# WATER, HIGH-ALTITUDE CONDENSATES, AND METHANE DEPLETION IN THE ATMOSPHERE OF THE WARM NEPTUNE WASP-107b

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# Submitted to ApJL

#### ABSTRACT

The transiting planet WASP-107b is an intriguing target for atmosphere characterization, with a large atmospheric scale height and a small, bright host star.

w107 is a good target for atmospheric characterization, raising the exciting possibility of characterizing its formation history

. With a mass similar to Neptune's and a radius close to Jupiter's, it occupies the transition region between ice giants and gas giants. The planet is also one of the strongest targets for atmospheric characterization yet discovered, thanks to its small, bright host star and large scale height. We report the first atmosphere characterization of WASP-107b, a Hubble Space Telescope measurement of its near-infrared transmission spectrum. We analyzed the planet's composition with two techniques: atmospheric retrieval based on the transmission spectrum and interior structure modeling based on the planet's mass and radius. We detect water absorption at  $6.5\,\sigma$  confidence and set an upper limit on the atmospheric metallicity of  $30\times$  solar. We find that the methane abundance is depleted relative to expectations for a solar abundance pattern (at  $3\,\sigma$  confidence), suggesting a low carbon-to-oxygen ratio or high internal heat flux. The amplitude of features in the transmission spectrum is smaller than expected for a cloudless atmosphere, crossing just one scale height, and requires an opaque condensate layer at high altitudes (0.1 - 3 mbar). We find that it is challenging for physically motivated cloud and haze models to produce opaque condensates at this height. Taken together, these

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findings serve as an illustration of the diversity and complexity of exoplanet atmospheres. We can look forward to more such results with the high precision and wide spectral coverage afforded by future observing facilities.

Keywords: planets and satellites: individual (WASP-107b), planets and satellites: atmospheres

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### 1. INTRODUCTION

The composition of a planet's atmosphere depends on where and how the planet formed. By measuring atmospheric metallicity and molecular abundance ratios, we can shed light on important aspects of the formation process such as location within the disk and the relative accretion rates of gas versus solids (Öberg et al. 2011; Fortney et al. 2013; Madhusudhan et al. 2014; Ali-Dib 2016; Mordasini et al. 2016; Espinoza et al. 2017).

The warm Neptune WASP-107b is an intriguing target for atmosphere characterization for several reasons. It is an intermediate size between ice giants and gas giants, with a mass similar to Neptune's and a radius close to Jupiter's  $(0.12\,M_{\rm Jup},\,0.94\,R_{\rm Jup};\,$  Anderson et al. 2017). Studying the atmospheres of planets in this transition region will provide additional clues in the much-debated mystery of what stunts the growth of Neptune-size planets (e.g Pollack et al. 1996; Dawson et al. 2016; Frelikh & Murray-Clay 2017).

WASP-107b also has a relatively low equilibrium temperature (780 K) compared to most other exoplanets that are amenable to atmosphere characterization. This results in a distinct atmospheric chemistry from other well-studied systems: at low temperatures, the dominant molecular reservoir for carbon transitions from carbon monoxide to methane (Moses et al. 2013). Spectral features from both water and methane are accessible with current observing facilities, raising the possibility of a spectroscopic estimate of the carbon-to-oxygen ratio (C/O). Previous measurements of C/O have been challenging because they rely on photometry that covers absorption features from multiple molecules (e.g. Madhusudhan et al. 2011; Line et al. 2014; Benneke 2015; Kreidberg et al. 2015). FIXME: maybe cut this.

In addition, WASP-107b is one of the best targets discovered to date for atmosphere characterization. Thanks to its large atmospheric scale height and small, bright host star, the expected signal-to-noise for the transmission spectrum is comparable to the best studied benchmarks in the field (e.g. HD 209458b, HD 189733b). The planet is also a feasible target for thermal emission measurements, with an expected secondary eclipse depth of  $\sim 0.1\%$  in Spitzer's  $4.5\,\mu\mathrm{m}$  channel. In this paper we report the first atmosphere characterization of WASP-107b: a near-infrared transmission spectrum measured with the  $Hubble\ Space\ Telescope\ (HST)$ .

#### 2. OBSERVATIONS

We observed a single transit of WASP-107b with HST's Wide Field Camera 3 (WFC3) instrument on UT 5-6 June 2017. The transit observation consisted of five HST orbits. At the beginning of each 96-minute orbit,

we took an image of the target with the F130N filter (exposure time = 4.2 s). This direct image is used for wavelength calibration. For the remainder of the target visibility period (about 45 minutes), we obtained time series spectra with the G141 grism, which provides low-resolution spectroscopy over the wavelength range  $1.1-1.7\,\mu\mathrm{m}$ . We used the NSAMP=6, SPARS\_25 readout mode (exposure time = 112 s) to optimize the efficiency of the observations, as determined by the PandExo\_HST planning tool<sup>1</sup>. As is standard for WFC3 observations of bright targets, we used the spatial scanning observing mode, which slews the telescope in the spatial direction over the course of an exposure. The scan rate was 0.12 arcseconds/sec.

# 3. DATA REDUCTION

We reduced the data with the custom pipeline described in Kreidberg et al. (2014a), which we summarize briefly here. For each exposure, we extracted the spectrum from each up-the-ramp sample (or "stripe") separately using the optimal extraction algorithm of Horne (1986). The stripe spectra were then summed to create the final spectrum. For each stripe, the extraction box was 80 pixels high and centered on the stripe's midpoint in the spatial direction. To correct the change in dispersion solution over the length of the spatial scan, we interpolated each row to the wavelength scale of the row corresponding to the spectral trace. We then corrected for slight drift in the spectral direction (< 0.1 pixels) by interpolating each spectrum to the wavelength scale of the first exposure. To subtract the background, we took the median of sky pixels that were uncontaminated by the target spectrum (rows 5-250, columns 5-15). The typical background counts were low: 40 photoelectrons/pixel, in comparison to  $3 \times 10^4$  photoelectrons/pixel in the stellar spectrum.

# 4. LIGHT CURVE ANALYSIS

The data analysis had two parts: the band-integrated "white" light curve fit and the spectroscopic light curve fits.

# 4.1. White Light Curve

To create the raw white light curve, we summed each spectrum over the 181 pixels in the spectral trace. The white light curve has systematic trends that are typical for WFC3 observations (Zhou et al. 2017): the flux increases increases asymptotically over each orbit (the "ramp" effect) and there is a visit-long linear

https://github.com/spacetelescope/PandExo\_HST

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trend. The largest ramp occurs in the initial orbit (orbit zero), so we only fit data from orbits one through four in our analysis, following common practice. We fit the light curve with the analytic model of the form  $F_{\rm white}(t) = S_{\rm white}(t) \times T_{\rm white}(t)$ , where  $S_{\rm white}$  is a systematics model and  $T_{\rm white}$  is a transit model. We used the same systematics model as Kreidberg et al. (2015), Equation 1. To model the transit, we used the batman package (Kreidberg 2015). The transit model parameters are the orbital period p, time of inferior conjunction  $t_0$ , transit depth  $r_p/r_s$ , ratio of semi-major axis to stellar radius  $a/r_s$ , orbital inclination i, and the quadratic stellar limb darkening parameters  $u_1$  and  $u_2$ .

# 4.1.1. Star Spot Crossing

In our initial analysis, we noticed a bump in the light curve during orbit three that was not fit well with our model. We attribute this feature to a star spot crossing event, as WASP-107 is an active star and spot crossings have been observed before (Dai & Winn 2017; Močnik et al. 2017). In our subsequent analysis, we gave the data in orbit three no weight in the fit. The amplitude of the spot crossing feature is 300 ppm, as illustrated in Figure 1.

# 4.1.2. Final Fit

In our final fit, we fixed the transit parameters  $a/r_s$ , i, p on the precise estimates from the Kepler light curve (Dai & Winn 2017). These values are consistent with our best fit when we allowed them to vary freely. We also fixed the limb darkening parameters on predictions from a PHOENIX model for a star with effective temperature 4300 K, calculated with the limb-darkening package from Espinoza & Jordán (2015). The remaining free parameters were  $t_0$ ,  $r_p/r_s$ , and the systematics parameters for the visit-long and orbit-long trends.

For the best fit white light curve, the root-meansquare (rms) residuals were 93 ppm (excluding the star spot crossing), which is somewhat larger than the expected shot noise of 50 ppm. We attribute the excess noise to loss of flux off the edge of the detector, which can occur if there is variation in the position or length of the spatial scan. There is no evidence for correlated noise in the residuals, so to account for the excess noise we simply increased the perpoint uncertainties by a factor of 1.7 to achieve a  $\chi^2_{\nu}$ value of unity. We then used the Markov chain Monte Carlo (MCMC) algorithm to estimate parameter uncertainties (Foreman-Mackey et al. 2013). The chain had 50 walkers which each ran for 10<sup>4</sup> steps with the first 10% discarded as burn-in. We tested for convergence by dividing the chain in two halves and confirming that they gave consistent results. The transit time was  $t_0 = 2457910.45407 \pm 6e - 5$  BJD<sub>TDB</sub> and the planet/star radius was  $r_p/r_s = 0.14399 \pm 0.00017$ .

# 4.2. Spectroscopic Light Curve Fits

We binned the spectrum into 20 spectrophotometric channels from 1.12 to 1.65  $\mu$ m, shown in Figure 1. We fit the light curves with the divide-white technique, which assumes that the light curve systematics have the same morphology at all wavelengths (Stevenson et al. 2014; Kreidberg et al. 2014a). For this method, the transit model  $T_{\lambda}(t)$  is multiplied by the systematics vector from the white light curve fit  $(F_{\text{white}}/T_{\text{white}})$ , and rescaled by a factor  $C_{\lambda} + V_{\lambda}t$ . One advantage of this approach is that it removes the star spot crossing feature, enabling us to use orbit three with no additional correction. The amplitude of the feature has no detectable wavelength dependence at the level of precision of our data. As for the white light curve, we fixed some of the transit parameters on the estimates from Dai & Winn (2017) and fixed the limb darkening on the PHOENIX model. The final spectroscopic light curve fits had just three free parameters:  $C_{\lambda}$ ,  $V_{\lambda}$ , and  $r_p/r_s$ .

The best fit light curves have a median  $\chi^2_{\nu}$  value of 1.16. To ensure that we did not underestimate the uncertainty on the transit depths, we rescaled the photometric uncertainties for all spectroscopic channels such that the  $\chi^2_{\nu}$  values are unity. We performed an MCMC fit to the light curves with emcee. For each light curve we ran a fit with 50 walkers and 1000 steps per walker, and tested for convergence as we did for the white light curve. The median transit depths and  $1\,\sigma$  uncertainties are given in Table 1.

We explored several alternative choices for the spectroscopic light curve fits, but found that none of them made a significant difference in the transmission spectrum. For example, we fit the spectroscopic light curves with the same analytic model we used for the white light curve and obtained nearly identical relative transit depths (differing by just  $0.3\sigma$  on average), except with a small constant offset due to the uncorrected star-spot crossing feature. This offset does not affect our final analysis because the planet's one-bar radius is a free parameter in the atmospheric retrieval (see  $\S 5.2$ ). We also fit for a linear limb darkening parameter rather than fixing the limb darkening on the PHOENIX model values. We found that the fitted limb darkening coefficients are consistent with the model predictions, so we opted to fix the coefficients in our final analysis because it improves the precision on the transit depths by about 10%. We also checked that the uncertainty in the stellar parameters does not significantly affect the PHOENIX model predictions at the level of precision of our data.

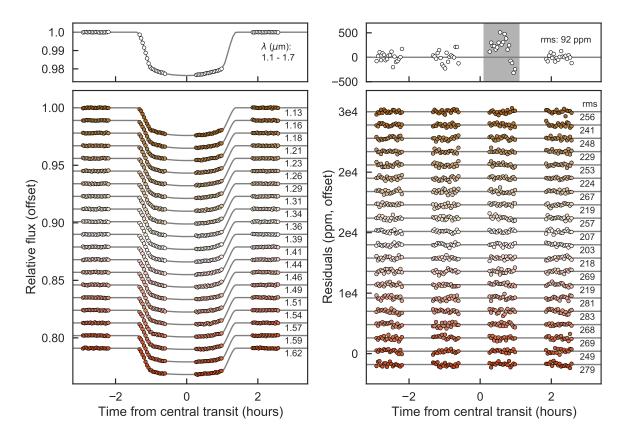


Figure 1. Broadband and spectrophotometric transit light curves for WASP-107b measured with HST/WFC3 compared to best fit models (left) and residuals from the best fit (right). Annotations indicate the central wavelength and root-mean-square (rms) residuals for each light curve. A possible star-spot crossing feature is shaded in gray in the upper right; our systematic error correction removes this feature from the spectroscopic light curves.

# 4.2.1. Transit Depths Redder than $1.62~\mu m$

The red edge of the transmission spectrum is of interest for our analysis because methane is expected to be the dominant absorber over water at wavelengths greater than 1.6  $\mu$ m. Unfortunately, we find that the our reddest spectroscopic light curves (> 1.62 $\mu$ m) are too poor in quality to robustly measure the transit depth. The residuals exhibit correlated noise and the fits have  $\chi^2_{\nu} > 2$ . The transit depths are also sensitive to which method we use to fit for instrument systematics. We therefore opt not to report transit depths redder than the 1.62  $\mu$ m channel.

# 4.2.2. Independent Analysis

We also performed an independent data reduction and fit using K. Stevenson's pipeline.

#### 5. COMPOSITION OF THE ATMOSPHERE

In this section we discuss constraints on the composition of WASP-107b's atmosphere based on interior structure modeling and atmospheric retrieval of the measured transmission spectrum.

# 5.1. Atmospheric Metallicity from Interior Structure Modeling

Given WASP-107b's unusually low density, we quantitatively explored the range of atmospheric metallicities that are consistent with the observed mass and radius using the structure evolution modeling of Thorngren et al. (2016). These models assume a thermally inert heavy-element core with a convective envelope of additively mixed H/He (Saumon et al. 1995) and heavy-element impurities. The heavy elements were a 50-50 rock-ice mix from ANEOS (?). We evolved the planets in time using the atmospheric models of Fortney et al. (2007). The results are sensitive to assumptions about the stellar age, which is uncertain (either  $0.6 \pm 0.2$  to  $8.3 \pm 4.3$  Gyr depending on model assumptions; Močnik et al. 2017). We therefore ran two models, with uniform age priors of either 0.2-1.0 or 1.0-13.8 Gyr. We used

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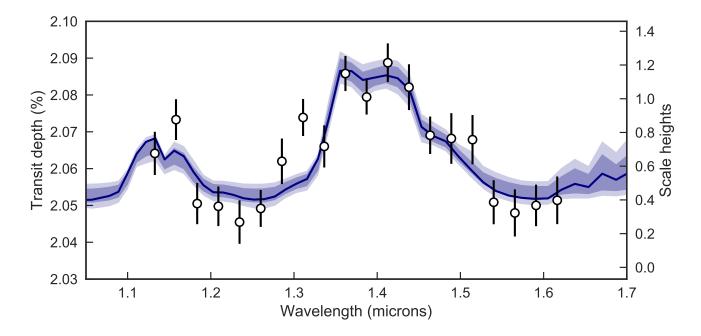


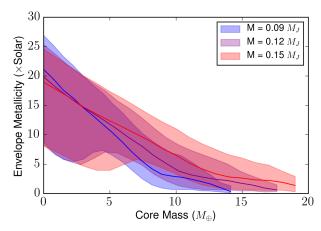
Figure 2. The transmission spectrum of WASP-107b (points with  $1\sigma$  error bars) compared to retrieved models (blue line with shaded 1 and  $2\sigma$  confidence intervals). The features at 1.15 and 1.4  $\mu$ m are due to water absorption. The right-hand axis indicates the normalized atmospheric scale height assuming a  $10\times$  solar composition.

the published mass and radius estimates (0.12±0.01  $M_{\rm J}$ , 0.94 ± 0.02; Anderson et al. 2017).

Based on these assumptions, we fit for envelope metallicity and core mass using an MCMC with uniform priors on both parameters. The MCMC burned in for 10<sup>3</sup> steps and then collected  $4 \times 10^6$  samples, which we thinned to  $10^5$ . The resulting envelope metal mass fractions were converted to metallicities by assuming the mean molecular weight of the metals was 18 (the value for water), using the approach of Fortney et al. (2013). Figure 3 shows the results. We find that the inferred atmospheric metallicity and core mass are inversely proportional, as expected (the more massive the core, the lighter the envelope must be to maintain the observed radius). Larger core masses and envelope metallicities are allowed for the younger stellar age since planets cool and contract as they age. For the younger (older) stellar age, we find an upper limit on the core mass of FIXME and an upper limit on atmospheric metallicity of FIXME.

# 5.2. Retrieval

We also inferred the composition of the atmosphere directly from the transmission spectrum using the CHIMERA chemically-consistent retrieval tool described in Kreidberg et al. (2015). Briefly, CHIMERA solves the transmission geometry problem using the equations in Brown (2001); Tinetti et al. (2012). We parameterized atmospheric composition with metallic-



**Figure 3.** Estimated envelope metallicity and core mass based on interior structure modeling of the mass and radius of WASP-107b. FIXME ages.

ity and carbon-to-oxygen ratio under the assumption of thermochemical equilibrium using the NASA CEA routine (?) to compute the molecular abundances for H<sub>2</sub>, He, H<sub>2</sub>O, CH<sub>4</sub>, CO, CO<sub>2</sub>, NH<sub>3</sub>, H<sub>2</sub>S, Na, K, HCN, C<sub>2</sub>H<sub>2</sub>, TiO, VO, and FeH. We updated the transmission model to use correlated-K opacities (Lacis & Oinas 1991; Mollière et al. 2015; Amundsen et al. 2016) from the pre-tabulated line-by-line cross section database described in Freedman et al. (2014). The transmission forward model is coupled with the PyMultiNest tool

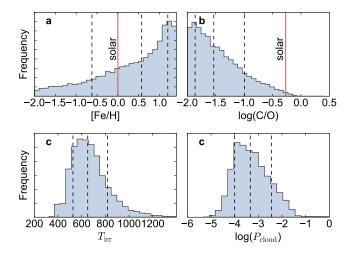
Table 1. WASP-107b transmission spectrum

Transit depth	Uncertainty
0.020641	5.9e-05
0.020733	5.5 e-05
0.020505	5.6e-05
0.020498	5.4e-05
0.020455	5.9e-05
0.020492	5.0e-05
0.020620	6.2 e-05
0.020739	5.0e-05
0.020660	5.7e-05
0.020858	4.8e-05
0.020794	4.8e-05
0.020888	5.2e-05
0.020821	6.2 e-05
0.020691	5.1 e-05
0.020682	6.9 e-05
0.020679	6.7e-05
0.020509	6.0 e-05
0.020480	6.4 e - 05
0.020500	5.6e-05
0.020514	6.5e-05
	0.020641 0.020733 0.020505 0.020498 0.020455 0.020492 0.020620 0.020739 0.020660 0.020858 0.020794 0.020888 0.020821 0.020691 0.020682 0.020679 0.020509 0.020480 0.020500

(Buchner 2016) to solve the parameter estimation and model selection problems.

Our nominal model included a temperature-pressure profile (parameterized via the Guillot 2010 relations), the atmospheric metallicity, the C/O, a gray cloud-top pressure, and the planet's 10-bar radius. We fixed the T-P profile morphology but scaled the irradiation temperature to allow for the unknown albedo and heat transport efficiency. We put a uniform prior on the atmospheric metallicity of  $0.01-30\times$  solar based on the upper limit from § 5.1.

The best fit model provides a good fit to the data  $(\chi_{\nu}^2 = 1.2)$ . There is one 3.4 $\sigma$  outlier data point (at 1.34  $\mu$ m), so we explored a few retrieval scenarios with additional complexity. We tested the addition of cloud patchiness (as described by Line et al. 2016) and a quench pressure for nitrogen and carbon species (to account for transport-induced disequilibrium chemistry, e.g. Morley et al. 2017). These models did not significantly improve the fit quality, and the main retrieval



**Figure 4.** Retrieved distributions for (a) metallicity, (b) carbon-to-oxygen ratio, (c) irradiation temperature, and (d) cloud-top pressure in bars. Dashed vertical lines show the median and  $\pm 1\,\sigma$  confidence interval. Solar metallicity and C/O values are indicated with solid vertical lines.

results were unchanged. We also tested the effect of varying the planet's surface gravity within the published FIXME  $\sigma$  range, and found that our results were again minimally changed.

The nominal retrieval results are shown in Figure 4. The metallicity distribution spans the full range allowed by our priors, with some preference for larger values. The cloud top pressure is estimated to be 0.01-3 mbar at  $1\,\sigma$  confidence. These are not particularly precise constraints because the metallicity and cloud height are somewhat degenerate (?). The retrieved irradiation temperature is  $525-820~{\rm K}~(1~\sigma~{\rm confidence})$ . We find that the C/O value is less than solar (0.54) at  $2.7\,\sigma~{\rm confidence}$ .

# 5.2.1. Methane Abundance

We ran two additional retrievals to explore whether methane depletion is the underlying cause of the inferred low C/O. Even though water is the dominant absorber in the WFC3 bandpass, there is enough methane opacity to change the shape of the spectral features at a detectable level for high precision data. In one test, we assumed chemical equilibrium but excluded methane opacity. This set-up resulted in a much broader distribution of C/O values (0.02-1.6 at  $1\,\sigma)$ , resolving the tension with the solar value.

We also performed a "free" retrieval that allowed the abundances of CH<sub>4</sub>, H<sub>2</sub>O and NH<sub>3</sub> to vary with no assumption of chemical equilibrium. The  $3\,\sigma$  upper limit on the methane abundance is  $1.2\times10^{-3}$ . We compared this to the expected methane abundance for the temper-

ature and pressure sensed at the terminator. Assuming solar C/O and  $3\times$  solar metallicity (the median value for the chemical equilbrium retrieval), the methane abundance is predicted to be  $1.3\times10^{-3}$ , inconsistent with our estimated value. Based on these tests, we conclude that the atmosphere of WASP-107b is depleted in methane relative to expectations for a solar abundance pattern.

#### 5.3. Condensate Properties

In addition to the atmospheric retrieval, we also performed forward modeling of physically motivated, self-consistent clouds and hazes using the methods described in Fortney et al. (2008); Morley et al. (2015). We model clouds that form in cool atmospheres (Na<sub>2</sub>S, KCl, ZnS; see Morley et al. 2012), for a range of metallicites from  $1-50\times$  solar. We vary the cloud sedimentation efficiency from 0.1 to 3 (highly lofted, small particulate clouds). None of the models produce sufficiently low amplitude spectral features to match the observed spectrum. FIXME: what did we assume about surface gravity?

We also model an  $ad\ hoc$  photochemical "soot" layer near the top of the atmosphere, scaling results from previous photochemical models for GJ 436b (Line et al. 2011; Morley et al. 2017). With the most efficient haze production and particle sizes around 0.03-0.1 microns, the amplitude of the model water feature matches that of the observations. However, these photochemical hazes are assumed to form from hydrocarbons generated by methane photolysis, and we found in the previous section that methane is depleted in the atmosphere of WASP-107b. Further modeling of the condensates is needed for a satisfactory explanation of the data.

### 6. CONCLUSIONS

We analyzed the atmospheric composition of WASP-107b based on its measured near-infrared transmission spectrum and interior structure models of the planet's mass and radius. Key results from this analysis include:

• The upper limit on atmospheric metallicity is 30× solar (assuming the star is young) or FIXME solar for an older system. Higher metallicity envelopes are not allowed because they decrease the planet's radius below the observed value. Based on the Solar System trend of increasing planet metallicity with decreasing planet mass, WASP-107b is expected to have a metallicity of 30× solar, just at

the edge of our allowed range (Kreidberg et al. 2014b). Further characterization of the stellar age is needed to determine whether WASP-107b is consistent with expectations, or discrepant with the Solar System trend, which would suggest an intriguing difference in its formation history. Either way, this planet stands in contrast to the similar mass and temperature planet GJ 436b, which is thought to have a metallicity greater than  $100 \times \text{solar}$  (Morley et al. 2017). Together, these exoplanets suggest a greater diversity of compositions than exists in the Solar System.

- The methane abundance is depleted relative to expectations for a solar abundance pattern. This may be due to an instrinsically low carbon-to-oxygen ratio, which could arise from accretion of water-rich planetesimals (Mordasini et al. 2016; Espinoza et al. 2017). Another possibility is that the planet has a hot interior (~ 500 K), and abundances are quenched at pressure levels where CO is stable (as observed in some directly imaged planets; Skemer et al. 2014; Zahnle & Marley 2014). Such a high internal temperature could be due to latent heat of formation if the planet is very young, and/or tidal heating (Fortney et al. 2008; Morley et al. 2017).
- $\bullet$  Optically thick condensates are present at high altitudes (0.1 3 mbar). Existing models of physically-motivated cloud and haze formation do not satisfactorily reproduce the observed . Clouds form too deep in the atmosphere . (?) GJ 1214b

WASP-107b is slated to be observed with numerous facilities. Transits were recently observed with the WFC3/G102 grism and Spitzer 3.6 and 4.5  $\mu$ m channels. Spitzer eclipses are planned (Program FIXME; PI L. Kreidberg). In addition, WASP-107b is included in the JWST Guaranteed Time Observations.

We thank Fei Dai, Jessica Spake, and Ian Crossfield for productive conversations. L.R.K. acknowledges support from the Harvard Society of Fellows and the Harvard Astronomy Department Institute for Theory and Computation.

Facilities: HST(WFC3)

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