## 1 Model

For our example, we adapt the model from Wolkovich & Donahue 2020, which is itself an adaptation of a common model of community dynamics, often conceptualized for annual plants with a seedbank (as we do here). A more detailed description of the model can be found in Wolkovich & Donahue 2020.

In this model, a community of n species, the seedbank (N) of species i at time t+1 (where t represented interannual time) is determined by the survival (s) of ungerminated seeds from the previous season  $(1-g_i(t))$  plus new biomass  $(B_i)$  produced during the following growing season  $(\delta)$ , which is converted to seeds at rate  $\phi$ :

$$N_i(t+1) = sN_i(t)(1 - g_i(t)) + \phi B_i(t+\delta)$$
(1)

Basic  $R^*$  competition controls new biomass each season, depending on species i's resource uptake (f(R)) converted into biomass at rate  $c_i$ ) minus maintenance costs (m), with resource uptake controlled by species-level parameters that define how the uptake increases as R increases (a), the inverse of the maximum uptake (u), and the shape of the uptake  $(\theta)$ :

$$\frac{\mathrm{d}B_i}{\mathrm{d}t} = (c_i f(R) - m)B_i + G_i(t) \tag{2}$$

$$f(R) = \frac{aR^{\theta}}{1 + auR^{\theta}} \tag{3}$$

The resource (R) itself declines across a growing season due to uptake by all species and abiotic loss  $(\epsilon)$ :

$$\frac{\mathrm{d}R}{\mathrm{d}t} = -\sum_{i=1}^{n} f_i(R)B_i - \epsilon R \tag{4}$$

Our model departs from many similar community models but explicitly modeling germination over the season  $(G_i(t))$  by modeling more of the physiology of germination—specifically that species may delay germination beyond the start of the season (according to the resource) depending on winter conditions, including what we call 'chilling.' Germination thus depends both on the traits of the species and on the environment each year. To achieve this, we modeled  $G_i(t)$  germination as a time dependent forcing function that adds daily biomass to the ODE according to a Hill equation:

$$G_i(t) = N_0 s_i b_i g_i(t) \tag{5}$$

$$g_i(t) = g_{max,i} \left( \frac{\text{within-season-time}^{nH}}{\tau_{g50}^{nH} + \text{within-season-time}^{nH}} \right)$$
 (6)

where  $b_i$  is the biomass per seed and where  $\tau_{g50}$  is a Poisson random variable for the days of delay due to chilling,  $\xi$ , according to:

$$\tau_{g50} \sim \text{Poisson}(\tau_{delay})$$
(7)

$$\tau_{delay} = \tau_{max} e^{-\tau_{\xi}\xi} \tag{8}$$

ADD: While explaining the model, will need to reference (and include in figures), the plots that are made in Prieff\_Species.R to visualize.

## Simulations:

Given an overview of simulations performed, be sure to mention: two-species communities, species vary in what and explain a little what that does (for example: We varied species' resource use efficiency (via  $c_i$ ), yielding species with different  $R^*$  (a metric of resource competition where a lower  $R^*$  means a species can draw the resource down to a lower level and is thus considered the superior competitor)) and then state something like "All other parameters were identical between species (Table S1)." Also need: starting conditions (for example: both species were initialized with a census size of N(0) = 100 per unit area, and the temporally varying parameters  $R_0(t)$  and  $\tau_p(t)$  were generated) and then some re-wording of this:

Within-year  $R^*$  competition dynamics were solved using an ode solver (ode in the R package deSolve) and ended when the resource was drawn down to  $min(R^*)$ , i.e. the  $R^*$  value of the better resource competitor. The end-of-season biomass of each species was converted to seeds, and the populations were censused. At each census, a minimum cutoff was applied to define extinction from the model. Note that 'coexistence' in this model is defined by joint persistence through time and not by low density growth rate.

Table S1: Parameter values, definitions, and units.

Parameter	Value(s)	meter values, definitions, and un Definition	Unit
$N_i$	initial conditions	census of seedbank of species	seeds per unit area
·	$N_i(0) =$	$\mid i \mid$	1
	$100; min(N_i(t)) =$		
	$10^{-4}$		
s	0.8	survival of species $i$	unitless
$B_i$	see Eqn 2	biomass of species $i$	biomass
$R_0$	$\sim log N(\mu, \sigma) mu =$	annually varying initial value	resource
	$log(2), \sigma = 0.2$	of resource at the beginning of	
		the growing season	
$\xi_0$	~??	chilling	chilling
$c_i$	$\sim$ Unif(8,20)	conversion efficiency of $R$ to	biomass resource
		biomass of species $i$	
m	0.05	maintenance costs during	$days^{-1}$
		growth season $i$	
a	20	uptake increase as $R$ increases	$days^{-1}$
		for species $i$	
u	1	inverse of maximum uptake	(days)(biomass) resource
		for species $i$	resource
$\theta$	1	shape of uptake for species $i$	unitless
$\phi$	0.05	conversion of end-of-season	biomass <sup>-1</sup> , but concep-
		biomass to seeds	tually $\frac{\text{seeds}}{(\text{biomass})(\text{seeds})}$
$\epsilon$	1	abiotic loss of $R$	$days^{-1}$
$g_{max}$	0.5	maximum germination rate of	unitless
		species	
h	100	controls the the rate at which	$days^{-2}$
		germination declines as $\tau_p$	
		deviates from optimum for	
		species $i$	
$g_i$	see Eqn 6	germination rate	unitless
$ au_g$	$\sim \beta(?,?)$	days of delay (given on weeks	days
		of chilling)	
$ au_{g_{50}}$	$\sim \operatorname{Pois}(\tau_g)$	??	days
$\xi_{ au}$	~ ?,?	rate of delay (given weeks of	days/week
		chilling) $i$	
$b_i$	1	biomass of a seedling	biomass seeds
f(R)	see Eqn 3	resource uptake rate for	resource (days)(biomass)
		species $i$	
t	1	annual timestep	years
$0 \to \delta$	determined by rate	time during the growing sea-	days
	of resource depletion	son	