

CS3300 : Compiler Design

Assignment - 1

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Ans. 1 - a - (i) - Regular expression for C comments -
single line comment : `"//".*`

(ii) string literals : `\"(\\ | [^\\"])*\"`
\\ for (") and \\. to match string like "a" then `[^\\"]` matches all char except \ and "

Ans 1- b - `.*("abb").*` matches all string with abb as substring.

Ans 1- d- regular expression for pascal keywords which are case in sensitive

Begin : `[bB][eE][gG][iI][nN]` ;

End : `[eE][nN][dD]`;

Function : `[fF][uU][nN][cC][tT][iI][oO][nN]`;

Absolute : `[Aa][bB][sS][oO][lL][uU][tT][eE]` ;

Ans : 2 : Scheme to convert a Grammar ϵ -free is :

For all Non-terminal Z which has production like $Z \rightarrow \epsilon$, we look for all productions whose right side contains Z and replace each occurrence of Z in each of these productions to obtain the non ϵ -productions.

The resultant non- ϵ production are then added to the grammar to retain the language.

If the goal goes to ϵ production we add ϵ production to the goal.

Ex:

$S' \rightarrow S$;

$S \rightarrow aSbS \mid bSaS \mid \epsilon$.

Here $S \rightarrow \epsilon$ so we replace all occurrence of right side of S as ϵ which gives

$S \rightarrow abS \mid aSb \mid ab$ for $S \rightarrow aSbS$

$S \rightarrow baS \mid bSa \mid bs$ for $S \rightarrow bSaS$

$S' \rightarrow \epsilon$ for $S' \rightarrow \epsilon$

our grammar becomes :

$S' \rightarrow S \mid \epsilon$;

$S \rightarrow aSbS \mid bSaS \mid abS \mid aSb \mid baS \mid bSa \mid ab \mid bs$;

Ans : 3 : c) CFG for palindromes with 0,1 and 2

$$\begin{aligned} S &\rightarrow 0 S 0 \\ &\quad | 1 S 1 \\ &\quad | 2 S 2 \\ &\quad | 1 \\ &\quad | 2 \\ &\quad | 0 \\ &\quad | \epsilon \end{aligned}$$

Ans : 3 : d) CFG for all strings of 0's and 1's that doesn't contain 011 as substring

$$\begin{aligned} A &\rightarrow 1 A \\ &\quad | B \end{aligned}$$
$$\begin{aligned} B &\rightarrow 0 B \\ &\quad | C \end{aligned}$$
$$\begin{aligned} C &\rightarrow 01 C \\ &\quad | 0 C \\ &\quad | \epsilon \end{aligned}$$

Ans : 3 : b) CFG for java comments

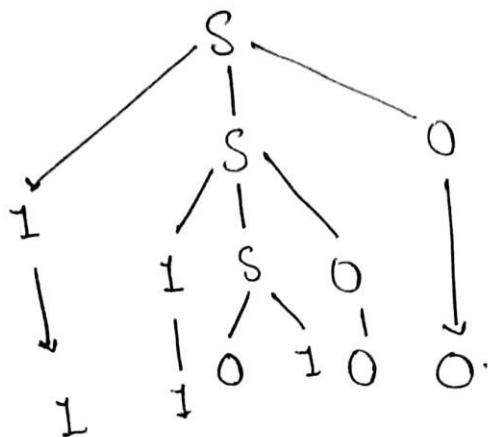
allChar belongs to the set of all valid characters except '\n' new-line

$$\begin{aligned} S &\rightarrow // A \\ &\quad | /* B \end{aligned}$$
$$\begin{aligned} A &\rightarrow \text{allChar } A \\ &\quad | \epsilon \end{aligned}$$
$$\begin{aligned} B &\rightarrow A N B \\ &\quad | */ \end{aligned}$$
$$N \rightarrow \backslash n$$

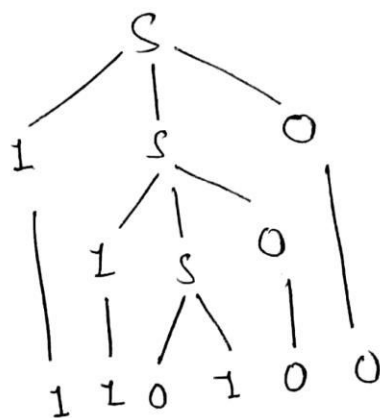
Ans-9: (a) $S \rightarrow 1S0101$

given String: 110100.

Left-derivation Tree



Right-Derivation Tree:



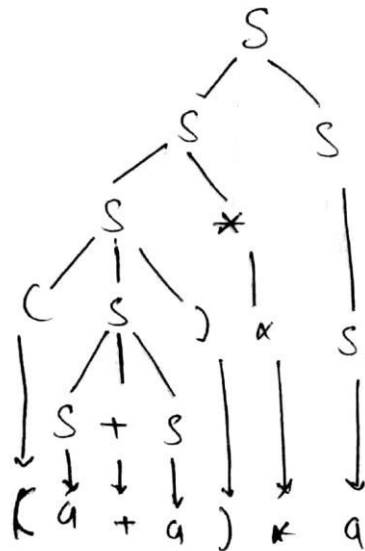
The grammar is not ambiguous as left and right subtree are same.

4(b) - $S \rightarrow S + S$
 $\quad \quad \quad | SS$
 $\quad \quad \quad | (S)$
 $\quad \quad \quad | S^*$
 $\quad \quad \quad | a.$

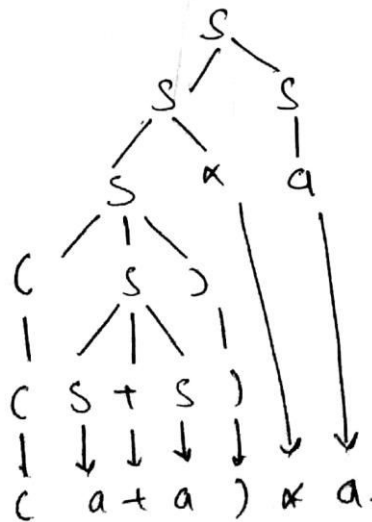
given string

: $(a+a)*a$

Left-derivation tree:



Right derivation: tree.



The above grammar is ambiguous left derivation tree is not same as right derivation tree .

$$4- (c) \quad S \rightarrow S \ S \ S$$

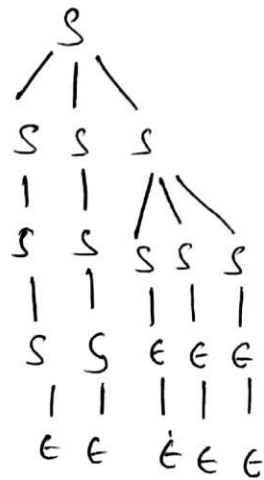
$$| \epsilon$$

String = ϵ (empty string)

Left Derivation:



Right Derivation:



The given grammar is ambiguous as right-derivation tree is different from left derivation tree.

Ans 6:

$$S \rightarrow SS+ \mid SS* \mid T$$

$$T \rightarrow id \mid num$$

(a) building LR(0) parsing Table

we add $S' \rightarrow S \$$

States.

$$I_0: S' \rightarrow \cdot S \$$$

$$S \rightarrow \cdot SS +$$

$$S \rightarrow \cdot SS *$$

$$S \rightarrow \cdot T$$

$$T \rightarrow \cdot id$$

$$T \rightarrow \cdot num$$

$$I_1: S' \rightarrow S \cdot \$$$

$$S \rightarrow S \cdot S +$$

$$S \rightarrow S \cdot S *$$

$$S \rightarrow \cdot SS +$$

$$S \rightarrow \cdot SS *$$

$$S \rightarrow \cdot T$$

$$T \rightarrow \cdot id$$

$$T \rightarrow \cdot num$$

$$I_2: S \rightarrow T \cdot$$

$$I_3: T \rightarrow id \cdot$$

$$I_4: T \rightarrow num \cdot$$

$$I_5: S' \rightarrow S \$ \cdot$$

$$I_7: S \rightarrow SS + \cdot$$

$$I_8: S \rightarrow SS * \cdot$$

$$I_6: S \rightarrow SS \cdot +$$

$$S \rightarrow SS \cdot *$$

$$S \rightarrow S \cdot S +$$

$$S \rightarrow S \cdot S *$$

$$S \rightarrow \cdot SS +$$

$$S \rightarrow \cdot SS *$$

$$S \rightarrow \cdot T$$

$$T \rightarrow \cdot id$$

$$T \rightarrow \cdot num$$

Parse Table :

state	Actions					GOTO	
	+	*	ld	num	\$	S	T
0	-	-	s3	s4	-	1	2
1	-	-	s3	s4	s5	6	2
2	r3	r3	r3	r3	r3	-	-
3	r4	r4	r4	r4	r4	-	-
4	r5	r5	r5	r5	r5	-	-
5	acc	acc	acc	acc	acc	-	-
6	s7	s8	s3	s4	-	6	2
7	r2	r2	r2	r2	r2	-	-
8	r3	r3	r3	r3	r3	-	-

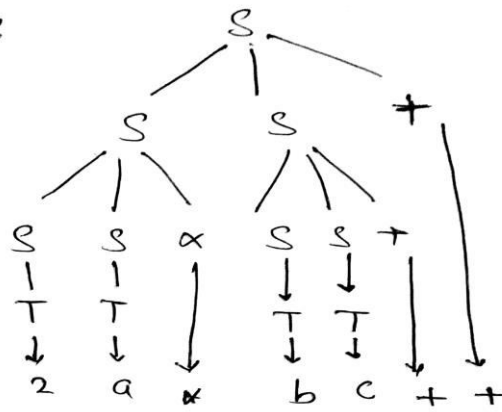
The given grammar is LR(0) , as there is no shift reduce conflicts in parse table.

The Sequence of action for String : 2 a * b c + +

The sequence of actions.

Stack	input.	Actions.
0	2 a * b c + + \$	s4
0 4	a * b c + + \$	r5
0 2	a * b c + + \$	r3
0 1	a * b c + + \$	s3.
0 1 3	* b c + + \$	r4
0 1 2	* b c + + \$	r3
0 1 6	* b c + + \$	s8.
0 1 6 8	■ b c + + \$	r2.
0 1	● b c + + \$	s6
0 1	c + + \$	s6
0 1 6	+ + \$	s7
0 1 6 6	+ \$	r1.
0 1 6 6 7	+ \$	s7
0 1 6	\$	r1.
0 1 6 7	\$	s5
0 1	\$	acc.
0 1 5		

Ans 6: Parse Tree:



ANSWER 7 -- LR(1) Parse Table for the given grammar :

Ans: 1. Crownpipe \rightarrow 1 Ka. Crownpipe
2. 1 Ka.

we add
0.51 \rightarrow crowninide \$

$I_0: s' \rightarrow \text{.Crownwise}, \$$
 $\text{Crownwise} \rightarrow \text{.Kaa Crownwise}, \$$
 $\text{Crownwise} \rightarrow \text{.Kaa}, \$$

$$I_1: \quad s' \rightarrow \text{Growth rate, } \%$$

I 2:

Crownwise	→	kaa. Crownwise, \$
Crownwise	→	Kaa. \$
Crownwise	→	.kaa Crownwise, \$
Crownwise	→	.kaa, \$

T₃: Crownoids → kaa Crownoids, \$

Parse Table LR(1)

	Actions		GoTo
	Kaa	\$	Crownwise.
0	S2	-	1
1	-	acc	-
2	S2	82	3
3	-	81	-

for string "kaa kaa kaa"

Stack	input	Actions.
0	kaa kaa kaa \$	S 2
0 2	kaa kaa \$	S 2
0 2 2	kaa \$	S 2
0 2 2 2	\$	X 2
0 2 2 3	\$	X 1
0 2 3	\$	X 1.
0 1	\$	accept.

Ans - (a) SLR(1) items and goto functions for

(1) 4(b)	$S \rightarrow S + S$	1
	$ S S$	2
	$ (S)$	3
	$ S \alpha$	4
	$ a$	5

Ques. We have $S' \rightarrow S \$$ 0.

$I_0: S' \rightarrow \cdot S \$$
 $S \rightarrow \cdot S + S$
 $S \rightarrow \cdot S S$
 $S \rightarrow \cdot S \alpha$
 $S \rightarrow \cdot (S)$
 $S \rightarrow \cdot a$

$I_1: S' \rightarrow S \cdot \$$
 $S \rightarrow S \cdot + S$
 $S \rightarrow S \cdot S$
 $S \rightarrow S \cdot \alpha$
 $S \rightarrow S \cdot (S)$
 $S \rightarrow S \cdot a$

$I_2: S \rightarrow (\cdot S)$
 $S \rightarrow \cdot S + S$
 $S \rightarrow \cdot S S$
 $S \rightarrow \cdot S \alpha$
 $S \rightarrow \cdot (S)$
 $S \rightarrow \cdot a$

$I_3: S \rightarrow a \cdot$

$I_4: S \rightarrow S \alpha \cdot$

$I_5: S \rightarrow S S \cdot$
 $S \rightarrow S \cdot + S$
 $S \rightarrow S \cdot S$
 $S \rightarrow S \cdot \alpha$
 $S \rightarrow S \cdot (S)$
 $S \rightarrow S \cdot a$

$I_6: S \rightarrow S + \cdot$

$I_7: S \rightarrow (S \cdot)$
 $S \rightarrow S \cdot + S$
 $S \rightarrow S \cdot S$
 $S \rightarrow S \cdot \alpha$
 $S \rightarrow S \cdot (S)$
 $S \rightarrow S \cdot a$

(Continue)

$\rightarrow I_8: S \rightarrow \cdot (S)$
 $S \rightarrow \cdot a$

$I_4: S \rightarrow S + S -$

$S \rightarrow \cdot SS$

$S \rightarrow \cdot S + S$

$S \rightarrow \cdot S *$

$S \rightarrow \cdot ()$

$S \rightarrow \cdot a$

$I_8: S \rightarrow S + S,$

$S \rightarrow S \cdot S$

$S \rightarrow S \cdot + S$

$S \rightarrow S \cdot *$

$S \rightarrow \cdot S + S$

$S \rightarrow \cdot SS$

$S \rightarrow \cdot S *$

$S \rightarrow \cdot ()$

$S \rightarrow \cdot a$

$I_9: S \rightarrow (S) .$

Parse Table:

Follow of $S = +, *, a, ($

	Actions.						GOTO.
	a	+	*	()	\$	
0	S3	-	-	S2	-	-	S
1	S3	S4	S6	S2	-	acc	5
2	S3	-	-	S2	-	-	7
3	r5	r5	r5	r5	-	-	-
4	S3	-	-	S2	-	-	8
5	S4/r2	r2	r2/s6	r2/s2	-	-	5
6	r4	r4	r4	r4	-	-	-
7	S3	S4	S6	S2	S9	-	5
8	S3/r1	r1/s4	r1/s6	S2/r1	-	-	5
9	r3	r3	r3	r3	-	-	-

The grammar is ambiguous as it has diff reduce conflicts.

$$\text{Ans} - (b) \quad S \rightarrow S S S \mid \epsilon \quad \begin{matrix} 1 \\ 2 \end{matrix}$$

$$S' \rightarrow S \$ \quad 0.$$

$$\begin{aligned} I_0: & S' \rightarrow \cdot S \$ \\ & S \rightarrow \cdot S S S \\ & S \rightarrow \cdot \epsilon \end{aligned}$$

$$\begin{aligned} I_1: & S \rightarrow S \cdot \$ \\ & S \rightarrow S \cdot S S \\ & S \rightarrow \cdot S S S \\ & S \rightarrow \cdot \epsilon \end{aligned}$$

$$I_2: S \rightarrow \epsilon \cdot$$

$$\begin{aligned} I_3: & S \rightarrow S S \cdot S \\ & S \rightarrow \cdot S S S \\ & S \rightarrow \cdot \epsilon \\ & S \rightarrow S \cdot S S \end{aligned}$$

$$\begin{aligned} I_4: & S \rightarrow S S S \cdot \\ & S \rightarrow S \cdot S S \\ & S \rightarrow \cdot \epsilon \\ & S \rightarrow S S \cdot S \end{aligned}$$

The grammar is ambiguous in state 4 we can reduce using rule 1 for ϵ as well as shift to state 2 so there is a shift/reduce conflict.