# Supplemental materials: How environmental tracking shapes communities in stationary & non-stationary systems

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## 1 Literature review

We systematically reviewed the literature for studies examining tracking and other traits. We searched ISI in August 2019 for:

- 1. Topic: 'phenolog\* chang\*' and Title: phenolog\* AND trait\*
- 2. Topic: 'warming shift\*' AND trait\* and Title: phenolog\*
- 3. Topic: 'phenolog\* track\*' AND trait\* and Title: phenolog\*
- 4. Topic: 'phenolog\* sensitiv\*' AND trait\* and Title: phenolog\*

Most studies examined tracking as how a phenophase related to temperature (85% of all tracking metrics), followed by precipitation (10%, includes snow removal), followed by photoperiod (3%), the climate mode NAO (1%), water table depth (0.5%), and year (0.5%). Four of the 30 studies examined more than one major climate metric, though some measured many versions of temperature and/or precipitation metrics (e.g., 15 precipitation and/or temperature metrics considered in ?).

## 2 Model

We used a simple including within- and between-year dynamics to contribute to coexistence. The model includes a suite of species traits, including (and particularly relevant for our aims) traits controlling species response to the environment via germination each year and traits related to how species may bet-hedge across years (via a seedbank), as well as traits relating to resource competition each year. Within-season dynamics are controlled by resource competition resulting in fitness differences, while interannual variation in the environment provides opportunities for coexistence via fluctuation-dependent mechanisms (i.e., niche differences resulting from different germination functions).

Across years, for a community of n species, the seedbank (N) of species i at time t+1 is determined by the survival (s) of seeds that did not germinate in last season  $(1-g_i(t))$  plus new biomass  $(B_i)$  produced during the length of the growing season  $(\delta)$  converted to seeds at rate  $\phi$ :

$$N_i(t+1) = sN_i(t)(1 - q_i(t)) + \phi B_i(t+\delta)$$
(1)

The production of new biomass each season follows a basic R\* competition model: new biomass production depends on its resource uptake (f(R) converted into biomass at rate  $c_i$ ) less maintenance costs (m), with uptake controlled by a, u, and  $\theta$ :

$$\frac{\mathrm{d}B_i}{\mathrm{d}t} = c_i f(R) - mB_i \tag{2}$$

$$f(R) = \frac{aR^{\theta}}{1 + auR^{\theta}} \tag{3}$$

With the initial condition:

$$B_i(t+0) = N_i(t)g_i(t)b_0 \tag{4}$$

where  $b_0$  is the initial biomass per seed.

The resource (R) itself declines across a growing season due to uptake by all species and abiotic loss  $(\epsilon)$ :

$$\frac{\mathrm{d}R}{\mathrm{d}t} = -\sum_{i=1}^{n} f_i(R)B_i - \epsilon R \tag{5}$$

Germination depends both on the traits of the species and on the environment that year. The fraction of seeds germinating for a species each year is determined by the distance between  $\tau_i$ , a species characteristic, and  $\tau_p(t)$ , an attribute of the environment, which varies year-to-year. Germination fraction declines according to a Gaussian as the distance between  $\tau_i$  and  $\tau_p(t)$  grows (we refer to this distribution as the 'germination curve').

$$g_i(t) = g_{max}e^{-h(\tau_p(t) - \tau_i)^2}$$
 (6)

The model is designed for multiple conceptualizations (?); given our focus here, we consider  $\tau_p(t)$  to represent the environmental (abiotic) start of the growing season that varies from year-to-year and refer to it as the 'environmental start time.'  $\tau_i$  represents the 'intrinsic biological start time' for species i. How well matched a species is to its environment each year can be measured as

 $\tau_i$ - $\tau_p(t)$ , or the distance between the intrinsic (biological) start time and the environmental start time.

Adding phenological tracking to model:

Biological start time,  $\tau_i$ , can be considered a fixed characteristic of a species, but it may also respond to the environment dynamically through what we refer to as environmental tracking. Tracking ( $\alpha$ , which can vary between 0 to 1) decreases the distance between  $\tau_i$  and  $\tau_p(t)$ , i.e., moving the intrinsic start time closer to the environmental start time in that year, resulting in a higher germination fraction (e.g., species B in Fig. 3b-c).

$$\alpha_i \in [0, 1]$$

$$\hat{\tau}_i = \alpha_i \tau_p(t) + (1 - \alpha_i) \tau_i \tag{7}$$

Thus,

when 
$$\alpha_i = 0, \hat{\tau}_i = \tau_i$$
  
when  $\alpha_i = 1, \hat{\tau}_i = \tau_p(t)$ 

We refer to  $\hat{\tau}_i$  as 'effective biological start time' for species i (or 'effective  $\tau_i$ '). Simulations:

Using this model framework, we simulated a suite of two-species communities in stationary and non-stationary environments and examined persistence. As our interest is primarily in the role of environmental tracking, we focus on situations where species vary in their match to the environment through both a fixed response  $(\tau_i)$  or tracking  $(\alpha)$  and, thus, examined simulations with only non-trackers and simulations where all species had some level of tracking. We also varied species' resource use efficiency (via  $c_i$ ), yielding species with different  $R^*$  (where a lower  $R^*$  means a species can draw the resource down to a lower level and is thus considered the superior competitor). We focused on resource competition as it has been often linked to environmental tracking (see Box 'Trait trade-offs with tracking'). Each simulation was composed of two sequential parts: first, a 500-year stationary period where the underlying distribution of the environment does not change (but is stochastic, yielding year-to-year variation) followed by a 500-year non-stationary period where the underlying distribution of the environment shifts to an earlier start of season. Thus, only species that persisted through the first stationary period continued into the non-stationary period (see Supporting Information, SI, for more details). The two species coexistence model (see Equations 1-6 above) includes both interannual variation in the environment and intra-annual resource competition. The model was modified from ?, which was originally conceptualized for annual plants with a seedbank. Although the model can

In the model, the population census of seeds, N, occurs at time t at the end of the growing season (Equation 1). Seeds survive over winter at rate s and are lost from the population at rate (1-s). Surviving seeds germinate at rate  $g_i(t)$ . Seeds that do not germinate remain in the seed bank until the next census at t+1. Germination rate is a Gaussian function that declines with

be conceived of more generally, we use the language of annual plant germination for concreteness.

the distance between  $\tau_i$ , the species-specific preferred germination time, and  $\tau_p(t)$ , the timing of the resource pulse in year t, with maximum germination when  $\tau_i = \tau_p(t)$  (Equation 6, Fig. 3a,b). In cases that include tracking, the distance between  $\tau_i$  and  $\tau_{p(t)}$  can be reduced by tracking,  $\alpha_i$ , resulting in greater germination fraction (Equation 7).

Germinating seeds are converted to seedling biomass at rate  $b_0$  (Equation 4). Within year dynamics of the two species follows  $R^*$  competition for a single resource. The growing season begins with a single resource pulse  $R_0(t)$ . Both species consume the resource at rate f(R) (Equation 3), and the resource undergoes abiotic loss (e.g., evapotranspiration) at rate  $\epsilon$  (Equation 5). Differences in  $R_i^*$  were generated by differences in conversion efficiency,  $c_i$ . Species were otherwise identical in resource update parameters  $(a, u, \text{ and } \theta)$  and in metabolic loss (m). Biomass at the end of the season is converted into seeds at rate  $\phi$ , and the population of seeds is censused at t+1.

Interannual variation occurs in both the timing and the amount of the resource pulse. The timing of the resource pulse varies from year to year and is given by  $\tau_p(t)$ , which is drawn from a  $\beta$  distribution. The amount of resource available at the beginning of each season,  $R_0(t)$ , varies from year to year and is drawn from a log-normal distribution. Each model run is comprised of a 500 year stationary period and a 500 year nonstationary period. During the stationary period,  $R_0(t)$  and  $\tau_p(t)$  are each drawn from a stationary distribution. During the nonstationary period, the timing of the resource pulse,  $\tau_p(t)$ , gradually shifts earlier in the season (Fig. ??). For the model runs displayed in Fig. 4 and Fig. 5, this shift in the timing of the resource pulse is the only change in the environment during the nonstationary period. We also discuss model runs in which the amount of resource,  $R_0(t)$ , declines during the nonstationary period along with the shift in timing,  $\tau_p(t)$  (Fig. ??).

To simulate competitive dynamics, both species were initialized with a census size of N(0) = 100 per unit area, and the temporally varying parameters  $R_0(t)$  and  $\tau_p(t)$  were generated for the stationary and nonstationary periods. Species-specific parameters  $(c_i, \tau_i, \text{ and } \alpha_i)$  were drawn from uniform random distributions with the ranges given in Table ??. All other parameters were identical between species (Table ??). Within-year  $R^*$  competition dynamics were solved using an ode solver (ode in the R package deSolve) and ended when the resource was drawn down to  $min(R^*)$ , i.e., the  $R^*$  value of the better resource competitor. The end of season biomass of each species was converted to seeds, and the populations were censused. At each census, a minimum cutoff was applied to define extinction from the model. Note that "coexistence" in this model is defined by joint persistence through time and not by low density growth rate.

## 3 References

4 Tables & figures

Table S1: Table of parameter values, definitions, and units.

Parameter	Value(s)	parameter values, definitions, and Definition	Unit Unit	
$\frac{1}{N_i}$	$init cond N_i(0) =$		seeds per unit area	
1 1 2	$100; \min(N_i(t)) =$	i	seeds per unit area	
	$100, min(10) = 10^{-4}$			
s	0.8	survival of species $i$	unitless	
$B_i$	cf. Eqn 2	biomass of species $i$	biomass	
$R_0$	$\sim log N(\mu, \sigma) mu =$	annually varying initial value	resource	
100	$log(2), \sigma = 0.2$	of resource at the beginning of	resource	
	$log(z), \sigma = 0.2$	the growing season		
	$\sim$ Unif(8,20)	conversion efficiency of $R$ to	biomass resource	
$c_i$	$\sim$ 0 IIII(8,20)		resource	
	0.05	biomass of species i	$days^{-1}$	
m	0.05	maintenance costs during	g days	
	20	growth season i	1 -1	
a	20	uptake increase as $R$ increases	$days^{-1}$	
		for species i	(days)(biomass)	
u	1	inverse of max uptake for	resource	
		species i		
θ	1	shape of uptake for species $i$	unitless	
$\phi$	0.05	conversion of end-of-season	biomass <sup>-1</sup> , but concep-	
		biomass to seeds	tually $\frac{\text{seeds}}{(\text{biomass})(\text{seeds})}$	
$\epsilon$	1	abiotic loss of $R$	$days^{-1}$	
$g_{max}$	0.5	max germination rate of	unitless	
		species		
h	100	controls the the rate at which	$days^{-2}$	
		germination declines as $\tau_p$		
		deviates from optimum for		
		species $i$		
$g_i$	cf. Eqn 6	germination rate	unitless	
$ au_p$	$\sim \beta(10, 10)$	timing of pulse	days	
$ au_i$	$\sim \text{Unif}(0.1,0.9)$	timing of max germination of	days	
		species $i$		
$\alpha_i$	$\sim \text{Unif}(0,1)$	phenological tracking of	unitless	
		species $i$		
$b_0$	1	biomass of a seedling	biomass seeds	
f(R)	cf. Eqn 3	resource uptake rate for	resource	
• \ /	•	species $i$	(days)(biomass)	
t	1	annual timestep	years	
$0 \to \delta$	determined by rate	time during the growing sea-	days	
J / J	of resource depletion	son		

Table S2: Summary of traits related to phenological tracking in the literature and whether papers reported statistical evidence that they were linked or not. See Table S2 for an extended version.

Trait	n linked	n not linked	
diet traits	0	3	
early/late phenophase	10	4	
habitat traits	1	3	
height	1	0	
hibernation stage	0	3	
leaf/shoot size	1	0	
migration traits	3	2	
mobility	1	3	
nativeness	1	3	
niche breadth	3	2	
other Lepidopteran traits	3	4	
other bird traits	1	1	
other leaf traits	4	3	
other plant traits	1	1	
overwintering	2	1	
range traits	1	4	
root traits	3	0	
seed weight/size/number	1	2	
woody/herbaceous	1	0	

Table S3: Summary of results from literature on phenological tracking showing which phenophases researchers found were linked to which traits, or not.

Taxa	Phenophase	Trait	n linked	n not linked
Lepidoptera	activity length	hibernation stage		1
Lepidoptera	activity length	migration traits		1
Lepidoptera	activity length	other Lepidopteran traits	1	
Lepidoptera	appearance/collection date	diet traits		1
Lepidoptera	appearance/collection date	early/late phenophase	2	
Lepidoptera	appearance/collection date	habitat traits		2
Lepidoptera	appearance/collection date	hibernation stage		1
Lepidoptera	appearance/collection date	migration traits	1	
Lepidoptera	appearance/collection date	mobility		2
Lepidoptera	appearance/collection date	niche breadth	2	1
Lepidoptera	appearance/collection date	other Lepidopteran traits	1	2
Lepidoptera	appearance/collection date	overwintering	2	
Lepidoptera	appearance/collection date	range traits	1	2
Lepidoptera	flight timing	early/late phenophase	1	1
Lepidoptera	flight timing	mobility	1	1
Lepidoptera	flight timing	niche breadth		1
Lepidoptera	flight timing	other Lepidopteran traits		1
Lepidoptera	flight timing	overwintering		1
Lepidoptera	flight timing	range traits		1
Lepidoptera	last/median emergence dates	diet traits		1
Lepidoptera	last/median emergence dates	habitat traits		1
Lepidoptera	last/median emergence dates	hibernation stage		1
Lepidoptera	last/median emergence dates	migration traits		1
Lepidoptera	last/median emergence dates	other Lepidopteran traits	1	1
passerine birds	breeding time	diet traits		1
passerine birds	breeding time	habitat traits	1	
passerine birds	breeding time	migration traits	2	
passerine birds	breeding time	niche breadth	1	
passerine birds	breeding time	other bird traits	1	1
plants	budbreak/leafing	early/late phenophase	3	1
plants	budbreak/leafing	nativeness		1
plants	budbreak/leafing	other leaf traits	2	1
plants	budbreak/leafing	range traits		1
plants	flowering/fruiting	early/late phenophase	4	2
plants	flowering/fruiting	height	1	
plants	flowering/fruiting	leaf/shoot size	1	
plants	flowering/fruiting	nativeness	1	2
plants	flowering/fruiting	other leaf traits	$\frac{1}{2}$	2
plants	flowering/fruiting	other plant traits	1	1
plants	flowering/fruiting	root traits	3	-
plants	flowering/fruiting	seed weight/size/number	1	2
plants	flowering/fruiting	woody/herbaceous	1	_

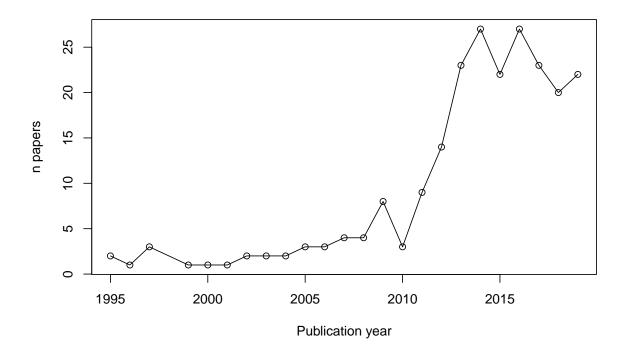
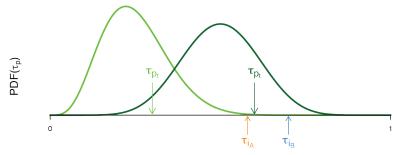
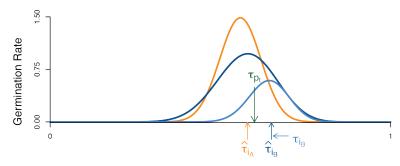


Figure S1: Trends in all papers using search terms over time. Of papers from which we could extract data all 25 of 30 were published in 2011 or onward.

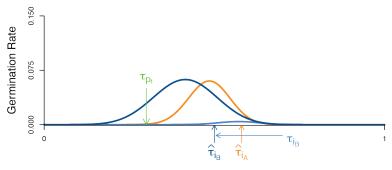
### (a) Distributions of resource timing under stationary and non-stationary periods



#### (b) Realized germination rates (draw from stationary period)



#### (c) Realized germination rates (draw from end of non-stationary period)



Timing of Resource Pulse,  $\tau_p$ 

Figure S2: The distributions of the environment (a) and species' germination for two sample years (b-c) in our seed germination model. (a) The timing of the resource pulse  $(\tau_p(t))$ , which defines the environmental start of season, is  $\beta$ -distributed with parameters  $\beta(10, 10)$  during the stationary period (dark green) shifting to  $\beta(5, 15)$  through the nonstationary period (light green). (b) Realized germination rate as a function of  $\tau_p(t)$  for two species during the stationary period: the orange line is a non-tracking species A with preferred germination time,  $\tau_{iA}$ , that is close to the mean of the stationary period; the blue lines show the difference in realized germination rate of a tracking species with a preferred germination time,  $\tau_{iB}$ , that is further from the mean of the stationary period both without (light blue) and with (dark blue) the effect of tracking; note the shift from  $\tau_{iB}$  to  $\tau_{iB}$ . (c) Realized germination rate of species A and species B at the end of the nonstationary period. Note the change in axes from (b) to (c) shows the decline in overall germination rate as the environment moves away from the preferred germination time of both species.

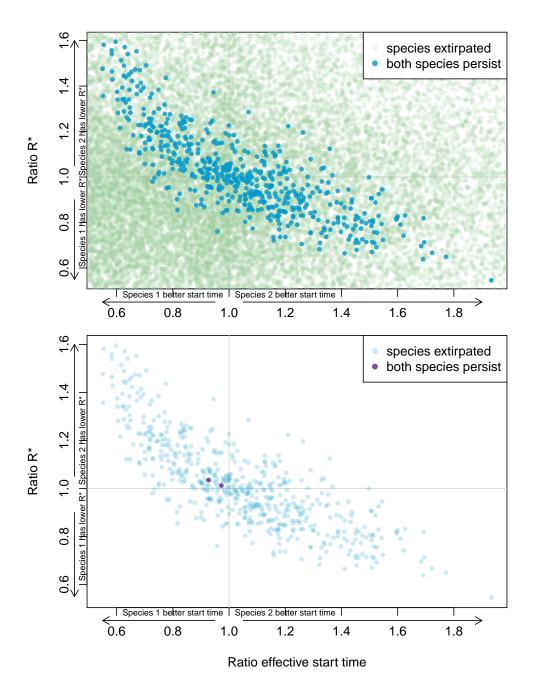


Figure S3: How non-stationarity reshapes two-species communities in a simple model where effective start time (X axis: species 1/species 2) trades off with  $R^*$  (Y axis: species 1/species 2): each point represents one two-species community color-coded by whether both species persisted or one or more species was extirpated through 500 years of a stationary environment (top), followed by an additional 500 years of non-stationary environment (bottom), where the abiotic start of the season shifts earlier. Only two-species communities that persisted through the stationary period are shown in the bottom panel. See Fig. ?? for an alternative version of this figure detailing one-species outcomes.

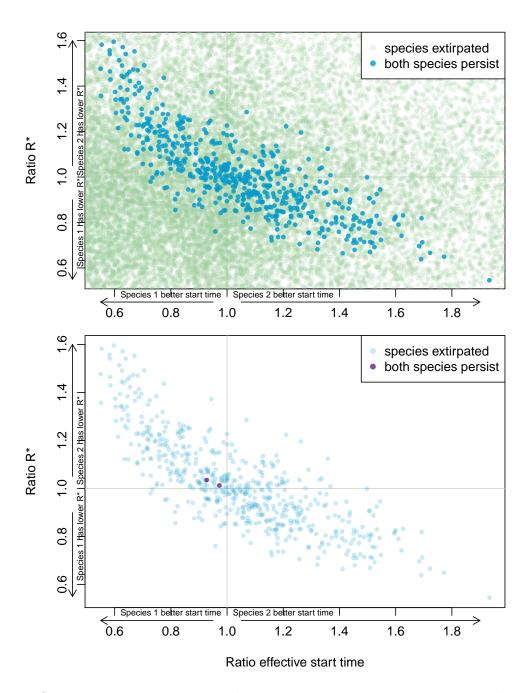


Figure S4: How non-stationarity reshapes two-species communities in a simple model where effective start time (X axis: species 1/species 2) trades off with  $R^*$  (Y axis: species 1/species 2): each point represents one two-species community color-coded by whether both species persisted or one or more species was extirpated through 500 years of a stationary environment (top), followed by an additional 500 years of non-stationary environment (bottom), where the abiotic start of the season shifts earlier. Only two-species communities that persisted through the stationary period are shown in the bottom panel. See Fig. ?? for an alternative version of this figure detailing one-species outcomes.

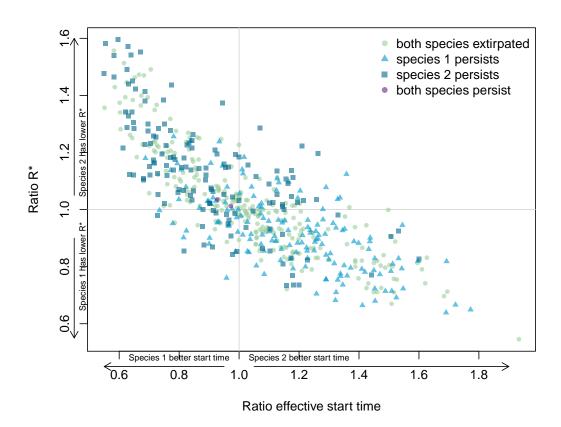


Figure S5: How non-stationarity reshapes two-species communities in a simple model where effective start time (X axis: species 1/species 2) trades off with  $R^*$  (Y axis: species 1/species 2): each point represents one two-species community that persisted through 500 years of stationary dynamics while the shape and color represent the outcome for that two-species community of 500 years of non-stationarity, where the abiotic start of the season shifts earlier.

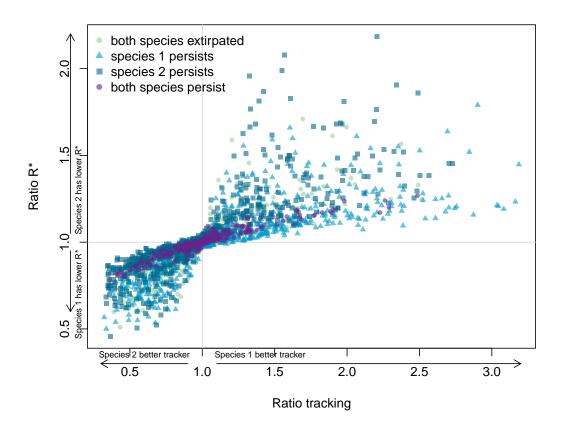


Figure S6: How non-stationarity reshapes two-species communities in a simple model where tracking (X axis: species 1/species 2) trades off with  $R^*$  (Y axis: species 1/species 2): each point represents one two-species community that persisted through 500 years of stationary dynamics while the shape and color represent the outcome for that two-species community of 500 years of non-stationarity, where the abiotic start of the season shifts earlier.