

# PARTIAL LOCAL MORAN

HANDLING LOCAL CONFOUNDING

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**LOCAL CONFOUNDING**

**PRIOR ART IN ESDA**

**PARTIAL CONDITIONING**

**AFFORDABILITY OUTLIERS**



Bristol's big  
housing  
conversation



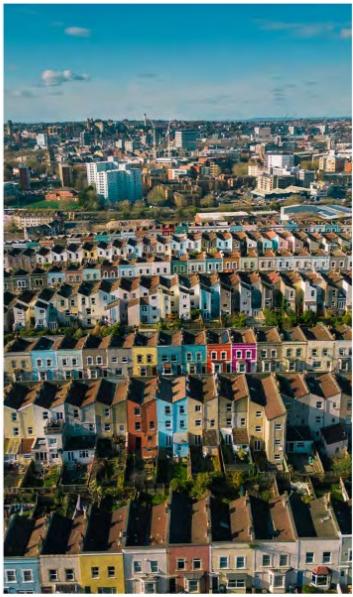
Bristol Living Rent  
Commission



BRISTOL  
ONE CITY



HOW CAN WE FIND RENT AFFORDABILITY OUTLIERS?



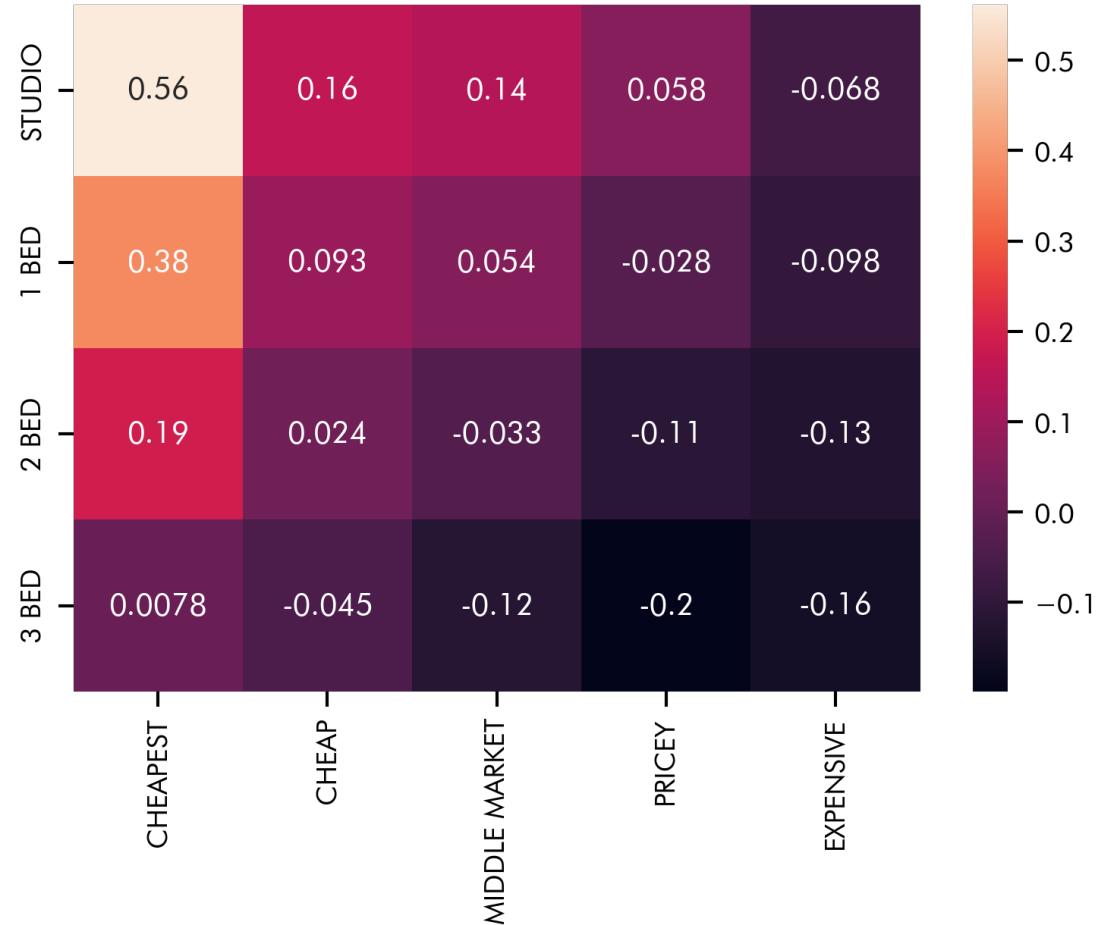
Bristol's big  
housing  
conversation



Bristol Living Rent  
Commission



BRISTOL  
ONE CITY



HOW CAN WE FIND RENT AFFORDABILITY OUTLIERS?



Bristol's big  
housing  
conversation

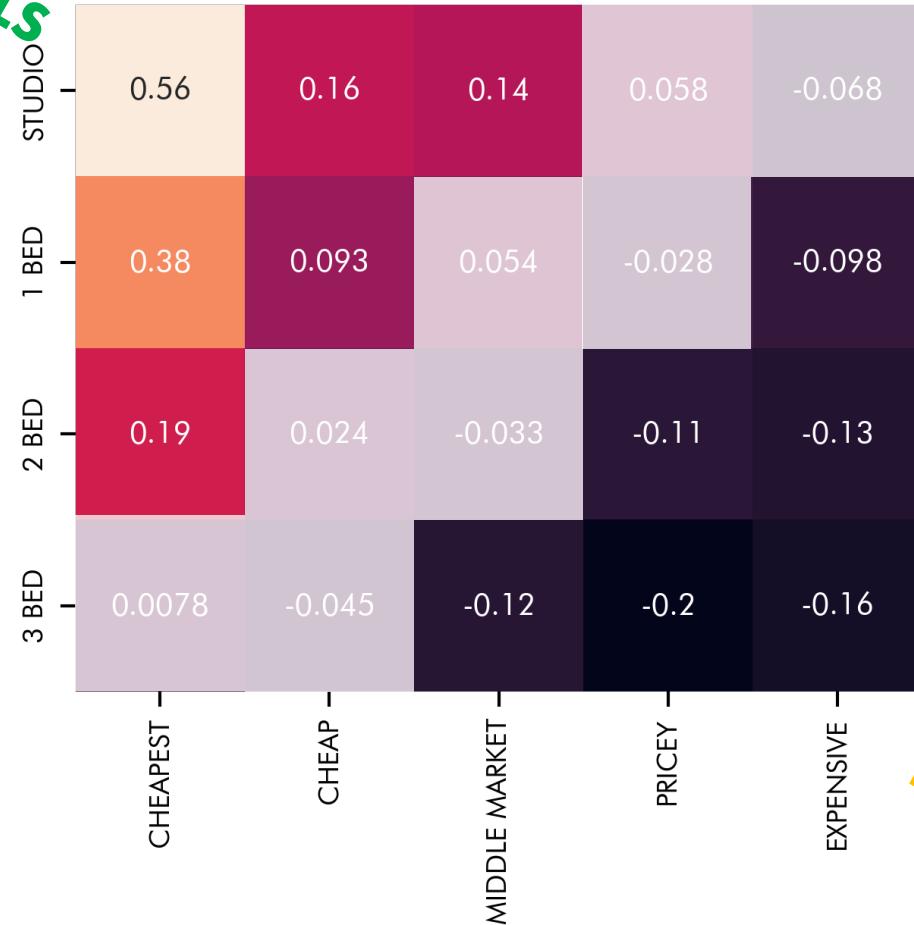


SMALL  
STEALS

Bristol Living Rent  
Commission



BRISTOL  
ONE CITY  
CITY COUNCIL



LARGE  
LEMONS

HOW CAN WE FIND RENT AFFORDABILITY OUTLIERS?

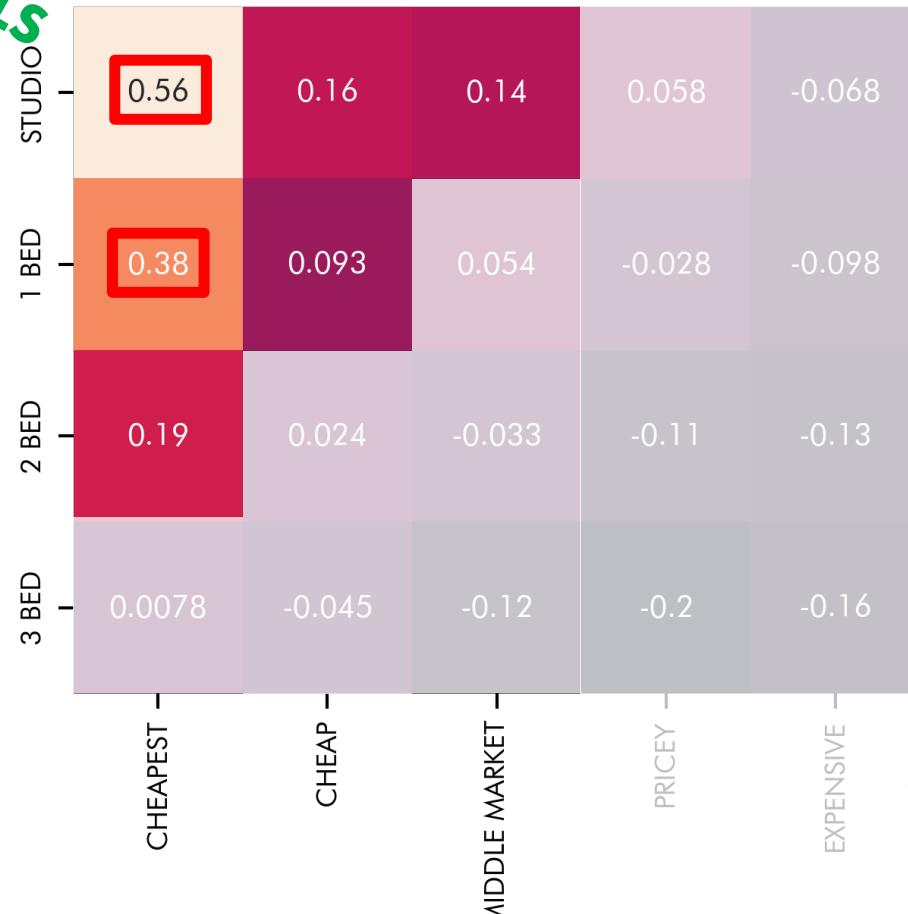


Bristol's big  
housing  
conversation



SMALL  
STEALS

DOUBLED RENT W/IN 2 YEARS



LARGE  
LEMONS

Bristol Living Rent  
Commission



BRISTOL  
ONE CITY  
CITY COUNCIL

HOW CAN WE FIND RENT AFFORDABILITY OUTLIERS?



Bristol's big  
housing  
conversation



Bristol Living Rent  
Commission



BRISTOL  
ONE CITY



*How the rent will be decided depends on the type of rent case...*

*The tribunal will look at the market or rents of similar properties in the local area.*

**HOW CAN WE FIND RENT AFFORDABILITY OUTLIERS?**



Bristol's big  
housing  
conversation



Bristol Living Rent  
Commission



BRISTOL  
ONE CITY



*How the rent will be decided depends on the type of rent case...*

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**HOW CAN WE FIND RENT AFFORDABILITY OUTLIERS?**



Bristol Living Rent  
Commission



BRISTOL  
ONE CITY



*How the rent will be decided depends on the type of rent case...*

*The tribunal will look at the market or rents of similar properties in the local area.*

What is the “rent?”

No central database of what rents are charged, only rents that are advertised.

HOW CAN WE FIND RENT AFFORDABILITY OUTLIERS?



Bristol's big  
housing  
conversation



Bristol Living Rent  
Commission



BRISTOL  
ONE CITY



*How the rent will be decided depends on the type of rent case...*

*The tribunal will look at the market or rents of similar properties in the local area.*

What is “similar?”

Depends on judgement of the assessor during inspection, structural factors, and local intangibles.

HOW CAN WE FIND RENT AFFORDABILITY OUTLIERS?



Bristol Living Rent  
Commission



BRISTOL  
ONE CITY



*How the rent will be decided depends on the type of rent case...*

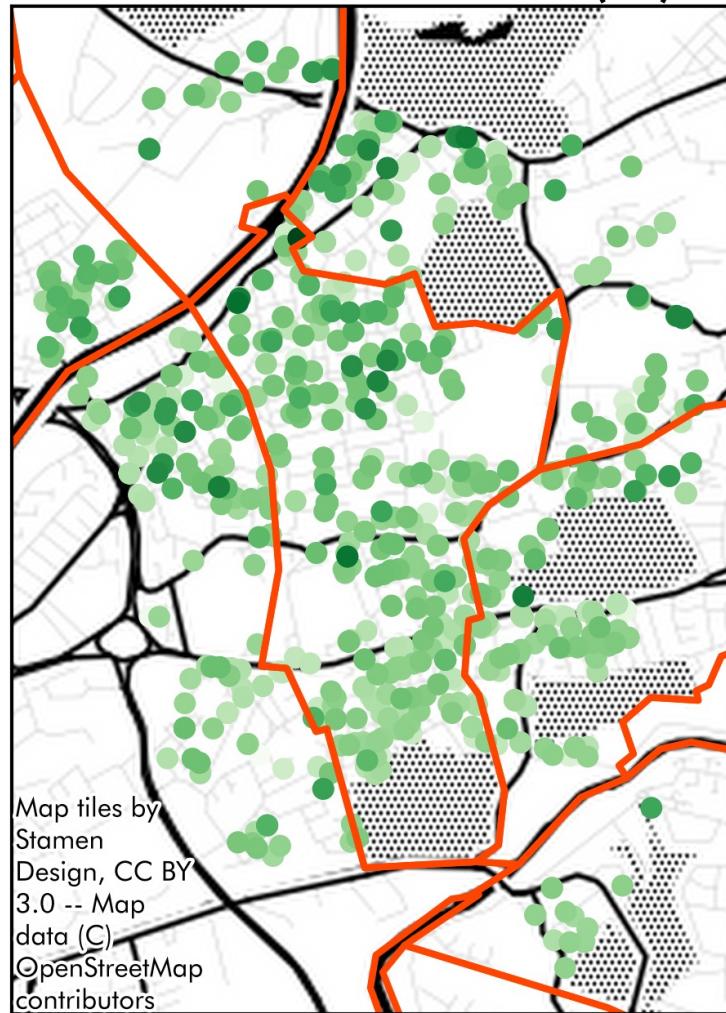
*The tribunal will look at the market or rents of similar properties in the local area.*

What is “local area?”

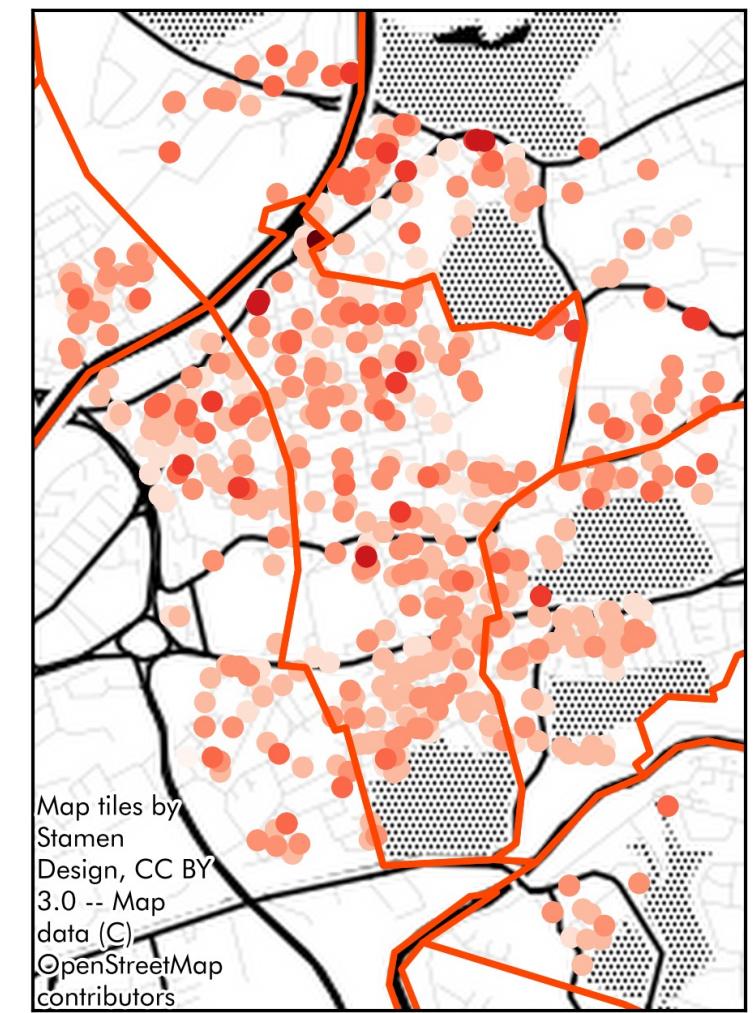
No specific guidance to decide upon  
street < n’hood < town < labor market

HOW CAN WE FIND RENT AFFORDABILITY OUTLIERS?

## WEEKLY RENT (£)

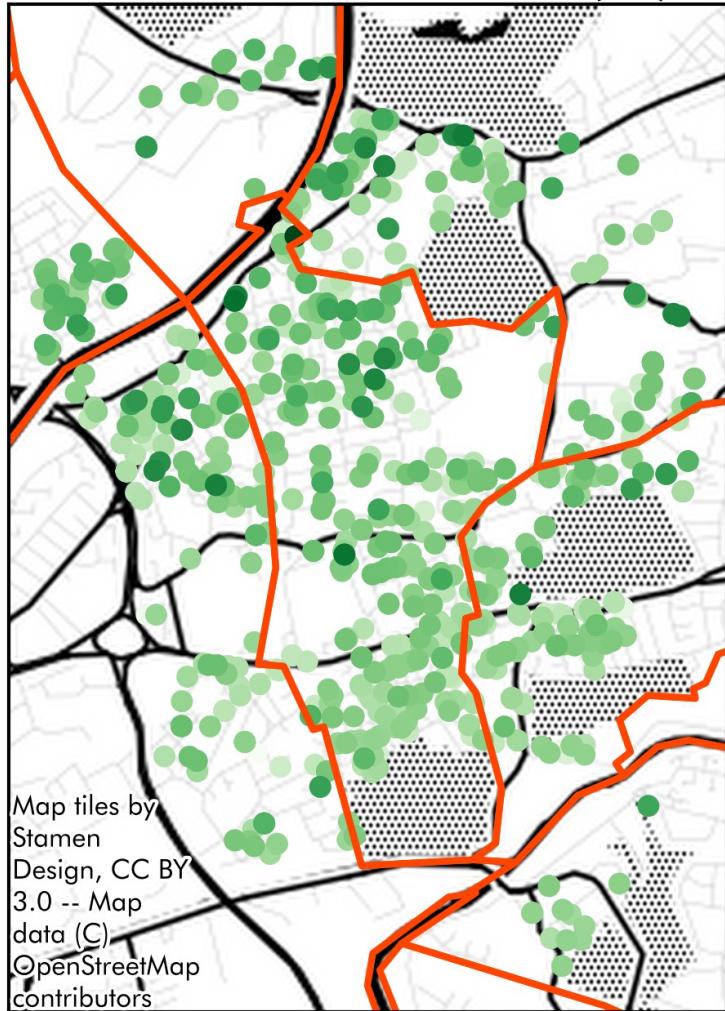


## BEDROOMS



HOW CAN WE FIND RENT AFFORDABILITY OUTLIERS?

## WEEKLY RENT (£)

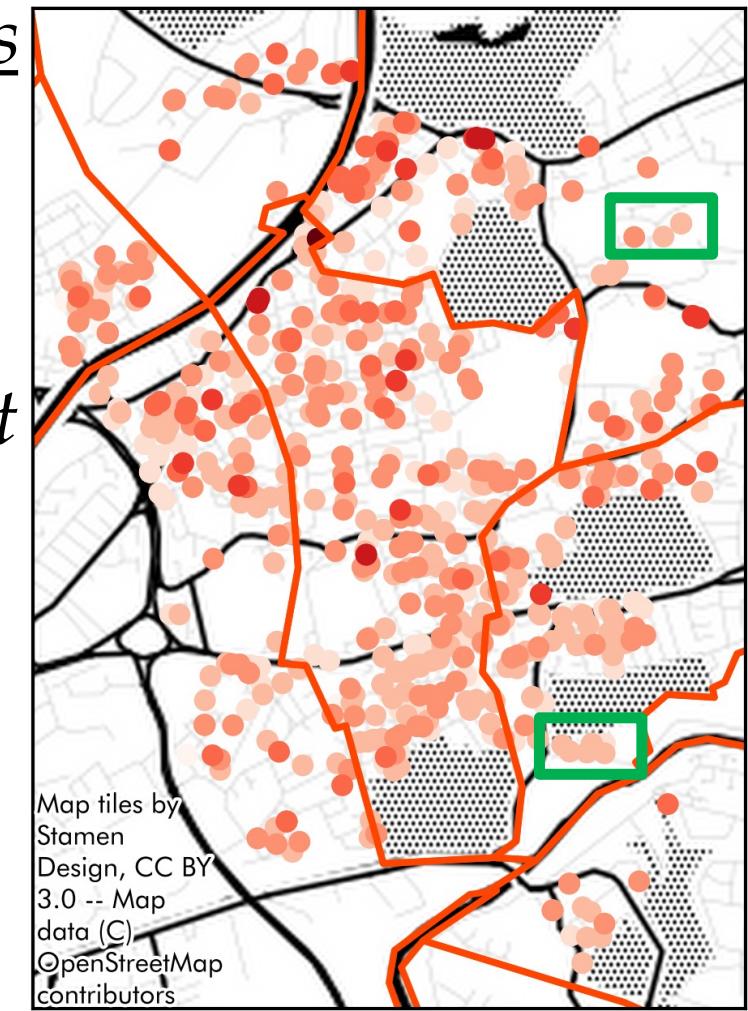


similar properties

*Lettings that are substitutes for a reasonable tenant looking to house themselves or their family.*

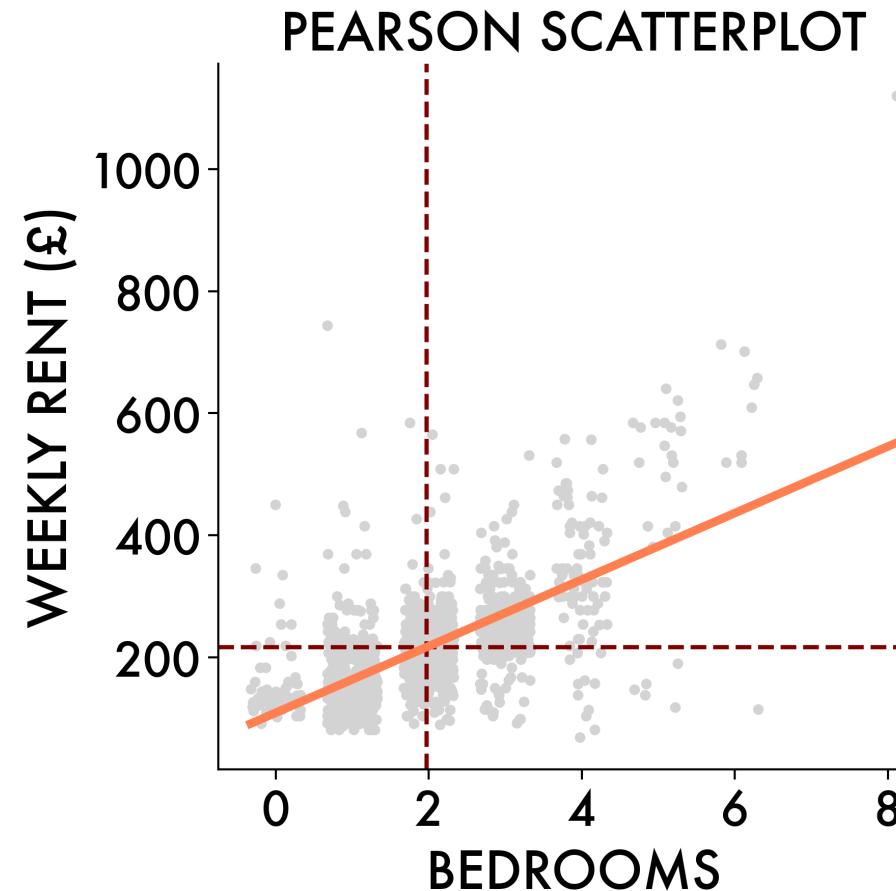
*Same bedrooms, ca. baths, receptions within some distance*

## BEDROOMS



HOW CAN WE FIND RENT AFFORDABILITY OUTLIERS?

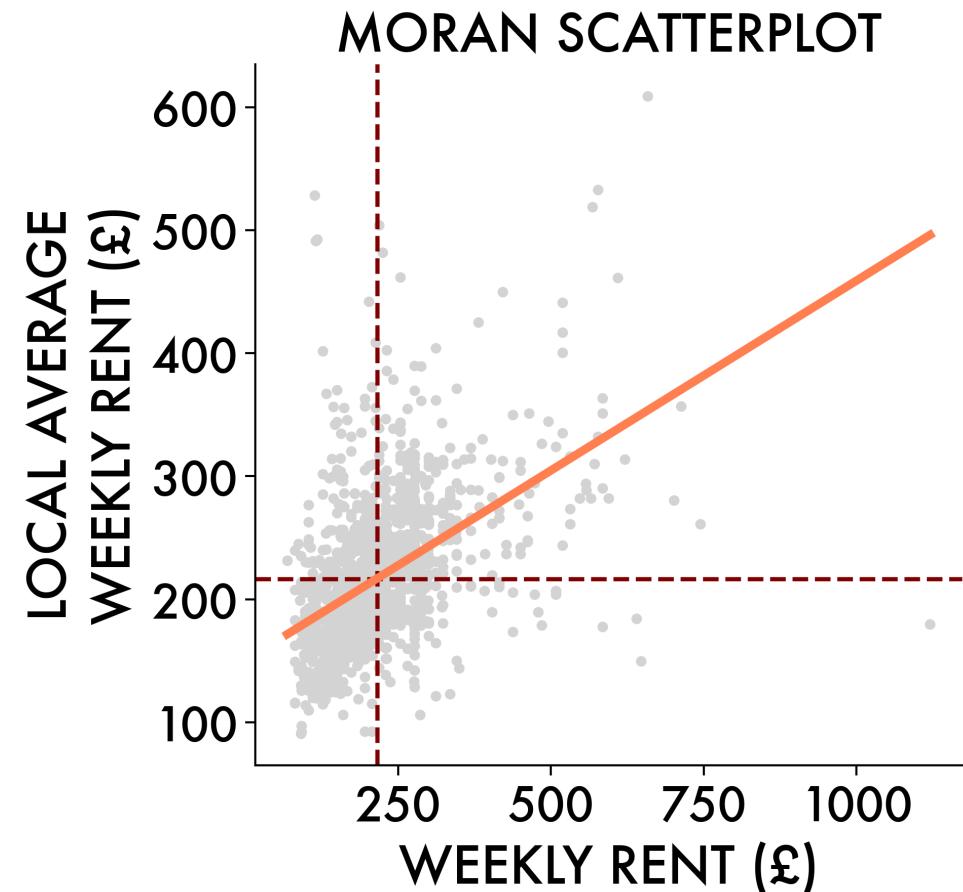
*Properties with fewer bedrooms  
are generally lower rent.*



HOW CAN WE FIND RENT AFFORDABILITY OUTLIERS?

*Properties with fewer bedrooms  
are generally lower rent.*

*Nearby properties tend to have  
similar rent levels*

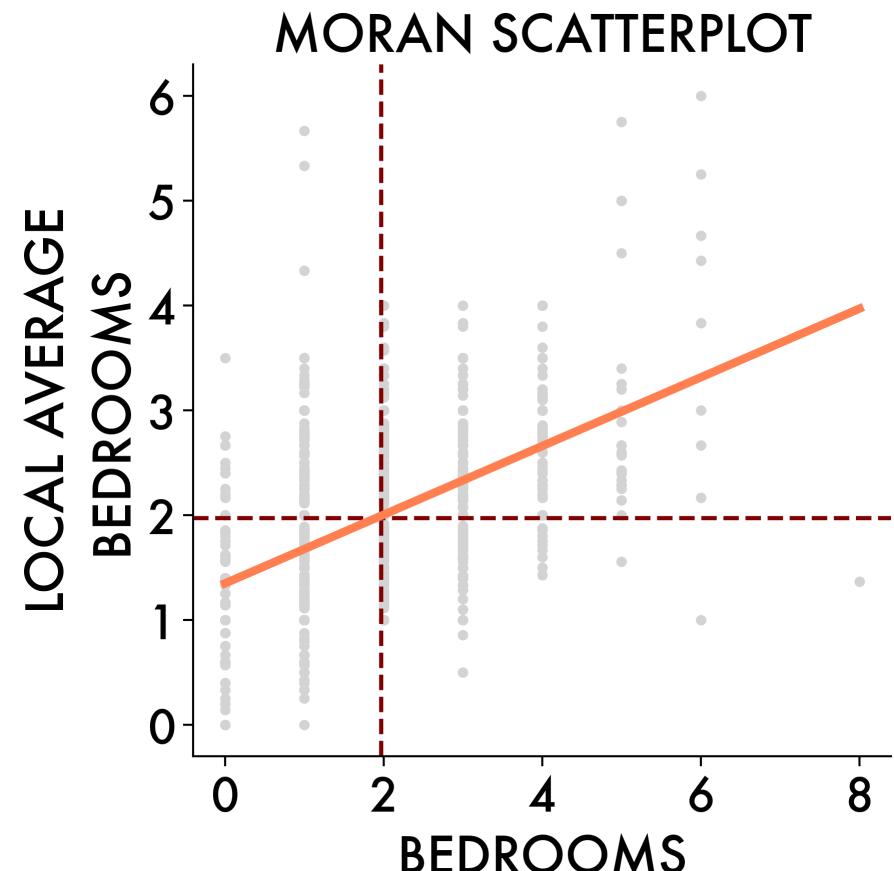


HOW CAN WE FIND RENT AFFORDABILITY OUTLIERS?

*Properties with fewer bedrooms  
are generally lower rent.*

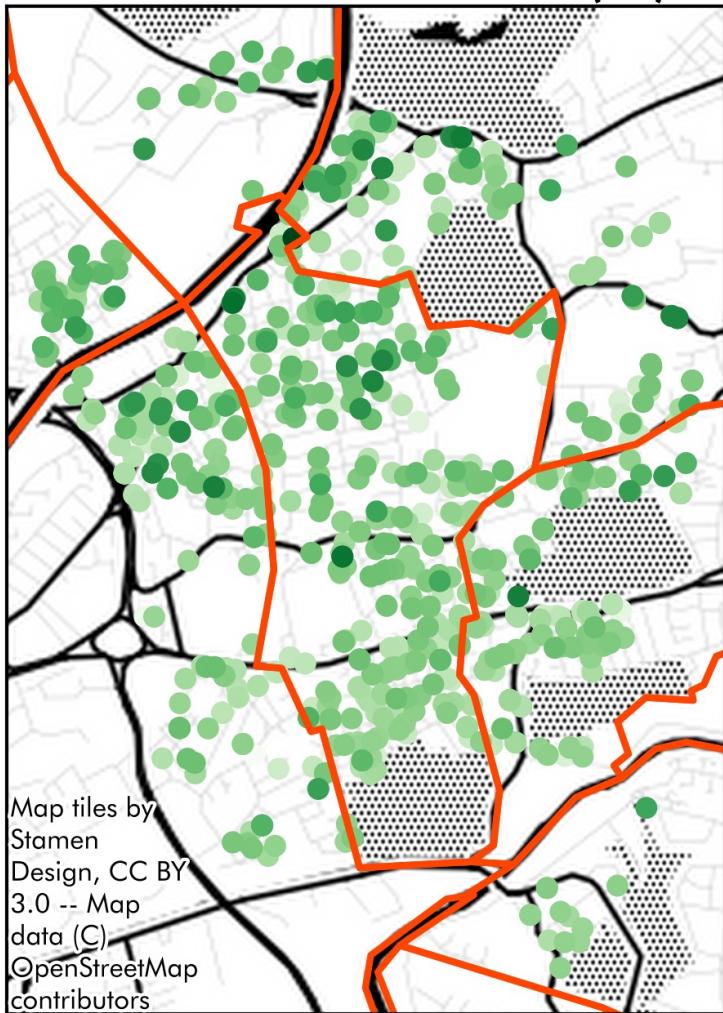
*Nearby properties tend to have  
similar rent levels*

*Nearby properties also tend to be  
of similar size as well*



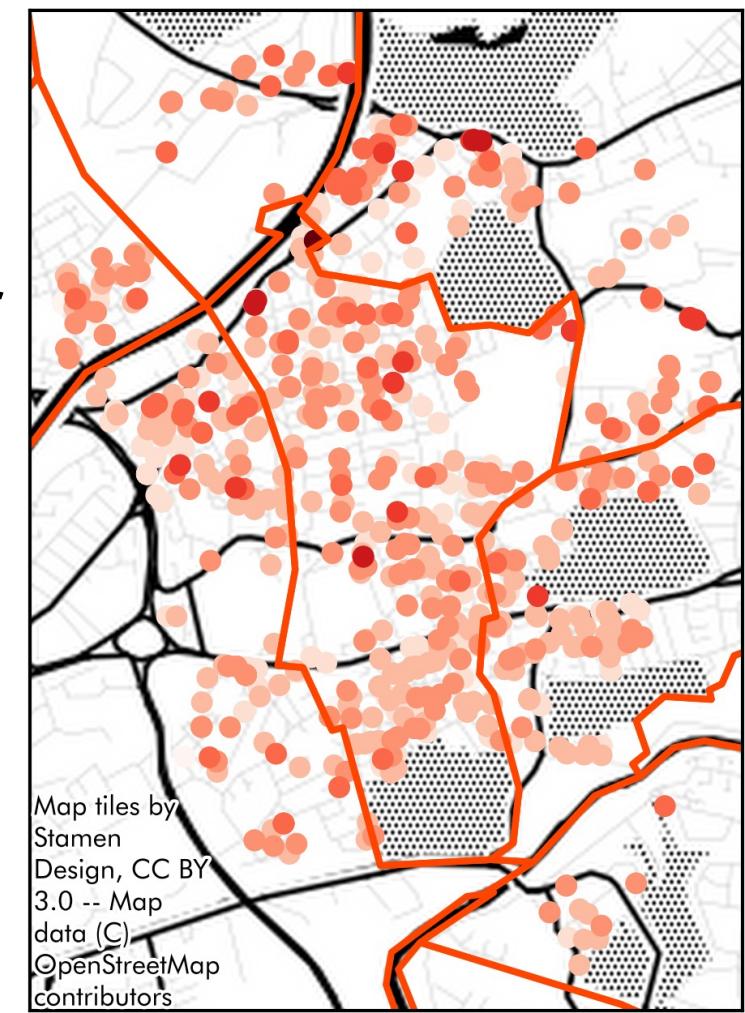
HOW CAN WE FIND RENT AFFORDABILITY OUTLIERS?

## WEEKLY RENT (£)



*How can we find locally-unusual rents given the characteristics of properties?*

## BEDROOMS



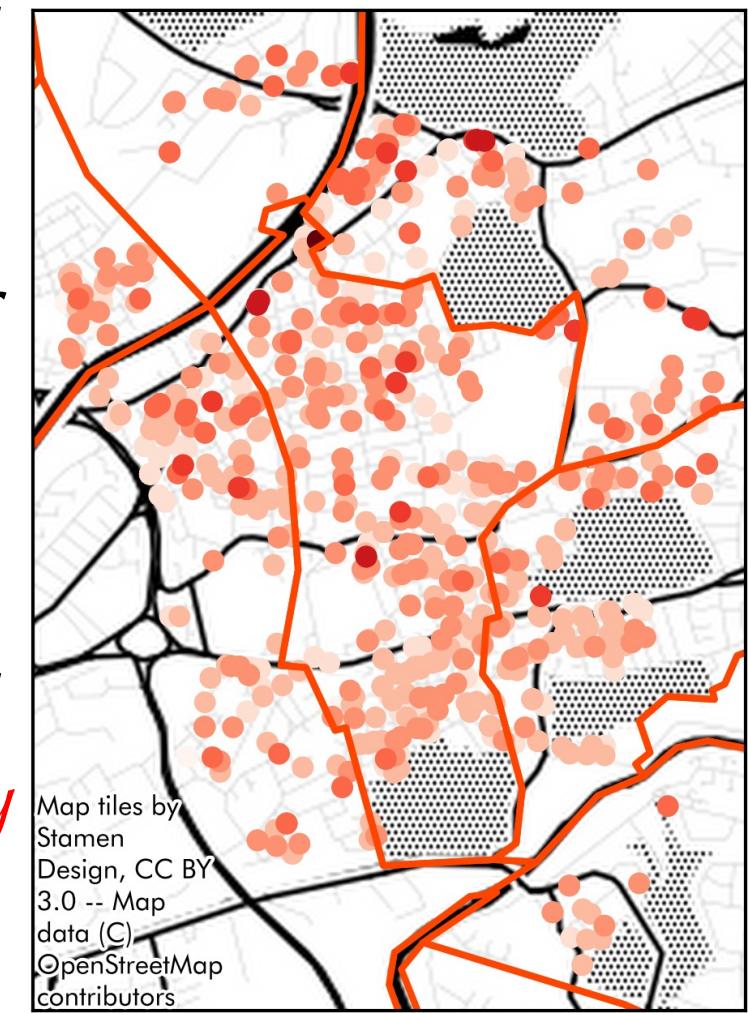
**HOW CAN WE FIND RENT AFFORDABILITY OUTLIERS?**

## WEEKLY RENT (£)



*How can we find locally-unusual rents given the characteristics of properties?*

## BEDROOMS



*How can we find local affordability outliers?*

**HOW CAN WE FIND RENT AFFORDABILITY OUTLIERS?**

# LOCAL CONFOUNDING

*size effects on rent vary*

## PRIOR ART IN ESDA

## PARTIAL CONDITIONING

## AFFORDABILITY OUTLIERS

$$\rho = \sum_i^N \frac{(x'_i - \bar{x}') (y'_i - \bar{y}')} {\sigma(x') \sigma(y')}$$

CLASSICAL CORRELATION & LOCAL PEARSON

$$x = \frac{x' - \bar{x}'}{\sigma(x')}$$

$$y = \frac{y' - \bar{y}'}{\sigma(y')}$$

$$\rho = \sum_i^N \frac{(x'_i - \bar{x}') (y'_i - \bar{y}')}{\sigma(x') \sigma(y')}$$

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CLASSICAL CORRELATION & LOCAL PEARSON

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CLASSICAL CORRELATION & LOCAL PEARSON

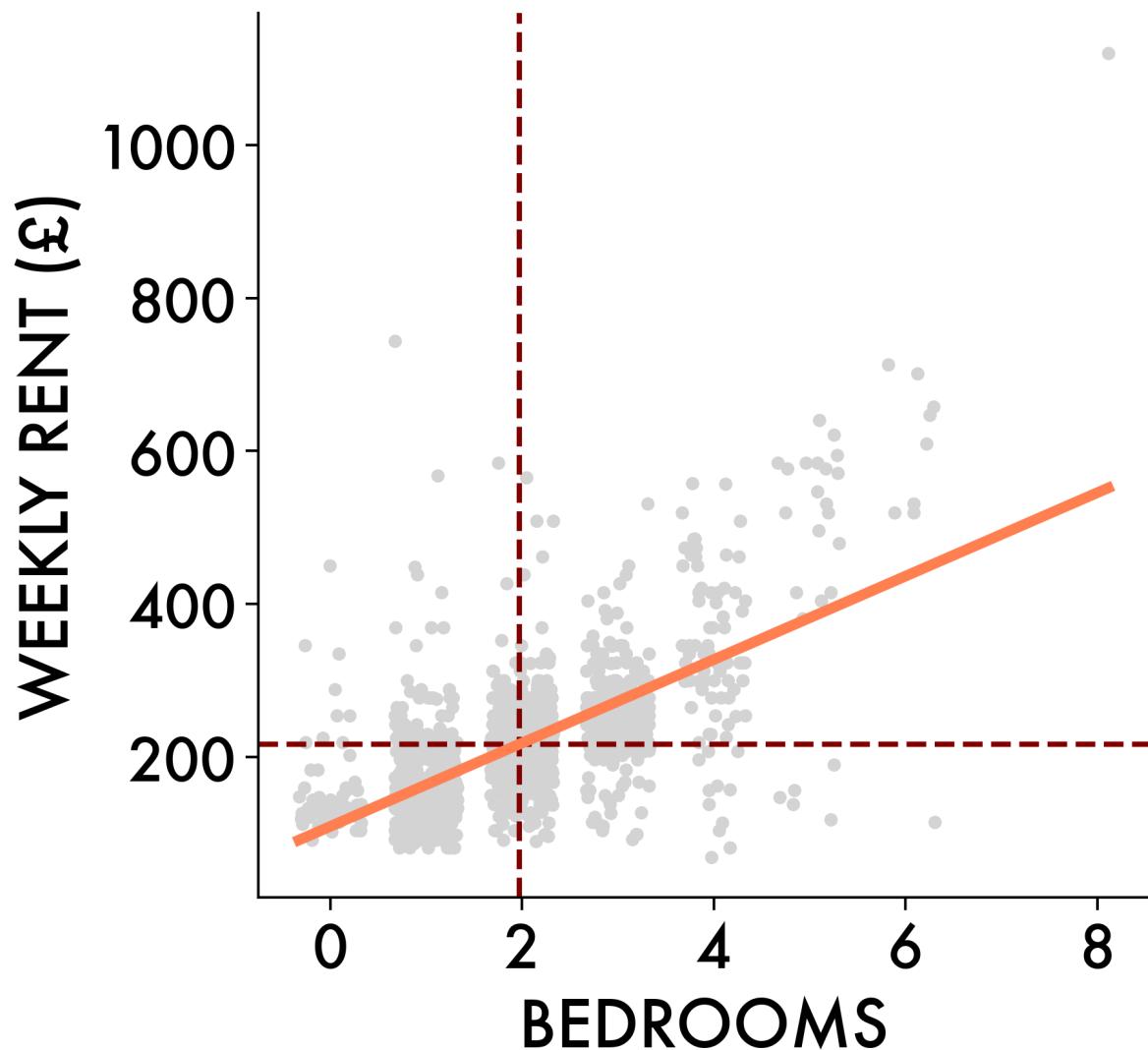
$$x = \frac{x' - \bar{x}'}{\sigma(x')}$$

$$y = \frac{y' - \bar{y}'}{\sigma(y')}$$

$$\rho_i = \frac{(x'_i - \bar{x}') (y'_i - \bar{y}')}{\sigma(x') \sigma(y')} = x_i y_i$$

CLASSICAL CORRELATION & LOCAL PEARSON

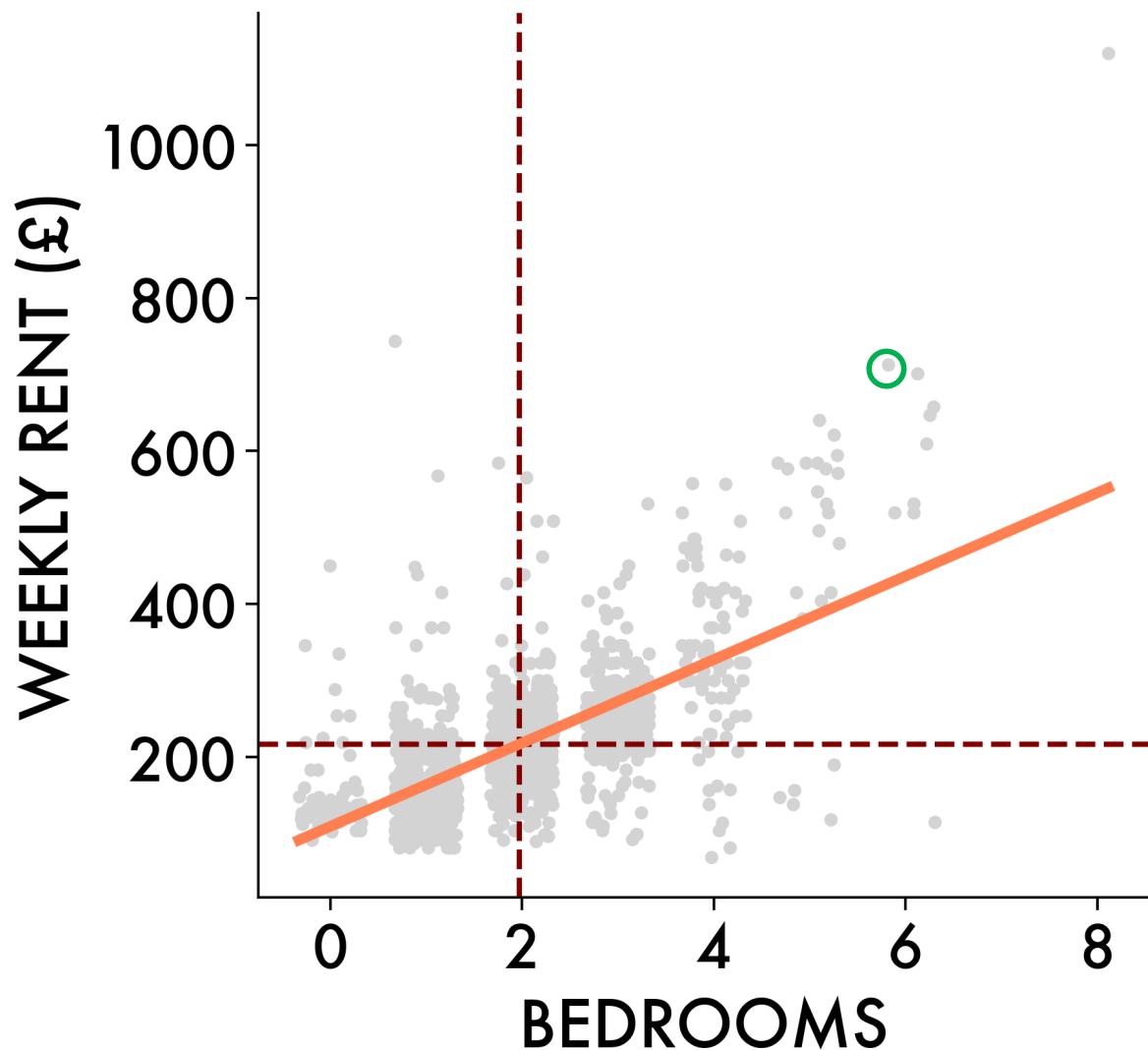
## PEARSON SCATTERPLOT



$x_i y_i$

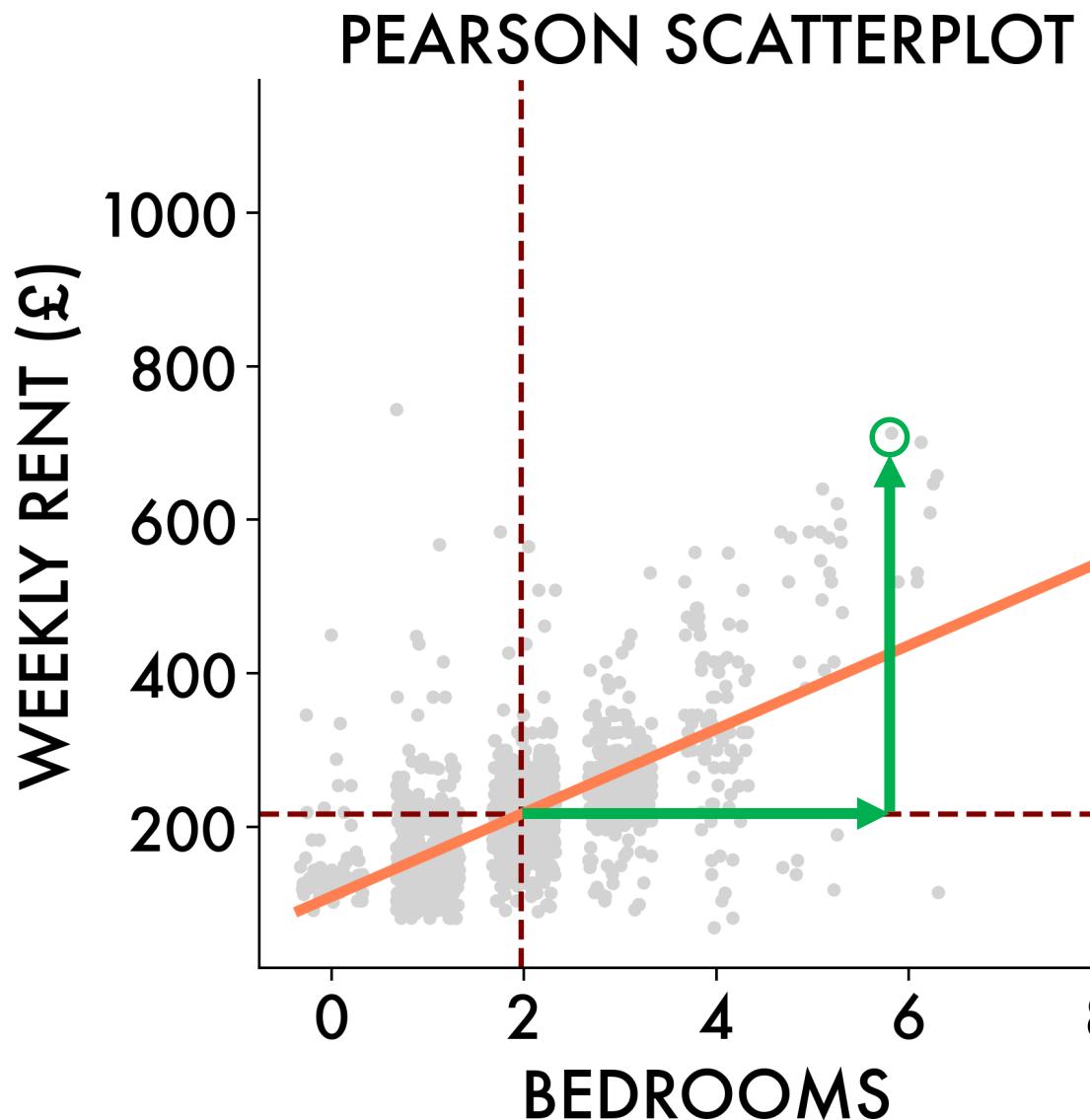
CLASSICAL CORRELATION & LOCAL PEARSON

## PEARSON SCATTERPLOT

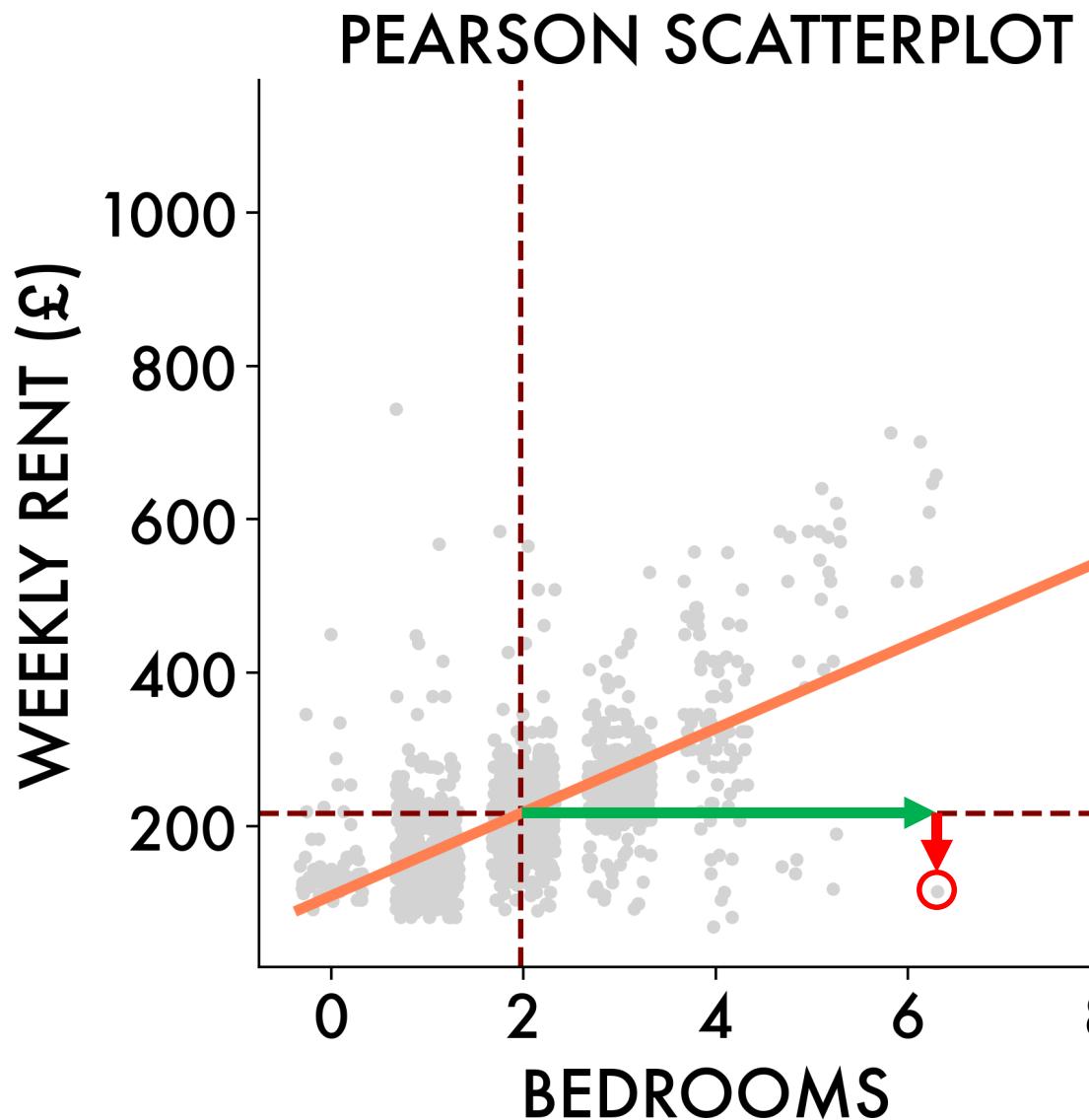


$x_i y_i$

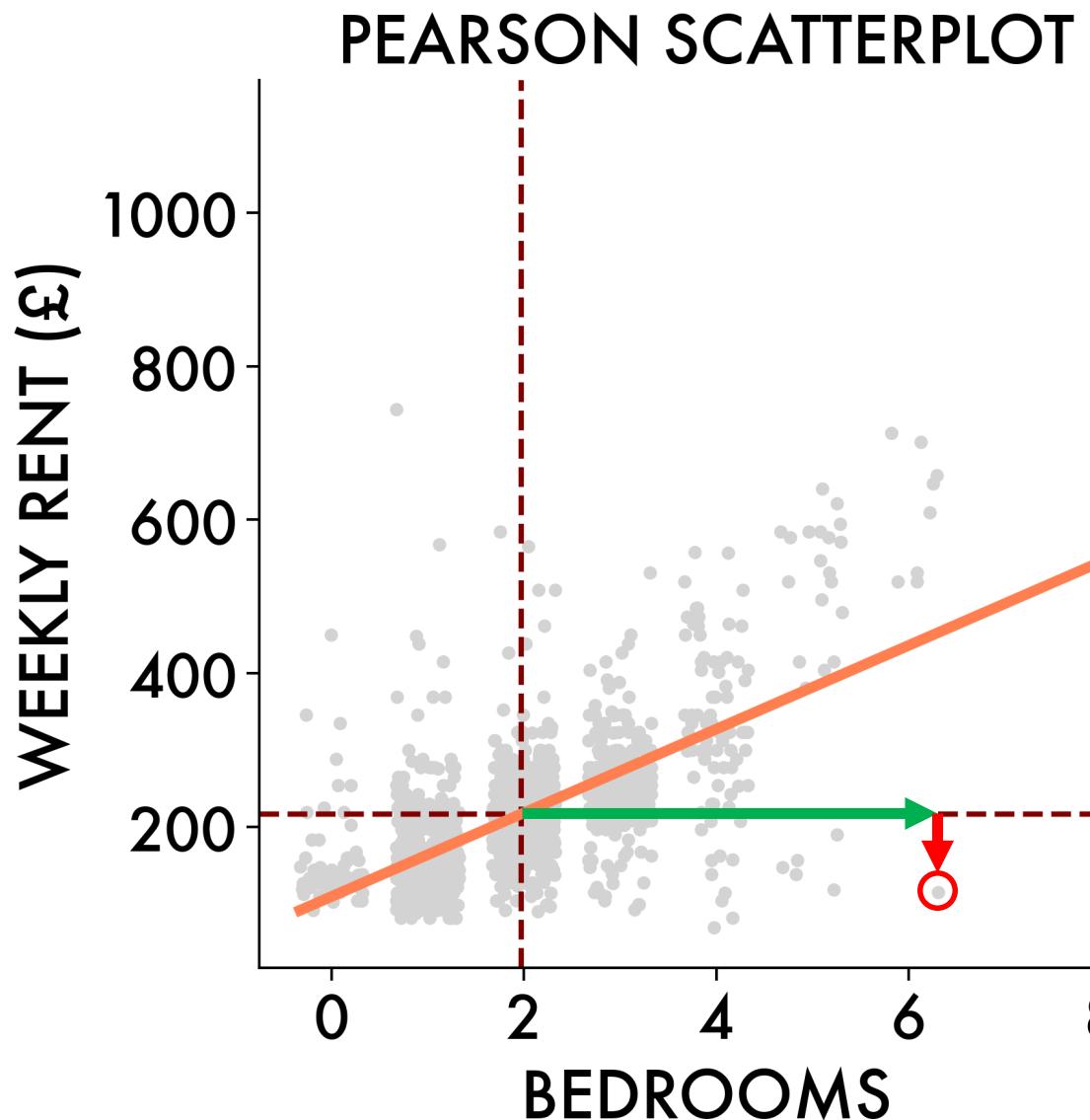
CLASSICAL CORRELATION & LOCAL PEARSON



CLASSICAL CORRELATION & LOCAL PEARSON

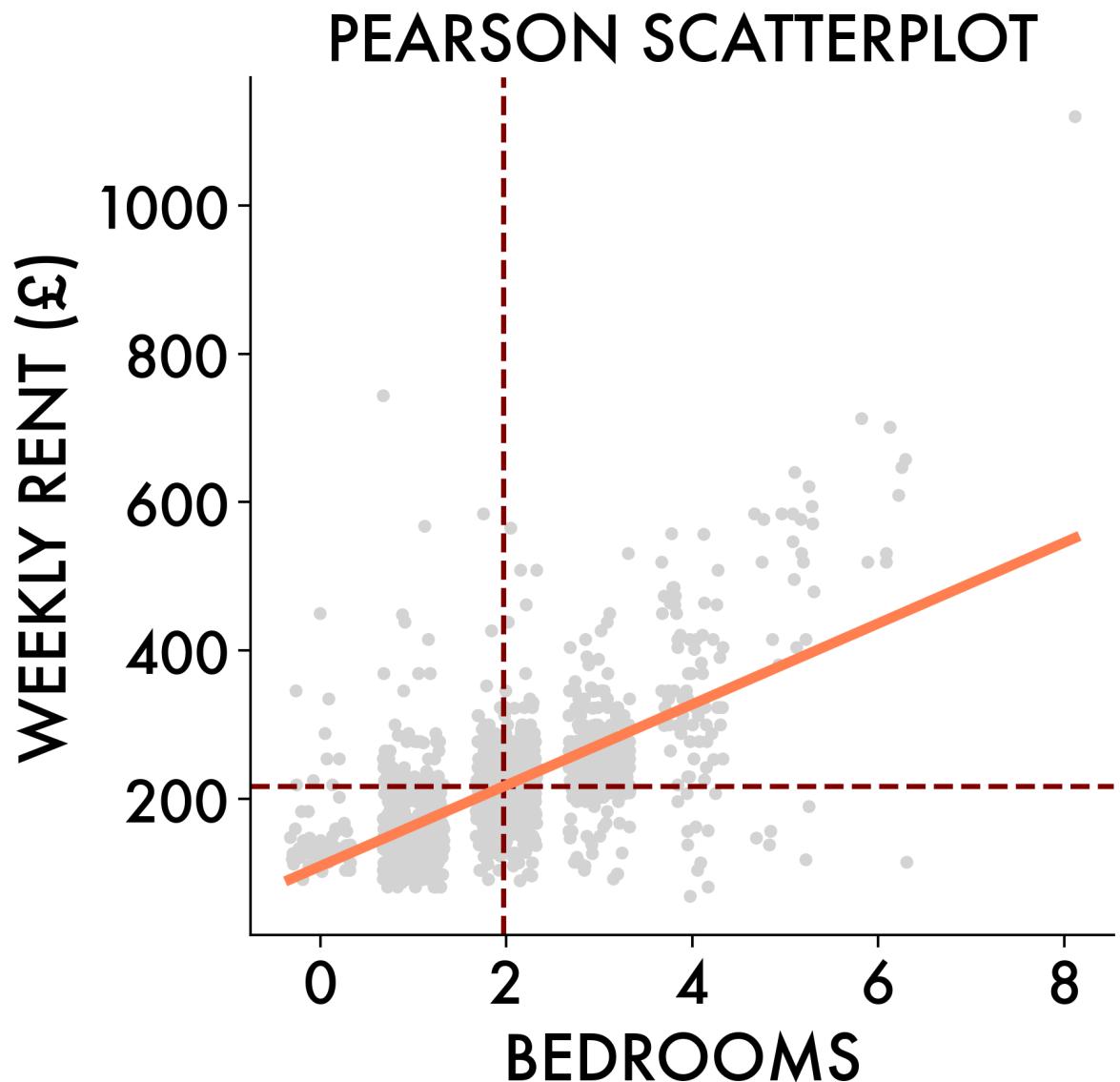
 $x_i y_i$ 

CLASSICAL CORRELATION & LOCAL PEARSON



$$\rho_i = x_i y_i$$

CLASSICAL CORRELATION & LOCAL PEARSON



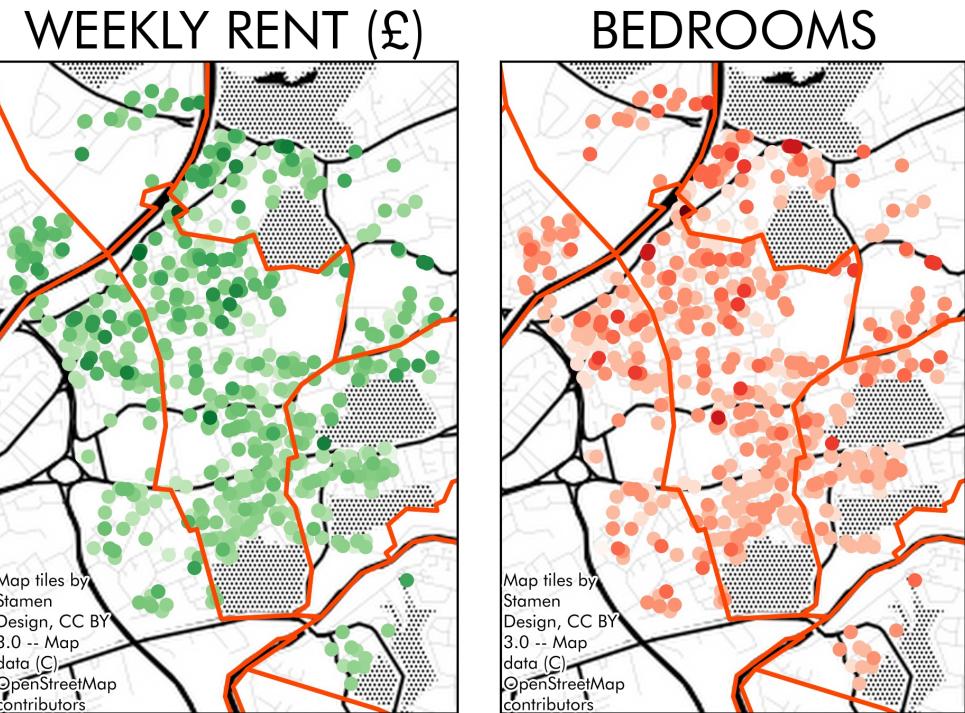
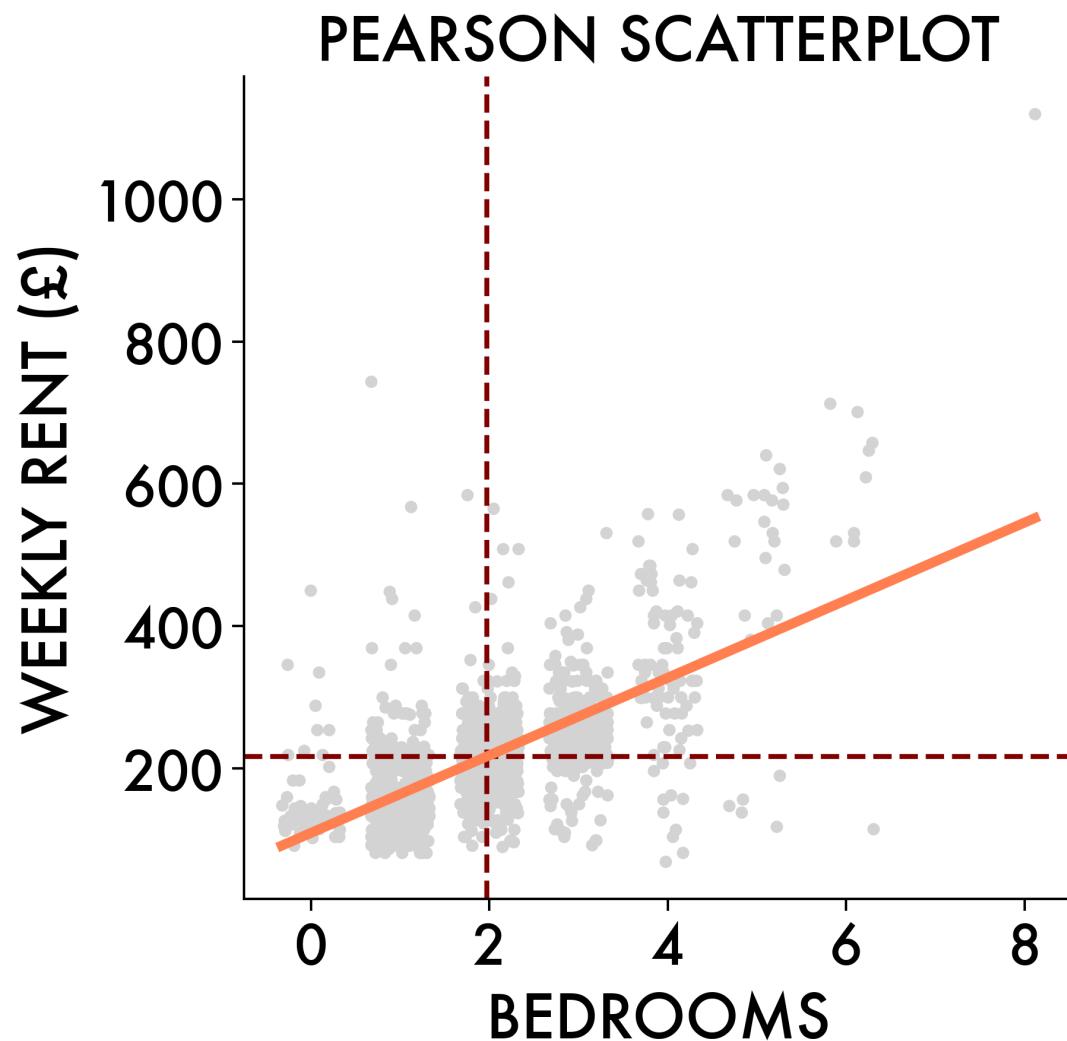
$$\rho = \begin{bmatrix} x_1 y_1 \\ x_2 y_2 \\ \vdots \\ x_N y_N \end{bmatrix} = x \circ y$$

$$\sum_i^N \rho_i = \rho$$

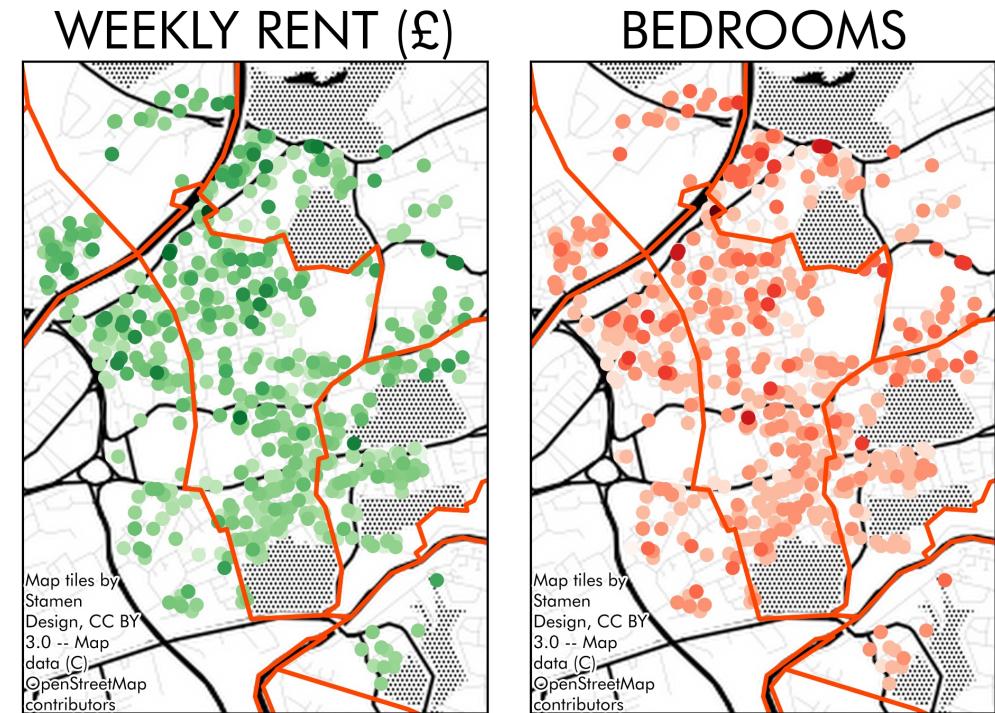
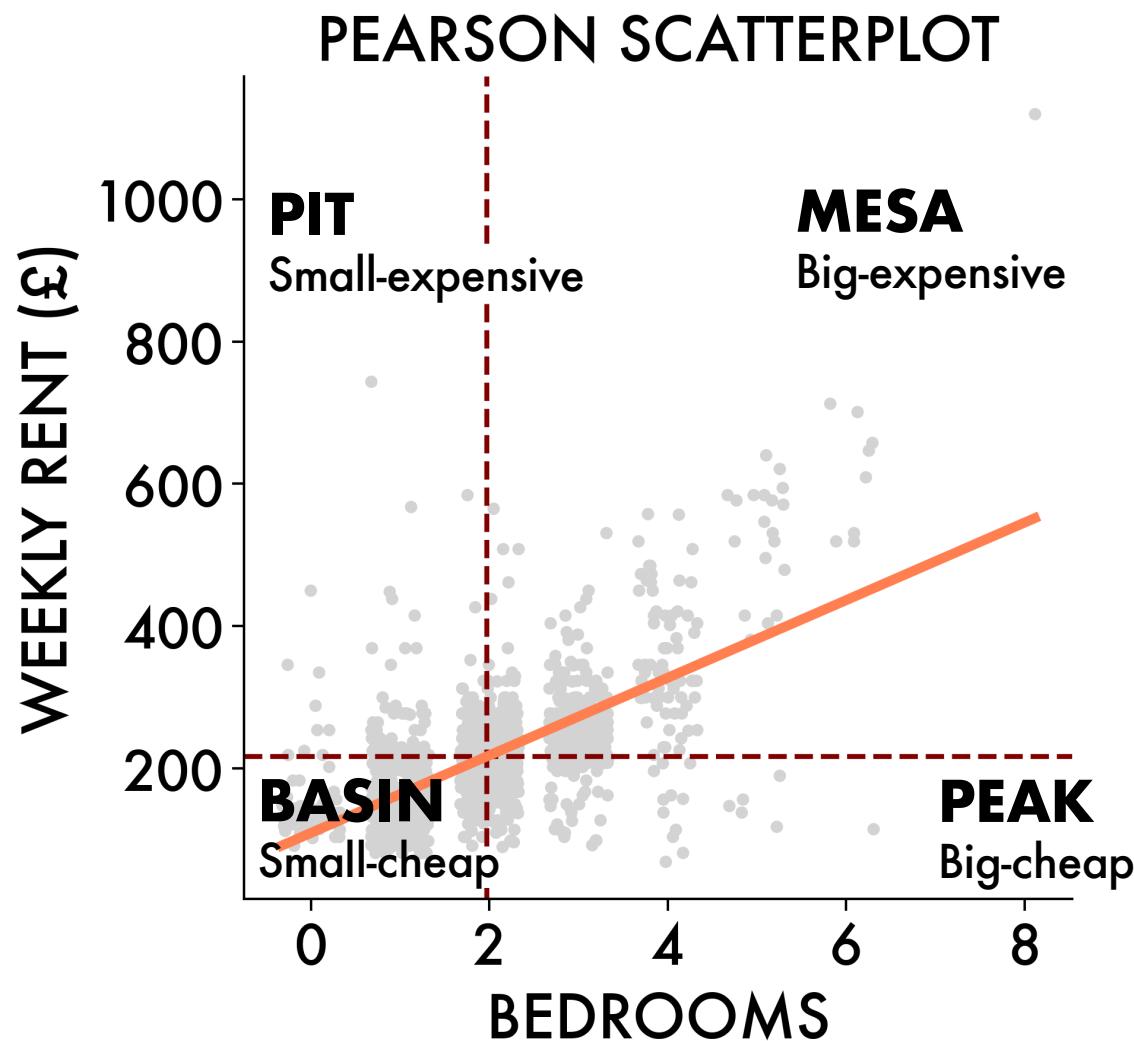
CLASSICAL CORRELATION & LOCAL PEARSON

*A sufficient condition to turn  
a global summary statistic  
into an Anselin (1995) LISA  
statistic is to swap in an  
elementwise product where  
an inner product is used.*

$$\rho = \begin{bmatrix} x_1 y_1 \\ x_2 y_2 \\ \vdots \\ x_N y_N \end{bmatrix} = x \circ y$$
$$\rho = x \cdot y$$

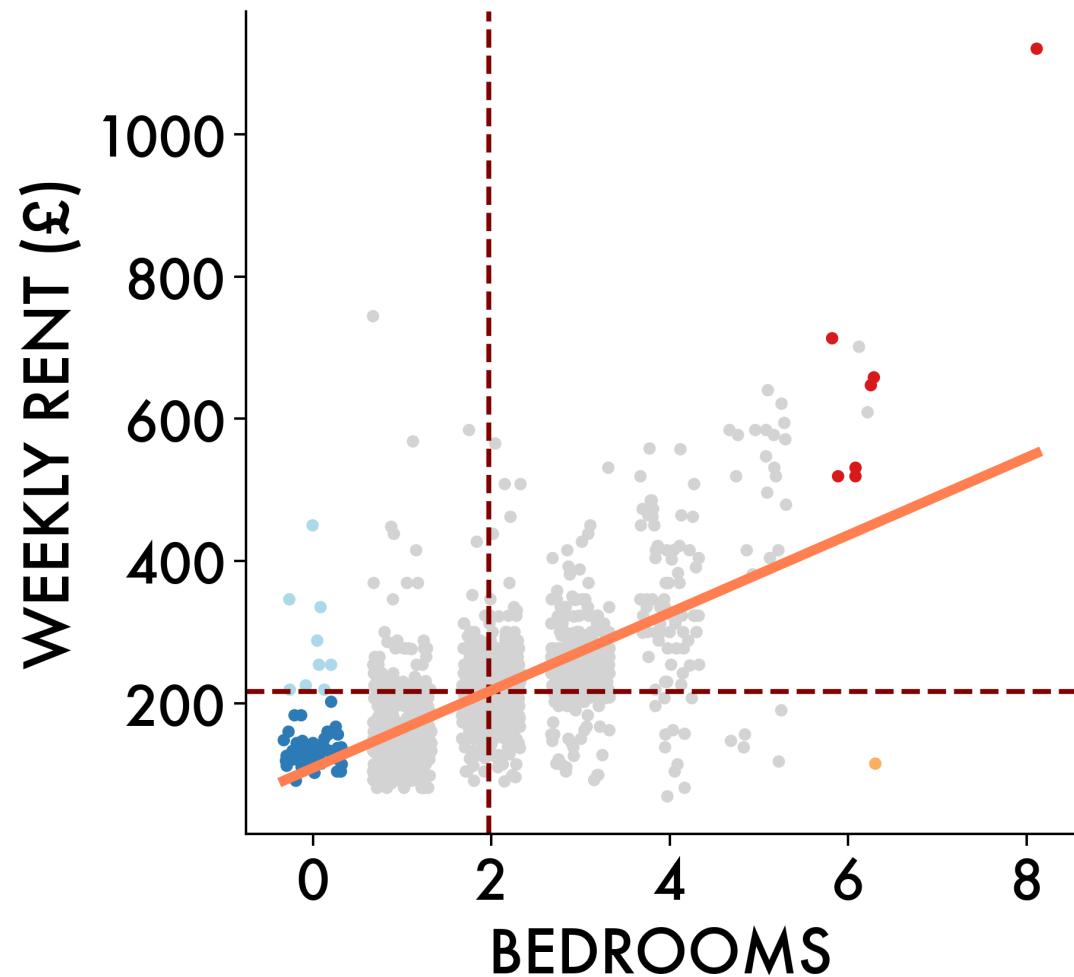


### LOCAL PEARSON SCATTERPLOT

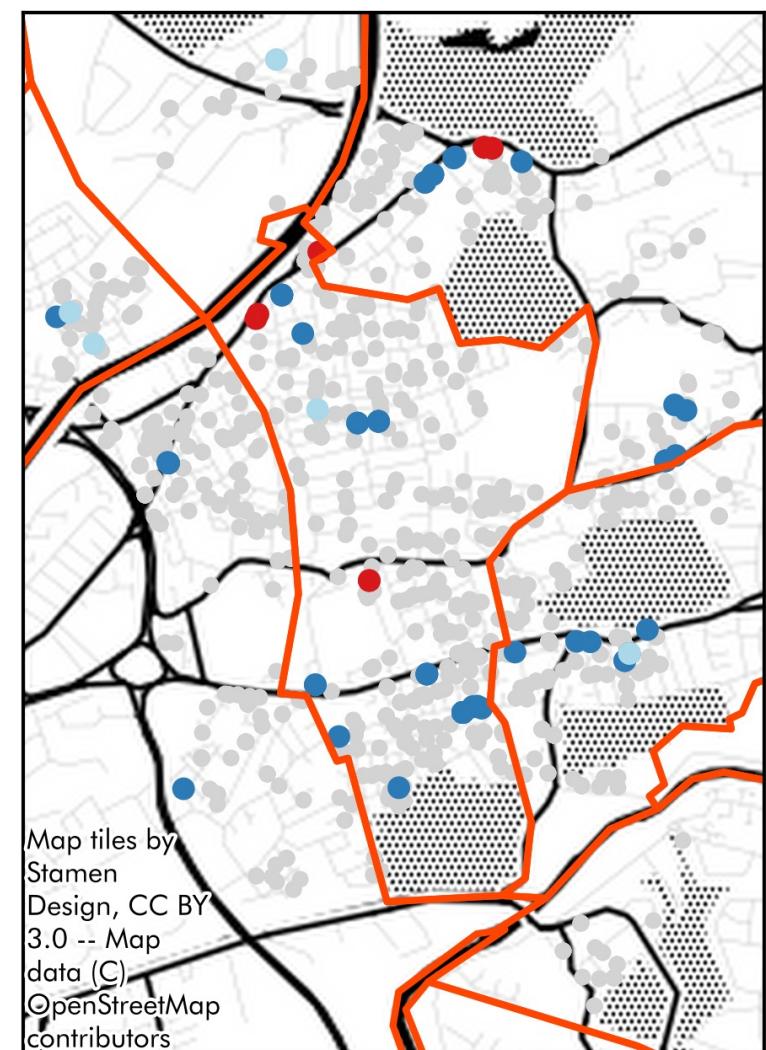


LOCAL PEARSON SCATTERPLOT

## PEARSON SCATTERPLOT

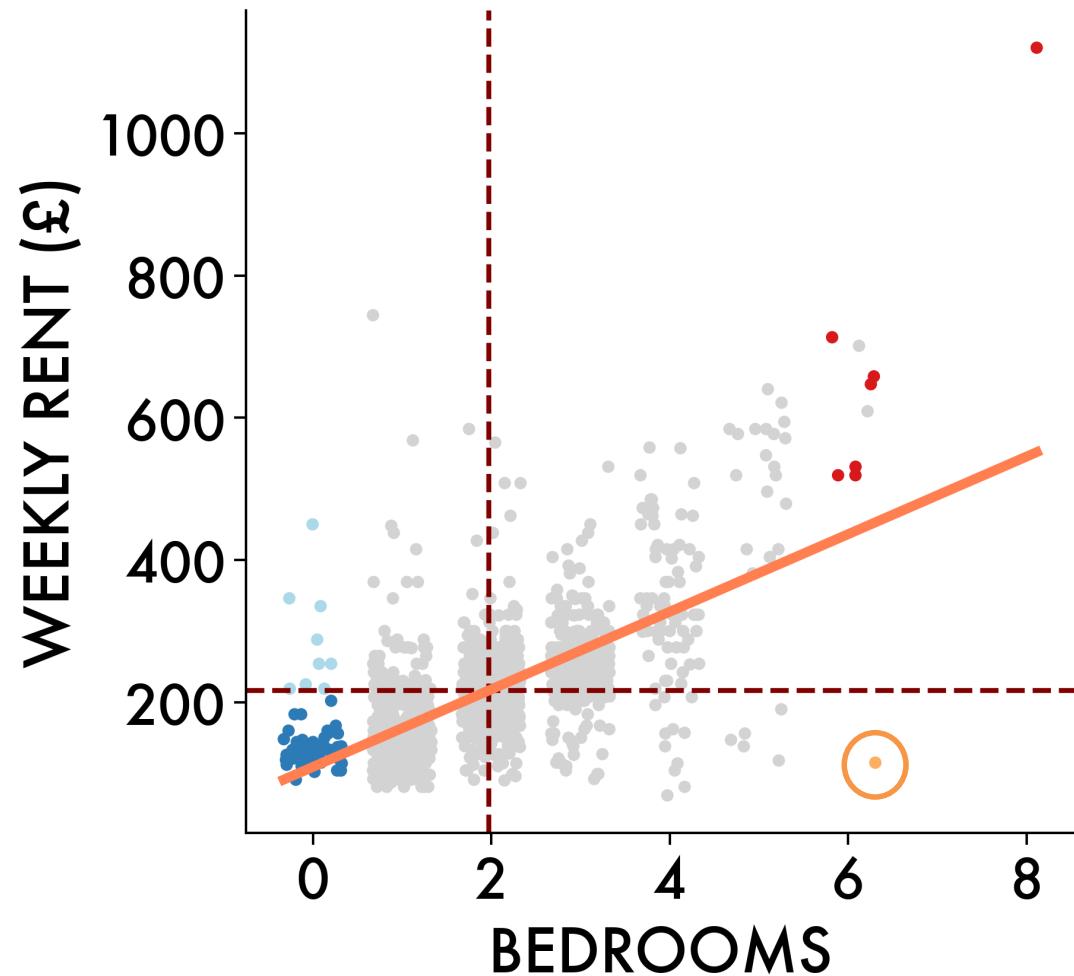


## PEARSON CLASSES

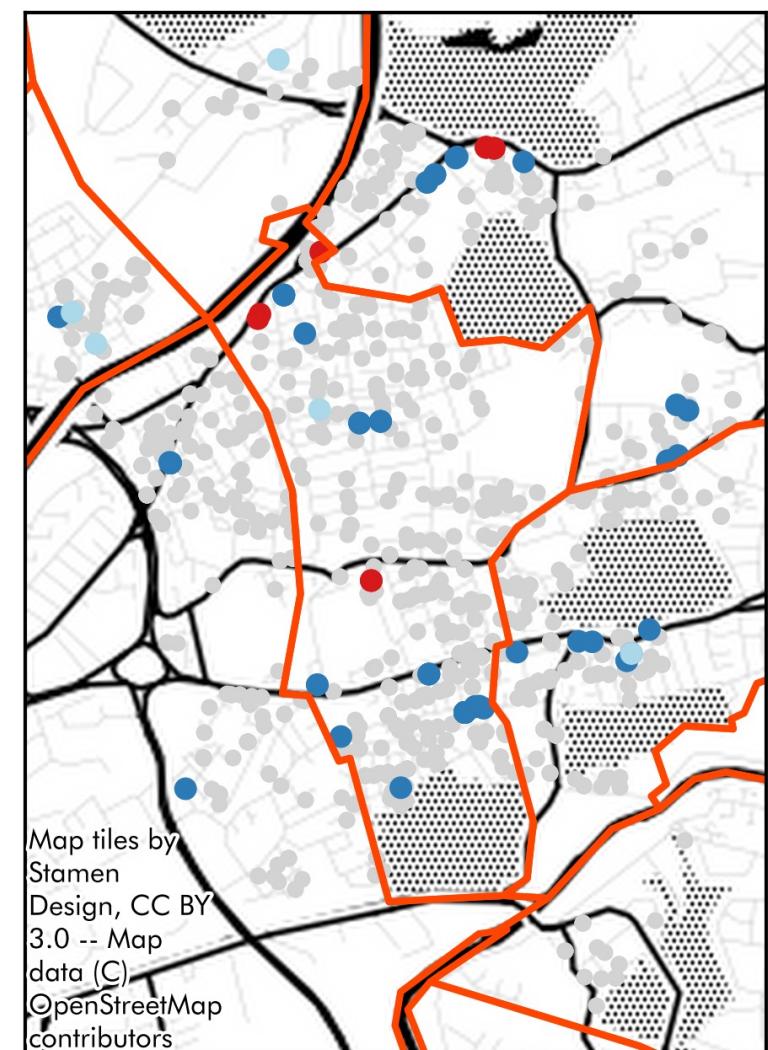


LOCAL PEARSON SCATTERPLOT

## PEARSON SCATTERPLOT

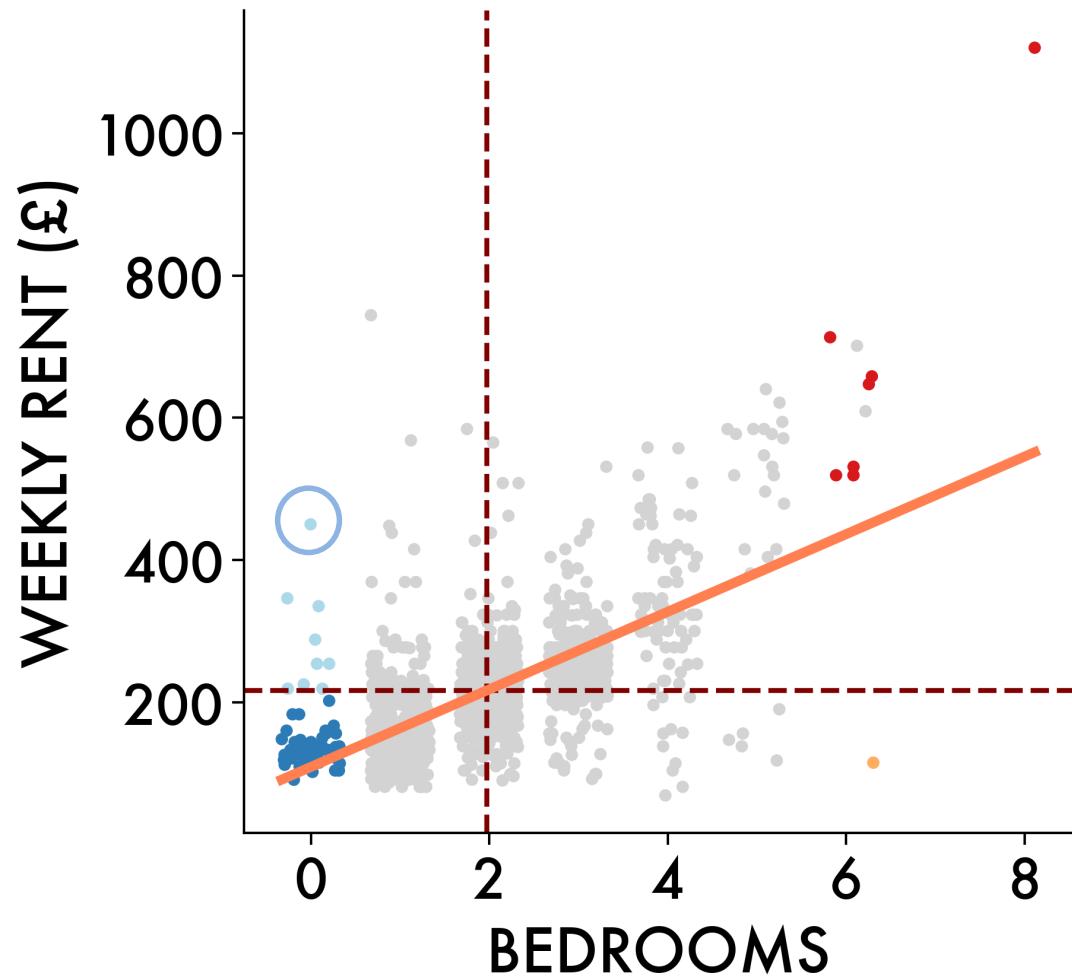


## PEARSON CLASSES

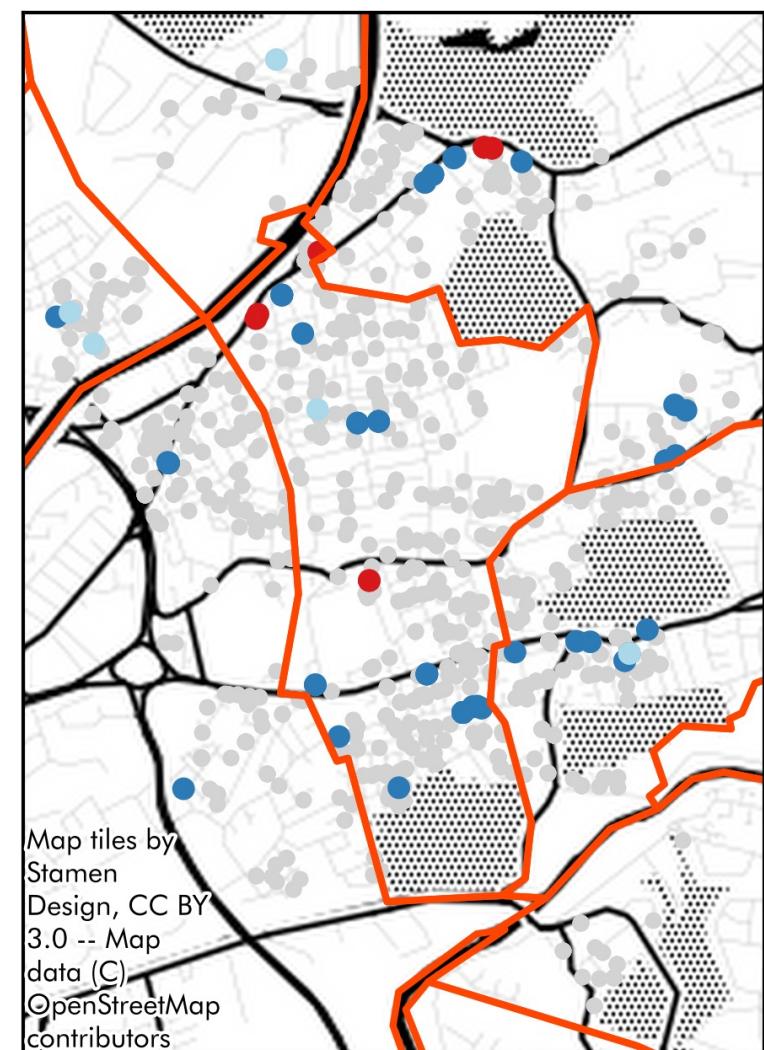


LOCAL PEARSON SCATTERPLOT

## PEARSON SCATTERPLOT

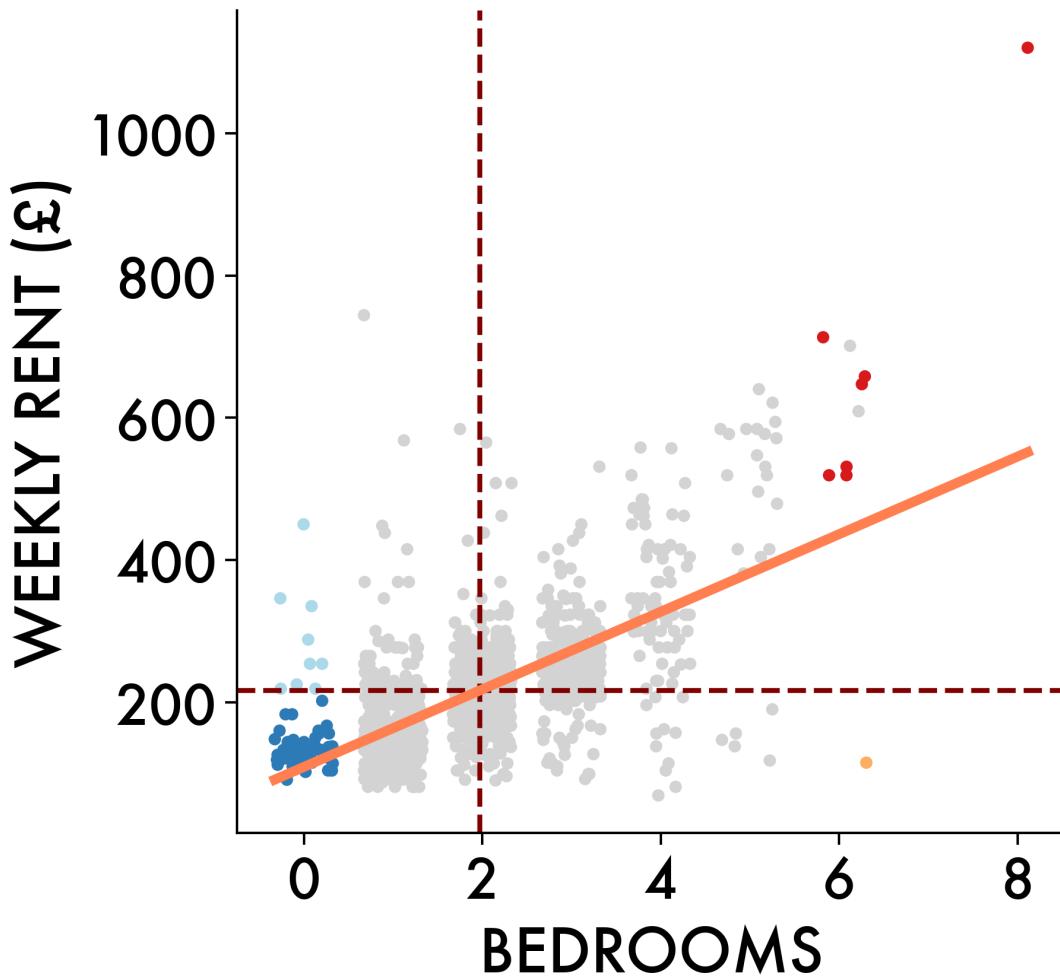


## PEARSON CLASSES



LOCAL PEARSON SCATTERPLOT

## PEARSON SCATTERPLOT



*How can we find locally-unusual rents given the characteristics of properties nearby?*

*Local correlation only summarizes site by site*

## LOCAL PEARSON SCATTERPLOT

LOCAL CONFOUNDING

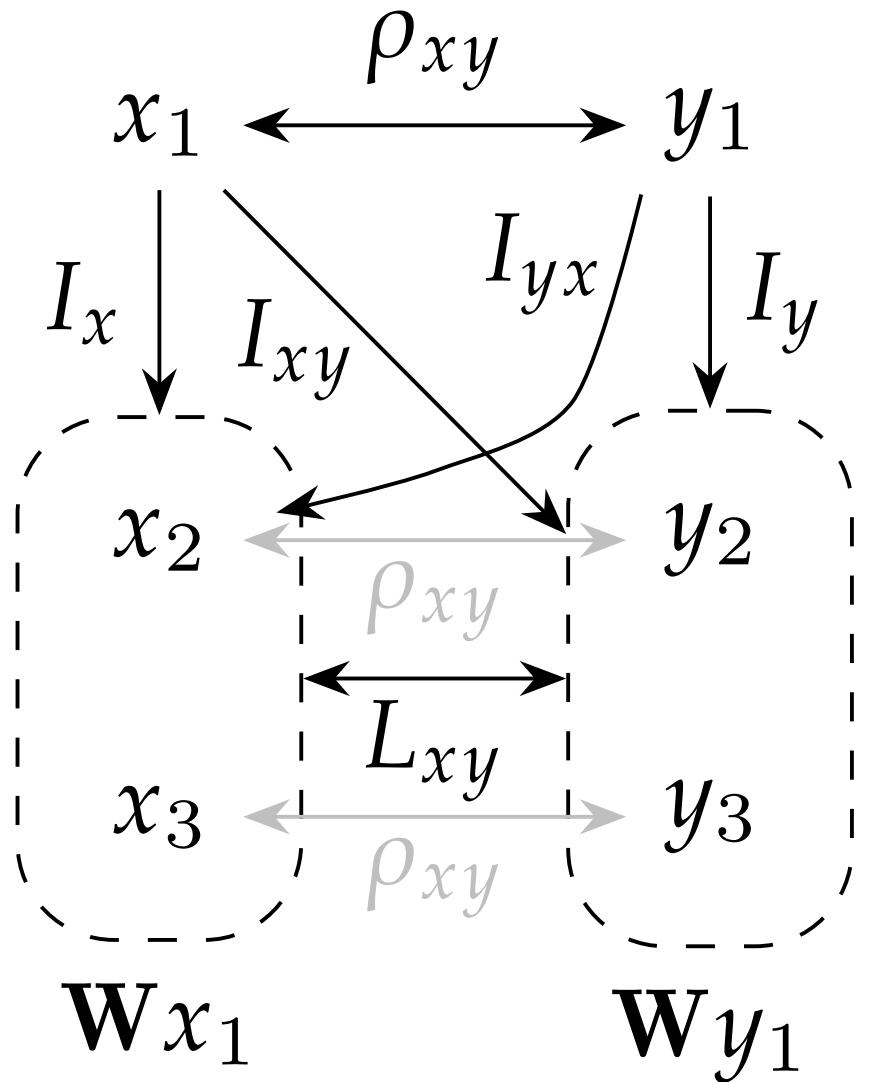
*size effects on rent vary*

PRIOR ART IN ESDA

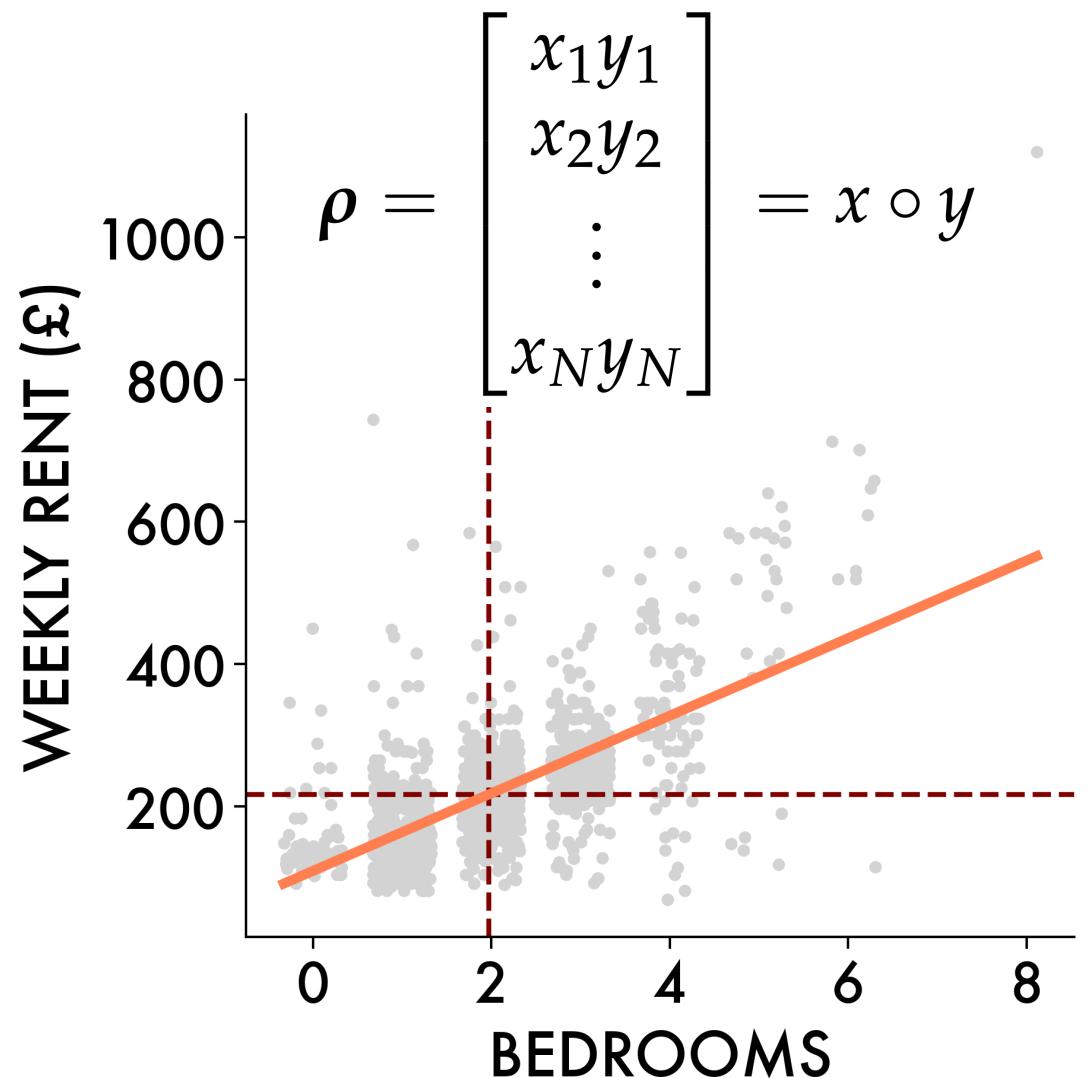
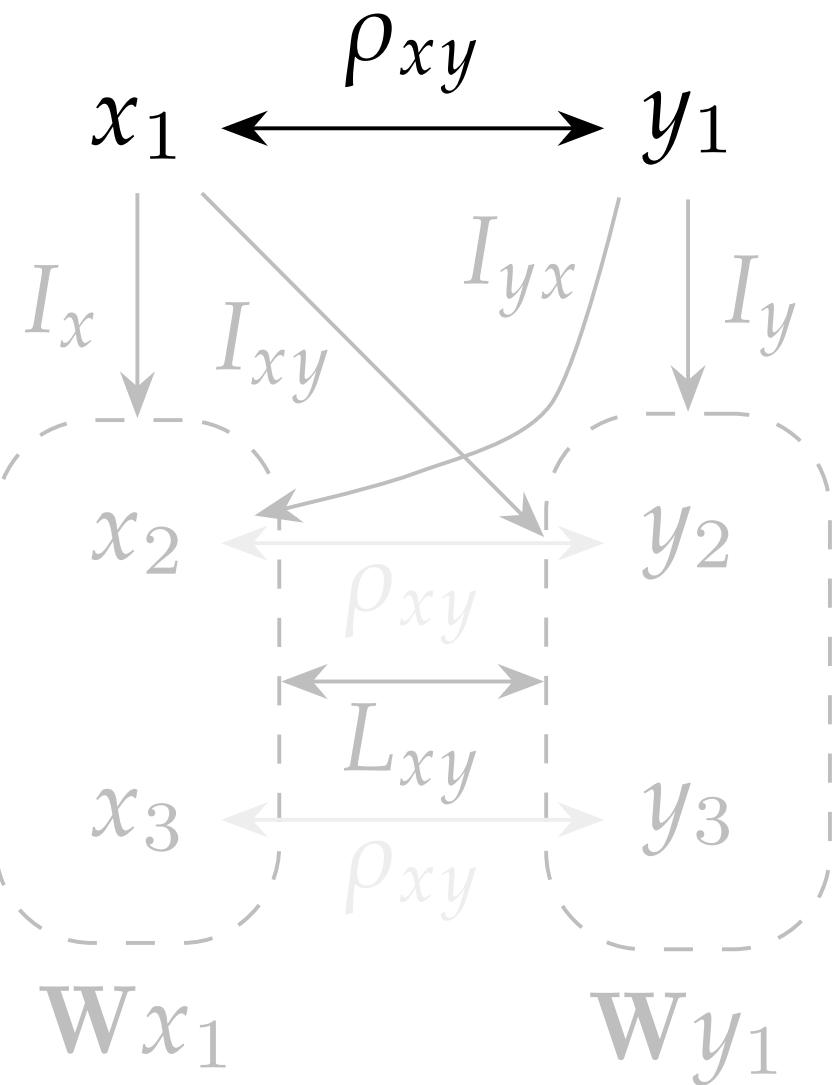
*The Moran-Form Regression*

PARTIAL CONDITIONING

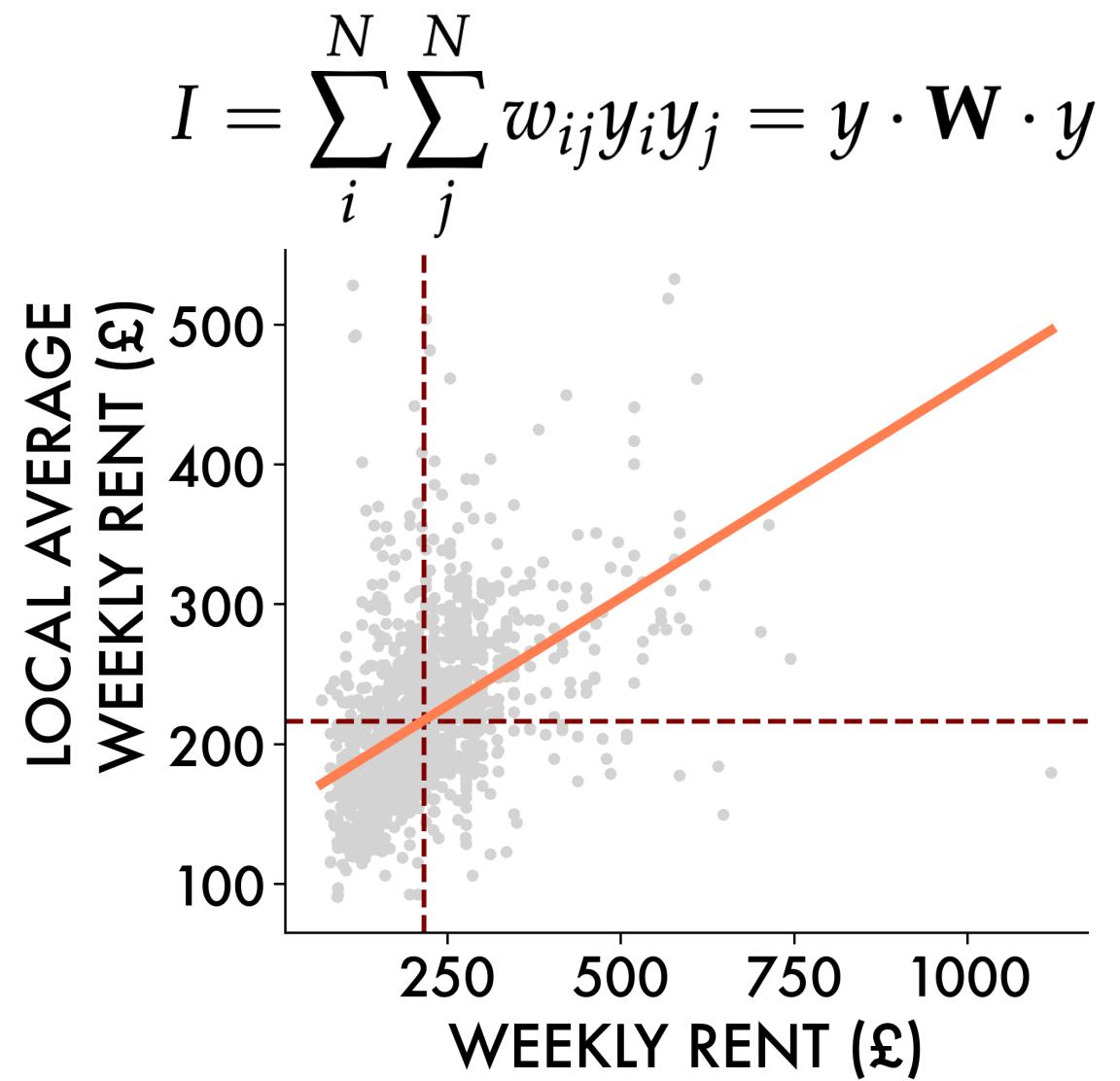
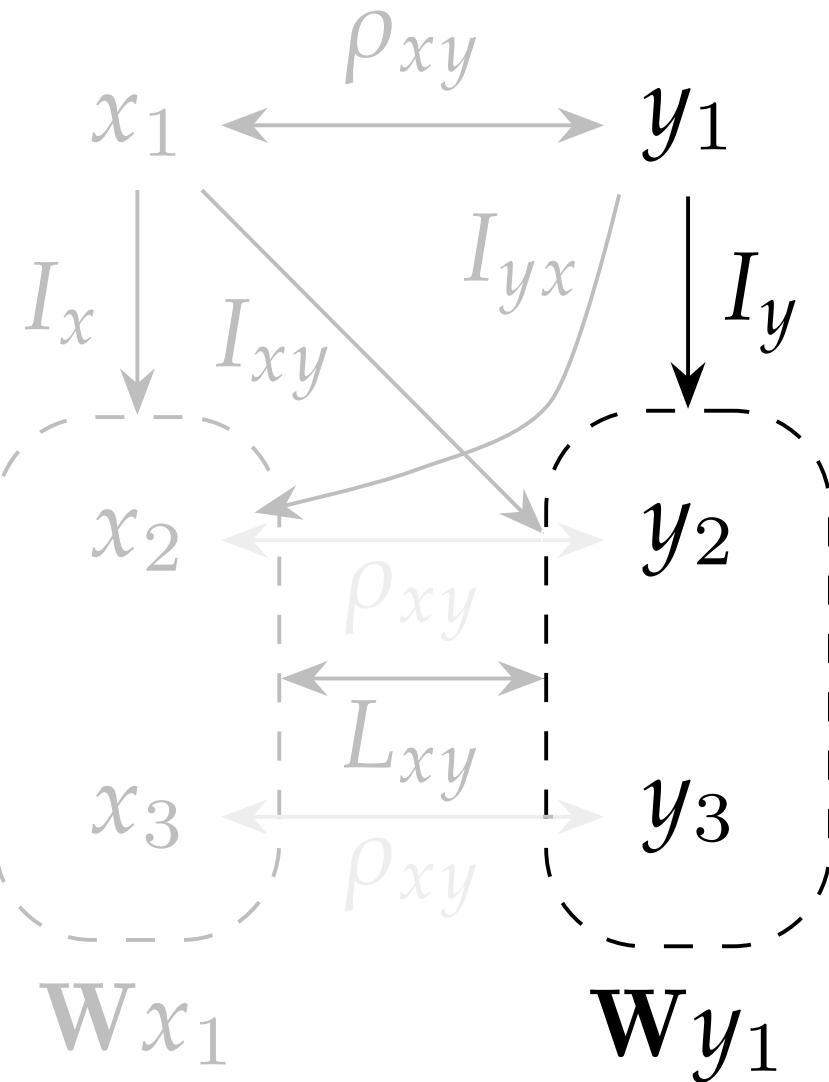
AFFORDABILITY OUTLIERS



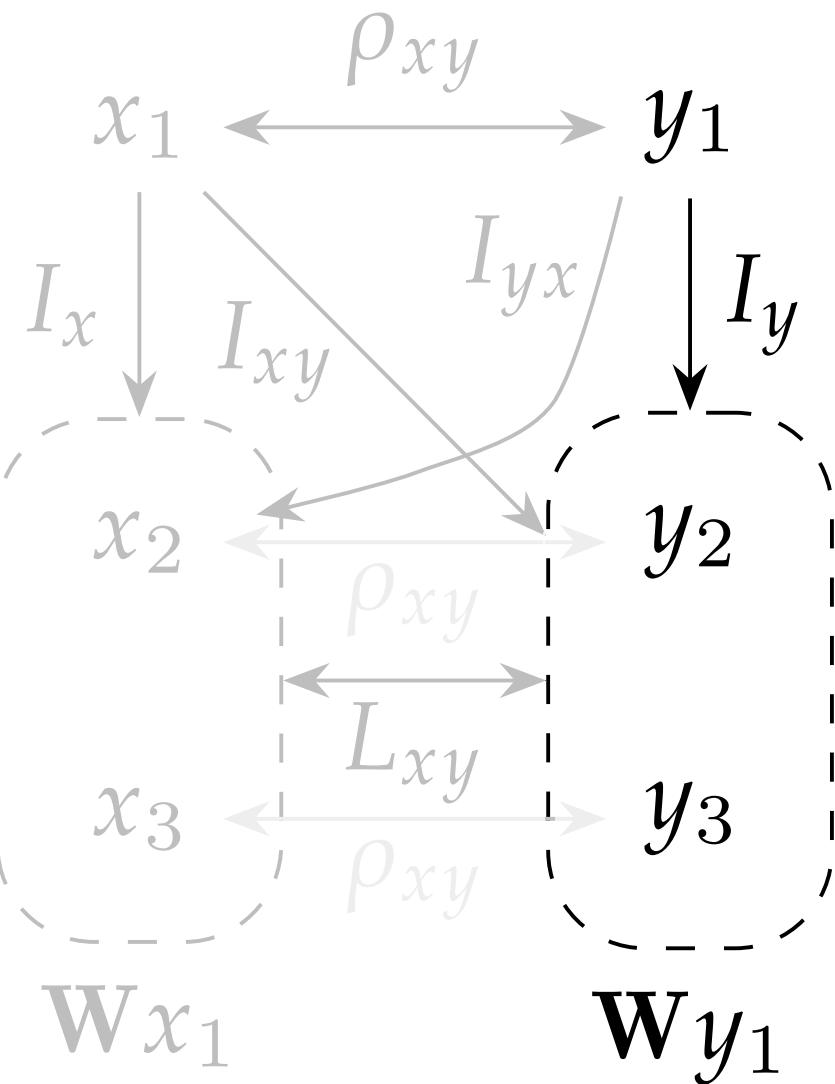
LOCAL COVARIANCE DAGS



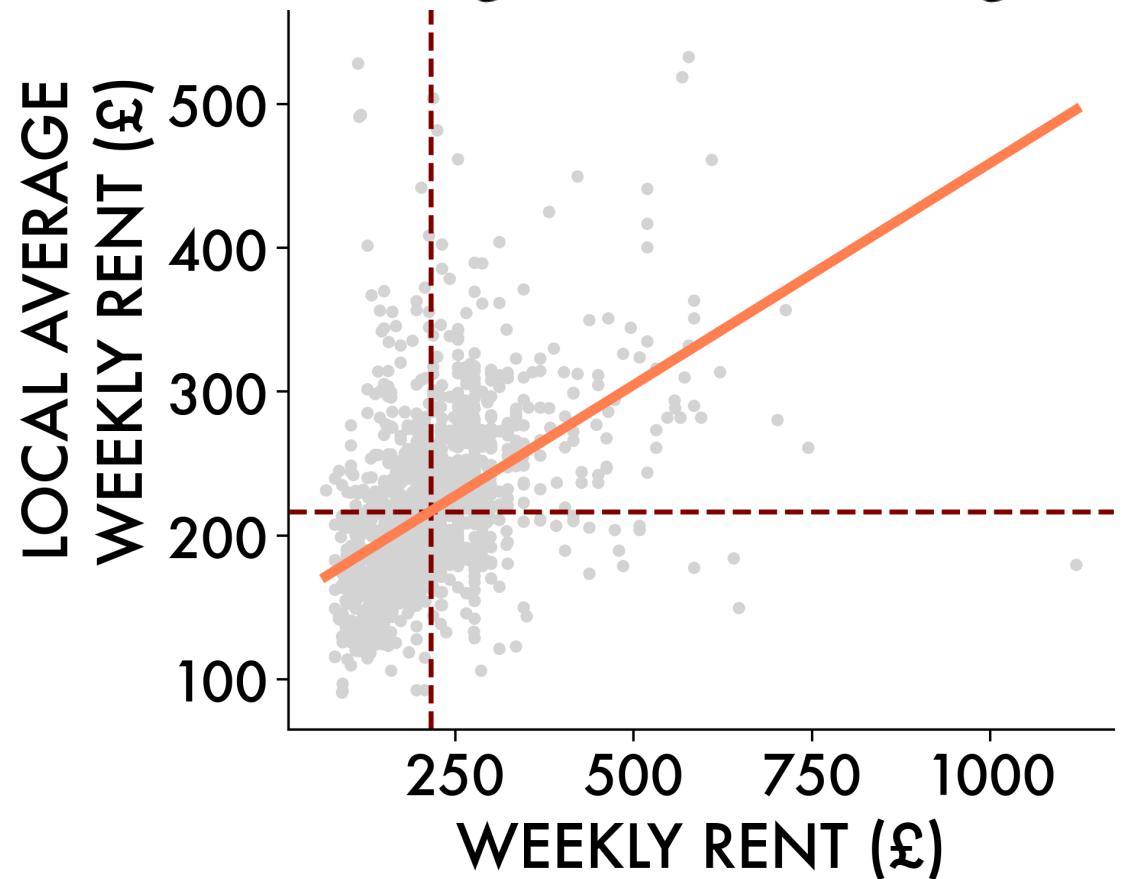
## PEARSON CORRELATION



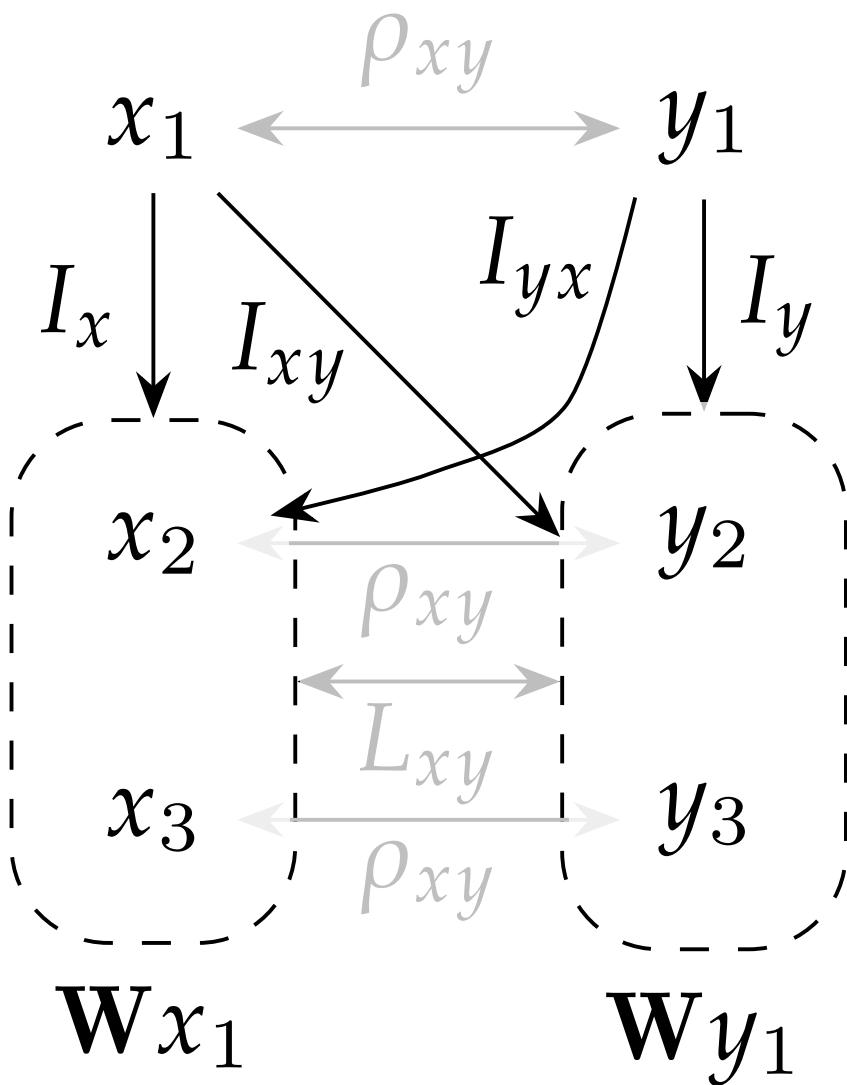
MORAN ASSOCIATION



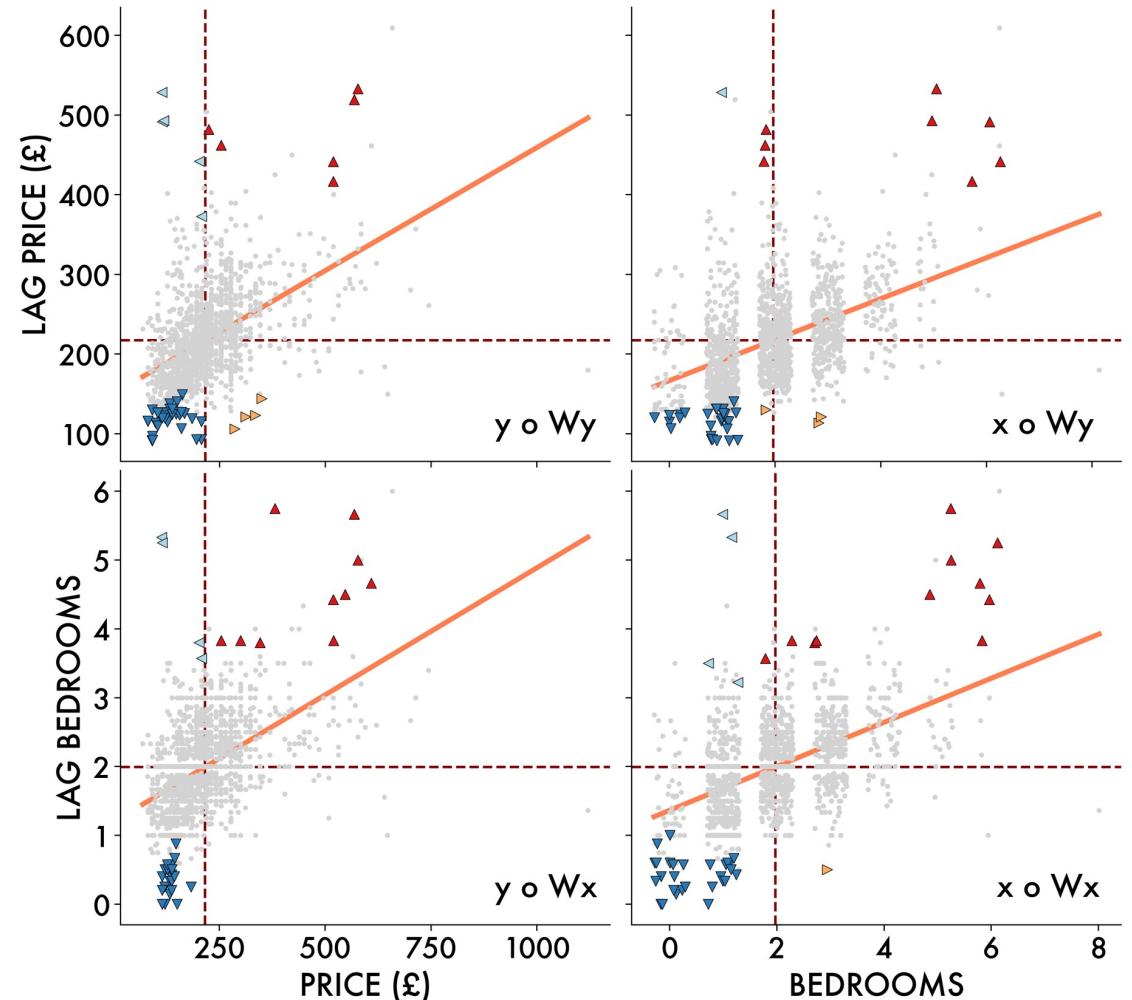
$$\mathbf{I} = \mathbf{y} \circ \mathbf{W} \cdot \mathbf{y}$$



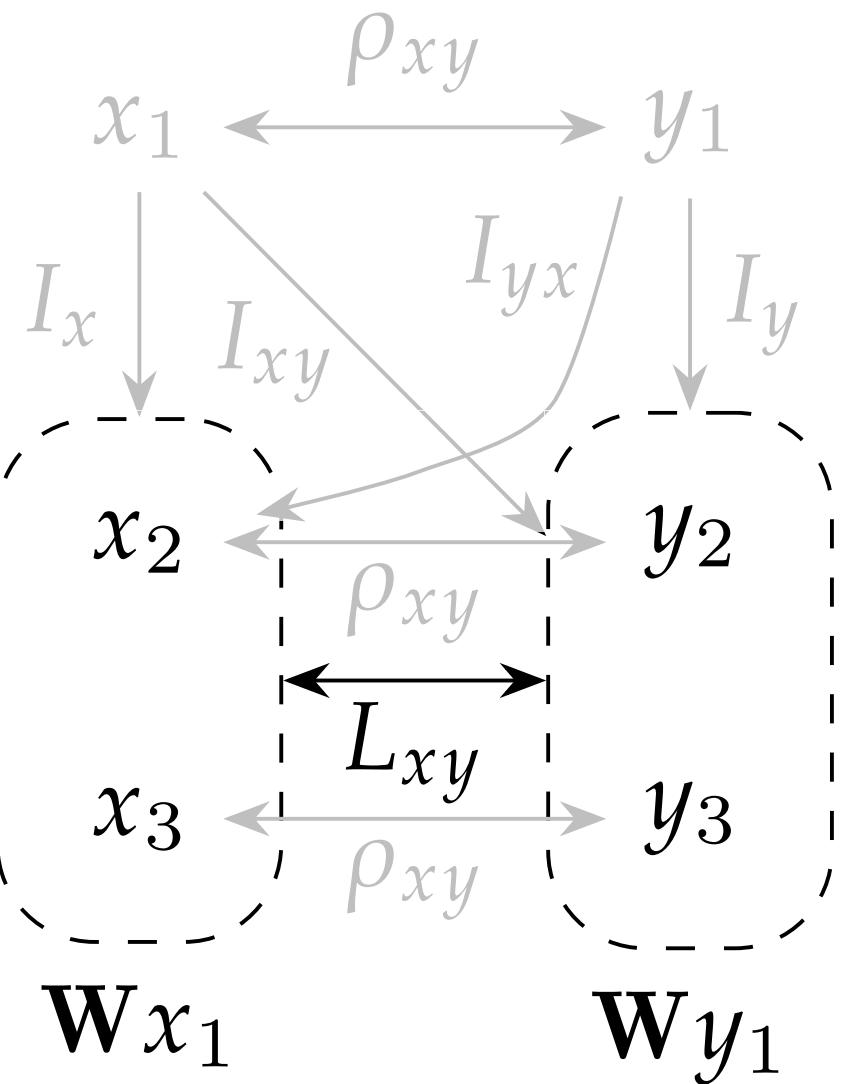
MORAN ASSOCIATION



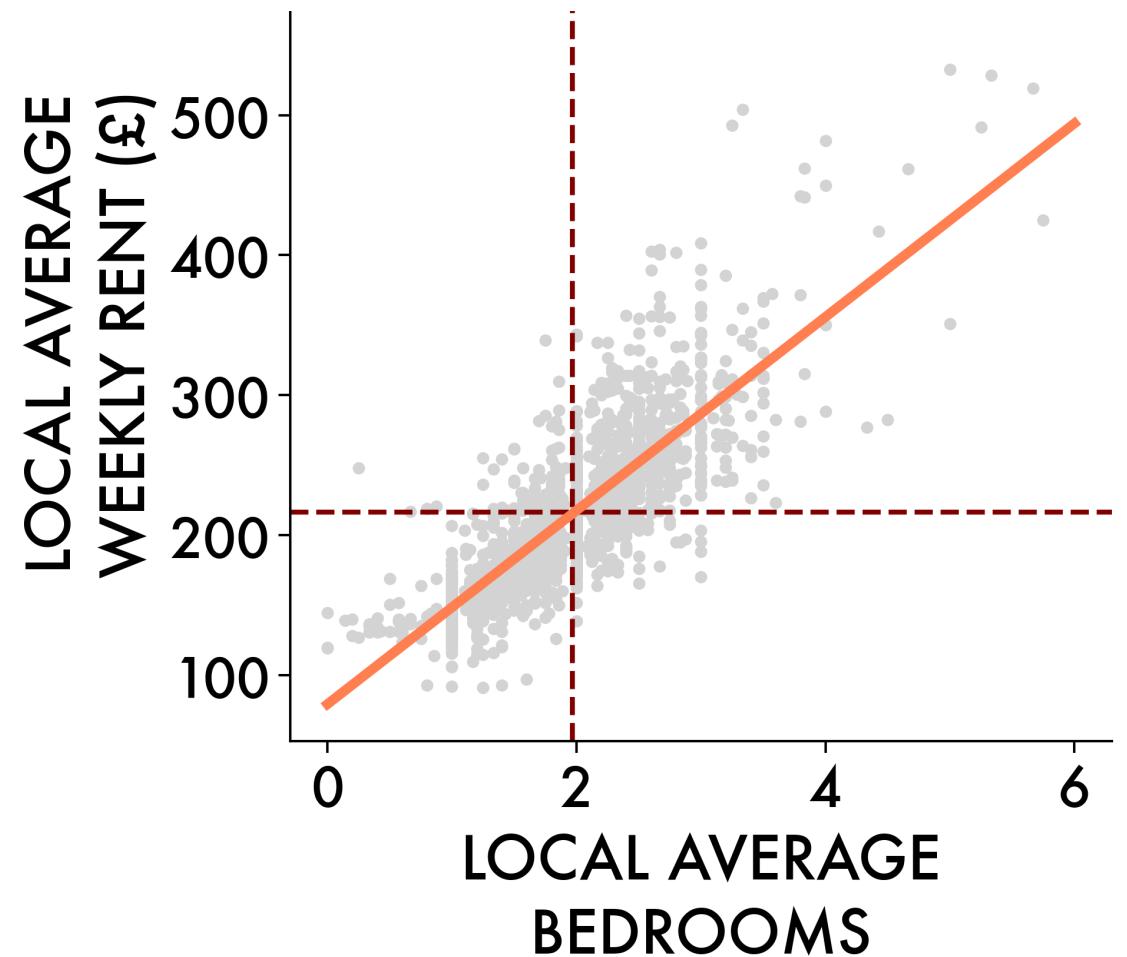
$$\mathbf{I}_{xy} = x \circ \mathbf{W} \cdot y$$



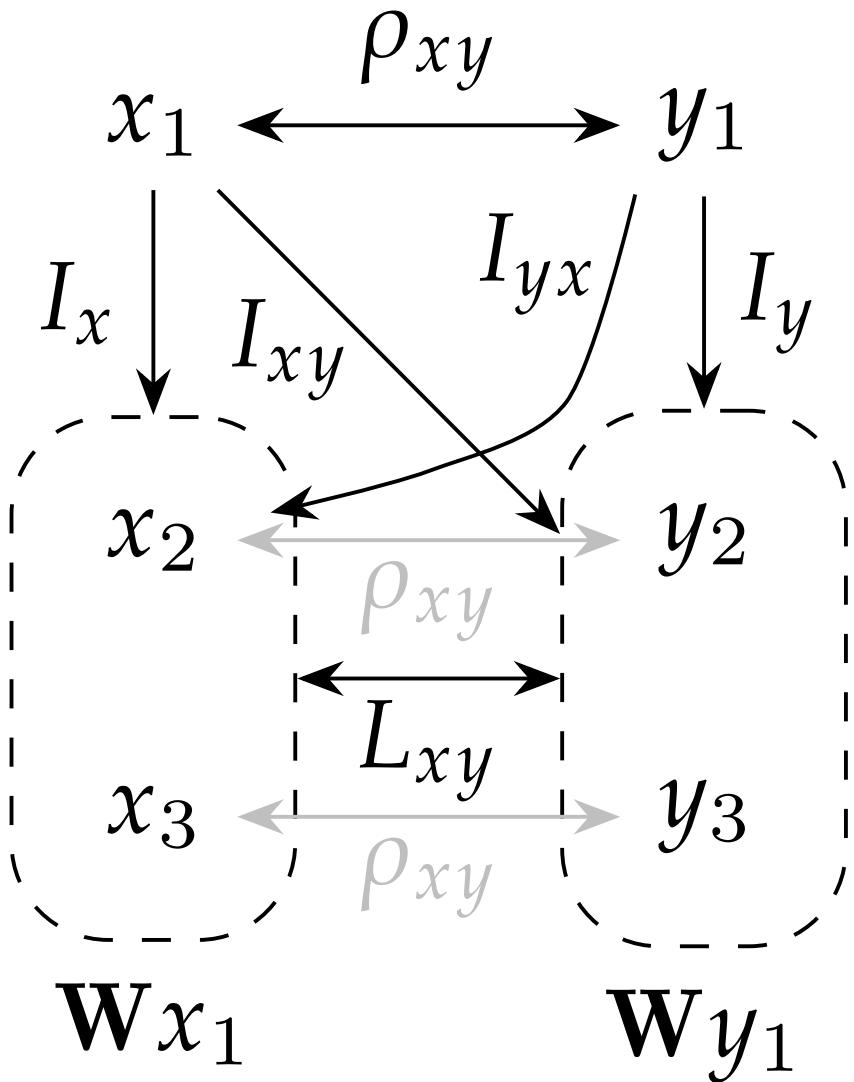
WARTENBERG MORAN MATRIX



$$L_{xy} = \mathbf{W} \cdot \mathbf{x} \circ \mathbf{W} \cdot \mathbf{y}$$

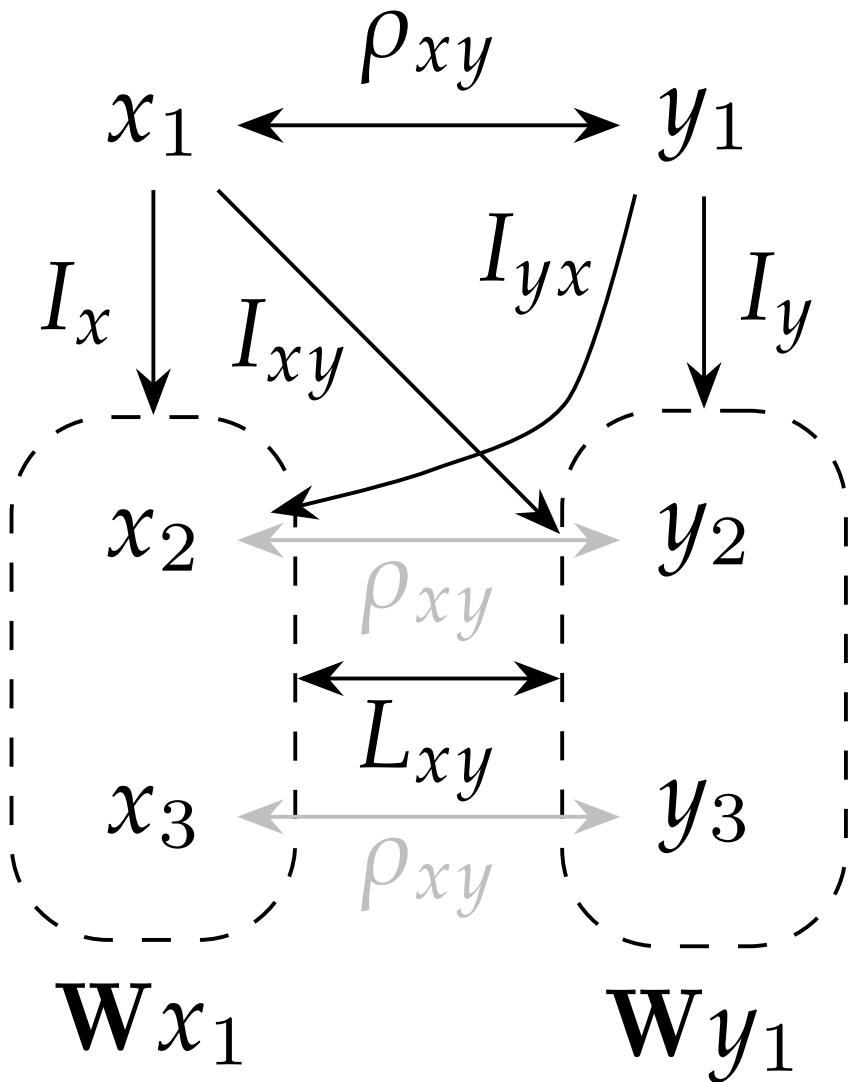


LEE'S SPATIAL PEARSON



*Is this house's rent unusual  
for its area, given its size?*

DO ANY OF THESE WORK?



*Is this house's rent unusual for its area, given its size?*

$$\mathbf{I} = y \circ \mathbf{W} \cdot y$$

*Is this house's rent unusual for its area?*

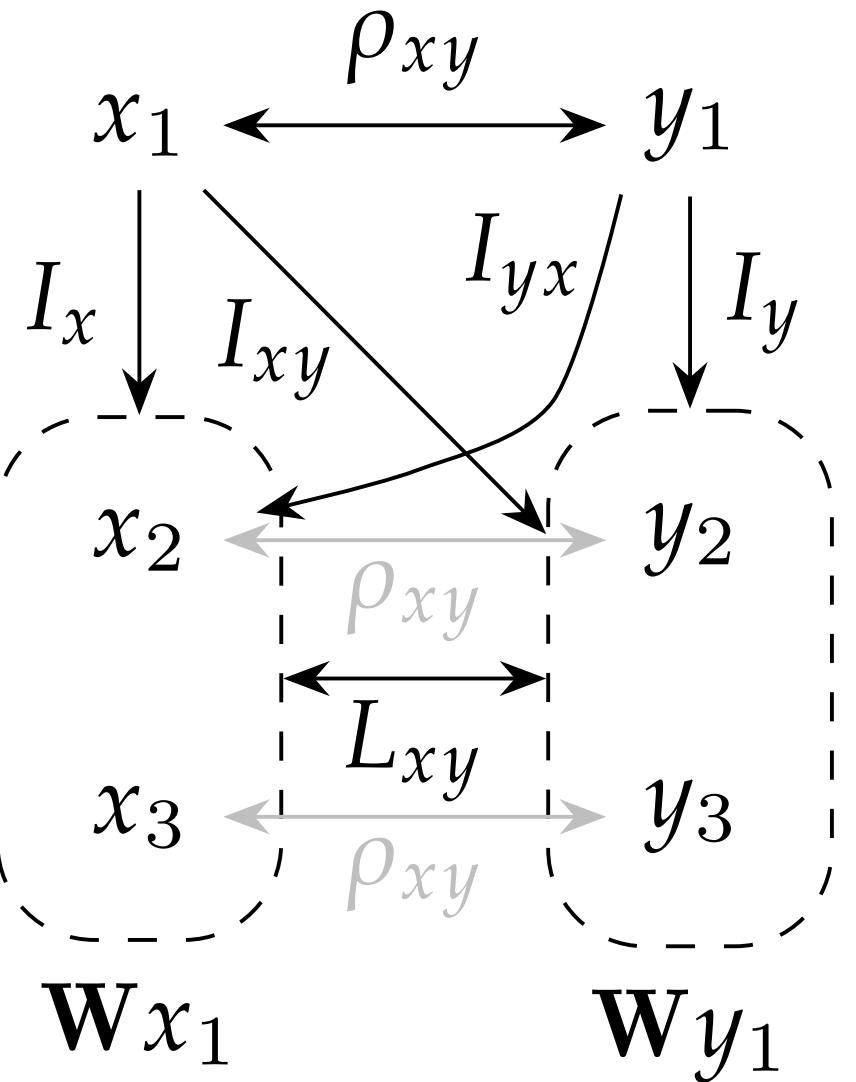
$$\mathbf{I}_{xy} = x \circ \mathbf{W} \cdot y$$

*Is this lot size unusual for house rent in this area?*

$$\mathbf{L}_{xy} = \mathbf{W} \cdot x \circ \mathbf{W} \cdot y$$

*Are this area's rents unusual for this area's lot sizes?*

DO ANY OF THESE WORK?



*Is this house's rent unusual for its area, given its size?*

$$\mathbf{I} = y \circ \mathbf{W} \cdot y$$

*Is this house's rent unusual for its area?*

$$\mathbf{I}_{xy} = x \circ \mathbf{W} \cdot y$$

*Is this lot size unusual for house rent in this area?*

$$\mathbf{L}_{xy} = \mathbf{W} \cdot x \circ \mathbf{W} \cdot y$$

*Are this area's rents unusual for this area's lot sizes?*

DO ANY OF THESE WORK? NOPE!

# LOCAL CONFOUNDING

*size effects on rent vary*

# PRIOR ART IN ESDA

*The Moran-Form Regression*

# PARTIAL CONDITIONING

*Three approaches to "control"*

# AFFORDABILITY OUTLIERS

$$y = (\mathbf{I} - \lambda \mathbf{W})^{-1}(\mathbf{x}\beta + \epsilon)$$

## THE SPATIAL LAG MODEL

$$y = (\mathbf{I} - \lambda \mathbf{W})^{-1}(\mathbf{x}\beta + \epsilon)$$

Rents              At Site              Nearby              Bedrooms

## THE SPATIAL LAG MODEL

$$y = (\mathbf{I} - \lambda \mathbf{W})^{-1}(\mathbf{x}\beta + \epsilon)$$

Rents      At Site      Nearby      Bedrooms      Premium?

## THE SPATIAL LAG MODEL

$$y = (\mathbf{I} - \lambda \mathbf{W})^{-1}(\mathbf{x}\beta + \epsilon)$$

Rents              At Site              Nearby              Bedrooms              Premium?

$$e = y - (\mathbf{I} - \hat{\lambda} \mathbf{W})^{-1} \mathbf{x}\hat{\beta}$$

$$e = y - \mathbf{x}\hat{\beta} - \hat{\lambda} \mathbf{W} \mathbf{x}\hat{\beta} - \hat{\lambda}^2 \mathbf{W}^2 \mathbf{x}\hat{\beta} + \dots$$

## THE SPATIAL LAG MODEL

$$y = (\mathbf{I} - \lambda \mathbf{W})^{-1}(\mathbf{x}\beta + \epsilon)$$

Rents      At Site      Nearby      Bedrooms      Premium?

$$e = y - (\mathbf{I} - \hat{\lambda} \mathbf{W})^{-1} \mathbf{x}\hat{\beta}$$

$$e = y - \mathbf{x}\hat{\beta} - \hat{\lambda} \mathbf{W} \mathbf{x}\hat{\beta} - \hat{\lambda}^2 \mathbf{W}^2 \mathbf{x}\hat{\beta} + \dots$$

Premium?      Rents      Site Size      Nearby Sizes

## THE SPATIAL LAG MODEL

$$y = (\mathbf{I} - \lambda \mathbf{W})^{-1}(\mathbf{x}\beta + \epsilon)$$

Rents              At Site              Nearby              Bedrooms              Premium?

$$e = y - (\mathbf{I} - \hat{\lambda} \mathbf{W})^{-1} \mathbf{x}\hat{\beta}$$

Still “filtered” by  $(\mathbf{I} - \lambda \mathbf{W})^{-1}$

Can ID unusual prices

Not a covariance

## THE SPATIAL LAG MODEL

$$y = x\beta + \epsilon$$

Rents                      Bedrooms                      Premium at site

AUXILIARY REGRESSION

$$y = x\beta + \epsilon$$

$$e = y - x\hat{\beta}$$

AUXILIARY REGRESSION

$$y = x\beta + \epsilon$$

$$e = y - x\hat{\beta}$$

$$\mathbf{I}_{x \rightarrow y} = e \circ \mathbf{W}e$$

*Is this premium unusual given the premium people are paying for space in the area?*

## AUXILIARY REGRESSION

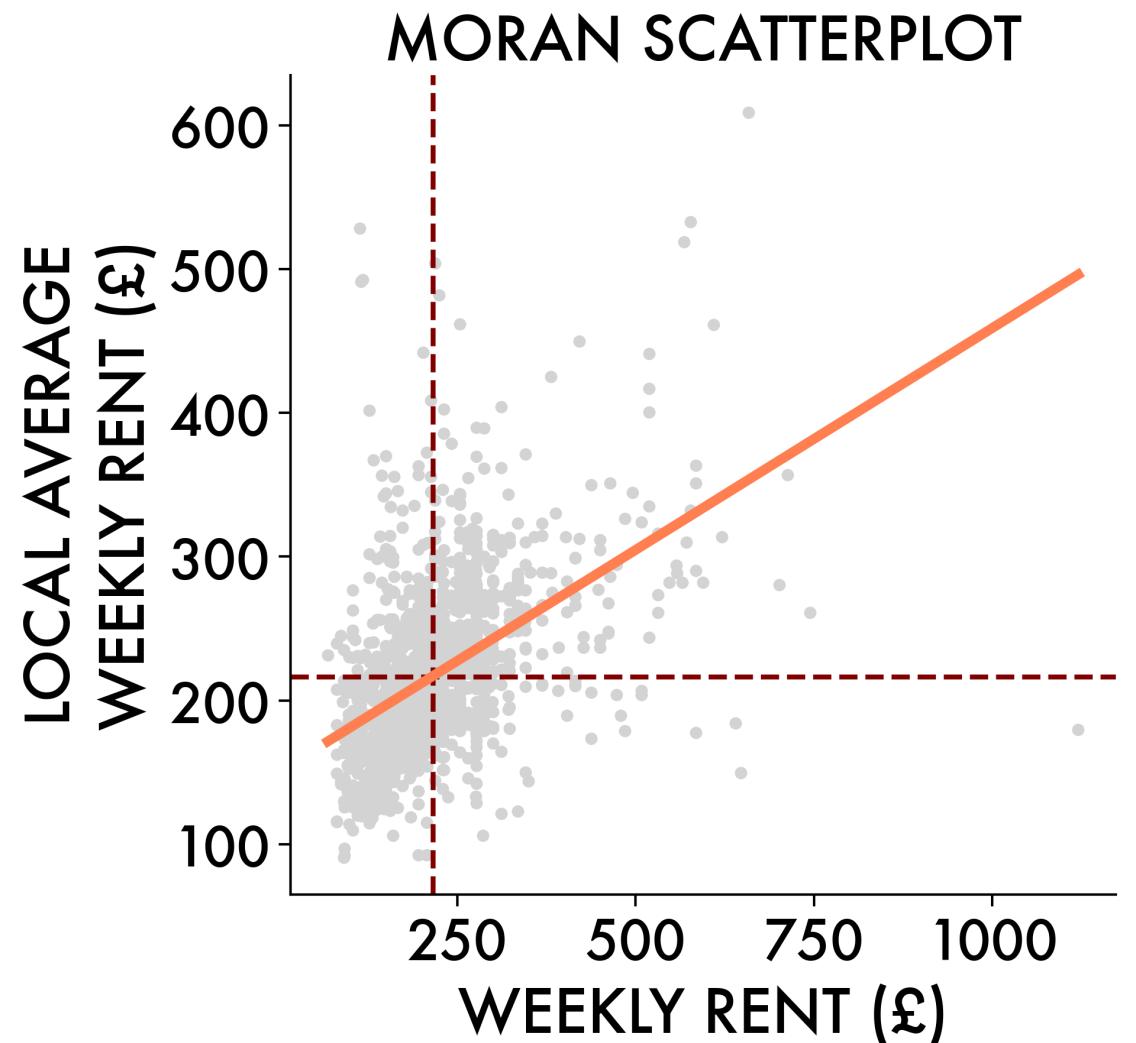
$$y = x\beta + \epsilon$$

$$e = y - x\hat{\beta}$$

$$\mathbf{I}_{x \rightarrow y} = e \circ \mathbf{W}e$$

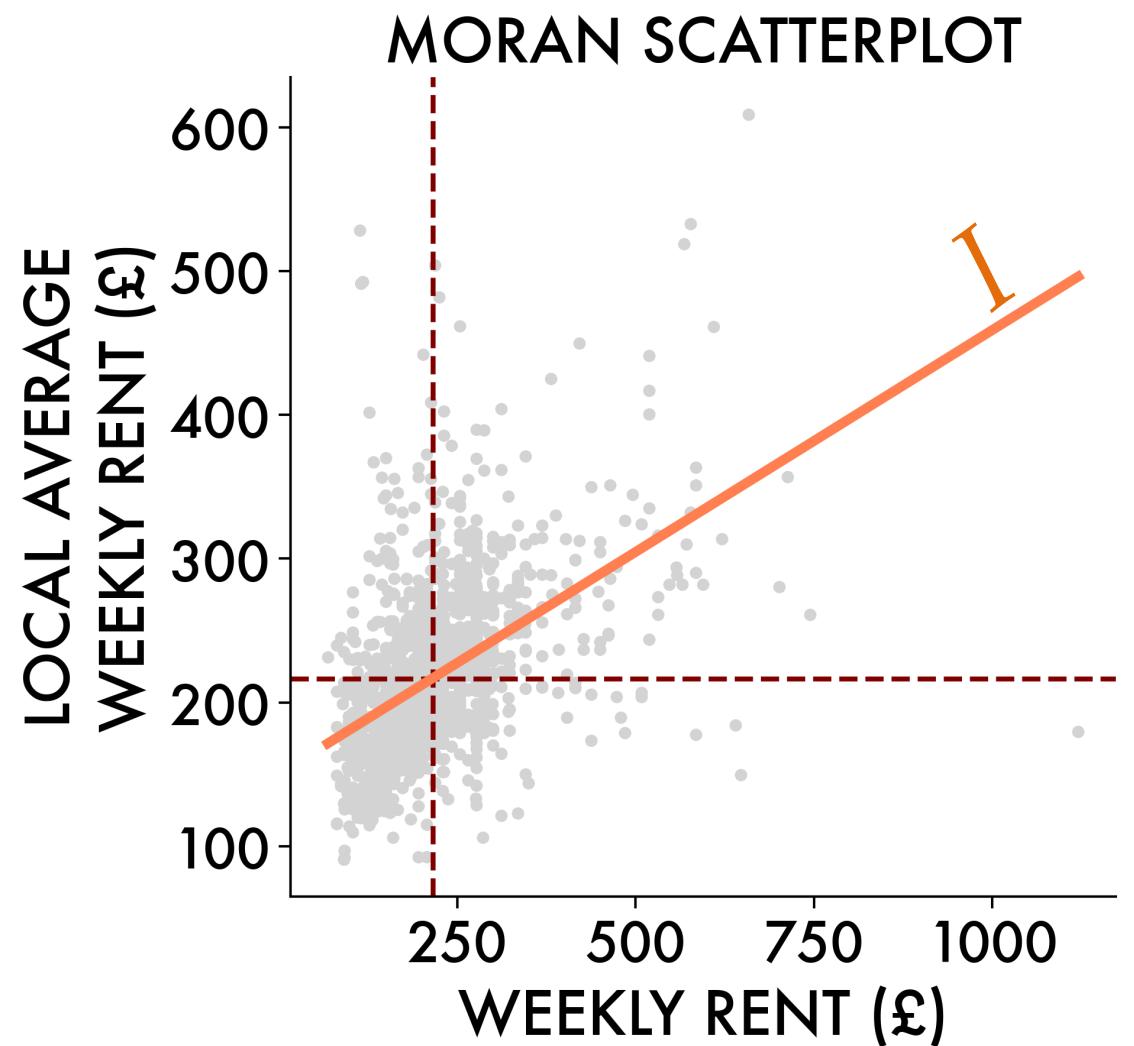
*Is this premium unusual given the premium people  
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## AUXILIARY REGRESSION



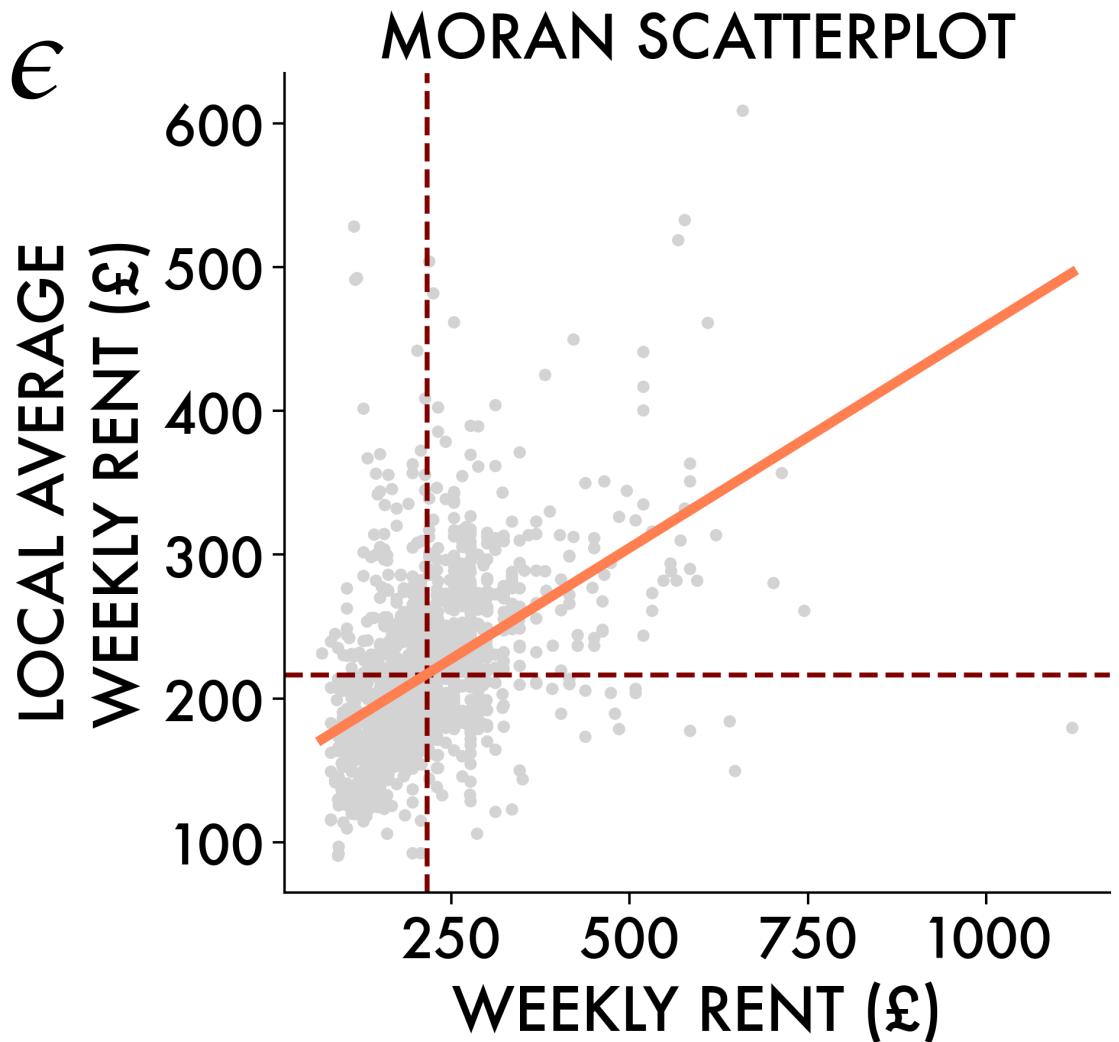
## MORAN-FORM REGRESSIONS

$$W\mathbf{y} = I\mathbf{y} + \epsilon$$



MORAN-FORM REGRESSIONS

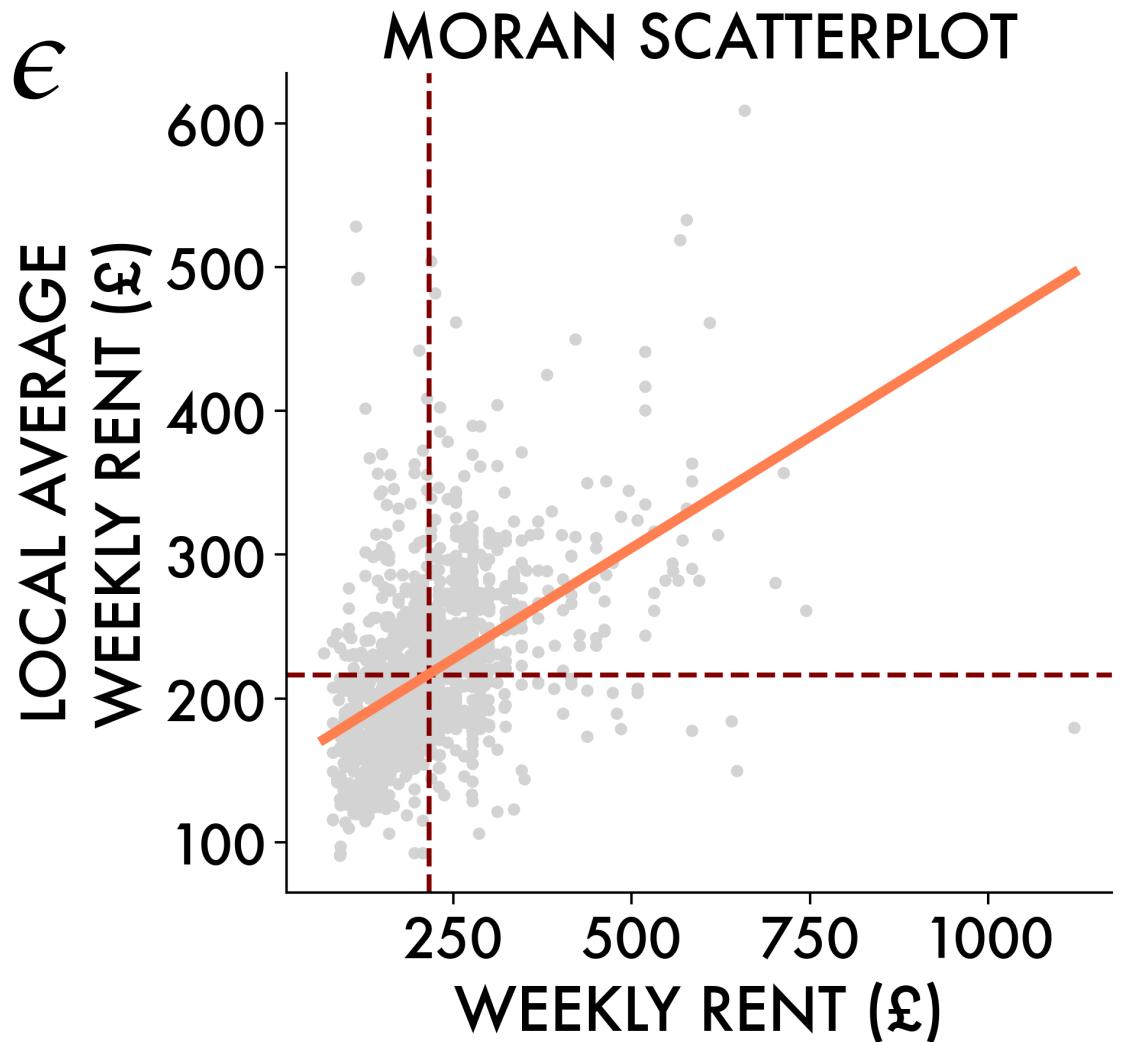
$$W\gamma = I\gamma + x\beta + \epsilon$$



MORAN-FORM REGRESSIONS

$$W\gamma = I\gamma + x\beta + \epsilon$$

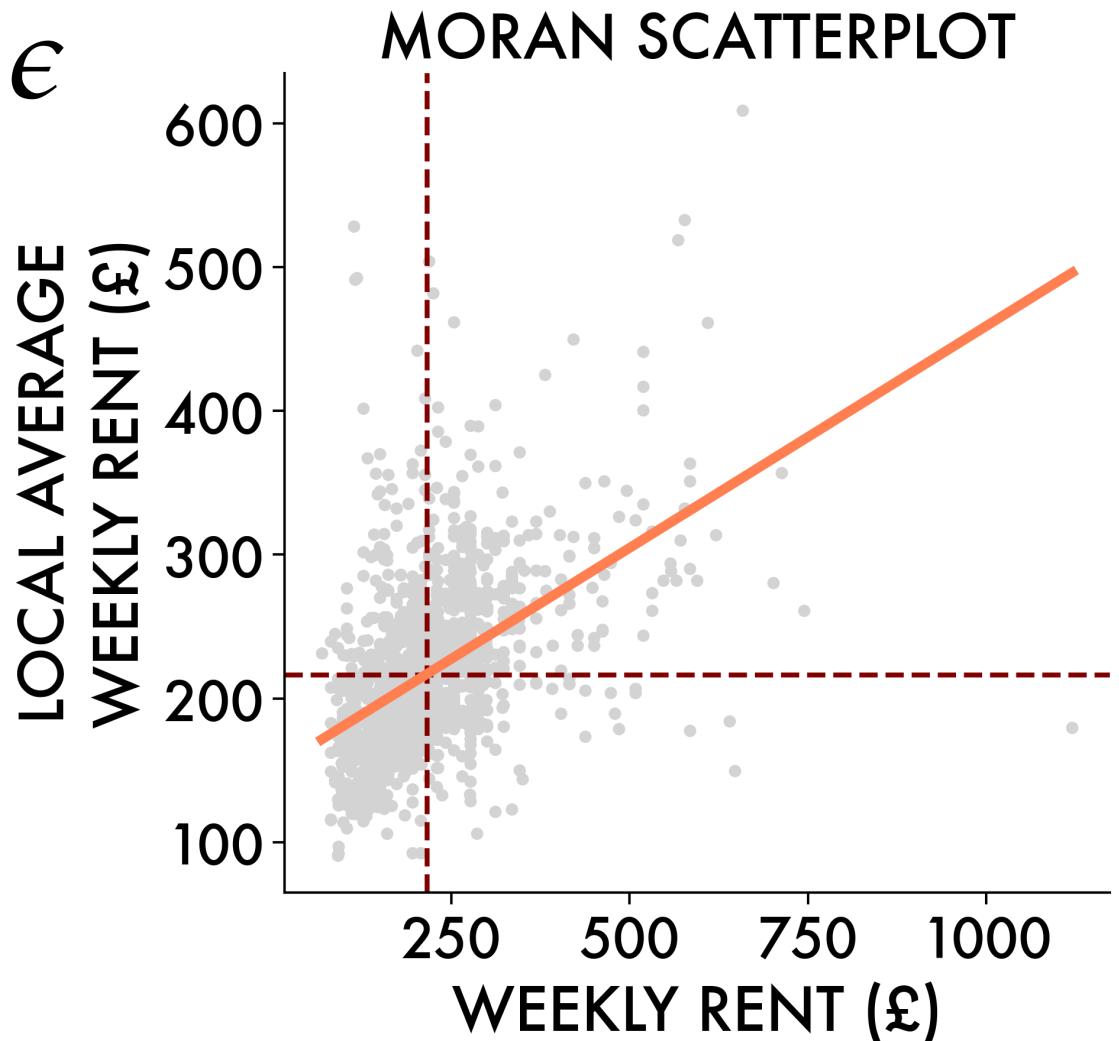
*What is the relationship between a house's rent and nearby rents, holding the house's size constant?*



MORAN-FORM REGRESSIONS

$$W\gamma = I\gamma + x\beta + \epsilon$$

*What is the relationship  
between a house's rent and  
nearby rents, holding the  
house's size constant?* 



## MORAN-FORM REGRESSIONS

$$\mathbf{W}y = Iy + x\beta + \epsilon \quad \mathbf{W}\vec{y} = \mathbf{W} [y \quad y \quad \dots]$$

$$\mathbf{D} = [y \quad x]$$

$$\mathbf{I}_{y|x} = (\mathbf{D}'\mathbf{D})^{-1}\mathbf{D} \circ \mathbf{W}\vec{y}$$

A LOCAL “CETERIS PARIBUS” STATISTIC

$$\mathbf{W}y = Iy + x\beta + \epsilon \quad \mathbf{W}\vec{y} = \mathbf{W} [y \quad y \quad \dots]$$

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$$\mathbf{I}_{y|x} \propto \mathbf{I}_y - \rho \mathbf{I}_{xy}$$

A LOCAL “CETERIS PARIBUS” STATISTIC

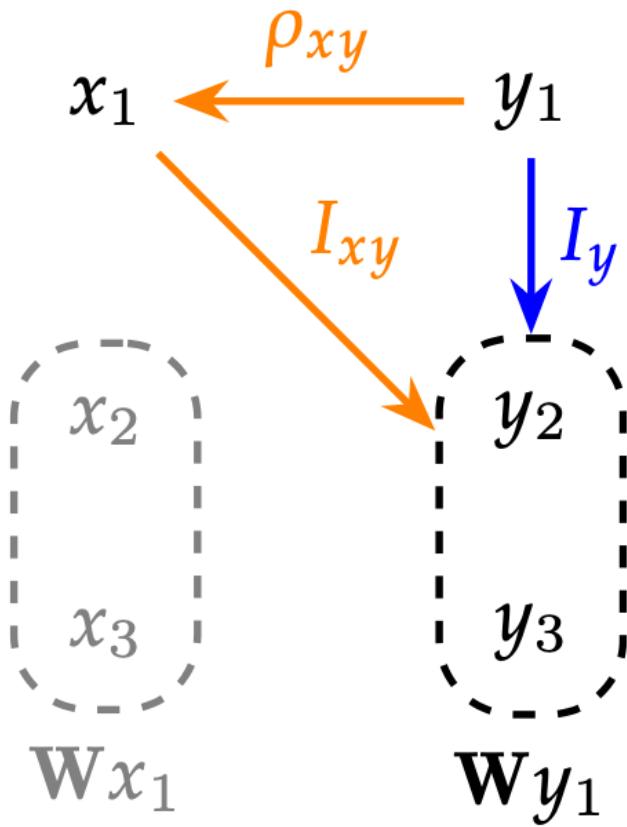
$$I_{y|x} \propto I_y - \rho I_{xy}$$

THE PARTIAL LOCAL MORAN

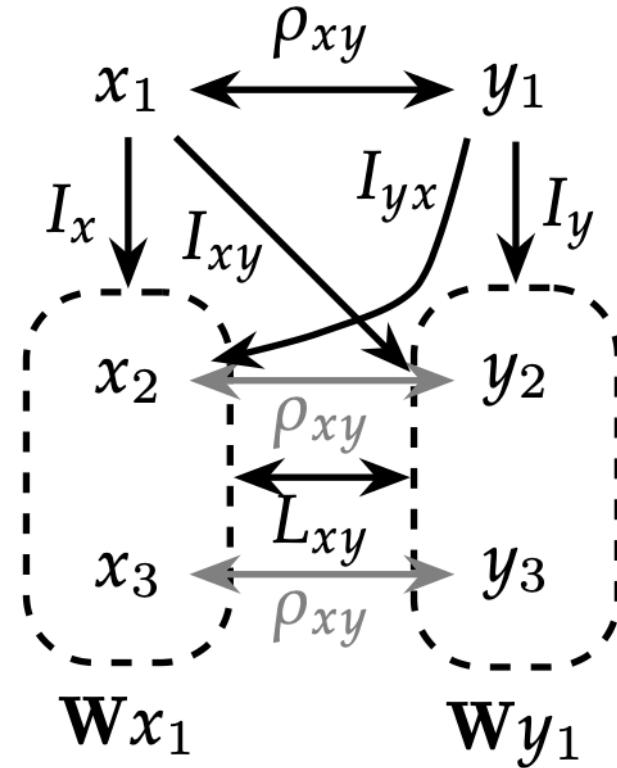
$$I_{y|x} \propto I_y - \rho I_{xy}$$

Spatial association within  $y$   
Adjusted by  $x$ 's association  
with nearby  $y$  and  $y$  itself

## PARTIAL LOCAL MORAN

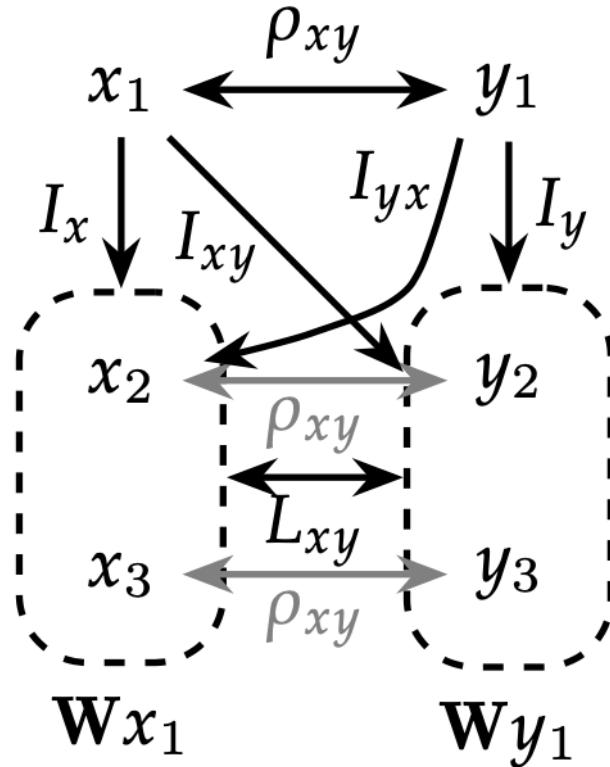
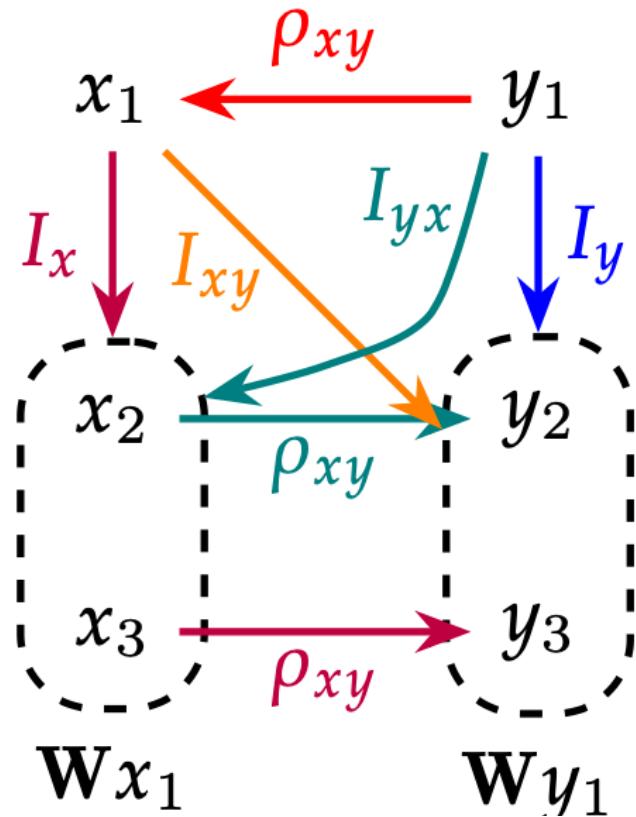


$$I_{y|x} \propto \underline{I_y} - \underline{\rho I_{xy}}$$



Classic Statistics

PARTIAL LOCAL MORAN



$$I_{x \rightarrow y} \propto \underline{I_y} - \underline{\rho I_{xy}} - \underline{\rho I_{yx}} + \underline{\rho^2 I_x}$$

AUXILIARY REGRESSION MORAN IS FULL CONDITIONING

$$W\gamma = X\beta + Iy + e$$

HIGHER DIMENSIONAL PARTIAL CONDITIONING BY FWL

$$W\mathbf{y} = \mathbf{X}\boldsymbol{\beta} + I\mathbf{y} + e$$

Now have  $p$  features  
needing adjustment

HIGHER DIMENSIONAL PARTIAL CONDITIONING BY FWL

$$\mathbf{W}\mathbf{y} = \mathbf{X}\boldsymbol{\beta} + \mathbf{I}\mathbf{y} + \mathbf{e}$$

$$\mathbf{M} = \mathbf{I} - \mathbf{X}'(\mathbf{X}'\mathbf{X})^{-1}\mathbf{X}'$$

Residual Maker Matrix, so-called because  $\mathbf{M}\mathbf{y} = \mathbf{e}$

HIGHER DIMENSIONAL PARTIAL CONDITIONING BY FWL

$$\mathbf{W}\mathbf{y} = \mathbf{X}\boldsymbol{\beta} + I\mathbf{y} + \mathbf{e}$$

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Residual Maker Matrix, so-called because  $\mathbf{M}\mathbf{y} = \mathbf{e}$

$$\mathbf{M}\mathbf{W}\mathbf{y} = I_{y|x}\mathbf{M}\mathbf{y} + \epsilon$$

HIGHER DIMENSIONAL PARTIAL CONDITIONING BY FWL

$$\mathbf{M}\mathbf{W}\mathbf{y} = I_{y|x} \mathbf{M}\mathbf{y} + \epsilon$$

$$I_{y|x} \propto (\mathbf{M}\mathbf{y})' \mathbf{M}\mathbf{W}\mathbf{y}$$

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$$I_{y|x} \propto (\mathbf{M}\mathbf{y})' \mathbf{M}\mathbf{W}\mathbf{y}$$

$$\propto \mathbf{y}' \mathbf{W}\mathbf{y} - (\mathbf{x}' (\mathbf{x}' \mathbf{x})^{-1} \mathbf{x}' \mathbf{y})' \mathbf{W}\mathbf{y}$$

$$I_y$$

HIGHER DIMENSIONAL PARTIAL CONDITIONING BY FWL

$$\mathbf{M}\mathbf{W}\mathbf{y} = I_{y|x}\mathbf{M}\mathbf{y} + \epsilon$$

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$$\propto \mathbf{y}' \mathbf{W}\mathbf{y} - (\mathbf{x}' (\mathbf{x}'\mathbf{x})^{-1} \mathbf{x}'\mathbf{y})' \mathbf{W}\mathbf{y}$$

$$I_y \qquad (\mathbf{x}' \boldsymbol{\beta})' \mathbf{W}\mathbf{y}$$

HIGHER DIMENSIONAL PARTIAL CONDITIONING BY FWL

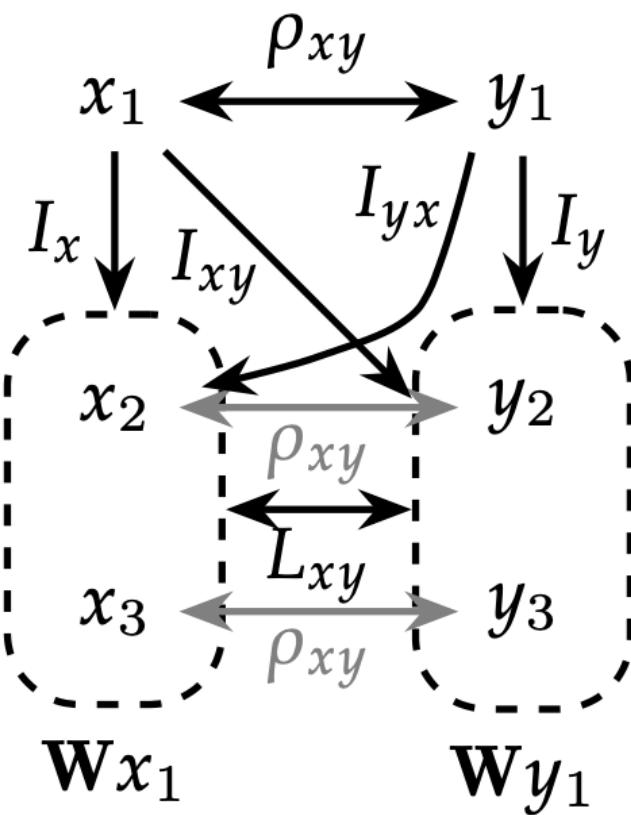
$$\mathbf{M}\mathbf{W}\mathbf{y} = I_{y|x}\mathbf{M}\mathbf{y} + \epsilon$$

$$I_{y|x} \propto (\mathbf{M}\mathbf{y})' \mathbf{M}\mathbf{W}\mathbf{y}$$

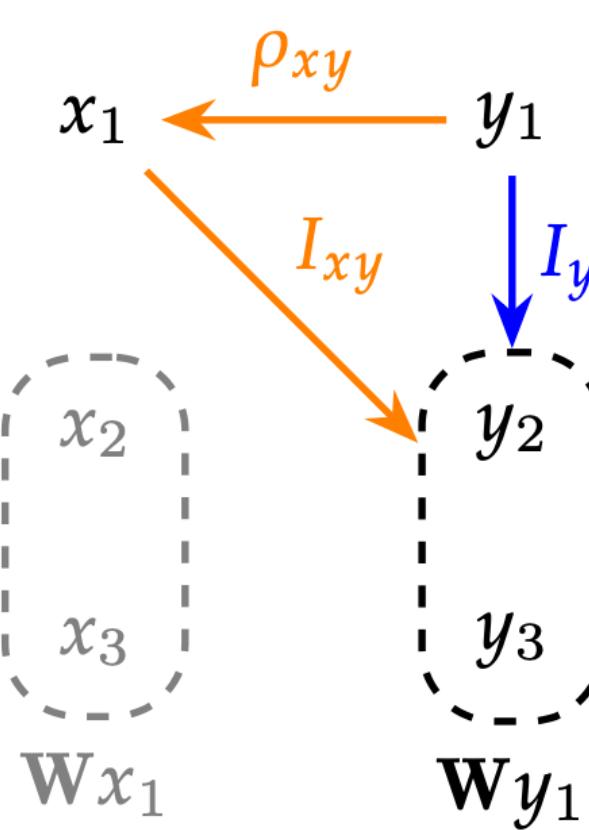
$$\propto \mathbf{y}' \mathbf{W}\mathbf{y} - (\mathbf{x}' (\mathbf{x}'\mathbf{x})^{-1} \mathbf{x}'\mathbf{y})' \mathbf{W}\mathbf{y}$$

$$I_y \quad (\mathbf{P}\mathbf{y})' \mathbf{W}\mathbf{y}$$

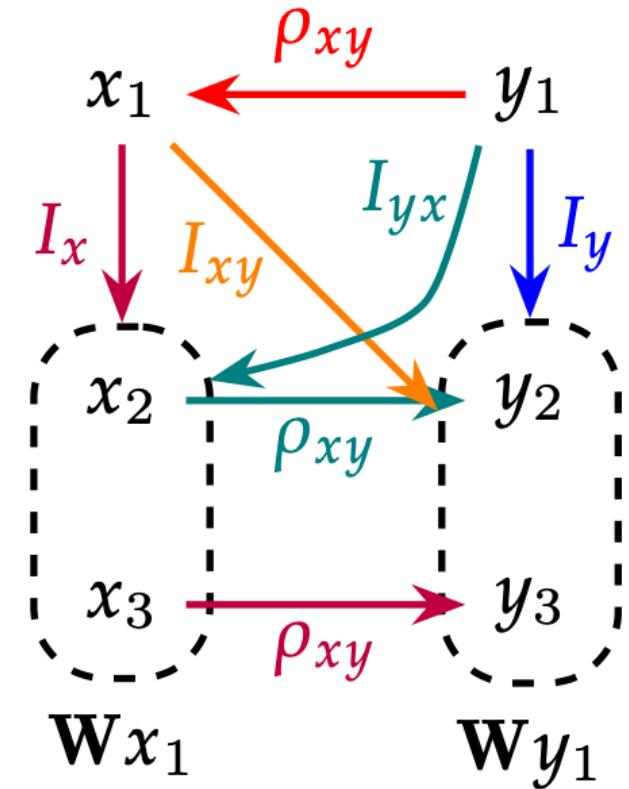
HIGHER DIMENSIONAL PARTIAL CONDITIONING BY FWL



Classic Statistics



Partial  $I_{y|x}$



Full  $I_{x \rightarrow y}$

THE POINT REMAINS: CORRECT Y FOR X (& MAYBE WX)

# LOCAL CONFOUNDING

*confounding is not stationary*

# PRIOR ART IN ESDA

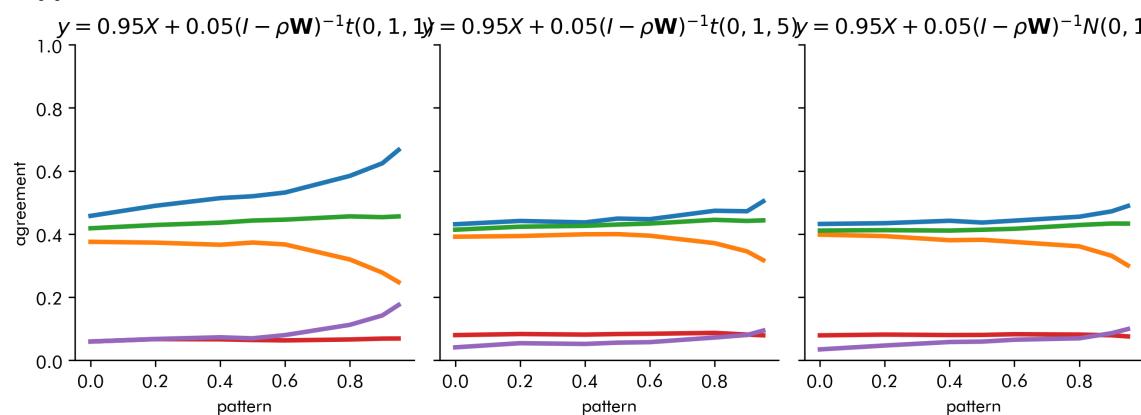
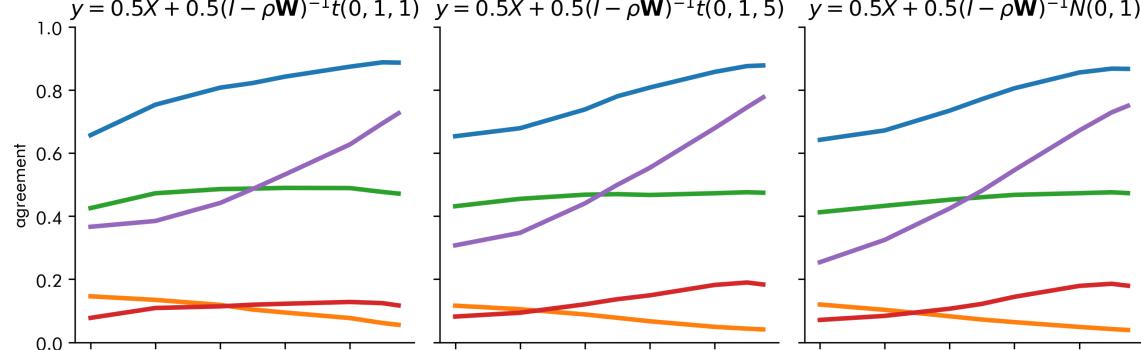
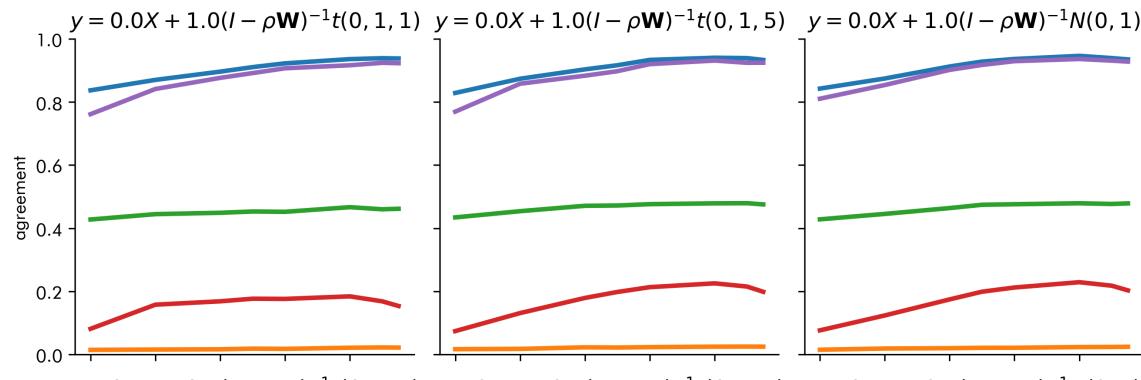
*The Moran-Form Regression*

# PARTIAL CONDITIONING

*Two approaches to "control"*

# AFFORDABILITY OUTLIERS

*Where are the good deals?*



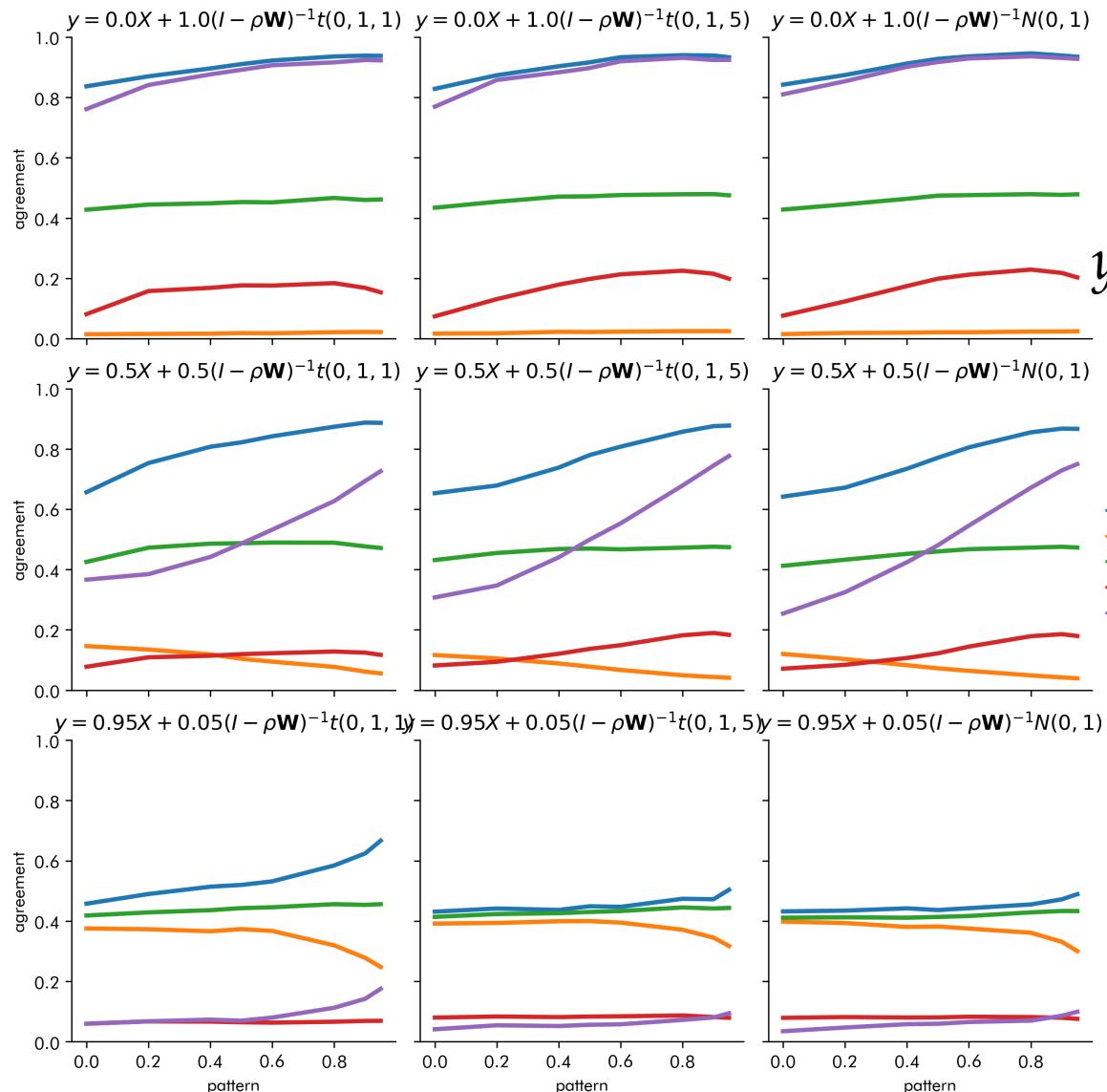
*SAR t-distributed random effects process  
(SARTRE)*

$$y = \alpha x + (1 - \alpha)(I - \lambda \mathbf{W})^{-1}t(\mu, \tau^2, \nu)$$

stat

- uvl\_y
- uvl\_x0
- bvl\_x0
- lee\_x0
- plmo

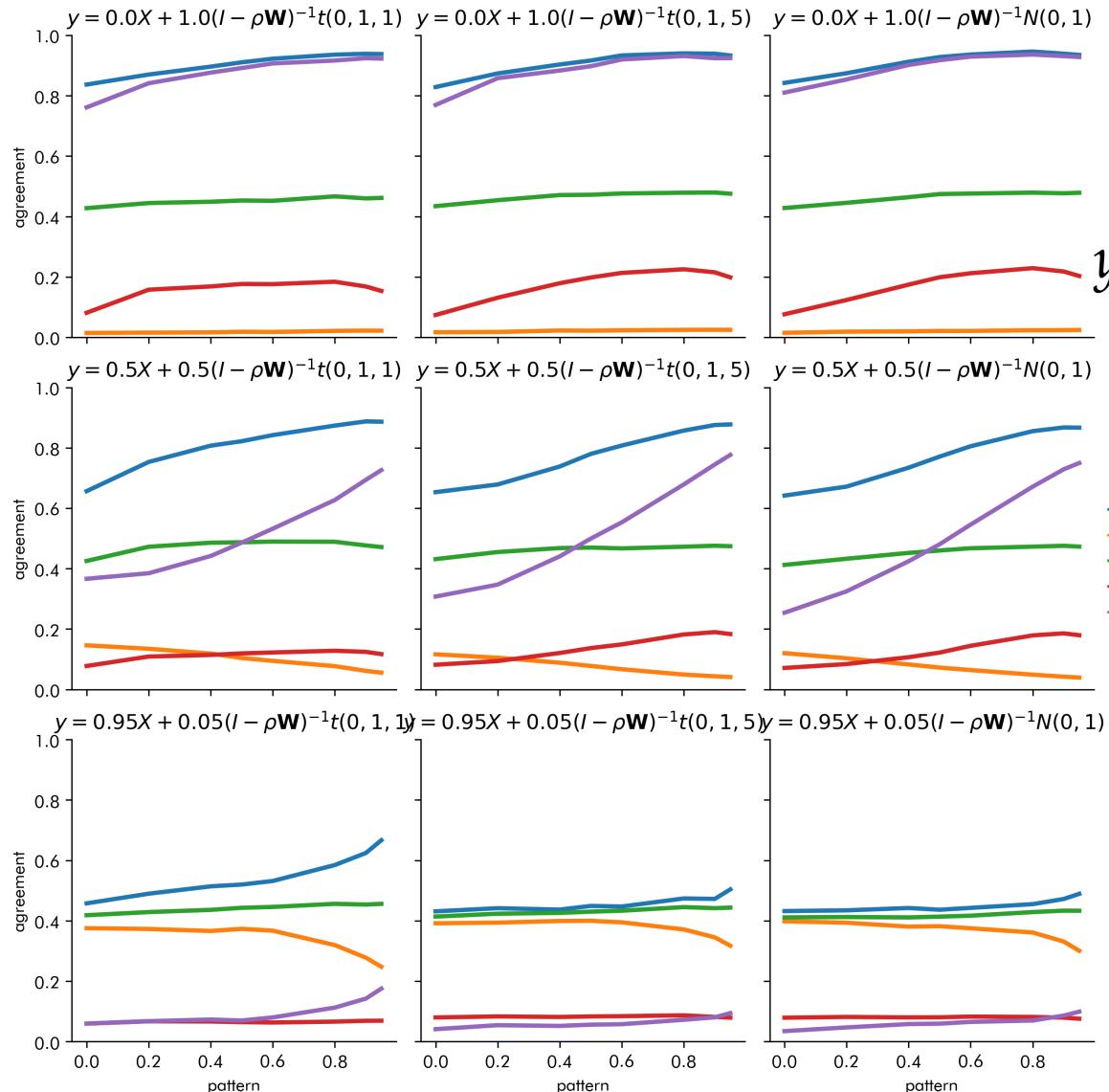
**SURPRISE! SIMULATION RESULTS FIRST!**



*SAR t-distributed random effects process  
(SARTRE)*

$y = \alpha x + (1 - \alpha)(I - \lambda\mathbf{W})^{-1}t(\mu, \tau^2, \nu)$   
 confounder      SAR patterning      random effect  
 $\alpha \in [0, 1]$

**SURPRISE! SIMULATION RESULTS FIRST!**



*SAR t-distributed random effects process  
(SARTRE)*

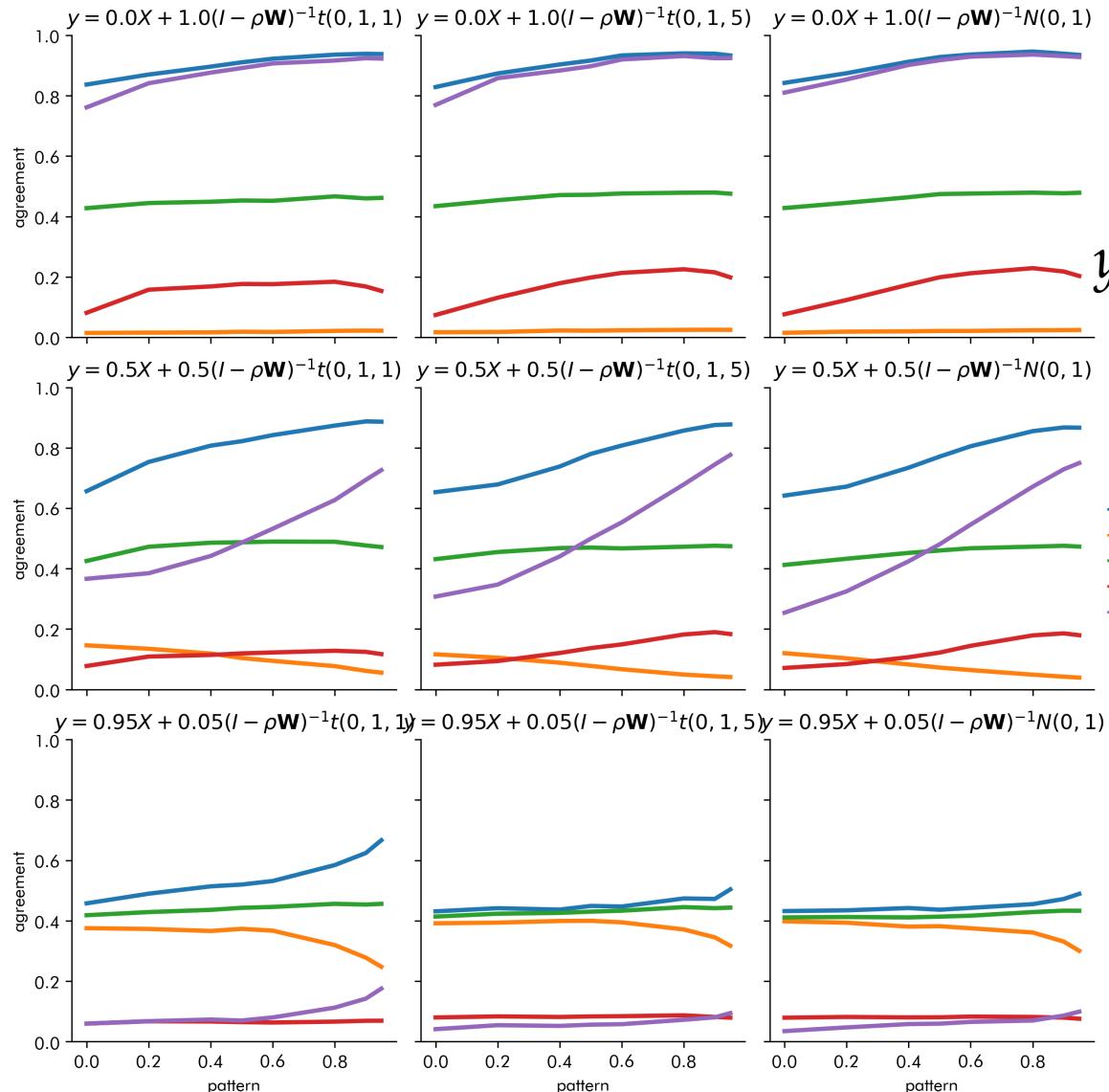
$$y = \alpha x + (1 - \alpha)(I - \lambda \mathbf{W})^{-1}t(\mu, \tau^2, \nu)$$

confounder      SAR patterning      random effect

$$\alpha \in [0, 1]$$

*Blend a spatially-unpatterned "confounding effect" with a spatially-structured part with controlled tail thickness.*

**SURPRISE! SIMULATION RESULTS FIRST!**

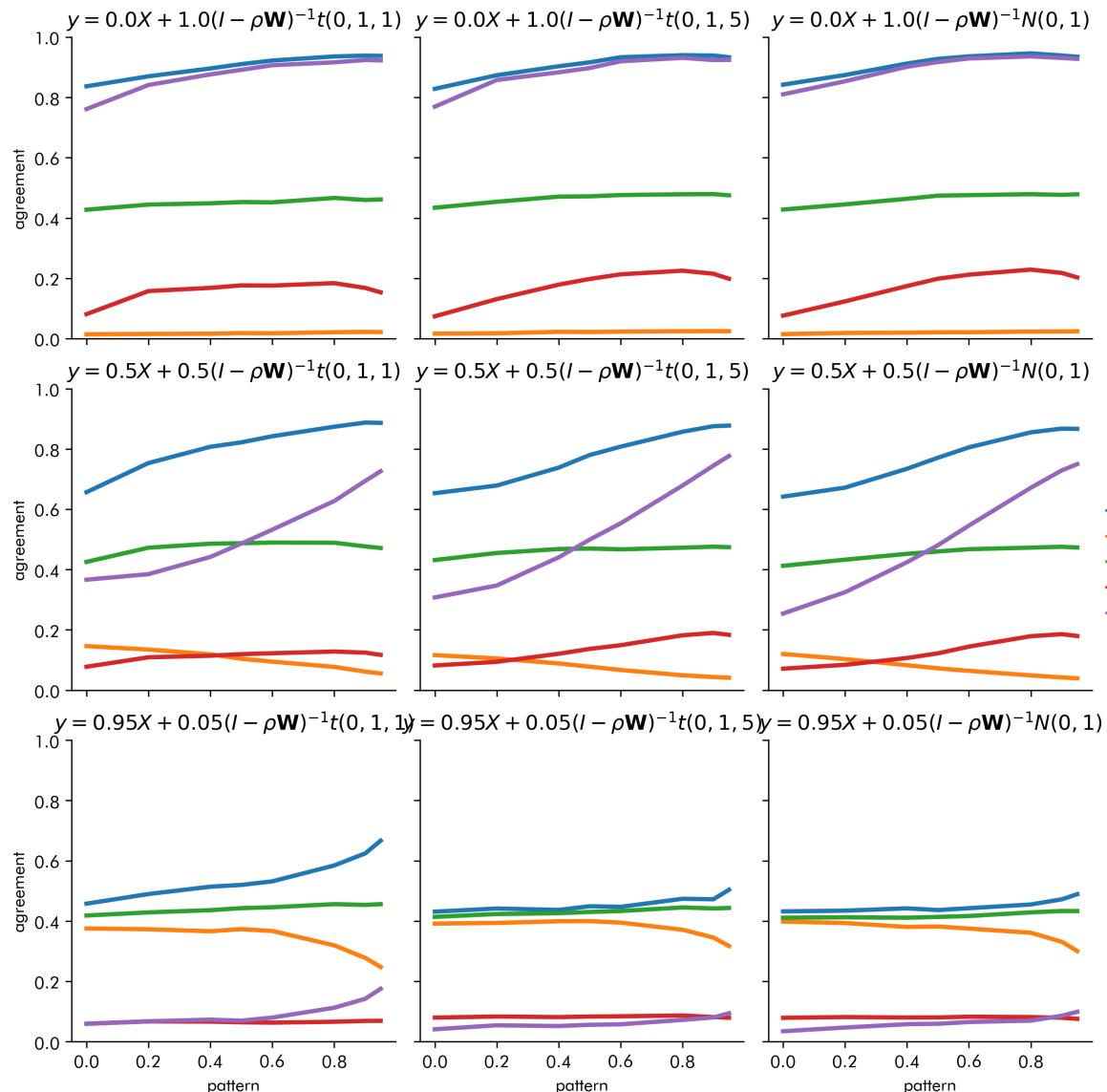


*SAR t-distributed random effects process  
(SARTRE)*

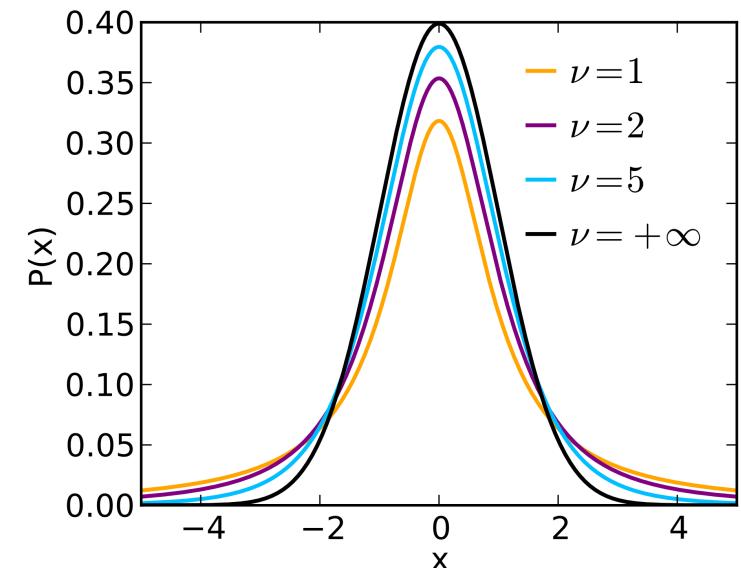
$$y = \alpha x + (1 - \alpha)(I - \lambda\mathbf{W})^{-1}t(\mu, \tau^2, \nu)$$

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**SURPRISE! SIMULATION RESULTS FIRST!**



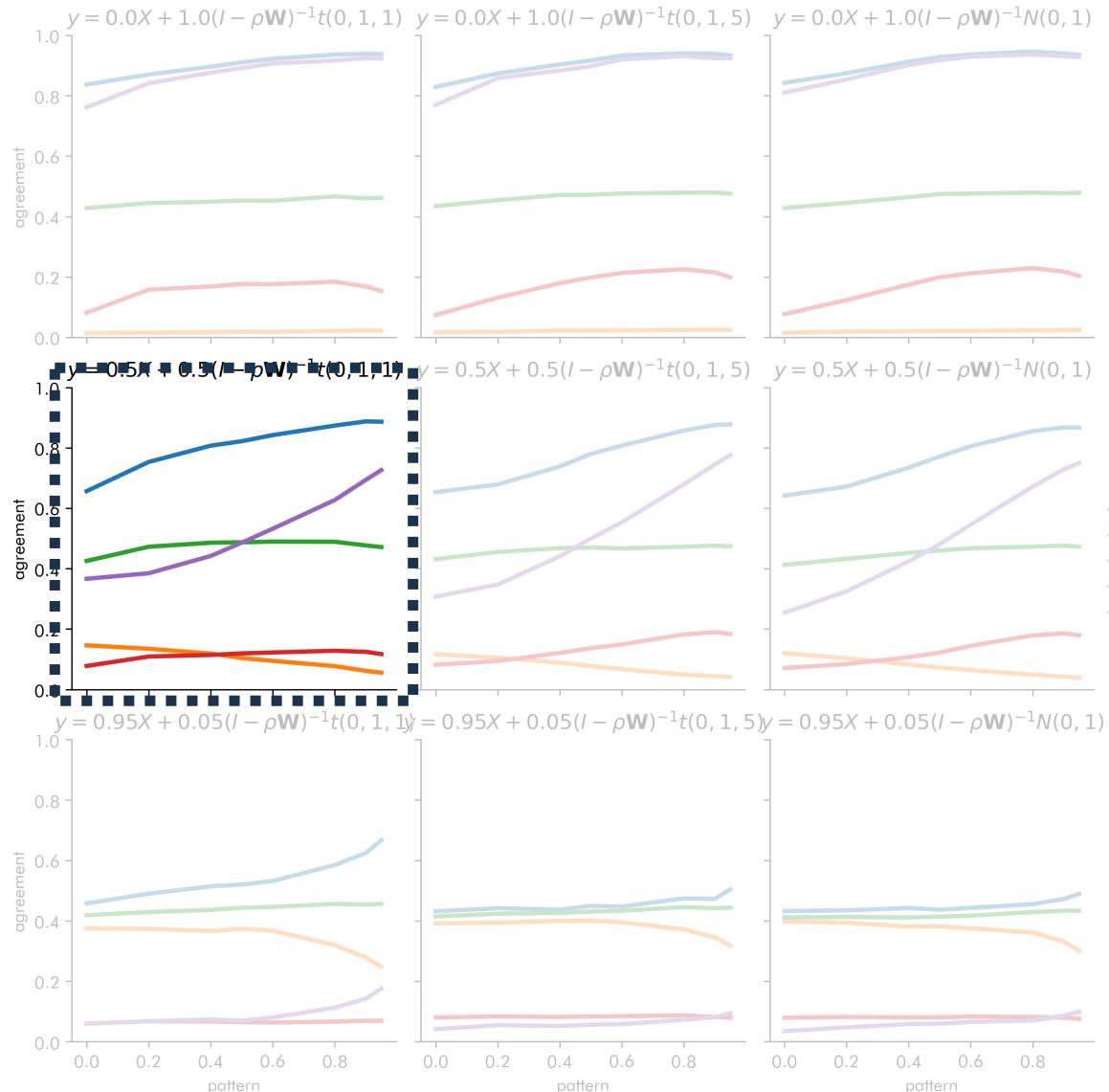
SAR  $t$ -distributed random effects process  
(SARTRE)



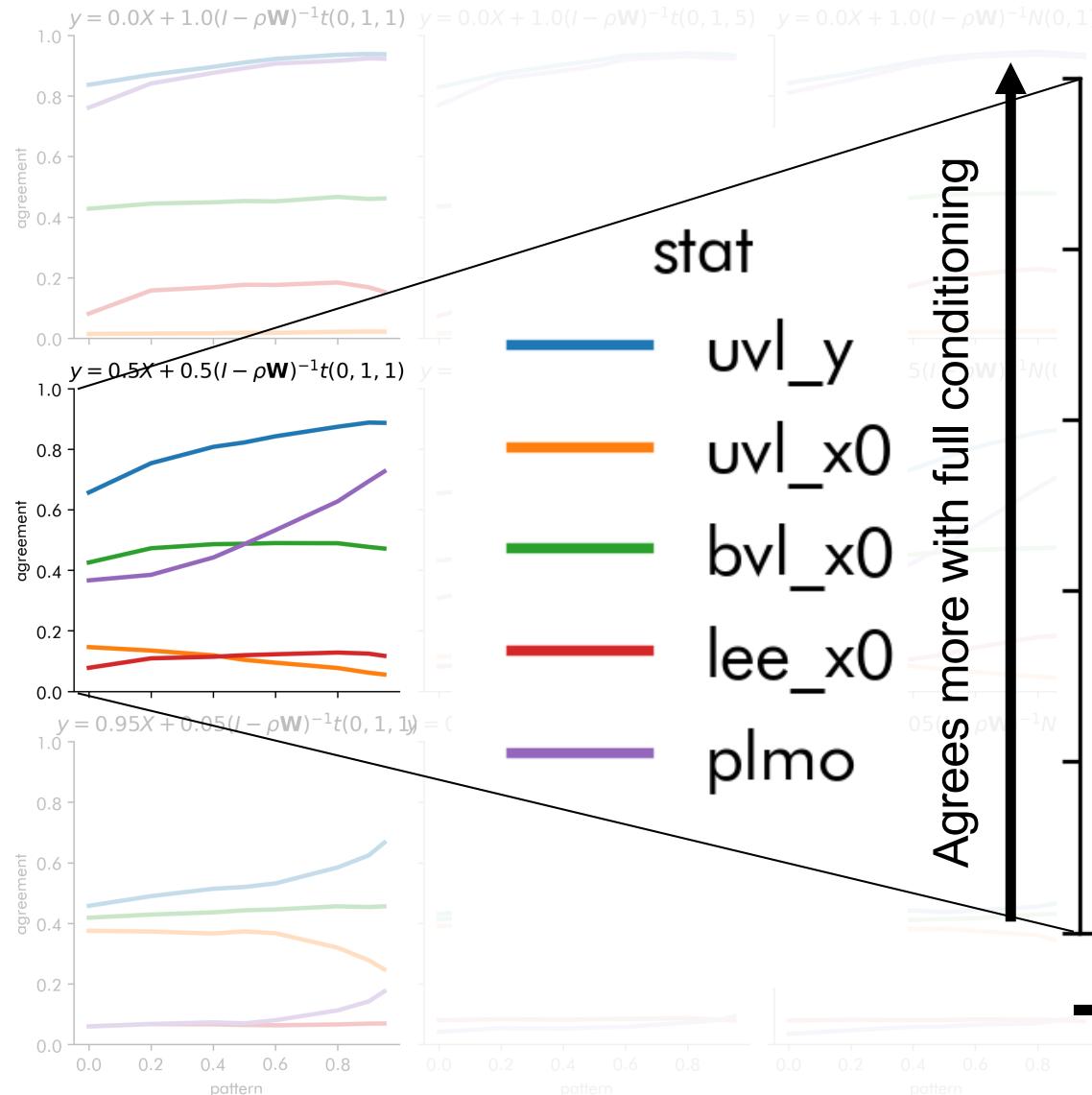
Blend a spatially-unpatterned "confounding effect" with a spatially-structured part with controlled tail thickness.

$$\nu \rightarrow \infty$$

SURPRISE! SIMULATION RESULTS FIRST!  $t(\mu, \tau^2, \nu) \rightarrow \mathcal{N}(\mu, \tau^2)$



**SURPRISE! SIMULATION RESULTS FIRST!**

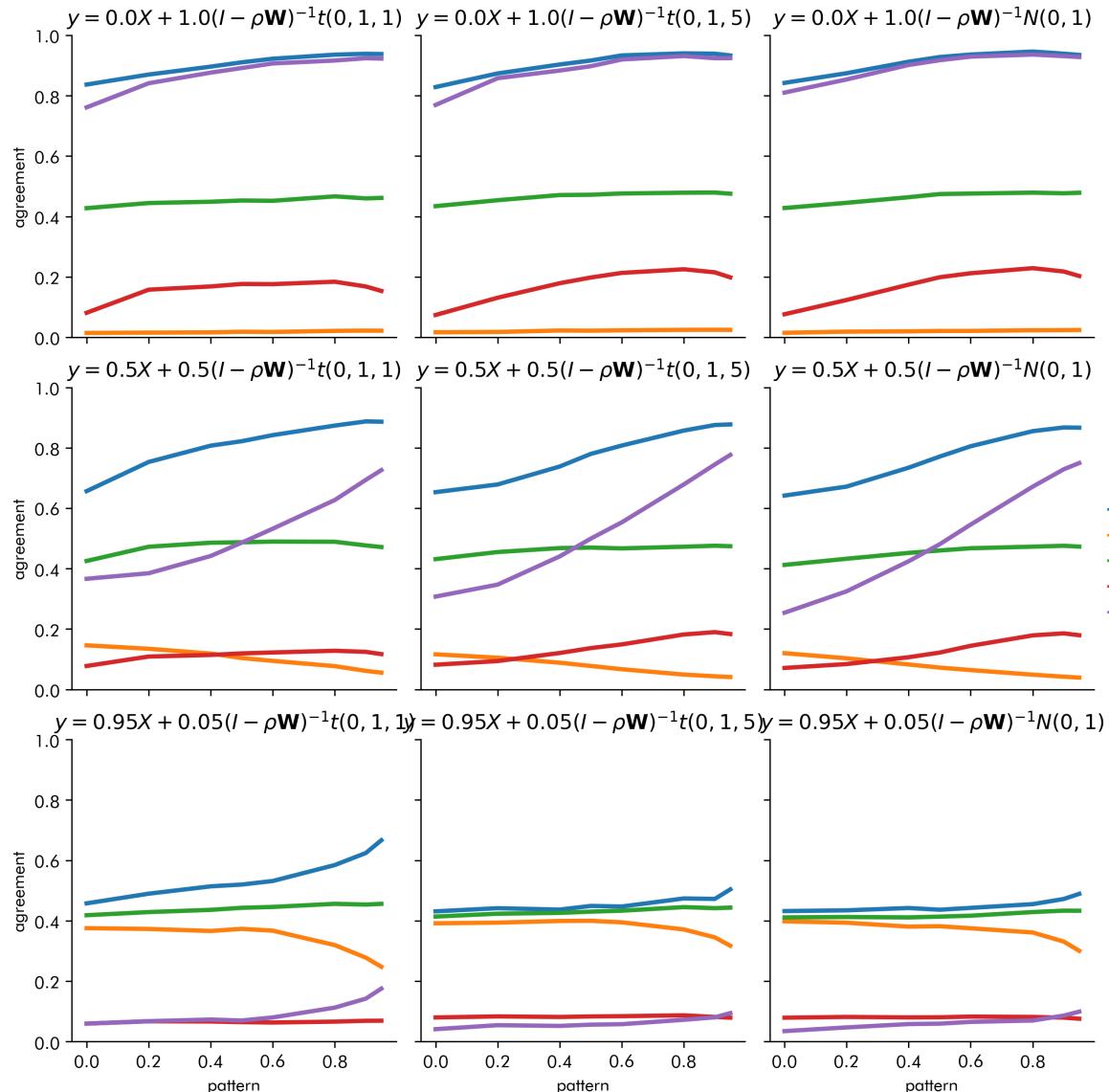


Agrees more with full conditioning



Stronger SAR error dependence

SURPRISE! SIMULATION RESULTS FIRST!

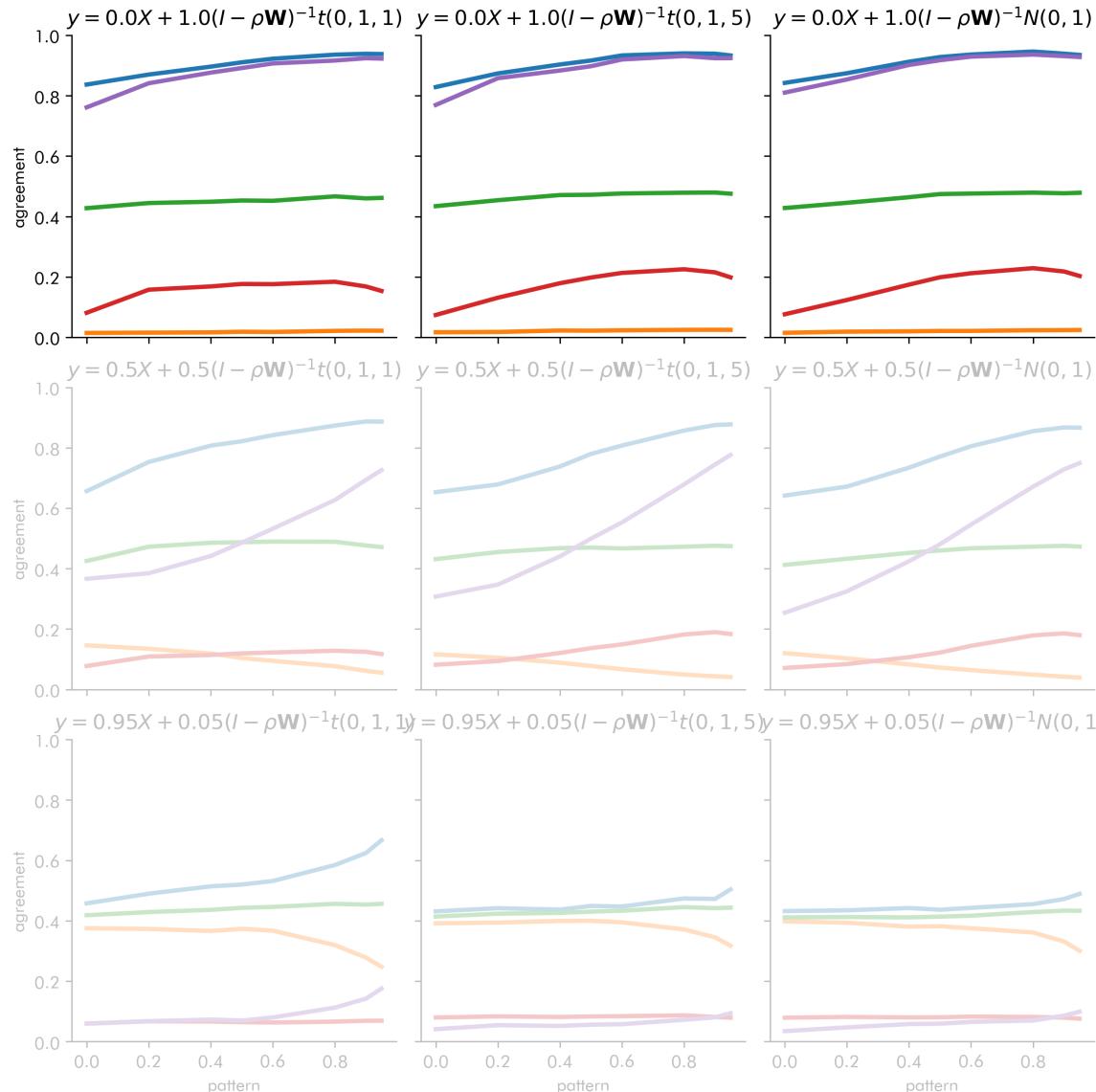


- Increasing SD right within facets
- Increasing “agreement” w/ aux. reg. moving up within facets
- Thinner tails moving right over facets
- Increasing confounding moving down over facets

stat

- $uvly$
- $uvlx_0$
- $bvlx_0$
- $lee_x_0$
- $plmo$

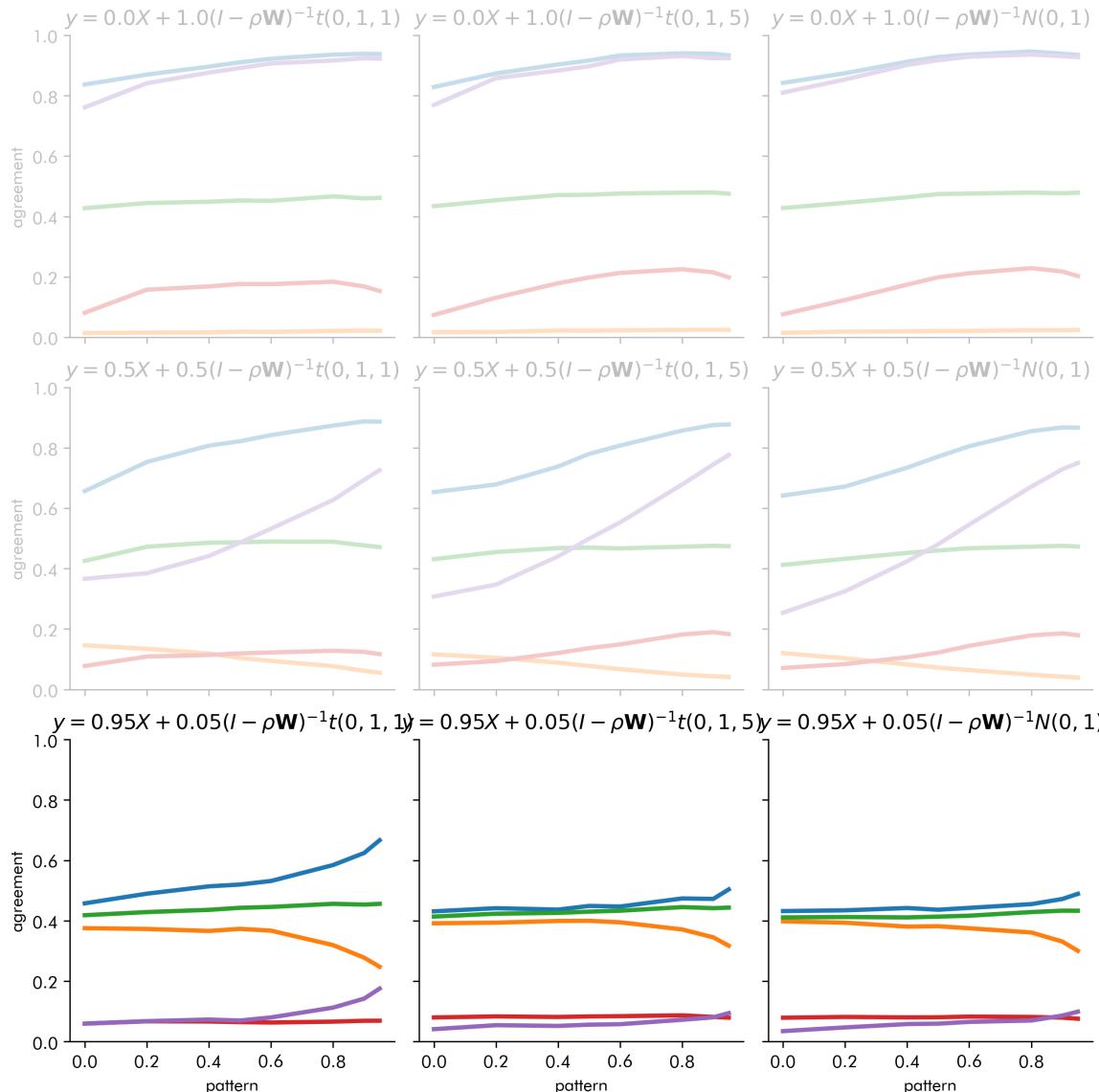
# SURPRISE! SIMULATION RESULTS FIRST!



- Increasing SD right within facets
- Increasing “agreement” w/ aux. reg. moving up within facets
- Thinner tails moving right over facets
- Increasing confounding moving down over facets

**WHEN  $x$  IS IRRELEVANT,**  
 (P)LMo both correctly ignore  $x$   
 Pairwise stats incorrectly sensitive to  $x$

SURPRISE! SIMULATION RESULTS FIRST!



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**WHEN  $x$  IS IRRELEVANT,**

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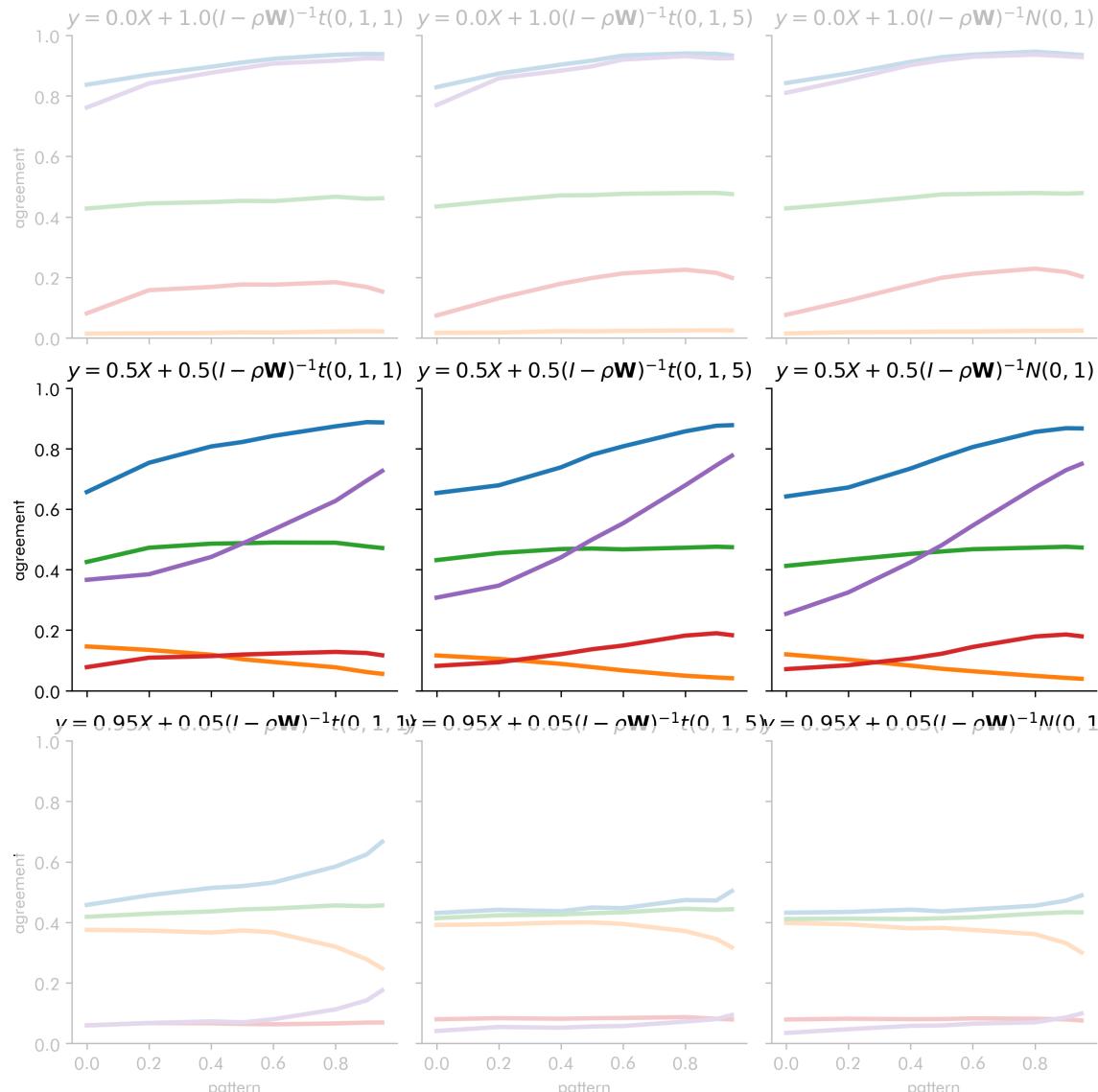
Pairwise stats incorrectly sensitive to  $x$

**WHEN MAINLY  $x$  MATTERS,**

Lee & PLMo disagree with full conditioning

Univariate approaches broadly agree

**SURPRISE! SIMULATION RESULTS FIRST!**



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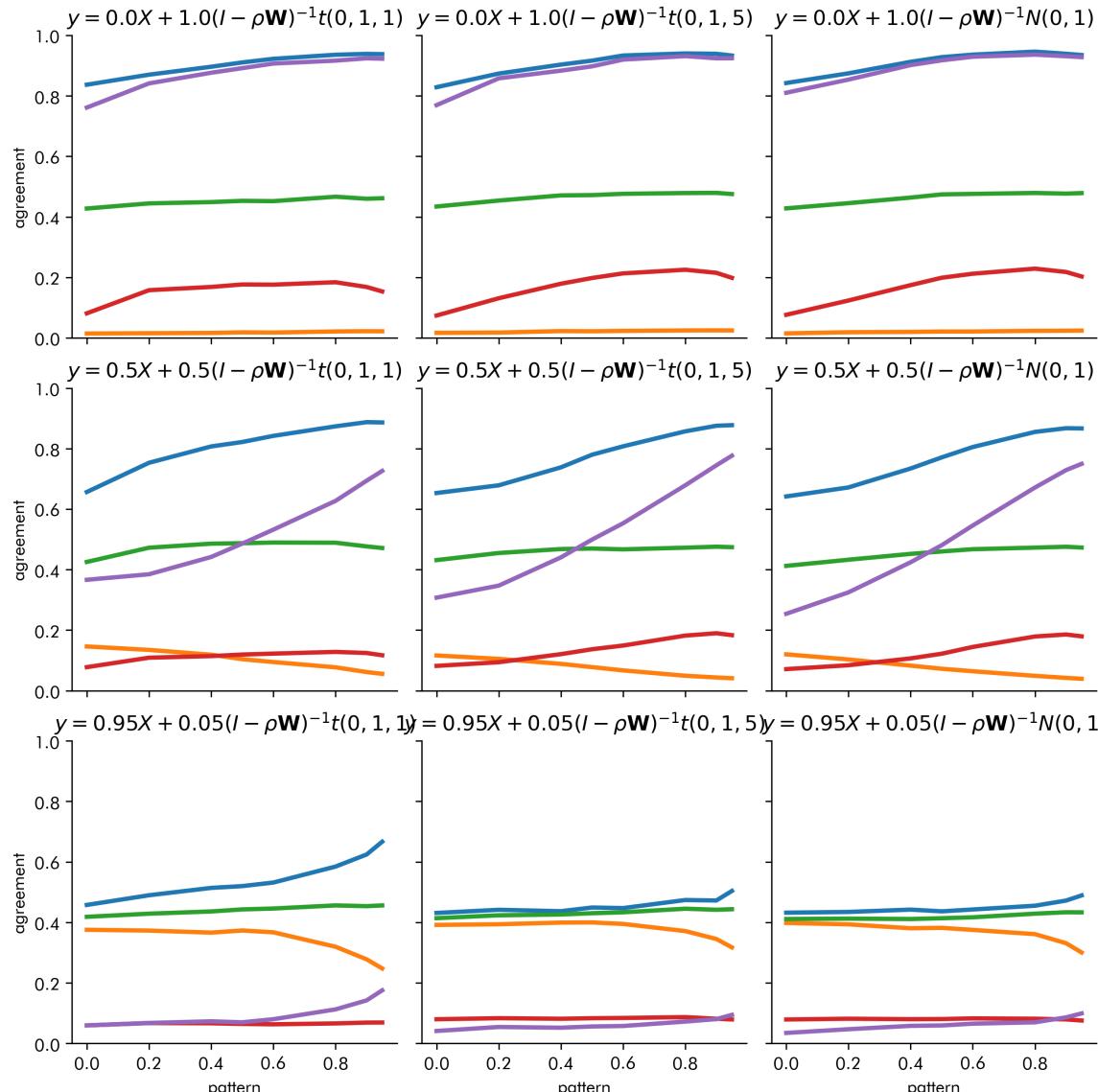
### WHEN BOTH MATTER

LMo<sub>x</sub> and Lee both problematic

BVLMo fails to recognize SD+

(P)LMo become more similar as SD+

**SURPRISE! SIMULATION RESULTS FIRST!**



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### **WHEN $x$ IS IRRELEVANT,**

stat  
 (P)LMo both correctly ignore  $x$   
 BVLMo  
 Pairwise stats incorrectly sensitive to  $x$   
 plmo

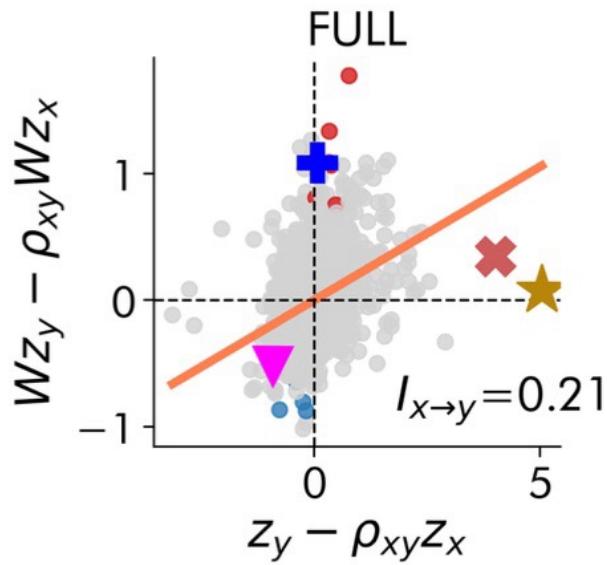
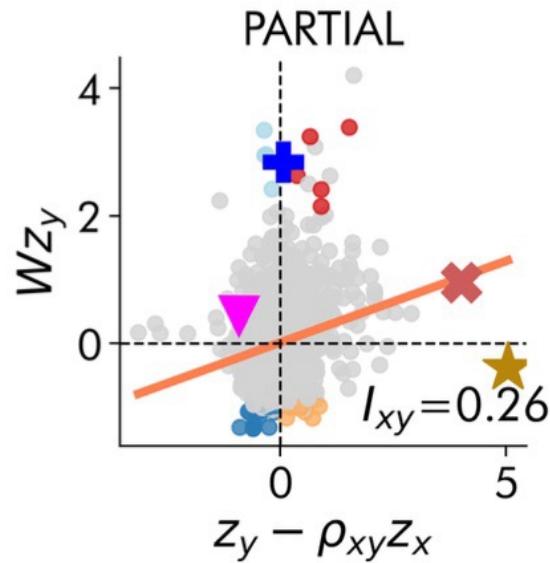
### **WHEN MAINLY $x$ MATTERS,**

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### **WHEN BOTH MATTER**

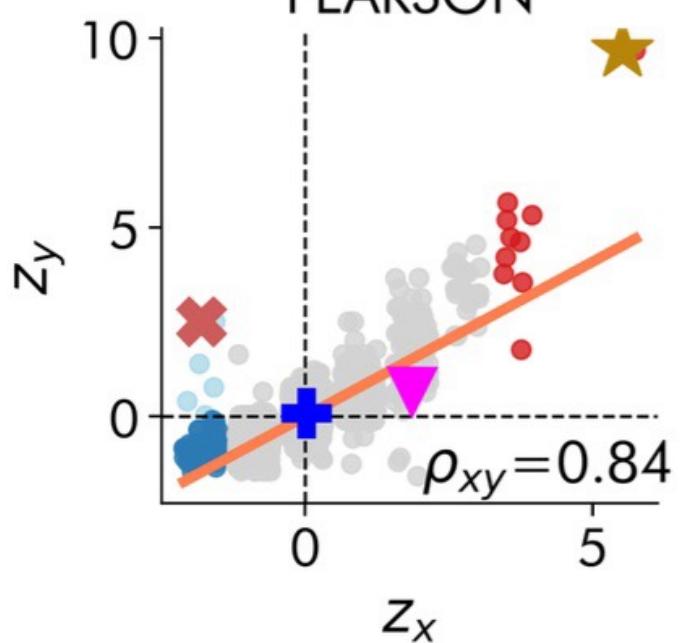
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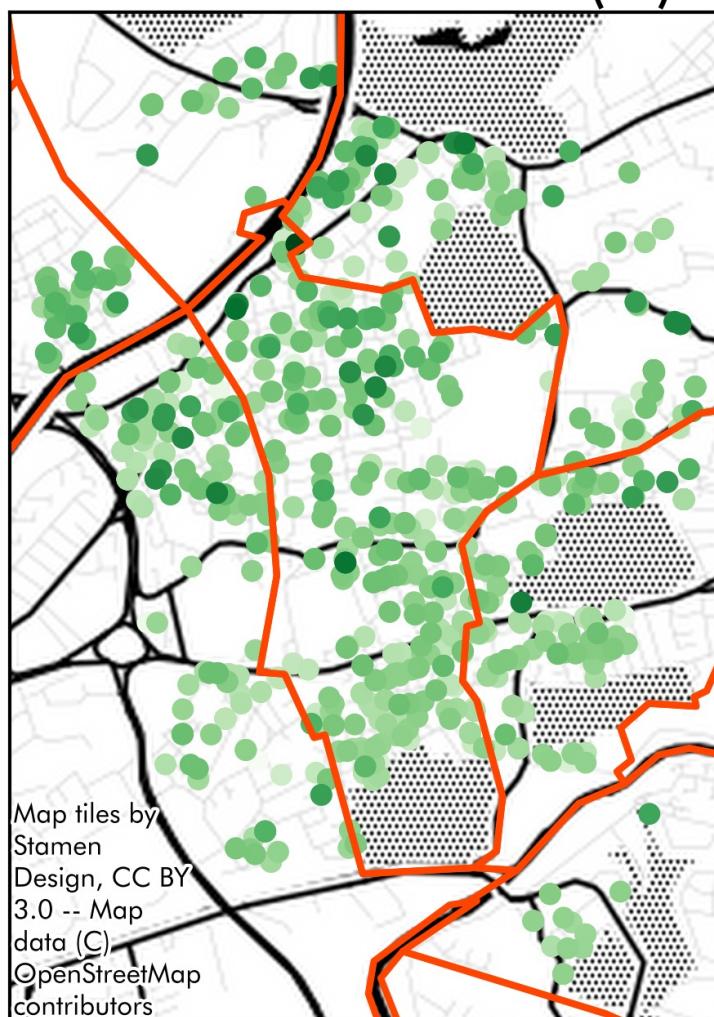


GOOD DEALS MAY NOT HAVE STRONG RELATIVE PREMIA

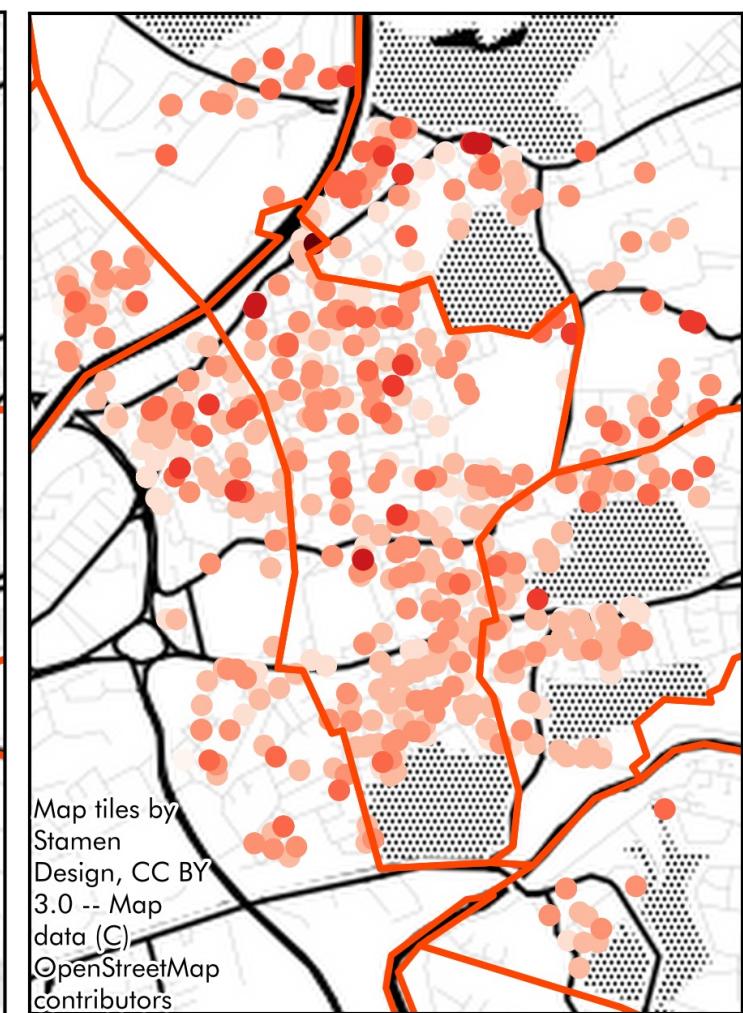
PEARSON



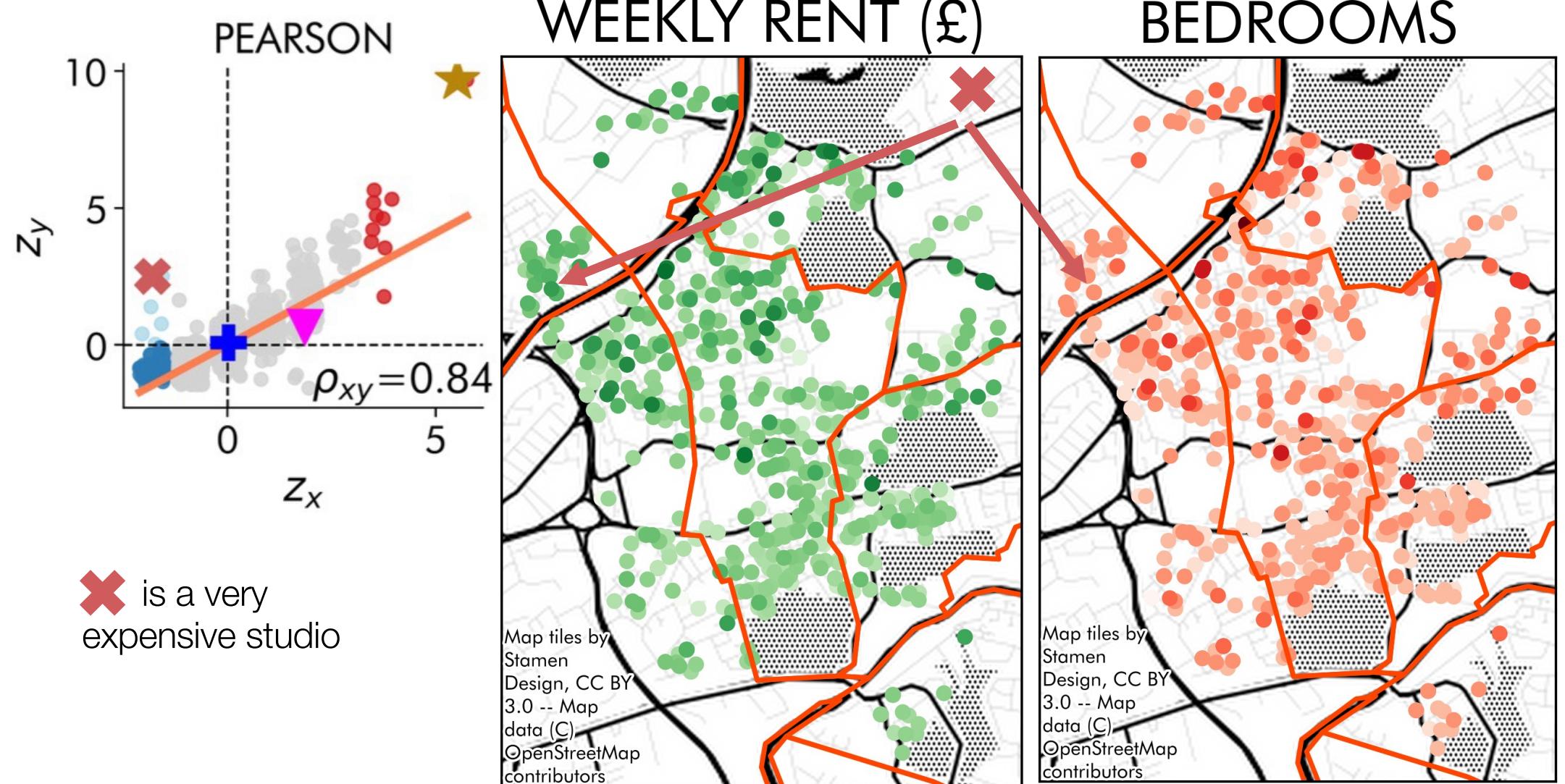
WEEKLY RENT (£)



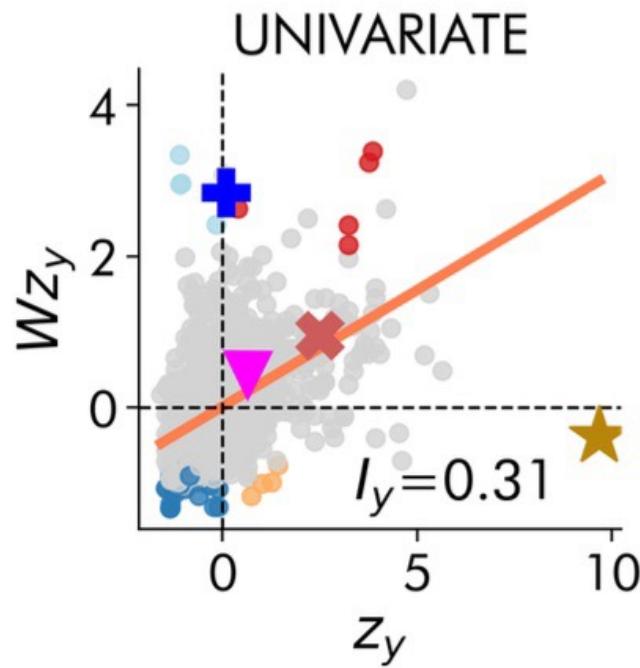
BEDROOMS



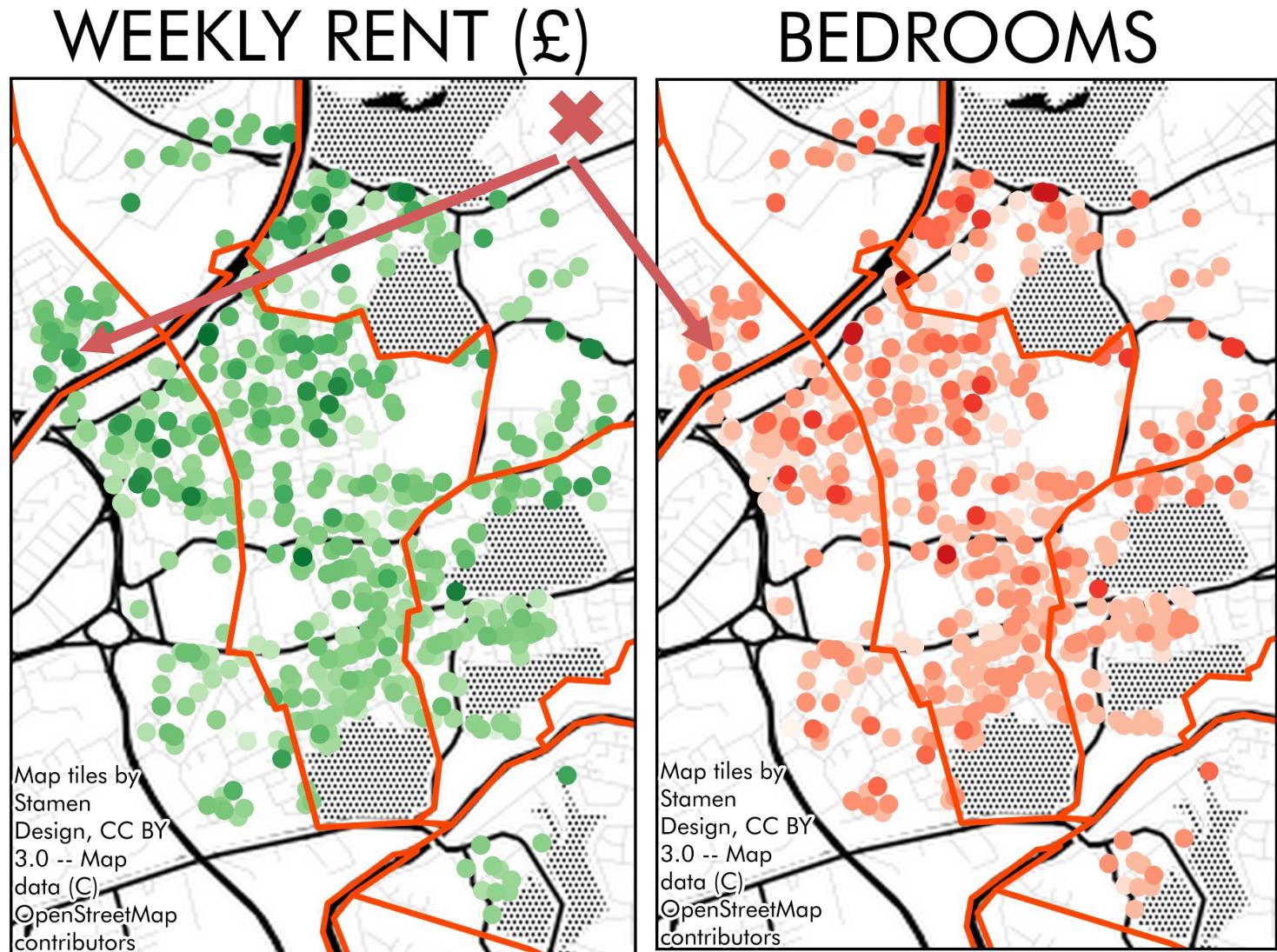
GOOD DEALS MAY NOT HAVE STRONG RELATIVE PREMIA



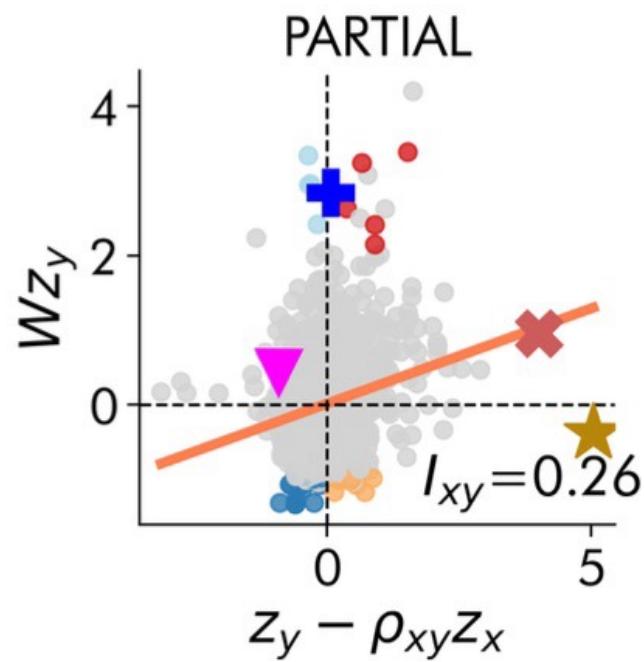
GOOD DEALS MAY NOT HAVE STRONG RELATIVE PREMIA



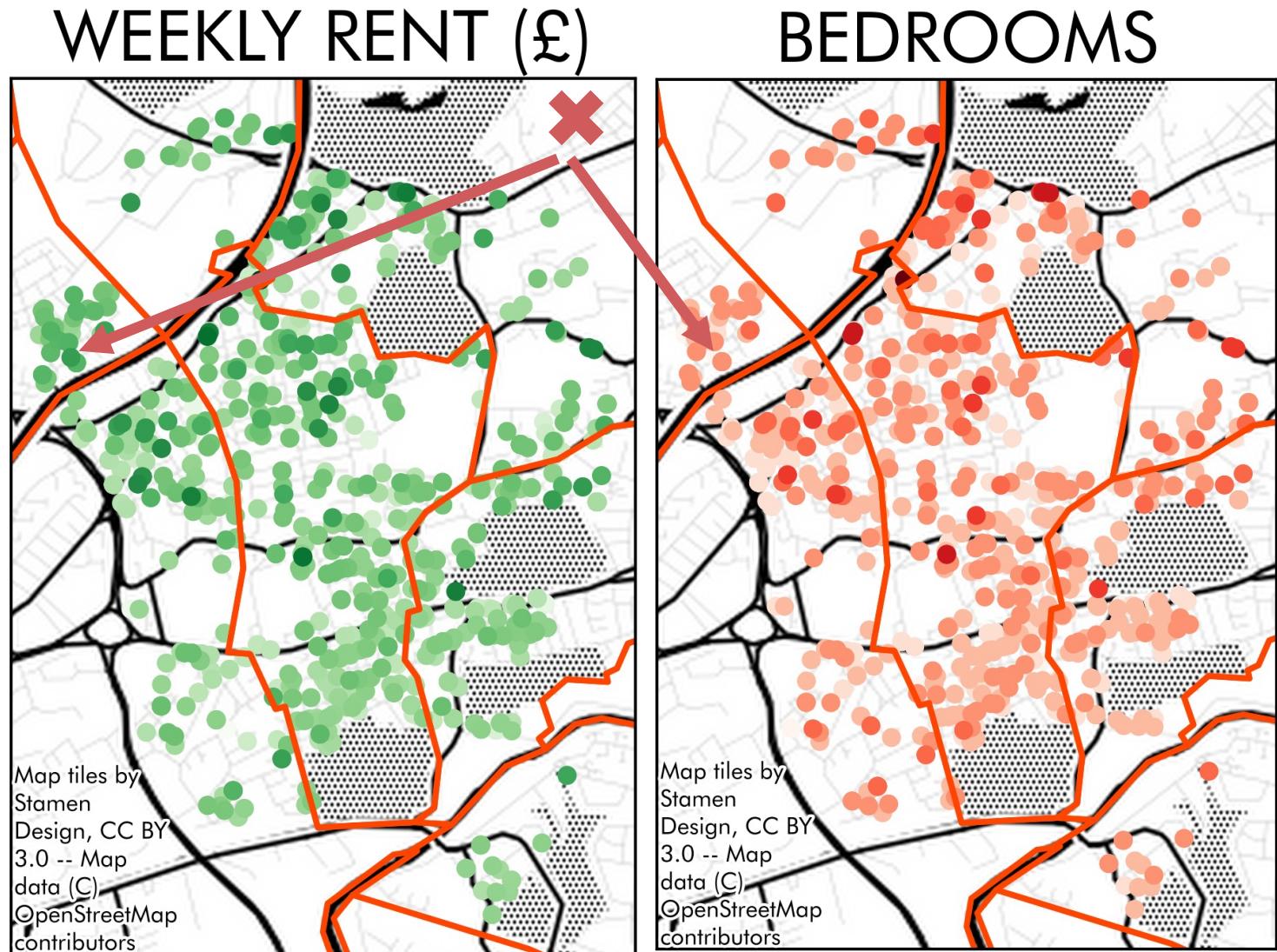
✖ is a very expensive studio, but it's not a rent outlier.



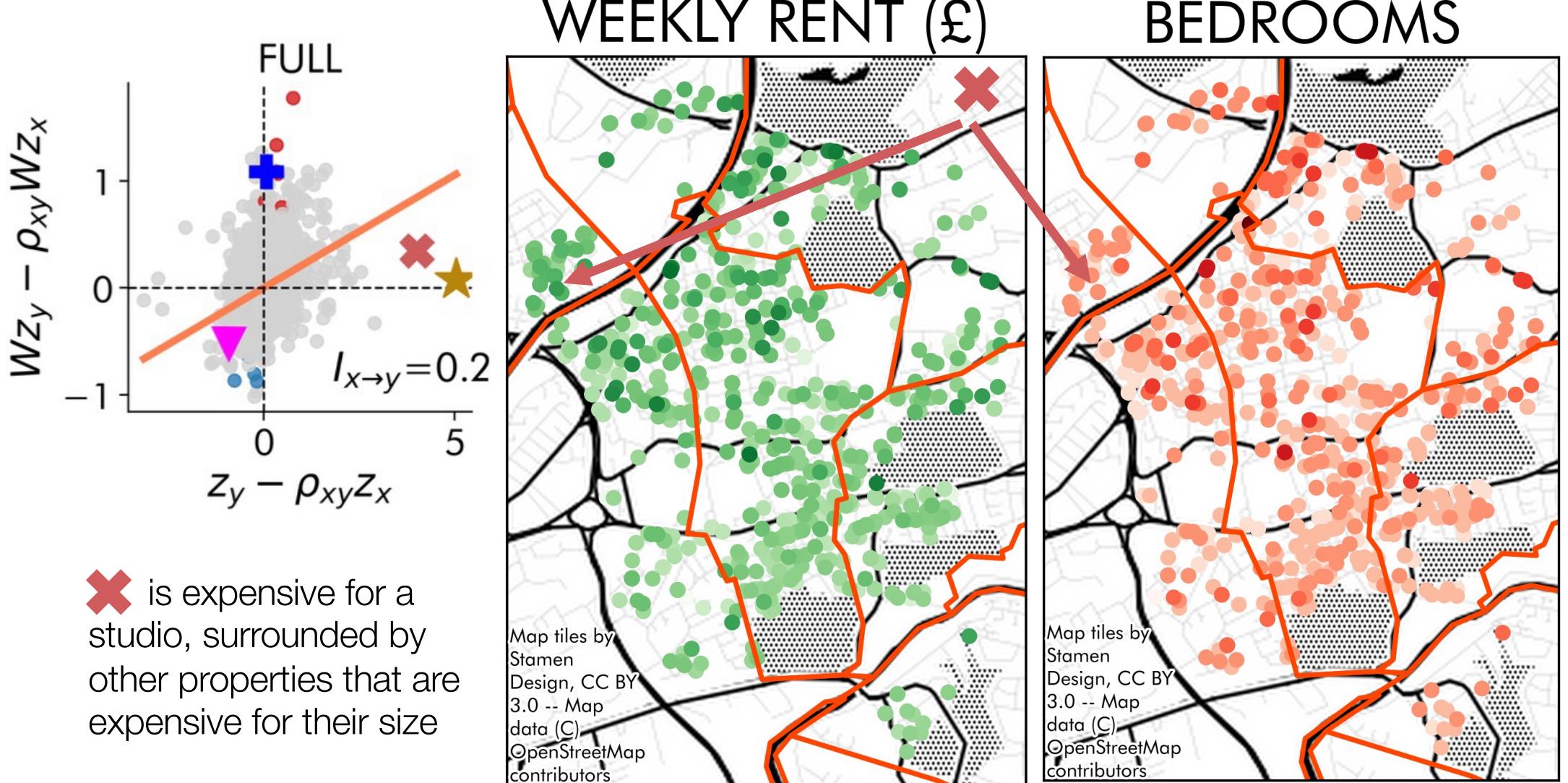
GOOD DEALS MAY NOT HAVE STRONG RELATIVE PREMIA



✗ is expensive for a studio, surrounded by expensive properties.



GOOD DEALS MAY NOT HAVE STRONG RELATIVE PREMIA



GOOD DEALS MAY NOT HAVE STRONG RELATIVE PREMIA

# LOCAL CONFOUNDING

*confounding is not stationary*

# PRIOR ART IN ESDA

*The Moran-Form Regression*

# PARTIAL CONDITIONING

*Two approaches to "control"*

# AFFORDABILITY OUTLIERS

*Where are the good deals?*

# PARTIAL LOCAL MORAN

HANDLING LOCAL CONFOUNDING

LEVI JOHN WOLF

UNIVERSITY OF BRISTOL

[levi.john.wolf@bristol.ac.uk](mailto:levi.john.wolf@bristol.ac.uk)

