# RHMC Code Documentation

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## 1 Introduction

A simple RHMC code to simulate  $n_f$  flavors of unimproved staggered fermions with the Wilson SU(3) gauge action.

## 2 QCD formulation

### 2.1 Gauge Action

Wilson SU(3) plaquette lattice gauge action,

$$S_g[U] = -\frac{\beta}{3} \sum_{x} \sum_{\mu < \nu} Re \operatorname{Tr} \left[ U_{\mu}(x) U_{\nu}(x + \hat{\mu}) U_{\mu}^{\dagger}(x + \hat{\nu}) U_{\nu}^{\dagger}(x) \right]$$
 (2.1)

where  $U_{\mu}(x)$  is a 3x3 complex matrix at the site x in the direction  $\mu$ .

#### 2.2 Fermion Action

$$S_f[U] = \phi^{\dagger} (DD^{\dagger})^{-2} \phi \tag{2.2}$$

where D is the staggered lattice Dirac operator

$$D_{nm} = \sum_{\mu} \eta_{\mu}(x) \left( U_{\mu}(x) \delta_{nm} \right) \tag{2.3}$$

and  $\eta_{\mu}(x)$  are the space-dependent staggered equivalent of Dirac  $\gamma$ -matrices,

$$\eta_0(x) = 1, etc \tag{2.4}$$

## 3 HMC

The action simulated by the HMC is

- 3.1 Momenta
- 3.2 Gauge Force
- 3.3 Fermion Force
- 4 Inverters
- 4.1 CG
- 4.2 CG-Multishift
- 4.3 CG-Block