## Answers to the exercises for chapter: Parsing

- 1. Given two transitions one an input symbol, replace that by a single transition to a new state, and  $\epsilon$ -transitions to the original two destination states. If an NFA has an  $\epsilon$ -transition from state 1 to state 2, we can replace that by a jump from state 0 to state 2, triggered by the symbol that made the transition from 0 to 1.
- 2. no answer given
- 3. Given a mapping I × S → O, and denote o<sub>i,s</sub> the output symbol for input i and state s. For each state s, introduce a new state s<sub>i</sub> for any input symbol that has a defined transition out of s. Let that state output the symbol o<sub>i,s</sub>. Now define an ε-transition from s<sub>i</sub> to the state that was the original transition from s under i. Give that state no output.

The reverse equivalence is trivial: if a state maps to an output, then it maps to that output with every input. Formally, if  $s \mapsto o$  in the second definition, then  $\{i, s\} \mapsto o$  for all i in the first.

- 4. no answer given
- 5. no answer given
- 6. no answer given
- 7. This question derives from http://www.gnu.org/software/bison/manual/html\_node/Shift-Reduce.html Proof of shifting, which implies right associativity:

```
%{
#include "sr.h"
extern int yylval;

%}

%%

[0-9]+ {yylval = atoi(yytext); return N;}
[+\n-] {return *yytext;}

%token N

%%

P : E '\n' {printf("Result: %d\n",$$);}
```

```
E : E '+' E {$$ = $1+$3;}
| E '-' E {$$ = $1-$3;}
| N

%%
  int main(void)
{
   yyparse();
}
Ouput
%% sr
1-2+5
Result: -6
```