

H — check matrix

y — vector to decode

$L_1(y) = (f(y_1), f(y_2), \dots, f(y_n))$, where

$$f(x) = \begin{cases} 1, & x = 0 \\ -1, & \text{else} \end{cases}$$

$L_2(S) = (g(S_1), g(S_2), \dots, g(S_n))$, where

$$g(x) = \begin{cases} 1, & x < 0 \\ 0, & \text{else} \end{cases}$$

Algorithm

0. **Init:** $M_+ = 0$, $S = L_1(y)$,
1. **Calculate M^- :** $M_{ji}^- = H_{ji}(S_i - M_{ji}^+)$,
2. **Calculate M^+ :** $M_{ji}^+ = H_{ji} \cdot \left(\min_{k \neq i, H_{jk}=1} |M_{jk}^-| \right) \cdot \left(\prod_{k \neq i, H_{jk}=1} \text{sgn } M_{jk}^- \right)$,
3. **Calculate syndrome:** $S_i = L(y) + \sum_j M_{ji}^+$,
4. **Check syndrome:** if $Hy_i^T = 0$ then **decoded** (result is y_i), else **goto (1)**, where $y_i = L_2(S_i)$.