

That’s No Moon: New Analysis Shows No Evidence for Lunar Companion Orbiting Kepler-1625b

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ABSTRACT

Observations of the Kepler-1625 system with the Kepler and Hubble Space Telescopes have suggested the presence of a candidate exomoon, Kepler-1625b-i, a Neptune-radius satellite orbiting a long-period Jovian planet. Here we present a new analysis of the Hubble observations from an independent data reduction pipeline. We find that the transit light curve is well fit with a planet-only model, with a best-fit χ^2_ν equal to 1.01. The addition of a moon does not significantly improve the fit quality. We compare our results directly with [Teachey & Kipping \(2018\)](#), and find that we obtain a better fit to the light curve using a model with fewer free parameters (no moon). We discuss possible sources for the discrepancy in our results, and conclude that there is no single explanation for the difference but rather that it is the sum of many small choices. We conclude that future follow-up efforts for exomoons should focus on alternate targets.

Keywords: planets and satellites: individual (Kepler-1625b)

1. INTRODUCTION

Moons are abundant in the Solar System, and provide clues to the formation history, evolution, and even habitability of the planets they orbit. The great scientific potential of moons has prompted extensive search for lunar companions in exoplanetary systems (exomoons), and creative development of new search techniques (e.g. [Kipping 2009a,b](#); [Kipping et al. 2013](#); [Simon et al. 2010](#); [Peters & Turner 2013](#); [Heller et al. 2014](#); [Noyola et al. 2014](#); [Hippke 2015](#); [Agol et al. 2015](#); [Sengupta & Marley 2016](#); [Vanderburg et al. 2018](#)).

Recently, a potential exomoon candidate was identified in the Kepler-1625 system ([Teachey et al. 2018](#)). The host planet, Kepler-1625b has radius consistent with that of Jupiter and an orbital period of 287 days. The first evidence for the exomoon candidate, Kepler-1625b I, came from three transit observations from the *Kepler* primary mission that showed FIXME ([Teachey et al. 2018](#))...

2. OBSERVATIONS AND DATA REDUCTION

The Kepler-1625 system was observed with 26 continuous *HST* orbits on 28 - 29 October, 2017 (Program GO 15149: PI: A. Teachey). The observations used the Wide Field Camera 3 (WFC3) G141 grism in staring mode, which fixed the spectrum in a constant position on the

detector. At the beginning of the visit, there was a single exposure taken with the F130N filter, which is used to determine the position of the spectral trace. The following exposures used the G141 grism with the SPARS25, NSAMP=15 readout pattern (exposure time of 290.8 seconds; 9 exposures per orbit). For additional description of the observation design, see [Teachey & Kipping \(2018\)](#).

We reduced the *HST* data using custom software developed in [Kreidberg et al. \(2014\)](#). This software has yielded consistent results with multiple independent pipelines (e.g. [Knutson et al. 2014](#); [Spake et al. 2018](#)). We ran our pipeline on the `flt` data product provided by the Space Telescope Science Institute (STScI). The `flt` files are corrected for dark current, bias, and non-linearity, and they are cleaned of cosmic ray hits based on a fit to the up-the-ramp samples. In keeping with previous WFC3 analysis, we discarded the first orbit of data, where the instrument systematics have larger amplitude. We also discard exposures taken during the South Atlantic Anomaly passage (exposures 107, 116, 125, and 126).

To begin the data reduction, we fit the centroid of the direct image with a two-dimensional Gaussian. The centroid position determines the position of the spectral trace, which we calculated using the coefficients provided in the configuration file

from STScI: `G141.F130N.V4.32.conf`¹. To process the spectra, we flatfielded the raw data using the spectroscopic flatfield coefficients provided by STScI in `WFC3.IR.G141.flat.2.fits`, following the instructions in Section 6 of the aXe User Manual². We then created an extraction box centered on the spectral trace. We varied the height and width of the box in 1-pixel increments to find the window that minimized the root-mean-square (rms) deviation from the best fit to the transit light curve. The best was $450 < X < 574$, and $522 < Y < 536$, where X and Y are physical pixels in the spectral and spatial direction, respectively.

We reduced the grism exposures with the optimal extraction routine of Horne (1986), which minimizes background noise in the extracted spectrum by weighting pixels that are dominated by the target spectrum more heavily than pixels dominated by the background. The inputs for optimal extraction are the background-subtracted data array, the error array (including photon noise read noise, and uncertainty due to background subtraction), an initial guess for the spectrum and its uncertainty, and a mask array for bad pixels. For the initial guess of the spectrum and its uncertainty, we did a simple box extraction (sum over all rows in the extraction window), and assumed the variance was equal to the box-extracted spectrum (expected for photon noise limit). We measured and subtracted the background from the data array as described in 2.1. For the error array, we used a quadrature sum of the photon noise (the square root of the pixel counts), the read noise (12 photoelectrons for `flt` files; WFC3 Data Handbook³), and the error due to background subtraction (described in 2.1). The initial pixel mask marked all pixels as good.

In brief, optimal extraction is an iterative procedure with the following steps. First, we created a smoothed image by median-filtering each row of the data with a 9-pixel-wide window. We then normalized the smoothed image by dividing each column by its sum, and multiplied it by the best guess spectrum. We compared the smoothed image to the real data and masked outliers in the data that are greater than a threshold σ_{cut} . We then recomputed the best guess spectrum with the new mask and the optimal weights from Horne (1986). The process is iterated until no outliers greater than the threshold remain. This procedure masks any cosmic rays or bad pixels that were missed by the initial `flt` calibration.

¹ available at http://www.stsci.edu/hst/wfc3/analysis/grism_obs/calibrations/wfc3_g141.html

² <http://axe-info.stsci.edu/>

³ <http://www.stsci.edu/hst/wfc3/documents/handbooks/currentDHB/>

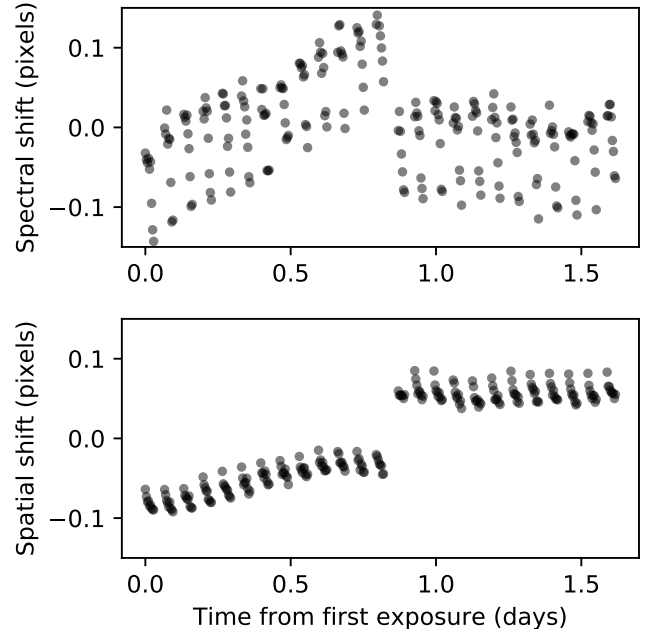


Figure 1. Shift (in pixels) relative to the mean position of the spectrum in the spectral direction (top) and spatial direction (bottom). The largest shift occurs after orbit 14 due to a guide star reacquisition.

We tested a range of thresholds ($7.5 < \sigma_{\text{cut}} < 15$) and found that different σ_{cut} choices did not significantly change the final transit light curve. The data reported in this work use $\sigma_{\text{cut}} = 7.5$. To create the broadband transit light curve, we sum each spectrum over all wavelengths.

2.1. Background Subtraction

The star Kepler-1625 is faint (H mag = 14.0) relative to most other exoplanet host stars observed with WFC3, which makes accurate background subtraction especially important for this target. Moreover, the host star is in a crowded field, so the pixels used to estimate the background must be chosen carefully to avoid contamination from other stars. To estimate the background counts, we masked pixels with total counts larger than 800 electrons (2.7 electrons/sec) and took the median count in the unmasked pixels. The per pixel uncertainty due to background subtraction is 1.4826 times the median absolute deviation.

2.2. Pointing Drift Measurement

The position of the spectrum on the detector shifts slightly over time (~ 0.1 pixel/day) due to the spacecraft's pointing drift. This drift can change the flux measured for the target star: if the spectrum moves onto less sensitive pixels, fewer photoelectrons are recorded.

To enable a correction for this effect, we measured the position of the spectrum over time.

To measure shifts in the spatial direction, we first summed each `flt` image over all columns (which we dub the “column sum”). We used the first exposure in the visit as a template, and for each subsequent exposure, we used least-squares minimization to calculate the shift in pixels that minimized the difference between its column sum and the template. The shifts are a fraction of a pixel, so we used the NumPy `interp` routine to do linear interpolation on a sub-pixel scale. The WFC3 point spread function is undersampled, so we convolved each column sum with a 4-pixel-wide Gaussian before the interpolation (following Deming et al. 2013).

To measure the spectral shifts, we repeated this procedure with two differences: (1) we used the optimally extracted spectrum rather than the column sum; and (2) in addition to calculating the best fit shift, we also calculated a best fit normalization factor (a scalar multiple for the whole spectrum), to ensure that our results are not biased by the varying brightness of the host star during the planet’s transit.

Figure 1 shows the best fit shifts. Over the entire 26-orbit visit, the maximum shift is less than 0.2 pixel in the spatial direction and 0.3 pixel in the spectral direction. The largest shift occurs after orbit 14, when the telescope reacquired the guide stars.

3. ANALYSIS

The raw light transit light curve (shown in Figure 2) contains both astrophysical signal and instrument systematic noise, which we model simultaneously.

3.1. Astrophysics Model

For the astrophysics, we used the `planetplanet` package (Luger et al. 2017), a photodynamical code that calculates light curves for multiple occulting bodies orbiting a star. Within `planetplanet`, the orbits are computed with the N-body integrator REBOUND (Rein & Liu 2012). The `planetplanet` model returns the system flux at a specified orbital architecture and time.

In our analysis, we considered two scenarios: a no-moon model and a moon model. The free parameters for the no-moon model were: the stellar radius R_* , the planet radius R_{planet} , the time of central transit t_{planet} , and the planet inclination i . For the moon model, we added a third body with radius R_{moon} , transit time t_{moon} , and orbital period P_{moon} . We allowed the moon period to vary from 1.6 to 260 days. These limits span the duration of the *HST* observations (so there is one possible moon occultation event), to the orbit at 0.5 the Hill radius, based on the stability limit for prograde

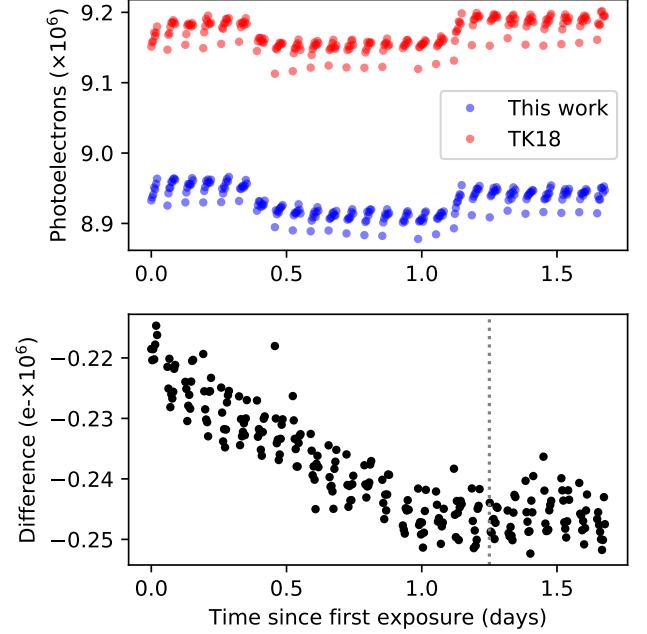


Figure 2. Top: raw data from this work (blue) compared to TK18 (red). Bottom: the difference in raw photoelectron counts between the data sets. The moon ingress identified by TK18 is marked by the dotted gray line.

moon orbits (Domingos et al. 2006). The Hill radius calculation assumed the planet and stellar masses are $1 M_{\text{Jup}}$ and $1.37 M_{\odot}$.

The models also fix several parameters that are poorly constrained by the light curve shape. For the moon model, we fixed inclination of the moon to 90° to exclude grazing transit scenarios, where the moon radius could be arbitrarily large. We also fixed the moon mass and eccentricity to zero. For both the no-moon and moon models, we fixed the planet’s orbital period to 287.378949 days (Teachey & Kipping 2018). We also fixed the planet eccentricity to zero and the mass to $1 M_{\text{Jup}}$.

3.1.1. Stellar Parameters

For both the moon and no-moon scenarios, we used a quadratic stellar limb darkening law and fixed the coefficients to the prediction for a 5700 K, solar metallicity PHOENIX model from Espinoza & Jordán (2015); $u_1, u_2 = [0.216, 0.183]$.

We estimated the host star parameters using the Gaia DR2 parallax (Gaia Collaboration et al. 2016, 2018) along with UBV photometry from Everett et al. (2012) and JHK photometry from 2MASS (Skrutskie et al. 2006). We employed the isochrone python package (Morton 2015) with the Dartmouth isochrone grid (Dotter et al. 2008) to obtain posterior constraints on the

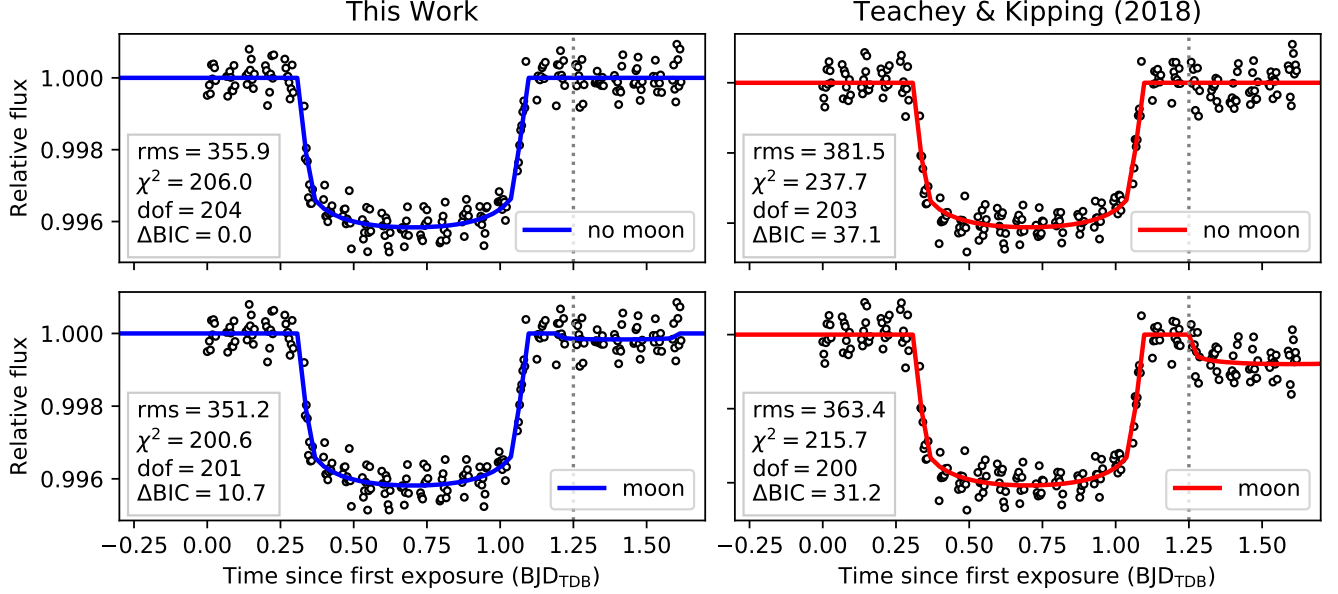


Figure 3. Best fit models compared to normalized transit light curves from this work (left, blue) and from TK18 (right, red). The top panel shows the best fit no-moon model, and the bottom shows the best fit moon model. The lower left of each panel indicates the fit rms (in ppm), the χ^2 , the degrees of freedom, and the change in BIC relative to the lowest value. Each light curve is divided by its best fit systematics model (XY decorrelation for this work; second-order polynomial and offset for TK18). The dotted gray line marks the possible moon ingress identified by TK18.

stellar parameters. The resulting parameters indicate that Kepler-1625 has stellar mass $1.37^{+0.13}_{-0.16} M_{\odot}$, radius $1.81^{+0.18}_{-0.16} R_{\odot}$, and age $2.8^{+1.6}_{-1.2}$ Gyr. In our analysis, we fixed the stellar mass to the best fit value ($1.37 M_{\odot}$), and used a Gaussian prior on the radius, $R_* \sim N(1.81, 0.17)$.

3.2. Instrument Systematics Model

There are two systematic trends in the data. One is the orbit-long ramp, attributed to charge traps in the detector filling up over the orbit (Zhou et al. 2017). The other is a visit-long trend over multiple orbits, which could be due to shifts in the target star position onto more/less sensitive pixels.

To fit the orbit-long ramp, we used the non-parametric model from Teachey & Kipping (2018), which assigns each of the nine exposures per orbit a normalization constant, c_1, \dots, c_9 . To fit the visit-long trend, we used a linear combination of X and Y position (the shift relative to the mean in the spatial and spectral directions, respectively; shown in Figure 1). In sum, for exposure number i , the systematics model S is:

$$S_i = c_j \times (1 + aX_i + bY_i) \quad (1)$$

where a and b , and c_j are free parameters, and $j = i \bmod 9 + 1$ is the exposure number relative to the first exposure in the orbit.

3.3. Light Curve Fits

We fit the raw, broadband transit light curve using the models described above. We determined the best fit model parameters with least-squares minimization. We also ran a Markov chain Monte Carlo (MCMC) fit to determine the posterior probability of each parameters. For the MCMC, we held the ramp parameters c_1, \dots, c_9 fixed at their best-fit values. The MCMC used the `emcee` package (Foreman-Mackey et al. 2013) with 50 walkers and ran for 5000 steps. We discarded the first 20% of the MCMC chain as burn-in. As a quick test for convergence, we divided the remainder of the chain in half and confirmed that the results from the first half were consistent with the second half.

4. RESULTS

We obtained an excellent fit to the light curve with the no-moon model, as illustrated in Figure 3. The residuals to the no-moon model fit have rms equal to 356 parts per million (ppm), which is within 3% of the predicted photon shot noise (367 ppm), and yields a $\chi^2_{\nu} = 1.01$. The binned rms decreases with the square root of the number of points per bin, as expected for photon noise-limited statistics (see rms versus bin size in Figure 4).

We obtained a slightly better fit with the moon model (rms = 351 ppm; $\chi^2_{\nu} = 0.998$); however, this is not a large enough improvement in fit quality to merit the addition of three additional free parameters. According to the Bayesian information criterion (BIC), which pe-

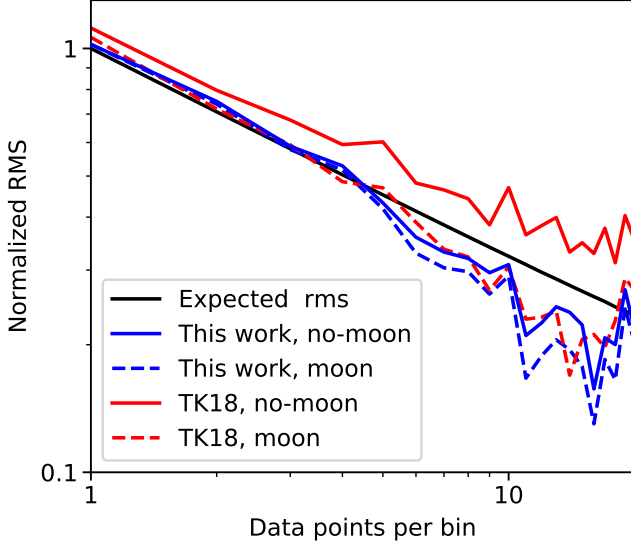


Figure 4. Light curve rms versus bin size for the best fit no-moon model (solid lines) and moon model (dashed lines), for data from this work (red) and TK18 (blue). The fits to data from this work agree well with the expected photon-limited, \sqrt{N} decrease in rms with bin size (black line). We also reach the photon limit for the TK18 data, but only for the moon model. The rms for the no-moon fit (red dashed line) ranges from $1.1 - 1.5\times$ the photon limit for 1 to 20 points per bin.

nalizes unnecessary model complexity, the moon model is disfavored with $\Delta\text{BIC} = 10.7$. This constitutes strong evidence against the inclusion of a moon (Kass & Raftery 1995). In addition, the moon transit time is not well-constrained by the data. As shown in the posterior distribution in Figure 5, the 2σ confidence interval for the moon’s transit includes the entire duration of the observations. The upper limit on the moon radius is $3.2 R_{\oplus}$ at 2σ confidence and $4.0 R_{\oplus}$ at 3σ .

4.1. Comparison with Teachey & Kipping (2018)

Teachey & Kipping (2018) found evidence for the transit of a Neptune-size moon in their analysis of the HST data, in contrast to the findings presented here. To make a direct comparison with their results, we fit the raw TK18 data directly.

We fit the data with both the no-moon and models. For the systematics, we tested the XY decorrelation model described above, but found that it did not perform as well as the systematics models presented in TK18 (10% higher rms and time-correlated residuals). We therefore opted to use a TK18 systematics model to enable a fair comparison between our results. We obtained the best fit using a second-order polynomial trend in time, a constant offset after orbit 14 (where the guide stars are reacquired), and the non-parametric

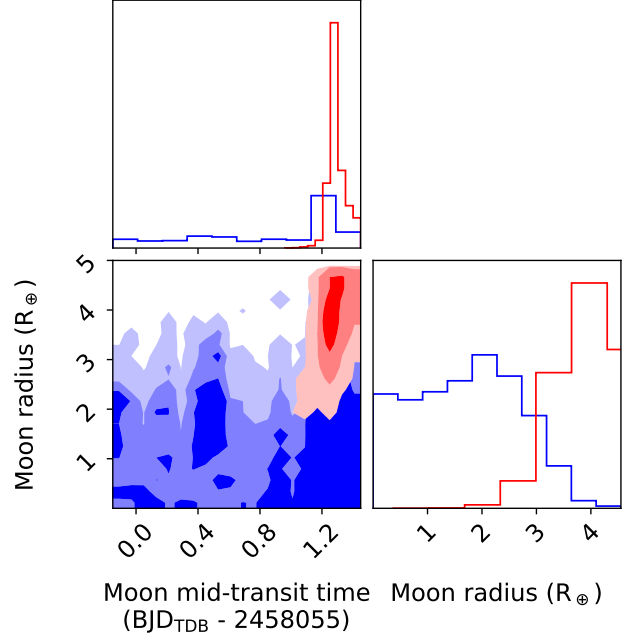


Figure 5. Posterior distributions for the moon radius and time of transit based on an MCMC fit to data from this work (blue) and from TK18 (red). The shading corresponds to $1-$, $2-$, and 3σ contours (from darkest to lightest). These values are marginalized over all other model parameters.

orbit-long ramp model. This model has one more free parameter than the systematics model given in Equation 1. Figure 3 shows the best fit models.

Similar to the findings of TK18, the moon model improved the fit quality by a $\Delta\chi^2 = 22.0$. Notably, however, the moon model fit to the TK18 data does not perform better than the no-moon model fit to our new data (rms of 363 versus 356 ppm), even with the additional four free parameters. This difference in fit quality corresponds to $\Delta\text{BIC} = 31.2$, which is strong evidence against the moon.

The moon model also yields qualitatively different posterior distributions for the two data sets. As shown in Figure 5, for the TK18 data the moon radius and transit time are peaked at $r_{\text{moon}} = 4.0^{+0.8}_{-0.6} R_{\oplus}$ and $t_{\text{moon}} = 2458056.29^{+0.06}_{-0.04} \text{BJD}_{\text{TDB}}$. By contrast, the fit to the new data presented here yields an upper limit on the moon radius of $(4.0 R_{\oplus})$ at 3σ confidence, and the transit time is unconstrained.

5. DISCUSSION

A natural question arising from our results is what the difference is between TK18 and the new fits presented here. One possibility is that the source of the discrepancy is the raw data itself. As shown in Figure 2, our measured count rate ranges from 2.46 – 2.74% lower

than the TK18 measurement, and there is a small bump in the difference between the two data sets near the location of the moon transit identified in the TK18 data (see the bottom panel).

We explored several modifications to our pipeline to attempt to reproduce the TK18 reduction. These included rotating the image by 0.5 degrees, using the same aperture as TK18 to extract the spectrum, and scaling the master sky flat for the background subtraction (rather than just subtracting the median). None of these modifications had a significant effect on our results.

There are a few other steps in the TK18 data reduction that would require substantial modification of our pipeline to recreate, but seem unlikely to be responsible for the difference. One of these is outlier masking. TK18 identify outliers with a Gaussian process fit to the pixel-level light curves, compared to our optimal extraction approach. Despite the difference, both methods flag $\sim 0.01\%$ of pixels as bad. We also do not use the STScI software **axeprep** to embed the raw 256×256 image in a larger array; however, this process primarily affects the edge of the image, many pixels distant from the extraction box, so it is unclear how this step would bias the light curve.

In addition to these differences in data reduction, we also used a new detrending model. We opted for a decorrelation against X and Y position, motivated by known variation in the sensitivity of individual pixels on the detector and the presence of small shifts in the position of the spectrum (see Figure 1). We applied this detrending model to the TK18 data, and obtained a poor fit to the light curve compared to the polynomial detrending (for the moon model with X-Y decorrelation, the rms was 404 ppm). We did not recover a large moon in this fit (the best fit was $r_{\text{moon}} = 1.2R_{\oplus}$), but there was correlated noise present in the data that precluded a robust measurement of the uncertainty on the moon radius for this model. The poor quality of the fit points toward the raw data as the culprit for the difference in our results, but as we discuss, we could not identify a specific choice in the data reduction that is responsible.

We conclude that no single choice in the data reduction or the modeling provides an easy explanation for the difference in our results, but rather that the difference is in the sum of many subtle choices.

6. CONCLUSION

The hunt for exomoons remains exciting and volatile. Our analysis of the exomoon candidate Kepler-1625b-i shows that the evidence in favor of the moon is highly sensitive to details of the data reduction and modeling. Future allocation of follow-up resources should prioritize alternative targets.

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