# 1 Parameterizing the model

This section describes how we set the model's parameters. First, we estimate the extent to which consumers 'splurge' when receiving an income shock. Given the lack of empirical evidence on the marginal propensity to consume over time for the US, we instead use Norwegian data to estimate the splurge. Specifically, we calibrate our model to the Norwegian economy and match evidence from Norway on the profile of the marginal propensity to spend over time and across different wealth levels, as provided by Fagereng, Holm, and Natvik (2021).<sup>1</sup>

Second, we set up the full model on U.S. data, taking the splurge factor as given from the Norwegian estimation. In the full model, agents differ according to their level of education and their subjective discount factors. A subset of the parameters in the model are calibrated equally for all types, and some parameters are calibrated to be specific to each education group. Finally, a distribution of subjective discount factors is estimated separately for each education group to match features of each within-group liquid wealth distribution.

### 1.1 Estimation of the splurge factor

The splurge allows us to capture the shorter- and longer-term response of consumption to income shocks, especially for consumers with significant liquid wealth. The main aim of this paper, however, is to rank consumption stimulus policies, not to provide a microfoundation for the splurging behavior. We view the splurge factor as a model device that enables us to rank the policies in a model that is consistent with the best available micro-evidence of spending patterns over time after a transitory income shock. In Appendix ?? we provide results from our model without a splurge factor. There we show that such a model provides a worse fit to the moments in the data that we are interested in, but not dramatically so, and that our conclusions regarding the ranking of the policies are not affected. However, in our view, this version of the model requires households with unreasonably low discount factors.

The specific exercise we carry out in this section, is to show that our model can account well for the results of Fagereng, Holm, and Natvik (2021), who study the effect of lottery winnings in Norway on consumption using millions of records from the Norwegian population registry. We calibrate our model to reflect the Norwegian economy and, using their results, estimate the splurge factor, as well as the distribution of discount factors in the population, to match two empirical moments.

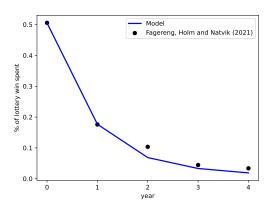
First, we take from Fagereng, Holm, and Natvik (2021) the marginal propensity to consume out of a one-period income shock. We target not only the initial (aggregate) response of consumption to the income shock, but also the subsequent effect on consumption in years one through four after the shock. We also target the initial consumption response in the cross-section, i.e. across the quartiles of the liquid wealth distribution,

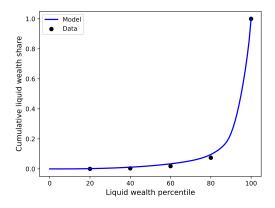
<sup>&</sup>lt;sup>1</sup>Appendix ?? discusses an alternative calibration method, which solely relies on US data. The main results derived in that calibration are in line with those discussed in the main text.

for which empirical estimates are also provided. The shares of lottery winnings expended at different time horizons, as found in Fagereng, Holm, and Natvik (2021), are plotted in figure ??. Table ?? (second row) shows the initial consumption response across liquid wealth quartiles.

Second, we match the steady-state distribution of liquid wealth in the model to its empirical counterpart. Because of the lack of data on the liquid wealth distribution in Norway, we use the corresponding data from the United States, assuming that liquid wealth inequality is comparable across these countries.<sup>2</sup> Specifically, we impose as targets the cumulative liquid wealth shares for the entire population at the 20th, 40th, 60th, and 80th income percentiles, which, in data from the Survey of Consumer Finances (SCF) in 2004 (see section ?? for further details), equal 0.03 percent, 0.35 percent, 1.84 percent, and 7.42 percent, respectively. Hence, 92.6 percent of the total liquid wealth is held by the top income quintile. We also target the mean liquid wealth to income ratio of 6.60. The data are plotted in figure ??.

Figure 1 Model fit to spending behavior and wealth distribution





(a) Spending dynamics after lottery win

(b) Liquid wealth distribution

Note: This figure demonstrates the calibration of the splurge factor (Section ??). Panel (a) shows the model's fit to the dynamic consumption response following lottery wins in Norway, as estimated by Fagereng, Holm, and Natvik (2021) using millions of population registry records. The splurge factor of  $\varsigma=0.249$  allows the model to match both the high initial MPC and the gradual spending over subsequent years. Panel (b) shows the model's fit to the U.S. liquid wealth distribution from the 2004 SCF, with 92.6% of liquid wealth held by the top income quintile. See Section ?? for the liquid wealth definition following Kaplan and Violante (2014).

For this estimation exercise, the remaining model parameters are calibrated to reflect the Norwegian economy. Specifically, we set the real interest rate to 2 percent annually and the unemployment rate to 4.4 percent, in line with Aursland, Frankovic, Kanik, and Saxegaard (2020). The quarterly probability to survive is calibrated to 1-1/160, reflecting an expected working life of 40 years. Aggregate productivity growth is set

<sup>&</sup>lt;sup>2</sup>Data from the Norwegian tax registry contains information on liquid assets, but not liquid debt. Only total debt is reported – which is mainly mortgage debt. Therefore, we cannot construct liquid wealth as Kaplan and Violante (2014) can for the U.S.

Table 1 MPC's across wealth quartiles and in total

Targeting K/Y and avg MPC by quartile

	1st WQ	2nd WQ	3rd WQ	4th WQ	Agg	K/Y
Model	0.27	0.49	0.60	0.66	0.50	6.59
Data	0.39	0.39	0.55	0.66	0.51	6.60

to 1 percent annually, following Kravik and Mimir (2019). The unemployment net replacement rate is calibrated to 60 percent, following OECD (2020). Finally, we set the real interest rate on liquid debt to 13.6 percent, following data from the Norwegian debt registry Gjeldsregistret (2022).<sup>3</sup>

Estimates of the standard deviations of the permanent and transitory shocks are taken from Crawley, Holm, and Tretvoll (2024), who estimate an income process on administrative data for Norwegian males from 1971 to 2014. The estimated annual variances for the permanent and transitory shocks are 0.004 and 0.033, respectively.<sup>4</sup> As in Carroll, Crawley, Slacalek, Tokuoka, and White (2020), these are converted to quarterly values by multiplying the permanent and transitory shock variances by 1/4 and 4, respectively. Thus, we obtain quarterly standard deviations of  $\sigma_{\psi} = 0.0316$  and  $\sigma_{\xi} = 0.363$ .

Using the calibrated model, we simulated unexpected lottery winnings and calculate the share of the lottery spent in each year. Specifically, each simulated agent receives a lottery win in a random quarter of the first year of the simulation. The size of the lottery win is itself random and spans the range of lottery sizes found in Fagereng, Holm, and Natvik (2021). The estimation procedure minimizes the distance between the target and model moments by selecting the splurge factor and the distribution of discount factors in the population, where the latter are assumed to be uniformly distributed in the range  $[\beta - \nabla, \beta + \nabla]$ . We approximate the uniform distribution of discount factors with a discrete approximation and let the population consist of seven different types.

The estimation yields a splurge factor of 0.249 and a distribution of discount factors described by  $\beta=0.968$  and  $\nabla=0.0578$ . Given these estimated parameters and the remaining calibrated ones, the model is able to replicate the time path of consumption in response to a lottery win from Fagereng, Holm, and Natvik (2021) and the targeted distribution of liquid wealth very well, see Figure ??. Also, the targeted moments discussed in Table ?? are captured relatively well. In particular, the model is able to account for the empirical fact, in the first column, that the MPC for high-wealth agents is substantially larger than zero.

<sup>&</sup>lt;sup>3</sup>Specifically, we determine the average volume-weighted interest rate on liquid debt, which consists of consumer loans, credit and payment card debt and all other unsecured debt. We use data from December 2019. Note that although these data let us pin down aggregate quantities, they do not solve the issue referred to in footnote ??, since we cannot link them to the tax registry at the individual level. We set the borrowing limit on liquid debt to zero.

<sup>&</sup>lt;sup>4</sup>As shown in Crawley, Holm, and Tretvoll (2024), an income process of the form that we use here is more accurately estimated using moments in levels not differences. Hence, we take the numbers from column 3 of Panel C in their table 4.

### 1.2 Data on permanent income, liquid wealth, and education

Before we move on to the parameterization of the full model, we describe in detail the data that we use to get measures of permanent income, liquid wealth, and the division of households into educational groups in the United States. We use data on the distribution of liquid wealth from the 2004 wave of the SCF. We restrict our attention to households where the head is of working age, which we define to be in the range from 25 to 62. The SCF-variable "normal annual income" is our measure of the household's permanent income, and, to exclude outliers, we drop the observations that make up the bottom 5 percent of the distribution of this variable. The smallest value of permanent income for households in our sample is thus \$16,708.

Liquid wealth is defined as in Kaplan and Violante (2014) and consists of cash, money market, checking, savings, and call accounts; directly held mutual funds; and stocks and bonds. We subtract off liquid debt, which is the revolving debt on credit card balances. Note that the SCF does not contain information on cash holdings, so these are imputed with the procedure described in Appendix B.1 of Kaplan and Violante (2014), which also describes the credit card balances that are considered part of liquid debt. We drop any households that have negative liquid wealth.

Households are classified into three educational groups. The first group, "Dropout," applies to households where the head of household has not obtained a high school diploma; the second group, "Highschool," includes heads of households who have a high school diploma and those who, in addition, have some years of college education without obtaining a bachelor's degree; and the third group, "College," consists of heads of households who have obtained a bachelor's degree or higher. With this classification of the education groups, the Dropout group makes up 9.3 percent of the population, the Highschool group 52.7 percent, and the College group 38.0 percent.

With our sample selection criteria, we are left with a sample representing about 61.3 million U.S. households.

### 1.3 Parameters in the full model

With households classified into the three education groups using the SCF data, we proceed to set the parameters of the model as follows. First, we calibrate a set of parameters that apply to all types of households in the model. Second, we calibrate another set of parameters that are specific to each education group to capture broad differences across these groups. Finally, given the calibrated parameters we estimate discount factor distributions for each education group that allow us to match the distribution of liquid wealth in each group.

The model is a simplified model for households in that we do not take into account heterogeneity across household size or composition. The households are ex-ante heterogeneous in their subjective discount factors as well as their level of education. We classify the education level of the household based on the education of the head of the household, and we typically think of individual characteristics as applying to that person.

A period in the model is one quarter. This choice makes it realistic to consider stimulus policies that are implemented in the same period as a recession starts.

#### 1.3.1 Calibrated parameters — Normal times

Table ?? presents our calibration of the model parameters in normal times. Panel A lists parameters that are calibrated equally across all types in the model, and Panel B lists parameters in the model that are education specific. In the next subsection we present how certain model parameters change when the economy enters a recession.

Preferences, survival and interest rates. All households are assumed to have a coefficient of relative risk aversion equal to  $\gamma = 2$ . We also assume that all households have the same propensity to splurge out of transitory income gains and set  $\varsigma = 0.249$ , the value estimated in section ??. However, each education group is divided into types that differ in their subjective discount factors. The distributions of discount factors for each education group are estimated to fit the distribution of liquid wealth within that group, and this estimation is described in detail in section ??. Regardless of type, households face a constant survival probability each quarter. This probability is set to 1 - 1/160, reflecting an expected working life of 40 years. The real interest rate on households' savings is set to 1 percent per quarter.

Labor market risk while employed. When consumers are born, they receive an initial level of permanent income. This initial value is drawn from a log-normal distribution that depends on the education level the household is born with. For each education group, the parameters of the distribution are determined by the mean and standard deviation of log-permanent income for households in that group where the head of the household is of age 25 in the SCF 2004. For the Dropout group, the mean initial value of quarterly permanent income is \$6,200; for the Highschool group, it is \$11,100; and for the College group, it is \$14,500. The standard deviations of the log-normal distributions for each group are, respectively, 0.32, 0.42, and 0.53.

While households remain employed, their income is subject to both permanent and transitory idiosyncratic shocks. These shocks are distributed equally for the three education groups. The standard deviations of these shocks are taken from Carroll, Crawley, Slacalek, Tokuoka, and White (2020), who set the standard deviations of the transitory and permanent shocks to  $\sigma_{\xi} = 0.346$  and  $\sigma_{\psi} = 0.0548$ , respectively.

Permanent income also grows, on average, with a growth factor  $\Gamma_{e(i)}$  that depends on the level of education. These average growth rates are based on numbers from Carroll, Crawley, Slacalek, and White (2020), who construct age-dependent expected permanent income growth factors using numbers from Cagetti (2003) and fit the age-dependent numbers to their life-cycle model. We construct the quarterly growth rates of permanent income in our perpetual-youth model by taking the average of the age-dependent growth rates during a household's working life. The average gross quarterly growth rates that we obtain for the three education groups are then  $\Gamma_d = 1.0036$ ,  $\Gamma_h = 1.0045$ , and  $\Gamma_c = 1.0049$ .

**Unemployment.** Consumers also face the risk of becoming unemployed and will then

**Table 2** Calibrated Model Parameters — Normal times

Panel A: Parameters that apply to all types

Parameter	Notation	Value
Risk aversion	$\gamma$	2.0
Splurge	ς	0.249
Survival probability, quarterly	1 - D	0.994
Risk free interest rate, quarterly (gross)	R	1.01
Standard deviation of transitory shock	$\sigma_{\xi}$	0.346
Standard deviation of permanent shock	$\sigma_{\psi}$	0.0548
Unemp. benefits replacement rate (share of PI)	$ ho_b$	0.7
Unemp. income w/o benefits (share of PI)	$ ho_{nb}$	0.5
Avg. dur. of unemp. benefits in normal times (quarters)		2
Avg. dur. of unemp. spell in normal times (quarters)		1.5
Prob. of leaving unemp.	$\pi_{ue}$	0.667
Consumption elasticity of aggregate demand effect	$\kappa$	0.3

Shows parameters calibrated the same for all types.

Panel B: Parameters calibrated for each education group

	Dropout	Highschool	College
Percent of population	9.3	52.7	38.0
Avg. quarterly PI of "newborn" agent (\$1000)	6.2	11.1	14.5
Std. dev. of log(PI) of "newborn" agent	0.32	0.42	0.53
Avg. quarterly gross growth factor for PI $(\Gamma_e)$	1.0036	1.0045	1.0049
Unemp. rate in normal times (percent)	8.5	4.4	2.7
Prob. of entering unemp. $(\pi_{eu}^e, percent)$	6.2	3.1	1.8

Shows parameters calibrated for each education group. ("PI" is permanent income).

have access to unemployment benefits for a certain period. The parameters describing the unemployment benefits in normal times are based on the work of Rothstein and Valletta (2017), who study the effects on household income of unemployment and of running out of eligibility for benefits. The unemployment benefits replacement rate is thus set to  $\rho_b = 0.7$  for all households, and when benefits run out, the unemployment replacement rate without any benefits is set to  $\rho_{nb} = 0.5$ . These replacement rates are set as a share of the households' permanent income and are based on the initial drop in income upon entering an unemployment spell, presented in figure 3 in Rothstein and Valletta (2017).<sup>5</sup>

<sup>&</sup>lt;sup>5</sup>See the lines for their UI exhaustee sample including and excluding UI income. Rothstein and Valletta (2017) also point out that "UI benefits replace about 40 percent of the lost earnings on average" (page 894). For a household with two income earners with equal income, these findings would mean that income drops to 70 percent when one earner becomes unemployed and to 50 percent when benefits run out. In this paper we ignore several of the channels studied by Rothstein and Valletta (2017) such

The duration of unemployment benefits in normal times is set to two quarters, so that our Markov transition matrix  $\Pi$  has four states. This length of time corresponds to the mean duration of unemployment benefits across U.S. states from 2004 to mid-2008 of 26 weeks, reported by Rothstein and Valletta (2017).

The probability of transitioning out of unemployment is set to match the average duration of an unemployment spell in normal times. In data from the Bureau of Labor Statistics, this average duration was 19.6 weeks or 1.5 quarters in 2004. We do not have data on education-specific duration rates, however, so we set the average duration of unemployment to 1.5 quarters for all households. This implies that the transition probability from unemployment to employment is set to  $\pi_{ue} = 2/3$ .

The Bureau of Labor Statistics provide data on unemployment rates for different education groups, and we match the average rate in each group in 2004 by setting an education-specific probability of transitioning from employment into unemployment. Note that this calibration strategy is consistent with the results in Mincer (1991) who finds that the main difference between education groups is in the incidence of unemployment, and not its duration.<sup>6</sup> More recent work by Elsby and Hobijn (2010) includes data up to 2009 and echoes Mincer's results.

The average unemployment rate in 2004 was 8.5 percent for the Dropout group, 4.4 percent for the Highschool group, and 2.7 percent for the College group. These values imply that the probabilities of transitioning into unemployment in normal times are  $\pi_{eu}^d = 6.2$  percent,  $\pi_{eu}^h = 3.1$  percent, and  $\pi_{eu}^c = 1.8$  percent, respectively.<sup>7</sup>

Finally, the strength of the aggregate demand effect in recessions is determined by the consumption elasticity of productivity. We follow Krueger, Mitman, and Perri (2016) and set this to  $\kappa=0.3$ .

#### 1.3.2 Calibrated parameters — Recession

Table ?? shows the model parameters that change when a recession hits. Panel A shows the change in two parameters that apply to all types, and Panel B shows changes in some parameters that differ across education groups. For completeness, panel C summarizes the remaining parameters describing how we model a recession and the three policies we consider as potential responses to a recession.

as within household insurance and other social programs that can provide income even after UI benefits have run out.

<sup>&</sup>lt;sup>6</sup>Mincer (1991) states that "the reduction of the incidence of unemployment [at higher education levels] is found to be far more important than the reduced duration of unemployment in creating the educational differentials in unemployment rates" (page 1).

<sup>&</sup>lt;sup>7</sup>Also note that the probability of transitioning from employment to unemployment is the probability of a job separation times the conditional probability of unemployment given a job separation. Mincer (1991) reports that both of these are lower for higher education levels. For our calibration, this means that a higher job finding rate within the quarter of the job separation for more educated workers translates into a lower probability of transitioning from employment to unemployment during a quarter. In that sense, our calibration is consistent with short-term job-finding rates being higher for more educated workers.

The two immediate changes that occur at the outset of a recession is that the unemployment rate doubles for all education groups, and the expected duration of an unemployment spell increases from 1.5 to 4 quarters. The duration of unemployment is the same across the three education groups, and this implies that the probability of leaving unemployment is set to  $\pi_{ue} = 0.25$  in a recession.

The increase in the expected duration of unemployment combined with the doubling of the education-specific unemployment rates pin down new values for the probabilities of transitioning from employment to unemployment during the recession. Due to the large increase in the unemployment duration, the values that we obtain end up being slightly smaller than those transition probabilities in normal times. The probability  $\pi_{eu}$  in a recession is set to 5.1 percent for the Dropout group, 2.4 percent for the Highschool group, and 1.4 for the College group.

Our calibration of the transition probabilities between employment and unemployment during a recession are thus broadly in line with the results of Elsby and Hobijn (2010). They find that unemployment duration does not vary much between education groups and that the flow from unemployment to employment drops sharply for all groups in a recession. The flow into unemployment is more stable, but they find that it tends to increase a little bit in recessions.<sup>8</sup> This differs from the small decrease in the transition probabilities from employment into unemployment that our calibration strategy implies, which follows from our choice of targeting a doubling of the unemployment rate for each group rather than an even larger increase.

#### 1.3.3 Estimating the discount factor distributions

Discount factor distributions are estimated separately for each education group to match the distribution of liquid wealth for households in that group. To do so, we let each education group consist of types that differ in their subjective discount factor,  $\beta$ . The discount factors within each group  $e \in \{d, h, c\}$  are assumed to be uniformly distributed in the range  $[\beta_e - \nabla_e, \beta_e + \nabla_e]$ . The parameters  $\beta_e$  and  $\nabla_e$  are chosen for each group separately to match the median liquid-wealth-to-permanent-income ratio and the 20th, 40th, 60th, and 80th percentile points of the Lorenz curve for liquid wealth for that group. We approximate the uniform distribution of discount factors with a discrete approximation and let each education group consist of seven different types.

Panel A of table ?? shows the estimated values of  $(\beta_e, \nabla_e)$  for each education group. The panel also shows the minimum and maximum values of the discount factors we actually use in the model when we use a discrete approximation with seven values to approximate the uniform distribution of discount factors. Panel B of table ?? shows that with these estimated distributions, we can exactly match the median liquid-wealth-to-permanent-income ratios for each education group. Figure ?? shows that with the estimated distributions, the model quite closely matches the distribution of liquid wealth within each education group as well as for the population as a whole. Thus, our model

<sup>&</sup>lt;sup>8</sup>See the bottom row of Figure 8 in Elsby and Hobijn (2010) for these results.

**Table 3** Calibrated Model Parameters — Recession

Panel A: Parameters that apply to all types

Parameter	Notation	Value
Avg. duration of unemp. spell in a recession (quarters)		4
Prob. of leaving unemployment in a recession	$\pi_{ue}$	0.25

Panel B: Parameters calibrated for each education group

	Dropout	Highschool	College
Unemp. rate at the start of a recession (percent)	17.0	8.8	5.4
Prob. of entering unemployment $(\pi_{eu}^e, percent)$	5.1	2.4	1.4

Panel C: Parameters describing policy experiments

Parameter	Value
Average length of recession	6 quarters
Size of stimulus check	\$1,200
PI threshold for reducing check size	\$100,000
PI threshold for not receiving check	\$150,000
Extended unemployment benefits	4 quarters
Length of payroll tax cut	8 quarters
Income increase from payroll tax cut	2 percent
Belief (probability) that tax cut is extended	50 percent

Note: "PI" refers to Permanent Income

does not suffer from the "missing middle" problem, identified in Kaplan and Violante (2022), in which the middle of the wealth distribution has too little wealth.<sup>9</sup>

Note that several of the types in the Dropout group have very low discount factors and are very impatient. In this way, the model fits the feature of the data for the Dropout group that the bottom quintiles do not save at all and do not accumulate any liquid wealth. Very low estimates for discount factors are in line with those obtained in the literature on payday lending.<sup>10</sup>

<sup>&</sup>lt;sup>9</sup>One technical point to note about our estimation, is that we impose the constraint that the Growth Impatience Condition (GIC), discussed in Carroll (2022), is never violated. (The GIC is required to prevent the ratio of total wealth to total income of any group from approaching infinity. It does this by making sure that the growth of wealth of the group is less than or equal to the growth of income.) The constraint is imposed by calculating an upper bound for the discount factors  $\beta^{\rm GIC}$  where the GIC holds with equality. The estimation procedure ensures that no type ends up with a discount factor higher than this upper bound.

<sup>&</sup>lt;sup>10</sup>See, for example, Skiba and Tobacman (2008), who estimate two-week discount rates of 21 percent, and Allcott, Kim, Taubinsky, and Zinman (2021), who estimate an initial period discount factor between

Table 4 Estimated discount factor distributions and estimation targets

Panel A: Estimated discount factor distributions

	Dropout	Highschool	College
$(\beta_e, \nabla_e)$	(0.719, 0.318)	(0.925, 0.077)	(0.983, 0.014)
(Min, max) in approximation	(0.447, 0.991)	(0.859, 0.990)	(0.971, 0.995)

Panel B: Estimation targets

	Dropout	Highschool	College
Median LW/ quarterly PI (data, percent)	4.64	30.2	112.8
Median LW/ quarterly PI (model, percent)	4.64	30.2	112.8

Note: Panel (A) shows the estimated parameters of the discount distributions for each education group. It also shows the minimum and maximum values we use in our discrete approximation to the uniform distribution of discount factors for each group. Panel (B) shows the weighted median ratio of liquid wealth to permanent income from the 2004 SCF and in the model. In the annual data from the SCF, the annual PI is divided by 4 to obtain a quarterly number.

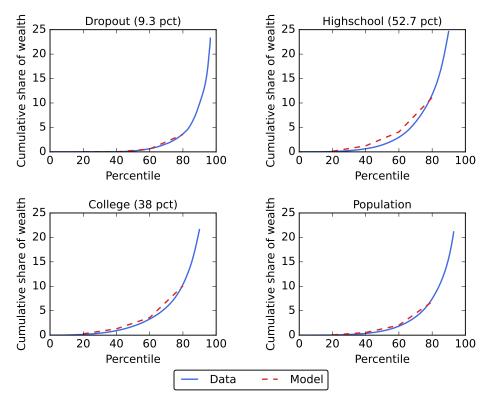
### 1.3.4 Implications for non-targeted moments

Before we move on to compare different consumption stimulus policies in the calibrated model, we also report implications of the model for some non-targeted moments. Panel A of table ?? shows the wealth distribution across the three education groups in the data and in the model. The model matches these shares quite closely, which may not be surprising given that we calibrate the size of each group and we manage to fit the wealth distribution within each group separately. The panel also reports the average marginal propensity to consume for the different groups. To be comparable to numbers reported in Fagereng, Holm, and Natvik (2021), these are calculated as the average MPC in the year of a lottery win. Lottery wins occur in a random quarter of the year that differs across individuals. The MPC for an individual depends on the spending pattern after the win, and these are averaged across individuals within each education group.

Panel B of table ?? shows similar numbers to Panel A, sorted by quartiles of the liquid wealth distribution instead of education groups. Our model yields a slightly more concentrated liquid wealth distribution than in the data. However, it does produce a fairly high MPC even for households in the highest quartile of the liquid wealth distribution. This is consistent with the results found in the Norwegian data by Fagereng, Holm, and Natvik (2021), but also with recent results in Graham and McDowall (2024). In an administrative dataset from a large US financial institution, they find that the spending response to an income receipt is large across the distribution of liquid asset holdings. In our model, we obtain this result due to the inclusion of the splurge factor.

<sup>0.74</sup> and 0.83 in a model where a period is eight weeks long. Both of these papers use quasi-hyperbolic preferences, so the estimates are not directly comparable with parameters in our model. Nevertheless, they support the point that very high discount rates are necessary to model the part of the population that takes out payday loans at very high interest rates.

Figure 2 Wealth distribution fit by education group



Note: This figure validates the discount factor estimation methodology (Section ??). Separate discount factor distributions  $\beta_e \pm \nabla_e$  are estimated for each education group to match the median liquid-wealth-to-permanent-income ratio and the 20th, 40th, 60th, and 80th percentile points of the Lorenz curve for liquid wealth. The model successfully avoids the "missing middle" problem identified by Kaplan and Violante (2022), where insufficient wealth accumulation occurs in the middle of the distribution. The "Population" panel demonstrates that pooling the three calibrated education groups produces a realistic aggregate liquid wealth distribution.

As shown in Appendix ??, the model is not able to generate a high MPC for the highest wealth quartile without splurge consumption.

Finally, we consider the implications of our model for two different patterns of spending over time. The first pattern is the dynamics of spending after a lottery win from Fagereng, Holm, and Natvik. This pattern was used in the estimation of the splurge factor in section ??, but was not targeted when estimating the discount factor distributions for each education group in section ??. Figure ?? shows that the model that is estimated taking the value of the splurge as given, results in a distribution of spending over time that is very similar to the one found in the Norwegian data.

The second pattern concerns the dynamics of income and spending for households that become unemployed and remain unemployed long enough for unemployment benefits to expire. Figure ?? shows the pattern of income and spending for such households. Ganong and Noel (2019) report the empirical result that nondurable spending drops by

 Table 5
 Model fit with respect to non-targeted moments

Panel A: Non-targeted moments by education group

	Dropout	Highschool	College	Population
Percent of liquid wealth (data)	0.8	17.9	81.2	100
Percent of liquid wealth (model)	1.2	16.8	82.0	100
Avg. lottery-win-year MPC	0.78	0.61	0.38	0.54

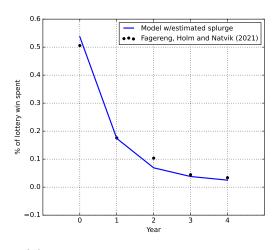
Panel B: Non-targeted moments by wealth quartile

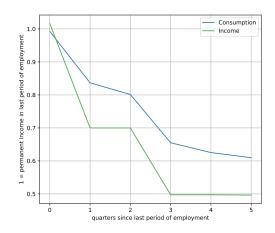
	WQ 4	WQ 3	WQ 2	WQ 1
Percent of liquid wealth (data)	0.14	1.60	8.51	89.76
Percent of liquid wealth (model)	0.12	0.98	3.85	95.06
Avg. lottery-win-year MPC	0.74	0.61	0.48	0.32

**Note**: Percent of liquid wealth held by each group in the 2004 SCF and in the model, and average MPCs after a lottery win for each group. MPCs are calculated for each individual for the year of a lottery win, taking into account that the win takes place in a random quarter of the year that differs across individuals.

12 percent the month when benefits expire. Our quarterly model is broadly consistent with this as the drop in spending the quarter after the expiry of UI benefits is 18 percent.

Figure 3 Model validation for non-targeted spending patterns





- (a) Dynamic spending after lottery win
- (b) Spending upon UI benefit expiry

Note: This figure demonstrates model performance on non-targeted validation moments (Section ??). Subfigure (a) shows the model's dynamic consumption response compared to Fagereng, Holm, and Natvik (2021) estimates using the discount factor distributions estimated separately for each education group. Subfigure (b) validates the model against Ganong and Noel (2019), who find that nondurable spending drops by 12% the month when UI benefits expire; our quarterly model predicts an 18% drop the quarter after benefit expiry, demonstrating broad consistency with this empirical pattern.

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