# A Likelihood Ratio Test for Hybridization Under the Multispecies Coalescent

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In the following sections, we show the supplemental figures of detection power and type I error using our LR test, HyDe and ABBA-BABA test under JC69 and HKY85+Gamma model with different branch lengths and number of sites in section 2.3.

#### S1. Comparison of three hybridization tests under HKY85+I model

In this section, we consider 500 CIS datasets simulated under HKY85+I model for each setting. For the speciation times in Figure S1(a)–(c), we assigned the vector  $(\tau_1, \tau_2, \tau_3) = (0.25, 0.5, 1.0)$ , while in Figures S1(d)–(f), we assigned the vector  $(\tau_1, \tau_2, \tau_3) = (0.5, 1.0, 2.0)$ . The hybridization parameter  $\gamma$  is chosen to be 0 or to vary from 0.06 to 0.5 by 0.02.

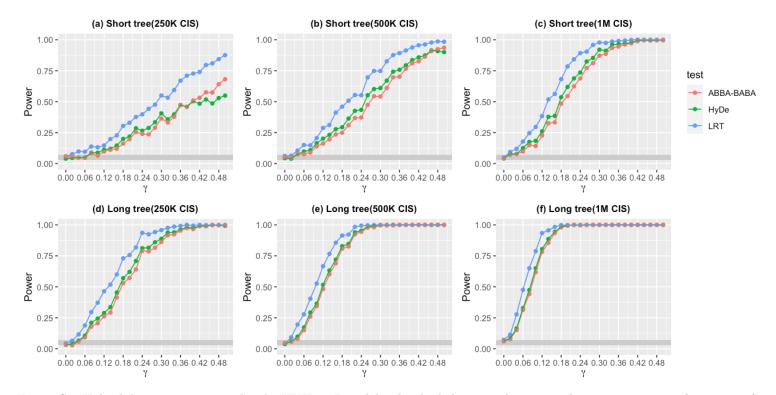


Figure S1: Hybrid detection power under the HKY85+I model. The shaded area is the expected acceptance region (0.031,0.069) of the empirical type I error rate. (a) – type I error rates are 0.058 (LRT), 0.040 (HyDe) and 0.060 (ABBA-BABA). (b) – type I error rates are 0.062 (LRT), 0.044 (HyDe) and 0.054 (ABBA-BABA). (c) – type I error rates are 0.050 (LRT), 0.042 (HyDe) and 0.048 (ABBA-BABA). (d) – type I error rates are 0.042 (LRT), 0.032 (HyDe) and 0.036 (ABBA-BABA). (e) – type I error rates are 0.040 (LRT), 0.038 (HyDe) and 0.048 (ABBA-BABA). (f) – type I error rates are 0.072 (LRT), 0.062 (HyDe) and 0.060 (ABBA-BABA).

## S2. Comparison of three hybridization tests under HKY85+I+ $\Gamma$ model

In this section, we consider 500 CIS datasets simulated under HKY85+I+ $\Gamma$  model for each setting. For the speciation times in Figure S2(a)–(c), we assigned the vector  $(\tau_1, \tau_2, \tau_3) = (0.25, 0.5, 1.0)$ , while in Figures S2(d)–(f), we assigned the vector  $(\tau_1, \tau_2, \tau_3) = (0.5, 1.0, 2.0)$ . The hybridization parameter  $\gamma$  is chosen to be 0 or to vary from 0.06 to 0.5 by 0.02.

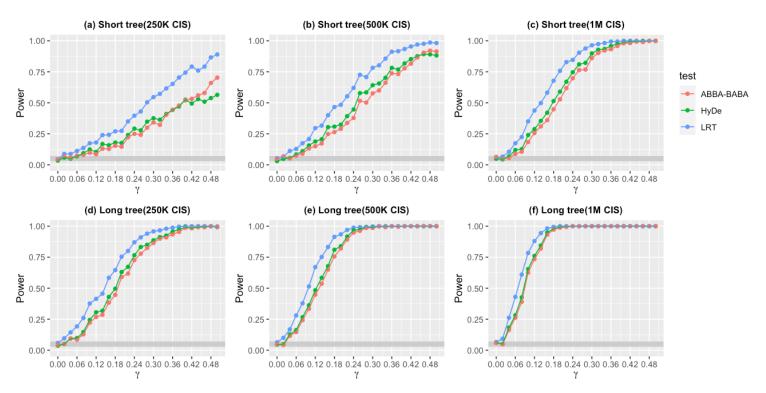


Figure S2: Hybrid detection power under the HKY85+I+ $\Gamma$  model. The shaded area is the expected acceptance region (0.031,0.069) of the empirical type I error rate. (a) – type I error rates are 0.044 (LRT), 0.034 (HyDe) and 0.044 (ABBA-BABA). (b) – type I error rates are 0.054 (LRT), 0.030 (HyDe) and 0.048 (ABBA-BABA). (c) – type I error rates are 0.050 (LRT), 0.050 (HyDe) and 0.064 (ABBA-BABA). (d) – type I error rates are 0.058 (LRT), 0.036 (HyDe) and 0.042 (ABBA-BABA). (e) – type I error rates are 0.064 (LRT), 0.044 (HyDe) and 0.048 (ABBA-BABA). (f) – type I error rates are 0.066 (LRT), 0.060 (HyDe) and 0.060 (ABBA-BABA).

### S3. Comparison of three hybridization tests under JC69 model

#### S3.1. Short branch tree

In this section, we consider CIS and multilocus datasets simulated under JC69 model. For the speciation times in Figure ??, we assigned the vector  $(\tau_1, \tau_2, \tau_3) = (0.25, 0.5, 1.0)$ . The hybridization parameter  $\gamma$  is chosen to be 0 or to vary from 0.06 to 0.5 by 0.02.

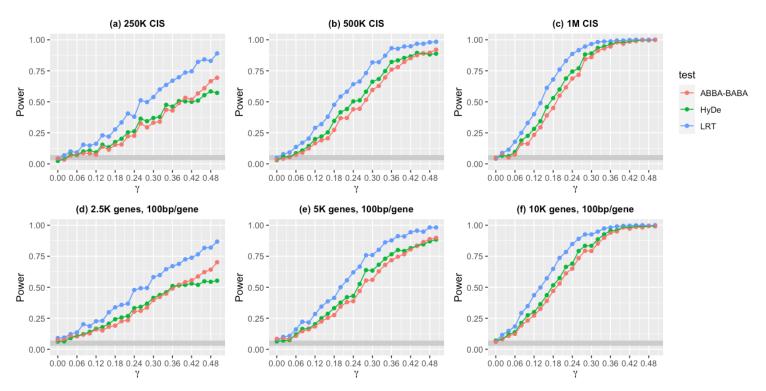


Figure S3: Hybrid detection power under JC69 for the short branch tree. The shaded area is the expected acceptance region (0.031,0.069) of the empirical type I error rate. (a) -250K CIS data with type I error rates 0.040 (LR), 0.024 (HyDe), 0.044 (ABBA-BABA); (b) -500K CIS data with type I error rates 0.048 (LR), 0.030 (HyDe), 0.036 (ABBA-BABA); (c) -1M CIS data with type I error rates 0.042 (LR), 0.048 (HyDe), 0.050 (ABBA-BABA); (d) -1 multilocus data with 0.048 (

#### S3.2. Long branch tree

For the speciation times in Figure ??, we assigned the vector  $(\tau_1, \tau_2, \tau_3) = (0.5, 1.0, 2.0)$ . The hybridization parameter  $\gamma$  is chosen to be 0 or to vary from 0.06 to 0.5 by 0.02.

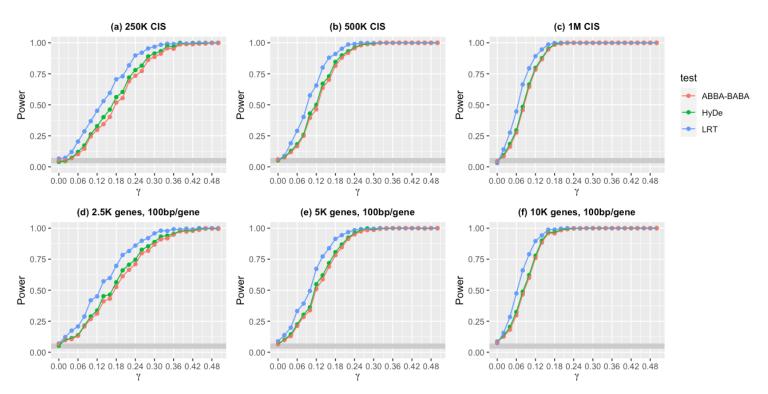


Figure S4: Hybrid detection power under JC69 for the long branch tree. The shaded area is the expected acceptance region (0.031,0.069) of the empirical type I error rate. (a) -250K CIS data with type I error rates 0.066 (LR), 0.040 (HyDe), 0.052 (ABBA-BABA); (b) -500K CIS data with type I error rates 0.056 (LR), 0.052 (HyDe), 0.060 (ABBA-BABA); (c) -1M CIS data with type I error rates 0.030 (LR), 0.044 (HyDe), 0.046 (ABBA-BABA); (d) -1 multilocus data with 0.052 (0