NJU SICP

期中试卷讲解

jjppp

2024-11-15

1. 我负责...

- Environment Diagram
- Trees
- Remember Me!

2. Environment Diagram

```
1 def fix(f):
2   def inner(n):
3    return 1 if n ≤ 1 else f(n)
4   return inner
5   6 fact = lambda n: n * fact(n - 1)
7 fact = fix(fact)
8 result = fact(2)
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考点:

- name lookup
- function as values
- 故意有点难(没想到这么惨)

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 - ▶ 递归漏终止条件
 - ► RecursionError

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 - ▶ 补上终止条件
- 青春版动态更新
 - ▶ 停服维护 vs 不停服维护

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 - ▶ result = fact(2) = 2

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- fact(n): 阶乘函数
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- 总共出现了三个函数
 - 1. fix
 - 2. inner
 - 3. lambda<6>

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- fact(n): 阶乘函数
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- 总共出现了三个函数
 - 1. fix
 - 2. inner
 - 3. lambda<6>
- fact 被赋值了两次
 - ▶ fact 有两条边: lambda<6>,inner

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• parent frame:

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- parent frame:
 - parent[fix] = global

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- parent frame:
 - parent[fix] = global
 - parent[inner] = fix

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- parent frame:
 - parent[fix] = global
 - parent[inner] = fix
 - parent[lambda<6>] = global

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- 参数 f
 - ▶ 传入 fact,值为 lambda<6>

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- 参数 f
 - ▶ 传入 fact,值为 lambda<6>
- 函数调用
 - fact = fix(fact)
 - global \Rightarrow fix

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- 参数 f
 - ▶ 传入 fact,值为 lambda<6>
- 函数调用

```
▶ fact = fix(fact)
   - global ⇒ fix
▶ result = fact(2)
   - global ⇒ fact{inner}(2)
        ⇒ f{lambda<6>}(2)
        ⇒ fact{inner}(1)
```

3. Trees

```
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考点:

- data abstraction
- recursion
- 送分

Cool Stuff:

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考点:

- data abstraction
- recursion
- 送分

Cool Stuff:

- "还差一个题,送点分吧"
- "上了实验课的同学应该都送到了"



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```
t1 = tree(1, [
              tree(2, [
                        tree(4)]),
              tree(3, [
                        tree(5)])])
```

改卷反馈:

3.2 t1

- 大部分人都送到了
- 错误示范 ::
 - ▶ [1, [2, [4]], [3, [5]]]
 - ▶ tree(1, [tree(2, tree(4))], [tree(3, tree(5))])

3. Trees

3.3 map_tree

```
def map_tree(t, f):
    return tree(
    f(label(t)),
    [map_tree(b, f) for b in branches(t)]
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递归:

• is_leaf: 直接调用 f 作用在 label(t) 上

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- doctest 透露了上一题的答案
- 答案不唯一
 中括号不是必须的(why?)
 不考虑 is_leaf 也 OK(why?)

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3. Trees

3.3 map_tree

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改卷反馈:

• f(t)★: f 是作用在 label 上的函数 学会读 doctest

3. Trees

3.4 height

```
def height(t, f):
   if is_leaf(t):
     return 1
   return 1 + max([
     height(b) for b in branches(t)
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递归:

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- 然后返回最大值+1
- 答案不唯一
 - ▶ 1+ 放里面
 - ▶ sorted(...)[-1] 很有想象力
 - ▶ 中括号不是必须的(why?)

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• 忘了+1 学会读题

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- 忘了+1学会读题
- sum() 学会读题

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Line #	Correct Answer	Comment
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• 4 和 6 对照着看, 6 分

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- 4 和 6 对照着看, 6 分
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- 好多同学空着(why?)

4.1 命题意图



考点:

- 长文阅读(~900 词)
- higher order functions
- pure functions
- ADT
- 在课程 code 中出现过 (同学的提问也能学到东西)

Cool Stuff:

4.1 命题意图



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Cool Stuff:

- Python adecorator 的原理 有没有研究过 cats.py 的代码?
- (几乎) 全自动的程序优化

```
4.2 count_calls
```

```
def count_calls(n):
   if n = 1 or n = 2:
     return 1
   return count_calls(n - 1) + count_calls(n - 2) + 1
```

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思路:

• 数 call tree 节点数

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- 数 call tree 节点数
- count_calls 的增长速度:

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- 数 call tree 节点数
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 - 1. 注意到 count_calls(n) ≥ fib(n)
 - 2.
 - 3.

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def count_calls(n):
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改卷反馈:

不少人写了又一个 fib题目提示 count_calls(5)是 9学会读题

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- 不少人写了又一个 fib题目提示 count_calls(5)是 9学会读题
- 有同学试图写通项 很可惜写错了 (通项和 fib 类似)

4.3 Pure

```
import random
                                                            F
def lottery():
  return random.randint(6, 71)
def fact(n):
  return 1 if n = 1 else fact(n - 1) * n
t = []
                                                             F
def append_len(x):
                                                  print(append_len('A'))
  t.append(x)
                                                  print(append_len('B'))
  return len(t)
def fun(x):
  def safe(y, total):
                                                     nonlocal x 是酱油
    nonlocal x
                                                     调用 safe 使 y 少 1
    if y \leq 0:
      return total
                                                     当 y ≤ 0, total 为 0
    x = (y - 1) * 2
                                                     (有限度的)副作用
    return safe(y - 1, x * (total + 1))
  return safe(x, 0)
```

```
mem = memory()
def fib_r(n):
    if recall(mem, n):
        return recall(mem, n)
    Fn = 1
    if n \geq 3:
        Fn = fib_r(n - 1) + fib_r(n - 2)
        remember(mem, n, Fn)
    return Fn
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改卷反馈:

· 不少同学第二个空填 not recall

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- 有同学填了 n ≥ 2
 - ▶ 很可惜错了(why?)

```
def remember_me(f):
    mem = memory()
    def inner(n):
        if recall(mem, n):
            return recall(mem, n)
        Fn = f(n)
        remember(mem, n, Fn)
        return inner
```

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    mem = memory()
    def inner(n):
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```

- ·一些同学认为这里还在算 fib
 - ► remember_me 是通用的记忆化函数 我们在后面还记忆化了 count_k

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- ·一些同学认为这里还在算 fib
 - ► remember_me 是通用的记忆化函数 我们在后面还记忆化了 count_k
- 答案不唯一

```
def two_to_one(f):
    return lambda nk: f(nk[0], nk[1])

count_k = two_to_one(count_k)

# old_count_k: (n: int, k: int) → int
# new_count_k: (nk: (int, int)) → int
```

4. Remember Me!

```
def two to one(f):
    return lambda nk: f(nk[0], nk[1])
count_k = two_to_one(count k)
# old_count_k: (n: int, k: int) \rightarrow int
# new_count_k: (nk: (int, int)) \rightarrow int
new_count_k((5, 3))
  \Rightarrow (lambda nk: old_count_k(nk[0], nk[1]))((5, 3))
  \Rightarrow old count k(5, 3)
  \Rightarrow count_k(5 - i, 3) # Which count_k?
                          # new count k!
                          # TypeError
```

- 我是故意的(1分)
- · 灵感源自群里关于 argument unpacking 的提问
- 不少人算了半天 13/ 其它数
- 做对的同学不多

5. Bonus

- 得分率不高
 - ▶ 奖励认真读教材的同学
 - ▶ 也可能是没做到最后一题?
- 单词写不对
 - Interptation
 - ... of Computer Science
 - ... of Composing Programs
 - ▶ 英语很重要