Supplementary Materials for The Effect of Recycled Individuals in the Jolly-Seber Tag Loss Model

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Web Appendix A: The Jolly-Seber Tag Loss Model

Assumptions

Assumptions of the JSTL model with constant survival, capture, and tag retention probabilities and time-varying entry probabilities are as follows:

- The effect of recycled individuals is negligible
- All individuals (marked and unmarked) are equally catchable, and that capture probabilities for all individuals are the same for all individuals at all sample time
- All individuals (marked and unmarked) have equal survival probabilities between all sample times
- All individuals have equal entry (birth or immigration) probabilities, but entry probabilities can vary between sample times
- All marked individuals have equal tag retention probabilities between all sample times
- For double-tagged individuals, tag loss is independent between tags
- There is independence across all individuals
- The sampling period is relatively short compared to the interval between sampling times

Notation

The following is a description of statistics and parameters used in the JSTL model where survival, capture, and tag retention probabilities are assumed to be constant across time.

Statistics:

```
number of sample times
k =
m =
            number of unique tag histories
i =
            index for a tag history, i = 0, 1, 2, ..., m. i = 0 refers to the tag history of individuals never captured
            the number of tags on individuals at sample time j, j=1,2,...,k.
nt_i =
            total individuals captured at time j
            the total number of individuals captured with no tags and treated as new individuals; when no
n_{\rm obs} =
            recycling is present, n_{\rm obs} is the number of unique individuals observed throughout the study
f_i = l_i = l_i
            the first sample time where the individual with tag history i was captured
            the last sample time where the individual with tag history i was observed
            first sample time where tag d was known missing for the individual with capture history i
l_{id} =
            the last sample time where tag d is present on the individual with tag history i, d = 1, 2 for a
            double-tagging experiment
\omega_i * =
            capture history vector \omega_i * = (\omega_{i1} *, \omega_{i2} *, ..., \omega_{ik} *), i=0,1,...,m, where
                          1 if the individual with tag history i captured for the first time at sample time j.
            \omega_{ij}* = \begin{cases} 1 & \text{if the individual with tag instery } i \text{ captured at sample time } j. \\ 1 & \text{if the individual with tag history } i \text{ captured at sample time } f_i < j \text{ with at least one tag present.} \\ 0 & \text{if the individual with tag history } i \text{ not captured at sample time } j. \end{cases}
            tag history vector \omega_i = (\omega_{i,1,1}, \omega_{i,1,2}, \omega_{i,2,1}, \omega_{i,2,2}, ..., \omega_{i,k,1}, \omega_{i,k,2}), i=0,1,...,m, where
            \omega_{ijd}* = \begin{cases} 1 & \text{if the individual with tag history } i \text{ captured and tag } d \text{ was present at sample time } j. \\ 0 & \text{if the individual with tag history } i \text{ captured and tag } d \text{ was not present at sample time } j. \\ 0 & \text{if the individual with tag history } i \text{ not captured at sample time } j. \end{cases}
            number of \omega_i tag histories
n_{\omega_i}
          the probability that an individual is recaptured at a sample time given that the individual was alive
          at the previous sample time
          the probability that an individual survives and remain in the population between a sample time
          and the next sample time
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the probability that an individual enters the system between sample times j and j + 1. j = 0, 1, ..., k - 1. $b_i =$ b_0 is the expected fraction of individuals alive just prior to the first sample time.

the probability that an individual captured will be lost on capture

the probability that an individual is marked with d tags. Note that the probability of marking with a single tag is one minus the probability of marking with a double tag: $T_1 = 1 - T_2$

 $\lambda =$ the probability that an individual captured will retain its tag between time periods given that it remains alive

N =super-population size, the total number of individuals ever present in population and available for capture during the study

Functions of Parameters:

the expected fraction of the population remaining to enter the population that enters between $b_i * =$ sample times j and j + 1, j = 0, 1, ..., k - 1.

sample times
$$j$$
 and $j + 1$, $j = 0, 1, ..., k - 1$

$$b_{j}* = \begin{cases} b_{0} & \text{if } j = 0 \\ b_{j} / \sum_{u=j}^{k-1} b_{u} & \text{if } j = 1, ..., k - 1 \\ 1 & \text{if } j = k - 1 \end{cases}$$
net births: the number of individuals wh

net births; the number of individuals who enter the population after sample time i and survive $B_i =$ to sample time j+1; j=0,1,...,k-1. B_0 is the number of individuals alive just before the first sample time. Note that $E(B_j|N) = Nb_j$.

the probability that the individual with capture history i is first seen at f_i and not seen after $\chi_{(f_i,l_i,nt)} =$ sample time l_i , with nt tags. This is a recursive function of ϕ , p, and λ . If $f_i = 0$, this indicates individuals not yet captured but alive at time l_i .

For individuals not yet captured:
$$\chi_{(0,j,0)} = \begin{cases} 1 - \phi + \phi(1-p)\chi_{(0,j+1,0)} & \text{if } j < k \\ 1 & \text{if } j = k \end{cases}$$

For single tagged individuals:

$$\chi_{(f_i,j,1)} = \begin{cases} 1 - \phi + \phi(1-p)\lambda\chi_{(f_i,j+1,1)} + \phi(1-\lambda) & \text{if } j < k \\ 1 & \text{if } j = k \end{cases}$$

For single tagged individuals:
$$\chi_{(f_i,j,1)} = \begin{cases} 1-\phi+\phi(1-p)\lambda\chi_{(f_i,j+1,1)}+\phi(1-\lambda) & \text{if } j < k \\ 1 & \text{if } j = k \end{cases}$$
 For double tagged individuals:
$$\chi_{(f_i,j,2)} = \begin{cases} 1-\phi+\phi(1-p)\lambda^2\chi_{(f_i,j+1,2)}+\phi(1-\lambda)^2+2\phi(1-p)\lambda(1-\lambda)\chi_{(f_i,j+1,1)} & \text{if } j < k \\ 1 & \text{if } j = k \end{cases}$$

probability that an individual enters the population, is still alive and is not seen before time j; $\psi_j =$ j = 1, 2, ..., k

population size at time j. $E(N_1|N) = B_0$, $E(N_{j+1}|N) = (N_j - N_j p v)\phi + B_j$, which is the $N_j =$ number of individuals that survive from time j minus the number lost on capture plus the number of births.

Likelihood and Estimation

The likelihood of the JSTL model can be divided into three parts: the probability of observing n_{obs} , the number of tag histories, given the super-population size (L_1^A) , the probability of observing recaptures given the number of tag histories (L_1^B) , and the probability of observing the number of individuals lost on capture $(L_3).$

The probability of observing $n_{\rm obs}$ capture histories is given by a binomial distribution conditional on the super-population size.

$$L_1^A = [n_{\text{obs}}|N] \sim \text{Binomial}(N, 1 - P_0), \text{ where}$$

$$P_0$$
 is the probability of never being seen, given by $P_0 = \sum_{j=0}^{k-1} b_j (1-p) \chi_{(0,j+1,0)}$.

The probability of observing each unique tag history ω_i is modeled by a multinomial conditional upon being observed at least once.

$$L_1^B = [n_{\omega_i} | n_{obs}] \sim \text{Multinomial}(n_{obs}, \pi_{\omega_i}), \text{ where}$$

$$\pi_{\omega_i} = P_{\omega_i}/(1 - P_0)$$
 and

$$P(\omega_i) = \psi_{f_i} T_d \left\{ \prod_{j=f_i}^{l_i} p^{w*_{ij}} (1-p)^{(1-w*_{ij})} \right\} \left\{ \phi^{l_i-1-f_i} \right\} \times \prod_{d=1}^{2} \left\{ \left(\lambda^{l_{id}-1-f_i} \right) \left(1 - \lambda^{q_{id}-1-l_{id}} \right)^{I(l_{id} \neq l_i)} \right\} \times \chi_{f_i, l_i, nt_{l_i}}$$

The third component L_3 models the number of losses on capture as a binomial. In this study we assume there is no possibility of loss on capture, this third component of the likelihood simplifies to 1.

The complete likelihood for the Jolly-Seber tag loss model assuming no possibility of loss of capture and assuming homogeneous survival, capture, and tag retention probabilities is given below.

$$L = \binom{N}{n_{\text{obs}}} \left\{ \sum_{j=0}^{k-1} b_j (1-p) \chi_{(0,j+1,0)} \right\}^{(N-n_{\text{obs}})} \times \left\{ 1 - \sum_{j=0}^{k-1} b_j (1-p) \chi_{(0,j+1,0)} \right\}^{n_{\text{obs}}} \times \left\{ 1 - \sum_{j=0}^{k-1} b_j (1-p) \chi_{(0,j+1,0)} \right\}^{n_{\text{obs}}} \times \left\{ 1 - \sum_{j=0}^{k-1} b_j (1-p) \chi_{(0,j+1,0)} \right\}^{n_{\text{obs}}} \times \left\{ 1 - \sum_{j=0}^{k-1} b_j (1-p) \chi_{(0,j+1,0)} \right\}^{n_{\text{obs}}} \times \left\{ 1 - \sum_{j=0}^{k-1} b_j (1-p) \chi_{(0,j+1,0)} \right\}^{n_{\text{obs}}} \times \left\{ 1 - \sum_{j=0}^{k-1} b_j (1-p) \chi_{(0,j+1,0)} \right\}^{-n_{\text{obs}}}$$

Recycled Individuals

Web Table 1: Examples of the fraction of recycled individuals (number of recycled individuals captured / total number of individuals captured) at each sample occasion for a 10 occasion experiment with superpopulation size N=1000 with 100% double-tagging.

	Sampling Times									
	1	2	3	4	5	6	7	8	9	10
$\phi = 0.9, p = 0.9, \lambda = 0.2$	0.00	0.30	0.36	0.47	0.51	0.53	0.54	0.55	0.56	0.57
$\phi = 0.9, p = 0.9, \lambda = 0.5$	0.00	0.12	0.12	0.20	0.29	0.26	0.29	0.30	0.31	0.31
$\phi = 0.9, p = 0.9, \lambda = 0.9$	0.00	0.01	0.02	0.02	0.01	0.01	0.03	0.04	0.04	0.03
$\phi = 0.9, p = 0.5, \lambda = 0.2$	0.00	0.14	0.28	0.38	0.43	0.48	0.54	0.54	0.55	0.56
$\phi = 0.9, p = 0.5, \lambda = 0.5$	0.00	0.02	0.12	0.14	0.27	0.28	0.28	0.33	0.29	0.38
$\phi = 0.9, p = 0.5, \lambda = 0.9$	0.00	0.00	0.00	0.00	0.01	0.02	0.02	0.04	0.06	0.06
$\phi = 0.9, p = 0.2, \lambda = 0.2$	0.00	0.05	0.15	0.35	0.18	0.28	0.30	0.33	0.40	0.37
$\phi = 0.9, p = 0.2, \lambda = 0.5$	0.00	0.00	0.06	0.09	0.14	0.13	0.20	0.21	0.30	0.26
$\phi = 0.9, p = 0.2, \lambda = 0.9$	0.00	0.00	0.00	0.00	0.00	0.01	0.02	0.02	0.04	0.03
$\phi = 0.5, p = 0.9, \lambda = 0.2$	0.00	0.18	0.23	0.27	0.34	0.36	0.32	0.32	0.32	0.26
$\phi = 0.5, p = 0.9, \lambda = 0.5$	0.00	0.10	0.10	0.15	0.10	0.15	0.18	0.13	0.19	0.12
$\phi = 0.5, p = 0.9, \lambda = 0.9$	0.00	0.00	0.00	0.01	0.01	0.00	0.01	0.01	0.01	0.01
$\phi = 0.2, p = 0.9, \lambda = 0.2$	0.00	0.10	0.14	0.07	0.15	0.10	0.11	0.13	0.13	0.12
$\phi = 0.2, p = 0.9, \lambda = 0.5$	0.00	0.02	0.06	0.05	0.05	0.11	0.04	0.06	0.08	0.09
$\phi = 0.2, p = 0.9, \lambda = 0.9$	0.00	0.01	0.00	0.01	0.00	0.00	0.00	0.00	0.00	0.00
$\phi = 0.5, p = 0.5, \lambda = 0.5$	0.00	0.01	0.07	0.06	0.12	0.13	0.14	0.16	0.13	0.14

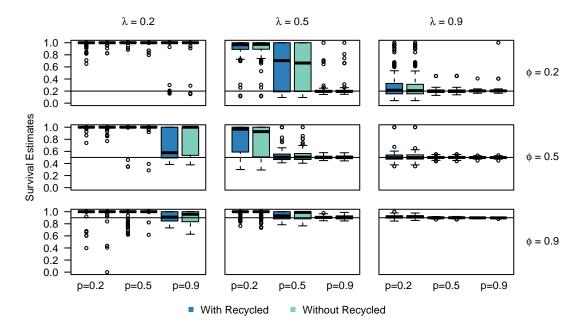
Web Table 2: Examples of the fraction of recycled individuals (number of recycled individuals captured / total number of individuals captured) at each sample occasion for a 7 occasion experiment with superpopulation size N=1000 with 100% double-tagging.

	Sampling Times								
	1	2	3	4	5	6	7		
$\phi = 0.9, p = 0.9, \lambda = 0.2$	0.00	0.32	0.40	0.49	0.50	0.53	0.55		
$\phi = 0.9, p = 0.9, \lambda = 0.5$	0.00	0.10	0.18	0.21	0.22	0.29	0.29		
$\phi = 0.9, p = 0.9, \lambda = 0.9$	0.00	0.01	0.01	0.02	0.02	0.02	0.02		
$\phi = 0.9, p = 0.5, \lambda = 0.2$	0.00	0.12	0.30	0.35	0.42	0.47	0.50		
$\phi = 0.9, p = 0.5, \lambda = 0.5$	0.00	0.06	0.15	0.22	0.26	0.24	0.27		
$\phi = 0.9, p = 0.5, \lambda = 0.9$	0.00	0.01	0.00	0.02	0.02	0.03	0.04		
$\phi = 0.9, p = 0.2, \lambda = 0.2$	0.00	0.05	0.12	0.15	0.22	0.21	0.30		
$\phi = 0.9, p = 0.2, \lambda = 0.5$	0.00	0.00	0.06	0.10	0.15	0.20	0.20		
$\phi = 0.9, p = 0.2, \lambda = 0.9$	0.00	0.00	0.00	0.00	0.00	0.01	0.01		
$\phi = 0.5, p = 0.9, \lambda = 0.2$	0.00	0.19	0.30	0.32	0.30	0.34	0.38		
$\phi = 0.5, p = 0.9, \lambda = 0.5$	0.00	0.09	0.12	0.13	0.15	0.11	0.14		
$\phi = 0.5, p = 0.9, \lambda = 0.9$	0.00	0.00	0.00	0.02	0.00	0.00	0.01		
$\phi = 0.2, p = 0.9, \lambda = 0.2$	0.00	0.10	0.11	0.12	0.13	0.16	0.08		
$\phi = 0.2, p = 0.9, \lambda = 0.5$	0.00	0.04	0.05	0.07	0.07	0.03	0.02		
$\phi = 0.2, p = 0.9, \lambda = 0.2$	0.00	0.00	0.00	0.00	0.00	0.00	0.00		
$\phi = 0.5, p = 0.5, \lambda = 0.5$	0.00	0.05	0.04	0.05	0.09	0.11	0.12		

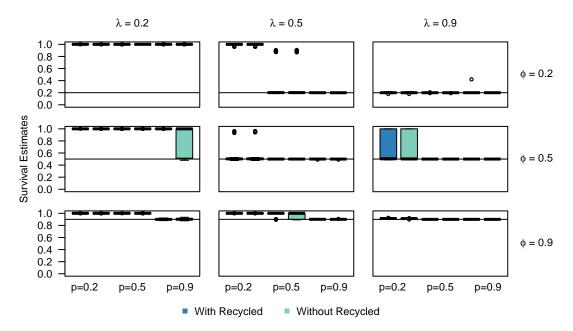
Web Table 3: Examples of the fraction of recycled individuals (number of recycled individuals captured / total number of individuals captured) at each sample occasion for a 5 occasion experiment with superpopulation size N=1000 with 100% double-tagging.

	Sampling Times							
		1 0						
	1	2	3	4	5			
$\phi = 0.9, p = 0.9, \lambda = 0.2$	0.00	0.29	0.34	0.45	0.52			
$\phi = 0.9, p = 0.9, \lambda = 0.5$	0.00	0.08	0.22	0.23	0.28			
$\phi = 0.9, p = 0.9, \lambda = 0.9$	0.00	0.01	0.01	0.02	0.02			
$\phi = 0.9, p = 0.5, \lambda = 0.2$	0.00	0.14	0.27	0.33	0.38			
$\phi = 0.9, p = 0.5, \lambda = 0.5$	0.00	0.05	0.13	0.18	0.25			
$\phi = 0.9, p = 0.5, \lambda = 0.9$	0.00	0.00	0.01	0.01	0.02			
$\phi = 0.9, p = 0.2, \lambda = 0.2$	0.00	0.06	0.15	0.16	0.29			
$\phi = 0.9, p = 0.2, \lambda = 0.5$	0.00	0.03	0.06	0.08	0.12			
$\phi = 0.9, p = 0.2, \lambda = 0.9$	0.00	0.00	0.00	0.01	0.01			
$\phi = 0.5, p = 0.9, \lambda = 0.2$	0.00	0.14	0.25	0.30	0.33			
$\phi = 0.5, p = 0.9, \lambda = 0.5$	0.00	0.05	0.13	0.10	0.15			
$\phi = 0.5, p = 0.9, \lambda = 0.9$	0.00	0.00	0.01	0.01	0.00			
$\phi = 0.2, p = 0.9, \lambda = 0.2$	0.00	0.11	0.10	0.13	0.12			
$\phi = 0.2, p = 0.9, \lambda = 0.5$	0.00	0.02	0.03	0.05	0.04			
$\phi = 0.2, p = 0.9, \lambda = 0.9$	0.00	0.00	0.00	0.00	0.00			
$\phi = 0.5, p = 0.5, \lambda = 0.5$	0.00	0.03	0.09	0.10	0.12			

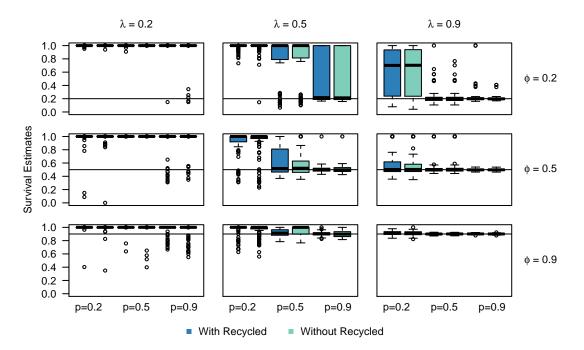
Survival Estimates



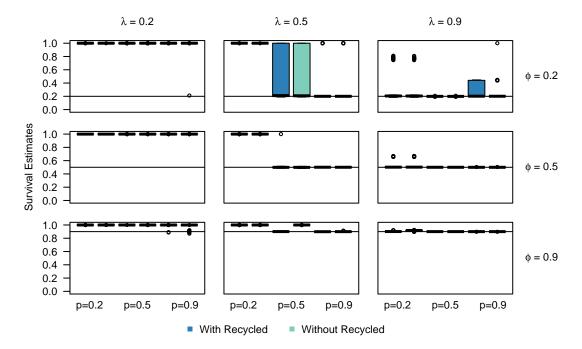
WEB FIGURE 1: Boxplots of survival estimates $(\hat{\phi})$ of 100 simulated datasets analyzed with and without the effect of recycled individuals for population size 1000 with $T_2 = 1$ with 10 time periods for varying survival $(\phi = 0.2, 0.5, 0.9)$, capture (p = 0.2, 0.5, 0.9), and tag retention $(\lambda = 0.2, 0.5, 0.9)$ probabilities. The black line indicates the true value of ϕ used to simulate the data for each model.



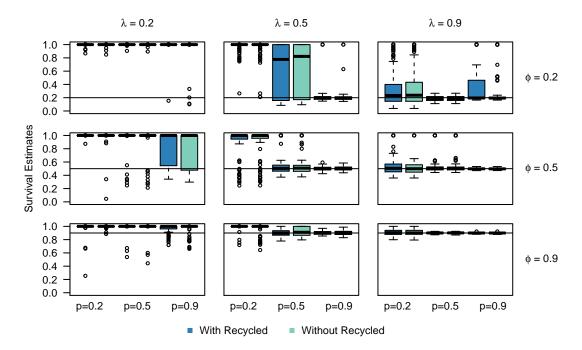
WEB FIGURE 2: Boxplots of survival estimates $(\hat{\phi})$ of 100 simulated datasets analyzed with and without the effect of recycled individuals for population size 100000 with $T_2 = 1$ with 10 time periods for varying survival $(\phi = 0.2, 0.5, 0.9)$, capture (p = 0.2, 0.5, 0.9), and tag retention $(\lambda = 0.2, 0.5, 0.9)$ probabilities. The black line indicates the true value of ϕ used to simulate the data for each model.



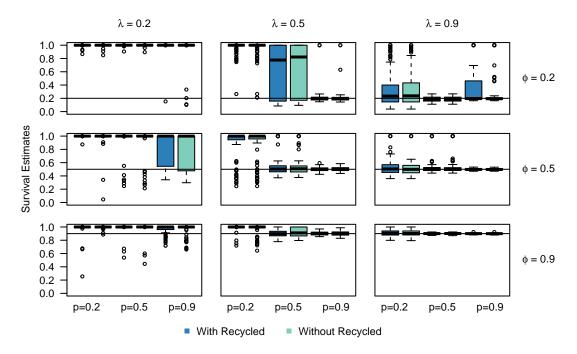
WEB FIGURE 3: Boxplots of survival estimates $(\hat{\phi})$ of 100 simulated datasets analyzed with and without the effect of recycled individuals for population size 1000 with $T_2 = 0.5$ with 10 time periods for varying survival $(\phi = 0.2, 0.5, 0.9)$, capture (p = 0.2, 0.5, 0.9), and tag retention $(\lambda = 0.2, 0.5, 0.9)$ probabilities. The black line indicates the true value of ϕ used to simulate the data for each model.



WEB FIGURE 4: Boxplots of survival estimates $(\hat{\phi})$ of 100 simulated datasets analyzed with and without the effect of recycled individuals for population size 100000 with $T_2 = 0.5$ with 10 time periods for varying survival $(\phi = 0.2, 0.5, 0.9)$, capture (p = 0.2, 0.5, 0.9), and tag retention $(\lambda = 0.2, 0.5, 0.9)$ probabilities. The black line indicates the true value of ϕ used to simulate the data for each model.

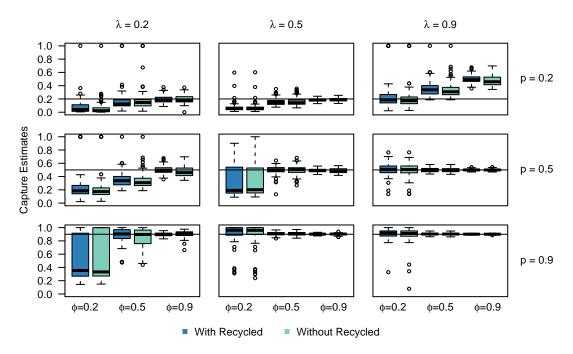


WEB FIGURE 5: Boxplots of survival estimates $(\hat{\phi})$ of 100 simulated datasets analyzed with and without the effect of recycled individuals for population size 1000 with $T_2 = 1$ with 5 time periods for varying survival $(\phi = 0.2, 0.5, 0.9)$, capture (p = 0.2, 0.5, 0.9), and tag retention $(\lambda = 0.2, 0.5, 0.9)$ probabilities. The black line indicates the true value of ϕ used to simulate the data for each model.

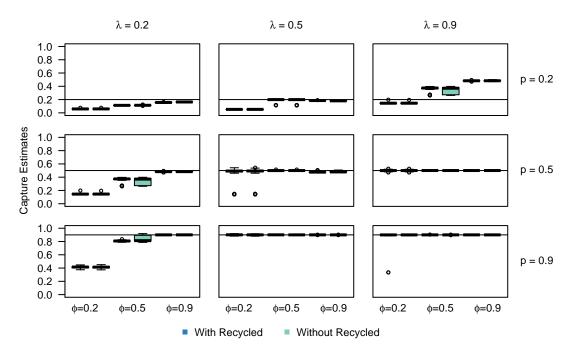


WEB FIGURE 6: Boxplots of survival estimates $(\hat{\phi})$ of 100 simulated datasets analyzed with and without the effect of recycled individuals for population size 1000 with $T_2 = 1$ with 7 time periods for varying survival $(\phi = 0.2, 0.5, 0.9)$, capture (p = 0.2, 0.5, 0.9), and tag retention $(\lambda = 0.2, 0.5, 0.9)$ probabilities. The black line indicates the true value of ϕ used to simulate the data for each model.

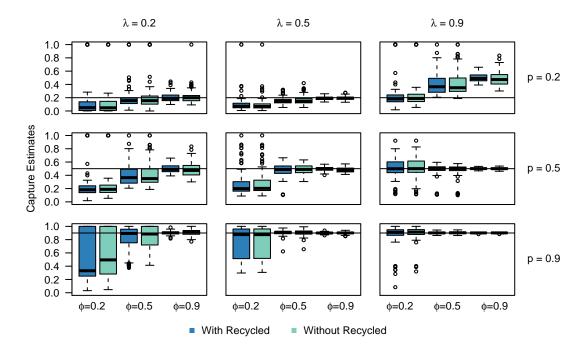
Capture Estimates



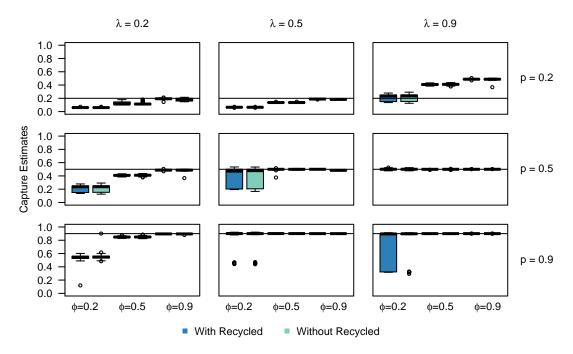
WEB FIGURE 7: Boxplots of capture estimates (\hat{p}) of 100 simulated datasets analyzed with and without the effect of recycled individuals for population size 1000 with $T_2 = 1$ with 10 time periods for varying survival $(\phi = 0.2, 0.5, 0.9)$, capture (p = 0.2, 0.5, 0.9), and tag retention $(\lambda = 0.2, 0.5, 0.9)$ probabilities. The black line indicates the true value of p used to simulate the data for each model.



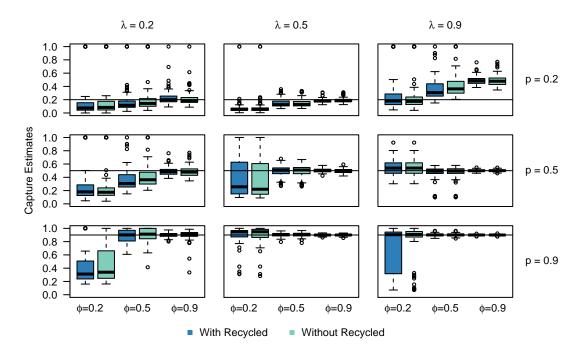
WEB FIGURE 8: Boxplots of capture estimates (\hat{p}) of 100 simulated datasets analyzed with and without the effect of recycled individuals for population size 100000 with $T_2 = 1$ with 10 time periods for varying survival $(\phi = 0.2, 0.5, 0.9)$, capture (p = 0.2, 0.5, 0.9), and tag retention $(\lambda = 0.2, 0.5, 0.9)$ probabilities. The black line indicates the true value of p used to simulate the data for each model.



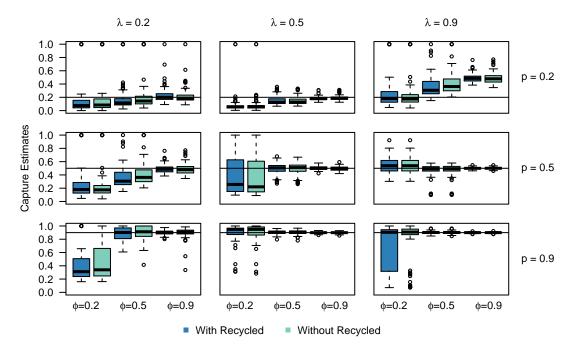
WEB FIGURE 9: Boxplots of capture estimates (\hat{p}) of 100 simulated datasets analyzed with and without the effect of recycled individuals for population size 1000 with $T_2 = 0.5$ with 10 time periods for varying survival $(\phi = 0.2, 0.5, 0.9)$, capture (p = 0.2, 0.5, 0.9), and tag retention $(\lambda = 0.2, 0.5, 0.9)$ probabilities. The black line indicates the true value of p used to simulate the data for each model.



WEB FIGURE 10: Boxplots of capture estimates (\hat{p}) of 100 simulated datasets analyzed with and without the effect of recycled individuals for population size 100000 with $T_2 = 0.5$ with 10 time periods for varying survival $(\phi = 0.2, 0.5, 0.9)$, capture (p = 0.2, 0.5, 0.9), and tag retention $(\lambda = 0.2, 0.5, 0.9)$ probabilities. The black line indicates the true value of p used to simulate the data for each model.

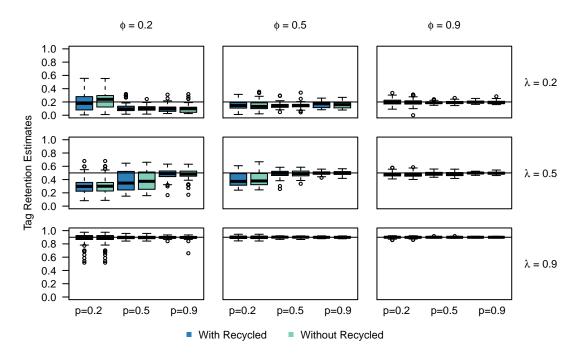


WEB FIGURE 11: Boxplots of capture estimates (\hat{p}) of 100 simulated datasets analyzed with and without the effect of recycled individuals for population size 1000 with $T_2 = 1$ for 5 time periods for varying survival $(\phi = 0.2, 0.5, 0.9)$, capture (p = 0.2, 0.5, 0.9), and tag retention $(\lambda = 0.2, 0.5, 0.9)$ probabilities. The black line indicates the true value of p used to simulate the data for each model.

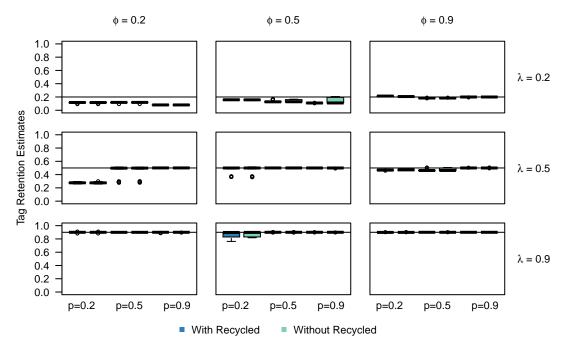


WEB FIGURE 12: Boxplots of capture estimates (\hat{p}) of 100 simulated datasets analyzed with and without the effect of recycled individuals for population size 1000 with $T_2 = 1$ for 7 time periods for varying survival $(\phi = 0.2, 0.5, 0.9)$, capture (p = 0.2, 0.5, 0.9), and tag retention $(\lambda = 0.2, 0.5, 0.9)$ probabilities. The black line indicates the true value of p used to simulate the data for each model.

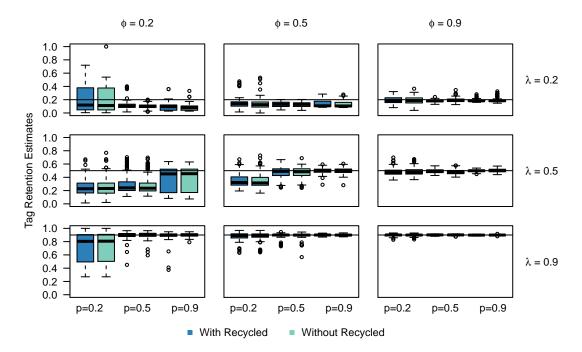
Tag Retention Estimates



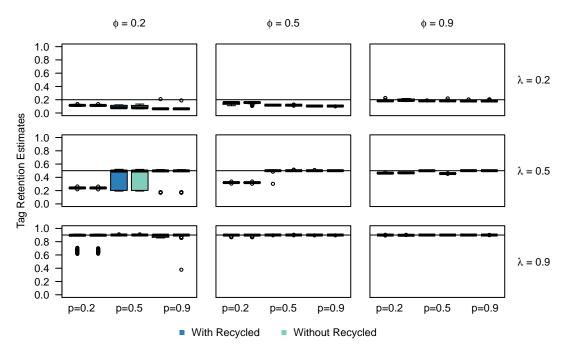
WEB FIGURE 13: Boxplots of tag retention estimates $(\hat{\lambda})$ of 100 simulated datasets analyzed with and without the effect of recycled individuals for population size 1000 with $T_2 = 1$ with 10 time periods for varying survival $(\phi = 0.2, 0.5, 0.9)$, capture (p = 0.2, 0.5, 0.9), and tag retention $(\lambda = 0.2, 0.5, 0.9)$ probabilities. The black line indicates the true value of λ used to simulate the data for each model.



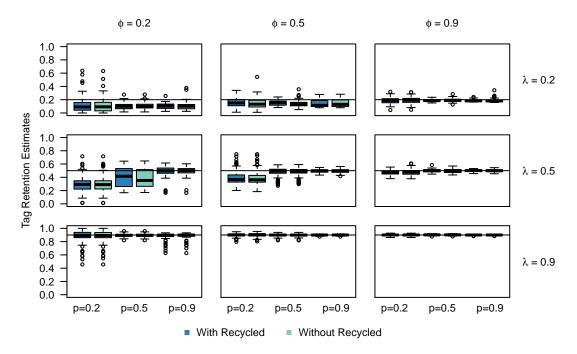
WEB FIGURE 14: Boxplots of tag retention estimates $(\hat{\lambda})$ of 100 simulated datasets analyzed with and without the effect of recycled individuals for population size 100000 with $T_2 = 1$ with 10 time periods for varying survival ($\phi = 0.2, 0.5, 0.9$), capture (p = 0.2, 0.5, 0.9), and tag retention ($\lambda = 0.2, 0.5, 0.9$) probabilities. The black line indicates the true value of λ used to simulate the data for each model.



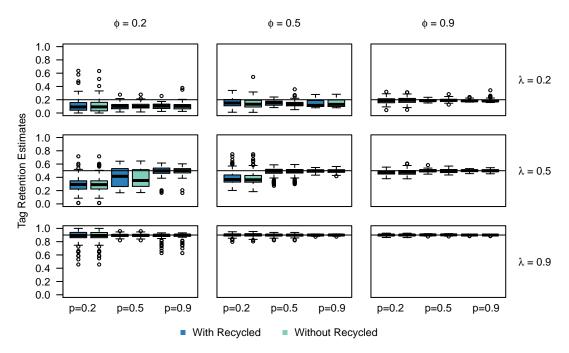
WEB FIGURE 15: Boxplots of tag retention estimates $(\hat{\lambda})$ of 100 simulated datasets analyzed with and without the effect of recycled individuals for population size 1000 with $T_2 = 0.5$ with 10 time periods for varying survival $(\phi = 0.2, 0.5, 0.9)$, capture (p = 0.2, 0.5, 0.9), and tag retention $(\lambda = 0.2, 0.5, 0.9)$ probabilities. The black line indicates the true value of λ used to simulate the data for each model.



WEB FIGURE 16: Boxplots of tag retention estimates ($\hat{\lambda}$) of 100 simulated datasets analyzed with and without the effect of recycled individuals for population size 100000 with $T_2 = 0.5$ with 10 time periods for varying survival ($\phi = 0.2, 0.5, 0.9$), capture (p = 0.2, 0.5, 0.9), and tag retention ($\lambda = 0.2, 0.5, 0.9$) probabilities. The black line indicates the true value of λ used to simulate the data for each model.

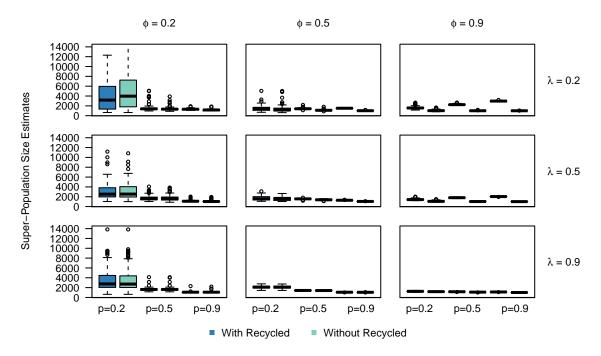


WEB FIGURE 17: Boxplots of tag retention estimates $(\hat{\lambda})$ of 100 simulated datasets analyzed with and without the effect of recycled individuals for population size 1000 with $T_2 = 1$ for 5 time periods for varying survival $(\phi = 0.2, 0.5, 0.9)$, capture (p = 0.2, 0.5, 0.9), and tag retention $(\lambda = 0.2, 0.5, 0.9)$ probabilities. The black line indicates the true value of λ used to simulate the data for each model.

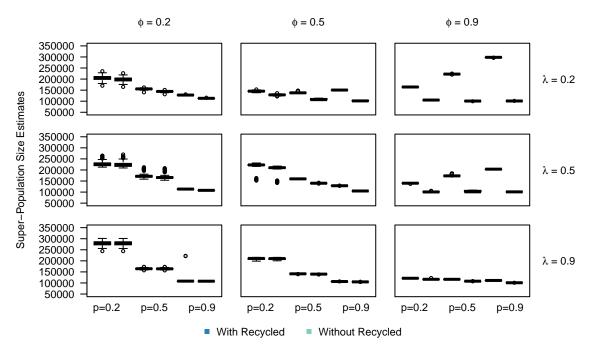


WEB FIGURE 18: Boxplots of tag retention estimates $(\hat{\lambda})$ of 100 simulated datasets analyzed with and without the effect of recycled individuals for population size 1000 with $T_2 = 1$ for 7 time periods for varying survival $(\phi = 0.2, 0.5, 0.9)$, capture (p = 0.2, 0.5, 0.9), and tag retention $(\lambda = 0.2, 0.5, 0.9)$ probabilities. The black line indicates the true value of λ used to simulate the data for each model.

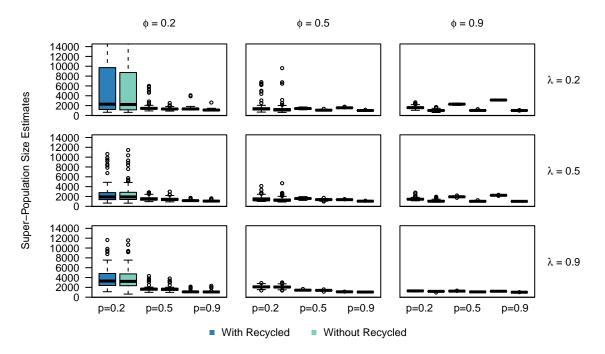
Super-Population Size Estimates



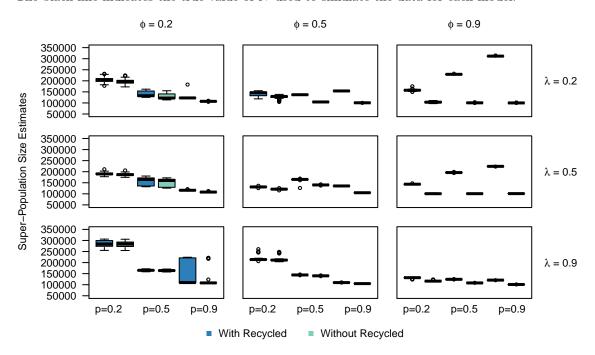
WEB FIGURE 19: Boxplots of super-population size estimates (N) of 100 simulated datasets analyzed with and without the effect of recycled individuals for population size 1000 with $T_2 = 1$ with 10 time periods for varying survival ($\phi = 0.2, 0.5, 0.9$), capture (p = 0.2, 0.5, 0.9), and tag retention ($\lambda = 0.2, 0.5, 0.9$) probabilities. The black line indicates the true value of N used to simulate the data for each model.



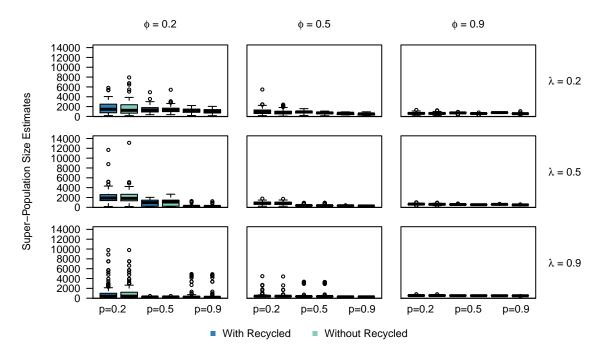
WEB FIGURE 20: Boxplots of super-population size estimates (N) of 100 simulated datasets analyzed with and without the effect of recycled individuals for population size 100000 with $T_2 = 1$ with 10 time periods for varying survival $(\phi = 0.2, 0.5, 0.9)$, capture (p = 0.2, 0.5, 0.9), and tag retention $(\lambda = 0.2, 0.5, 0.9)$ probabilities. The black line indicates the true value of N used to simulate the data for each model.



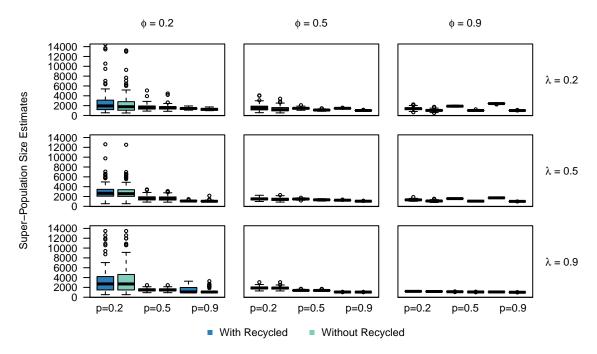
WEB FIGURE 21: Boxplots of super-population size estimates (N) of 100 simulated datasets analyzed with and without the effect of recycled individuals for population size 1000 with $T_2 = 0.5$ with 10 time periods for varying survival ($\phi = 0.2, 0.5, 0.9$), capture (p = 0.2, 0.5, 0.9), and tag retention ($\lambda = 0.2, 0.5, 0.9$) probabilities. The black line indicates the true value of N used to simulate the data for each model.



WEB FIGURE 22: Boxplots of super-population size estimates (N) of 100 simulated datasets analyzed with and without the effect of recycled individuals for population size 100000 with $T_2 = 0.5$ with 10 time periods for varying survival ($\phi = 0.2, 0.5, 0.9$), capture (p = 0.2, 0.5, 0.9), and tag retention ($\lambda = 0.2, 0.5, 0.9$) probabilities. The black line indicates the true value of N used to simulate the data for each model.

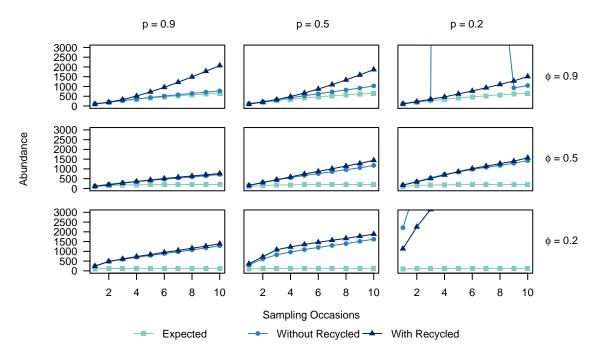


WEB FIGURE 23: Boxplots of super-population size estimates (N) of 100 simulated datasets analyzed with and without the effect of recycled individuals for population size 1000 with $T_2 = 1$ for 5 time periods for varying survival ($\phi = 0.2, 0.5, 0.9$), capture (p = 0.2, 0.5, 0.9), and tag retention ($\lambda = 0.2, 0.5, 0.9$) probabilities. The black line indicates the true value of N used to simulate the data for each model.

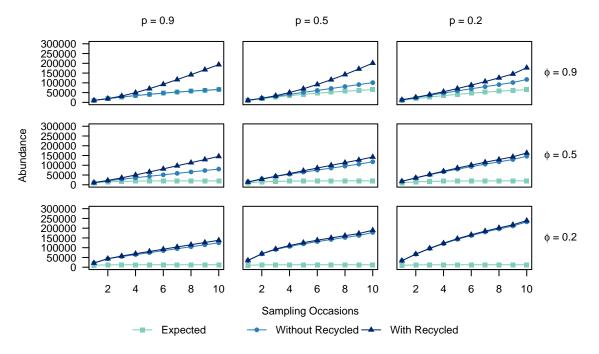


WEB FIGURE 24: Boxplots of super-population size estimates (N) of 100 simulated datasets analyzed with and without the effect of recycled individuals for population size 1000 with $T_2 = 1$ for 7 time periods for varying survival ($\phi = 0.2, 0.5, 0.9$), capture (p = 0.2, 0.5, 0.9), and tag retention ($\lambda = 0.2, 0.5, 0.9$) probabilities. The black line indicates the true value of N used to simulate the data for each model.

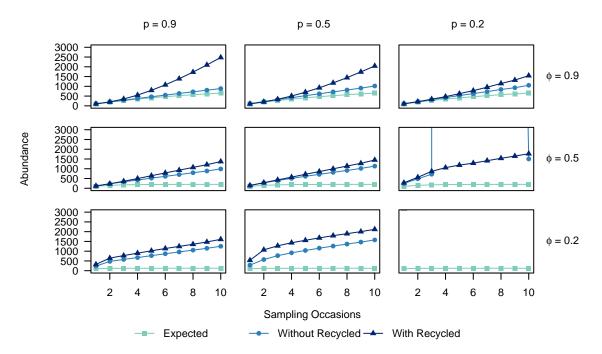
Abundance Estimates



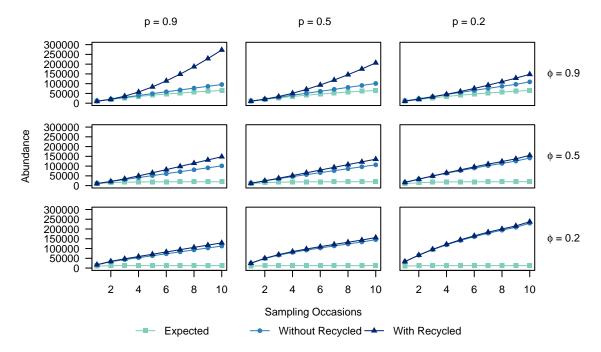
WEB FIGURE 25: Mean abundance estimates $(N_j$'s) for each sample time (k=10) between analysis with and without recycled individuals with population size N=1000 with $T_2=1$ with 10 time periods for low tag retention $(\lambda=0.2)$, varying survival probabilities $(\phi=0.2,0.5,0.9)$ and varying capture probabilities (p=0.2,0.5,0.9).



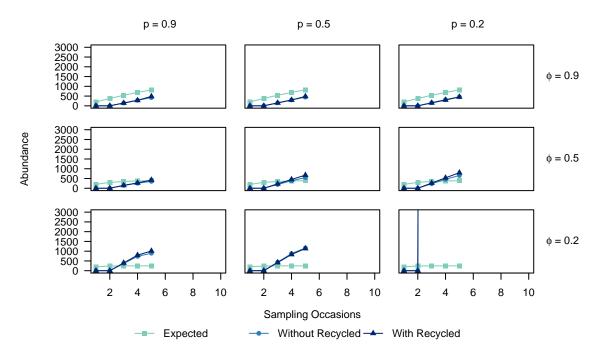
WEB FIGURE 26: Mean abundance estimates $(N_j$'s) for each sample time (k=10) between analysis with and without recycled individuals with population size N=100000 with $T_2=1$ with 10 time periods for low tag retention $(\lambda=0.2)$, varying survival probabilities $(\phi=0.2,0.5,0.9)$ and varying capture probabilities (p=0.2,0.5,0.9).



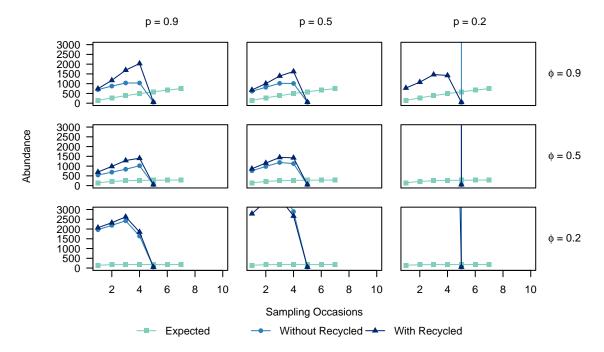
WEB FIGURE 27: Mean abundance estimates $(N_j$'s) for each sample time (k=10) between analysis with and without recycled individuals with population size N=1000 with $T_2=0.5$ with 10 time periods for low tag retention $(\lambda=0.2)$, varying survival probabilities $(\phi=0.2,0.5,0.9)$ and varying capture probabilities (p=0.2,0.5,0.9).



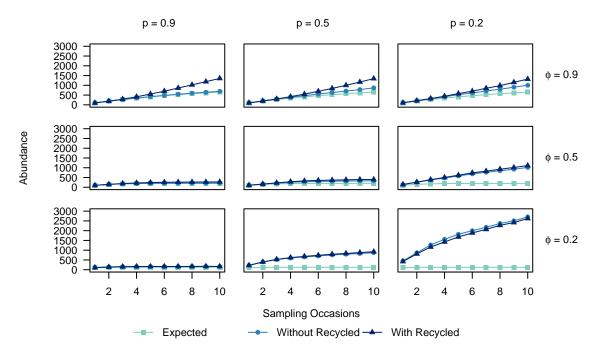
WEB FIGURE 28: Mean abundance estimates $(N_j$'s) for each sample time (k=10) between analysis with and without recycled individuals with population size N=100000 with $T_2=0.5$ with 10 time periods for low tag retention $(\lambda=0.2)$, varying survival probabilities $(\phi=0.2,0.5,0.9)$ and varying capture probabilities (p=0.2,0.5,0.9).



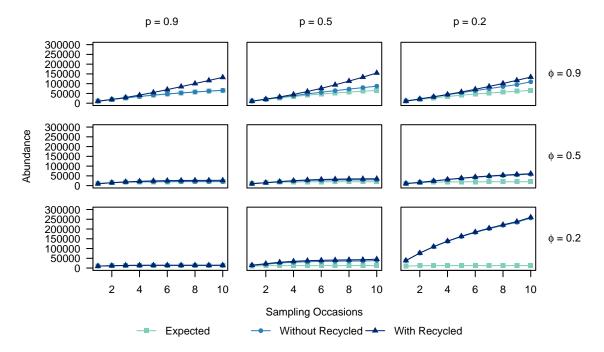
WEB FIGURE 29: Mean abundance estimates $(N_j$'s) for each sample time (k=5) between analysis with and without recycled individuals with population size N=1000 with $T_2=1$ with 5 time periods for low tag retention $(\lambda=0.2)$, varying survival probabilities $(\phi=0.2,0.5,0.9)$ and varying capture probabilities (p=0.2,0.5,0.9).



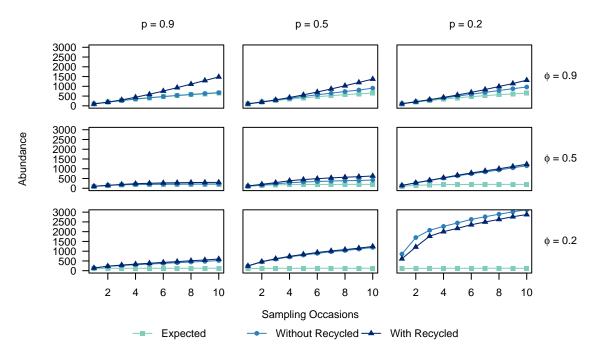
WEB FIGURE 30: Mean abundance estimates $(N_j$'s) for each sample time (k=7) between analysis with and without recycled individuals with population size N=1000 with $T_2=1$ with 7 time periods for low tag retention $(\lambda=0.2)$, varying survival probabilities $(\phi=0.2,0.5,0.9)$ and varying capture probabilities (p=0.2,0.5,0.9).



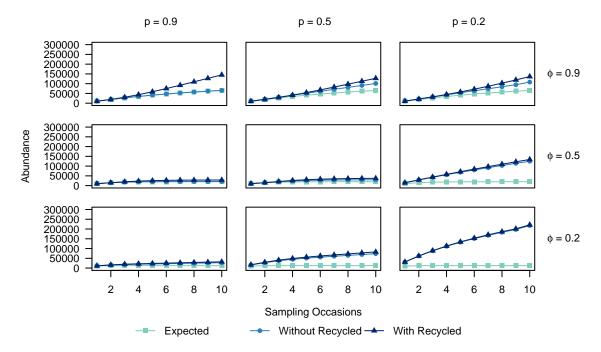
WEB FIGURE 31: Mean abundance estimates $(N_j$'s) for each sample time (k=10) between analysis with and without recycled individuals with population size N=1000 with $T_2=1$ with 10 time periods for medium tag retention $(\lambda=0.5)$, varying survival probabilities $(\phi=0.2,0.5,0.9)$ and varying capture probabilities (p=0.2,0.5,0.9).



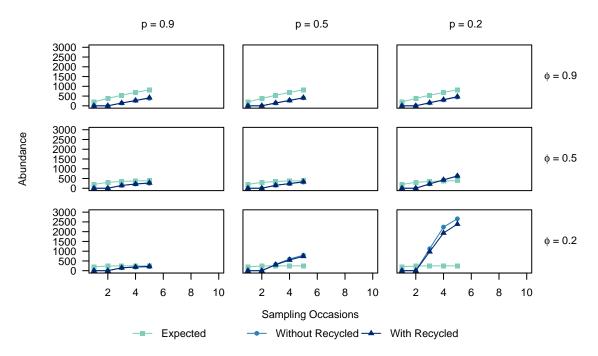
WEB FIGURE 32: Mean abundance estimates $(N_j$'s) for each sample time (k=10) between analysis with and without recycled individuals with population size N=100000 with $T_2=1$ with 10 time periods for medium tag retention $(\lambda=0.5)$, varying survival probabilities $(\phi=0.2,0.5,0.9)$ and varying capture probabilities (p=0.2,0.5,0.9).



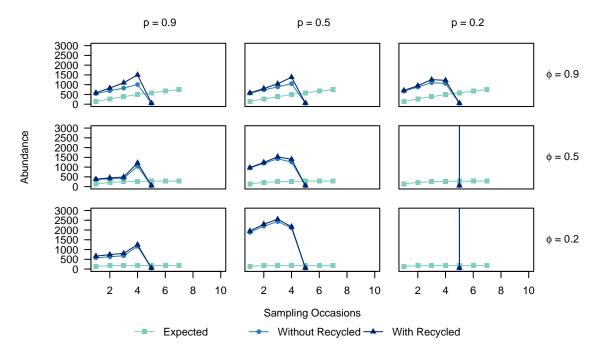
WEB FIGURE 33: Mean abundance estimates $(N_j$'s) for each sample time (k=10) between analysis with and without recycled individuals with population size N=1000 with $T_2=0.5$ with 10 time periods for medium tag retention $(\lambda=0.5)$, varying survival probabilities $(\phi=0.2,0.5,0.9)$ and varying capture probabilities (p=0.2,0.5,0.9).



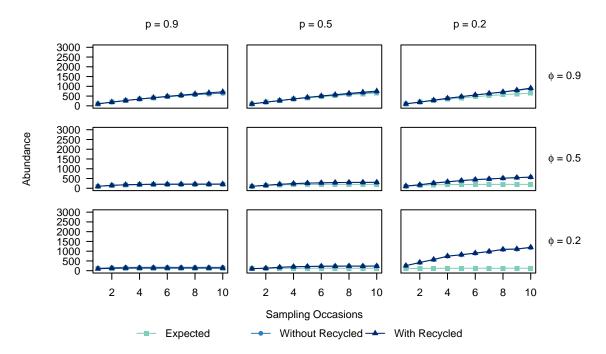
WEB FIGURE 34: Mean abundance estimates $(N_j$'s) for each sample time (k=10) between analysis with and without recycled individuals with population size N=100000 with $T_2=0.5$ with 10 time periods for medium tag retention $(\lambda=0.5)$, varying survival probabilities $(\phi=0.2,0.5,0.9)$ and varying capture probabilities (p=0.2,0.5,0.9).



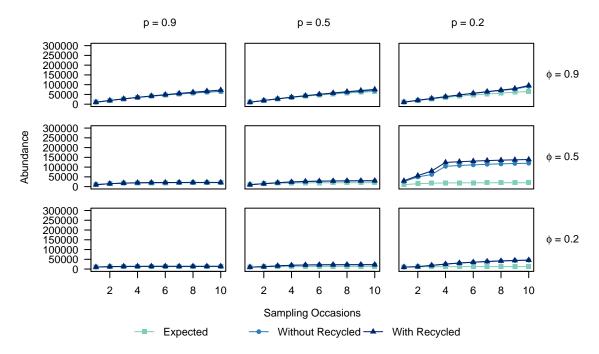
WEB FIGURE 35: Mean abundance estimates $(N_j$'s) for each sample time (k=5) between analysis with and without recycled individuals with population size N=1000 with $T_2=1$ with 5 time periods for medium tag retention $(\lambda=0.5)$, varying survival probabilities $(\phi=0.2,0.5,0.9)$ and varying capture probabilities (p=0.2,0.5,0.9).



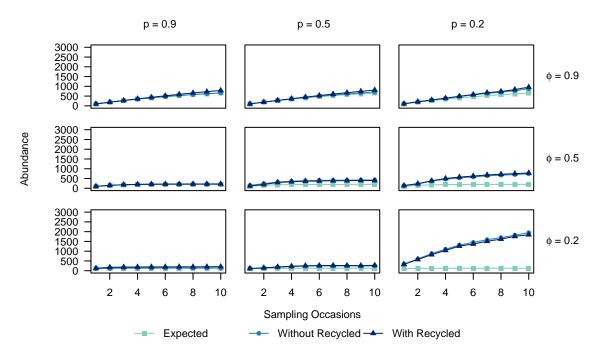
WEB FIGURE 36: Mean abundance estimates $(N_j$'s) for each sample time (k=7) between analysis with and without recycled individuals with population size N=1000 with $T_2=1$ with 7 time periods for medium tag retention $(\lambda=0.5)$, varying survival probabilities $(\phi=0.2,0.5,0.9)$ and varying capture probabilities (p=0.2,0.5,0.9).



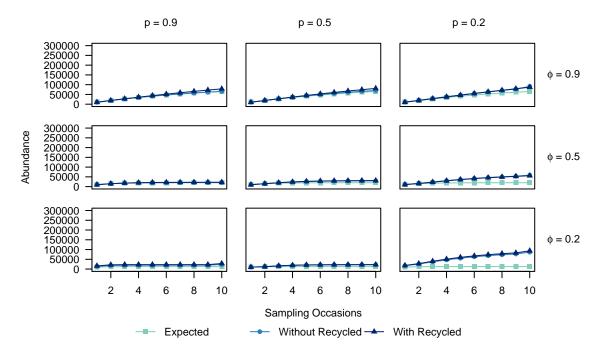
WEB FIGURE 37: Mean abundance estimates $(N_j$'s) for each sample time (k = 10) between analysis with and without recycled individuals with population size N = 1000 with $T_2 = 1$ with 10 time periods for high tag retention $(\lambda = 0.9)$, varying survival probabilities $(\phi = 0.2, 0.5, 0.9)$ and varying capture probabilities (p = 0.2, 0.5, 0.9).



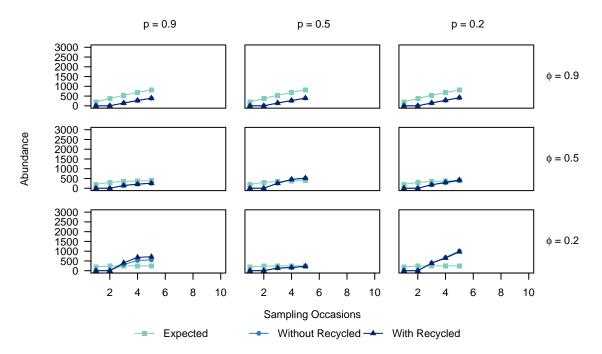
WEB FIGURE 38: Mean abundance estimates $(N_j$'s) for each sample time (k=10) between analysis with and without recycled individuals with population size N=100000 with $T_2=1$ with 10 time periods for high tag retention $(\lambda=0.9)$, varying survival probabilities $(\phi=0.2,0.5,0.9)$ and varying capture probabilities (p=0.2,0.5,0.9).



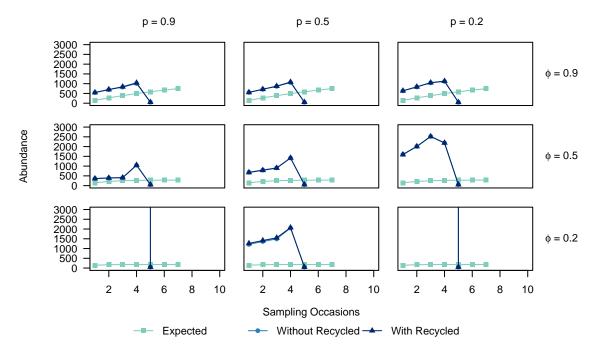
WEB FIGURE 39: Mean abundance estimates $(N_j$'s) for each sample time (k=10) between analysis with and without recycled individuals with population size N=1000 with $T_2=0.5$ with 10 time periods for high tag retention $(\lambda=0.9)$, varying survival probabilities $(\phi=0.2,0.5,0.9)$ and varying capture probabilities (p=0.2,0.5,0.9).



WEB FIGURE 40: Mean abundance estimates $(N_j$'s) for each sample time (k=10) between analysis with and without recycled individuals with population size N=100000 with $T_2=0.5$ with 10 time periods for high tag retention $(\lambda=0.9)$, varying survival probabilities $(\phi=0.2,0.5,0.9)$ and varying capture probabilities (p=0.2,0.5,0.9).



WEB FIGURE 41: Mean abundance estimates $(N_j$'s) for each sample time (k=5) between analysis with and without recycled individuals with population size N=1000 with $T_2=1$ with 5 time periods for high tag retention $(\lambda=0.9)$, varying survival probabilities $(\phi=0.2,0.5,0.9)$ and varying capture probabilities (p=0.2,0.5,0.9).



WEB FIGURE 42: Mean abundance estimates $(N_j$'s) for each sample time (k=7) between analysis with and without recycled individuals with population size N=1000 with $T_2=1$ with 5 time periods for high tag retention $(\lambda=0.9)$, varying survival probabilities $(\phi=0.2,0.5,0.9)$ and varying capture probabilities (p=0.2,0.5,0.9).