Yelpers in The Great Recession: A Case Study 2/7/2017

outline

intro data set explantions yelp data fred analysis yelp users time series yelp reviews time series yelp review stars time series fred data for recession analysis yelp stock data conclusion

Abstract

Introduction

This is a case study into Yelp restaurant goers' consumer behavior during The Great Recession based off the Yelp Challenge 9.

Data Sets

Yelp Challenge 9:
FRED:
Yahoo Finance:
BEA:

Challenges and Data Issues Addressed

Early Yelp data is not very good Most recent Yelp data does not include entire month subset relevant data from beginning of 2006 to end of 2016 Recession only happened in US, data from worldwide

Motivation

If restaurant Yelpers' behavior during and aroud The Great Recession period can be modeled, then there can be conclusions about Yelpers' behavior. If recessionary behavior can be understood, then restaurants can react accordingly.

The Process

After gathering the data, I examined all the potentially relevant information.

Then gathered any additional data that may help

Then test to see if assumptions about the inner workings and dynamics were true

Finally, try to model the consumer's behavior

```
# SETUP
setwd("C:/cygwin64/home/Lester/yelp challenge 9")
# load data example json_file =
# file('yelp_academic_dataset_checkin.json') json_data =
# jsonlite::stream_in(json_file) head(json_data)
# length(json_data$business_id)
load_json = function(filename) {
    json_file = file(filename)
    json_data = jsonlite::stream_in(json_file)
    return(json_data)
}
# business = load_json('yelp_academic_dataset_business.json')
# review = load_json('yelp_academic_dataset_review.json')
# checkin = load_json('yelp_academic_dataset_checkin.json')
# tip = load_json('yelp_academic_dataset_tip.json') user =
# load_json('yelp_academic_dataset_user.json')
remove_lists_from_df = function(df) {
    i = 1
    while (i <= length(df)) {</pre>
        if (class(df[, i]) == "list") {
            df[i] = sapply(df[, i], paste, collapse = "|")
        }
        i = i + 1
    }
    return(df)
}
add_recession_dummy = function(1) {
    rec = c()
    for (i in 1:length(l)) {
        if (1[i] \ge as.Date("2007-12-01") & 1[i] \le as.Date("2009-07-01")) {
            rec = c(rec, 1)
        } else {
            rec = c(rec, 0)
    }
    return(rec)
```

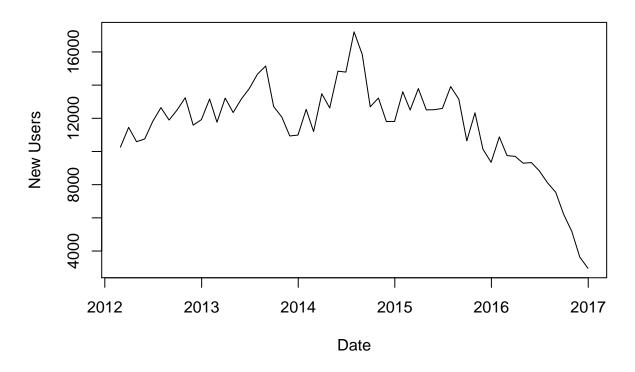
user data

Users, Stocks, & Reviews

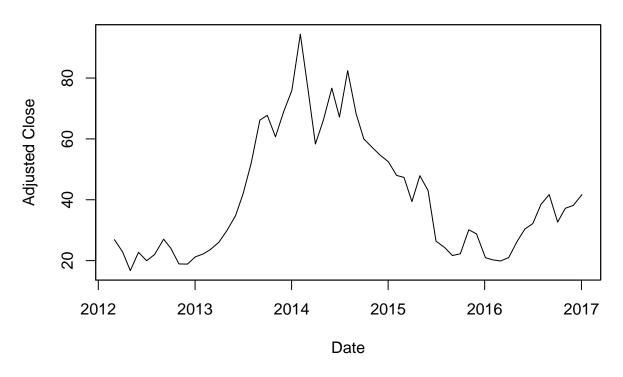
First, I will explore the Yelp stock data to see if it is of any relevance in an attempt to handle any cases of endogeneity.

```
plot(stock_users, type = "1", ylab = "New Users", xlab = "Date",
    main = "New User Acounts by Month")
```

New User Acounts by Month



Yelp Stock



```
test_stationary = function(t) {
    print(kpss.test(t))
    print(adf.test(t))
}
test_cointegration = function(resid) {
    print(test_stationary(resid))
}
test_stationary(ts(stock_users$coredata.ts_m., start = c(2012,
    3), freq = 12))
## Warning in kpss.test(t): p-value smaller than printed p-value
##
   KPSS Test for Level Stationarity
##
##
## data: t
## KPSS Level = 1.1995, Truncation lag parameter = 1, p-value = 0.01
##
##
##
    Augmented Dickey-Fuller Test
##
## data: t
## Dickey-Fuller = -1.0302, Lag order = 3, p-value = 0.9257
```

alternative hypothesis: stationary

```
test_stationary(yelp_stock)
## KPSS Test for Level Stationarity
##
## data: t
## KPSS Level = 0.53728, Truncation lag parameter = 1, p-value =
## 0.03327
##
##
## Augmented Dickey-Fuller Test
##
## data: t
## Dickey-Fuller = -1.4945, Lag order = 3, p-value = 0.7789
## alternative hypothesis: stationary
log_user_growth = as.data.frame(diff(log(stock_users$coredata.ts_m.)))
log_yelp_growth = as.data.frame(diff(log(yelp_stock)))
# log_user_growth log_yelp_growth
ts_users = ts(log_user_growth, start = c(2012, 4), freq = 12)
test_stationary(ts_users)
## Warning in kpss.test(t): p-value smaller than printed p-value
##
## KPSS Test for Level Stationarity
##
## KPSS Level = 0.8162, Truncation lag parameter = 1, p-value = 0.01
##
##
## Augmented Dickey-Fuller Test
##
## data: t
## Dickey-Fuller = -2.5657, Lag order = 3, p-value = 0.3463
## alternative hypothesis: stationary
ts_yelp = ts(log_yelp_growth, start = c(2012, 4), freq = 12)
test_stationary(ts_yelp)
## Warning in kpss.test(t): p-value greater than printed p-value
## KPSS Test for Level Stationarity
##
## data: t
## KPSS Level = 0.13073, Truncation lag parameter = 1, p-value = 0.1
##
## Augmented Dickey-Fuller Test
```

```
##
## data: t
## Dickey-Fuller = -3.9873, Lag order = 3, p-value = 0.01641
## alternative hypothesis: stationary
combined = cbind(ts_yelp, ts_users)
select = VARselect(combined, lag.max = 12, type = c("const",
    "trend", "both", "none"), season = NULL, exogen = NULL)
vm = VAR(combined, p = select$select[1])
# plot(vm$y)
summary(vm)
##
## VAR Estimation Results:
## =========
## Endogenous variables: ts_yelp, ts_users
## Deterministic variables: const
## Sample size: 46
## Log Likelihood: 104.197
## Roots of the characteristic polynomial:
## 1.121 0.9968 0.9968 0.9859 0.9859 0.9739 0.9739 0.9716 0.9716 0.9556 0.9556 0.9471 0.9423 0.9423 0.9
## Call:
## VAR(y = combined, p = select$select[1])
##
## Estimation results for equation ts_yelp:
## ===============
## ts_yelp = ts_yelp.11 + ts_users.11 + ts_yelp.12 + ts_users.12 + ts_yelp.13 + ts_users.13 + ts_yelp.1
##
##
               Estimate Std. Error t value Pr(>|t|)
                                    0.922
## ts_yelp.l1
                0.22443
                           0.24350
                                             0.367
## ts_users.l1
                0.27950
                           0.43228
                                   0.647
                                             0.525
## ts_yelp.12
               -0.02723
                           0.26692 -0.102
                                             0.920
## ts_users.12 -0.12729
                           0.44781 -0.284
                                             0.779
## ts_yelp.13
                0.06446
                           0.25133
                                   0.256
                                             0.800
## ts_users.13 -0.11399
                           0.47105 -0.242
                                             0.811
                           0.26027 -0.583
## ts_yelp.14
               -0.15175
                                             0.566
## ts_users.14 0.41380
                           0.39727
                                   1.042
                                             0.309
## ts_yelp.15
                                   1.398
                0.34786
                          0.24875
                                             0.177
## ts_users.15 -0.04790
                           0.41595 -0.115
                                             0.909
## ts_yelp.16
                0.23889
                           0.29288
                                   0.816
                                             0.424
## ts_users.16 -0.01589
                           0.38874 -0.041
                                             0.968
## ts_yelp.17
               -0.07162
                           0.29937 -0.239
                                             0.813
## ts_users.17 -0.33711
                           0.38189 -0.883
                                             0.387
## ts_yelp.18
                0.01820
                           0.29149
                                    0.062
                                             0.951
## ts_users.18 -0.22491
                           0.40855 - 0.551
                                             0.588
## ts_yelp.19
                0.07345
                           0.27828
                                   0.264
                                             0.794
## ts_users.19 0.40564
                           0.37089
                                   1.094
                                             0.286
## ts_yelp.110 -0.15597
                           0.24322 -0.641
                                             0.528
## ts_users.110 0.31981
                           0.38672
                                   0.827
                                             0.418
                           0.22890 -0.727
## ts_yelp.l11 -0.16642
                                             0.475
## ts_users.l11 -0.26574
                           0.41547 - 0.640
                                             0.529
                           0.23143 -0.593
## ts_yelp.112 -0.13732
                                             0.559
## ts_users.112 0.05773
                           0.44119
                                   0.131
                                             0.897
## const
                0.01366
                           0.03194
                                   0.428
                                             0.673
```

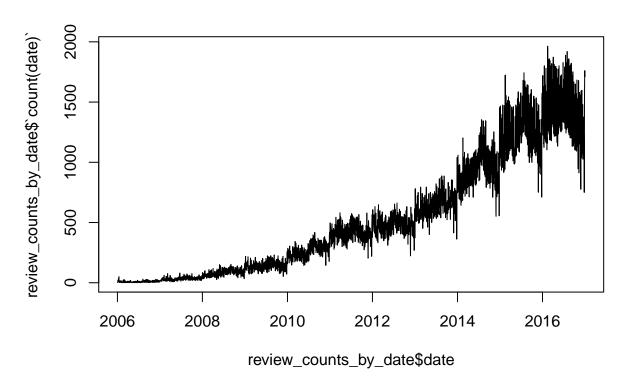
```
##
##
## Residual standard error: 0.1904 on 21 degrees of freedom
## Multiple R-Squared: 0.411, Adjusted R-squared: -0.2621
## F-statistic: 0.6106 on 24 and 21 DF, p-value: 0.8779
##
##
## Estimation results for equation ts_users:
## ts_users = ts_yelp.11 + ts_users.11 + ts_yelp.12 + ts_users.12 + ts_yelp.13 + ts_users.13 + ts_yelp.
##
                Estimate Std. Error t value Pr(>|t|)
## ts_yelp.l1
               -0.158567
                          0.103539 -1.531 0.14058
## ts_users.l1
                0.062517
                          0.183814
                                    0.340 0.73715
## ts_yelp.12
                                    -0.301 0.76657
               -0.034134
                          0.113501
## ts_users.12
                0.353135
                          0.190419
                                     1.855 0.07776 .
## ts_yelp.13
                0.004447
                          0.106872
                                     0.042 0.96720
## ts_users.13
              0.185054
                          0.200299
                                     0.924 0.36604
## ts_yelp.14
               -0.072499
                          0.110674 -0.655 0.51954
## ts_users.14 -0.073652
                          0.168926 -0.436 0.66728
## ts_yelp.15
               -0.163585
                          0.105773 -1.547 0.13691
## ts_users.15
              0.041078
                                    0.232 0.81859
                          0.176871
## ts_yelp.16
                0.235357
                          0.124538
                                    1.890 0.07266 .
## ts users.16
                0.140393
                          0.165300
                                    0.849 0.40528
## ts_yelp.17
               -0.105272
                          0.127298 -0.827 0.41755
## ts_users.17
               0.428628
                          0.162388
                                     2.640 0.01533 *
## ts_yelp.18
                0.053978
                          0.123949
                                     0.435 0.66765
## ts_users.18 0.031861
                          0.173722
                                    0.183 0.85624
## ts_yelp.19
               -0.015866
                         0.118330 -0.134 0.89462
## ts_users.19 -0.097292
                          0.157710 -0.617 0.54393
## ts_yelp.110
                0.053363
                          0.103420
                                     0.516 0.61126
## ts_users.110 0.264388
                          0.164440
                                     1.608 0.12281
## ts_yelp.l11
                0.092298
                          0.097331
                                     0.948 0.35377
## ts_users.111 0.439468
                          0.176665
                                     2.488 0.02134 *
## ts_yelp.112 -0.029449
                          0.098410
                                    -0.299
                                           0.76769
## ts_users.112 0.662858
                          0.187602
                                     3.533 0.00197 **
## const
               -0.009345
                          0.013580 -0.688 0.49886
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 0.08095 on 21 degrees of freedom
## Multiple R-Squared: 0.798, Adjusted R-squared: 0.5672
## F-statistic: 3.457 on 24 and 21 DF, p-value: 0.002768
##
##
##
## Covariance matrix of residuals:
            ts_yelp ts_users
## ts_yelp 0.036241 0.007759
## ts_users 0.007759 0.006553
## Correlation matrix of residuals:
##
           ts_yelp ts_users
```

```
## ts_yelp
             1.0000
                      0.5035
## ts_users 0.5035
                      1.0000
grangertest(ts_users ~ ts_yelp)
## Granger causality test
##
## Model 1: ts_users ~ Lags(ts_users, 1:1) + Lags(ts_yelp, 1:1)
## Model 2: ts_users ~ Lags(ts_users, 1:1)
    Res.Df Df
                    F Pr(>F)
## 1
         54
## 2
         55 -1 0.2396 0.6265
# users and stock no effects
\# sp500 =
\# get.hist.quote('^GSPC',quote='AdjClose',compression='m',start=as.Date('2012-03-01','%Y-\%m-\%d'),end=as
# # sp500 test_stationary(sp500) log_sp500_growth =
\# as.data.frame(diff(log(sp500))) ts_sp500 =
# ts(log_sp500_growth,start=c(2012,4),freq=12) # ts_sp500
# test_stationary(ts_sp500) # ts_yelp # ts_sp500
# plot(ts_users,col='blue') lines(ts_yelp,col='red') combined
\# = cbind(ts\_yelp, ts\_sp500)
# select=VARselect(combined, lag.max=12, type=c('const', 'trend', 'both', 'none'), season=NULL, exogen=NULL)
# vm=VAR(combined,p=select$select[1]) plot(vm$y) summary(vm)
```

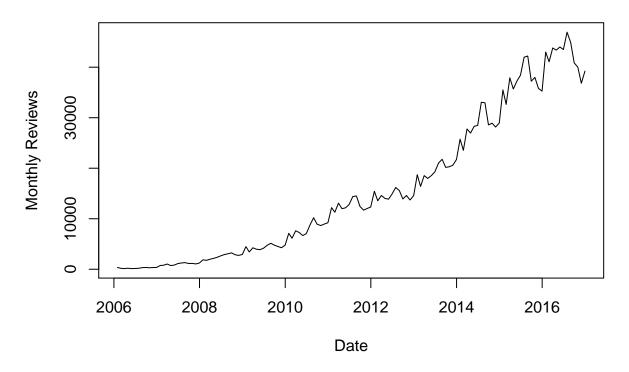
Growth rate of users do not have an effect on the stock value of Yelp - no correlation to stock market. good! This elinates the possibility that effects are due to yelp as a company doing good or bad. Eliminate stock data from our study

review scores and gdp

```
plot(review_counts_by_date$date, review_counts_by_date$`count(date)`,
    type = "1")
```



New Reviews by Month



```
# review growth rates/new user growth rates
log_rev_count = diff(log(df_rev_count$coredata.df_rev_m.))
# log_rev_count[1]=NA
log_rev_count = na.omit(log_rev_count)
log_rev_count = ts(log_rev_count, start = c(2006, 2), freq = 12)
\# ts m
log_user_count = diff(log(ts_m[, 1]))
log_user_count = na.omit(log_user_count)
log_user_count = ts(log_user_count, start = c(2006, 2), freq = 12)
# plot(log_rev_count, type='l', main='growth rate of user
# reviews and accounts') lines(log_user_count[,1],col='red')
# do a var model between growth rate of users revs and
# accounts
# create var of growth rates
rates_combined = cbind(log_rev_count, log_user_count)
select = VARselect(rates_combined, lag.max = 12, type = c("const",
    "trend", "both", "none"), season = NULL, exogen = NULL)
vm_rates = VAR(rates_combined, select$select[1])
# plot(vm_rates$y)
summary(vm rates)
```

##

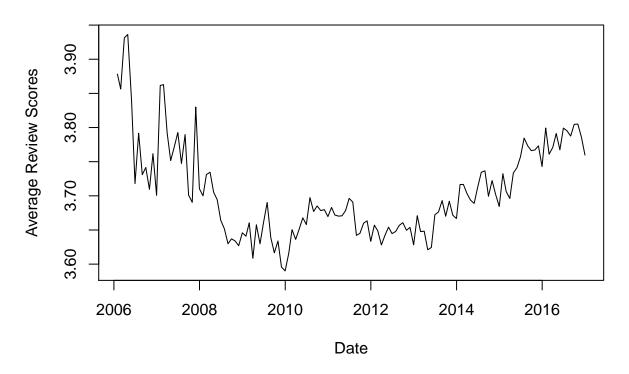
```
## VAR Estimation Results:
## ==========
## Endogenous variables: log_rev_count, log_user_count
## Deterministic variables: const
## Sample size: 119
## Log Likelihood: 297.714
## Roots of the characteristic polynomial:
## 1.048 0.9737 0.9737 0.9716 0.9716 0.97 0.97 0.9687 0.9581 0.9581 0.9101 0.9101 0.8859 0.8859 0.857
## Call:
## VAR(y = rates_combined, p = select$select[1])
##
## Estimation results for equation log_rev_count:
## ==============
## log_rev_count = log_rev_count.11 + log_user_count.11 + log_rev_count.12 + log_user_count.12 + log_rev_count.
##
##
                    Estimate Std. Error t value Pr(>|t|)
                   -0.447591
                            0.102482 -4.367 3.23e-05 ***
## log_rev_count.l1
## log_user_count.l1 0.073934
                            0.092299 0.801 0.425138
## log_rev_count.12
                  -0.140889 0.109751 -1.284 0.202398
## log_user_count.12  0.208054  0.097639  2.131  0.035711 *
## log_rev_count.13
                  0.024924 0.105031 0.237 0.812936
## log_user_count.13 -0.053311 0.095380 -0.559 0.577540
                  0.210029 0.098349 2.136 0.035316 *
## log_rev_count.14
## log_user_count.14 -0.405138 0.096096 -4.216 5.72e-05 ***
## log_rev_count.15
                   0.005835 0.095989 0.061 0.951655
## log_user_count.15 -0.071718 0.102943 -0.697 0.487721
## log_rev_count.16
                   0.113966 0.094900 1.201 0.232807
## log_user_count.16  0.108670  0.101916  1.066  0.289033
## log_rev_count.17
                   0.103038 1.204 0.231678
## log_user_count.17
                  0.124041
## log_rev_count.18 -0.084966 0.095834 -0.887 0.377561
## log_rev_count.19
                   ## log_user_count.19
                  0.122566 0.101162
                                      1.212 0.228713
                            0.095714 -1.930 0.056592 .
## log_rev_count.110 -0.184751
## log_user_count.110 0.299530 0.100755 2.973 0.003748 **
## log_rev_count.l11 -0.132124
                            0.086128 -1.534 0.128376
## log_user_count.111 0.214219
                            0.101571
                                       2.109 0.037598 *
## log_rev_count.112
                    0.092019
                            0.066103 1.392 0.167189
## log_user_count.112 0.373805
                             0.096160 3.887 0.000189 ***
                    0.032366
                             0.013296 2.434 0.016811 *
## const
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.07862 on 94 degrees of freedom
## Multiple R-Squared: 0.6877, Adjusted R-squared: 0.6079
## F-statistic: 8.623 on 24 and 94 DF, p-value: 7.305e-15
##
## Estimation results for equation log user count:
## log_user_count = log_rev_count.l1 + log_user_count.l1 + log_rev_count.l2 + log_user_count.l2 + log_r
```

```
##
##
                      Estimate Std. Error t value Pr(>|t|)
## log rev count.l1
                     -0.228340
                                 0.108927 -2.096 0.03874 *
## log_user_count.l1
                      0.085515
                                 0.098103
                                            0.872
                                                   0.38560
## log_rev_count.12
                      0.109457
                                 0.116653
                                            0.938
                                                   0.35049
## log user count.12
                      0.032154
                                 0.103779
                                            0.310 0.75738
## log rev count.13
                      0.155007
                                 0.111635
                                            1.389
                                                   0.16826
## log_user_count.13
                      0.086143
                                 0.101378
                                            0.850
                                                   0.39764
## log_rev_count.14
                      0.212001
                                 0.104533
                                            2.028
                                                   0.04538 *
## log_user_count.14 -0.139470
                                 0.102139 -1.365
                                                   0.17536
## log_rev_count.15
                      -0.003095
                                 0.102025 -0.030
                                                   0.97586
## log_user_count.15
                                            0.589
                      0.064438
                                 0.109416
                                                   0.55732
## log_rev_count.16
                     -0.001041
                                 0.100868 -0.010
                                                   0.99179
                                 0.108324
## log_user_count.16
                     0.187274
                                            1.729
                                                   0.08712 .
                      -0.085882
                                 0.100767
                                           -0.852
                                                   0.39622
## log_rev_count.17
## log_user_count.17
                      0.260097
                                  0.109517
                                            2.375
                                                   0.01958 *
                                           -2.088
## log_rev_count.18
                      -0.212682
                                 0.101861
                                                   0.03951 *
## log user count.18
                     0.012833
                                  0.110413
                                            0.116
                                                   0.90772
                                 0.096246 -3.224
## log_rev_count.19
                      -0.310263
                                                   0.00174 **
## log_user_count.19
                      0.237115
                                 0.107524
                                            2.205
                                                   0.02988 *
## log_rev_count.110 -0.282063
                                 0.101732 -2.773
                                                   0.00671 **
## log_user_count.110 0.349787
                                            3.266
                                 0.107091
                                                   0.00152 **
## log_rev_count.l11 -0.161645
                                 0.091543
                                           -1.766
                                                   0.08068 .
## log user count.111 0.258147
                                  0.107957
                                            2.391
                                                   0.01879 *
## log_rev_count.112
                      0.256980
                                  0.070259
                                            3.658
                                                   0.00042 ***
## log_user_count.112 0.257381
                                  0.102207
                                            2.518
                                                   0.01348 *
                      -0.008062
                                 0.014132 -0.570 0.56971
## const
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 0.08356 on 94 degrees of freedom
## Multiple R-Squared: 0.618, Adjusted R-squared: 0.5204
## F-statistic: 6.336 on 24 and 94 DF, p-value: 3.029e-11
##
##
##
## Covariance matrix of residuals:
                 log_rev_count log_user_count
##
## log_rev_count
                      0.006181
                                     0.002504
                      0.002504
## log user count
                                      0.006982
##
## Correlation matrix of residuals:
##
                 log_rev_count log_user_count
## log_rev_count
                        1.0000
                                       0.3811
                                        1.0000
## log_user_count
                         0.3811
# do granger causality test
grangertest(log_rev_count ~ log_user_count, order = select$select[1])
## Granger causality test
##
## Model 1: log_rev_count ~ Lags(log_rev_count, 1:12) + Lags(log_user_count, 1:12)
## Model 2: log_rev_count ~ Lags(log_rev_count, 1:12)
    Res.Df Df
##
                    F
                         Pr(>F)
```

```
## 1
## 2
       106 -12 5.9487 1.318e-07 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
grangertest(log_user_count ~ log_rev_count, order = select$select[1])
## Granger causality test
##
## Model 1: log_user_count ~ Lags(log_user_count, 1:12) + Lags(log_rev_count, 1:12)
## Model 2: log_user_count ~ Lags(log_user_count, 1:12)
    Res.Df Df
                  F Pr(>F)
## 1
        94
## 2
       106 -12 3.4167 0.000354 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
user_rev_lm = lm(log_rev_count ~ log_user_count)
summary(user rev lm)
##
## Call:
## lm(formula = log_rev_count ~ log_user_count)
##
## Residuals:
       Min
                 1Q
                     Median
                                   30
                                           Max
## -0.68573 -0.04008 0.00958 0.04946 0.41635
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
                             0.01183
                                       1.801 0.0741 .
## (Intercept)
                  0.02131
## log_user_count 0.77640
                             0.08763
                                       8.860 5.44e-15 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1341 on 129 degrees of freedom
## Multiple R-squared: 0.3783, Adjusted R-squared: 0.3735
## F-statistic: 78.51 on 1 and 129 DF, p-value: 5.444e-15
test_cointegration(resid(user_rev_lm))
## Warning in kpss.test(t): p-value greater than printed p-value
##
## KPSS Test for Level Stationarity
##
## data: t
## KPSS Level = 0.27805, Truncation lag parameter = 2, p-value = 0.1
## Warning in adf.test(t): p-value smaller than printed p-value
##
##
   Augmented Dickey-Fuller Test
##
## data: t
## Dickey-Fuller = -4.91, Lag order = 5, p-value = 0.01
## alternative hypothesis: stationary
##
```

```
##
##
    Augmented Dickey-Fuller Test
##
## data: t
## Dickey-Fuller = -4.91, Lag order = 5, p-value = 0.01
## alternative hypothesis: stationary
# users and num reviews granger cause each other and are
# cointegrated, just use one
# stars by month
stars_by_date = xts(review_date_star$stars, as.Date(review_date_star$date,
    "%Y-%m-%d"))
df_stars_m = apply.monthly(stars_by_date, sum)
df_stars = data.frame(date = index(df_stars_m), coredata(df_stars_m))
df_stars$avg = df_stars$coredata.df_stars_m./df_rev_count$coredata.df_rev_m.
# head(df stars)
plot(df_stars$date, df_stars$avg, type = "l", xlab = "Date",
    ylab = "Average Review Scores", main = "Average Review Scores by Month")
```

Average Review Scores by Month



```
# evidence of recession in stars
stars_recession_dummy = add_recession_dummy(df_stars$date)
stars_avg = df_stars$avg
stars_lm = lm(stars_avg ~ stars_recession_dummy)
```

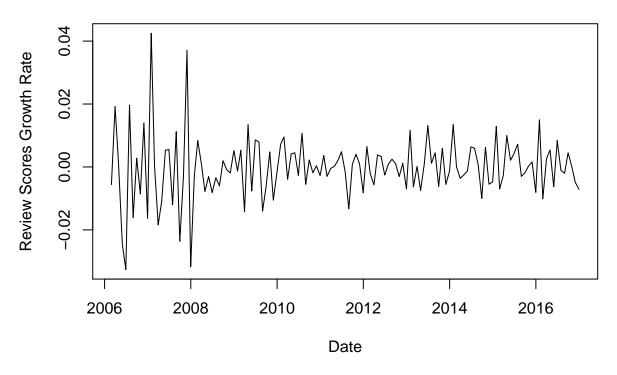
```
summary(stars_lm)
##
## Call:
## lm(formula = stars_avg ~ stars_recession_dummy)
## Residuals:
##
       Min
                1Q
                    Median
                                  3Q
                                          Max
## -0.12291 -0.04541 -0.01606 0.04614 0.22330
## Coefficients:
                        Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                        3.712971
                                 0.006261 593.052 < 2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.06655 on 130 degrees of freedom
## Multiple R-squared: 0.06246, Adjusted R-squared: 0.05525
## F-statistic: 8.661 on 1 and 130 DF, p-value: 0.003851
test_stationary(df_stars$avg)
## Warning in kpss.test(t): p-value smaller than printed p-value
##
## KPSS Test for Level Stationarity
##
## data: t
## KPSS Level = 0.84648, Truncation lag parameter = 2, p-value = 0.01
##
##
##
  Augmented Dickey-Fuller Test
##
## data: t
## Dickey-Fuller = -1.9674, Lag order = 5, p-value = 0.5901
## alternative hypothesis: stationary
# convert to growth rates
df_stars_diff_log = as.data.frame(diff(log(df_stars$avg)))
df_stars_diff_log$date = df_stars$date[2:length(df_stars$date)]
df_stars_diff_log
##
      diff(log(df_stars$avg))
## 1
               -5.619865e-03 2006-02-28
## 2
                1.923989e-02 2006-03-31
## 3
                1.265143e-03 2006-04-29
## 4
               -2.443172e-02 2006-05-31
                -3.263090e-02 2006-06-30
## 5
## 6
                1.963358e-02 2006-07-31
## 7
               -1.612599e-02 2006-08-31
## 8
                2.800839e-03 2006-09-30
               -8.594358e-03 2006-10-31
## 9
## 10
                1.400202e-02 2006-11-30
## 11
               -1.633079e-02 2006-12-31
```

```
## 12
                  4.251363e-02 2007-01-31
## 13
                  3.453816e-04 2007-02-28
## 14
                 -1.845148e-02 2007-03-31
## 15
                 -1.075444e-02 2007-04-30
## 16
                  5.325714e-03 2007-05-31
## 17
                  5.534589e-03 2007-06-30
                 -1.201243e-02 2007-07-31
## 18
                  1.122151e-02 2007-08-31
## 19
## 20
                 -2.366109e-02 2007-09-30
## 21
                 -2.852157e-03 2007-10-31
## 22
                  3.710066e-02 2007-11-30
## 23
                 -3.173946e-02 2007-12-31
## 24
                 -2.795006e-03 2008-01-31
                  8.392467e-03 2008-02-29
## 25
## 26
                  8.993568e-04 2008-03-31
## 27
                 -7.813701e-03 2008-04-30
## 28
                 -3.015577e-03 2008-05-31
## 29
                 -8.163412e-03 2008-06-30
## 30
                 -3.424082e-03 2008-07-31
## 31
                 -6.027338e-03 2008-08-31
## 32
                  1.996352e-03 2008-09-30
## 33
                 -8.728518e-04 2008-10-31
                 -1.921703e-03 2008-11-30
## 34
                  5.202632e-03 2008-12-31
## 35
## 36
                 -1.341539e-03 2009-01-31
## 37
                  5.339377e-03 2009-02-28
## 38
                 -1.426190e-02 2009-03-31
## 39
                  1.348717e-02 2009-04-30
## 40
                 -7.656413e-03 2009-05-31
## 41
                  8.582641e-03 2009-06-30
## 42
                  7.958529e-03 2009-07-31
## 43
                 -1.406197e-02 2009-08-31
## 44
                 -6.107051e-03 2009-09-30
                  4.783419e-03 2009-10-31
## 45
## 46
                 -1.056028e-02 2009-11-30
## 47
                 -1.577807e-03 2009-12-31
## 48
                  7.166652e-03 2010-01-31
## 49
                  9.542976e-03 2010-02-28
## 50
                 -3.927418e-03 2010-03-31
## 51
                  4.125844e-03 2010-04-30
                  4.519455e-03 2010-05-31
## 52
## 53
                 -2.684434e-03 2010-06-30
## 54
                  1.074447e-02 2010-07-31
## 55
                 -5.534875e-03 2010-08-31
                  2.208555e-03 2010-09-30
## 56
## 57
                 -1.857518e-03 2010-10-31
## 58
                  3.900998e-04 2010-11-30
## 59
                 -2.770717e-03 2010-12-31
## 60
                  3.639439e-03 2011-01-31
## 61
                 -3.016042e-03 2011-02-28
## 62
                 -4.471740e-04 2011-03-31
## 63
                  1.281053e-04 2011-04-30
## 64
                  2.094403e-03 2011-05-31
## 65
                  4.849414e-03 2011-06-30
```

```
## 66
                 -1.482645e-03 2011-07-31
## 67
                 -1.330958e-02 2011-08-31
                  8.154915e-04 2011-09-30
## 68
## 69
                  4.060745e-03 2011-10-31
## 70
                  9.731713e-04 2011-11-30
                 -8.223230e-03 2011-12-31
## 71
                  6.484596e-03 2012-01-31
## 72
                 -2.251225e-03 2012-02-29
## 73
## 74
                 -5.706624e-03 2012-03-31
## 75
                  3.849061e-03 2012-04-30
## 76
                  3.306098e-03 2012-05-31
## 77
                 -2.592167e-03 2012-06-30
## 78
                  8.750600e-04 2012-07-31
## 79
                  2.467858e-03 2012-08-31
## 80
                  1.041843e-03 2012-09-30
## 81
                 -3.053989e-03 2012-10-31
                  1.161721e-03 2012-11-30
## 82
## 83
                 -6.995426e-03 2012-12-31
## 84
                  1.166825e-02 2013-01-31
## 85
                 -6.350921e-03 2013-02-28
## 86
                  1.749019e-04 2013-03-31
## 87
                 -7.492477e-03 2013-04-30
                  9.204614e-04 2013-05-31
## 88
                  1.312812e-02 2013-06-30
## 89
## 90
                  1.147936e-03 2013-07-31
## 91
                  4.490404e-03 2013-08-31
## 92
                 -6.214124e-03 2013-09-30
## 93
                  5.951240e-03 2013-10-31
## 94
                 -5.569303e-03 2013-11-30
## 95
                 -1.303337e-03 2013-12-31
## 96
                  1.348184e-02 2014-01-31
## 97
                  4.870529e-05 2014-02-28
## 98
                 -3.615021e-03 2014-03-31
## 99
                 -2.585917e-03 2014-04-30
## 100
                 -1.311054e-03 2014-05-31
## 101
                  6.378572e-03 2014-06-30
## 102
                  5.917766e-03 2014-07-31
## 103
                  5.419283e-04 2014-08-31
## 104
                 -1.002166e-02 2014-09-30
## 105
                  6.225047e-03 2014-10-31
## 106
                 -5.479281e-03 2014-11-30
## 107
                 -4.762909e-03 2014-12-31
## 108
                  1.292571e-02 2015-01-31
## 109
                 -7.020857e-03 2015-02-28
                 -2.731912e-03 2015-03-31
## 110
                  1.000075e-02 2015-04-30
## 111
## 112
                  2.110902e-03 2015-05-31
## 113
                  4.274085e-03 2015-06-30
## 114
                  7.234081e-03 2015-07-31
## 115
                 -3.011319e-03 2015-08-31
## 116
                 -1.848002e-03 2015-09-30
## 117
                  2.730000e-04 2015-10-31
## 118
                  1.595003e-03 2015-11-30
## 119
                 -8.085294e-03 2015-12-31
```

```
## 120
                 1.497098e-02 2016-01-31
## 121
                -1.014415e-02 2016-02-29
## 122
                 2.609374e-03 2016-03-31
                 5.401924e-03 2016-04-30
## 123
## 124
                -6.305894e-03 2016-05-31
## 125
                 8.415438e-03 2016-06-30
## 126
                -1.068921e-03 2016-07-31
                -2.013443e-03 2016-08-31
## 127
## 128
                 4.508334e-03 2016-09-30
                 1.314815e-04 2016-10-31
## 129
## 130
                 -4.937163e-03 2016-11-30
                 -7.075452e-03 2016-12-31
## 131
colnames(df_stars_diff_log) = c("avg", "date")
test_stationary(df_stars_diff_log$avg)
## Warning in kpss.test(t): p-value greater than printed p-value
##
## KPSS Test for Level Stationarity
##
## data: t
## KPSS Level = 0.20563, Truncation lag parameter = 2, p-value = 0.1
## Warning in adf.test(t): p-value smaller than printed p-value
##
## Augmented Dickey-Fuller Test
##
## data: t
## Dickey-Fuller = -5.5779, Lag order = 5, p-value = 0.01
## alternative hypothesis: stationary
stars_recession_diff_log_dummy = add_recession_dummy(df_stars_diff_log$date)
# stars_reg = lm(df_stars_diff_log$avg ~
# stars_recession_diff_log_dummy) summary(stars_reg)
plot(df_stars_diff_log$date, df_stars_diff_log$avg, type = "l",
   main = "Growth Rate of Review Scores by Month", xlab = "Date",
   ylab = "Review Scores Growth Rate")
```

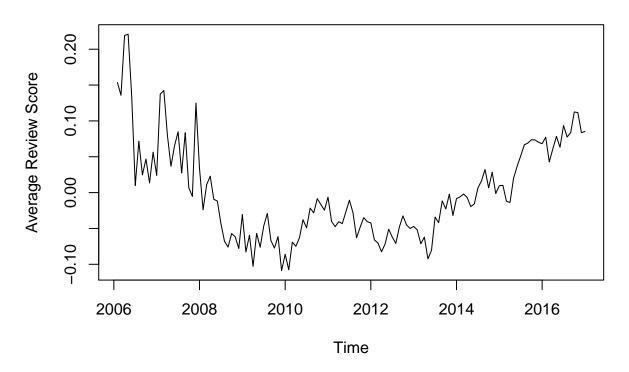
Growth Rate of Review Scores by Month



```
stars diff log avg = df stars diff log$avg
stars_diff_log_lm = lm(stars_diff_log_avg ~ stars_recession_diff_log_dummy)
summary(stars_diff_log_lm)
##
## Call:
## lm(formula = stars_diff_log_avg ~ stars_recession_diff_log_dummy)
## Residuals:
##
         Min
                    1Q
                          Median
                                        3Q
                                                 Max
  -0.032757 -0.005360 0.000147 0.004525 0.042388
##
##
## Coefficients:
##
                                    Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                   0.0001261 0.0009446
                                                          0.133
                                                                   0.894
## stars_recession_diff_log_dummy -0.0025015  0.0024803
                                                         -1.009
                                                                   0.315
## Residual standard error: 0.009997 on 129 degrees of freedom
## Multiple R-squared: 0.007823,
                                    Adjusted R-squared:
## F-statistic: 1.017 on 1 and 129 DF, p-value: 0.3151
# however, intuitively we should be looking at level, not
# growth rates so lets detrend the data and season
ts_stars = ts(df_starssavg, start = c(2006, 2), freq = 12)
stars_tslm = tslm(ts_stars ~ trend + season)
```

```
summary(stars_tslm)
##
## Call:
## tslm(formula = ts_stars ~ trend + season)
## Residuals:
##
       Min
                1Q Median
                                 3Q
## -0.10883 -0.04940 -0.01198 0.04378 0.22099
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 3.677e+00 2.426e-02 151.563
                                          <2e-16 ***
            -2.068e-05 1.619e-04 -0.128
## trend
                                            0.899
## season2
             4.736e-02 3.015e-02 1.571
                                          0.119
## season3
             4.357e-02 3.014e-02 1.446
                                          0.151
## season4
             3.505e-02 3.013e-02
                                  1.163
                                          0.247
## season5
             3.822e-02 3.012e-02
                                   1.269
                                          0.207
## season6
             2.959e-02 3.011e-02 0.983 0.328
             3.114e-02 3.011e-02 1.034 0.303
## season7
             4.315e-02 3.010e-02 1.433
                                          0.154
## season8
## season9
             2.931e-02 3.010e-02 0.974
                                           0.332
## season10
            1.768e-02 3.010e-02 0.587
                                          0.558
             1.906e-02 3.009e-02 0.633
## season11
                                            0.528
             2.838e-02 3.009e-02 0.943
## season12
                                            0.347
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.07057 on 119 degrees of freedom
## Multiple R-squared: 0.03497, Adjusted R-squared: -0.06235
## F-statistic: 0.3593 on 12 and 119 DF, p-value: 0.9748
# plot(ts_stars) lines(stars_tslm$fitted.values,col='red')
detrend_stars = resid(stars_tslm)
plot(detrend_stars, main = "Detrended & Seasonally Adjusted Review Scores by Month",
   ylab = "Average Review Score")
```

Detrended & Seasonally Adjusted Review Scores by Month



```
detrend_stars_lm = lm(detrend_stars ~ stars_recession_dummy)
summary(detrend_stars_lm)
```

```
##
## Call:
## lm(formula = detrend_stars ~ stars_recession_dummy)
##
## Residuals:
##
        Min
                  1Q
                       Median
                                            Max
  -0.11605 -0.04819 -0.01401
                              0.05040
                                        0.21376
##
  Coefficients:
##
##
                          Estimate Std. Error t value Pr(>|t|)
                          0.007226
## (Intercept)
                                     0.006128
                                                1.179 0.24049
  stars_recession_dummy -0.050203
                                     0.016153
                                              -3.108 0.00231 **
##
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 0.06514 on 130 degrees of freedom
## Multiple R-squared: 0.06917,
                                    Adjusted R-squared: 0.06201
## F-statistic: 9.66 on 1 and 130 DF, p-value: 0.002314
```

the growth rates plot shows that even during recession we don't see a dip in either. if there was constant account creation but a dip in reviews, that would mean the recession has an effect on num of reviews

descriptive stats of reviews and stars

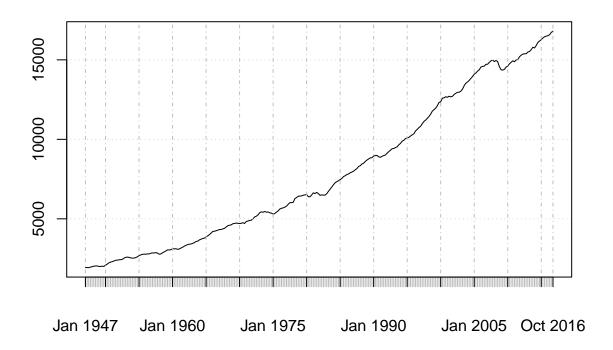
```
sd(df_rev_count$coredata.df_rev_m.)
## [1] 14205.68
mean(df_rev_count$coredata.df_rev_m.)
## [1] 15550.11
sd(log_rev_count)
## [1] 0.1694621
mean(log_rev_count)
## [1] 0.0357887
sd(df_stars$avg)
## [1] 0.06847152
mean(df_stars$avg)
## [1] 3.705981
```

fred data

```
# real gdp
getSymbols("GDPC96", src = "FRED")

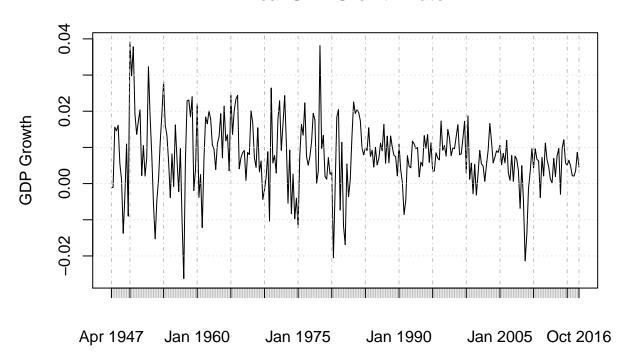
## As of 0.4-0, 'getSymbols' uses env=parent.frame() and
## auto.assign=TRUE by default.
##
## This behavior will be phased out in 0.5-0 when the call will
## default to use auto.assign=FALSE. getOption("getSymbols.env") and
## getOptions("getSymbols.auto.assign") are now checked for alternate defaults
##
## This message is shown once per session and may be disabled by setting
## options("getSymbols.warning4.0"=FALSE). See ?getSymbols for more details.
## [1] "GDPC96"
gdp = GDPC96
plot(gdp, main = "Real GDP")
```

Real GDP



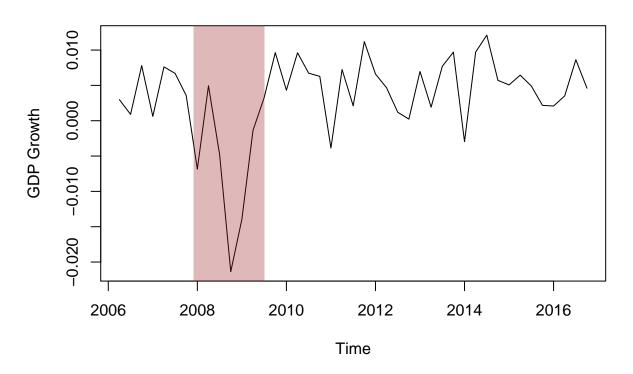
```
gdp_growth = na.omit(diff(log(gdp)))
plot(gdp_growth, ylab = "GDP Growth", main = "Real GDP Growth Rate")
```

Real GDP Growth Rate

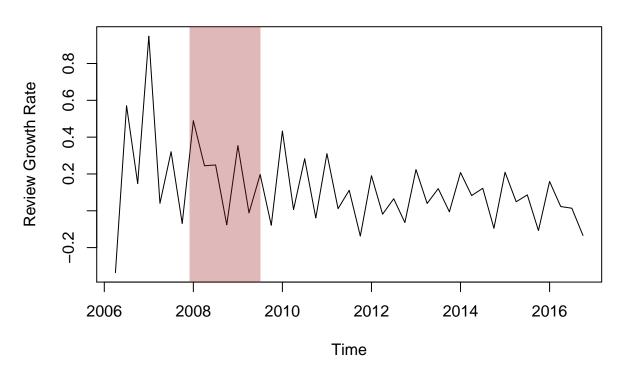


```
gdp_growth_subset = with(gdp_growth, gdp_growth[index(gdp_growth) >=
    "2006-04-01" & index(gdp_growth) < "2016-12-30", ])
gdp_growth_subset = ts(gdp_growth_subset, start = c(2006, 2),
    frequency = 4)
plot(gdp_growth_subset, ylab = "GDP Growth", main = "Real GDP Growth 2006Q2 to 2016Q4")
rect(2007.9166667, -1, 2009.5, 1, col = rgb(red = 150/255, green = 25/255,
    blue = 25/255, alpha = 0.3), border = NA)</pre>
```

Real GDP Growth 2006Q2 to 2016Q4



Review Growth Rate by Quarter



```
# length(log_rev_quarter) length(gdp_growth_subset)
# var of gdp and user reviews growth rates
gdp_combined = cbind(log_rev_quarter, gdp_growth_subset)
select = VARselect(gdp_combined, lag.max = 12, type = c("const",
    "trend", "both", "none"), season = NULL, exogen = NULL)
vm_gdp = VAR(gdp_combined, p = 12)
# plot(vm_gdp$y)
summary(vm_gdp)
##
## VAR Estimation Results:
## Endogenous variables: log_rev_quarter, gdp_growth_subset
## Deterministic variables: const
## Sample size: 31
## Log Likelihood: 238.784
## Roots of the characteristic polynomial:
## 0.9987 0.9987 0.9921 0.9921 0.9906 0.9795 0.9795 0.9699 0.9612 0.9612 0.9576 0.9576 0.9327 0.9327 0.
## Call:
## VAR(y = gdp_combined, p = 12)
##
## Estimation results for equation log_rev_quarter:
## log_rev_quarter = log_rev_quarter.l1 + gdp_growth_subset.l1 + log_rev_quarter.l2 + gdp_growth_subset
```

```
##
##
                         Estimate Std. Error t value Pr(>|t|)
## log_rev_quarter.l1
                          0.41495
                                     0.36251
                                               1.145
                        -0.69319
                                     3.48625
                                             -0.199
                                                       0.8490
## gdp_growth_subset.l1
## log_rev_quarter.12
                          0.28843
                                     0.37771
                                               0.764
                                                       0.4740
                          4.10864
                                               1.300
                                                       0.2412
## gdp growth subset.12
                                     3.15933
## log_rev_quarter.13
                          0.27193
                                     0.32528
                                               0.836
                                                       0.4352
## gdp_growth_subset.13
                          1.55990
                                     3.26731
                                               0.477
                                                       0.6500
## log_rev_quarter.14
                          0.63886
                                     0.20809
                                               3.070
                                                       0.0219 *
## gdp_growth_subset.14
                          1.46361
                                     2.96026
                                               0.494
                                                       0.6386
## log_rev_quarter.15
                         -0.21532
                                     0.23826
                                             -0.904
                                                       0.4010
## gdp_growth_subset.15
                        -0.43820
                                     3.45264
                                              -0.127
                                                       0.9032
                                     0.22996
                                             -0.721
                                                       0.4979
## log_rev_quarter.16
                         -0.16586
## gdp_growth_subset.16
                          4.69612
                                     3.45845
                                              1.358
                                                       0.2233
                                             -0.541
## log_rev_quarter.17
                         -0.13165
                                     0.24321
                                                       0.6078
## gdp_growth_subset.17
                         -4.04228
                                     2.95912
                                              -1.366
                                                       0.2209
                                     0.24925
                                               0.234
                                                       0.8226
## log_rev_quarter.18
                          0.05838
                          5.04951
                                     3.49119
                                               1.446
                                                       0.1982
## gdp_growth_subset.18
                          0.11847
                                     0.20277
                                               0.584
                                                       0.5803
## log_rev_quarter.19
## gdp_growth_subset.19
                          0.05217
                                     3.36605
                                               0.016
                                                       0.9881
## log_rev_quarter.110
                          0.11208
                                     0.13776
                                               0.814
                                                       0.4470
                                               1.968
                                                       0.0966 .
## gdp_growth_subset.110
                         6.34267
                                     3.22213
                                             -0.535
                         -0.08093
                                     0.15120
                                                       0.6117
## log_rev_quarter.l11
                                             -0.828
## gdp_growth_subset.l11 -1.75022
                                     2.11397
                                                       0.4394
## log_rev_quarter.112
                          0.43781
                                     0.17667
                                               2.478
                                                       0.0479 *
## gdp_growth_subset.l12 2.53313
                                     2.12131
                                               1.194
                                                       0.2775
                                             -0.808
                                                       0.4502
## const
                         -0.16460
                                     0.20382
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 0.04107 on 6 degrees of freedom
## Multiple R-Squared: 0.9823, Adjusted R-squared: 0.9117
## F-statistic: 13.9 on 24 and 6 DF, p-value: 0.001734
##
##
## Estimation results for equation gdp_growth_subset:
## gdp_growth_subset = log_rev_quarter.l1 + gdp_growth_subset.l1 + log_rev_quarter.l2 + gdp_growth_subs
##
##
                         Estimate Std. Error t value Pr(>|t|)
                                     0.038485 -0.947
                                                        0.3800
## log_rev_quarter.l1
                         -0.036465
## gdp_growth_subset.11
                        -0.473658
                                     0.370109 -1.280
                                                        0.2479
                                     0.040098 -1.072
## log_rev_quarter.12
                         -0.042996
                                                        0.3248
                        -0.403692
                                     0.335402 -1.204
                                                        0.2741
## gdp_growth_subset.12
                                     0.034533 -0.153
## log_rev_quarter.13
                         -0.005267
                                                        0.8838
## gdp_growth_subset.13
                        -0.410470
                                     0.346866 -1.183
                                                        0.2814
## log_rev_quarter.14
                         -0.034836
                                     0.022091 - 1.577
                                                        0.1659
                                     0.314269 -1.944
                        -0.611076
                                                        0.0998
## gdp_growth_subset.14
                         -0.004935
                                     0.025294
                                               -0.195
                                                        0.8518
## log_rev_quarter.15
                        -0.259610
                                     0.366540
                                              -0.708
                                                        0.5053
## gdp_growth_subset.15
## log_rev_quarter.16
                         0.026056
                                     0.024413
                                                1.067
                                                        0.3269
## gdp_growth_subset.16
                        -0.470368
                                     0.367157 -1.281
                                                        0.2474
## log_rev_quarter.17
                         -0.014837
                                     0.025820 -0.575
                                                        0.5864
```

```
## gdp_growth_subset.17 -0.179878
                                    0.314147 -0.573
                                                       0.5877
                                    0.026461 -1.077
                                                       0.3228
## log_rev_quarter.18 -0.028504
## gdp_growth_subset.18 -0.567262
                                    0.370633 -1.531
                                                       0.1768
                        -0.002516
                                    0.021527 -0.117
                                                       0.9108
## log_rev_quarter.19
## gdp_growth_subset.19 -0.410645
                                    0.357347 -1.149
                                                       0.2942
                                   0.014625 -1.492
## log_rev_quarter.110 -0.021819
                                                      0.1863
                                    0.342069 -0.553
## gdp_growth_subset.110 -0.189002
                                                       0.6006
                                    0.016052 -2.155
## log_rev_quarter.l11
                        -0.034597
                                                       0.0746 .
## gdp_growth_subset.111 0.090608
                                    0.224424
                                              0.404
                                                       0.7004
## log_rev_quarter.112
                       -0.014337
                                    0.018756 -0.764
                                                       0.4736
## gdp_growth_subset.112 -0.408396
                                    0.225203 -1.813
                                                       0.1197
                         0.043626
                                    0.021638
                                              2.016
                                                       0.0904 .
## const
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 0.00436 on 6 degrees of freedom
## Multiple R-Squared: 0.7602, Adjusted R-squared: -0.1992
## F-statistic: 0.7924 on 24 and 6 DF, p-value: 0.6886
##
##
##
## Covariance matrix of residuals:
##
                    log_rev_quarter gdp_growth_subset
## log_rev_quarter
                          0.0016865
                                            1.157e-04
## gdp_growth_subset
                          0.0001157
                                            1.901e-05
##
## Correlation matrix of residuals:
##
                    log_rev_quarter gdp_growth_subset
## log_rev_quarter
                             1.0000
                                               0.6464
## gdp_growth_subset
                             0.6464
                                               1.0000
# do a var on quarterly qdp growth and quarterly avg review
# score
recession_dummy_reviews_q = add_recession_dummy(df_rev_quarter$date)
reg_reviews = lm(df_rev_quarter$coredata.df_rev_m_quarter. ~
   recession_dummy_reviews_q)
summary(reg_reviews)
##
## lm(formula = df_rev_quarter$coredata.df_rev_m_quarter. ~ recession_dummy_reviews_q)
##
## Residuals:
##
     Min
             1Q Median
                           3Q
                                 Max
  -53417 -28547 -3776 24826
                               78800
##
## Coefficients:
                            Estimate Std. Error t value Pr(>|t|)
##
                                                  8.225 2.72e-10 ***
## (Intercept)
                               53903
                                           6553
                                          16430 -2.775 0.00821 **
## recession_dummy_reviews_q
                              -45589
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 39860 on 42 degrees of freedom
## Multiple R-squared: 0.1549, Adjusted R-squared: 0.1348
## F-statistic: 7.699 on 1 and 42 DF, p-value: 0.008211
# first req is misleading because trend
# look at growth rates
rec_dummy_rev_growth_q = recession_dummy_reviews_q[2:length(recession_dummy_reviews_q)]
reg_log_reviews = lm(log_rev_quarter ~ rec_dummy_rev_growth_q)
summary(reg_log_reviews)
##
## Call:
## lm(formula = log_rev_quarter ~ rec_dummy_rev_growth_q)
##
## Residuals:
                 1Q Median
##
       Min
                                   30
                                           Max
## -0.44588 -0.13871 -0.02718 0.09270 0.83847
##
## Coefficients:
                         Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                          0.10999
                                     0.03739
                                               2.941 0.00535 **
                                             0.632 0.53093
## rec_dummy_rev_growth_q 0.05857
                                     0.09268
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2244 on 41 degrees of freedom
## Multiple R-squared: 0.009647, Adjusted R-squared:
## F-statistic: 0.3994 on 1 and 41 DF, p-value: 0.5309
log_reviews_lm = lm(log_rev_quarter ~ rec_dummy_rev_growth_q)
summary(log_reviews_lm)
##
## Call:
## lm(formula = log_rev_quarter ~ rec_dummy_rev_growth_q)
## Residuals:
##
       Min
                 1Q
                     Median
                                   3Q
## -0.44588 -0.13871 -0.02718 0.09270 0.83847
##
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
                                     0.03739 2.941 0.00535 **
                          0.10999
## (Intercept)
                                     0.09268
                                               0.632 0.53093
## rec_dummy_rev_growth_q 0.05857
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2244 on 41 degrees of freedom
## Multiple R-squared: 0.009647, Adjusted R-squared: -0.01451
```

examine social dynamics during recessions through dollar signs as well as review texts

do people eat at cheaper places? do people care more about overpriced food?

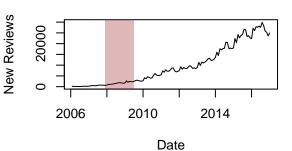
```
dollars_1_xts = xts(dollars_gbd_1$`count(date)`, as.Date(dollars_gbd_1$date,
    "%Y-%m-%d")
df_d_1 = apply.monthly(dollars_1_xts, sum)
df_dollars_1 = data.frame(date = index(df_d_1), coredata(df_d_1))
# df dollars 1
dollars_2_xts = xts(dollars_gbd_2$`count(date)`, as.Date(dollars_gbd_2$date,
    "%Y-%m-%d")
df_d_2 = apply.monthly(dollars_2_xts, sum)
df_dollars_2 = data.frame(date = index(df_d_2), coredata(df_d_2))
# df dollars 2
dollars_3_xts = xts(dollars_gbd_3$`count(date)`, as.Date(dollars_gbd_3$date,
    "%Y-%m-%d")
df_d_3 = apply.monthly(dollars_3_xts, sum)
df_dollars_3 = data.frame(date = index(df_d_3), coredata(df_d_3))
# df_dollars_3
dollars_4_xts = xts(dollars_gbd_4$`count(date)`, as.Date(dollars_gbd_4$date,
    "%Y-%m-%d")
df_d_4 = apply.monthly(dollars_4_xts, sum)
df_dollars_4 = data.frame(date = index(df_d_4), coredata(df_d_4))
# df_dollars_4
recession_dummy_dollars_m = add_recession_dummy(df_dollars_1$date)
# par(mfrow=c(2,2))
# plot(df_dollars_1, type='l', xlab='Date', ylab='New Reviews',
# main='New Reviews of $ Restaurants')
# plot(df_dollars_2, type='l', xlab='Date', ylab='New Reviews',
# main='New Reviews of $$ Restaurants')
 \begin{tabular}{ll} \# \ plot(df\_dollars\_3, type='l', xlab='Date', ylab='New \ Reviews', \\ \end{tabular} 
# main='New Reviews of $$$ Restaurants')
# plot(df_dollars_4, type='l', xlab='Date', ylab='New Reviews',
# main='New Reviews of $$$$ Restaurants') highly seasonal
df_dollars_1_dlog = as.data.frame(diff(log(df_dollars_1$coredata.df_d_1.)))
df_dollars_2_dlog = as.data.frame(diff(log(df_dollars_2$coredata.df_d_2.)))
df_dollars_3_dlog = as.data.frame(diff(log(df_dollars_3$coredata.df_d_3.)))
df_dollars_4_dlog = as.data.frame(diff(log(df_dollars_4$coredata.df_d_4.)))
# ts of dlogs
ts_dollar_1 = ts(df_dollars_1$coredata.df_d_1., start = c(2006,
    2), freq = 12)
ts_dollar_2 = ts(df_dollars_2$coredata.df_d_2., start = c(2006,
```

```
2), freq = 12)
ts_dollar_3 = ts(df_dollars_3$coredata.df_d_3., start = c(2006,
    2), freq = 12)
ts_dollar_4 = ts(df_dollars_4$coredata.df_d_4., start = c(2006,
    2), freq = 12)
par(mfrow = c(2, 2))
plot(ts_dollar_1, type = "l", xlab = "Date", ylab = "New Reviews",
    main = "New Reviews of $ Restaurants")
rect(2007.9166667, -1000, 2009.5, 20000, col = rgb(red = 150/255,
    green = 25/255, blue = 25/255, alpha = 0.3), border = NA)
plot(ts_dollar_2, type = "l", xlab = "Date", ylab = "New Reviews",
    main = "New Reviews of $$ Restaurants")
rect(2007.9166667, -3000, 2009.5, 40000, col = rgb(red = 150/255,
    green = 25/255, blue = 25/255, alpha = 0.3), border = NA)
plot(ts_dollar_3, type = "1", xlab = "Date", ylab = "New Reviews",
    main = "New Reviews of $$$ Restaurants")
rect(2007.9166667, -1000, 2009.5, 7000, col = rgb(red = 150/255,
    green = 25/255, blue = 25/255, alpha = 0.3), border = NA)
plot(ts_dollar_4, type = "l", xlab = "Date", ylab = "New Reviews",
    main = "New Reviews of $$$$ Restaurants")
rect(2007.9166667, -1000, 2009.5, 2000, col = rgb(red = 150/255,
    green = 25/255, blue = 25/255, alpha = 0.3), border = NA)
```

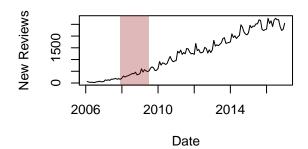
New Reviews of \$ Restaurants

2006 2010 2014 Date

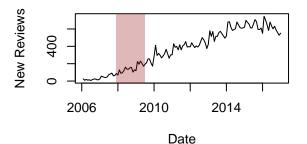
New Reviews of \$\$ Restaurants



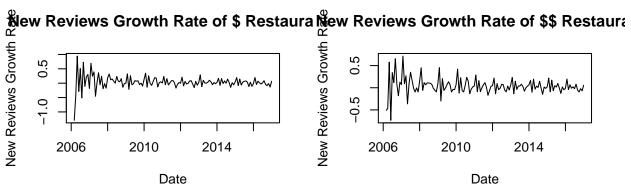
New Reviews of \$\$\$ Restaurants

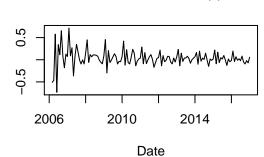


New Reviews of \$\$\$\$ Restaurants

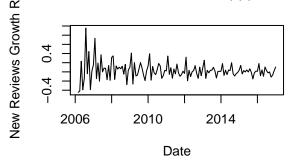


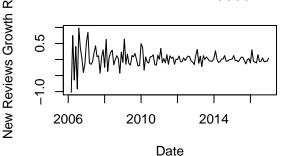
```
dollars_1_dlog = diff(log(ts_dollar_1))
dollars_2_dlog = diff(log(ts_dollar_2))
dollars_3_dlog = diff(log(ts_dollar_3))
dollars_4_dlog = diff(log(ts_dollar_4))
par(mfrow = c(2, 2))
plot(dollars_1_dlog, xlab = "Date", ylab = "New Reviews Growth Rate",
   main = "New Reviews Growth Rate of $ Restaurants")
plot(dollars_2_dlog, xlab = "Date", ylab = "New Reviews Growth Rate",
   main = "New Reviews Growth Rate of $$ Restaurants")
plot(dollars_3_dlog, xlab = "Date", ylab = "New Reviews Growth Rate",
   main = "New Reviews Growth Rate of $$$ Restaurants")
plot(dollars 4 dlog, xlab = "Date", ylab = "New Reviews Growth Rate",
   main = "New Reviews Growth Rate of $$$$ Restaurants")
```





New Reviews Growth Rate of \$\$\$ Restaur Reviews Growth Rate of \$\$\$\$ Restaur





```
# we can see highly seasonal
# lm dollars recession dummy =
# recession_dummy_dollars_m[2:length(recession_dummy_dollars_m)]
```

seasonally adjust the data

```
# seasonally adjust data and remove trend
```

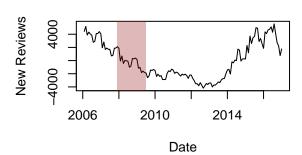
```
par(mfrow = c(2, 2))
# levels
tslm_d1 = tslm(ts_dollar_1 ~ trend + season)
# summary(tslm_d1)
tslm_d1_resid = resid(tslm_d1)
plot(tslm_d1_resid, xlab = "Date", ylab = "New Reviews", main = "Adjusted Reviews, $")
rect(2007.9166667, -3000, 2009.5, 3000, col = rgb(red = 150/255,
    green = 25/255, blue = 25/255, alpha = 0.3), border = NA)
lm_d1_adj = lm(tslm_d1_resid ~ recession_dummy_dollars_m)
summary(lm_d1_adj)
##
## Call:
## lm(formula = tslm_d1_resid ~ recession_dummy_dollars_m)
## Residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -1932.8 -1098.0 -162.2 975.3 2613.1
## Coefficients:
##
                            Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                               33.99 120.76 0.281
                                                           0.779
## recession_dummy_dollars_m -236.11
                                         318.30 -0.742
                                                           0.460
## Residual standard error: 1284 on 130 degrees of freedom
## Multiple R-squared: 0.004215, Adjusted R-squared:
## F-statistic: 0.5502 on 1 and 130 DF, p-value: 0.4596
tslm_d2 = tslm(ts_dollar_2 ~ trend + season)
# summary(tslm d1)
tslm_d2_resid = resid(tslm_d2)
plot(tslm_d2_resid, xlab = "Date", ylab = "New Reviews", main = "Adjusted Reviews, $$")
rect(2007.9166667, -7000, 2009.5, 7000, col = rgb(red = 150/255,
    green = 25/255, blue = 25/255, alpha = 0.3), border = NA)
lm_d2_adj = lm(tslm_d2_resid ~ recession_dummy_dollars_m)
summary(lm_d2_adj)
##
## Call:
## lm(formula = tslm_d2_resid ~ recession_dummy_dollars_m)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
## -4262.1 -2293.1 -201.7 2170.2 5499.9
##
## Coefficients:
                            Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                               71.32
                                         259.47 0.275
                                                           0.784
## recession_dummy_dollars_m -495.52
                                         683.92 -0.725
                                                           0.470
## Residual standard error: 2758 on 130 degrees of freedom
## Multiple R-squared: 0.004022, Adjusted R-squared: -0.00364
## F-statistic: 0.5249 on 1 and 130 DF, p-value: 0.47
```

```
tslm_d3 = tslm(ts_dollar_3 ~ trend + season)
# summary(tslm d1)
tslm_d3_resid = resid(tslm_d3)
plot(tslm_d3_resid, xlab = "Date", ylab = "New Reviews", main = "Adjusted Reviews, $$$")
rect(2007.9166667, -500, 2009.5, 500, col = rgb(red = 150/255,
    green = 25/255, blue = 25/255, alpha = 0.3), border = NA)
lm_d3_adj = lm(tslm_d3_resid ~ recession_dummy_dollars_m)
summary(lm_d3_adj)
##
## Call:
## lm(formula = tslm_d3_resid ~ recession_dummy_dollars_m)
## Residuals:
      Min
##
               1Q Median
                               3Q
                                      Max
## -301.93 -84.56 -10.65 76.69 290.26
##
## Coefficients:
##
                            Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                               14.40
                                          10.99 1.310 0.19253
                                          28.97 -3.453 0.00075 ***
## recession_dummy_dollars_m -100.01
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 116.8 on 130 degrees of freedom
## Multiple R-squared: 0.084, Adjusted R-squared: 0.07695
## F-statistic: 11.92 on 1 and 130 DF, p-value: 0.0007496
tslm d4 = tslm(ts dollar 4 ~ trend + season)
# summary(tslm_d1)
tslm_d4_resid = resid(tslm_d4)
plot(tslm_d4_resid, xlab = "Date", ylab = "New Reviews", main = "Adjusted Reviews, $$$$")
rect(2007.9166667, -500, 2009.5, 500, col = rgb(red = 150/255,
   green = 25/255, blue = 25/255, alpha = 0.3), border = NA)
```

Adjusted Reviews, \$

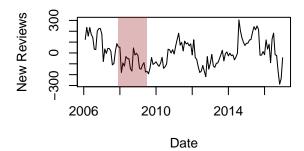
New Reviews 2000 2000 2014

Adjusted Reviews, \$\$

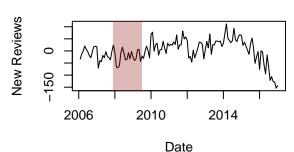


Adjusted Reviews, \$\$\$

Date



Adjusted Reviews, \$\$\$\$



```
lm_d4_adj = lm(tslm_d4_resid ~ recession_dummy_dollars_m)
summary(lm_d4_adj)
```

```
##
## Call:
## lm(formula = tslm_d4_resid ~ recession_dummy_dollars_m)
##
## Residuals:
##
       Min
                    Median
                1Q
                                3Q
                                       Max
                                    107.62
   -158.13
           -21.63
                      5.18
                             29.74
##
##
  Coefficients:
                             Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                                4.168
                                            4.353
                                                    0.958
                                                            0.3400
   recession_dummy_dollars_m -28.960
                                           11.472 -2.524
                                                            0.0128 *
##
                  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 46.27 on 130 degrees of freedom
## Multiple R-squared: 0.04673,
                                    Adjusted R-squared:
## F-statistic: 6.372 on 1 and 130 DF, p-value: 0.0128
```

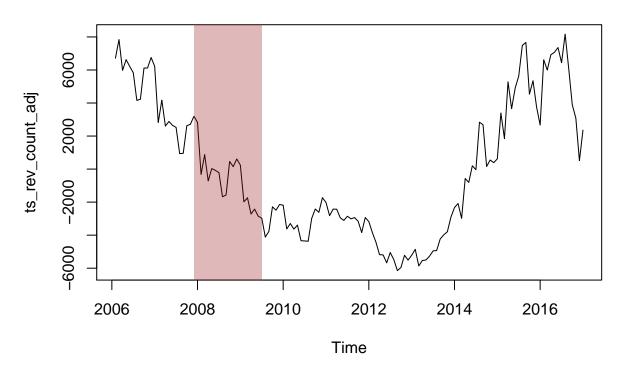
introduce num of reviews into model

control for number of new reviews, to make sure that the recession dummy doesn't accidentally capture an effect from new review numbers, in other words if the number of reviews dropped it would make sense that the number of reviews for a certain amount of dollar signs drops too

```
lm_d1_adj_rev = lm(tslm_d1_resid ~ recession_dummy_dollars_m +
   df_rev_count$coredata.df_rev_m.)
summary(lm_d1_adj_rev)
##
## Call:
## lm(formula = tslm_d1_resid ~ recession_dummy_dollars_m + df_rev_count$coredata.df_rev_m.)
## Residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -1829.6 -917.4 -307.4 1123.4
##
## Coefficients:
##
                                    Estimate Std. Error t value Pr(>|t|)
                                  -4.521e+02 1.852e+02 -2.441 0.016016 *
## (Intercept)
                                   1.689e+02 3.291e+02
                                                          0.513 0.608659
## recession_dummy_dollars_m
## df rev count$coredata.df rev m. 2.751e-02 8.162e-03
                                                          3.370 0.000991 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1235 on 129 degrees of freedom
## Multiple R-squared: 0.0848, Adjusted R-squared: 0.07061
## F-statistic: 5.976 on 2 and 129 DF, p-value: 0.003295
lm d2 adj rev = lm(tslm d2 resid ~ recession dummy dollars m +
   df rev count$coredata.df rev m.)
summary(lm_d2_adj_rev)
##
## Call:
## lm(formula = tslm_d2_resid ~ recession_dummy_dollars_m + df_rev_count$coredata.df_rev_m.)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -4138.1 -1943.8 -620.9 2367.0 6147.7
##
## Coefficients:
##
                                    Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                  -977.68395 397.81376 -2.458 0.015313 *
## recession_dummy_dollars_m
                                   378.55976
                                              706.74989
                                                          0.536 0.593133
## df_rev_count$coredata.df_rev_m.
                                     0.05937
                                                0.01753
                                                          3.387 0.000938 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 2653 on 129 degrees of freedom
## Multiple R-squared: 0.08534,
                                   Adjusted R-squared:
## F-statistic: 6.018 on 2 and 129 DF, p-value: 0.003171
```

```
lm_d3_adj_rev = lm(tslm_d3_resid ~ recession_dummy_dollars_m +
   df_rev_count$coredata.df_rev_m.)
summary(lm_d3_adj_rev)
##
## Call:
## lm(formula = tslm_d3_resid ~ recession_dummy_dollars_m + df_rev_count$coredata.df_rev_m.)
## Residuals:
##
       Min
                 10
                      Median
                                   30
                                           Max
## -315.824 -83.622 -8.919 77.962 280.690
## Coefficients:
##
                                    Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                   3.403e+00 1.754e+01
                                                        0.194 0.84646
## recession_dummy_dollars_m
                                 -9.085e+01 3.116e+01 -2.916 0.00418 **
## df_rev_count$coredata.df_rev_m. 6.221e-04 7.729e-04 0.805 0.42231
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 117 on 129 degrees of freedom
## Multiple R-squared: 0.08857,
                                  Adjusted R-squared: 0.07444
## F-statistic: 6.268 on 2 and 129 DF, p-value: 0.002523
lm_d4_adj_rev = lm(tslm_d4_resid ~ recession_dummy_dollars_m +
   df_rev_count$coredata.df_rev_m.)
summary(lm_d4_adj_rev)
##
## lm(formula = tslm_d4_resid ~ recession_dummy_dollars_m + df_rev_count$coredata.df_rev_m.)
##
## Residuals:
       Min
                 1Q
                    Median
                                   30
                                           Max
## -145.400 -28.213
                     4.314
                               30.616 111.525
##
## Coefficients:
##
                                    Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                   1.591e+01 6.836e+00 2.327 0.02152 *
## recession_dummy_dollars_m
                                  -3.874e+01 1.214e+01 -3.190 0.00179 **
## df_rev_count$coredata.df_rev_m. -6.644e-04 3.012e-04 -2.206 0.02919 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 45.6 on 129 degrees of freedom
## Multiple R-squared: 0.08137, Adjusted R-squared: 0.06712
## F-statistic: 5.713 on 2 and 129 DF, p-value: 0.004195
# detrend review counts
ts_rev_count = ts(df_rev_count$coredata.df_rev_m., start = c(2006,
   2), freq = 12)
ts_rev_count_tslm = tslm(ts_rev_count ~ trend + season)
summary(ts_rev_count_tslm)
```

```
##
## Call:
## tslm(formula = ts_rev_count ~ trend + season)
## Residuals:
##
      Min
                1Q Median
                                3Q
                                       Max
## -6146.8 -3161.7 -642.9 3115.8 8167.5
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept) -10135.277
                            1480.253
                                     -6.847 3.52e-10 ***
                                             < 2e-16 ***
                               9.876
                                      36.056
## trend
                 356.093
## season2
                 3427.756
                           1839.239
                                       1.864
                                               0.0648 .
                           1838.682
                                               0.3383
## season3
                 1767.844
                                       0.961
## season4
                 3223.751
                            1838.178
                                               0.0820 .
                                       1.754
## season5
                 2287.839
                            1837.727
                                       1.245
                                               0.2156
                 2263.018
                                               0.2205
## season6
                            1837.329
                                       1.232
## season7
                 2320.834
                            1836.984
                                       1.263
                                               0.2089
## season8
                 3676.922
                                               0.0476 *
                            1836.692
                                       2.002
## season9
                 3374.556
                            1836.453
                                       1.838
                                               0.0686 .
## season10
                 1166.008
                            1836.267
                                       0.635
                                               0.5267
## season11
                 750.823
                            1836.134
                                       0.409
                                               0.6833
## season12
                 -197.361
                            1836.054
                                               0.9146
                                     -0.107
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 4306 on 119 degrees of freedom
## Multiple R-squared: 0.9165, Adjusted R-squared: 0.9081
## F-statistic: 108.9 on 12 and 119 DF, p-value: < 2.2e-16
ts_rev_count_adj = resid(ts_rev_count_tslm, ylab = "New Reviews",
   main = "Adjusted Reviews, Total")
plot(ts_rev_count_adj)
rect(2007.9166667, -9000, 2009.5, 9000, col = rgb(red = 150/255,
   green = 25/255, blue = 25/255, alpha = 0.3), border = NA)
```



```
lm_d1_adj_rev_adj = lm(tslm_d1_resid ~ recession_dummy_dollars_m +
   ts_rev_count_adj)
summary(lm_d1_adj_rev_adj)
##
## Call:
## lm(formula = tslm_d1_resid ~ recession_dummy_dollars_m + ts_rev_count_adj)
##
## Residuals:
##
      Min
                1Q
                   Median
                                3Q
                                       Max
   -303.05
           -50.07
                    -3.11
                             56.55
                                    359.65
##
##
## Coefficients:
##
                              Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                             -4.796724
                                         9.627037
                                                   -0.498
                                                             0.619
                                                             0.192
## recession_dummy_dollars_m 33.324607
                                        25.434935
                                                    1.310
## ts_rev_count_adj
                              0.311485
                                         0.002184 142.630
                                                            <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 102.3 on 129 degrees of freedom
## Multiple R-squared: 0.9937, Adjusted R-squared: 0.9936
## F-statistic: 1.021e+04 on 2 and 129 DF, p-value: < 2.2e-16
lm_d2_adj_rev_adj = lm(tslm_d2_resid ~ recession_dummy_dollars_m +
   ts_rev_count_adj)
summary(lm_d2_adj_rev_adj)
```

```
##
## Call:
## lm(formula = tslm_d2_resid ~ recession_dummy_dollars_m + ts_rev_count_adj)
## Residuals:
               1Q Median
                               3Q
##
      Min
                                      Max
## -257.51 -74.84
                   -1.27
                            80.55 428.91
##
## Coefficients:
##
                              Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                            -12.196577 10.777970 -1.132 0.25989
## recession_dummy_dollars_m 84.734117 28.475734
                                                   2.976 0.00349 **
## ts_rev_count_adj
                              0.670808
                                         0.002445 274.365 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 114.5 on 129 degrees of freedom
## Multiple R-squared: 0.9983, Adjusted R-squared: 0.9983
## F-statistic: 3.779e+04 on 2 and 129 DF, p-value: < 2.2e-16
lm_d3_adj_rev_adj = lm(tslm_d3_resid ~ recession_dummy_dollars_m +
   ts_rev_count_adj)
summary(lm_d3_adj_rev_adj)
##
## Call:
## lm(formula = tslm_d3_resid ~ recession_dummy_dollars_m + ts_rev_count_adj)
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
                            58.72 244.76
## -351.65 -55.54
                   -0.17
##
## Coefficients:
                              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                             12.307561
                                         8.912974
                                                   1.381 0.169710
## recession_dummy_dollars_m -85.505163 23.548357 -3.631 0.000406 ***
                              0.016770
                                        0.002022
                                                   8.294 1.25e-13 ***
## ts_rev_count_adj
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 94.71 on 129 degrees of freedom
## Multiple R-squared: 0.4026, Adjusted R-squared: 0.3933
## F-statistic: 43.47 on 2 and 129 DF, p-value: 3.712e-15
lm_d4_adj_rev_adj = lm(tslm_d4_resid ~ recession_dummy_dollars_m +
   ts_rev_count_adj)
summary(lm_d4_adj_rev_adj)
##
## lm(formula = tslm_d4_resid ~ recession_dummy_dollars_m + ts_rev_count_adj)
##
## Residuals:
       Min
                      Median
                                   3Q
                                           Max
                 1Q
## -156.602 -22.164
                       6.943
                               27.480 101.189
```

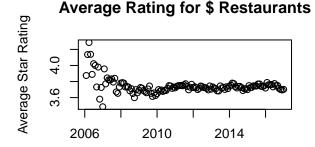
```
##
## Coefficients:
                              Estimate Std. Error t value Pr(>|t|)
##
                              4.662e+00 4.092e+00
                                                   1.139 0.25668
## (Intercept)
## recession_dummy_dollars_m -3.239e+01 1.081e+01 -2.996 0.00328 **
## ts rev count adj
                            -3.962e-03 9.282e-04 -4.269 3.78e-05 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 43.48 on 129 degrees of freedom
## Multiple R-squared: 0.1647, Adjusted R-squared: 0.1518
## F-statistic: 12.72 on 2 and 129 DF, p-value: 9.082e-06
vif(lm_d1_adj_rev_adj)
## recession_dummy_dollars_m
                                      ts_rev_count_adj
                   1.005547
                                              1.005547
vif(lm_d2_adj_rev_adj)
## recession_dummy_dollars_m
                                      ts_rev_count_adj
                    1.005547
                                              1.005547
vif(lm_d3_adj_rev_adj)
## recession_dummy_dollars_m
                                      ts_rev_count_adj
##
                    1.005547
                                              1.005547
vif(lm_d4_adj_rev_adj)
## recession_dummy_dollars_m
                                     ts_rev_count_adj
##
                   1.005547
                                              1.005547
```

re examine stars, but subset by dollar signs

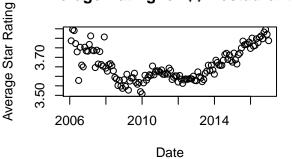
```
par(mfrow = c(2, 2))
dollars_1_star_xts = xts(dollars_obd_1_star$stars, as.Date(dollars_obd_1_star$date,
    "%Y-%m-%d")
df_d_1_star = apply.monthly(dollars_1_star_xts, sum)
df_dollars_1_star = data.frame(date = index(df_d_1_star), coredata(df_d_1_star))
df_dollars_1_star$avg = df_dollars_1_star$coredata.df_d_1_star./df_dollars_1$coredata.df_d_1.
plot(df_dollars_1_star$date, df_dollars_1_star$avg, xlab = "Date",
   ylab = "Average Star Rating", main = "Average Rating for $ Restaurants")
d1_star_lm = lm(df_dollars_1_star$avg ~ recession_dummy_dollars_m)
summary(d1 star lm)
##
## Call:
## lm(formula = df dollars 1 star$avg ~ recession dummy dollars m)
## Residuals:
                     Median
       Min
                  1Q
                                    3Q
                                            Max
  -0.26498 -0.03895 -0.01530 0.01052 0.53502
##
```

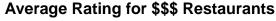
```
## Coefficients:
##
                              Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                              3.750694
                                        0.009036 415.069
## recession_dummy_dollars_m -0.044273
                                        0.023818 -1.859
                                                             0.0653 .
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.09606 on 130 degrees of freedom
## Multiple R-squared: 0.02589, Adjusted R-squared: 0.0184
## F-statistic: 3.455 on 1 and 130 DF, p-value: 0.06532
dollars_2_star_xts = xts(dollars_obd_2_star$stars, as.Date(dollars_obd_2_star$date,
    "%Y-%m-%d"))
df_d_2_star = apply.monthly(dollars_2_star_xts, sum)
df_dollars_2_star = data.frame(date = index(df_d_2_star), coredata(df_d_2_star))
df_dollars_2_star$avg = df_dollars_2_star$coredata.df_d_2_star./df_dollars_2$coredata.df_d_2.
plot(df_dollars_2_star$date, df_dollars_2_star$avg, xlab = "Date",
    ylab = "Average Star Rating", main = "Average Rating for $$ Restaurants")
d2_star_lm = lm(df_dollars_2_star$avg ~ recession_dummy_dollars_m)
summary(d2_star_lm)
##
## Call:
## lm(formula = df_dollars_2_star$avg ~ recession_dummy_dollars_m)
## Residuals:
                     Median
       Min
                  1Q
                                    30
                                            Max
## -0.16317 -0.06408 -0.01288 0.06248 0.17477
##
## Coefficients:
##
                              Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                              3.671420
                                        0.007485 490.516 < 2e-16 ***
                                         0.019728 -3.869 0.000172 ***
## recession_dummy_dollars_m -0.076331
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.07956 on 130 degrees of freedom
## Multiple R-squared: 0.1033, Adjusted R-squared: 0.09637
## F-statistic: 14.97 on 1 and 130 DF, p-value: 0.000172
dollars_3_star_xts = xts(dollars_obd_3_star$stars, as.Date(dollars_obd_3_star$date,
    "^{\prime\prime}_{Y}-^{\prime\prime}_{m}-^{\prime\prime}_{d}"))
df_d_3_star = apply.monthly(dollars_3_star_xts, sum)
df_dollars_3_star = data.frame(date = index(df_d_3_star), coredata(df_d_3_star))
df_dollars_3_star$avg = df_dollars_3_star$coredata.df_d_3_star./df_dollars_3$coredata.df_d_3.
plot(df_dollars_3_star$date, df_dollars_3_star$avg, xlab = "Date",
    ylab = "Average Star Rating", main = "Average Rating for $$$ Restaurants")
d3_star_lm = lm(df_dollars_3_star$avg ~ recession_dummy_dollars_m)
summary(d3 star lm)
##
## lm(formula = df_dollars_3_star$avg ~ recession_dummy_dollars_m)
## Residuals:
```

```
##
                  1Q
                       Median
  -0.25080 -0.05478 -0.00522 0.03954
                                        0.40509
##
##
  Coefficients:
##
                              Estimate Std. Error t value Pr(>|t|)
  (Intercept)
                              3.800796
                                         0.008157 465.945
                                                            <2e-16 ***
##
## recession_dummy_dollars_m -0.020898
                                                   -0.972
                                                             0.333
                                         0.021501
##
## Signif. codes:
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.08671 on 130 degrees of freedom
## Multiple R-squared: 0.007215,
                                    Adjusted R-squared:
## F-statistic: 0.9447 on 1 and 130 DF, p-value: 0.3329
dollars_4_star_xts = xts(dollars_obd_4_star$stars, as.Date(dollars_obd_4_star$date,
    "%Y-%m-%d")
df_d_4_star = apply.monthly(dollars_4_star_xts, sum)
df_dollars_4_star = data.frame(date = index(df_d_4_star), coredata(df_d_4_star))
df_dollars_4_star$avg = df_dollars_4_star$coredata.df_d_4_star./df_dollars_4$coredata.df_d_4.
plot(df_dollars_4_star$date, df_dollars_4_star$avg, xlab = "Date",
    ylab = "Average Star Rating", main = "Average Rating for $$$$ Restaurants")
```

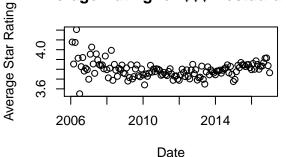


Average Rating for \$\$ Restaurants

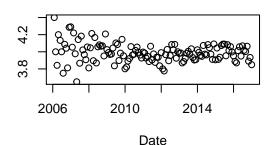




Date



Average Rating for \$\$\$\$ Restaurants



```
d4_star_lm = lm(df_dollars_4_star$avg ~ recession_dummy_dollars_m)
summary(d4_star_lm)
```

Call: Average Star Rating

```
## lm(formula = df_dollars_4_star$avg ~ recession_dummy_dollars_m)
##
## Residuals:
##
                    Median
                                   3Q
       Min
                 1Q
                                           Max
## -0.33494 -0.06462 -0.00311 0.06433 0.41506
##
## Coefficients:
##
                            Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                             3.98494
                                       0.01040 383.33
                                                          <2e-16 ***
## recession_dummy_dollars_m 0.03506
                                        0.02740
                                                   1.28
                                                           0.203
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1105 on 130 degrees of freedom
                                   Adjusted R-squared: 0.004841
## Multiple R-squared: 0.01244,
## F-statistic: 1.637 on 1 and 130 DF, p-value: 0.203
# looks like the stars dropping during a recession was only
# in 1 and 2 dollar signs restaurants
```

how bout use stars in reg for dolla dolla

```
lm_d1_adj_rev_adj_star = lm(tslm_d1_resid ~ recession_dummy_dollars_m +
   ts_rev_count_adj + df_dollars_1_star$avg)
summary(lm_d1_adj_rev_adj_star)
##
## lm(formula = tslm_d1_resid ~ recession_dummy_dollars_m + ts_rev_count_adj +
##
       df_dollars_1_star$avg)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -298.43 -50.98
                     0.42
                            55.13 365.21
##
## Coefficients:
##
                               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                            -351.19798 380.16876 -0.924
                                                             0.357
## recession_dummy_dollars_m
                              36.69179
                                          25.71834
                                                     1.427
                                                              0.156
## ts_rev_count_adj
                                           0.00237 131.083
                                                             <2e-16 ***
                               0.31065
## df_dollars_1_star$avg
                              92.38432 101.35747
                                                    0.911
                                                              0.364
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 102.4 on 128 degrees of freedom
## Multiple R-squared: 0.9938, Adjusted R-squared: 0.9936
## F-statistic: 6801 on 3 and 128 DF, p-value: < 2.2e-16
lm_d2_adj_rev_adj_star = lm(tslm_d2_resid ~ recession_dummy_dollars_m +
   ts_rev_count_adj + df_dollars_2_star$avg)
summary(lm_d2_adj_rev_adj_star)
```

```
## Call:
## lm(formula = tslm_d2_resid ~ recession_dummy_dollars_m + ts_rev_count_adj +
      df dollars 2 star$avg)
##
## Residuals:
               1Q Median
##
      Min
                               3Q
                                      Max
## -255.96 -76.18 -4.78 72.52 402.90
##
## Coefficients:
##
                              Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                            -6.772e+02 8.070e+02 -0.839 0.40291
## recession_dummy_dollars_m 9.608e+01 3.166e+01
                                                   3.035 0.00292 **
## ts_rev_count_adj
                             6.679e-01 4.259e-03 156.841 < 2e-16 ***
## df_dollars_2_star$avg
                             1.812e+02 2.199e+02
                                                  0.824 0.41137
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 114.7 on 128 degrees of freedom
## Multiple R-squared: 0.9983, Adjusted R-squared: 0.9983
## F-statistic: 2.513e+04 on 3 and 128 DF, p-value: < 2.2e-16
lm_d3_adj_rev_adj_star = lm(tslm_d3_resid ~ recession_dummy_dollars_m +
   ts_rev_count_adj + df_dollars_3_star$avg)
summary(lm_d3_adj_rev_adj_star)
##
## Call:
## lm(formula = tslm d3 resid ~ recession dummy dollars m + ts rev count adj +
      df_dollars_3_star$avg)
##
##
## Residuals:
      Min
               1Q Median
                               3Q
                                      Max
                            64.36 241.80
                   -0.01
## -333.28 -58.64
## Coefficients:
                              Estimate Std. Error t value Pr(>|t|)
                             8.423e+02 4.110e+02
                                                   2.049 0.042474 *
## (Intercept)
## recession_dummy_dollars_m -8.814e+01 2.331e+01 -3.781 0.000238 ***
                            1.900e-02 2.283e-03
                                                  8.323 1.11e-13 ***
## ts_rev_count_adj
                            -2.184e+02 1.082e+02 -2.020 0.045488 *
## df_dollars_3_star$avg
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 93.6 on 128 degrees of freedom
## Multiple R-squared: 0.421, Adjusted R-squared: 0.4075
## F-statistic: 31.03 on 3 and 128 DF, p-value: 3.839e-15
lm_d4_adj_rev_adj_star = lm(tslm_d4_resid ~ recession_dummy_dollars_m +
   ts rev count adj + df dollars 4 star$avg)
summary(lm_d4_adj_rev_adj_star)
##
## Call:
## lm(formula = tslm_d4_resid ~ recession_dummy_dollars_m + ts_rev_count_adj +
      df_dollars_4_star$avg)
```

```
##
## Residuals:
                     Median
##
       Min
                 1Q
                                   30
                                            Max
## -155.685 -23.921
                       6.389
                                         99.837
                               25.495
## Coefficients:
                              Estimate Std. Error t value Pr(>|t|)
                            -6.299e+01 1.430e+02 -0.440 0.66034
## (Intercept)
## recession_dummy_dollars_m -3.309e+01 1.094e+01 -3.023 0.00302 **
## ts_rev_count_adj
                            -4.083e-03 9.652e-04 -4.230 4.42e-05 ***
## df_dollars_4_star$avg
                             1.698e+01 3.588e+01
                                                    0.473 0.63684
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 43.61 on 128 degrees of freedom
## Multiple R-squared: 0.1662, Adjusted R-squared: 0.1466
## F-statistic: 8.503 on 3 and 128 DF, p-value: 3.411e-05
vif(lm_d1_adj_rev_adj_star)
## recession_dummy_dollars_m
                                     ts_rev_count_adj
##
                    1.026731
                                              1.182581
##
       df_dollars_1_star$avg
##
                    1.207316
vif(lm_d2_adj_rev_adj_star)
## recession_dummy_dollars_m
                                     ts_rev_count_adj
##
                   1.240119
                                              3.043228
##
       df_dollars_2_star$avg
                   3.374949
vif(lm_d3_adj_rev_adj_star)
## recession dummy dollars m
                                      ts_rev_count_adj
##
                                              1.312308
                   1.008711
##
       df_dollars_3_star$avg
##
                    1.314554
vif(lm_d4_adj_rev_adj_star)
## recession_dummy_dollars_m
                                     ts_rev_count_adj
##
                   1.024237
                                              1.080757
##
       df_dollars_4_star$avg
                    1.088332
# not really a difference, star ratings dynamics not really
# linked to review numbers, but both effected by rec in dif
# ways
```

comment out for now, cuz takes too long to process

```
analyze word usages
buildCorpus = function(data, stem) {
   corpus = Corpus(VectorSource(data))
```

```
corpus = tm_map(corpus, content_transformer(tolower))
    corpus = tm_map(corpus, PlainTextDocument)
    corpus = tm_map(corpus, removePunctuation)
    corpus = tm_map(corpus, removeWords, stopWords)
    if (stem == 1)
        corpus = tm_map(corpus, stemDocument)
   return(corpus)
}
buildWordCloud = function(corpus, pal, val, name) {
   wordcloud(corpus, max.words = 75, random.order = FALSE, colors = brewer.pal(val,
       pal), main = name)
stopWords = removePunctuation(stopwords("SMART"))
restaurant_reviews_rec = with(restaurant_reviews, restaurant_reviews[(restaurant_reviews$date >=
    "2007-12" & restaurant_reviews$date <= "2009-06"), ])
restaurant_reviews_norec = with(restaurant_reviews, restaurant_reviews[(restaurant_reviews$date >
    "2009-06" & restaurant_reviews$date <= "2011-12"), ])
# create corupses
corpus_reviews_rec = buildCorpus(restaurant_reviews_rec$text,
dtm rec = DocumentTermMatrix(corpus reviews rec)
tidy rec = tidy(dtm rec)
ap_sentiments <- tidy_rec %>% inner_join(get_sentiments("bing"),
    by = c(term = "word"))
ap_sentiments
## # A tibble: 436,171 \times 4
##
         document
                             term count sentiment
##
            <chr>
                             <chr> <dbl>
                                            <chr>>
## 1 character(0)
                             died
                                      1 negative
## 2 character(0)
                       enthusiasm
                                      1 positive
## 3 character(0)
                        fantastic
                                      2 positive
## 4 character(0)
                             good
                                      1 positive
                                      1 negative
## 5 character(0)
                         horrible
## 6 character(0)
                             love
                                      1 positive
## 7 character(0) recommendations
                                      1 positive
## 8 character(0)
                             good
                                      1 positive
## 9 character(0)
                             nice
                                      1 positive
                             pure
## 10 character(0)
                                      1 positive
## # ... with 436,161 more rows
ap sentiments %>% count(document, sentiment, wt = count) %>%
    ungroup() %>% spread(sentiment, n, fill = 0) %>% mutate(sentiment = positive -
   negative) %>% arrange(sentiment)
## # A tibble: 1 × 4
         document negative positive sentiment
##
            <chr>
                    <dbl> <dbl>
                                        <dbl>
```

```
## 1 character(0)
                     158714
                              346991
                                         188277
ap_sentiments %>% count(sentiment, term, wt = count) %>% ungroup() %>%
    filter(n >= 2000) %>% mutate(n = ifelse(sentiment == "negative",
    -n, n)) %>% mutate(term = reorder(term, n)) %>% ggplot(aes(term,
    n, fill = sentiment)) + geom_bar(stat = "identity") + theme(axis.text.x = element_text(angle = 90,
    hjust = 1)) + ylab("Contribution to sentiment")
   40000 -
Contribution to sentiment
   30000 -
                                                                                  sentiment
   20000 -
                                                                                      negative
                                                                                      positive
    10000 -
                                                recomme
                                         term
# negative: 158714 positive: 346991 percent negative: 31.4%
# cheap: 3rd highest negative word expensive: 7th
corpus_reviews_norec = buildCorpus(restaurant_reviews_norec$text,
dtm_norec = DocumentTermMatrix(corpus_reviews_norec)
tidy_norec = tidy(dtm_norec)
ap_sentiments <- tidy_norec %>% inner_join(get_sentiments("bing"),
    by = c(term = "word"))
ap_sentiments
## # A tibble: 2,121,102 × 4
```

```
## # A tibble: 2,121,102 × 4
## document term count sentiment
## <chr> <chr> <chr> <dbl> <chr>
## 1 character(0) amazingly 1 positive
## 2 character(0) awesome 1 positive
```

```
## 3 character(0)
                         fast
                                     positive
## 4
      character(0)
                                  1 negative
                      fucking
      character(0)
                        great
                                     positive
     character(0)
## 6
                                     positive
                         holy
                                  1
      character(0)
                         nice
                                     positive
## 8 character(0)
                                     negative
                         shit
## 9 character(0)
                                     negative
                         weak
## 10 character(0)
                         work
                                  1
                                     positive
## # ... with 2,121,092 more rows
ap_sentiments %>% count(document, sentiment, wt = count) %>%
    ungroup() %>% spread(sentiment, n, fill = 0) %>% mutate(sentiment = positive -
    negative) %>% arrange(sentiment)
## # A tibble: 1 × 4
##
         document negative positive sentiment
##
                      <dbl>
                               <dbl>
                                          <dbl>
                                         998609
## 1 character(0)
                     733329 1731938
ap_sentiments %>% count(sentiment, term, wt = count) %>% ungroup() %>%
    filter(n >= 7500) %>% mutate(n = ifelse(sentiment == "negative",
    -n, n)) %>% mutate(term = reorder(term, n)) %>% ggplot(aes(term,
    n, fill = sentiment)) + geom_bar(stat = "identity") + theme(axis.text.x = element_text(angle = 90,
    hjust = 1)) + ylab("Contribution to sentiment")
   200000 -
Sontribution to sentiment
    150000 -
                                                                                 sentiment
   100000 -
                                                                                     negative
                                                                                     positive
    50000 -
                                          term
# negative: 733329 positive: 1731938 percent negative: 29.75%
# cheap: 5th expensive: 8th
```

par(mfrow = c(1, 2))

```
## Warning in wordcloud(corpus, max.words = 75, random.order = FALSE, colors
## = brewer.pal(val, : atmosphere could not be fit on page. It will not be
## plotted.
## Warning in wordcloud(corpus, max.words = 75, random.order = FALSE, colors
## = brewer.pal(val, : favorite could not be fit on page. It will not be
## plotted.
## Warning in wordcloud(corpus, max.words = 75, random.order = FALSE, colors =
## brewer.pal(val, : burger could not be fit on page. It will not be plotted.
## Warning in wordcloud(corpus, max.words = 75, random.order = FALSE, colors =
## brewer.pal(val, : places could not be fit on page. It will not be plotted.
## Warning in wordcloud(corpus, max.words = 75, random.order = FALSE, colors =
## brewer.pal(val, : buffet could not be fit on page. It will not be plotted.
## Warning in wordcloud(corpus, max.words = 75, random.order = FALSE, colors =
## brewer.pal(val, : sweet could not be fit on page. It will not be plotted.
## Warning in wordcloud(corpus, max.words = 75, random.order = FALSE, colors =
## brewer.pal(val, : long could not be fit on page. It will not be plotted.
## Warning in wordcloud(corpus, max.words = 75, random.order = FALSE, colors =
## brewer.pal(val, : amazing could not be fit on page. It will not be plotted.
## Warning in wordcloud(corpus, max.words = 75, random.order = FALSE, colors
## = brewer.pal(val, : sandwich could not be fit on page. It will not be
## plotted.
buildWordCloud(corpus reviews norec, "Spectral", 8, "test2")
## Warning in wordcloud(corpus, max.words = 75, random.order = FALSE, colors
## = brewer.pal(val, : experience could not be fit on page. It will not be
## plotted.
## Warning in wordcloud(corpus, max.words = 75, random.order = FALSE, colors =
## brewer.pal(val, : drinks could not be fit on page. It will not be plotted.
## Warning in wordcloud(corpus, max.words = 75, random.order = FALSE, colors =
## brewer.pal(val, : dish could not be fit on page. It will not be plotted.
## Warning in wordcloud(corpus, max.words = 75, random.order = FALSE, colors =
## brewer.pal(val, : worth could not be fit on page. It will not be plotted.
## Warning in wordcloud(corpus, max.words = 75, random.order = FALSE, colors =
## brewer.pal(val, : fried could not be fit on page. It will not be plotted.
## Warning in wordcloud(corpus, max.words = 75, random.order = FALSE, colors
## = brewer.pal(val, : favorite could not be fit on page. It will not be
## plotted.
## Warning in wordcloud(corpus, max.words = 75, random.order = FALSE, colors =
## brewer.pal(val, : steak could not be fit on page. It will not be plotted.
## Warning in wordcloud(corpus, max.words = 75, random.order = FALSE, colors =
## brewer.pal(val, : flavor could not be fit on page. It will not be plotted.
## Warning in wordcloud(corpus, max.words = 75, random.order = FALSE, colors =
```

buildWordCloud(corpus_reviews_rec, "Spectral", 8, "test")

brewer.pal(val, : area could not be fit on page. It will not be plotted.

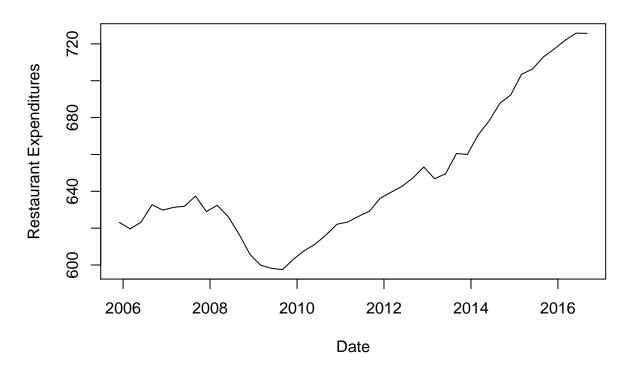
```
## Warning in wordcloud(corpus, max.words = 75, random.order = FALSE, colors =
## brewer.pal(val, : minutes could not be fit on page. It will not be plotted.
## Warning in wordcloud(corpus, max.words = 75, random.order = FALSE, colors =
## brewer.pal(val, : drink could not be fit on page. It will not be plotted.
## Warning in wordcloud(corpus, max.words = 75, random.order = FALSE, colors =
## brewer.pal(val, : special could not be fit on page. It will not be plotted.
## Warning in wordcloud(corpus, max.words = 75, random.order = FALSE, colors =
## brewer.pal(val, : friends could not be fit on page. It will not be plotted.
```

meat small made area meal sauce dinnerwine fries drinks chicken table back great tasty people find pretty for the people find pre



connect with restaurants

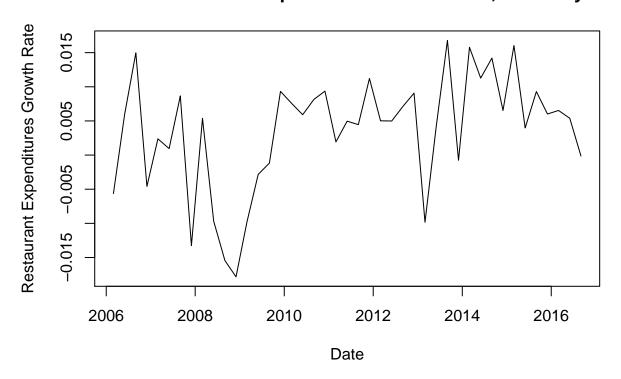
Real Restaurant Expenditures, Quarterly



```
test_stationary(restaurant_expenditures$real_exp)
```

```
## Warning in kpss.test(t): p-value smaller than printed p-value
##
   KPSS Test for Level Stationarity
##
##
## KPSS Level = 1.7047, Truncation lag parameter = 1, p-value = 0.01
##
##
    Augmented Dickey-Fuller Test
##
##
## data: t
## Dickey-Fuller = -2.4338, Lag order = 3, p-value = 0.4021
## alternative hypothesis: stationary
rest_real_exp_diff_log = diff(log(restaurant_expenditures$real_exp))
test_stationary(rest_real_exp_diff_log)
##
   KPSS Test for Level Stationarity
##
## KPSS Level = 0.69776, Truncation lag parameter = 1, p-value =
## 0.01375
##
```

Real Restaurant Expenditures Growth Rate, Quarterly



```
## Roots of the characteristic polynomial:
## 0.829 0.7485 0.7485 0.7006 0.5467 0.5467
## VAR(y = gdp_exp_combined, p = select$select[1])
##
## Estimation results for equation rest real exp diff log:
## rest_real_exp_diff_log = rest_real_exp_diff_log.l1 + gdp_growth_subset.l1 + rest_real_exp_diff_log.l
##
##
                             Estimate Std. Error t value Pr(>|t|)
## rest_real_exp_diff_log.11 -0.3061642 0.2190439 -1.398 0.17152
                                                 2.796 0.00857 **
## gdp_growth_subset.l1
                            0.7168516 0.2564126
                                                0.824 0.41584
## rest_real_exp_diff_log.12  0.1645218  0.1996566
## gdp_growth_subset.12
                            0.1951121 0.2662260
                                                0.733 0.46880
## rest_real_exp_diff_log.13  0.1923951  0.1868020
                                                 1.030 0.31053
## gdp_growth_subset.13
                           0.1265239 0.2690216
                                                0.470 0.64123
## const
                           -0.0001735 0.0013498 -0.129 0.89852
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 0.007011 on 33 degrees of freedom
## Multiple R-Squared: 0.4144, Adjusted R-squared: 0.3079
## F-statistic: 3.892 on 6 and 33 DF, p-value: 0.004777
##
## Estimation results for equation gdp_growth_subset:
## gdp_growth_subset = rest_real_exp_diff_log.11 + gdp_growth_subset.11 + rest_real_exp_diff_log.12 + g
##
##
                            Estimate Std. Error t value Pr(>|t|)
## rest_real_exp_diff_log.l1 -0.095202 0.191103 -0.498 0.6217
## gdp_growth_subset.l1
                                     0.223705
                                               2.097 0.0437 *
                            0.469106
## rest_real_exp_diff_log.12  0.070094
                                     0.174189
                                                0.402 0.6900
## gdp_growth_subset.12
                          -0.008452
                                     0.232267 -0.036 0.9712
## rest real exp diff log.13 0.323437 0.162974 1.985 0.0556.
## gdp_growth_subset.13
                           -0.292756
                                     0.234706 -1.247
                                                        0.2211
## const
                            0.001641
                                     0.001178
                                               1.393 0.1729
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.006116 on 33 degrees of freedom
## Multiple R-Squared: 0.2667, Adjusted R-squared: 0.1333
                  2 on 6 and 33 DF, p-value: 0.09384
## F-statistic:
##
##
## Covariance matrix of residuals:
                        rest_real_exp_diff_log gdp_growth_subset
## rest_real_exp_diff_log
                                    4.915e-05
                                                     2.948e-05
## gdp_growth_subset
                                    2.948e-05
                                                     3.741e-05
##
```

```
## Correlation matrix of residuals:
##
                         rest_real_exp_diff_log gdp_growth_subset
## rest real exp diff log
                                          1.0000
                                          0.6874
                                                            1.0000
## gdp_growth_subset
grangertest(rest_real_exp_diff_log ~ gdp_growth_subset[1:length(gdp_growth_subset)],
   order = select$select[1])
## Granger causality test
##
## Model 1: rest_real_exp_diff_log ~ Lags(rest_real_exp_diff_log, 1:3) + Lags(gdp_growth_subset[1:lengt
## Model 2: rest real exp diff log ~ Lags(rest real exp diff log, 1:3)
    Res.Df Df
                   F Pr(>F)
##
## 1
        33
## 2
         36 -3 2.8912 0.05002 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
grangertest(gdp_growth_subset[1:length(gdp_growth_subset)] ~
   rest_real_exp_diff_log, order = select$select[1])
## Granger causality test
##
## Model 1: gdp_growth_subset[1:length(gdp_growth_subset)] ~ Lags(gdp_growth_subset[1:length(gdp_growth
## Model 2: gdp_growth_subset[1:length(gdp_growth_subset)] ~ Lags(gdp_growth_subset[1:length(gdp_growth
    Res.Df Df
                   F Pr(>F)
## 1
         33
## 2
         36 -3 1.3863 0.2642
rec_exp_diff_log_dummy = add_recession_dummy(rest_exp_dates_diff)
lm_rest_real_exp_diff_log = lm(rest_real_exp_diff_log ~ rec_exp_diff_log_dummy)
summary(lm_rest_real_exp_diff_log)
##
## Call:
## lm(formula = rest real exp diff log ~ rec exp diff log dummy)
##
## Residuals:
##
                      1Q
                             Median
                                            30
                                                      Max
## -0.0158435 -0.0038443 -0.0000908 0.0033176 0.0144583
##
## Coefficients:
                           Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                           0.005997
                                      0.001061
                                                 5.654 1.34e-06 ***
## rec_exp_diff_log_dummy -0.015065
                                      0.002629 -5.730 1.05e-06 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.006364 on 41 degrees of freedom
## Multiple R-squared: 0.4447, Adjusted R-squared: 0.4312
## F-statistic: 32.84 on 1 and 41 DF, p-value: 1.046e-06
```

yes gdp granger causes restaurant expenditures and recession dummy

connect num of reviews with restaurants

need to convert number of reviews to be on same scale as rest expenditure growth rates

```
rev_exp_combined = cbind(rest_real_exp_diff_log, log_rev_quarter)
select = VARselect(rev_exp_combined, lag.max = 4, type = c("const",
   "trend", "both", "none"), season = NULL, exogen = NULL)
vm_rev_exp = VAR(rev_exp_combined, select$select[1])
# plot(vm_rev_exp$y)
summary(vm_rev_exp)
##
## VAR Estimation Results:
## =========
## Endogenous variables: rest_real_exp_diff_log, log_rev_quarter
## Deterministic variables: const
## Sample size: 39
## Log Likelihood: 190.353
## Roots of the characteristic polynomial:
## 0.9262 0.9126 0.868 0.868 0.5991 0.5991 0.5268 0.5268
## VAR(y = rev_exp_combined, p = select$select[1])
##
##
## Estimation results for equation rest_real_exp_diff_log:
## rest_real_exp_diff_log = rest_real_exp_diff_log.l1 + log_rev_quarter.l1 + rest_real_exp_diff_log.l2
##
##
                            Estimate Std. Error t value Pr(>|t|)
## rest_real_exp_diff_log.l1 0.2010747 0.1805061 1.114
                                                        0.2741
## log rev quarter.l1
                          -0.0077785 0.0088976 -0.874
                                                        0.3889
## rest_real_exp_diff_log.12 0.2249583 0.1755076 1.282 0.2097
## log_rev_quarter.12
                         -0.0041271 0.0076756 -0.538 0.5948
## rest_real_exp_diff_log.13  0.1365037  0.1726607  0.791
                                                        0.4354
## log_rev_quarter.13
                           0.0005648 0.0077776
                                               0.073
                                                        0.9426
## rest_real_exp_diff_log.14 -0.0140669 0.1650931 -0.085
                                                        0.9327
## log_rev_quarter.14
                          -0.0107478 0.0078840 -1.363
                                                        0.1830
                           0.0044418 0.0025252
                                               1.759
## const
                                                        0.0888
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 0.007607 on 30 degrees of freedom
## Multiple R-Squared: 0.3578, Adjusted R-squared: 0.1866
## F-statistic: 2.09 on 8 and 30 DF, p-value: 0.06888
##
##
## Estimation results for equation log rev quarter:
## log_rev_quarter = rest_real_exp_diff_log.11 + log_rev_quarter.11 + rest_real_exp_diff_log.12 + log_r
##
##
                          Estimate Std. Error t value Pr(>|t|)
## rest_real_exp_diff_log.l1 -0.87806
                                     1.83748 -0.478 0.63621
## log_rev_quarter.l1
                           0.12723
                                     0.09057 1.405 0.17040
```

```
## rest_real_exp_diff_log.12 3.28692
                                       1.78660
                                                 1.840 0.07572 .
## log_rev_quarter.12
                             0.07675
                                     0.07813 0.982 0.33380
## rest real exp diff log.13 0.73014
                                     1.75762 0.415 0.68080
                                       0.07917 -2.103 0.04397 *
## log_rev_quarter.13
                          -0.16649
## rest_real_exp_diff_log.14 -5.18564
                                       1.68058 -3.086 0.00434 **
                                     0.08026 6.823 1.44e-07 ***
## log rev quarter.14
                           0.54755
## const
                             0.03019
                                     0.02571 1.174 0.24945
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 0.07744 on 30 degrees of freedom
## Multiple R-Squared: 0.8139, Adjusted R-squared: 0.7642
## F-statistic: 16.4 on 8 and 30 DF, p-value: 5.127e-09
##
##
##
## Covariance matrix of residuals:
                         rest_real_exp_diff_log log_rev_quarter
                                                0.0001152
## rest real exp diff log
                                     5.787e-05
## log_rev_quarter
                                     1.152e-04
                                                     0.0059970
## Correlation matrix of residuals:
                         rest_real_exp_diff_log log_rev_quarter
                                        1.0000
## rest_real_exp_diff_log
                                                        0.1955
## log_rev_quarter
                                        0.1955
                                                        1.0000
grangertest(rest_real_exp_diff_log ~ log_rev_quarter, order = select$select[1])
## Granger causality test
##
## Model 1: rest_real_exp_diff_log ~ Lags(rest_real_exp_diff_log, 1:4) + Lags(log_rev_quarter, 1:4)
## Model 2: rest_real_exp_diff_log ~ Lags(rest_real_exp_diff_log, 1:4)
##
   Res.Df Df
                   F Pr(>F)
## 1
        30
## 2
        34 -4 0.9082 0.4718
grangertest(log_rev_quarter ~ rest_real_exp_diff_log, order = select$select[1])
## Granger causality test
##
## Model 1: log_rev_quarter ~ Lags(log_rev_quarter, 1:4) + Lags(rest_real_exp_diff_log, 1:4)
## Model 2: log_rev_quarter ~ Lags(log_rev_quarter, 1:4)
## Res.Df Df
                F Pr(>F)
## 1
        30
## 2
        34 -4 2.8674 0.04005 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
# try to seasonally adjust leave trend in because the
# original seasonally adjusted rest exp had a trend
log_rev_quarter_tslm = tslm(log_rev_quarter ~ season)
summary(log_rev_quarter_tslm)
```

```
## Call:
## tslm(formula = log_rev_quarter ~ season)
## Residuals:
                 1Q
                    Median
                                  3Q
## -0.34782 -0.07594 -0.00878 0.04565 0.59583
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
                         0.05057
## (Intercept) 0.35264
                                  6.973 2.34e-08 ***
## season2
              -0.34070
                         0.06988 -4.876 1.85e-05 ***
## season3
              -0.15807
                         0.06988 -2.262 0.0293 *
## season4
              -0.41248
                         0.06988 -5.903 7.06e-07 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1599 on 39 degrees of freedom
## Multiple R-squared: 0.5214, Adjusted R-squared: 0.4846
## F-statistic: 14.16 on 3 and 39 DF, p-value: 2.155e-06
log_rev_quarter_adj = resid(log_rev_quarter_tslm)
# plot(log_rev_quarter_adj)
rev_exp_adj_combined = cbind(rest_real_exp_diff_log, log_rev_quarter_adj)
select = VARselect(rev_exp_adj_combined, lag.max = 4, type = c("const",
   "trend", "both", "none"), season = NULL, exogen = NULL)
vm_rev_adj_exp = VAR(rev_exp_adj_combined, select$select[1])
# plot(vm_rev_adj_exp$y)
summary(vm_rev_adj_exp)
##
## VAR Estimation Results:
## ==========
## Endogenous variables: rest_real_exp_diff_log, log_rev_quarter_adj
## Deterministic variables: const
## Sample size: 39
## Log Likelihood: 196.578
## Roots of the characteristic polynomial:
## 0.9055 0.828 0.721 0.721 0.5383 0.5383 0.4846 0.4846
## Call:
## VAR(y = rev_exp_adj_combined, p = select$select[1])
##
##
## Estimation results for equation rest real exp diff log:
## rest_real_exp_diff_log = rest_real_exp_diff_log.l1 + log_rev_quarter_adj.l1 + rest_real_exp_diff_log
##
##
                            Estimate Std. Error t value Pr(>|t|)
## rest_real_exp_diff_log.l1 0.180897
                                     0.180663
                                                1.001
                                                          0.325
                                     0.014668 -0.730
## log_rev_quarter_adj.l1
                           -0.010709
                                                          0.471
## rest_real_exp_diff_log.12 0.239154
                                                1.338
                                      0.178751
                                                          0.191
                                      0.011875 -0.339
## log_rev_quarter_adj.12
                         -0.004026
                                                          0.737
## rest_real_exp_diff_log.13  0.099466
                                     0.168370 0.591
                                                          0.559
## log_rev_quarter_adj.13
                            0.003002 0.012594 0.238
                                                          0.813
```

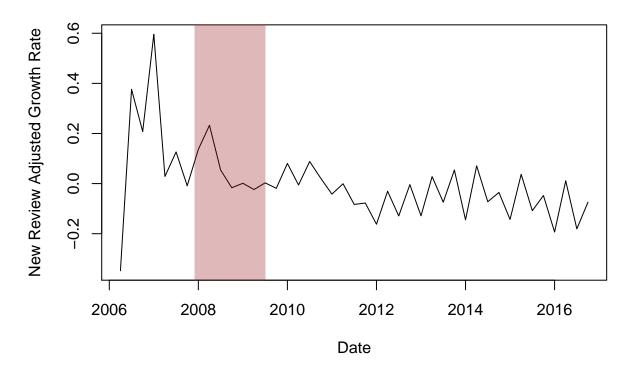
```
## rest_real_exp_diff_log.14 0.026576 0.166231
                                                  0.160
                                                            0.874
## log_rev_quarter_adj.14
                                      0.011398 -1.049
                                                           0.302
                            -0.011961
## const
                                                            0.262
                             0.001700
                                      0.001486
                                                 1.144
##
## Residual standard error: 0.007706 on 30 degrees of freedom
## Multiple R-Squared: 0.3411, Adjusted R-squared: 0.1654
## F-statistic: 1.941 on 8 and 30 DF, p-value: 0.09013
##
##
## Estimation results for equation log_rev_quarter_adj:
## log_rev_quarter_adj = rest_real_exp_diff_log.11 + log_rev_quarter_adj.11 + rest_real_exp_diff_log.12
##
##
                            Estimate Std. Error t value Pr(>|t|)
## rest_real_exp_diff_log.l1 -2.47221
                                        1.57285 -1.572 0.12649
## log_rev_quarter_adj.l1
                             0.15930
                                        0.12770
                                                1.247 0.22186
## rest_real_exp_diff_log.12 2.79746
                                      1.55620
                                                1.798 0.08231
## log_rev_quarter_adj.12
                            0.22813
                                       0.10338 2.207 0.03513 *
## rest_real_exp_diff_log.13 -0.09956
                                        1.46582 -0.068 0.94630
## log_rev_quarter_adj.13
                          -0.15938
                                       0.10964 -1.454 0.15643
## rest_real_exp_diff_log.14 -2.85185
                                       1.44720 -1.971 0.05806 .
                            0.28534
                                        0.09923 2.875 0.00735 **
## log_rev_quarter_adj.14
                            -0.01439
                                       0.01293 -1.112 0.27477
## const
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.06709 on 30 degrees of freedom
## Multiple R-Squared: 0.5769, Adjusted R-squared: 0.4641
## F-statistic: 5.114 on 8 and 30 DF, p-value: 0.0004486
##
##
##
## Covariance matrix of residuals:
                         rest_real_exp_diff_log log_rev_quarter_adj
## rest_real_exp_diff_log
                                      5.938e-05
                                                           0.000157
## log_rev_quarter_adj
                                      1.570e-04
                                                           0.004501
##
## Correlation matrix of residuals:
                         rest_real_exp_diff_log log_rev_quarter_adj
## rest_real_exp_diff_log
                                         1.0000
                                                             0.3038
                                         0.3038
                                                             1.0000
## log_rev_quarter_adj
grangertest(rest_real_exp_diff_log ~ log_rev_quarter_adj, order = select$select[1])
## Granger causality test
## Model 1: rest_real_exp_diff_log ~ Lags(rest_real_exp_diff_log, 1:4) + Lags(log_rev_quarter_adj, 1:4)
## Model 2: rest_real_exp_diff_log ~ Lags(rest_real_exp_diff_log, 1:4)
    Res.Df Df
                   F Pr(>F)
## 1
        30
```

2

34 -4 0.6949 0.6014

```
grangertest(log_rev_quarter_adj ~ rest_real_exp_diff_log, order = select$select[1])
## Granger causality test
##
## Model 1: log_rev_quarter_adj ~ Lags(log_rev_quarter_adj, 1:4) + Lags(rest_real_exp_diff_log, 1:4)
## Model 2: log_rev_quarter_adj ~ Lags(log_rev_quarter_adj, 1:4)
##
    Res.Df Df
                   F Pr(>F)
## 1
         30
         34 -4 2.2997 0.08183 .
## 2
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
plot(log_rev_quarter_adj, xlab = "Date", ylab = "New Review Adjusted Growth Rate",
    main = "New Review Adjusted Growth Rate, Quarterly")
rect(2007.9166667, -1, 2009.5, 1, col = rgb(red = 150/255, green = 25/255,
   blue = 25/255, alpha = 0.3), border = NA)
```

New Review Adjusted Growth Rate, Quarterly



```
# plot(rest_real_exp_diff_log,type='l')

# only the lags
lm_temp = lm(log_rev_quarter_adj ~ rest_real_exp_diff_log)

summary(lm_temp)

##
## Call:
```

```
## lm(formula = log_rev_quarter_adj ~ rest_real_exp_diff_log)
##
## Residuals:
##
       Min
                 1Q Median
                                   3Q
                                           Max
## -0.35555 -0.07711 -0.01678 0.04534 0.58897
##
## Coefficients:
                          Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                          0.002987 0.025818 0.116
                                                         0.908
                                                         0.769
## rest_real_exp_diff_log -0.842576
                                   2.849128 -0.296
## Residual standard error: 0.1558 on 41 degrees of freedom
## Multiple R-squared: 0.002129, Adjusted R-squared:
## F-statistic: 0.08746 on 1 and 41 DF, p-value: 0.7689
```

build rest exp into the dollar signs models

```
# convert to quarterly add in rest exp try var model with
# adding in rest exp
# adjusted num new rev by dollar signs
d1_quarterly = apply.quarterly(as.xts(tslm_d1_resid), FUN = sum)
ts_d1_quarterly = ts(d1_quarterly, start = c(2006, 1), freq = 4)
d2 quarterly = apply.quarterly(as.xts(tslm d2 resid), FUN = sum)
ts_d2_quarterly = ts(d2_quarterly, start = c(2006, 1), freq = 4)
d3_quarterly = apply.quarterly(as.xts(tslm_d3_resid), FUN = sum)
ts d3 quarterly = ts(d3 \text{ quarterly}, \text{ start} = c(2006, 1), \text{ freq = 4})
d4_quarterly = apply.quarterly(as.xts(tslm_d4_resid), FUN = sum)
ts_d4_quarterly = ts(d4_quarterly, start = c(2006, 1), freq = 4)
# review counts by quarter
rev_count_adj_q = apply.quarterly(as.xts(ts_rev_count_adj), FUN = sum)
ts_rev_count_adj_q = ts(rev_count_adj_q, start = c(2006, 1),
   freq = 4)
# dolla dolla stars
d1_star_quarterly = apply.quarterly(xts(df_dollars_1_star$avg,
    as.Date(df_dollars_1_star$date, "%Y-%m-%d")), FUN = sum)
ts_d1_star_quarterly = ts(d1_star_quarterly, start = c(2006,
    1), freq = 4)
d2_star_quarterly = apply.quarterly(xts(df_dollars_2_star$avg,
    as.Date(df_dollars_2_star$date, "%Y-%m-%d")), FUN = sum)
ts_d2_star_quarterly = ts(d2_star_quarterly, start = c(2006,
    1), freq = 4)
d3_star_quarterly = apply.quarterly(xts(df_dollars_3_star$avg,
    as.Date(df_dollars_3_star$date, "%Y-%m-%d")), FUN = sum)
ts_d3_star_quarterly = ts(d3_star_quarterly, start = c(2006,
```

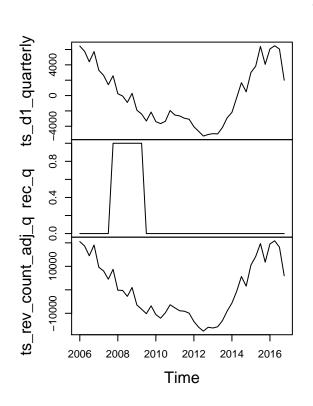
```
1), freq = 4)
d4_quarterly = apply.quarterly(xts(df_dollars_4_star$avg, as.Date(df_dollars_4_star$date,
    "%Y-%m-%d")), FUN = sum)
ts_d4_star_quarterly = ts(d4_quarterly, start = c(2006, 1), freq = 4)
# rec quarter
rec q = add recession dummy(index(d1 star quarterly))
# since in levels, use trend adjusted level of expenditures
# (detrend)
rest exp q = ts(restaurant expenditures$real exp, start = c(2006,
    1), freq = 4)
rest_exp_q_tslm = tslm(rest_exp_q ~ trend)
rest_exp_q_adj = resid(rest_exp_q_tslm)
lm_d1_full = lm(ts_d1_quarterly ~ rec_q + ts_rev_count_adj_q +
   ts_d1_star_quarterly + rest_exp_q_adj)
summary(lm d1 full)
##
## Call:
## lm(formula = ts_d1_quarterly ~ rec_q + ts_rev_count_adj_q + ts_d1_star_quarterly +
##
       rest_exp_q_adj)
##
## Residuals:
               10 Median
                               3Q
                                      Max
## -569.29 -97.37 -17.66 121.28 408.08
## Coefficients:
                         Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                      -8.777e+02 1.536e+03 -0.572
                                                        0.571
## rec_q
                                                        0.538
                       5.358e+01 8.628e+01 0.621
## ts_rev_count_adj_q 3.034e-01 5.399e-03 56.207
                                                       <2e-16 ***
## ts_d1_star_quarterly 7.738e+01 1.364e+02 0.567
                                                        0.574
                        5.007e+00 3.017e+00 1.660
## rest_exp_q_adj
                                                        0.105
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 201.6 on 39 degrees of freedom
## Multiple R-squared: 0.9975, Adjusted R-squared: 0.9972
## F-statistic: 3851 on 4 and 39 DF, p-value: < 2.2e-16
lm_d2_full = lm(ts_d2_quarterly ~ rec_q + ts_rev_count_adj_q +
   ts_d2_star_quarterly + rest_exp_q_adj)
summary(lm_d2_full)
```

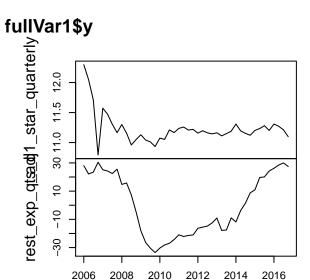
##

```
## Call:
## lm(formula = ts_d2_quarterly ~ rec_q + ts_rev_count_adj_q + ts_d2_star_quarterly +
      rest_exp_q_adj)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -502.56 -211.31
                     6.58 205.47 656.43
##
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                       -2.595e+03 4.914e+03 -0.528
                                              1.896
                        2.731e+02 1.440e+02
                                                      0.0654 .
## rec_q
                        6.637e-01 8.055e-03 82.387
                                                       <2e-16 ***
## ts_rev_count_adj_q
## ts_d2_star_quarterly 2.323e+02 4.462e+02
                                              0.521
                                                       0.6056
                        2.197e+00 4.883e+00
                                             0.450
                                                       0.6552
## rest_exp_q_adj
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 277.9 on 39 degrees of freedom
## Multiple R-squared: 0.999, Adjusted R-squared: 0.9989
## F-statistic: 9367 on 4 and 39 DF, p-value: < 2.2e-16
lm_d3_full = lm(ts_d3_quarterly \sim rec_q + ts_rev_count_adj_q +
   ts_d3_star_quarterly + rest_exp_q_adj)
summary(lm_d3_full)
##
## Call:
## lm(formula = ts_d3_quarterly ~ rec_q + ts_rev_count_adj_q + ts_d3_star_quarterly +
##
      rest_exp_q_adj)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -568.78 -164.74
                    9.84 174.17 465.42
##
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                        4.254e+03 3.553e+03
                                             1.197 0.2384
                       -2.089e+02 1.039e+02 -2.011
                                                       0.0513 .
## rec_q
## ts_rev_count_adj_q
                        2.963e-02 6.739e-03 4.397 8.22e-05 ***
## ts_d3_star_quarterly -3.705e+02 3.116e+02 -1.189
                                                     0.2418
## rest_exp_q_adj
                       -6.025e+00 3.829e+00 -1.573
                                                       0.1237
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 247.2 on 39 degrees of freedom
## Multiple R-squared: 0.5027, Adjusted R-squared: 0.4517
## F-statistic: 9.856 on 4 and 39 DF, p-value: 1.311e-05
lm_d4_full = lm(ts_d4_quarterly ~ rec_q + ts_rev_count_adj_q +
   ts_d4_star_quarterly + rest_exp_q_adj)
summary(lm_d4_full)
## Call:
```

```
## lm(formula = ts_d4_quarterly ~ rec_q + ts_rev_count_adj_q + ts_d4_star_quarterly +
##
      rest_exp_q_adj)
##
## Residuals:
      Min
                1Q Median
                                3Q
                                       Max
                             65.89 215.63
## -316.46 -67.73
                    15.81
## Coefficients:
##
                          Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                        -9.689e+02 1.208e+03 -0.802
                                                       0.4273
## rec_q
                        -7.340e+01 4.909e+01 -1.495
                                                        0.1429
                                                       0.7221
                        1.116e-03 3.115e-03
                                               0.358
## ts_rev_count_adj_q
## ts_d4_star_quarterly 8.192e+01 1.010e+02
                                               0.811
                                                        0.4224
                        -3.740e+00 1.710e+00 -2.187
                                                        0.0348 *
## rest_exp_q_adj
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 114.6 on 39 degrees of freedom
## Multiple R-squared: 0.2986, Adjusted R-squared: 0.2267
## F-statistic: 4.152 on 4 and 39 DF, p-value: 0.006758
vif(lm d1 full)
##
                          ts_rev_count_adj_q ts_d1_star_quarterly
                  rec_q
##
               1.078443
                                    4.614419
                                                         1.318413
##
         rest_exp_q_adj
               4.514264
vif(lm_d2_full)
##
                  rec_q
                          ts_rev_count_adj_q ts_d2_star_quarterly
##
               1.581756
                                    5.405495
                                                         6.411727
##
         rest_exp_q_adj
##
               6.224056
vif(lm_d3_full)
##
                          ts_rev_count_adj_q ts_d3_star_quarterly
                  rec_q
##
               1.039758
                                    4.779719
                                                         2.219843
##
         rest_exp_q_adj
##
               4.836175
vif(lm_d4_full)
##
                          ts_rev_count_adj_q ts_d4_star_quarterly
                  rec q
##
               1.079835
                                    4.752153
                                                         1.268115
##
        rest_exp_q_adj
##
              4.487196
# lots of insignificance and multicollinearity how about a
# var
combinedFull1 = cbind(ts_d1_quarterly, rec_q, ts_rev_count_adj_q,
   ts_d1_star_quarterly, rest_exp_q_adj)
select = VARselect(combinedFull1, lag.max = 4, type = c("const",
    "trend", "both", "none"), season = NULL, exogen = NULL)
fullVar1 = VAR(combinedFull1, p = select$select[1])
```

plot(fullVar1\$y)





Time

summary(fullVar1)

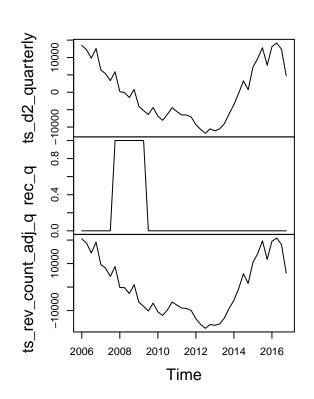
```
##
## VAR Estimation Results:
## =========
## Endogenous variables: ts_d1_quarterly, rec_q, ts_rev_count_adj_q, ts_d1_star_quarterly, rest_exp_q_a
## Deterministic variables: const
## Sample size: 40
## Log Likelihood: -607.768
## Roots of the characteristic polynomial:
## 0.9619 0.9619 0.9122 0.9122 0.9091 0.9091 0.8924 0.8924 0.8686 0.8686 0.8103 0.8103 0.7115 0.7048 0.
## VAR(y = combinedFull1, p = select$select[1])
##
##
## Estimation results for equation ts_d1_quarterly:
## ts_d1_quarterly = ts_d1_quarterly.l1 + rec_q.l1 + ts_rev_count_adj_q.l1 + ts_d1_star_quarterly.l1 +
##
##
                            Estimate Std. Error t value Pr(>|t|)
## ts_d1_quarterly.l1
                             -2.4505
                                         0.9469 -2.588 0.01805 *
                          -1296.1353
                                       674.3661 -1.922 0.06973 .
## rec_q.l1
## ts_rev_count_adj_q.l1
                              0.9371
                                         0.2587
                                                  3.622
                                                        0.00181 **
## ts_d1_star_quarterly.l1 -2428.5334 1747.9646 -1.389 0.18080
```

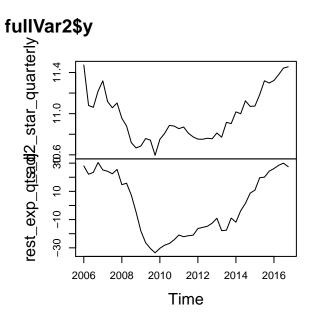
```
45.8319
                                       42.1551
                                                 1.087 0.29054
## rest_exp_q_adj.l1
                                        0.9752 -0.230 0.82043
## ts_d1_quarterly.12
                            -0.2245
## rec q.12
                           812.1205
                                      876.3552
                                                 0.927 0.36570
                                        0.2901
## ts_rev_count_adj_q.12
                             0.1788
                                                 0.616 0.54505
## ts_d1_star_quarterly.12 -2021.2192 1317.7635
                                               -1.534
                                                       0.14156
                                       46.6645 -0.408 0.68808
## rest_exp_q_adj.12
                           -19.0230
## ts_d1_quarterly.13
                            -0.7753
                                        0.9386 -0.826 0.41907
## rec_q.13
                           -409.2881
                                      883.2202 -0.463 0.64834
## ts_rev_count_adj_q.13
                             0.1171
                                        0.2809
                                                0.417
                                                       0.68131
## ts_d1_star_quarterly.13 -1187.8833 1081.3469 -1.099
                                                       0.28570
## rest_exp_q_adj.13
                            74.6138
                                       47.7373
                                                1.563 0.13455
## ts_d1_quarterly.14
                            -4.1616
                                        0.7263 -5.730
                                                       1.6e-05
## rec_q.14
                           -278.5479
                                      931.0872 -0.299
                                                       0.76806
## ts_rev_count_adj_q.14
                             1.3468
                                        0.2403
                                                5.604
                                                       2.1e-05 ***
                                      691.6660 -1.875 0.07620
## ts_d1_star_quarterly.14 -1297.1193
## rest_exp_q_adj.14
                                       38.1129
                                                -0.830
                                                       0.41673
                           -31.6419
## const
                          77721.5970 37132.9713
                                                 2.093 0.05000 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 758.6 on 19 degrees of freedom
## Multiple R-Squared: 0.9776, Adjusted R-squared: 0.954
## F-statistic: 41.43 on 20 and 19 DF, p-value: 1.2e-11
##
## Estimation results for equation rec_q:
## rec_q = ts_d1_quarterly.l1 + rec_q.l1 + ts_rev_count_adj_q.l1 + ts_d1_star_quarterly.l1 + rest_exp_q
##
##
                            Estimate Std. Error t value Pr(>|t|)
## ts_d1_quarterly.l1
                          -1.461e-04 2.642e-04 -0.553 0.586741
## rec_q.11
                           7.662e-01
                                    1.881e-01
                                                 4.073 0.000649 ***
                           2.935e-05 7.217e-05
                                                 0.407 0.688747
## ts_rev_count_adj_q.11
## ts_d1_star_quarterly.l1 -7.929e-02 4.876e-01 -0.163 0.872542
## rest_exp_q_adj.l1
                         -1.228e-03 1.176e-02 -0.104 0.917929
## ts_d1_quarterly.12
                          -3.517e-04 2.721e-04 -1.293 0.211625
                          -2.050e-01 2.445e-01 -0.838 0.412266
## rec_q.12
## ts_rev_count_adj_q.12
                           1.005e-04 8.093e-05
                                                1.242 0.229475
## ts_d1_star_quarterly.12 9.548e-02 3.676e-01 0.260 0.797879
## rest_exp_q_adj.12
                          1.161e-02 1.302e-02 0.892 0.383461
                          -2.358e-04 2.618e-04 -0.901 0.379108
## ts_d1_quarterly.13
## rec_q.13
                           9.077e-02 2.464e-01 0.368 0.716660
## ts_rev_count_adj_q.13
                           6.173e-05 7.835e-05 0.788 0.440474
                                                0.556 0.584481
## ts_d1_star_quarterly.13 1.678e-01 3.017e-01
## rest_exp_q_adj.13
                           3.998e-03 1.332e-02
                                                0.300 0.767293
## ts_d1_quarterly.14
                          -7.021e-05 2.026e-04 -0.346 0.732780
## rec_q.14
                          -3.850e-02 2.597e-01 -0.148 0.883743
## ts_rev_count_adj_q.14
                           4.796e-05 6.704e-05
                                                0.715 0.483041
## ts_d1_star_quarterly.14 -4.711e-01
                                     1.930e-01
                                                -2.442 0.024575
## rest_exp_q_adj.14
                          -2.287e-03 1.063e-02 -0.215 0.831996
## const
                           3.305e+00 1.036e+01
                                                0.319 0.753154
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
##
##
## Residual standard error: 0.2116 on 19 degrees of freedom
## Multiple R-Squared: 0.8526, Adjusted R-squared: 0.6975
## F-statistic: 5.497 on 20 and 19 DF, p-value: 0.0002359
##
##
## Estimation results for equation ts_rev_count_adj_q:
## ts_rev_count_adj_q = ts_d1_quarterly.l1 + rec_q.l1 + ts_rev_count_adj_q.l1 + ts_d1_star_quarterly.l1
##
                           Estimate Std. Error t value Pr(>|t|)
##
## ts_d1_quarterly.l1
                         -8.486e+00 3.495e+00 -2.428 0.02530 *
## rec_q.11
                         -4.701e+03 2.489e+03 -1.889 0.07431 .
## ts_rev_count_adj_q.11
                          3.162e+00 9.550e-01
                                               3.311 0.00367 **
## ts_d1_star_quarterly.l1 -9.240e+03
                                    6.452e+03 -1.432
                                                      0.16840
## rest_exp_q_adj.l1
                          1.595e+02 1.556e+02
                                              1.025 0.31811
## ts_d1_quarterly.12
                         -1.134e+00 3.600e+00 -0.315 0.75613
## rec_q.12
                          2.728e+03 3.235e+03
                                              0.843 0.40958
## ts_rev_count_adj_q.12
                          6.697e-01 1.071e+00
                                               0.625 0.53920
## ts_d1_star_quarterly.12 -8.071e+03 4.864e+03 -1.659 0.11351
                         -5.756e+01 1.723e+02 -0.334 0.74190
## rest_exp_q_adj.12
## ts_d1_quarterly.13
                         -2.651e+00 3.465e+00 -0.765 0.45355
## rec_q.13
                         -1.436e+03 3.260e+03 -0.440 0.66462
## ts_rev_count_adj_q.13
                          4.921e-01 1.037e+00
                                              0.475 0.64042
## ts_d1_star_quarterly.13 -4.684e+03 3.992e+03 -1.173 0.25511
                                              1.234 0.23209
## rest_exp_q_adj.13
                          2.175e+02 1.762e+02
## ts_d1_quarterly.14
                         -1.452e+01 2.681e+00 -5.416 3.16e-05 ***
## rec_q.14
                         -1.388e+03 3.437e+03 -0.404 0.69088
                         4.648e+00 8.871e-01
## ts_rev_count_adj_q.14
                                              5.239 4.67e-05 ***
## ts_d1_star_quarterly.14 -4.557e+03 2.553e+03 -1.785 0.09026
## rest_exp_q_adj.14
                         -6.438e+01 1.407e+02 -0.458 0.65241
## const
                          2.977e+05 1.371e+05
                                               2.172 0.04275 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 2800 on 19 degrees of freedom
## Multiple R-Squared: 0.9699, Adjusted R-squared: 0.9383
## F-statistic: 30.64 on 20 and 19 DF, p-value: 1.836e-10
##
##
## Estimation results for equation ts_d1_star_quarterly:
## ts_d1_star_quarterly = ts_d1_quarterly.l1 + rec_q.l1 + ts_rev_count_adj_q.l1 + ts_d1_star_quarterly.
##
##
                           Estimate Std. Error t value Pr(>|t|)
## ts_d1_quarterly.l1
                         -2.754e-05 8.599e-05 -0.320 0.752245
                          5.655e-02 6.124e-02
## rec_q.11
                                               0.923 0.367365
## ts_rev_count_adj_q.11
                          1.374e-05 2.349e-05
                                               0.585 0.565476
## ts_d1_star_quarterly.l1 -8.605e-02 1.587e-01 -0.542 0.594077
## rest_exp_q_adj.l1
                         -4.349e-03 3.828e-03 -1.136 0.270056
                         -2.109e-05 8.856e-05 -0.238 0.814304
## ts_d1_quarterly.12
## rec q.12
                         -1.626e-01 7.958e-02 -2.044 0.055116 .
```

```
## ts_rev_count_adj_q.12
                           4.982e-06 2.635e-05
                                                 0.189 0.852019
## ts_d1_star_quarterly.12 -7.464e-02 1.197e-01 -0.624 0.540234
                           2.949e-04 4.238e-03
## rest_exp_q_adj.12
                                                 0.070 0.945253
## ts_d1_quarterly.13
                          -1.122e-04 8.524e-05 -1.316 0.203875
## rec_q.13
                          -9.149e-02 8.021e-02 -1.141 0.268188
## ts_rev_count_adj_q.13
                           2.878e-05 2.551e-05
                                                1.129 0.273137
## ts_d1_star_quarterly.13 -6.640e-03 9.820e-02 -0.068 0.946796
## rest_exp_q_adj.13
                           2.915e-04 4.335e-03
                                                 0.067 0.947097
## ts_d1_quarterly.14
                          -1.281e-04 6.596e-05 -1.943 0.067027 .
## rec_q.14
                          -9.021e-02 8.455e-02 -1.067 0.299373
                           4.595e-05 2.182e-05
                                                 2.106 0.048775 *
## ts_rev_count_adj_q.14
## ts_d1_star_quarterly.14 2.471e-01 6.281e-02
                                                 3.934 0.000891 ***
                           2.977e-03 3.461e-03
                                                 0.860 0.400484
## rest_exp_q_adj.14
## const
                           1.033e+01 3.372e+00
                                                 3.064 0.006392 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 0.06889 on 19 degrees of freedom
## Multiple R-Squared: 0.8397, Adjusted R-squared: 0.671
## F-statistic: 4.977 on 20 and 19 DF, p-value: 0.0004646
##
##
## Estimation results for equation rest_exp_q_adj:
## rest_exp_q_adj = ts_d1_quarterly.l1 + rec_q.l1 + ts_rev_count_adj_q.l1 + ts_d1_star_quarterly.l1 + r
##
##
                            Estimate Std. Error t value Pr(>|t|)
## ts_d1_quarterly.l1
                           6.031e-05 5.307e-03
                                                 0.011
                                                         0.9911
                          -6.766e+00
                                     3.779e+00 -1.790
                                                         0.0894 .
## rec_q.11
## ts_rev_count_adj_q.l1
                           3.180e-04
                                     1.450e-03
                                                 0.219
                                                         0.8287
## ts_d1_star_quarterly.l1 -1.046e+00
                                     9.796e+00 -0.107
                                                         0.9161
## rest_exp_q_adj.l1
                           6.094e-01
                                     2.362e-01
                                                 2.580
                                                         0.0184 *
## ts_d1_quarterly.12
                          -9.275e-04
                                     5.465e-03 -0.170
                                                         0.8670
                           8.373e-01
                                                 0.170
                                                         0.8664
## rec_q.12
                                     4.911e+00
## ts_rev_count_adj_q.12
                           2.247e-04 1.626e-03
                                                 0.138
                                                        0.8915
## ts_d1_star_quarterly.12 -2.740e+00 7.385e+00 -0.371
                                                         0.7147
                                                0.576
## rest_exp_q_adj.12
                           1.506e-01 2.615e-01
                                                         0.5715
## ts_d1_quarterly.13
                                     5.260e-03 -0.276
                          -1.452e-03
                                                         0.7855
## rec_q.13
                          -5.699e+00
                                     4.950e+00 -1.151
                                                         0.2639
## ts_rev_count_adj_q.13
                           3.304e-04 1.574e-03
                                                0.210
                                                         0.8360
## ts_d1_star_quarterly.13 6.560e-01 6.060e+00
                                                 0.108
                                                         0.9149
## rest_exp_q_adj.13
                           1.604e-01 2.675e-01
                                                 0.600
                                                         0.5558
## ts_d1_quarterly.14
                          -7.497e-03 4.070e-03 -1.842
                                                         0.0812
## rec_q.14
                          -3.198e+00
                                     5.218e+00 -0.613
                                                         0.5473
                                                 1.703
## ts_rev_count_adj_q.14
                           2.293e-03
                                     1.347e-03
                                                         0.1050
## ts_d1_star_quarterly.14 -3.813e+00
                                     3.876e+00 -0.984
                                                         0.3377
## rest_exp_q_adj.14
                           9.428e-03 2.136e-01
                                                 0.044
                                                         0.9653
## const
                           8.026e+01 2.081e+02
                                                 0.386
                                                         0.7040
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 4.251 on 19 degrees of freedom
```

```
## Multiple R-Squared: 0.98, Adjusted R-squared: 0.9588
## F-statistic: 46.43 on 20 and 19 DF, p-value: 4.238e-12
##
##
##
## Covariance matrix of residuals:
                                          rec_q ts_rev_count_adj_q
                       ts d1 quarterly
                                                        2067622.85
                            575512.07 -6.170e+01
## ts_d1_quarterly
## rec_q
                                -61.70 4.479e-02
                                                             -183.88
                            2067622.85 -1.839e+02
                                                        7842058.98
## ts_rev_count_adj_q
## ts_d1_star_quarterly
                                18.06 -1.698e-03
                                                               67.87
                                244.78 -1.052e-01
## rest_exp_q_adj
                                                            1110.43
##
                       ts_d1_star_quarterly rest_exp_q_adj
## ts_d1_quarterly
                                  18.059377
                                                  244.7838
## rec_q
                                  -0.001698
                                                   -0.1052
## ts_rev_count_adj_q
                                  67.874425
                                                 1110.4343
                                                   -0.1275
## ts_d1_star_quarterly
                                 0.004746
## rest_exp_q_adj
                                 -0.127510
                                                   18.0752
## Correlation matrix of residuals:
##
                       ts_d1_quarterly rec_q ts_rev_count_adj_q
## ts_d1_quarterly
                               1.0000 -0.3843
                                                        0.97326
                               -0.3843 1.0000
                                                         -0.31026
## rec q
## ts_rev_count_adj_q
                                0.9733 -0.3103
                                                          1.00000
                               0.3455 -0.1165
## ts_d1_star_quarterly
                                                          0.35182
## rest_exp_q_adj
                                0.0759 -0.1169
                                                          0.09327
##
                       ts_d1_star_quarterly rest_exp_q_adj
## ts_d1_quarterly
                                     0.3455
                                                  0.07590
## rec_q
                                    -0.1165
                                                  -0.11693
## ts_rev_count_adj_q
                                     0.3518
                                                  0.09327
## ts_d1_star_quarterly
                                     1.0000
                                                  -0.43534
## rest_exp_q_adj
                                    -0.4353
                                                   1.00000
combinedFull2 = cbind(ts_d2_quarterly, rec_q, ts_rev_count_adj_q,
   ts_d2_star_quarterly, rest_exp_q_adj)
select = VARselect(combinedFull2, lag.max = 4, type = c("const",
    "trend", "both", "none"), season = NULL, exogen = NULL)
fullVar2 = VAR(combinedFull2, p = select$select[1])
plot(fullVar2$y)
```





summary(fullVar2)

```
##
## VAR Estimation Results:
## =========
## Endogenous variables: ts_d2_quarterly, rec_q, ts_rev_count_adj_q, ts_d2_star_quarterly, rest_exp_q_a
## Deterministic variables: const
## Sample size: 40
## Log Likelihood: -591.043
## Roots of the characteristic polynomial:
## 1.032 1.032 0.9771 0.9771 0.9426 0.9426 0.9144 0.9066 0.9066 0.8902 0.8632 0.8632 0.8596 0.8596 0.74
## VAR(y = combinedFull2, p = select$select[1])
##
##
## Estimation results for equation ts_d2_quarterly:
## ts_d2_quarterly = ts_d2_quarterly.l1 + rec_q.l1 + ts_rev_count_adj_q.l1 + ts_d2_star_quarterly.l1 + rec_q.l1
##
##
                            Estimate Std. Error t value Pr(>|t|)
## ts_d2_quarterly.11
                           5.866e+00 1.926e+00
                                                  3.046 0.00664 **
## rec_q.11
                          -1.835e+03 2.172e+03 -0.845 0.40860
## ts_rev_count_adj_q.11
                          -3.220e+00 1.270e+00 -2.536
                                                         0.02016 *
## ts_d2_star_quarterly.l1 -3.106e+03 7.528e+03 -0.413
                                                         0.68453
## rest_exp_q_adj.l1
                           3.470e+02 1.159e+02
                                                  2.994
                                                         0.00747 **
## ts_d2_quarterly.12
                          -7.587e+00 2.501e+00 -3.034
                                                         0.00683 **
```

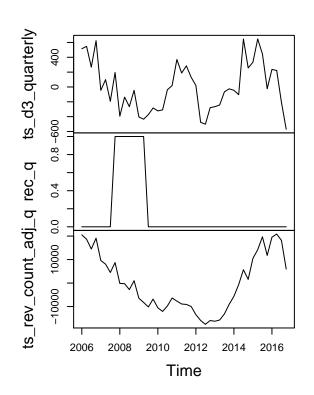
```
## rec_q.12
                           2.477e+03 2.368e+03
                                                 1.046 0.30869
                                                 3.335 0.00348 **
## ts_rev_count_adj_q.12
                           5.279e+00 1.583e+00
## ts_d2_star_quarterly.12 3.096e+03 7.095e+03
                                                 0.436
                                                       0.66751
                          -2.398e+02 1.226e+02 -1.956
## rest_exp_q_adj.12
                                                       0.06537
## ts_d2_quarterly.13
                          -1.920e+00 3.062e+00 -0.627
                                                        0.53810
## rec q.13
                          -1.003e+02 2.543e+03 -0.039 0.96896
## ts_rev_count_adj_q.13
                           8.223e-01 1.975e+00
                                                0.416 0.68176
## ts_d2_star_quarterly.13 -5.025e+03 5.855e+03 -0.858 0.40145
## rest_exp_q_adj.13
                           4.949e+01 1.331e+02
                                                 0.372 0.71414
## ts_d2_quarterly.14
                          7.118e+00 2.402e+00
                                                 2.963
                                                       0.00799 **
## rec_q.14
                          -7.759e+02 2.670e+03 -0.291
                                                       0.77449
## ts_rev_count_adj_q.14
                          -4.632e+00 1.601e+00 -2.894
                                                        0.00930 **
## ts_d2_star_quarterly.14 -1.049e+04 6.487e+03 -1.618
                                                       0.12223
## rest_exp_q_adj.14
                           1.223e+01 1.154e+02
                                                 0.106 0.91674
## const
                           1.701e+05 1.448e+05
                                                 1.174 0.25480
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 2052 on 19 degrees of freedom
## Multiple R-Squared: 0.9645, Adjusted R-squared: 0.9271
## F-statistic: 25.79 on 20 and 19 DF, p-value: 8.543e-10
##
##
## Estimation results for equation rec_q:
## =============
## rec_q = ts_d2_quarterly.l1 + rec_q.l1 + ts_rev_count_adj_q.l1 + ts_d2_star_quarterly.l1 + rest_exp_q
##
##
                            Estimate Std. Error t value Pr(>|t|)
## ts_d2_quarterly.11
                           1.495e-04 1.457e-04
                                                 1.026 0.31765
## rec_q.l1
                           4.687e-01
                                     1.643e-01
                                                 2.853 0.01018 *
## ts_rev_count_adj_q.11
                          -9.164e-05 9.608e-05 -0.954
                                                       0.35213
## ts_d2_star_quarterly.l1 -1.530e+00
                                     5.694e-01 -2.686
                                                       0.01462 *
## rest_exp_q_adj.l1
                          -3.825e-03 8.768e-03 -0.436
                                                       0.66758
## ts_d2_quarterly.12
                          -1.589e-05
                                     1.892e-04 -0.084
                                                        0.93393
## rec_q.12
                          -6.470e-02 1.791e-01 -0.361 0.72191
## ts_rev_count_adj_q.12
                           2.719e-05 1.197e-04
                                                0.227 0.82282
## ts_d2_star_quarterly.12 -9.971e-01 5.367e-01 -1.858 0.07875 .
                                                 0.352
## rest_exp_q_adj.12
                           3.266e-03 9.274e-03
                                                        0.72857
## ts_d2_quarterly.13
                           3.026e-04 2.317e-04
                                                 1.306 0.20705
## rec q.13
                          -1.012e-02 1.924e-01 -0.053 0.95860
                          -2.244e-04 1.494e-04 -1.502 0.14947
## ts_rev_count_adj_q.13
## ts_d2_star_quarterly.13 1.385e+00 4.429e-01
                                                 3.127
                                                        0.00555 **
## rest_exp_q_adj.13
                         -1.509e-03 1.007e-02 -0.150 0.88243
## ts_d2_quarterly.14
                          1.522e-04 1.817e-04
                                                0.838 0.41266
                                     2.020e-01 -2.661
## rec_q.14
                          -5.374e-01
                                                        0.01544 *
                         -9.552e-05 1.211e-04 -0.789
## ts_rev_count_adj_q.14
                                                        0.43987
## ts_d2_star_quarterly.14 1.614e-01 4.907e-01
                                                 0.329
                                                        0.74586
## rest_exp_q_adj.14
                           8.811e-03 8.732e-03
                                                 1.009
                                                        0.32564
## const
                           1.100e+01 1.096e+01
                                                 1.004 0.32805
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
```

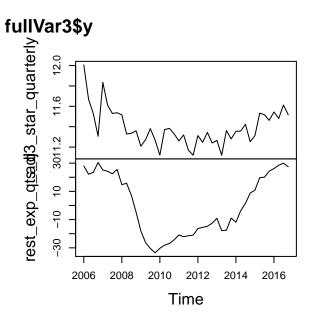
##

```
## Residual standard error: 0.1552 on 19 degrees of freedom
## Multiple R-Squared: 0.9207, Adjusted R-squared: 0.8372
## F-statistic: 11.03 on 20 and 19 DF, p-value: 1.206e-06
##
## Estimation results for equation ts rev count adj q:
## ts_rev_count_adj_q = ts_d2_quarterly.l1 + rec_q.l1 + ts_rev_count_adj_q.l1 + ts_d2_star_quarterly.l1
##
##
                           Estimate Std. Error t value Pr(>|t|)
## ts_d2_quarterly.l1
                          8.178e+00 3.026e+00
                                               2.702 0.01412 *
                         -2.870e+03 3.414e+03 -0.841 0.41099
## rec_q.11
                         -4.364e+00 1.996e+00 -2.186 0.04154 *
## ts_rev_count_adj_q.l1
## ts_d2_star_quarterly.l1 -5.636e+03 1.183e+04 -0.476 0.63926
                                               2.734 0.01319 *
## rest_exp_q_adj.l1
                          4.980e+02 1.822e+02
## ts_d2_quarterly.12
                         -1.158e+01
                                    3.931e+00 -2.947
                                                      0.00828 **
## rec_q.12
                          3.999e+03 3.721e+03
                                               1.075 0.29602
## ts_rev_count_adj_q.12
                          8.035e+00 2.488e+00
                                               3.229 0.00441 **
                                              0.385 0.70455
## ts_d2_star_quarterly.12 4.293e+03 1.115e+04
## rest_exp_q_adj.12
                         -3.583e+02 1.927e+02 -1.860
                                                      0.07847
## ts_d2_quarterly.13
                         -2.231e+00 4.814e+00 -0.464 0.64823
                         -4.709e+02 3.997e+03 -0.118 0.90746
## rec q.13
## ts_rev_count_adj_q.13
                         7.634e-01 3.104e+00
                                              0.246 0.80835
## ts_d2_star_quarterly.13 -7.344e+03 9.202e+03 -0.798 0.43469
## rest_exp_q_adj.13
                          1.062e+02 2.092e+02
                                              0.508 0.61762
## ts_d2_quarterly.14
                          1.021e+01 3.776e+00
                                               2.703 0.01409 *
                         -1.596e+03 4.196e+03 -0.380
## rec_q.14
                                                      0.70792
## ts_rev_count_adj_q.14
                         -6.600e+00 2.515e+00 -2.624
                                                      0.01672 *
## ts_d2_star_quarterly.14 -1.575e+04 1.020e+04 -1.544 0.13897
## rest_exp_q_adj.14
                         -9.019e+00 1.814e+02 -0.050 0.96087
## const
                          2.677e+05 2.277e+05
                                               1.176 0.25414
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3226 on 19 degrees of freedom
## Multiple R-Squared: 0.9601, Adjusted R-squared: 0.9181
## F-statistic: 22.86 on 20 and 19 DF, p-value: 2.479e-09
##
##
## Estimation results for equation ts_d2_star_quarterly:
## ts_d2_star_quarterly = ts_d2_quarterly.l1 + rec_q.l1 + ts_rev_count_adj_q.l1 + ts_d2_star_quarterly.
##
##
                           Estimate Std. Error t value Pr(>|t|)
## ts_d2_quarterly.11
                          2.511e-04 5.336e-05
                                              4.706 0.000154 ***
## rec_q.l1
                         -1.318e-01 6.019e-02 -2.190 0.041202 *
## ts_rev_count_adj_q.l1
                         -1.512e-04 3.520e-05 -4.296 0.000390 ***
## ts_d2_star_quarterly.l1 3.043e-01 2.086e-01
                                              1.459 0.160954
## rest_exp_q_adj.l1
                         -2.271e-03 3.212e-03 -0.707 0.488183
## ts_d2_quarterly.12
                         -1.416e-04 6.931e-05 -2.043 0.055191
## rec_q.12
                         -1.136e-01 6.562e-02 -1.731 0.099602 .
## ts_rev_count_adj_q.12 9.729e-05 4.387e-05
                                              2.218 0.038960 *
## ts_d2_star_quarterly.12 -1.106e-01 1.966e-01 -0.563 0.580260
```

```
-5.119e-03 3.397e-03 -1.507 0.148340
## rest_exp_q_adj.12
## ts_d2_quarterly.13
                          8.447e-05 8.487e-05
                                                0.995 0.332151
                         -5.572e-02 7.048e-02 -0.791 0.438943
## rec q.13
                         -5.479e-05 5.473e-05 -1.001 0.329327
## ts_rev_count_adj_q.13
## ts_d2_star_quarterly.13 -1.873e-01 1.623e-01 -1.154 0.262702
## rest_exp_q_adj.13
                          5.113e-03 3.689e-03
                                               1.386 0.181722
## ts_d2_quarterly.14
                         -1.665e-05 6.658e-05 -0.250 0.805216
## rec_q.14
                         -1.116e-01 7.399e-02 -1.508 0.147899
## ts_rev_count_adj_q.14 -8.959e-08 4.436e-05 -0.002 0.998409
## ts_d2_star_quarterly.14 1.987e-01 1.798e-01
                                               1.106 0.282726
## rest_exp_q_adj.14
                          3.444e-03 3.199e-03 1.076 0.295201
## const
                          8.803e+00 4.014e+00
                                                2.193 0.040966 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 0.05687 on 19 degrees of freedom
## Multiple R-Squared: 0.9714, Adjusted R-squared: 0.9414
## F-statistic: 32.31 on 20 and 19 DF, p-value: 1.141e-10
##
## Estimation results for equation rest_exp_q_adj:
## rest_exp_q_adj = ts_d2_quarterly.l1 + rec_q.l1 + ts_rev_count_adj_q.l1 + ts_d2_star_quarterly.l1 + r
##
                           Estimate Std. Error t value Pr(>|t|)
## ts_d2_quarterly.l1
                          5.163e-03 3.809e-03
                                                1.356 0.19114
## rec_q.11
                         -4.483e+00 4.296e+00 -1.043 0.30983
                         -3.128e-03 2.512e-03 -1.245 0.22819
## ts_rev_count_adj_q.l1
## ts_d2_star_quarterly.l1 -5.651e+00 1.489e+01 -0.380 0.70849
## rest_exp_q_adj.l1
                          7.596e-01
                                     2.292e-01
                                                3.313 0.00365 **
## ts_d2_quarterly.12
                         -1.459e-03 4.947e-03 -0.295
                                                      0.77128
## rec_q.12
                          9.946e-01 4.683e+00
                                                0.212 0.83407
                                                0.413 0.68430
## ts_rev_count_adj_q.12
                          1.293e-03 3.131e-03
## ts_d2_star_quarterly.12 -7.451e+00 1.403e+01 -0.531
                                                      0.60158
## rest_exp_q_adj.12
                          3.495e-02 2.425e-01
                                               0.144 0.88690
## ts_d2_quarterly.13
                         -2.842e-03 6.057e-03 -0.469 0.64430
## rec_q.13
                         -5.639e+00 5.030e+00 -1.121 0.27628
                                                0.472 0.64221
## ts_rev_count_adj_q.13
                          1.844e-03 3.906e-03
## ts_d2_star_quarterly.13 1.995e+01 1.158e+01
                                               1.723 0.10116
## rest_exp_q_adj.13
                         -1.055e-01 2.633e-01 -0.401 0.69312
                         -3.932e-04 4.751e-03 -0.083 0.93491
## ts_d2_quarterly.14
## rec_q.14
                         -5.516e+00 5.281e+00 -1.045
                                                      0.30931
## ts_rev_count_adj_q.14
                          4.214e-05 3.166e-03
                                               0.013 0.98952
## ts_d2_star_quarterly.14 -2.054e+01 1.283e+01 -1.601 0.12583
## rest_exp_q_adj.14
                          1.787e-01 2.283e-01
                                                0.783 0.44354
## const
                          1.527e+02 2.865e+02
                                                0.533 0.60032
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4.059 on 19 degrees of freedom
## Multiple R-Squared: 0.9817, Adjusted R-squared: 0.9625
## F-statistic: 51.03 on 20 and 19 DF, p-value: 1.784e-12
```

```
##
##
##
## Covariance matrix of residuals:
                        ts_d2_quarterly
                                           rec_q ts_rev_count_adj_q
## ts_d2_quarterly
                              4.212e+06 50.210696
                                                          6.590e+06
                              5.021e+01 0.024100
                                                           7.471e+01
## rec q
                              6.590e+06 74.712202
                                                           1.040e+07
## ts_rev_count_adj_q
## ts_d2_star_quarterly
                              4.282e+01 -0.003881
                                                           6.338e+01
                                                           5.437e+03
                              3.502e+03 -0.057205
## rest_exp_q_adj
                        ts_d2_star_quarterly rest_exp_q_adj
## ts_d2_quarterly
                                   42.824546
                                                  3.502e+03
                                   -0.003881
                                                 -5.720e-02
## rec_q
                                                 5.437e+03
## ts_rev_count_adj_q
                                   63.384622
## ts_d2_star_quarterly
                                    0.003235
                                                  9.767e-03
## rest_exp_q_adj
                                    0.009767
                                                  1.648e+01
##
## Correlation matrix of residuals:
##
                        ts_d2_quarterly
                                         rec_q ts_rev_count_adj_q
                                 1.0000 0.15760
## ts d2 quarterly
                                                             0.9955
## rec_q
                                 0.1576 1.00000
                                                             0.1492
## ts_rev_count_adj_q
                                 0.9955 0.14920
                                                             1.0000
## ts_d2_star_quarterly
                                 0.3669 -0.43952
                                                             0.3455
## rest_exp_q_adj
                                 0.4204 -0.09078
                                                             0.4153
##
                        ts_d2_star_quarterly rest_exp_q_adj
## ts_d2_quarterly
                                     0.36690
                                                    0.42036
## rec_q
                                    -0.43952
                                                   -0.09078
                                     0.34551
                                                    0.41526
## ts_rev_count_adj_q
                                                    0.04231
## ts_d2_star_quarterly
                                     1.00000
                                     0.04231
                                                    1.00000
## rest_exp_q_adj
combinedFull3 = cbind(ts_d3_quarterly, rec_q, ts_rev_count_adj_q,
    ts_d3_star_quarterly, rest_exp_q_adj)
select = VARselect(combinedFull3, lag.max = 4, type = c("const",
    "trend", "both", "none"), season = NULL, exogen = NULL)
fullVar3 = VAR(combinedFull3, p = select$select[1])
plot(fullVar3$y)
```





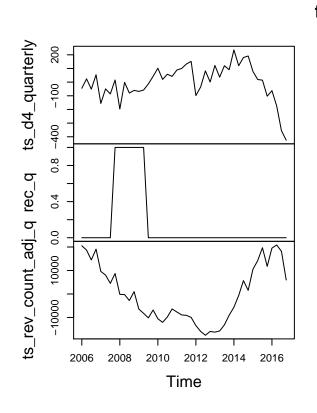
summary(fullVar3)

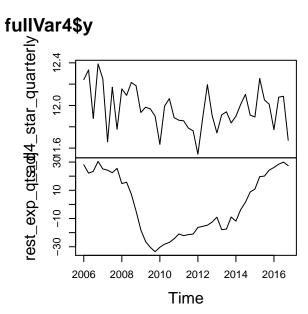
```
##
## VAR Estimation Results:
## =========
## Endogenous variables: ts_d3_quarterly, rec_q, ts_rev_count_adj_q, ts_d3_star_quarterly, rest_exp_q_a
## Deterministic variables: const
## Sample size: 43
## Log Likelihood: -763.689
## Roots of the characteristic polynomial:
## 0.8855 0.8855 0.7869 0.4815 0.04915
## Call:
## VAR(y = combinedFull3, p = select$select[1])
##
##
## Estimation results for equation ts_d3_quarterly:
## ts_d3_quarterly = ts_d3_quarterly.l1 + rec_q.l1 + ts_rev_count_adj_q.l1 + ts_d3_star_quarterly.l1 + rec_q.l1
##
##
                           Estimate Std. Error t value Pr(>|t|)
## ts_d3_quarterly.11
                          5.397e-01 1.883e-01
                                               2.866 0.00682 **
## rec_q.11
                         -1.817e+02 1.217e+02 -1.493 0.14392
## ts_rev_count_adj_q.11
                         -1.043e-03 8.931e-03 -0.117
                                                      0.90762
## ts_d3_star_quarterly.l1 2.586e+02 3.446e+02
                                               0.750
                                                      0.45772
## rest_exp_q_adj.l1
                         -7.448e-01
                                    4.360e+00 -0.171
                                                      0.86531
## const
                         -2.936e+03 3.931e+03 -0.747
                                                      0.45979
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 267.6 on 37 degrees of freedom
## Multiple R-Squared: 0.4141, Adjusted R-squared: 0.3349
## F-statistic: 5.23 on 5 and 37 DF, p-value: 0.0009912
##
##
## Estimation results for equation rec_q:
## ===========
## rec_q = ts_d3_quarterly.l1 + rec_q.l1 + ts_rev_count_adj_q.l1 + ts_d3_star_quarterly.l1 + rest_exp_q
##
##
                          Estimate Std. Error t value Pr(>|t|)
                        -3.473e-05 1.428e-04 -0.243
## ts_d3_quarterly.l1
                                                    0.8091
## rec_q.11
                         7.808e-01 9.229e-02
                                             8.460 3.55e-10 ***
                        -1.001e-05 6.771e-06 -1.478
## ts_rev_count_adj_q.11
                                                    0.1478
## ts_d3_star_quarterly.11 -2.555e-02 2.613e-01 -0.098
                                                     0.9226
                         8.216e-03 3.306e-03
                                             2.485
                                                    0.0176 *
## rest_exp_q_adj.l1
                         3.311e-01 2.980e+00
## const
                                             0.111
                                                     0.9121
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2029 on 37 degrees of freedom
## Multiple R-Squared: 0.7402, Adjusted R-squared: 0.7051
## F-statistic: 21.08 on 5 and 37 DF, p-value: 6.405e-10
##
##
## Estimation results for equation ts_rev_count_adj_q:
## ts_rev_count_adj_q = ts_d3_quarterly.l1 + rec_q.l1 + ts_rev_count_adj_q.l1 + ts_d3_star_quarterly.l1
##
##
                          Estimate Std. Error t value Pr(>|t|)
## ts_d3_quarterly.l1
                          -0.7711
                                  3.2127 -0.240 0.8116
## rec_q.11
                        -3535.7649 2076.9402 -1.702 0.0971 .
## ts_rev_count_adj_q.l1
                          0.7922
                                     0.1524 5.199 7.62e-06 ***
## ts_d3_star_quarterly.l1 -295.3277 5880.1673 -0.050
                                                    0.9602
                                   74.3943
                                              1.030
## rest_exp_q_adj.l1
                          76.6078
                                                     0.3098
                         3631.0451 67065.0351 0.054
## const
                                                    0.9571
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4565 on 37 degrees of freedom
## Multiple R-Squared: 0.8715, Adjusted R-squared: 0.8541
## F-statistic: 50.19 on 5 and 37 DF, p-value: 1.775e-15
##
## Estimation results for equation ts_d3_star_quarterly:
## ts_d3_star_quarterly = ts_d3_quarterly.l1 + rec_q.l1 + ts_rev_count_adj_q.l1 + ts_d3_star_quarterly.
##
##
                          Estimate Std. Error t value Pr(>|t|)
```

```
## ts_d3_quarterly.l1
                        -7.828e-05 7.221e-05 -1.084 0.2854
                        -6.431e-02 4.668e-02 -1.378 0.1766
## rec_q.11
## ts_rev_count_adj_q.11 6.607e-06 3.425e-06 1.929 0.0614.
## ts_d3_star_quarterly.l1 -2.741e-04 1.322e-01 -0.002 0.9984
## rest_exp_q_adj.l1
                         2.662e-03 1.672e-03 1.592 0.1199
## const
                         1.140e+01 1.507e+00 7.560 5.15e-09 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 0.1026 on 37 degrees of freedom
## Multiple R-Squared: 0.6154, Adjusted R-squared: 0.5634
## F-statistic: 11.84 on 5 and 37 DF, p-value: 7.024e-07
##
##
## Estimation results for equation rest_exp_q_adj:
## rest_exp_q_adj = ts_d3_quarterly.l1 + rec_q.l1 + ts_rev_count_adj_q.l1 + ts_d3_star_quarterly.l1 + r
##
##
                          Estimate Std. Error t value Pr(>|t|)
## ts_d3_quarterly.l1
                        -0.0011843 0.0029922 -0.396 0.695
## rec q.11
                        -9.6317060 1.9344305 -4.979 1.50e-05 ***
                        0.0001337 0.0001419 0.942 0.352
## ts_rev_count_adj_q.l1
## ts d3 star quarterly.l1 -4.0970909 5.4766986 -0.748
                                                    0.459
## rest_exp_q_adj.l1
                        ## const
                        48.2197370 62.4633550 0.772 0.445
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4.252 on 37 degrees of freedom
## Multiple R-Squared: 0.9654, Adjusted R-squared: 0.9608
## F-statistic: 206.7 on 5 and 37 DF, p-value: < 2.2e-16
##
##
##
## Covariance matrix of residuals:
                     ts_d3_quarterly rec_q ts_rev_count_adj_q
##
                    71595.326 6.4368767 9.309e+05
## ts_d3_quarterly
                              6.437 0.0411518
                                                     4.811e+01
## rec_q
## ts_rev_count_adj_q
                        930881.022 48.1078324
                                                    2.084e+07
## ts_d3_star_quarterly
                            -1.661 -0.0028005
                                                    -1.866e+01
## rest_exp_q_adj
                            441.690 0.0006136
                                                      6.659e+03
##
                     ts_d3_star_quarterly rest_exp_q_adj
## ts_d3_quarterly
                               -1.66131
                                         4.417e+02
                                           6.136e-04
## rec_q
                                -0.00280
## ts_rev_count_adj_q
                               -18.66098
                                           6.659e+03
## ts_d3_star_quarterly
                                0.01053
                                          -6.391e-02
## rest_exp_q_adj
                               -0.06391
                                            1.808e+01
##
## Correlation matrix of residuals:
                     ts_d3_quarterly
                                      rec_q ts_rev_count_adj_q
## ts_d3_quarterly
                           1.00000 0.1185874
                                                      0.76207
                            0.11859 1.0000000
## rec q
                                                       0.05195
```

```
0.76207 0.0519472
                                                               1.00000
## ts_rev_count_adj_q
                                                               -0.03984
## ts_d3_star_quarterly
                               -0.06051 -0.1345389
                                0.38823 0.0007114
                                                               0.34308
## rest_exp_q_adj
##
                        ts_d3_star_quarterly rest_exp_q_adj
## ts_d3_quarterly
                                     -0.06051
                                                   0.3882274
                                     -0.13454
                                                   0.0007114
## rec q
## ts_rev_count_adj_q
                                     -0.03984
                                                   0.3430760
## ts_d3_star_quarterly
                                      1.00000
                                                  -0.1464891
## rest_exp_q_adj
                                     -0.14649
                                                   1.0000000
combinedFull4 = cbind(ts_d4_quarterly, rec_q, ts_rev_count_adj_q,
    ts_d4_star_quarterly, rest_exp_q_adj)
select = VARselect(combinedFull4, lag.max = 4, type = c("const",
    "trend", "both", "none"), season = NULL, exogen = NULL)
fullVar4 = VAR(combinedFull4, p = select$select[1])
plot(fullVar4$y)
```





```
summary(fullVar4)
```

```
## 0.912 0.912 0.7136 0.7136 0.2047
## Call:
## VAR(y = combinedFull4, p = select$select[1])
##
## Estimation results for equation ts_d4_quarterly:
## ts_d4_quarterly = ts_d4_quarterly.l1 + rec_q.l1 + ts_rev_count_adj_q.l1 + ts_d4_star_quarterly.l1 + :
##
##
                          Estimate Std. Error t value Pr(>|t|)
## ts_d4_quarterly.l1
                         5.565e-01 1.441e-01 3.863 0.000436 ***
                        -4.811e+01 4.026e+01 -1.195 0.239684
## rec_q.11
## ts_rev_count_adj_q.11
                        -4.586e-03 2.473e-03 -1.854 0.071677
## ts_d4_star_quarterly.l1 1.110e+02 8.287e+01 1.340 0.188415
                        -2.196e-01 1.435e+00 -0.153 0.879257
## rest_exp_q_adj.l1
## const
                        -1.327e+03 9.916e+02 -1.339 0.188873
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 89.85 on 37 degrees of freedom
## Multiple R-Squared: 0.5899, Adjusted R-squared: 0.5344
## F-statistic: 10.64 on 5 and 37 DF, p-value: 2.177e-06
##
## Estimation results for equation rec_q:
## ==============
## rec_q = ts_d4_quarterly.l1 + rec_q.l1 + ts_rev_count_adj_q.l1 + ts_d4_star_quarterly.l1 + rest_exp_q
##
                          Estimate Std. Error t value Pr(>|t|)
## ts_d4_quarterly.l1
                         4.582e-06 3.234e-04 0.014 0.9888
## rec_q.11
                         7.781e-01 9.036e-02 8.611 2.29e-10 ***
                        -1.168e-05 5.552e-06 -2.103 0.0423 *
## ts_rev_count_adj_q.l1
## ts_d4_star_quarterly.l1 1.314e-01 1.860e-01
                                             0.706
                                                     0.4844
                         8.151e-03 3.222e-03
                                              2.530
                                                     0.0158 *
## rest_exp_q_adj.l1
                        -1.534e+00 2.226e+00 -0.689
## const
                                                     0.4950
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 0.2017 on 37 degrees of freedom
## Multiple R-Squared: 0.7432, Adjusted R-squared: 0.7085
## F-statistic: 21.42 on 5 and 37 DF, p-value: 5.185e-10
##
## Estimation results for equation ts_rev_count_adj_q:
## ts_rev_count_adj_q = ts_d4_quarterly.l1 + rec_q.l1 + ts_rev_count_adj_q.l1 + ts_d4_star_quarterly.l1
##
##
                          Estimate Std. Error t value Pr(>|t|)
                         1.023e+01 7.103e+00 1.440
                                                       0.158
## ts_d4_quarterly.l1
## rec_q.11
                        -2.720e+03 1.985e+03 -1.370
                                                       0.179
## ts_rev_count_adj_q.l1
                         7.646e-01 1.219e-01 6.270 2.71e-07 ***
## ts d4 star quarterly.11 2.322e+03 4.086e+03
                                             0.568
```

```
9.852e+01 7.077e+01 1.392
                                                      0.172
## rest_exp_q_adj.l1
                        -2.777e+04 4.889e+04 -0.568
                                                     0.573
## const
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4430 on 37 degrees of freedom
## Multiple R-Squared: 0.879, Adjusted R-squared: 0.8627
## F-statistic: 53.77 on 5 and 37 DF, p-value: 5.887e-16
##
##
## Estimation results for equation ts_d4_star_quarterly:
## ts_d4_star_quarterly = ts_d4_quarterly.l1 + rec_q.l1 + ts_rev_count_adj_q.l1 + ts_d4_star_quarterly.
##
##
                          Estimate Std. Error t value Pr(>|t|)
## ts_d4_quarterly.l1
                        4.346e-04 2.809e-04 1.547
                                                   0.1303
                        1.744e-01 7.849e-02 2.222
                                                   0.0325 *
## rec q.11
## ts_rev_count_adj_q.l1
                        2.520e-06 4.822e-06 0.523 0.6044
## ts_d4_star_quarterly.l1 -1.073e-01 1.616e-01 -0.664
                                                   0.5108
## rest_exp_q_adj.l1
                        3.546e-03 2.799e-03 1.267 0.2131
## const
                        1.322e+01 1.933e+00 6.837 4.68e-08 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1752 on 37 degrees of freedom
## Multiple R-Squared: 0.2702, Adjusted R-squared: 0.1715
## F-statistic: 2.739 on 5 and 37 DF, p-value: 0.03337
##
##
## Estimation results for equation rest_exp_q_adj:
## rest_exp_q_adj = ts_d4_quarterly.l1 + rec_q.l1 + ts_rev_count_adj_q.l1 + ts_d4_star_quarterly.l1 + r
##
##
                          Estimate Std. Error t value Pr(>|t|)
## ts d4 quarterly.l1
                         0.0060711 0.0067898 0.894 0.377
                        -8.6075302 1.8973409 -4.537 5.84e-05 ***
## rec_q.11
                        0.0000934 0.0001166
                                            0.801
## ts_rev_count_adj_q.11
## ts_d4_star_quarterly.l1 -1.3425796 3.9056055 -0.344
                                                      0.733
## rest_exp_q_adj.l1
                        17.3877254 46.7346891 0.372 0.712
## const
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4.234 on 37 degrees of freedom
## Multiple R-Squared: 0.9657, Adjusted R-squared: 0.9611
## F-statistic: 208.4 on 5 and 37 DF, p-value: < 2.2e-16
##
##
##
## Covariance matrix of residuals:
                     ts_d4_quarterly
##
                                      rec_q ts_rev_count_adj_q
```

```
## ts_d4_quarterly
                              8.073e+03 1.223753
                                                           1.755e+05
## rec_q
                              1.224e+00 0.040672
                                                           3.994e+01
## ts_rev_count_adj_q
                                                           1.962e+07
                              1.755e+05 39.938485
## ts_d4_star_quarterly
                              3.323e+00 -0.005123
                                                           1.579e+02
                              8.474e+01 0.009275
## rest_exp_q_adj
                                                           6.156e+03
##
                        ts_d4_star_quarterly rest_exp_q_adj
## ts d4 quarterly
                                    3.323017
                                                  8.474e+01
## rec q
                                                  9.275e-03
                                   -0.005123
## ts_rev_count_adj_q
                                  157.891513
                                                  6.156e+03
## ts_d4_star_quarterly
                                                 -1.964e-02
                                   0.030685
## rest_exp_q_adj
                                   -0.019635
                                                  1.793e+01
##
## Correlation matrix of residuals:
##
                        ts_d4_quarterly
                                           rec_q ts_rev_count_adj_q
## ts_d4_quarterly
                                1.00000 0.06754
                                                            0.44106
## rec_q
                                0.06754 1.00000
                                                            0.04471
## ts_rev_count_adj_q
                                0.44106 0.04471
                                                            1.00000
## ts_d4_star_quarterly
                                0.21113 -0.14503
                                                            0.20349
## rest_exp_q_adj
                                0.22274 0.01086
                                                            0.32818
                        ts_d4_star_quarterly rest_exp_q_adj
##
## ts_d4_quarterly
                                     0.21113
                                                    0.22274
## rec q
                                    -0.14503
                                                    0.01086
## ts_rev_count_adj_q
                                     0.20349
                                                    0.32818
## ts d4 star quarterly
                                     1.00000
                                                   -0.02647
## rest_exp_q_adj
                                    -0.02647
                                                    1.00000
```

old stuff

 $sources: fred yelp \ https://www.bea.gov/iTable/iTable.cfm?reqid=9\&step=1\&acrdn=2\#reqid=9\&step=1\&ivi=1\&904=2004\&903=64\&906=q\&905=2016\&910=x\&911=0\ https://cran.r-project.org/web/packages/tidytext/vignettes/tidying_casting.html$