

The program is written to handle the N-queen problem using RNN. But the energy function needs to change according to N. Click “save” bottom to save the result.

The energy function of the Four Queen Problem:

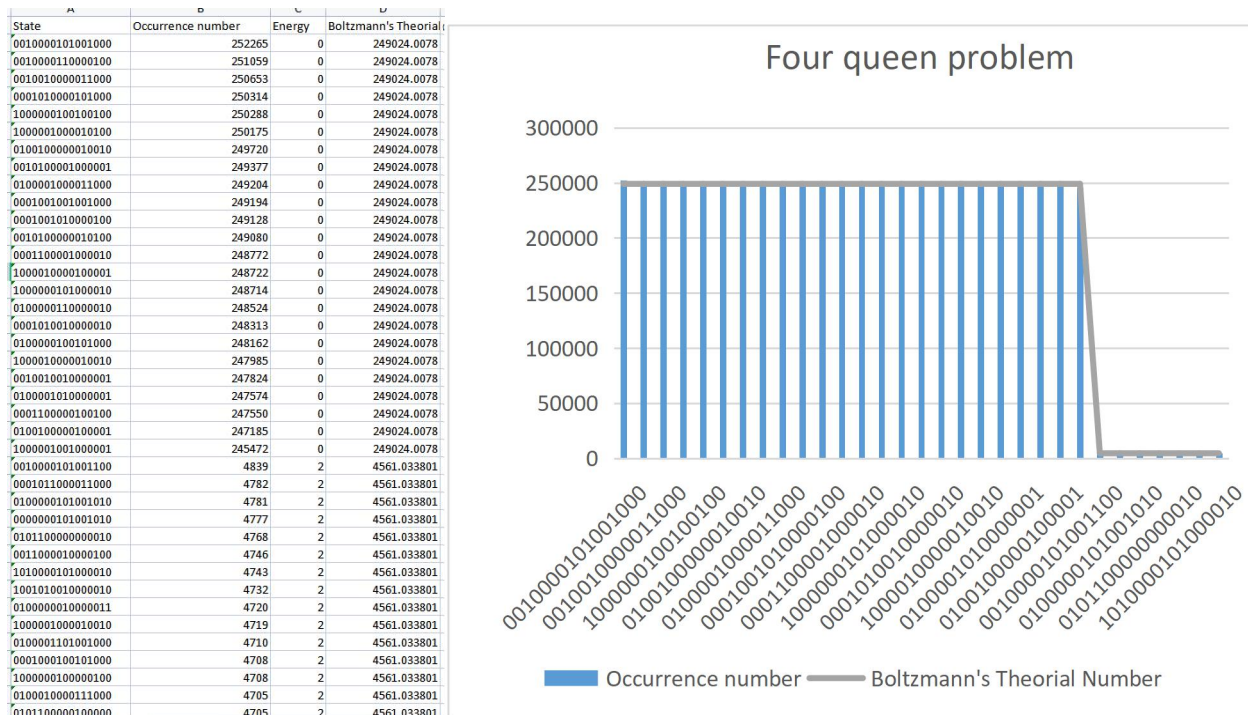
$$E(x_{ij}) = \sum_{i=1}^4 \left(\sum_{j=1}^4 x_{ij} - 1 \right)^2 + \sum_{j=1}^4 \left(\sum_{i=1}^4 x_{ij} - 1 \right)^2$$

There are 16 positions on the chessboard, and each position is set with a neuron ($x_{11} \sim x_{44}$). There are 17 neurons in total, including a dummy neuron (x_{00}).

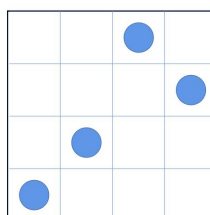
The calculated weights are:

	x00	x11	x12	x13	x14	x21	x22	x23	x24	x31	x32	x33	x34	x41	x42	x43	x44
x00	0	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2
x11	2	0	-2	-2	-2	-2	0	0	0	-2	0	0	0	-2	0	0	0
x12	2	-2	0	-2	-2	0	-2	0	0	0	-2	0	0	0	-2	0	0
x13	2	-2	-2	0	-2	0	0	-2	0	0	0	-2	0	0	0	-2	0
x14	2	-2	-2	-2	0	0	0	0	-2	0	0	0	-2	0	0	0	-2
x21	2	-2	0	0	0	0	-2	-2	-2	-2	0	0	0	-2	0	0	0
x22	2	0	-2	0	0	-2	0	-2	-2	0	-2	0	0	0	-2	0	0
x23	2	0	0	-2	0	-2	-2	0	-2	0	0	-2	0	0	0	-2	0
x24	2	0	0	0	-2	-2	-2	-2	0	0	0	0	-2	0	0	0	-2
x31	2	-2	0	0	0	-2	0	0	0	0	-2	-2	-2	-2	0	0	0
x32	2	0	-2	0	0	0	-2	0	0	-2	0	-2	-2	0	-2	0	0
x33	2	0	0	-2	0	0	0	-2	0	-2	-2	0	-2	0	0	-2	0
x34	2	0	0	0	-2	0	0	0	-2	-2	-2	-2	0	0	0	0	-2
x41	2	-2	0	0	0	-2	0	0	0	-2	0	0	0	0	-2	-2	-2
x42	2	0	-2	0	0	0	-2	0	0	0	-2	0	0	-2	0	-2	-2
x43	2	0	0	-2	0	0	0	-2	0	0	0	-2	0	-2	-2	0	-2
x44	2	0	0	0	-2	0	0	0	-2	0	0	0	-2	-2	-2	-2	0

In one cycle, 16 neurons are updated. Then 1000000 updates of cycles are repeated. The result is shown in the table.



We can see from the table and figure. The number of occurrences is very close to the calculated Boltzmann's theoretical number. There are 24 states that their energy is 0, which means it's the solution to the problem. The state “0010000101001000” means:



The energy function of 8 Queen Problem should be:

The calculated weights are shown in the table(stored in 8QueenWeight.xlsx):

[illegible]