LJasny

Node Leve Permutation

Quadratic Assignmen Procedure

Network Autocorrelation

Baseline Models

Moving Beyond Descriptives

Lorien Jasny¹

¹University of Exeter L.Jasny@exeter.ac.uk



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- Setup
 - R
 - RStudio
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 - datafiles for the class
- Basic SNA Measures
 - centrality measures
 - graph correlation
 - reciprocity
 - transitivity
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 - for Graph level indices
 - Conditional Uniform Graph (CUG) Models

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Relating Node level indices to covariates

• Node Level Indices: centrality measures, brokerage, constraint

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Relating Node level indices to covariates

- Node Level Indices: centrality measures, brokerage, constraint
- Node Covariates: measures of power, career advancement, gender really anything you want to study that varies at the node level

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Baseline

Emergent Multi-Organizational Networks (EMON) Dataset

• 7 case studies of EMONs in the context of search and rescue activities from Drabek et. al. (1981)

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Emergent Multi-Organizational Networks (EMON) Dataset

- 7 case studies of EMONs in the context of search and rescue activities from Drabek et. al. (1981)
- Ties between organizations are self-reported levels of communication coded from 1 to 4 with 1 as most frequent

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Emergent Multi-Organizational Networks (EMON) Dataset

Attribute Data

- Command Rank Score (CRS): mean rank (reversed) for prominence in the command structure
- Decision Rank Score (DRS): mean rank (reversed) for prominence in decision making process
- Paid Staff: number of paid employees
- Volunteer Staff: number of volunteer staff
- Sponsorship: organization type (City, County, State, Federal, or Private)

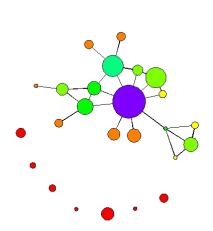
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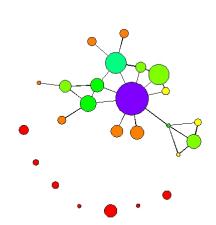
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Correlation between DRS and Degree?

• Subsample of Mutually Reported "Continuous Communication" in Texas EMON



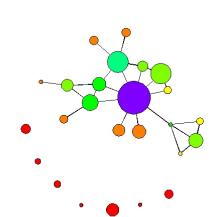
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- Subsample of Mutually Reported "Continuous Communication" in Texas EMON
- Degree is shown in color (darker is bigger)



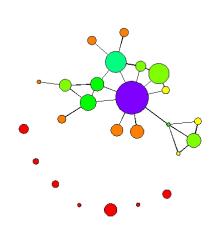
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Baseline Models

- Subsample of Mutually Reported "Continuous Communication" in Texas EMON
- Degree is shown in color (darker is bigger)
- DRS in size



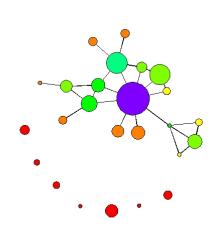
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- Subsample of Mutually Reported "Continuous Communication" in Texas EMON
- Degree is shown in color (darker is bigger)
- DRS in size
- Empirical corelation $\rho = 0.86$

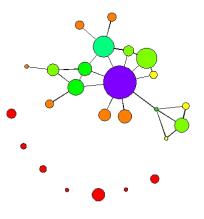


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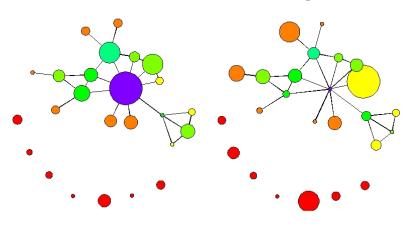
$$\rho = 0.86$$

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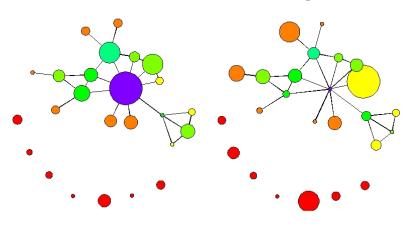
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$$\rho = 0.86$$

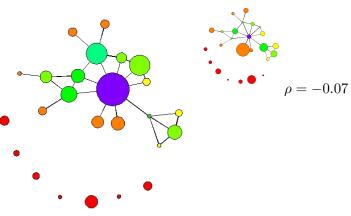
$$\rho = -0.07$$

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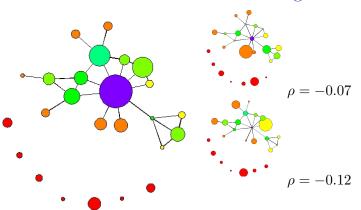
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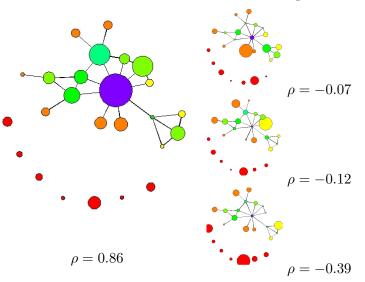
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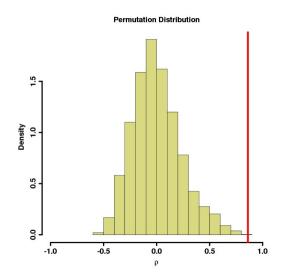


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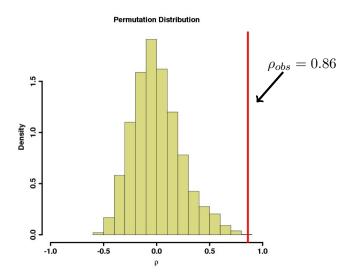


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Baseline Models

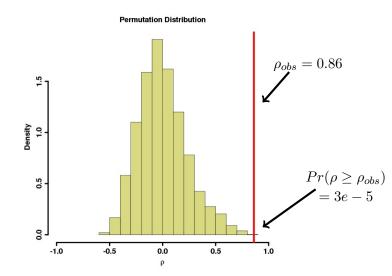


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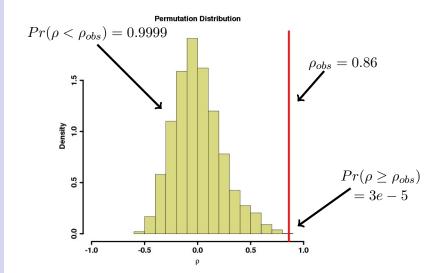


Node Level Permutation

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Baseline Models Regression?

Regression?

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Baseline Models • Can use Node Level Indices as independent variables in a regression

Permutation

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Baseline Models

Regression?

- Can use Node Level Indices as independent variables in a regression
- Big assumption: *position* predicts the *properties of* those who hold them

Node Level Permutation

Regression?

- Can use Node Level Indices as independent variables in a regression
- Big assumption: position predicts the properties of those who hold them
- Conditioning on NLI values, so dependence in accounted for assuming no error in the network

Node Level Permutation

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Baseline Models

- Can use Node Level Indices as independent variables in a regression
- Big assumption: *position* predicts the *properties of* those who hold them
- Conditioning on NLI values, so dependence in accounted for *assuming no error in the network*
- NLIs as dependent variables more problematic due to autocorrelation

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Node Level Permutation

Code Time

Sections 1-2.3

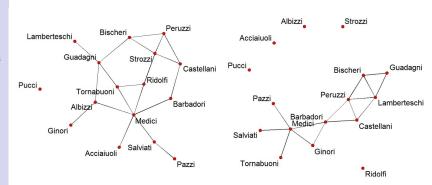
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Baseline Models

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Marriage

Business

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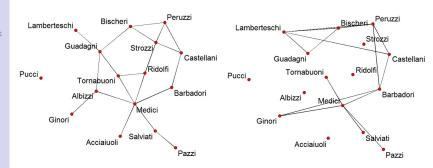
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Graph Correlation

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Graph Correlation

• Simple way of comparing graphs on the same vertex set by element

Quadratic Assignment Procedure

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Graph Correlation

- Simple way of comparing graphs on the same vertex set by element
- $gcor\left(\begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix}, \begin{bmatrix} 1 & 1 \\ 2 & 2 \end{bmatrix}\right) = cor([1, 1, 1, 0], [1, 1, 2, 2])$

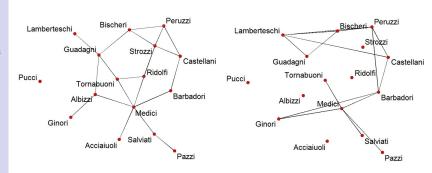
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Baseline Models

Do business ties coincide with marriages?



Marriage

Business

 $\rho = 0.372$

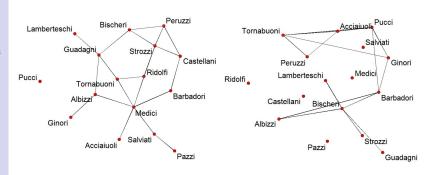
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Baseline Models

Do business ties coincide with marriages?



Marriage

Business

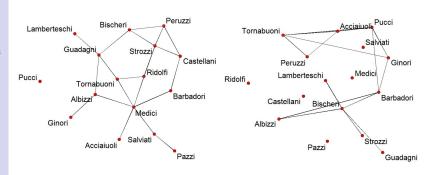
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Baseline Models

Do business ties coincide with marriages?



Marriage

Business

 $\rho = 0.169$

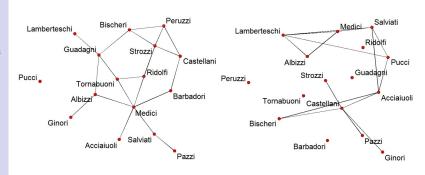
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Baseline Models

Do business ties coincide with marriages?



Marriage

Business

$$\rho = -0.034$$

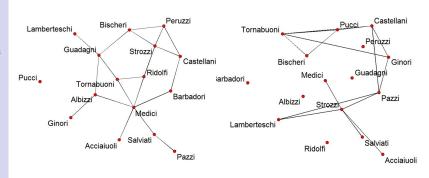
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Baseline Models

Do business ties coincide with marriages?



Marriage

Business

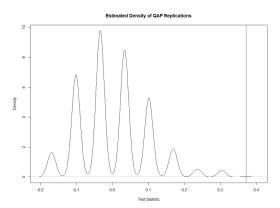
$$\rho = -0.101$$

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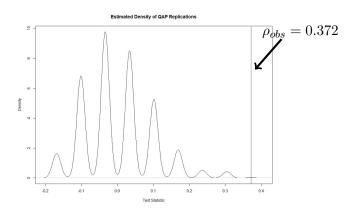


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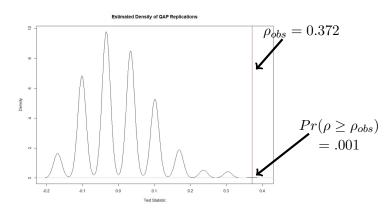
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QAP Test

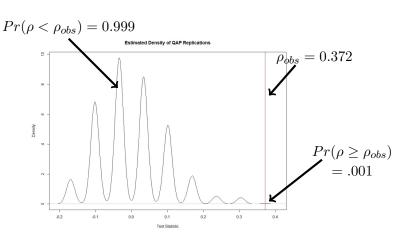


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Moving Beyond Descriptives

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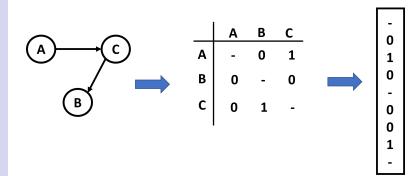
Baseline Models Why can't we use the same permutation test?

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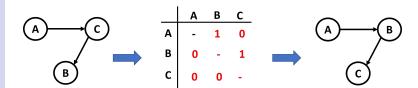


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Baseline Models • Family of models predicting social ties

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Network Autocorre

Baseline Models

- Family of models predicting social ties
 - Special case of standard OLS regression

Node Leve Permutation

Quadratic Assignment Procedure

Network Autocorrelation

Baseline Models

- Family of models predicting social ties
 - Special case of standard OLS regression
 - Dependent variable is a network adjacency matrix

Node Leve Permutation

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Network Autocorrelation

Baseline Models

- Family of models predicting social ties
 - Special case of standard OLS regression
 - Dependent variable is a network adjacency matrix

•
$$\mathbf{E}Y_{ij} = \beta_0 + \beta_1 X_{1ij} + \beta_2 X_{2ij} + \dots + \beta_\rho X_{\rho ij}$$

Baseline Models

- Family of models predicting social ties
 - Special case of standard OLS regression
 - Dependent variable is a network adjacency matrix
- $\mathbf{E}Y_{ij} = \beta_0 + \beta_1 X_{1ij} + \beta_2 X_{2ij} + \dots + \beta_\rho X_{\rho ij}$
 - Where \mathbf{E} is the expectation operator (analogous to "mean" or "average")

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Network Autocorre-

Baseline Models

- Family of models predicting social ties
 - Special case of standard OLS regression
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 - Where **E** is the expectation operator (analogous to "mean" or "average")
 - Y_{ij} is the value from i to j on the dependent relation with adjacency matrix Y

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Network Autocorrelation

Baseline Models

- Family of models predicting social ties
 - Special case of standard OLS regression
 - Dependent variable is a network adjacency matrix
- $\mathbf{E}Y_{ij} = \beta_0 + \beta_1 X_{1ij} + \beta_2 X_{2ij} + \dots + \beta_\rho X_{\rho ij}$
 - Where **E** is the expectation operator (analogous to "mean" or "average")
 - Y_{ij} is the value from i to j on the dependent relation with adjacency matrix Y
 - X_{kij} is the value of the kth predictor for the (i, j) ordered pair, and $\beta_0, \ldots \beta_\rho$ are coefficients

Moving Beyond Descriptives

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Data Prep

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Baseline Models • Dependent variable is an adjacency matrix

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Network Autocorrelation

- Dependent variable is an adjacency matrix
 - Standard case: dichotomous data

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- Dependent variable is an adjacency matrix
 - Standard case: dichotomous data
 - Valued case

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Baseline Models

- Dependent variable is an adjacency matrix
 - Standard case: dichotomous data
 - Valued case
- Independent variables also in adjacency matrix form

Quadratic Assignment Procedure

Network Autocorrelation

Baseline Models

- Dependent variable is an adjacency matrix
 - Standard case: dichotomous data
 - Valued case
- Independent variables also in adjacency matrix form
 - Always takes matrix form, but may be based on vector data

Quadratic Assignment Procedure

Network Autocorrelation

Baseline Models

- Dependent variable is an adjacency matrix
 - Standard case: dichotomous data
 - Valued case
- Independent variables also in adjacency matrix form
 - Always takes matrix form, but may be based on vector data
 - eg. simple adjacency matrix, sender/receiver effects, attribute differences, elements held in common

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Baseline Models Code Time

Sections 2.4-2.5

Network Autocorrelation Models

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Baseline Models

Network Autocorrelation Models

• Family of models for estimating how covariates relate to each other through ties

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Network Autocorrelation

Baseline Models

- Family of models for estimating how covariates relate to each other through ties
 - Special case of standard OLS regression

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Network Autocorrelation

Baseline Models

- Family of models for estimating how covariates relate to each other through ties
 - Special case of standard OLS regression
 - Dependent variable is a vertex attribute

Network Autocorrelation

- Family of models for estimating how covariates relate to each other through ties
 - Special case of standard OLS regression
 - Dependent variable is a vertex attribute
- $y = (I \Theta W)^{-1}(X\beta + (I \psi Z)^{-1}v)$

Network

Autocorrelation

- Family of models for estimating how covariates relate to each other through ties
 - Special case of standard OLS regression
 - Dependent variable is a vertex attribute
- $y = (I \Theta W)^{-1} (X\beta + (I \psi Z)^{-1} v)$
 - where Θ is the matrix for the Auto-Regressive weights

Network Autocorrelation

Baseline Models

- Family of models for estimating how covariates relate to each other through ties
 - Special case of standard OLS regression
 - Dependent variable is a vertex attribute
- $y = (I \Theta W)^{-1} (X\beta + (I \psi Z)^{-1} v)$
 - where Θ is the matrix for the Auto-Regressive weights
 - and ψ is the matrix for the Moving Average weights

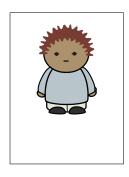
The Classical Regression Model

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Quadratic Assignment Procedure

Network Autocorrelation



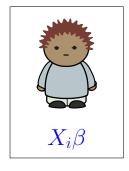
Node Leve Permutation

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Baseline Models

The Classical Regression Model



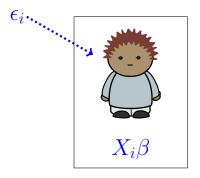
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The Classical Regression Model



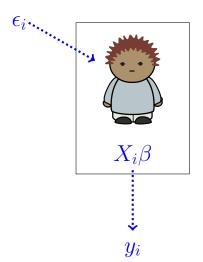
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The Classical Regression Model



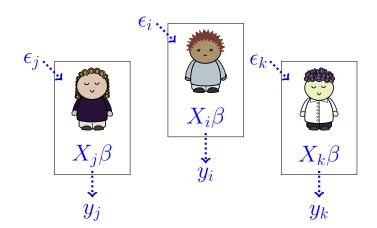
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Baseline Models

Adding Network AR Effects



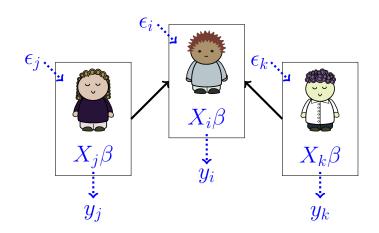
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Baseline Models

Adding Network AR Effects



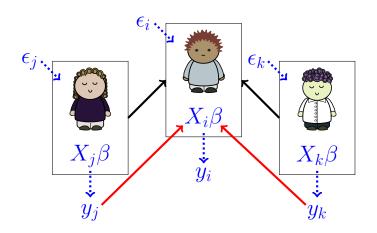
Node Leve Permutation

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Baseline Models

Adding Network AR Effects



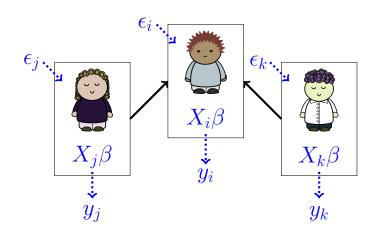
Node Leve Permuta-

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Adding Network MA Effects



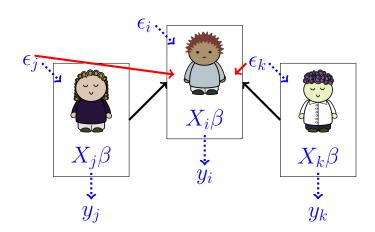
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Adding Network MA Effects



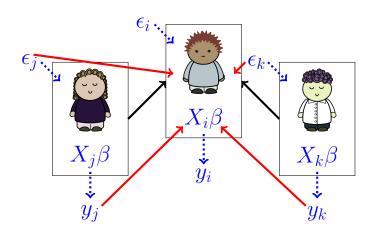
Node Leve Permutation

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Baseline Models

Network ARMA Model

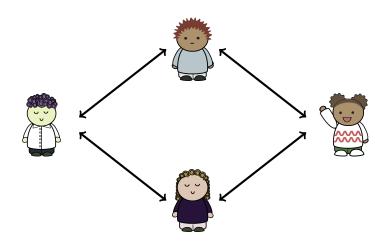


Node Level Permutation

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Baseline Models

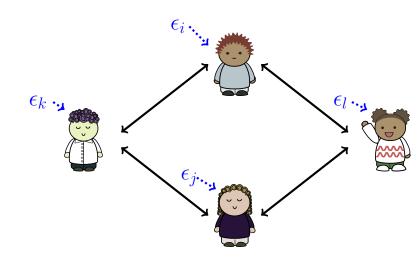


Node Leve Permutation

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Baseline Models

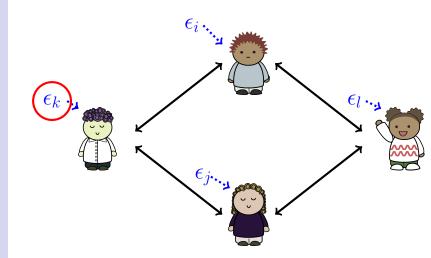


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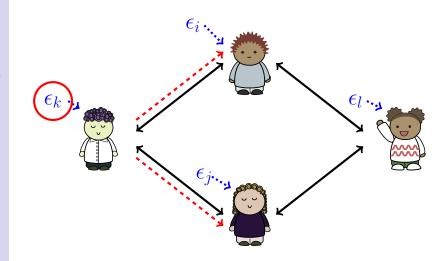


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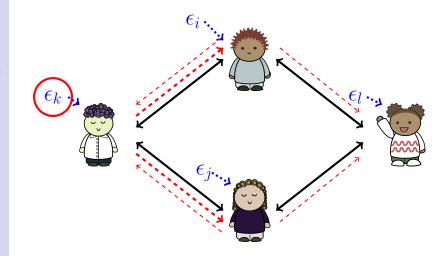


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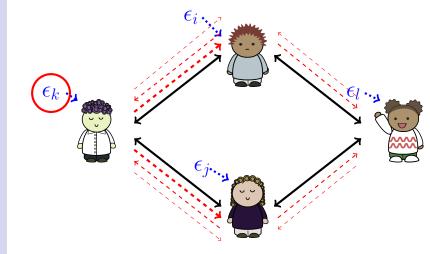


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Moving Beyond Descriptives

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Node Level Permutation

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Network Autocorrelation

Baseline Models

Inference with the Network Autocorrelation Model

• Usually observe \mathbf{y} , \mathbf{X} , and \mathbf{Z} and/or \mathbf{Z} , want to infer β , θ , and ϕ

Node Leve Permutation

Quadratic Assignment Procedure

Network Autocorrelation

Baseline Models

- Usually observe \mathbf{y} , \mathbf{X} , and \mathbf{Z} and/or \mathbf{Z} , want to infer β , θ , and ϕ
- Need each $\mathbf{I} \mathbf{W}, \mathbf{I} \mathbf{Z}$ invertible for solution to exist

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Network Autocorrelation

Baseline Models

- Usually observe \mathbf{y} , \mathbf{X} , and \mathbf{Z} and/or \mathbf{Z} , want to infer β , θ , and ϕ
- Need each I W, I Z invertible for solution to exist
- error in disturbance autocorrelation, v, assumed as iid, $v_i N(0, \sigma^2)$

Node Leve Permutation

Assignment Procedure

Network Autocorrelation

Baseline Models

- Usually observe \mathbf{y} , \mathbf{X} , and \mathbf{Z} and/or \mathbf{Z} , want to infer β , θ , and ϕ
- Need each I W, I Z invertible for solution to exist
- error in disturbance autocorrelation, v, assumed as iid, $v_i N(0, \sigma^2)$
- Standard errors based on the inverse information matrix at the MLE

Node Leve Permutation

Quadratic Assignment Procedure

Network Autocorrelation

Baseline Models

- Usually observe \mathbf{y} , \mathbf{X} , and \mathbf{Z} and/or \mathbf{Z} , want to infer β , θ , and ϕ
- Need each $\mathbf{I} \mathbf{W}, \mathbf{I} \mathbf{Z}$ invertible for solution to exist
- error in disturbance autocorrelation, v, assumed as iid, $v_i N(0, \sigma^2)$
- Standard errors based on the inverse information matrix at the MLE
- Compare models in the usual way (eg AIC, BIC)

Choosing the Weight Matrix

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Quadratic Assignment Procedure

Network Autocorrelation

Baseline Models

Network Autocorrelation

Choosing the Weight Matrix

crucial modeling issue to choose the right form

Node Leve Permutation

Quadratic Assignment Procedure

Network Autocorrelation

Baseline Models

- crucial modeling issue to choose the right form
 - standard adjacency matrix

Node Leve Permutation

Quadratic Assignment Procedure

Network Autocorrelation

Baseline Models

- crucial modeling issue to choose the right form
 - standard adjacency matrix
 - row-normalized adjancecy matrix

Node Leve Permutation

Quadratic Assignment Procedure

Network Autocorrelation

Baseline Models

- crucial modeling issue to choose the right form
 - standard adjacency matrix
 - row-normalized adjancecy matrix
 - structural equivalence distance

Node Leve Permutation

Quadratic Assignment Procedure

Network Autocorrelation

Baseline Models

- crucial modeling issue to choose the right form
 - standard adjacency matrix
 - row-normalized adjancecy matrix
 - structural equivalence distance
- Many suggestions given by Leenders 2002

Moving Beyond Descriptives

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Node Level Permutation

Quadratic Assignment Procedure

Network Autocorrelation

Baseline Models

Data Prep

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Quadratic Assignment Procedure

Network Autocorrelation

Baseline Models • Dependent variable is a vertex attribute

Quadratic Assignment Procedure

Network Autocorrelation

Baseline Models

- Dependent variable is a vertex attribute
- Covariates are in matrix form with one column per attribute

Quadratic Assignment Procedure

Network Autocorrelation

Baseline Models

- Dependent variable is a vertex attribute
- Covariates are in matrix form with one column per attribute
- \bullet Can include an intercept term by adding a column of 1s

Quadratic Assignment Procedure

Network Autocorrelation

Baseline Models

- Dependent variable is a vertex attribute
- Covariates are in matrix form with one column per attribute
- Can include an intercept term by adding a column of 1s
- Weight matrices for both AR and MA terms in matrix form

Node Leve Permutation

Quadratic Assignment Procedure

Network Autocorrelation

Baseline Models

- Dependent variable is a vertex attribute
- Covariates are in matrix form with one column per attribute
- \bullet Can include an intercept term by adding a column of 1s
- Weight matrices for both AR and MA terms in matrix form
- Can include multiple weight matrices (as a list) for both AR and MA

Node Leve Permutation

Quadratic Assignment Procedure

Network Autocorrelation

Baseline Models

Leenders 2002



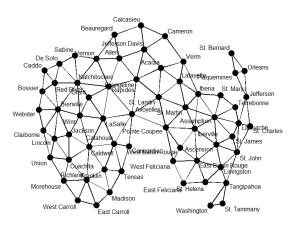
Node Leve Permutation

Quadratic Assignmen Procedure

Network Autocorrelation

Baseline Models

Leenders 2002



Permutation
Quadratic

Assignmen Procedure

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Baseline Models

Variables

• Dependent variable: proportion of support in a parish for democratic presidential candidate Kennedy in the 1960 elections

Variables

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tion
Quadratic

Network Autocorre-

lation

Baseline Models

- Dependent variable: proportion of support in a parish for democratic presidential candidate Kennedy in the 1960 elections
- Covariates:

Quadratic Assignment

Network Autocorrelation

Baseline Models

- Dependent variable: proportion of support in a parish for democratic presidential candidate Kennedy in the 1960 elections
- Covariates:
 - ullet B is the percentage of African American residents in the parish

Quadratic Assignment

Network Autocorrelation

Raseline

Models Models

- Dependent variable: proportion of support in a parish for democratic presidential candidate Kennedy in the 1960 elections
- Covariates:
 - ullet B is the percentage of African American residents in the parish
 - ullet C is the percentage of Catholic residents in the parish

Quadratic

Network Autocorre-

Autocorrelation

Baseline Models

- Dependent variable: proportion of support in a parish for democratic presidential candidate Kennedy in the 1960 elections
- Covariates:
 - ullet B is the percentage of African American residents in the parish
 - ullet C is the percentage of Catholic residents in the parish
 - ullet U is the percentage of the parish considered urban

Network Autocorrelation

Baseline Models

- Dependent variable: proportion of support in a parish for democratic presidential candidate Kennedy in the 1960 elections
- Covariates:
 - ullet B is the percentage of African American residents in the parish
 - ullet C is the percentage of Catholic residents in the parish
 - ullet U is the percentage of the parish considered urban
 - BPE is a measure of 'black political equality'

Network Autocorre-

lation

- Dependent variable: proportion of support in a parish for democratic presidential candidate Kennedy in the 1960 elections
- Covariates:
 - B is the percentage of African American residents in the parish
 - C is the percentage of Catholic residents in the parish
 - U is the percentage of the parish considered urban
 - BPE is a measure of 'black political equality'
- Weight matrix (ρ) : simple contiguity network

Leenders 2002

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Network Autocorrelation Table 3 Network effects model for the Louisiana voting data

3	OLS	$w_{ij}^{[1]}$	$w_{ij}^{[2]}$	$w_{ij}^{[6]}$	$w_{ij}^{[9]}$
ρ		0.31* (0.10)	0.07 (0.06)	0.12 (0.25)	0.04 (0.12)
Constant	21.03* (4.40)	13.87* (4.67)	19.83* (4.34)	16.78 (10.06)	19.80* (5.62)
В	0.01 (0.08)	-0.00(0.07)	0.00 (0.08)	0.01 (0.08)	0.01 (0.08)
C	0.30* (0.04)	0.22* (0.05)	0.28* (0.04)	0.29* (0.05)	0.29 (0.05)
U	-0.11*(0.04)	-0.10* (0.04)	-0.11* (0.04)	-0.11* (0.04)	-0.11* (0.04)
BPE	0.39* (0.06)	0.30* (0.06)	0.37* (0.06)	0.38* (0.06)	0.38* (0.06)

^{*}P < 0.05.

Table 4
Network disturbances model for the Louisiana voting data

	$w_{ij}^{[1]}$	$w_{ij}^{[2]}$	$w_{ij}^{[6]}$	$w_{ij}^{[9]}$
ρ	0.69* (0.10)	0.53* (0.13)	0.22 (0.42)	0.74* (0.15)
Constant	26.99* (4.50)	24.98* (4.22)	21.52* (4.30)	24.51* (5.06)
В	-0.11 (0.07)	-0.07 (0.07)	-0.00(0.08)	-0.09 (0.08)
C	0.37* (0.05)	0.35* (0.04)	0.31* (0.04)	0.38* (0.04)
U	-0.07* (0.03)	0.08* (0.03)	-0.11* (0.04)	-0.10*(0.04)
BPE	0.24* (0.06)	0.30* (0.06)	0.38* (0.06)	0.29* (0.06)

^{*}P < 0.05

Leenders 2002

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Node Level Permutation

Assignment Procedure

Network Autocorrelation

Table 5 Order of W matrices and autocorrelation models according to AIC

	Weight matrix	AIC	Order within model	Overall order
Network effects model	$w_{ij}^{[1]}$	439.12	1	3
	$w_{ij}^{[2]}$	445.52	2	5
	$w_{ij}^{[9]}$	446.78	4	8
	$w_{ij}^{[6]}$	446.44	3	6
Network disturbances model	$w_{ij}^{[1]}$	431.92	1	1
	$w_{ij}^{[2]}$	436.33	2	2
	$w_{ij}^{[9]}$	446.69	4	7
	$w_{ij}^{[6]}$	440.95	3	4
OLS	_	446.82	_	9

Code Time

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Network Autocorrelation

Baseline Models Section 2.6

Baseline Models

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Node Level Permutation

Assignmen Procedure

Autocorre

Baseline Models

Baseline Models

• treats social structure as maximally random given some fixed constraints

Quadratic Assignment Procedure

Network Autocorrelation

Baseline Models

- treats social structure as maximally random given some fixed constraints
- methodological premise from Mayhew

Quadratic Assignment Procedure

Network Autocorrelation

Baseline Models

- treats social structure as maximally random given some fixed constraints
- methodological premise from Mayhew
 - identify potentially constraining factors

Node Leve Permutation

Quadratic Assignment Procedure

Network Autocorrelation

Baseline Models

- treats social structure as maximally random given some fixed constraints
- methodological premise from Mayhew
 - identify potentially constraining factors
 - compare observed properties to baseline model

Node Leve Permutation

Assignment Procedure

Network Autocorrelation

Baseline Models

- treats social structure as maximally random given some fixed constraints
- methodological premise from Mayhew
 - identify potentially constraining factors
 - compare observed properties to baseline model
 - useful even when baseline model is not 'realistic'

Node Level Permuta-

Quadratic Assignmen Procedure

Network Autocorre

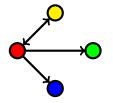
Baseline Models

Node Leve Permutation

Quadratic Assignment Procedure

Network Autocorre

Baseline Models



Empirical Network

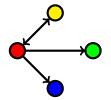
Node Leve Permutation

Quadratic Assignment Procedure

Network Autocorrelation

Baseline Models





Empirical Network

Moving Beyond Descriptives

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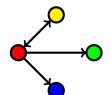
Node Leve Permutation

Quadratic Assignment Procedure

Network Autocorre-

 $\begin{array}{c} {\rm Baseline} \\ {\rm Models} \end{array}$







Empirical Network

Moving Beyond Descriptives

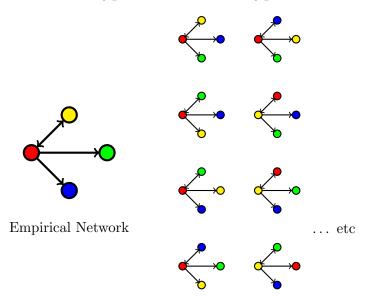
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Node Leve Permuta-

Quadratic Assignment Procedure

Network Autocorre-

 $\begin{array}{c} {\rm Baseline} \\ {\rm Models} \end{array}$

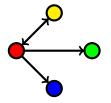


Node Leve Permutation

Quadratic Assignment Procedure

Network Autocorre

Baseline Models



Empirical Network

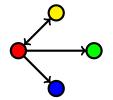
Node Leve Permutation

Quadratic Assignment Procedure

Network Autocorrelation

Baseline Models





Empirical Network

Moving Beyond Descriptives

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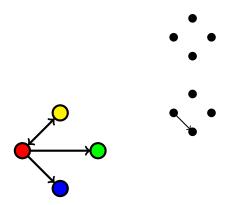
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Quadratic Assignment Procedure

Network Autocorrelation

 $\begin{array}{c} {\rm Baseline} \\ {\rm Models} \end{array}$

Types of Baseline Hypotheses



Empirical Network

Moving Beyond Descriptives

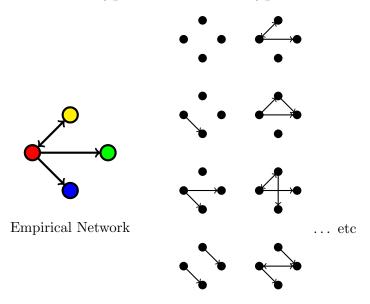
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Quadratic Assignment Procedure

Network Autocorre-

Baseline Models



Node Level Permutation

Assignmen Procedure

Network Autocorre

Baseline Models

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Network Autocorre lation

Baseline Models

Types of Baseline Models

• **Size:** given the number of individuals, all structures are equally likely

tion Quadratic

Network Autocorre-

lation

Baseline Models

- Size: given the number of individuals, all structures are equally likely
- Number of edges/probability of an edge: given the number of individuals and interactions (aka Erdös-Renyi random graphs)

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Baseline Models

- Size: given the number of individuals, all structures are equally likely
- Number of edges/probability of an edge: given the number of individuals and interactions (aka Erdös-Renyi random graphs)
- **Dyad census:** given number of individuals, mutuals, asymmetric, and null relationships

Node Level Permutation

Procedure
Network

Autocorrelation

Baseline Models

- Size: given the number of individuals, all structures are equally likely
- Number of edges/probability of an edge: given the number of individuals and interactions (aka Erdös-Renyi random graphs)
- **Dyad census:** given number of individuals, mutuals, asymmetric, and null relationships
- **Degree distribution:** given the number of individuals and each individual's outgoing/incoming ties

Node Level Permutation

Assignmen Procedure Network

Network Autocorrelation

Baseline Models

- **Size:** given the number of individuals, all structures are equally likely
- Number of edges/probability of an edge: given the number of individuals and interactions (aka Erdös-Renyi random graphs)
- **Dyad census:** given number of individuals, mutuals, asymmetric, and null relationships
- **Degree distribution:** given the number of individuals and each individual's outgoing/incoming ties
- Number of triangles: not implemented due to complexity with ERGM, can condition on the expected number of triangles

Method

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Assignmen Procedure

Network Autocorre lation

Method

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Quadratic Assignment Procedure

Network Autocorrelation

Baseline Models • Select a test statistic (graph correlation, reciprocity, transitivity...)

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Quadratic Assignment Procedure

Network Autocorrelation

- Select a test statistic (graph correlation, reciprocity, transitivity...)
- Select a baseline hypothesis (what you're conditioning on)

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Quadratic Assignment Procedure

Network Autocorrelation

- Select a test statistic (graph correlation, reciprocity, transitivity...)
- Select a baseline hypothesis (what you're conditioning on)
- Simulate from the baseline hypothesis

Method

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Network Autocorrelation

- Select a test statistic (graph correlation, reciprocity, transitivity...)
- Select a baseline hypothesis (what you're conditioning on)
- Simulate from the baseline hypothesis
- For each simulation, recalculate the test statistic

Node Leve Permutation

Procedure Network

Autocorrelation

- Select a test statistic (graph correlation, reciprocity, transitivity...)
- Select a baseline hypothesis (what you're conditioning on)
- Simulate from the baseline hypothesis
- For each simulation, recalculate the test statistic
- Compare empirical value to null distribution, just as in standard statistical testing

Example

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Quadratic Assignmen Procedure

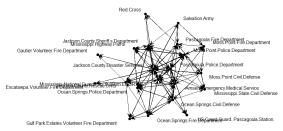
Network Autocorrelation

Baseline Models Transitivity in the Hurricane Frederic EMON

Baseline Models

Example

Transitivity in the Hurricane Frederic EMON



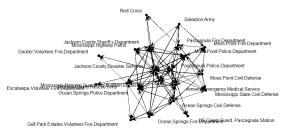
Baseline Models

Transitivity in the Hurricane Frederic EMON

• $\rho = 0.475$

indicates that roughly half the time that $i \to j \to k$

 $i \to k$



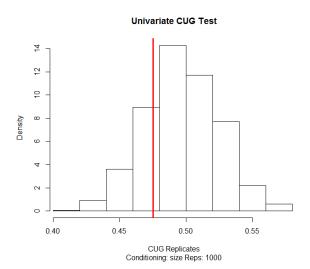
Example

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Permutation

Quadratic Assignment Procedure

Network Autocorrelation



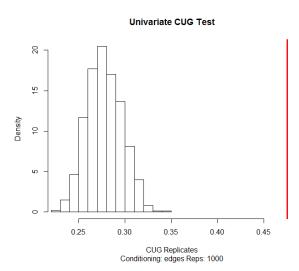
Example

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Quadratic Assignment Procedure

Network Autocorrelation



Bodin and Tengo

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Quadratic Assignmen Procedure

Network Autocorre

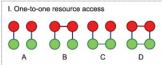
Baseline Models $\hbox{``Disentangling intangible social-ecological systems''}$

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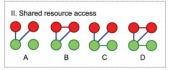
Baseline Models

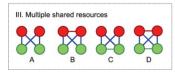
Bodin and Tengo

Symmetric resource access



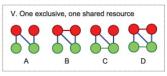


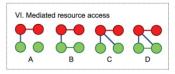


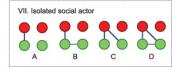




Asymmetric resource access







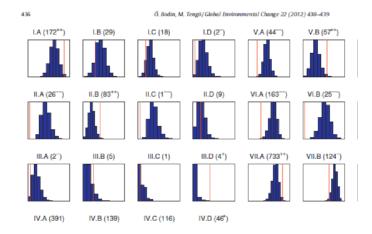
Bodin and Tengo

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Summary

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Node Leve Permutation

Quadratic Assignment Procedure

Network Autocorrelation

Baseline Models • Network indices as independent variables in regression

Node Leve Permutation

Procedure

Autocorrelation

- Network indices as independent variables in regression
- QAP regression (edges are the dependent variable)

tion Quadratic

Network Autocorre-

Baseline Models

Summary

- Network indices as independent variables in regression
- QAP regression (edges are the dependent variable)
- Network Autocorrelation Model (vertex attribute is dependent variable)

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Node Leve Permutation

Assignment Procedure

Network Autocorrelation

- Network indices as independent variables in regression
- QAP regression (edges are the dependent variable)
- Network Autocorrelation Model (vertex attribute is dependent variable)
- CUG tests (network is dependent variable)

Code Time

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Quadratic Assignment Procedure

Network Autocorrelation

Baseline Models • the rest! whew!