

STATISTICS FUNDAMENTALS, PART 2

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STATISTICS FUNDAMENTALS, PART 2

LEARNING OBJECTIVES

- Explain the difference between causation and correlation
- Test a hypothesis within a sample case study
- Validate your findings using statistical analysis (p-values, confidence intervals)

INTRODUCTION

- If an association is observed, the first question to ask should always be... is it real?
- Think of various examples you've seen in the media related to food.

FRIDAY, MAY 23, 2014 08:15 AM SGT

10 foods touted as health miracles, then vilified as health hazards

One reason Americans have trouble maintaing a healthy diet: They're suffering from "food information overload"

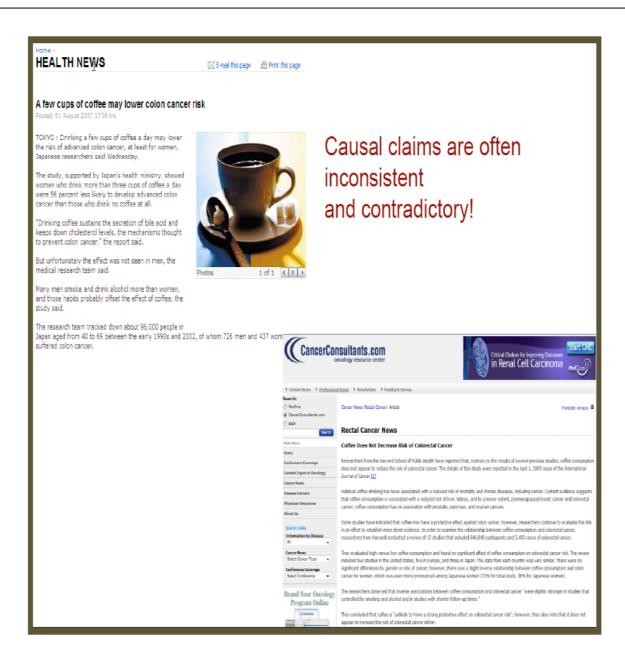
ALEX HENDERSON, ALTERNET



SKIP TO COMMENTS

TOPICS: ALTERNET, CAFFEINE, COFFEE, OLIVE OIL, ORANGE JUICE, UNIVERSITY OF MINNESOTA, LIFE NEWS



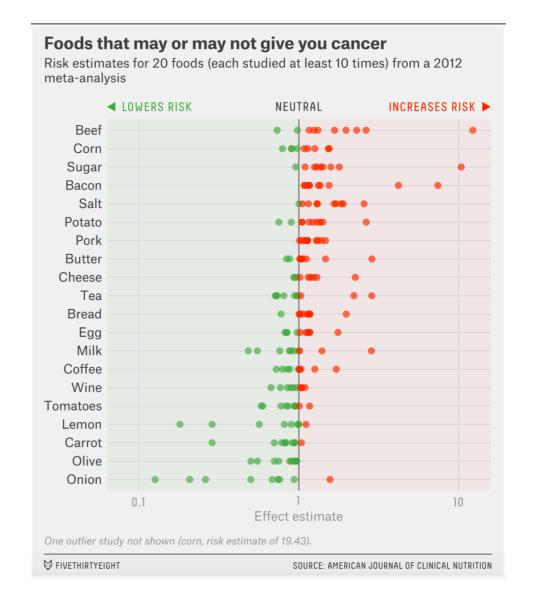


SPURIOUS CORRELATIONS

Our shocking new study finds that ...

EATING OR DRINKING	IS LINKED TO	P-VALUE
Raw tomatoes	Judaism	<0.0001
Egg rolls	Dog ownership	<0.0001
Energy drinks	Smoking	<0.0001
Potato chips	Higher score on SAT math vs. verbal	0.0001
Soda	Weird rash in the past year	0.0002
Shellfish	Right-handedness	0.0002
Lemonade	Belief that "Crash" deserved to win best picture	0.0004
Fried/breaded fish	Democratic Party affiliation	0.0007
Beer	Frequent smoking	0.0013
Coffee	Cat ownership	0.0016
Table salt	Positive relationship with Internet service provider	0.0014
Steak with fat trimmed	Lack of belief in a god	0.0030
Iced tea	Belief that "Crash" didn't deserve to win best picture	0.0043
Bananas	Higher score on SAT verbal vs. math	0.0073
Cabbage	Innie bellybutton	0.0097

SOURCE: FFQ & FIVETHIRTYEIGHT SUPPLEMENT

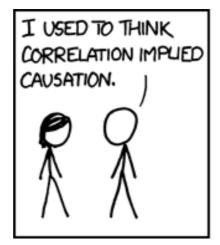


http://fivethirtyeight.com/features/you-cant-trust-what-you-read-about-nutrition/

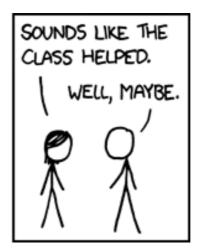
- Why is this?
- Sensational headlines?
- There is neglect of a robust data analysis.

- There is also often a lack of understanding of the difference between causation and correlation.
- Understanding this difference is critical in the data science workflow, especially when **Identifying** and **Acquiring** data.
- We need to fully articulate our question and use the right data to answer it, including any *confounders*.

- Additionally, this comes up when we **Present** our results to stakeholders.
- We don't want to overstate what our model measures.
- Be careful not to say "caused" when you really mean "measured" or "associated".







LECTURE

CAUSATION S CORRELATION

- Causal criteria is one approach to assessing causal relationships.
- However, it's **very hard to define** universal causal criteria.
- One attempt that is commonly used in the medical field is based on work by Bradford Hill.

- He developed a list of "tests" that an analysis must pass in order to indicate a causal relationship. A relationship is more likely to be causal if:
 - **Strength**: The correlation coefficient is large and statistically significant
 - Consistency: It can be replicated
 - **Specificity**: There is no other likely explanation
 - **Temporality**: The effect always occurs after the cause
 - **Gradient**: A greater exposure to the suspected cause leads to a greater effect
 - **Plausibility**: There is a plausible mechanism between the cause and the effect
 - Coherence: It is compatible with related facts and theories
 - **Experiment**: It can be verified experimentally
 - Analogy: There are proven relationships between similar causes and effects

- This is not an exhaustive checklist, but it's useful for understanding that your predictor/exposure **must have occurred before your outcome**.
- For example, in order for smoking to cause cancer, one must have started smoking prior to getting cancer.

- Most commonly, we find an *association* between two variables. This means there is an observed **correlation** between the variables.
- We may not fully understand the causal direction (e.g. does smoking cause cancer or does cancer cause smoking?).
- We also might not understand *other* factors influencing the association.

ACTIVITY: KNOWLEDGE CHECK

ANSWER THE FOLLOWING QUESTIONS



1. What is the difference between causation and association?

DELIVERABLE

Answers to the above questions

INTRODUCTION

CONFOUNDING AND DAGS

CONFOUNDING

• Often times, associations may be influenced by another *confounding* factor.

Let's say we did an analysis to understand what causes lung cancer.

We find that people who carry cigarette lights are 2.4 times more likely

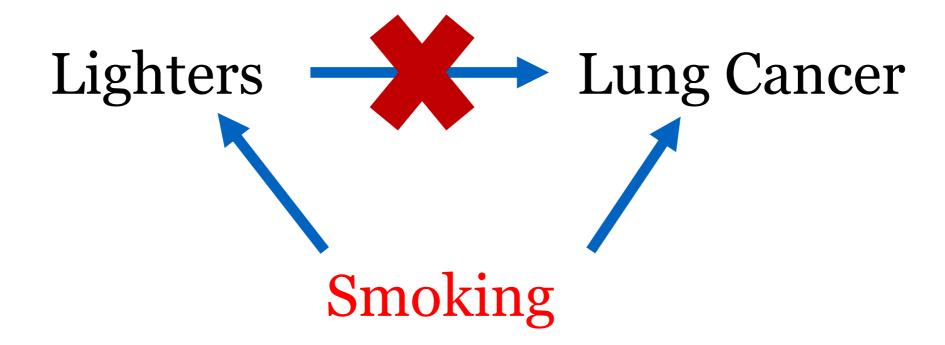
to contract lung cancer as people who don't carry lighters.

Does this mean that the lighters are causing cancer?



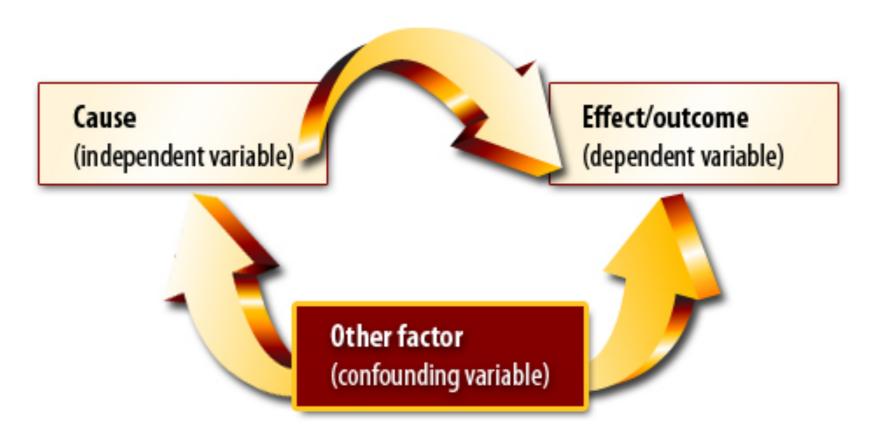
CONFOUNDING

No!



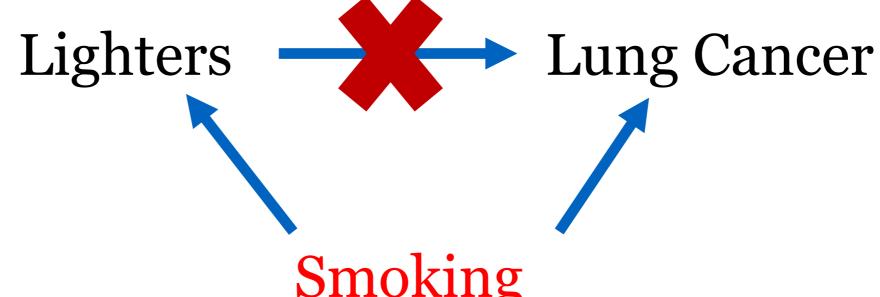
CONFOUNDING

• Confounding variables often hide the true association between causes and outcomes.



• A *Directed Acyclic Graph* (DAG) can help determine which variables are most important for your model. It helps visually demonstrate the logic of your models.

• A DAG always includes at least one exposure/predictor and one outcome.



• Suppose we have the following output from a model:

Dep. Variable:	Sales	R-squared:	0.612
Model:	OLS	Adj. R-squared:	0.610
Method:	Least Squares	F-statistic:	312.1
Date:	Thu, 03 Sep 2015	Prob (F-statistic):	1.47e-42
Time:	18:58:58	Log-Likelihood:	-519.05
No. Observations:	200	AIC:	1042.
Df Residuals:	198	BIC:	1049.
Df Model:	1		
Covariance Type:	nonrobust		

	coef	std err	t	P> t	[95.0% Conf. Int.]
Intercept	7.0326	0.458	15.360	0.000	6.130 7.935
TV	0.0475	0.003	17.668	0.000	0.042 0.053

Omnibus:	0.531	Durbin-Watson:	1.935
Prob(Omnibus):	0.767	Jarque-Bera (JB):	0.669
Skew:	-0.089	Prob(JB):	0.716
Kurtosis:	2.779	Cond. No.	338.

- The exposure/predictor is TV ads, associated with the outcome: sales.
- We can measure the strength to demonstrate a strong association.
- What other factors may increase sales?
- What other types of ads?

• The DAG for this might look like the following:



THINK, PAIR, SHARE

DAGS

SEASONALITY

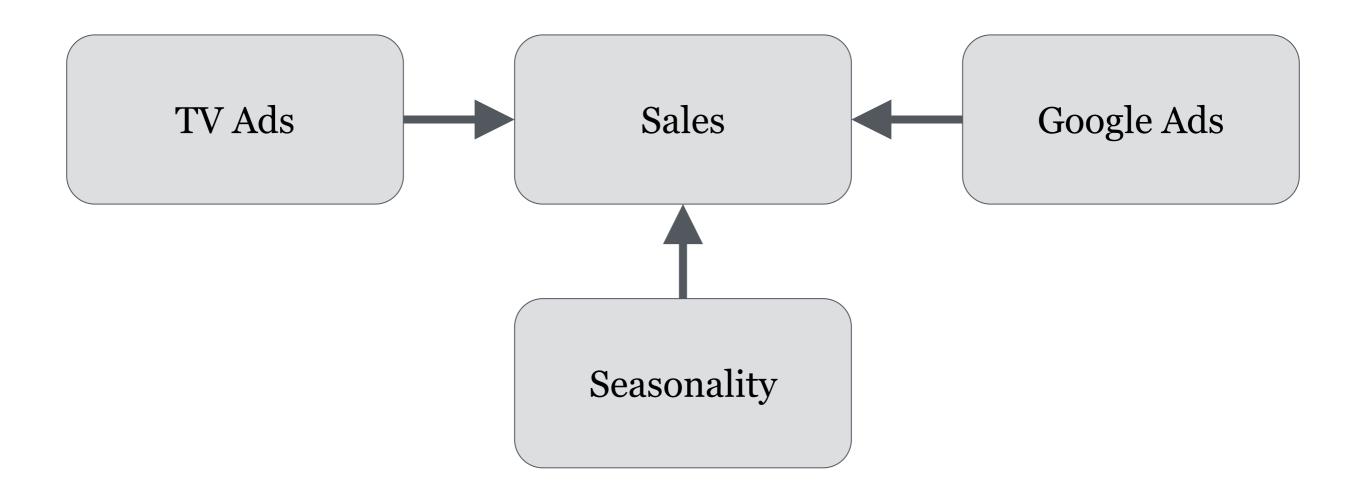
- Suppose TV ads were run in November/December (peak buying season) while Google ads were run during February/March (low buying season).
- If we compare the two, we're likely to reach the wrong conclusion! Seasonal trends are affecting our associations.
- This is an example of *bias* and *confounding*. It isn't that TV ads are better than Google ads; it's that November/December is a better buying season than February/March, an inherent bias.

SEASONALITY

- Let's take a look at the association between TV Ads and Sales while taking into account *seasonality* (recurring regular patterns over time).
- What are some examples of seasonality with relation to sales?

SEASONALITY

• A DAG incorporating seasonality might look like this.



ACTIVITY: KNOWLEDGE CHECK

ANSWER THE FOLLOWING QUESTIONS



- 1. What is bias?
- 2. What is confounding?
- 3. What could we do differently in this example to avoid these elements?

DELIVERABLE

Answers to the above questions

A FEW KEY TAKEAWAYS

- It is important to have deep subject area knowledge to be aware of biases in your field. This knowledge supplements statistical techniques.
- A DAG can be a useful tool for thinking through the logic of your model.
- There is a difference between causation and correlation. Statistics usually show *correlation*, not *causation* (remember our smoking example).
- Good data is important. Your analysis is only as good as your understanding of the problem and the data you have to work with.

INTRODUCTION

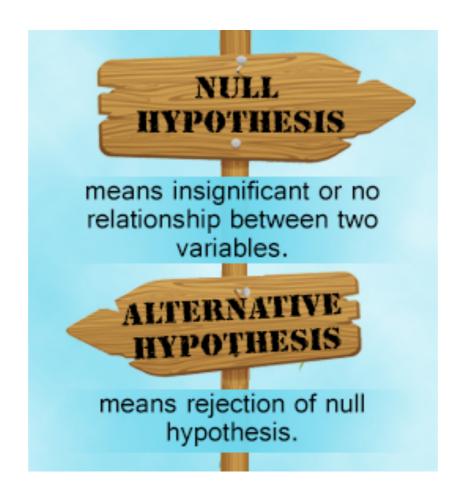
HYPOTHESIS TESTING

HYPOTHESIS TESTING

- How can we tell the difference between two groups of observations (e.g. smokers vs. non-smokers)?
- Imagine we are testing the health of smokers vs. non-smokers. At a cursory glance, our results may show that smokers are marginally healthier than non-smokers.
- Are they healthier due to random chance or is there a statistically significant difference? Maybe we happened to assemble a strange group of smoking triathletes and a group of non-smoking couch potatoes.
- This is where hypothesis testing can help.

HYPOTHESIS TESTING STEPS

• First, you need a hypothesis to test, referred to as the *null hypothesis*. The opposite of this would be the *alternative hypothesis*.



HYPOTHESIS TESTING STEPS

- For example, if we want to test the relationship between gender and sales, we may have the following hypotheses.
- Null hypothesis: There is no relationship between Gender and Sales.
- Alternative hypothesis: There is a relationship between Gender and Sales.

HYPOTHESIS TESTING STEPS

- Once you have your hypotheses, you can check whether the data supports rejecting the null hypothesis or failing to reject the hypothesis.
- **Note**: Failing to reject the null is **NOT** the same as accepting the alternate. While the alternative hypothesis **might** be true, we don't have enough data to support that claim specifically.
- Keep this in mind so you don't overstate your findings.

HYPOTHESIS TESTING CASE STUDY

HYPOTHESIS TESTING CASE STUDY

- We're going to walk through Part 1 of the guided-demo-starter-code notebook in the class repo for lesson 4.
- There are several questions to answer. We'll answer those questions in small groups and then discuss with the class.

ACTIVITY: KNOWLEDGE CHECK

ANSWER THE FOLLOWING QUESTIONS



- 1. What is the null hypothesis?
- 2. Why is this important to use?

DELIVERABLE

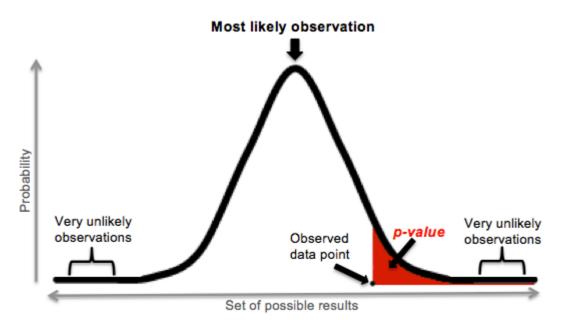
Answers to the above questions

INTRODUCTION

FINDINGS YOUR

- We know how to carry out a hypothesis test, but how do we tell if the association we found is *statistically significant*?
- Statistical significance is the likelihood that a result or relationship is caused by something other than random chance.
- Statistical hypothesis testing is traditionally employed to determine if a result is statistically significant or not.

• Typically, a cut point of 5% is used. This means that we say something is statistically significant if there is a less than a 5% chance that our finding was due to random chance alone.



A p-value (shaded red area) is the probability of an observed (or more extreme) result arising by chance

TABLE 1
Relationship between Common Language and Hypothesis Testing

COMMON LANGUAGE	STATISTICAL STATEMENT	CONVENTIONAL TEST THRESHOLD
"Statistically significant" "Unlikely due to chance"	The null hypothesis was rejected.	P < 0.05
"Not significant" "Due to chance"	The null hypothesis could not be rejected.	P > 0.05

- When we present results, we say we found something significant using this criteria.
- We will use an example to dive further into this and understand p-values and confidence intervals.

P-VALUES AND CONFIDENCE INTERVALS CASE STUDY

P-VALUES AND CONFIDENCE INTERVALS CASE STUDY

- We're now going to walk through Part 2 of the guided-demo-starter-code notebook in the class repo for lesson 4.
- There are several questions to answer. We'll answer those questions in small groups and then discuss with the class.

ACTIVITY: KNOWLEDGE CHECK

ANSWER THE FOLLOWING QUESTIONS



1. What does a 95% confidence interval indicate?

DELIVERABLE

Answers to the above questions

DEMO

A/BTESTING

INDEPENDENT PRACTICE

INTERPRETING RESULTS

ACTIVITY: INTERPRETING RESULTS



DIRECTIONS (35 minutes)

- 1. Using the lab-start-code-4, you will look through a variety of analyses and interpret the findings.
- 2. You will be presented with a series of outputs and tables from a published analysis.
- 3. Read the outputs and determine if the findings are statistically significant or not.

DELIVERABLE

Answers to the questions in the notebook

CONCLUSION

LAB REVIEW

LAB REVIEW

• Let's review the answers to the questions in the labs.

• Any other questions?

COURSE

BEFORE NEXT CLASS

BEFORE NEXT CLASS

DUE DATE

Project: Unit Project 1

LESSON

Q&A

LESSON

EXITICKET

DON'T FORGET TO FILL OUT YOUR EXIT TICKET