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You can download the sources of this presentation here:

**[github.com/severin-lemaignan/lecture-hri-data-analysis](https://github.com/severin-lemaignan/lecture-hri-data-analysis)**



**UWE  
Bristol**

University  
of the  
West of  
England



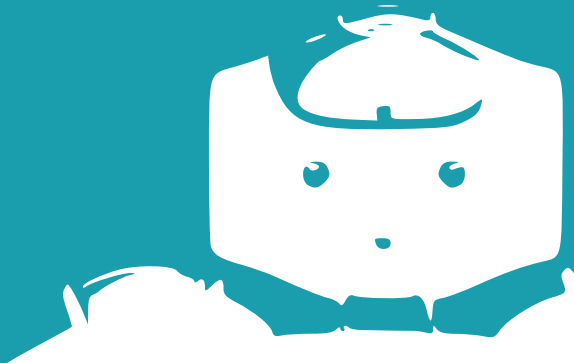
University of  
**BRISTOL**

# Human-Robot Interaction

## Data Analysis for HRI

Séverin Lemaignan

**Bristol Robotics Lab**  
University of the West of England



## IN THIS LECTURE

- Two questions to answer:

## IN THIS LECTURE

- Two questions to answer:  
Are my groups different?

## IN THIS LECTURE

- Two questions to answer:
  - Are my groups different?
  - Does a specific variable explain the difference?

## IN THIS LECTURE

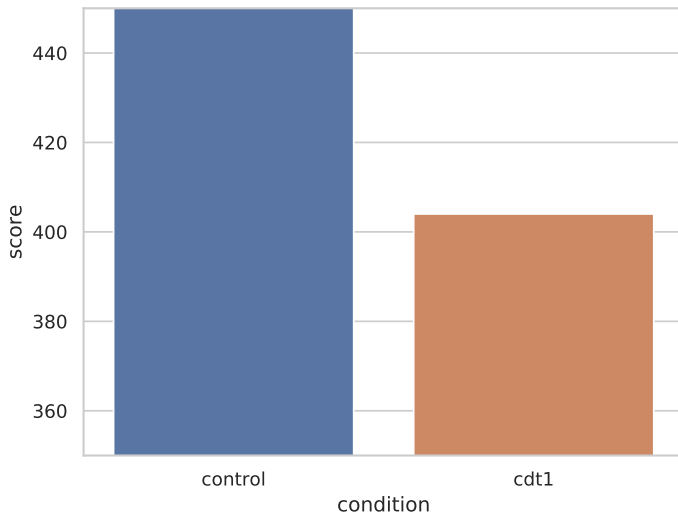
- Two questions to answer:
  - Are my groups different?
  - Does a specific variable explain the difference?
- Hands-on data analysis with Python!

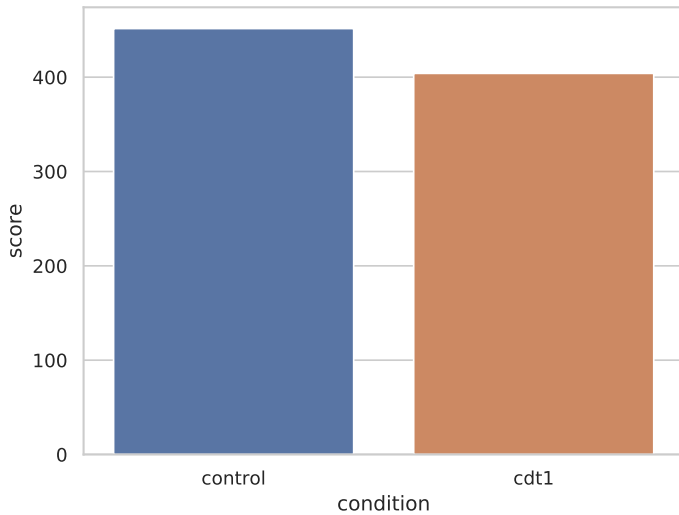
ARE MY TWO GROUPS DIFFERENT?

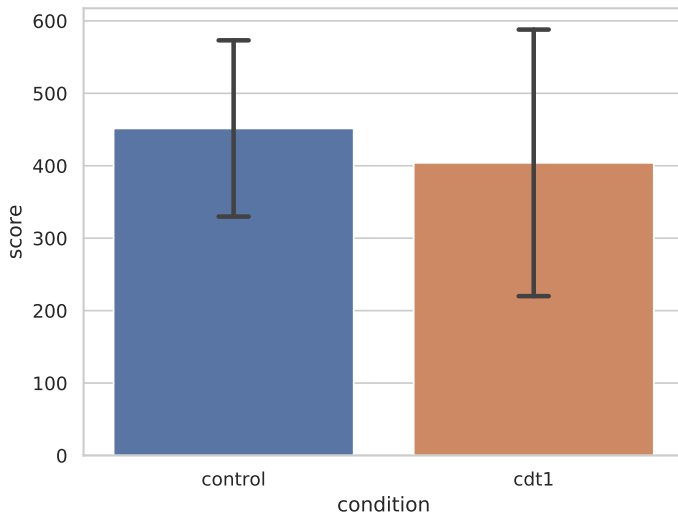
## A DATASET

pptID	age	condition	score	heartrate
1	22	control	643	76
2	26	cdt1	234	72
3	24	control	356	73
4	24	cdt1	587	75
5	29	cdt1	561	75
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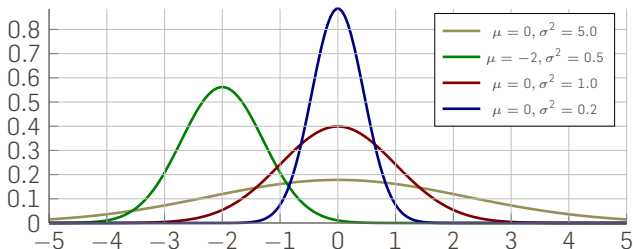


Is there a difference?

- Are the distributions the same?
- How big the difference?
- Could chance explain that difference?

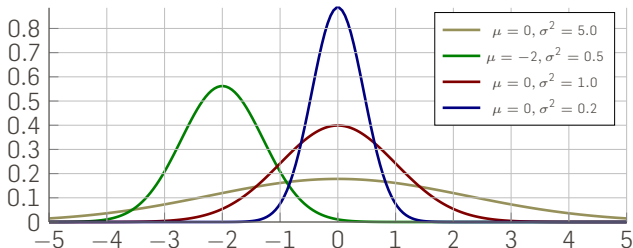
## IS THE DISTRIBUTION THE SAME?

Data often (but not always!) follows a **normal** (or Gaussian) distribution. Two parameters: **mean**  $\mu$  and **variance**  $\sigma^2$ .



## IS THE DISTRIBUTION THE SAME?

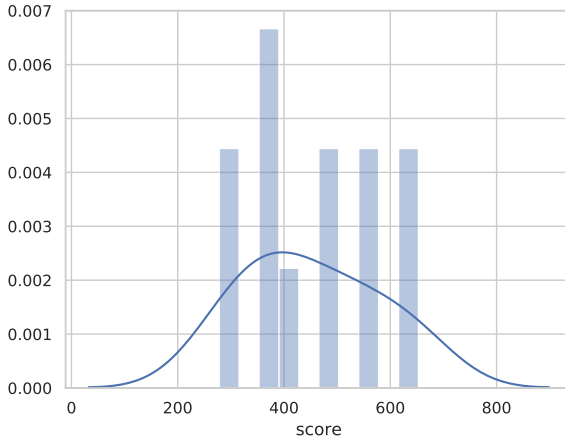
Data often (but not always!) follows a **normal** (or Gaussian) distribution. Two parameters: **mean**  $\mu$  and **variance**  $\sigma^2$ .



Many statistical tests only work if the underlying data follows a normal distribution – so-called **parametric tests**.

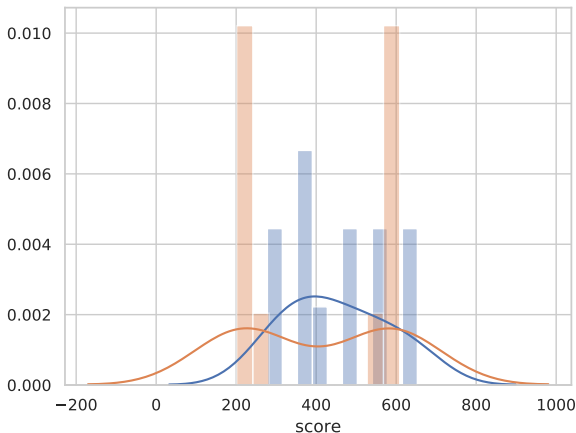
*You need to check that your data is normally distributed first!  
(for instance, by plotting it)*

# COMPARE DISTRIBUTIONS (HISTOGRAMS, DENSITY)



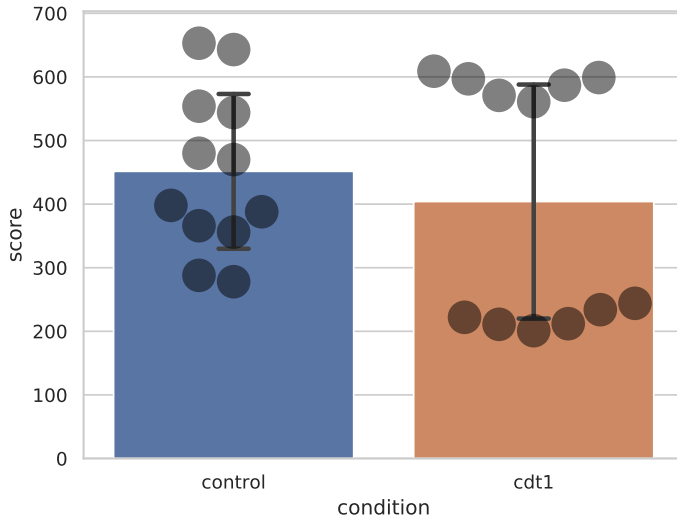
Control group

## COMPARE DISTRIBUTIONS (HISTOGRAMS, DENSITY)



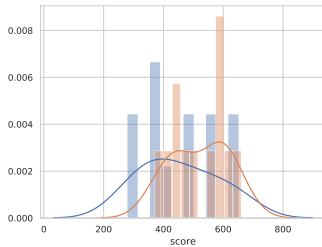
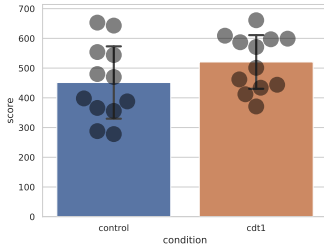
Control + condition group → beware the bimodal distribution!



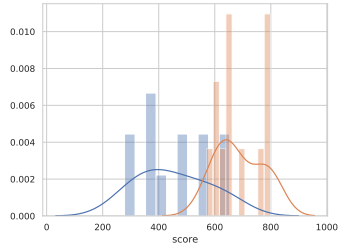
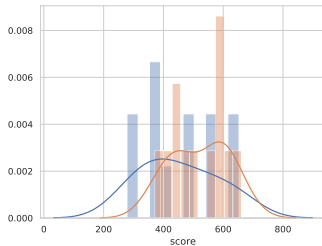
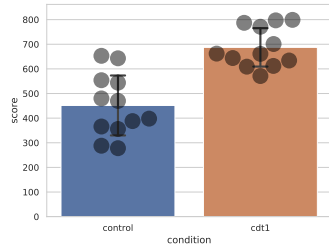
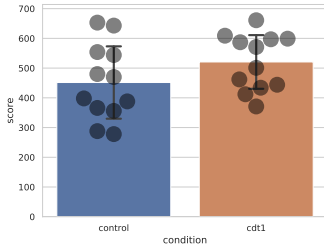


Show the underlying data!

## TWO ADDITIONAL DATASETS



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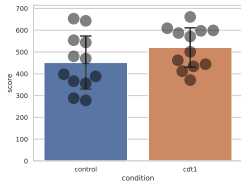


Are my two groups different?  
ooooooooo●ooooooooo

Does one variable explain the difference?  
oooooooo

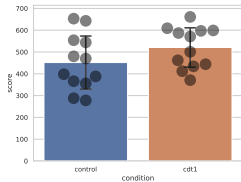
In practice  
oooo

## HOW BIG IS THE DIFFERENCE?

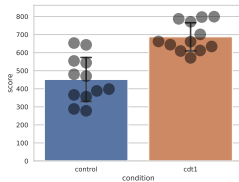


	mean	std
cdt1	516.5	85.3
control	451.5	127.1
$\mu_1 - \mu_2$	69.2	

# HOW BIG IS THE DIFFERENCE?

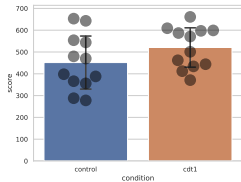


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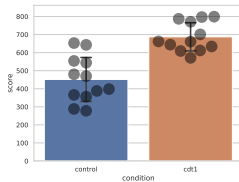


	mean	std
cdt1	687.3	81.5
control	451.5	127.1
$\mu_1 - \mu_2$	235.8	

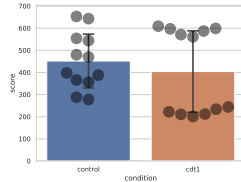
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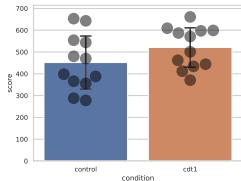


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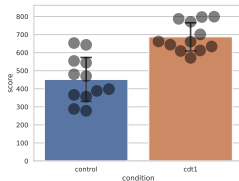


	mean	std
cdt1	404.0	192.2
control	451.5	127.1
$\mu_1 - \mu_2$	47.5	

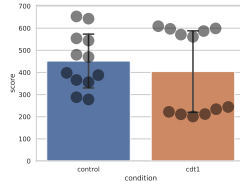
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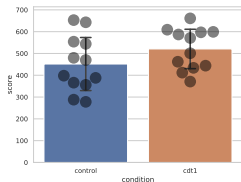
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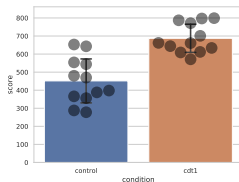
	mean	std
cdt1	404.0	192.2
control	451.5	127.1
$\mu_1 - \mu_2$	47.5	

**does not account for the variance in the dataset**

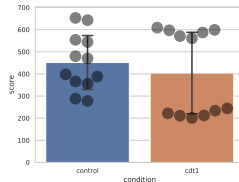
# HOW BIG IS THE DIFFERENCE?



	mean	std
cdt1	516.5	85.3
control	451.5	127.1
$\mu_1 - \mu_2$	69.2	
$\frac{\mu_1 - \mu_2}{\sigma}$	0.62	



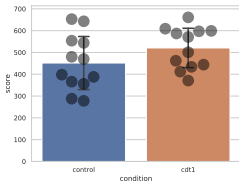
	mean	std
cdt1	687.3	81.5
control	451.5	127.1
$\mu_1 - \mu_2$	235.8	
$\frac{\mu_1 - \mu_2}{\sigma}$	2.21	



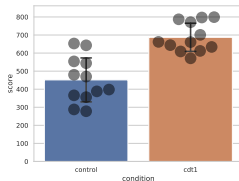
	mean	std
cdt1	404.0	192.2
control	451.5	127.1
$\mu_1 - \mu_2$	47.5	
$\frac{\mu_1 - \mu_2}{\sigma}$	0.29	



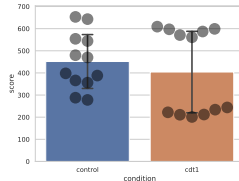
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A common measure of effect size: **Cohen's  $d$**  =  $\frac{\mu_1 - \mu_2}{\sigma}$

→ Interactive visualisation and interpretation of Cohen's  $d$

## DIFFERENCE DUE TO CHANCE?

A statistical hypothesis test makes an assumption about the outcome, called the **null hypothesis**.

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⇒ **Meaning of a low *p*-value?**

To interpret *p*, you need to choose a *significance level*  $\alpha$ .  
For instance, 10% (0.1), 5% (0.05), 2% (0.02)...

$$p = 0.05$$

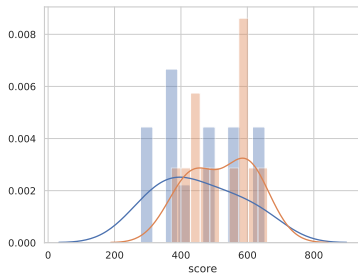
'There's only 5% of chance of observing these distributions if my null hypothesis is true (ie, no difference between my groups).'

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- If parametric data, **Student's  $t$ -test**

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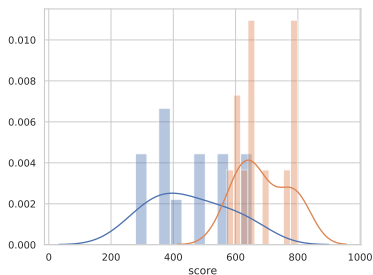
---

$t$ statistic	-1.51
$p$	0.155

---

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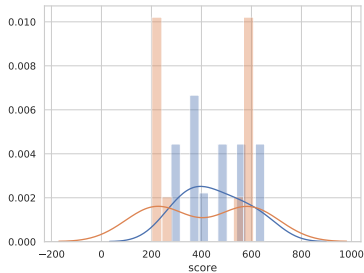
---

$t$ statistic	-5.41
$p$	< 0.001

---

## HOW TO CALCULATE $P$ ?

- If parametric data, **Student's  $t$ -test**



$t$ statistic	0.71
$p$	0.48

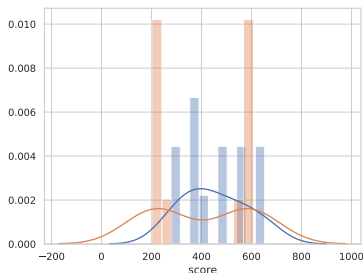


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$U$ statistic	46.0
$p$	0.07

See [Wikipedia page](#) for examples and interpretation of  $U$

## IMPACT OF $N$ ?

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## BE CAREFUL WITH "STATISTICALLY SIGNIFICANT"!

<b>gender</b>	<b>iq</b>
male	76.51
male	76.53
female	76.66
female	76.65
female	76.64
female	76.63
male	76.54
female	76.64
male	76.51
female	76.60
female	76.63
male	76.52
female	76.64
male	76.51
female	76.60
female	76.63

## BE CAREFUL WITH "STATISTICALLY SIGNIFICANT"!

---

<i>t</i> statistic	12.52
<i>p</i>	< 0.001
Mean female	76.64
Mean male	76.54

---

$$M_{female} > M_{male}, p < 0.001$$

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Girls are more intelligent! We knew it!



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### Cohen's *d*

$$d = \frac{\mu_1 - \mu_2}{\sigma} = 4.12 \Rightarrow \text{high, because } \sigma \text{ very low}$$

# STATISTICAL POWER ANALYSIS

## Statistical power

The statistical power of a hypothesis test is the probability of detecting an effect, if there is a true effect present to detect.

or:

## Statistical power

The statistical power of the test is the probability that the test correctly rejects a *false* null hypothesis.

# STATISTICAL POWER ANALYSIS

## Types of errors

- **Type I error:** Reject the null hypothesis when there is in fact no significant effect (*too optimistic!*)
- **Type II error:** Not reject the null hypothesis when there is a significant effect (*too pessimistic!*)

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## The boy who cried wolf

- **Type I error:**  
*"there's a wolf!"* (too optimistic: there's no wolf!)
- **Type II error:**  
*...the villager don't respond when there really is a wolf*  
(too pessimistic: there is indeed a wolf!)

# STATISTICAL POWER ANALYSIS

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The statistical power of a hypothesis test is the probability of detecting an effect, if there is a true effect present to detect.

$$\text{Power} = 1 - \text{Type II Error}$$

# STATISTICAL POWER ANALYSIS

A puzzle with four pieces:

- **Effect size**
- **Sample size**
- **Significance** (chance of Type I error – found inexistant effect)
- **Statistical power** ( $1 -$  chance of Type II error – missed the effect)



## EXAMPLE: POWER ANALYSIS OF STUDENT'S $T$ -TEST

- **Effect size:** Cohen's  $d > 0.8$
- **Significance:** 5%
- **Statistical power:** 80%
- **Sample size?**

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 $n = 25.5$  (per condition)

A good read on statistical power analysis:

A Gentle Introduction to Statistical Power and Power Analysis in  
Python

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- 2 groups, independent measures, normal distribution:  
**Independent  $t$ -test**

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Always report an **effect size** (for instance, **Cohen's  $d$** )

Keep a close eye on your data distributions (**plot them**)

DOES ONE VARIABLE EXPLAIN THE  
DIFFERENCE?

## OUR DATASET

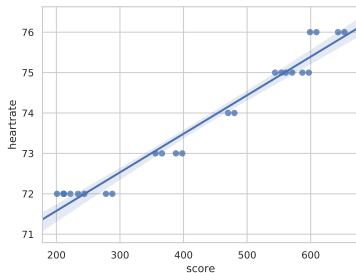
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14	21	cdt1	597	75
15	22	cdt1	571	75
16	30	control	554	75

# ASSOCIATION

**What is the degree of association between two variables?**

→ **main tool: correlation**

# PEARSON CORRELATION



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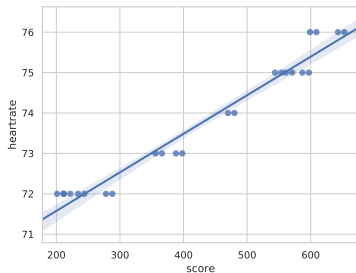
Pearson's correlation

$\rho$  0.98

$p$  < 0.001

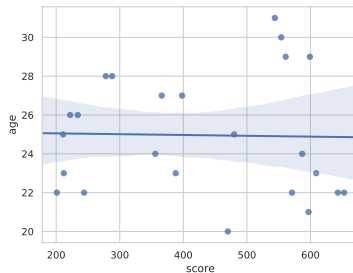
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# PEARSON CORRELATION



Pearson's correlation

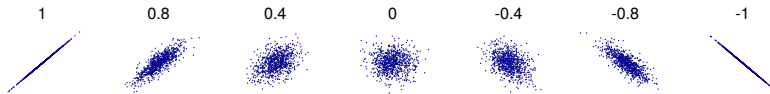
$\rho$	0.98
$p$	< 0.001



Pearson's correlation

$\rho$	-0.022
$p$	0.92

# INTERPRETATION OF $\rho$

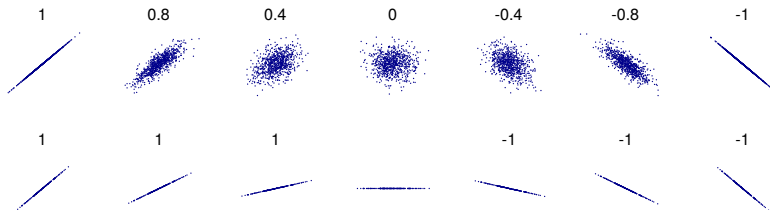


$\rho$  reflects the degree of linearity and direction

Source: *Wikipedia*

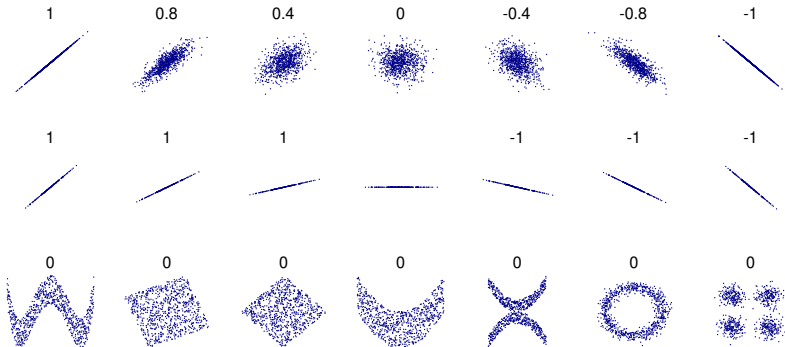


# INTERPRETATION OF $\rho$



$\rho$  does not reflect the slope of the regression line

# INTERPRETATION OF $\rho$



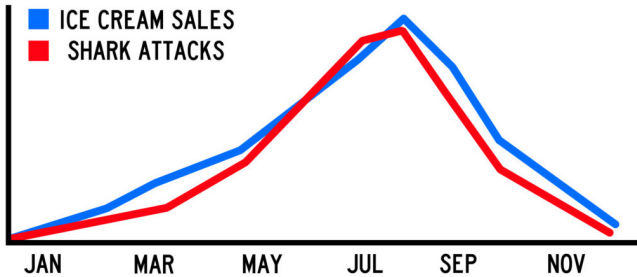
$\rho$  does not capture non-linear interactions

Source: *Wikipedia*

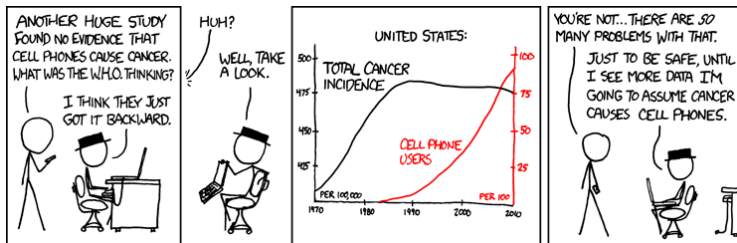
## OTHER MEASURES OF ASSOCIATION

- Non-parametric ordinal data: **Spearman rank correlation**
- Association between categorical data (for instance, relationship between 'gender' and 'preferred style of cuisine'): **Pearson's Chi-Square  $\chi^2$**

# CORRELATION IS NOT CAUSATION

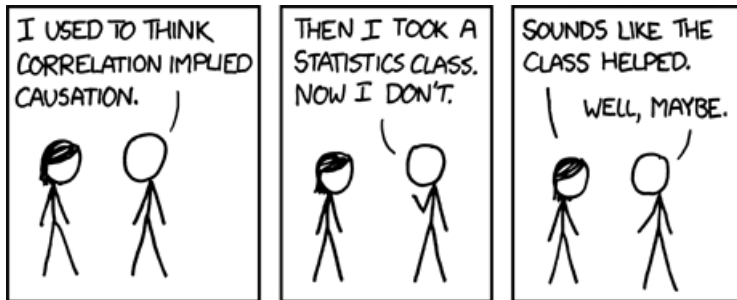


# CORRELATION IS NOT CAUSATION



Source: XKCD

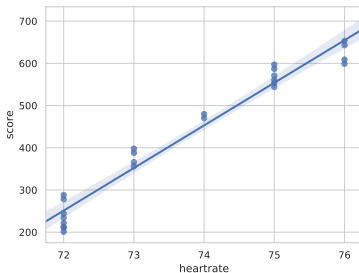
# CORRELATION IS NOT CAUSATION



Source: XKCD

## CORRELATION IS NOT CAUSATION

Be careful when tempted to write something like:



*“the significant positive correlation between the heart rate and the score shows that you need to have a high heart rate to win”*

## TO CONCLUDE: ANSCOMBE'S QUARTET

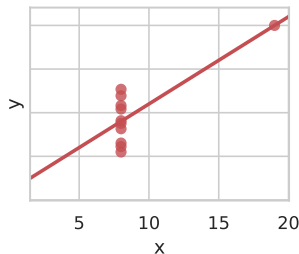
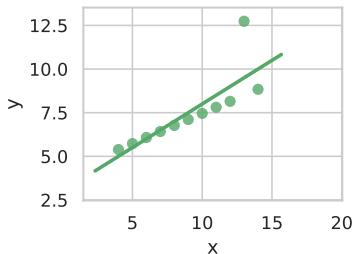
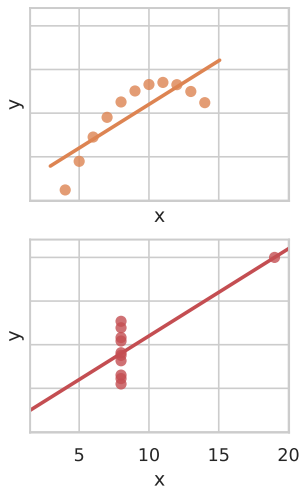
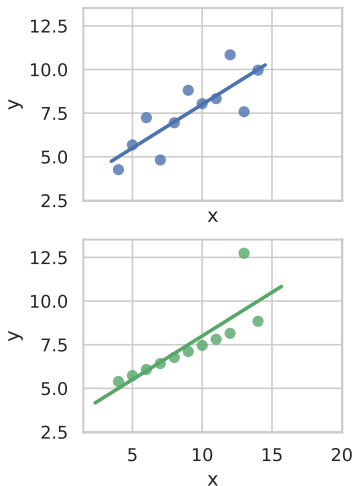
I		II		III		IV	
<i>x</i>	<i>y</i>	<i>x</i>	<i>y</i>	<i>x</i>	<i>y</i>	<i>x</i>	<i>y</i>
10.0	8.04	10.0	9.14	10.0	7.46	8.0	6.58
8.0	6.95	8.0	8.14	8.0	6.77	8.0	5.76
13.0	7.58	13.0	8.74	13.0	12.74	8.0	7.71
9.0	8.81	9.0	8.77	9.0	7.11	8.0	8.84
11.0	8.33	11.0	9.26	11.0	7.81	8.0	8.47
14.0	9.96	14.0	8.10	14.0	8.84	8.0	7.04
6.0	7.24	6.0	6.13	6.0	6.08	8.0	5.25
4.0	4.26	4.0	3.10	4.0	5.39	19.0	12.50
12.0	10.84	12.0	9.13	12.0	8.15	8.0	5.56
7.0	4.82	7.0	7.26	7.0	6.42	8.0	7.91
5.0	5.68	5.0	4.74	5.0	5.73	8.0	6.89



## TO CONCLUDE: ANSCOMBE'S QUARTET

Property	Value
Mean of x	9
Sample variance of x	11
Mean of y	7.50
Sample variance of y	4.125
Correlation between x and y	0.816
Linear regression line	$y = 3.00 + 0.500x$
Coefficient of determination of the linear regression	0.67

## TO CONCLUDE: ANSCOMBE'S QUARTET



IN PRACTICE

# THE TOOLS

Data analysis tools:

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- Python's Pandas: **[pandas.pydata.org](http://pandas.pydata.org)**

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Jupyter notebooks are a great way of creating an interactive, easy-to-follow, data analysis.

## (SIDE NOTE ON PYTHON FOR DATA ANALYSIS)

Python is the leading language in data analysis/data mining/machine learning. **Learn it!**

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- `anaconda` (and a few other): Python distribution for scientific computing

**Let's give it a go!**