## CS 532: Homework Assignment 3

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## 1 Harris corner detection and matching

First, I computed the images derivatives using convolution, which is a fast function in Matlab. Second, I calculated the kernel of the gaussian smoothing using standard deviation equals to 1.5 for this distribution then I aplied this kernel to  $I_x^2$ ,  $I_y^2$  and  $I_{xy}$  also using convolution. Now I had everything I needed to apply the Harris operator in each pixel of both images calculating the ration determinant(H)/trace(H). Then I selected the corners that have ratio > 120k. After that, I used non-maximum suppresion in 3x3 windows and ended up with 314 corners in left image and 376 in the right one. Then I computed the distances between corners in left image to the ones in the right image using SAD. I got a little confused in this part because the in the next step we were supposed to compare these values with the disparities in groundtruth. So I computed the distances with respect to the intensities in 3x3 windows, but I kept track of the estimated disparity of correspondences in epipolar lines, so I could compare these values with groundtruth. Finally, bellow are the correct and wrong correspondences report.

## 2 Errors report

 $\bullet~5\%$  most likely correspondences

Correct: 65 Wrong: 5839

• 10% most likely correspondences

Correct: 116 Wrong: 11691

• 15% most likely correspondences

Correct: 155 Wrong: 17555

• 20% most likely correspondences

Correct: 203 Wrong: 23410

• 25% most likely correspondences

Correct: 241 Wrong: 29275  $\bullet~30\%$  most likely correspondences

Correct: 278 Wrong: 35142

• 35% most likely correspondences

Correct: 320 Wrong: 41003

• 40% most likely correspondences

Correct: 361 Wrong: 46865

• 45% most likely correspondences

Correct: 397 Wrong: 52732

• 50% most likely correspondences

Correct: 440 Wrong: 58592

 $\bullet$  55% most likely correspondences

Correct: 482 Wrong: 64454

• 60% most likely correspondences

Correct: 520 Wrong: 70319

• 65% most likely correspondences

Correct: 555 Wrong: 76187

• 70% most likely correspondences

Correct: 602 Wrong: 82043

• 75% most likely correspondences

Correct: 653 Wrong: 87895

 $\bullet~80\%$  most likely correspondences

Correct: 706 Wrong: 93746

• 85% most likely correspondences

Correct: 766 Wrong: 99589

• 90% most likely correspondences

Correct: 816 Wrong: 105442

- 95% most likely correspondences Correct: 876 Wrong: 111285
- 100% most likely correspondences Correct: 918 Wrong: 117146

## 3 Matlab code

```
clc; clear all;
lft = double(imread('teddyL.pgm'));
rgt = double(imread('teddyR.pgm'));
height = size(lft, 1);
width = size(lft, 2);
deriv = \begin{bmatrix} -1 & 0 & 1 \end{bmatrix}
          -1 \ 0 \ 1
          -1 \ 0 \ 1;
IIx = conv2(lft , deriv , 'same');
lIy = conv2(lft , deriv', 'same');
rIx = conv2(rgt , deriv , 'same');
rIy = conv2(rgt, deriv', 'same');
% Ix = zeros(size(lft));
% Iy = zeros(size(lft));
\% for i = 2:height-1
%
       for j = 2: width-1
%
            window = lft(i-1:i+1, j-1:j+1);
%
            Ix(i,j) = sum(window(:,3) - window(:,1));
%
            Iy(i,j) = sum(window(3,:) - window(1,:));
%
       end
% end
lIxy = lIx . * lIy;
rIxy = rIx.*rIy;
\%~\%~\%~mean~filter
\% win_{-}filter = 5;
\% half_-filter = (win_-filter - 1)/2;
% filtered = zeros(size(lft));
```

```
\% for i = win_filter: height-win_filter
                   for j = win_filter: width-win_filter
%
                                window = lft(i-half\_filter:i+half\_filter, j-half\_filter:j+half\_filter)
%
                                                   filtered(i,j) = uint8(sum(sum(window)))/(win_filter*win_filter));
%
                   end
% end
win_{gauss} = 5;
half_gauss = (win_gauss - 1)/2;
sig = 1.5;
[\,x\,,y\,] \;=\; \mathbf{meshgrid}(-\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alf\,\_g\,a\,u\,s\,s\,:\,h\,alg\,\_g\,a\,u\,s\,s\,:\,h\,alg\,\_g\,a\,u\,s\,s\,:\,h\,alg\,\_g\,a\,u\,s\,s\,:\,h\,a
G = \exp(-(x.^2 + y.^2)/(2*sig^2));
G = G./sum(G(:));
1Ix2g = conv2(1Ix.^2, G, 'same');
1Iy2g = conv2(1Iy.^2, G, 'same');
lIxyg = conv2(lIxy, G, 'same');
rIx2g = conv2(rIx.^2, G, 'same');
rIy2g = conv2(rIy.^2, G, 'same');
rIxyg = conv2(rIxy, G, 'same');
win_harris = 5; % Matlab default
half_harris = (win_harris - 1)/2;
thresh = 120000;
flft = zeros(size(lft));
frgt = zeros(size(rgt));
for i = half_harris+1:height-half_harris-1
             for j = half_harris+1: width-half_harris-1
                         1Sx2 = sum(sum(1Ix2g(i-half_harris:i+half_harris, j-half_harris:j+half_h
                         lSy2 = sum(sum(lIy2g(i-half_harris:i+half_harris, j-half_harris:j+half_h
                         1Sxy = sum(sum(1Ixyg(i-half_harris:i+half_harris, j-half_harris:j+half_harris)
                          flft(i,j) = (lSx2*lSy2 - lSxy*lSxy)/(lSx2+lSy2);
                         rSx2 = sum(sum(rIx2g(i-half_harris:i+half_harris, j-half_harris:j+half_h
                         rSy2 = sum(sum(rIy2g(i-half_harris:i+half_harris, j-half_harris:j+half_h
                         rSxy = sum(sum(rIxyg(i-half_harris:i+half_harris, j-half_harris:j+half_harris))
                          frgt(i,j) = (rSx2*rSy2 - rSxy*rSxy)/(rSx2+rSy2);
            end
end
flft(flft < thresh) = 0;
frgt(frgt < thresh) = 0;
```

```
cnt1 = 1;
cnt2 = 1;
half_nms = 1;
\% non max suppression, 3x3 window
for i = half_nms + 1: size(lft, 1) - half_nms - 1
    for j = half_nms + 1: size(lft, 2) - half_nms - 1
         if flft (i,j) = 0
             window = flft(i-half_nms:i+half_nms, j-half_nms:j+half_nms);
             if sum(sum(flft(i,j) < window)) == 0
                  corlft(cnt1,:) = [flft(i,j) i j];
                 cnt1 = cnt1+1;
             else
                  flft(i,j) = 0;
             end
        end
         \mathbf{if} \operatorname{frgt}(\mathbf{i},\mathbf{j}) = 0
             window = frgt(i-half_nms:i+half_nms, j-half_nms:j+half_nms);
             if sum(sum(frgt(i,j) < window)) == 0
                 corrgt(cnt2,:) = [frgt(i,j) i j];
                 cnt2 = cnt2 + 1;
             else
                  frgt(i,j) = 0;
             end
        end
    end
end
im = [lft rgt];
ff = figure;
imshow(im, [min(im(:)) max(im(:))]);
hold on; scatter(corlft(:,3), corlft(:,2), 'MarkerFaceColor', 'm');
hold on; scatter(width+corrgt(:,3), corrgt(:,2), 'MarkerFaceColor', 'g');
disp('number_of_corners:')
disp(length(corlft))
disp(length(corrgt))
cnt = 1;
half_sad = 1;
% SAD 3x3 ?????
for i = 1:length(corlft)
    for j = 1:length(corrgt)
```

```
xl = corlft(i, 2);
             yl = corlft(i,3);
             xr = corrgt(j, 2);
             yr = corrgt(j,3);
             windowl = lft(xl-half_sad:xl+half_sad, yl-half_sad:yl+half_sad);
             windowr = rgt(xr-half_sad:xr+half_sad; yr-half_sad:yr+half_sad);
             if (xl==xr)
                  aa = yl-yr; % have to save this so I can compare with groundtrut
             else
                  aa = Inf;
             distances(cnt,:) = [sum(sum(abs(windowl-windowr))) aa i j];
             cnt = cnt + 1;
    end
end
for k = 5:5:100
    n = ceil((k/100)*length(distances));
    dd = sortrows (distances);
    dd = dd (1:n,:);
    XX = [corlft(dd(:,3),2)'; corrgt(dd(:,4),2)'];
    YY = [corlft(dd(:,3),3)'; width+corrgt(dd(:,4),3)'];
    figure (ff); hold on;
    line (YY(:,1:25),XX(:,1:25), 'Color', [1 0 0]);
    \mathbf{gt} = \operatorname{imread}('\operatorname{disp}2.\operatorname{pgm}');
    gt = ceil(double(gt)./4);
    correct = 0;
    for i = 1:length(dd)
         d = dd(i, 4);
         dgt = gt(corlft(dd(i,3),2), corlft(dd(i,3),3));
         if abs(d-dgt) \ll 1
             correct = correct + 1;
         end
    end
    % disp('error rate:');
    \% \ disp([1 - correct/length(dd)]);
    % disp('correct/wrong correspondences: ')
    \% \ disp(\lceil correct \ length(dd) - correct \rceil)
```

 $\mathbf{end}$