

Automated Verification of Safety Properties of Declarative Networking Programs

Chen Chen¹, **Lay Kuan Loh**², Limin Jia², Wenchao Zhou³, Boon Thau Loo¹
¹University of Pennsylvania, ²Carnegie Mellon University, ³Georgetown University

July 15, 2015

Networks are complex and error-prone

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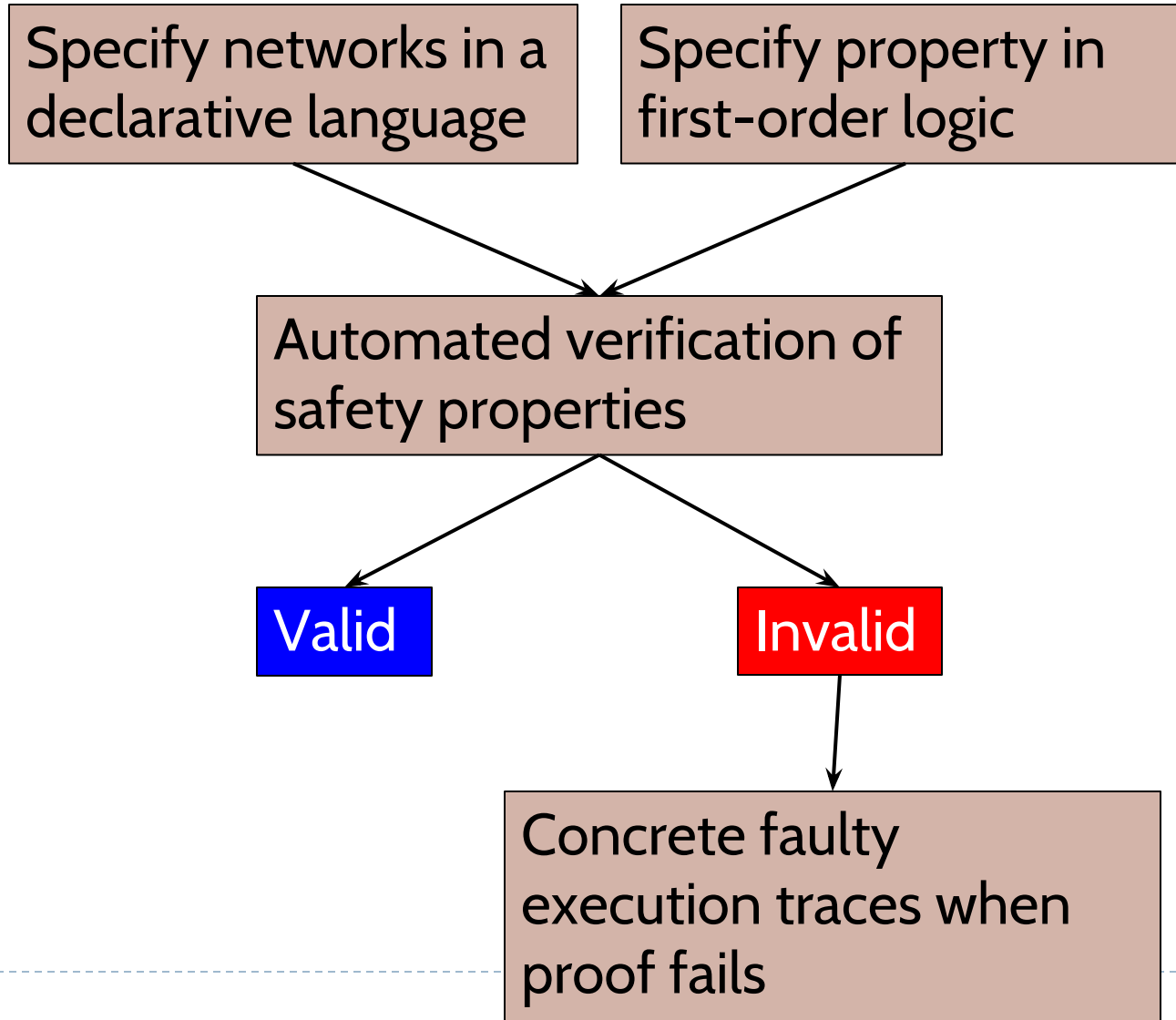


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Our solution

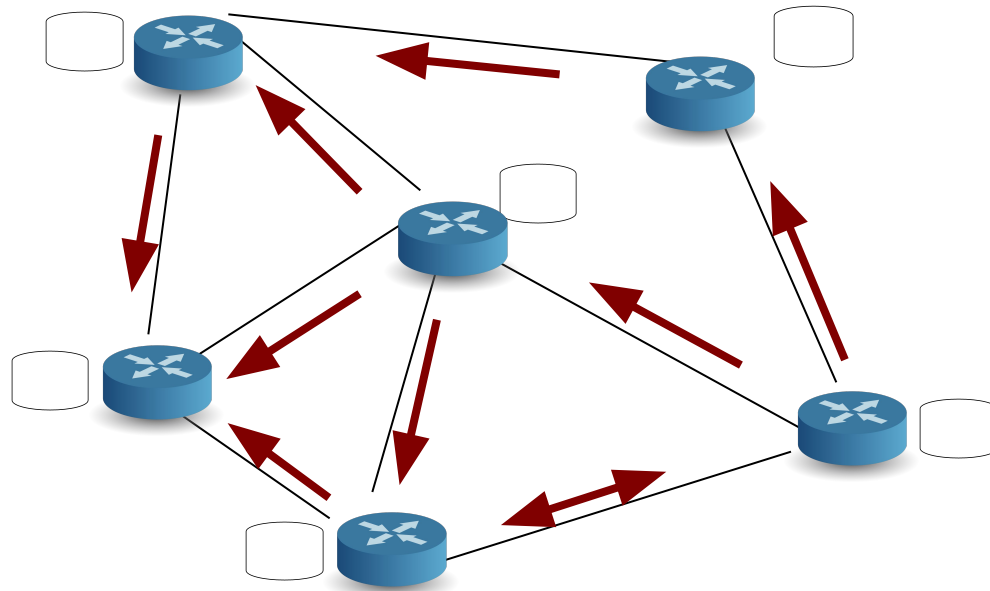


Roadmap

- Introduction of NDLog (Network Datalog)
- Algorithm analysis
 - Derivation pool construction
 - Property query
 - Network constraints
 - Recursive programs
- Case study
- Conclusion

Network Datalog (NDLog) [CACM'09]

- A distributed variant of Datalog
- Recursive query language over network states



Traditional Networks

- Network state 
- Network Protocol

Declarative Networks

- Distributed Database
- Datalog Program

Rule format of NDLog

- Rule Head :- Body₁, Body₂, ..., Body_n, Constraint
- @: Location specifier

Twohops

R1 onehop(@z,x,c2) :- link(@z,x,c2)

R2 twohops(@x,y,c) :- link(@z,y,c1), onehop(@z,x,c2), c=c1+c2

Running an example NDLog program

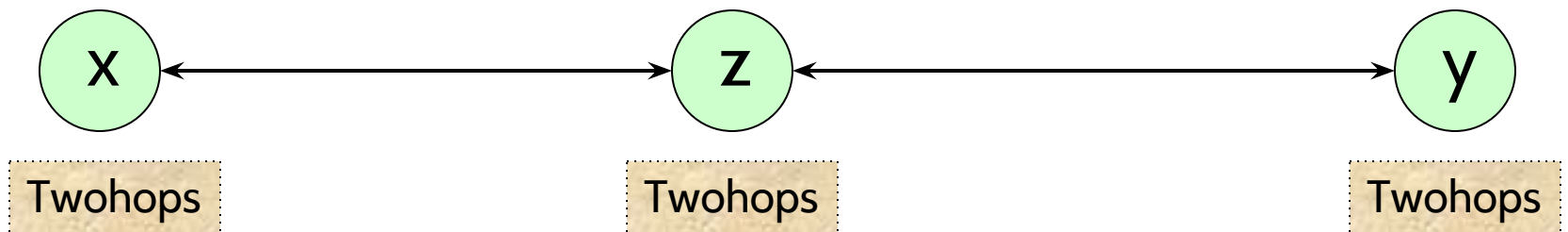
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R1 onehop(@z,x,c2) :- link(@z,x,c2)

R2 twohops(@x,y,c) :- link(@z,y,c1), onehop(@z,x,c2), $c=c1+c2$

link

@Src	Dst	Cost
@z	y	c1
@z	x	c2



Running an example NDLog program

Twohops

R1 onehop(@z,x,c2) :- link(@z,x,c2)

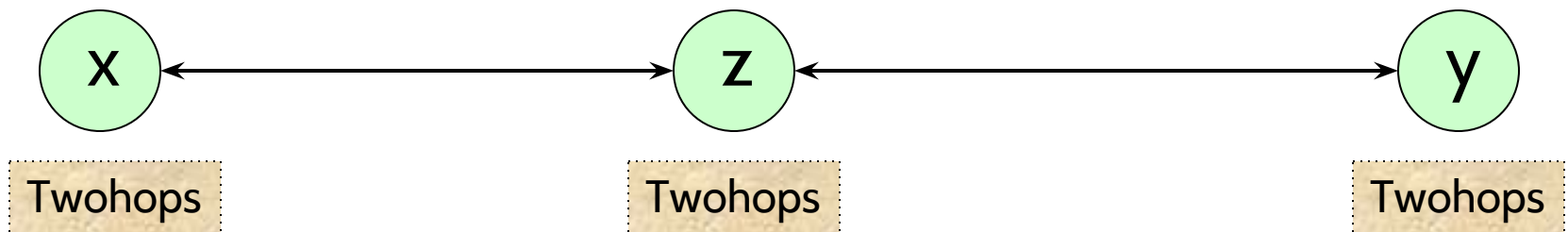
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link

@Src	Dst	Cost
@z	y	c1
@z	x	c2

oneho

@Src	Dst	Cost
@z	x	c2



Running an example NDLog program

Twohops

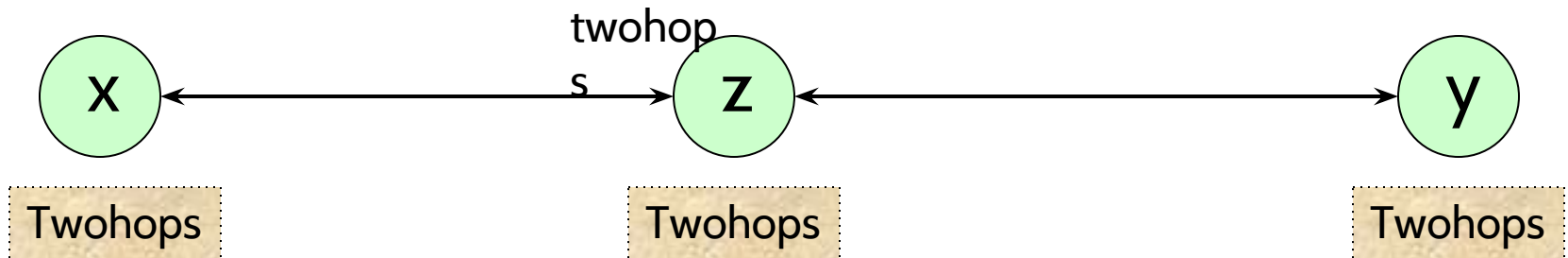
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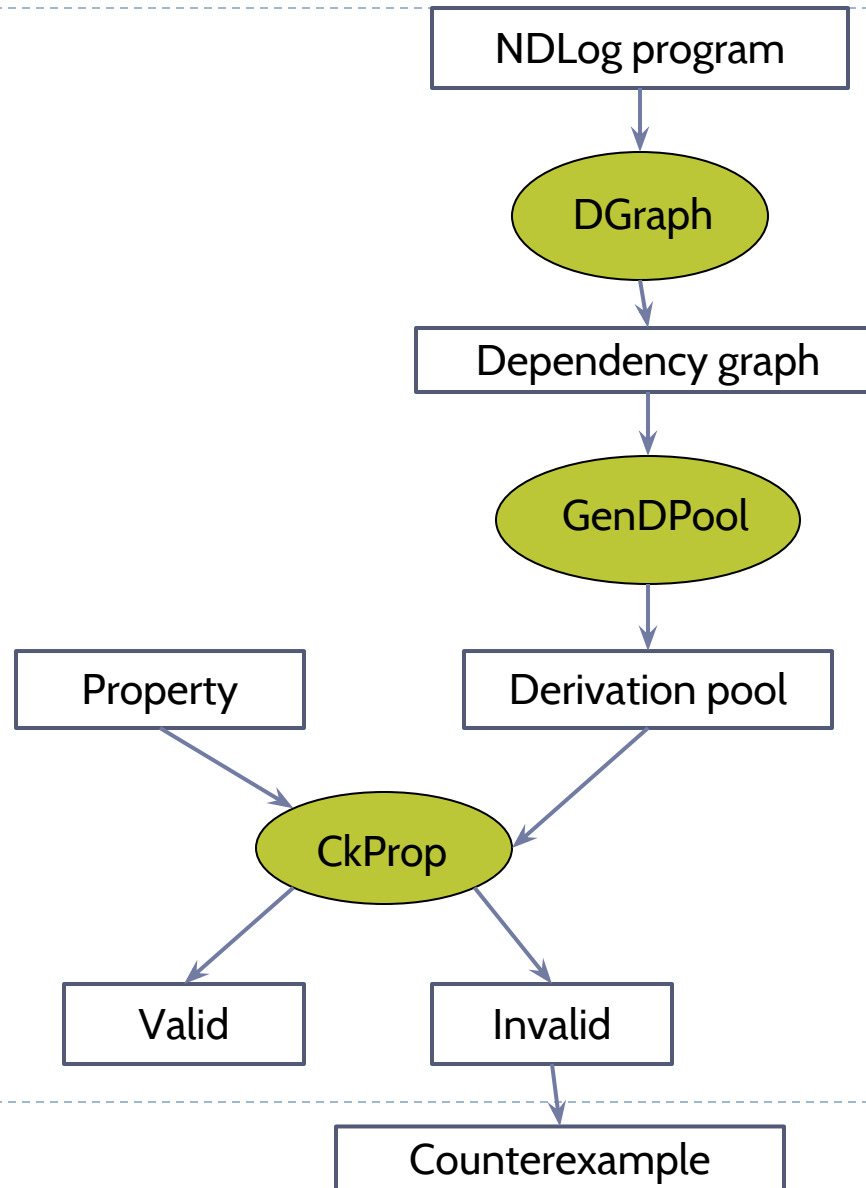
@Src	Dst	Cost
@x	y	c

link		
@Src	Dst	Cost
@z	y	c1
@z	x	c2

oneho		
@Src	Dst	Cost
@z	x	c2



Overview of framework



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NDLog program \Rightarrow Dependency graph

- Dependency Graph G:

Vertex:

- V1: Tuple nodes
- V2: Rule nodes

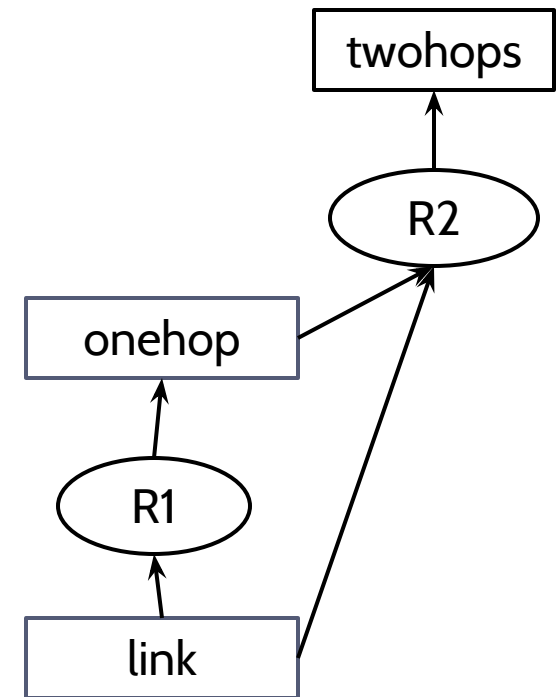
Edge:

- (rule node \rightarrow head node)
- (body node \rightarrow rule node)

Twohops

R1 onehop(@z,x,c2) :- link(@z,x,c2)

R2 twohops(@x,y,c) :- link(@z,y,c1), onehop(@z,x,c2),
c=c1+c2



Dependency graph \Rightarrow Derivation pool

R1 onehop(@z,x,c2) :- link(@z,x,c2)
 R2 twohops(@x,y,c) :- link(@z,y,c1), onehop(@z,x,c2), c=c1+c2



R1 onehop(@x₁,x₂,x₃) :- link(@x₄,x₅,x₆), x₁=x₄ \wedge x₂=x₅ \wedge x₃=x₆
 R2 twohops(@x₇,x₈,x₉) :- link(@x₁₀,x₁₁,x₁₂), onehop(@x₁₃,x₁₄,x₁₅), x₇=x₁₄ \wedge x₈=x₁₁ \wedge x₁₀=x₁₃ \wedge x₉=x₁₂+x₁₅

Constraints Derivations

Link	Onehop
(BaseTuple, link (z _{λ1} ,z _{λ2} ,z _{λ3}))	(R1, onehop(z _{o1} ,z _{o2} ,z _{o3}), (BaseTuple, link(z _{o4} ,z _{o5} ,z _{o6}))::nil)
True	z _{o1} =z _{o4} \wedge z _{o2} =z _{o5} \wedge z _{o3} =z _{o6}

Twohops
(R2, twohops(z _{t7} ,z _{t8} ,z _{t9}), (BaseTuple,link(z _{t10} ,z _{t11} ,z _{t12})) :::(R1,onehop(z _{t13} ,z _{t14} ,z _{t15}), (BT,link(z _{t3} ,z _{t4} ,z _{t5})):: nil) ::nil)
(z _{t3} =z _{t13} \wedge z _{t4} =z _{t14} \wedge z _{t5} =z _{t15}) \wedge (x _{t7} =x _{t14} \wedge x _{t8} =x _{t11} \wedge x _{t10} =x _{t13} \wedge x _{t9} =x _{t12} +x _{t15})

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Property specification

- Safety property
 - Something bad never happens
- Restricted property format:
 - ♦ Indicates the temporal operation “past”

$$\forall \mathbf{x}_1.p_1(\mathbf{x}_1) \wedge \forall \mathbf{x}_2.p_2(\mathbf{x}_2) \wedge \dots \wedge \forall \mathbf{x}_n.p_n(\mathbf{x}_n) \wedge c_q(\mathbf{x}_1, \dots, \mathbf{x}_n) \supset \\ \exists \mathbf{y}_1.\diamond q_1(\mathbf{y}_1) \wedge \exists \mathbf{y}_2.\diamond q_2(\mathbf{y}_2) \wedge \dots \wedge \exists \mathbf{y}_m.\diamond q_m(\mathbf{y}_m) \wedge c_q(\mathbf{x}_1, \dots, \mathbf{x}_n, \mathbf{y}_1, \dots, \mathbf{y}_m)$$

- Example:
 - $\forall x_1, x_2, x_3. \text{onehop}(x_1, x_2, x_3) \wedge x_3 > 0 \supset$
 $\exists y_1, y_2, y_3. \diamond \text{link}(y_1, y_2, y_3) \wedge y_3 < 0$

Property verification algorithm

- Verify the property holds for all possible derivations
 - Enumerate all derivations for the tuples in the antecedent

$$\varphi = \forall x_1, x_2, x_3. \text{onehop}(x_1, x_2, x_3) \wedge x_3 > 0 \supset \exists y_1, y_2, y_3. \blacklozenge \text{link}(y_1, y_2, y_3) \wedge y_3 < 0$$

link?

Derivation of onehop in derivation pool

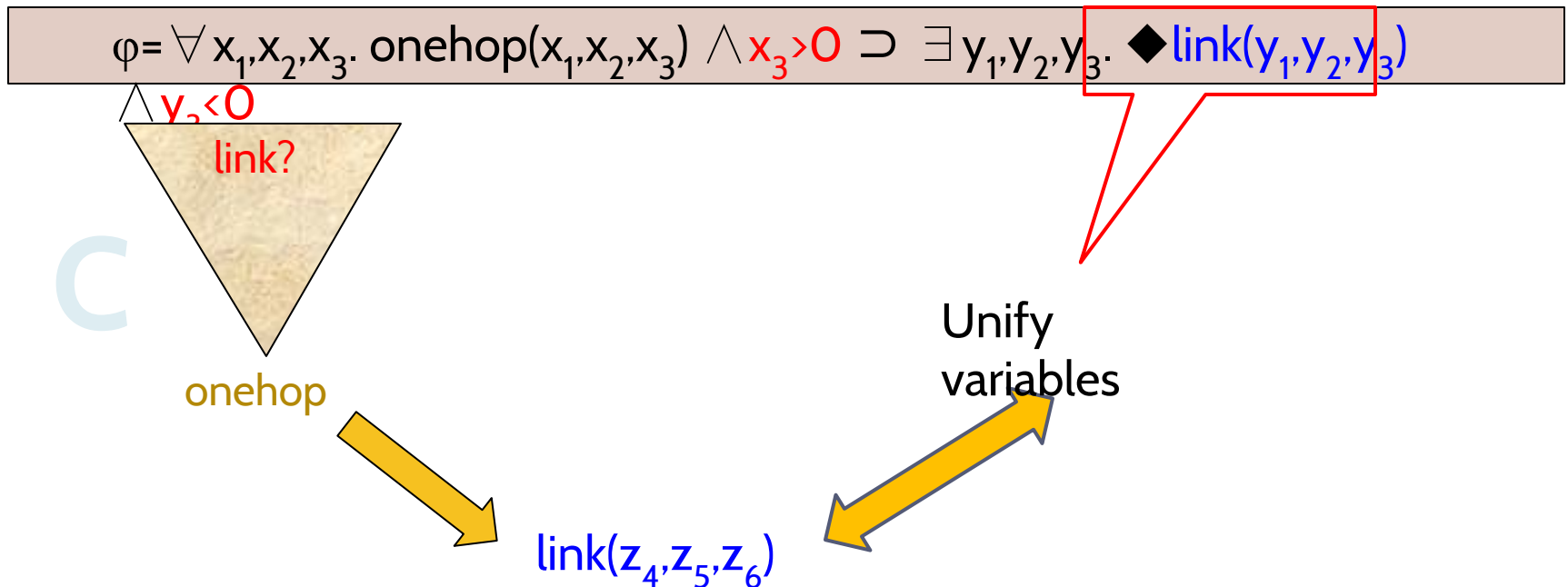
onehop



Constraint in derivation pool for the derivation on onehop

Property verification algorithm

- Verify existence of tuples in the conclusion
 - Look for instances of tuples in the given derivation



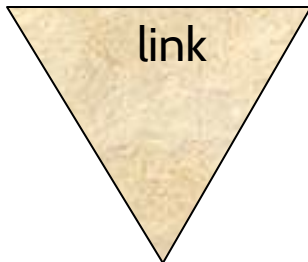
Property verification algorithm

- Verify validity of constraints
 - SMT solver

$$\varphi = \forall x_1, x_2, x_3. \text{onehop}(x_1, x_2, x_3) \wedge x_3 > 0 \supset \exists y_1, y_2, y_3. \blacklozenge \text{link}(y_1, y_2, y_3)$$

$$\wedge y_3 < 0$$

C



onehop



$x_3 > 0$



$y_3 < 0$



SMT
solver

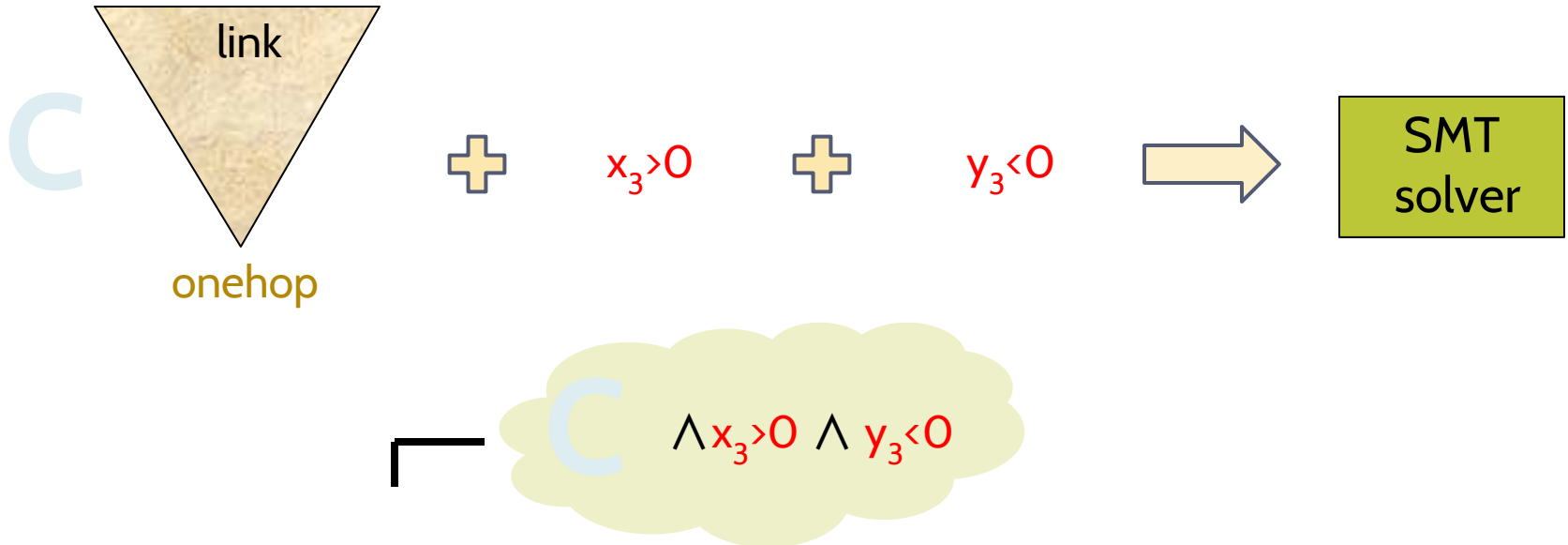
INVALID

Property verification algorithm

- Find a satisfying substitution for the negation of the constraints to generate a concrete counterexample

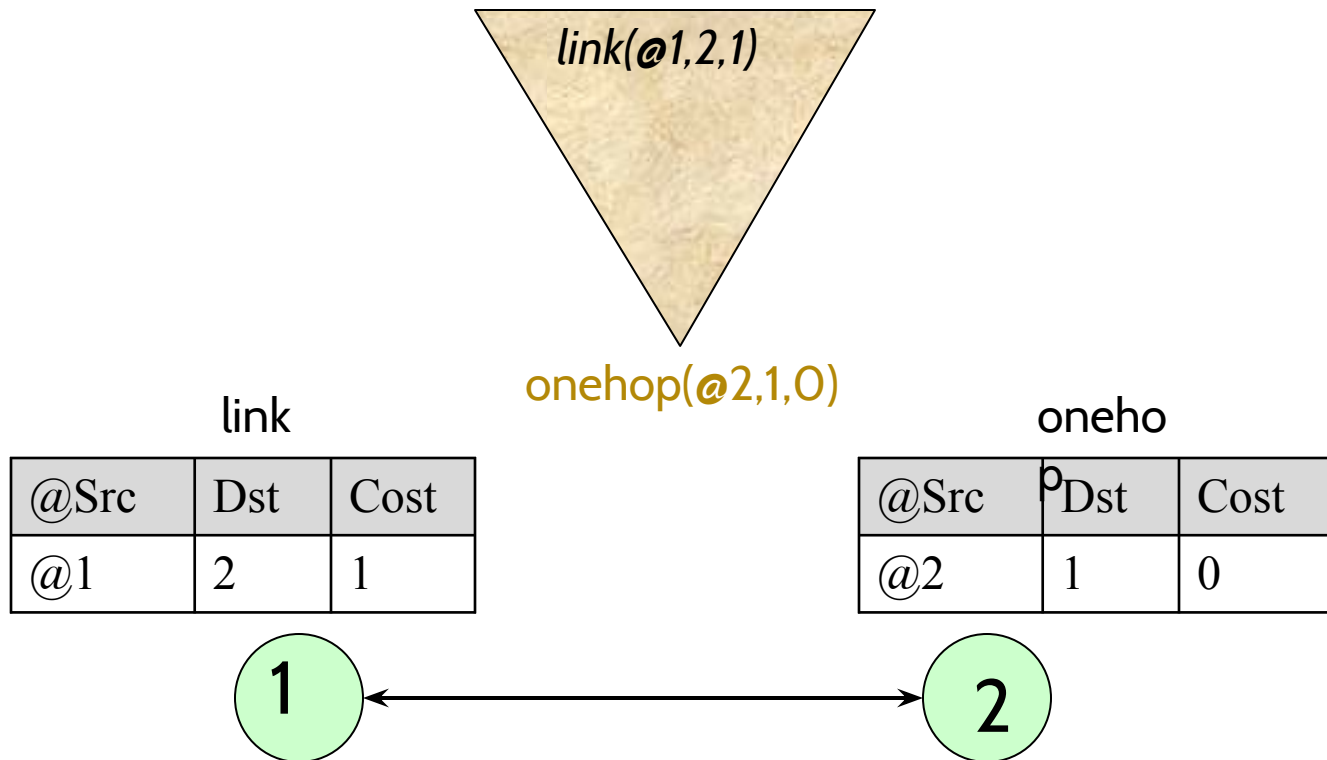
$$\varphi = \forall x_1, x_2, x_3. \text{onehop}(x_1, x_2, x_3) \wedge x_3 > 0 \supset \exists y_1, y_2, y_3. \blacklozenge \text{link}(y_1, y_2, y_3)$$

$$\wedge y_3 < 0$$



Property verification algorithm

$$\varphi = \forall x_1, x_2, x_3. \text{onehop}(x_1, x_2, x_3) \wedge x_3 > 0 \supset \exists y_1, y_2, y_3. \blacklozenge \text{link}(y_1, y_2, y_3) \wedge y_3 < 0$$

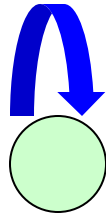


Roadmap

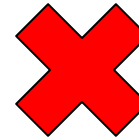
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Network constraint examples

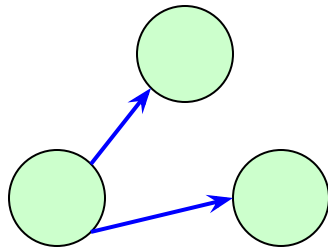
$$\varphi_{\text{net}} = \forall u_1, u_2, u_3. \text{link}(u_1, u_2, u_3) \supset u_1 \neq u_2$$



No self-loops



$$\varphi_{\text{net}} = \forall u_1, u_2, u_3. \text{link}(u_1, u_2, u_3) \wedge \forall u_4, u_5, u_6. \text{link}(u_4, u_5, u_6) \supset (u_1 = u_4 \rightarrow u_2 \neq u_5)$$



Every node in the network
has only one outgoing link



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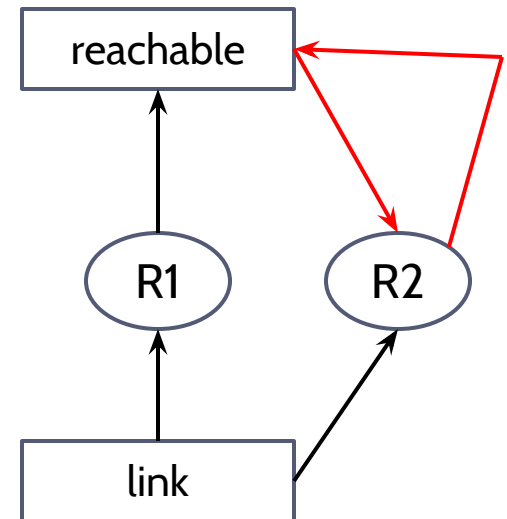
Recursive programs

- Dependency graph has cycles
- Break the cycle using user-provided annotations on tuples on the cycle
 - Equivalent to disjunction of constraints over the list of possible derivations for tuples on the cycle

Reachability

R1 reachable(*@x,y*) :- link(*@x,y*)

R2 reachable(*@x,y*) :- link(*@x,z*), reachable(*@z,y*)

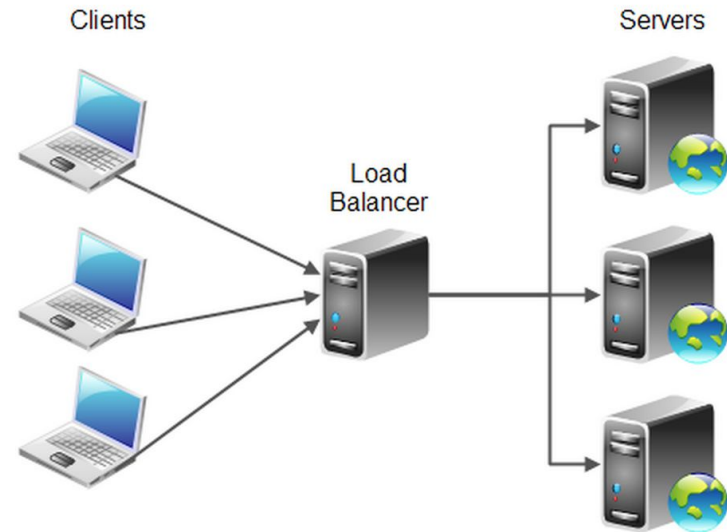


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Introduction to load balancers

- A way to distribute client requests to an application onto multiple servers
 - Allows application to process a higher work load
 - Provides redundancy in an application
- Flow affinity
 - Packets received on different servers cannot share the same source address



Flow affinity

- Packets received on different servers cannot share the same

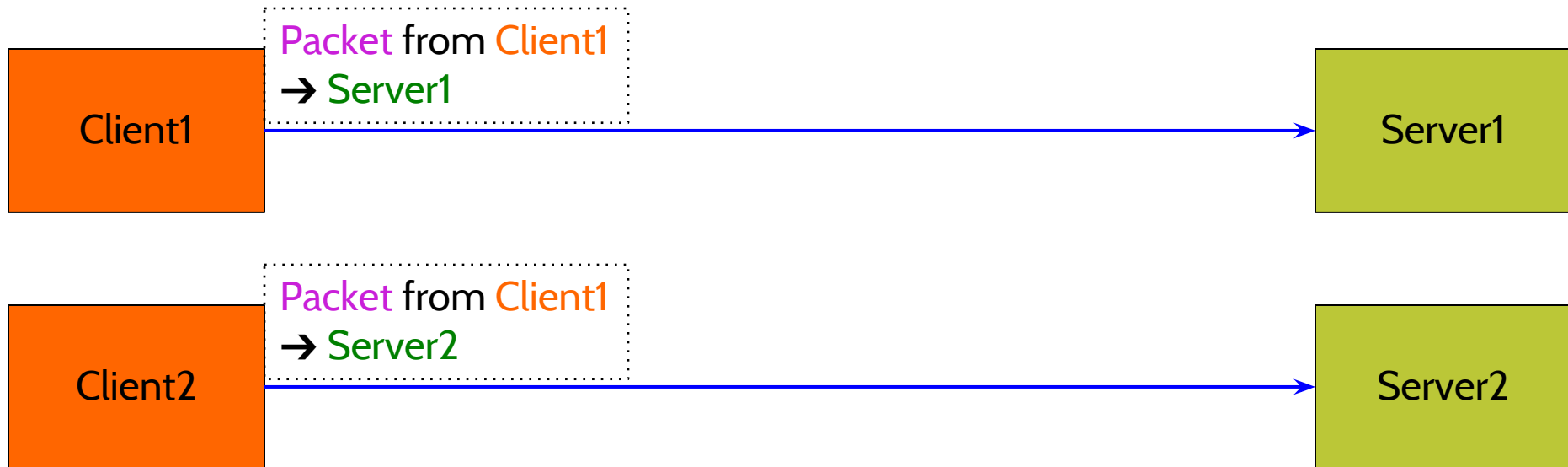
\forall Server1, Client1, LoadBalancer1. \forall Server2, Client2, LoadBalancer2.

$\text{recvPacket}(\text{Server1}, \text{Client1}, \text{LoadBalancer1})$

$\wedge \text{recvPacket}(\text{Server2}, \text{Client2}, \text{LoadBalancer2})$

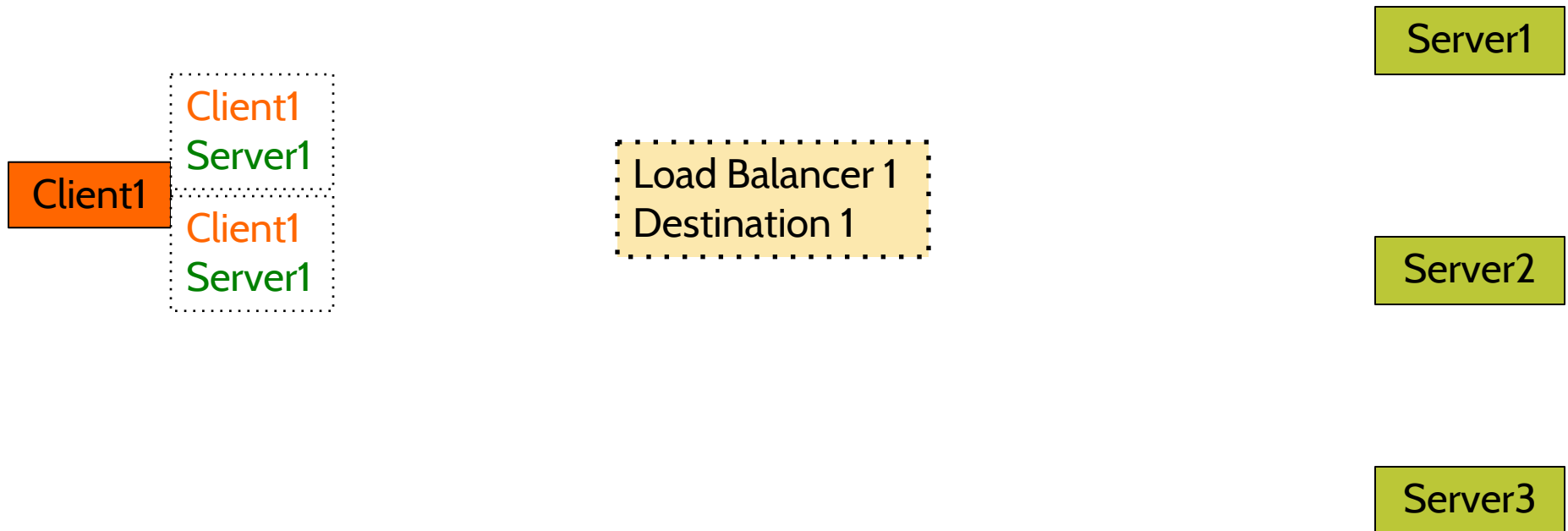
$\wedge \text{Server1} \neq \text{Server2} \supset$

$\text{Client1} \neq \text{Client2}$

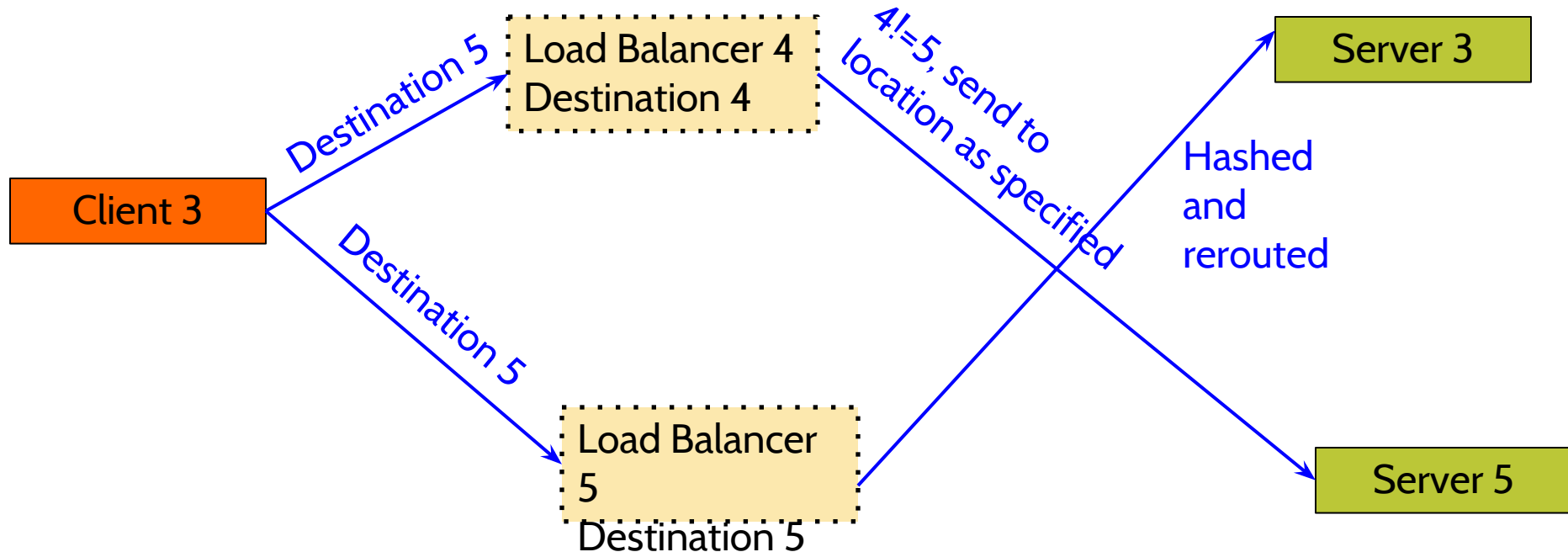


A naïve load balancer

- Our load balancer balances traffic towards a specific destination address
 - Determines the path of a packet based on the hash value of its source address



Counterexample produced by our tool



∇ Server1, Client1, LoadBalancer1. ∇ Server2, Client2, LoadBalancer2.

$\text{recvPacket}(\text{Server1}, \text{Client1}, \text{LoadBalancer1})$

$\wedge \text{recvPacket}(\text{Server2}, \text{Client2}, \text{LoadBalancer2})$

$\wedge \text{Server1} \neq \text{Server2} \supset$

$\text{Client1} \neq \text{Client2}$

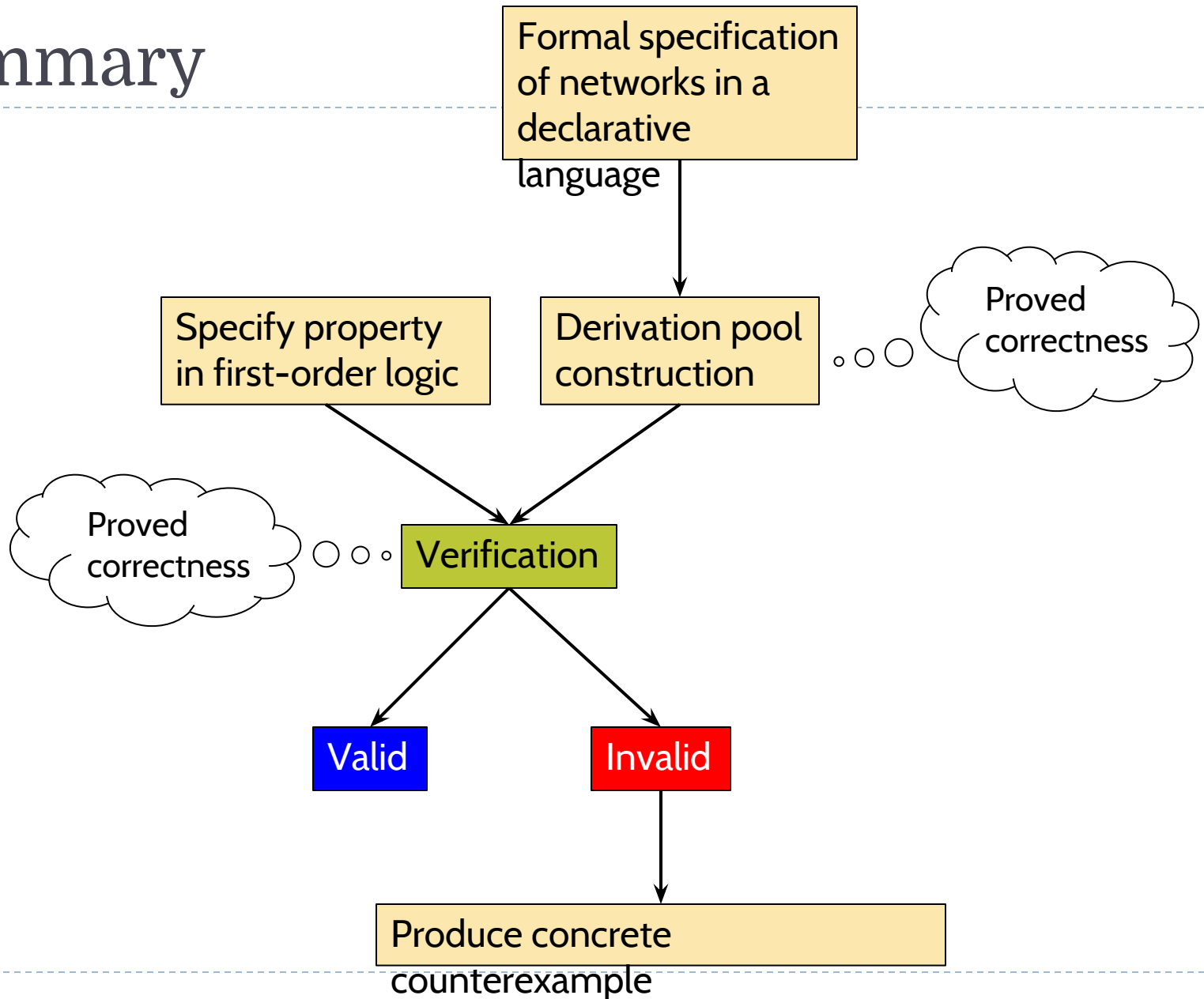
Case studies

Test Case	# rules	# properties	# counterexamples	Max eval time (ms)
Ethernet source learning	11	5	2	60
Firewall	5	3	0	40
Load balancer	4	1	1	80
Address resolution	9	2	0	210

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Summary



Related work

- **Network verification**
 - Model network behavior using trace semantics. Relies on manual proofs
 - Examples: FORTE'14, TPHOLs'09
 - *Our solution: Enables automated static analysis of safety properties, generates counterexamples for debugging purposes*
- **Software defined networking (SDN) verification**
 - Specific to analyzing SDN controllers and data places
 - Examples: PLDI'14, SIGCOMM'11
 - *Our solution: Does the above, can also analyze other distributed systems expressible in NDLog*
- **Verification of declarative programs**
 - Proves correctness properties of networking protocols using theorem provers. User experience with theorem provers required.
 - Example: PADL'09
 - *Our solution: Validate protocol correctness using an SMT solver. User experience with SMT solvers unnecessary.*

Future work

- Analyze liveness properties
 - Something good eventually happens
- Provenance related topics

Questions?



Time complexity (non-recursive)

- Notation

- $P = p_1, \dots, p_n$
 - $|P|=n$
- $Q = q_1, \dots, q_m$
 - $|Q|=m$
- Given an NDLog program with R rules
 - Each rule has at most W body tuples

$$\begin{aligned} & \forall \mathbf{x}_1. p_1(\mathbf{x}_1) \wedge \forall \mathbf{x}_2. p_2(\mathbf{x}_2) \wedge \dots \wedge \forall \mathbf{x}_n. p_n(\mathbf{x}_n) \\ & \wedge c_q(\mathbf{x}_1, \dots, \mathbf{x}_n) \supset \\ & \quad \exists \mathbf{y}_1. \blacklozenge q_1(\mathbf{y}_1) \wedge \exists \mathbf{y}_2. \blacklozenge q_2(\mathbf{y}_2) \wedge \dots \wedge \exists \mathbf{y}_m. \blacklozenge q_m(\mathbf{y}_m) \\ & \wedge c_q(\mathbf{x}_1, \dots, \mathbf{x}_n, \mathbf{y}_1, \dots, \mathbf{y}_m) \end{aligned}$$

- Time complexity: $O((R^{nW^R})n^mW^{Rn})$
- In practice, R and W are small
 - Can be treated as constants

Possible ways to fix the network counterexample

- Add network assumptions
 - Servers are connected to at most one load balancer
- Change property specification
 - Load balanced packets that are forwarded out of different load balancers were not sent out by the same client