

# Learning Pupilometry From Theory to Analyses

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# Agenda

## Day 1: Theory & Experimental Design

What is pupillometry? What can pupil size tell us?

Why and how do we measure pupil size?

Experimental design considerations

e.g., potential confounds, simulating pupil data, pre-existing datasets

## Day 2: Pre-processing & Analyses

Hands-on coding workshop covering a variety of potentially useful analyses, from condition-averaging the pupil dilation response, to analyzing the dynamics of single-trial pupil time series.

# Agenda

## Day 1: Theory & Experimental Design

What is pupillometry?

What is the pupil?

Why does the pupil appear black?

What are the neural underpinnings of pupil changes?

Why does the pupil change size?

What are the visual and cognitive functions of changes in pupil size?

How fast can the pupil move?

How long does the pupil take to respond?

Is the pupil subject to voluntary control?

How do we measure pupil size?

Experimental design considerations

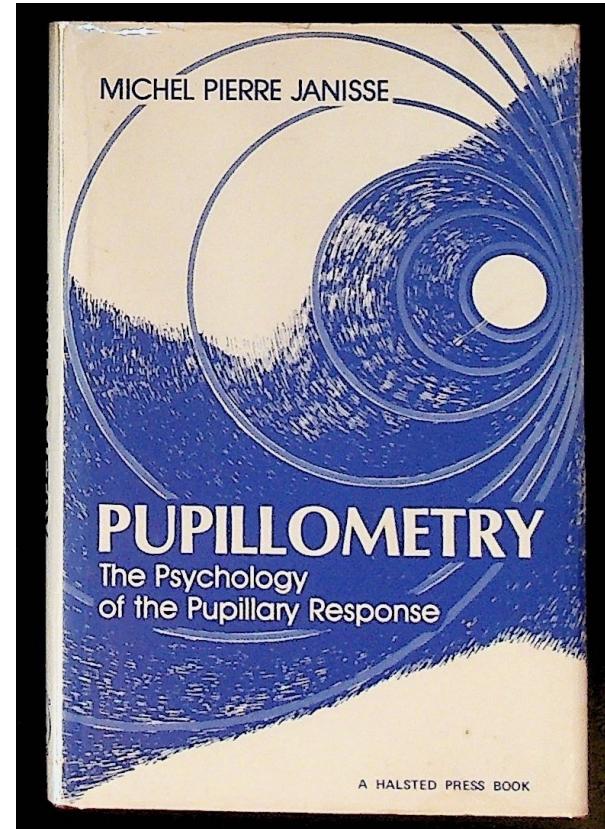
# What is pupillometry?

**Generally**, pupillometry refers to the measurement of the pupil(s), or the study of the pupil(s)

**Within experimental psychology**, pupillometry has come to be associated with measuring attention and/or cognitive effort

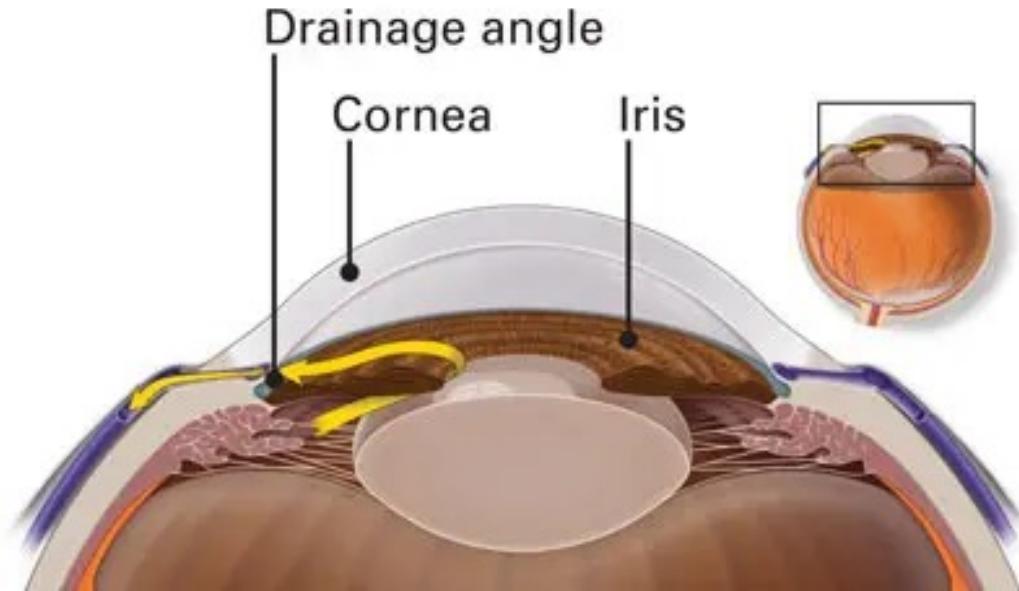
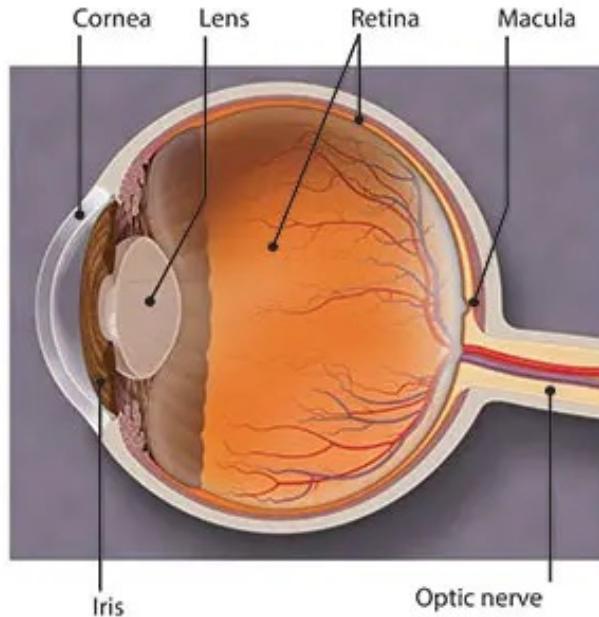
*“[. . .] has more advantages than disadvantages than most other dependent measures of behaviour”*

- Janisse, *Pupillometry*



# What is the pupil?

Hole in center of iris!



<https://www.aao.org/eye-health/anatomy/parts-of-eye>

# Why does the pupil appear as a black hole?



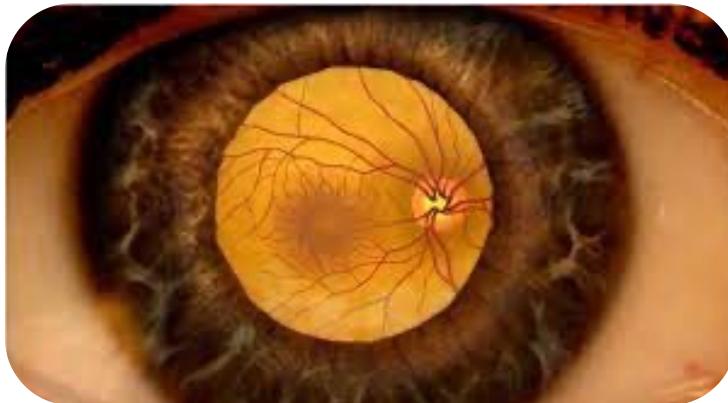
<https://www.ifa.hawaii.edu/2023/02/first-observational-evidence-linking-black-holes-to-dark-energy/>

## Why does the pupil appear as a black hole?

Light entering eye is absorbed by tissues in the eye (e.g., retina)



Dilated eye exam



<https://www.youtube.com/watch?v=M6IIOKXICqs>

Red eye in photos



[https://en.wikipedia.org/wiki/Red-eye\\_effect#/media/File:BoldRedEye.JPG](https://en.wikipedia.org/wiki/Red-eye_effect#/media/File:BoldRedEye.JPG)

# Iris muscles alter pupil appearance

Radial vs. circular muscles are innervated by:

Sympathetic

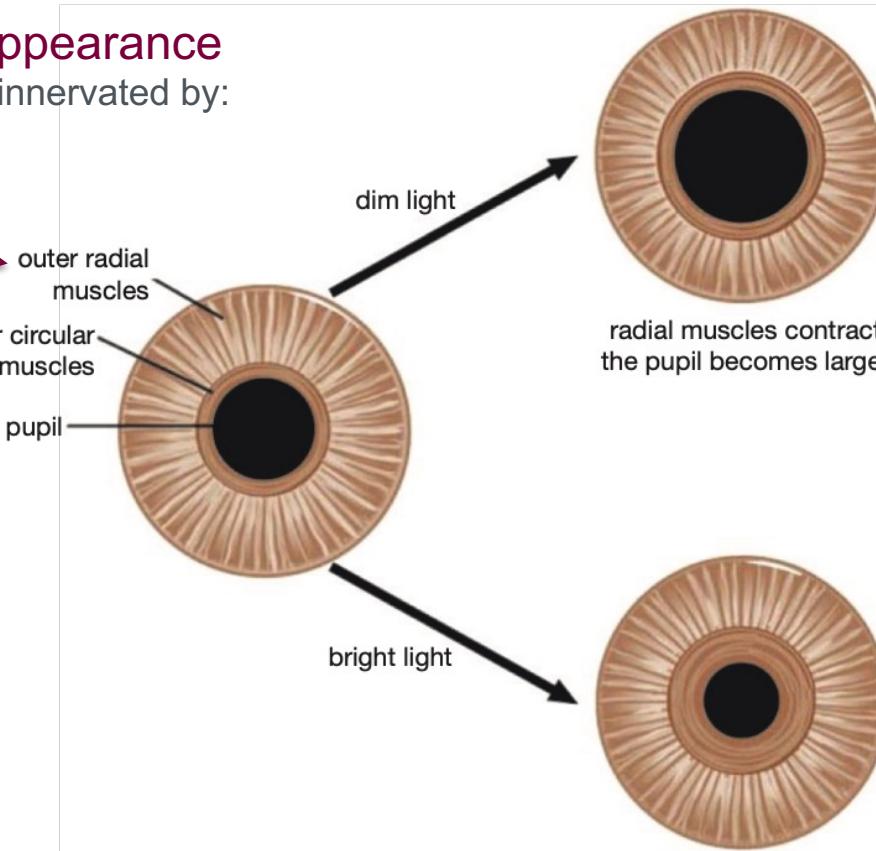
Nervous System

- superior cervical ganglion

Parasympathetic

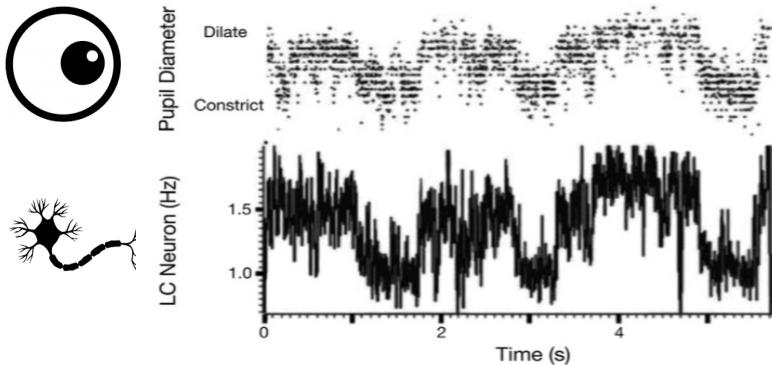
Nervous System

- Edinger-Westphal nucleus



BUT. Lots of interactions

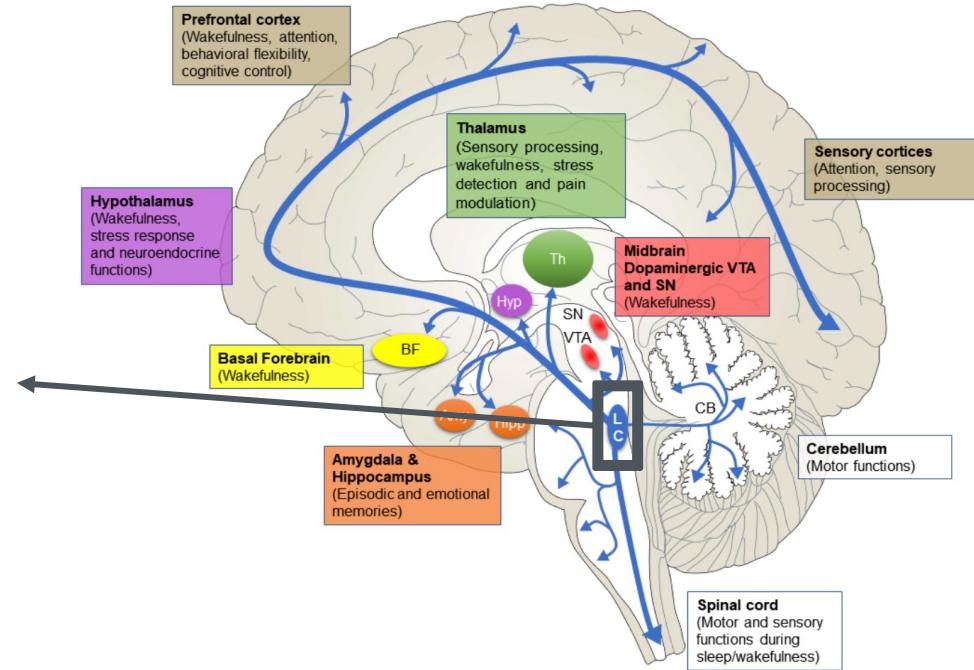
# The pupil as an index of Locus Coeruleus / Noradrenergic activity



(Rajkowska et al., 1993)

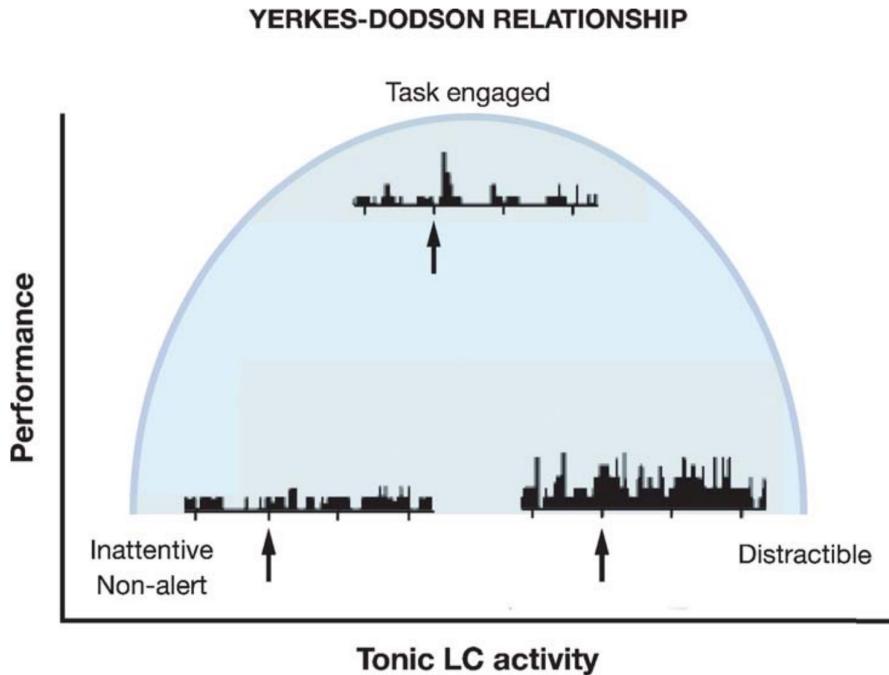
BUT. Lots of interactions

## Norepinephrine system

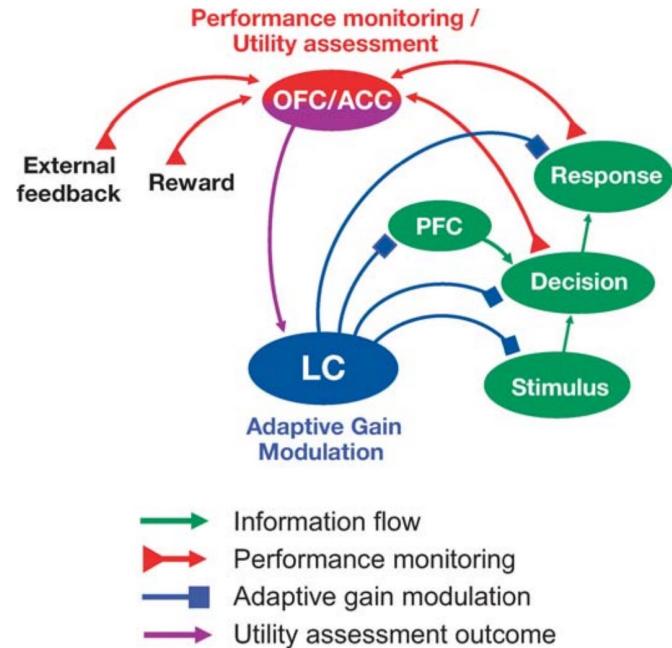


(Bari, Chokshi, Schmidt, 2020)

# LC-NA activity & Adaptive Gain Theory

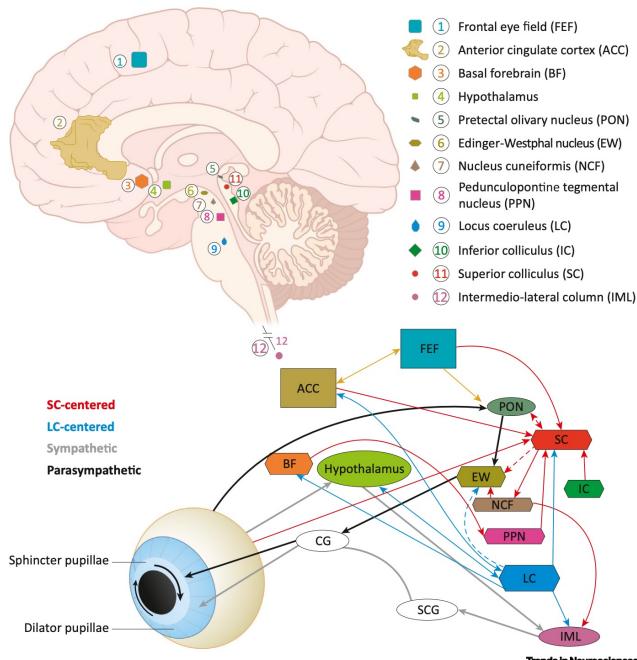


Aston-Jones & Cohen, 2005

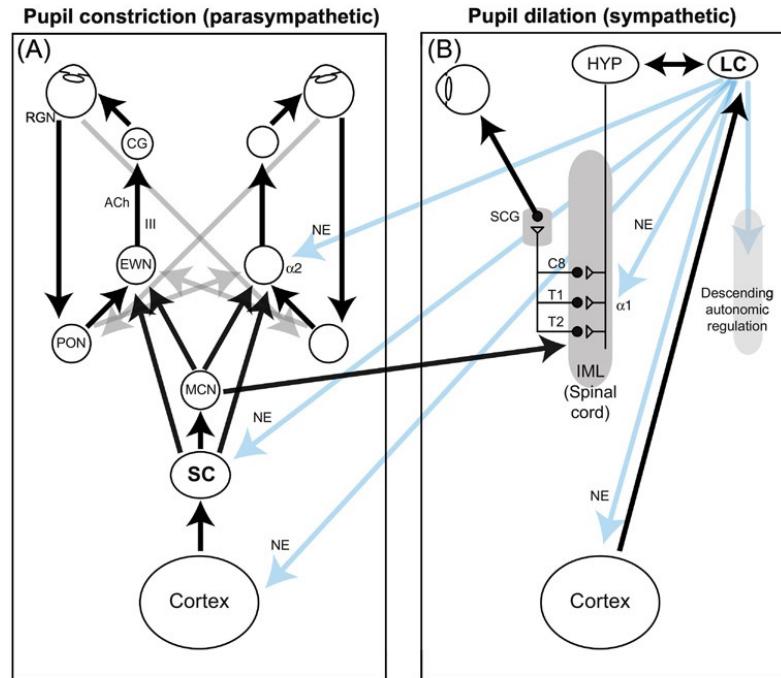


# Additional neuromodulatory and neuroanatomical influences on pupil size

**Cholinergic** (Reimer et al., 2016); **Serotonergic** (Schmid et al., 2015); **Dopaminergic** (de Gee et al., 2014)



Strauch et al., 2022



Joshi & Gold, 2020

Trends in Cognitive Sciences

# Why does the pupil change size?

## Many reasons!

One recently proposed taxonomy (Strauch et al., 2022):

### **Low level**

- Light level
- Focal distance

### **Intermediate level**

- Alerting & Orienting

### **High level**

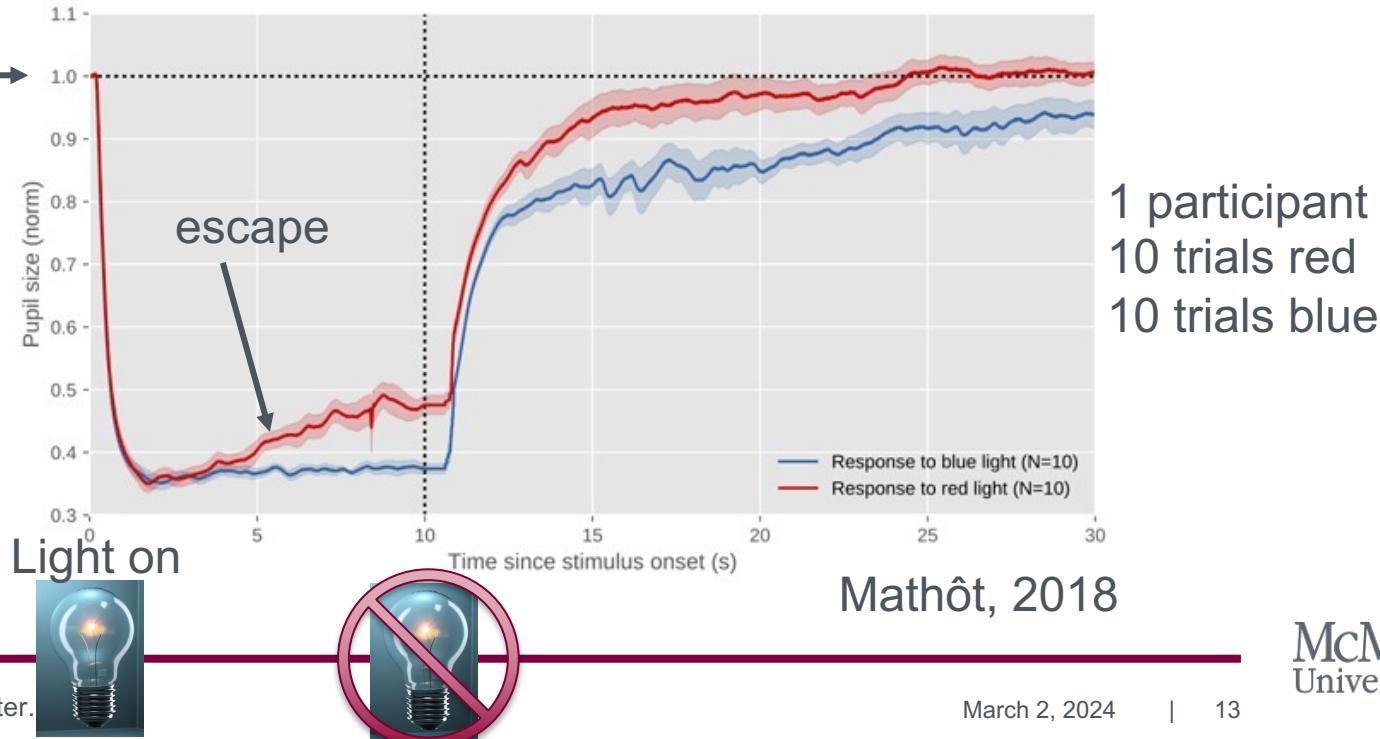
- Executive control

# Why does the pupil change size?

## Pupillary light reflex

- Constriction of pupil in response to light
  - Sequence: constriction to minimum, escape (or not), return to original size

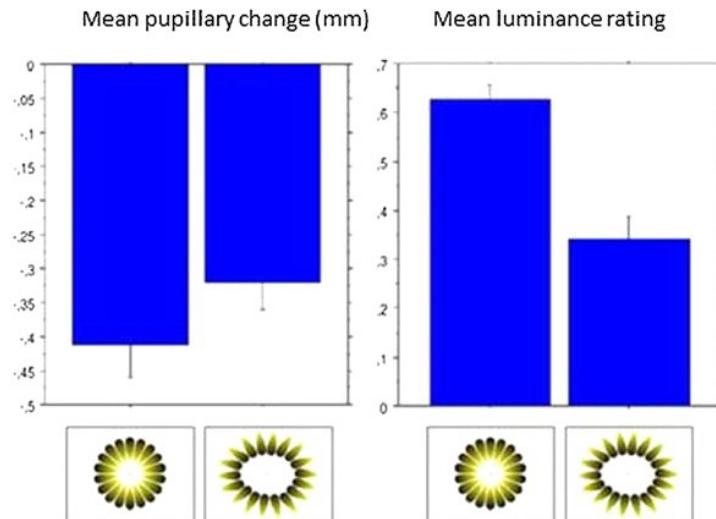
Baseline  
pupil size



# Why does the pupil change size?

## Pupillary light “reflex”

- Sensitive to top-down influences (e.g., attention, processing, interpretation)
  - **Perceived brightness**

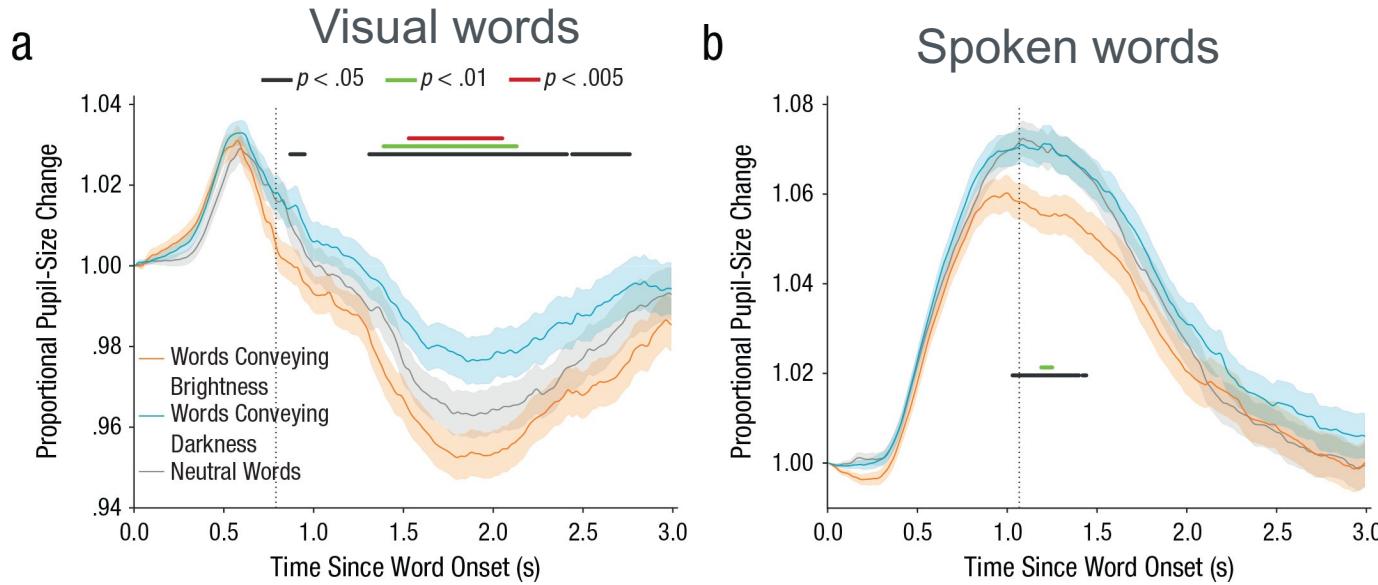


Laeng & Endestad, 2012

# Why does the pupil change size?

## Pupillary light “reflex”

- Sensitive to top-down influences (e.g., attention, processing, interpretation)
  - **Words conveying brightness**

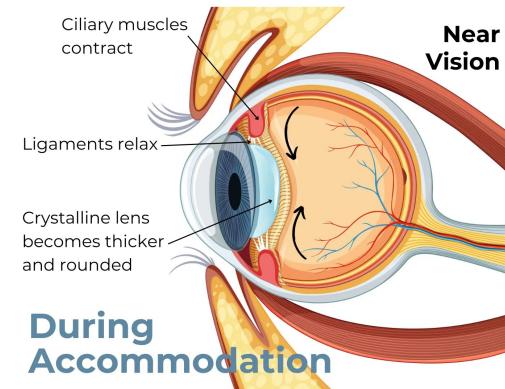
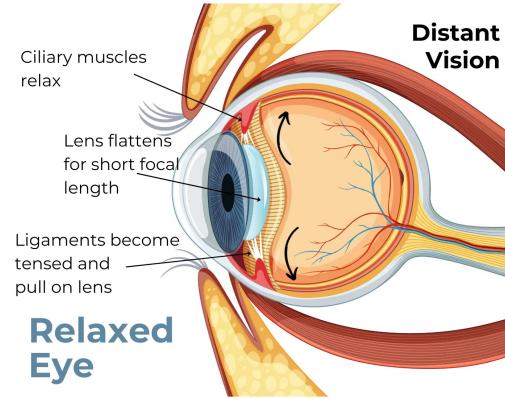


Mathôt et al., 2018

# Why does the pupil change size?

Learn about other pupillary reflexes here:  
[https://eyewiki.aao.org/Reflexes\\_and\\_the\\_Eye](https://eyewiki.aao.org/Reflexes_and_the_Eye)

- **Dark reflex:** dilation response to darkness
- **Ciliospinal reflex:** dilation response to noxious stimuli
- **Near accommodation:** constriction response when focusing on close objection



<https://www.accuvision.co.uk/glossary/accommodation/>

# What are the visual functions of changes in pupil size?

## Dilation

- Better visual detection in dim environments
  - See e.g., Franke et al., 2022
- Help with adaptation from bright to dark (when rods/cones still adapting slowly)

## Constriction

- Increase depth of field / visual sharpness (small pupil = small lens = less visual distortion)

# Why does the pupil change size?

## Cognitive or psychosensory reasons:

- Mental effort
- Attention
- Uncertainty, decision-making
- Surprise, salience, prediction error
- Sexual or emotional arousal
- Response preparation, motor activity
- Fatigue, time-on-task
- Imagined arousal, effort, brightness
- Memory, familiarity

Sometimes pre-conscious effects!

Learn more: <https://link.springer.com/article/10.3758/s13428-023-02098-1/tables/1>  
Fink et al., 2023

# Why does the pupil change size?

Cognitive process	Key papers	Key findings
Mental effort	Kahneman and Beatty (1966); Kahnemann and Beatty (1967); Johnson (1971); Kramer et al. (2013)	Pupil size sensitive to variations in effort (greater effort, greater pupil size)
Attention (general)	Kahneman (1973); Hoeks and Levelt (1993); Iriki et al. (1996); Smallwood et al. (2011); Wierda et al. (2012)	Pupil signal indexes changes in attention over time. Pupil time course can be modeled via attentional pulses. Pupil exhibits greater spontaneous fluctuation when attention is decoupled from task
Attention (spatial)	Mathôt et al. (2013); Binda et al. (2013); Naber et al. (2013a)	When focusing attention on a visual object (even covertly), the pupil adjusts to the objects' brightness
Uncertainty, decision-making	Friedman et al. (1973); Einhäuser et al. (2008); Jepma and Nieuwenhuis (2011); Laeng et al. (2012); de Gee et al. (2014); Urai et al. (2017); Kawaguchi et al. (2018); Colizoli et al. (2018a)	Pupil diameter increases prior to perceptual shifts and decision-making. Negative relationship between pupil size and decision confidence
Surprise, salience, orienting, prediction error	Beatty (1982a); Preuschoff et al. (2011); Wang et al. (2014); Fink et al. (2018); Alamia et al. (2019)	Pupil dilation response to surprising / alerting / salient stimuli, even when below perceptual threshold or unconscious and irrelevant to the task. Positive relationship between pupil size and prediction error
Sexual or emotional arousal	Hess and Polt (1960); Bradley et al. (2008)	Greater arousal correlated with greater pupil size. Heart rate and skin conductance also correlated with pupil activity
Response preparation, motor activity	Einhäuser et al. (2008); Reimer et al. (2014); McCloy et al. (2016)	Making a motor response (e.g., a button press) increases pupil dilation, which begins prior to the motor response. In mice, fluctuations in pupil size correlated with locomotion activity
Fatigue, task performance	Lowenstein et al. (1963); Beatty (1982a); Aston-Jones and Cohen (2005); Murphy et al. (2011); Eldar et al. (2013); McGinley et al. (2015); Knapen et al. (2016)	Performance on a task follows an inverse U-shaped function, with optimal performance at intermediate pupil sizes. Tonic pupil size decreases with time-on-task. Pupil size and behavior are correlated with changes in neural gain
Imagined arousal, effort, or brightness	Whipple et al. (1992); Laeng and Sulutvedt (2014); Sulutvedt et al. (2018); Kang and Banaji (2020)	Even during imagery or visual illusions, the pupil follows the same dilation patterns as observed during naturalistic conditions
Memory and familiarity	Võ et al. (2008); Kafkas and Montaldi (2011); Naber et al. (2013b); Papesh et al. (2012); Gomes et al. (2021)	Greater pupil size for greater familiarity; however, false alarms also produce pupil dilation (i.e., the pupil may not distinguish accurate familiarity, rather participants' belief). Greater pupil size at encoding predicts greater retrieval success. cf. Beukema et al. (2019) and "Surprise" section above

# What are the more general functions of changes in pupil size?

Why is it that “higher” level processes like mental effort should be connected with the neural systems that control a light reflex, all indexed by pupil size?

Your thoughts?

<https://PollEv.com/laurenfink203>



# What are the more general functions of changes in pupil size?

Why is it that “higher” level processes like mental effort should be connected with the neural systems that control a light reflex, all indexed by pupil size?

## Possible answers:

1. Whenever the ascending arousal system – of which the noradrenergic LC is a key center – becomes active (e.g., because of cognitive or affective processing) the pupil dilates in proportion of the LC activation (e.g., Alnæs et al., 2014)
2. Active vision / nervous system, as a whole, should prime itself for an optimal response
  - Increased pupil size (due to load) might act as a compensatory mechanism for making sure that important changes in the environment are not missed

## How fast can the pupil move?

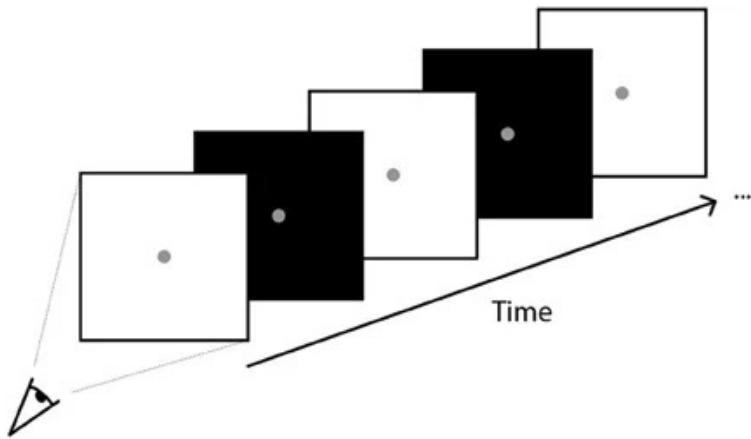
What is the fastest frequency we might care about in pupil data?

<https://PollEv.com/laurenfink203>

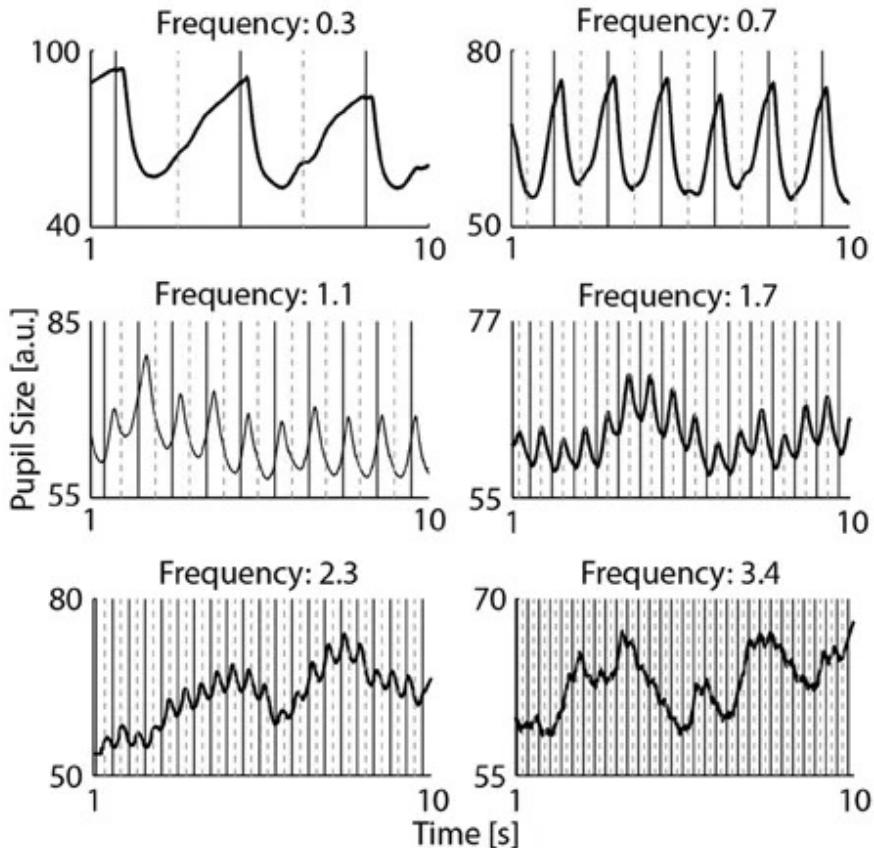


# How fast can the pupil move?

Flashing screen black and white  
at different frequencies

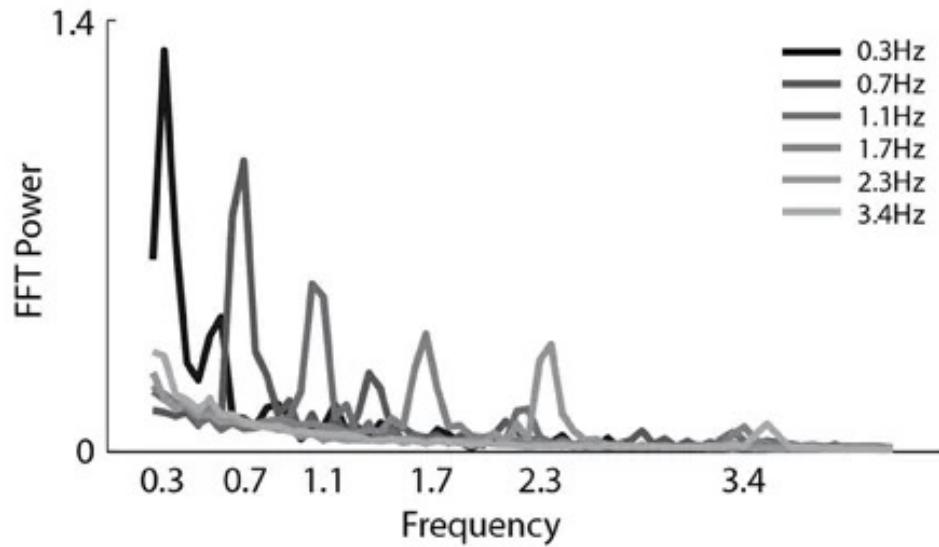
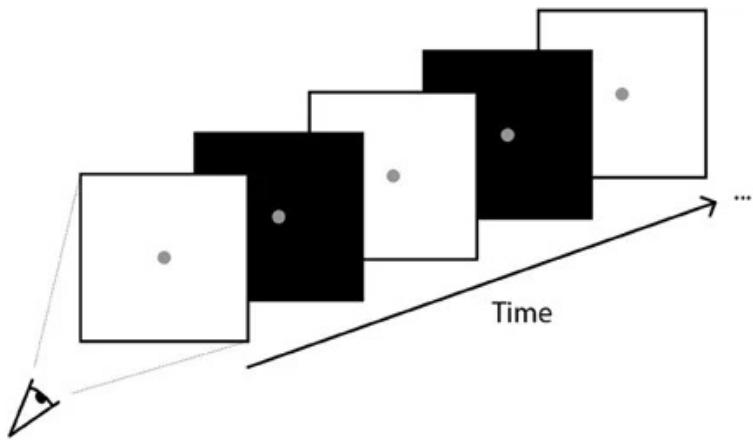


Naber et al., 2013



# How fast can the pupil move?

Flashing screen black and white  
at different frequencies



Answer: Not much faster than 3 Hz

Naber et al., 2013

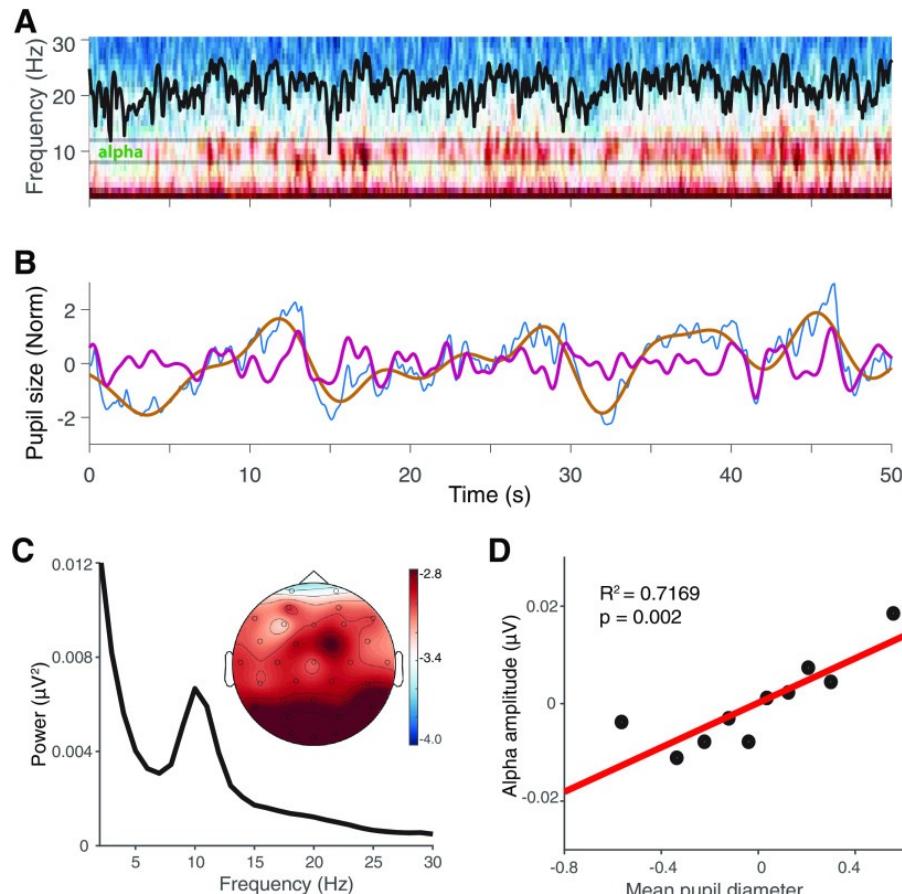
# “Low” vs. “High” Frequency activity

Montefusco-Siegmund et al., 2022

High: 0.2 and 1 Hz

Low: 0.05 and 0.2 Hz

High-frequency pupil activity  
and alpha power covary



# How long does the pupil take to respond?

Hoeks & Levelt, 1993; McCloy et al., 2016

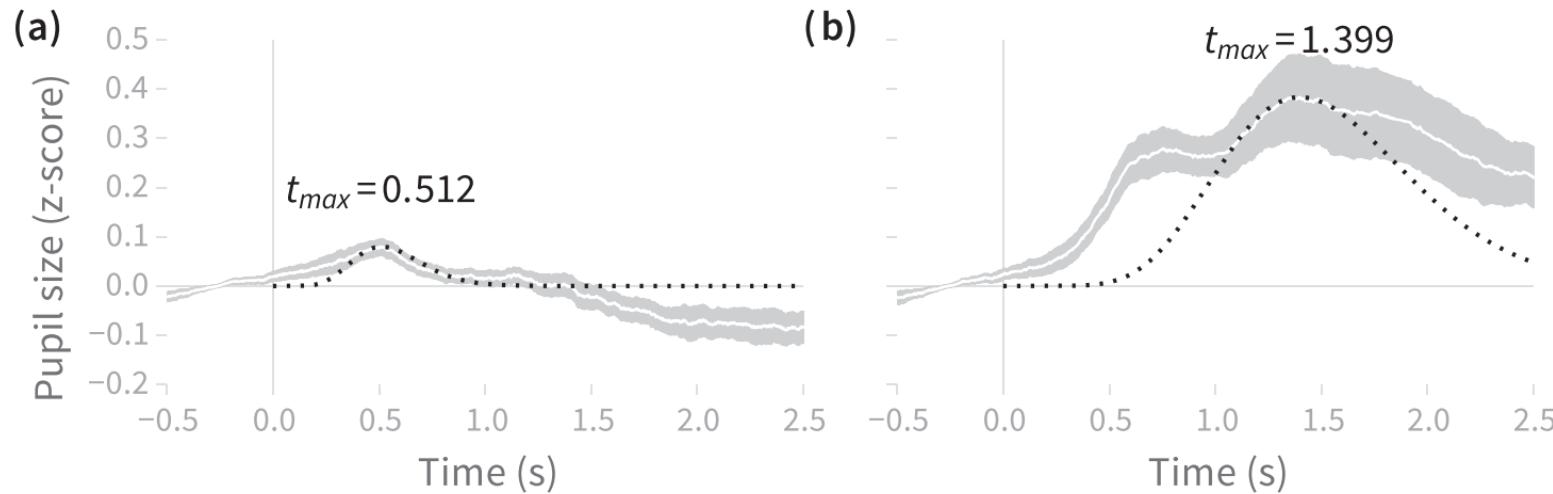
Pupillary Response Function

$$\text{PRF} = t^n e^{\left(-\frac{nt}{t_{\max}}\right)}$$

$t$  = delay until pupil size returns to baseline

$n$  = number of neural signaling steps between impulse and pupil response

$t_{\max}$  = pupil response peak latency

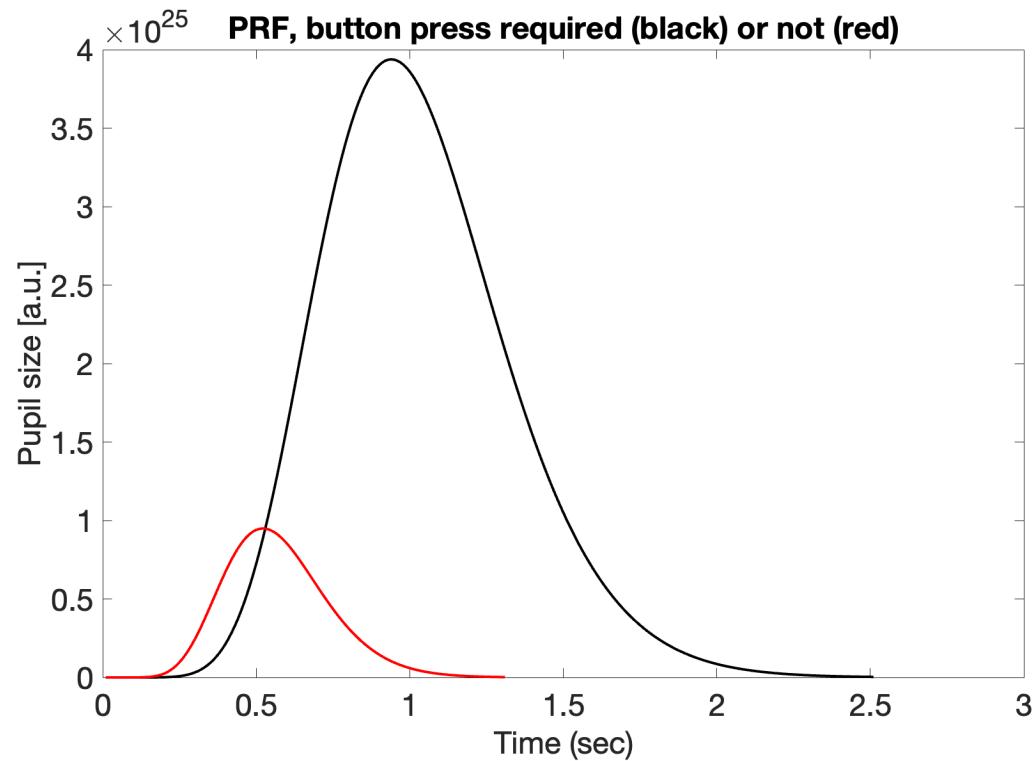


# How long does the pupil take to respond?

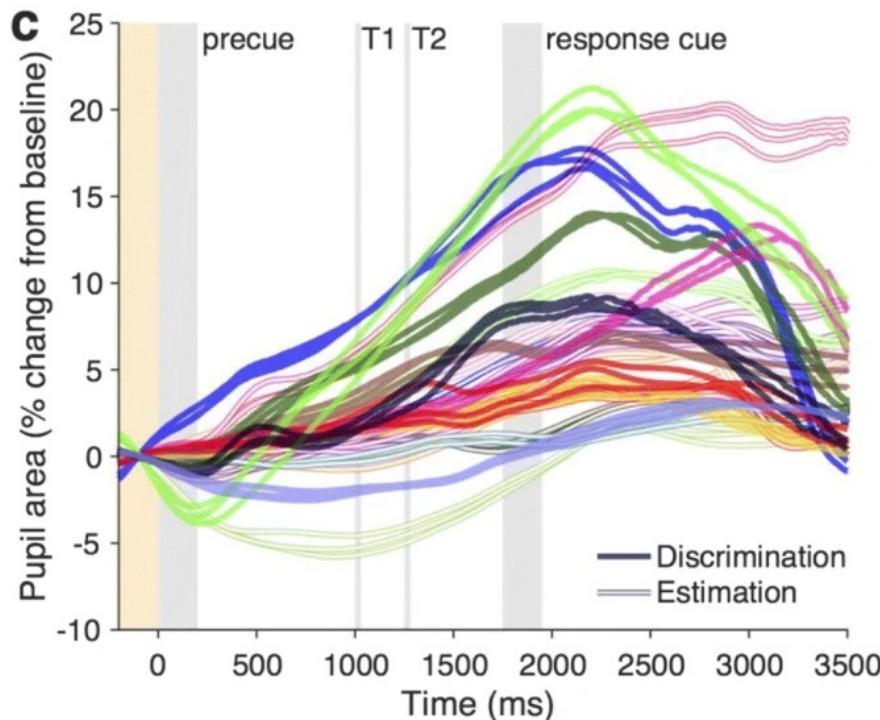
$$\text{PRF} = t^n e^{\left(-\frac{nt}{t_{\max}}\right)}$$

**It depends on:**

- Button press requirement
- Stimulus intensity
- Cognitive state
- Individual differences



# Individual differences in pupillary response function



$$\text{PRF} = t^n e^{\left( -\frac{nt}{t_{\max}} \right)}$$

**Recommend fitting individual response function**

**t\_max** varies widely across individuals, but consistent within an individual

<https://github.com/jacobaparker/PRET>

Denison et al., 2020

Is the pupil subject to voluntary control?

<https://PollEv.com/laurenfink203>



# Is the pupil subject to voluntary control?

Generally, the answer is thought to be **NO**

- And that is one of the core advantages of this method!

If people claim to have control over pupil size, it is usually through *indirect* strategies

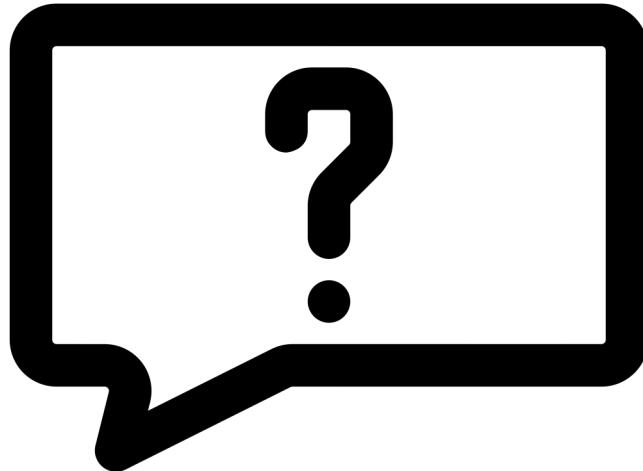
- Imagining something bright
- Imagining something arousing
- Change in focus / vergence  
(accommodation reflex)

**HOWEVER:**

See case study in Eberhardt et al. (2021)



# Questions?

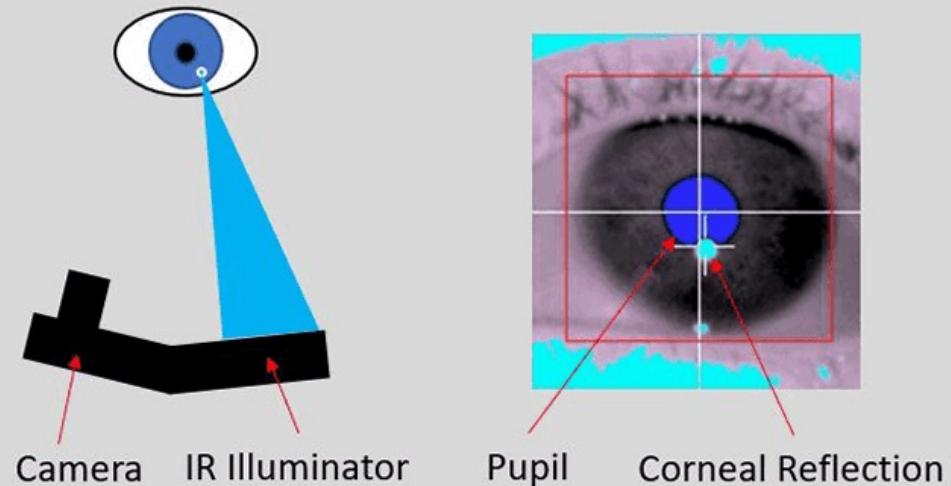


# Measuring pupil size

## How do we measure pupil size?

Feature based	Appearance Based
External light source reflections -> Eye features -> 3D Eye model	2D Images -> Machine Learning Model
Infrared cameras (commercial eye trackers)	Off-the-shelf camera
High accuracy More restrictive More expensive	Lower accuracy Wide range of applications Cheaper

# How do we measure pupil size?



<https://www.sr-research.com/about-eye-tracking/>

# Cameras can be “remote” or “head-mounted”; Proprietary or open-source

## Remote camera



<https://www.sr-research.com/eyelink-1000-plus/>



<https://www.amazon.ca/100fps-Infrared-Webcamera-Android-Windows/dp/B07PPN7TXQ>

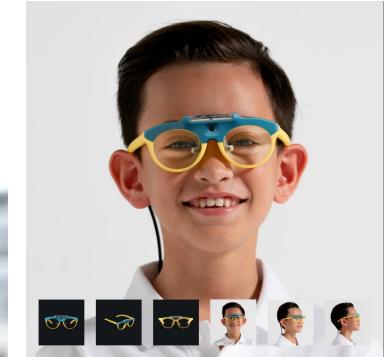


<https://www.laptopmag.com/features/im-a-laptop-reviewer-and-webcams-suck-but-these-3-laptops-have-the-best-ones>

## Head-mounted camera(s)



<https://pupil-labs.com/products/neon/shop>



<https://pupil-labs.com/products/neon/shop>

<https://www.tobii.com/products/eye-trackers/wearables/tobii-pro-glasses-3>

# Hardware considerations

## Remote vs. Head-Mounted

What is your use case?

- Stimuli on screen or in natural environments?
- Seated and relatively stationary or standing and moving?

## Feature or appearance-based

What is your use case?

- What is accuracy required?
- What is your budget?



~35000 EUR

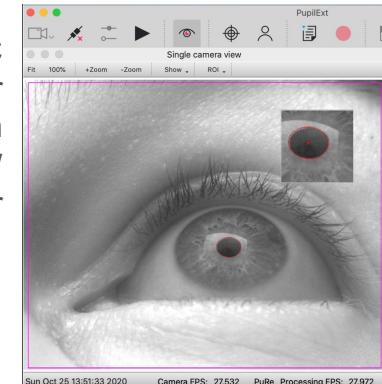
<https://www.sr-research.com/eyelink-1000-plus/>



~6000 EUR

<https://pupil-labs.com/products/neon/shop>

BYOC  
Bring your  
own  
camera/  
computer



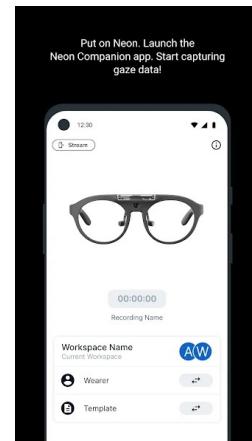
<https://www.frontiersin.org/journals/ neuroscience/articles/10.3389/fnins.2021.676220/full>

# Over-arching hardware / software workflow

## 1. Eye-tracking hardware



## 2. Data Collection software



*PsychoPy*



## 3. Data Analysis software



FOSS or custom

gazeR (Geller et al., 2020)

pupilometryR (Forbes, 2020)

PyTrack (Ghose et al., 2020)

PuPI (Kinley & Levy, 2021)

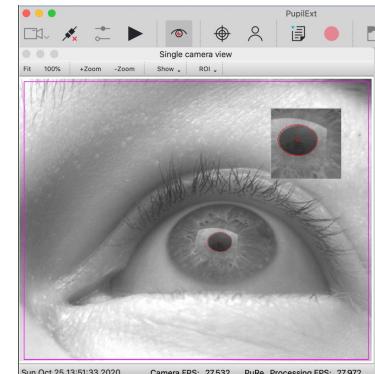
CHAP (Hershman et al., 2019)

# [Data Collection & Analysis] Free & Open-Source Software

## PupilEXT

Zandi, B., Lode, M., Herzog, A., Sakas, G., & Khanh, T. Q. (2021). PupilEXT: Flexible open-source platform for high-resolution pupillometry in vision research. *Frontiers in neuroscience*, 15, 603.

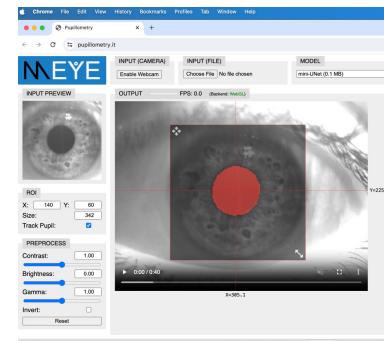
- Highly accurate, **in-lab** solution (bring your own high-res, high Fs camera)
- Choose from pupil detection algorithms (Starburst, Swirski, ExCuSe, ElSe, PuRe and PuReST)
- <https://github.com/openPupil/Open-PupilEXT>



## MEYE

Mazzotti, R., Carrara, F., Viglione, A., Lupori, L., Verde, L. L., Benedetto, A., ... & Pizzorusso, T. (2021). MEYE: web app for translational and real-time pupillometry. *eneuro*, 8(5).

- **Webcam (BYO IR cam), browser-based (OS-independent) solution**
- Modern laptop Intel(R) Core(TM) i7-9750H 2.60GHz CPU and an Intel(R) UHD Graphics 630 GPU can process up to 28 frames/s (fps).
- <https://github.com/fabiocarrara/meye>



# [Data Collection & Analysis] Free & Open-Source Software

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- <https://github.com/fabiocarrara/meye>

"A USB IR webcam (model Walfront5k3psmv97x, Walfront) equipped with a Varifocal 6–22 mm M12 objective (catalog #149129, Sodial) was used to acquire images of the eye. The camera was equipped with six IR LEDs to illuminate the eye uniformly, optimizing contrast between the iris and the pupil. Photic stimulation was delivered using an Arduino Due (Arduino) microcontroller connected via USB to the notebook and programmed to emulate a keyboard. The Arduino emulates a keyboard (using the keyboard.h library) to send event triggers to MEYE in the form of keystroke events. The microcontroller drives a stripe of four LEDs (WS2813, WorldSemi) using the FastLED.h library, flashing bright white light for 500 ms with an interstimulus interval of 5 s (see Fig. 3A). The subject sat in front of a monitor screen (24 inches; model CF390, Samsung) at a distance of 60 cm, with the head stabilized by a chin rest and instructed to maintain fixation on a small dot presented in the center of the screen for the whole duration of the recording (57 s). A total of 10 flash stimuli have been presented through the strip of LEDs mounted above the screen."



## Software considerations

How is pupil size/diameter calculated?

Do you care to know?

- If yes, need open-source software

Do you want to create your own customizations / real-time applications?

- If yes, need open-source software

How much compute power do you have / need?

Which operating system(s) is required?

Do you need dedicated support and/or actively maintained code-bases?

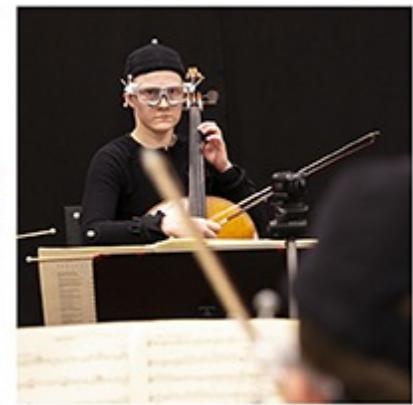
# Possible experimental scenarios



<https://www.sr-research.com/about-eye-tracking/>



<https://eyereply.com/en/home/research/eye-tracking/>



Bishop et al., 2021

## Should we do pupillometry “in the wild”?

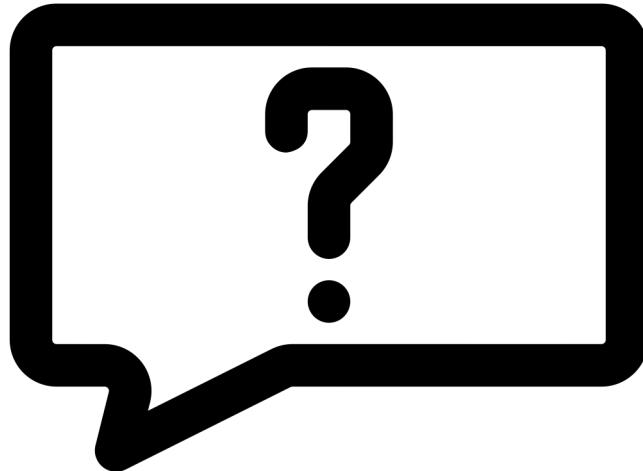
What are the potential issues?

<https://PollEv.com/laurenfink203>



We can return to this question after we discuss experimental design considerations

# Questions?



# Experimental Design Considerations

## Design

Stimuli should ideally be constant between conditions ("the Hillyard principle")

Eye position should ideally be constant between conditions

Trials should ideally be slow-paced

Pupil size should ideally be measured while participants do nothing

Ambient lighting should ideally be intermediate and matched to display brightness

All data should ideally be stored in a single file per participant

Stimuli should ideally be constant between conditions ("the Hillyard principle")

Basic idea is to vary the cognitive process or state (not stimuli)

- Unless of course you are interested in understanding the effects of different stimulus features!

Examples visual features that affect pupil size:

- Brightness
- Motion
- Color
- Rhythm (Naber et al., 2013)

Example auditory features that affect pupil size

- Intensity (Wang & Munoz, 2015)
- Rhythm (Fink et al., 2018; Damsma, 2017)
- Timbre (e.g., voice vs. cello; Akça et al. 2022)

Eye position should ideally be constant between conditions

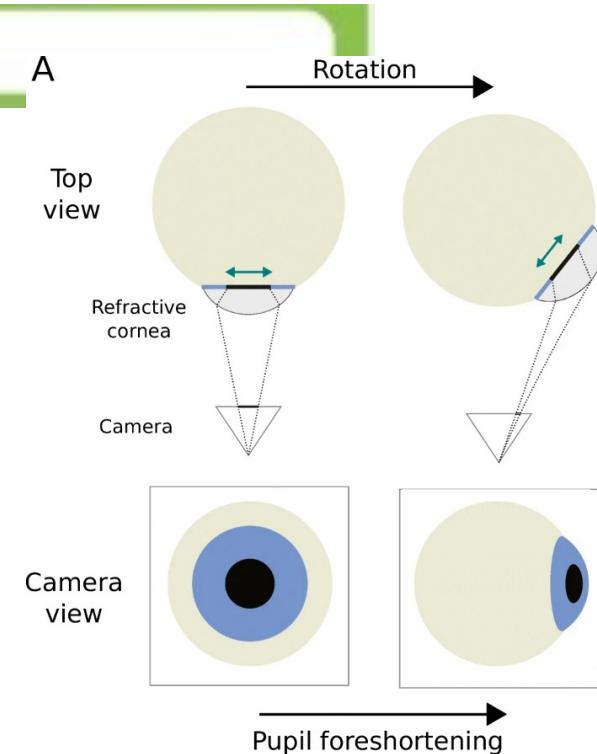
Why? Eye movements affect measured pupil size

## Pupil Foreshortening Error

There are options to correct, but depends on type of eye-tracker used and task demands.

But also (beyond measurement issues):

- Eye movements and blinks really do alter pupil size
- Certain eye positions may really affect pupil size (e.g., due to greater effort to look there)

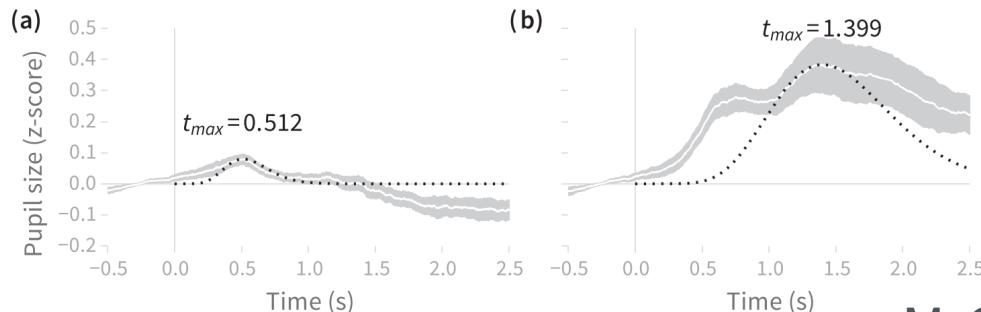


Petersch & Dierkes, 2022

Trials should ideally be slow-paced

We have already talked about modeling the pupillary response function

RECALL



McCloy et al., 2016

## Experimental design considerations: Inter-stimulus-Intervals

How much time do you need between stimuli / trials?

Consider what we learned about physiological limits of changes in pupil size

Consider what we learned about PRF

- Individual differences
- Button press required or not
  - Alters time til max dilation

<https://PollEv.com/laurenfink203>



# Experimental design considerations

Trials should ideally be slow-paced

Mathôt & Vilotijević, 2022

We can actually simulate how long our trials or inter-stimulus intervals should be!

<https://tinyurl.com/PRFCONV>

Pupil size should ideally be measured while participants do nothing

Say you are comparing two conditions which may differ in cognitive load

You are interested in the effect of load on pupil size

If participants are required to make a button press, we already know it will affect their pupil size and response latency



## What could you do?

- Require passive viewing post-stimulus presentation, but pre-decision (still might be subject to motor preparation effects)
- Measure pre-target pupil size (but maybe not the effect of interest?)

Ambient lighting should ideally be intermediate and matched to display brightness



Photo by Gighi Hardha from Noun Project



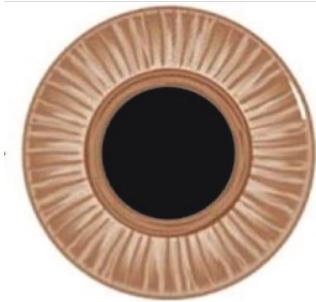
2mm

**Dynamic range of pupil = 2-8 millimeters**

- If pupil already at dilation max (little room to see dilation effects)
- If pupil already at constriction minimum (little room to see constriction effects)



Photo by Gighi Hardha from Noun Project



8mm

Ideal to conduct experiments  
at intermediate pupil size

Ambient lighting should ideally be intermediate and matched to display brightness

Also avoid large differences between room lighting and stimulus display



“Discomfort glare”

<https://higginsvisioncare.com/how-to-prevent-digital-eye-strain/>

# Experimental design considerations: Do you even need to collect data?

Collecting data is:

- Costly
- Time-consuming
- Environmentally unfriendly
- Not possible for some researchers (e.g., no access to specialized equipment or funding)

Can your research question be answered with a pre-existing dataset?

<https://PollEv.com/laurenfink203>



## Pre-registering new experiment or analysis

“Preregistration is the practice of **documenting your research plan** at the beginning of your study and storing that plan in a **read-only public repository**” <https://help.osf.io/article/145-preregistration>

Have you ever pre-registered a study?



<https://PollEv.com/laurenfink203>

Benefits of pre-registration:

- Increase discoverability of research
- Reduce unintentional false positive inflation
- Distinguish exploratory from confirmatory analyses

“Pre-registration is a plan not a prison”

<https://www.cos.io/blog/preregistration-plan-not-prison>

## Experimental design considerations: Sample size, # of trials, etc.

How many participants do you need? How many trials do you need?

There is no generic "right" answer to these questions.

It depends on:

- Type of participant(s), task, experimental design and planned analysis (e.g., 2x2 ANOVA, time series analysis), etc. etc.

### Strategy:

1. Look for other studies similar to the one you want to do!
  - What are the reported effect sizes? What sample size did they need for such an effect?
2. Follow general guidelines w/r/t to your final planned statistical model(s); see e.g., Brysbaert, 2019 (<https://jrnalofcognition.org/articles/10.5334/joc.72>)

## Homework before tomorrow (optional)

Find a pre-existing, publicly available dataset that interests you!

### General repositories:

OpenNeuro.org

Open Science Framework (osf.io),

Google Dataset Search (<https://datasetsearch.research.google.com/>)

### Specific papers (non-exhaustive!):

Grenzebach et al. (2021); Bishop et al. (2021); Pajkossy and Racsmány (2019); Kooijman et al. (2021); Winter et al. (2021); Mathôt et al. (2017); Scheepers et al. (2016); Urai (2016); Pelagatti et al. (2020); Lehmann et al. (2019); Chapman and Hallowell (2020); Rozado (2019); Wahn et al. (2016); Nakakoga et al. (2020); Kucewicz (2021); Colizoli et al. (2018b); Moeller et al. (2021); Pavlov et al. (2021); Gee et al. (2017b); Zhao et al. (2020); Lee et al. (2019, 2021); Ribeiro and Castelo-Branco (2021); Clewett et al. (2019); Hanke et al. (2016); Bianco et al. (2021); Madore (2020); Keung (2020); Keitel et al. (2021)



What are you most hoping to learn tomorrow?

<https://PollEv.com/laurenfink203>



What is your preferred programming language?

<https://PollEv.com/laurenfink203>



What is your main take-away from today?  
Did you learn something new?

<https://PollEv.com/laurenfink203>

A wide-angle photograph of a university campus during autumn. On the left, a large, multi-story stone building is covered in green ivy and features several arched windows. In the foreground, a group of five students are sitting on the grass, surrounded by fallen orange and yellow leaves. A bicycle is leaning against a tree to the left of the group. The background shows more buildings and trees, with bright sunlight filtering through the foliage.

**Thank you!!**

**Questions?**

**Contact:**  
[finkl1@mcmaster.ca](mailto:finkl1@mcmaster.ca)

# Learning Pupilometry From Theory to Analyses

**Lauren Fink, PhD**

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Dept. of Psychology, Neuroscience & Behaviour  
McMaster Institute for Music & the Mind / LIVELab  
School of Computational Science & Engineering  
Center for Advanced Research in Experimental  
& Applied Linguistics (ARiEAL)

University of  
Konstanz



# Agenda

## Day 2: Pre-processing & Analyses

Hands-on coding workshop covering a variety of potentially useful analyses, from condition-averaging the pupil dilation response, to analyzing the dynamics of single-trial pupil time series.

Pre-processing pupil data

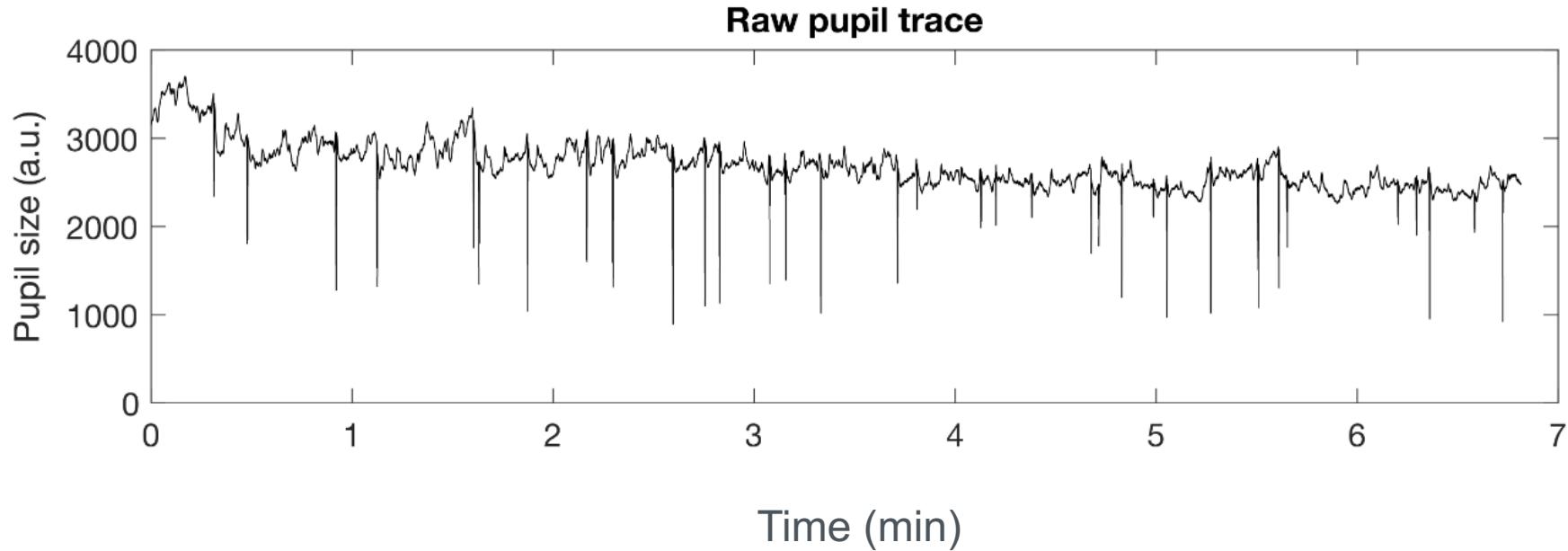
Condition averaged analyses

The importance of data visualization

Time series analyses & signal-to-signal approaches

# What does raw pupil data look like?

What are these spikes?



## Pre-processing pupil data

How should we get rid of them?

Step 1. Find them

Step 2. Set them to NaN

Step 3. Interpolate them (necessary depending on analysis)

## Pre-processing pupil data

How should we get rid of them?

Step 1. Find them  
→ How?

Step 2. Set them to NaN

Step 3. Interpolate them (necessary depending on analysis)  
→ How?

## Pre-processing pupil data

Some eye-trackers will return a “flag” to specify “valid” pupil data

It is important to understand what that means in the context of your own eye-tracker

timestamp [ns]	pupil diameter [mm]
1709835084722379215	4.61620569229126
1709835084727379215	4.652669906616211
1709835084732504215	4.679261207580566
1709835084737504215	4.6961588859558105
1709835084742504215	4.659944534301758
1709835084747504215	4.728400230407715
1709835084752504215	4.780755043029785
1709835084757503215	4.703244686126709
1709835084762504215	4.659246444702148
1709835084767503215	4.67100191116333
1709835084772504215	4.679454803466797
1709835084777509215	4.677417278289795

is valid

1  
1  
1  
0  
0  
0  
0  
-

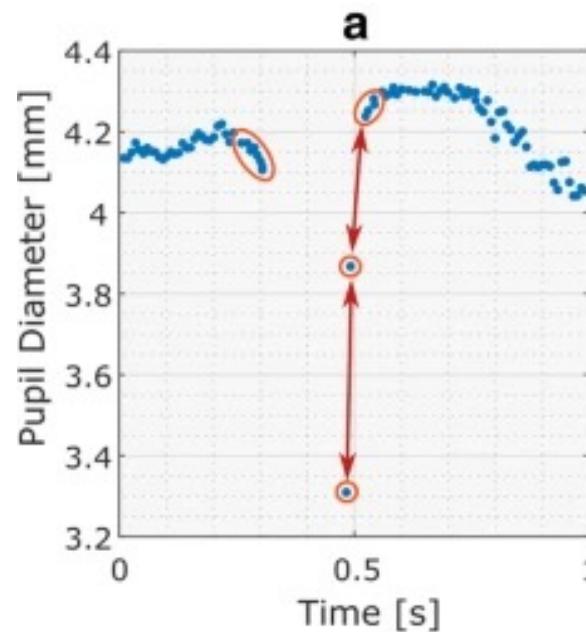
is blink  
is saccade  
gaze x  
gaze y

Great for helping you find problematic data!

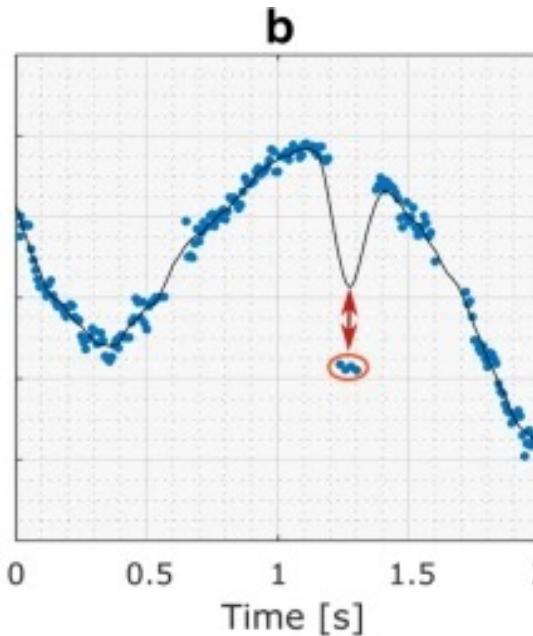
## Pre-processing pupil data

What about other potentially problematic data points?

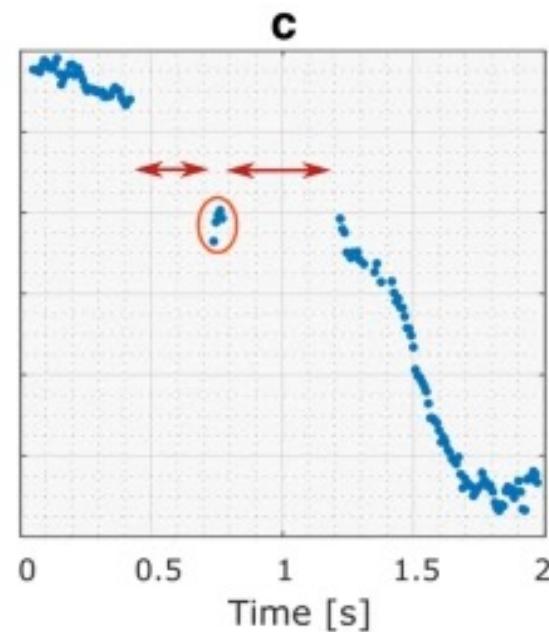
Speed outliers



Trend line deviations



Temporally isolated samples



# Pre-processing pupil data

How should we get rid of them?

Step 1. Find them  
→ How?

Multiple open-source algorithms for doing this.

gazeR (Geller et al., 2020)

pupillometryR (Forbes, 2020)

PyTrack (Ghose et al., 2020)

Mathôt and Vilotijević (2022)

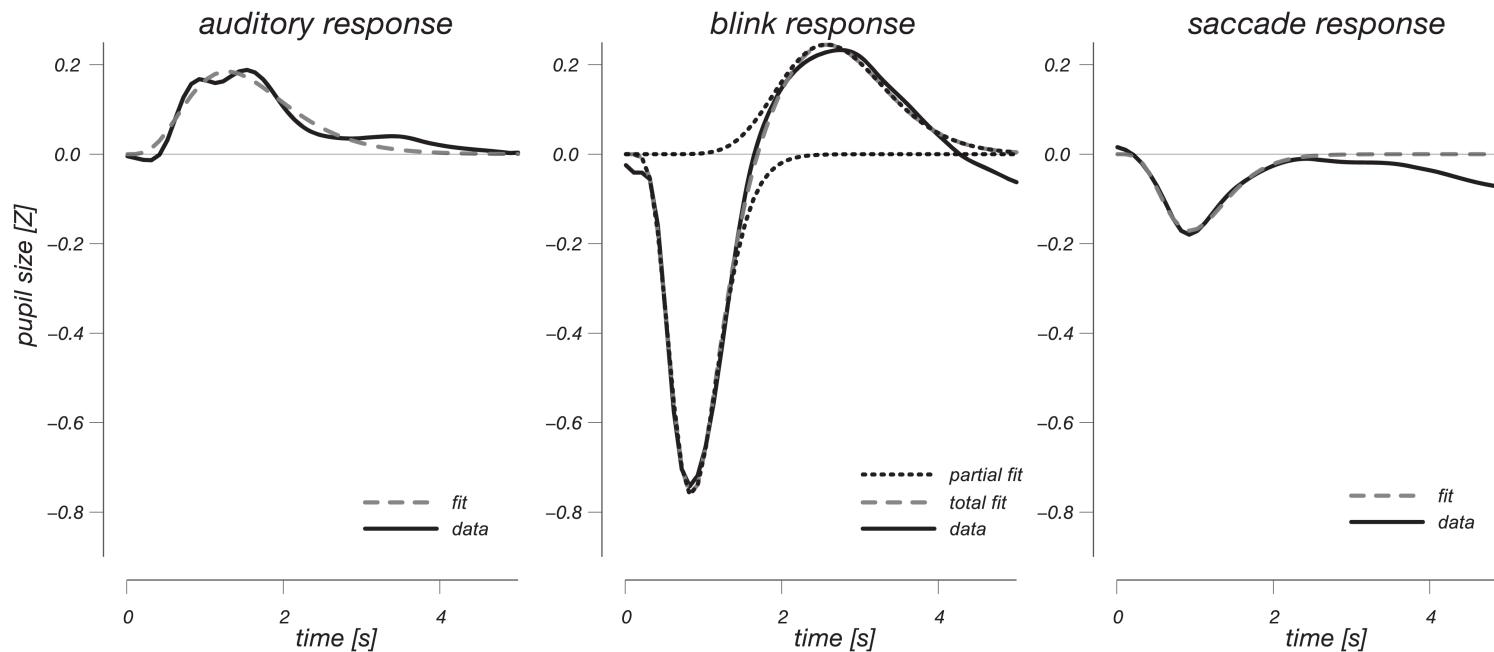
PuPI (Kinley & Levy, 2021)

CHAP (Hershman et al., 2019)

1. Don't re-invent the wheel
2. Would be great if the field moved towards more standardized tools (it is!)

# Pre-processing pupil data

Previous steps take care of blinks. But is it enough? What about saccades?



Knapen et al., 2016

## Quick side note: Blinks



Types: Voluntary, Reflexive, Spontaneous

Function: Protect and hydrate eyes (4 blinks per min; Doane, 1980)

Why blink more often than necessary? (15-20 per minute avg)

Lose **150-400msec** of information each blink = roughly 44 min of each day

Function: Provide attentional breaks

Activate default mode network (Nakano et al., 2013; Nakano, 2015)

Used as index of:

**Striatal dopamine** (Disrupted in clinical conditions involving dopamine; c.f. dopamine debate: Jongkees and Colzato, 2016 vs. Sescousse et al., 2018; Dang et al., 2017)

**Attention / effort / cognitive load / information chunking / fatigue**

(Cummins, 2012; Nakano & Kitizawa, 2010; Orchard & Stern, 1991; Hall, 1945; Bauer et al., 1987; Johns, 2003)

- e.g., occur at pauses / turns in speech; increase when tired; decrease with load

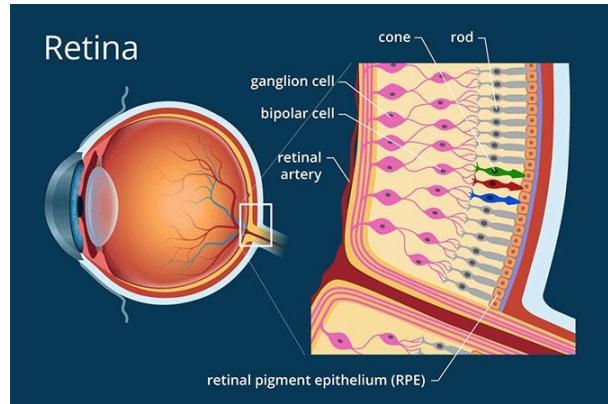
## Quick side note: Eye movements

**Fixations:** to foveate target

Average duration = 150-300 ms

→ fixational eye movements (e.g., microsaccades)

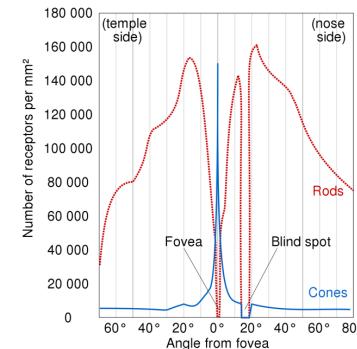
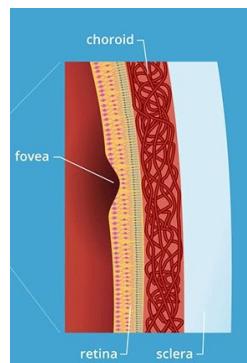
→ To maintain foveation on target



**Retina**  
comprised of light-sensitive cells (rods and cones), which send info to brain

**Saccades:** to change point of fixation

- Average duration = 20-40ms
- Linear relationship between saccade amplitude and duration
- (smaller saccades = shorter dur)



**Fovea** has highest density of cones (responsible for color and fine detail)

**Smooth pursuit:** to maintain foveation on moving target

<https://www.allaboutvision.com/resources/retina.htm & .. eye-anatomy/fovea/>

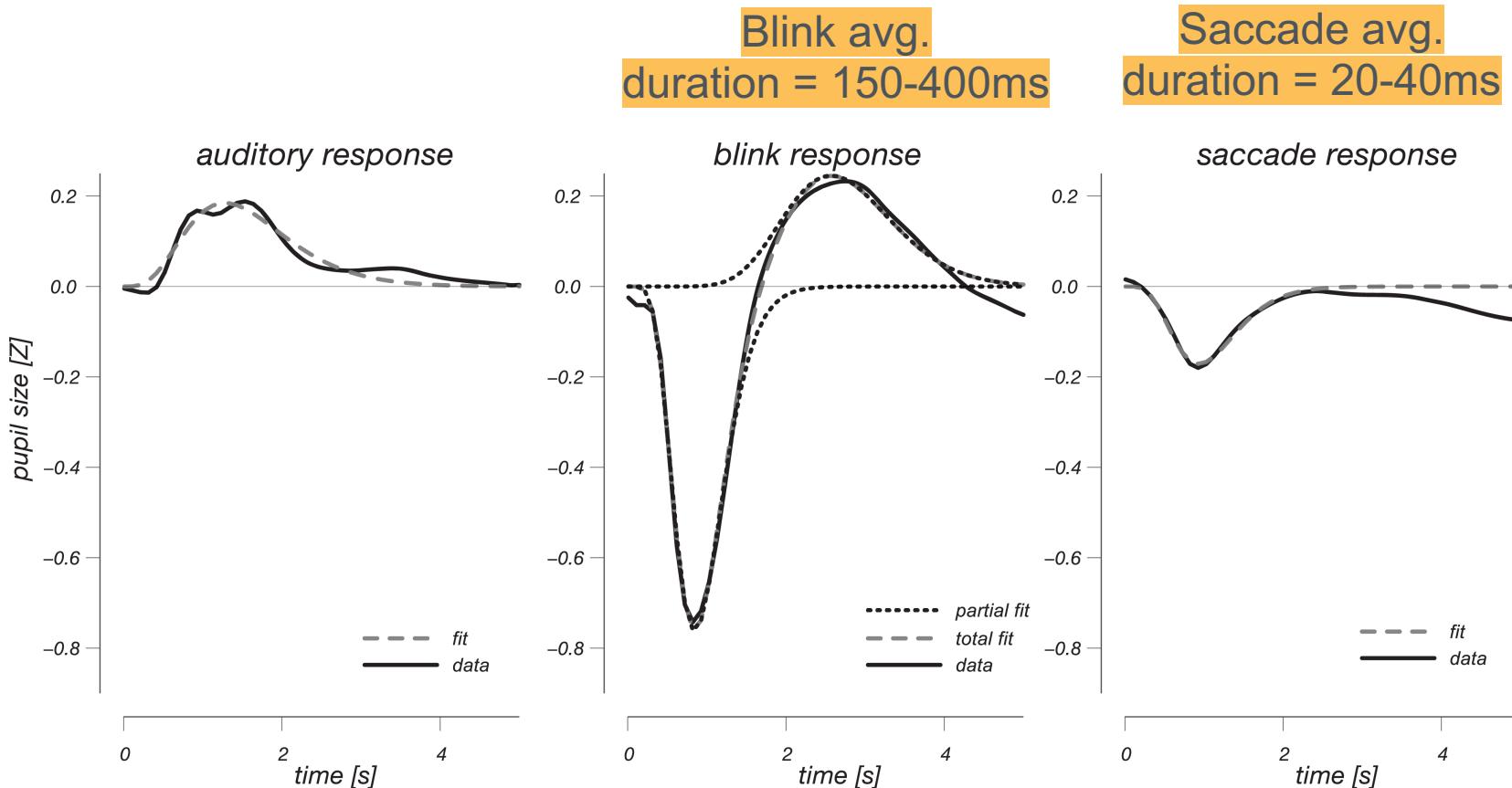
## Quick side note: Why you might want to record data at a higher sampling rate

Recall from yesterday: the pupil is slow → ~ 3 Hz

Why do we often record eye-tracking data at higher sampling rates?

- To be able to accurately identify saccades (and microsaccades)!

# Pre-processing pupil data



## Pre-processing pupil data

So, should you model (individually, for each subject, the pupillary response to blinks and saccades?)

Practically, speaking I think it would be easier to rather design your experiment well. Blink and saccade effects will only confound your results if they systematically differ between the conditions you are comparing.

→ It would be easier to quickly analyze blink and saccade data by condition, than to fit individual response functions and correcting pupil data

→ Why?

→ Many observations of blinks and saccades are necessary to form an accurate model. Blinks are sparse events. You might not be able to fit a good model from your data.

# Pre-processing pupil data

How should we get rid of them?

Step 1. Find them  
→ How?

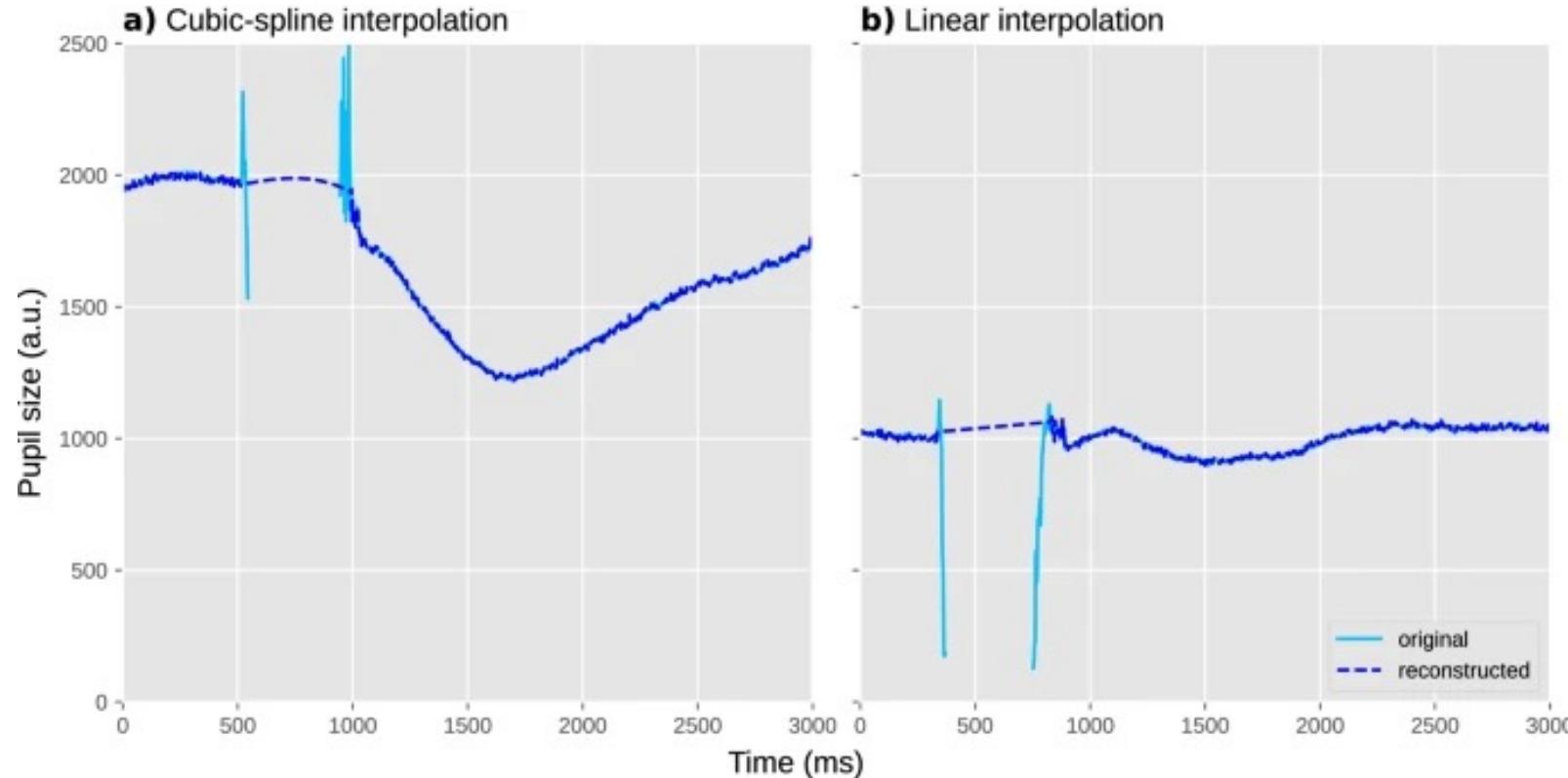
Step 2. Set them to NaN

Step 3. Interpolate them (necessary depending on analysis)  
→ How?

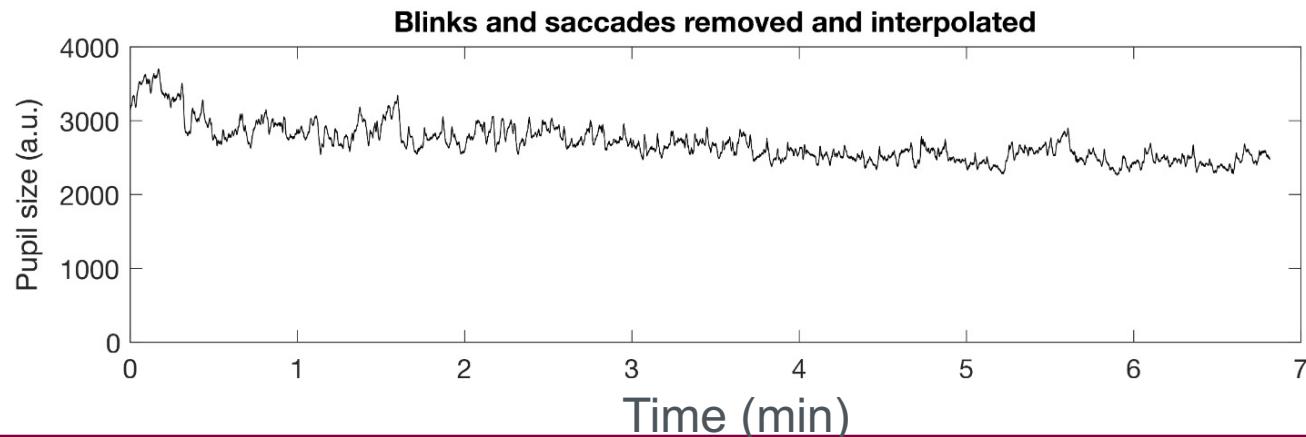
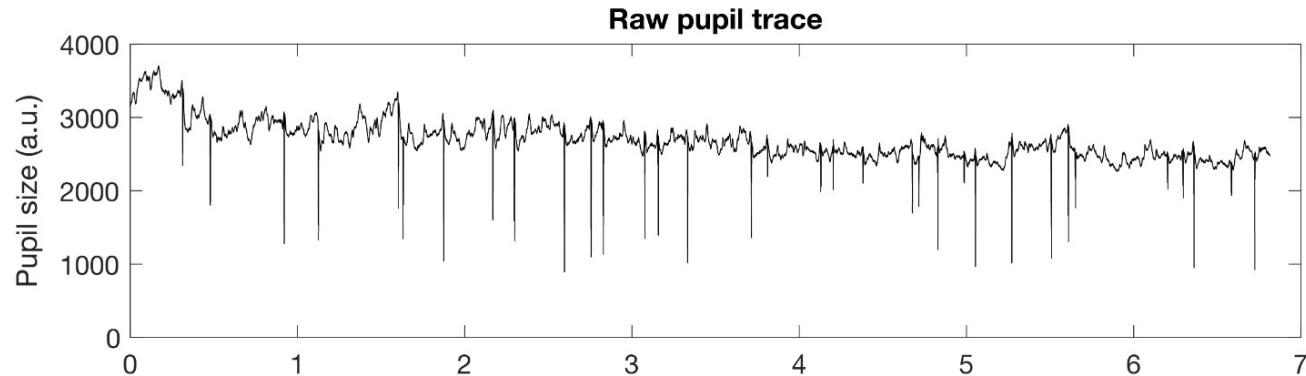
→ Linear or spline interpolation

→ Why?  
→ Missing data reduces statistical power; might create edge artifacts in plots  
→ Time series analyses require evenly sampled, continuous data

## Pre-processing pupil data: Interpolation



## Pre-processing pupil data: After interpolation

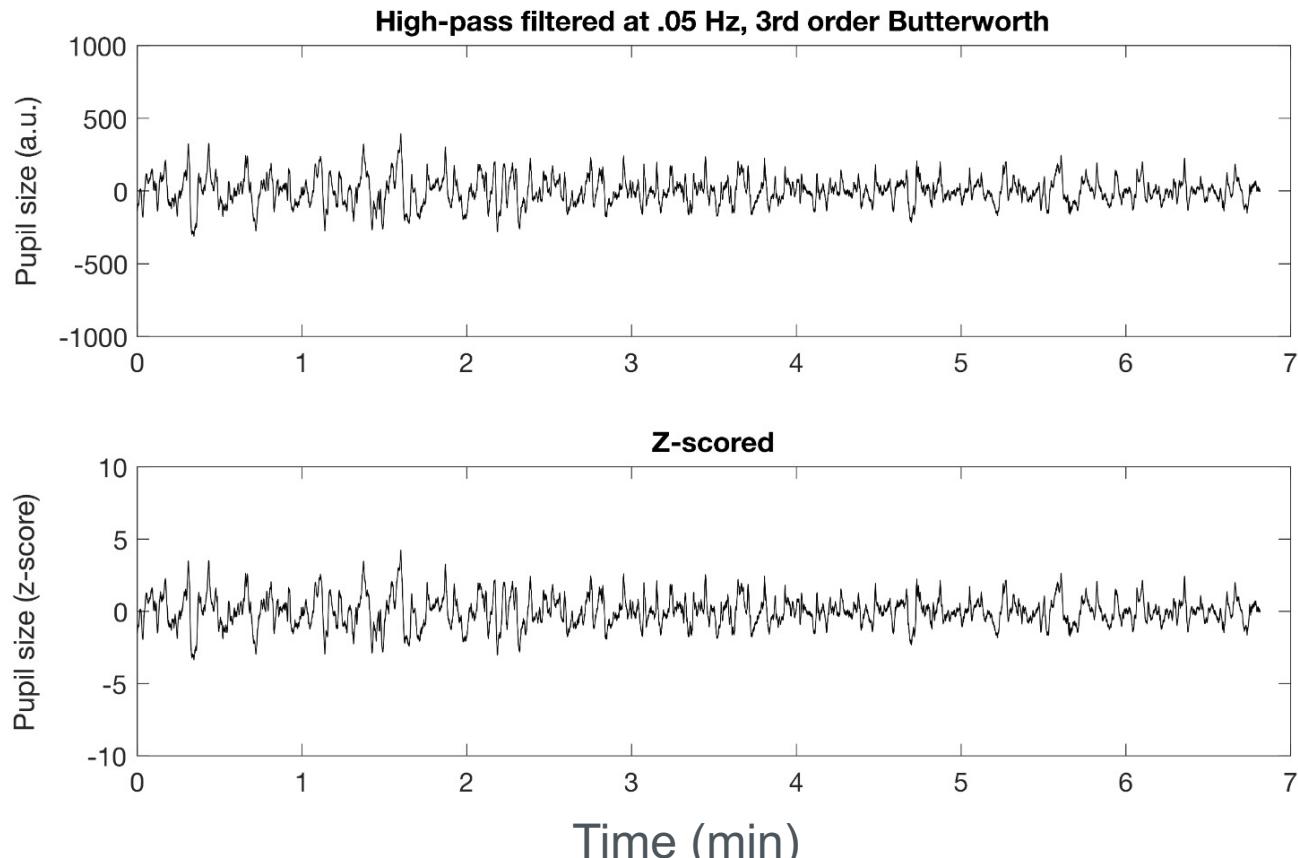


# Pre-processing pupil data: **Transformations**

Possibly:

- **Convert** from arbitrary units to millimeters
  - Re: yesterday's question:
    - Support page (need log in credential): <https://www.sr-research.com/support/thread-154.html>
- **Downsample**
  - Might want more highly sampled data for:
    - Looking at light reflex (quick constriction)
    - Smoother-looking figures
    - **100 Hz is more than enough!**
- **Filter**
  - Which frequencies do you care about?
  - Are you going to do analyses over longer time scales?
  - Do you need to? (can introduce artefacts, autocorrelation)

## Pre-processing pupil data: Transformations



## Pre-processing pupil data: **Transformations**

Possibly:

- **Normalization**

$$x' = \frac{x - \bar{x}}{S(x)}$$

(e.g., Fink et al., 2018)

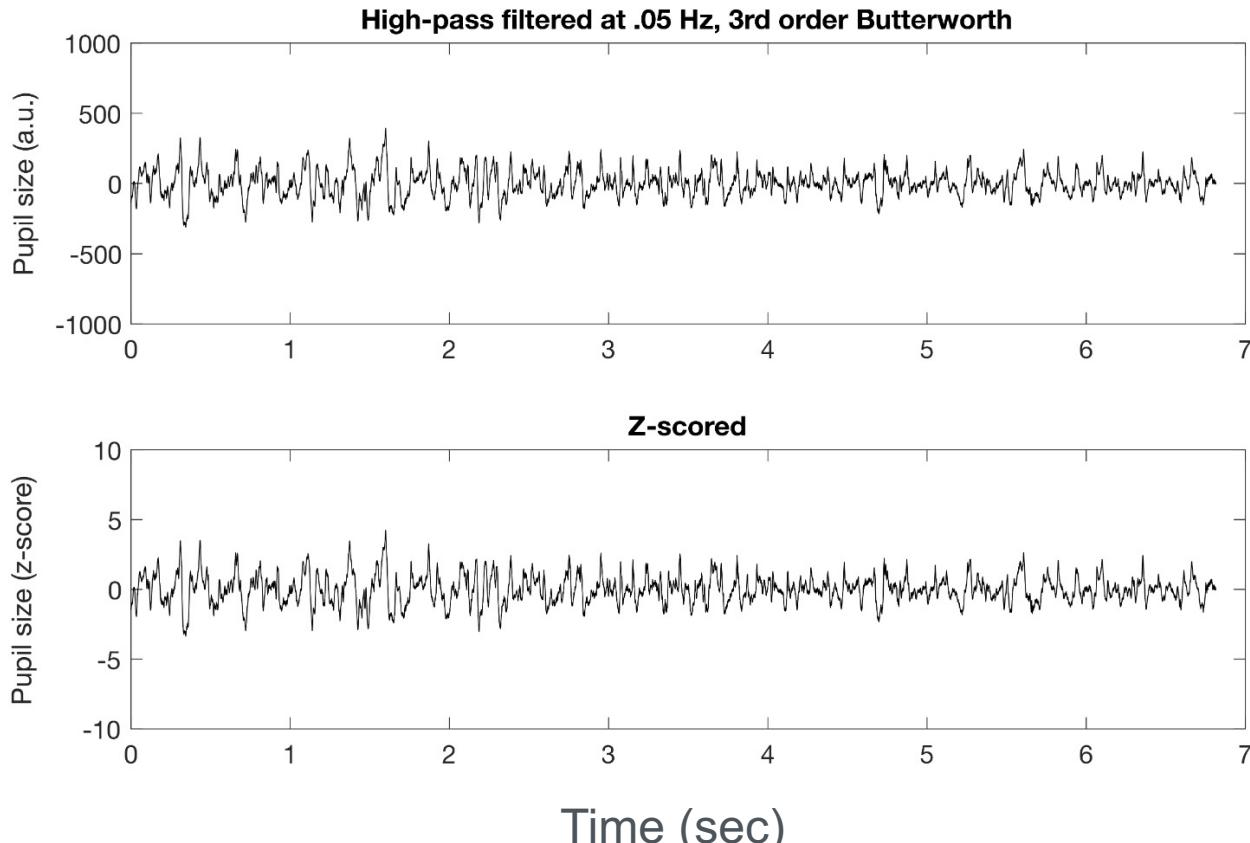
$$x' = \frac{x - x_{\min}}{x_{\max} - x_{\min}} * 100$$

(e.g., Piccado et al., 2010)

Note that normalization puts pupil data in relative units (not millimeters!)

- **Baseline correction**
  - Often used in epoch-based analyses
  - Note that correction results in negative relationship between baseline and epoch pupil dilation (Mathôt & Vilotijević, 2022)

## Pre-processing pupil data: **Transformations**



## Pre-processing pupil data: **Transformations**

Possibly:

- **Normalization**

$$x' = \frac{x - \bar{x}}{S(x)}$$

(e.g., Fink et al., 2018)

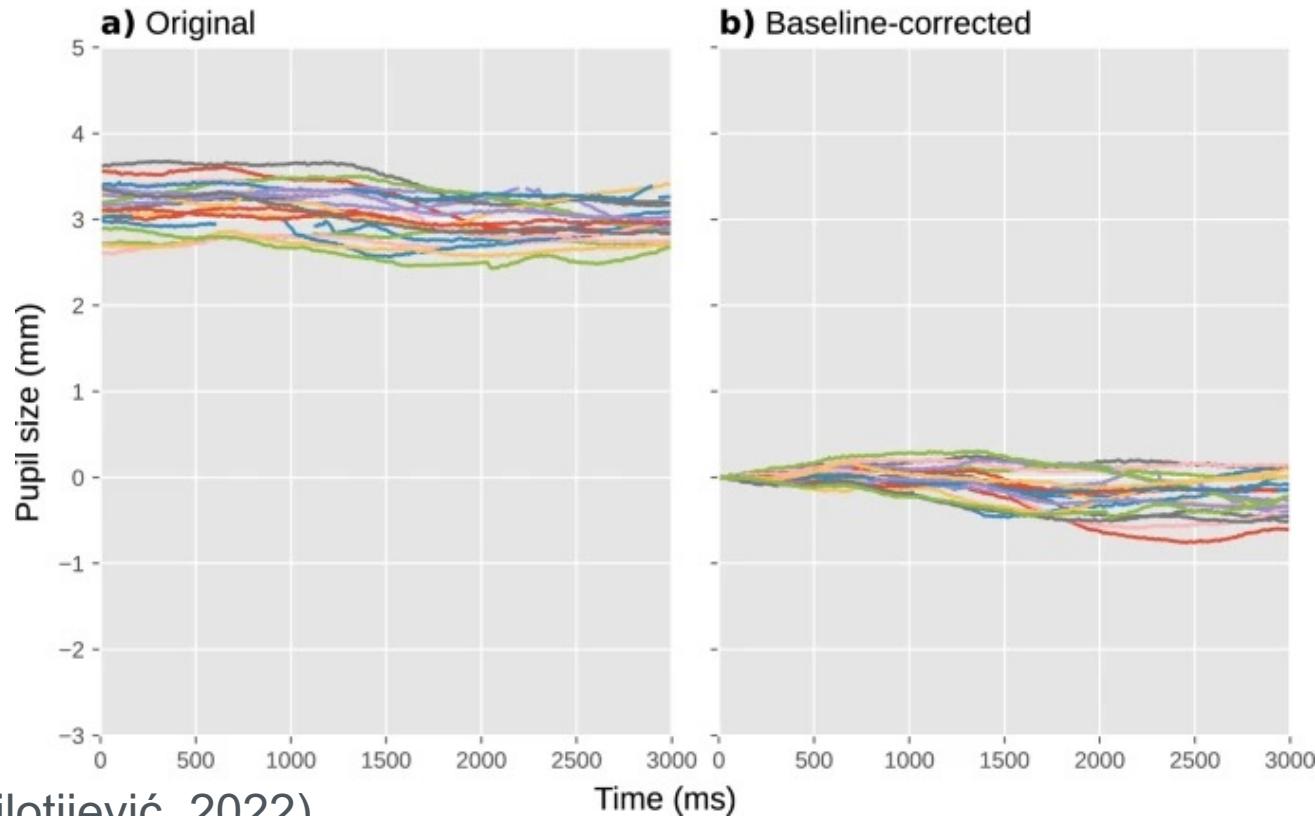
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- **Baseline correction**
  - Often used in epoch-based analyses
  - Note that correction results in negative relationship between baseline and epoch pupil dilation (Mathôt & Vilotijević, 2022)

## Pre-processing pupil data: **Transformations**



(Mathôt & Vilotijević, 2022)

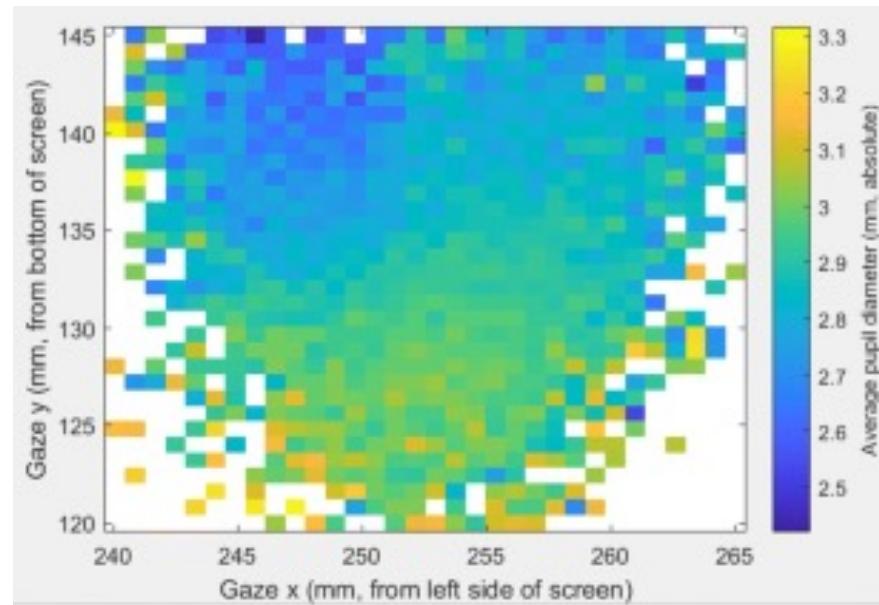
## Pre-processing pupil data: **Gaze-correcting pupil size**

This would only be necessary if participants were not fixating centrally during your task

Toolboxes exist!

See Kinley & Levy (2022)

Pupil size (color) across screen location



## Pre-processing pupil data: **Summary & Recommendations**

Think about what steps are necessary for your research context

Consider pre-registering pre-processing plan

- Not covered today: how will outlying participants and trials be determined (if at all?)

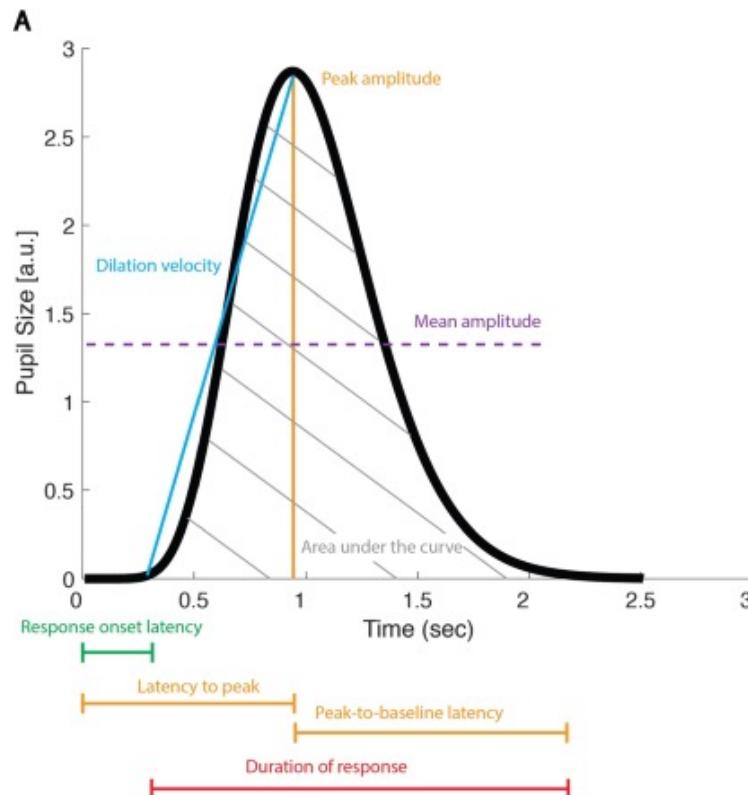
Be sure to visualize data for each participant (some participants might have unexpectedly noisy signals or e.g., blink dynamics)

Visually check for discontinuities (artefacts) after data cleaning

Make sure you understand how any pre-processing steps affect your final interpretation of what the pupil signal represents

# Condition-averaged analyses

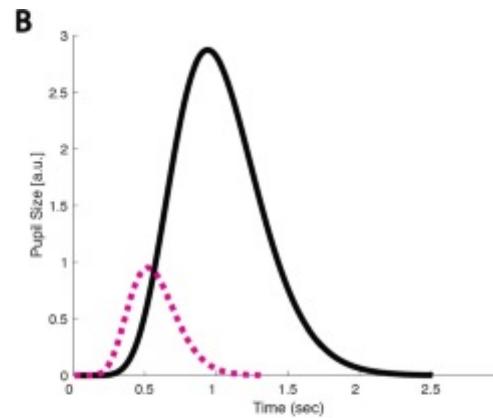
# Condition averaged analyses: Potential metrics of interest



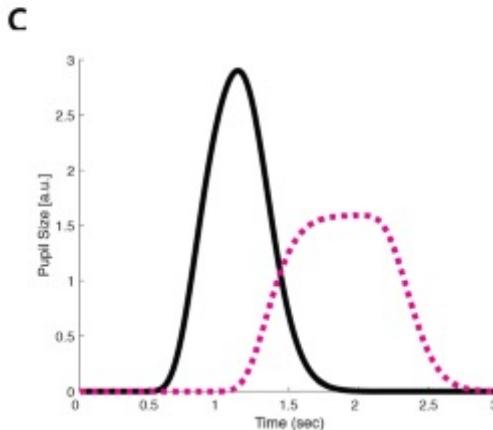
Fink et al., 2023

# Condition averaged analyses

Same slope, different mean



Same mean, different slope and onset latency



Fink et al., 2023

# Let's play with some data!



Pretend these data are already pre-processed perfectly.

Your task is to print summary statistics and plot pupil size by condition

Here are the data:

[https://beatlab.mcmaster.ca/assets/pupilTutorial/KonstanzWorkshop\\_pupilData\\_byCondition.csv](https://beatlab.mcmaster.ca/assets/pupilTutorial/KonstanzWorkshop_pupilData_byCondition.csv)

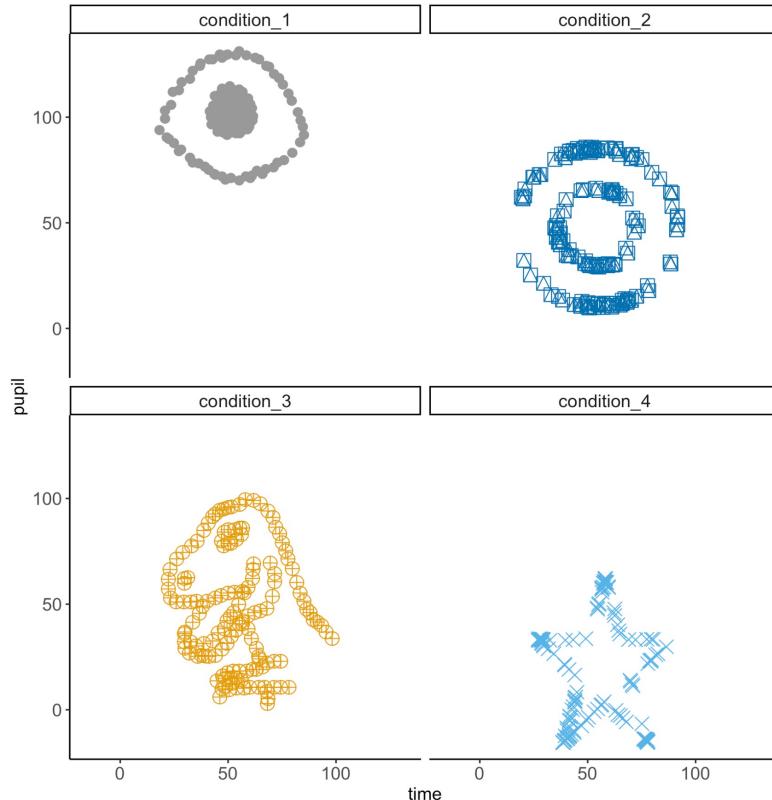
Let's play with some data!



Possible approach provided here:

<https://beatlab.mcmaster.ca/assets/pupilTutorial/KonstanzPupilWorkshop.html>

# Why should you visualize data?

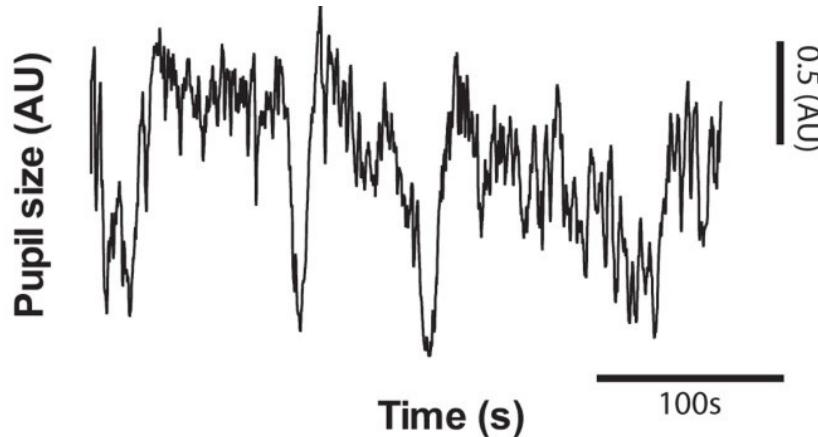


To make sure  
you aren't looking at noise!

## Why should you visualize data?

To make sure you aren't looking at noise!

What would actual pupil data look like?

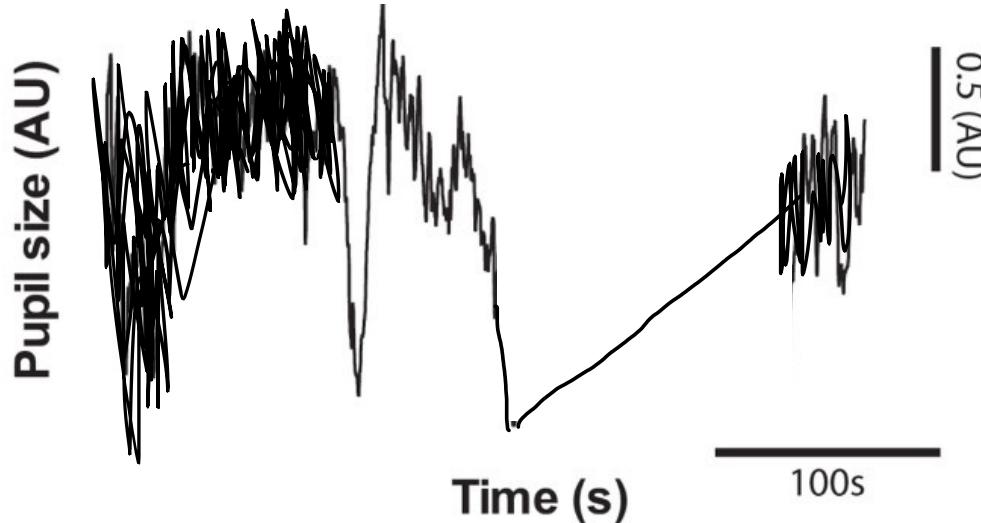


Zenon, 2017

## Why should you visualize data?

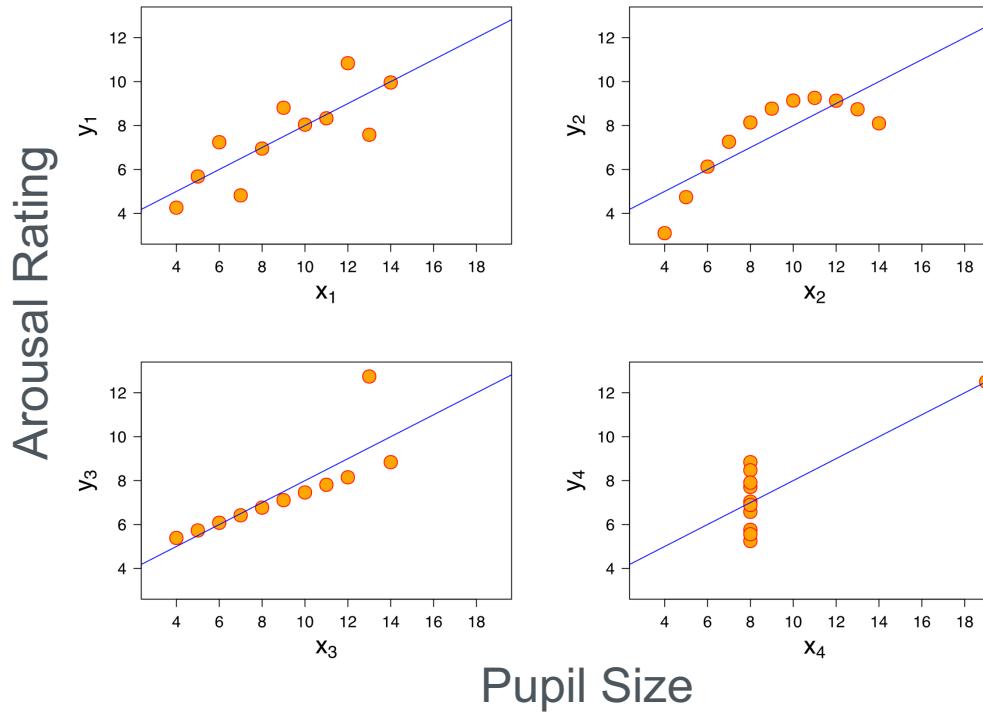
To make sure you aren't looking at noise!

What would noise look like?



# Why should you visualize data?

To understand what statistical tests and models are appropriate!



The mapping between data types and visualizations

(not all visualizations are appropriate!)

## What options exist?

<https://python-graph-gallery.com/>

<https://r-graph-gallery.com/>

## How do you choose?

<https://www.data-to-viz.com/#explore>

## Caveats.. (every plot has pros and cons! Some more than others..)



The spaghetti chart

A line graph with too many lines becomes unreadable: it is called a spaghetti graph.



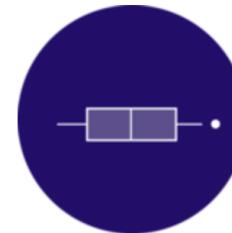
Pie chart

The human eye is bad at reading angles. See how to replace the most criticized chart ever.



Play with histogram bin size

Always try different bin sizes when you build a histogram, it can lead to different insights.



Do boxplots hide information?

Boxplots are a great way to summarize a distribution but hide the sample size and their distribution.

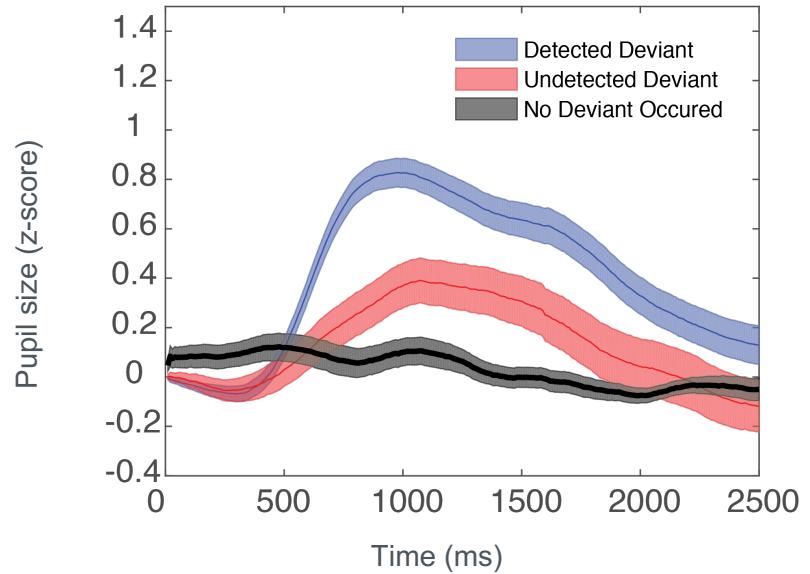
<https://www.data-to-viz.com/caveats.html>

## Summary: Condition-averaged analyses

Even if only interested in mean pupil size,  
please plot your data!

All the tools you need are available!

- gazeR (Geller et al., 2020)
- pupillometryR (Forbes, 2020)
- PyTrack (Ghose et al., 2020)
- Mathôt and Vilotijević (2022)
- PuPI (Kinley & Levy, 2021)
- CHAP (Hershman et al., 2019)



# Time Series Analyses & Signal-to-Signal Approaches

# Time series analyses & signal-to-signal approaches



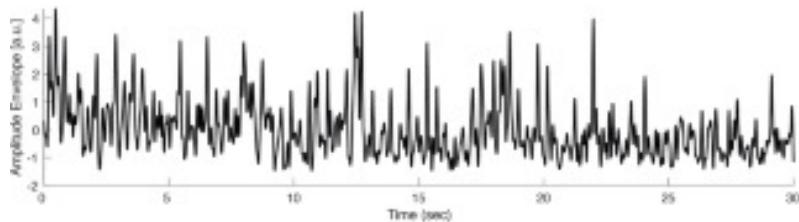
Why?

1. Lots of information is lost when averaging over time
2. We might want to know something about the relationship between the pupil and some other signal
  - Other signal could be e.g.,
    - Speech, music, movie, etc.
    - Another physiological signal (respiration, EKG, EEG, GSR, etc.)
3. We might learn something new!

# Time series analyses & signal-to-signal approaches

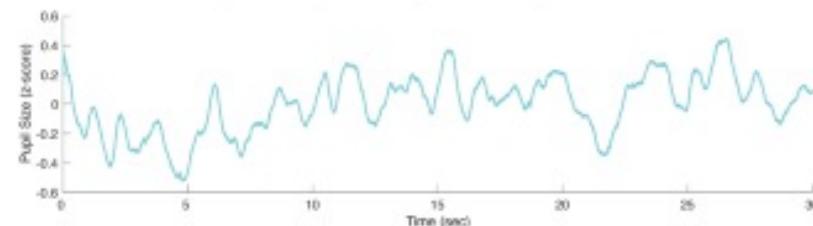
A

Signal 1: Stimulus



B

Signal 2: Pupil during stimulus presentation



What is the temporal relationship between these two signals?

How far behind is the pupil?

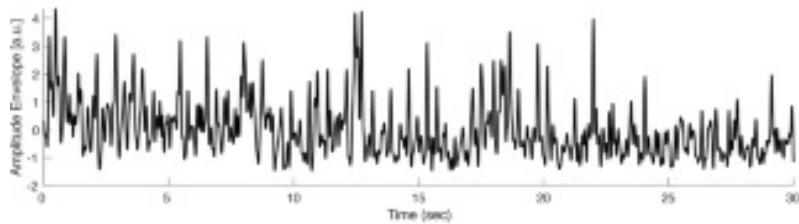
How much variance in the pupil data does the stimulus data explain?

(a mean won't work)

# Time series analyses & signal-to-signal approaches

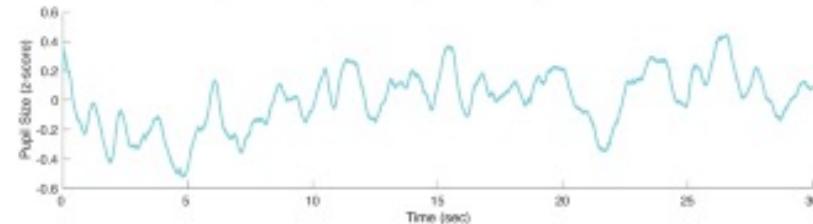
A

Signal 1: Stimulus



B

Signal 2: Pupil during stimulus presentation



What is the temporal relationship between these two signals?

How far behind is the pupil?

→ Lag correlation

How much variance in the pupil data does the stimulus data explain?

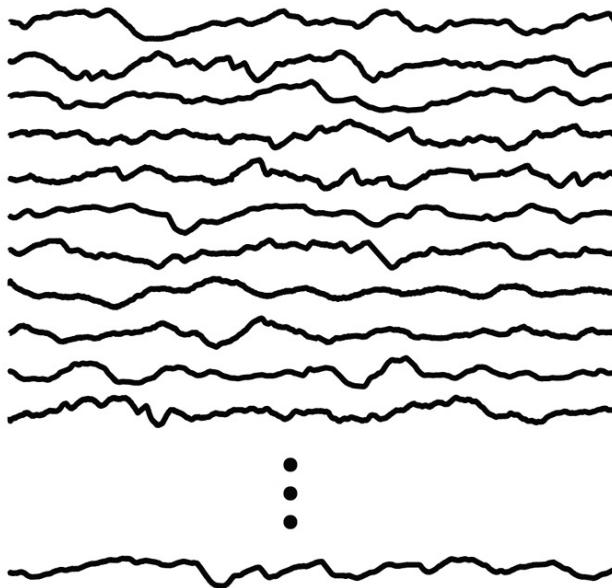
→ Correlation

→ Regression

# Time series analyses & signal-to-signal approaches

B

Pupil Traces of Participants  
Listening to Same Stimulus



What if you have multiple traces and you want to know at which time points all participants respond similarly?

(a mean won't work)

Inter-Subject Correlation (ISC)

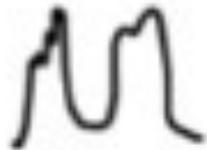
Shown to reflect stimulus processing, attentional engagement; e.g., ISC while watching educational video predicted test scores (Madsen et al., 2021, PNAS)

# Time series analyses & signal-to-signal approaches

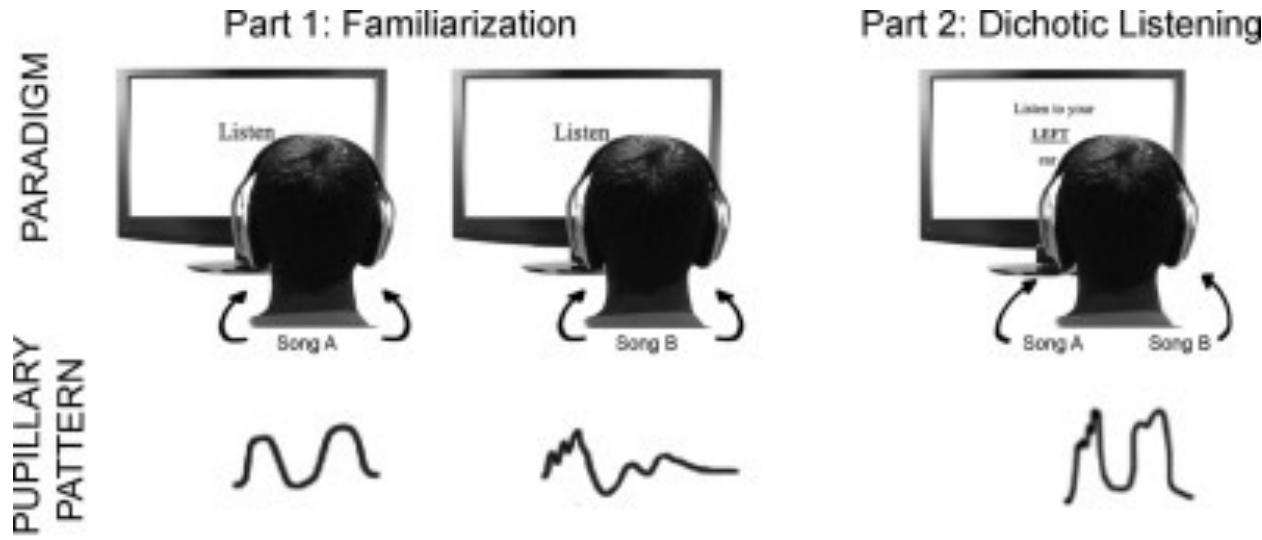


Can we decode which stimulus the person is listening to during dichotic presentation?

(a mean won't work)



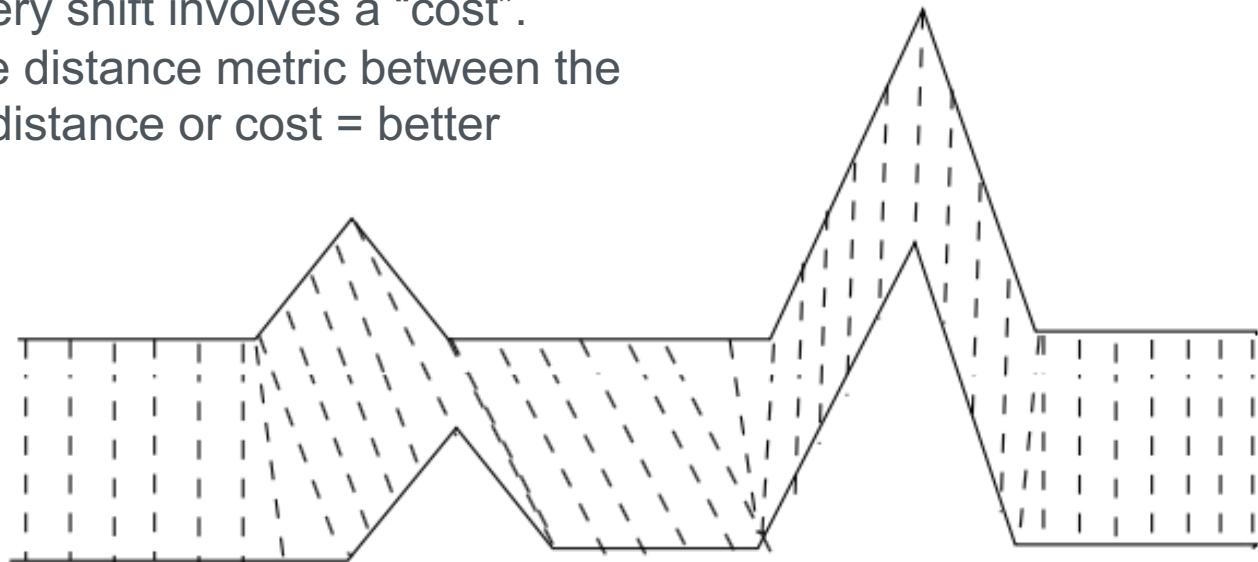
# Time series analyses & signal-to-signal approaches



# Dynamic Time Warping

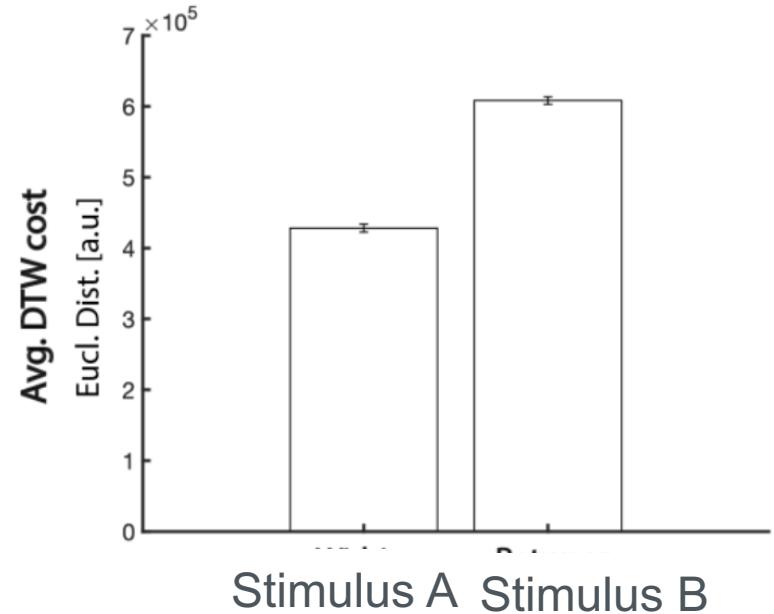
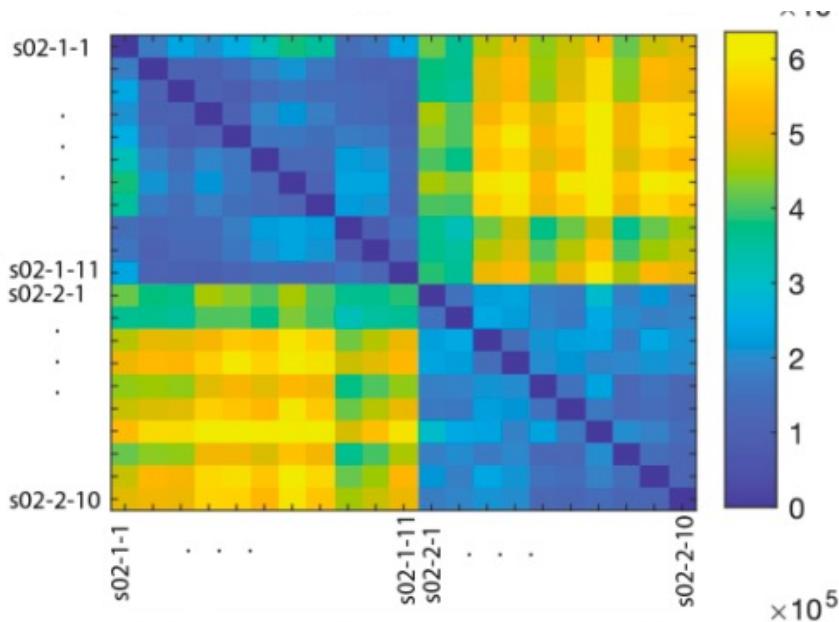
Allow for shifting of samples between signals to find best match. Every shift involves a “cost”.

Ultimately use some distance metric between the two signals. Lower distance or cost = better



<https://commons.wikimedia.org/w/index.php?curid=41617143>

## Dynamic Time Warping



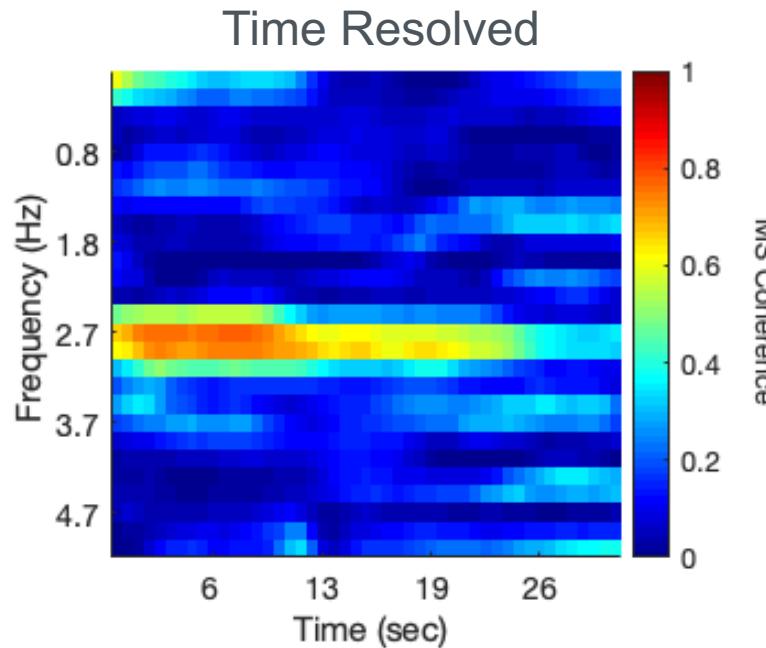
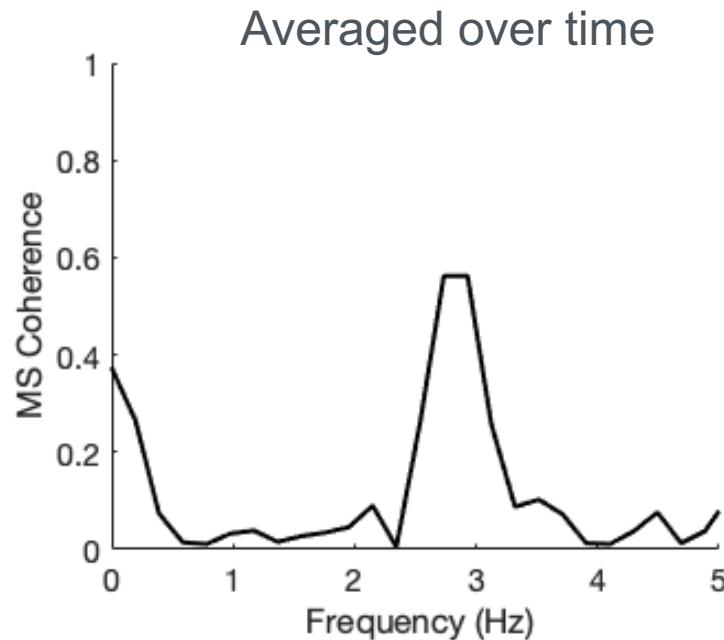
# Time series analyses & signal-to-signal approaches

What if you want to know how synchronized two signals are?

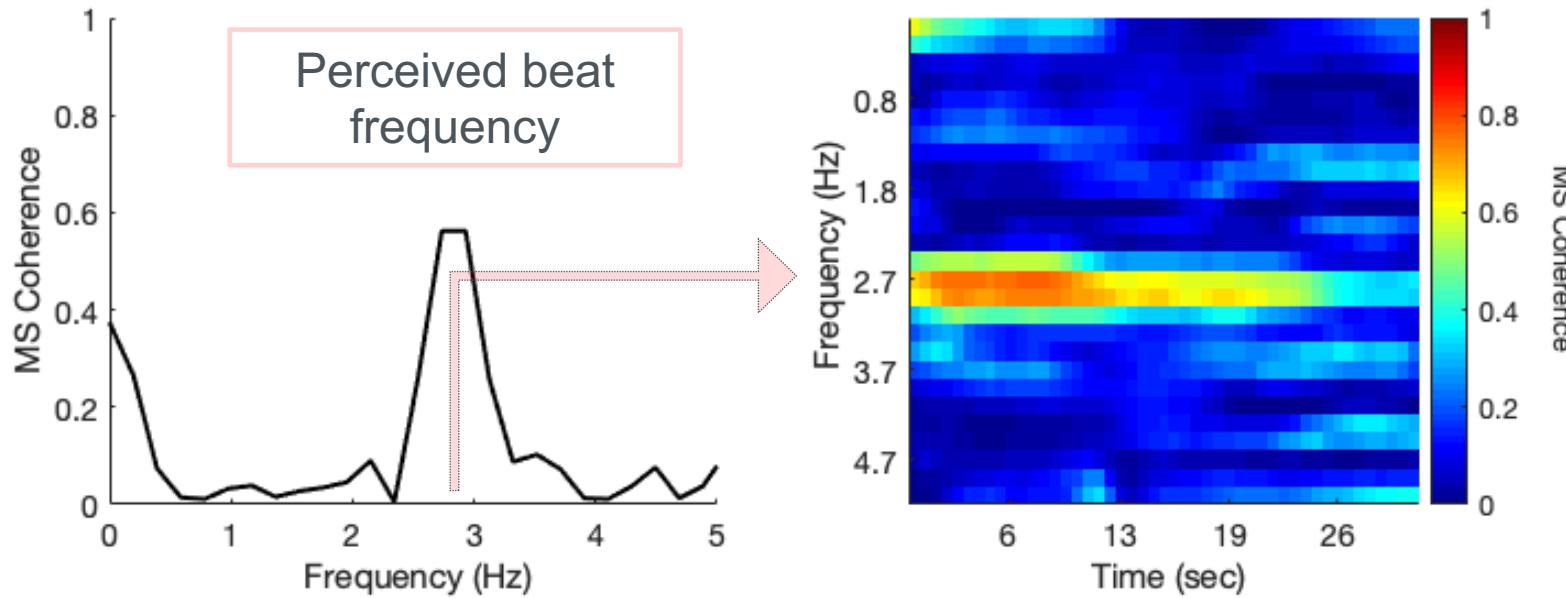
(a mean won't work)



## Phase Clustering

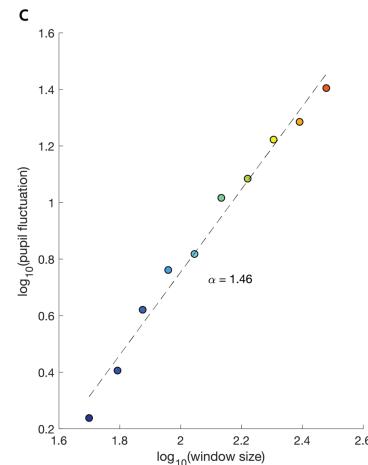
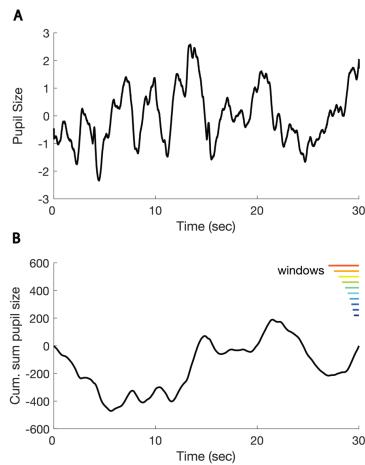


## Phase Clustering

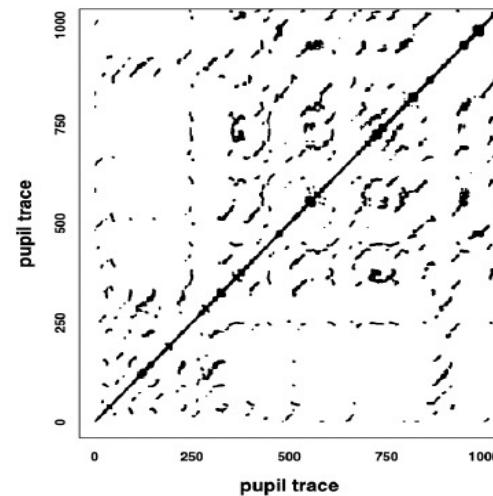


## Take-away: Novel analytic approaches → Novel insights

Detrended Fluctuation Analysis  
(e.g., do long range temporal correlations increase or decrease during certain states?)



Recurrence-based analyses  
(e.g., do patterns repeat in the data?)



Fink et al., 2023, *BRM*

# Let's play with some data!



Here are the data:

[https://beatlab.mcmaster.ca/assets/pupilTutorial/KonstanzWorkshop\\_pupilStimulus\\_TimeSeries.csv](https://beatlab.mcmaster.ca/assets/pupilTutorial/KonstanzWorkshop_pupilStimulus_TimeSeries.csv)

# Let's play with some data!



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These data come from the full code tutorial that accompanies the paper:

Fink, L., Simola, J., Tavano, A., Lange, E., Wallot, S., & Laeng, B. (2023).

From pre-processing to advanced dynamic modeling of pupil data. *Behavior Research Methods*, 1-37.

Code and more resources here: <https://github.com/lkfink/pupilTutorial>

The background image shows a beautiful autumn day on a university campus. A large, multi-story stone building with ivy growing on its walls is visible on the left. In the foreground, several students are sitting on the grass, which is covered with fallen orange and yellow leaves. A bicycle is leaning against a tree on the left. The sun is shining through the trees, creating a warm glow and lens flare. A large red circular graphic is positioned on the right side of the slide.

**Thank you!!**

**Questions?**

**Contact:**  
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