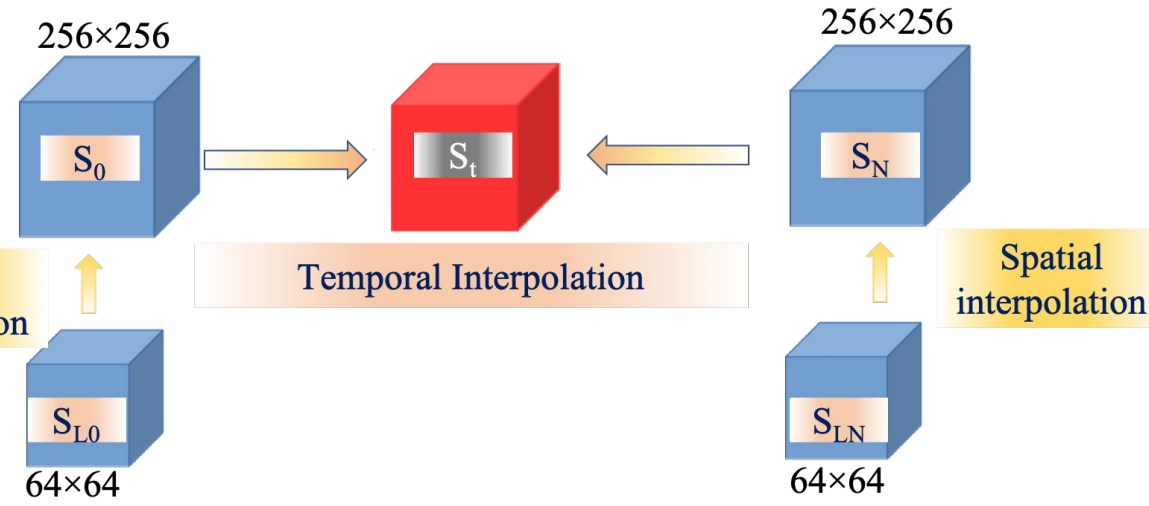


## Introduction

Fluid dynamics simulations are **computationally expensive** and **require massive storage**.

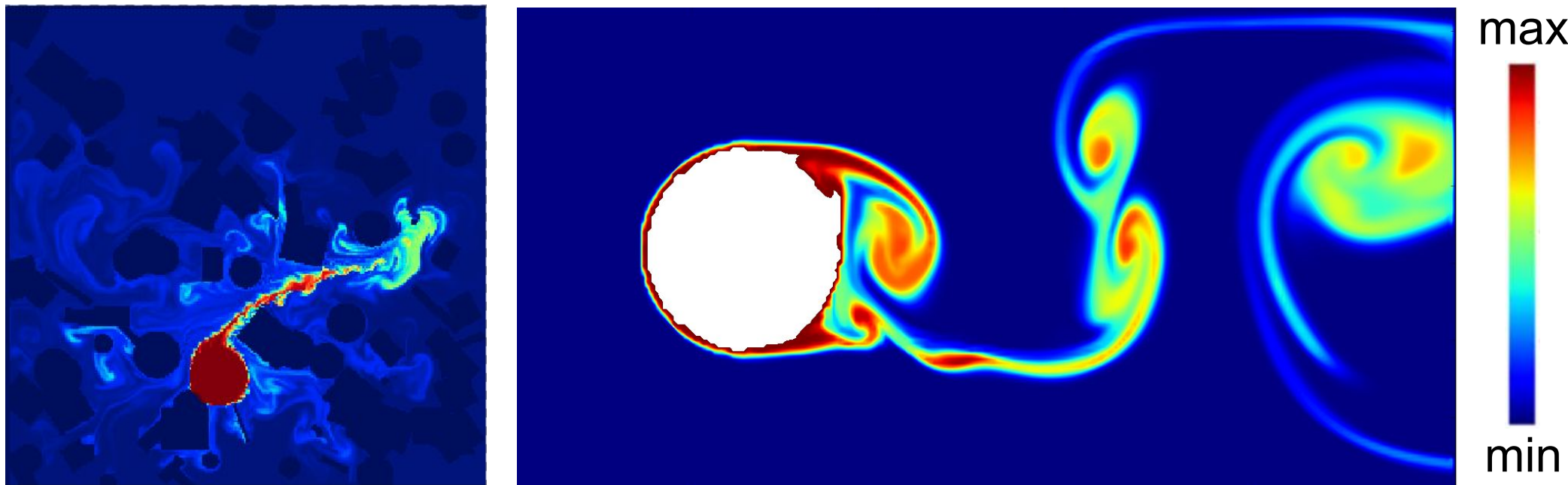
- Datasets saved are often **temporally coarse**.
- Massively parallel computation** needed for simulation.

**Solution:**  
Use **spatial and temporal interpolation** to re-generate fine-grain data from coarse grain-data



## Dataset

Deep-learning models require large, diverse datasets across several physical scenarios. Currently, the interpolation is performed **only on the density field**. We **write our own simulations** using an open source solver, **MantaFlow**. We generate **40,000+ data points** across two types of scenes - Plume and Karman Vortex Street.

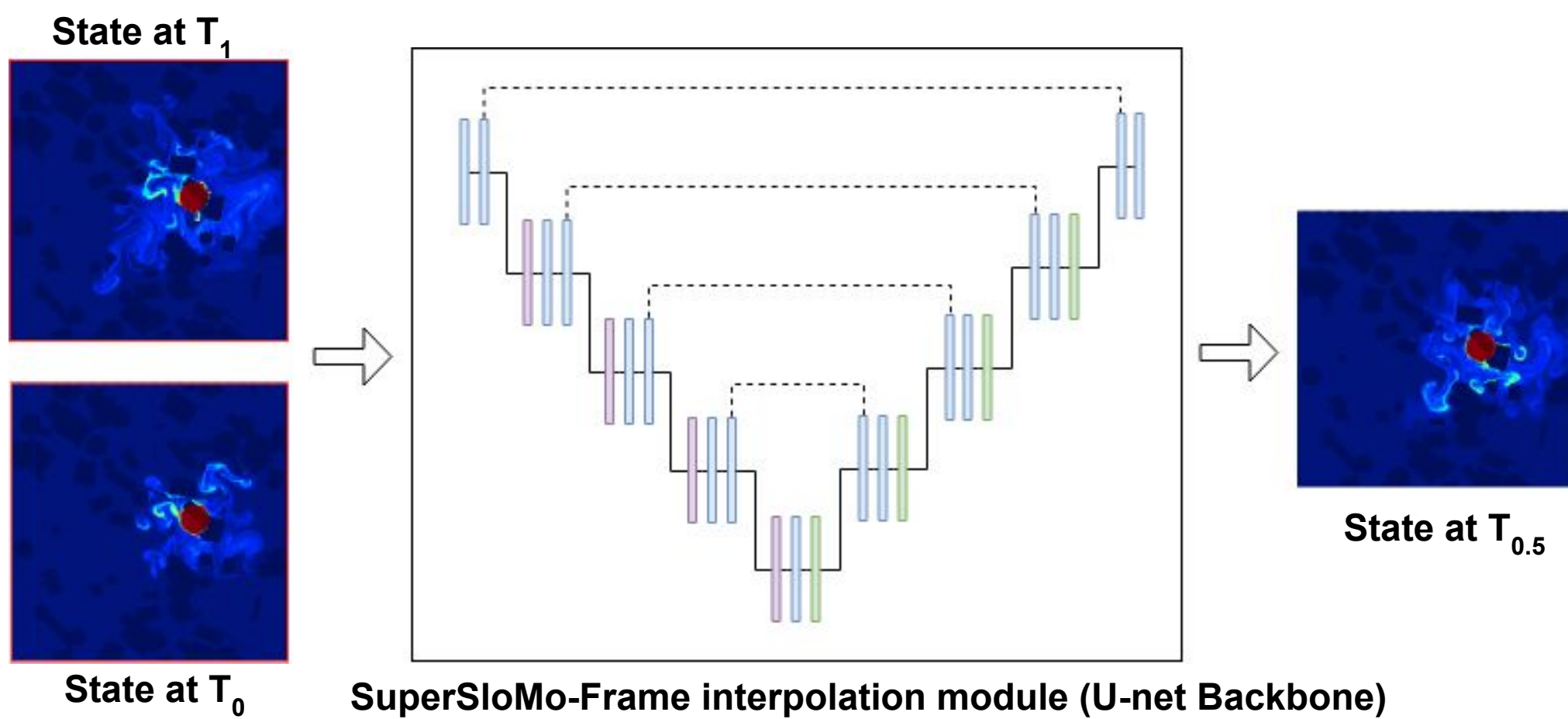


Density field of 2D Plume (left) and Karman Vortex Street (right)

## Models

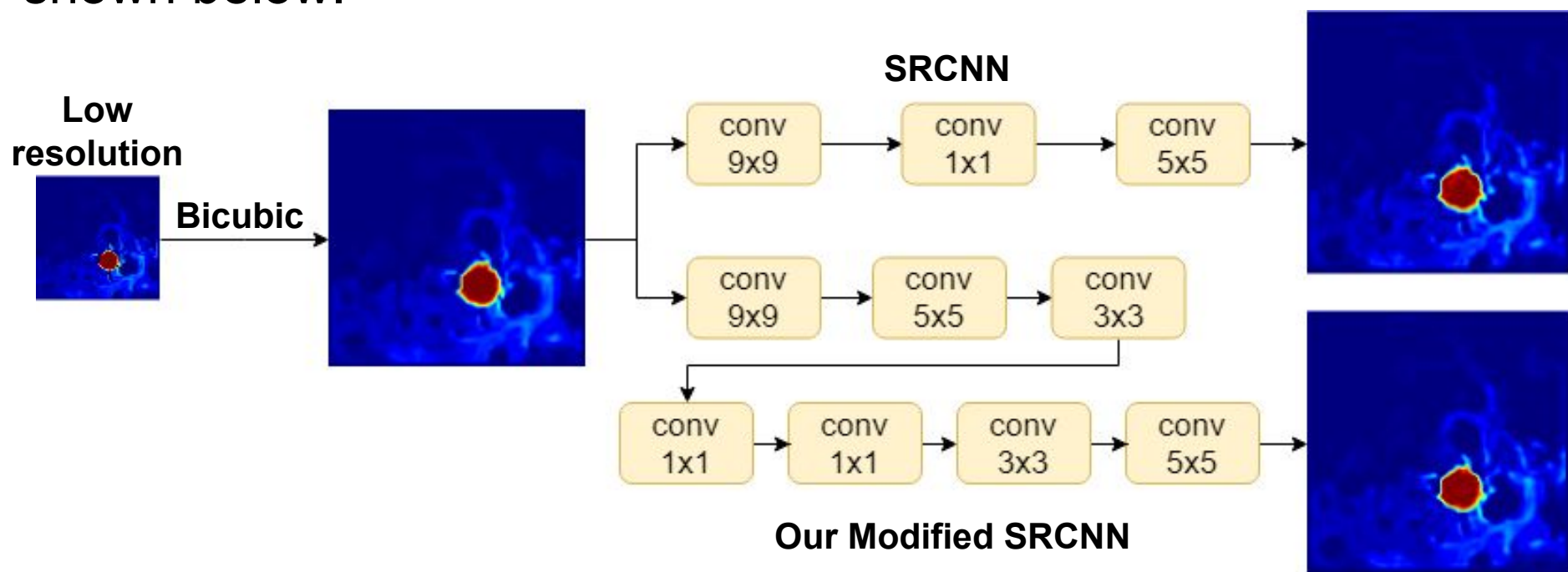
### Temporal Interpolation

Temporal interpolation network is inspired from a state-of-the-art video-frame interpolation method **SuperSloMo** with a few changes to accommodate fluid data. Most notably, we avoid computing the optical flow and fix timestep interpolation at 0.5. A summary of our model can be seen below.

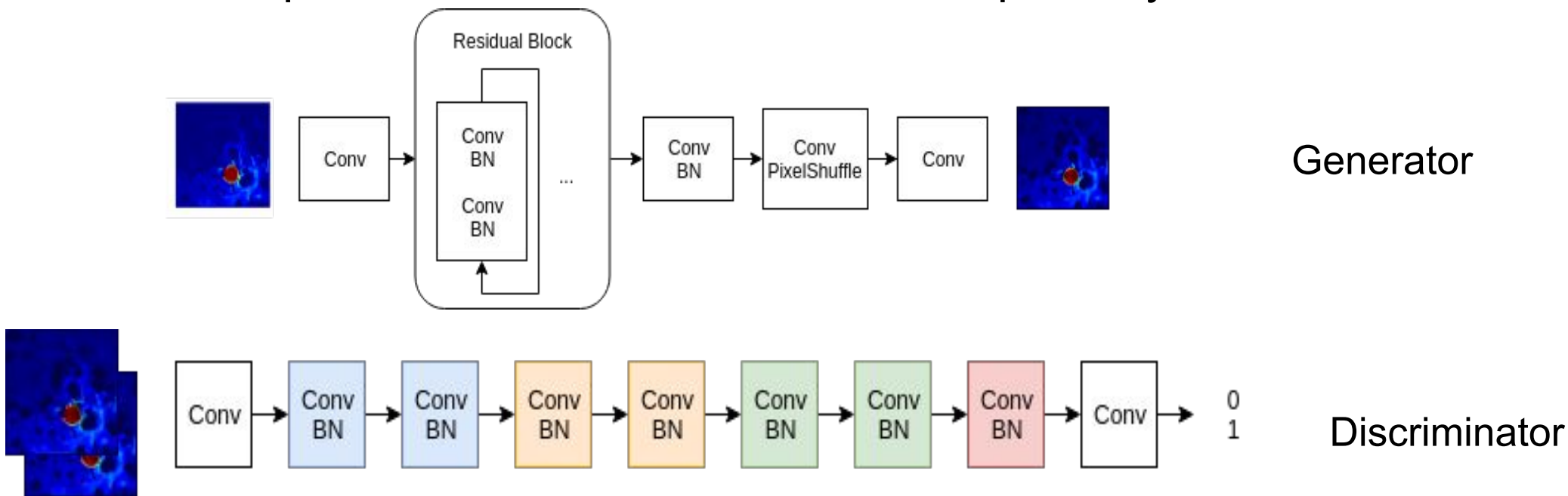


### Spatial Interpolation

We implemented and compared two deep learning architectures inspired by **SRCNN** -- the vanilla SRCNN and our improved modified SRCNN (DSRCNN). A detailed comparison of these two models are shown below.



We also implemented a third architecture inspired by **SRGAN**.

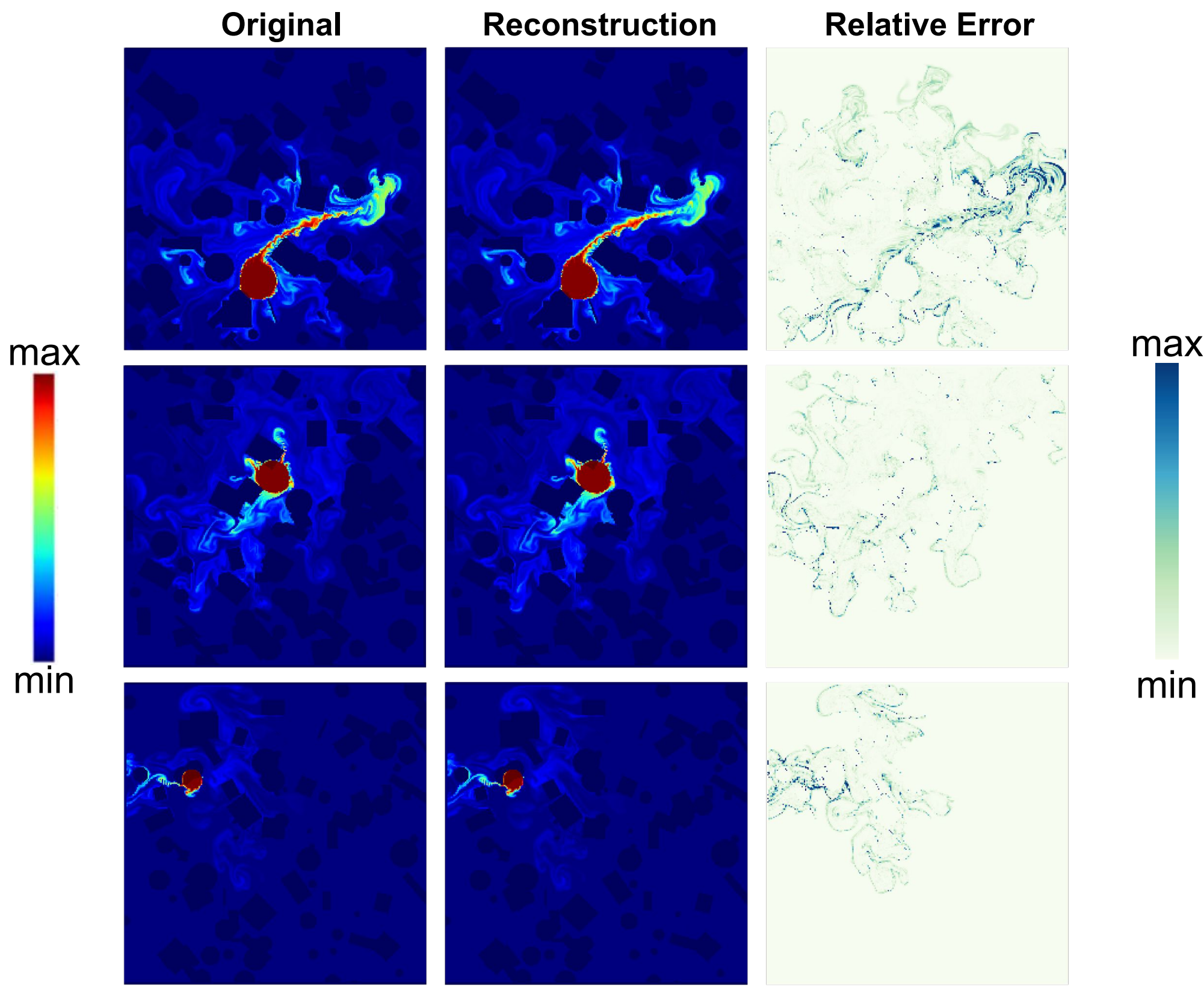


## Results

### Temporal Interpolation

Based on our experimentation, our model is able to reconstruct the simulations fairly well. Besides this, our model also proved to be **30-60 times faster** depending on the complexity of the simulation. A summary of our results and some reconstructions can be seen below.

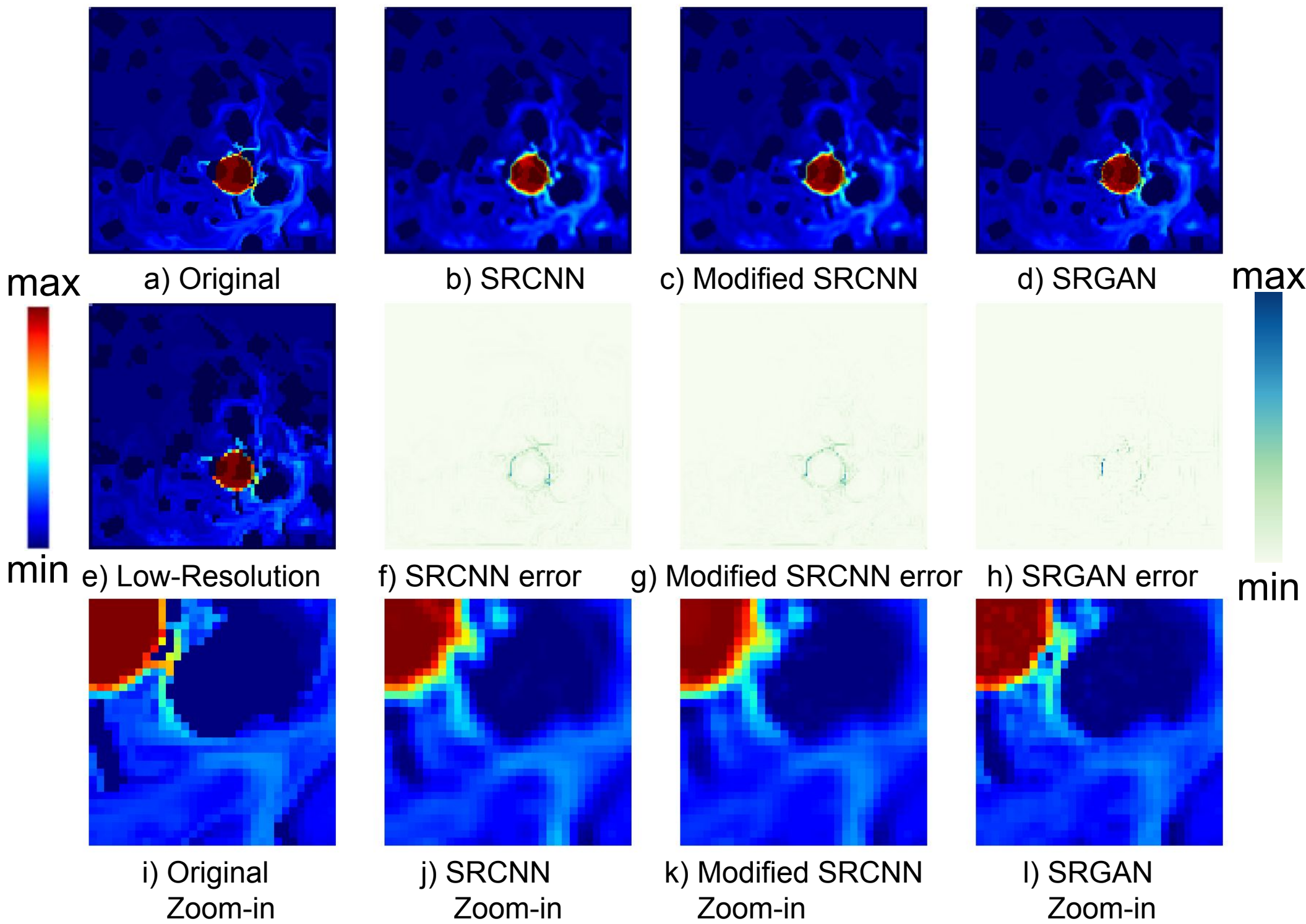
Model / Reconstruction	Mean absolute error	Mean relative error
Base - 1 frame window	<b>0.00080</b>	<b>3.37%</b>
Base - 2 frames window	0.0018	7.79%
Base - 3 frames window	0.0030	12.68%



### Spatial Interpolation

The reconstruction results of all three spatial models are reasonable. The SRGAN model turns out to have the smallest reconstruction loss among the three. Our improved modified SRCNN comes second. A summary of the results is shown below.

Model	Mean absolute error	Mean relative error
SRCNN	0.0018	15.23%
Modified SRCNN	0.0014	12.47%
SRGAN	<b>0.0006</b>	<b>11.52%</b>



## Conclusion

We have created a novel way to compress data and accelerate fluid dynamics simulations using spatial and temporal interpolation.

## Future Work

- Experiment with continuous filter convolutional neural networks.
- Improve Navier-Stokes constraints loss term implementation.
- Experiment and train on several other physical phenomena.