# Nuclear-powered Shipping

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### Abstract

Nuclear power was analyzed as an alternative to fossil fuel combustion for propulsion of large boats. In particular,  $\dots$ 

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## 2 Background and State of the Art

Background and state of the art

#### 3 Conceptual Design

- Naval concept 3.1
- 3.1.1Oceanic tug boat
- 3.1.2Offshore power plant and coastal tug boat
- 3.2 Reactor concept
- 3.2.1 Core concept
- 3.2.2Neutronics analysis

The following analysis determines the enrichment required to reach  $k_{\infty} = 1$ :

$$k_{\infty} = \eta f = 1 \tag{1}$$

$$= \nu \frac{\sigma_f^F}{\sigma_a^F} \frac{\Sigma_a^F}{\Sigma_a} \tag{2}$$

Approximate values of these parameters are given in table 1.

Table 1: Approximate values of nuclear properties germaine to equation 2, [9]

Parameter	Value	Unit
ν	2.4	-
σ_f, 235	1.2	barns
σ_a, 238	0.1	barns

The macroscopic cross section is by definition  $\Sigma = N\sigma = \frac{\rho N_{av}}{A}\omega$ . Equation 2 then reduces to:

$$1 = \nu \frac{235 \sigma_f}{235 \sigma_a} \frac{\frac{\omega}{235} 235 \sigma_a}{\frac{1-\omega}{238} \sigma_a}$$

$$= \nu \frac{235 \sigma_f}{238 \sigma_a} \frac{238\omega}{235(1-\omega)}$$

$$(3)$$

$$=\nu \frac{^{235}\sigma_f}{^{238}\sigma_a} \frac{238\omega}{235(1-\omega)} \tag{4}$$

Upon defining a new variable  $\xi = \nu^{\frac{235}{\sigma_f}}_{\frac{238}{\sigma_a}}$ , we find:

$$\frac{1}{\xi} = \frac{238\omega}{235(1-\omega)}\tag{5}$$

$$\frac{1}{\xi} = \frac{238\omega}{235(1-\omega)}$$

$$\omega = \frac{235}{238\xi + 235} < 1$$
(5)

Upon inserting the tabulated values for these cross sections, we find  $\xi = 4.2$ and  $\omega = 0.0336 = 3.4\%$ . The bulk of the reactor can thus be fueled without HEU.

If the fuel is  $UO_2$ , then the mass of Uranium per mass of fuel is:

$$\frac{m_U}{m_{UO2}} = \frac{238(1-\omega) + 235\omega}{238(1-\omega) + 235\omega + 32}$$

$$= 0.8817 \frac{grams}{gram}$$
(8)

$$=0.8817 \frac{grams}{gram} \tag{8}$$

It is now easy to find the number of  $U_{235}$  atoms per gram of fuel:

$$n_{235} = \omega \frac{m_u}{m_{UO_2}} \frac{N_{av}}{235} \tag{9}$$

$$=7.906 \times 10^{21} \tag{10}$$

If we assume that  $\frac{3}{4}$  of the fissions occur in  $U_{235}$ , then the total fissile atoms per gram of fuel is  $1.05 \times 10^{21}$ .

We can now determine the required mass of Uranium to produce a certain amount of energy. The core's power is related to the fission rate by a factor of 200 MeV per fission. We will assume a core power of 1.75 GWth for this analysis. This value roughly corresponds to 500 MWe for typical values of efficiency, which is close to the power output of the reactors we seek to imitate. The fission rate in our reactor is then  $1.75 \times 10^9 \frac{Joules}{sec} \times \frac{1MeV}{1.6 \times 10^{-13} Joules} \times \frac{1Fission}{200 MeV} =$  $5.5 \times 10^{19} \frac{fissions}{second}$ 

In an assumed 2-year refueling cycle we would then need  $5.5 \times$  $10^{19} \frac{fissions}{second} \times \frac{3.15 \times 10^7 s}{y} = 1.723 \times 10^{27}$  fissile atoms. Returning to our value of fissile atoms per gram of  $UO_2$ , we can find the

mass of Uranium required to power our core for two years. This number is  $5.5 \times 10^{19} \frac{fissions}{second} \times \frac{6.3 \times 10^7 s}{2years} = 3.5 \times 10^{27} \frac{fissions}{cycle}$ , which can be used to find the mass of fuel, and ultimately the volume of the reactor. Recall that we anticipate  $1.05 \times 10^{21}$  fissile nuclei per gram of fuel. The mass of fuel needed is then  $\frac{3.05 \times 10^{27}}{1.05 \times 10^{21}} = 2.90 \times 10^6 g = 2900 kg$ . However, we do not expect to burn every fissile isotope, so this value should be adjusted by a factor of 1.7, so that our first estimate of the mass of fuel is 4930 kg.

The density of  $UO_2$  is  $10970\frac{kg}{m^3}$ . The Volume of this much fuel is therefore  $V=\frac{4930kg}{10970\frac{kg}{m^3}}=4.50m^3$ 

We will assume that the volume of our cylindrical core is equal to the volume of a cylinder of the same radius, which is to say  $H = \frac{4}{3}\pi R$ . Under this assumption, the radius of our core is  $(\frac{3}{4}\pi V)^{1/3} = 2.20$  meters, giving a height of 2.93 meters. This first estimate of the height (which will most likely be shorter than the final value) will be very useful in the thermal analysis.

### 3.2.3 Thermal analysis

Let us begin by estimating the mass flow rate required to remove the fission heat at steady state. With a simple energy balance, it becomes apparent that heat flux is related to the heat capacity and mass flow rate of the coolant and the temperature change across the length of the channel as follows:

$$q'' = \dot{m}c_p \Delta T \tag{11}$$

$$\dot{m} = \frac{q''}{c_n \Delta T} \tag{12}$$

We can estimate q" by dividing the thermal power by the surface area of the fuel, which gives us  $q'' = \frac{1.5 \times 10^9}{2\pi N 2.93 \times 10^{-2}}$  if there are N fuel rods, each with 1-cm radius 2.93 meters tall

### 3.2.4 Materials analysis

#### 3.2.5 Alternatives

Conceptual design

## 4 Conclusions

Conclusions

## 5 Acknowledgements

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