

Answers to the exercises for chapter: Lambda calculus

1.

```
\def\IsNil#1{#1{\expandafter\False\gobbletwo}{\True}}
\test{Detect NIL}{\IsNil\Nil}
\test{Detect non-NIL}{\IsNil{\Singleton\Nil}}
```

Output:

Detect NIL Detect non-NIL

2.

```
\def\IsOne#1{#1{\IsZero{\Tail{#1}}}\False}
```
3.

```
\def\Sub#1#2{#1{\SubFrom{#2}}{#2}}
\def\SubFrom#1#2#3{#1{\SubMinOne{#3}}\Error}
\def\SubMinOne#1#2#3{\Sub{#1}{#3}}
```

Explanation:

```
Sub <total> <term>⇒<term> SubFrom<total> Zero
if <term> is empty⇒then <total>
    otherwise⇒SubFrom<total> <term-head> <term-tail>
        ⇒<total> SubMinOne<term-tail> Error
        ⇒SubMinOne<term-tail> <total-head> <total-tail>
        ⇒Sub <total-tail> <term-tail>
```