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How Riemannian Geometry transformed BCI?



Bernhard Riemann
1826-1866



Elwin Bruno
Christoffel
1829-1900



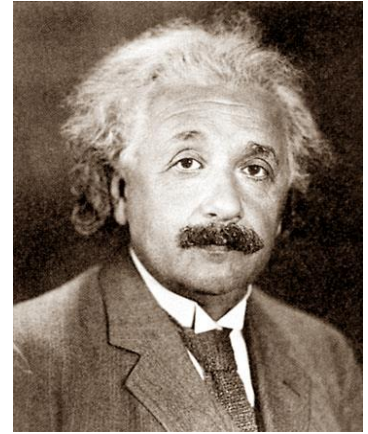
Gregorio Ricci
Cubastro
1853-1925



Tullio Levi-Civita
1873-1941



Albert Eninstein
1879-1955

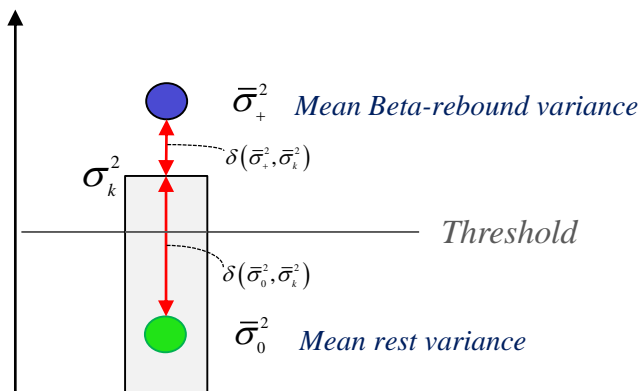
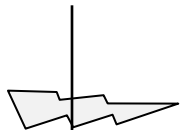


Riemannian Geometry in BCI: a Short History

1977

Vidal

UCLA



1995

Only six
research
groups

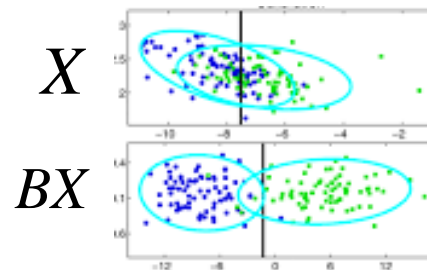
2000

Ramoser et *al.*
UTG



Introduction of the Fukunaga-Koontz transform

$$\lambda_i b_i = (C_1^{-1} C_2) b_i$$



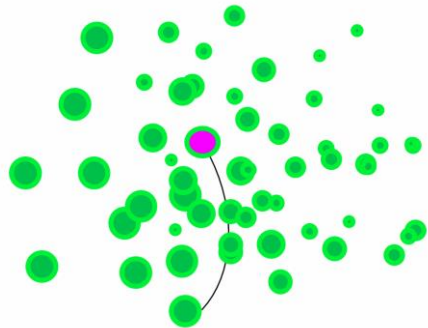
2010

Barachant et *al.*
UGA

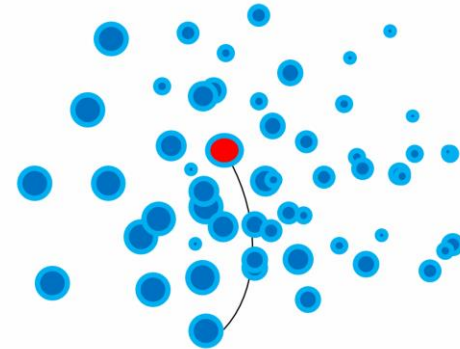


Introduction of Riemannian Geometry

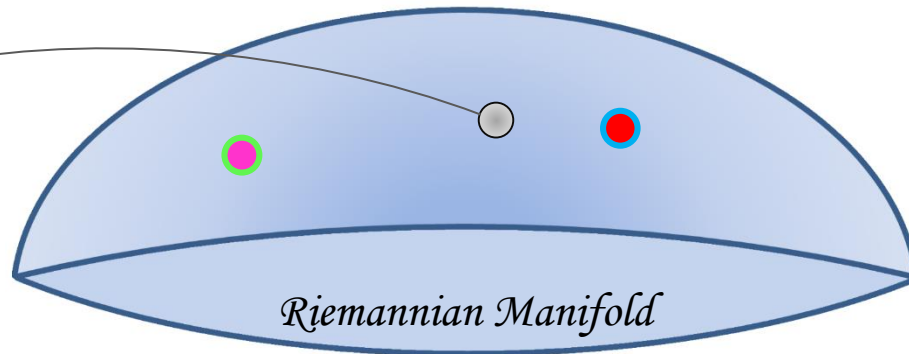
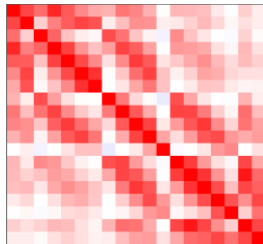
Minimum Distance to Mean (MDM) Classifier



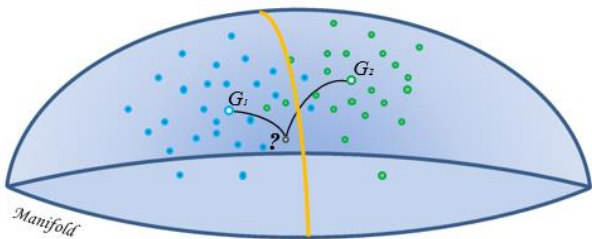
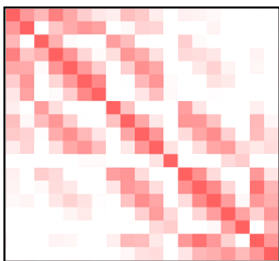
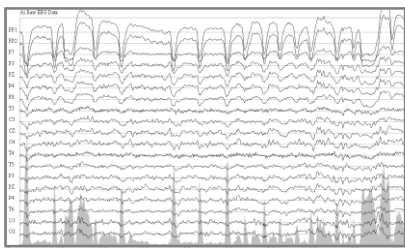
Class 1



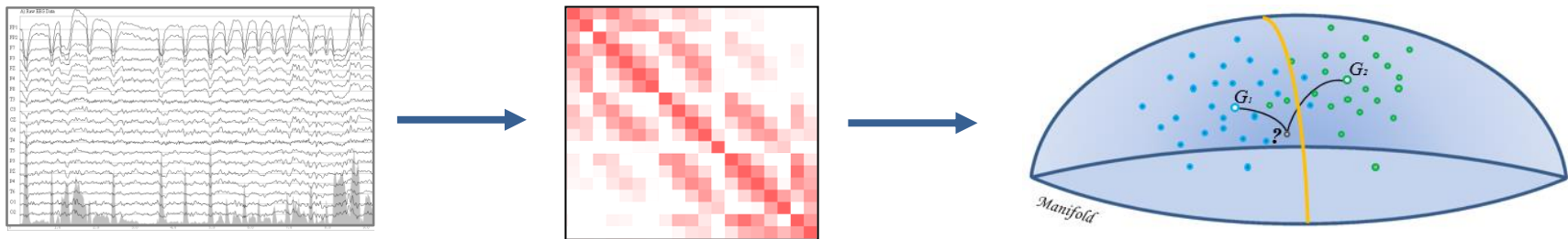
Class 2



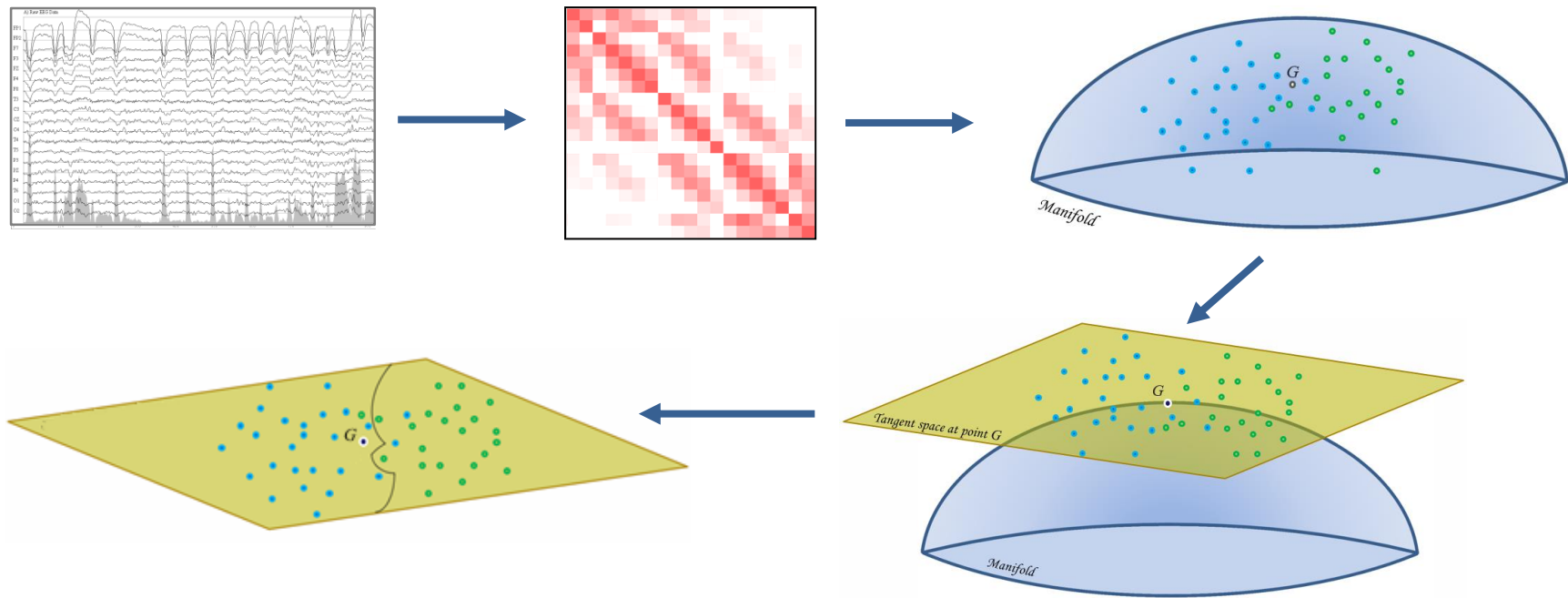
ML on Manifold



ML on Manifold



ML on Tangent Space



2012

Barachant et *al.*
UGA



Riemannian MDM and TS classification
(seminal paper)

2013

Barachant et *al.*
UGA



First *Transfer Learning* attempts

2014

Barachant & Congedo
UGA



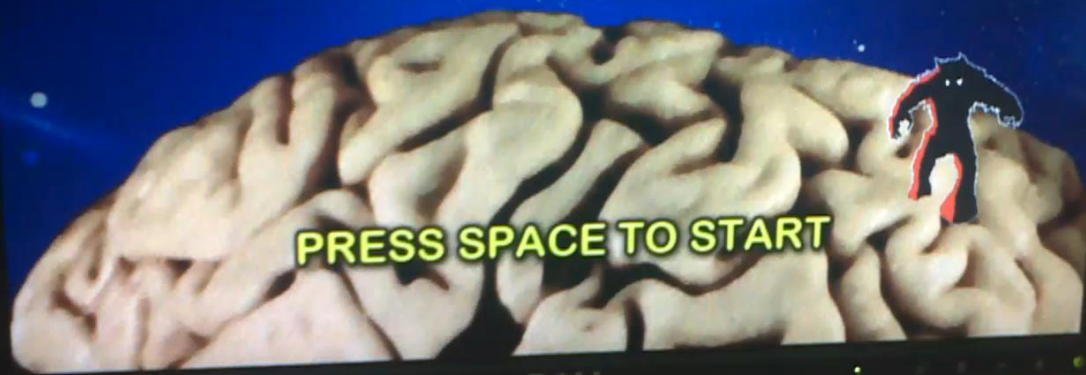
First working demonstrator of *calibration-less* BCI
« Brain Invaders »





gipsa-lab

BRAIN INVADERS



PRESS SPACE TO START

DELL

2013

F. Yger and
S. Chevallier

Independent groups in the BCI field
start contributing and confirming efficacy

2014

Barachant.
UGA



Riemannian Geometry wins an international
competition (over 301 participants)

2015

Korczowski et al.
UGA



First working demonstrator of a *multi-user* BCI

2015

Barachant

Riemannian Geometry wins two more international
Competition (over 311 & 452 participants)

2016

Barachant

Riemannian Geometry wins two more international
Competition (over 688 & 7 participants)



2017

Congedo et al.
Yger et al.



First comprehensive reviews on Riemannian
Geometry for BCI.

2018

Zanini et al.
UGA

Unsupervised Transfer Learning

2019

Rodrigues et al.
UGA



Riemannian Procrustes Analysis (RPA):
Semi-supervised Transfer Learning

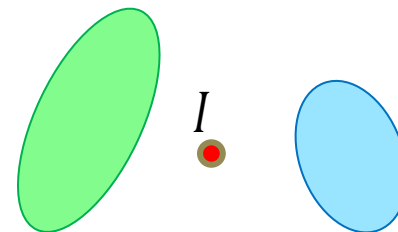


Riemannian Procrustes Analysis (RPA)

unsupervised
supervised

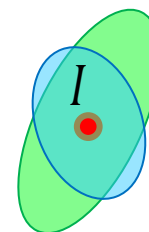
Original Data

$$C_k$$



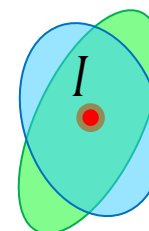
Recentering

$$C_k \leftarrow G^{-1/2} C_k G^{-1/2}$$



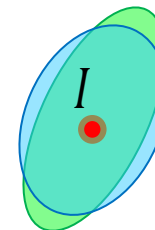
Stretching

$$C_k \leftarrow C_k^p$$

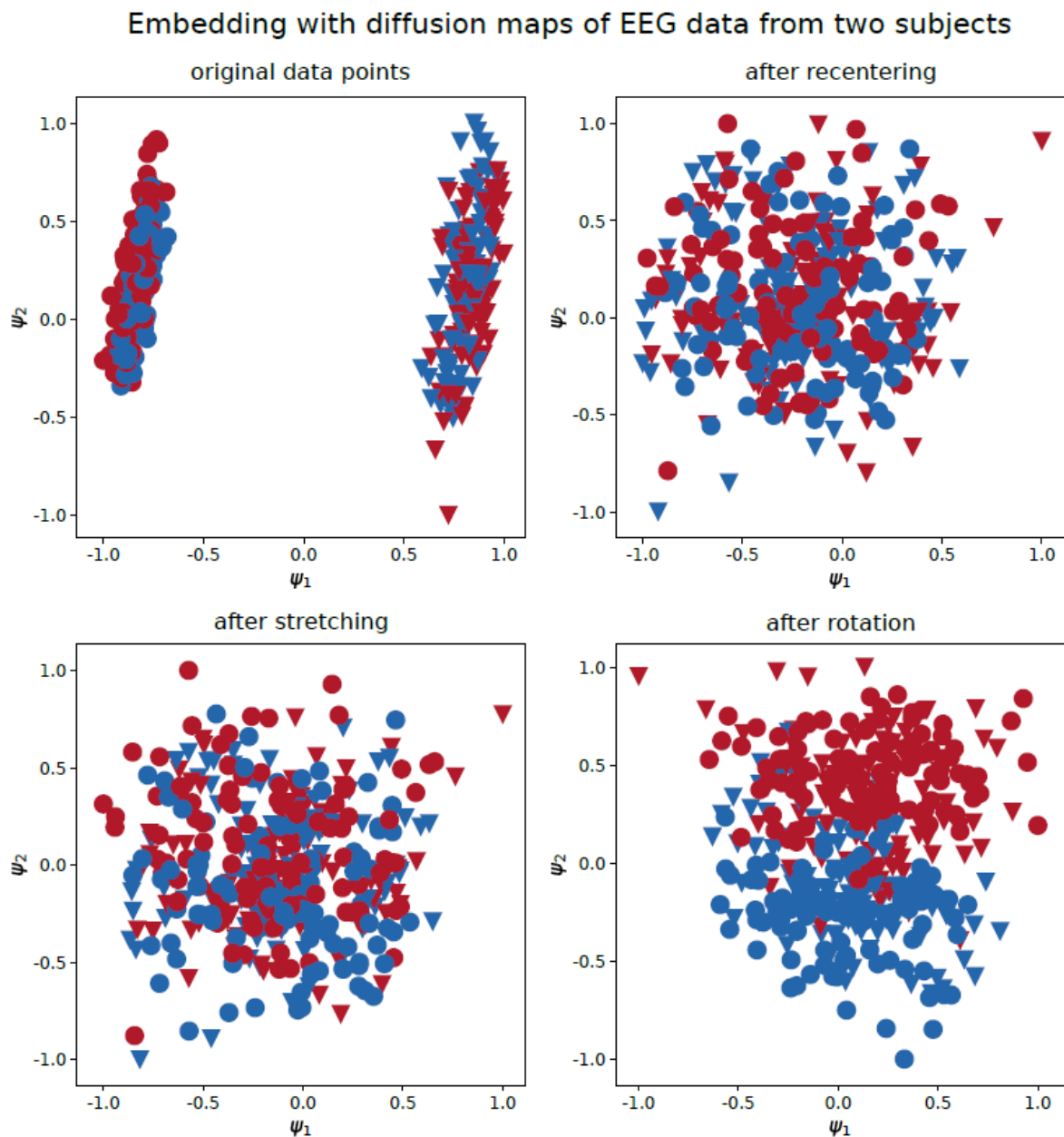


Rotation

$$C_k \leftarrow U C_k U^T$$



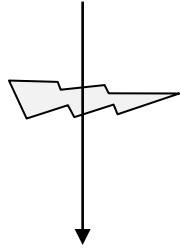
Real Data Example



Cho2017 (MI, 40 ss, 23 elec., 2 classes).

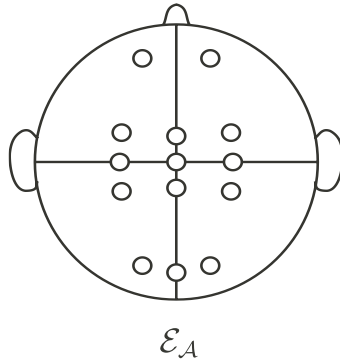
Visualization: Spectral Embedding
 ψ_1 ψ_2 are the eigenvalues of the Laplacian

2021
Rodrigues et al.
UGA



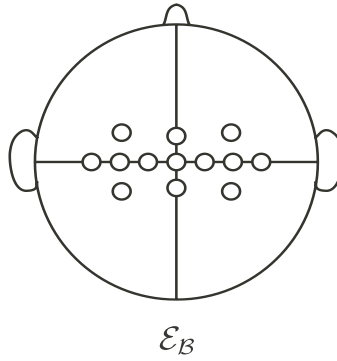
RPA for heterogeneous domains

Zhou2016



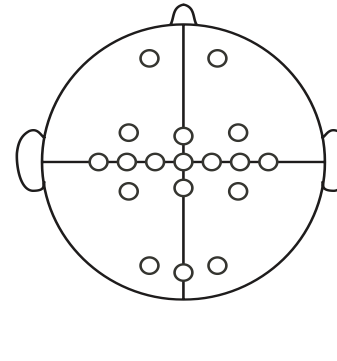
(14 electrodes)

BNCI2015001



(13 electrodes)

UNION



(18 electrodes)

$$T(C_{RPA}) = UP \begin{pmatrix} \left(G^{-1/2} C_k G^{-1/2} \right)^p & 0 \\ 0 & I \end{pmatrix} P^T U^T$$

Code for Riemannian geometry

(**Julia** – Python – R – Matlab – C++ – Delphi)

<https://sites.google.com/site/marcocongedo/science/code-resources>

P300-BCI Data

<https://sites.google.com/site/marcocongedo/science/EEG-data>

7 *Databases*

273 *Subjects*

1446 *Sessions*

BCI in Virtual Reality and on a PC

Description: Visual P300 BCI experiment on PC and virtual reality (passive head-mounted display) (2018)

Subjects: 21
Sessions: 2
Electrodes: 16 wet Silver/Silver Chloride electrodes
EEGMachine: g.tec g.USBamp
Sampling Rate: 512 sps
Database ID: VR.EEG.2018-GIPSA

Brain Invaders Multi-User Cooperation vs. Competition

Description: Multi-User Brain Invaders: Cooperation versus Competition condition (2015)

Subjects: 44
Sessions: 2
Electrodes: 32 wet Silver/Silver Chloride electrodes
EEGMachine: g.tec g.USBamp
Sampling Rate: 512 sps
Database ID: bi2015b

Brain Invaders Multi-User flash duration

Description: Brain Invaders calibration-less P300-based BCI with modulation of flash duration (2015)

Subjects: 50
Sessions: 3
Electrodes: 32 wet Silver/Silver Chloride electrodes
EEGMachine: g.tec g.USBamp
Sampling Rate: 512 sps
Database ID: bi2015a

Brain Invaders Solo vs. Multi-User Collaboration

Description: Multi-User Brain Invaders in Solo versus Collaboration condition (2014)

Subjects: 38
Sessions: 3
Electrodes: 32 wet Silver/Silver Chloride electrodes
EEGMachine: g.tec g.USBamp
Sampling Rate: 512 sps
Database ID: bi2014b

Brain Invaders dry electrodes

Description: Brain Invaders calibration-less P300-based BCI with dry electrodes (2014)

Subjects: 71
Sessions: up to three per participant
Electrodes: 16 metal dry electrodes
EEGMachine: g.tec g.USBamp
Sampling Rate: 512 sps
Database ID: bi2014a

Brain Invaders Adaptive vs. Non-Adaptive

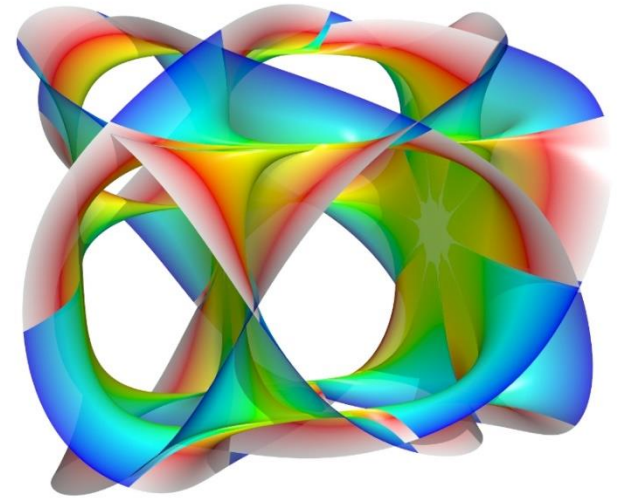
Description: First Brain Invaders dataset of a BCI working without calibration (2013)

Subjects: 24
Sessions: 8 for subjects 1-7, one for the remaining.
Electrodes: 16 wet Silver/Silver Chloride electrodes
EEGMachine: g.tec g.USBamp
Sampling Rate: 512 sps
Database ID: BLEEG.2013-GIPSA

Building Brain Invaders

Description: First Brain Invaders BCI dataset (2012)

Subjects: 25
Sessions: 2
Electrodes: 16 wet Silver/Silver Chloride electrodes
EEG Machine: TMSI Porti
Sampling Rate: 128 sps
Database ID: BLEEG.2012-GIPSA



Collaborators @GIPSA-lab

Prof. C. Jutten

Ingeneer: A. Andreev

Post-Doc: A. Barachant, P. Zanini

PhD Students: L. Korczowski, F. Bouchard, P.L.C. Rodrigues, A. Bleuzé

