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College Name: Indian Institute of Technology - Madras

Course & Branch: \_\_\_\_\_

Passing out year: \_\_\_\_\_

Marks (% or GPA): \_\_\_\_\_

Undergrad Course & Branch: \_\_\_\_\_

Marks (% or GPA): \_\_\_\_\_

Email Address: \_\_\_\_\_

Position: **Software Engineer/ Software Engineer in Test/ Both**

**Instructions:**

1. Duration of the test: **60 minutes**.
2. Section A contains objective questions. For questions with multiple-choices, only ONE is correct.
3. Section B contains 1 question. Write a **neat, legible** and **well structured** code / pseudo-code in the box only. Use meaningful variable names while writing code.
4. Try not to spend more than **20 minutes** for Section A
5. -0.25 for each wrong answer in Section A. +1 for each correct answer
6. Use of calculators is allowed
7. Additional sheets are provided for doing rough work

## Section A

1. Quick-sort is run on two inputs shown below to sort in ascending order

(i) 1, 2, 3, ..., n

(ii) n, n - 1, n - 2, ..., 2, 1

Let  $C_1$  and  $C_2$  be the number of comparisons made for the inputs (i) and (ii) respectively. Then,

a)  $C_1 < C_2$

b)  $C_1 > C_2$

c)  $C_1 = C_2$

d) We cannot say anything for arbitrary n

2. Which of the following languages over  $\{0, 1\}$  is regular?

a)  $0^i 1^j$  such that  $i \leq j$

b)  $0^i w 1^j$  such that  $w \in \{0, 1\}^*$  and  $i \geq 0$

c) All strings of 0s and 1s such that every pth character is 0 where p is prime

d) None of the above

3. We are given a set  $X = \{x_1, x_2, \dots, x_n\}$  where  $x_i = 2^i$ . A sample S (which is a subset of X) is drawn by selecting each  $x_i$  independently with probability  $p_i = 1/2$ . The expected value of the smallest number in sample S is:

a)  $1/n$

b) 2

c)  $\sqrt{n}$

d) n

4. Let S be an NP-complete problem and Q and R be two other problems not known to be in NP. Q is polynomial time reducible to S and S is polynomial-time reducible to R. Which one of the following statements is true?

a) R is NP-complete

b) R is NP-hard

c) Q is NP-complete

d) Q is NP-hard

5. For any string  $s \in (0 + 1)^*$ , let  $d(s)$  denote the decimal value of s (eg:  $d(101) = 5$ ,  $d(011) = 3$ ).

Let  $L = \{s \in (0+1)^* \mid d(s) \bmod 5 = 2 \text{ and } d(s) \bmod 7 = 4\}$ . Which of the following statements is true?

a) L is recursively enumerable, but not recursive

b) L is recursive, but not context-free

c) L is context-free, but not regular

d) L is regular

Common data for questions 6 and 7

The  $2^n$  vertices of a graph  $G$  corresponds to all subsets of a set of size  $n$ . Two vertices of  $G$  are adjacent if and only if the corresponding sets intersect in exactly 2 elements

6. The number of vertices of degree zero in  $G$  is:

- a) 1
- b)  $n$
- c)  $2n - 1$
- d) None

7. The number of connected components in  $G$  is:

- a)  $2n$
- b)  $n + 2$
- c)  $n \text{ C } 2$
- d) None

8. There are 5 nested loops written as follows,

```
int counter = 0;
for (int loop_1=0; loop_1 < 10; loop_1++) {
    for (int loop_2=loop_1 + 1; loop_2 < 10; loop_2++) {
        for (int loop_3=loop_2 + 1; loop_3 < 10; loop_3++) {
            for (int loop_4=loop_3 + 1; loop_4 < 10; loop_4++) {
                for (int loop_5=loop_4 + 1; loop_5 < 10; loop_5++) {
                    counter++;
                }
            }
        }
    }
}
```

What will be the value of counter in the end (after all the loops finished running)?

- a)  $15C5$
- b)  $14C5$
- c)  $10C5$
- d)  $10 * 9 * 8 * 7 * 6 * 5$

9. The enter\_CS() and leave\_CS() functions to implement critical section of a process are realized using test-and-set instruction as follows:

```
void enter_CS(X) {
    while(test-and-set(X));
}

void leave_CS(X) {
    x=0;
}
```

}

In the above solution , X is a memory location associated with the CS and is initialized to 0. Now consider the following statements:

1. The above solution to CS problem is deadlock free
2. The solution is not starvation free
3. The processes enter CS in FIFO order
4. More than one process can enter CS at the same time

Which of the above statements is **TRUE**

- a) 1
- b) 1 and 2
- c) 1 and 3
- d) 2 and 4

10. The following 'C' code prints:

```
void f(char *x) {  
    x++;  
    *x = 'a';  
}  
  
int main() {  
    char *str = "hello";  
    f(str);  
    printf("%s", str);  
}
```

- a) hello
- b) allo
- c) hallo
- d) empty string

11. An insurance company issues a policy on a small boat under the following conditions:

The replacement cost of \$5000 will be paid for a total loss. If it is not a total loss, but the damage is more than \$2000, then \$1500 will be paid. Nothing will be paid for damage costing \$2000 or less and of course nothing is paid out if there is no damage. The company estimates the probability of the first three events as .02, .10, and .30 respectively. The amount the company should charge for the policy if it wishes to make a profit of \$50 per policy on average is:

- a) \$250
- b) \$201
- c) \$300

d) \$1200

12. We are given an array A with 8 distinct elements. Arrays B and C have 5 and 3 elements respectively and they are populated with elements from A. (The union of elements in B and C give the elements in A)

In how many ways can the arrays B & C be populated such that both B and C have elements in sorted (ascending) order.

- a) 56
- b) 128
- c) 256
- d) None

13. Increasing the RAM of a computer typically improves performance because:

- a. Virtual memory increases
- b. Larger RAMs are faster
- c. Fewer segmentation faults occur
- d. Fewer page faults occur

14. Suppose we want to synchronize two concurrent processes P and Q using binary semaphores S and T. The code for the processes P and Q is shown below.

**Process P:**

```
while (1) {  
    W:  
    print '0';  
    print '0';  
    X:  
}
```

**Process Q:**

```
while (1) {  
    Y:  
    print '1'  
    print '1'  
    Z:  
}
```

Synchronization statements can be inserted only at points W, X, Y and Z.

V() increments the semaphore, whereas P() decrements it

Which of the following will always lead to an output starting with '001100110011' ?

- a) P(S) at W, V(S) at X, P(T) at Y, V(T) at Z, S and T initially 1
- b) P(S) at W, V(T) at X, P(T) at Y, V(S) at Z, S initially 1, and T initially 0
- c) P(S) at W, V(T) at X, P(T) at Y, V(S) at Z, S and T initially 1
- d) P(S) at W, V(S) at X, P(T) at Y, V(T) at Z, S initially 1, and T initially 0

15. Which of the following statements are true?

- I Shortest remaining time first scheduling may cause starvation
- II Preemptive scheduling may cause starvation
- III Round robin is better than first come first serve in terms of response time

- a) I only
- b) I and III only
- c) II and III only
- d) I, II and III

16. A 4-stage pipeline has the stage delays as 150, 120, 160 and 140 ns (nano seconds) respectively. Registers that are used between the stages have a delay of 5 ns each. Assuming constant clocking rate, the total time taken to process 1000 data items on this pipeline will approximately be

- a. 120 us (micro seconds)
- b. 165 us
- c. 180 us
- d. 175 us

17. Consider a disk system with 100 cylinders. The requests to access the cylinders occur in following sequences

**4, 34, 10, 7, 19, 73, 2, 15, 6, 20**

Assuming that the head is currently at cylinder 50, what is the time taken to satisfy all requests if it takes 1ms to move from one cylinder to adjacent one and shortest seek time first policy is used?

- a. 95ms
- b. 119ms
- c. 233ms
- d. 276ms

### Section B

Write the code to find lexicographic minimum in a circular array, e.g. for the array BCABDADAB, the lexicographic minimum is ABBCABDAD.

optional - explain logic here

code / pseudo code here