

ENEE631

DIGITAL IMAGE AND VIDEO PROCESSING

Mobile Scanner

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May 16, 2017

Declaration of Authorship

I, Lakshman Kumar K N, declare that this project report titled, "Mobile Scanner" and the work presented in it are my own. I confirm that:

- This work was done wholly for the course ENEE631 - Digital Image and Video Processing at the University of Maryland, College Park.
- Where I have consulted the published work of others, this is always clearly attributed.
- Where I have quoted from the work of others, the source is always given. With the exception of such quotations, this project is entirely my own work.
- I have acknowledged all main sources of help.

Signed:

Date: May 16, 2017

Abstract

Mobile Scanner

by Lakshman Kumar K N

Cell phones have become an integral part of our life. These devices are now being used to scan a document with its camera. This project attempts to model and implement the technique, by which a document is being scanned by a cell phone's camera and being registered to extract text from a filled form, used by several mobile scanner applications in the digital app stores of cell phones. The modeled technique was then tested on several images and the results were found to be almost close to the output of popular mobile scanner applications. The said techniques comprises of algorithms such as Canny Edge Detection, Border Following based Contour Estimation, ORB Feature Detection/Matching, Harris Corner Detection, Gaussian Minus C Adaptive Thresholding etc.

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List of Abbreviations

OCR	Optical Character Recognition
FAST	Features from Accelerated Segment Test
BRIEF	Binary Robust Independent Elementary Features
ORB	Oriented FAST and Rotated BRIEF
API	Application Programming Interface
KNN	K Nearest Neighbor
SIFT	Scale Invariant Feature Transform
SURF	Speeded Up Robust Features
RANSAC	RANDom SAmple Consensus

1 Overview

1.1 Introduction

With increasing prevalence of cell phones among all the people, traditional devices, that have been used for various functions, are being replaced by cell phones. One such device is the scanner, which has been traditionally used to scan paper documents like forms, receipts, ID's. As the cell phone has a camera in it, the images of paper documents can be captured by it and advanced image processing techniques can be used to extract the document properly. The methodology behind document extraction from camera images and image registration has been implemented and analyzed as a part of this project.

1.2 Problem Statement

The goal of the project is to implement and investigate the techniques that goes behind extracting a document from a mobile phone's image. Apart from just extracting the document, an enhanced functionality, that allows for image registration of a reference blank page and extraction of the filled content, has to be implemented.

1.3 Assumptions Made

- The reference document is captured in a well lit and contrasting environment.
- The reference document is rectangular and convex.
- The reference document's 4 edges and 4 corners are clearly visible.
- The reference document occupies the most area in the captured image.
- The document with filled content has sufficient features.

1.4 Related Works

Various mobile scanning apps, like CamScanner, ScanBot, Evernote Scannable, Turbo Scan, are now available on app stores of Android, Apple and Windows phones. These apps include various sophisticated features, like OCR, Text Extraction, Image Annotation, Document Categorization etc., apart from the basic document extraction functionality .

2 Document Extraction

2.1 Flow Chart

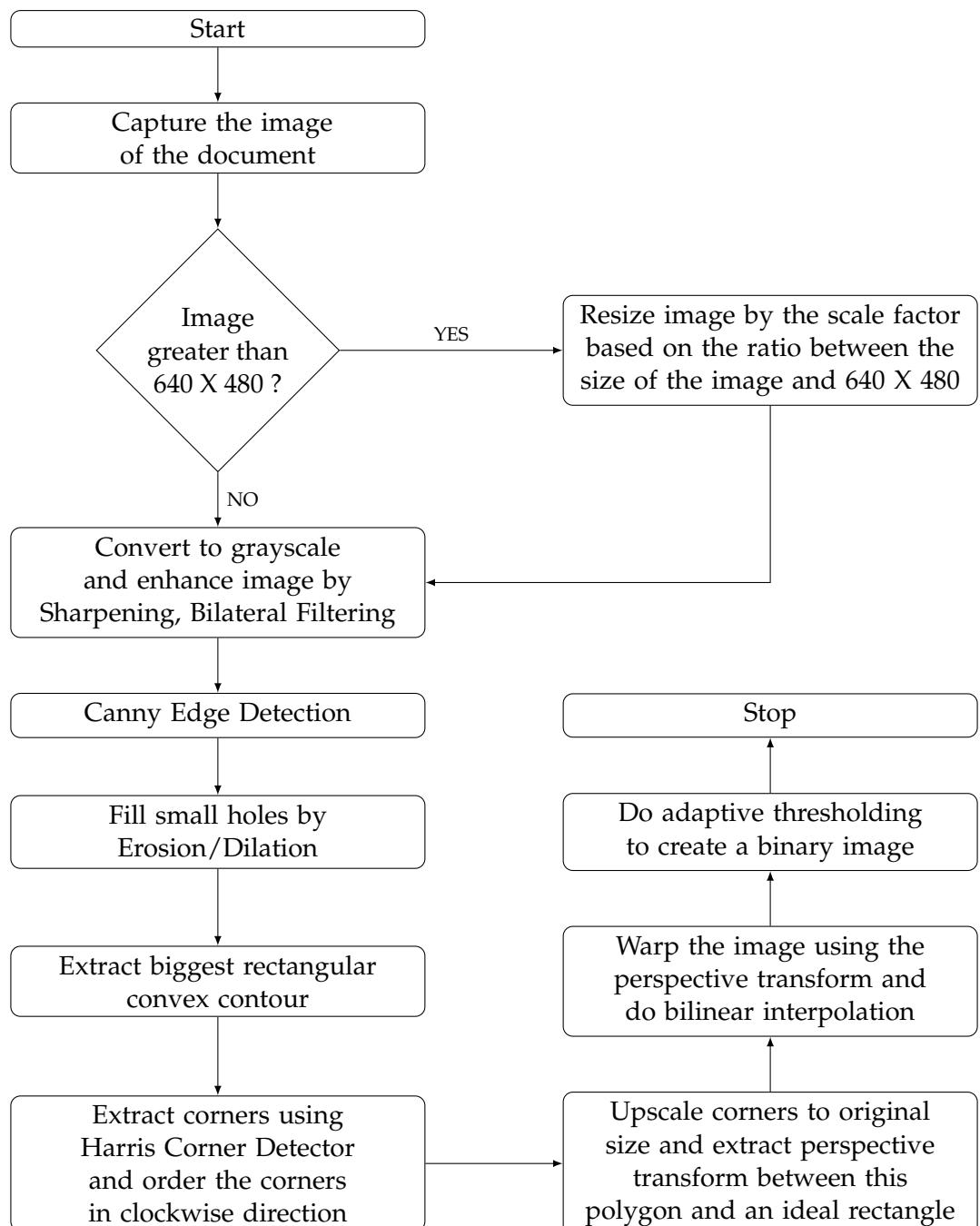


FIGURE 2.1: Flow Chart for Document Extraction

2.2 Document Extraction Techniques

Consider the image shown below from which the document is to be extracted.

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Step 2: RRL User Account Setup Form

Please complete this form and email to Alice Mobaidein at mobaidein@umd.edu.

Date:		
FRS #:		
Principal Investigator Name:		
Principal Investigator Email:		
Department:		
Dept. Business Contact Name:		
Dept. Business Contact Email:		
Dept. Business Contact Phone:		
Account Name (<i>optional</i>): (i.e. ENEE 416, NSF-last_name, etc.)		
Authorized Users: The following users are authorized to charge to this FRS #:		
Name	Phone	Email
Principal Investigator Name:	Date:	
Dept. Business Contact Name:	Date:	
Reviewed by NanoCenter Staff:	Date:	

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FIGURE 2.2: Reference Image.

All the techniques involved in extracting the document/sheet from the given image are briefly explained below.

2.2.1 Image Enhancement

The input RGB image is resized to be below 640 X 480 pixels, if the image size is greater than that. Then the resized image is converted to grayscale by doing weighted addition of R, G and B components and normalizing them to fit 0 to 255 scale. Then the image is sharpened in-order to boost its edges. The edges can be **sharpened** by adding a portion of the high pass filtered image to the original image. In order to smoothen out any noise in the image, **bilateral filter** (Tomasi and Manduchi, 1998) is used. The bilinear filter implemented as a part of this project uses a kernel size of 5 with gaussian weight of 25 and range weight of 15 . The bilateral filter basically does gaussian filtering everywhere in the image except at the edges.

The resulting enhanced image is shown below.

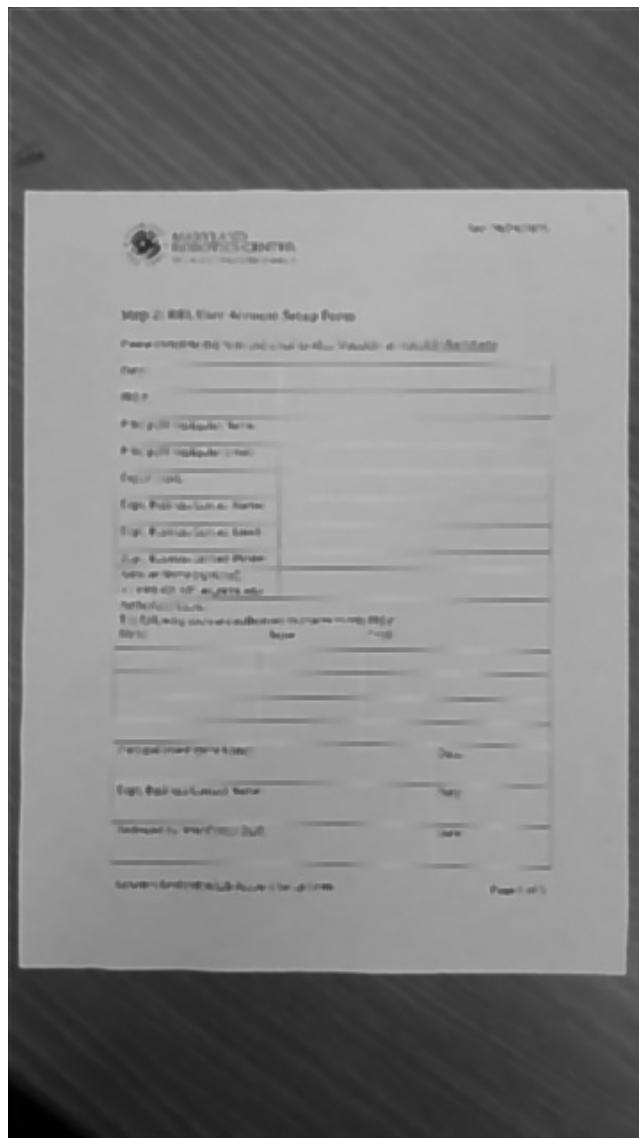


FIGURE 2.3: Image Enhancement.

2.2.2 Canny Edge Detection

The edges from the enhanced image can be extracted using the **Canny Edge Detection** method (Canny, 1986).

The canny edge detection algorithm proceeds as shown in the flow chart below.

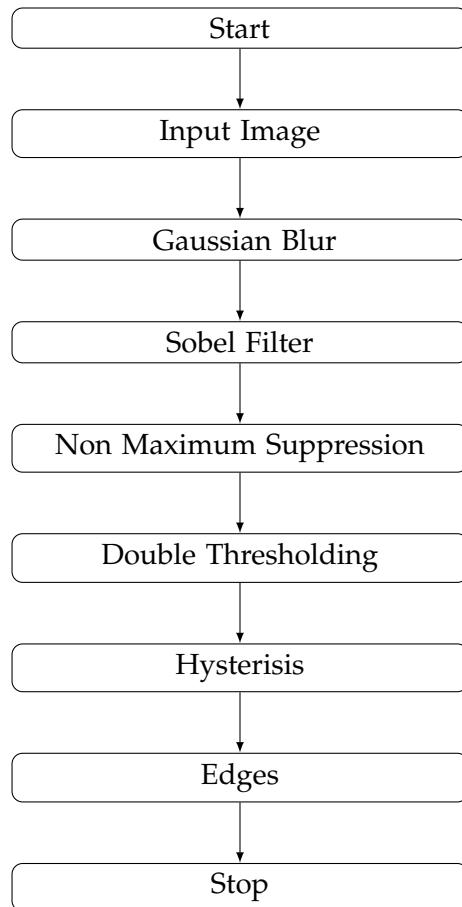


FIGURE 2.4: Flow Chart for Canny Edge Detection

This is a multi-step edge detection algorithm that typically uses and optimizes other edge detection operators such as Prewitt, Robert and Sobel. First the input image is smoothed with a **Gaussian Filter**. Then an edge detection operator like **Sobel Filter** is applied to the image and the intensity gradient and direction is computed. Based on the gradient and its direction, **non maximum suppression** is applied to make the edges thinner. Strong and weak edges from the resulting image are identified by **double thresholding** it. The weak edges are then tracked to see if its connected to other strong edges, in which case the weak edge will now be considered as strong edge or will be eliminated otherwise. This process is called **hysterisis**.

The result of canny edge detection on the previously enhance image is shown below.

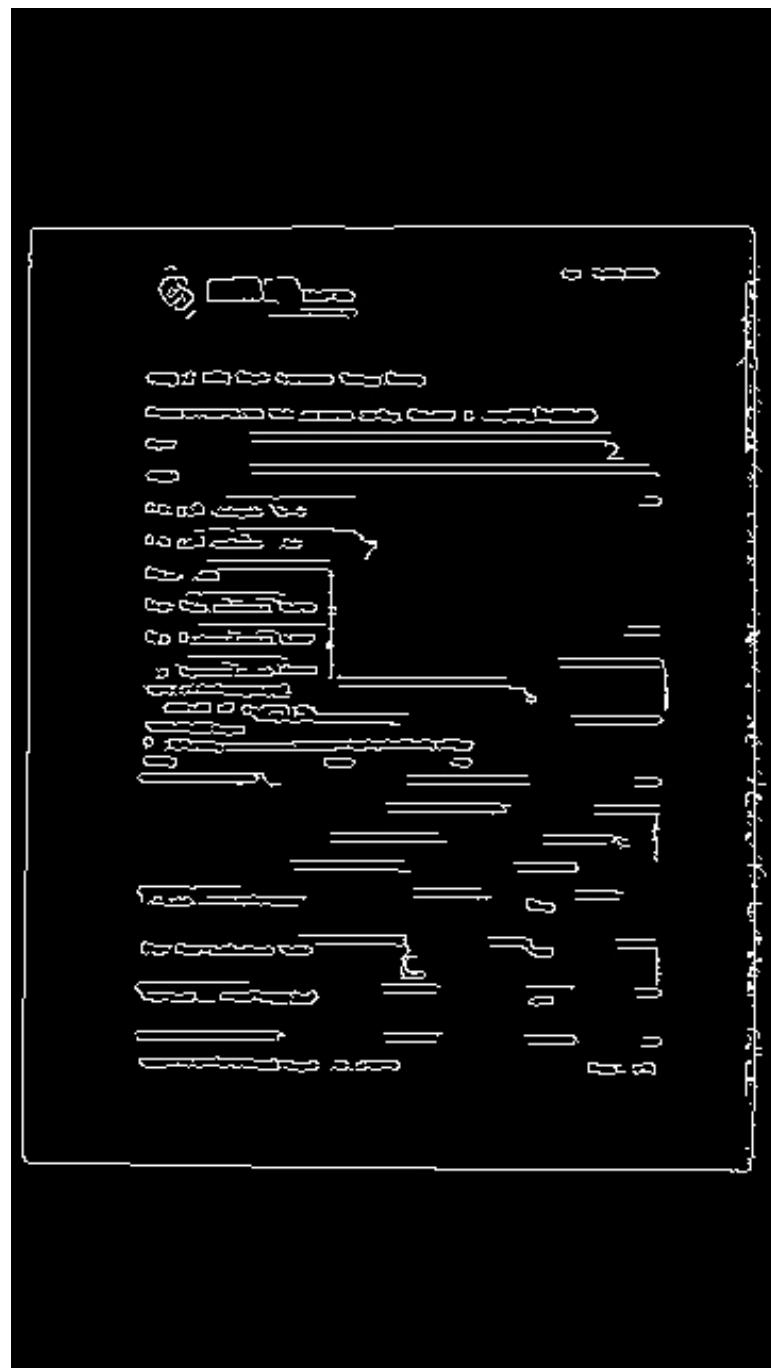


FIGURE 2.5: Canny Edge Detection.

2.2.3 Morphological Operations

The edges extracted from the enhanced image can sometimes have some discontinuities and minute holes that might need to be eliminated for further processing to work. In order to do that, a variety of morphological operations, namely **Erosion** and **Dilation**, are used. Dilation replaces the pixel in an image with the pixel that has the highest value. Hence, this operation thickens the white edges. Erosion on the other hand replaces the pixel in an image with the pixel that has the lowest value. Thus, this operation thins the white edges. A combination of these two operations can be used to do morphological opening and closing. The edges are first dilated and then eroded in order to close the discontinuities. This combination is referred to as **morphological closing**. Then the edges are eroded and dilated in order to make the edges thinner. This combination is referred to as **morphological opening**.

The result of morphological closing and opening on the extracted edges are shown below.

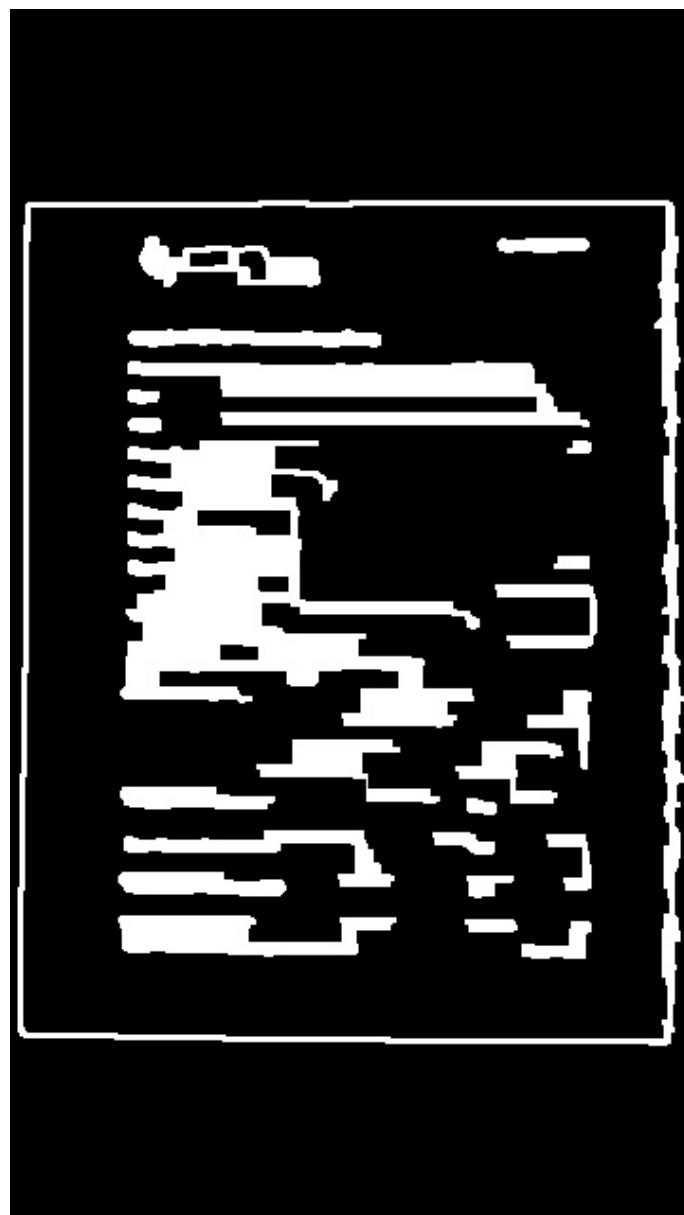


FIGURE 2.6: Morphological Operations.

2.2.4 Contour Detection

The image computed previously contains a lot of **contours**. The contours from this image are extracted using OpenCV's (Bradski, 2000) '**findContour**' function . Contours are estimated by using the **Boundary Following Algorithm for Topological Analysis**, proposed by Suzuki and Abe, 1985. The largest convex contour, with 4 vertices, is found and the pixels inside this contour is assumed to contain the document that has to be scanned .

The estimated contour is overlaid on the original image and shown below.

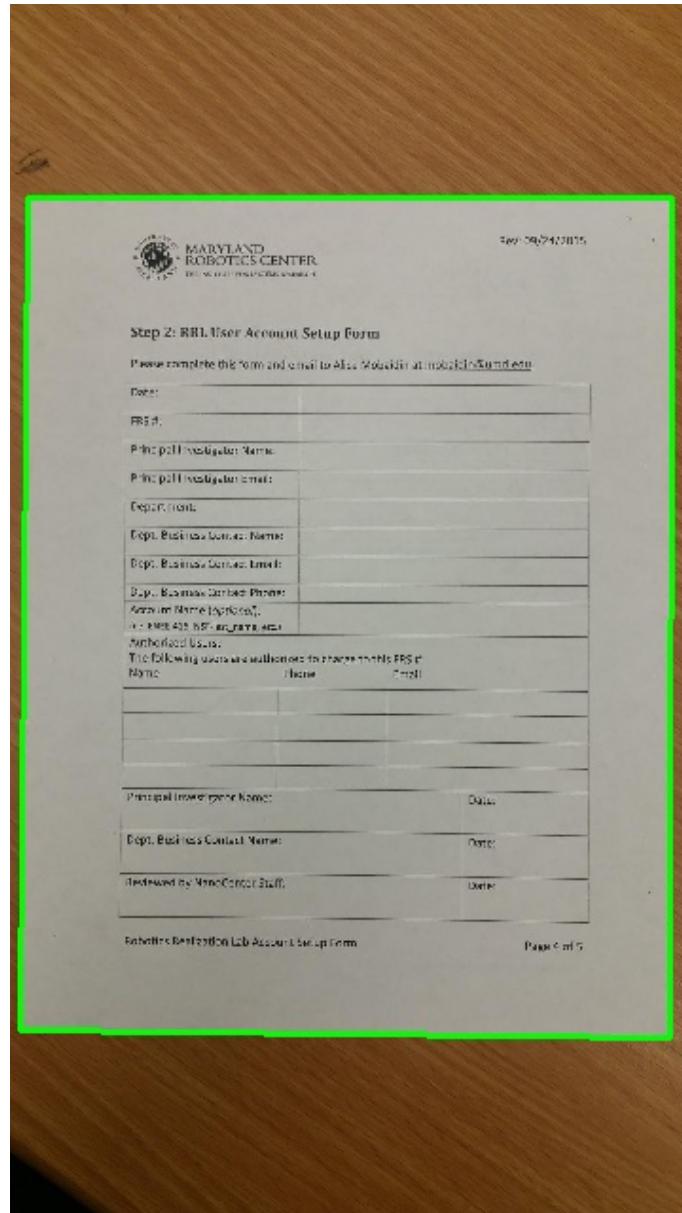


FIGURE 2.7: Contour Detection.

2.2.5 Harris Corner Detection

The contour estimated above basically has 4 corners. In order to compute them **Harris Corner Detection** (Harris and Stephens, 1988) is used.

The Harris Corner Detection algorithm proceeds as shown in the flow chart below.

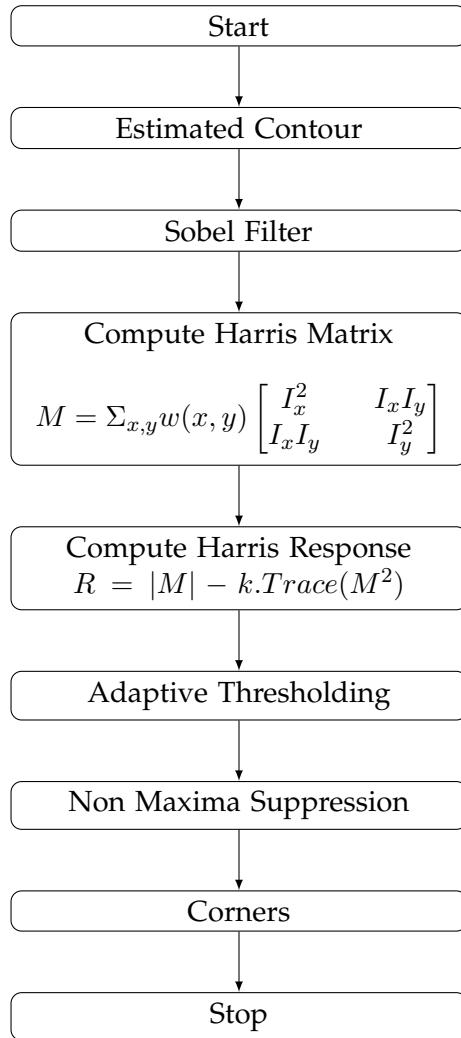


FIGURE 2.8: Flow Chart for Harris Corner Detection

Harris Corner Detection method estimates the location of corners based on the gradients at each pixel. It fundamentally relies on the property that corners have large gradients in both x and y direction. The algorithm proceeds by computing the x and y gradients of the image using operators like Sobel. Based on these gradients, the Harris Matrix is computed. Then the Harris Response is obtained from the Harris Matrix M where k 's best estimate by Harris was found to be 0.04. The response image is adaptively thresholded in order to obtain the corners. There might be a lot of estimated corners very close to each other , these group of corners are replaced by just one corner by doing non-maxima suppression.

The result of harris corner detection on the estimated contour is overlaid on the original image shown below

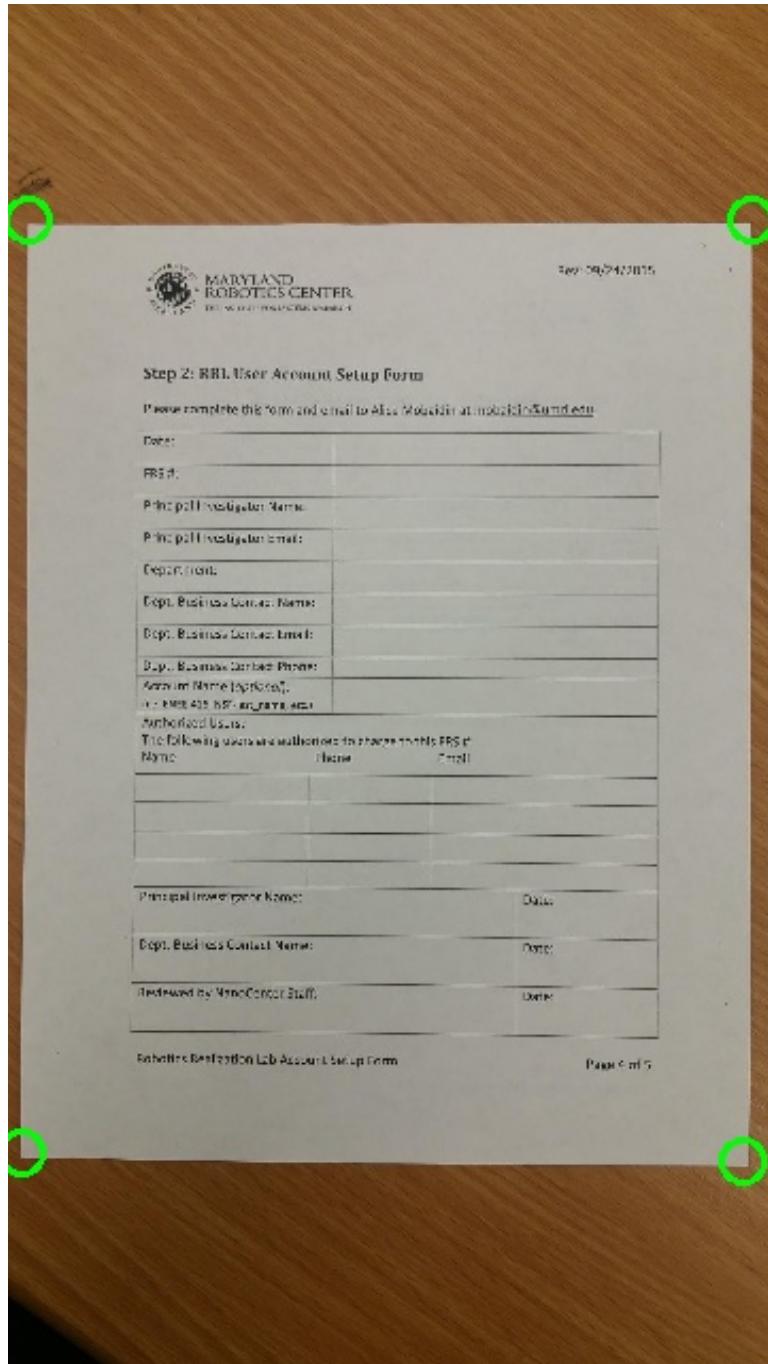


FIGURE 2.9: Corner Detection.

2.2.6 Perspective Transform and Warping

The four corners obtained above are ordered in the clockwise manner. The width and height of the contour are approximated based on the location of these corners and then a reference rectangle is constructed based on this.

The **perspective transform** (Mundy and Zisserman, 1992) between the corners of the contour and the corners of the reference rectangle can be computed to warp the image as shown below.

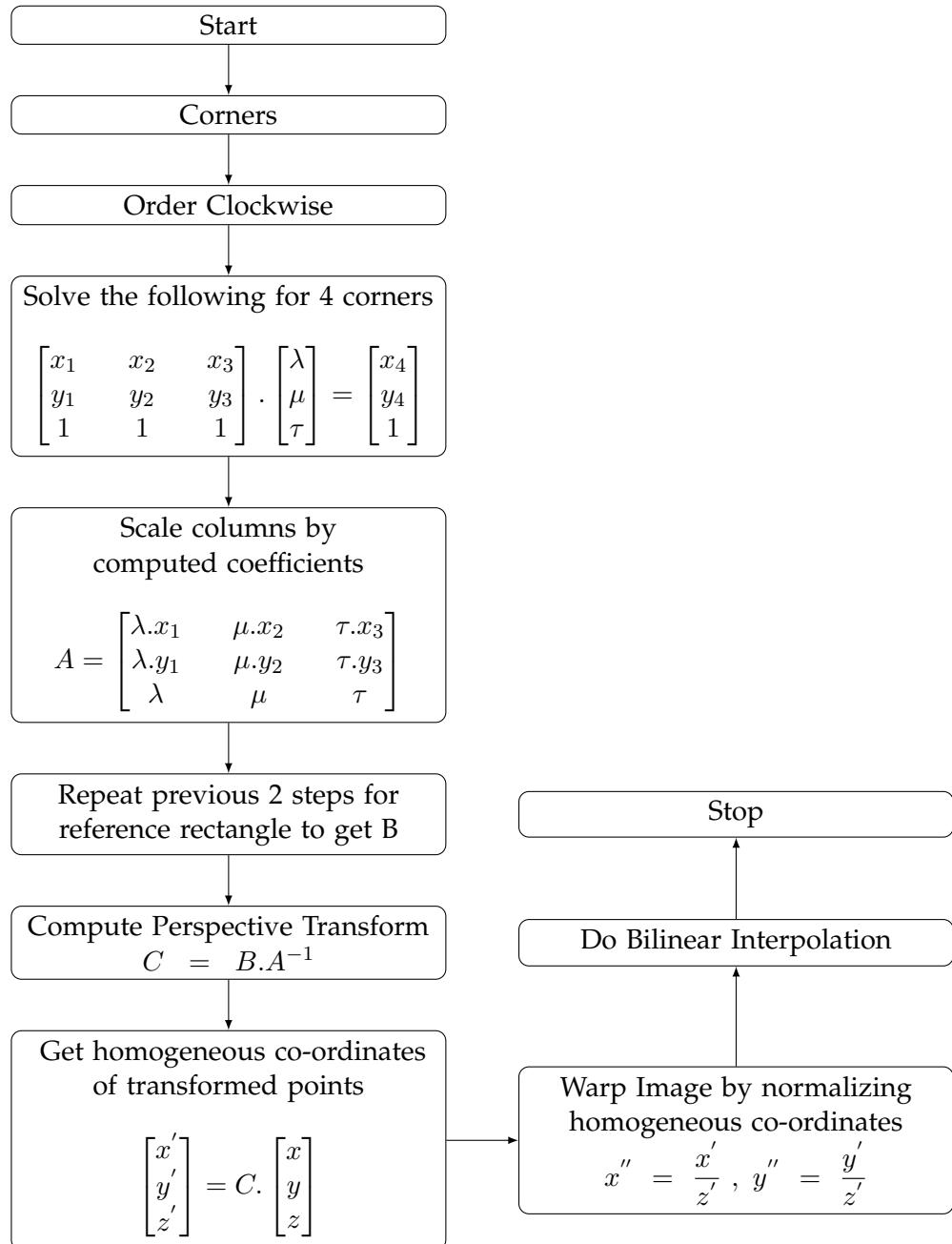
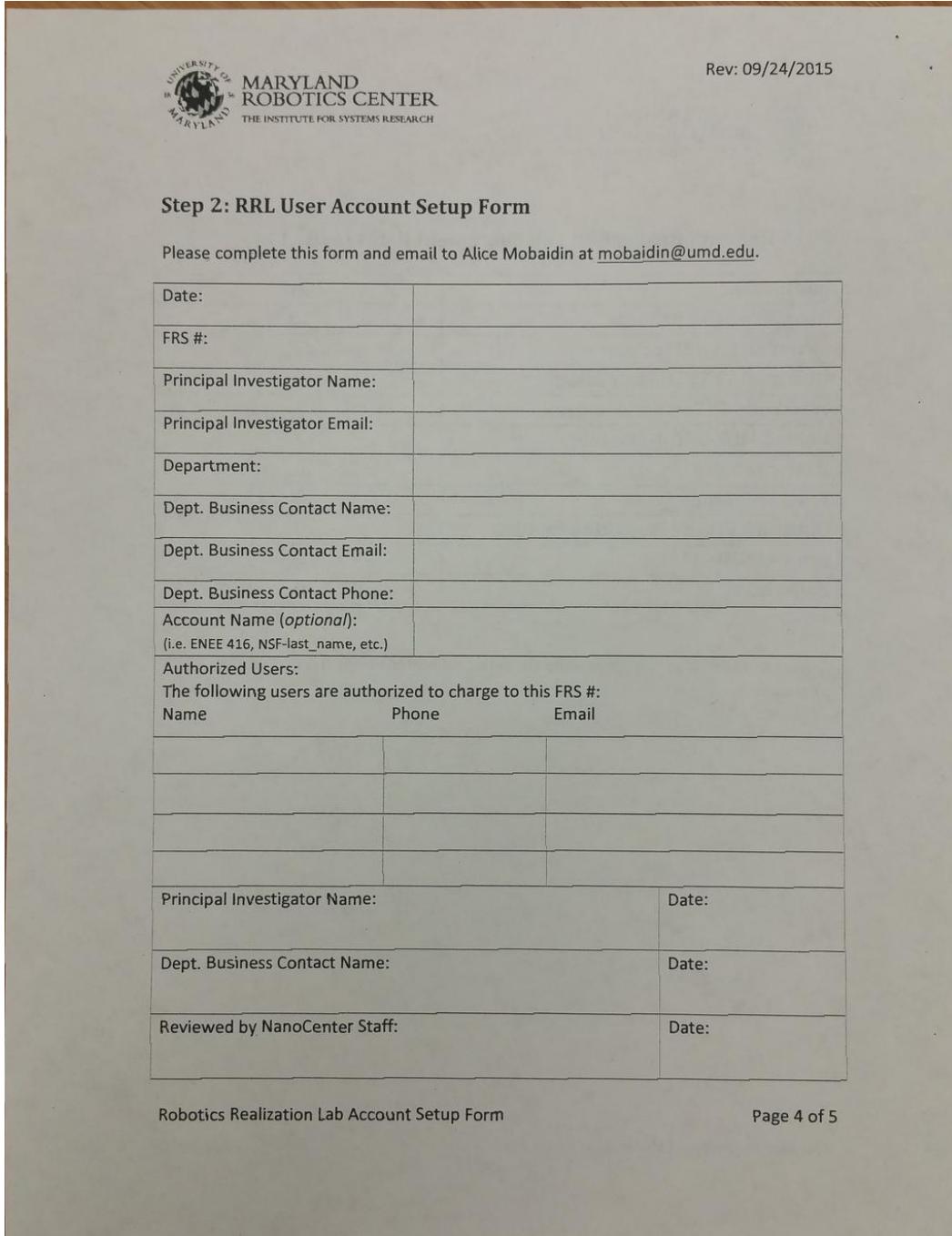


FIGURE 2.10: Flow Chart for Computing Perspective Transform

The result of **warping** the image using the computed perspective transform and doing **bilinear interpolation** is shown below



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Dept. Business Contact Phone:		
Account Name (<i>optional</i>): (i.e. ENEE 416, NSF-last_name, etc.)		
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FIGURE 2.11: Warped Reference image.

2.2.7 Adaptive Thresholding

The warped RGB image can be converted to binary Black/White format, suitable for printing/registration purposes, by doing **Adaptive Thresholding** (Fisher et al., 1997) . This is a data dependent thresholding technique. It's fundamental principle is that the region of interest can be segmented out by using the blurred version of an image minus a constant as the threshold. Different types of filters like Mean filters, Gaussian filter , Median filter can be used to blur the image. Here the Gaussian Minus C algorithm is used. C was experimentally determined to be 5. This would be really useful for **text segmentation** (Fletcher and Kasturi, 1988)

The adaptively thresholded reference image is shown below.

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Account Name (<i>optional</i>): <small>(i.e. ENEE 416, NSF-last_name, etc.)</small>																	
Authorized Users: The following users are authorized to charge to this FRS #: <table border="1"> <thead> <tr> <th>Name</th> <th>Phone</th> <th>Email</th> </tr> </thead> <tbody> <tr><td></td><td></td><td></td></tr> <tr><td></td><td></td><td></td></tr> <tr><td></td><td></td><td></td></tr> <tr><td></td><td></td><td></td></tr> </tbody> </table>			Name	Phone	Email												
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FIGURE 2.12: Adaptive Thresholding.

3 Image Registration

3.1 Flow Chart

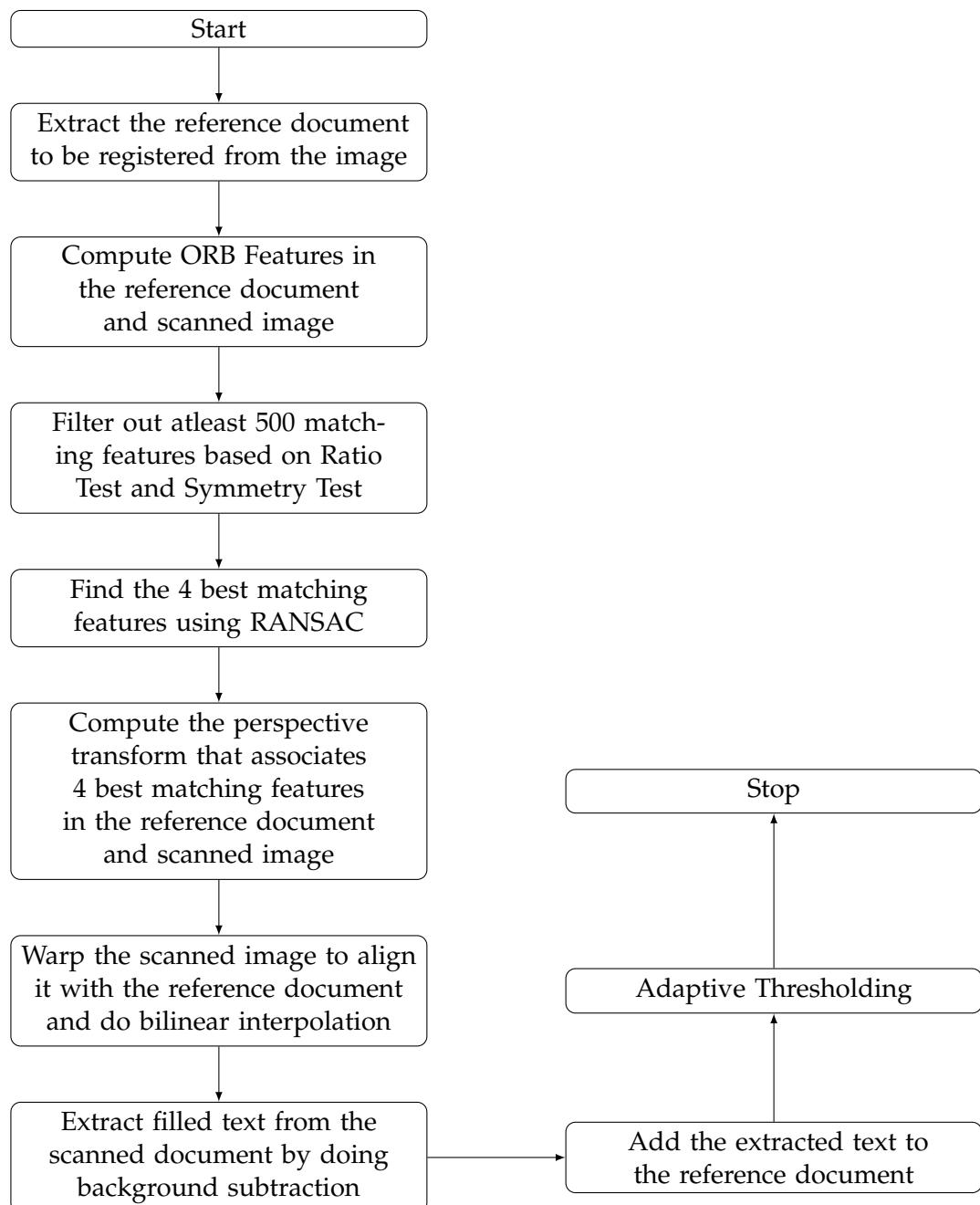


FIGURE 3.1: Flow Chart for Image Registration

3.2 Image Registration Techniques

Consider the image shown below from which the text is to be extracted and overlaid on top of the reference document.

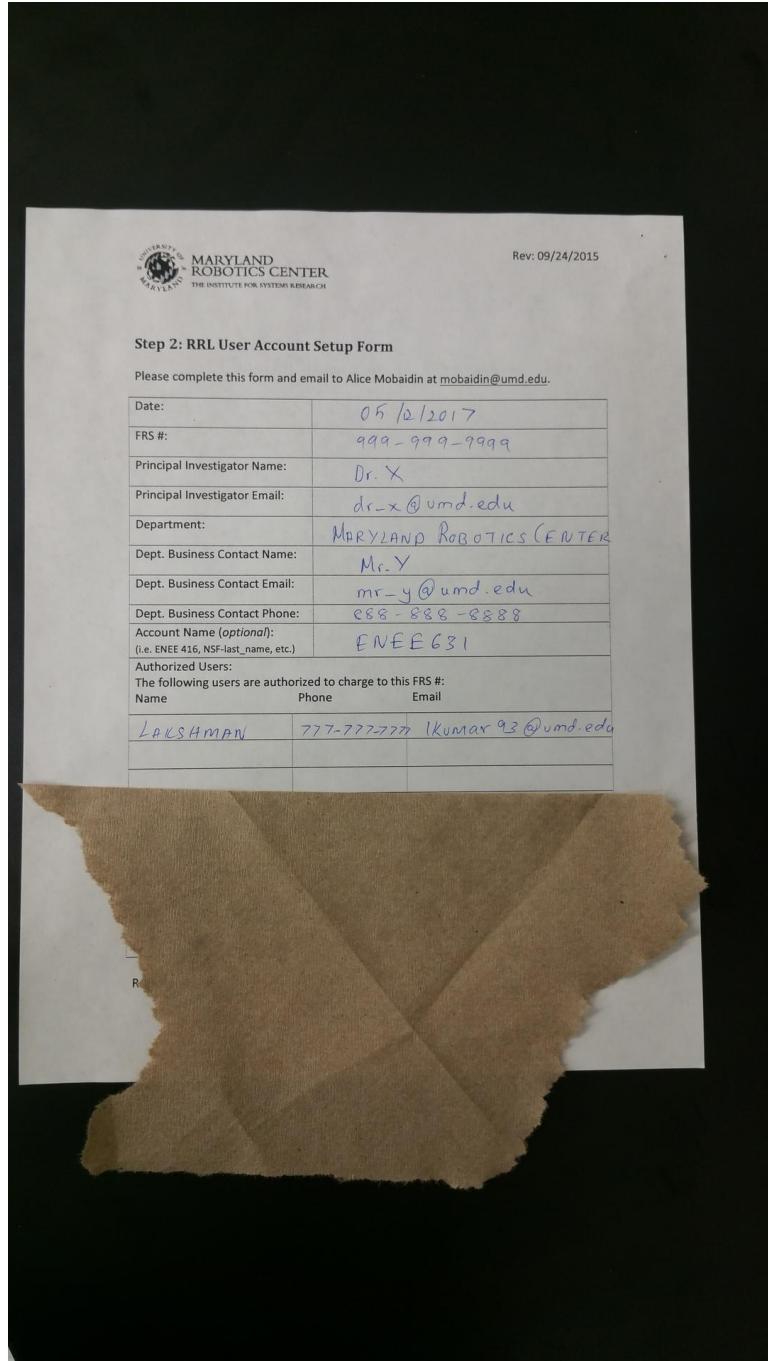


FIGURE 3.2: Scanned Image

All the techniques involved in extracting filled text from the scanned image and overlaying it on top of the reference document are briefly explained below.

3.2.1 Image Alignment

ORB feature detector (Ethan et al., 2011) is an effective replacement to **SIFT** (Lowe, 2004) and **SURF** (Bay et al., 2008) in terms of computation cost. It is basically a rotational invariant version of **FAST** keypoint detector (Rosten and Drummond, 2005) and **BRIEF** keypoint descriptor (Calonder et al., 2010). ORB features are computed in both the reference document and the scanned image using **OpenCV's feature detection API**. These features are then matched between the reference document and scanned image using **Brute Force Hamming** technique with **KNN** (Altman, 1992), the rest of features are weeded out. These features are further filtered on whether they satisfy the ratio test and the symmetry test. As per the ratio test, matching features, for which the ratio of the nearest neighbor distance to the second nearest neighbor distance is greater than 0.8, are rejected to extract good matches. As per the symmetry test, good matches that correspond from reference image to scanned image and vice versa should be the same or else they are eliminated. Hence better matches can be extracted. It is also made sure that there are at least 500 matches that satisfy both tests between the two images. Hence the number of ORB features are iteratively increased until this constraint is satisfied.

The better matches computed in both the reference document and scanned document are shown below.

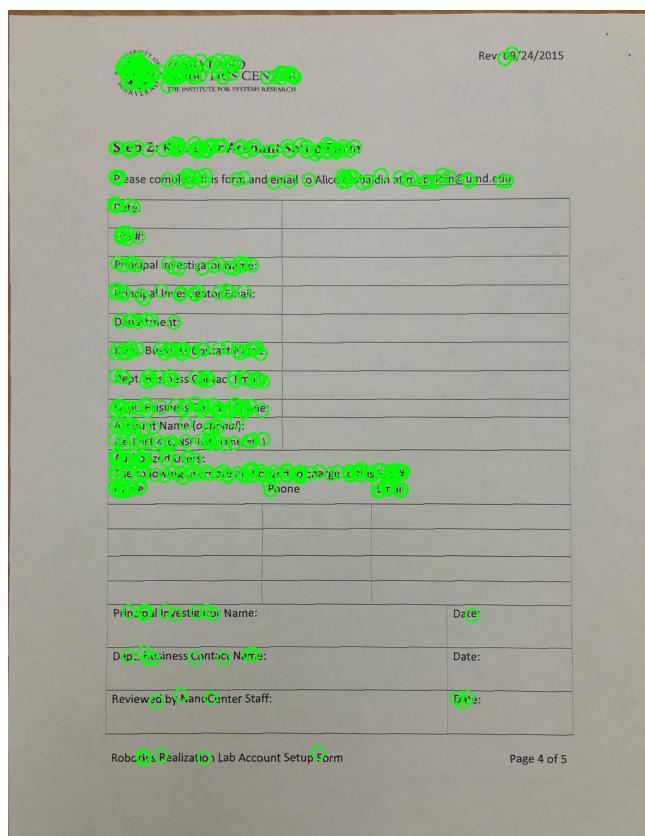


FIGURE 3.3: Matching Orb Features in Reference Document.

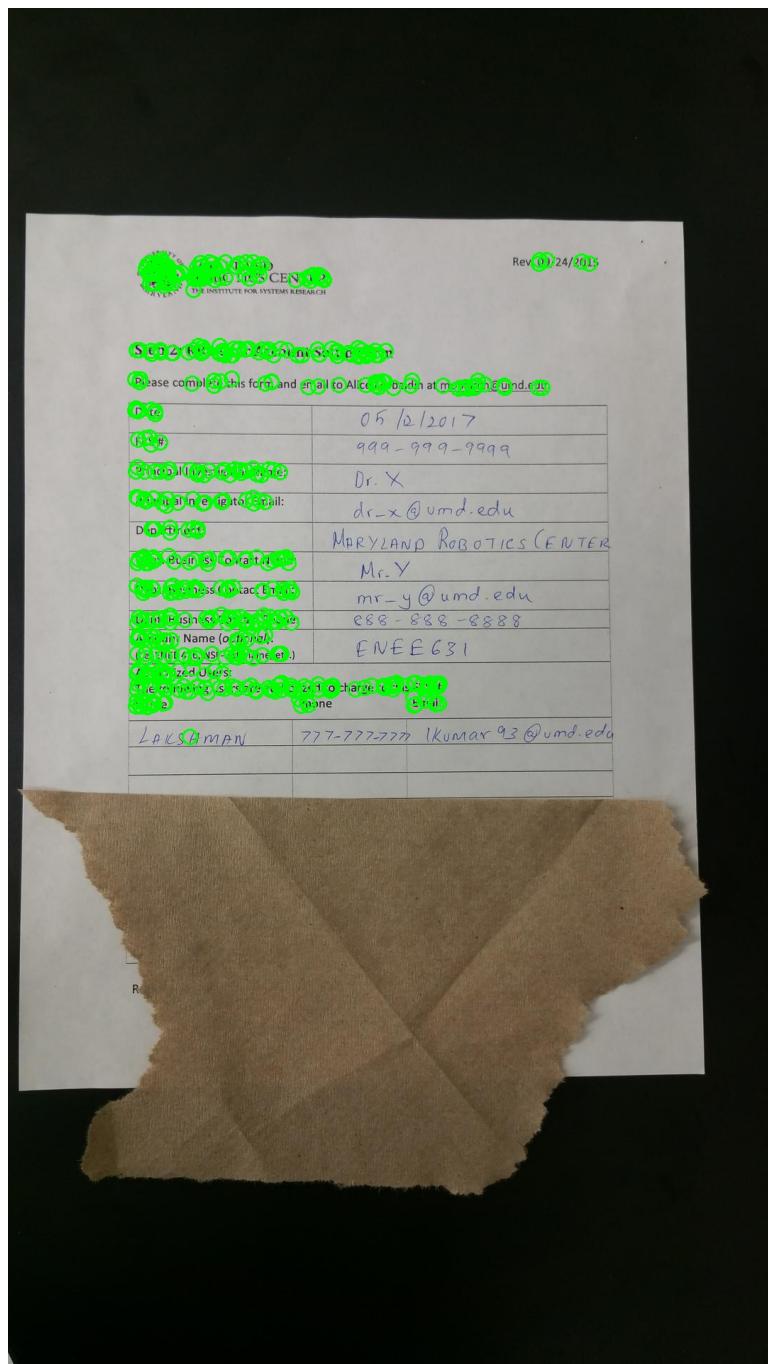


FIGURE 3.4: Matching Orb Features in Scanned image.

In order to obtain the perspective transform linking the two images, 4 matches are required. The best 4 matches can be computed using **RANSAC** (Fischler and Bolles, 1981). RANSAC is an iterative method to remove outliers. RANSAC initially randomly chooses 4 non-identical matches from the set of better matches and computes the perspective transform between these 4 matches of both the images. The matching features in the scanned image are then warped by the computed perspective transform and checked to see if the euclidean distance between the warped feature and the matching feature in the reference document is less than a certain threshold, which was experimentally determined to be 0.175. If so, that particular feature is considered to be matching. This process is repeated for all the better matches and for a certain number of iterations, in this case, 50000. The perspective transform that has the most number of matching points is considered to be the best and this is used to warp the scanned image to align with the reference document.

The best four matches are shown below

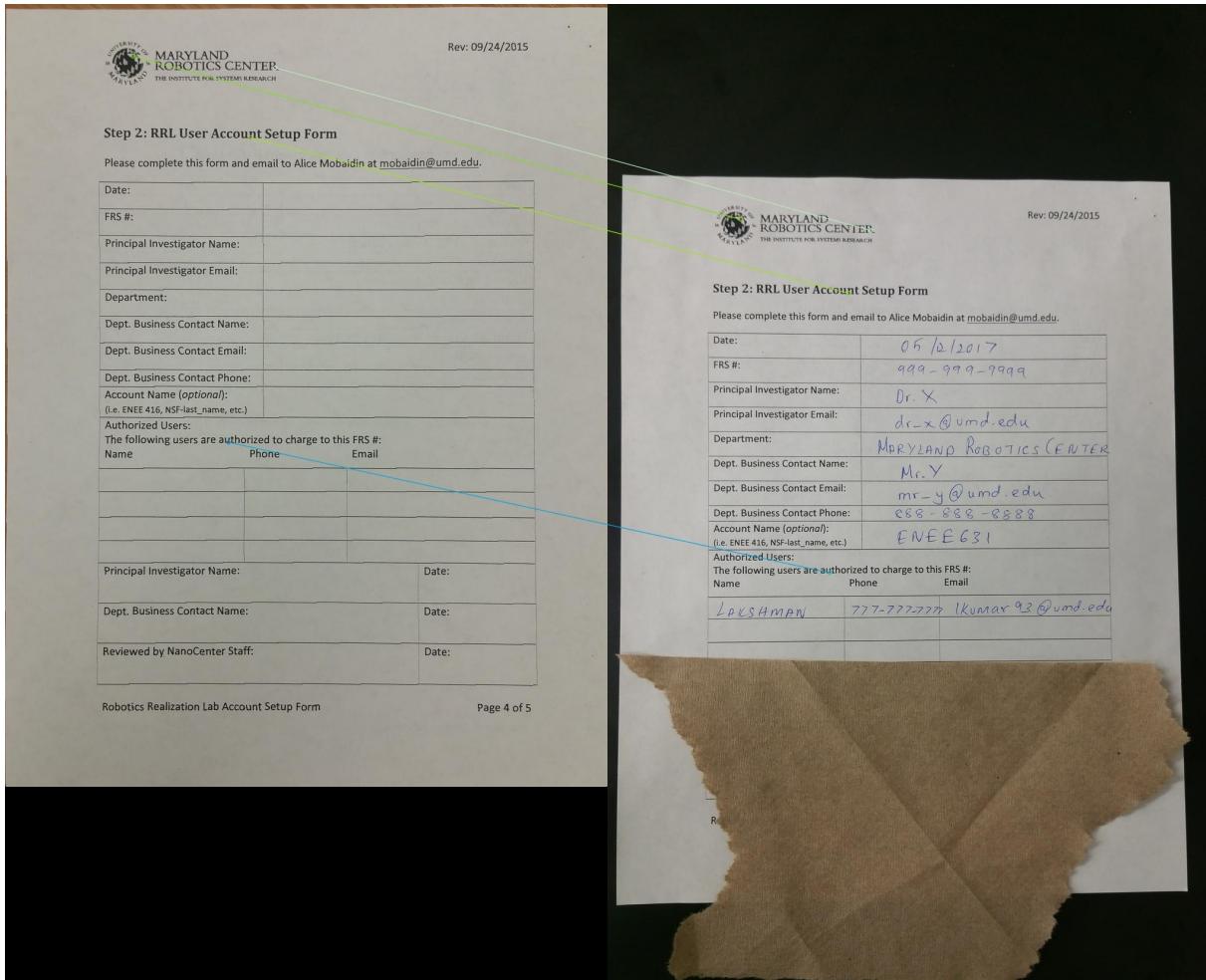


FIGURE 3.5: Best Matches.

The aligned version of scanned document is shown below

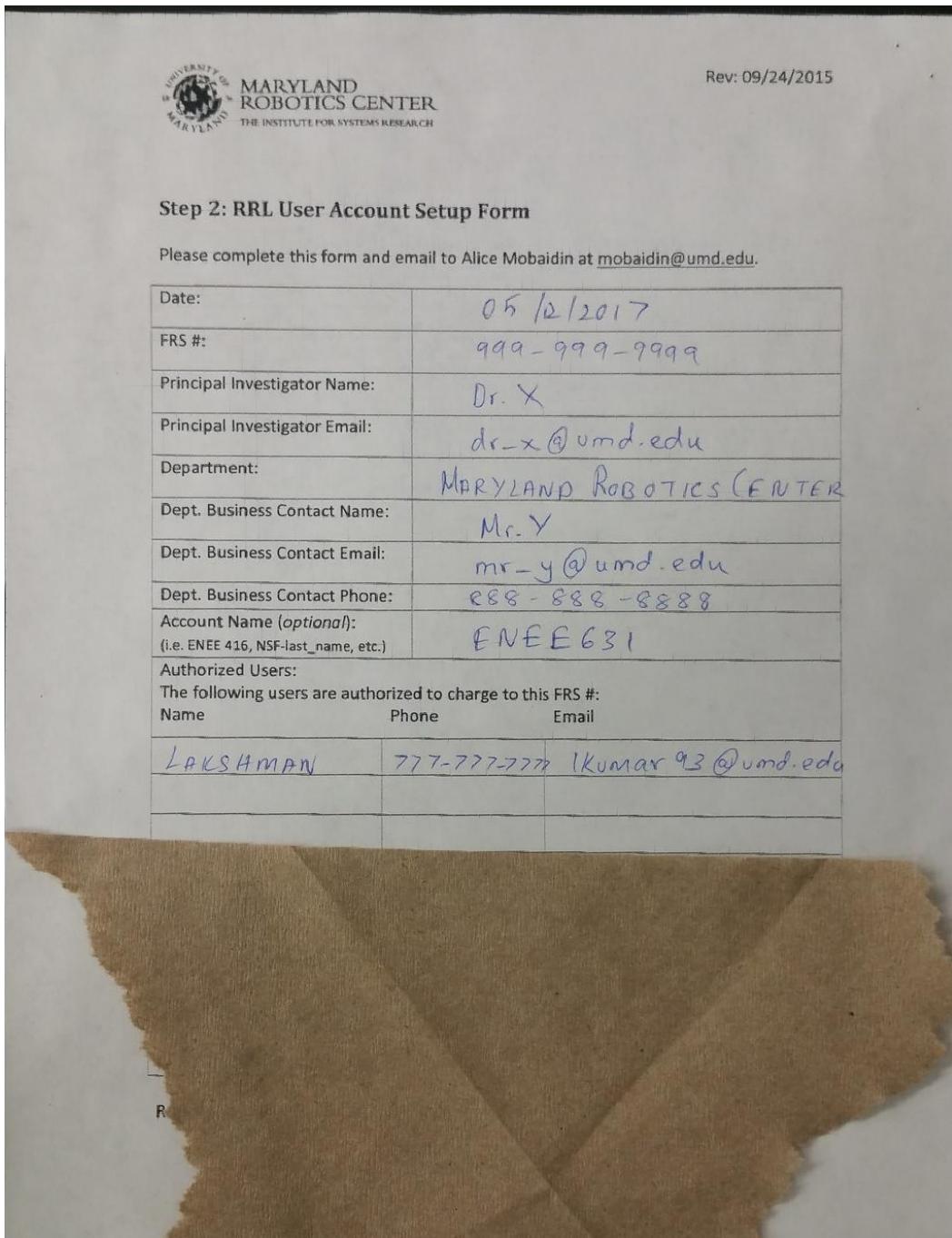


FIGURE 3.6: Warped Scanned Document.

3.2.2 Background Subtraction

Background Subtraction is done in order to extract the filled text from scanned document. In order to do that , both the reference document and the scanned document are converted to grayscale and then sharpened to boost its edges. The sharpened images are then further adaptively thresholded to convert them to a binary image.

The adaptively thresholded images are shown below.

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Principal Investigator Email:		
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Dept. Business Contact Name:		
Dept. Business Contact Email:		
Dept. Business Contact Phone:		
Account Name (optional): (i.e. NLE 416, RSL-123, etc.)		
Authorized Users: The following users are authorized to charge to this FRS #:		
Name	Phone	Email
Principal Investigator Name:	Date:	
Dept. Business Contact Name:	Date:	
Reviewed by NanoCenter Staff:	Date:	

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FIGURE 3.7: Thresholded Reference Document.

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Date:	05/12/2017	
FRS #:	999-999-9999	
Principal Investigator Name:	Dr. X	
Principal Investigator Email:	dr-x@umd.edu	
Department:	MARYLAND ROBOTICS (FNRTR)	
Dept. Business Contact Name:	Mr. Y	
Dept. Business Contact Email:	mr-y@umd.edu	
Dept. Business Contact Phone:	888-888-8888	
Account Name (optional): (i.e. ENEE 416, NSF-last_name, etc.)	ENE E631	
Authorized Users: The following users are authorized to charge to this FRS #:		
Name	Phone	Email
LAKSHMAN	777-777-7777	Ikumar_03@umd.edu

FIGURE 3.8: Thresholded Scanned Document.

Based on the values in both the thresholded images, the additional content in the scanned document is extracted from the reference document . The extracted foreground is then filtered a bit by dilation and median filtering. It can be seen from the image below that almost the entire filled content has been extracted. However, there might be some additional residue due to minute differences in alignment either because of Bilinear Interpolation or lesser number of iterations in RANSAC.

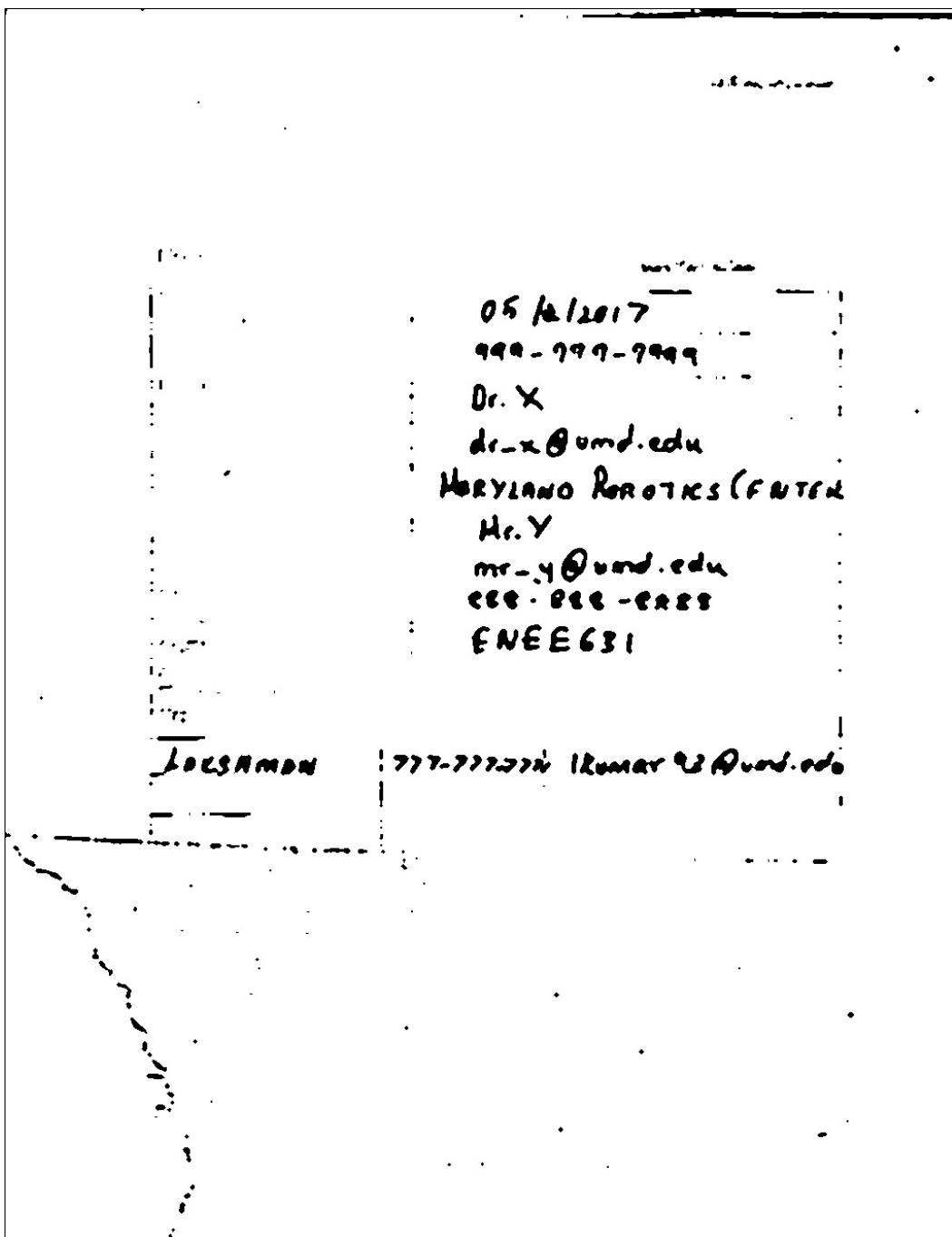


FIGURE 3.9: Background Subtraction.

3.2.3 Foreground Addition

Based on the extracted foreground, pixels in the scanned image are overlaid on top of the reference document. From the resultant images, it can be observed that most of the content is properly overlaid, however, there are some noises and artifacts due to border effects, minute differences in alignment, adaptive thresholding parameters and edges of obstructions in the image of scanned document.

The binary version of the restored image is shown below.

The image shows a binary restored version of a user account setup form. At the top, it features the University of Maryland Robotics Center logo and the text "MARYLAND ROBOTICS CENTER THE INSTITUTE FOR SYSTEMS RESEARCH". To the right, it says "Rev: 09/24/2015". Below this, the title "Step 2: RRL User Account Setup Form" is printed. A note below the title reads "Please complete this form and email to Alice Mobaideen at mobaideen@umd.edu". The form contains several input fields:

Date:	05/02/2017	
FRS #:	999-999-9999	
Principal Investigator Name:	Dr. X	
Principal Investigator Email:	dr-x@umd.edu	
Department:	MARYLAND ROBOTICS CENTER	
Dept. Business Contact Name:	Mr. Y	
Dept. Business Contact Email:	mr-y@umd.edu	
Dept. Business Contact Phone:	888-888-8888	
Account Name (optional): (i.e. EEE 416, NSF-last_name, etc.)	ENEE 631	
Authorized Users: The following users are authorized to charge to this FRS #:		
Name:	Phone:	Email:
LAKSHMAN	777-777-7777	lkumar93@umd.edu
Principal Investigator Name:	Date:	
Dept. Business Contact Name:	Date:	
Reviewed by NanoCenter Staff:	Date:	

At the bottom, it says "Robotics Realization Lab Account Setup Form" and "Page 4 of 5".

FIGURE 3.10: Binary Restored Image.

The RGB version of the restored image is shown below.

The image shows a scanned document titled "Step 2: RRL User Account Setup Form". At the top right is the text "Rev: 09/24/2015". The header includes the University of Maryland logo and the text "MARYLAND ROBOTICS CENTER THE INSTITUTE FOR SYSTEMS RESEARCH". Below the header, the form is titled "Step 2: RRL User Account Setup Form". A note says "Please complete this form and email to Alice Mobaidin at mobaidin@umd.edu". The form contains handwritten responses to various fields:

Date:	05/02/2017	
FRS #:	999-999-9999	
Principal Investigator Name:	Dr. X	
Principal Investigator Email:	dr-x@umd.edu	
Department:	MARYLAND ROBOTICS CENTER	
Dept. Business Contact Name:	Mr. Y	
Dept. Business Contact Email:	mr-y@umd.edu	
Dept. Business Contact Phone:	888-888-8888	
Account Name (optional): (i.e. ENEE 416, NSF-last_name, etc.)	ENEE 631	
Authorized Users: The following users are authorized to charge to this FRS #:		
Name	Phone	Email
LAKSHMAN	777-777-7777	Ikumar_93@umd.edu
Principal Investigator Name:	Date:	
Dept. Business Contact Name:	Date:	
Reviewed by NanoCenter Staff:	Date:	

At the bottom left is the text "Robotics Realization Lab Account Setup Form" and at the bottom right is "Page 4 of 5".

FIGURE 3.11: Restored Image.

4 Conclusion

4.1 Observations

In this project, a sequential method to extract a document from an image and register it in order to do content extraction of the filled version of the same document has been laid out and implemented. Based on the experiments conducted as a part of this project, a few keen observations can be made as follows.

- The technique works well as long as the **Assumptions Made** are satisfied.
- **Document Extraction** takes roughly 5 to 7 seconds and **Image Registration** with Content Extraction takes roughly 15 to 25 seconds depending on the size and nature of the image. Hence totally the program takes about 30 seconds to execute.
- Sometimes specific tuning for parameters like Adaptive Thresholding Constant, Kernel Sizes, to suit a particular image is required.
- As **Assumptions Made** made do not require any sort of markings or specific ink color for the filled content, the output is not perfect .
- Background subtraction works well in-spite of having obstructions in the scanned image.

4.2 Future Works

- Optimize the code and algorithm to take less then 2 seconds to give the final output.
- Reduce the number of **Assumptions Made** .
- Do additional filtering to remove artifacts due to border effects, obstructions and minute differences in image alignment.
- Automated tuning of certain parameters based on the nature of the image.
- Integrate OCR.

A Experimental Results

A.1 Document Extraction

Given below are few scanned images and their corresponding document extractions.



FIGURE A.1: Scanned Image 2 (Source : images.google.com).

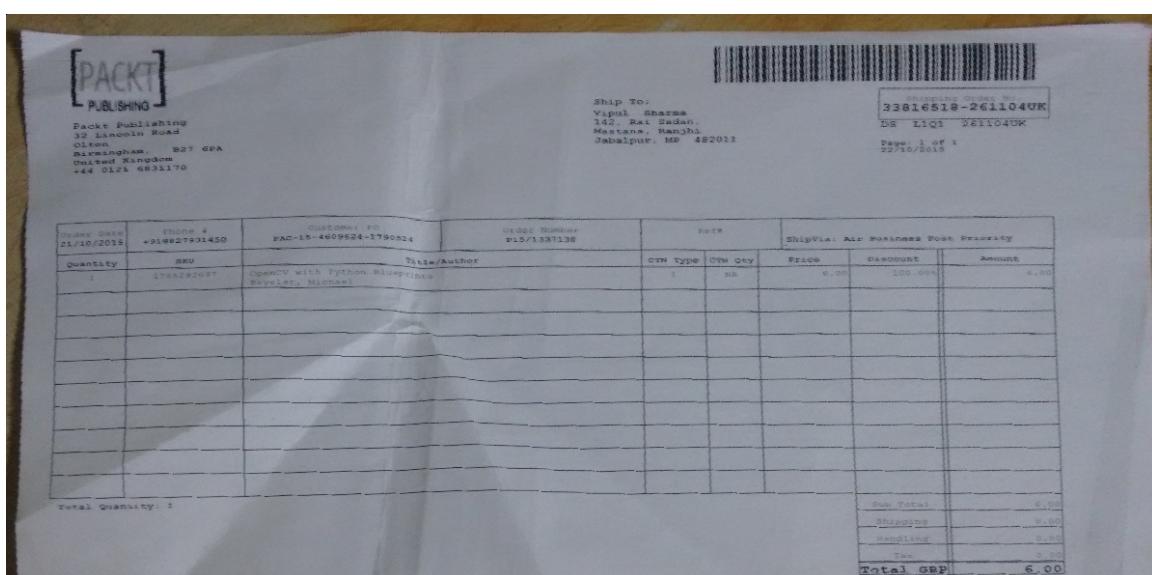


FIGURE A.2: Warped Image 2.



FIGURE A.3: Scanned Image 3 (Source : images.google.com).



FIGURE A.4: Warped Image 3.

A.2 Image Registration

Given below are few reference documents and scanned images and their corresponding image registrations/content extractions.

Laboratory Personnel Safety Check List

Employee/Student Name _____ Date _____
Print

Department/ISR _____ Bldg. 093 _____ Rm. # 0307 _____

Principal Investigator Bergbreiter _____ or Lab Supervisor _____
Print

The following procedures have been reviewed with this employee/student.

1. _____ Has the PI/Lab Supervisor discussed the nature of the research being conducted in the laboratory?

2. _____ Has the PI/Lab Supervisor discussed all hazardous components of the research?
a. _____ chemical
b. _____ biological
c. _____ physical

3. _____ N/A Has the employee/student received instruction on known symptoms associated with exposure to highly toxic chemicals or infectious agents used in the laboratory?

4. _____ N/A Has the PI/Lab Supervisor discussed the need for the employee/student to inform health care providers of the hazardous substances used in the laboratory during each medical visit?

5. _____ Has the PI/Lab Supervisor reviewed the laboratory Chemical Hygiene Plan and all Standard Operating Procedures with the employee/student?

6. _____ Has the PI/Lab Supervisor identified the location of Material Safety Data Sheets to the employee/student and demonstrated methods of access? (e.g., DES web site, hardcopy, etc.).

7. _____ Has hazard assessment information concerning Personal Protective Equipment required in laboratory been reviewed, and has the supervisor and employee signed off?

8. _____ N/A Does the employee/student need a respirator? If yes, arrange for exposure evaluation, training and fit testing through the Department of Environmental Safety at x53980.

9. _____ Has the location of the Emergency Response Guide Wall Chart been identified to the employee/student and pertinent procedures reviewed for?
a. _____ spills
b. _____ fire
c. _____ personal injury

FIGURE A.5: Reference Image 2.

Laboratory Personnel Safety Check List

Employee/Student Name: LAKSHMAN KUMAR Date: 5/7/2017
Print

Department: ISR ROBOTICS Bldg: 093 Rm. #: 0307
Print

Principal Investigator: Bergbreiter Print or Lab Supervisor Print

The following procedures have been reviewed with this employee/student.

1. YES Has the PI/Lab Supervisor discussed the nature of the research being conducted in the laboratory?

2. YES Has the PI/Lab Supervisor discussed all hazardous components of the research?

a. chemical
b. N/A
c. physical

3. N/A Has the employee/student received instruction on known symptoms associated with exposure to highly toxic chemicals or infectious agents used in the laboratory?

4. N/A Has the PI/Lab Supervisor discussed the need for the employee/student to inform health care providers of the hazardous substances used in the laboratory during each medical visit?

5. YES Has the PI/Lab Supervisor reviewed the laboratory Chemical Hygiene Plan and all Standard Operating Procedures with the employee/student?

6. YES Has the PI/Lab Supervisor identified the location of Material Safety Data Sheets to the employee/student and demonstrated methods of access? (e.g., DES web site, hardcopy, etc.)

7. No Has hazard assessment information concerning Personal Protective Equipment required in laboratory been reviewed, and has the supervisor and employee signed off?

8. N/A Does the employee/student need a respirator? If yes, arrange for exposure evaluation, training and fit testing through the Department of Environmental Safety at x53980.

9. YES Has the location of the Emergency Response Guide Wall Chart been identified to the employee/student and pertinent procedures reviewed for:

a. spills
b. fire
c. personal injury

FIGURE A.6: Filled Document.

Laboratory Personnel Safety Check List

Employee/Student Name LAKSHMAN KUMAR Date 5/7/2017
Print

Department ISR R&ROTICS Bldg. 093 _____ Rm. # 0307 _____

Principal Investigator Bergbreiter _____ or Lab Supervisor _____
Print

The following procedures have been reviewed with this employee/student.

1. Yes Has the PI/Lab Supervisor discussed the nature of the research being conducted in the laboratory?

2. Yes Has the PI/Lab Supervisor discussed all hazardous components of the research?
a. chemical
b. N/A
c. physical

3. N/A Has the employee/student received instruction on known symptoms associated with exposure to highly toxic chemicals or infectious agents used in the laboratory?

4. N/A Has the PI/Lab Supervisor discussed the need for the employee/student to inform health care providers of the hazardous substances used in the laboratory during each medical visit?

5. Yes Has the PI/Lab Supervisor reviewed the laboratory Chemical Hygiene Plan and all Standard Operating Procedures with the employee/student?

6. Yes Has the PI/Lab Supervisor identified the location of Material Safety Data Sheets to the employee/student and demonstrated methods of access? (e.g., DES web site, hardcopy, etc.).

7. No Has hazard assessment information concerning Personal Protective Equipment required in laboratory been reviewed, and has the supervisor and employee signed off?

8. N/A Does the employee/student need a respirator? If yes, arrange for exposure evaluation, training and fit testing through the Department of Environmental Safety at x53980.

9. Yes Has the location of the Emergency Response Guide Wall Chart been identified to the employee/student and pertinent procedures reviewed for?
a. spills
b. fire
c. personal injury

FIGURE A.7: Restored Image 2.

Laboratory Personnel Safety Check List

Employee/Student Name LAKSHMAN KUMAR Print _____ Date 5/7/2017
Department ISR ROBOTICS Bldg. 093 _____ Rm. # 0307 _____
Principal Investigator Bergbreiter Print _____ or Lab Supervisor _____ Print _____

The following procedures have been followed with this employee/student.

1. YES Has the PI/LI informed the employee/student about the nature of the research conducted in the laboratory?

2. YES Has the PI/LI informed the employee/student about the safety aspects of the research?

a. b. c.

3. N/A Has the employee/student been informed of all emergency procedures associated with the work being done in the laboratory?

4. N/A Has the PI/LI informed the employee/student about the location of the nearest fire alarm?

5. YES Has the PI/LI informed the employee/student about the location of the nearest exit?

6. YES Has the PI/LI informed the employee/student about the location of the nearest eyewash?

7. No Has the PI/LI informed the employee/student about the location of the nearest emergency equipment?

8. N/A Does the employee/student know how to respond to an emergency exposure event?

Environmental Safety:

9. YES Has the location of the Emergency Equipment been identified to the employee/student?

a. spills
b. fire
c. personal injury

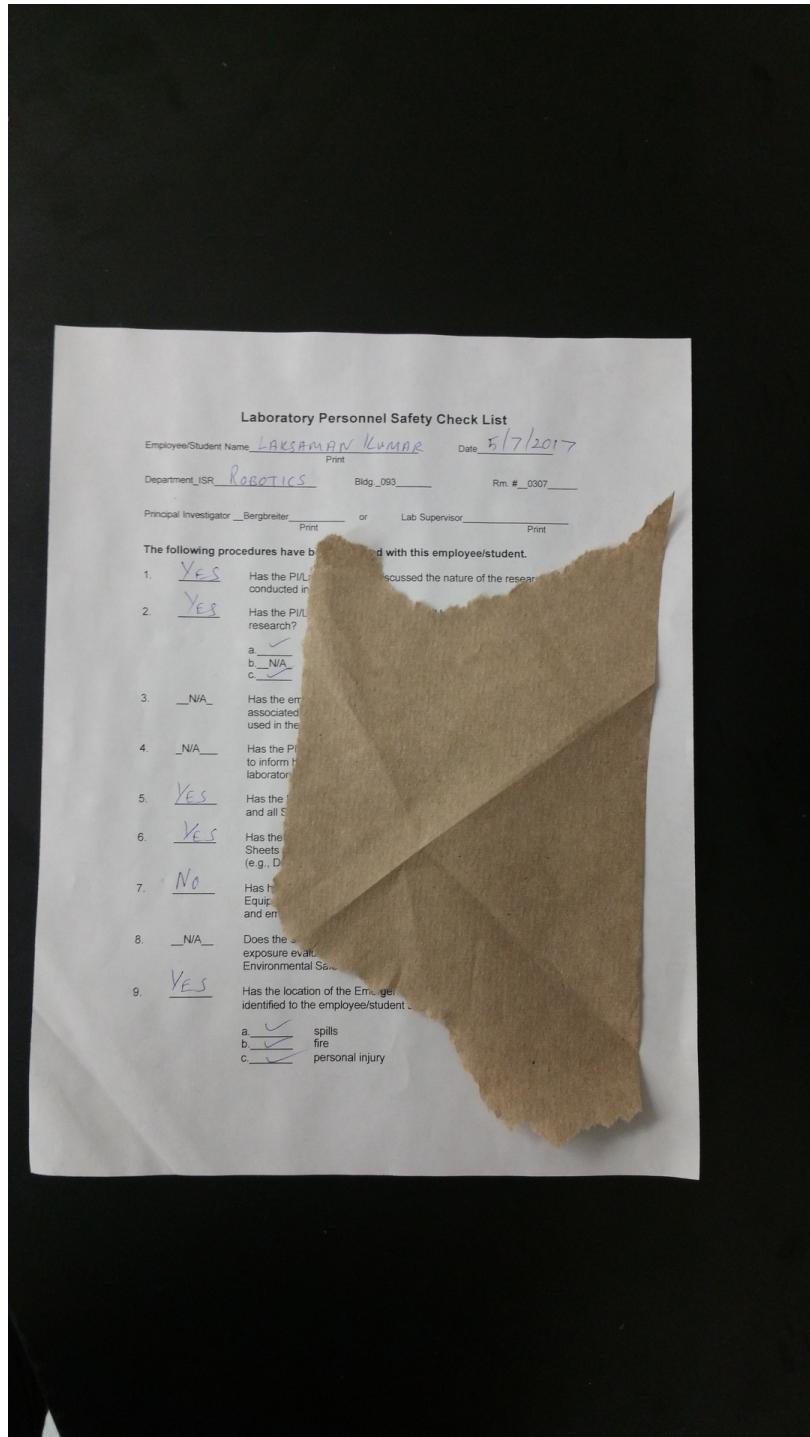


FIGURE A.8: Filled Document 2.

Laboratory Personnel Safety Check List

Employee/Student Name AKSHAY KUMAR Date 5/7/2017
Print

Department ISR R&D Bldg. 093 Rm. # 0307

Principal Investigator Bergbreiter or Lab Supervisor _____ Print _____

The following procedures have been reviewed with this employee/student.

1. Yes Has the PI/Lab Supervisor discussed the nature of the research being conducted in the laboratory?
2. Yes Has the PI/Lab Supervisor discussed all hazardous components of the research?
a. ✓ chemical
b. N/A biological
c. ✓ physical
3. N/A Has the employee/student received instruction on known symptoms associated with exposure to highly toxic chemicals or infectious agents used in the laboratory?
4. N/A Has the PI/Lab Supervisor discussed the need for the employee/student to inform health care providers of the hazardous substances used in the laboratory during each medical visit?
5. Yes Has the PI/Lab Supervisor reviewed the laboratory Chemical Hygiene Plan and all Standard Operating Procedures with the employee/student?
6. Yes Has the PI/Lab Supervisor identified the location of Material Safety Data Sheets to the employee/student and demonstrated methods of access? (e.g., DES web site, hardcopy, etc.)
7. No Has hazard assessment information concerning Personal Protective Equipment required in laboratory been reviewed, and has the supervisor and employee signed off?
8. N/A Does the employee/student need a respirator? If yes, arrange for exposure evaluation, training and fit testing through the Department of Environmental Safety at x53980.
9. Yes Has the location of the Emergency Response Guide Wall Chart been identified to the employee/student and pertinent procedures reviewed for:
a. ✓ spills
b. ✓ fire
c. ✓ personal injury

FIGURE A.9: Restored Image 3.

B Source Code

The source code for the entire project can be found at

https://github.com/lkumar93/Image-Processing/blob/master/mobile_scanner

B.1 Image Transformation

B.1.1 Header

```
// image_transformation.h

#ifndef IMAGE_TRANSFORMATION_H_
#define IMAGE_TRANSFORMATION_H_

#include <iostream>
#include <opencv2/opencv.hpp>

using namespace cv;
using namespace std;

void bilinearInterpolation(Mat image, int vacant_pixel_value=0);
Mat perspective_transform(Point2f corner_points[], Point2f
    reference_points[]);
void warp_image(const Mat& input_image, Mat& output_image, const Mat&
    perspective_transform);
Mat resize_image(const Mat& input_image, int width, int height);

#endif // IMAGE_TRANSFORMATION_H
```

B.1.2 Source

```
// image_transformation.cpp

#include "image_transformation.h"

void bilinearInterpolation(Mat image, int vacant_pixel_value)
{
    if(image.type() == CV_8UC3)
    {
        Vec3b vacant_pixel;
        vacant_pixel[0] = vacant_pixel_value;
        vacant_pixel[1] = vacant_pixel_value;
        vacant_pixel[2] = vacant_pixel_value;

        for(int j = 0; j < image.rows ; j++)
        {
            for(int i = 0; i < image.cols; i++)

```

```
{  
if(image.at<Vec3b>(j, i) == vacant_pixel)  
{  
int count_r = i;  
//get right most filled_neighbour  
while( image.at<Vec3b>(j, count_r) == vacant_pixel && count_r < image.cols)  
{  
count_r++;  
}  
int count_l = i;  
//get left most filled_neighbour  
while( image.at<Vec3b>(j, count_l) == vacant_pixel && count_l >= 0 )  
{  
count_l--;  
}  
  
int count_b = j;  
//get bottom most filled_neighbour  
while( image.at<Vec3b>(count_b, i) == vacant_pixel && count_b < image.rows  
)  
{  
count_b++;  
}  
  
int count_t = j;  
//get top most filled_neighbour  
while( image.at<Vec3b>(count_t, i) == vacant_pixel && count_t >= 0 )  
{  
count_t--;  
}  
  
if(count_r >= image.cols)  
count_r = image.cols-1;  
  
if(count_l < 0)  
count_l = 0;  
  
if(count_b >= image.rows)  
count_b = image.rows-1;  
  
if(count_t < 0)  
count_t = 0;  
  
float left_offset = i-count_l;  
float right_offset = count_r-i;  
  
float top_offset = j-count_t;  
float bottom_offset = count_b-j;  
  
float col_offset = left_offset+right_offset;  
float row_offset = top_offset+bottom_offset;  
  
if(col_offset > 0)  
{  
left_offset = (1-left_offset/col_offset)/2.0;  
right_offset = (1-right_offset/col_offset)/2.0;
```

```
}

if(row_offset >0)
{
top_offset = (1-top_offset/row_offset)/2.0;
bottom_offset = (1-bottom_offset/row_offset)/2.0;
}

Vec3b top_pixel = image.at<Vec3b>(count_t, i);
Vec3b bottom_pixel = image.at<Vec3b>(count_b, i);

Vec3b right_pixel = image.at<Vec3b>(j, count_r);
Vec3b left_pixel = image.at<Vec3b>(j, count_l);

Vec3b interpolated_value;

if(left_pixel == vacant_pixel)
left_offset = 0;

if(right_pixel == vacant_pixel)
right_offset = 0;

if(top_pixel == vacant_pixel)
top_offset = 0;

if(bottom_pixel == vacant_pixel)
bottom_offset = 0;

col_offset = left_offset+right_offset;
row_offset = top_offset+bottom_offset;

if(col_offset > 0)
{
left_offset = left_offset/(2*col_offset);
right_offset = right_offset/(2*col_offset);
}

if(row_offset >0)
{
top_offset = top_offset/(2*row_offset);
bottom_offset = bottom_offset/(2*row_offset);
}

float total = left_offset + right_offset + top_offset +bottom_offset;

if(total > 0)
{
left_offset/=total;
right_offset/=total;
top_offset/=total;
bottom_offset/=total;
}

interpolated_value[0] = left_offset*left_pixel[0] +
right_offset*right_pixel[0] + top_offset*top_pixel[0]
```

```
+ bottom_offset*bottom_pixel[0];

interpolated_value[1] = left_offset*left_pixel[1] +
    right_offset*right_pixel[1] + top_offset*top_pixel[1]
+ bottom_offset*bottom_pixel[1];

interpolated_value[2] = left_offset*left_pixel[2] +
    right_offset*right_pixel[2] + top_offset*top_pixel[2]
+ bottom_offset*bottom_pixel[2];

image.at<Vec3b>(j, i) = interpolated_value;
}
}
}
}
else if(image.type() == CV_8UC1)
{

// Bilinear Interpolation
for(int j = 0; j < image.rows ; j++)
{
    for(int i = 0; i < image.cols; i++)
    {
        if(image.at<uchar>(j, i) == vacant_pixel_value)
        {
            int count_r = i;
            //get right most filled_neighbour
            while( image.at<uchar>(j, count_r) == vacant_pixel_value && count_r<
                image.cols)
            {
                count_r++;
            }
            int count_l = i;
            //get left most filled_neighbour
            while( image.at<uchar>(j, count_l) == vacant_pixel_value && count_l >= 0 )
            {
                count_l--;
            }

            int count_b = j;
            //get bottom most filled_neighbour
            while( image.at<uchar>(count_b, i) == vacant_pixel_value && count_b <
                image.rows )
            {
                count_b++;
            }

            int count_t = j;
            //get top most filled_neighbour
            while( image.at<uchar>(count_t, i) == vacant_pixel_value && count_t >= 0 )
            {
                count_t--;
            }

            if(count_r >=image.cols)
                count_r = image.cols-1;
            else if(count_l <= 0)
                count_l = 0;
            else if(count_b <= 0)
                count_b = 0;
            else if(count_t >= image.rows)
                count_t = image.rows-1;
            else
                count_t = count_t+1;
            float weight_r = (float)(count_r - i) / (float)(count_r - count_l);
            float weight_b = (float)(count_b - j) / (float)(count_b - count_t);
            float weight_t = (float)(j - count_t) / (float)(count_r - count_t);
            float weight_l = (float)(i - count_l) / (float)(count_r - count_l);
            float weight = (float)(j - count_b) / (float)(count_b - count_t);
            float value = (1 - weight) * (1 - weight_r) * left_pixel[0] +
                (1 - weight) * (1 - weight_b) * top_pixel[0] +
                (1 - weight) * (1 - weight_t) * bottom_pixel[0] +
                (1 - weight) * weight_r * right_pixel[0] +
                (1 - weight) * weight_b * bottom_pixel[0] +
                (1 - weight) * weight_t * bottom_pixel[0] +
                weight * (weight_r * (1 - weight_b) * (1 - weight_t) * left_pixel[0] +
                    weight_r * (1 - weight_b) * weight_t * top_pixel[0] +
                    weight_r * weight_b * (1 - weight_t) * bottom_pixel[0] +
                    weight_r * weight_b * weight_t * right_pixel[0] +
                    weight * (1 - weight_b) * weight_t * bottom_pixel[0] +
                    weight * weight_b * weight_t * bottom_pixel[0]);
            image.at<uchar>(j, i) = value;
        }
    }
}
```

```
if(count_l < 0)
count_l = 0;

if(count_b >=image.rows)
count_b = image.rows-1;

if(count_t < 0)
count_t = 0;

float left_offset = i-count_l;
float right_offset = count_r-i;

float top_offset = j-count_t;
float bottom_offset = count_b-j;

float col_offset = left_offset+right_offset;
float row_offset = top_offset+bottom_offset;

if(col_offset > 0)
{
left_offset = (1-left_offset/col_offset)/2.0;
right_offset = (1-right_offset/col_offset)/2.0;
}

if(row_offset >0)
{
top_offset = (1-top_offset/row_offset)/2.0;
bottom_offset = (1-bottom_offset/row_offset)/2.0;
}

int top_pixel = image.at<uchar>(count_t, i);
int bottom_pixel = image.at<uchar>(count_b, i);

int right_pixel = image.at<uchar>(j, count_r);
int left_pixel = image.at<uchar>(j, count_l);

int interpolated_value;

if(left_pixel == vacant_pixel_value)
left_offset = 0;

if(right_pixel == vacant_pixel_value)
right_offset = 0;

if(top_pixel == vacant_pixel_value)
top_offset = 0;

if(bottom_pixel == vacant_pixel_value)
bottom_offset = 0;

if(col_offset > 0)
{
left_offset = left_offset/(2*col_offset);
right_offset = right_offset/(2*col_offset);
}
```

```
if(row_offset >0)
{
top_offset = top_offset/(2*row_offset);
bottom_offset = bottom_offset/(2*row_offset);
}

float total = left_offset + right_offset + top_offset +bottom_offset;

if(total > 0)
{
left_offset/=total;
right_offset/=total;
top_offset/=total;
bottom_offset/=total;
}

interpolated_value = left_offset*left_pixel + right_offset*right_pixel +
    top_offset*top_pixel
+ bottom_offset*bottom_pixel;

image.at<uchar>(j, i) = interpolated_value;
}
}
}
}
}
```

```
Mat perspective_transform(Point2f input_rectangle[], Point2f
    output_rectangle[])
{
Mat A = Mat::ones( 3, 3, CV_32F );
Mat B = Mat::ones( 3, 1, CV_32F );

A.at<float>(0,0) = input_rectangle[0].x;
A.at<float>(1,0) = input_rectangle[0].y;

A.at<float>(0,1) = input_rectangle[1].x;
A.at<float>(1,1) = input_rectangle[1].y;

A.at<float>(0,2) = input_rectangle[2].x;
A.at<float>(1,2) = input_rectangle[2].y;

B.at<float>(0,0) = input_rectangle[3].x;
B.at<float>(1,0) = input_rectangle[3].y;

Mat C = Mat::ones( 3, 1, CV_32F );
C = A.inv()*B;

Mat M = Mat::ones( 3, 3, CV_32F );

M.at<float>(0,0) = C.at<float>(0,0)*input_rectangle[0].x;
M.at<float>(1,0) = C.at<float>(0,0)*input_rectangle[0].y;
M.at<float>(2,0) = C.at<float>(0,0);
```

```
M.at<float>(0,1) = C.at<float>(1,0)* input_rectangle[1].x;
M.at<float>(1,1) = C.at<float>(1,0)*input_rectangle[1].y;
M.at<float>(2,1) = C.at<float>(1,0);

M.at<float>(0,2) = C.at<float>(2,0)*input_rectangle[2].x;
M.at<float>(1,2) = C.at<float>(2,0)*input_rectangle[2].y;
M.at<float>(2,2) = C.at<float>(2,0);

Mat D = Mat::ones( 3, 3, CV_32F );
Mat E = Mat::ones( 3, 1, CV_32F );

D.at<float>(0,0) = output_rectangle[0].x;
D.at<float>(1,0) = output_rectangle[0].y;

D.at<float>(0,1) = output_rectangle[1].x;
D.at<float>(1,1) = output_rectangle[1].y;

D.at<float>(0,2) = output_rectangle[2].x;
D.at<float>(1,2) = output_rectangle[2].y;

E.at<float>(0,0) = output_rectangle[3].x;
E.at<float>(1,0) = output_rectangle[3].y;

Mat F = Mat::ones( 3, 1, CV_32F );
F = D.inv()*E;

Mat N = Mat::ones( 3, 3 , CV_32F );

N.at<float>(0,0) = F.at<float>(0,0)*output_rectangle[0].x;
N.at<float>(1,0) = F.at<float>(0,0)*output_rectangle[0].y;
N.at<float>(2,0) = F.at<float>(0,0);

N.at<float>(0,1) = F.at<float>(1,0)*output_rectangle[1].x;
N.at<float>(1,1) = F.at<float>(1,0)*output_rectangle[1].y;
N.at<float>(2,1) = F.at<float>(1,0);

N.at<float>(0,2) = F.at<float>(2,0)*output_rectangle[2].x;
N.at<float>(1,2) = F.at<float>(2,0)*output_rectangle[2].y;
N.at<float>(2,2) = F.at<float>(2,0);

Mat perspective_transform= Mat::ones( 3, 3, CV_32F );
perspective_transform = N*M.inv();

return perspective_transform;
}

Mat resize_image(const Mat& input_image, int width, int height)
{
Mat resized_image ;

float scale_x = (float)height/(float)input_image.rows;
float scale_y = (float)width/(float)input_image.cols;

if(input_image.type() == CV_8UC3)
{
resized_image = Mat::ones(height,width,CV_8UC3)*0;
```

```
for( int j = 0; j < input_image.rows ; j++ )
for( int i = 0; i < input_image.cols; i++ )
{
int x = cvFloor(scale_x*j);
int y = cvFloor(scale_y*i);

if(x >= 0 && x < height && y >=0 && y< width)
resized_image.at<Vec3b>(x,y) = input_image.at<Vec3b>(j,i);

}
}

else if(input_image.type() == CV_8UC1)
{
resized_image = Mat::ones(height,width,CV_8UC1)*0;

for( int j = 0; j < input_image.rows ; j++ )
for( int i = 0; i < input_image.cols; i++ )
{
int x = cvFloor(scale_x*j);
int y = cvFloor(scale_y*i);

if(x >= 0 && x < height && y >=0 && y< width)
resized_image.at<uchar>(x,y) = input_image.at<uchar>(j,i);

}
}

else
{
cout<<"Resize operation not available for this image type"<<endl;
return resized_image;
}

bilinearInterpolation(resized_image,0);

return resized_image;
}

void warp_image(const Mat& input_image, Mat& output_image, const Mat&
perspective_transform)
{

Mat given_point = Mat::ones(3,1,CV_32F);
Mat transformed_point = Mat::ones(3,1,CV_32F);

if(input_image.type() == CV_8UC3)
{
for( int j = 0; j < input_image.rows ; j++ )
for( int i = 0; i < input_image.cols; i++ )
{
given_point.at<float>(0,0) = i;
given_point.at<float>(1,0) = j;

transformed_point = perspective_transform*given_point;
}
```

```
int x =
    cvFloor(transformed_point.at<float>(1,0)/transformed_point.at<float>(2,0));
int y =
    cvFloor(transformed_point.at<float>(0,0)/transformed_point.at<float>(2,0));

if(x >= 0 && x < output_image.rows && y >=0 && y< output_image.cols)
output_image.at<Vec3b>(x,y) = input_image.at<Vec3b>(j,i);

}

}

else if(input_image.type() == CV_8UC1)
{
for( int j = 0; j < input_image.rows ; j++ )
for( int i = 0; i < input_image.cols; i++ )
{
given_point.at<float>(0,0) = i;
given_point.at<float>(1,0) = j;

transformed_point = perspective_transform*given_point;

int x =
    cvFloor(transformed_point.at<float>(1,0)/transformed_point.at<float>(2,0));
int y =
    cvFloor(transformed_point.at<float>(0,0)/transformed_point.at<float>(2,0));

if(x >= 0 && x < output_image.rows && y >=0 && y< output_image.cols)
output_image.at<uchar>(x,y) = input_image.at<uchar>(j,i);

}
}
```

B.2 Image Enhancement

B.2.1 Header

```
// image_enhancement.h

#ifndef IMAGE_ENHANCEMENT_H_
#define IMAGE_ENHANCEMENT_H_

#include <iostream>
#include <opencv2/opencv.hpp>

#define R_WEIGHT 0.2989
#define G_WEIGHT 0.5870
#define B_WEIGHT 0.1140

using namespace cv;

Mat convert_to_grayscale(const Mat& input_image);
void compute_histogram(const Mat& input_image, int histogram[]);
void display_histogram(int histogram[], const char* name);
void compute_cumulative_histogram(int histogram[], int
    cumulative_histogram[]);
int scale_histogram(int cumulative_histogram[], int scaled_histogram[],
    float scaling_factor);
Mat equalize_image(const Mat& input_image);
Mat log_transformation(const Mat& input_image, int
    transformation_constant);
Mat inverse_transformation(const Mat& input_image);
Mat gamma_correction(const Mat& input_image, int gamma);
Mat sharpen(const Mat& input_image, int kernel_size, float alpha);
void threshold_image(const Mat& input_image, Mat& thresholded_image, float
    threshold, bool inverse = false, bool adaptive = false);

#endif // IMAGE_ENHANCEMENT_H_
```

B.2.2 Source

```
// image_enhancement.cpp

#include "image_enhancement.h"
#include "image_filters.h"

Mat convert_to_grayscale(const Mat& input_image)
{

Mat rgb_image = input_image.clone();

if(rgb_image.type() != CV_8UC1)
    rgb_image.convertTo(rgb_image, CV_8UC1);

Mat grayscale_image = cv::Mat(rgb_image.rows, rgb_image.cols, CV_8UC1,
    cv::Scalar(0, 0, 0));

for(int j = 0; j < grayscale_image.rows; j++)
```

```
for(int i = 0; i < grayscale_image.cols; i++)
{
    Vec3b rgb_value = rgb_image.at<Vec3b>(j, i);
    grayscale_image.at<uchar>(j, i) = R_WEIGHT*rgb_value[0] +
        G_WEIGHT*rgb_value[1] + B_WEIGHT*rgb_value[2];
}

return grayscale_image;
}

void compute_histogram(const Mat& input_image, int histogram[])
{
    Mat image = input_image.clone();

    if(image.type() != CV_8UC1)
        image.convertTo(image, CV_8UC1);

    for (int i = 0 ; i < 256 ; i++)
        histogram[i] = 0;

    // Store the frequency of intensities
    for(int j = 0; j < image.rows; j++)
        for(int i = 0; i < image.cols; i++)
    {
        histogram[image.at<uchar>(j, i)]++;
    }
}

void display_histogram(int histogram[], const char* name)
{
    int hist[256];

    for(int i = 0; i < 256; i++)
    {
        hist[i]=histogram[i];
    }

    // draw the histograms
    int hist_w = 512; int hist_h = 400;
    int bin_w = cvRound((double) hist_w/256);

    Mat histogram_image(hist_h, hist_w, CV_8UC1, Scalar(255, 255, 255));

    // find the maximum intensity element from histogram
    int max = hist[0];
    for(int i = 1; i < 256; i++){
        if(max < hist[i]){
            max = hist[i];
        }
    }

    // normalize the histogram between 0 and histImage.rows

    for(int i = 0; i < 256; i++){
        hist[i] = ((double)hist[i]/max)*histogram_image.rows;
    }
}
```

```
}

// draw the intensity line for histogram
for(int i = 0; i < 256; i++)
{
line(histogram_image, Point(bin_w*(i), hist_h),
Point(bin_w*(i), hist_h - hist[i]),
Scalar(0,0,0), 1, 8, 0);
}

// display histogram
namedWindow(name, CV_WINDOW_AUTOSIZE);
imshow(name, histogram_image);

std::ostringstream display_string ;

display_string<<"../results/histogram_equalization/"<< name << ".jpg";

imwrite( display_string.str(), histogram_image );
}

void compute_cumulative_histogram(int histogram[], int
cumulative_histogram[])
{
cumulative_histogram[0] = histogram[0];

for(int j = 1; j < 256 ; j++)
{
cumulative_histogram[j] = histogram[j]+cumulative_histogram[j-1];
}
}

int scale_histogram(int cumulative_histogram[],int scaled_histogram[],
float scaling_factor)
{

for(int j = 0; j < 256 ; j++)
{
scaled_histogram[j] = cvRound(cumulative_histogram[j]*scaling_factor);
}

}

Mat equalize_image(const Mat& input_image)
{
int histogram[256];

compute_histogram(input_image, histogram);

int cumulative_histogram[256], scaled_histogram[256];

int image_size = input_image.rows*input_image.cols;

// Compute alpha (scaling factor) based on total number of pixels and
// maximum intensity
float scaling_factor = 255.0/image_size;
```

```
// Compute probability of each intensity by normalizing the histogram
double intensity_probability[256];

for(int i = 0; i < 256 ; i++)
{
intensity_probability[i] = histogram[i]/image_size;
}

// Compute the cumulative histogram by adding all values of lower
// intensities
compute_cumulative_histogram(histogram, cumulative_histogram);

// Scaled the cumulative histogram by the scaling factor
scale_histogram(cumulative_histogram, scaled_histogram, scaling_factor);

Mat equalized_image = input_image.clone();

// Equalize the image by looking at the value from scaled histogram at the
// intensity
// level at the corresponding pixel

for(int j = 0; j < equalized_image.rows; j++)
for(int i = 0; i < equalized_image.cols; i++)
{
equalized_image.at<uchar>(j,i) =
    saturate_cast<uchar>(scaled_histogram[equalized_image.at<uchar>(j,i)]);
}

return equalized_image;
}

Mat log_transformation(const Mat& input_image, int transformation_constant)
{

Mat log_image = input_image.clone();

if(log_image.type() != CV_8UC1)
log_image.convertTo(log_image, CV_8UC1);

for(int j = 0; j < log_image.rows ; j++)
for(int i = 0; i < log_image.cols; i++)
{
log_image.at<uchar>(j,i) =
    transformation_constant*log(abs(log_image.at<uchar>(j,i))+1);
}

return log_image;
}

Mat inverse_transformation(const Mat& input_image)
{
Mat inverse_image = input_image.clone();
```

```
if(inverse_image.type() != CV_8UC1)
inverse_image.convertTo(inverse_image, CV_8UC1);

for(int j = 0; j < inverse_image.rows ; j++)
for(int i = 0; i < inverse_image.cols; i++)
{
inverse_image.at<uchar>(j,i) = 255 - inverse_image.at<uchar>(j,i);
}

return inverse_image;
}

Mat gamma_correction(const Mat& input_image, int gamma)
{
Mat gamma_corrected_image = input_image.clone();

if(gamma_corrected_image.type() != CV_8UC1)
gamma_corrected_image.convertTo(gamma_corrected_image, CV_8UC1);

for(int j = 0; j < gamma_corrected_image.rows ; j++)
for(int i = 0; i < gamma_corrected_image.cols; i++)
{
gamma_corrected_image.at<uchar>(j,i) = pow(
    gamma_corrected_image.at<uchar>(j,i) , gamma );
}

return gamma_corrected_image;
}

Mat sharpen(const Mat& input_image, int kernel_size, float alpha)
{
Mat image, low_pass_filtered_image, high_pass_filtered_image,
sharpened_image;
image = input_image.clone();

if(image.type()!=CV_8UC1)
image.convertTo(image,CV_8UC1);

//Low pass filter the image using Mean Filter
low_pass_filtered_image = mean_filter(image, kernel_size);

high_pass_filtered_image = image;
sharpened_image = image;

for(int j = 0; j < input_image.rows; j++)
for(int i = 0; i < input_image.cols; i++)
{

//High pass filter the image by subtracting input_image from low pass
// filtered image and saturate the output
high_pass_filtered_image.at<uchar>(j,i) =
    saturate_cast<uchar>(input_image.at<uchar>(j,i) -
    low_pass_filtered_image.at<uchar>(j,i));

//Sharpen the image by doing weighted addition of the high pass filtered
// image to the input image and saturate the output
}
```

```
sharpened_image.at<uchar>(j,i) =
    saturate_cast<uchar>(input_image.at<uchar>(j,i) +
    alpha*high_pass_filtered_image.at<uchar>(j,i));
}

return sharpened_image;
}

void threshold_image(const Mat& input_image, Mat& thresholded_image, float
    threshold, bool inverse, bool adaptive)
{
thresholded_image = input_image.clone();
int image_type = input_image.type();
thresholded_image.convertTo(thresholded_image,CV_8UC1);
Mat blurred_image;

if(image_type == CV_32F)
blurred_image = gaussian_filter(thresholded_image,5,1.4);
else if(image_type == CV_8UC3)
std::cout<<"Thresholding not available for non CV_8UC1 & CV_32F
    images"<<std::endl;
else
blurred_image = gaussian_filter(input_image,11,1.8);

if(blurred_image.type() != image_type)
blurred_image.convertTo(blurred_image,image_type);

float c = threshold;
for(int j = 1; j < input_image.rows-1; j++)
for(int i =1; i < input_image.cols-1; i++)
{
if(image_type == CV_8UC1)
{
if(adaptive)
{
threshold =(int) saturate_cast<uchar>(blurred_image.at<uchar>(j,i) - c);

}

if (input_image.at<uchar>(j,i) >= threshold)
if(inverse)
thresholded_image.at<uchar>(j,i) = 0;
else
thresholded_image.at<uchar>(j,i) = 255;
else
if(inverse)
thresholded_image.at<uchar>(j,i) = 255;
else
thresholded_image.at<uchar>(j,i) = 0;
}
else if(image_type == CV_32F)
{
if(adaptive)
```

```
{  
threshold = (blurred_image.at<float>(j,i) - c);  
  
if (input_image.at<float>(j,i) >= threshold)  
if(inverse)  
thresholded_image.at<uchar>(j,i) = 0;  
else  
thresholded_image.at<uchar>(j,i) = 255;  
else  
if(inverse)  
thresholded_image.at<uchar>(j,i) = 255;  
else  
thresholded_image.at<uchar>(j,i) = 0;  
  
}  
}  
}
```

B.3 Image Filters

B.3.1 Header

```
// image_filters.h

#ifndef IMAGE_FILTERS_H_
#define IMAGE_FILTERS_H_


#include <iostream>
#include <opencv2/opencv.hpp>

#define PI 3.14159

using namespace cv;

void merge(int A[ ] , int start, int mid, int end);

void merge_sort (int A[ ] , int start , int end );

Mat image_padding(const Mat& input_image, int offset);

Mat image_depadding(const Mat& input_image, int offset);

Mat convolve(const Mat& input_image, const Mat& kernel);

Mat median_filter(const Mat& input_image, int kernel_size);

Mat morphological_filter(const Mat& input_image, int kernel_size,bool max,bool ignore_center_pixel);

Mat mean_filter(const Mat& input_image, int kernel_size);

Mat gaussian_filter(const Mat& input_image, int kernel_size, float sigma);

Mat bilateral_convolve(const Mat& input_image, const Mat& gaussian_kernel,
                      float sigma_r);

Mat bilateral_filter(const Mat& input_image, int kernel_size, float
                     sigma_g, float sigma_r);

Mat image_padding_for_dft(const Mat& input_image);

Mat add_noise(const Mat& input_image, int std_dev);

Mat get_gaussian_blur_kernel(int kernel_size, float sigma);

Mat get_motion_blur_kernel(int kernel_size);

Mat fourier_transform(const Mat& padded_image);

Mat power_spectrum(const Mat& input_image);

Mat wiener_filter(const Mat& noisy_image, const Mat& signal_spectrum, Mat
                  kernel, int kernel_size, float threshold, float std_dev);
```

```

Mat inverse_filter(const Mat& noisy_image, Mat kernel, int kernel_size,
                  float std_dev, float threshold = 0.2, bool pseudo_inverse = false);

Mat pad_kernel(cv::Size size,const Mat& kernel, int kernel_size);

#endif // IMAGE_FILTERS_H_

```

B.3.2 Source

```

// image_filters.cpp

#include "image_filters.h"

void merge(float A[ ] , int start, int mid, int end) {

    //stores the starting position of both parts in temporary variables.
    int p = start ,q = mid+1;

    float Arr[end-start+1];
    int k=0;

    for(int i = start ;i <= end ;i++) {
        if(p > mid) //checks if first part comes to an end or not .
        Arr[ k++ ] = A[ q++ ] ;

        else if ( q > end) //checks if second part comes to an end or not
        Arr[ k++ ] = A[ p++ ] ;

        else if( A[ p ] < A[ q ]) //checks which part has smaller element.
        Arr[ k++ ] = A[ p++ ] ;

        else
        Arr[ k++ ] = A[ q++ ];
    }
    for (int p=0 ; p< k ;p ++){
        /* Now the real array has elements in sorted manner including both
        parts.*/
        A[ start++ ] = Arr[ p ] ;
    }
}

void merge_sort (float A[ ] , int start , int end ) {
    if( start < end ) {
        int mid = (start + end ) / 2 ; // defines the current array in 2 parts .
        merge_sort (A, start , mid ) ;      // sort the 1st part of array .
        merge_sort (A,mid+1 , end ) ;      // sort the 2nd part of array .

        // merge the both parts by comparing elements of both the parts.
        merge(A,start , mid , end );
    }
}

Mat image_padding(const Mat& input_image, int offset)
{

```

```
Mat padded_image = Mat(input_image.rows+2*offset,
                      input_image.cols+2*offset, CV_32F, 0.0);

Mat image = input_image.clone();

// if(image.type() != CV_8UC1)
// image.convertTo(image, CV_8UC1);

for(int j = 0; j < input_image.rows ; j++)
for(int i = 0; i < input_image.cols; i++)
{
if(image.type() == CV_8UC1)
padded_image.at<float>(j+offset,i+offset) = image.at<uchar>(j,i);

else if(image.type() == CV_32F)
padded_image.at<float>(j+offset,i+offset) = image.at<float>(j,i);
}

return padded_image;
}

Mat image_depadding(const Mat& input_image, int offset)
{
Mat depadded_image = Mat(input_image.rows-2*offset,
                         input_image.cols-2*offset, CV_32F, 0.0);

for(int j = 0; j < input_image.rows-2*offset ; j++)
for(int i = 0; i < input_image.cols-2*offset; i++)
{
depadded_image.at<float>(j,i) = input_image.at<float>(j+offset,i+offset);
}

return depadded_image;
}

Mat convolve(const Mat& input_image, const Mat& kernel)
{

int kernel_size = kernel.rows;

int offset;

if(kernel_size % 2 != 0)
{
offset = (kernel_size+1)/2 - 1;
}
else
{
offset = (kernel_size)/2 - 1;
}

Mat padded_image = image_padding(input_image, offset);

Mat flipped_kernel = Mat(kernel.rows, kernel.cols, CV_32F, 0.0);

for(int m = 0; m < kernel_size ; m++)
```

```
for(int n = 0; n < kernel_size; n++)
{
flipped_kernel.at<float>(m,n) =
    kernel.at<float>(kernel_size-m-1,kernel_size-n-1);
}

Mat convolved_image = Mat(padded_image.rows, padded_image.cols, CV_32F,
0.0);

float value = 0.0;
for(int j = offset; j < padded_image.rows - offset ; j++)
for(int i = offset; i < padded_image.cols - offset; i++)
{

for(int m = 0; m < kernel_size ; m++)
for(int n = 0; n < kernel_size; n++)
{

value +=
    (padded_image.at<float>(j+m-offset,i+n-offset))*flipped_kernel.at<float>(m,n);

}

convolved_image.at<float>(j,i) = value;

value = 0;
}

Mat depadded_image = image_depading(convolved_image, offset);

return depadded_image;
}

Mat bilateral_convolve(const Mat& input_image, const Mat& gaussian_kernel,
                      float sigma_r)
{

int kernel_size = gaussian_kernel.rows;

int offset;

if(kernel_size % 2 != 0)
{
offset = (kernel_size+1)/2 - 1;
}
else
{
offset = (kernel_size)/2 - 1;
}

Mat padded_image = image_padding(input_image, offset);

Mat convolved_image = Mat(padded_image.rows, padded_image.cols, CV_32F,
0.0);

float value, range_weight, weight, cumulative_weight;
```

```
int pixel_intensity, neighboring_pixel_intensity ;

for(int j = offset; j < padded_image.rows - offset ; j++)
for(int i = offset; i < padded_image.cols - offset; i++)
{

int pixel_intensity = padded_image.at<float>(j,i);
cumulative_weight = 0.0;
value = 0.0;
for(int m = 0; m < kernel_size ; m++)
for(int n = 0; n < kernel_size; n++)
{
neighboring_pixel_intensity =
    padded_image.at<float>(j+m-offset,i+n-offset);
range_weight = (float) exp(-1.0* ( pow(pixel_intensity -
    neighboring_pixel_intensity,2) ) / ( 2.0 * pow(sigma_r,2) ) );
weight = gaussian_kernel.at<float>(m,n) * range_weight ;
value += neighboring_pixel_intensity*weight;
cumulative_weight += weight ;
//std::cout<<flipped_kernel.at<double>(m,n)<<std::endl;
}

// Normalize the value
convolved_image.at<float>(j,i) = (value/cumulative_weight);
}

Mat depadded_image = image_depadding(convolved_image, offset);

// if(depadded_image.type() != input_image.type())
// depadded_image.convertTo(depadded_image,input_image.type());

return depadded_image;
}

Mat gaussian_filter(const Mat& input_image, int kernel_size, float sigma)
{

Mat kernel = Mat(kernel_size, kernel_size, CV_32F, 0.0);
int k;

if(kernel_size % 2 != 0)
{
k = (kernel_size-1)/2;
}
else
{
k = (kernel_size)/2;
}

float value = 0.0,value2 = 0.0;

// Create the Gaussian Kernel
for(int j = 0; j < kernel_size ; j++)
for(int i = 0; i < kernel_size; i++)
{
```

```
kernel.at<float>(j,i) = (float)( 1.0 / ( 2.0*PI*pow(sigma,2) ) ) *
    exp(-1.0* ( pow(i+1-(k+1),2) + pow(j+1-(k+1),2) ) / ( 2.0 *
    pow(sigma,2) ) ) ;
value += kernel.at<float>(j,i);
}

// Normalize kernel , so that the sum of all elements in the kernel is 1
for(int j = 0; j < kernel_size ; j++)
for(int i = 0; i < kernel_size; i++)
{
kernel.at<float>(j,i) = kernel.at<float>(j,i)/value ;
}

Mat filtered_image = convolve(input_image, kernel);

if(filtered_image.type() != input_image.type())
filtered_image.convertTo(filtered_image,input_image.type());

return filtered_image;
}

Mat mean_filter(const Mat& input_image, int kernel_size)
{

Mat kernel = Mat(kernel_size, kernel_size, CV_32F, 0.0);

for(int j = 0; j < kernel_size ; j++)
for(int i = 0; i < kernel_size; i++)
{
kernel.at<float>(j,i) = ( 1.0 / pow(kernel_size,2)) ;
}

Mat filtered_image = convolve(input_image, kernel);

if(filtered_image.type() != input_image.type())
filtered_image.convertTo(filtered_image,input_image.type());

return filtered_image;
}

Mat morphological_filter(const Mat& input_image, int kernel_size, bool
max, bool ignore_center_pixel=false )
{
int offset;

if(kernel_size % 2 != 0)
{
offset = (kernel_size+1)/2 - 1;
}
else
{
offset = (kernel_size)/2 - 1;
}

Mat padded_image = image_padding(input_image, offset);
```

```
Mat filtered_image = Mat(padded_image.rows, padded_image.cols, CV_32F,
0.0);

int size = kernel_size*kernel_size;

float neighborhood[size];

int k;

float value = 0.0;
for(int j = offset; j < padded_image.rows - offset ; j++)
for(int i = offset; i < padded_image.cols - offset; i++)
{
k = 0;

for(int m = 0; m < kernel_size ; m++)
for(int n = 0; n < kernel_size; n++)
{
int row = j+m-offset;
int col = i+n-offset;

if(ignore_center_pixel)
{
if(j!=row && i!=col)
{
neighborhood[k] = padded_image.at<float>(row,col) ;
k++;
}
}
else
{
neighborhood[k] = padded_image.at<float>(row,col) ;
k++;
}

}

if(ignore_center_pixel)
merge_sort(neighborhood,0,size-2);
else
merge_sort(neighborhood,0,size-1);

if(max)
{
if(ignore_center_pixel)
filtered_image.at<float>(j,i) = neighborhood[k-2];
else
filtered_image.at<float>(j,i) = neighborhood[k-1];
}
else
filtered_image.at<float>(j,i) = neighborhood[0];
}

Mat depadded_image = image_depadding(filtered_image, offset);
```

```
if(depadded_image.type() != input_image.type())
depadded_image.convertTo(depadded_image,input_image.type());

return depadded_image;

}

Mat median_filter(const Mat& input_image, int kernel_size)
{
int offset;

if(kernel_size % 2 != 0)
{
offset = (kernel_size+1)/2 - 1;
}
else
{
offset = (kernel_size)/2 - 1;
}

Mat padded_image = image_padding(input_image, offset);

Mat filtered_image = Mat(padded_image.rows, padded_image.cols, CV_32F,
0.0);

int size = kernel_size*kernel_size;
float neighborhood[size];

int k;

int mid ;

if(kernel_size % 2 != 0)
{
mid = (size+1)/2-1;
}
else
{
mid = (size)/2-1;
}

float value = 0.0;
for(int j = offset; j < padded_image.rows - offset ; j++)
for(int i = offset; i < padded_image.cols - offset; i++)
{
k = 0;

for(int m = 0; m < kernel_size ; m++)
for(int n = 0; n < kernel_size; n++)
{

neighborhood[k] = padded_image.at<float>(j+m-offset,i+n-offset) ;
k++;
}
```

```
merge_sort(neighborhood,0,size-1);

filtered_image.at<float>(j,i) = (float)neighborhood[mid];
}

Mat depadded_image = image_depadding(filtered_image, offset);

if(depadded_image.type() != input_image.type())
depadded_image.convertTo(depadded_image,input_image.type());

return depadded_image;

}

Mat bilateral_filter(const Mat& input_image, int kernel_size, float
sigma_g, float sigma_r)
{
Mat kernel = Mat(kernel_size, kernel_size, CV_32F, 0.0);
int k;

if(kernel_size % 2 != 0)
{
k = (kernel_size-1)/2;
}
else
{
k = (kernel_size)/2;
}

// Create the Gaussian Kernel
for(int j = 0; j < kernel_size ; j++)
for(int i = 0; i < kernel_size; i++)
{
kernel.at<float>(j,i) = (float) exp(-1.0* ( pow(i+1-(k+1),2) +
pow(j+1-(k+1),2) ) / ( 2.0 * pow(sigma_g,2) ) ) ; // ( 1.0 /(
2.0*PI*pow(sigma_g,2) ) ) *

}

Mat filtered_image = bilateral_convolve(input_image, kernel, sigma_r);

if(filtered_image.type() != input_image.type())
filtered_image.convertTo(filtered_image,input_image.type());

return filtered_image;

}

Mat image_padding_for_dft(const Mat& input_image)
{
Mat padded_image ;
int rows = getOptimalDFTSize(input_image.rows);
int cols = getOptimalDFTSize(input_image.cols);
copyMakeBorder(input_image, padded_image, 0, rows - input_image.rows, 0,
cols - input_image.cols, BORDER_CONSTANT, Scalar::all(0));
return padded_image;
}
```

```
Mat add_noise(const Mat& input_image, float std_dev)
{
    Mat noisy_image(input_image.rows, input_image.cols, CV_8U);
    Mat noise(input_image.rows, input_image.cols, CV_32F);
    randn(noise, Scalar::all(0), Scalar::all(std_dev));
    noise.convertTo(noisy_image, CV_8U);
    noisy_image += input_image.clone();
    return noisy_image;
}

Mat pad_kernel(cv::Size size, const Mat& kernel, int kernel_size)
{
    Mat padded_kernel = Mat::zeros(size, CV_32F);

    for(int j = 0; j < kernel_size ; j++)
    for(int i = 0; i < kernel_size; i++)
    {

        padded_kernel.at<float>(j,i) = kernel.at<float>(j,i);
    }

    return padded_kernel;
}

Mat get_gaussian_blur_kernel(int kernel_size, float sigma)
{
    Mat kernel = Mat(kernel_size, kernel_size, CV_32F, 0.0);
    int k;

    if(kernel_size % 2 != 0)
    {
        k = (kernel_size-1)/2;
    }
    else
    {
        k = (kernel_size)/2;
    }

    float value = 0.0;

    // Create the Gaussian Kernel
    for(int j = 0; j < kernel_size ; j++)
    for(int i = 0; i < kernel_size; i++)
    {
        kernel.at<float>(j,i) = (float) ( 1.0 / ( 2.0*PI*pow(sigma,2) ) ) *
            exp(-1.0* ( pow(i+1-(k+1),2) + pow(j+1-(k+1),2) ) / ( 2.0 *
                pow(sigma,2) ) );
        value += kernel.at<float>(j,i);
    }

    // Normalize kernel , so that the sum of all elements in the kernel is 1
```

```
for(int j = 0; j < kernel_size ; j++)
for(int i = 0; i < kernel_size; i++)
{
kernel.at<float>(j,i) = kernel.at<float>(j,i)/value ;
}

return kernel;
}

Mat get_motion_blur_kernel(int kernel_size)
{
Mat kernel = Mat::zeros(kernel_size, kernel_size, CV_32F);

int j = kernel_size/2;

for(int i = 0; i < kernel_size; i++)
{
kernel.at<float>(j,i) = 1.0/kernel_size ;
}

return kernel;
}

Mat fourier_transform(const Mat& padded_image)
{
Mat image;
padded_image.convertTo(image,CV_32F);
//Real part and imaginary part
Mat images[] = {Mat_<float>(image), Mat::zeros(image.size(), CV_32F)};
Mat complex_image;
merge(images, 2, complex_image);
dft(complex_image,complex_image);
return complex_image;
}

Mat power_spectrum(const Mat& input_image)
{
Mat complex_image = fourier_transform(input_image);
Mat images[2],image_magnitude,spectrum_image;
split(complex_image, images);
magnitude(images[0],images[1],image_magnitude);
multiply(image_magnitude,image_magnitude,spectrum_image);
return spectrum_image;
}

Mat wiener_filter(const Mat& noisy_image, const Mat& signal_spectrum, Mat
kernel, int kernel_size, float threshold, float std_dev)
{
Mat noise(noisy_image.rows,noisy_image.cols,CV_8U);
randn(noise,Scalar::all(0),Scalar::all(std_dev));

Scalar mean_input_image = mean(noisy_image);

Mat noise_spectrum = power_spectrum(noise);
```

```
Mat images[2], kernel_images[2];

Mat complex_image = fourier_transform(noisy_image);

split(complex_image,images);

Mat padded_kernel = pad_kernel(noisy_image.size(),kernel,kernel_size);

Mat kernel_spectrum = power_spectrum(padded_kernel);

Mat kernel_spectrum_squared;

Mat kernel_complex_image = fourier_transform(padded_kernel);

split(kernel_complex_image,kernel_images);

multiply(kernel_spectrum,kernel_spectrum,kernel_spectrum_squared);

Mat inv_snr = noise_spectrum/signal_spectrum;

Mat weight = Mat::zeros(noisy_image.size(), CV_32F) ;

for(int j = 0; j < noisy_image.rows ; j++)
for(int i = 0; i < noisy_image.cols; i++)
{
if( kernel_spectrum.at<float>(j,i) > threshold)
weight.at<float>(j,i) =
((kernel_spectrum_squared.at<float>(j,i))/(kernel_spectrum_squared.at<float>(j,i))
+ inv_snr.at<float>(j,i)) / kernel_spectrum.at<float>(j,i) ;

else
weight.at<float>(j,i) = 0.0;
}

multiply(images[0],weight,images[0]);
multiply(images[1],weight,images[1]);

merge(images,2,complex_image);

idft(complex_image,complex_image);

split(complex_image,images);

Scalar mean_restored_image = mean(images[0]);

double scale_factor = mean_input_image.val[0]/mean_restored_image.val[0];

multiply(images[0],scale_factor,images[0]);

Mat normalized_image ;

images[0].convertTo(normalized_image,CV_8UC1);

return normalized_image;
}
```

```
Mat inverse_filter(const Mat& noisy_image, Mat kernel, int kernel_size,
                  float std_dev, float threshold, bool pseudo_inverse)
{
    Mat noise(noisy_image.rows,noisy_image.cols,CV_8U);
    randn(noise,Scalar::all(0),Scalar::all(std_dev));

    Scalar mean_input_image = mean(noisy_image);

    Mat images[2], kernel_images[2];

    Mat complex_image = fourier_transform(noisy_image);

    split(complex_image,images);

    Mat padded_kernel = pad_kernel(noisy_image.size(),kernel,kernel_size);

    Mat kernel_spectrum = power_spectrum(padded_kernel);

    Mat kernel_spectrum_squared;

    Mat kernel_complex_image = fourier_transform(padded_kernel);

    split(kernel_complex_image,kernel_images);

    multiply(kernel_spectrum,kernel_spectrum,kernel_spectrum_squared);

    Mat weight = Mat::zeros(noisy_image.size(), CV_32F) ;

    for(int j = 0; j < noisy_image.rows ; j++)
        for(int i = 0; i < noisy_image.cols; i++)
    {
        if (pseudo_inverse)
        {
            if( kernel_spectrum.at<float>(j,i) > threshold)
                weight.at<float>(j,i) = (1/kernel_spectrum.at<float>(j,i)) ;

            else
                weight.at<float>(j,i) = 0.0;
        }
        else
        {
            weight.at<float>(j,i) = (1/kernel_spectrum.at<float>(j,i)) ;
        }
    }

    multiply(images[0],weight,images[0]);
    multiply(images[1],weight,images[1]);

    merge(images,2,complex_image);

    idft(complex_image,complex_image);
```

```
split(complex_image,images);

Scalar mean_restored_image = mean(images[0]);

double scale_factor = mean_input_image.val[0]/mean_restored_image.val[0];

multiply(images[0],scale_factor,images[0]);

Mat normalized_image ;

images[0].convertTo(normalized_image,CV_8UC1);

return normalized_image;
}
```

B.4 Edge Detection

B.4.1 Header

```
// edge_detection.h

#ifndef EDGE_DETECTION_H_
#define EDGE_DETECTION_H_

#include <iostream>
#include <opencv2/opencv.hpp>
#include <math.h>
#include <string>

#define THRESHOLD_CANNY 35

#define INTERPOLATION true

#define STRONG_EDGE 2
#define WEAK_EDGE 1
#define NOT_EDGE 0

using namespace cv;

Mat get_image_gradient(const Mat& input_image, const Mat&
    horizontal_image, const Mat& vertical_image);

Mat get_image_gradient_direction(const Mat& input_image, const Mat&
    horizontal_image, const Mat& vertical_image);

Mat non_maximum_suppression(const Mat& image_gradient, const Mat&
    gradient_direction, const Mat& horizontal_image, const Mat&
    vertical_image);

bool check_for_connected_strong_edges(int arr[], int size);

Mat hysteresis(const Mat& input_image, int max_threshold, int
    min_threshold);

void sobel_edge_detection(const Mat& input_image, Mat& image_gradient,
    Mat& image_gradient_direction, Mat& horizontal_image, Mat&
    vertical_image);

void prewitt_edge_detection(const Mat& input_image, Mat& image_gradient,
    Mat& image_gradient_direction, Mat& horizontal_image, Mat&
    vertical_image);

Mat canny_edge_detection(const Mat& input_image, float threshold_l, float
    threshold_h);

#endif // EDGE_DETECTION_H_
```

B.4.2 Source

```
// edge_detection.cpp

#include "image_filters.h"
#include "image_enhancement.h"
#include "edge_detection.h"

void sobel_edge_detection(const Mat& input_image, Mat& image_gradient,
    Mat& image_gradient_direction, Mat& horizontal_image, Mat&
    vertical_image)
{

    Mat horizontal_kernel = Mat(3, 3, CV_32F, 0.0);
    Mat vertical_kernel = Mat(3, 3, CV_32F, 0.0);
    Mat nms_image, double_thresholded_image;

    horizontal_kernel.at<float>(0,0) = 1 ;
    horizontal_kernel.at<float>(0,1) = 0 ;
    horizontal_kernel.at<float>(0,2) = -1 ;

    horizontal_kernel.at<float>(1,0) = 2 ;
    horizontal_kernel.at<float>(1,1) = 0 ;
    horizontal_kernel.at<float>(1,2) = -2 ;

    horizontal_kernel.at<float>(2,0) = 1 ;
    horizontal_kernel.at<float>(2,1) = 0 ;
    horizontal_kernel.at<float>(2,2) = -1 ;

    vertical_kernel.at<float>(0,0) = 1 ;
    vertical_kernel.at<float>(0,1) = 2 ;
    vertical_kernel.at<float>(0,2) = 1 ;

    vertical_kernel.at<float>(1,0) = 0 ;
    vertical_kernel.at<float>(1,1) = 0 ;
    vertical_kernel.at<float>(1,2) = 0 ;

    vertical_kernel.at<float>(2,0) = -1 ;
    vertical_kernel.at<float>(2,1) = -2 ;
    vertical_kernel.at<float>(2,2) = -1 ;

    horizontal_image = convolve(input_image, horizontal_kernel);
    vertical_image = convolve(input_image, vertical_kernel);

    image_gradient = get_image_gradient(input_image, horizontal_image,
        vertical_image);

    image_gradient_direction = get_image_gradient_direction(input_image,
        horizontal_image, vertical_image);
}

void prewitt_edge_detection(const Mat& input_image, Mat& image_gradient,
    Mat& image_gradient_direction, Mat& horizontal_image, Mat&
    vertical_image)
{
```

```
Mat horizontal_kernel = Mat(3, 3, CV_32F, 0.0);
Mat vertical_kernel = Mat(3, 3, CV_32F, 0.0);

horizontal_kernel.at<float>(0,0) = 1 ;
horizontal_kernel.at<float>(0,1) = 0 ;
horizontal_kernel.at<float>(0,2) = -1 ;

horizontal_kernel.at<float>(1,0) = 1 ;
horizontal_kernel.at<float>(1,1) = 0 ;
horizontal_kernel.at<float>(1,2) = -1 ;

horizontal_kernel.at<float>(2,0) = 1 ;
horizontal_kernel.at<float>(2,1) = 0 ;
horizontal_kernel.at<float>(2,2) = -1 ;

vertical_kernel.at<float>(0,0) = 1 ;
vertical_kernel.at<float>(0,1) = 1 ;
vertical_kernel.at<float>(0,2) = 1 ;

vertical_kernel.at<float>(1,0) = 0 ;
vertical_kernel.at<float>(1,1) = 0 ;
vertical_kernel.at<float>(1,2) = 0 ;

vertical_kernel.at<float>(2,0) = -1 ;
vertical_kernel.at<float>(2,1) = -1 ;
vertical_kernel.at<float>(2,2) = -1 ;

horizontal_image = convolve(input_image, horizontal_kernel);
vertical_image = convolve(input_image, vertical_kernel);

image_gradient = get_image_gradient(input_image, horizontal_image,
    vertical_image);
image_gradient_direction = get_image_gradient_direction(input_image,
    horizontal_image, vertical_image);

}

Mat get_image_gradient(const Mat& input_image, const Mat&
    horizontal_image, const Mat& vertical_image)
{
    Mat filtered_image = Mat(input_image.rows, input_image.cols, CV_8UC1, 0.0);

    for(int j = 1; j < input_image.rows-1 ; j++)
        for(int i = 1; i < input_image.cols-1; i++)
    {
        filtered_image.at<uchar>(j,i) = (( sqrt(
            pow(horizontal_image.at<float>(j,i),2) +
            pow(vertical_image.at<float>(j,i),2)))) ;
    }

    return filtered_image;
}
```

```
Mat get_image_gradient_direction(const Mat& input_image, const Mat&
    horizontal_image, const Mat& vertical_image)
{
    Mat filtered_image = Mat(input_image.rows, input_image.cols, CV_32F, 0.0);

    for(int j = 1; j < input_image.rows-1 ; j++)
    for(int i = 1; i < input_image.cols-1; i++)
    {
        filtered_image.at<float>(j,i) =(float) (atan2(
            vertical_image.at<float>(j,i), horizontal_image.at<float>(j,i))*180/PI);
    }

    return filtered_image;
}

Mat non_maximum_suppression(const Mat& image_gradient,const Mat&
    gradient_direction, const Mat& horizontal_image, const Mat&
    vertical_image)
{
    Mat nms_image = image_gradient.clone();

    for(int j = 1; j < image_gradient.rows-1; j++)
    for(int i =1; i < image_gradient.cols-1; i++)
    {
        float angle = gradient_direction.at<float>(j,i);

        float top_elements[2];
        float bottom_elements[2];
        float ratio;

        float current_gradient = image_gradient.at<uchar>(j,i) ;

        float bottom_interpolation,top_interpolation;

        if(INTERPOLATION)
        {

            if( (angle >= 0 && angle <= 45) || (angle < -135 && angle >= -180) )
            {
                bottom_elements[0] = image_gradient.at<uchar>(j,i+1);
                bottom_elements[1] = image_gradient.at<uchar>(j+1,i+1);

                top_elements[0] = image_gradient.at<uchar>(j,i-1);
                top_elements[1] = image_gradient.at<uchar>(j-1,i-1);

                ratio = abs(vertical_image.at<float>(j,i)/current_gradient);

                bottom_interpolation = (bottom_elements[1] - bottom_elements[0])*ratio
                    +bottom_elements[0];
                top_interpolation = (top_elements[1] - top_elements[0])*ratio
                    +top_elements[0];

                if(current_gradient < bottom_interpolation ||
                    current_gradient < top_interpolation )
            }
        }
    }
}
```

```
{nms_image.at<uchar>(j,i) = 0; }

else if( (angle > 45 && angle <= 90) || (angle < -90 && angle >= -135))

{
bottom_elements[0] = image_gradient.at<uchar>(j+1,i);
bottom_elements[1] = image_gradient.at<uchar>(j+1,i+1);

top_elements[0] = image_gradient.at<uchar>(j-1,i);
top_elements[1] = image_gradient.at<uchar>(j-1,i-1);

ratio = abs(horizontal_image.at<float>(j,i)/current_gradient);

bottom_interpolation = (bottom_elements[1] - bottom_elements[0])*ratio
+bottom_elements[0];
top_interpolation = (top_elements[1] - top_elements[0])*ratio
+top_elements[0];

if(current_gradient < bottom_interpolation ||
current_gradient < top_interpolation )

{nms_image.at<uchar>(j,i) = 0; }

else if( (angle > 90 && angle <= 135) || (angle < -45 && angle >= -90))

{
bottom_elements[0] = image_gradient.at<uchar>(j+1,i);
bottom_elements[1] = image_gradient.at<uchar>(j+1,i-1);

top_elements[0] = image_gradient.at<uchar>(j-1,i);
top_elements[1] = image_gradient.at<uchar>(j-1,i+1);

ratio = abs(horizontal_image.at<float>(j,i)/current_gradient);

bottom_interpolation = (bottom_elements[1] - bottom_elements[0])*ratio
+bottom_elements[0];
top_interpolation = (top_elements[1] - top_elements[0])*ratio
+top_elements[0];

if(current_gradient < bottom_interpolation ||
current_gradient < top_interpolation )

{nms_image.at<uchar>(j,i) = 0; }

else if( (angle > 135 && angle <= 180) || (angle < 0 && angle >= -45))

{
bottom_elements[0] = image_gradient.at<uchar>(j,i-1);
bottom_elements[1] = image_gradient.at<uchar>(j+1,i-1);
```

```
top_elements[0] = image_gradient.at<uchar>(j,i+1);
top_elements[1] = image_gradient.at<uchar>(j-1,i+1);

ratio = abs(horizontal_image.at<float>(j,i)/current_gradient);

bottom_interpolation = (bottom_elements[1] - bottom_elements[0])*ratio
+bottom_elements[0];
top_interpolation = (top_elements[1] - top_elements[0])*ratio
+top_elements[0];

if(current_gradient < bottom_interpolation ||
current_gradient < top_interpolation )

{nms_image.at<uchar>(j,i) = 0;    }
}

else {

if( (angle >= -22.5 && angle <= 22.5) || (angle < -157.5 && angle >= -180))

if(image_gradient.at<uchar>(j,i) < image_gradient.at<uchar>(j,i+1) ||
image_gradient.at<uchar>(j,i) < image_gradient.at<uchar>(j,i-1) )

{nms_image.at<uchar>(j,i) = 0;    }

else if( (angle >= 22.5 && angle <= 67.5) || (angle < -112.5 && angle >=
-157.5))

if(image_gradient.at<uchar>(j,i) < image_gradient.at<uchar>(j+1,i+1) ||
image_gradient.at<uchar>(j,i) < image_gradient.at<uchar>(j-1,i-1) )

{nms_image.at<uchar>(j,i) = 0;    }

else if( (angle >= 67.5 && angle <= 112.5) || (angle < -67.5 && angle >=
-112.5))

if(image_gradient.at<uchar>(j,i) < image_gradient.at<uchar>(j+1,i) ||
image_gradient.at<uchar>(j,i) < image_gradient.at<uchar>(j-1,i) )

{nms_image.at<uchar>(j,i) = 0;    }

else if( (angle >= 112.5 && angle <= 157.5) || (angle < -22.5 && angle >=
-67.5))

if(image_gradient.at<uchar>(j,i) < image_gradient.at<uchar>(j+1,i-1) ||
image_gradient.at<uchar>(j,i) < image_gradient.at<uchar>(j-1,i+1) )

{nms_image.at<uchar>(j,i) = 0;    }

}
```

```
}

return nms_image;

}

bool check_for_connected_strong_edges(int arr[], int size)
{
int count = 0;
for(int i = 0; i < size; i++)
if(arr[i] == STRONG_EDGE)
// count++;
// if(count > 1)
return true;

return false;
}

Mat hysteresis(const Mat& input_image, int max_threshold, int
min_threshold)
{

Mat double_thresholded_image = input_image.clone() ;
Mat edge_strength_image = input_image.clone();

int size = input_image.rows * input_image.cols;

float strong_edges_row[size];

int neighborhood[9];
int k = 0;

for(int j = 1; j < input_image.rows-1; j++)
for(int i = 1; i < input_image.cols-1; i++)
{
if (input_image.at<uchar>(j,i) >= max_threshold)
edge_strength_image.at<uchar>(j,i) = STRONG_EDGE;

else if (input_image.at<uchar>(j,i) > min_threshold &&
input_image.at<uchar>(j,i) < max_threshold)
edge_strength_image.at<uchar>(j,i) = WEAK_EDGE ;

else
edge_strength_image.at<uchar>(j,i) = NOT_EDGE;
}

for(int j = 1; j < input_image.rows-1; j++)
for(int i = 1; i < input_image.cols-1; i++)
{
if (edge_strength_image.at<uchar>(j,i) == WEAK_EDGE)
{
k = 0;
```

```
for(int m = -1; m < 2 ; m++)
for(int n = -1; n < 2; n++)
{
neighborhood[k] = edge_strength_image.at<uchar>(j+m,i+n) ;
k++;
}

if( check_for_connected_strong_edges( neighborhood, 9) )
{
double_thresholded_image.at<uchar>(j,i) = 255 ;
edge_strength_image.at<uchar>(j,i) = STRONG_EDGE;
}
else
{
double_thresholded_image.at<uchar>(j,i) = 0 ;
edge_strength_image.at<uchar>(j,i) = WEAK_EDGE;
}
}

else if (edge_strength_image.at<uchar>(j,i) == STRONG_EDGE)
double_thresholded_image.at<uchar>(j,i) = 255 ;

else
double_thresholded_image.at<uchar>(j,i) = 0 ;
}

return double_thresholded_image;

}

Mat canny_edge_detection(const Mat& input_image, float threshold_l, float
threshold_h)
{
Mat gaussian_filtered_image, image_gradient,nms_image,
double_thresholded_image;
Mat gradient_direction, horizontal_image, vertical_image,
sobel_filtered_image;

gaussian_filtered_image = input_image.clone();

GaussianBlur(gaussian_filtered_image,gaussian_filtered_image,Size(5,5),
1.4, 1.4, BORDER_DEFAULT);

sobel_edge_detection(gaussian_filtered_image,
image_gradient,gradient_direction, horizontal_image, vertical_image);

threshold_image(image_gradient,sobel_filtered_image, THRESHOLD_CANNY);

nms_image = non_maximum_suppression(image_gradient,gradient_direction,
horizontal_image, vertical_image) ;

double min, max;
```

```
cv::minMaxLoc(nms_image, &min, &max);

int max_threshold = max*threshold_h;
int min_threshold = max_threshold*threshold_l;

double_thresholded_image = hysteresis( nms_image, max_threshold,
min_threshold);

return double_thresholded_image;

}
```

B.5 Harris Corner Detection

B.5.1 Header

```
// harris_corner_detection.h

#ifndef HARRIS_CORNER_DETECTION_H_
#define HARRIS_CORNER_DETECTION_H_

#include <iostream>
#include <opencv2/opencv.hpp>
#include "image_filters.h"

#define THRESHOLD 35000000000 // 
#define DISTANCE_THRESHOLD 30

using namespace cv;
using namespace std;

struct IndexT
{
    int col;
    int row;

    float distance(int j, int i);

    bool operator!=(const IndexT& rhs);

    bool operator==(const IndexT& rhs);
};

struct CornerT
{
    std::vector<IndexT> corner_indices;
    Mat corner_image;
};

CornerT harris_corner_detection(const Mat& input_image, float
    threshold=-0.25, int iterations = 10, float step_size = 0.02, int
    min_corners_num = 0);

#endif // HARRIS_CORNER_DETECTION_H_
```

B.5.2 Source

```
// harris_corner_detection.cpp

#include "harris_corner_detection.h"
#include "image_enhancement.h"
#include "image_filters.h"
#include "edge_detection.h"

float IndexT::distance(int j, int i)
{
    return sqrt(pow((row-j),2)+pow((col-i),2));
}

bool IndexT::operator!=(const IndexT& rhs)
{
    if(this->row != rhs.row && this->col != rhs.col)
        return true;
    else
        return false;
}

bool IndexT::operator==(const IndexT& rhs)
{
    if(this->row == rhs.row && this->col == rhs.col)
        return true;
    else
        return false;
}

CornerT harris_corner_detection(const Mat& input_image, float threshold,
                                int iterations, float step_size, int min_corners_num)
{

    Mat horizontal_kernel = Mat(3, 3, CV_32F, 0.0);
    Mat vertical_kernel = Mat(3, 3, CV_32F, 0.0);
    Mat image_gradient, image_gradient_direction, converted_image,
        horizontal_image, vertical_image;

    sobel_edge_detection(input_image, image_gradient,
                         image_gradient_direction, horizontal_image, vertical_image);

    if(horizontal_image.type() != CV_32F)
        horizontal_image.convertTo(horizontal_image,CV_32F);

    if(vertical_image.type() != CV_32F)
        vertical_image.convertTo(vertical_image,CV_32F);

    Mat horizontal_image_squared = Mat(horizontal_image.rows,
                                        horizontal_image.cols, CV_32F, 0.0);
    Mat vertical_image_squared = Mat(horizontal_image.rows,
                                      horizontal_image.cols, CV_32F, 0.0);
    Mat horizontal_vertical_image = Mat(horizontal_image.rows,
                                         horizontal_image.cols, CV_32F, 0.0);

    Mat combined_image = Mat(horizontal_image.rows, horizontal_image.cols,
                            CV_32F, 0.0);
```

```
for(int j = 0; j < horizontal_image.rows ; j++)
for(int i = 0; i < horizontal_image.cols ; i++)
{
combined_image.at<float>(j,i) = horizontal_image.at<float>(j,i) +
    vertical_image.at<float>(j,i);
horizontal_image_squared.at<float>(j,i) = pow(
    horizontal_image.at<float>(j,i), 2);
vertical_image_squared.at<float>(j,i) = pow(
    vertical_image.at<float>(j,i), 2);
horizontal_vertical_image.at<float>(j,i) =
    horizontal_image.at<float>(j,i)*vertical_image.at<float>(j,i) ;

}

horizontal_image_squared = gaussian_filter(horizontal_image_squared, 9,
    1.4);
vertical_image_squared = gaussian_filter(vertical_image_squared, 9, 1.4);
horizontal_vertical_image = gaussian_filter(horizontal_vertical_image, 9,
    1.4);

if(horizontal_image_squared.type() != CV_32F)
horizontal_image_squared.convertTo(horizontal_image_squared,CV_32F);

if(vertical_image_squared.type() != CV_32F)
vertical_image_squared.convertTo(vertical_image_squared,CV_32F);

if(horizontal_vertical_image.type() != CV_32F)
horizontal_vertical_image.convertTo(horizontal_vertical_image,CV_32F);

Mat harris_response= Mat(horizontal_image.rows, horizontal_image.cols,
    CV_32F, 0.0);
Mat corners = Mat::zeros(horizontal_image.rows, horizontal_image.cols,
    CV_8UC1 );//Mat(horizontal_image.rows, horizontal_image.cols, CV_8UC1,
0);

float k = 0.04;

for(int j = 0; j < horizontal_image.rows ; j++)
for(int i = 0; i < horizontal_image.cols ; i++)
{
//R = Det(H) - k(Trace(H))^2;

harris_response.at<float>(j,i) =
    horizontal_image_squared.at<float>(j,i)*vertical_image_squared.at<float>(j,i)
    -pow(horizontal_vertical_image.at<float>(j,i),2)
-
    k*(pow(horizontal_image_squared.at<float>(j,i)+vertical_image_squared.at<float>(j,i),
1));
}

Mat corners2 = Mat::zeros(horizontal_image.rows, horizontal_image.cols,
    CV_8UC1 );

int size = 5;

int offset = (size+1)/2 - 1;
```

```
normalize(harris_response, harris_response, 1, 0, NORM_MINMAX);

std::vector<IndexT> best_corner_indices;

if(min_corners_num == 0)
{
threshold_image(harris_response, corners, threshold, false, true);

if(corners.type() != CV_8UC1)
corners.convertTo(corners,CV_8UC1);

std::vector<IndexT> corner_indices;

for(int j = 0; j < horizontal_image.rows ; j++)
for(int i = 0; i < horizontal_image.cols ; i++)
{
IndexT current_index;
current_index.row = j;
current_index.col = i;

if( corners.at<uchar>(j,i) > 200)
if(corner_indices.empty())
corner_indices.push_back(current_index);
else
{
bool corner_neighbor = false;
for (std::vector<IndexT>::iterator it = corner_indices.begin() ; it != corner_indices.end(); ++it)
{
if(it->distance(j,i) < DISTANCE_THRESHOLD)
corner_neighbor = true;
}

if(!corner_neighbor)
corner_indices.push_back(current_index);
}
}

best_corner_indices = corner_indices;
}

else
{

int min_corners = 10000;

float max_area = 0.0;

int count = 0;

float local_threshold = threshold - ( step_size*iterations/2.0);

int corner_size = min_corners;

while(count < iterations)
{
```

```
corners = Mat::zeros(horizontal_image.rows, horizontal_image.cols, CV_8UC1
);

threshold_image(harris_response, corners, local_threshold, false, true);

if(corners.type() != CV_8UC1)
corners.convertTo(corners,CV_8UC1);

std::vector<IndexT> corner_indices;

for(int j = 0; j < horizontal_image.rows ; j++)
for(int i = 0; i < horizontal_image.cols ; i++)
{
IndexT current_index;
current_index.row = j;
current_index.col = i;

if( corners.at<uchar>(j,i) > 200)
if(corner_indices.empty())
corner_indices.push_back(current_index);
else
{
bool corner_neighbor = false;
for (std::vector<IndexT>::iterator it = corner_indices.begin() ; it != corner_indices.end(); ++it)
{
if(it->distance(j,i) < DISTANCE_THRESHOLD)
corner_neighbor = true;
}

if(!corner_neighbor)
corner_indices.push_back(current_index);
}
}

std::cout<<"Iteration = "<<count<< " ,num corners =
"<<corner_indices.size()<<" ,local threshold ="<< local_threshold<<endl;

if(corner_indices.size()<=min_corners )
{

if(corner_indices.size() >= min_corners_num )
{

if(corner_indices.size() == min_corners_num)
{
float width = abs(corner_indices[0].row -corner_indices[1].row) +
abs(corner_indices[0].col -corner_indices[1].col);
float height = abs(corner_indices[0].row -corner_indices[2].row) +
abs(corner_indices[0].col -corner_indices[2].col);
float area = width * height;
if(area > max_area)
{
max_area = area;
best_corner_indices = corner_indices;
}
```

```
min_corners = corner_indices.size();
}

}

else
{
if(corner_indices.size() <= min_corners && corner_indices.size() >=
    min_corners_num)
{
best_corner_indices = corner_indices;
min_corners = corner_indices.size();
}
else
{
break;
}

}

}

}

else
{
break;
}

count++;

local_threshold+=step_size;

corner_size = corner_indices.size();

}

}

cout<<"HARRIS CORNER DETECTION"<<endl;

for (std::vector<IndexT>::iterator it = best_corner_indices.begin() ; it
    != best_corner_indices.end(); ++it)
{
cout<<"corner at row = "<<it->row<<" , col="<<it->col<<endl;
corners2.at<uchar>(it->row,it->col) = 255;

}

Mat image_with_corners = input_image.clone();

for( int j = 0; j < corners2.rows ; j++ )
{ for( int i = 0; i < corners2.cols; i++ )
{
if( (int) corners2.at<uchar>(j,i) == 255 )
{
circle( image_with_corners, Point( i, j ), 10, Scalar(150), 2, 8, 0 );
}
```

```
}

}

}

CornerT CornerData;
CornerData.corner_indices = best_corner_indices;
CornerData.corner_image = image_with_corners;
return CornerData;
}
```

B.6 Mobile Scanner

B.6.1 Source

```
// mobile_scanner.cpp

#include <iostream>
#include <opencv2/opencv.hpp>
#include <algorithm>
#include "image_filters.h"
#include "image_enhancement.h"
#include "edge_detection.h"
#include "harris_corner_detection.h"
#include "image_transformation.h"
#include <opencv2/features2d.hpp>

#define THRESHOLD_RATIO_H 0.24
#define THRESHOLD_RATIO_L 0.

using namespace cv;
using namespace std;

struct RansacT
{
    Mat best_perspective_transform;
    std::vector<int> best_four_matches;
};

RansacT get_best_perspective_transform(vector<KeyPoint> keypoints1,
    vector<KeyPoint> keypoints2, std::vector<DMatch> matches, int
    iterations = 50000, float threshold = 0.175)
{
    std::vector<int> num_vector;

    for (int i=0; i<matches.size(); ++i) num_vector.push_back(i);

    int count = 0;

    int best_matched_points = 0;
    Mat best_perspective_transform;
    std::vector<int> best_index_vector;

    //DO RANSAC
    while(count<iterations)
    {
        std::random_shuffle ( num_vector.begin(), num_vector.end() );

        Point2f point1[4], point2[4];

        int index1 = num_vector[0];
        int index2 = num_vector[1];
        int index3 = num_vector[2];
        int index4 = num_vector[3];

        std::vector<int> index_vector;
        index_vector.push_back(index1);
```

```
index_vector.push_back(index2);
index_vector.push_back(index3);
index_vector.push_back(index4);

point1[0] = Point2f(keypoints1[matches[index1].queryIdx].pt.x,
    keypoints1[matches[index1].queryIdx].pt.y);
point2[0] = Point2f(keypoints2[matches[index1].trainIdx].pt.x,
    keypoints2[matches[index1].trainIdx].pt.y);

point1[1] = Point2f(keypoints1[matches[index2].queryIdx].pt.x,
    keypoints1[matches[index2].queryIdx].pt.y);
point2[1] = Point2f(keypoints2[matches[index2].trainIdx].pt.x,
    keypoints2[matches[index2].trainIdx].pt.y);

point1[2] = Point2f(keypoints1[matches[index3].queryIdx].pt.x,
    keypoints1[matches[index3].queryIdx].pt.y);
point2[2] = Point2f(keypoints2[matches[index3].trainIdx].pt.x,
    keypoints2[matches[index3].trainIdx].pt.y);

point1[3] = Point2f(keypoints1[matches[index4].queryIdx].pt.x,
    keypoints1[matches[index4].queryIdx].pt.y);
point2[3] = Point2f(keypoints2[matches[index4].trainIdx].pt.x,
    keypoints2[matches[index4].trainIdx].pt.y);

Mat pt = perspective_transform(point2, point1);

int matched_points = 0;

for (int i=0; i<matches.size(); ++i)
{
    Mat B = Mat::ones( 3, 1, CV_32F );
    B.at<float>(0,0) = keypoints2[matches[i].trainIdx].pt.x;
    B.at<float>(1,0) = keypoints2[matches[i].trainIdx].pt.y;

    Mat A = Mat::ones( 3, 1, CV_32F );
    A.at<float>(0,0) = keypoints1[matches[i].queryIdx].pt.x;
    A.at<float>(1,0) = keypoints1[matches[i].queryIdx].pt.y;

    Mat Warped_B = pt*B;

    float euclidean_distance =
        sqrt(pow(A.at<float>(0,0)-Warped_B.at<float>(0,0),2)+pow(A.at<float>(1,0)-Warped_B.at<float>(1,0),2));

    if(euclidean_distance <= threshold)
        matched_points+=1;
}

if(matched_points > best_matched_points)
{
    best_matched_points = matched_points;
    best_perspective_transform = pt;
    best_index_vector = index_vector;
}

count++;
}
```

```
RansacT data;
data.best_perspective_transform = best_perspective_transform ;
data.best_four_matches = best_index_vector;

return data;
}

//Order the points as Top_Left, Top_Right, Bottom_Right, Bottom_Left
void order_points(std::vector<IndexT> corner_indices, IndexT
                  ordered_points[])
{
int max_sum = 0;
int min_sum = 100000;
int max_diff = -100000;
int min_diff = 100000;

for (std::vector<IndexT>::iterator it = corner_indices.begin() ; it != 
     corner_indices.end(); ++it)
{
int sum = it->row + it->col;
int diff = it->row - it->col;

if(sum > max_sum)
{
max_sum = sum ;
ordered_points[2] = *it;
}

if(sum < min_sum)
{
min_sum = sum ;
ordered_points[0] = *it;
}

if(diff < min_diff)
{
min_diff = diff ;
ordered_points[1] = *it;
}

if(diff > max_diff)
{
max_diff = diff ;
ordered_points[3] = *it;
}

}

cout<<" Ordered Points : Top_Left, Top_Right, Bottom_Right,
Bottom_Left"<<endl;

for(int i = 0 ; i<4 ; i++)
{
```

```
cout<<"row = "<<ordered_points[i].row<<" ,  
    col="<<ordered_points[i].col<<endl;  
}  
  
}  
  
Mat scan_document(const Mat& input_image, bool image_registration = false)  
{  
  
    Mat grayscale_image, equalized_image,detected_edges,  
    canny_detected_edges,receipt,warped_image;  
  
    float row_ratio = cvCeil(input_image.rows/640);  
    float col_ratio = cvCeil(input_image.cols/480);  
  
    int scale_factor = row_ratio>col_ratio?row_ratio:col_ratio;  
  
    if(scale_factor < 1)  
        scale_factor = 1;  
  
    Mat rgb_image_resized = Mat::zeros( input_image.rows/scale_factor,  
        input_image.cols/scale_factor, CV_8UC3 );  
  
    if(input_image.cols > 480 || input_image.rows >640 )  
        rgb_image_resized =  
            resize_image(input_image,input_image.cols/scale_factor,input_image.rows/scale_factor);  
  
    else  
    {  
        rgb_image_resized = input_image.clone();  
        scale_factor = 1;  
    }  
  
    grayscale_image = convert_to_grayscale(rgb_image_resized);  
    grayscale_image = gaussian_filter(grayscale_image,3, 1.4);  
  
    equalized_image = grayscale_image;  
  
    equalized_image = bilateral_filter(equalized_image, 5, 25, 15);  
  
    if(equalized_image.type() != CV_8UC1)  
        equalized_image.convertTo(equalized_image, CV_8UC1);  
  
    equalized_image = sharpen(equalized_image,5, 1);  
  
    canny_detected_edges = canny_edge_detection(equalized_image,  
        THRESHOLD_RATIO_L, THRESHOLD_RATIO_H);  
  
    detected_edges = canny_detected_edges;  
  
    detected_edges = morphological_filter( detected_edges, 5, true, false);  
    detected_edges = morphological_filter( detected_edges, 3, false, false);  
    detected_edges = morphological_filter( detected_edges, 3, false, false);  
    detected_edges = morphological_filter( detected_edges, 7, true, false);  
    detected_edges = morphological_filter( detected_edges, 3, true, false);  
    detected_edges = morphological_filter( detected_edges, 5, false, false);
```

```
detected_edges = morphological_filter( detected_edges, 3, false, false);

vector<vector<Point> > contours;
vector<Vec4i> hierarchy;
vector<Point> largest_contour;
vector<Point> rectangle;

findContours( detected_edges, contours, hierarchy, CV_RETR_TREE,
CV_CHAIN_APPROX_SIMPLE, Point(0, 0) );

int number_of_contours = contours.size();

if (number_of_contours > 0 )
{
float previous_area = 0.0;
float current_area = 0.0;
int current_number_of_vertices = 0;
int largest_contour_id = 0;
float largest_contour_length;
float largest_contour_area;
int largest_contour_center_x;
int largest_contour_center_y;
int number_of_vertices;

Mat image_of_contours = Mat::zeros( rgb_image_resized.rows,
rgb_image_resized.cols, CV_8UC1 );//rgb_image_resized;//Mat::zeros(
detected_edges.size(), CV_8UC3 );
Mat viz_corner = rgb_image_resized.clone();
Mat viz_contour = rgb_image_resized.clone();

RNG rng(12345);

// Find contour with largest area
for( int i = 0; i < number_of_contours ; i++ )
{
cv::approxPolyDP(cv::Mat(contours[i]), contours[i],
cv::arcLength(cv::Mat(contours[i]), true)*0.05, true);
current_area = contourArea(contours[i]);
current_number_of_vertices = contours[i].size();

if ( current_area > previous_area )
{
largest_contour_area = current_area;
largest_contour_id = i;
number_of_vertices = current_number_of_vertices;
previous_area = current_area;
}

}

Scalar color = Scalar( 255 );
drawContours( image_of_contours , contours, largest_contour_id, color, 2,
8, hierarchy, 0, Point());
drawContours( viz_contour , contours, largest_contour_id, Scalar(0,
255,0),2, 8, hierarchy, 0, Point());

Mat detected_corners;
```

```
CornerT corner_data =
    harris_corner_detection(image_of_contours,-0.25,30,0.03,4);

detected_corners = corner_data.corner_image;

IndexT ordered_points[4];

if(corner_data.corner_indices.size() < 4)
{
cout<<"Cannot process image with less than 4 corners"<<endl;
return input_image;
}
else
cout<<"Image with "<<corner_data.corner_indices.size()<<" corners
found"<<endl;

order_points(corner_data.corner_indices, ordered_points);

cout<<"Scaled Corner Points"<<endl;

for(int i = 0 ; i<4 ; i++)
{
cout<<"row = "<<ordered_points[i].row*scale_factor<<" ,
    col="<<ordered_points[i].col*scale_factor<<endl;
circle( viz_corner, Point( ordered_points[i].col, ordered_points[i].row ),
    10, Scalar(0,255,0), 2, 8, 0 );
ordered_points[i].row = cvFloor(ordered_points[i].row*scale_factor);
ordered_points[i].col = cvFloor(ordered_points[i].col*scale_factor);
}

int width1 = cvFloor(sqrt(pow(ordered_points[3].col -
    ordered_points[2].col,2) + pow(ordered_points[3].row -
    ordered_points[2].row,2)));
int width2 = cvFloor(sqrt(pow(ordered_points[1].col -
    ordered_points[0].col,2) + pow(ordered_points[1].row -
    ordered_points[0].row,2)));

int width = (width1 > width2) ? width1 : width2;

int height1 = cvFloor(sqrt(pow(ordered_points[1].col -
    ordered_points[2].col,2) + pow(ordered_points[1].row -
    ordered_points[2].row,2)));
int height2 = cvFloor(sqrt(pow(ordered_points[3].col -
    ordered_points[0].col,2) + pow(ordered_points[3].row -
    ordered_points[0].row,2)));

int height = (height1 > height2) ? height1 : height2;

Point2f input_rectangle[4], output_rectangle[4];

input_rectangle[0] = Point2f(ordered_points[0].col, ordered_points[0].row);
input_rectangle[1] = Point2f(ordered_points[1].col, ordered_points[1].row);
input_rectangle[2] = Point2f(ordered_points[2].col, ordered_points[2].row);
input_rectangle[3] = Point2f(ordered_points[3].col, ordered_points[3].row);

output_rectangle[0] = Point2f(0,0);
```

```
output_rectangle[1] = Point2f(width-1,0);
output_rectangle[2] = Point2f(width-1,height-1);
output_rectangle[3] = Point2f(0,height-1);

Mat lambda( 2, 4, CV_32FC1 );

int vacant_pixel_value = 0;

warped_image = Mat:::ones(height,width,CV_8UC3)*vacant_pixel_value;

rgb_image_resized = input_image.clone();

Mat warped_grayscale_image;

Mat pt = perspective_transform(input_rectangle, output_rectangle);

warp_image(rgb_image_resized, warped_image, pt);

bilinearInterpolation(warped_image,vacant_pixel_value);

warped_grayscale_image = convert_to_grayscale(warped_image);

receipt = warped_grayscale_image;

threshold_image(gaussian_filter(warped_grayscale_image,3, 1.4), receipt,
5, false, true);

if(!image_registration)
{
namedWindow("Input", WINDOW_AUTOSIZE);
imwrite( "../results/document_scan/resized_input.jpg", rgb_image_resized );
imshow("Input",rgb_image_resized);

namedWindow("Image Enhancement", WINDOW_AUTOSIZE);
imwrite( "../results/document_scan/image_enhancement.jpg", equalized_image
);
imshow("Image Enhancement",equalized_image);

namedWindow("Canny Edge Detection", WINDOW_AUTOSIZE);
imwrite( "../results/document_scan/canny_edge_detection.jpg",
canny_detected_edges );
imshow("Canny Edge Detection",canny_detected_edges);

namedWindow("Morphological Operations", WINDOW_AUTOSIZE);
imwrite( "../results/document_scan/morphological_operation.jpg",
detected_edges );
imshow("Morphological Operations",detected_edges);

namedWindow("Contour Detection", WINDOW_AUTOSIZE);
imwrite( "../results/document_scan/contour_detection.jpg", viz_contour );
imshow("Contour Detection",viz_contour);

namedWindow("Corner Detection", WINDOW_AUTOSIZE);
imwrite( "../results/document_scan/corner_detection.jpg", viz_corner );
imshow("Corner Detection",viz_corner);

namedWindow("Warp with Perspective Transform", WINDOW_AUTOSIZE);
```

```
imwrite( "../results/document_scan/warped_image.jpg", warped_image );
imshow("Warp with Perspective Transform",warped_image);

namedWindow("Adaptive Thresholding", WINDOW_AUTOSIZE);
imwrite( "../results/document_scan/adaptive_thresholding.jpg", receipt );
imshow("Adaptive Thresholding",receipt);
}

cout<<"Width = "<<width<<std::endl;
cout<<"Height = "<<height<<std::endl;
}
return warped_image;
}

Mat background_subtraction(Mat image1, Mat image2)
{
Mat thresholded_image1,thresholded_image2,
    subtracted_image1,subtracted_image2;
Mat improved_image1 =
    sharpen(gaussian_filter(convert_to_grayscale(image1),5, 2),5,1);
Mat improved_image2 =
    sharpen(gaussian_filter(convert_to_grayscale(image2),5, 1.4),5,1) ;

threshold_image(improved_image1,thresholded_image1, 5, false, true);
threshold_image(improved_image2,thresholded_image2, 5, false, true);

subtracted_image1 = Mat::zeros(image1.rows,image1.cols,CV_8UC1);
subtracted_image2 = Mat::zeros(image1.rows,image1.cols,CV_8UC1);

for(int j = 0; j < image1.rows ; j++)
for(int i = 0; i < image1.cols; i++)
{
if(thresholded_image1.at<uchar>(j,i) == thresholded_image2.at<uchar>(j,i)
    && thresholded_image1.at<uchar>(j,i) == 0)
    subtracted_image1.at<uchar>(j,i) = 255;
else
    subtracted_image1.at<uchar>(j,i) = 0;
}

subtracted_image1 = morphological_filter( subtracted_image1, 5, true,
    false);

for(int j = 0; j < image1.rows ; j++)
for(int i = 0; i < image1.cols; i++)
{
if(subtracted_image1.at<uchar>(j,i) == thresholded_image2.at<uchar>(j,i)
    && thresholded_image2.at<uchar>(j,i) == 0 )
    subtracted_image2.at<uchar>(j,i) = 0;
else
    subtracted_image2.at<uchar>(j,i) = 255;
}

imshow("Thresholded Reference Image",thresholded_image1);
imwrite( "../results/image_registration/thresholded_reference_image.jpg",
    thresholded_image1);

imshow("Thresholded Scanned Image",thresholded_image2);
```

```
imwrite( "../results/image_registration/thresholded_scanned_image.jpg",
thresholded_image2);

subtracted_image2 = morphological_filter( subtracted_image2, 3, false,
false);
subtracted_image2 = median_filter(subtracted_image2,5);

return subtracted_image2;
}

Mat foreground_addition(const Mat& image1, const Mat& image2, const Mat&
foreground)
{
Mat restored_image = image1.clone();

for(int j = 10; j < image1.rows-10 ; j++)
for(int i = 10; i < image1.cols-10; i++)
{
if(foreground.at<uchar>(j,i) == 0 )
{
if(image1.type() == CV_8UC3)
restored_image.at<Vec3b>(j,i) = image2.at<Vec3b>(j,i);
else
restored_image.at<uchar>(j,i) = image2.at<uchar>(j,i);
}
}

return restored_image;
}

Mat image_matching(Mat reference_image, Mat scanned_image)
{

int size = 0;
int count = 0;
int max_iterations = 20;

std::vector<DMatch> matches;

vector<KeyPoint> keypoints1, keypoints2;

while(size < 500 && count < max_iterations)
{
Ptr<FeatureDetector> detector = ORB::create(5000 + count*500);
Ptr<DescriptorExtractor> extractor = ORB::create();

detector->detect(reference_image, keypoints1);
detector->detect(scanned_image, keypoints2);

Mat descriptors1,descriptors2;
extractor->compute(reference_image, keypoints1,descriptors1);
extractor->compute(scanned_image, keypoints2,descriptors2);
}
```

```
vector< vector<DMatch> > matches12, matches21;
Ptr<DescriptorMatcher> matcher =
    DescriptorMatcher::create("BruteForce-Hamming");
matcher->knnMatch( descriptors1, descriptors2, matches12, 2 );
matcher->knnMatch( descriptors2, descriptors1, matches21, 2 );

std::vector<DMatch> good_matches1, good_matches2;

// Ratio Test proposed by David Lowe
float ratio = 0.8;
for(int i=0; i < matches12.size(); i++) {
if(matches12[i][0].distance < ratio * matches12[i][1].distance)
good_matches1.push_back(matches12[i][0]);
}

for(int i=0; i < matches21.size(); i++) {
if(matches21[i][0].distance < ratio * matches21[i][1].distance)
good_matches2.push_back(matches21[i][0]);
}

// Symmetric Test
std::vector<DMatch> better_matches;
for(int i=0; i<good_matches1.size(); i++) {
for(int j=0; j<good_matches2.size(); j++) {
if(good_matches1[i].queryIdx == good_matches2[j].trainIdx &&
   good_matches2[j].queryIdx == good_matches1[i].trainIdx) {
better_matches.push_back(DMatch(good_matches1[i].queryIdx,
                                good_matches1[i].trainIdx, good_matches1[i].distance));
break;
}
}
}
size = better_matches.size();
matches = better_matches;
count++;
cout<<"Feature Detection : Iteration ="<<count<<" , num features =
"<<size<<endl;
}

Mat orb_reference_image = reference_image.clone();
Mat orb_scanned_image = scanned_image.clone();

for(int i=0; i<matches.size(); i++)
{
int col1 = keypoints1[matches[i].queryIdx].pt.x;
int row1 = keypoints1[matches[i].queryIdx].pt.y;

int col2 = keypoints2[matches[i].trainIdx].pt.x;
int row2 = keypoints2[matches[i].trainIdx].pt.y;

circle( orb_reference_image, Point( col1, row1), 10, Scalar(0,255,0), 2,
        8, 0 );
circle( orb_scanned_image, Point( col2, row2), 10, Scalar(0,255,0), 2, 8,
        0 );
}
```

```
RansacT data = get_best_perspective_transform(keypoints1, keypoints2,
                                              matches);
Mat best_perspective_transform = data.best_perspective_transform;

vector<KeyPoint> best_keypoints1,best_keypoints2;
std::vector<DMatch> best_matches;

for(int i=0; i<4; i++)
{
    DMatch match = matches[data.best_four_matches[i]];

    KeyPoint keypoint1 = keypoints1[match.queryIdx];
    KeyPoint keypoint2 = keypoints2[match.trainIdx];

    best_keypoints1.push_back(KeyPoint(keypoint1.pt,keypoint1.size));
    best_keypoints2.push_back(KeyPoint(keypoint2.pt,keypoint2.size));
    best_matches.push_back(DMatch(i, i, match.distance));
}

Mat best_match_image;
drawMatches(reference_image, best_keypoints1, scanned_image,
           best_keypoints2, best_matches, best_match_image);

Mat output_image =
    Mat::zeros(reference_image.rows,reference_image.cols,CV_8UC3);

warp_image(scanned_image,output_image,best_perspective_transform);

bilinearInterpolation(output_image);

imshow("Better Matches Reference Image",orb_reference_image);
imwrite( "../results/image_registration/orb_reference_image.jpg",
         orb_reference_image);

imshow("Better Matches Scanned Image",orb_scanned_image);
imwrite( "../results/image_registration/orb_scanned_image.jpg",
         orb_scanned_image);

imshow("Best Four Matches RANSAC",best_match_image);
imwrite( "../results/image_registration/best_four_matches_ransac.jpg",
         best_match_image);

return output_image;

}

int main(int argc, char** argv )
{
    Mat image1, image2;

    int registration = 1;

    if(argc>=2)
    {
        try
        {
            registration = atoi(argv[1]);
        }
    }
}
```

```
}

catch (Exception e)
{
//do nothing
}

}

if(registration == 1)
{
image2 = imread( "../images/image_registration/scanned_image.jpg", 1 );
image1 = imread( "../images/image_registration/reference_image.jpg", 1 );

if ( !image1.data || !image2.data)
{
printf("No image data \n");
return -1;
}

Mat scanned_image = image2;
Mat reference_image = scan_document(image1,true);
Mat warped_scanned_image = image_matching(reference_image,scanned_image);
Mat foreground = background_subtraction(reference_image,
    warped_scanned_image);
Mat restored_image = foreground_addition(reference_image,
    warped_scanned_image, foreground);
Mat thresholded_restored_image;
threshold_image(convert_to_grayscale(restored_image),thresholded_restored_image,
    6, false, true);

imshow("Reference Image",reference_image);
imwrite( "../results/image_registration/reference_image.jpg",
    reference_image);

imshow("Warped Scanned Image",warped_scanned_image);
imwrite( "../results/image_registration/warped_scanned_image.jpg",
    warped_scanned_image);

imshow("Background Subtraction",foreground);
imwrite( "../results/image_registration/background_subtraction.jpg",
    foreground);

imshow("Thresholded Restored Image",thresholded_restored_image);
imwrite( "../results/image_registration/thresholded_restored_image.jpg",
    thresholded_restored_image);

imshow("Restored Image",restored_image);
imwrite( "../results/image_registration/restored_image.jpg",
    restored_image);
}

else
{

image1 = imread( "../images/document_scan/scanned_image.jpg", 1 );
if (!image1.data)
{
```

```
printf("No image data \n");
return -1;
}
scan_document(image1);

}

waitFor(0);

return 0;
}
```

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