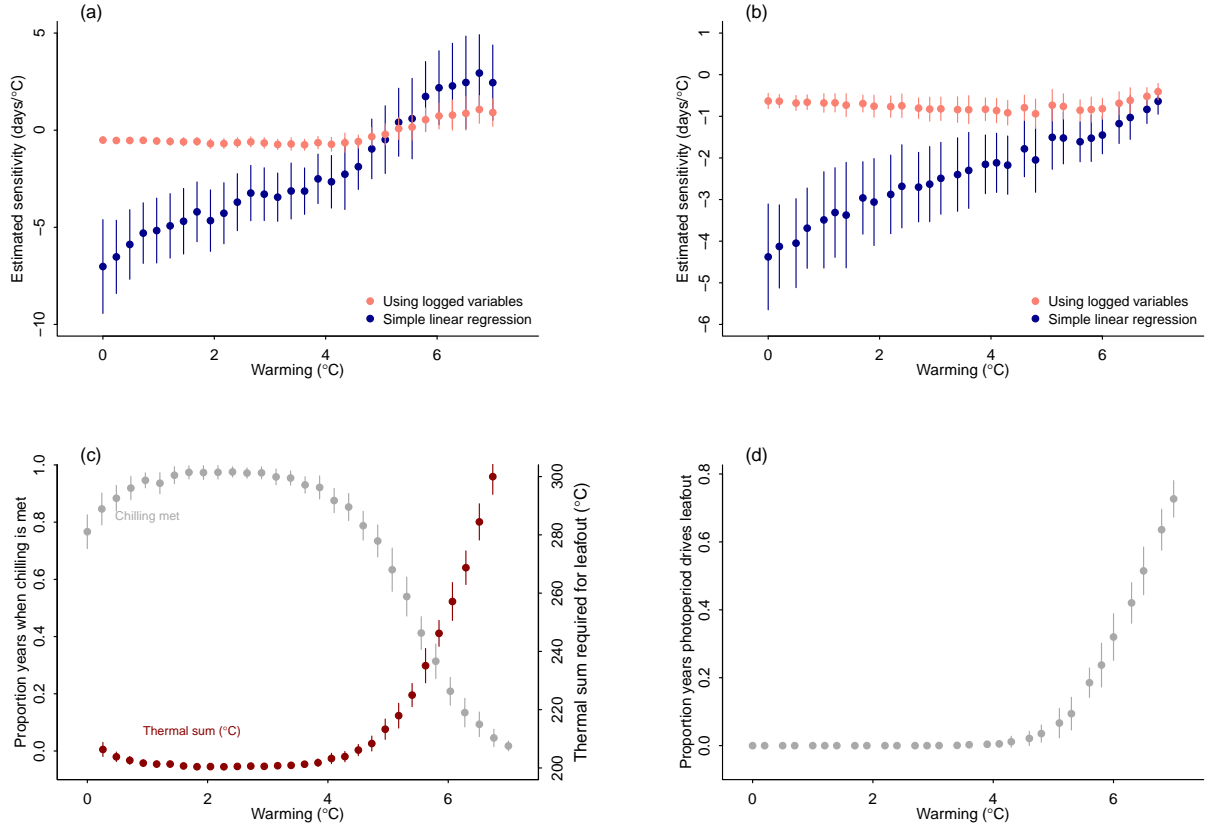
Figure S4: **Simulated leafout as a function of temperature across different levels of warming with shifts in underlying biology through lower chilling.** Here we simulated sets of data where leafout occurs at a thermal sum of 200 (sum of mean daily temperatures with 0°C as base temperature) when chilling is met, and requires a higher thermal sum when chilling is not met. We show estimated sensitivities in the top panel, and the shifting cues in the bottom panel. Simulated leafout as a function of temperature across different levels of warming with shifts in underlying biology through a daylength threshold. Here we simulated sets of data where leafout occurs at a thermal sum of 200 (sum of mean daily temperatures with 0°C as base temperature) as long as the daylength of that day is ≥ 12 hours; otherwise leafout occurs on the day when daylength is 12 hours. We show estimated sensitivities in the top panel, and the shifting cues in the bottom panel.
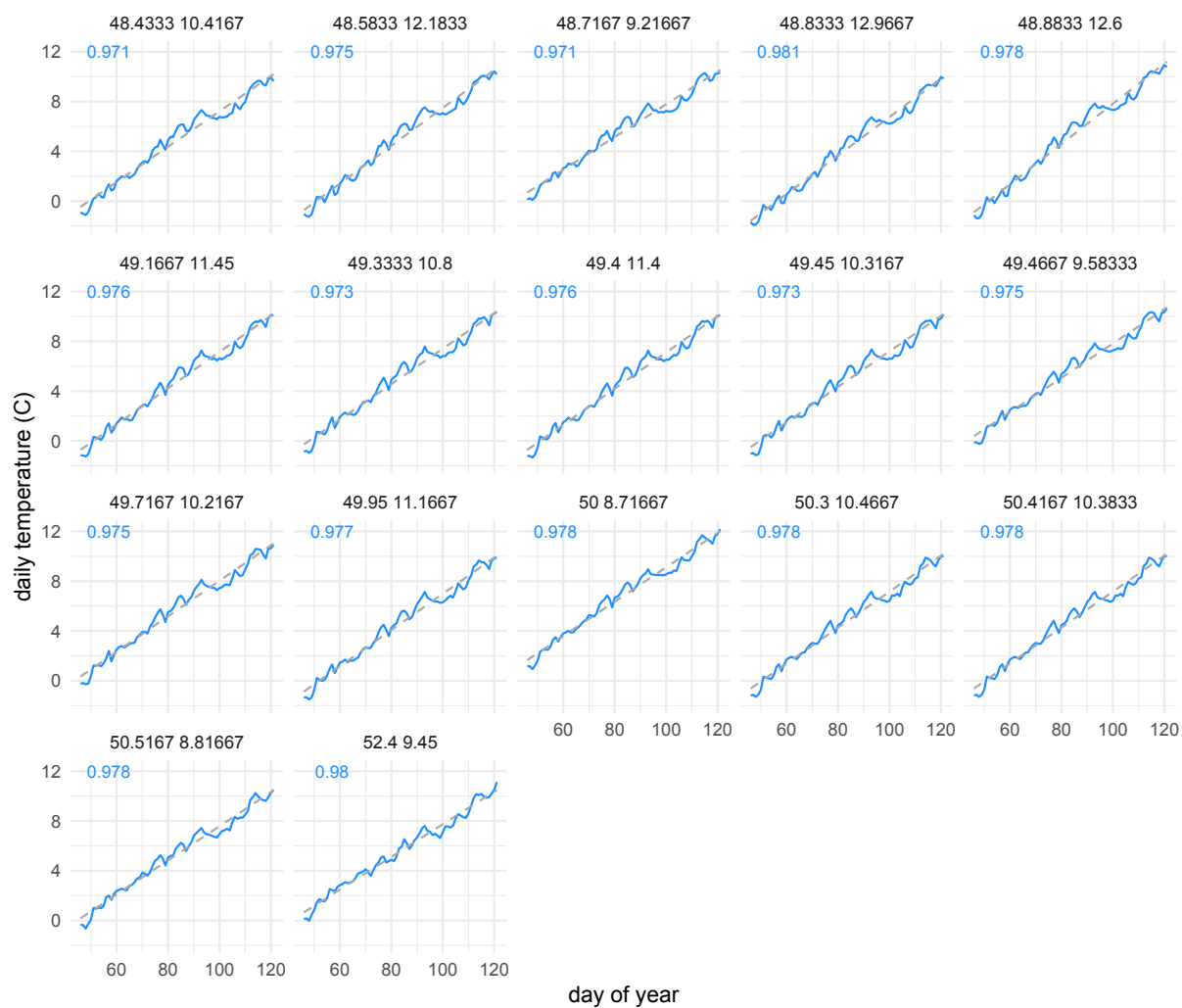
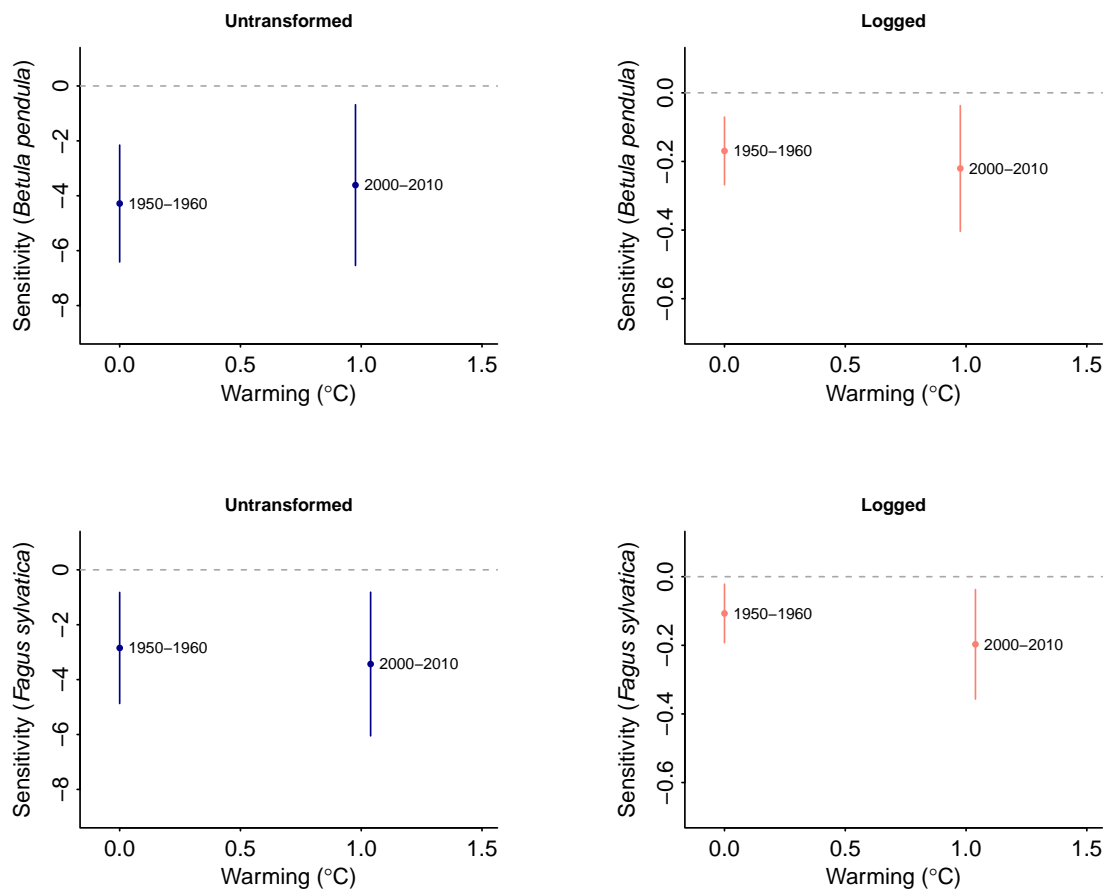Figure S5: **Mean daily temperatures at 14 PEP725 sites.**

Figure S6: **Sensitivities from PEP725 data using 10 year windows of data** for two species (top – *Betula pendula*, bottom – *Fagus sylvatica*; all lines show 78% confidence intervals from linear regressions). Amounts of warming are calculated relative to 1950-1960 and we used only sites with leafout data in all years shown here. See Table S1 for further details.
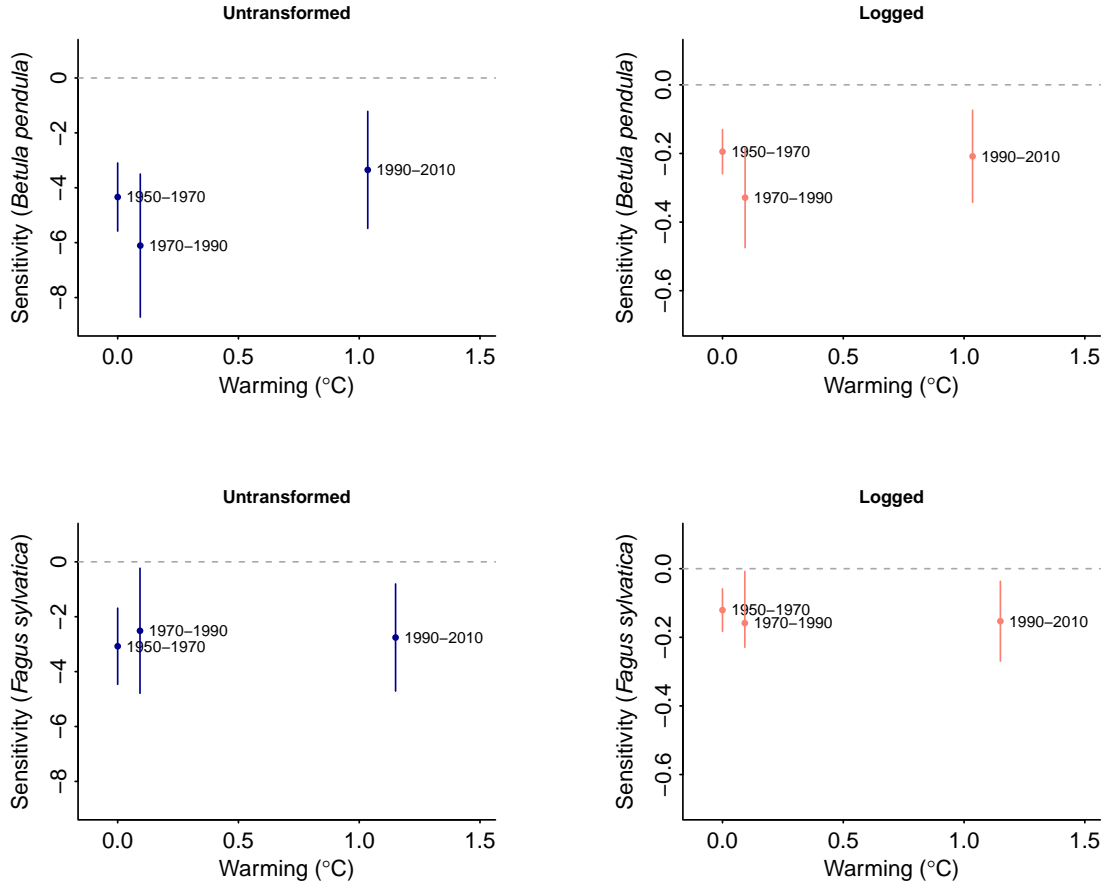
Figure S7: **Sensitivities from PEP725 data using 20 year windows of data** for two species (top – *Betula pendula*, bottom – *Fagus sylvatica*; all lines show 78% confidence intervals from linear regressions). Amounts of warming are calculated relative to 1950-1970 and we used only sites with leafout data in all years shown here. See Table S2 for further details.