

# Assignment 2 of Algorithm Design and Analysis

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## 1 Divide and Conquer(2)

QUESTION:

Try to find the median number from two databases, whose sizes are  $n$  respectively in  $O(\lg n)$  time complexity.

Notes: the given databases can only be accessed through queries.

Pseudo-Code:

**Get-Median**( $A, B, n, a, b$ )  $A, B$  denotes databases;

1:  $k = \lfloor n/2 \rfloor$ ;

2: **if**  $n = 1$  **then**

3: **return**  $\min(A(a + k), B(b + k))$ ;

4: **endif**

5: **if**  $A(a + k) < B(b + k)$  **then**

6: **return** **Get-Median**( $A, B, k, a + k, b$ );

7: **else**

8: **return** **Get-Median**( $A, B, k, a, b + k$ );

9: **endif**

Complexity Analysis:

$$T(n) \leq T(n/2) + 2$$

As a result, we have  $T(n) = O(\lg n)$

## 2 Sorting(2)

My test results are shown in the followig table, which are based on three random integer arrays whose sizes are 100,000, 1,000,000, 10,000,000 respectively.

**Comparision of different Sorting Methods**

<b>METHODS \ No.</b>	$10^5$	$10^6$	$10^7$
<i>MergeSort</i>	0.05s	0.62s	7.07s
<i>QuickSort</i>	0.03s	0.40s	4.75s
<i>M_QuickSort</i>	0.04s	0.42s	5.04s
<i>MergeSort_Stack</i>	0.06s	0.68s	7.71s
<i>QuickSort_Stack</i>	0.04s	0.50s	5.72s
<i>M_QuickSort_Stack</i>	0.04s	0.48s	5.47s

while if the input integer arrays are already in order, running time VARIES distinctively.

<b>METHODS. \ No.</b>	$10^5$
<i>MergeSort</i>	0.04s
<i>QuickSort</i>	59.71s
<i>M_QuickSort</i>	0.02s
<i>MergeSort_Stack</i>	0.04s
<i>QuickSort_Stack</i>	59.71s
<i>M_QuickSort_Stack</i>	0.03s