



# Bonds and Their Valuation

---



## What is a bond?

---

- A long-term debt instrument in which a borrower agrees to make payments of principal and interest, on specific dates, to the holders of the bond.



# Bond Characteristics

---

- Par Value = Stated face value that is the amount the issuer must repay
- Coupon Interest Rate
- $\text{Coupon} = \text{Coupon Rate} * \text{Par Value}$
- Maturity Date = when the par value is repaid
  
- Special Features:
  - Call provisions = right of issuer to repay (buy back) the bond before maturity (call premium)
  - Conversion options = right of bondholders to convert bonds into common stocks of issuing firm
- Different types of Bonds
  - Fixed rate bonds, Floating rate bonds, Callable bonds, Puttable bonds, Convertible Bonds (CBs), Bond with Warrants (BWPs), Exchangeable bonds (EBs), Perpetual Bonds (Consols), Zero coupon bonds (STRIPs)



## Bond markets

---

- Primarily traded in the over-the-counter (OTC) market.
- Most bonds are owned by and traded among large financial institutions.
- Full information on bond trades in the OTC market is not published.



# Bond Valuation

---

Time Line,

$$V_B = \text{INT}(\text{PVIFA}_{k_d, N}) + M(\text{PVIF}_{k_d, N})$$

INT = \$ coupon interest,  $k_d$  = required return

$N$  = # of years until maturity

$M$  = Par value of the bond, usually \$1,000



## Bond Valuation – Example 1

---

$M = \$1,000$  par value,  $INT = \$80$  annual coupon,  $k_d = 10\%$ ,  $N = 12$  years

$$V_B =$$

Let's play with this example.

What is the new bond value if the required return changes to 8%?

$$V_B =$$

What if  $k_d = 6\%$ ?

$$V_B =$$



## Some Key Relationships from Example 1

---

The coupon rate was  $\$80/\$1000$  or 8%

When required rate = coupon rate

Par value (M)

Bond value

When required rate > coupon rate

Par value (M)

Bond value

When required rate < coupon rate

Par value (M)

Bond value



## Bond Value Changes over Time

---

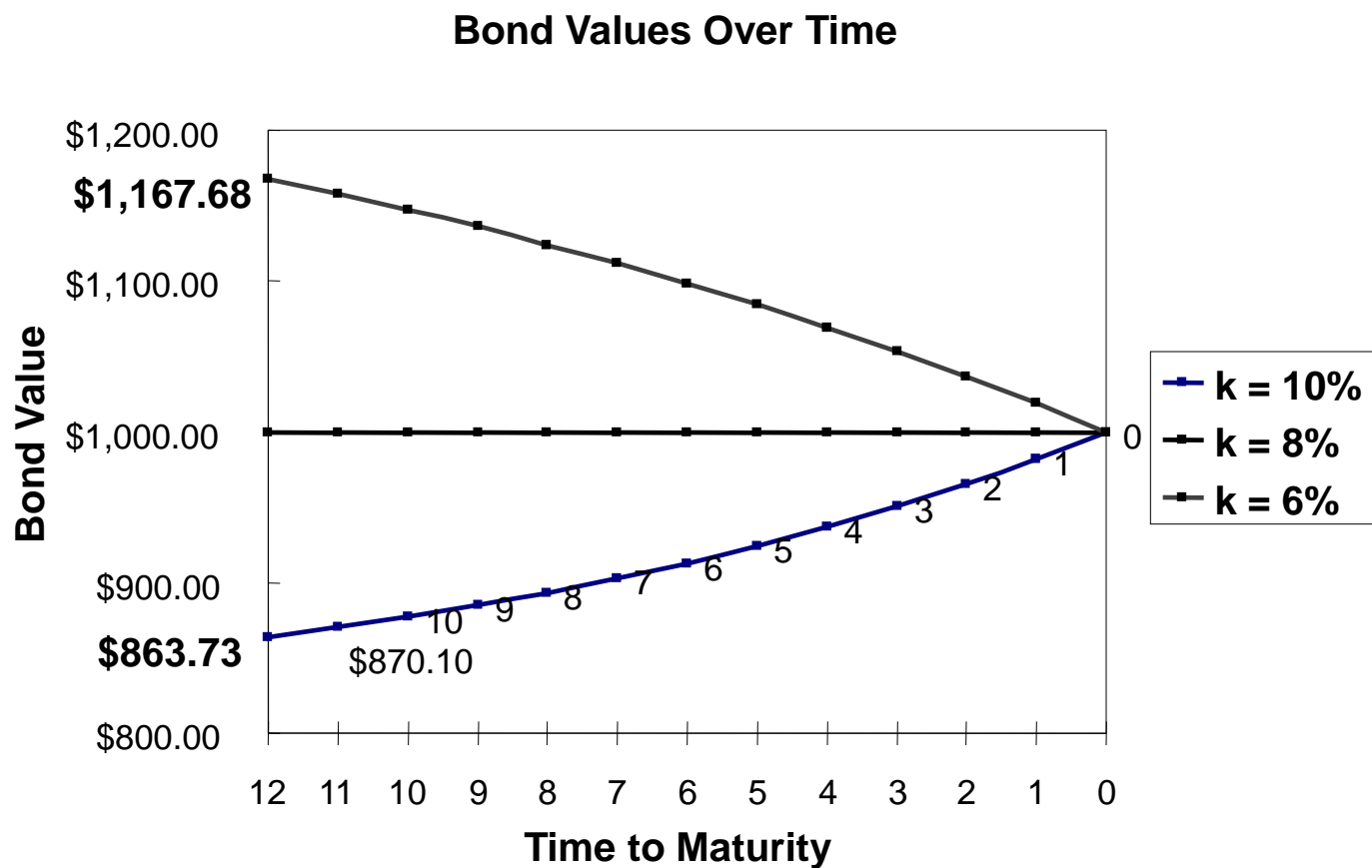
Returning to the original example #1, where  $k_d = 10\%$ ,  $N = 12$ ,  $\text{INT(PMT)} = \$80$ ,  $M(\text{FV}) = \$1,000$ , and  $V_B = \$863.73$

What is bond value one year later when  $N = 11$  and  $k_d$  is still  $= 10\%$ ?

$V_B =$



# Bond Values Over Time





## What is the bond's return over this year?

---

Total Rate of Return = Current Yield + Capital Gains Yield

Beg. Bond Value (Purchase price) = 863.73

End. Bond Value (Sale price) = 870.10

Current Yield = Annual Coupon (INT)/ Beg. Bond Value (or Purchase Price)

C.Y =

C.G.Y =

Total Return =



## Finding a bond's expected rate of return?

---

In the marketplace, we know a bond's current price (PV), but not its return.

Yield to Maturity (YTM) = the rate of return the bond would earn if purchased at today's price and held until maturity

Yield to Call (YTC) = the rate of return the bond would earn if purchased at today's price and held until could be called



## Finding a bond's expected rate of return? – cont'd..

---

- Yield to Maturity Example:

\$1000 face value bond with a 10% coupon rate paid annually with 20 years left to maturity sells for \$1091.29

What is this bond's YTM?

YTM =



## Bonds with Semiannual Coupons

---

Double the number of years, and divide required return and annual coupon by 2.

$$V_B = (\text{INT}/2)(\text{PVIFA}_{k_d/2, 2N}) + M(\text{PVIF}_{k_d/2, 2N})$$

### ■ Semiannual Example:

A \$1000 par value bond with an annual coupon rate of 9% pays coupon semiannually with 15 years left to maturity. What is the most you would be willing to pay for this bond if your required return is 8% APR?

$V_B =$



## Risks of Bonds

---

Let's suppose we have 5 different bonds. Assume that required rates of return on those bonds are all  $k\%$ , and par values are all \$1,000

Bond1: 10-yr, 10% annual coupon

$$V_B = \$100(PVIFA_{k,10}) + \$1000(PVIF_{k,10})$$

Bond2-4: zero coupon bonds, bond2 with  $N=10$ , bond 3 with  $N=5$ , bond4 with  $N=30$

$$V_B = \$1000(PVIF_{k,N})$$

Bond 5: \$100 Perpetuity

$$V_B = PMT/k = \$100/k$$



## Risks of Bonds – cont'd...

---

- Interest Rate Risk

Bond	K = 7%	K = 8%	% Change
10-yr, 10% annual coupon	\$1210.71	\$1134.20	-6.32%
10-yr zero coupon	\$508.35	\$463.19	-8.88%
5-yr zero coupon	\$712.99	\$680.58	-4.55%
30-yr zero coupon	\$131.37	\$99.38	-24.35%
\$100 perpetuity	\$1428.57	\$1250.00	-12.50%



## Risks of Bonds – cont'd...

---

Comparing Bonds 1 and 5 shows longer term bonds have greater bond price changes = More interest rate risk

Comparing Bonds 2, 3, and 4 also confirms that

Comparing the two 10-yr (1 & 2), the zero had the greater price change = More interest rate risk for lower coupon bonds





## Risks of Bonds – cont'd...

---

- Reinvestment Rate Risk

Greater for short-term bonds = risk that income from bonds will fall

- Default Risk

Measured by bond ratings = ability of issuer to fulfill debt obligations  
(see table 8-1 in the text)

**Ex) AAA, best rating, lowest default risk**



## Evaluating default risk: Bond ratings

---

	Investment Grade				Junk Bonds			
<b>Moody's</b>	Aaa	Aa	A	Baa	Ba	B	Caa	C
<b>S &amp; P</b>	AAA	AA	A	BBB	BB	B	CCC	D

- Bond ratings are designed to reflect the probability of a bond issue going into default.



# Stocks and Their Valuation

---



## Facts about Common Stock

---

- Claim on income after interest and dividend payments to the creditors and preferred stock holders
- Represents ownership and Ownership implies control
- Shareholders get cash flow rights and control rights
- Limited liability



## Advantages of Financing with Stock

---

- No required fixed payments
- No maturity
- No default, no repayment to investors



## Disadvantages of Financing with Stock

---

- Controlling shareholders may lose some control (Dilution of ownership)
- Future earnings shared with new stockholders.  
=>Possible EPS Dilution
- Higher flotation costs vs. debt
- Higher component cost of capital
- Too little debt may encourage a takeover bid



## Intrinsic Value and Stock Price

---

- Outside investors, corporate insiders, and analysts use a variety of approaches to estimate a stock's intrinsic value ( $P_0$ ).
- In equilibrium we assume that a stock price equals its intrinsic value.
  - Outsiders estimate intrinsic value to help determine which stocks are attractive to buy and/or sell.
  - Stocks with a price below (above) its intrinsic value are *undervalued* (*overvalued*) by the market.



## Different approaches for estimating the intrinsic value of a common stock

---

- Dividend growth model
- Corporate value model
- Using the multiples of comparable firms





# Stock Valuation

---

Stock value = PV of Dividends

$$\hat{P}_0 = \frac{D_1}{(1+k_s)^1} + \frac{D_2}{(1+k_s)^2} + \frac{D_3}{(1+k_s)^3} + \dots + \frac{D_\infty}{(1+k_s)^\infty}$$

For Valuation: we will assume stocks fall into one of the following dividend growth patterns.

- Constant growth rate in dividends
- Zero growth rate in dividends
- “Supernormal” (non-constant) growth rate in dividends



## Constant Growth Stock Valuation Model

---

$$D_1 = D_0(1 + g)^1$$

$$D_2 = D_0(1 + g)^2$$

$$D_t = D_0(1 + g)^t$$

If  $g$  is constant, then

$$\hat{P}_0 = \frac{D_0(1 + g)}{k_s - g} = \frac{D_1}{k_s - g}$$

,where

$D_0$  = today's (or current) dividend

$D_1$  = expected dividend at the end of this year (year1)

$K_s$  = stocks' required rate of return

$g$  = the constant growth rate in dividends



## Example

---

ABC Inc. currently pays a dividend of \$3 per share, and this dividend is expected to grow at a constant annual rate of 8% forever. ABC's stock has a beta of 1.6, the risk-free rate is 5%, and the market risk premium is 9%. What is the most a well-diversified investor would be willing to pay for a share of ABC Inc.?



## Example – cont'd...

---

- Solution

$D_0 = \$3$ ,  $g = 8\%$  or  $0.08$ ,  $D_1 = \$3(1.08) = \$3.24$ , need  $k_s$

Can find required return from

$$\hat{P}_0 =$$



## Expected Return of Constant Growth Stocks

---

Expected rate of return = Expected dividend yield + Expected Capital Gains Yield

$D_1/P_0$  = Expected Dividend Yield

$g$  = Expected Capital Gains Yield

From our example,  $D_1 = \$3.24$ ,  $P_0 = \$28.42$ ,  $g = 8\%$

$\hat{k}_s =$



## Expected Return of Constant Growth Stocks -cont'd..

---

*What happens if  $g > k_s$  ?*

We can't use model unless (1)  $k_s > g$  and (2)  $g$  is expected to be constant forever.



## Zero Growth Stock Valuation

---

Just a special case of constant growth valuation,  $g = 0$

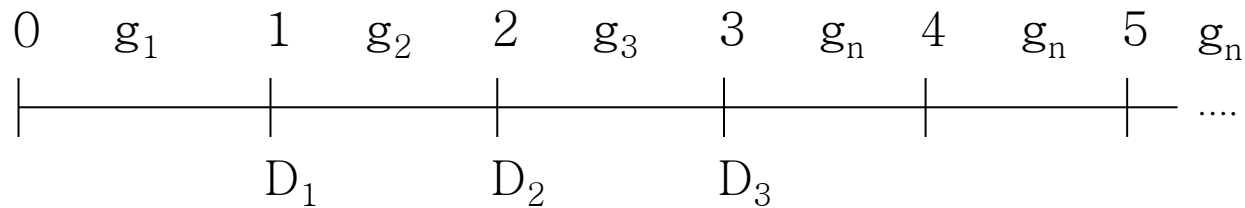
$$P = D/k_s, \text{ and } k_s = D/P$$



## “Supernormal” Growth Stock Valuation

---

- Framework: Assume Stock has period of non-constant growth in dividends and earnings and then eventually settles into a normal constant growth pattern ( $g_n$ )







## “Supernormal” Growth Stock Valuation – cont’d...

---

- ***Supernormal Growth Valuation Process*** ( 3 Step Process )

Step 1: Estimate dividends during “supernormal” growth period

Step 2: Estimate price, which is the PV of the constant growth dividends, at the end of “supernormal” growth period which is also the beginning of the constant growth period.

Step 3: Find the PV of “supernormal” dividends and constant growth price. The total of these PVs = Today’s estimated stock value.



## Example

---

Webscape Software currently pays no dividends. Webscape plans to pay a \$1 per share dividend a year from today. Analysts predict that Webscape's dividends and earnings per share will grow by 30% in year 2, and 50% in year 3. After year three, analysts predict that Webscape's dividends and earnings will grow at a constant 10% annual rate forever. What is the value of Webscape's stock if the stock's required return is 20%?

### ■ Solution

$$D_1 = \$1, g_2 = 30\% \text{ or } 0.3, g_3 = 50\% \text{ or } 0.5, g_n = 10\% \text{ or } 0.1, k_s = 20\% \text{ or } 0.2$$



## Example – cont’d...

---

Find “Supernormal” Dividends:

$$D_1 =$$

$$D_2 =$$

$$D_3 =$$

Need to find  $P_3$  : Recall  $g_n = 10\%$ ,  $k_s = 20\%$

$$P_3 =$$

Now, we need to find the PV of the supernormal dividends and PV of  $P_3$  at the required rate of return.

The sum of these PVs will be the today’s value of the stock.



## Preferred Stock Characteristics

---

- Unlike common stock, no ownership interest
- Second to debt holders on claim on company's assets in the event of bankruptcy
- Like bonds, preferred stockholders receive a fixed dividend that must be paid before dividends are paid to common stockholders.
- Annual dividend yield as a percentage of par value
- Preferred dividends must be paid before common dividends



## Preferred Stock Valuation

---

- Promises to pay the same dividend year after year forever, never matures.
- A perpetuity
- $V_{ps} = D/k_{ps}$



## Preferred Stock Valuation – cont'd...

---

- Example: GM preferred stock has a \$25 par value with a 8% dividend yield. What price would you pay if your required return is 9%?

$D =$

$V_{ps} =$



## Expected Return on Preferred Stock

---

Just adjust the valuation model:

$$\bar{k}_{ps} = \frac{D}{P_0}$$

Example:

If we know the preferred stock price is \$40, and the preferred dividend is \$4.125, the expected return is:



## Corporate value model

---

- Also called the free cash flow method. Suggests the value of the entire firm equals the present value of the firm's free cash flows.
- Remember, free cash flow is the firm's after-tax operating income less the net capital investment
  - $FCF = NOPAT - \text{Net capital investment}$





## Applying the corporate value model

---

- Find the value of the firm, by finding the PV of the firm's future FCFs.
- Subtract the value of firm's debt and preferred stock to get the value of common stock.
- Divide the value of common stock by the number of shares outstanding to get intrinsic stock price.

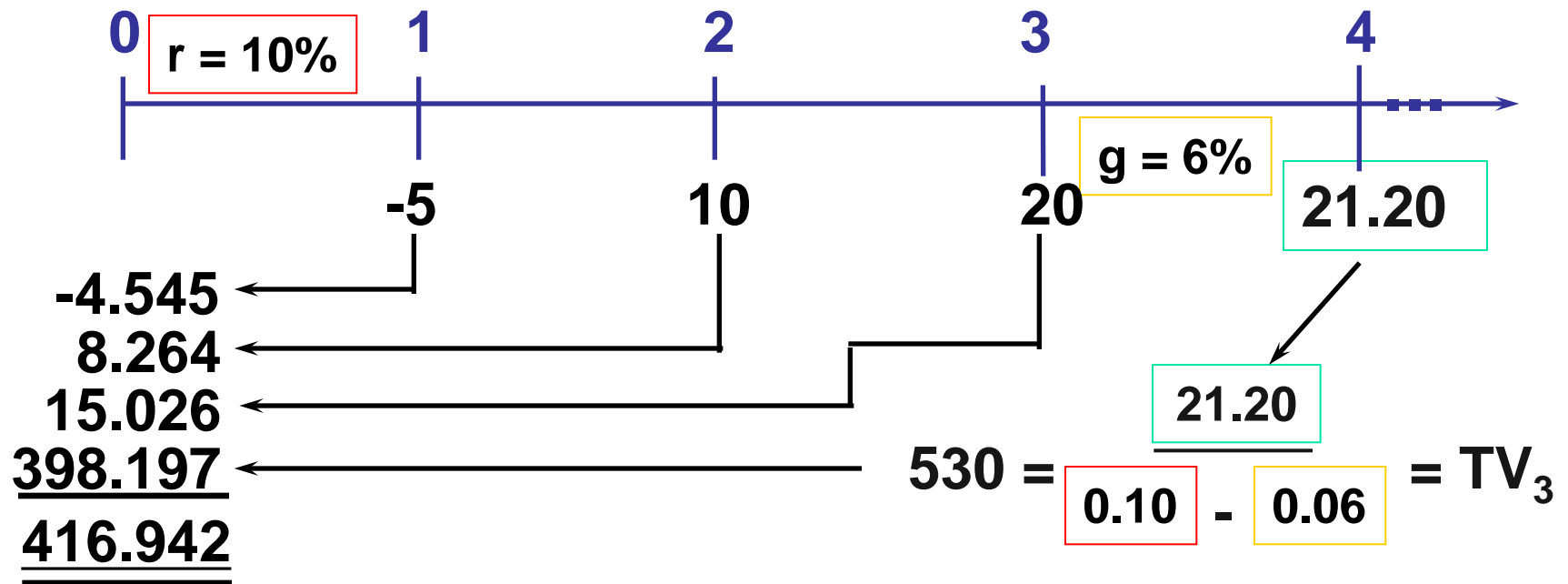


## Issues regarding the corporate value model

---

- Often preferred to the dividend growth model, especially when considering number of firms that don't pay dividends or when dividends are hard to forecast.
- Similar to dividend growth model, assumes at some point free cash flow will grow at a constant rate.
- Terminal value ( $TV_N$ ) represents value of firm at the point that growth becomes constant.

Given the long-run  $g_{\text{FCF}} = 6\%$ , and  $r = 10\%$ , use the corporate value model to find the firm's intrinsic value.





If the firm has \$40 million in debt and has 10 million shares of stock, what is the firm's intrinsic value per share?

---

- Value of equity = value of firm – value of debt
$$= \$416.94 - \$40$$
$$= \$376.94 \text{ million}$$
- Value per share = value of equity / # of shares
$$= \$376.94 / 10$$
$$= \$37.69$$



## Firm multiples method

---

- Analysts often use the following multiples to value stocks.
  - $P / E$
  - $P / CF$
  - $P / \text{Sales}$
- **EXAMPLE:** Based on comparable firms, estimate the appropriate  $P/E$ . Multiply this by expected earnings to back out an estimate of the stock price.



## What is market equilibrium?

---

- In equilibrium, stock prices are stable and there is no general tendency for people to buy versus to sell.
- In equilibrium, two conditions hold:
  - The current market stock price equals its intrinsic value ( $P_0 = P_0$ ).
  - Expected returns must equal required returns.

$$\hat{r}_s = \frac{D_1}{P_0} + g = \hat{r}_s = r_{RF} + (r_M - r_{RF})b$$



## Market equilibrium

---

- Expected returns are determined by estimating dividends and expected capital gains.
- Required returns are determined by estimating risk and applying the CAPM.



## How is market equilibrium established?

---

- If price is below intrinsic value ...
  - The current price ( $P_0$ ) is “too low” and offers a bargain.
  - Buy orders will be greater than sell orders.
  - $P_0$  will be bid up until expected return equals required return.





## What is a bond?

---

- A long-term debt instrument in which a borrower agrees to make payments of principal and interest, on specific dates, to the holders of the bond.



## Bond Characteristics

---

- Par Value = Stated face value that is the amount the issuer must repay
- Coupon Interest Rate
- $\text{Coupon} = \text{Coupon Rate} * \text{Par Value}$
- Maturity Date = when the par value is repaid
- Call provisions = right of issuer to repay (buy back) the bond before maturity (call premium)
- Sinking Funds = mechanism for retirement of bond issue
- Other Features: Convertible Bonds



## Bond markets

---

- Primarily traded in the over-the-counter (OTC) market.
- Most bonds are owned by and traded among large financial institutions.
- Full information on bond trades in the OTC market is not published.



# Bond Valuation

---

Time Line,

$$V_B = \text{INT}(\text{PVIFA}_{k_d, N}) + M(\text{PVIF}_{k_d, N})$$

INT = \$ coupon interest,  $k_d$  = required return

N = # of years until maturity

M = Par value of the bond, usually \$1,000



## Bond Valuation – Example 1

---

$M = \$1,000$  par value,  $INT = \$80$  annual coupon,  $k_d = 10\%$ ,  $N = 12$  years

$$V_B =$$

Let's play with this example.

What is the new bond value if the required return changes to 8%?

$$V_B =$$

What if  $k_d = 6\%$ ?

$$V_B =$$



## Some Key Relationships from Example 1

---

The coupon rate was  $\$80/\$1000$  or 8%

When required rate = coupon rate

Par value (M)

Bond value

When required rate > coupon rate

Par value (M)

Bond value

When required rate < coupon rate

Par value (M)

Bond value



## Bond Value Changes over Time

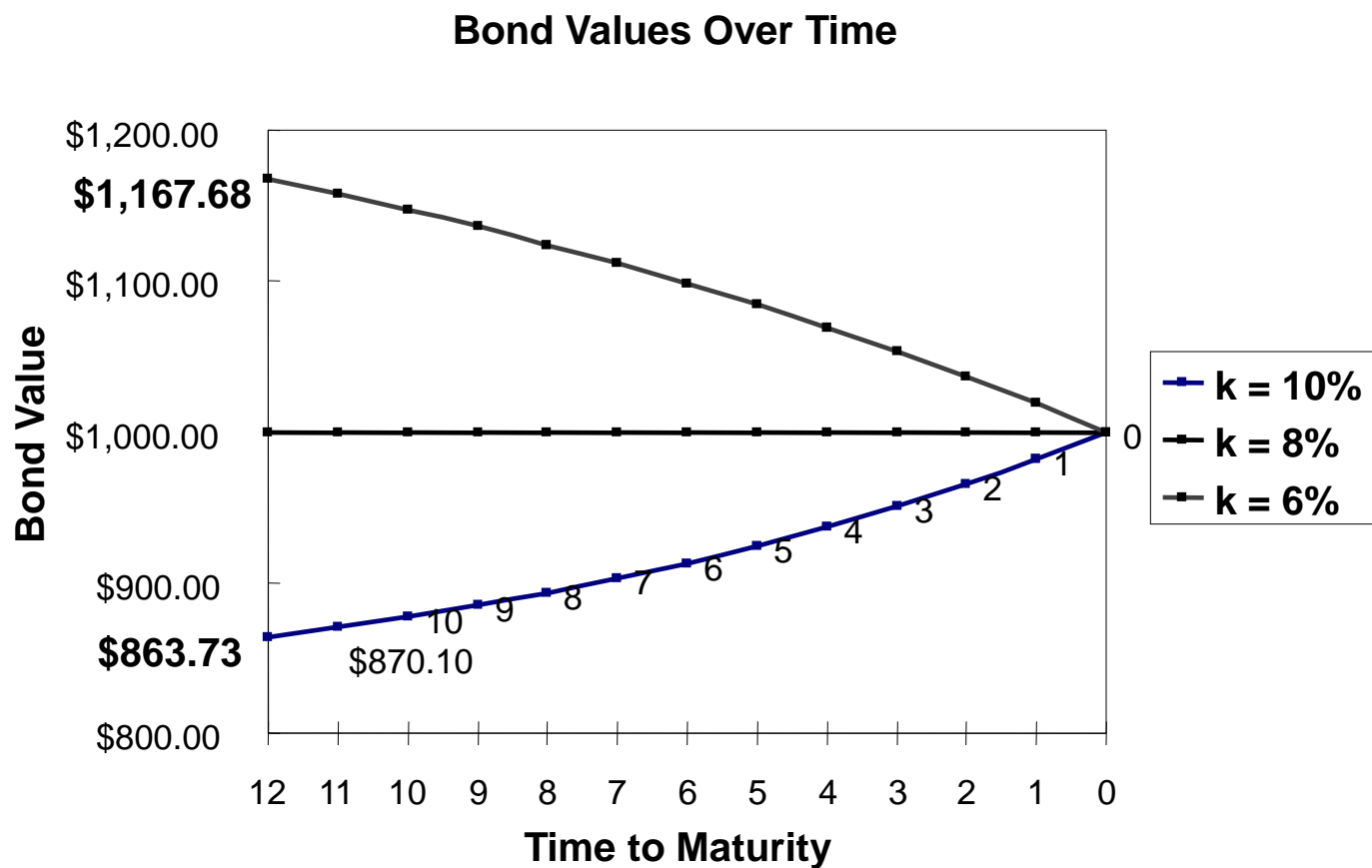
---

Returning to the original example #1, where  $k_d = 10\%$ ,  $N = 12$ ,  $\text{INT(PMT)} = \$80$ ,  $M(\text{FV}) = \$1,000$ , and  $V_B = \$863.73$

What is bond value one year later when  $N = 11$  and  $k_d$  is still  $= 10\%$ ?

$V_B =$

# Bond Values Over Time







## What is the bond's return over this year?

---

Total Rate of Return = Current Yield + Capital Gains Yield

Beg. Bond Value (Purchase price) = 863.73

End. Bond Value (Sale price) = 870.10

Current Yield = Annual Coupon (INT)/ Beg. Bond Value (or Purchase Price)

C.Y =

C.G.Y =

Total Return =



## Finding a bond's expected rate of return?

---

In the marketplace, we know a bond's current price (PV), but not its return.

Yield to Maturity (YTM) = the rate of return the bond would earn if purchased at today's price and held until maturity

Yield to Call (YTC) = the rate of return the bond would earn if purchased at today's price and held until could be called



## Finding a bond's expected rate of return? – cont'd..

---

- Yield to Maturity Example:

\$1000 face value bond with a 10% coupon rate paid annually with 20 years left to maturity sells for \$1091.29

What is this bond's YTM?

YTM =



## Bonds with Semiannual Coupons

---

Double the number of years, and divide required return and annual coupon by 2.

$$V_B = (\text{INT}/2)(\text{PVIFA}_{k_d/2, 2N}) + M(\text{PVIF}_{k_d/2, 2N})$$

### ■ Semiannual Example:

A \$1000 par value bond with an annual coupon rate of 9% pays coupon semiannually with 15 years left to maturity. What is the most you would be willing to pay for this bond if your required return is 8% APR?

$V_B =$



## Risks of Bonds

---

Let's suppose we have 5 different bonds. Assume that required rates of return on those bonds are all  $k\%$ , and par values are all \$1,000

Bond1: 10-yr, 10% annual coupon

$$V_B = \$100(PVIFA_{k,10}) + \$1000(PVIF_{k,10})$$

Bond2-4: zero coupon bonds, bond2 with  $N=10$ , bond 3 with  $N=5$ , bond4 with  $N=30$

$$V_B = \$1000(PVIF_{k,N})$$

Bond 5: \$100 Perpetuity

$$V_B = PMT/k = \$100/k$$



## Risks of Bonds – cont'd...

---

- Interest Rate Risk

Bond	K = 7%	K = 8%	% Change
10-yr, 10% annual coupon	\$1210.71	\$1134.20	-6.32%
10-yr zero coupon	\$508.35	\$463.19	-8.88%
5-yr zero coupon	\$712.99	\$680.58	-4.55%
30-yr zero coupon	\$131.37	\$99.38	-24.35%
\$100 perpetuity	\$1428.57	\$1250.00	-12.50%



## Risks of Bonds – cont'd...

---

Comparing Bonds 1 and 5 shows longer term bonds have greater bond price changes = More interest rate risk

Comparing Bonds 2, 3, and 4 also confirms that

Comparing the two 10-yr (1 & 2), the zero had the greater price change = More interest rate risk for lower coupon bonds



## Risks of Bonds – cont'd...

---

- Reinvestment Rate Risk

Greater for short-term bonds = risk that income from bonds will fall

- Default Risk

Measured by bond ratings = ability of issuer to fulfill debt obligations  
(see table 8-1 in the text)

**Ex) AAA, best rating, lowest default risk**





## Evaluating default risk: Bond ratings

---

	Investment Grade				Junk Bonds			
<b>Moody's</b>	Aaa	Aa	A	Baa	Ba	B	Caa	C
<b>S &amp; P</b>	AAA	AA	A	BBB	BB	B	CCC	D

- Bond ratings are designed to reflect the probability of a bond issue going into default.



# Stocks and Their Valuation

---



## Facts about Common Stock

---

- Claim on income after interest and dividend payments to the creditors and preferred stock holders
- Represents ownership and Ownership implies control
- Limited liability
- Stockholders elect directors = voting rights
- Directors elect management
- Management's goal: Maximize shareholders' wealth (= Maximize stock price)



## Advantages of Financing with Stock

---

- No required fixed payments
- No maturity
- Improves capital structure



## Disadvantages of Financing with Stock

---

- Controlling shareholders may lose some control
- Future earnings shared with new stockholders.  
=>Possible EPS Dilution
- Higher flotation costs vs. debt
- Higher component cost of capital
- Too little debt may encourage a takeover bid



## Intrinsic Value and Stock Price

---

- Outside investors, corporate insiders, and analysts use a variety of approaches to estimate a stock's intrinsic value ( $P_0$ ).
- In equilibrium we assume that a stock's price equals its intrinsic value.
  - Outsiders estimate intrinsic value to help determine which stocks are attractive to buy and/or sell.
  - Stocks with a price below (above) its intrinsic value are *undervalued* (*overvalued*) by the market.



## Different approaches for estimating the intrinsic value of a common stock

---

- Dividend growth model
- Corporate value model
- Using the multiples of comparable firms



# Stock Valuation

---

Stock value = PV of Dividends

$$\hat{P}_0 = \frac{D_1}{(1+k_s)^1} + \frac{D_2}{(1+k_s)^2} + \frac{D_3}{(1+k_s)^3} + \dots + \frac{D_\infty}{(1+k_s)^\infty}$$

For Valuation: we will assume stocks fall into one of the following dividend growth patterns.

- Constant growth rate in dividends
- Zero growth rate in dividends
- “Supernormal” (non-constant) growth rate in dividends





## Constant Growth Stock Valuation Model

---

$$D_1 = D_0(1 + g)^1$$

$$D_2 = D_0(1 + g)^2$$

$$D_t = D_{t-1}(1 + g)^t$$

If  $g$  is constant, then

$$\hat{P}_0 = \frac{D_0(1 + g)}{k_s - g} = \frac{D_1}{k_s - g}$$

,where

$D_0$  = today's (or current) dividend

$D_1$  = expected dividend at the end of this year (year1)

$K_s$  = stocks' required rate of return

$g$  = the constant growth rate in dividends



## Example

---

ABC Inc. currently pays a dividend of \$3 per share, and this dividend is expected to grow at a constant annual rate of 8% forever. ABC's stock has a beta of 1.6, the risk-free rate is 5%, and the market risk premium is 9%. What is the most a well-diversified investor would be willing to pay for a share of ABC Inc.?



## Example – cont'd...

---

- Solution

$D_0 = \$3$ ,  $g = 8\%$  or  $0.08$ ,  $D_1 = \$3(1.08) = \$3.24$ , need  $k_s$

Can find required return from

$$\hat{P}_0 =$$



## Expected Return of Constant Growth Stocks

---

Expected rate of return = Expected dividend yield + Expected Capital Gains Yield

$D_1/P_0$  = Expected Dividend Yield

$g$  = Expected Capital Gains Yield

From our example,  $D_1 = \$3.24$ ,  $P_0 = \$28.42$ ,  $g = 8\%$

$\hat{k}_s =$



## Expected Return of Constant Growth Stocks -cont'd..

---

*What happens if  $g > k_s$  ?*

We can't use model unless (1)  $k_s > g$  and (2)  $g$  is expected to be constant forever.



## Zero Growth Stock Valuation

---

Just a special case of constant growth valuation,  $g = 0$

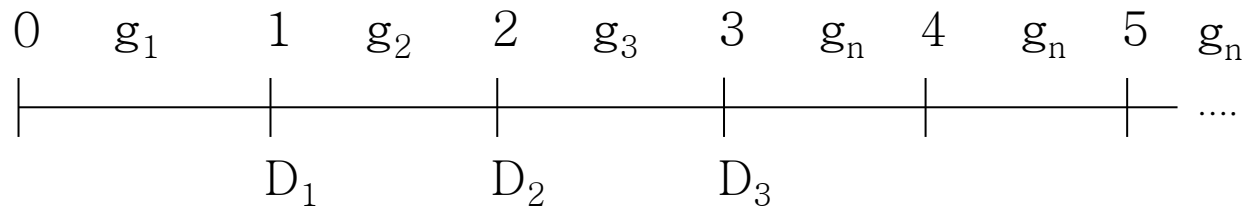
$$P = D/k_s, \text{ and } k_s = D/P$$



## “Supernormal” Growth Stock Valuation

---

- Framework: Assume Stock has period of non-constant growth in dividends and earnings and then eventually settles into a normal constant growth pattern ( $g_n$ )





## “Supernormal” Growth Stock Valuation – cont’d...

---

- ***Supernormal Growth Valuation Process*** ( 3 Step Process )

Step 1: Estimate dividends during “supernormal” growth period

Step 2: Estimate price, which is the PV of the constant growth dividends, at the end of “supernormal” growth period which is also the beginning of the constant growth period.

Step 3: Find the PV of “supernormal” dividends and constant growth price. The total of these PVs = Today’s estimated stock value.





## Example

---

Webscape Software currently pays no dividends. Webscape plans to pay a \$1 per share dividend a year from today. Analysts predict that Webscape's dividends and earnings per share will grow by 30% in year 2, and 50% in year 3. After year three, analysts predict that Webscape's dividends and earnings will grow at a constant 10% annual rate forever. What is the value of Webscape's stock if the stock's required return is 20%?

### ■ Solution

$$D_1 = \$1, g_2 = 30\% \text{ or } 0.3, g_3 = 50\% \text{ or } 0.5, g_n = 10\% \text{ or } 0.1, k_s = 20\% \text{ or } 0.2$$



## Example – cont’d...

---

Find “Supernormal” Dividends:

$$D_1 =$$

$$D_2 =$$

$$D_3 =$$

Need to find  $P_3$  : Recall  $g_n = 10\%$ ,  $k_s = 20\%$

$$P_3 =$$

Now, we need to find the PV of the supernormal dividends and PV of  $P_3$  at the required rate of return.

The sum of these PVs will be the today’s value of the stock.



## Preferred Stock Characteristics

---

- Unlike common stock, no ownership interest
- Second to debt holders on claim on company's assets in the event of bankruptcy
- Like bonds, preferred stockholders receive a fixed dividend that must be paid before dividends are paid to common stockholders.
- Annual dividend yield as a percentage of par value
- Preferred dividends must be paid before common dividends
- If cumulative preferred, all missed past dividends must be paid before common dividends can be paid



## Preferred Stock Valuation

---

- Promises to pay the same dividend year after year forever, never matures.
- A perpetuity
- $V_{ps} = D/k_{ps}$



## Preferred Stock Valuation – cont'd...

---

- Example: GM preferred stock has a \$25 par value with a 8% dividend yield. What price would you pay if your required return is 9%?

$D =$

$V_{ps} =$



## Expected Return on Preferred Stock

---

Just adjust the valuation model:

$$\bar{k}_{ps} = \frac{D}{P_0}$$

Example:

If we know the preferred stock price is \$40, and the preferred dividend is \$4.125, the expected return is:



## Corporate value model

---

- Also called the free cash flow method. Suggests the value of the entire firm equals the present value of the firm's free cash flows.
- Remember, free cash flow is the firm's after-tax operating income less the net capital investment
  - $FCF = NOPAT - \text{Net capital investment}$



## Applying the corporate value model

---

- Find the value of the firm, by finding the PV of the firm's future FCFs.
- Subtract the value of firm's debt and preferred stock to get the value of common stock.
- Divide the value of common stock by the number of shares outstanding to get intrinsic stock price.



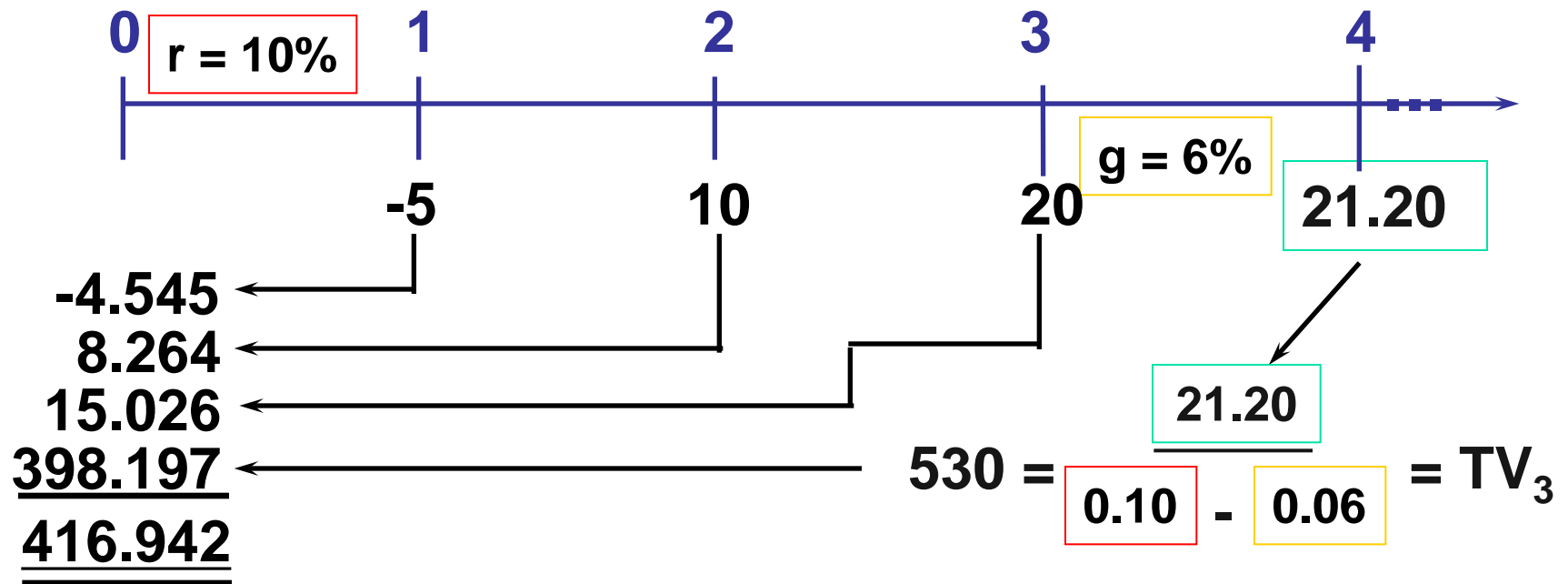


## Issues regarding the corporate value model

---

- Often preferred to the dividend growth model, especially when considering number of firms that don't pay dividends or when dividends are hard to forecast.
- Similar to dividend growth model, assumes at some point free cash flow will grow at a constant rate.
- Terminal value ( $TV_N$ ) represents value of firm at the point that growth becomes constant.

Given the long-run  $g_{\text{FCF}} = 6\%$ , and  $r = 10\%$ , use the corporate value model to find the firm's intrinsic value.





If the firm has \$40 million in debt and has 10 million shares of stock, what is the firm's intrinsic value per share?

---

- Value of equity = value of firm – value of debt
$$= \$416.94 - \$40$$
$$= \$376.94 \text{ million}$$
- Value per share = value of equity / # of shares
$$= \$376.94 / 10$$
$$= \$37.69$$



## Firm multiples method

---

- Analysts often use the following multiples to value stocks.
  - $P / E$
  - $P / CF$
  - $P / \text{Sales}$
- **EXAMPLE:** Based on comparable firms, estimate the appropriate  $P/E$ . Multiply this by expected earnings to back out an estimate of the stock price.



## What is market equilibrium?

---

- In equilibrium, stock prices are stable and there is no general tendency for people to buy versus to sell.
- In equilibrium, two conditions hold:
  - The current market stock price equals its intrinsic value ( $P_0 = P_0$ ).
  - Expected returns must equal required returns.

$$\hat{r}_s = \frac{D_1}{P_0} + g = \hat{r}_s = r_{RF} + (r_M - r_{RF})b$$



## Market equilibrium

---

- Expected returns are determined by estimating dividends and expected capital gains.
- Required returns are determined by estimating risk and applying the CAPM.



## How is market equilibrium established?

---

- If price is below intrinsic value ...
  - The current price ( $P_0$ ) is “too low” and offers a bargain.
  - Buy orders will be greater than sell orders.
  - $P_0$  will be bid up until expected return equals required return.