3. $EX_n = \sum_{k=1}^{N} d_k \sqrt{2} E \cos(d_k n - U_k) = 0$, $Y(n+1, n) = EY = X - E(\frac{N}{N}) \sqrt{2} \cos(d_k n - U_k) = 0$

 $Y_{X}(n+\tau,n) = EX_{n+\tau}X_n = E\left[\frac{N}{k=1}d_k\sqrt{2}\cos(d_k(n+\tau)-U_k)\right]\left[\frac{N}{k=1}d_k\sqrt{2}\cos(d_kn-U_k)\right]$ $=\sum_{k=1}^{N}2d_k^2E\cos(d_k(n+\tau)-U_k)\cos(d_kn-U_k)\frac{33.44}{2n_k^2}\sum_{k=1}^{N}d_k^2E\cos d_k\tau = \sum_{k=1}^{N}d_k^2\cos d_k\tau = R(\tau), (\tau \in \mathbf{Z})$ to $\{X_n, n \in \mathbf{Z}\}$ 为年程。

6. 因为{X(t)}为平巷, 故 Var(X(t))=E(X(t)-m)=5 (常数), 以前:
0=(E(X(t)-m))/_t=E2(X(t)-m)X(t)=2cov(X(t),X(t)), ? X(t).5X(t)2.相差。

7. (i) 分見(X(t)) る事経。 EZ(t) W(t) 毛X(t+1) X(t-1)=R_X(2)=4e⁻⁴, E(Z(t)+W(t))=2R_X(2)+2R_X(2) (ii) $f_{\underline{z}}(s) = \frac{1}{2\sqrt{m}} \exp(-s^{2}/8)$. か Z(t) ~ N(o, 4), P(Z(t)<1)=更(o,5); (iii) (Z(t), W(t)) ~ N(o, 0, 4, 4, e⁻⁴), TR という3± $f_{\underline{z}}$ 以(3.w)。

8.证明:无妨没的有了她的取信者: a, a, ….a, 则.

 $P\{Y(e,+h) \leq x_1, \dots, Y(e,+h) \leq x_k\} = P\{X(e,+h-\epsilon) \leq x_1, \dots, X(e,+h-\epsilon) \leq x_k\}$

 $= \sum_{k=1}^{n} P\{\mathcal{E}=a_i\} P\{X(\mathbf{x}_i+h-\mathbf{E}) \leq x_i, \dots, X(\mathbf{x}_k+h-\mathbf{E}) \leq x_k | \mathcal{E}=a_i\}$

 $= \sum_{i=1}^{h} P\{\varepsilon = \alpha_i\} P\{\chi(\varepsilon_i - \alpha_i + h) \leq \chi_i, \dots, \chi(\varepsilon_k - \alpha_i + h) \leq \chi_k | \varepsilon = \alpha_i\}$

= $\sum_{i=1}^{n} P\{E=a_i\} P\{X(t_i-a_i) \leq x_i, \dots, X(t_k-a_i) \leq x_k | E=a_i\}$

= PEX(e-E) < x1, ... X(4-E) < x2 = PEX(e,) < x1, ... Y(e) < x2 (keN) + (keN)

11. 图{X(t)} 为Gauss过程, 级(X(t) + X(t))/At 肠从还充布, 根据有关经达可 安见 lim (X(t) + X(t))/At = X(t) 新服从还充分布。又图为{X(t)}年程, 别根据 由方至函数性发生可知{X(t)}并平稳且有: EX(t)=0, Var(X(t))=-Rx(v). 从而《事 例: X(t)~N(o, 以(o))进而容易并得: P{X(t) < a}=更(a/厌心)。

14: izif主 注(Xn. neZ} 均位有益的 4号并元 XN = 1 N Xk 別有: (12 N RCC))2=(11 N COV (X-N, Xk))2=(COV (X-N, XN))2ift Var(X-N) Var(XN)

 $=R(0)E(X_{N}-m)^{2} \rightarrow 0. (N\rightarrow +\infty)$ $=R(0)E(X_{N}-m)^{2} \rightarrow 0. (N\rightarrow +\infty)$ $=\lim_{N\rightarrow +\infty} \frac{1}{2N+1} \sum_{k=0}^{2N} R(x) = 0, \text{ if } C(x) = 0, \text{ if } C(x) = 0. \text{i$

其中AN显然差更而BN则有 $|B_N| = \left|\frac{1}{(2N+1)^2} \sum_{0 \le j < i \le 2N} R(i-j)\right| = \left|\frac{2N}{(2N+1)^2} \sum_{T=1}^{2N} (2N+1-T)R(T)\right|$ $= \left| \frac{1}{(2N+1)^2} \left[2N \times R(1) + (2N+1) \times R(2) + \dots + [\times R(2N)] \right] = \left| \frac{1}{(2N+1)^2} \left[\sum_{\tau=1}^{2N} R(\tau) + \sum_{\tau=1}^{2N-1} R(\tau) + \dots + R(1) \right] \right|$ $\leq \frac{1}{2N+1} \left(\frac{|ku\rangle l}{l} + \frac{|\vec{l}|^{2}R(x)|}{2} + \dots + \frac{|\vec{l}|^{2}R(x)|}{2N} \right) \longrightarrow 0. (N \to +\infty) \left(\frac{|\vec{l}|^{2}}{2} + \frac{3}{2} \right) \left(\frac{|\vec{l}|^{2}}{2} + \frac{3}{2} \right$ 人人面由《文文》是可表。. fim E(Xv-m)2=0, 即均性病历性对意。# 15.记明建设4.3:对于国建的TeZ,论XntcXn=Kn,则EKn=K(记)(常数),且可证 明{1/13的曲方差级与时间差有关(名后),即1={1/11.11至}为年税行到。又易名 X={Xn,neZ}的的方案五数温历性或至的克曼会中是Y={Kn,neZ}的均定 温历性难。而接起目提市政价有: $R_{y}(\tau_{i}) = E Y_{n+\tau_{i}} Y_{n} - R_{x}^{2}(\tau) = E Y_{n+\tau_{i}} + \tau X_{n+\tau_{i}} Y_{n+\tau_{i}} X_{n} - R_{x}^{2}(\tau)$ = $R_{X}^{2}(T_{1}) + R_{X}^{2}(T_{1}) + R_{X}(T_{1} + T_{1})R_{X}(T_{1} - T_{1}) - R_{X}^{2}(T_{1}) + R_{X}(T_{1} + T_{1})R_{X}(T_{1} - T_{1}) + R_{X}(T_{1} -$ 由此可知: | R(は) | < R(は)+ (R(は,+も)+ R(は,-も))/2, 放曲途程所给委件等到: $\left|\frac{1}{N}\sum_{t=0}^{N-1}R_{\lambda}(t_{i})\right|\leq\frac{1}{N}\sum_{t=0}^{N-1}\left|R_{\lambda}(t_{i})\right|\leq\frac{1}{N}\sum_{t=0}^{N-1}\left|R_{\lambda}^{2}(t_{i})+\left(R_{\lambda}^{2}(t_{i}+t)+R_{\lambda}^{2}(t_{i}-t)\right)/2\right|\rightarrow0,\ (N\rightarrow+\infty)$ 国的重强4.1的(i)可知, Y={Kn, neZ}的均能高历性对差,并对X={Kn, neZ} 的物方是主教;高历性对益。这样。 16.发52~{\Xn, n20}为再趋序刻: EXO=5/2x2dx = 2/3 13EXn=2/3, 21EXn+1=E[E(Xn+1/Xo,...Xn)]=E(1-Xn/2)=1-\frac{1}{2}x\frac{2}{3}=2/3

16. \$\frac{2}{2}\text{\left{\lambda}}\left{\lambda}\right{\frac{1}{2}}.

\[
\text{EX_0 = \int_0'2\text{2}'d\times = 2/3} \text{\lambda}\text{\left{\right{\

21:
$$S(\omega) = \int_{-\infty}^{\infty} e^{\frac{1}{2}t} \frac{dt}{dt} dt = \int_{-\infty}^{\infty} e^{\frac{1}{2}t} \frac{dt}{dt} - \int_{-\infty}^{\infty} e^{\frac{1}{2}t} \frac{dt}{dt} = \int_{-\infty}^{\infty} e^{\frac{1}{2}t} \frac{dt}{dt} \frac{dt}{dt} \frac{dt}{dt} = \int_{-\infty}^{\infty} e^{\frac{1}{2}t} \frac{dt}{dt} \frac{dt}{dt} \frac{dt}{dt} \frac{dt}{dt} = \int_{-\infty}^{\infty} e^{\frac{1}{2}t} \frac{dt}{dt} \frac{dt}{dt} \frac{dt}{dt} \frac{dt}{dt} = \int_{-\infty}^{\infty} e^{\frac{1}{2}t} \frac{dt}{dt} \frac{dt$$

31.j是{Xn,neZ}的给危的,物强的风口),

(1)沒分*=aXn为Xnn的前往预报,完用报报影道强老角:E(Xnn-分*)bXn= = bE(Xn+1 Xn-aXn2)=0. (Y be IR) 7/3/2 b + 0.2/1. R(1)-aR(0)=0, = a= R(1)

(3) X(2)的约方没差级的,且有:

(4)

$$a = \frac{R(o)R(k) - R(N-k)R(N)}{R^{2}(o) - R^{2}(N)}, b = \frac{R(o)R(N-k) - R(k)R(N)}{R^{2}(o) - R^{2}(N)};$$

$$(b) a = b = \frac{\sum_{k=0}^{N} R(k)}{R(o) + R(N)}.$$

26. 叙记注: 若dsw) 鱼s~w)为诸密從函数,则s~w)为人心的s~x)为 单调增。

又5(60)60不可能21任(306股对之(公到560)为单洲减),故处行生的6股 (彭鲁5似)=0>0,从而多心,心的,5心)不及,故而有:

$$\int_{\omega_0}^{\omega} S(t) dt / a(\omega - \omega_0), \text{ fill } S(\omega) > S(\omega_0) + a(\omega - \omega_0)$$

显然这样的SW)在R上是不可较的,矛盾。

$$S(\omega) \stackrel{(437)}{=} \delta^{2}(\alpha, \alpha+2\alpha, \omega + 1).$$

$$(2) EX_{n} = 0, Y_{x}(n+C, n) = \delta^{2} \sum_{k=0}^{\infty} \beta_{k} \beta_{k+|C|} = R(T)$$

$$S(\omega) = \sum_{k=0}^{\infty} \sum_{k=0}^{$$