

On the adaptation of reference sets using niching and pair-potential energy functions for multi-objective optimization

Supplementary material

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Abstract

This supplementary material provides additional tables and figures to further discuss the performance of MOEAs using our adaptation method on MOPs with regular and irregular PF shapes. First, the tables with the performance assessment of MOEAs containing the complete numerical results are provided. Then, the final populations obtained by all MOEAs on each MOP are shown. Finally, additional convergence and diversity graphs of MOEAs on MOPs with regular and irregular PF shapes are given.

1 Numerical results

Tables 5 to 10 of the main paper present the ranks obtained by MOEAs using the same algorithmic framework (i.e., MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks) in terms of HV and SPD on MOPs with regular and irregular PF shapes. Additionally, such tables show if A-NSGA-III and all versions of NSGA-III-Ada \mathcal{K} , RVEA* and all versions of RVEA-Ada \mathcal{K} , and AdaW and all versions of MOEA/D-Ada \mathcal{K} perform significantly better, significantly worse, or statistically equivalent than NSGA-III, RVEA, and MOEA/D, respectively. Thus, in this supplementary material, we include the tables that contain the mean and standard deviations of MOEAs among 30 independent runs on each MOP.

1.1 Regular PF shapes

Tables 1 and 2 present the results of NSGA-III, A-NSGA-III, and all versions of NSGA-III-Ada \mathcal{K} on MOPs with regular PF shapes in terms of HV and SPD, respectively. Then, the performance comparison of RVEA, RVEA*, and all versions of RVEA-Ada \mathcal{K} on MOPs with regular PF shapes based on HV and SPD is shown in Tables 3 and 4, respectively. Finally, Tables 5 and 6 contain the results of MOEA/D, AdaW, and all versions of MOEA/D-Ada \mathcal{K} on MOPs with regular PF shapes in terms of HV and SPD, respectively. Among the obtained results, it can be seen that all versions of NSGA-III-Ada \mathcal{K} , RVEA-Ada \mathcal{K} , and MOEA/D-Ada \mathcal{K} can maintain or improve the performance of NSGA-III, RVEA, and MOEA/D, respectively, on most MOPs in terms of HV and SPD. In contrast, A-NSGA-III and RVEA* degrade the performance of their original versions on most MOPs in terms of HV and SPD. Also, AdaW degrades the performance of MOEA/D on most MOPs in terms of HV, while it maintains or improves the performance of MOEA/D on slightly more than half of the MOPs in terms of SPD. However, all versions of MOEA/D-Ada \mathcal{K} maintain or improve the performance of MOEA/D on more MOPs than AdaW based on HV and SPD. Thus, results show that our proposed adaptation method avoids degrading the performance of MOEAs that use predefined WVRSSs on most MOPs with regular PF shapes regardless of their algorithmic framework.

1.2 Irregular PF shapes

The performance comparison of NSGA-III, A-NSGA-III, and all versions of NSGA-III-Ada \mathcal{K} on MOPs with irregular PF shapes based on HV and SPD can be observed in Tables 7 and 8, respectively. Then, Tables 9 and 10 show the results of RVEA, RVEA*, and all versions of RVEA-Ada \mathcal{K} on MOPs with irregular PF shapes in terms of HV and SPD, respectively. Finally, the results of MOEA/D, AdaW, and all versions of

Table 1: Mean and standard deviations (in parenthesis) of the HV indicator obtained by MOEAs using the NSGA-III framework on MOPs with regular PF shapes. The two best mean values per MOP are highlighted in grayscale, where the darker tone corresponds to the best one. The symbols “+”, “-”, and “=” are placed when the MOEA performs significantly better, significantly worse, or statistically equivalent to NSGA-III based on a one-tailed Wilcoxon test using a significance level of $\alpha = 0.05$. The % of satisfaction refers to the percentage of MOPs where the MOEA performs significantly better or statistically equivalent to NSGA-III. The superscripts are the obtained rank in the comparison.

| MOP | Obj. | Gen. | NSGA-III | A-NSGA-III | NSGA-III-AdaRSE | NSGA-III-AdaGAE | NSGA-III-AdaMPT | NSGA-III-AdaCOU | NSGA-III-AdaPT | NSGA-III-AdaKRA |
|-------|------|------|----------------------------------|----------------------------------|----------------------------------|----------------------------------|----------------------------------|----------------------------------|----------------------------------|------------------------------------|
| DTLZ1 | 3 | 400 | 7.7868e+0 ⁷ (2.36e-3) | 7.7845e+0 ⁸ (3.65e-3) | 7.7872e+0 ³ (1.44e-3) | 7.7872e+0 ⁴ (1.96e-3) | 7.7873e+0 ² (1.59e-3) | 7.7871e+0 ⁵ (2.19e-3) | 7.7877e+0 ¹ (1.15e-3) | 7.7869e+0 ⁶ (1.80e-3) = |
| | 5 | 600 | 3.1967e+1 ⁷ (1.19e-4) | 3.1967e+1 ⁸ (3.10e-4) | 3.1967e+1 ⁹ (1.97e-4) | 3.1967e+1 ³ (1.38e-4) | 3.1967e+1 ⁴ (1.41e-4) | 3.1967e+1 ⁵ (1.85e-4) | 3.1967e+1 ² (1.10e-4) | 3.1967e+1 ⁷ (2.03e-4) = |
| | 8 | 750 | 2.5599e+2 ² (1.20e-4) | 2.5599e+2 ³ (3.11e-4) | 2.5599e+2 ² (9.23e-5) | 2.5599e+2 ⁵ (1.42e-4) | 2.5599e+2 ³ (1.36e-4) | 2.5599e+2 ⁶ (1.63e-4) | 2.5599e+2 ⁸ (6.93e-4) | 2.5599e+2 ⁹ (2.31e-3) = |
| | 10 | 1000 | 1.0240e+3 ² (9.45e-6) | 1.0240e+3 ³ (3.35e-5) | 1.0240e+3 ¹ (2.96e-5) | 1.0240e+3 ² (8.42e-6) | 1.0240e+3 ⁵ (1.56e-5) | 1.0240e+3 ⁶ (1.45e-5) | 1.0240e+3 ⁹ (4.74e-4) | 1.0240e+3 ¹ (1.34e-5) = |
| DTLZ2 | 3 | 250 | 7.4134e+0 ⁴ (1.01e-4) | 7.4116e+0 ⁸ (9.75e-4) | 7.4134e+0 ² (1.34e-4) | 7.4134e+0 ⁷ (1.48e-4) | 7.4134e+0 ⁵ (1.48e-4) | 7.4134e+0 ¹ (1.52e-4) | 7.4134e+0 ³ (1.39e-4) | 7.4134e+0 ⁶ (1.32e-4) = |
| | 5 | 350 | 3.1697e+1 ⁴ (1.97e-4) | 3.1696e+1 ⁸ (9.59e-4) | 3.1697e+1 ⁵ (1.53e-4) | 3.1697e+1 ³ (1.96e-4) | 3.1697e+1 ⁶ (1.35e-4) | 3.1697e+1 ⁷ (1.44e-4) | 3.1697e+1 ² (1.76e-4) | 3.1697e+1 ⁷ (1.90e-4) = |
| | 8 | 500 | 2.5584e+2 ² (3.79e-4) | 2.5584e+2 ³ (1.35e-3) | 2.5584e+2 ² (4.38e-4) | 2.5584e+2 ⁷ (3.03e-4) | 2.5584e+2 ⁵ (4.60e-4) | 2.5584e+2 ⁸ (3.13e-4) | 2.5584e+2 ⁹ (3.45e-4) | 2.5584e+2 ⁸ (4.01e-4) = |
| | 10 | 750 | 1.0239e+3 ² (1.55e-4) | 1.0239e+3 ³ (3.88e-4) | 1.0239e+3 ¹ (1.71e-4) | 1.0239e+3 ² (1.30e-4) | 1.0239e+3 ⁵ (1.40e-4) | 1.0239e+3 ⁶ (1.42e-4) | 1.0239e+3 ⁹ (1.57e-4) | 1.0239e+3 ¹ (1.51e-4) = |
| DTLZ3 | 3 | 1000 | 7.4072e+0 ⁴ (5.50e-3) | 7.4037e+0 ⁸ (6.27e-3) | 7.4072e+0 ⁵ (3.41e-3) | 7.4066e+0 ⁶ (7.00e-3) | 7.4066e+0 ⁷ (5.91e-3) | 7.4083e+0 ⁴ (4.20e-3) | 7.4075e+0 ³ (3.95e-3) | 7.4075e+0 ² (5.11e-3) = |
| | 5 | 1000 | 3.1696e+1 ⁴ (1.87e-3) | 3.1694e+1 ⁸ (1.53e-3) | 3.1695e+1 ² (1.88e-3) | 3.1695e+1 ⁸ (2.36e-3) | 3.1695e+1 ³ (2.05e-3) | 3.1695e+1 ⁵ (1.87e-3) | 3.1695e+1 ³ (2.03e-3) | 3.1695e+1 ² (2.03e-3) = |
| | 8 | 1000 | 2.5582e+2 ² (9.60e-3) | 2.5582e+2 ³ (9.16e-3) | 2.5583e+2 ² (9.31e-3) | 2.5582e+2 ⁵ (9.03e-3) | 2.5581e+2 ⁸ (7.86e-2) | 2.5583e+2 ² (5.92e-3) | 2.5583e+2 ⁷ (2.25e-3) | 2.5582e+2 ⁷ (1.34e-2) = |
| | 10 | 1500 | 1.0239e+3 ² (1.20e-3) | 1.0239e+3 ³ (1.94e-3) | 1.0239e+3 ¹ (1.13e-3) | 1.0239e+3 ² (1.54e-3) | 1.0239e+3 ⁵ (1.05e-3) | 1.0239e+3 ⁶ (1.77e-3) | 1.0239e+3 ⁹ (9.40e-4) | 1.0239e+3 ¹ (6.98e-4) = |
| DTLZ4 | 3 | 600 | 7.1862e+0 ² (8.66e-1) | 7.2980e+0 ⁸ (6.23e-1) | 7.0044e+0 ⁴ (1.05e+0) | 7.2661e+0 ⁴ (6.44e-1) | 7.3000e+0 ⁷ (6.23e-1) | 7.4110e+0 ¹ (1.49e-2) | 7.1862e+0 ⁷ (8.66e-1) | 7.1862e+0 ⁶ (8.66e-1) = |
| | 5 | 1000 | 3.1696e+1 ⁶ (2.57e-4) | 3.1696e+1 ⁸ (3.32e-4) | 3.1698e+1 ⁵ (1.27e-4) | 3.1698e+1 ³ (1.12e-4) | 3.1698e+1 ² (2.38e-4) | 3.1698e+1 ⁸ (8.91e-5) | 3.1698e+1 ⁷ (1.71e-4) | 3.1698e+1 ⁴ (1.44e-4) = |
| | 8 | 1250 | 2.5584e+2 ² (1.82e-4) | 2.5584e+2 ³ (6.05e-4) | 2.5584e+2 ² (2.32e-4) | 2.5584e+2 ⁷ (2.10e-4) | 2.5584e+2 ⁵ (1.99e-4) | 2.5584e+2 ⁸ (1.78e-4) | 2.5584e+2 ⁹ (1.95e-4) | 2.5584e+2 ⁸ (1.63e-4) = |
| | 10 | 2000 | 1.0239e+3 ² (7.24e-5) | 1.0239e+3 ³ (2.84e-4) | 1.0239e+3 ¹ (1.24e-4) | 1.0239e+3 ² (1.20e-4) | 1.0239e+3 ⁵ (9.71e-5) | 1.0239e+3 ⁶ (8.69e-5) | 1.0239e+3 ⁹ (1.05e-4) | 1.0239e+3 ¹ (1.05e-4) = |
| WFG1 | 3 | 400 | 5.3974e+0 ⁸ (1.92e-2) | 5.4059e+0 ⁷ (2.11e-2) | 5.4305e+0 ⁴ (2.67e-2) | 5.4182e+0 ⁵ (1.94e-2) | 5.4188e+0 ⁴ (2.31e-2) | 5.4225e+0 ³ (2.48e-2) | 5.4228e+0 ² (2.47e-2) | 5.4179e+0 ⁶ (2.38e-2) = |
| | 5 | 750 | 2.0487e+1 ⁷ (8.62e-2) | 2.0339e+1 ⁸ (7.50e-2) | 2.0455e+1 ⁷ (6.17e-2) | 2.0441e+1 ⁷ (6.84e-2) | 2.0465e+1 ⁵ (7.36e-2) | 2.0479e+1 ⁹ (5.99e-2) | 2.0485e+1 ² (8.53e-2) | 2.0474e+1 ⁴ (6.60e-2) = |
| | 8 | 1500 | 1.6764e+2 ² (3.65e-0) | 1.6363e+2 ³ (3.86e-0) | 1.6668e+2 ² (3.85e-0) | 1.6663e+2 ⁸ (3.71e-0) | 1.6606e+2 ⁶ (3.18e-0) | 1.6597e+2 ⁹ (3.24e-0) | 1.6756e+2 ² (3.74e-0) | 1.6647e+2 ⁷ (3.14e-0) = |
| | 10 | 2000 | 7.8149e+2 ² (1.47e-1) | 7.8061e+2 ³ (2.36e-1) | 7.5135e+2 ⁸ (1.81e-1) | 7.5482e+2 ² (2.41e-1) | 7.5692e+2 ⁶ (1.91e-1) | 7.7138e+2 ⁹ (2.00e-1) | 7.6203e+2 ² (2.03e+1) | 7.6446e+2 ² (1.90e-1) = |
| WFG4 | 3 | 400 | 7.3736e+0 ² (5.60e-3) | 7.3657e+0 ⁸ (7.61e-3) | 7.3717e+0 ⁶ (6.14e-3) | 7.3716e+0 ¹ (5.73e-3) | 7.3717e+0 ³ (6.13e-3) | 7.3731e+0 ² (6.96e-3) | 7.3738e+0 ² (5.76e-3) | 7.3730e+0 ² (5.03e-3) = |
| | 5 | 750 | 3.1558e+1 ³ (1.81e-2) | 3.1535e+1 ⁸ (2.18e-2) | 3.1557e+1 ⁴ (2.46e-2) | 3.1554e+1 ² (2.23e-2) | 3.1556e+1 ⁹ (1.97e-2) | 3.1561e+1 ¹ (1.67e-2) | 3.1560e+1 ² (1.80e-2) | 3.1556e+1 ⁵ (1.66e-2) = |
| | 8 | 1500 | 2.5539e+2 ² (1.81e-2) | 2.5534e+2 ³ (2.12e-1) | 2.5541e+2 ² (9.31e-3) | 2.5542e+2 ⁷ (1.08e-1) | 2.5539e+2 ⁵ (1.20e-1) | 2.5538e+2 ⁹ (1.20e-1) | 2.5538e+2 ² (1.20e-1) | 2.5540e+2 ³ (9.76e-2) = |
| | 10 | 2000 | 1.0229e+3 ² (2.20e-1) | 1.0229e+3 ³ (2.82e-2) | 1.0230e+3 ² (2.70e-1) | 1.0230e+3 ⁹ (2.75e-1) | 1.0229e+3 ⁶ (2.76e-1) | 1.0229e+3 ⁹ (2.52e-1) | 1.0228e+3 ⁹ (3.16e-1) | 1.0228e+3 ¹ (2.00e-1) = |
| WFG5 | 3 | 400 | 7.2281e+0 ⁴ (1.45e-3) | 7.2258e+0 ⁸ (3.53e-3) | 7.2281e+0 ⁵ (1.05e-3) | 7.2279e+0 ⁷ (1.63e-3) | 7.2282e+0 ³ (1.10e-3) | 7.2284e+0 ¹ (1.05e-3) | 7.2284e+0 ² (1.27e-3) | 7.2281e+0 ⁶ (1.37e-3) = |
| | 5 | 750 | 3.0787e+1 ⁵ (1.62e-3) | 3.0785e+1 ⁸ (2.92e-3) | 3.0787e+1 ² (5.31e-3) | 3.0787e+1 ⁶ (2.51e-3) | 3.0787e+1 ³ (5.10e-2) | 3.0787e+1 ⁷ (1.75e-3) | 3.0787e+1 ² (1.95e-3) | 3.0786e+1 ⁷ (1.91e-3) = |
| | 8 | 1500 | 2.4724e+2 ² (6.38e-3) | 2.4724e+2 ³ (6.13e-3) | 2.4725e+2 ² (4.85e-3) | 2.4725e+2 ⁵ (5.06e-3) | 2.4724e+2 ⁸ (3.99e-2) | 2.4725e+2 ⁹ (5.45e-3) | 2.4724e+2 ² (3.59e-3) | 2.4724e+2 ³ (5.17e-3) = |
| | 10 | 2000 | 9.8697e+2 ² (7.25e-3) | 9.8697e+2 ³ (1.42e-2) | 9.8697e+2 ⁸ (6.35e-3) | 9.8697e+2 ⁵ (8.82e-3) | 9.8697e+2 ² (6.51e-3) | 9.8697e+2 ⁹ (6.72e-3) | 9.8697e+2 ² (5.17e-3) | 9.8697e+2 ³ (5.17e-3) = |
| WFG6 | 3 | 400 | 7.2288e+0 ² (2.23e-2) | 7.2333e+0 ⁸ (2.30e-2) | 7.2263e+0 ⁷ (2.06e-2) | 7.2344e+0 ¹ (1.99e-2) | 7.2246e+0 ⁴ (1.97e-2) | 7.2440e+0 ⁸ (1.82e-2) | 7.2255e+0 ⁸ (2.11e-2) | 7.2340e+0 ³ (1.75e-2) = |
| | 5 | 750 | 3.0806e+1 ⁴ (8.98e-2) | 3.0806e+1 ⁸ (8.75e-2) | 3.0808e+1 ⁶ (7.73e-2) | 3.0808e+1 ² (7.81e-2) | 3.0808e+1 ⁹ (7.33e-2) | 3.0804e+1 ⁷ (7.41e-2) | 3.0803e+1 ² (6.19e-2) | 3.0813e+1 ³ (9.35e-2) = |
| | 8 | 1500 | 2.4714e+2 ² (1.20e+0) | 2.4702e+2 ³ (1.08e+0) | 2.4730e+2 ² (1.18e+0) | 2.4742e+2 ⁹ (1.30e+0) | 2.4730e+2 ⁵ (1.10e+0) | 2.4725e+2 ² (1.33e+0) | 2.4726e+2 ³ (1.24e+0) | 2.4728e+2 ² (1.20e+0) = |
| | 10 | 2000 | 3.8554e+2 ² (3.97e+0) | 9.8390e+2 ³ (4.75e-0) | 9.8359e+2 ⁸ (5.07e+0) | 9.8361e+2 ⁶ (6.37e+0) | 9.8364e+2 ² (3.99e+0) | 9.8364e+2 ⁹ (4.86e+0) | 9.8386e+2 ² (3.41e+0) | 9.8386e+2 ³ (3.41e+0) = |
| WFG7 | 3 | 400 | 7.3857e+0 ² (3.56e-3) | 7.3801e+0 ⁸ (5.28e-3) | 7.3852e+0 ⁴ (4.14e-3) | 7.3841e+0 ⁷ (4.85e-3) | 7.3855e+0 ² (4.22e-3) | 7.3843e+0 ⁵ (5.01e-3) | 7.3842e+0 ⁶ (4.98e-3) | 7.3854e+0 ³ (4.24e-3) = |
| | 5 | 750 | 3.1364e+1 ⁵ (7.89e-3) | 3.1363e+1 ⁸ (1.23e-2) | 3.1643e+1 ² (8.41e-3) | 3.1639e+1 ⁶ (9.58e-3) | 3.1639e+1 ⁹ (9.81e-3) | 3.1643e+1 ² (7.12e-3) | 3.1640e+1 ⁴ (8.25e-3) | 3.1639e+1 ² (9.65e-3) = |
| | 8 | 1500 | 2.5575e+2 ² (4.76e-2) | 2.5570e+2 ³ (4.75e-2) | 2.5573e+2 ² (3.63e-2) | 2.5573e+2 ⁹ (3.15e-2) | 2.5573e+2 ⁵ (3.15e-2) | 2.5572e+2 ⁸ (3.62e-2) | 2.5573e+2 ² (2.64e-2) | 2.5574e+2 ⁹ (2.64e-2) = |
| | 10 | 2000 | 1.0236e+3 ² (7.68e-2) | 1.0236e+3 ³ (8.28e-2) | 1.0237e+3 ⁵ (5.64e-2) | 1.0237e+3 ⁹ (4.58e-2) | 1.0237e+3 ⁶ (5.65e-2) | 1.0237e+3 ⁹ (5.90e-2) | 1.0237e+3 ⁹ (5.37e-2) | 1.0237e+3 ³ (5.16e-2) = |
| WFG8 | 3 | 400 | 7.2306e+0 ² (1.53e-2) | 7.2039e+0 ⁸ (3.27e-2) | 7.2277e+0 ⁷ (1.60e-2) | 7.2304e+0 ⁴ (1.95e-2) | 7.2247e+0 ⁴ (1.48e-2) | 7.2344e+0 ² (1.42e-2) | 7.2344e+0 ² (1.42e-2) | 7.2322e+0 ³ (1.52e-2) = |
| | 5 | 750 | 3.1142e+1 ⁵ (5.03e-2) | 3.1072e+1 ⁸ (5.65e-2) | 3.1136e+1 ² (4.29e-2) | 3.1121e+1 ⁶ (5.37e-2) | 3.1135e+1 ⁹ (5.10e-2) | 3.1124e+1 ² (4.62e-2) | 3.1135e+1 ⁷ (4.01e-2) | 3.1111e+1 ⁷ (4.29e-2) = |
| | 8 | 1500 | 2.5239e+2 ² (4.76e-1) | 2.5126e+2 ³ (5.36e-1) | 2.5233e+2 ² (5.01e-1) | 2.5242e+2 ⁹ (4.62e-1) | 2.5242e+2 ⁵ (4.20e-1) | 2.5242e+2 ⁸ (3.82e-1) | 2.5242e+2 ² (4.79e-1) | 2.5255e+2 ² (4.79e-1) = |
| | 10 | 2000 | 1.0157e+3 ² (1.34e-0) | 1.0097e+3 ³ (2.29e-0) | 1.0154e+3 ¹ (1.18e-0) | 1.0153e+3 ² (1.23e-0) | 1.0153e+3 ⁹ (1.09e-0) | 1.0156e+3 ⁴ (1.51e-0) | 1.0156e+3 ³ (1.46e-0) | 1.0153e+3 ² (1.46e-0) = |
| WFG9 | 3 | 400 | 7.1726e+0 ² (8.56e-2) | 7.1696e+0 ⁸ (8.14e-2) | 7.1668e+0 ⁷ (7.87e-2) | 7.1676e+0 ⁶ (6.86e-2) | 7.1852e+0 ² (5.93e-2) | 7.1686e+0 ⁵ (7. | | |

Table 2: Mean and standard deviations (in parenthesis) of the SPD indicator obtained by MOEAs using the NSGA-III framework on MOPs with regular PF shapes. The two best mean values per MOP are highlighted in grayscale, where the darker tone corresponds to the best one. The symbols “+”, “-”, and “=” are placed when the MOEA performs significantly better, significantly worse, or statistically equivalent to NSGA-III based on a one-tailed Wilcoxon test using a significance level of $\alpha = 0.05$. The % of satisfaction refers to the percentage of MOPs where the MOEA performs significantly better or statistically equivalent to NSGA-III. The superscripts are the obtained rank in the comparison.

| MOP | Obj. | Gen. | NSGA-III | A-NSGA-III | NSGA-III-AdaRSE | NSGA-III-AdaGAE | NSGA-III-AdaMPT | NSGA-III-AdaCOU | NSGA-III-AdaPT | NSGA-III-AdaKRA |
|-------|------|------|-------------------------|-------------------------|-------------------------|-------------------------|-------------------------|-------------------------|-------------------------|-------------------------|
| DTLZ1 | 3 | 400 | $2.3395e+1^0$ (1.09e-1) | $2.3325e+1^0$ (2.30e-1) | $2.3379e+1^0$ (6.90e-2) | $2.3377e+1^0$ (9.43e-2) | $2.3371e+1^0$ (7.74e-2) | $2.3381e+1^0$ (1.04e-1) | $2.3357e+1^0$ (5.52e-2) | $2.3388e+1^0$ (8.27e-2) |
| | 5 | 600 | $7.0393e+1^0$ (1.02e-1) | $7.2767e+1^0$ (3.60e-1) | $7.3070e+1^0$ (1.63e-1) | $7.3049e+1^0$ (1.07e-1) | $7.3055e+1^0$ (1.13e-1) | $7.3098e+1^0$ (1.49e-1) | $7.3056e+1^0$ (1.01e-1) | $7.3104e+1^0$ (1.64e-1) |
| | 8 | 750 | $1.0869e+2^0$ (3.79e-1) | $1.0800e+2^0$ (9.47e-1) | $1.0866e+2^0$ (2.65e-1) | $1.0882e+2^0$ (3.98e-1) | $1.0876e+2^0$ (3.50e-1) | $1.0868e+2^0$ (3.48e-1) | $1.0846e+2^0$ (1.17e+0) | $1.0811e+2^0$ (2.42e+0) |
| | 10 | 1000 | $1.7699e+2^0$ (3.30e-1) | $1.7662e+2^0$ (5.99e-1) | $1.7698e+2^0$ (3.16e-1) | $1.7683e+2^0$ (1.75e-1) | $1.7697e+2^0$ (2.79e-1) | $1.7701e+2^0$ (4.53e-1) | $1.7607e+2^0$ (4.66e+0) | $1.7702e+2^0$ (4.04e-1) |
| DTLZ2 | 3 | 250 | $3.2763e+1^0$ (4.15e-3) | $3.2614e+1^0$ (1.15e-1) | $3.2760e+1^0$ (6.86e-3) | $3.2763e+1^0$ (5.42e-3) | $3.2763e+1^0$ (3.97e-3) | $3.2762e+1^0$ (4.86e-3) | $3.2762e+1^0$ (6.09e-3) | $3.2762e+1^0$ (6.09e-3) |
| | 5 | 350 | $3.3954e+2^0$ (4.02e-2) | $3.3898e+2^0$ (3.44e-1) | $3.3954e+2^0$ (4.25e-2) | $3.3954e+2^0$ (3.06e-2) | $3.3954e+2^0$ (3.04e-2) | $3.3952e+2^0$ (3.04e-2) | $3.3954e+2^0$ (2.63e-2) | $3.3954e+2^0$ (2.51e-2) |
| | 8 | 500 | $4.7487e+2^0$ (5.16e-2) | $4.7534e+2^0$ (3.01e-1) | $4.7490e+2^0$ (6.71e-2) | $4.7488e+2^0$ (5.98e-2) | $4.7489e+2^0$ (5.34e-2) | $4.7478e+2^0$ (6.40e-2) | $4.7478e+2^0$ (4.62e-2) | $4.7478e+2^0$ (4.62e-2) |
| | 10 | 750 | $2.6059e+2^0$ (8.06e-2) | $2.6026e+2^0$ (2.55e-1) | $2.6058e+2^0$ (9.03e-2) | $2.6058e+2^0$ (6.85e-2) | $2.6056e+2^0$ (5.98e-2) | $2.6060e+2^0$ (8.73e-2) | $2.6059e+2^0$ (8.27e-2) | $2.6057e+2^0$ (8.42e-2) |
| DTLZ3 | 3 | 1000 | $3.2921e+1^0$ (1.36e-1) | $3.2819e+1^0$ (1.90e-1) | $3.2926e+1^0$ (8.37e-2) | $3.2936e+1^0$ (1.78e-1) | $3.2939e+1^0$ (1.50e-1) | $3.2893e+1^0$ (1.06e-1) | $3.2915e+1^0$ (1.00e-1) | $3.2915e+1^0$ (1.29e-1) |
| | 5 | 1000 | $3.4809e+2^0$ (2.81e-1) | $3.4712e+2^0$ (6.91e-1) | $3.4785e+2^0$ (7.25e-1) | $3.4798e+2^0$ (7.00e-1) | $3.4786e+2^0$ (9.00e-1) | $3.4775e+2^0$ (7.90e-1) | $3.4769e+2^0$ (1.50e+0) | $3.4791e+2^0$ (9.78e-1) |
| | 8 | 1000 | $2.6059e+2^0$ (1.37e-1) | $2.6014e+2^0$ (4.58e-1) | $2.6060e+2^0$ (1.75e-1) | $2.6063e+2^0$ (1.90e-1) | $2.6059e+2^0$ (1.49e-1) | $2.6056e+2^0$ (1.26e-1) | $2.6053e+2^0$ (1.37e-1) | $2.6054e+2^0$ (1.11e-1) |
| | 10 | 1500 | $3.0639e+1^0$ (8.06e+0) | $3.1497e+1^0$ (5.81e+0) | $3.0795e+1^0$ (1.10e+0) | $3.0891e+1^0$ (7.16e+0) | $3.0169e+1^0$ (5.80e+0) | $3.0232e+1^0$ (1.26e+0) | $3.0640e+1^0$ (8.06e+0) | $3.0639e+1^0$ (8.06e+0) |
| DTLZ4 | 3 | 600 | $3.3946e+2^0$ (2.66e-2) | $3.1938e+2^0$ (1.41e-1) | $3.3946e+2^0$ (2.95e-2) | $3.1934e+2^0$ (1.75e-2) | $3.1945e+2^0$ (3.05e-2) | $3.1945e+2^0$ (2.01e-2) | $3.1946e+2^0$ (3.02e-2) | $3.1945e+2^0$ (2.79e-2) |
| | 5 | 1000 | $3.3954e+2^0$ (2.65e-2) | $3.1918e+2^0$ (6.46e-1) | $3.3981e+2^0$ (2.61e-1) | $3.1975e+2^0$ (3.15e-1) | $3.3982e+2^0$ (3.43e-1) | $3.1982e+2^0$ (3.43e-1) | $3.3978e+2^0$ (2.23e-1) | $3.3977e+2^0$ (2.33e-1) |
| | 8 | 1250 | $3.4785e+2^0$ (5.18e-2) | $3.4782e+2^0$ (1.39e-1) | $3.4785e+2^0$ (4.46e-2) | $3.4785e+2^0$ (4.14e-2) | $3.4785e+2^0$ (4.60e-2) | $3.4785e+2^0$ (5.33e-2) | $3.4787e+2^0$ (3.84e-2) | $3.4785e+2^0$ (4.82e-2) |
| | 10 | 2000 | $2.6056e+2^0$ (6.71e-2) | $2.6049e+2^0$ (2.25e-1) | $2.6056e+2^0$ (6.46e-2) | $2.6056e+2^0$ (5.79e-2) | $2.6060e+2^0$ (6.29e-2) | $2.6058e+2^0$ (7.18e-2) | $2.6060e+2^0$ (7.63e-2) | $2.6056e+2^0$ (6.45e-2) |
| WFG1 | 3 | 400 | $1.7660e+1^0$ (5.07e-1) | $1.7188e+1^0$ (5.33e-1) | $1.6597e+1^0$ (4.49e-1) | $1.6329e+1^0$ (4.00e-1) | $1.6446e+1^0$ (3.39e-1) | $1.6370e+1^0$ (3.58e-1) | $1.6465e+1^0$ (3.02e-1) | $1.6531e+1^0$ (3.76e-1) |
| | 5 | 750 | $3.3484e+1^0$ (6.48e-1) | $3.2930e+1^0$ (1.64e-1) | $3.3411e+1^0$ (6.81e-1) | $3.2868e+1^0$ (6.89e-1) | $3.3039e+1^0$ (7.20e-1) | $3.3039e+1^0$ (7.74e-1) | $3.3043e+1^0$ (8.20e-1) | $3.3137e+1^0$ (7.84e-1) |
| | 8 | 1500 | $3.9677e+1^0$ (2.41e+0) | $3.7923e+1^0$ (2.74e-1) | $3.9594e+1^0$ (2.19e+0) | $4.0223e+1^0$ (2.41e+0) | $4.0426e+1^0$ (2.89e-1) | $4.0091e+1^0$ (2.03e+0) | $4.0008e+1^0$ (2.20e+0) | $4.0353e+1^0$ (2.42e+0) |
| | 10 | 2000 | $3.7512e+1^0$ (2.04e+0) | $3.3866e+1^0$ (1.96e+0) | $4.0868e+1^0$ (2.90e+0) | $3.9948e+1^0$ (2.91e+0) | $4.0487e+1^0$ (3.13e+0) | $4.0900e+1^0$ (3.48e+0) | $4.1395e+1^0$ (3.76e+0) | $4.1833e+1^0$ (3.61e+0) |
| WFG4 | 3 | 400 | $3.2743e+1^0$ (1.39e-2) | $3.2575e+1^0$ (3.22e-1) | $3.2730e+1^0$ (7.32e-2) | $3.2740e+1^0$ (1.66e-2) | $3.2737e+1^0$ (1.52e-2) | $3.2735e+1^0$ (2.17e-2) | $3.2736e+1^0$ (2.42e-2) | $3.2735e+1^0$ (1.90e-2) |
| | 5 | 750 | $3.1919e+2^0$ (5.32e-2) | $3.1875e+2^0$ (3.70e-1) | $3.1920e+2^0$ (6.26e-2) | $3.1920e+2^0$ (5.55e-2) | $3.1920e+2^0$ (4.82e-2) | $3.1920e+2^0$ (5.16e-2) | $3.1919e+2^0$ (4.57e-2) | $3.1919e+2^0$ (4.57e-2) |
| | 8 | 1500 | $3.4780e+2^0$ (3.97e-2) | $3.4778e+2^0$ (9.78e-2) | $3.4781e+2^0$ (4.41e-2) | $3.4778e+2^0$ (4.61e-2) | $3.4778e+2^0$ (4.47e-2) | $3.4780e+2^0$ (4.60e-2) | $3.4778e+2^0$ (4.75e-2) | $3.4779e+2^0$ (3.36e-2) |
| | 10 | 2000 | $2.6054e+2^0$ (6.12e-2) | $2.6047e+2^0$ (1.64e-1) | $2.6054e+2^0$ (6.15e-2) | $2.6054e+2^0$ (6.55e-2) | $2.6055e+2^0$ (6.64e-2) | $2.6053e+2^0$ (5.86e-2) | $2.6056e+2^0$ (6.45e-2) | $2.6056e+2^0$ (6.45e-2) |
| WFG5 | 3 | 400 | $3.2725e+1^0$ (1.46e-2) | $3.2559e+1^0$ (1.25e-1) | $3.2723e+1^0$ (1.22e-2) | $3.2717e+1^0$ (3.13e-2) | $3.2729e+1^0$ (1.27e-2) | $3.2727e+1^0$ (1.29e-2) | $3.2726e+1^0$ (1.09e-2) | $3.2718e+1^0$ (2.44e-2) |
| | 5 | 750 | $3.1931e+2^0$ (2.00e-2) | $3.1900e+2^0$ (3.50e-1) | $3.1931e+2^0$ (1.70e-2) | $3.1931e+2^0$ (2.15e-2) | $3.1930e+2^0$ (2.01e-2) | $3.1931e+2^0$ (1.96e-2) | $3.1930e+2^0$ (1.93e-2) | $3.1930e+2^0$ (1.93e-2) |
| | 8 | 1500 | $3.4779e+2^0$ (1.36e-2) | $3.4777e+2^0$ (1.24e-1) | $3.4779e+2^0$ (1.19e-2) | $3.4777e+2^0$ (1.08e-2) | $3.4778e+2^0$ (1.08e-2) | $3.4778e+2^0$ (1.21e-2) | $3.4779e+2^0$ (1.25e-2) | $3.4779e+2^0$ (1.25e-2) |
| | 10 | 2000 | $2.6045e+2^0$ (2.59e-2) | $2.6036e+2^0$ (1.76e-1) | $2.6044e+2^0$ (2.75e-2) | $2.6044e+2^0$ (2.60e-2) | $2.6044e+2^0$ (1.51e-2) | $2.6044e+2^0$ (2.96e-2) | $2.6045e+2^0$ (2.72e-2) | $2.6045e+2^0$ (3.08e-2) |
| WFG6 | 3 | 400 | $3.2763e+1^0$ (1.15e-1) | $3.2554e+1^0$ (1.30e-1) | $3.2767e+1^0$ (1.96e-2) | $3.2765e+1^0$ (1.27e-2) | $3.2764e+1^0$ (1.15e-2) | $3.2760e+1^0$ (1.04e-2) | $3.2761e+1^0$ (1.45e-2) | $3.2760e+1^0$ (1.57e-2) |
| | 5 | 750 | $3.1935e+2^0$ (2.60e-2) | $3.1905e+2^0$ (2.77e-1) | $3.1937e+2^0$ (2.15e-2) | $3.1935e+2^0$ (1.88e-2) | $3.1936e+2^0$ (2.20e-2) | $3.1936e+2^0$ (1.91e-2) | $3.1936e+2^0$ (2.52e-2) | $3.1936e+2^0$ (2.52e-2) |
| | 8 | 1500 | $3.4783e+2^0$ (2.86e-2) | $3.4780e+2^0$ (1.02e-1) | $3.4783e+2^0$ (3.62e-2) | $3.4784e+2^0$ (3.96e-2) | $3.4783e+2^0$ (2.92e-2) | $3.4783e+2^0$ (3.50e-2) | $3.4783e+2^0$ (4.24e-2) | $3.4782e+2^0$ (3.36e-2) |
| | 10 | 2000 | $2.6054e+2^0$ (5.48e-2) | $2.6039e+2^0$ (2.94e-1) | $2.6053e+2^0$ (6.05e-2) | $2.6053e+2^0$ (6.43e-2) | $2.6053e+2^0$ (5.68e-2) | $2.6053e+2^0$ (6.49e-2) | $2.6051e+2^0$ (6.20e-2) | $2.6051e+2^0$ (6.20e-2) |
| WFG7 | 3 | 400 | $3.2848e+1^0$ (2.37e-2) | $3.2642e+1^0$ (1.47e-1) | $3.2850e+1^0$ (2.19e-2) | $3.2853e+1^0$ (2.10e-2) | $3.2849e+1^0$ (2.41e-2) | $3.2852e+1^0$ (2.10e-2) | $3.2859e+1^0$ (2.76e-2) | $3.2846e+1^0$ (2.03e-2) |
| | 5 | 750 | $3.1970e+2^0$ (7.95e-2) | $3.1933e+2^0$ (3.35e-1) | $3.1969e+2^0$ (5.94e-2) | $3.1972e+2^0$ (6.64e-2) | $3.1970e+2^0$ (7.71e-2) | $3.1970e+2^0$ (6.95e-2) | $3.1970e+2^0$ (8.08e-2) | $3.1973e+2^0$ (7.47e-2) |
| | 8 | 1500 | $3.4791e+2^0$ (4.17e-2) | $3.4789e+2^0$ (1.16e-1) | $3.4791e+2^0$ (4.27e-2) | $3.4791e+2^0$ (4.57e-2) | $3.4791e+2^0$ (4.37e-2) | $3.4793e+2^0$ (4.16e-2) | $3.4793e+2^0$ (5.36e-2) | $3.4792e+2^0$ (4.09e-2) |
| | 10 | 2000 | $2.6079e+2^0$ (2.04e-1) | $2.6051e+2^0$ (2.96e-1) | $2.6077e+2^0$ (1.81e-1) | $2.6079e+2^0$ (1.66e-1) | $2.6076e+2^0$ (1.39e-1) | $2.6076e+2^0$ (9.97e-2) | $2.6077e+2^0$ (9.98e-2) | $2.6077e+2^0$ (9.98e-2) |
| WFG8 | 3 | 400 | $3.2455e+1^0$ (2.34e-2) | $3.2273e+1^0$ (2.34e-1) | $3.2559e+1^0$ (2.86e-2) | $3.2559e+1^0$ (4.82e-2) | $3.2552e+1^0$ (8.12e-2) | $3.2552e+1^0$ (8.12e-2) | $3.2587e+1^0$ (9.36e-2) | $3.2547e+1^0$ (9.05e-2) |
| | 5 | 750 | $3.1910e+2^0$ (7.35e-2) | $3.1858e+2^0$ (4.20e-1) | $3.1910e+2^0$ (1.00e-1) | $3.1909e+2^0$ (8.45e-2) | $3.1909e+2^0$ (1.06e-1) | $3.1909e+2^0$ (6.63e-2) | $3.1911e+2^0$ (2.01e-1) | $3.1911e+2^0$ (8.16e-2) |
| | 8 | 1500 | $3.4737e+2^0$ (2.51e-2) | $3.4649e+2^0$ (6.02e-1) | $3.4774e+2^0$ (1.21e-1) | $3.4774e+2^0$ (1.63e-1) | $3.4774e+2^0$ (1.47e-1) | $3.4774e+2^0$ (1.79e-1) | $3.4760e+2^0$ (1.51e-1) | $3.4766e+2^0$ (1.83e-1) |
| | 10 | 2000 | $2.6019e+2^0$ (6.70e-1) | $2.5856e+2^0$ (9.73e-1) | $2.6083e+2^0$ (8.91e-1) | $2.6096e+2^0$ (5.70e-1) | $2.6096e+2^0$ (7.61e-1) | $2.6031e+2^0$ (6.38e-1) | $2.6073e+2^0$ (7.36e-1) | $2.6090e+2^0$ (5.86e-1) |
| WFG9 | 3 | 400 | $3.1803e+1^0$ (1.87e-1) | $3.1470e+1^0$ (2.15e-1) | $3.1645e+1^0$ (1.78e-1) | $3.1690e+1^0$ (1.77e-1) | $3.1699e+1^0$ (1.36e-1) | $3.1749e+1^0$ (2.03e-1) | $3.1633e+1^0$ (1.74e-1) | $3.1697e+1^0$ (2.00e-1) |
| | | | | | | | | | | |

Table 3: Mean and standard deviations (in parenthesis) of the HV indicator obtained by MOEAs using the RVEA framework on MOPs with regular PF shapes. The two best mean values per MOP are highlighted in grayscale, where the darker tone corresponds to the best one. The symbols “+”, “-”, and “=” are placed when the MOEA performs significantly better, significantly worse, or statistically equivalent to RVEA based on a one-tailed Wilcoxon test using a significance level of $\alpha = 0.05$. The % of satisfaction refers to the percentage of MOPs where the MOEA performs significantly better or statistically equivalent to RVEA. The superscripts are the obtained rank in the comparison.

| MOP | Obj. | Gen. | RVEA | RVEA* | RVEA-AdaRSE | RVEA-AdaGAE | RVEA-AdaMPT | RVEA-AdaCOU | RVEA-AdaPT | RVEA-AdaKRA |
|-------|------|------|----------------------------------|----------------------------------|----------------------------------|----------------------------------|----------------------------------|----------------------------------|----------------------------------|----------------------------------|
| DTLZ1 | 3 | 400 | 7.7876e+0 ⁹ (2.09e-3) | 7.7705e+0 ⁸ (6.04e-3) | 7.7880e+0 ⁷ (1.72e-3) | 7.7878e+0 ⁷ (1.55e-3) | 7.7873e+0 ⁷ (1.89e-3) | 7.7875e+0 ⁷ (1.42e-3) | 7.7874e+0 ⁸ (2.52e-3) | 7.7874e+0 ⁶ (2.37e-3) |
| | 5 | 600 | 3.1967e+1 ⁸ (1.30e-4) | 3.1958e+1 ⁸ (2.04e-3) | 3.1967e+1 ⁸ (1.13e-4) | 3.1967e+1 ⁸ (1.03e-4) | 3.1967e+1 ⁸ (8.08e-5) | 3.1967e+1 ⁸ (8.64e-5) | 3.1967e+1 ⁷ (1.29e-4) | 3.1967e+1 ⁷ (1.35e-4) |
| | 7 | 750 | 2.5599e+2 ⁹ (6.09e-4) | 2.5599e+2 ⁹ (5.51e-3) | 2.5599e+2 ⁹ (4.43e-4) | 2.5599e+2 ⁹ (7.34e-4) | 2.5599e+2 ⁹ (2.63e-4) | 2.5599e+2 ⁹ (7.34e-4) | 2.5599e+2 ⁹ (2.13e-4) | 2.5599e+2 ⁹ (1.15e-4) |
| | 10 | 1000 | 1.0240e+3 ⁹ (2.67e-5) | 1.0240e+3 ⁹ (5.02e-3) | 1.0240e+3 ⁹ (3.15e-5) | 1.0240e+3 ⁹ (6.98e-6) | 1.0240e+3 ⁹ (3.86e-6) | 1.0240e+3 ⁹ (7.65e-6) | 1.0240e+3 ⁹ (4.90e-6) | 1.0240e+3 ⁹ (8.14e-6) |
| DTLZ2 | 3 | 250 | 7.4131e+0 ⁹ (1.14e-4) | 7.3889e+0 ⁸ (6.23e-3) | 7.4131e+0 ⁸ (2.11e-4) | 7.4131e+0 ⁸ (4.04e-4) | 7.4131e+0 ⁸ (2.54e-4) | 7.4131e+0 ⁷ (2.03e-4) | 7.4131e+0 ⁷ (2.17e-4) | 7.4131e+0 ⁷ (1.81e-4) |
| | 5 | 350 | 3.1698e+1 ⁸ (1.21e-4) | 3.1666e+1 ⁸ (8.65e-3) | 3.1698e+1 ⁸ (1.40e-4) | 3.1698e+1 ⁸ (1.23e-4) | 3.1698e+1 ⁸ (1.05e-4) | 3.1698e+1 ⁸ (1.09e-4) | 3.1698e+1 ⁸ (1.16e-4) | 3.1698e+1 ⁸ (1.03e-4) |
| | 7 | 500 | 2.5584e+2 ⁹ (1.27e-4) | 2.5583e+2 ⁹ (4.95e-3) | 2.5584e+2 ⁹ (1.62e-4) | 2.5584e+2 ⁹ (1.74e-4) | 2.5584e+2 ⁹ (1.35e-4) | 2.5584e+2 ⁹ (1.75e-4) | 2.5584e+2 ⁹ (1.36e-4) | 2.5584e+2 ⁹ (1.65e-4) |
| | 10 | 750 | 1.0239e+3 ⁹ (4.97e-5) | 1.0239e+3 ⁹ (6.60e-3) | 1.0239e+3 ⁹ (5.75e-5) | 1.0239e+3 ⁹ (6.47e-5) | 1.0239e+3 ⁹ (5.58e-5) | 1.0239e+3 ⁹ (5.99e-5) | 1.0239e+3 ⁹ (6.64e-5) | 1.0239e+3 ⁹ (5.14e-5) |
| DTLZ3 | 3 | 1000 | 7.4085e+0 ⁹ (2.98e-3) | 7.3844e+0 ⁸ (1.00e-2) | 7.4066e+0 ⁷ (5.91e-3) | 7.4089e+0 ⁷ (4.33e-3) | 7.4088e+0 ⁷ (3.54e-3) | 7.4077e+0 ⁷ (5.19e-3) | 7.4069e+0 ⁸ (5.03e-3) | 7.4079e+0 ⁴ (4.21e-3) |
| | 5 | 1000 | 3.1696e+1 ⁸ (3.17e-3) | 3.1670e+1 ⁸ (7.40e-3) | 3.1696e+1 ⁸ (1.49e-3) | 3.1696e+1 ⁸ (1.49e-3) | 3.1696e+1 ⁸ (1.06e-3) | 3.1696e+1 ⁸ (1.41e-3) | 3.1697e+1 ⁸ (1.41e-3) | 3.1697e+1 ⁸ (9.22e-4) |
| | 8 | 1000 | 2.5583e+2 ⁹ (4.22e-3) | 2.5583e+2 ⁹ (1.04e-2) | 2.5583e+2 ⁹ (4.10e-3) | 2.5583e+2 ⁹ (4.37e-3) | 2.5583e+2 ⁹ (3.26e-3) | 2.5583e+2 ⁹ (3.61e-3) | 2.5583e+2 ⁹ (4.23e-3) | 2.5583e+2 ⁹ (3.40e-3) |
| | 10 | 1500 | 1.0239e+3 ⁹ (5.24e-4) | 1.0239e+3 ⁹ (5.09e-3) | 1.0239e+3 ⁹ (4.89e-4) | 1.0239e+3 ⁹ (4.35e-4) | 1.0239e+3 ⁹ (3.88e-4) | 1.0239e+3 ⁹ (6.51e-4) | 1.0239e+3 ⁹ (4.54e-4) | 1.0239e+3 ⁹ (4.87e-4) |
| DTLZ4 | 3 | 600 | 7.4138e+0 ⁹ (8.27e-5) | 7.0202e+0 ⁸ (7.17e-1) | 7.4138e+0 ⁸ (2.30e-5) | 7.4138e+0 ⁸ (3.34e-5) | 7.3802e+0 ⁸ (1.84e-1) | 7.4138e+0 ⁸ (3.57e-5) | 7.4138e+0 ⁸ (5.38e-5) | 7.4138e+0 ⁴ (3.05e-5) |
| | 5 | 1000 | 3.1698e+1 ⁷ (2.36e-5) | 3.1681e+1 ⁸ (7.08e-3) | 3.1698e+1 ⁷ (2.55e-5) | 3.1698e+1 ⁷ (2.77e-5) | 3.1698e+1 ⁷ (2.59e-5) | 3.1698e+1 ⁷ (3.03e-5) | 3.1698e+1 ⁷ (2.25e-5) | 3.1698e+1 ⁷ (2.14e-5) |
| | 8 | 1250 | 2.5584e+2 ⁹ (1.06e-4) | 2.5583e+2 ⁹ (1.54e-3) | 2.5584e+2 ⁹ (1.68e-5) | 2.5584e+2 ⁹ (6.06e-5) | 2.5584e+2 ⁹ (6.52e-5) | 2.5584e+2 ⁹ (4.06e-2) | 2.5584e+2 ⁹ (7.79e-2) | 2.5583e+2 ⁹ (4.04e-2) |
| | 10 | 2000 | 1.0239e+3 ⁹ (4.64e-5) | 1.0239e+3 ⁹ (2.00e-3) | 1.0239e+3 ⁹ (4.29e-5) | 1.0239e+3 ⁹ (3.83e-5) | 1.0239e+3 ⁹ (3.43e-5) | 1.0239e+3 ⁹ (4.53e-5) | 1.0239e+3 ⁹ (3.40e-5) | 1.0239e+3 ⁹ (3.34e-5) |
| WFG1 | 3 | 400 | 5.3371e+0 ⁹ (4.70e-2) | 5.2803e+0 ⁸ (3.41e-2) | 5.2736e+0 ⁸ (3.66e-2) | 5.2812e+0 ⁸ (4.19e-2) | 5.2795e+0 ⁸ (3.80e-2) | 5.2747e+0 ⁷ (3.66e-2) | 5.2786e+0 ⁷ (3.79e-2) | 5.2824e+0 ⁷ (4.08e-2) |
| | 5 | 750 | 2.1186e+1 ⁸ (3.40e-1) | 1.9492e+1 ⁸ (1.21e-1) | 2.0866e+1 ⁸ (2.03e-1) | 2.0789e+1 ⁸ (2.35e-1) | 2.0902e+1 ⁸ (2.77e-1) | 2.0920e+1 ⁸ (2.47e-1) | 2.0759e+1 ⁸ (1.95e-1) | 2.0727e+1 ⁷ (1.81e-1) |
| | 8 | 1500 | 1.8773e+2 ⁹ (4.95e-0) | 1.5316e+2 ⁹ (1.46e-2) | 1.7263e+2 ⁹ (3.73e-0) | 1.7266e+2 ⁹ (4.73e-0) | 1.7169e+2 ⁹ (3.93e-0) | 1.7366e+2 ⁹ (4.47e-0) | 1.7341e+2 ⁹ (4.77e-0) | 1.7371e+2 ⁹ (4.34e-0) |
| | 10 | 2000 | 9.1928e+2 ⁹ (2.15e-1) | 7.1806e+2 ⁹ (2.38e-1) | 7.7076e+2 ⁹ (1.99e-1) | 7.7482e+2 ⁹ (1.99e-1) | 7.8111e+2 ⁹ (2.07e-1) | 7.8851e+2 ⁹ (1.85e-1) | 7.8249e+2 ⁹ (1.73e-1) | 7.7888e+2 ⁹ (1.95e-1) |
| WFG4 | 3 | 400 | 7.3563e+0 ⁹ (6.18e-3) | 7.3042e+0 ⁸ (2.38e-2) | 7.3543e+0 ⁸ (1.10e-2) | 7.3543e+0 ⁸ (6.88e-3) | 7.3526e+0 ⁸ (7.97e-3) | 7.3526e+0 ⁸ (8.42e-3) | 7.3562e+0 ⁸ (9.83e-3) | 7.3549e+0 ⁸ (8.45e-3) |
| | 5 | 750 | 3.1564e+1 ⁷ (1.84e-2) | 3.1209e+1 ⁸ (4.83e-2) | 3.1561e+1 ⁷ (1.94e-2) | 3.1558e+1 ⁷ (1.99e-2) | 3.1562e+1 ⁷ (2.05e-2) | 3.1557e+1 ⁷ (2.41e-2) | 3.1559e+1 ⁷ (1.89e-2) | 3.1554e+1 ⁷ (2.34e-2) |
| | 8 | 1500 | 2.5539e+2 ⁹ (9.39e-2) | 2.5263e+2 ⁹ (4.51e-1) | 2.5534e+2 ⁹ (1.35e-1) | 2.5529e+2 ⁹ (1.37e-1) | 2.5534e+2 ⁹ (1.31e-1) | 2.5535e+2 ⁹ (1.44e-1) | 2.5537e+2 ⁹ (1.37e-1) | 2.5536e+2 ⁹ (1.31e-1) |
| | 10 | 2000 | 1.0231e+3 ⁹ (1.81e-1) | 1.0165e+3 ⁹ (1.26e-1) | 1.0229e+3 ⁹ (2.77e-1) | 1.0229e+3 ⁹ (3.41e-1) | 1.0229e+3 ⁹ (2.33e-1) | 1.0230e+3 ⁹ (2.55e-1) | 1.0231e+3 ⁹ (2.22e-1) | 1.0230e+3 ⁹ (2.40e-1) |
| WFG5 | 3 | 400 | 7.2228e+0 ⁹ (2.91e-3) | 7.1859e+0 ⁸ (1.98e-2) | 7.2199e+0 ⁷ (1.47e-2) | 7.2234e+0 ⁷ (1.46e-3) | 7.2235e+0 ⁷ (1.79e-3) | 7.2225e+0 ⁷ (2.18e-3) | 7.2222e+0 ⁸ (3.12e-3) | 7.2220e+0 ⁶ (3.90e-3) |
| | 5 | 750 | 3.0788e+1 ⁷ (1.83e-2) | 3.0663e+1 ⁸ (4.22e-2) | 3.0788e+1 ⁷ (2.23e-2) | 3.0788e+1 ⁷ (1.91e-2) | 3.0788e+1 ⁷ (2.35e-2) | 3.0788e+1 ⁷ (1.56e-2) | 3.0788e+1 ⁷ (1.85e-3) | 3.0788e+1 ⁷ (2.13e-3) |
| | 8 | 1500 | 2.4725e+2 ⁹ (2.75e-3) | 2.4678e+2 ⁹ (8.57e-2) | 2.4725e+2 ⁹ (2.76e-3) | 2.4725e+2 ⁹ (2.91e-2) | 2.4725e+2 ⁹ (2.89e-2) | 2.4725e+2 ⁹ (2.92e-3) | 2.4725e+2 ⁹ (2.49e-3) | |
| | 10 | 2000 | 9.8697e+2 ⁹ (5.02e-3) | 9.8613e+2 ⁹ (1.93e-1) | 9.8697e+2 ⁹ (4.52e-3) | 9.8698e+2 ⁹ (4.58e-3) | 9.8697e+2 ⁹ (4.18e-3) | 9.8698e+2 ⁹ (3.01e-3) | 9.8697e+2 ⁹ (4.35e-3) | 9.8697e+2 ⁹ (4.06e-3) |
| WFG6 | 3 | 400 | 7.2119e+0 ⁹ (1.68e-2) | 7.1699e+0 ⁸ (2.27e-2) | 7.2137e+0 ⁸ (2.12e-2) | 7.2196e+0 ⁸ (2.55e-2) | 7.2192e+0 ⁸ (2.31e-2) | 7.2192e+0 ⁸ (2.43e-2) | 7.2211e+0 ⁷ (2.43e-2) | 7.2211e+0 ⁷ (1.82e-2) |
| | 5 | 750 | 3.0840e+1 ⁷ (9.96e-2) | 3.0539e+1 ⁸ (8.48e-2) | 3.0874e+1 ⁷ (1.00e-1) | 3.0837e+1 ⁸ (8.47e-2) | 3.0878e+1 ⁷ (9.29e-2) | 3.0832e+1 ⁸ (8.71e-2) | 3.0842e+1 ⁸ (1.18e-1) | 3.0858e+1 ⁸ (9.60e-2) |
| | 8 | 1500 | 2.4725e+2 ⁹ (1.44e-0) | 2.4534e+2 ⁹ (1.27e-1) | 2.4732e+2 ⁹ (1.59e-0) | 2.4685e+2 ⁹ (1.40e-0) | 2.4682e+2 ⁹ (1.65e-0) | 2.4750e+2 ⁹ (2.10e-0) | 2.4705e+2 ⁹ (1.53e-0) | |
| | 10 | 2000 | 9.8498e+2 ⁹ (6.57e-0) | 9.7434e+2 ⁹ (6.16e-1) | 9.8390e+2 ⁹ (7.54e-0) | 9.8351e+2 ⁹ (7.64e-0) | 9.8341e+2 ⁹ (7.85e-0) | 9.8322e+2 ⁹ (7.36e-0) | 9.8520e+2 ⁹ (5.07e-0) | |
| WFG7 | 3 | 400 | 7.3701e+0 ⁹ (7.26e-3) | 7.3362e+0 ⁸ (1.93e-2) | 7.3666e+0 ⁸ (8.29e-3) | 7.3662e+0 ⁸ (5.52e-3) | 7.3714e+0 ⁸ (5.55e-3) | 7.3694e+0 ⁸ (6.02e-3) | 7.3677e+0 ⁸ (4.32e-3) | 7.3685e+0 ⁸ (6.17e-3) |
| | 5 | 750 | 3.1649e+1 ⁷ (8.17e-3) | 3.1461e+1 ⁸ (3.68e-2) | 3.1642e+1 ⁷ (9.38e-3) | 3.1642e+1 ⁷ (7.51e-3) | 3.1642e+1 ⁷ (7.68e-3) | 3.1642e+1 ⁷ (8.99e-3) | 3.1642e+1 ⁷ (7.05e-3) | 3.1641e+1 ⁷ (8.03e-3) |
| | 8 | 1500 | 2.5568e+2 ⁹ (3.70e-2) | 2.5407e+2 ⁹ (3.92e-1) | 2.5549e+2 ⁹ (1.03e-1) | 2.5547e+2 ⁹ (1.72e-1) | 2.5550e+2 ⁹ (1.25e-1) | 2.5559e+2 ⁹ (7.14e-2) | 2.5559e+2 ⁹ (6.87e-2) | |
| | 10 | 2000 | 1.0236e+3 ⁹ (9.66e-2) | 1.0196e+3 ⁹ (1.01e-0) | 1.0232e+3 ⁹ (2.23e-1) | 1.0232e+3 ⁹ (2.52e-1) | 1.0233e+3 ⁹ (2.31e-1) | 1.0235e+3 ⁹ (1.09e-1) | 1.0235e+3 ⁹ (1.56e-1) | 1.0235e+3 ⁹ (1.19e-1) |
| WFG8 | 3 | 400 | 7.2117e+0 ⁹ (1.37e-2) | 7.1906e+0 ⁸ (4.14e-2) | 7.1956e+0 ⁸ (2.92e-2) | 7.1831e+0 ⁸ (4.16e-2) | 7.1916e+0 ⁸ (3.00e-2) | 7.2041e+0 ⁸ (2.43e-2) | 7.2002e+0 ⁸ (2.78e-2) | 7.1897e+0 ⁷ (3.54e-2) |
| | 5 | 750 | 3.0969e+1 ⁷ (7.33e-2) | 3.0622e+1 ⁸ (1.12e-1) | 3.0948e+1 ⁷ (6.96e-2) | 3.0943e+1 ⁸ (7.26e-2) | 3.0939e+1 ⁷ (7.60e-2) | 3.0956e+1 ⁷ (7.05e-2) | 3.0972e+1 ⁷ (8.14e-2) | 3.0944e+1 ⁷ (7.48e-2) |
| | 8 | 1500 | 2.4135e+2 ⁹ (8.54e+0) | 2.2950e+2 ⁹ (6.46e+0) | 2.3847e+2 ⁹ (1.21e+0) | 2.4167e+2 ⁹ (6.07e+0) | 2.4148e+2 ⁹ (6.18e+0) | 2.4173e+2 ⁹ (4.04e+0) | 2.4171e+2 ⁹ (8.98e+0) | 2.4162e+2 ⁹ (6.66e+0) |
| | 10 | 2000 | 9.5069e+2 ⁹ (5.70e+0) | 9.1865e+2 ⁹ (5.46e+0) | 9.3560e+2 ⁹ (5.72e+0) | 9.4663e+2 ⁹ (5.89e+0) | 9.9262e+2 ⁹ (6.26e+1) | 9.4938e+2 ⁹ (6.41e+1) | 9.3337e+2 ⁹ (6.71e+1) | |
| WFG9 | 3 | 400 | 7.1480e+0 ⁹ (8.01e-2) | 7.1227e+0 ⁸ (7.33e-2) | 7.1431e+0 ⁸ (6.67e-2) | 7.1419e+0 ⁸ (7.48e-2) | 7.1612e+0 ⁸ (6.88e-2) | 7.1608e+0 ⁸ (5.63e-2) | 7.1559e+0 ⁸ (5.55e-2) | 7.1432e+0 ⁸ (7.04e-2) |
| | 5 | 750 | 3.0849e+1 ⁷ (8.82e-2) | 3.0356e+1 ⁸ (1.92e-1) | 3.0812e+1 ⁷ (5.10e-1) | 3.0838e+1 ⁸ (9.76e-2) | 3.0847e+1 ⁷ (1.22e-1) | 3.0 | | |

Table 4: Mean and standard deviations (in parenthesis) of the SPD indicator obtained by MOEAs using the RVEA framework on MOPs with regular PF shapes. The two best mean values per MOP are highlighted in grayscale, where the darker tone corresponds to the best one. The symbols “+”, “-”, and “=” are placed when the MOEA performs significantly better, significantly worse, or statistically equivalent to RVEA based on a one-tailed Wilcoxon test using a significance level of $\alpha = 0.05$. The % of satisfaction refers to the percentage of MOPs where the MOEA performs significantly better or statistically equivalent to RVEA. The superscripts are the obtained rank in the comparison.

| MOP | Obj. | Gen. | RVEA | RVEA* | RVEA-AdaRSE | RVEA-AdaGAE | RVEA-AdaMPT | RVEA-AdaCOU | RVEA-AdaPT | RVEA-AdaKRA |
|-------|------|------|--|----------------------------------|--|--|--|--|--|--|
| DTLZ1 | 3 | 400 | 2.3357e+1 ⁹ (9.76e-2) | 2.2423e+1 ⁸ (1.95e-1) | 2.3339e+1 ⁷ (7.91e-2) | 2.3349e+1 ⁶ (6.97e-2) | 2.3337e+1⁵ (9.00e-2) | 2.3364e+1 ⁴ (7.11e-2) | 2.3368e+1 ² (1.27e-1) | 2.3365e+1 ³ (1.11e-1) |
| | 5 | 600 | 7.3023e+1 ² (1.12e-0) | 6.6500e+1 ⁸ (7.02e-1) | 7.3008e+1 ⁵ (1.07e-1) | 7.3016e+1 ³ (8.68e-2) | 7.2995e+1 ² (6.72e-2) | 7.3008e+1 ⁴ (7.08e-2) | 7.3036e+1 ¹ (1.08e-1) | 7.3006e+1 ⁵ (1.06e-2) |
| | 8 | 750 | 1.0782e+2 ² (5.92e-1) | 9.6977e+1 ⁸ (2.12e+0) | 1.0803e+2 ⁰ (4.70e-1) | 1.0810e+2 ⁰ (2.80e-1) | 1.0805e+2 ⁴ (4.61e-1) | 1.0824e+2 ⁰ (2.05e-1) | 1.0804e+2 ² (3.82e-1) | 1.0819e+2 ² (2.12e-1) |
| | 10 | 1000 | 1.7619e+2 ² (5.13e-1) | 1.5156e+2 ⁸ (3.16e+0) | 1.7636e+2 ⁹ (4.77e-1) | 1.7638e+2 ⁵ (3.86e-1) | 1.7547e+2 ⁴ (2.48e-1) | 1.7565e+2 ² (2.27e-1) | 1.7562e+2 ³ (1.91e-1) | 1.7657e+2² (2.36e-1) |
| DTLZ2 | 3 | 250 | 3.2775e+1 ⁸ (4.45e-3) | 3.2171e+1 ⁸ (1.49e-1) | 3.2769e+1 ⁸ (1.85e-2) | 3.2767e+1 ⁷ (1.65e-2) | 3.2772e+1 ⁵ (1.53e-2) | 3.2775e+1 ³ (7.22e-3) | 3.2775e+1 ² (1.32e-2) | 3.2768e+1 ⁶ (1.84e-2) |
| | 5 | 350 | 3.3955e+2 ² (2.75e-2) | 3.1817e+2 ⁸ (4.70e-1) | 3.1954e+2 ² (2.81e-2) | 3.1955e+2² (2.11e-2) | 3.1954e+2 ⁶ (2.36e-2) | 3.1954e+2 ⁴ (2.51e-2) | 3.1954e+2 ⁴ (2.31e-2) | 3.1954e+2 ⁵ (2.69e-2) |
| | 8 | 500 | 1.0782e+2 ² (5.92e-1) | 1.4961e+2 ⁸ (1.18e-1) | 1.4786e+2 ⁸ (2.81e-1) | 1.4780e+2 ² (1.82e-1) | 1.4785e+2 ⁵ (3.03e-2) | 1.4786e+2 ² (2.78e-2) | 1.4785e+2 ⁴ (2.35e-2) | 1.4778e+2 ⁸ (2.20e-1) |
| | 10 | 750 | 2.6051e+2 ² (1.38e-1) | 2.6400e+2 ⁸ (3.76e-1) | 2.6044e+2 ⁸ (2.29e-1) | 2.6047e+2 ⁸ (1.80e-1) | 2.6050e+2 ⁴ (1.29e-1) | 2.6051e+2 ² (1.22e-1) | 2.6049e+2 ⁵ (1.28e-1) | 2.6043e+2 ⁸ (3.00e-1) |
| DTLZ3 | 3 | 1000 | 3.2889e+1 ⁵ (7.20e-2) | 3.2461e+1 ⁸ (2.43e-1) | 3.2936e+1³ (1.44e-1) | 3.2877e+1 ⁷ (1.10e-1) | 3.2884e+1 ⁶ (9.04e-2) | 3.2911e+1 ³ (1.27e-1) | 3.2924e+1² (1.23e-1) | 3.2907e+1 ⁴ (1.07e-1) |
| | 5 | 1000 | 3.1965e+2 ² (1.86e-1) | 1.3833e+2 ⁸ (7.48e-1) | 1.3971e+2 ² (2.19e-1) | 1.3967e+2 ⁸ (2.21e-1) | 1.3965e+2 ⁶ (1.91e-1) | 1.3968e+2 ⁴ (1.91e-1) | 1.3961e+2 ⁶ (1.67e-1) | 1.3961e+2 ⁷ (1.14e-1) |
| | 8 | 1000 | 1.4796e+2 ² (2.18e-1) | 1.4951e+2 ⁸ (2.98e-1) | 1.4799e+2 ⁸ (3.30e-1) | 1.4798e+2 ⁵ (1.46e-1) | 1.4795e+2 ⁶ (1.15e-1) | 1.4796e+2 ⁵ (1.18e-1) | 1.4791e+2 ⁷ (2.45e-1) | 1.4781e+2 ⁸ (5.43e-1) |
| | 10 | 1500 | 2.6051e+2 ² (7.92e-2) | 2.6408e+2 ⁸ (3.20e-1) | 2.6047e+2 ⁸ (2.18e-1) | 2.6052e+2 ⁸ (5.65e-2) | 2.6046e+2 ⁸ (1.88e-1) | 2.6047e+2 ⁷ (1.32e-1) | 2.6048e+2 ⁵ (1.43e-1) | 2.6051e+2 ⁸ (6.39e-2) |
| DTLZ4 | 3 | 600 | 3.2758e+1 ⁷ (2.71e-3) | 2.4895e+1 ⁸ (1.14e-1) | 3.2757e+1 ⁸ (9.88e-3) | 3.2757e+1 ⁵ (9.31e-1) | 3.1954e+1 ⁷ (4.40e+0) | 3.2757e+1² (1.07e-1) | 3.2757e+1 ² (1.07e-1) | 3.2757e+1 ³ (1.18e-3) |
| | 5 | 1000 | 3.3943e+2 ² (5.82e-3) | 3.1771e+2 ⁸ (4.46e-1) | 3.1943e+2 ⁸ (5.73e-3) | 3.1943e+2 ⁶ (5.64e-3) | 3.1943e+2 ⁵ (5.37e-3) | 3.1943e+2 ⁵ (4.81e-3) | 3.1943e+2 ⁴ (4.88e-3) | 3.1943e+2 ⁵ (4.31e-3) |
| | 8 | 1250 | 3.4785e+2 ² (2.93e-2) | 3.4951e+2 ⁸ (1.99e-1) | 3.4581e+2 ⁸ (2.10e-1) | 3.4584e+2 ⁵ (2.44e-2) | 3.4785e+2 ⁸ (2.46e-2) | 3.4645e+2 ⁸ (5.30e-0) | 3.4526e+2 ⁸ (6.67e+0) | 3.4714e+2 ⁸ (3.86e+0) |
| | 10 | 2000 | 2.6055e+2 ² (4.31e-2) | 2.6501e+2 ⁸ (1.85e-1) | 2.6052e+2 ⁸ (1.71e-1) | 2.6049e+2 ⁸ (1.77e-1) | 2.6051e+2 ⁸ (1.56e-1) | 2.6050e+2 ⁸ (1.19e-1) | 2.6050e+2 ⁸ (1.81e-1) | 2.6053e+2 ⁸ (1.09e-1) |
| WFG1 | 3 | 400 | 1.7499e+1⁷ (2.33e-1) | 1.5934e+1 ² (4.43e-1) | 1.5657e+1 ⁸ (1.03e+0) | 1.5829e+1 ³ (9.89e-1) | 1.5493e+1 ⁶ (1.24e+0) | 1.5112e+1 ⁸ (1.21e+0) | 1.5698e+1 ⁴ (1.09e-0) | 1.5384e+1 ⁷ (1.19e-0) |
| | 5 | 750 | 3.0556e+1 ⁷ (7.75e-1) | 2.8783e+1 ⁸ (8.15e-1) | 2.7317e+1 ⁸ (1.62e-0) | 2.7567e+1 ² (2.43e-0) | 2.6686e+1 ⁸ (1.71e-0) | 2.7305e+1 ⁷ (2.16e-0) | 2.8131e+1 ⁴ (2.24e-0) | 2.8477e+1 ³ (1.99e-0) |
| | 8 | 1500 | 3.2393e+1 ⁸ (2.56e+0) | 3.2680e+1 ² (2.31e-0) | 3.2689e+1 ⁸ (2.14e+0) | 3.1619e+1 ⁸ (1.60e+0) | 3.2455e+1 ⁵ (1.87e+0) | 3.2497e+1 ⁸ (1.58e+0) | 3.4046e+1 ² (1.83e+0) | 3.4732e+1 ² (3.26e-0) |
| | 10 | 2000 | 2.4462e+1 ⁸ (2.04e+0) | 2.8583e+1 ⁷ (1.46e+0) | 3.9023e+1 ⁴ (2.63e+0) | 3.8408e+1 ² (2.37e+0) | 3.8720e+1 ² (2.17e+0) | 4.0177e+1 ³ (2.45e+0) | 4.2794e+1 ² (2.38e+0) | 4.2965e+1 ¹ (2.17e+0) |
| WFG4 | 3 | 400 | 3.2795e+1 ⁷ (8.90e-2) | 3.1056e+1 ⁸ (3.12e-1) | 3.2806e+1 ⁸ (1.08e-0) | 3.2811e+1² (8.80e-2) | 3.2807e+1 ⁵ (1.02e-1) | 3.2800e+1 ² (1.25e-0) | 3.2800e+1 ² (1.25e-0) | 3.2825e+1 ¹ (8.63e-2) |
| | 5 | 750 | 3.3914e+2 ² (9.61e-2) | 2.1284e+2 ⁸ (1.64e-0) | 3.1910e+2 ⁸ (8.59e-2) | 3.1912e+2 ⁸ (8.89e-2) | 3.1912e+2 ⁸ (8.60e-2) | 3.1913e+2 ⁸ (1.07e-1) | 3.1915e+2 ⁸ (7.10e-2) | 3.1915e+2 ⁸ (7.10e-2) |
| | 8 | 1500 | 3.4740e+2 ² (2.54e-1) | 1.3071e+2 ⁸ (1.78e-0) | 1.4737e+2 ⁸ (2.75e-1) | 1.4739e+2 ⁸ (2.11e-1) | 1.4732e+2 ⁸ (3.42e-1) | 1.4743e+2 ⁸ (1.99e-1) | 1.4744e+2 ⁸ (2.82e-1) | 1.4731e+2 ⁸ (3.37e-1) |
| | 10 | 2000 | 2.5844e+2 ² (9.96e-1) | 1.9407e+2 ⁸ (2.94e-0) | 2.5886e+2 ⁸ (7.67e-1) | 2.5874e+2 ⁸ (6.22e-1) | 2.5874e+2 ⁸ (1.10e+0) | 2.5831e+2 ⁸ (8.10e-1) | 2.5874e+2 ⁸ (8.12e-1) | 2.5819e+2 ⁸ (9.95e-1) |
| WFG5 | 3 | 400 | 3.2800e+1 ³ (4.60e-2) | 3.0862e+1 ⁸ (2.68e-1) | 3.2759e+1 ⁷ (2.38e-1) | 3.2810e+1³ (3.35e-2) | 3.2807e+1 ² (3.84e-2) | 3.2781e+1 ⁵ (6.41e-2) | 3.2782e+1 ⁴ (9.03e-2) | 3.2765e+1 ⁶ (1.34e-1) |
| | 5 | 750 | 3.1933e+2 ² (4.21e-2) | 1.8811e+2 ⁸ (9.47e-1) | 3.1933e+2 ⁸ (4.95e-2) | 3.1933e+2 ⁸ (4.90e-2) | 3.1933e+2 ⁸ (3.14e-2) | 3.1933e+2 ⁸ (2.58e-2) | 3.1933e+2 ⁸ (3.64e-2) | 3.1933e+2 ⁸ (4.52e-2) |
| | 8 | 1500 | 1.4737e+2 ² (2.06e-1) | 1.2926e+2 ⁸ (1.76e-0) | 1.4732e+2 ⁸ (2.28e-1) | 1.4734e+2 ⁸ (2.09e-1) | 1.4732e+2 ⁸ (1.79e-1) | 1.4735e+2 ⁸ (2.17e-1) | 1.4732e+2 ⁸ (2.42e-1) | 1.4731e+2 ⁸ (2.37e-1) |
| | 10 | 2000 | 2.5847e+2 ² (8.43e-1) | 1.8586e+2 ⁸ (2.67e-0) | 2.5851e+2 ⁸ (7.09e-1) | 2.5853e+2 ⁸ (5.46e-1) | 2.5856e+2 ⁸ (7.99e-1) | 2.5843e+2 ⁸ (7.56e-1) | 2.5858e+2 ⁸ (8.32e-1) | 2.5838e+2 ⁸ (7.85e-1) |
| WFG6 | 3 | 400 | 3.2853e+1 ⁷ (8.69e-2) | 3.1243e+1 ⁸ (1.23e-1) | 3.2822e+1 ⁸ (1.02e-1) | 3.2823e+1 ⁵ (8.82e-2) | 3.2823e+1 ² (1.02e-1) | 3.2813e+1 ⁷ (1.32e-1) | 3.2828e+1² (1.17e-1) | 3.2828e+1 ³ (1.15e-1) |
| | 5 | 750 | 3.1390e+2 ² (3.27e-2) | 1.2076e+2 ⁸ (1.36e-0) | 3.1939e+2 ⁸ (5.44e-2) | 3.1939e+2 ⁸ (4.07e-2) | 3.1939e+2 ⁸ (4.65e-2) | 3.1939e+2 ⁸ (6.08e-2) | 3.1938e+2 ⁸ (3.70e-2) | 3.1939e+2 ⁸ (3.67e-2) |
| | 8 | 1500 | 1.4654e+2 ² (8.15e-1) | 1.2761e+2 ⁸ (2.54e-0) | 1.4599e+2 ⁸ (6.88e-1) | 1.4605e+2 ⁸ (1.02e-0) | 1.4567e+2 ⁸ (8.04e-1) | 1.4613e+2 ⁸ (8.94e-1) | 1.4626e+2 ⁸ (9.03e-1) | 1.4626e+2 ⁸ (1.03e-0) |
| | 10 | 2000 | 2.5726e+2 ² (1.13e+0) | 1.9057e+2 ⁸ (3.16e-0) | 2.5711e+2 ⁸ (1.17e-0) | 2.5703e+2 ⁸ (9.21e-1) | 2.5719e+2 ⁸ (2.13e-0) | 2.5729e+2 ⁸ (1.08e-0) | 2.5752e+2 ⁸ (1.08e-0) | 2.5755e+2 ⁸ (9.10e-1) |
| WFG7 | 3 | 400 | 3.2964e+1 ⁵ (1.00e-1) | 3.1178e+1 ⁸ (3.46e-1) | 3.2955e+1 ⁷ (9.43e-2) | 3.2965e+1 ⁴ (8.82e-2) | 3.2957e+1 ⁶ (8.00e-2) | 3.2996e+1³ (8.35e-2) | 3.2999e+1 ² (6.86e-2) | 3.2991e+1 ³ (8.37e-2) |
| | 5 | 750 | 3.1397e+2 ² (6.29e-2) | 1.2123e+2 ⁸ (1.30e-0) | 3.1971e+2 ⁸ (6.29e-2) | 3.1968e+2 ⁸ (6.50e-2) | 3.1966e+2 ⁸ (7.62e-2) | 3.1971e+2 ⁸ (7.13e-2) | 3.1970e+2 ⁸ (7.37e-2) | 3.1970e+2 ⁸ (8.27e-2) |
| | 8 | 1500 | 1.4705e+2 ² (4.54e-1) | 1.2764e+2 ⁸ (2.14e-0) | 1.4646e+2 ⁸ (5.25e-1) | 1.4657e+2 ⁸ (4.93e-1) | 1.4672e+2 ⁸ (5.38e-1) | 1.4689e+2 ⁸ (4.70e-1) | 1.4704e+2 ⁸ (3.92e-1) | 1.4690e+2 ⁸ (4.17e-1) |
| | 10 | 2000 | 2.5560e+2 ² (9.65e-1) | 1.8759e+2 ⁸ (3.42e-0) | 2.5592e+2 ⁸ (9.95e-1) | 2.5592e+2 ⁸ (8.59e-1) | 2.5546e+2 ⁸ (9.56e-1) | 2.5546e+2 ⁸ (9.68e-1) | 2.5572e+2 ⁸ (1.01e-0) | 2.5548e+2 ⁸ (1.30e-0) |
| WFG8 | 3 | 400 | 3.2289e+1 ⁷ (2.02e-0) | 3.1010e+1 ⁸ (2.59e-1) | 3.2449e+1 ⁸ (4.29e-1) | 3.2360e+1 ⁵ (2.31e-1) | 3.2460e+1 ² (2.11e-1) | 3.2469e+1 ⁷ (1.90e-1) | 3.2529e+1² (1.68e-1) | 3.2411e+1 ⁵ (1.89e-1) |
| | 5 | 750 | 3.1384e+2 ² (1.62e-1) | 1.2212e+2 ⁸ (1.12e-0) | 3.1895e+2 ⁸ (2.90e-1) | 3.1897e+2 ⁸ (2.16e-1) | 3.1899e+2 ⁸ (2.59e-1) | 3.1896e+2 ⁸ (2.15e-1) | 3.1892e+2 ⁸ (1.50e-1) | 3.1899e+2 ⁸ (2.09e-1) |
| | 8 | 1500 | 1.4495e+2 ² (1.30e-0) | 1.3521e+2 ⁸ (1.50e-0) | 1.4501e+2 ⁸ (1.81e-0) | 1.4480e+2 ⁸ (9.73e-1) | 1.4517e+2 ⁸ (9.32e-1) | 1.4480e+2 ⁸ (9.69e-1) | 1.4506e+2 ⁸ (8.69e-1) | 1.4506e+2 ⁸ (8.38e-1) |
| | 10 | 2000 | 2.5586e+2 ² (1.05e-0) | 1.9585e+2 ⁸ (2.75e-0) | 2.5526e+2 ⁸ (1.25e-0) | 2.5526e+2 ⁸ (1.93e-0) | 2.5542e+2 ⁸ (1.57e-0) | 2.5560e+2 ⁸ (1.26e-0) | 2.5563e+2 ⁸ (1.26e-0) | 2.5560e+2 ⁸ (1.39e-0) |
| WFG9 | 3 | 400 | 3.1843e+1² (2.29e-1) | 3.0293e+1 ⁸ (2.96e-1) | 3.1756e+1 ⁷ (2.33e-1) | 3.1794e+1 ⁵ (2.31e-1) | 3.1840e+1 ³ (3.14e-1) | 3.1854e+1² (1.77e-1) | 3.1841e+1 ² (2.40e-1) | 3.1779e+1 ⁶ (2.45e |

Table 5: Mean and standard deviations (in parenthesis) of the HV indicator obtained by MOEAs using the MOEA/D framework on MOPs with regular PF shapes. The two best mean values per MOP are highlighted in grayscale, where the darker tone corresponds to the best one. The symbols “+”, “-”, and “=” are placed when the MOEA performs significantly better, significantly worse, or statistically equivalent to MOEA/D based on a one-tailed Wilcoxon test using a significance level of $\alpha = 0.05$. The % of satisfaction refers to the percentage of MOPs where the MOEA performs significantly better or statistically equivalent to MOEA/D. The superscripts are the obtained rank in the comparison.

| MOP | Obj. | Gen. | MOEA/D | AdaW | MOEA/D-AdaRSE | MOEA/D-AdaGAE | MOEA/D-AdaMPT | MOEA/D-AdaCOU | MOEA/D-AdaPT | MOEA/D-AdaKRA |
|-------|------|------|----------------------------------|------------------------------------|------------------------------------|------------------------------------|------------------------------------|------------------------------------|------------------------------------|------------------------------------|
| DTLZ1 | 3 | 400 | 7.7871e+0 ² (1.25e-3) | 7.7843e+0 ⁸ (1.82e-3) = | 7.7870e+0 ⁵ (1.27e-3) = | 7.7865e+0 ⁷ (1.93e-3) = | 7.7869e+0 ⁶ (1.72e-3) = | 7.7873e+0 ⁴ (9.42e-4) = | 7.7871e+0 ⁴ (1.03e-3) = | 7.7871e+0 ³ (1.18e-3) = |
| | 5 | 600 | 3.1960e+1 ⁷ (1.94e-2) | 3.1965e+1 ⁸ (2.67e-3) = | 3.1964e+1 ⁹ (9.88e-3) = | 3.1964e+1 ⁸ (8.10e-3) = | 3.1955e+1 ⁸ (2.43e-3) = | 3.1963e+1 ⁹ (9.57e-3) = | 3.1962e+1 ⁶ (1.17e-2) = | 3.1963e+1 ⁵ (1.16e-2) = |
| | 8 | 750 | 2.5594e+2 ⁹ (5.02e-2) | 2.5594e+2 ⁹ (1.02e-1) = | 2.5596e+2 ⁹ (6.26e-2) = | 2.5594e+2 ⁹ (7.43e-2) = | 2.5596e+2 ⁹ (8.21e-2) + | 2.5596e+2 ⁹ (4.63e-2) + | 2.5596e+2 ⁹ (2.17e-2) + | |
| | 10 | 1000 | 1.0239e+3 ⁷ (1.62e-1) | 1.0240e+3 ⁷ (4.60e-2) + | 1.0239e+3 ⁷ (8.56e-2) = | 1.0239e+3 ⁷ (1.18e-1) = | 1.0239e+3 ⁷ (7.44e-2) = | 1.0239e+3 ⁷ (1.99e-1) = | 1.0239e+3 ⁷ (9.56e-2) = | 1.0239e+3 ⁷ (1.10e-1) = |
| DTLZ2 | 3 | 250 | 7.4134e+0 ² (1.53e-4) | 7.4022e+0 ⁸ (9.28e-3) = | 7.4134e+0 ⁴ (1.94e-4) = | 7.4134e+0 ⁶ (1.57e-4) = | 7.4133e+0 ⁴ (2.26e-4) = | 7.4133e+0 ⁵ (1.80e-4) = | 7.4134e+0 ⁴ (1.88e-4) = | 7.4133e+0 ⁷ (1.85e-4) = |
| | 5 | 350 | 3.1695e+1 ⁵ (1.10e-2) | 3.1669e+1 ⁸ (1.68e-3) = | 3.1697e+1 ⁸ (4.62e-3) = | 3.1696e+1 ⁹ (1.80e-2) = | 3.1694e+1 ⁷ (1.69e-2) = | 3.1697e+1 ⁷ (1.79e-4) = | 3.1697e+1 ² (2.70e-4) = | |
| | 8 | 500 | 2.5581e+2 ⁹ (6.70e-2) | 2.5568e+2 ⁹ (6.35e-2) = | 2.5579e+2 ⁹ (4.46e-2) = | 2.5558e+2 ⁹ (1.53e-1) = | 2.5578e+2 ⁹ (1.69e-1) = | 2.5581e+2 ⁹ (1.10e-1) = | 2.5584e+2 ⁹ (6.84e-3) + | 2.5583e+2 ⁹ (2.50e-2) + |
| | 10 | 750 | 1.0238e+3 ⁷ (3.33e-1) | 1.0238e+3 ⁷ (3.93e-2) = | 1.0239e+3 ⁷ (8.05e-2) + | 1.0239e+3 ⁷ (2.28e-1) = | 1.0239e+3 ⁷ (1.09e-1) = | 1.0239e+3 ⁷ (7.86e-2) + | 1.0239e+3 ⁷ (1.76e-3) + | |
| DTLZ3 | 3 | 1000 | 7.4111e+0 ² (1.64e-3) | 7.3988e+0 ⁸ (1.29e-2) = | 7.4100e+0 ⁸ (3.07e-3) = | 7.4096e+0 ⁷ (2.41e-3) = | 7.4105e+0 ³ (1.82e-3) = | 7.4107e+0 ² (2.40e-3) = | 7.4104e+0 ⁴ (2.09e-3) = | 7.4098e+0 ⁶ (3.45e-3) = |
| | 5 | 1000 | 3.1695e+1 ⁵ (2.04e-2) | 3.1659e+1 ⁸ (2.04e-2) = | 3.1662e+1 ⁸ (8.58e-2) = | 3.1634e+1 ⁹ (1.56e-1) = | 3.1648e+1 ⁸ (1.85e-1) = | 3.1643e+1 ⁷ (1.30e-1) = | 3.1690e+1 ² (3.22e-2) = | 3.1687e+1 ³ (2.86e-2) = |
| | 8 | 1000 | 2.5530e+2 ⁹ (1.12e+0) | 2.5529e+2 ⁹ (5.98e-1) = | 2.5561e+2 ⁹ (4.40e-1) = | 2.5541e+2 ⁹ (6.75e-1) = | 2.5520e+2 ⁹ (1.40e+0) = | 2.5535e+2 ⁹ (7.31e-1) = | 2.5557e+2 ⁹ (5.92e+0) = | 2.5559e+2 ⁹ (5.12e-1) = |
| | 10 | 1500 | 1.0237e+3 ⁷ (2.52e-1) | 1.0234e+3 ⁷ (5.57e-1) = | 1.0233e+3 ⁷ (1.04e+0) = | 1.0233e+3 ⁷ (7.73e-1) = | 1.0235e+3 ⁷ (1.92e+0) = | 1.0235e+3 ⁷ (7.73e-1) = | 1.0239e+3 ⁷ (1.92e+0) = | 1.0239e+3 ⁷ (7.07e-2) + |
| DTLZ4 | 3 | 600 | 7.2784e+0 ² (3.50e-4) | 7.4099e+0 ⁸ (6.65e-3) = | 7.1650e+0 ⁶ (6.92e-1) = | 7.2114e+0 ⁸ (4.67e-1) = | 7.1056e+0 ⁸ (4.67e-1) = | 7.3459e+0 ² (2.57e-1) = | 7.1452e+0 ⁷ (4.52e-1) = | 7.1787e+0 ⁵ (4.32e-1) = |
| | 5 | 1000 | 3.1517e+1 ⁵ (4.32e-1) | 3.1675e+1 ⁹ (2.18e-1) = | 3.1590e+1 ² (2.18e-1) = | 3.1536e+1 ⁹ (4.27e-1) = | 3.1538e+1 ⁹ (2.44e-1) = | 3.1429e+1 ⁷ (5.40e-1) = | 3.1471e+1 ⁸ (4.12e-1) = | 3.1329e+1 ⁹ (6.16e-1) = |
| | 8 | 1250 | 2.5553e+2 ⁹ (3.63e-2) | 2.5578e+2 ⁹ (2.58e-2) = | 2.5562e+2 ⁹ (3.53e-1) = | 2.5557e+2 ⁹ (1.93e-1) + | 2.5551e+2 ⁹ (3.69e-1) = | 2.5560e+2 ⁹ (3.06e-1) = | 2.5567e+2 ⁹ (2.19e-1) = | 2.5567e+2 ⁹ (1.94e-1) = |
| | 10 | 2000 | 1.0236e+3 ⁷ (2.84e-1) | 1.0236e+3 ⁷ (3.94e-1) = | 1.0237e+3 ⁷ (2.32e-1) + | 1.0237e+3 ⁷ (2.94e-1) + | 1.0236e+3 ⁷ (2.64e-1) = | 1.0237e+3 ⁷ (3.15e-1) + | 1.0236e+3 ⁷ (2.73e-1) = | |
| WFG1 | 3 | 400 | 5.5941e+0 ² (4.88e-2) | 5.4299e+0 ⁸ (2.57e-2) = | 5.6138e+0 ⁸ (6.20e-2) = | 5.6151e+0 ² (5.13e-2) + | 5.6156e+0 ² (6.98e-2) = | 5.5946e+0 ⁸ (5.70e-2) = | 5.6082e+0 ⁴ (5.72e-2) = | 5.5965e+0 ² (6.93e-2) = |
| | 5 | 750 | 2.5795e+1 ⁷ (1.07e-0) | 2.1581e+1 ⁸ (3.47e-1) = | 2.7081e+1 ⁸ (6.86e-1) = | 2.6763e+1 ⁹ (7.57e-1) = | 2.7059e+1 ⁷ (7.93e-1) = | 2.6684e+1 ⁹ (7.63e-2) = | 2.7083e+1 ² (8.23e-1) + | 2.7098e+1 ³ (8.88e-1) + |
| | 8 | 1500 | 2.2085e+2 ⁹ (1.00e-1) | 2.1755e+2 ⁹ (4.58e-2) = | 2.0373e+2 ⁹ (6.18e-0) = | 2.0423e+2 ⁹ (6.28e-0) = | 2.0372e+2 ⁹ (6.38e-0) = | 2.0549e+2 ⁹ (6.12e-0) = | 2.1696e+2 ⁹ (6.24e-0) = | 2.1622e+2 ⁹ (5.59e-0) = |
| | 10 | 2000 | 9.3962e+2 ⁹ (3.34e-1) | 9.3907e+2 ⁹ (2.71e-1) = | 9.6527e+2 ⁹ (1.37e-1) + | 9.6149e+2 ⁹ (1.98e-1) + | 9.6286e+2 ⁹ (1.90e-1) + | 9.5269e+2 ⁹ (2.25e-1) + | 9.6406e+2 ⁹ (1.48e-1) + | 9.7036e+2 ⁹ (1.34e-1) + |
| WFG4 | 3 | 400 | 7.3813e+0 ² (5.38e-3) | 7.3397e+0 ⁸ (1.37e-2) = | 7.3813e+0 ⁸ (6.13e-3) = | 7.3814e+0 ⁸ (6.64e-3) = | 7.3779e+0 ⁷ (1.46e-2) = | 7.3821e+0 ⁷ (6.02e-3) = | 7.3768e+0 ⁷ (1.77e-2) = | 7.3801e+0 ⁷ (5.14e-3) = |
| | 5 | 750 | 3.1626e+1 ⁷ (1.54e-2) | 3.1488e+1 ⁸ (3.31e-1) = | 3.1627e+1 ⁷ (1.74e-2) = | 3.1632e+1 ² (1.43e-2) = | 3.1632e+1 ⁶ (1.76e-2) = | 3.1631e+1 ³ (1.33e-2) = | 3.1633e+1 ¹ (1.79e-2) + | 3.1630e+1 ⁹ (1.12e-2) = |
| | 8 | 1500 | 2.2085e+2 ⁹ (9.23e-2) | 2.5372e+2 ⁹ (4.49e-1) = | 2.5553e+2 ⁹ (9.14e-2) = | 2.5554e+2 ⁹ (7.85e-2) = | 2.5555e+2 ⁹ (7.57e-2) = | 2.5554e+2 ⁹ (7.23e-2) = | 2.5555e+2 ⁹ (8.02e-2) = | 2.5555e+2 ⁹ (8.02e-2) = |
| | 10 | 2000 | 1.0234e+3 ⁷ (1.53e-1) | 1.0185e+3 ⁷ (3.17e-0) = | 1.0234e+3 ⁷ (2.30e-1) = | 1.0233e+3 ⁷ (2.03e-1) = | 1.0233e+3 ⁷ (1.89e-1) = | 1.0234e+3 ⁷ (1.50e-1) = | 1.0233e+3 ⁷ (1.91e-1) = | |
| WFG5 | 3 | 400 | 7.1945e+0 ² (3.97e-2) | 7.1714e+0 ⁸ (3.31e-2) = | 7.1691e+0 ⁷ (4.77e-2) = | 7.1874e+0 ⁵ (4.26e-2) = | 7.1966e+0 ⁴ (4.47e-2) = | 7.1673e+0 ⁸ (5.02e-2) = | 7.1938e+0 ³ (4.51e-2) = | 7.1898e+0 ⁴ (4.34e-2) = |
| | 5 | 750 | 3.0785e+1 ³ (1.70e-2) | 3.0700e+1 ⁸ (4.96e-2) = | 3.0785e+1 ⁸ (1.66e-2) = | 3.0787e+1 ⁹ (2.12e-2) = | 3.0788e+1 ⁷ (1.76e-3) = | 3.0785e+1 ⁹ (1.60e-2) = | 3.0784e+1 ⁷ (1.65e-2) = | |
| | 8 | 1500 | 2.4717e+2 ⁹ (5.23e-2) | 2.4633e+2 ⁹ (2.19e-1) = | 2.4710e+2 ⁹ (2.23e-2) = | 2.4719e+2 ⁹ (2.07e-2) = | 2.4717e+2 ⁹ (3.41e-1) = | 2.4718e+2 ⁹ (2.70e-2) = | 2.4717e+2 ⁹ (2.28e-2) = | 2.4718e+2 ⁹ (2.70e-2) = |
| | 10 | 2000 | 9.8681e+2 ⁹ (4.22e-2) | 9.8537e+2 ⁹ (4.63e-1) = | 9.8682e+2 ⁹ (3.73e-2) = | 9.8681e+2 ⁹ (4.24e-2) = | 9.8682e+2 ⁹ (4.85e-2) = | 9.8681e+2 ⁹ (4.43e-2) = | 9.8680e+2 ⁹ (4.74e-2) = | |
| WFG6 | 3 | 400 | 7.2387e+0 ² (2.75e-2) | 7.2260e+0 ⁸ (3.42e-2) = | 7.2401e+0 ⁴ (3.41e-2) = | 7.2493e+0 ⁸ (2.56e-2) + | 7.2476e+0 ⁸ (2.97e-2) = | 7.2527e+0 ⁴ (2.49e-2) + | 7.2509e+0 ³ (1.90e-2) = | 7.2517e+0 ² (2.37e-2) + |
| | 5 | 750 | 3.0922e+1 ⁷ (1.39e-1) | 3.0784e+1 ⁸ (1.64e-1) = | 3.0914e+1 ⁸ (1.53e-1) = | 3.0887e+1 ⁷ (1.64e-1) = | 3.0916e+1 ² (1.47e-1) = | 3.0897e+1 ⁹ (1.63e-1) = | 3.0912e+1 ⁴ (1.67e-1) = | 3.0903e+1 ⁵ (1.54e-1) = |
| | 8 | 1500 | 2.4775e+2 ⁹ (1.72e+0) | 2.4646e+2 ⁹ (1.78e+0) = | 2.4753e+2 ⁹ (1.67e+0) = | 2.4776e+2 ⁹ (2.02e+0) = | 2.4736e+2 ⁹ (1.91e+0) = | 2.4733e+2 ⁹ (1.66e+0) = | 2.4756e+2 ⁹ (1.84e+0) = | 2.4778e+2 ⁹ (1.76e+0) = |
| | 10 | 2000 | 9.8613e+2 ⁹ (9.53e+0) | 9.8271e+2 ⁹ (9.98e+0) = | 9.8439e+2 ⁹ (2.85e+0) = | 9.8755e+2 ⁹ (1.02e+1) = | 9.8420e+2 ⁹ (9.57e+0) = | 9.8749e+2 ⁹ (1.01e+1) = | 9.8744e+2 ⁹ (1.29e+1) = | 9.8599e+2 ⁹ (9.61e+0) = |
| WFG8 | 3 | 400 | 7.4034e+0 ² (1.52e-3) | 7.3787e+0 ⁸ (1.14e-2) = | 7.4025e+0 ⁸ (1.92e-3) = | 7.4026e+0 ⁸ (1.84e-3) = | 7.4024e+0 ⁷ (1.43e-3) = | 7.4033e+0 ³ (1.60e-3) = | 7.4034e+0 ² (1.99e-3) = | 7.4028e+0 ⁴ (1.88e-3) = |
| | 5 | 750 | 3.1675e+1 ³ (3.85e-3) | 3.1559e+1 ⁸ (2.26e-2) = | 3.1673e+1 ⁸ (3.92e-3) = | 3.1670e+1 ⁸ (2.57e-2) = | 3.1669e+1 ⁷ (2.88e-2) = | 3.1676e+1 ⁷ (3.56e-3) = | 3.1675e+1 ³ (4.23e-3) = | 3.1675e+1 ² (3.88e-3) = |
| | 8 | 1500 | 2.5573e+2 ⁹ (2.96e-2) | 2.5391e+2 ⁹ (4.31e-1) = | 2.5573e+2 ⁹ (3.18e-2) = | 2.5572e+2 ⁹ (2.82e-2) = | 2.5572e+2 ⁹ (3.30e-2) = | 2.5573e+2 ⁹ (2.37e-2) = | 2.5573e+2 ⁹ (3.10e-2) = | 2.5573e+2 ⁹ (2.48e-2) = |
| | 10 | 2000 | 1.0236e+3 ⁷ (1.16e-1) | 1.0191e+3 ⁷ (3.26e-0) = | 1.0236e+3 ⁷ (9.22e-2) = | 1.0236e+3 ⁷ (8.16e-2) = | 1.0236e+3 ⁷ (9.57e-2) = | 1.0236e+3 ⁷ (9.27e-2) = | 1.0236e+3 ⁷ (9.44e-2) = | 1.0236e+3 ⁷ (1.08e-1) = |
| WFG9 | 3 | 400 | 7.1780e+0 ² (8.59e-2) | 7.0898e+0 ⁸ (7.97e-2) = | 7.1560e+0 ⁸ (1.00e-1) = | 7.1597e+0 ⁸ (8.68e-2) = | 7.1886e+0 ² (9.80e-2) = | 7.1976e+0 ⁷ (7.61e-2) = | 7.1519e+0 ⁷ (9.84e-2) = | 7.1826e+0 ⁴ (8.26e-2) = |
| | 5 | 750 | 2.9915e+1 ⁷ (4.30e-1) | 2.9704e+1 ⁸ (3.12e-1) = | 3.0204e+1 ⁸ (6.51e-1) + | 3.0153e+1 ⁸ (5.91e-1) + | 3.0032e+1 ⁸ (4.93e-1) = | 3.0222e+1 ⁸ (6.30e-1) + | 3.0018e+1 ⁸ (4.91e-1) + | 3.0102e+1 ⁸ (5.87e-1) = |
| | 8 | 1500 | 2.4851e+2 ⁹ (5.08e-0) | 2.3506e+2 ⁹ (4.38e-0) = | 2.4836e+2 ⁹ (4.53e-0) = | 2.4817e+2 ⁹ (5.78e-0) = | 2.4875e+2 ⁹ (5.47e-0) = | 2.4875e+2 ⁹ (4.57e-0) = | 2.4932e+2 ⁹ (3.99e-0) = | 2.4930e+2 ⁹ (4.51e-0) = |
| | 10 | 2000 | 9.9390e+2 ⁹ (2.88e+1) | 9.4268e+2 ⁹ (1.93e+1) = | 9.9431e+2 ⁹ (2.56e+1) = | 9.9573e+2 ⁹ (2.45e+1) = | 1.0003e+3 ⁷ (1.93e+1) = | 1.0024e+3 ⁷ (1.53e+1) | | |

Table 6: Mean and standard deviations (in parenthesis) of the SPD indicator obtained by MOEAs using the MOEA/D framework on MOPs with regular PF shapes. The two best mean values per MOP are highlighted in grayscale, where the darker tone corresponds to the best one. The symbols “+”, “-”, and “=” are placed when the MOEA performs significantly better, significantly worse, or statistically equivalent to MOEA/D based on a one-tailed Wilcoxon test using a significance level of $\alpha = 0.05$. The % of satisfaction refers to the percentage of MOPs where the MOEA performs significantly better or statistically equivalent to MOEA/D. The superscripts are the obtained rank in the comparison.

| MOP | Obj. | Gen. | MOEA/D | AdaW | MOEA/D-AdaRSE | MOEA/D-AdaGAE | MOEA/D-AdaMPT | MOEA/D-AdaCOU | MOEA/D-AdaPT | MOEA/D-AdaKRA |
|-------|------|------|----------------------------------|------------------------------------|------------------------------------|------------------------------------|------------------------------------|------------------------------------|------------------------------------|------------------------------------|
| DTLZ1 | 3 | 400 | 2.3292e+1 ⁹ (7.42e-2) | 2.2924e+1 ⁸ (1.35e-1) = | 2.3294e+1 ⁹ (5.12e-2) = | 2.3269e+1 ⁷ (1.58e-1) = | 2.3315e+1 ⁹ (9.78e-2) = | 2.3279e+1 ⁶ (6.11e-2) = | 2.3293e+1 ⁴ (5.92e-2) = | 2.3298e+1 ² (5.48e-2) = |
| | 5 | 600 | 7.1189e+1 ⁶ (4.45e+0) | 6.6112e+1 ⁸ (1.96e+0) - | 7.2329e+1 ⁷ (2.07e+0) = | 7.1993e+1 ⁸ (2.68e+0) = | 7.0120e+1 ⁷ (5.65e+0) = | 7.0232e+1 ³ (2.11e+0) = | 7.1805e+1 ⁵ (2.82e+0) = | 7.2280e+1 ² (2.20e+0) = |
| | 8 | 750 | 9.4488e+1 ⁶ (1.38e+1) | 7.6885e+1 ⁸ (6.30e+0) - | 9.7578e+1 ⁹ (1.16e+1) = | 9.6831e+1 ⁸ (1.34e+1) = | 9.4327e+1 ⁷ (1.35e+1) = | 1.0020e+2 ⁰ (1.37e+1) + | 1.0047e+2 ⁰ (1.17e+1) + | 1.0391e+2 ⁰ (7.24e+0) + |
| | 10 | 1000 | 1.4262e+2 ⁰ (2.26e+1) | 9.6369e+1 ⁸ (7.73e+0) - | 1.6000e+2 ⁰ (1.57e+1) + | 1.3724e+2 ⁰ (2.54e+1) + | 1.5726e+2 ⁰ (1.74e+1) + | 1.3944e+2 ⁰ (3.43e+1) + | 1.5483e+2 ⁰ (2.05e+1) + | 1.6524e+2 ⁰ (1.29e+1) + |
| DTLZ2 | 3 | 250 | 3.2626e+1 ⁴ (4.73e-2) | 3.2149e+1 ⁸ (2.22e-1) - | 3.2611e+1 ⁸ (2.84e-2) - | 3.2632e+1 ⁷ (3.97e-2) = | 3.2600e+1 ⁷ (3.37e-2) - | 3.2632e+1 ⁷ (3.50e-2) = | 3.2631e+1 ³ (3.02e-2) = | 3.2618e+1 ⁵ (3.40e-2) = |
| | 5 | 350 | 1.3644e+2 ⁰ (5.64e+0) | 1.3451e+2 ⁰ (1.17e-0) - | 1.3696e+2 ⁰ (2.85e-0) = | 1.3657e+2 ⁰ (3.73e-0) = | 1.3551e+2 ⁰ (7.34e-0) = | 1.3642e+2 ⁰ (5.21e-0) = | 1.3770e+2 ⁰ (5.01e-0) = | 1.3777e+2 ⁰ (6.32e-1) = |
| | 8 | 500 | 1.3904e+2 ⁰ (8.57e+0) | 1.4825e+2 ⁰ (7.09e-1) + | 1.3777e+2 ⁰ (8.07e+0) - | 1.4042e+2 ⁰ (7.82e+0) = | 1.3825e+2 ⁰ (1.03e+1) = | 1.4090e+2 ⁰ (8.17e+0) + | 1.4195e+2 ⁰ (6.86e+0) + | 1.4218e+2 ⁰ (5.42e+0) + |
| | 10 | 750 | 2.3936e+2 ⁰ (3.23e+1) | 2.5895e+2 ⁰ (1.74e+0) - | 2.5266e+2 ⁰ (1.09e+1) = | 2.4875e+2 ⁰ (1.71e+1) = | 2.4412e+2 ⁰ (1.78e+1) = | 2.4989e+2 ⁰ (1.57e+1) = | 2.5265e+2 ⁰ (8.05e+0) = | 2.5408e+2 ⁰ (5.99e+0) = |
| DTLZ3 | 3 | 1000 | 3.2770e+1 ⁷ (4.55e-2) | 3.1751e+1 ⁸ (4.94e-1) - | 3.2775e+1 ⁸ (1.37e-1) = | 3.2801e+1 ⁷ (7.78e-2) + | 3.2770e+1 ⁵ (5.01e-2) = | 3.2773e+1 ⁴ (5.72e-2) = | 3.2770e+1 ⁶ (6.99e-2) = | 3.2779e+1 ² (9.29e-2) = |
| | 5 | 1000 | 3.3923e+2 ⁰ (2.30e-1) | 1.2371e+2 ⁰ (8.42e-1) - | 1.3468e+2 ⁰ (8.93e+0) = | 1.3206e+2 ⁰ (1.50e+1) = | 1.3554e+2 ⁰ (1.00e+1) = | 1.3139e+2 ⁰ (1.45e+1) = | 1.3719e+2 ⁰ (4.35e+0) = | 1.3626e+2 ⁰ (6.78e+0) = |
| | 8 | 1000 | 1.2078e+2 ⁰ (3.00e+1) | 9.6715e+1 ⁸ (2.16e+1) = | 1.2409e+2 ⁰ (1.34e+1) = | 1.2313e+2 ⁰ (1.86e+1) = | 1.1572e+2 ⁰ (1.81e+1) = | 1.2850e+2 ⁰ (1.57e+1) = | 1.2663e+2 ⁰ (1.52e+1) = | |
| | 10 | 1500 | 2.2377e+2 ⁰ (3.53e+1) | 1.6965e+2 ⁰ (3.77e+1) - | 2.1330e+2 ⁰ (3.93e+1) = | 2.1504e+2 ⁰ (3.67e+1) + | 2.2622e+2 ⁰ (3.70e+1) = | 2.1147e+2 ⁰ (3.84e+1) = | 2.2836e+2 ⁰ (3.48e+1) = | 2.4391e+2 ⁰ (1.56e+1) = |
| DTLZ4 | 3 | 600 | 2.9445e+1 ³ (8.30e+0) | 3.2333e+1 ⁸ (2.17e-1) = | 2.8436e+1 ⁸ (9.77e+0) = | 2.7892e+1 ⁸ (9.78e+0) = | 2.4843e+1 ⁸ (1.13e+1) = | 3.1083e+1 ⁶ (6.10e+0) = | 2.6296e+1 ⁷ (1.08e+1) = | 2.7073e+1 ⁶ (1.03e+1) = |
| | 5 | 1000 | 1.2324e+2 ⁰ (3.06e+1) | 1.2702e+2 ⁰ (2.30e+1) - | 1.2460e+2 ⁰ (2.86e+1) = | 1.2061e+2 ⁰ (2.68e+1) = | 1.1441e+2 ⁰ (3.47e-1) = | 1.1764e+2 ⁰ (3.15e+1) = | 1.0810e+2 ⁰ (3.78e+1) = | |
| | 8 | 1250 | 1.3793e+2 ⁰ (2.08e+1) | 1.4877e+2 ⁰ (1.55e+1) - | 1.3386e+2 ⁰ (1.59e+1) = | 1.3591e+2 ⁰ (1.69n+1) = | 1.4111e+2 ⁰ (8.55e+0) + | 1.2801e+2 ⁰ (1.95e+1) = | 1.3278e+2 ⁰ (1.63e+1) = | 1.3668e+2 ⁰ (1.09e+1) = |
| | 10 | 2000 | 2.4519e+2 ⁰ (1.98e+1) | 2.6263e+2 ⁰ (1.01e+0) + | 2.5235e+2 ⁰ (9.67e+0) = | 2.4687e+2 ⁰ (2.20e+1) = | 2.4437e+2 ⁰ (2.18e+1) = | 2.5447e+2 ⁰ (1.04e+1) = | 2.4558e+2 ⁰ (2.09e+1) = | |
| WFG1 | 3 | 400 | 1.5666e+1 ² (5.74e-1) | 1.7062e+1 ⁸ (7.89e-1) - | 1.4545e+1 ⁸ (1.09e+0) - | 1.4744e+1 ⁸ (9.79e-1) = | 1.4676e+1 ⁸ (1.03e+0) = | 1.4654e+1 ⁶ (6.99e-1) = | 1.4590e+1 ⁷ (8.57e-1) = | 1.4711e+1 ⁴ (1.08e+0) = |
| | 5 | 750 | 2.8848e+2 ⁰ (5.16e+0) | 3.2463e+1 ⁸ (1.12e+0) = | 2.5187e+1 ⁸ (3.73e+0) = | 2.4044e+1 ⁸ (3.83e+0) = | 2.5132e+1 ⁸ (2.78e+0) = | 2.6043e+1 ⁸ (3.67e+0) = | 2.7122e+1 ⁴ (4.21e+0) = | 2.7464e+1 ³ (3.74e+0) = |
| | 8 | 1500 | 3.6051e+1 ⁵ (5.56e+0) | 4.4348e+1 ⁸ (2.46e+0) = | 3.6753e+1 ⁸ (5.16e+0) = | 3.1467e+1 ⁸ (4.85e+0) = | 3.5686e+1 ⁸ (5.47e+0) = | 3.1608e+1 ⁷ (3.17e+0) = | 4.1186e+1 ⁷ (5.06e+0) = | 3.8966e+1 ⁴ (5.50e+0) = |
| | 10 | 2000 | 5.7761e+1 ⁸ (4.90e+0) | 5.2929e+1 ⁸ (4.76e+0) - | 3.9673e+1 ⁸ (8.17e+0) = | 3.6273e+1 ⁸ (6.29e+0) = | 3.8429e+1 ⁸ (6.93e+0) = | 3.5697e+1 ⁸ (8.66e+0) = | 5.0886e+1 ⁴ (1.05e+1) = | 5.2990e+1 ² (9.34e+0) = |
| WFG4 | 3 | 400 | 3.2192e+1 ⁸ (2.48e-1) | 3.1920e+1 ⁸ (2.59e-1) - | 3.2228e+1 ⁸ (2.98e-1) = | 3.2249e+1 ⁷ (2.23e-1) = | 3.2211e+1 ⁷ (4.17e-1) = | 3.2253e+1 ⁷ (2.50e-1) = | 3.2168e+1 ⁷ (4.14e-1) = | 3.2198e+1 ² (2.85e-1) = |
| | 5 | 750 | 3.1589e+2 ⁰ (2.95e+0) | 1.3401e+2 ⁰ (6.26e-1) - | 1.3587e+2 ⁰ (4.33e+0) = | 1.3673e+2 ⁰ (7.37e-1) = | 1.3575e+2 ⁰ (4.39e+0) = | 1.3649e+2 ⁰ (9.88e-1) = | 1.3583e+2 ⁰ (4.18e+0) = | 1.3680e+2 ⁰ (4.73e-1) = |
| | 8 | 1500 | 3.4615e+2 ⁰ (1.97e+0) | 1.4940e+2 ⁰ (2.78e-1) + | 1.4616e+2 ⁰ (2.10e+0) = | 1.4595e+2 ⁰ (2.92e+0) = | 1.4606e+2 ⁰ (2.20e+0) = | 1.4637e+2 ⁰ (1.63e+0) = | 1.4661e+2 ⁰ (6.82e-1) = | 1.4636e+2 ⁰ (1.85e-0) = |
| | 10 | 2000 | 2.5582e+2 ⁰ (9.58e-1) | 2.6402e+2 ⁰ (6.88e-1) + | 2.5773e+2 ⁰ (3.71e+0) = | 2.5784e+2 ⁰ (3.92e+0) = | 2.5849e+2 ⁰ (4.17e-1) = | 2.5743e+2 ⁰ (4.81e+0) = | 2.5855e+2 ⁰ (2.17e-1) = | 2.5836e+2 ⁰ (1.63e-1) = |
| WFG5 | 3 | 400 | 3.1709e+1 ³ (9.26e-1) | 3.1279e+1 ⁸ (4.17e-1) - | 3.1292e+1 ⁷ (1.03e+0) = | 3.1548e+1 ⁸ (9.49e-1) = | 3.1794e+1 ⁷ (9.60e-1) = | 3.1309e+1 ⁶ (1.05e+0) = | 3.1757e+1 ² (9.69e-1) = | 3.1575e+1 ⁴ (9.18e-1) = |
| | 5 | 750 | 3.1375e+2 ⁰ (4.05e+0) | 3.1389e+2 ⁰ (9.77e-1) - | 1.3773e+2 ⁰ (4.13e+0) = | 1.3806e+2 ⁰ (1.21e+0) = | 1.3816e+2 ⁰ (8.10e-1) = | 1.3746e+2 ⁰ (4.08e+0) = | 1.3764e+2 ⁰ (3.81e+0) = | 1.3754e+2 ⁰ (4.02e+0) = |
| | 8 | 1500 | 1.4237e+2 ⁰ (7.57e+0) | 1.4883e+2 ⁰ (2.23e-1) + | 1.4399e+2 ⁰ (4.14e+0) = | 1.4432e+2 ⁰ (4.18e+0) = | 1.4243e+2 ⁰ (6.21e+0) = | 1.4350e+2 ⁰ (5.40e+0) = | 1.4356e+2 ⁰ (4.75e+0) = | 1.4165e+2 ⁰ (5.65e+0) = |
| | 10 | 2000 | 2.5375e+2 ⁰ (5.82e+0) | 2.6308e+2 ⁰ (3.93e-1) + | 2.5450e+2 ⁰ (4.87e+0) = | 2.5351e+2 ⁰ (5.38e+0) = | 2.5399e+2 ⁰ (5.38e+0) = | 2.5402e+2 ⁰ (6.54e+0) = | 2.5472e+2 ⁰ (5.06e+0) = | 2.5337e+2 ⁰ (6.31e+0) = |
| WFG6 | 3 | 400 | 3.2200e+1 ⁸ (4.19e-1) | 3.1981e+1 ⁸ (2.06e-1) - | 3.2249e+1 ⁸ (3.28e-1) = | 3.2328e+1 ⁷ (3.31e-1) + | 3.2199e+1 ⁷ (3.68e-1) = | 3.2345e+1 ⁶ (2.06e-1) = | 3.2251e+1 ⁴ (5.37e-1) = | 3.2280e+1 ³ (2.99e-1) = |
| | 5 | 750 | 3.1358e+2 ⁰ (2.82e-1) | 1.3360e+2 ⁰ (6.92e-1) - | 1.3845e+2 ⁰ (5.11e-1) = | 1.3845e+2 ⁰ (5.82e-1) = | 1.3824e+2 ⁰ (4.52e-1) = | 1.3836e+2 ⁰ (5.12e-1) = | 1.3834e+2 ⁰ (2.92e-1) = | 1.3801e+2 ⁰ (2.82e-0) = |
| | 8 | 1500 | 1.4719e+2 ⁰ (2.80e-2) | 1.4947e+2 ⁰ (1.74e-1) + | 1.4561e+2 ⁰ (8.53e+0) = | 1.4678e+2 ⁰ (2.01e+0) = | 1.4715e+2 ⁰ (1.88e-1) = | 1.4664e+2 ⁰ (2.83e+0) = | 1.4705e+2 ⁰ (7.57e-1) = | 1.4715e+2 ⁰ (4.14e-1) = |
| | 10 | 2000 | 2.5827e+2 ⁰ (4.57e+0) | 2.6421e+2 ⁰ (3.66e-1) + | 2.5693e+2 ⁰ (6.93e+0) = | 2.5568e+2 ⁰ (2.88e+0) = | 2.5911e+2 ⁰ (6.79e-2) = | 2.5908e+2 ⁰ (1.61e-1) = | 2.5908e+2 ⁰ (3.72e-1) = | |
| WFG7 | 3 | 400 | 3.2639e+1 ³ (4.99e-2) | 3.2086e+1 ⁸ (2.77e-1) - | 3.2638e+1 ⁸ (3.43e-2) = | 3.2643e+1 ⁸ (3.10e-2) = | 3.2631e+1 ⁸ (4.84e-2) = | 3.2639e+1 ² (4.85e-2) = | 3.2629e+1 ⁶ (6.10e-2) = | 3.2625e+1 ⁷ (6.03e-2) = |
| | 5 | 750 | 1.3734e+2 ⁰ (5.90e-1) | 1.3353e+2 ⁰ (7.70e-1) - | 1.3730e+2 ⁰ (7.52e-1) = | 1.3671e+2 ⁰ (3.42e+0) = | 1.3623e+2 ⁰ (4.58e+0) = | 1.3696e+2 ⁰ (2.22e+0) = | 1.3731e+2 ⁰ (6.24e-1) = | 1.3715e+2 ⁰ (7.87e-1) = |
| | 8 | 1500 | 1.4707e+2 ⁰ (1.54e-1) | 1.4953e+2 ⁰ (3.29e-1) + | 1.4713e+2 ⁰ (8.61e-2) = | 1.4714e+2 ⁰ (9.91e-2) = | 1.4703e+2 ⁰ (6.73e-1) = | 1.4713e+2 ⁰ (1.70e-1) + | 1.4714e+2 ⁰ (7.65e-2) + | 1.4709e+2 ⁰ (1.50e-1) = |
| | 10 | 2000 | 2.5859e+2 ⁰ (1.74e-1) | 2.6491e+2 ⁰ (5.46e-1) + | 2.5830e+2 ⁰ (2.40e+0) = | 2.5802e+2 ⁰ (3.13e+0) = | 2.5856e+2 ⁰ (3.53e-1) = | 2.5856e+2 ⁰ (3.69e-1) = | 2.5857e+2 ⁰ (2.14e-1) = | |
| WFG8 | 3 | 400 | 2.6718e+1 ⁸ (2.82e-1) | 3.1686e+1 ⁸ (2.38e-1) + | 2.6977e+1 ⁸ (3.65e-1) = | 2.6738e+1 ⁸ (3.14e-1) = | 2.6976e+1 ⁸ (4.06e-1) = | 2.7009e+1 ² (3.05e-1) = | 2.7029e+1 ² (4.39e-1) = | |
| | 5 | 750 | 3.7058e+1 ⁸ (4.58e+0) | 1.3339e+2 ⁰ (8.16e-1) + | 5.3602e+1 ⁸ (4.50e+0) = | 5.4548e+1 ⁸ (6.84e+0) = | 5.4947e+1 ⁸ (5.12e+0) = | 4.5077e+1 ⁸ (5.24e+0) = | 4.4782e+1 ⁸ (6.22e+0) = | 4.6851e+1 ⁸ (6.00e+0) = |
| | 8 | 1500 | 6.0203e+1 ⁸ (6.42e+0) | 1.4982e+2 ⁰ (2.26e-1) + | 7.8424e+1 ⁸ (9.19e+0) = | 7.7074e+1 ⁸ (9.89e+0) = | 7.6460e+1 ⁸ (7.07e+0) = | 7.1594e+1 ⁸ (4.82e+0) = | 7.2616e+1 ⁸ (4.56e+0) = | 6.9144e+1 ⁸ (4.19e+0) = |
| | 10 | 2000 | 9.8031e+1 ⁸ (1.07e+1) | 2.6508e+2 ⁰ (4.61e-1) + | 1.4166e+2 ⁰ (1.91e+1) + | 1.5438e+2 ⁰ (1.89e+1) + | 1.4410e+2 ⁰ (2.07e+1) + | | | |

Table 7: Mean and standard deviations (in parenthesis) of the HV indicator obtained by MOEAs using the NSGA-III framework on MOPs with irregular PF shapes. The two best mean values per MOP are highlighted in grayscale, where the darker tone corresponds to the best one. The symbols “+”, “−”, and “=” are placed when the MOEA performs significantly better, significantly worse, or statistically equivalent to NSGA-III based on a one-tailed Wilcoxon test using a significance level of $\alpha = 0.05$. The % of satisfaction refers to the percentage of MOPs where the MOEA performs significantly better than NSGA-III. The superscripts are the obtained rank in the comparison.

| MOP | Obj. | Gen. | NSGA-III | A-NSGA-III | NSGA-III-AdaRSE | NSGA-III-AdaGAE | NSGA-III-AdaMPT | NSGA-III-AdaCOU | NSGA-III-AdaPT | NSGA-III-AdaKRA |
|---------------------|------|------|----------------------------------|----------------------------------|------------------------------------|------------------------------------|------------------------------------|------------------------------------|------------------------------------|------------------------------------|
| DTLZ5 | 3 | 400 | 5.4810e+0 ⁸ (5.67e-3) | 5.4900e+0 ⁷ (3.43e-3) | 5.5074e+0 ³ (8.57e-3) + | 5.5044e+0 ⁵ (1.12e-2) + | 5.5076e+0 ² (1.21e-3) + | 5.5060e+0 ¹ (1.66e-2) + | 5.5077e+0 ¹ (6.22e-3) + | 5.5001e+0 ⁶ (4.21e-2) + |
| | 5 | 600 | 3.1188e+0 ¹ (4.91e-2) | 3.1082e+0 ² (9.72e-1) | 3.0881e+0 ⁷ (1.76e-1) + | 3.0812e+0 ⁸ (2.42e-1) + | 3.0937e+0 ¹ (1.52e-1) + | 3.1143e+0 ² (8.07e-2) + | 3.1000e+0 ¹ (1.21e-1) + | 3.0988e+0 ⁵ (1.25e-1) + |
| | 8 | 750 | 2.4790e+0 ² (3.76e-1) | 2.4781e+0 ² (4.42e-1) | 2.4499e+0 ⁶ (2.03e-0) + | 2.4617e+0 ⁴ (1.63e-0) + | 2.4611e+0 ² (1.62e-0) + | 2.4789e+0 ² (8.97e-1) + | 2.4276e+0 ² (1.63e-0) + | 2.4252e+0 ² (1.34e-0) + |
| | 10 | 1000 | 9.9280e+0 ² (1.22e-0) | 9.9255e+0 ³ (1.84e+0) | 9.8255e+0 ⁶ (7.33e-0) + | 9.8326e+0 ⁵ (5.29e+0) + | 9.8448e+0 ⁴ (6.99e+0) + | 9.9683e+0 ² (2.82e+0) + | 9.7152e+0 ² (7.06e+0) + | 9.6961e+0 ² (5.16e+0) + |
| DTLZ6 | 3 | 400 | 5.4793e+0 ⁸ (6.74e-3) | 5.4893e+0 ⁷ (3.20e-3) | 5.5116e+0 ³ (6.32e-3) + | 5.5056e+0 ⁶ (8.96e-4) + | 5.5058e+0 ² (8.24e-4) + | 5.5110e+0 ¹ (4.65e-3) + | 5.5117e+0 ² (3.46e-3) + | 5.5119e+0 ¹ (2.69e-3) + |
| | 5 | 600 | 3.1882e+0 ¹ (1.73e-2) | 3.1870e+0 ² (1.96e-2) | 3.1820e+0 ⁸ (4.03e-2) + | 3.1828e+0 ⁷ (3.43e-2) + | 3.1829e+0 ⁶ (4.08e-2) + | 3.1837e+0 ² (3.50e-2) + | 3.1829e+0 ¹ (4.23e-2) + | 3.1848e+0 ¹ (3.66e-2) + |
| | 8 | 750 | 2.5507e+0 ² (2.42e-1) | 2.5503e+0 ² (1.48e-1) | 2.5455e+0 ² (2.89e-1) + | 2.5444e+0 ⁸ (4.04e-1) + | 2.5457e+0 ² (3.06e-1) + | 2.5458e+0 ² (2.58e-1) + | 2.5460e+0 ² (3.71e-1) + | 2.5459e+0 ² (3.06e-1) + |
| | 10 | 1000 | 1.0207e+0 ³ (2.42e-0) | 1.0177e+0 ³ (2.72e-0) | 1.0179e+0 ⁷ (1.73e+0) + | 1.0182e+0 ⁴ (1.47e+0) + | 1.0180e+0 ³ (1.83e+0) + | 1.0197e+0 ² (8.50e-1) + | 1.0182e+0 ³ (1.25e+0) + | 1.0182e+0 ³ (1.47e+0) + |
| DTLZ7 | 3 | 400 | 6.5205e+0 ⁶ (2.06e-1) | 6.5140e+0 ⁸ (2.54e-1) | 6.5455e+0 ⁴ (2.11e-1) + | 6.5708e+0 ³ (1.52e-1) + | 6.5716e+0 ² (1.50e-1) + | 6.5438e+0 ² (2.11e-1) + | 6.5730e+0 ¹ (1.51e-1) + | 6.5181e+0 ⁷ (2.54e-1) + |
| | 5 | 1000 | 2.5042e+0 ¹ (7.65e-2) | 2.4889e+0 ² (6.34e-2) | 2.5224e+0 ² (7.79e-2) + | 2.5126e+0 ⁵ (9.93e-2) + | 2.5097e+0 ¹ (1.21e-1) + | 2.5210e+0 ¹ (1.11e-1) + | 2.5225e+0 ¹ (6.88e-2) + | 2.5231e+0 ² (6.92e-2) + |
| | 8 | 1000 | 1.8183e+0 ² (6.41e-1) | 1.7840e+0 ² (5.15e-1) | 1.8639e+0 ⁴ (4.94e-1) + | 1.8574e+0 ⁴ (4.84e-1) + | 1.8665e+0 ² (5.01e-1) + | 1.8578e+0 ² (2.70e-1) + | 1.8656e+0 ² (4.41e-1) + | 1.8644e+0 ² (5.55e-1) + |
| | 10 | 1500 | 7.0037e+0 ² (2.64e+0) | 6.8765e+0 ⁸ (3.25e+0) | 7.1469e+0 ² (3.45e+0) + | 7.1431e+0 ⁴ (2.44e+0) + | 7.1544e+0 ² (1.80e+0) + | 7.1991e+0 ² (1.20e+0) + | 7.0767e+0 ² (3.77e+0) + | 7.0839e+0 ² (4.28e+0) + |
| WFG2 | 3 | 400 | 7.8650e+0 ⁸ (1.08e-2) | 7.8551e+0 ⁷ (1.34e-3) | 7.8653e+0 ⁷ (8.79e-3) + | 7.8574e+0 ⁷ (1.70e-2) + | 7.8610e+0 ⁷ (1.34e-2) + | 7.8596e+0 ⁷ (1.48e-2) + | 7.8595e+0 ⁷ (1.67e-2) + | 7.8644e+0 ³ (1.24e-2) + |
| | 5 | 750 | 3.1900e+0 ¹ (1.96e-2) | 3.1893e+0 ¹ (1.76e-2) | 3.1910e+0 ⁴ (1.74e-2) + | 3.1900e+0 ⁵ (1.71e-2) + | 3.1905e+0 ² (1.59e-2) + | 3.1906e+0 ¹ (1.41e-2) + | 3.1903e+0 ¹ (1.74e-2) + | 3.1901e+0 ¹ (1.89e-2) + |
| | 8 | 1500 | 2.5560e+0 ⁶ (1.14e-1) | 2.5553e+0 ⁸ (1.56e-1) | 2.5561e+0 ² (9.20e-2) + | 2.5548e+0 ¹ (9.19e-2) + | 2.5560e+0 ² (1.29e-1) + | 2.5561e+0 ¹ (9.63e-2) + | 2.5562e+0 ² (1.02e-1) + | 2.5564e+0 ² (9.82e-2) + |
| | 10 | 2000 | 1.0232e+0 ³ (2.58e-1) | 1.0229e+0 ³ (4.06e-1) | 1.0233e+0 ³ (2.93e-1) + | 1.0233e+0 ³ (3.21e-1) + | 1.0233e+0 ³ (2.54e-1) + | 1.0233e+0 ³ (2.88e-1) + | 1.0233e+0 ³ (2.37e-1) + | |
| WFG3 | 3 | 400 | 7.0237e+0 ⁶ (2.22e-2) | 7.0148e+0 ³ (2.10e-2) | 7.0054e+0 ⁶ (2.31e-2) - | 6.9911e+0 ⁸ (2.47e-2) - | 7.0007e+0 ⁷ (1.72e-2) - | 7.0154e+0 ⁷ (1.98e-2) - | 7.0066e+0 ⁷ (2.56e-2) - | 7.0087e+0 ⁴ (1.80e-2) - |
| | 5 | 750 | 2.8861e+0 ¹ (6.78e-2) | 2.8504e+0 ¹ (1.06e-2) | 2.8490e+0 ⁶ (1.01e-1) + | 2.8370e+0 ⁸ (1.21e-1) + | 2.8435e+0 ⁷ (1.01e-1) + | 2.8500e+0 ⁷ (1.46e-1) + | 2.8588e+0 ¹ (1.29e-1) + | 2.8603e+0 ² (1.23e-1) + |
| | 8 | 1500 | 7.2820e+0 ² (9.69e-1) | 2.2558e+0 ² (1.55e+0) | 2.2526e+0 ² (1.66e+0) + | 2.2556e+0 ² (1.72e+0) + | 2.2556e+0 ² (1.80e+0) + | 2.3232e+0 ² (1.04e+0) + | 2.3011e+0 ² (1.39e+0) + | 2.3005e+0 ² (1.59e+0) + |
| | 10 | 2000 | 9.1788e+0 ² (2.87e+0) | 9.0989e+0 ⁶ (5.45e+0) | 9.1245e+0 ² (6.46e+0) + | 9.0867e+0 ⁸ (6.13e+0) + | 9.0928e+0 ² (4.91e+0) + | 9.4403e+0 ² (2.74e+0) + | 9.3276e+0 ² (5.04e+0) + | 9.3371e+0 ² (4.11e+0) + |
| DTLZ1 ⁻¹ | 3 | 400 | 5.4225e+0 ⁸ (1.07e-0) | 5.4379e+0 ⁷ (6.38e-3) | 5.5049e+0 ³ (3.21e-3) + | 5.4959e+0 ⁶ (3.26e-3) + | 5.4966e+0 ² (2.87e-3) + | 5.5004e+0 ² (2.46e-3) + | 5.5039e+0 ³ (3.59e-3) + | 5.5042e+0 ² (3.81e-3) + |
| | 5 | 600 | 3.9324e+0 ¹ (1.41e-1) | 3.9167e+0 ² (4.23e-1) | 3.9060e+0 ⁴ (4.90e-2) + | 3.0469e+0 ⁶ (7.88e-2) + | 3.0636e+0 ⁵ (7.95e-2) + | 3.1274e+0 ¹ (1.87e-2) + | 3.1259e+0 ¹ (2.22e-2) + | 3.1269e+0 ¹ (2.04e-2) + |
| | 8 | 750 | 7.4554e+0 ² (4.15e-0) | 7.5574e+0 ⁸ (3.34e-1) | 2.0239e+0 ² (1.91e-1) + | 1.8639e+0 ¹ (3.15e-1) + | 1.9724e+0 ² (4.23e-1) + | 2.0363e+0 ¹ (4.94e-2) + | 2.0393e+0 ² (4.95e-2) + | 2.0386e+0 ² (4.80e-2) + |
| | 10 | 1000 | 8.4726e+0 ² (5.56e-1) | 8.5490e+0 ⁸ (5.54e-1) | 2.9734e+0 ⁴ (2.05e-1) + | 2.7414e+0 ⁴ (4.31e-1) + | 2.9744e+0 ⁵ (2.93e-1) + | 2.9754e+0 ¹ (6.14e-1) + | 2.9767e+0 ¹ (8.28e-2) + | 2.9749e+0 ¹ (7.36e-2) + |
| DTLZ2 ⁻¹ | 3 | 250 | 6.6630e+0 ⁸ (4.99e-3) | 6.6801e+0 ⁷ (6.12e-3) | 6.7162e+0 ¹ (2.09e-3) + | 6.7128e+0 ⁵ (2.76e-3) + | 6.7114e+0 ¹ (3.23e-3) + | 6.7128e+0 ⁰ (3.33e-3) + | 6.7150e+0 ² (2.57e-3) + | 6.7159e+0 ² (2.47e-3) + |
| | 5 | 350 | 1.6429e+0 ¹ (19.9e-2) | 1.6080e+0 ⁸ (9.68e-2) | 1.7409e+0 ⁵ (5.46e-2) + | 1.7142e+0 ⁶ (7.55e-2) + | 1.7241e+0 ¹ (8.36e-2) + | 1.7476e+0 ¹ (3.92e-2) + | 1.7424e+0 ¹ (5.63e-2) + | |
| | 8 | 500 | 2.7872e+0 ¹ (1.05e+0) | 2.1528e+0 ² (9.66e-1) | 4.1104e+0 ¹ (7.17e-1) + | 4.1928e+0 ² (5.90e-1) + | 4.2007e+0 ¹ (6.39e-1) + | 3.9060e+0 ¹ (4.18e-1) + | 3.7589e+0 ¹ (3.36e-1) + | 3.7890e+0 ¹ (5.03e-1) + |
| | 10 | 750 | 4.5254e+0 ¹ (1.30e+0) | 4.5131e+0 ⁸ (1.89e-1) | 7.2094e+0 ¹ (1.13e+0) + | 7.4089e+0 ² (1.65e+0) + | 7.4599e+0 ¹ (1.56e+0) + | 6.4514e+0 ¹ (5.20e-1) + | 6.1845e+0 ¹ (5.67e-1) + | 6.1582e+0 ¹ (5.13e-1) + |
| DTLZ3 ⁻¹ | 3 | 1000 | 6.6636e+0 ⁸ (5.25e-3) | 6.6814e+0 ⁷ (6.38e-3) | 6.6814e+0 ⁷ (6.76e-3) + | 6.7185e+0 ⁶ (1.76e-3) + | 6.7185e+0 ² (1.53e-3) + | 6.7195e+0 ¹ (1.51e-3) + | 6.7188e+0 ² (1.85e-3) + | 6.7185e+0 ² (1.95e-3) + |
| | 5 | 1000 | 1.6208e+0 ¹ (1.56e-1) | 1.5908e+0 ² (1.76e-1) | 1.7518e+0 ⁴ (5.99e-2) + | 1.7226e+0 ⁵ (8.85e-2) + | 1.7300e+0 ¹ (1.21e-1) + | 1.7552e+0 ¹ (3.75e-2) + | 1.7538e+0 ¹ (5.01e-2) + | |
| | 8 | 1000 | 2.6243e+0 ² (4.15e-0) | 2.6524e+0 ² (1.08e-0) | 3.9950e+0 ² (8.04e-1) + | 3.8758e+0 ³ (1.19e-0) + | 4.0172e+0 ² (1.44e-0) + | 3.8510e+0 ¹ (3.56e-1) + | 3.7270e+0 ¹ (5.88e-1) + | 3.7151e+0 ¹ (5.46e-1) + |
| | 10 | 1500 | 4.2963e+0 ² (1.19e+0) | 4.2629e+0 ² (1.63e+0) | 7.1389e+0 ¹ (2.56e-0) + | 7.0979e+0 ² (1.72e-0) + | 7.1928e+0 ¹ (1.68e-0) + | 6.4103e+0 ¹ (3.94e-1) + | 6.1396e+0 ¹ (6.07e-1) + | 6.1435e+0 ¹ (7.06e-1) + |
| DTLZ4 ⁻¹ | 3 | 600 | 6.6669e+0 ⁸ (4.87e-3) | 6.6844e+0 ⁷ (4.78e-3) | 6.7178e+0 ⁶ (2.33e-3) + | 6.7178e+0 ⁴ (2.64e-3) + | 6.7178e+0 ² (1.89e-3) + | 6.7180e+0 ⁵ (2.54e-3) + | 6.7184e+0 ² (1.95e-3) + | 6.7186e+0 ² (1.95e-3) + |
| | 5 | 1000 | 1.0775e+0 ¹ (1.27e-1) | 1.6948e+0 ² (1.79e-1) | 1.8526e+0 ⁴ (7.03e-2) + | 1.8094e+0 ⁵ (1.02e-1) + | 1.8204e+0 ² (1.61e-1) + | 1.8807e+0 ¹ (3.56e-2) + | 1.8826e+0 ¹ (3.14e-2) + | 1.8823e+0 ¹ (4.75e-2) + |
| | 8 | 1250 | 3.7093e+0 ² (1.79e-1) | 3.7076e+0 ¹ (6.27e-1) | 3.9412e+0 ¹ (3.61e-1) + | 3.9728e+0 ² (5.01e-1) + | 3.9942e+0 ¹ (5.30e-1) + | 3.8194e+0 ¹ (2.17e-1) + | 3.7045e+0 ¹ (2.92e-1) + | 3.7095e+0 ¹ (2.77e-1) + |
| | 10 | 2000 | 6.6342e+0 ¹ (1.46e+0) | 6.6518e+0 ² (1.06e+0) | 1.0700e+0 ¹ (3.24e-1) + | 1.1905e+0 ² (3.42e-1) + | 1.2016e+0 ² (1.72e-0) + | 6.3449e+0 ¹ (1.26e-1) + | 6.1518e+0 ¹ (4.65e-1) + | 6.1492e+0 ¹ (4.05e-1) + |
| DTLZ5 ⁻¹ | 3 | 400 | 6.7053e+0 ⁸ (9.11e-3) | 6.7203e+0 ⁷ (1.48e-3) | 6.7230e+0 ⁶ (1.85e-3) + | 6.7230e+0 ⁶ (1.85e-3) + | 6.7244e+0 ⁴ (2.52e-3) + | 6.7235e+0 ⁵ (2.27e-3) + | 6.7316e+0 ² (1.99e-3) + | 6.7318e+0 ² (1.85e-3) + |
| | 5 | 600 | 1.7756e+0 ¹ (1.27e-2) | 1.6948e+0 ² (1.79e-2) | 1.8526e+0 ⁴ (7.03e-2) + | 1.8094e+0 ⁵ (1.02e-2) + | 1.8204e+0 ² (1.61e-2) + | 1.8807e+0 ¹ (3.56e-2) + | 1.8826e+0 ¹ (3.14e-2) + | 1.8823e+0 ¹ (4.75e-2) + |
| | 8 | 750 | 3.2742e+0 ² (1.17e+0) | 3.2172e+0 ¹ (2.10e+0) | 3.9120e+0 ² (1.40e+0) + | 3.7212e+0 ¹ (2.32e+0) + | 3.9021e+0 ² (1.20e+0) + | 3.7500e+0 ¹ (2.36e+0) + | 3.5995e+0 ¹ (2.95e-1) + | 3.5257e+0 ¹ (3.02e-1) + |
| | 10 | 1000 | 5.6190e+0 ¹ (1.95e+0) | 4.9727e+0 | | | | | | |

Table 8: Mean and standard deviations (in parenthesis) of the SPD indicator obtained by MOEAs using the NSGA-III framework on MOPs with irregular PF shapes. The two best mean values per MOP are highlighted in grayscale, where the darker tone corresponds to the best one. The symbols “+”, “-”, and “=” are placed when the MOEA performs significantly better, significantly worse, or statistically equivalent to NSGA-III based on a one-tailed Wilcoxon test using a significance level of $\alpha = 0.05$. The % of satisfaction refers to the percentage of MOPs where the MOEA performs significantly better than NSGA-III. The superscripts are the obtained rank in the comparison.

| MOP | Obj. | Gen. | NSGA-III | A-NSGA-III | NSGA-III-AdaRSE | NSGA-III-AdaGAE | NSGA-III-AdaMPT | NSGA-III-AdaCOU | NSGA-III-AdaPT | NSGA-III-AdaKRA |
|---------|------|------|----------------------|----------------------|-------------------------|------------------------|-------------------------|------------------------|------------------------|------------------------|
| DTLZ5 | 3 | 400 | 1.0047e+18 (1.18e-1) | 1.0248e+17 (6.63e-2) | + 1.0427e+14 (1.33e-1) | + 1.0414e+15 (7.81e-2) | + 1.0437e+12 (1.59e-2) | + 1.0439e+12 (1.12e-1) | + 1.0449e+13 (3.75e-2) | + 1.0375e+16 (3.51e-1) |
| | 5 | 600 | 2.2132e+15 (1.42e+0) | 2.0791e+18 (1.72e+0) | + 2.2743e+12 (2.00e+0) | + 2.1600e+16 (2.25e+0) | + 2.1288e+17 (2.36e+0) | + 2.2315e+17 (1.32e+0) | + 2.5661e+13 (2.07e+0) | + 2.5146e+12 (2.43e+0) |
| | 8 | 750 | 3.3044e+14 (4.14e+0) | 3.8213e+14 (4.59e+0) | + 4.5677e+13 (7.99e+0) | + 3.3671e+17 (4.09e+0) | + 3.6354e+16 (5.71e+0) | + 3.7846e+15 (3.79e+0) | + 9.1547e+17 (7.02e+0) | + 9.4464e+16 (5.90e+0) |
| | 10 | 1000 | 6.1875e+17 (5.47e+0) | 9.4568e+13 (2.24e+1) | + 7.3127e+14 (1.29e+1) | + 5.2289e+18 (6.84e+0) | + 6.2351e+16 (9.07e+0) | + 6.5351e+15 (6.10e+0) | + 1.7715e+22 (5.42e+0) | + 1.7743e+24 (5.98e+0) |
| DTLZ6 | 3 | 400 | 9.9043e+08 (1.52e-1) | 1.0194e+17 (1.84e-1) | + 1.0480e+17 (1.83e-2) | + 1.0425e+16 (1.74e-2) | + 1.0443e+15 (7.54e-3) | + 1.0478e+13 (2.30e-2) | + 1.0513e+11 (1.65e-1) | + 1.0481e+12 (1.36e-2) |
| | 5 | 600 | 2.1323e+15 (1.42e+0) | 2.0791e+18 (1.72e+0) | + 2.2743e+12 (2.00e+0) | + 2.1600e+16 (2.25e+0) | + 2.1288e+17 (2.36e+0) | + 2.2315e+17 (1.32e+0) | + 2.5661e+13 (2.07e+0) | + 2.5146e+12 (2.43e+0) |
| | 8 | 750 | 2.5631e+17 (3.40e+0) | 3.4547e+13 (4.53e+0) | + 2.9918e+14 (3.16e+0) | + 2.8114e+16 (3.37e+0) | + 2.8967e+17 (3.99e+0) | + 2.4864e+15 (3.60e+0) | + 4.1893e+13 (6.04e+0) | + 4.3082e+13 (4.69e+0) |
| | 10 | 1000 | 4.0761e+19 (5.03e+0) | 9.9001e+11 (3.16e+1) | + 4.2746e+14 (5.00e+0) | + 3.9190e+17 (4.03e+0) | + 4.2121e+15 (3.69e+0) | + 3.7647e+18 (4.32e+0) | + 7.8143e+12 (7.69e+0) | + 7.3480e+13 (9.33e+0) |
| DTLZ7 | 3 | 400 | 9.9043e+08 (1.52e-1) | 1.0194e+17 (1.84e-1) | + 1.0480e+17 (1.83e-2) | + 1.0425e+16 (1.74e-2) | + 1.0443e+15 (7.54e-3) | + 1.0478e+13 (2.30e-2) | + 1.0513e+11 (1.65e-1) | + 1.0481e+12 (1.36e-2) |
| | 5 | 600 | 1.3755e+16 (1.20e+0) | 1.2791e+18 (1.04e+0) | + 1.7708e+13 (2.19e+0) | + 1.7001e+14 (1.78e+0) | + 1.6929e+15 (2.11e+0) | + 1.5402e+14 (1.80e+0) | + 1.9250e+11 (1.83e+0) | + 1.8738e+12 (1.55e+0) |
| | 8 | 750 | 2.5631e+17 (3.40e+0) | 3.4547e+13 (4.53e+0) | + 2.9918e+14 (3.16e+0) | + 2.8114e+16 (3.37e+0) | + 2.8967e+17 (3.99e+0) | + 2.4864e+15 (3.60e+0) | + 4.1893e+13 (6.04e+0) | + 4.3082e+13 (4.69e+0) |
| | 10 | 1000 | 4.0761e+19 (5.03e+0) | 9.9001e+11 (3.16e+1) | + 4.2746e+14 (5.00e+0) | + 3.9190e+17 (4.03e+0) | + 4.2121e+15 (3.69e+0) | + 3.7647e+18 (4.32e+0) | + 7.8143e+12 (7.69e+0) | + 7.3480e+13 (9.33e+0) |
| WFG2 | 3 | 1000 | 2.3038e+17 (2.97e+0) | 2.2156e+18 (3.52e+0) | + 2.4403e+14 (3.39e+0) | + 2.4615e+13 (2.45e+0) | + 2.4705e+12 (2.44e+0) | + 2.4352e+13 (3.37e+0) | + 2.4861e+11 (2.46e+0) | + 2.4019e+16 (4.10e+0) |
| | 5 | 1000 | 1.1640e+20 (1.66e+0) | 1.2835e+20 (2.55e+0) | + 1.5273e+17 (2.17e+0) | + 1.5098e+22 (2.27e+0) | + 1.5030e+23 (2.10e+0) | + 1.4101e+20 (3.12e+0) | + 1.4545e+21 (2.06e+0) | + 1.4502e+25 (2.53e+0) |
| | 8 | 1500 | 3.3044e+17 (2.17e+0) | 3.9399e+17 (2.77e+0) | + 5.1454e+24 (5.24e-1) | + 5.1421e+23 (5.82e-1) | + 5.1437e+23 (4.75e-1) | + 5.1526e+26 (5.12e-1) | + 5.1434e+24 (4.46e-1) | + 5.1447e+21 (4.24e-1) |
| | 10 | 1500 | 2.4481e+28 (2.30e+0) | 2.5074e+27 (2.74e+0) | + 2.7315e+22 (5.75e-1) | + 2.7278e+24 (2.41e+0) | + 2.7085e+29 (8.41e-1) | + 2.7300e+28 (6.29e-1) | + 2.7263e+22 (2.44e+0) | |
| WFG3 | 3 | 400 | 2.0618e+14 (2.51e-1) | 2.0190e+18 (3.62e-1) | + 2.0548e+17 (1.78e-1) | + 2.0648e+16 (1.54e-1) | + 2.0622e+13 (3.58e-1) | + 2.0565e+15 (2.72e-1) | + 2.0548e+19 (2.95e-1) | + 2.0637e+12 (2.13e-1) |
| | 5 | 750 | 4.0023e+11 (6.65e-1) | 3.9234e+18 (8.08e-1) | + 3.9767e+17 (7.57e-1) | + 3.9775e+15 (6.60e-1) | + 3.9774e+11 (6.49e-1) | + 3.9979e+11 (6.03e-1) | + 3.9973e+11 (7.39e-1) | + 3.9853e+14 (5.50e-1) |
| | 8 | 1500 | 5.1547e+17 (1.24e+0) | 4.9080e+18 (2.48e+0) | + 5.1740e+18 (6.43e-1) | + 5.1412e+14 (1.26e+0) | + 5.1420e+17 (1.28e+0) | + 5.1387e+19 (1.35e+0) | + 5.1402e+15 (1.12e+0) | + 5.1423e+13 (1.24e+0) |
| | 10 | 2000 | 6.9279e+16 (1.25e+0) | 5.9667e+18 (8.72e-1) | + 6.9726e+11 (1.30e+0) | + 6.7954e+14 (1.21e+0) | + 6.9314e+12 (1.41e+0) | + 6.8740e+16 (1.33e+0) | + 6.8896e+15 (1.78e+0) | + 6.9190e+14 (1.61e+0) |
| DTLZ1 | 3 | 400 | 1.2655e+15 (5.81e-1) | 1.2413e+17 (5.03e-1) | + 1.2733e+12 (3.90e-1) | + 1.2639e+16 (4.48e-1) | + 1.2684e+14 (4.20e-1) | + 1.2341e+13 (3.64e-1) | + 1.2709e+13 (3.73e-1) | + 1.2799e+11 (4.00e-1) |
| | 5 | 750 | 4.4270e+15 (6.26e-1) | 4.4373e+17 (6.16e-1) | + 4.3641e+16 (7.11e-1) | + 4.3734e+18 (7.34e-1) | + 4.3658e+17 (1.06e-1) | + 4.4278e+14 (7.56e-1) | + 4.8558e+11 (6.04e-1) | + 4.8529e+12 (5.34e-1) |
| | 8 | 1500 | 6.3767e+16 (1.40e+0) | 7.3987e+18 (8.11e-1) | + 8.2692e+12 (2.17e+0) | + 7.4538e+16 (2.07e+0) | + 7.7567e+15 (1.80e+0) | + 7.7952e+18 (5.50e-1) | + 8.5092e+12 (1.12e+0) | + 8.5172e+11 (1.27e-1) |
| | 10 | 2000 | 1.0317e+28 (1.50e+0) | 1.1389e+26 (8.40e-1) | + 1.2416e+23 (1.98e+0) | + 1.0911e+27 (2.10e+1) | + 1.1799e+25 (3.26e+0) | + 1.2248e+24 (3.77e+0) | + 1.2991e+21 (1.47e+0) | + 1.2982e+22 (1.51e+0) |
| DTLZ1-1 | 3 | 400 | 2.1750e+18 (2.43e-1) | 2.3014e+17 (1.00e-1) | + 2.3181e+16 (4.77e-2) | + 2.3148e+16 (5.76e-2) | + 2.3162e+16 (4.51e-2) | + 2.3169e+13 (3.80e-2) | + 2.3162e+14 (3.18e-2) | + 2.3174e+12 (4.59e-2) |
| | 5 | 600 | 4.2213e+16 (1.18e+0) | 4.5097e+17 (2.44e+0) | + 4.5977e+16 (5.89e-1) | + 6.0448e+14 (9.38e-1) | + 6.3551e+15 (8.66e-1) | + 7.2030e+12 (2.88e-1) | + 7.1666e+13 (2.74e-1) | + 7.1640e+13 (3.38e-1) |
| | 8 | 750 | 2.4903e+17 (1.94e-1) | 2.5673e+17 (1.59e-1) | + 1.0593e+20 (1.02e+0) | + 9.7300e+16 (1.25e-1) | + 1.0279e+20 (2.120e-1) | + 9.7898e+17 (1.01e+0) | + 9.7627e+11 (9.07e-1) | + 9.7617e+19 (9.66e-1) |
| | 10 | 1000 | 2.3717e+21 (2.36e+0) | 2.4039e+21 (2.37e+0) | + 1.7271e+21 (1.94e+0) | + 1.5559e+24 (2.69e+0) | + 1.6832e+21 (1.86e+0) | + 1.5556e+25 (1.25e-1) | | |
| DTLZ2 | 3 | 250 | 2.9548e+18 (3.11e-1) | 2.9796e+17 (3.99e-1) | + 3.2463e+12 (1.34e-1) | + 3.2052e+16 (2.10e-1) | + 3.2180e+14 (2.32e-1) | + 3.2175e+15 (1.60e-1) | + 3.2367e+13 (1.72e-1) | + 3.2489e+11 (1.52e-1) |
| | 5 | 350 | 1.0153e+20 (2.17e-1) | 1.0080e+28 (1.53e+0) | + 1.2848e+22 (1.57e-1) | + 1.1705e+26 (3.09e-1) | + 1.2130e+20 (3.34e-1) | + 1.3120e+21 (1.19e+0) | + 1.2465e+24 (1.19e+0) | + 1.2491e+22 (1.49e+0) |
| | 8 | 500 | 8.6972e+16 (4.38e+0) | 8.6035e+18 (1.53e+0) | + 8.3627e+21 (2.130e+0) | + 8.2174e+21 (2.02e+0) | + 8.3215e+24 (2.05e+0) | + 8.1348e+24 (1.51e+0) | + 8.3206e+25 (1.51e+0) | + 8.3279e+24 (1.85e+0) |
| | 10 | 750 | 1.2427e+20 (6.09e+0) | 1.2386e+28 (5.69e+0) | + 2.4543e+21 (2.42e+0) | + 2.2365e+26 (5.84e+0) | + 2.3533e+24 (3.33e+0) | + 2.3973e+24 (2.46e+0) | + 2.3524e+24 (1.87e+0) | + 2.3395e+24 (2.08e+0) |
| DTLZ3 | 3 | 1000 | 2.9623e+18 (3.09e-1) | 2.9700e+17 (3.13e-1) | + 3.2700e+13 (9.64e-2) | + 3.2464e+16 (1.39e-1) | + 3.2510e+15 (1.06e-1) | + 3.2510e+14 (2.99e-2) | + 3.2772e+11 (5.57e-2) | + 3.2704e+12 (8.27e-2) |
| | 5 | 1000 | 1.0425e+20 (1.99e-1) | 1.0011e+28 (1.20e-1) | + 1.3139e+22 (1.34e-1) | + 1.1917e+26 (2.29e-1) | + 1.2295e+20 (3.59e-1) | + 1.3441e+21 (9.99e-1) | + 1.2787e+24 (1.34e-1) | + 1.2852e+24 (1.44e-1) |
| | 8 | 1000 | 9.0102e+17 (3.42e-1) | 8.6076e+18 (2.06e-1) | + 1.3636e+22 (2.41e+0) | + 1.4181e+26 (3.28e+0) | + 1.2766e+20 (2.63e+0) | + 1.3590e+24 (1.82e+0) | + 1.3275e+24 (1.75e+0) | + 1.3342e+23 (1.59e+0) |
| | 10 | 1500 | 1.2796e+20 (8.32e+0) | 1.2796e+22 (6.60e+0) | + 2.4638e+22 (2.45e+0) | + 2.1153e+26 (4.87e+0) | + 2.2967e+22 (3.42e+0) | + 2.4227e+24 (2.56e+0) | + 2.3737e+24 (2.83e+0) | + 2.3784e+23 (2.83e+0) |
| DTLZ4 | 3 | 600 | 2.9714e+18 (3.39e-1) | 2.9745e+17 (2.83e-1) | + 3.2726e+11 (9.25e-2) | + 3.2430e+16 (1.10e-1) | + 3.2481e+14 (1.12e-1) | + 3.2466e+15 (8.50e-2) | + 3.2723e+12 (1.24e-1) | + 3.2710e+13 (1.24e-1) |
| | 5 | 1000 | 1.0579e+20 (2.13e-1) | 1.0568e+28 (1.89e-1) | + 1.3517e+20 (7.74e-1) | + 1.2804e+26 (1.02e-1) | + 1.2992e+20 (8.98e-1) | + 1.3060e+21 (5.80e-1) | + 1.2960e+22 (1.12e-1) | + 1.3038e+23 (1.22e-1) |
| | 8 | 1250 | 1.1630e+20 (3.59e-1) | 1.1588e+26 (3.66e-1) | + 1.4052e+22 (1.69e-1) | + 1.3956e+23 (1.54e-1) | + 1.4092e+24 (1.47e-1) | + 1.3703e+24 (1.41e-1) | + 1.3421e+24 (1.82e-1) | + 1.3413e+24 (1.21e-1) |
| | 10 | 2000 | 1.8845e+28 (5.70e+0) | 1.8929e+26 (2.65e+0) | + 2.5305e+22 (2.01e+0) | + 2.4970e+29 (2.09e+0) | + 2.5153e+24 (1.81e+0) | + 2.4423e+28 (2.37e+0) | + 2.3918e+26 (2.90e+0) | + 2.3991e+28 (1.62e+0) |
| DTLZ5-1 | 3 | 400 | 2.4637e+18 (1.86e-1) | 2.4801e+17 (2.01e-1) | + 2.6908e+12 (1.06e-1) | + 2.6311e+16 (1.50e-1) | + 2.6120e+15 (1.14e-1) | + 2.6581e+14 (1.14e-1) | + 2.7024e+12 (1.17e-1) | + 2.7039e+11 (1.06e-1) |
| | 5 | 600 | 7.7505e+17 (1.32e-1) | 7.5470e+18 (1.56e-1) | + 9.7868e+14 (6.92e-1) | + 9.5456e+16 (1.81e-1) | + 8.9001e+19 (1.64e-1) | + 1.0155e+21 (4.70e-1) | + 9.9716e+14 (7.57e-1) | + 9.7451e+17 (7.45e-1) |
| | 8 | 750 | 5.3928e+17 (2.42e-1) | 5.4285e+18 (3.28e-1) | + 1.2617e+21 (1.32e-1) | + 1.1322e+26 (3.52e-1) | + 1.2079e+24 (2.80e-1) | + 1.2528e+20 (1.69e-1) | + 1.1996e+25 (4.49e-1) | + 1.2001e+24 (1.26e-1) |
| | 10 | 1000 | 6.1414e+20 (4.25e-1) | 6.1919e+17 (4.13e-1) | + 2.2174e+22 (2.65e-1) | + 1.9012e+26 (4.14e-1) | + 2.0647e+24 (4.89e-1) | + 2.1903e+24 (2.52e-1) | + 2.0732e+24 (1.99e-1) | + 2.0750e+24 (2.76e-1) |
| DTLZ7-1 | 3 | 1000 | 1.4518e+17 (9.51e-1) | 1.4114e+18 (1.48e-1) | + 1.5117e+18 (8.23e-1) | + 1.4744e+16 (1.03e-1) | + 1.4868e+15 (3.11e-1) | + 1.4981e+13 (8.25e-2) | + 1.4913e+14 (2.62e-1) | + 1.5002e+14 (2.61e-1) |
| | 5 | 1000 | 9.6418e+17 (1.75e-1) | 1.0141e+24 (1.56e-1) | + 9.4879e+18 (1.65e-1) | + 1.0192e+29 (2.31e-1) | + 9.5955e+19 (1.95e-1) | + 1.1308e+22 (2.22e-1) | + 1.0858e+24 (2.22e-1) | |
| | 8 | 1000 | 1.3700e+20 (5.30e-1) | 1.3184e+28 (4.52e+0) | + 1.5348e+24 (3.09e-1) | + 1.5091e+29 (4.51e-1) | + 1.5390e+27 (3.70e-1) | + 1.5167e+29 (2.29e-1) | + 1.5421e+29 (2.92e-1) | + 1.5444e+29 (1.11e-1) |
| | 10 | 1500 | 2.4545e+20 (4.44e-1) | 2.6287e+24 (6.62e-1) | + 2.7011e+29 (2.15e-1) | + 2.7033e+29 (2.12e-1) | + 2.6594e+29 (3.94e-1) | + 2.7093e+29 (2.14e-1) | + 2.7097e+29 (2.14e-1) | |
| WFG1-1 | 3 | 400 | 1.6628e+18 (5.51e-1) | 1.8172e+11 (4.91e-1) | + 1.7227e+12 (4.91e-1) | + 1.6764e+17 (5.96e-1) | + 1.7060e+14 (3.59e-1) | + 1.7055e+15 (3.22e-1) | + 1.7224e+13 (4.36e-1) | + 1.7025e+1 |

Table 9: Mean and standard deviations (in parenthesis) of the HV indicator obtained by MOEAs using the RVEA framework on MOPs with irregular PF shapes. The two best mean values per MOP are highlighted in grayscale, where the darker tone corresponds to the best one. The symbols “+”, “-”, and “=” are placed when the MOEA performs significantly better, significantly worse, or statistically equivalent to RVEA based on a one-tailed Wilcoxon test using a significance level of $\alpha = 0.05$. The % of satisfaction refers to the percentage of MOPs where the MOEA performs significantly better than RVEA. The superscripts are the obtained rank in the comparison.

| MOP | Obj. | Gen. | RVEA | RVEA* | RVEA-AdaRSE | RVEA-AdaGAE | RVEA-AdaMPT | RVEA-AdaCOU | RVEA-AdaPT | RVEA-AdaKRA |
|---------|------|------|----------------------------------|------------------------------------|------------------------------------|------------------------------------|------------------------------------|-------------------------------------|------------------------------------|------------------------------------|
| DTLZ5 | 3 | 400 | 5.2469e+0 ⁸ (5.26e-3) | 5.5074e+0 ⁸ (1.27e-3) = | 5.4937e+0 ⁸ (7.79e-3) + | 5.4858e+0 ⁸ (5.68e-3) + | 5.4867e+0 ⁸ (5.82e-3) + | 5.4947e+0 ⁸ (8.73e-3) + | 5.4878e+0 ⁸ (2.89e-2) + | 5.4947e+0 ⁸ (7.30e-3) + |
| | 5 | 600 | 3.1213e+0 ⁸ (1.17e-2) | 3.1162e+0 ⁸ (2.69e-2) | 3.1215e+0 ⁸ (1.58e-2) = | 3.1203e+0 ⁸ (1.86e-2) + | 3.1202e+0 ⁸ (1.57e-2) + | 3.1272e+0 ⁸ (9.10e-3) + | 3.1222e+0 ⁸ (1.73e-2) + | 3.1224e+0 ⁸ (1.74e-2) + |
| | 8 | 750 | 2.4797e+0 ⁸ (3.68e-2) | 2.4824e+0 ⁸ (4.55e-2) + | 2.4877e+0 ⁸ (2.86e-1) + | 2.4861e+0 ⁸ (2.99e-1) + | 2.4864e+0 ⁸ (2.59e-1) + | 2.4980e+0 ⁸ (1.36e-1) + | 2.4886e+0 ⁸ (2.25e-1) + | 2.4886e+0 ⁸ (2.33e-1) + |
| | 10 | 1000 | 9.9364e+0 ⁸ (7.06e-1) | 9.9467e+0 ⁸ (1.43e+0) | 9.9525e+0 ⁸ (1.13e+0) | 9.9529e+0 ⁸ (9.87e-1) + | 9.9551e+0 ⁸ (9.06e-1) + | 1.0006e+0 ⁹ (4.27e-1) + | 9.9566e+0 ⁸ (9.59e-1) + | 9.9585e+0 ⁸ (6.97e-1) + |
| DTLZ6 | 3 | 400 | 5.2647e+0 ⁸ (7.03e-2) | 5.5070e+0 ⁸ (1.23e-3) + | 5.5075e+0 ⁸ (8.64e-3) + | 5.5032e+0 ⁸ (9.30e-3) + | 5.5009e+0 ⁸ (1.89e-2) + | 5.5072e+0 ⁸ (6.90e-3) + | 5.5076e+0 ⁸ (7.51e-3) + | 5.5065e+0 ⁸ (1.29e-2) + |
| | 5 | 600 | 3.1913e+0 ⁸ (1.19e-2) | 3.1922e+0 ⁸ (2.58e-2) | 3.1917e+0 ⁸ (2.77e-3) + | 3.1919e+0 ⁸ (1.53e-3) + | 3.1918e+0 ⁸ (1.33e-3) + | 3.1925e+0 ⁸ (2.65e-2) + | 3.1919e+0 ⁸ (2.75e-3) + | 3.1929e+0 ⁸ (2.71e-3) + |
| | 8 | 750 | 2.5498e+0 ⁸ (7.08e-2) | 2.5528e+0 ⁸ (3.40e-2) + | 2.5527e+0 ⁸ (3.83e-2) + | 2.5525e+0 ⁸ (4.19e-2) + | 2.5525e+0 ⁸ (2.93e-2) + | 2.5534e+0 ⁸ (2.52e-2) + | 2.5528e+0 ⁸ (2.73e-2) + | 2.5528e+0 ⁸ (2.27e-2) + |
| | 10 | 1000 | 1.0198e+0 ⁸ (2.82e-1) | 1.0210e+0 ⁸ (1.24e-1) | 1.0209e+0 ⁸ (1.24e-1) + | 1.0209e+0 ⁸ (1.35e-1) + | 1.0209e+0 ⁸ (1.40e-1) + | 1.0214e+0 ⁸ (8.29e-2) + | 1.0210e+0 ⁸ (3.96e-2) + | 1.0210e+0 ⁸ (8.40e-2) + |
| DTLZ7 | 3 | 400 | 6.5137e+0 ⁷ (6.20e-3) | 6.4793e+0 ⁸ (2.80e-1) = | 6.5617e+0 ⁷ (8.95e-3) + | 6.5551e+0 ⁷ (1.19e-2) + | 6.5586e+0 ⁷ (1.14e-2) + | 6.5575e+0 ⁷ (1.13e-2) + | 6.5596e+0 ⁷ (1.15e-2) + | 6.5628e+0 ⁷ (1.21e-2) + |
| | 5 | 1000 | 2.3430e+0 ⁸ (1.64e-2) | 2.5043e+0 ⁸ (3.36e-2) | 2.4424e+0 ⁸ (9.76e-2) + | 2.4256e+0 ⁸ (7.36e-2) + | 2.4282e+0 ⁸ (8.36e-2) + | 2.4831e+0 ⁸ (7.01e-2) + | 2.4724e+0 ⁸ (8.27e-2) + | 2.4724e+0 ⁸ (5.89e-2) + |
| | 8 | 1000 | 1.5744e+0 ⁸ (2.95e-0) | 1.7863e+0 ⁸ (1.88e-0) | 1.7011e+0 ⁸ (4.33e-0) + | 1.6536e+0 ⁸ (3.30e-0) + | 1.7555e+0 ⁸ (2.90e-0) + | 1.7226e+0 ⁸ (3.13e-0) + | 1.7258e+0 ⁸ (3.02e-0) + | 1.7258e+0 ⁸ (2.92e-0) + |
| | 10 | 1500 | 5.8589e+0 ⁸ (1.35e-1) | 6.8911e+0 ⁸ (2.31e+0) | 6.5590e+0 ⁸ (1.12e+1) | 6.5436e+0 ⁸ (9.87e+0) | 6.5483e+0 ⁸ (9.78e+0) | 6.8857e+0 ⁸ (6.93e+0) | 6.4067e+0 ⁸ (1.87e+1) + | 6.3766e+0 ⁸ (1.61e+1) + |
| WFG2 | 3 | 400 | 7.8154e+0 ⁸ (3.74e-2) | 7.7950e+0 ⁸ (3.19e-2) | 7.8143e+0 ⁸ (3.22e-2) = | 7.8131e+0 ⁸ (2.07e-2) + | 7.8110e+0 ⁸ (2.85e-2) + | 7.8126e+0 ⁸ (3.60e-2) + | 7.8120e+0 ⁸ (3.78e-2) + | 7.8163e+0 ⁸ (2.85e-2) + |
| | 5 | 750 | 3.1815e+0 ⁸ (2.80e-2) | 3.1615e+0 ⁸ (4.76e-2) | 3.1849e+0 ⁸ (3.17e-2) + | 3.1861e+0 ⁸ (3.11e-2) + | 3.1857e+0 ⁸ (3.42e-2) + | 3.1865e+0 ⁸ (3.09e-2) + | 3.1849e+0 ⁸ (2.47e-2) + | 3.1855e+0 ⁸ (3.61e-2) + |
| | 8 | 1500 | 2.5434e+0 ⁸ (4.69e-1) | 2.5212e+0 ⁸ (8.30e-1) | 2.5411e+0 ⁸ (4.13e-1) + | 2.5433e+0 ⁸ (4.48e-1) + | 2.5422e+0 ⁸ (4.12e-1) + | 2.5412e+0 ⁸ (1.23e-0) + | 2.5447e+0 ⁸ (5.69e-1) + | 2.5447e+0 ⁸ (5.90e-1) + |
| | 10 | 2000 | 1.0193e+0 ⁸ (1.12e-0) | 1.0137e+0 ⁸ (2.58e-0) | 1.0200e+0 ⁸ (1.23e+0) | 1.0199e+0 ⁸ (9.59e-1) + | 1.0202e+0 ⁸ (1.19e+0) + | 1.0203e+0 ⁸ (3.13e+0) + | 1.0208e+0 ⁸ (1.21e+0) + | 1.0208e+0 ⁸ (1.25e+0) + |
| WFG3 | 3 | 400 | 6.9429e+0 ⁷ (2.44e-2) | 6.9547e+0 ⁷ (6.07e-2) | 6.9331e+0 ⁷ (2.93e-2) + | 6.9098e+0 ⁷ (2.98e-2) + | 6.9071e+0 ⁸ (3.27e-2) + | 6.9328e+0 ⁷ (2.58e-2) + | 6.9303e+0 ⁷ (3.20e-2) + | 6.9217e+0 ⁷ (3.93e-2) + |
| | 5 | 750 | 2.8631e+0 ⁸ (1.18e-1) | 2.7634e+0 ⁸ (1.67e-1) | 2.8260e+0 ⁸ (1.85e-1) + | 2.8086e+0 ⁸ (1.43e-1) + | 2.8100e+0 ⁸ (1.26e-1) + | 2.8473e+0 ⁸ (1.30e-1) + | 2.8435e+0 ⁸ (2.44e-1) + | 2.8417e+0 ⁸ (1.63e-1) + |
| | 8 | 1500 | 2.0104e+0 ⁸ (1.43e-0) | 2.0269e+0 ⁸ (1.01e-0) + | 1.9811e+0 ⁸ (3.76e-1) + | 1.9933e+0 ⁸ (1.21e-1) + | 1.9655e+0 ⁸ (1.09e-1) + | 2.2784e+0 ⁸ (2.70e-0) + | 2.1762e+0 ⁸ (5.12e-0) + | 2.1623e+0 ⁸ (4.92e-0) + |
| | 10 | 2000 | 7.8449e+0 ⁸ (5.57e-1) | 8.1663e+0 ⁸ (5.11e-1) | 7.5023e+0 ⁸ (5.26e-1) + | 7.4238e+0 ⁸ (4.79e-1) + | 7.6058e+0 ⁸ (5.07e-1) | 9.3406e+0 ⁸ (1.47e-1) + | 8.6653e+0 ⁸ (3.01e-1) + | 8.7151e+0 ⁸ (2.81e-1) + |
| DTLZ1-1 | 3 | 400 | 5.3421e+0 ⁸ (7.47e-0) | 5.4313e+0 ⁸ (2.18e-0) | 5.4763e+0 ⁸ (1.71e-2) + | 5.4761e+0 ⁸ (1.10e-2) + | 5.4759e+0 ⁸ (2.16e-2) + | 5.4811e+0 ⁸ (0.71e-3) + | 5.4838e+0 ⁸ (5.49e-3) + | 5.4821e+0 ⁸ (1.03e-2) + |
| | 5 | 600 | 7.1834e+0 ⁸ (2.24e-0) | 8.9752e+0 ⁸ (4.74e-2) | 1.0916e+0 ⁹ (5.27e-2) + | 1.0307e+0 ⁹ (1.36e-1) + | 1.0507e+0 ⁹ (7.33e-2) + | 1.1229e+0 ⁹ (4.80e-2) + | 1.1213e+0 ⁹ (1.66e-2) + | 1.1218e+0 ⁹ (9.84e-3) + |
| | 8 | 750 | 3.6154e+0 ⁸ (1.33e-0) | 1.5214e+0 ⁸ (6.65e-1) | 1.7242e+0 ⁸ (1.44e-0) + | 1.5747e+0 ⁸ (1.45e-0) + | 1.6140e+0 ⁸ (1.86e-0) + | 1.9373e+0 ⁸ (1.12e-0) + | 1.9448e+0 ⁸ (1.15e-0) + | 1.8747e+0 ⁸ (1.67e-0) + |
| | 10 | 1000 | 2.7397e+0 ⁸ (6.89e-1) | 2.1858e+0 ⁸ (8.22e-1) | 2.4340e+0 ⁸ (2.76e-0) + | 2.1590e+0 ⁸ (1.65e-0) + | 2.3206e+0 ⁸ (2.97e-0) + | 2.8243e+0 ⁸ (2.51e-0) + | 2.7662e+0 ⁸ (2.92e-0) + | 2.7837e+0 ⁸ (2.45e-0) + |
| DTLZ2-1 | 3 | 250 | 6.6223e+0 ⁸ (8.64e-3) | 6.6613e+0 ⁷ (2.13e-2) | 6.6881e+0 ⁷ (8.03e-3) + | 6.6691e+0 ⁷ (1.19e-2) + | 6.6777e+0 ⁷ (1.29e-2) + | 6.6753e+0 ⁷ (1.40e-2) + | 6.6910e+0 ⁷ (9.51e-3) + | 6.6686e+0 ⁷ (9.42e-3) + |
| | 5 | 350 | 4.1318e+0 ⁸ (2.89e-2) | 1.5750e+0 ⁸ (2.77e-1) | 1.7123e+0 ⁸ (1.76e-2) + | 1.6717e+0 ⁸ (1.13e-1) + | 1.6861e+0 ⁸ (1.19e-2) + | 1.7347e+0 ⁸ (6.60e-2) + | 1.7267e+0 ⁸ (4.72e-2) + | 1.7267e+0 ⁸ (5.38e-2) + |
| | 8 | 500 | 1.8325e+0 ⁸ (8.08e-2) | 3.5217e+0 ⁸ (1.40e-0) | 4.2700e+0 ⁸ (5.55e-1) + | 4.0378e+0 ⁸ (8.80e-1) + | 4.1265e+0 ⁸ (9.17e-1) + | 4.1444e+0 ⁸ (8.62e-1) + | 3.8990e+0 ⁸ (6.02e-1) + | 3.9018e+0 ⁸ (6.26e-1) + |
| | 10 | 750 | 2.4020e+0 ⁸ (1.04e+0) | 6.6312e+0 ⁸ (1.65e+0) | 7.6947e+0 ⁸ (1.25e+0) + | 7.4214e+0 ⁸ (1.65e+0) + | 7.5594e+0 ⁸ (1.42e+0) + | 8.6701e+0 ⁸ (0.90e-1) + | 6.4298e+0 ⁸ (1.12e+0) + | 6.4068e+0 ⁸ (1.35e+0) + |
| DTLZ3-1 | 3 | 1000 | 6.6345e+0 ⁸ (3.64e-3) | 6.6879e+0 ⁷ (4.66e-3) | 6.7050e+0 ⁷ (4.86e-3) + | 6.6973e+0 ⁷ (1.12e-2) + | 6.6956e+0 ⁸ (8.42e-3) + | 6.7030e+0 ⁷ (4.24e-3) + | 6.7022e+0 ⁷ (8.97e-3) + | 6.7015e+0 ⁷ (1.16e-2) + |
| | 5 | 1000 | 4.1311e+0 ⁸ (2.14e-2) | 1.5962e+0 ⁸ (1.79e-1) | 1.7294e+0 ⁸ (8.75e-2) + | 1.6696e+0 ⁸ (1.16e-1) + | 1.6884e+0 ⁸ (7.59e-2) + | 1.7481e+0 ⁸ (3.48e-2) + | 1.7406e+0 ⁸ (5.55e-2) + | 1.7425e+0 ⁸ (4.66e-2) + |
| | 8 | 1000 | 1.8021e+0 ⁸ (8.91e-1) | 3.3952e+0 ⁸ (1.31e+0) | 4.0409e+0 ⁸ (7.73e-1) + | 3.7239e+0 ⁸ (8.84e-1) + | 3.8692e+0 ⁸ (1.02e+0) + | 3.9170e+0 ⁸ (7.32e-1) + | 3.7118e+0 ⁸ (1.95e-1) + | 3.7323e+0 ⁸ (5.23e-1) + |
| | 10 | 1500 | 2.3849e+0 ⁸ (7.36e-1) | 6.4779e+0 ⁸ (2.70e+0) | 7.4078e+0 ⁸ (1.31e+0) + | 6.9160e+0 ⁸ (1.86e-1) + | 6.9160e+0 ⁸ (9.45e-1) + | 6.9052e+0 ⁸ (1.07e+0) + | 6.1140e+0 ⁸ (1.11e+0) + | 6.1140e+0 ⁸ (1.11e+0) + |
| DTLZ4-1 | 3 | 600 | 6.5403e+0 ⁷ (1.08e-3) | 6.7138e+0 ⁷ (1.07e-3) + | 6.7774e+0 ⁷ (0.86e-3) + | 6.7275e+0 ⁷ (2.12e-2) + | 6.7367e+0 ⁷ (0.29e-2) + | 6.7544e+0 ⁷ (1.01e-2) + | 6.7759e+0 ⁷ (0.67e-3) + | 6.7728e+0 ⁷ (0.75e-3) + |
| | 5 | 600 | 1.5476e+0 ⁸ (5.43e-2) | 1.6411e+0 ⁸ (2.12e-1) | 1.8401e+0 ⁸ (4.89e-2) + | 1.7666e+0 ⁸ (1.40e-1) + | 1.7879e+0 ⁸ (0.95e-2) + | 1.8724e+0 ⁸ (3.48e-2) + | 1.8738e+0 ⁸ (3.02e-2) + | 1.8745e+0 ⁸ (4.13e-2) + |
| | 8 | 750 | 2.2063e+0 ⁸ (3.19e-1) | 4.0749e+0 ⁸ (1.76e-0) | 5.1885e+0 ⁸ (1.11e-0) + | 4.5646e+0 ⁸ (1.52e-0) + | 4.5650e+0 ⁸ (1.07e-0) + | 4.30275e+0 ⁸ (5.64e-1) + | 4.2853e+0 ⁸ (6.18e-0) + | 4.2936e+0 ⁸ (6.02e-0) + |
| | 10 | 1000 | 3.0194e+0 ⁸ (1.37e-0) | 8.4602e+0 ⁸ (4.22e-0) | 1.0325e+0 ⁹ (3.66e-0) + | 5.1827e+0 ⁸ (3.06e-1) + | 5.3573e+0 ⁸ (1.20e-1) + | 7.4644e+0 ⁸ (1.87e-1) + | 8.4930e+0 ⁸ (8.44e-0) + | 5.1617e+0 ⁸ (7.26e-0) + |
| DTLZ5-1 | 3 | 400 | 6.6535e+0 ⁸ (2.85e-3) | 6.6870e+0 ⁷ (1.17e-2) | 6.7250e+0 ⁷ (3.33e-3) + | 6.7154e+0 ⁷ (4.30e-3) + | 6.7188e+0 ⁷ (3.40e-3) + | 6.7193e+0 ⁷ (3.09e-3) + | 6.7262e+0 ⁷ (2.07e-3) + | 6.7255e+0 ⁷ (3.29e-3) + |
| | 5 | 600 | 1.4468e+0 ⁸ (3.89e-2) | 1.5939e+0 ⁸ (1.04e+0) | 1.7701e+0 ⁸ (1.21e-0) + | 1.7506e+0 ⁸ (1.65e-0) + | 1.7519e+0 ⁸ (1.50e-0) + | 1.7715e+0 ⁸ (3.19e-2) + | 1.7700e+0 ⁸ (2.50e-2) + | 1.7692e+0 ⁸ (1.32e-2) + |
| | 8 | 750 | 3.1796e+0 ⁸ (4.80e-0) | 3.6376e+0 ⁸ (1.29e+0) | 4.5369e+0 ⁸ (3.70e-1) + | 4.4554e+0 ⁸ (1.53e-1) + | 4.5325e+0 ⁸ (4.74e-1) + | 4.3002e+0 ⁸ (1.35e-1) + | 4.1866e+0 ⁸ (3.34e-1) + | 4.1388e+0 ⁸ (2.67e-1) + |
| | 10 | 1000 | 7.204 | | | | | | | |

Table 10: Mean and standard deviations (in parenthesis) of the SPD indicator obtained by MOEAs using the RVEA framework on MOPs with irregular PF shapes. The two best mean values per MOP are highlighted in grayscale, where the darker tone corresponds to the best one. The symbols “+”, “-”, and “=” are placed when the MOEA performs significantly better, significantly worse, or statistically equivalent to RVEA based on a one-tailed Wilcoxon test using a significance level of $\alpha = 0.05$. The % of satisfaction refers to the percentage of MOPs where the MOEA performs significantly better than RVEA. The superscripts are the obtained rank in the comparison.

| MOP | Obj. | Gen. | RVEA | RVEA* | RVEA-AdaRSE | RVEA-AdaGAE | RVEA-AdaMPT | RVEA-AdaCOU | RVEA-AdaPT | RVEA-AdaKRA |
|---------|------|------|----------------------------------|----------------------------------|------------------------------------|------------------------------------|------------------------------------|------------------------------------|------------------------------------|------------------------------------|
| DTLZ5 | 3 | 400 | 9.9863e+0 ⁸ (1.68e+0) | 1.0430e+1 ⁷ (2.08e-2) | + 1.0579e+1 ² (1.67e-1) | + 1.0545e+1 ⁵ (9.04e-2) | + 1.0560e+1 ³ (7.83e-2) | + 1.0619e+1 ¹ (2.47e-1) | + 1.0453e+1 ⁶ (5.83e-1) | + 1.0549e+1 ⁴ (1.09e-1) |
| | 5 | 600 | 2.5690e+1 ³ (2.29e+0) | 9.4552e+0 ⁸ (1.57e+0) | + 2.3509e+1 ² (2.72e+0) | + 2.1817e+1 ⁷ (1.72e+0) | + 2.1886e+1 ⁶ (2.46e+0) | + 2.2010e+1 ⁹ (1.47e+0) | + 2.6021e+1 ² (2.48e+0) | + 2.6893e+1 ¹ (2.61e+0) |
| | 8 | 750 | 4.3742e+1 ³ (9.61e+0) | 1.0077e+1 ⁸ (3.37e+0) | + 4.4195e+1 ² (9.61e+0) | + 3.5497e+1 ⁶ (6.96e+0) | + 3.9333e+1 ⁵ (8.09e+0) | + 6.3301e+1 ⁹ (4.02e+0) | + 6.2517e+1 ² (1.11e+1) | + 6.4966e+1 ¹ (1.27e+1) |
| | 10 | 1000 | 6.4458e+1 ⁶ (1.56e+1) | 1.4688e+1 ⁸ (5.40e+0) | + 7.6640e+1 ² (1.75e+1) | + 6.2726e+1 ⁷ (1.36e+1) | + 7.1055e+1 ⁴ (1.23e+1) | + 6.6458e+1 ⁹ (6.69e+0) | + 1.3283e+2 ¹ (1.84e+1) | + 1.2952e+2 ² (1.90e+1) |
| DTLZ6 | 3 | 400 | 1.0028e+1 ⁸ (1.59e+0) | 1.0417e+1 ⁷ (1.85e-2) | = 1.0594e+1 ³ (2.20e-1) | = 1.0446e+1 ⁶ (8.90e-2) | = 1.0461e+1 ² (7.80e-2) | = 1.0576e+1 ¹ (2.36e-1) | = 1.0554e+1 ⁴ (1.54e-1) | = 1.0606e+1 ² (2.47e-1) |
| | 5 | 600 | 6.4356e+1 ³ (1.46e+0) | 1.0368e+1 ⁸ (1.31e+0) | + 1.6436e+1 ² (1.97e+0) | + 1.5359e+1 ⁶ (2.07e+0) | + 1.6150e+1 ⁹ (1.93e+0) | + 1.3031e+1 ¹ (6.12e-1) | + 1.7206e+1 ² (1.79e+0) | + 1.7344e+1 ¹ (1.91e+0) |
| | 8 | 750 | 2.2878e+1 ⁷ (4.29e+0) | 1.3919e+1 ⁸ (2.02e+0) | + 3.5321e+1 ² (4.01e+0) | + 3.1030e+1 ⁵ (3.68e+0) | + 3.2405e+1 ⁴ (2.84e+0) | + 2.6510e+1 ⁹ (2.11e+0) | + 4.2783e+1 ¹ (5.45e+0) | + 4.0760e+1 ² (4.64e+0) |
| | 10 | 1000 | 3.6744e+1 ⁷ (6.55e+0) | 2.4455e+1 ⁸ (3.63e+0) | + 5.8852e+1 ² (8.12e+0) | + 5.0638e+1 ⁵ (8.25e+0) | + 5.3421e+1 ⁴ (8.16e+0) | + 4.5753e+1 ⁹ (3.12e+0) | + 7.5856e+1 ¹ (1.14e+1) | + 7.3618e+1 ² (1.05e+1) |
| DTLZ7 | 3 | 400 | 1.0028e+1 ⁸ (1.59e+0) | 1.0417e+1 ⁷ (1.85e-2) | = 1.0594e+1 ³ (2.20e-1) | = 1.0446e+1 ⁶ (8.90e-2) | = 1.0461e+1 ² (7.80e-2) | = 1.0576e+1 ¹ (2.36e-1) | = 1.0554e+1 ⁴ (1.54e-1) | = 1.0606e+1 ² (2.47e-1) |
| | 5 | 600 | 1.4365e+1 ³ (1.46e+0) | 1.0368e+1 ⁸ (1.31e+0) | + 1.6436e+1 ² (1.97e+0) | + 1.5359e+1 ⁶ (2.07e+0) | + 1.6150e+1 ⁹ (1.93e+0) | + 1.3031e+1 ¹ (6.12e-1) | + 1.7206e+1 ² (1.79e+0) | + 1.7344e+1 ¹ (1.91e+0) |
| | 8 | 750 | 2.2878e+1 ⁷ (4.29e+0) | 1.3919e+1 ⁸ (2.02e+0) | + 3.5321e+1 ² (4.01e+0) | + 3.1030e+1 ⁵ (3.68e+0) | + 3.2405e+1 ⁴ (2.84e+0) | + 2.6510e+1 ⁹ (2.11e+0) | + 4.2783e+1 ¹ (5.45e+0) | + 4.0760e+1 ² (4.64e+0) |
| | 10 | 1000 | 3.6744e+1 ⁷ (6.55e+0) | 2.4455e+1 ⁸ (3.63e+0) | + 5.8852e+1 ² (8.12e+0) | + 5.0638e+1 ⁵ (8.25e+0) | + 5.3421e+1 ⁴ (8.16e+0) | + 4.5753e+1 ⁹ (3.12e+0) | + 7.5856e+1 ¹ (1.14e+1) | + 7.3618e+1 ² (1.05e+1) |
| WFG2 | 3 | 1000 | 2.3108e+1 ⁷ (3.53e-1) | 2.2052e+1 ⁸ (4.15e+0) | = 2.5959e+1 ² (3.28e-1) | = 2.5293e+1 ⁶ (3.38e-1) | = 2.5552e+1 ⁵ (3.25e-1) | = 2.5586e+1 ⁴ (4.66e-1) | = 2.5903e+1 ³ (3.59e-1) | = 2.5916e+1 ² (3.80e-1) |
| | 5 | 1000 | 6.8259e+1 ⁸ (2.64e+0) | 1.2519e+1 ⁷ (1.32e+0) | + 1.3802e+2 ² (2.50e+0) | + 1.3652e+2 ⁵ (2.63e+0) | + 1.3672e+1 ⁹ (2.97e+0) | + 1.3042e+2 ⁹ (2.50e+0) | + 1.3807e+2 ¹ (2.77e+0) | + 1.3710e+2 ¹ (2.71e+0) |
| | 8 | 1500 | 4.7925e+1 ⁷ (5.92e+0) | 1.5053e+2 ² (5.75e+0) | + 8.7357e+1 ⁷ (7.13e+0) | + 8.7705e+1 ⁶ (5.93e+0) | + 8.9278e+1 ⁵ (6.06e+0) | + 9.1355e+1 ² (2.48e+0) | + 8.9362e+1 ¹ (3.53e+0) | + 9.0977e+1 ³ (3.24e+0) |
| | 10 | 2000 | 7.0384e+1 ⁸ (1.12e+0) | 2.7214e+2 ² (1.88e+0) | + 1.4442e+2 ³ (6.64e+0) | + 1.4281e+2 ⁶ (9.55e+0) | + 1.4614e+2 ² (8.84e+0) | + 1.4086e+2 ⁹ (6.66e+0) | + 1.4382e+2 ¹ (1.00e+0) | + 1.4392e+2 ⁴ (7.80e+0) |
| WFG3 | 3 | 400 | 1.9657e+1 ⁷ (4.94e-1) | 1.7700e+1 ⁸ (4.76e-1) | - 1.9792e+1 ³ (3.71e-1) | - 1.9902e+1 ³ (4.54e-1) | - 1.9913e+1 ² (5.78e-1) | - 1.9931e+1 ¹ (5.78e-1) | - 1.9777e+1 ⁹ (5.52e-1) | - 1.9824e+1 ⁴ (4.16e-1) |
| | 5 | 750 | 3.0137e+1 ⁷ (9.19e-1) | 2.1123e+1 ⁸ (1.26e+0) | + 2.9343e+1 ⁷ (1.26e-0) | + 2.9858e+1 ² (1.21e-0) | + 2.9702e+1 ⁹ (1.33e-0) | + 2.9602e+1 ⁹ (1.15e-0) | + 2.9913e+1 ³ (1.12e-0) | + 3.0159e+1 ² (9.84e-1) |
| | 8 | 1500 | 2.0408e+1 ⁸ (1.38e+0) | 1.1152e+1 ⁸ (1.13e+0) | + 2.0073e+1 ⁵ (1.42e+0) | + 2.0407e+1 ⁵ (1.46e-0) | + 1.9974e+1 ⁷ (1.62e+0) | + 2.0408e+1 ⁹ (1.20e+0) | + 2.1276e+1 ² (1.73e+0) | + 2.1593e+1 ¹ (1.85e+0) |
| | 10 | 2000 | 2.0636e+1 ⁸ (1.50e+0) | 9.8858e+1 ⁸ (1.06e+0) | + 2.2293e+1 ⁶ (1.94e+0) | + 2.2836e+1 ⁶ (1.65e+0) | + 2.2995e+1 ⁴ (1.81e+0) | + 2.3628e+1 ⁹ (1.98e+0) | + 2.4639e+1 ¹ (2.38e+0) | + 2.4636e+1 ² (1.89e+0) |
| DTLZ1 | 3 | 400 | 1.1568e+1 ⁷ (4.68e-1) | 1.0258e+1 ⁸ (3.67e-1) | - 1.1900e+1 ⁵ (4.02e-1) | - 1.1989e+1 ⁴ (5.06e-1) | - 1.2029e+1 ² (5.74e-1) | - 1.1632e+1 ⁹ (5.29e-1) | - 1.2004e+1 ³ (5.08e-1) | - 1.2117e+1 ¹ (5.77e-1) |
| | 5 | 750 | 2.6363e+1 ⁷ (1.05e+0) | 2.0317e+1 ⁸ (1.22e+0) | + 4.1319e+1 ⁷ (1.10e+0) | + 3.6094e+1 ² (1.06e+0) | + 3.1519e+1 ⁹ (1.04e+0) | + 4.1777e+1 ⁷ (8.84e-1) | + 4.6944e+1 ¹ (1.04e+0) | + 4.6929e+1 ² (7.99e-1) |
| | 8 | 1500 | 7.3123e+1 ⁷ (5.02e+0) | 4.9923e+1 ⁸ (4.23e+0) | + 7.2323e+1 ⁵ (2.77e+0) | + 6.4093e+1 ⁷ (3.95e+0) | + 6.7373e+1 ⁶ (3.89e+0) | + 7.3207e+1 ⁹ (1.49e-0) | + 7.6326e+1 ¹ (1.21e+0) | + 7.6065e+1 ² (1.11e+0) |
| | 10 | 2000 | 1.2129e+2 ² (7.77e+0) | 9.9133e+1 ⁸ (8.38e+0) | + 1.1649e+2 ⁵ (5.95e+0) | + 1.0597e+2 ⁷ (9.59e+0) | + 1.0989e+2 ⁶ (8.48e+0) | + 1.1721e+2 ⁴ (2.10e+0) | + 1.2001e+2 ² (1.74e+0) | + 1.1985e+2 ⁴ (1.81e+0) |
| DTLZ1-1 | 3 | 400 | 1.8496e+1 ⁷ (4.95e-1) | 2.1969e+1 ⁷ (1.91e-1) | - 1.9792e+1 ³ (3.71e-1) | - 1.9902e+1 ³ (4.54e-1) | - 1.9913e+1 ² (5.78e-1) | - 1.9931e+1 ¹ (5.78e-1) | - 1.9777e+1 ⁹ (5.52e-1) | - 1.9824e+1 ⁴ (4.16e-1) |
| | 5 | 600 | 2.4558e+1 ⁸ (1.45e+0) | 4.4742e+1 ⁷ (3.56e+0) | + 6.8803e+1 ² (6.72e-1) | + 6.0527e+1 ⁶ (1.49e-0) | + 6.3253e+1 ⁹ (7.89e-1) | + 7.0950e+1 ⁹ (4.00e-0) | + 7.1941e+1 ² (3.98e-1) | + 7.1337e+1 ¹ (3.20e-1) |
| | 8 | 750 | 3.3299e+1 ⁸ (3.16e+0) | 6.7949e+1 ⁷ (4.72e+0) | + 8.0385e+1 ² (1.18e+0) | + 7.0310e+1 ⁶ (1.21e+0) | + 7.1855e+1 ⁵ (1.44e-0) | + 8.7010e+1 ⁹ (8.08e+0) | + 8.7209e+1 ¹ (7.35e+0) | + 8.2096e+1 ² (1.22e+1) |
| | 10 | 1000 | 3.3956e+1 ⁸ (1.09e+0) | 9.8027e+1 ⁸ (6.63e+0) | + 1.2000e+2 ⁴ (2.61e+1) | + 9.6639e+1 ² (2.45e+0) | + 1.1120e+2 ⁶ (2.92e+0) | + 1.3837e+2 ² (2.05e+1) | + 1.3332e+2 ⁴ (2.34e+1) | + 1.3459e+2 ² (2.03e+1) |
| DTLZ2-1 | 3 | 250 | 2.7581e+1 ⁸ (1.47e-1) | 2.8527e+1 ⁷ (9.61e-1) | - 3.2031e+1 ² (1.82e-1) | - 3.1340e+1 ⁶ (4.80e-1) | - 3.1764e+1 ⁴ (4.34e-1) | - 3.1596e+1 ⁹ (3.66e-1) | - 3.2046e+1 ⁶ (2.75e-1) | - 3.2003e+1 ³ (3.11e-1) |
| | 5 | 350 | 4.3039e+1 ⁸ (2.83e-1) | 7.3369e+1 ⁷ (5.03e+0) | + 1.2302e+2 ² (3.03e+0) | + 1.0628e+2 ⁶ (4.64e+0) | + 1.1222e+2 ⁵ (3.71e+0) | + 1.0795e+2 ⁹ (4.00e-0) | + 1.1912e+2 ² (1.37e+0) | + 1.1921e+2 ¹ (2.37e+0) |
| | 8 | 500 | 3.1638e+1 ⁸ (2.40e+0) | 6.1817e+1 ⁷ (6.36e+0) | + 1.1431e+2 ⁴ (1.60e+0) | + 1.0140e+2 ⁶ (3.05e+0) | + 1.0603e+2 ⁶ (2.88e+0) | + 1.1805e+2 ⁹ (1.06e+0) | + 1.1517e+2 ² (1.34e+0) | + 1.1515e+2 ⁴ (1.34e+0) |
| | 10 | 750 | 4.0778e+1 ⁸ (1.09e+0) | 9.0955e+1 ⁷ (9.15e+0) | + 2.0356e+2 ⁴ (3.57e+0) | + 1.7952e+2 ⁶ (4.23e+0) | + 1.8934e+2 ⁹ (3.22e+0) | + 2.1551e+2 ¹ (1.34e+0) | + 2.0877e+2 ² (2.31e+0) | + 2.0912e+2 ⁴ (2.12e+0) |
| DTLZ3-1 | 3 | 1000 | 2.7663e+1 ⁸ (9.36e-2) | 3.0080e+1 ⁷ (4.12e-1) | - 3.2404e+1 ² (1.92e-1) | - 3.2128e+1 ⁶ (1.63e-1) | - 3.2160e+1 ⁵ (2.07e-1) | - 3.2148e+1 ⁹ (1.52e-1) | - 3.2399e+1 ² (2.13e-1) | - 3.2363e+1 ³ (2.01e-1) |
| | 5 | 1000 | 4.3127e+1 ⁸ (1.66e-1) | 7.8883e+1 ⁷ (5.36e+0) | + 1.2942e+2 ² (3.56e+0) | + 1.1726e+2 ⁶ (2.51e+0) | + 1.2128e+2 ⁵ (1.70e+0) | + 1.3250e+2 ⁹ (9.37e-1) | + 1.2375e+2 ¹ (1.38e-1) | + 1.2400e+2 ² (1.27e+0) |
| | 8 | 1500 | 3.1532e+1 ⁸ (2.58e+0) | 5.6711e+1 ⁷ (6.97e+0) | + 1.1813e+2 ² (1.66e+0) | + 1.0382e+2 ⁶ (2.57e+0) | + 1.0912e+2 ⁵ (3.03e+0) | + 1.2185e+2 ⁹ (1.46e-1) | + 1.1937e+2 ¹ (9.33e-1) | + 1.1937e+2 ² (1.21e-1) |
| | 10 | 2000 | 4.0493e+1 ⁸ (7.58e-1) | 1.0525e+2 ² (2.12e+0) | + 2.1267e+2 ⁴ (1.91e+0) | + 1.8517e+2 ⁶ (2.78e+0) | + 1.9587e+2 ⁹ (2.17e+0) | + 2.1987e+2 ¹ (1.07e+0) | + 2.1539e+2 ² (1.09e+0) | + 2.1539e+2 ⁴ (1.09e+0) |
| DTLZ4-1 | 3 | 600 | 2.7026e+1 ⁸ (3.62e+0) | 3.0202e+1 ⁷ (2.75e-1) | - 3.1773e+1 ² (4.40e+0) | - 3.2317e+1 ² (4.21e+0) | - 3.1643e+1 ⁴ (4.21e+0) | - 3.1512e+1 ⁵ (4.32e+0) | - 3.0994e+1 ⁶ (6.08e+0) | - 3.2587e+1 ¹ (1.21e-1) |
| | 5 | 1000 | 4.3371e+1 ⁷ (1.14e+0) | 7.8744e+1 ⁷ (2.62e+0) | + 1.2645e+2 ² (3.04e+0) | + 1.0136e+2 ⁶ (4.26e+0) | + 1.2030e+2 ⁵ (1.61e+0) | + 1.3392e+2 ⁹ (8.07e+0) | + 1.2616e+2 ¹ (2.06e+0) | + 1.2497e+2 ² (8.46e+0) |
| | 8 | 1250 | 2.7482e+1 ⁸ (5.32e+0) | 1.0811e+2 ² (1.21e+0) | + 1.2408e+2 ² (6.94e+0) | + 1.2150e+2 ⁶ (7.72e+0) | + 1.2146e+2 ⁵ (6.45e+0) | + 1.2151e+2 ⁹ (1.20e+0) | + 1.1926e+2 ¹ (2.02e+0) | + 1.1984e+2 ² (7.46e+0) |
| | 10 | 2000 | 3.8324e+1 ⁸ (1.70e+0) | 1.8774e+2 ² (9.19e+0) | + 2.2101e+2 ⁴ (6.40e+0) | + 2.1517e+2 ⁶ (9.50e+0) | + 2.2001e+2 ⁹ (7.71e+0) | + 2.1920e+2 ¹ (8.93e+0) | + 2.1477e+2 ² (9.74e+0) | + 2.0702e+2 ⁴ (1.78e+0) |

Table 11: Mean and standard deviations (in parenthesis) of the HV indicator obtained by MOEAs using the MOEA/D framework on MOPs with irregular PF shapes. The two best mean values per MOP are highlighted in grayscale, where the darker tone corresponds to the best one. The symbols “+”, “-”, and “=” are placed when the MOEA performs significantly better, significantly worse, or statistically equivalent to MOEA/D based on a one-tailed Wilcoxon test using a significance level of $\alpha = 0.05$. The % of satisfaction refers to the percentage of MOPs where the MOEA performs significantly better than MOEA/D. The superscripts are the obtained rank in the comparison.

| MOP | Obj. | Gen. | MOEA/D | AdaW | MOEA/D-AdaRSE | MOEA/D-AdaGAE | MOEA/D-AdaMPT | MOEA/D-AdaCOU | MOEA/D-AdaPT | MOEA/D-AdaKRA |
|-------|------|------|----------------------------------|------------------------------------|------------------------------------|------------------------------------|------------------------------------|------------------------------------|------------------------------------|------------------------------------|
| DTLZ5 | 3 | 400 | 5.4617e+0 ⁸ (5.13e-3) | 5.5063e+0 ⁸ (6.92e-3) + | 5.5045e+0 ⁵ (1.74e-3) + | 5.4978e+0 ⁷ (1.43e-3) + | 5.5004e+0 ⁶ (2.09e-3) + | 5.5046e+0 ¹ (1.82e-3) + | 5.5047e+0 ² (2.14e-3) + | 5.5053e+0 ² (1.84e-3) + |
| | 5 | 600 | 3.1082e+0 ⁸ (9.07e-3) | 3.1277e+0 ⁸ (1.16e-2) + | 3.1296e+0 ⁵ (1.08e-2) + | 3.1298e+0 ⁴ (8.48e-3) + | 3.1310e+0 ¹ (6.87e-3) + | 3.1302e+0 ² (5.59e-3) + | 3.1302e+0 ¹ (7.73e-3) + | 3.1302e+0 ² (1.06e-1) + |
| | 8 | 750 | 2.4715e+0 ⁸ (7.74e-4) | 2.4921e+0 ⁸ (1.61e+0) + | 2.5016e+0 ⁴ (1.61e-1) + | 2.5006e+0 ⁶ (1.87e-1) + | 2.5009e+0 ² (2.38e-1) + | 2.5038e+0 ² (6.94e-1) + | 2.5017e+0 ² (1.06e-1) + | 2.5018e+0 ² (1.37e-1) + |
| | 10 | 1000 | 9.8787e+0 ⁷ (3.98e+0) | 9.8522e+0 ⁸ (3.75e+1) + | 1.0014e+0 ³ (4.11e-1) + | 1.0013e+0 ⁵ (4.89e-1) + | 1.0012e+0 ³ (4.36e-1) + | 1.0024e+0 ³ (2.06e-1) + | 1.0014e+0 ³ (3.47e-1) + | 1.0015e+0 ³ (3.42e-1) + |
| DTLZ6 | 3 | 400 | 5.4612e+0 ⁸ (4.50e-5) | 5.5053e+0 ⁸ (4.08e-3) + | 5.5053e+0 ² (1.65e-4) + | 5.4960e+0 ⁷ (9.18e-4) + | 5.4994e+0 ⁶ (4.65e-4) + | 5.5052e+0 ² (2.68e-4) + | 5.5054e+0 ² (1.68e-4) + | 5.5053e+0 ² (2.94e-4) + |
| | 5 | 600 | 3.1897e+0 ⁸ (2.01e-0) | 3.1915e+0 ⁸ (4.55e-2) + | 3.1922e+0 ⁵ (2.52e-3) + | 3.1921e+0 ⁶ (2.53e-3) + | 3.1922e+0 ⁵ (3.26e-3) + | 3.1925e+0 ¹ (2.21e-1) + | 3.1923e+0 ² (2.36e-3) + | 3.1923e+0 ² (2.44e-3) + |
| | 8 | 750 | 2.5480e+0 ⁸ (8.29e-2) | 2.5520e+0 ⁸ (2.65e-1) + | 2.5553e+0 ² (1.92e-2) + | 2.5536e+0 ² (1.91e-2) + | 2.5535e+0 ² (2.48e-2) + | 2.5538e+0 ² (1.29e-2) + | 2.5533e+0 ² (1.82e-2) + | 2.5533e+0 ² (2.19e-2) + |
| | 10 | 1000 | 1.0189e+0 ⁸ (3.96e-1) | 1.0211e+0 ⁸ (6.92e-2) + | 1.0214e+0 ² (6.81e-2) + | 1.0214e+0 ³ (5.69e-2) + | 1.0213e+0 ³ (2.96e-1) + | 1.0215e+0 ³ (2.96e-2) + | 1.0213e+0 ³ (7.70e-2) + | 1.0213e+0 ³ (8.64e-2) + |
| DTLZ7 | 3 | 400 | 5.4612e+0 ⁸ (4.50e-5) | 5.5053e+0 ⁸ (4.08e-3) + | 5.5053e+0 ² (1.65e-4) + | 5.4960e+0 ⁷ (9.18e-4) + | 5.4994e+0 ⁶ (4.65e-4) + | 5.5052e+0 ² (2.68e-4) + | 5.5054e+0 ² (1.68e-4) + | 5.5053e+0 ² (2.94e-4) + |
| | 5 | 600 | 3.1897e+0 ⁸ (2.01e-0) | 3.1915e+0 ⁸ (4.55e-2) + | 3.1922e+0 ⁵ (2.52e-3) + | 3.1921e+0 ⁶ (2.53e-3) + | 3.1922e+0 ⁵ (3.26e-3) + | 3.1925e+0 ¹ (2.21e-1) + | 3.1923e+0 ² (2.36e-3) + | 3.1923e+0 ² (2.44e-3) + |
| | 8 | 750 | 2.5480e+0 ⁸ (8.29e-2) | 2.5520e+0 ⁸ (2.65e-1) + | 2.5553e+0 ² (1.92e-2) + | 2.5536e+0 ² (1.91e-2) + | 2.5535e+0 ² (2.48e-2) + | 2.5538e+0 ² (1.29e-2) + | 2.5533e+0 ² (1.82e-2) + | 2.5533e+0 ² (2.19e-2) + |
| | 10 | 1000 | 1.0189e+0 ⁸ (3.96e-1) | 1.0211e+0 ⁸ (6.92e-2) + | 1.0214e+0 ² (6.81e-2) + | 1.0214e+0 ³ (5.69e-2) + | 1.0213e+0 ³ (2.96e-1) + | 1.0215e+0 ³ (2.96e-2) + | 1.0213e+0 ³ (7.70e-2) + | 1.0213e+0 ³ (8.64e-2) + |
| WFG2 | 3 | 1000 | 6.5741e+0 ⁸ (2.71e-3) | 6.5872e+0 ⁷ (5.84e-3) + | 6.6044e+0 ¹ (3.44e-3) + | 6.5945e+0 ⁶ (5.36e-3) + | 6.5895e+0 ² (3.27e-3) + | 6.5979e+0 ² (3.12e-3) + | 6.6026e+0 ² (3.64e-3) + | 6.6033e+0 ² (3.60e-3) + |
| | 5 | 1000 | 2.4212e+0 ⁸ (3.09e-1) | 2.5295e+0 ⁸ (2.34e-1) + | 2.5235e+0 ¹ (3.72e-1) + | 2.5046e+0 ⁶ (3.67e-1) + | 2.4985e+0 ² (3.92e-1) + | 2.5263e+0 ¹ (3.79e-1) + | 2.5408e+0 ¹ (3.24e-1) + | 2.5314e+0 ¹ (5.82e-1) + |
| | 8 | 1500 | 1.6326e+0 ⁸ (3.01e-1) | 1.8750e+0 ⁸ (2.13e-0) + | 1.8424e+0 ² (9.57e-1) + | 1.8106e+0 ² (2.10e-0) + | 1.8261e+0 ² (1.00e+0) + | 1.8173e+0 ² (2.75e-0) + | 1.8242e+0 ² (1.03e+0) + | 1.8281e+0 ² (6.05e-1) + |
| | 10 | 2000 | 6.2176e+0 ⁸ (2.35e+0) | 7.2826e+0 ² (4.30e+0) + | 6.9682e+0 ² (9.52e-1) + | 6.9851e+0 ² (1.82e+0) + | 6.9774e+0 ² (1.74e+0) + | 7.1055e+0 ² (1.36e+0) + | 6.8022e+0 ² (6.32e+0) + | 6.7905e+0 ² (4.18e+0) + |
| WFG3 | 3 | 400 | 7.8822e+0 ⁸ (1.17e-0) | 7.8686e+0 ⁸ (1.62e-2) + | 7.8810e+0 ² (1.87e-2) + | 7.8509e+0 ⁷ (1.39e-1) + | 7.8577e+0 ² (1.35e-2) + | 7.8769e+0 ² (1.80e-2) + | 7.8856e+0 ² (6.13e-3) + | 7.8776e+0 ² (1.77e-2) + |
| | 5 | 750 | 3.1938e+0 ⁸ (1.80e-2) | 3.1900e+0 ⁸ (2.06e-2) + | 3.1944e+0 ² (1.62e-2) + | 3.1946e+0 ¹ (1.55e-2) + | 3.1940e+0 ⁵ (1.62e-2) + | 3.1934e+0 ¹ (1.10e-2) + | 3.1941e+0 ⁵ (1.31e-2) + | 3.1945e+0 ² (1.31e-2) + |
| | 8 | 1500 | 2.5563e+0 ⁸ (1.35e-0) | 2.5563e+0 ⁸ (2.98e-2) + | 2.5562e+0 ² (1.01e-1) + | 2.5565e+0 ² (2.18e-1) + | 2.5564e+0 ² (2.18e-1) + | 2.5562e+0 ² (1.20e-1) + | 2.5562e+0 ² (1.19e-1) + | 2.5562e+0 ² (1.53e-1) + |
| | 10 | 2000 | 1.0230e+0 ⁸ (3.81e-1) | 1.0232e+0 ⁸ (3.14e-0) + | 1.0232e+0 ² (3.19e-1) + | 1.0232e+0 ³ (2.99e-1) + | 1.0232e+0 ³ (3.01e-1) + | 1.0231e+0 ³ (3.67e-1) + | 1.0231e+0 ³ (3.29e-1) + | 1.0231e+0 ³ (2.92e-1) + |
| DTLZ1 | 3 | 400 | 7.0879e+0 ⁸ (1.25e-2) | 6.9990e+0 ⁸ (4.99e-2) + | 7.0631e+0 ² (2.37e-2) + | 7.0480e+0 ⁷ (2.11e-2) + | 7.0503e+0 ² (1.81e-2) + | 7.0616e+0 ² (1.95e-2) + | 7.0608e+0 ² (1.96e-2) + | 7.0625e+0 ² (1.87e-2) + |
| | 5 | 750 | 2.8695e+0 ⁸ (1.37e-0) | 2.8266e+0 ⁸ (1.34e-2) + | 2.9028e+0 ² (1.17e-1) + | 2.8917e+0 ² (1.21e-2) + | 2.8812e+0 ² (1.19e-1) + | 2.9268e+0 ¹ (1.10e-1) + | 2.9126e+0 ¹ (1.15e-1) + | 2.9182e+0 ² (9.61e-2) + |
| | 8 | 1500 | 2.2842e+0 ⁸ (1.79e-0) | 2.2093e+0 ⁸ (3.41e+0) + | 2.2299e+0 ² (2.42e+0) + | 2.2132e+0 ² (3.16e+0) + | 2.2305e+0 ² (3.17e+0) + | 2.3469e+0 ² (1.12e+0) + | 2.2897e+0 ² (2.61e+0) + | 2.2837e+0 ² (2.45e+0) + |
| | 10 | 2000 | 9.1294e+0 ⁸ (5.57e+0) | 9.0405e+0 ² (1.25e+1) + | 8.9662e+0 ² (1.32e+1) + | 8.9756e+0 ² (1.28e+1) + | 8.9824e+0 ² (0.95e+0) + | 9.4971e+0 ² (4.99e+0) + | 9.3078e+0 ² (8.84e+0) + | 9.2454e+0 ² (8.01e+0) + |
| DTLZ2 | 3 | 400 | 5.4412e+0 ⁸ (0.68e-6) | 5.4612e+0 ⁸ (4.08e-3) + | 5.4989e+0 ² (4.80e-3) + | 5.4927e+0 ⁶ (4.03e-3) + | 5.4954e+0 ² (2.69e-3) + | 5.4977e+0 ² (2.64e-3) + | 5.5004e+0 ² (2.76e-3) + | 5.5010e+0 ² (3.48e-3) + |
| | 5 | 600 | 3.8839e+0 ⁸ (8.61e-6) | 3.8839e+0 ⁸ (4.91e-2) + | 3.1086e+0 ² (4.91e-2) + | 3.1086e+0 ² (2.70e-2) + | 3.1071e+0 ² (1.74e-2) + | 3.1082e+0 ² (5.59e-2) + | 3.1285e+0 ² (1.76e-2) + | 3.1294e+0 ² (1.71e-2) + |
| | 8 | 750 | 2.6961e+0 ⁸ (5.21e-1) | 2.6916e+0 ⁸ (2.02e-1) + | 2.0438e+0 ² (1.43e-1) + | 1.9336e+0 ² (2.50e-1) + | 2.0011e+0 ² (1.70e-1) + | 2.0731e+0 ² (1.52e-2) + | 2.0712e+0 ² (4.75e-2) + | 2.0711e+0 ² (5.99e-2) + |
| | 10 | 1000 | 6.8175e+0 ⁸ (4.76e-1) | 6.8175e+0 ⁸ (3.30e-1) + | 2.9997e+0 ² (1.45e-1) + | 2.8311e+0 ² (2.26e-1) + | 2.9963e+0 ² (1.73e-1) + | 2.9952e+0 ² (6.25e-2) + | 2.9931e+0 ² (1.91e-1) + | 2.9931e+0 ² (5.77e-1) + |
| DTLZ3 | 3 | 250 | 6.6097e+0 ⁸ (3.15e-3) | 6.7062e+0 ⁸ (4.58e-3) + | 6.6984e+0 ⁴ (3.37e-3) + | 6.6940e+0 ⁶ (3.67e-3) + | 6.6952e+0 ² (3.82e-3) + | 6.6887e+0 ⁷ (5.33e-3) + | 6.6988e+0 ² (2.27e-3) + | 6.6986e+0 ³ (3.20e-3) + |
| | 5 | 350 | 1.3713e+0 ⁸ (1.25e-5) | 1.3776e+0 ⁸ (2.47e-2) + | 1.7764e+0 ² (1.24e-2) + | 1.7754e+0 ² (3.23e-2) + | 1.7750e+0 ² (3.34e-2) + | 1.7752e+0 ¹ (2.60e-2) + | 1.7741e+0 ¹ (1.75e-2) + | 1.7748e+0 ¹ (2.43e-2) + |
| | 8 | 500 | 2.1848e+0 ⁸ (1.56e-1) | 2.1848e+0 ⁸ (2.96e-1) + | 4.4642e+0 ² (1.96e-1) + | 4.5304e+0 ² (1.42e-1) + | 4.5285e+0 ² (3.06e-1) + | 4.2317e+0 ² (1.98e-1) + | 4.1537e+0 ² (1.05e-1) + | 4.1568e+0 ² (1.39e-1) + |
| | 10 | 750 | 3.1434e+0 ⁸ (1.29e-0) | 3.1434e+0 ⁸ (1.56e-1) + | 8.5683e+0 ² (1.59e-1) + | 8.5207e+0 ² (1.70e-1) + | 8.4831e+0 ² (4.27e-1) + | 7.2512e+0 ² (1.95e-1) + | 7.0312e+0 ² (7.56e-1) + | 7.0474e+0 ² (5.12e-1) + |
| DTLZ4 | 3 | 250 | 6.6096e+0 ⁸ (5.98e-3) | 6.7095e+0 ⁸ (3.54e-3) + | 6.6996e+0 ² (2.29e-3) + | 6.6991e+0 ³ (2.62e-3) + | 6.6951e+0 ² (3.74e-3) + | 6.6951e+0 ² (2.55e-3) + | 6.6988e+0 ² (2.27e-3) + | 6.6983e+0 ² (3.20e-3) + |
| | 5 | 500 | 1.5624e+0 ⁸ (1.90e-2) | 1.8829e+0 ⁸ (6.73e-2) + | 1.8859e+0 ² (2.65e-2) + | 1.8719e+0 ² (1.47e-2) + | 1.8751e+0 ² (3.62e-2) + | 1.8964e+0 ² (1.07e-2) + | 1.8966e+0 ² (1.79e-2) + | 1.8965e+0 ² (1.79e-2) + |
| | 8 | 750 | 2.6076e+0 ⁸ (8.34e-1) | 2.7156e+0 ⁸ (1.36e-1) + | 5.4975e+0 ² (6.63e-1) + | 5.4975e+0 ² (6.93e-1) + | 5.4975e+0 ² (3.10e-1) + | 5.7174e+0 ² (1.79e-1) + | 5.5944e+0 ² (1.22e-1) + | 5.5874e+0 ² (2.60e-1) + |
| | 10 | 1000 | 3.7079e+0 ⁸ (2.64e-1) | 3.7079e+0 ⁸ (2.64e-1) + | 1.4316e+0 ² (1.90e-1) + | 1.4296e+0 ² (2.60e-1) + | 1.4146e+0 ² (1.60e-1) + | 1.4148e+0 ² (6.06e-1) + | 1.0945e+0 ² (2.79e-1) + | 1.0929e+0 ² (1.79e-1) + |
| DTLZ5 | 3 | 400 | 7.2246e+0 ⁸ (3.11e-4) | 7.2444e+0 ⁸ (5.76e-3) + | 7.2500e+0 ² (7.88e-3) + | 7.2488e+0 ⁵ (9.12e-4) + | 7.2498e+0 ² (2.88e-4) + | 7.2486e+0 ² (5.02e-3) + | 7.2801e+0 ² (3.08e-3) + | 6.7785e+0 ² (3.37e-3) + |
| | 5 | 750 | 2.7217e+0 ⁸ (1.12e-1) | 2.8524e+0 ⁸ (7.46e-2) + | 2.8271e+0 ² (7.09e-1) + | 2.8413e+0 ² (6.48e-2) + | 2.8427e+0 ² (1.21e-1) + | 2.8497e+0 ² (1.64e-2) + | 2.8586e+0 ² (1.37e-2) + | 2.8586e+0 ² (2.53e-2) + |
| | 8 | 1000 | 2.1842e+0 ⁸ (2.11e+0) | 2.1842e+0 ⁸ (2.11e+0) + | 2.1700e+0 ² (1.86e-1) + | 2.0964e+0 ² (2.14e-1) + | 2.1608e+0 ² (1.20e+0) + | 2.1720e+0 ² (1.14e+0) + | 2.1592e+0 ² (2.14e+0 | |

Table 12: Mean and standard deviations (in parenthesis) of the SPD indicator obtained by MOEAs using the MOEA/D framework on MOPs with irregular PF shapes. The two best mean values per MOP are highlighted in grayscale, where the darker tone corresponds to the best one. The symbols “+”, “-”, and “=” are placed when the MOEA performs significantly better, significantly worse, or statistically equivalent to MOEA/D based on a one-tailed Wilcoxon test using a significance level of $\alpha = 0.05$. The % of satisfaction refers to the percentage of MOPs where the MOEA performs significantly better than MOEA/D. The superscripts are the obtained rank in the comparison.

| MOP | Obj. | Gen. | MOEA/D | AdaW | MOEA/D-AdaRSE | MOEA/D-AdaGAE | MOEA/D-AdaMPT | MOEA/D-AdaCOU | MOEA/D-AdaPT | MOEA/D-AdaKRA |
|-------|------|------|----------------------|------------------------|------------------------|------------------------|------------------------|------------------------|------------------------|------------------------|
| DTLZ5 | 3 | 400 | 9.5807e+08 (2.44e-3) | 1.0475e+11 (1.73e-2) | 1.0441e+14 (8.88e-3) + | 1.0363e+17 (2.12e-2) + | 1.0391e+16 (1.89e-2) + | 1.0443e+12 (8.95e-3) + | 1.0404e+15 (8.30e-3) + | 1.0443e+13 (8.42e-3) + |
| | 5 | 600 | 8.2579e+08 (9.33e-2) | 2.1431e+11 (1.63e+0) | 1.7421e+14 (2.46e-0) + | 1.5919e+17 (2.04e+0) + | 1.7348e+15 (1.96e+0) + | 1.6918e+19 (2.53e+0) + | 1.9041e+13 (3.25e+0) + | 1.9787e+12 (3.27e+0) + |
| | 8 | 750 | 1.0713e+18 (1.13e+0) | 4.4308e+11 (3.67e+0) + | 1.9340e+15 (3.18e+0) + | 1.7078e+17 (2.91e+0) + | 1.7232e+16 (2.87e+0) + | 2.3886e+14 (3.11e+0) + | 2.8686e+12 (5.38e+0) + | 2.6729e+12 (6.09e+0) + |
| | 10 | 1000 | 1.1711e+18 (1.75e+0) | 6.8096e+11 (9.41e+0) + | 2.4657e+15 (3.57e+0) + | 2.2109e+17 (3.71e+0) + | 2.3311e+16 (2.84e+0) + | 3.2873e+14 (1.96e+0) + | 4.0410e+12 (3.29e+0) + | 3.9336e+13 (4.97e+0) + |
| DTLZ6 | 3 | 400 | 9.5793e+08 (4.56e-4) | 1.0473e+11 (1.07e-2) | 1.0466e+13 (1.78e-3) + | 1.0370e+17 (9.99e-3) + | 1.0409e+16 (8.80e-3) + | 1.0466e+12 (2.26e-3) + | 1.0467e+12 (1.54e-3) + | 1.0466e+14 (3.07e-3) + |
| | 5 | 600 | 6.5083e+08 (9.17e-1) | 1.6187e+11 (7.19e-1) | 1.1693e+12 (1.25e+0) + | 1.0080e+17 (1.17e+0) + | 1.1208e+16 (1.24e+0) + | 1.0271e+19 (1.08e+0) + | 1.3733e+13 (1.68e+0) + | 1.3841e+12 (1.48e+0) + |
| | 8 | 750 | 7.1162e+08 (3.62e+0) | 3.2460e+11 (5.03e+0) + | 1.4508e+15 (1.51e+0) + | 1.3938e+17 (1.37e+0) + | 1.4242e+16 (1.99e+0) + | 1.6121e+14 (1.47e+0) + | 1.7707e+13 (1.63e+0) + | 1.8140e+12 (1.48e+0) + |
| | 10 | 1000 | 7.6380e+08 (2.46e-0) | 3.9083e+11 (5.55e+0) + | 1.5855e+15 (1.55e+0) + | 1.5698e+17 (1.63e+0) + | 1.5812e+16 (2.59e+0) + | 2.1001e+12 (1.33e+0) + | 2.0698e+11 (1.80e+0) + | 2.0809e+12 (1.72e+0) + |
| DTLZ7 | 3 | 400 | 9.5739e+08 (4.56e-4) | 1.0473e+11 (1.07e-2) | 1.0466e+13 (1.78e-3) + | 1.0370e+17 (9.99e-3) + | 1.0409e+16 (8.80e-3) + | 1.0466e+12 (2.26e-3) + | 1.0467e+12 (1.54e-3) + | 1.0466e+14 (3.07e-3) + |
| | 5 | 600 | 6.5083e+08 (9.17e-1) | 1.6187e+11 (7.19e-1) | 1.1693e+12 (1.25e+0) + | 1.0080e+17 (1.17e+0) + | 1.1208e+16 (1.24e+0) + | 1.0271e+19 (1.08e+0) + | 1.3733e+13 (1.68e+0) + | 1.3841e+12 (1.48e+0) + |
| | 8 | 750 | 7.1162e+08 (3.62e+0) | 3.2460e+11 (5.03e+0) + | 1.4508e+15 (1.51e+0) + | 1.3938e+17 (1.37e+0) + | 1.4242e+16 (1.99e+0) + | 1.6121e+14 (1.47e+0) + | 1.7707e+13 (1.63e+0) + | 1.8140e+12 (1.48e+0) + |
| | 10 | 1000 | 7.6380e+08 (2.46e-0) | 3.9083e+11 (5.55e+0) + | 1.5855e+15 (1.55e+0) + | 1.5698e+17 (1.63e+0) + | 1.5812e+16 (2.59e+0) + | 2.1001e+12 (1.33e+0) + | 2.0698e+11 (1.80e+0) + | 2.0809e+12 (1.72e+0) + |
| WFG2 | 3 | 1000 | 2.1486e+18 (4.51e-1) | 2.4268e+11 (1.74e-1) | 2.3538e+13 (4.12e-1) + | 2.3290e+17 (4.09e-1) + | 2.3336e+16 (4.02e-1) + | 2.3421e+15 (5.02e-1) + | 2.3594e+12 (4.66e-1) + | 2.3510e+14 (4.28e-1) + |
| | 5 | 1000 | 7.4502e+08 (4.56e-4) | 1.4144e+12 (8.57e+0) + | 1.2045e+16 (2.19e+0) + | 1.2224e+22 (1.24e+1) + | 1.1976e+20 (1.37e+1) + | 1.1139e+21 (9.80e+0) + | 1.2048e+22 (9.56e+0) + | 1.1813e+26 (1.55e+1) + |
| | 8 | 1500 | 7.3342e+18 (2.93e+0) | 1.5401e+12 (7.15e-1) | 1.2041e+14 (2.17e+0) + | 1.2002e+25 (1.82e+0) + | 1.2076e+22 (8.41e-1) + | 1.1522e+25 (5.07e+0) + | 1.1944e+26 (2.45e+0) + | 1.2057e+27 (4.10e+0) + |
| | 10 | 1500 | 1.1017e+28 (3.43e+0) | 2.7490e+21 (1.09e-1) + | 1.9025e+24 (9.33e-1) + | 1.9084e+23 (1.71e+0) + | 1.9095e+22 (2.29e+0) + | 1.8818e+29 (1.39e+0) + | 1.8762e+27 (3.26e+0) + | 1.8866e+28 (2.84e+0) + |
| WFG3 | 3 | 400 | 1.8528e+18 (5.66e-4) | 2.0577e+11 (2.51e-1) | 1.8938e+16 (3.79e-1) + | 1.8585e+17 (1.17e+0) + | 1.8835e+17 (2.51e-1) + | 1.8909e+19 (4.08e-1) + | 1.8831e+19 (4.35e-1) + | 1.8890e+14 (3.98e-1) + |
| | 5 | 750 | 3.6648e+18 (1.12e+0) | 4.0413e+12 (7.11e-1) | 3.6620e+16 (3.92e-1) + | 3.6806e+12 (5.63e-1) + | 3.6447e+17 (1.17e+0) + | 3.6401e+19 (1.54e-1) + | 3.6648e+18 (7.26e-1) + | 3.6650e+14 (4.19e-1) + |
| | 8 | 1500 | 4.4107e+18 (1.28e+0) | 5.3898e+11 (6.16e-1) | 4.4674e+19 (9.42e-1) + | 4.4657e+16 (1.12e+0) + | 4.4657e+16 (1.65e-1) + | 4.4678e+19 (0.55e-1) + | 4.4348e+17 (1.18e-0) + | 4.4666e+14 (8.92e-1) + |
| | 10 | 2000 | 5.2314e+18 (1.51e+0) | 6.4138e+16 (1.54e+0) + | 5.2559e+16 (1.67e+0) + | 5.3047e+16 (9.81e-1) + | 5.5263e+12 (1.31e+0) + | 5.2704e+19 (1.35e-0) + | 5.2533e+17 (9.84e-1) + | 5.2683e+15 (1.20e-1) + |
| DTLZ1 | 3 | 400 | 2.0907e+18 (4.06e-4) | 2.2506e+11 (1.55e-1) | 2.3103e+16 (6.64e-2) + | 2.3134e+15 (6.04e-2) + | 2.3134e+13 (3.10e-2) + | 2.3134e+14 (3.42e-2) + | 2.3119e+13 (2.05e-2) + | 2.3124e+13 (4.64e-2) + |
| | 5 | 600 | 2.5966e+18 (5.97e-3) | 6.6327e+16 (5.16e-1) | 6.9180e+14 (8.14e-1) + | 6.2651e+15 (1.07e+0) + | 6.5066e+16 (8.41e-1) + | 7.2001e+11 (1.59e-1) + | 7.1487e+13 (1.42e-1) + | 7.1510e+12 (1.55e-1) + |
| | 8 | 750 | 2.5942e+18 (8.50e-1) | 1.0496e+20 (1.79e+0) | 1.0518e+21 (7.55e-1) + | 9.7948e+20 (1.15e-0) + | 1.0226e+23 (9.14e-1) + | 9.9943e+19 (7.24e-1) + | 9.9079e+19 (6.55e-1) + | 9.9250e+19 (8.87e-1) + |
| | 10 | 1000 | 2.5662e+18 (1.16e+0) | 1.6242e+21 (3.32e+0) + | 1.6890e+21 (1.10e+0) + | 1.5338e+24 (2.09e+0) + | 1.9403e+20 (5.87e-1) + | 1.5303e+22 (6.36e-1) + | 1.5242e+22 (6.09e-1) + | 1.5227e+22 (6.09e-1) + |
| DTLZ2 | 3 | 250 | 2.7603e+18 (5.77e-1) | 3.0716e+11 (3.80e-1) | 3.0463e+14 (3.87e-1) + | 2.9313e+17 (6.03e-1) + | 2.9780e+15 (4.58e-1) + | 2.9625e+16 (4.19e-1) + | 3.0512e+13 (3.31e-1) + | 3.0603e+12 (3.56e-1) + |
| | 5 | 350 | 3.5972e+18 (1.01e+0) | 1.2146e+12 (1.15e+0) | 1.1975e+20 (1.30e+0) + | 1.0701e+27 (2.14e+0) + | 1.0976e+20 (1.27e+0) + | 1.2343e+22 (7.86e-1) + | 1.1957e+24 (0.98e-1) + | 1.1943e+22 (8.74e-1) + |
| | 8 | 500 | 7.1649e+18 (6.52e+0) | 1.4632e+12 (4.86e-1) | 1.4158e+25 (2.18e+0) + | 1.2799e+27 (3.45e-1) + | 1.3482e+20 (2.10e+0) + | 1.4517e+22 (1.54e-0) + | 1.4367e+22 (2.23e+0) + | 1.4243e+22 (2.77e+0) + |
| | 10 | 750 | 8.2551e+18 (7.89e-1) | 2.5856e+21 (7.96e-1) | 2.3742e+25 (3.40e+0) + | 2.1275e+27 (2.95e+0) + | 2.2327e+20 (3.05e+0) + | 2.4433e+24 (3.99e+0) + | 2.4086e+24 (3.64e+0) + | 2.4118e+24 (3.95e+0) + |
| DTLZ3 | 3 | 1000 | 2.7632e+18 (1.14e-1) | 3.1090e+11 (3.31e-1) | 3.1256e+12 (1.48e-1) + | 3.0792e+17 (3.72e-1) + | 3.0792e+15 (3.10e-1) + | 3.0765e+16 (2.43e-1) + | 3.1276e+11 (1.78e-1) + | 3.1224e+13 (2.83e-1) + |
| | 5 | 1000 | 3.5957e+18 (4.27e-1) | 1.2431e+12 (1.99e+0) | 1.2140e+25 (1.11e+0) + | 1.0638e+27 (1.93e-1) + | 1.0919e+20 (1.67e-1) + | 1.2510e+22 (8.55e-1) + | 1.2202e+24 (5.88e-1) + | 1.2187e+24 (5.28e-1) + |
| | 8 | 1000 | 7.8256e+18 (3.89e-1) | 1.4506e+12 (2.16e-1) | 1.4224e+25 (1.66e-1) + | 1.2491e+27 (3.13e-1) + | 1.3321e+20 (2.25e-1) + | 1.4740e+22 (1.13e-0) + | 1.4478e+24 (1.90e-0) + | 1.4449e+23 (1.47e-0) + |
| | 10 | 1500 | 8.7145e+18 (1.10e+0) | 2.5788e+21 (9.97e-1) | 2.4003e+25 (2.78e-0) + | 2.0944e+27 (3.59e-0) + | 2.2409e+20 (3.62e-0) + | 2.4621e+22 (3.86e-0) + | 2.4397e+24 (3.96e-0) + | 2.4404e+23 (4.10e-0) + |
| DTLZ4 | 3 | 600 | 2.7639e+18 (1.54e-1) | 3.1361e+12 (1.84e-1) | 3.1266e+14 (1.87e-1) + | 3.0857e+16 (2.76e-1) + | 3.1088e+15 (1.75e-1) + | 3.0835e+17 (2.36e-1) + | 3.1362e+11 (1.29e-1) + | 3.1321e+13 (1.27e-1) + |
| | 5 | 1000 | 3.5945e+18 (9.83e-1) | 3.1373e+12 (6.77e-1) | 3.1256e+12 (6.61e-1) + | 3.0752e+16 (6.61e-1) + | 3.0592e+14 (1.62e-1) + | 3.0751e+16 (2.43e-1) + | 3.1276e+11 (1.78e-1) + | 3.1224e+13 (2.83e-1) + |
| | 8 | 1250 | 3.8004e+18 (5.30e+0) | 4.8758e+12 (2.66e-1) | 4.6656e+14 (4.82e+0) + | 4.1086e+16 (5.35e-1) + | 4.1086e+15 (5.35e-1) + | 4.1268e+16 (2.38e-1) + | 4.1356e+12 (5.66e-1) + | 4.1235e+14 (4.81e-1) + |
| | 10 | 2000 | 4.0805e+18 (2.94e+0) | 6.2631e+12 (2.90e-1) | 5.2176e+16 (2.36e-0) + | 3.2901e+27 (3.05e-0) + | 2.4376e+20 (2.69e-0) + | 2.4393e+23 (7.20e-0) + | 2.4665e+24 (3.62e-0) + | 2.4630e+23 (7.02e-0) + |
| DTLZ5 | 3 | 400 | 2.3726e+18 (1.08e-0) | 2.5913e+11 (2.24e-1) | 2.6463e+12 (1.36e-1) + | 2.5732e+17 (1.96e-1) + | 2.5592e+14 (1.62e-1) + | 2.5199e+15 (2.05e-1) + | 2.6487e+11 (1.19e-1) + | 2.6454e+13 (1.18e-1) + |
| | 5 | 600 | 3.7309e+18 (7.42e-1) | 9.7818e+11 (9.37e-1) | 1.0021e+24 (4.84e-1) + | 9.3410e+16 (1.03e-0) + | 9.3849e+16 (1.81e-1) + | 1.0185e+21 (4.88e-1) + | 9.3636e+14 (1.46e-1) + | 9.3973e+14 (3.99e-1) + |
| | 8 | 750 | 5.0738e+18 (3.90e-1) | 1.3473e+12 (1.07e+0) | 1.2906e+24 (2.03e+0) + | 1.2060e+27 (2.10e+0) + | 1.2906e+20 (1.50e+0) + | 1.3174e+24 (2.16e-0) + | 1.2767e+24 (2.33e-0) + | 1.2767e+24 (2.17e-0) + |
| | 10 | 1000 | 5.5216e+18 (3.91e+0) | 2.3320e+12 (2.03e+0) + | 2.1097e+24 (3.55e-0) + | 2.1823e+27 (3.78e-0) + | 2.1532e+20 (2.27e-0) + | 2.0742e+24 (2.13e-0) + | 2.0659e+24 (2.17e-0) + | 2.0659e+24 (2.17e-0) + |
| DTLZ6 | 3 | 400 | 2.6249e+18 (6.88e-3) | 2.9665e+11 (1.70e-1) | 2.9812e+13 (8.91e-2) + | 2.9181e+17 (1.56e-1) + | 2.9285e+15 (1.45e-1) + | 2.9186e+16 (1.90e-1) + | 2.9823e+12 (9.70e-2) + | 2.9829e+11 (9.86e-2) + |
| | 5 | 600 | 3.5610e+18 (2.35e-0) | 1.8116e+21 (8.36e-1) | 1.7136e+20 (3.70e-1) + | 1.0801e+27 (1.00e+0) + | 1.1030e+20 (9.73e-1) + | 1.1798e+24 (2.40e-1) + | 1.1511e+24 (5.56e-1) + | 1.1506e+22 (4.79e-1) + |
| | 8 | 750 | 6.6295e+18 (5.44e-0) | 1.4412e+12 (2.49e-1) | 1.4193e+25 (8.85e-1) + | 1.3125e+21 (2.60e-0) + | 1.3496e+26 (2.50e-0) + | 1.4149e+29 (2.90e-0) + | 1.4069e+26 (2.05e-0) + | 1.4174e+24 (1.50e-0) + |
| | 10 | 1000 | 7.3376e+18 (7.62e-0) | 2.5340e+21 (8.65e-1) | 2.3417e+25 (2.95e-0) + | 2.1203e+27 (3.39e-0) + | 2.2046e+20 (2.51e-0) + | 2.4376e+24 (4.70e-0) + | 2.4365e+24 (3.45e-0) + | 2.4399e+24 (3.04e-0) + |
| DTLZ7 | 3 | 1000 | 1.2447e+18 (4.71e-1) | 1.4837e+11 (6.52e-1) | 1.3925e+14 (2.00e-1) + | 1.3697e+17 (2.31e-1) + | 1.3801e+16 (1.89e-1) + | 1.3870e+15 (2.14e-1) + | 1.3989e+12 (1.43e-1) + | 1.3946e+13 (1.88e-1) + |
| | 5 | 1000 | 3.6432e+18 (2.16e-0) | 7.2118e+12 (1.35e-1) | 6.4667e+16 (2.63e-1) + | 6.4666e+17 (6.63e-1) + | 6.4741e+16 (7.99e-1) + | 4.9331e+16 (6.16e-1) + | 4.9841e+17 (7.09e-1) + | 4.9707e+16 (6.78e-1) + |
| | 8 | 1000 | 4.7868e+18 (1.91e-0) | 1.2803e+12 (4.52e+0) | 4.9565e+16 (1.04e+0) + | 8.9746e+17 (2.81e-1) + | 9.3298e+16 (1.73e-0) + | 9.3025e+17 (2.10e+0) + | 9.4225e+17 (1.45e-0) + | 9.4007e+17 (1.23e-0) + |
| | 10 | 1500 | 6.5395e+18 (2.72e+0) | 1.5977e+21 (5.08e-0)</ | | | | | | |

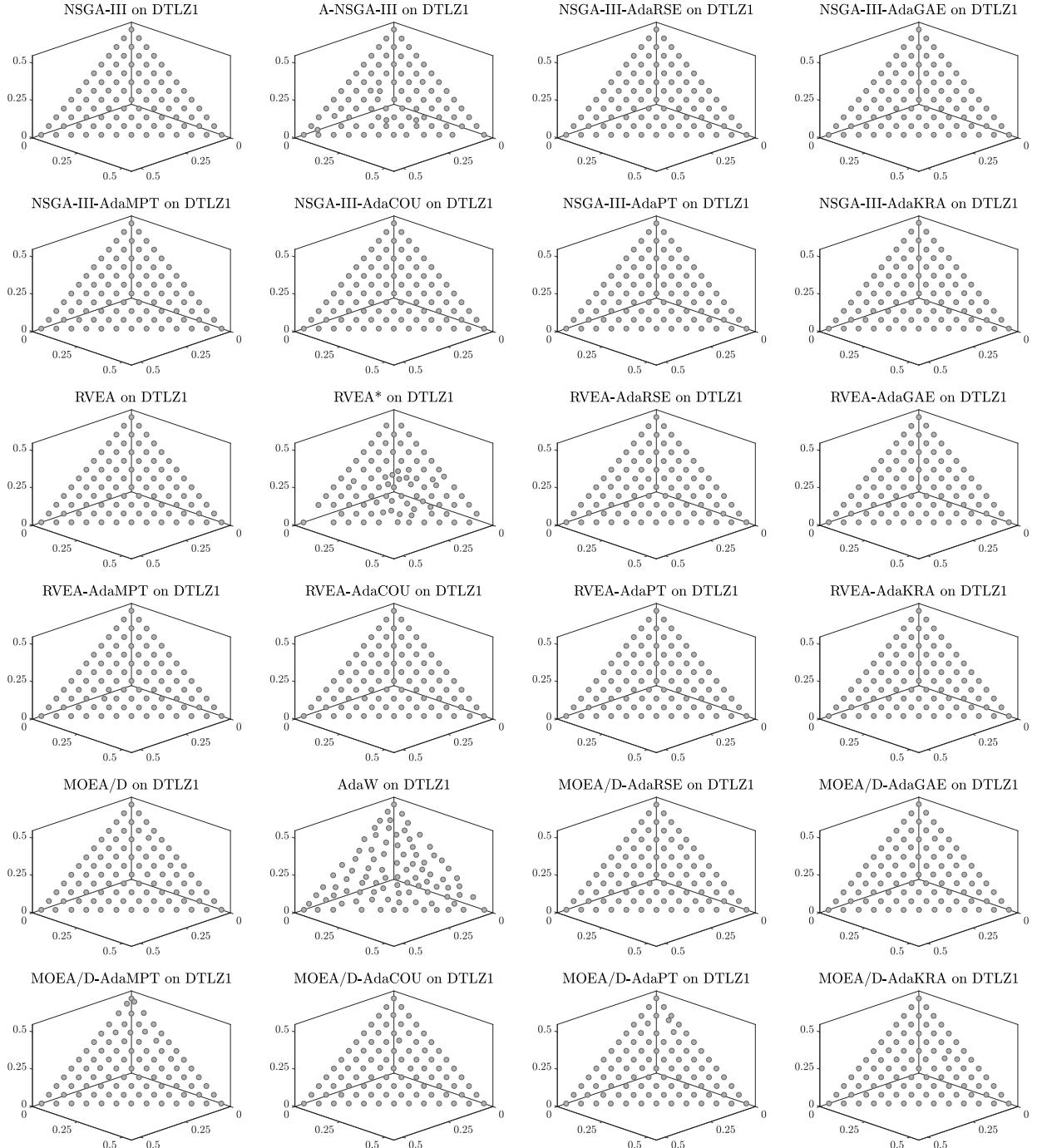


Figure 1: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ1 with 3 objective functions.

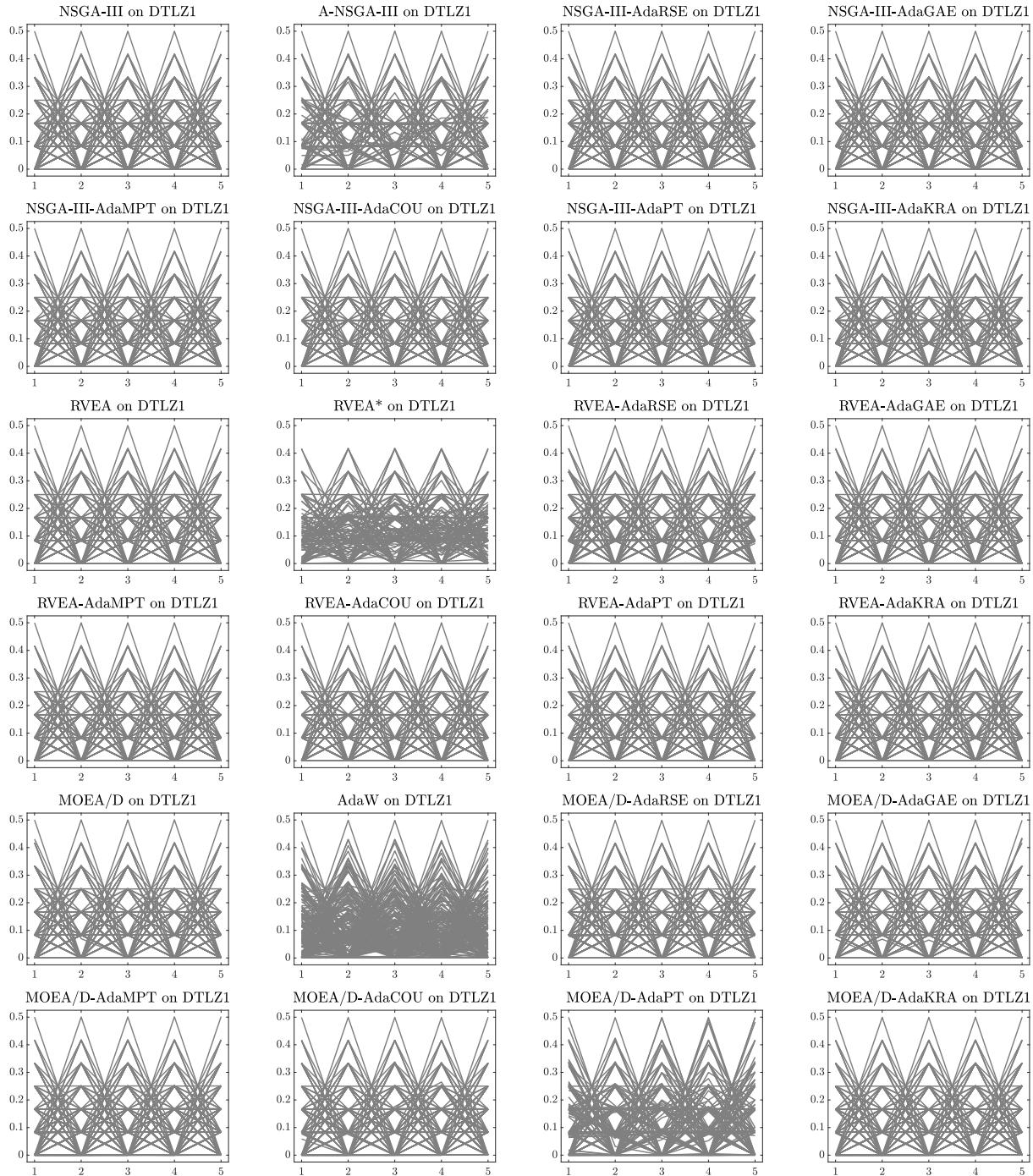


Figure 2: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ1 with 5 objective functions.

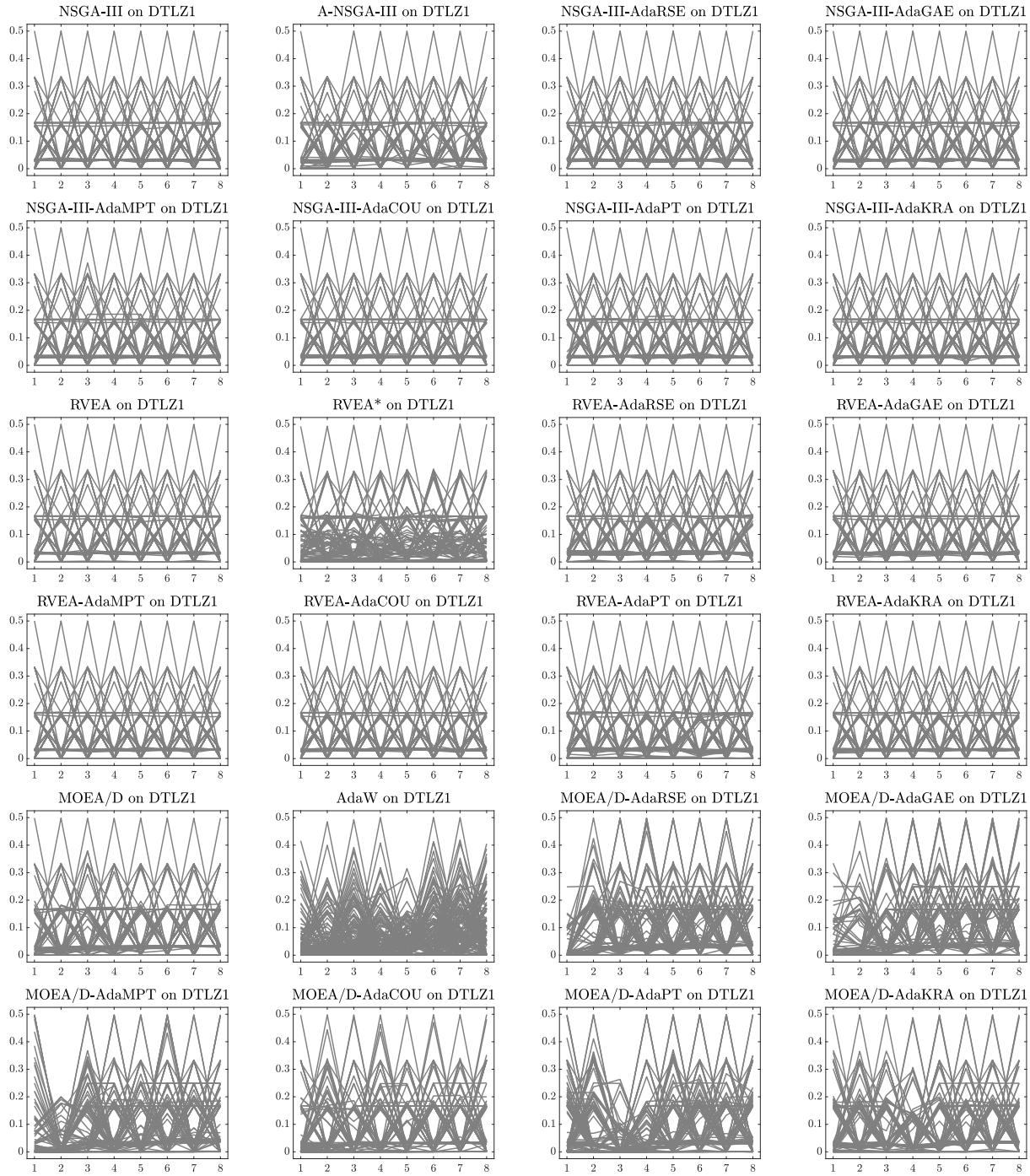


Figure 3: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ1 with 8 objective functions.

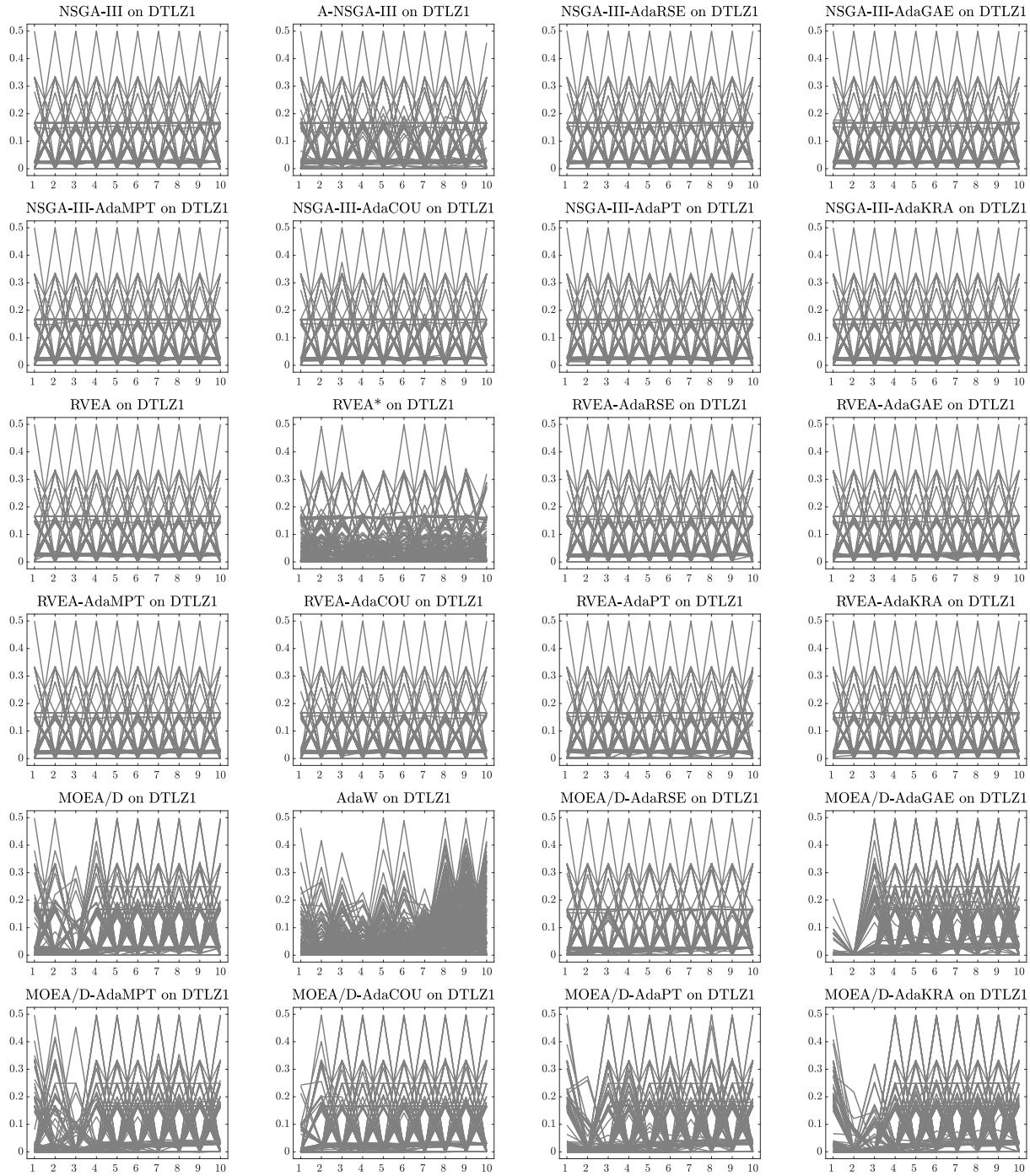


Figure 4: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ1 with 10 objective functions.

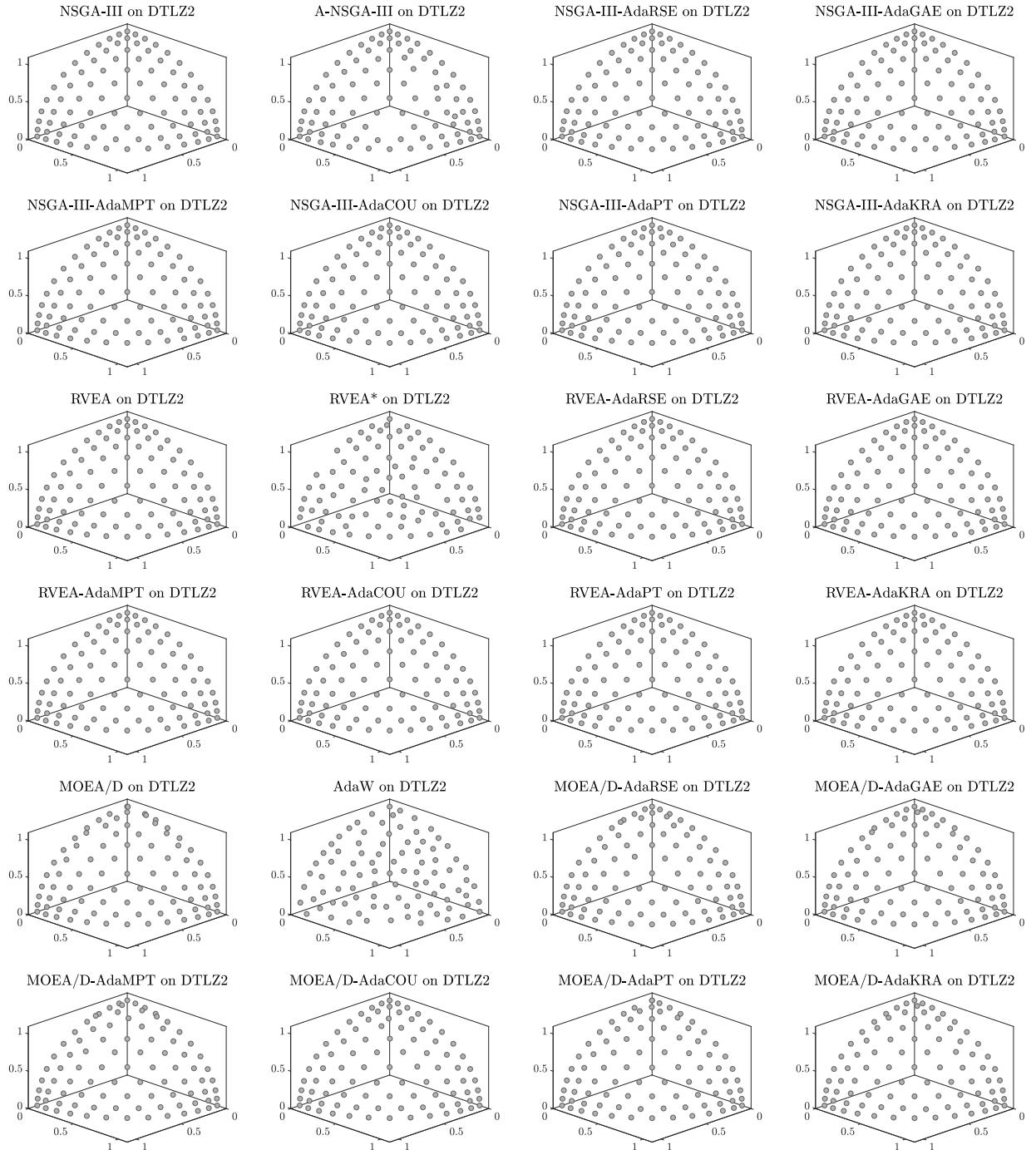


Figure 5: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ2 with 3 objective functions.

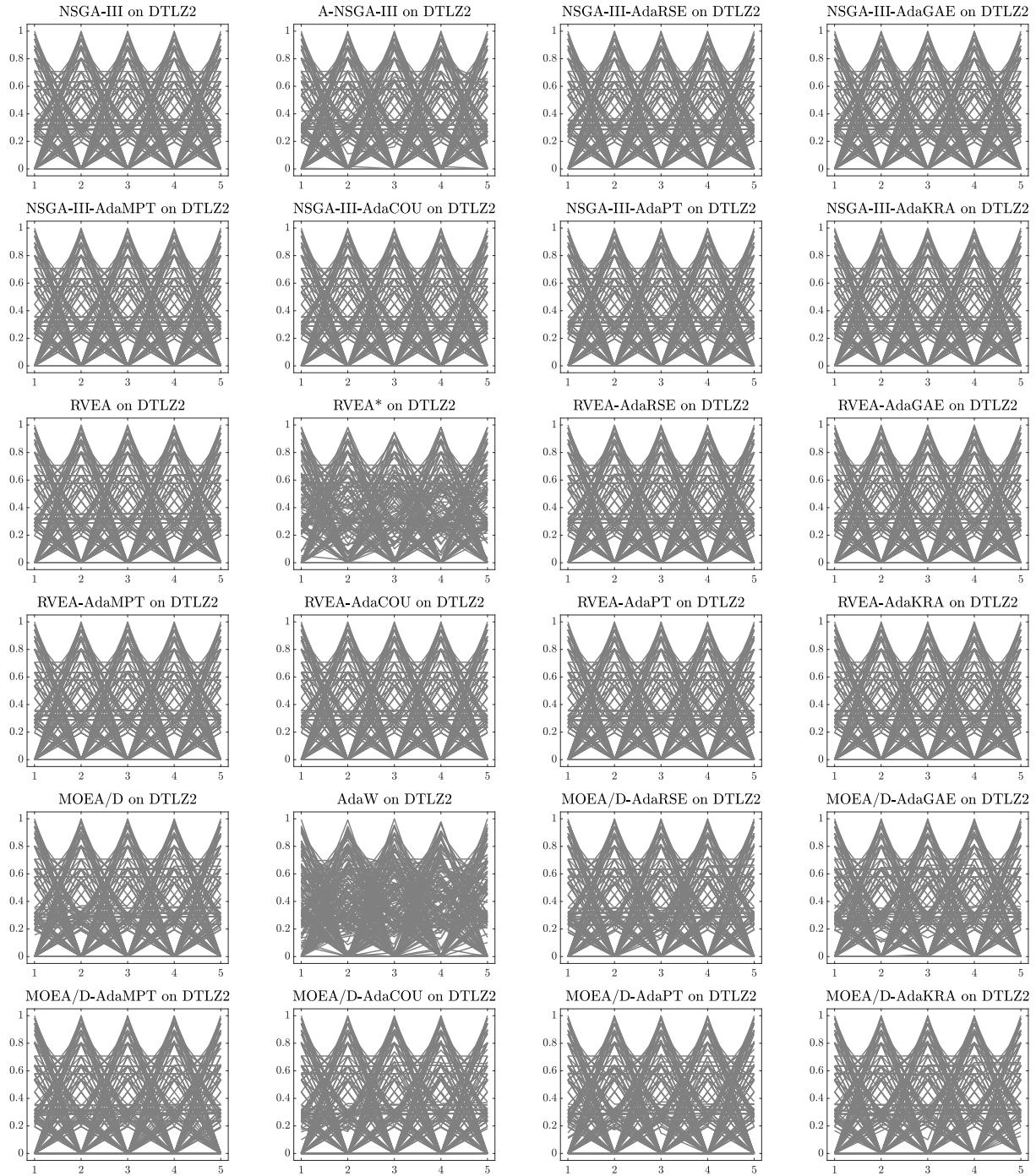


Figure 6: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ2 with 5 objective functions.

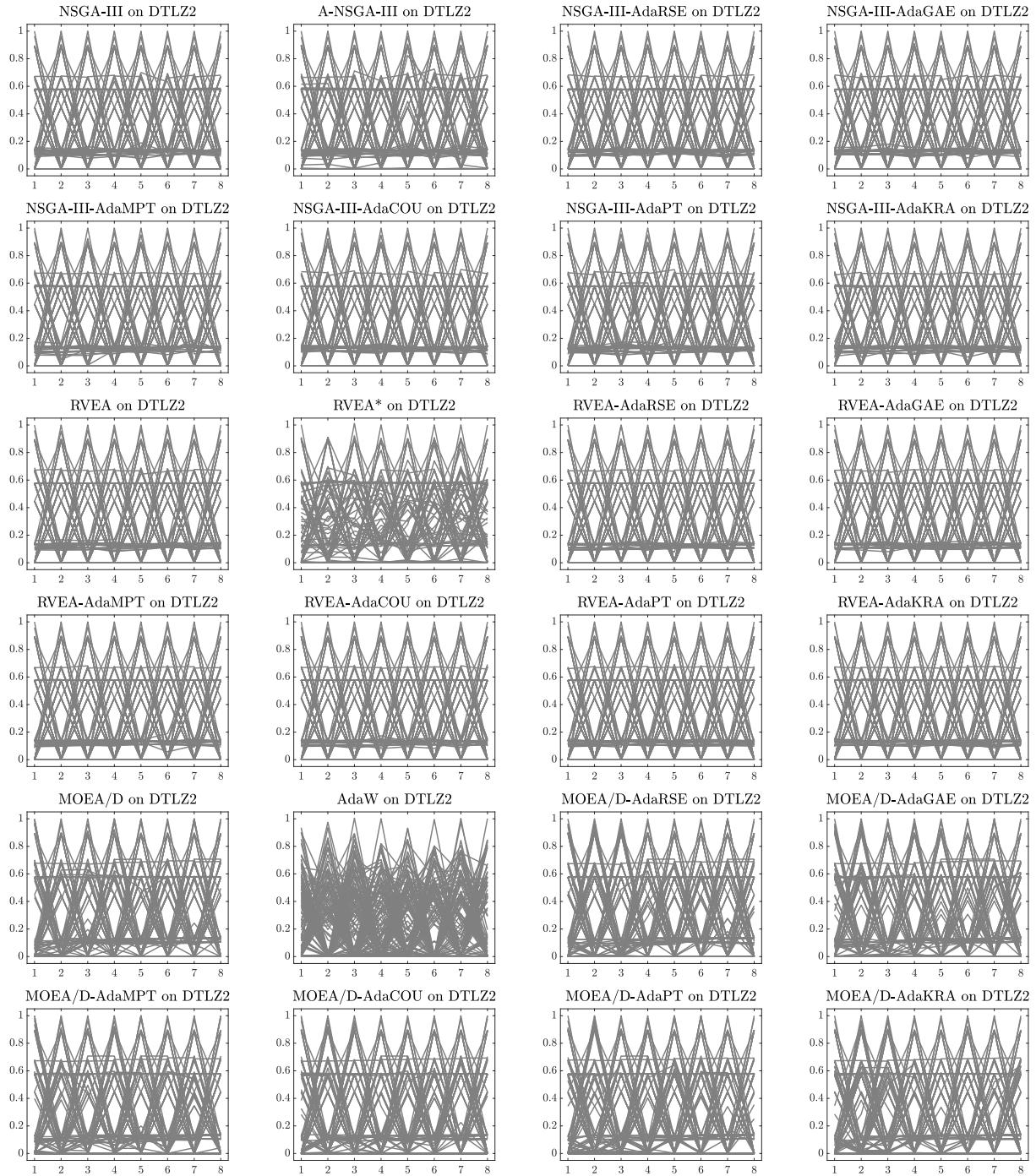


Figure 7: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ2 with 8 objective functions.

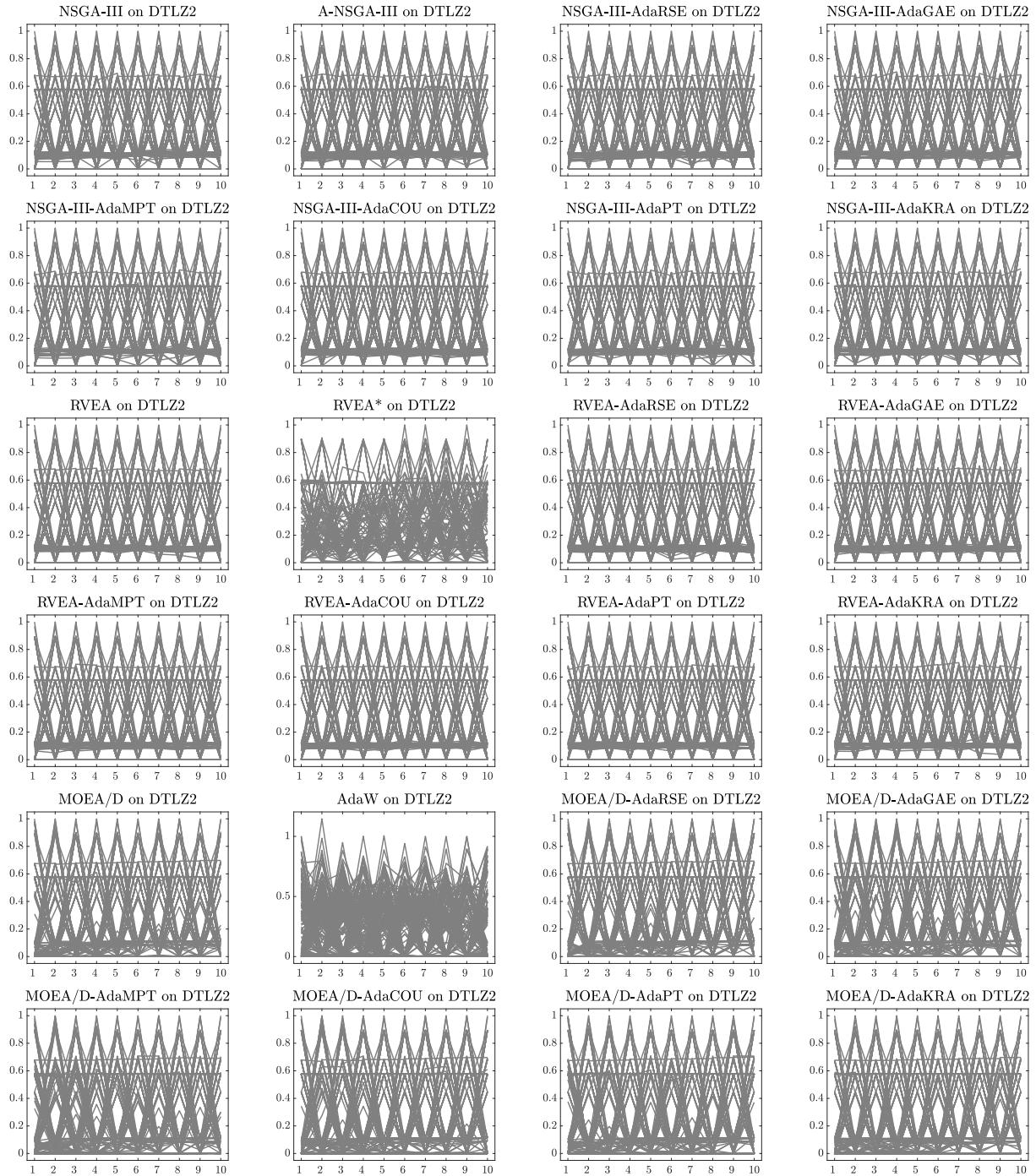


Figure 8: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ2 with 10 objective functions.

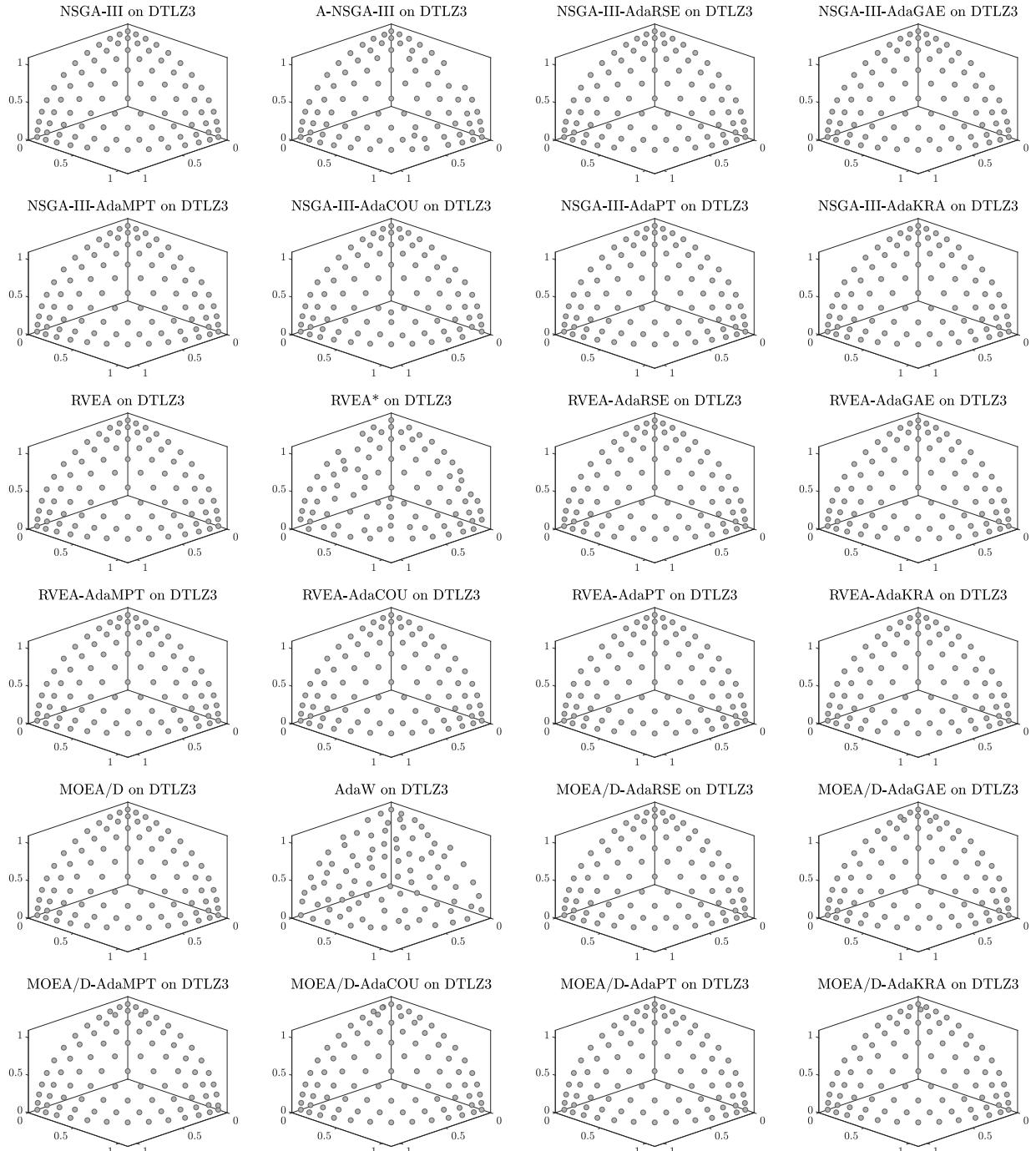


Figure 9: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ3 with 3 objective functions.

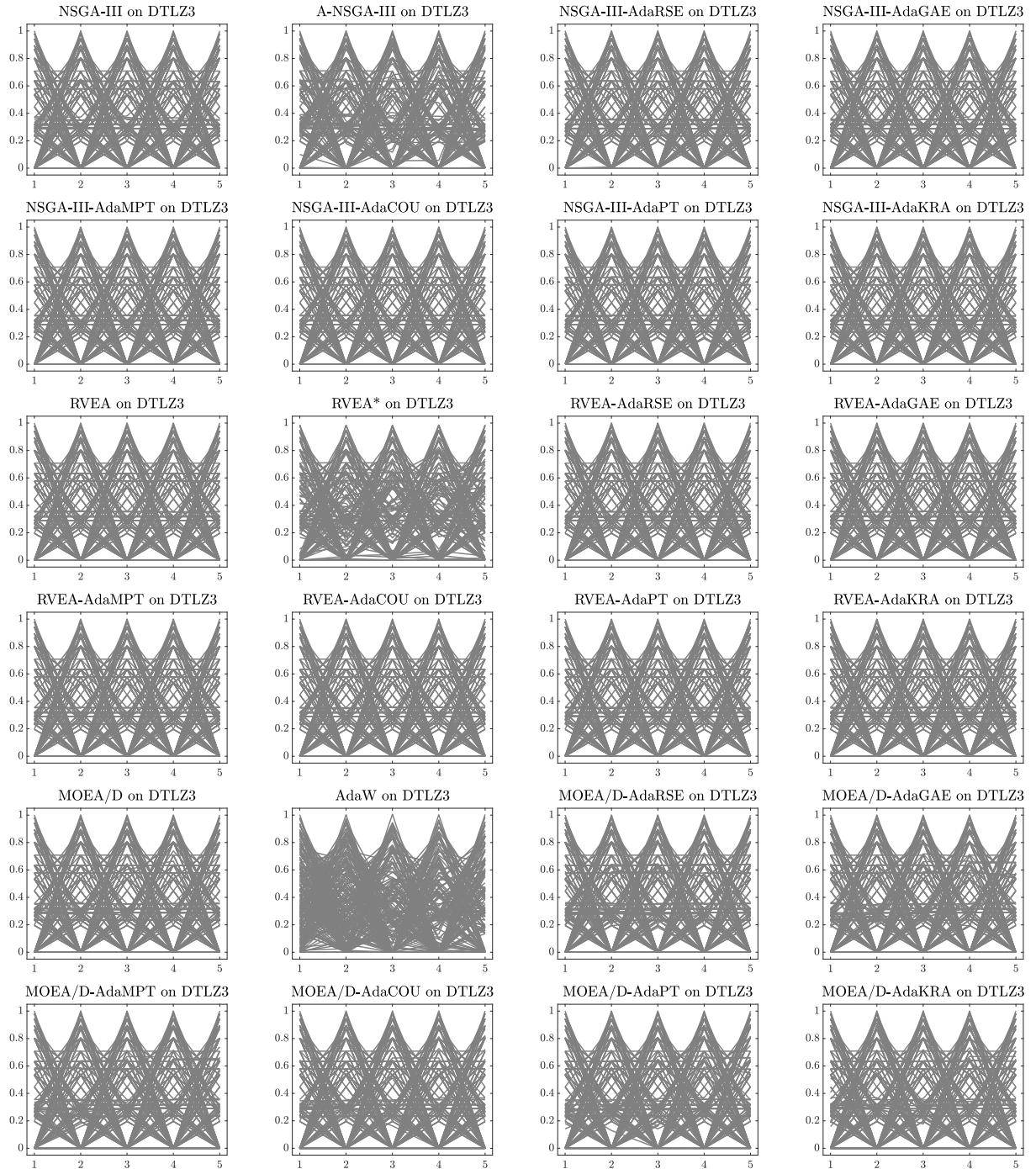


Figure 10: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ3 with 5 objective functions.

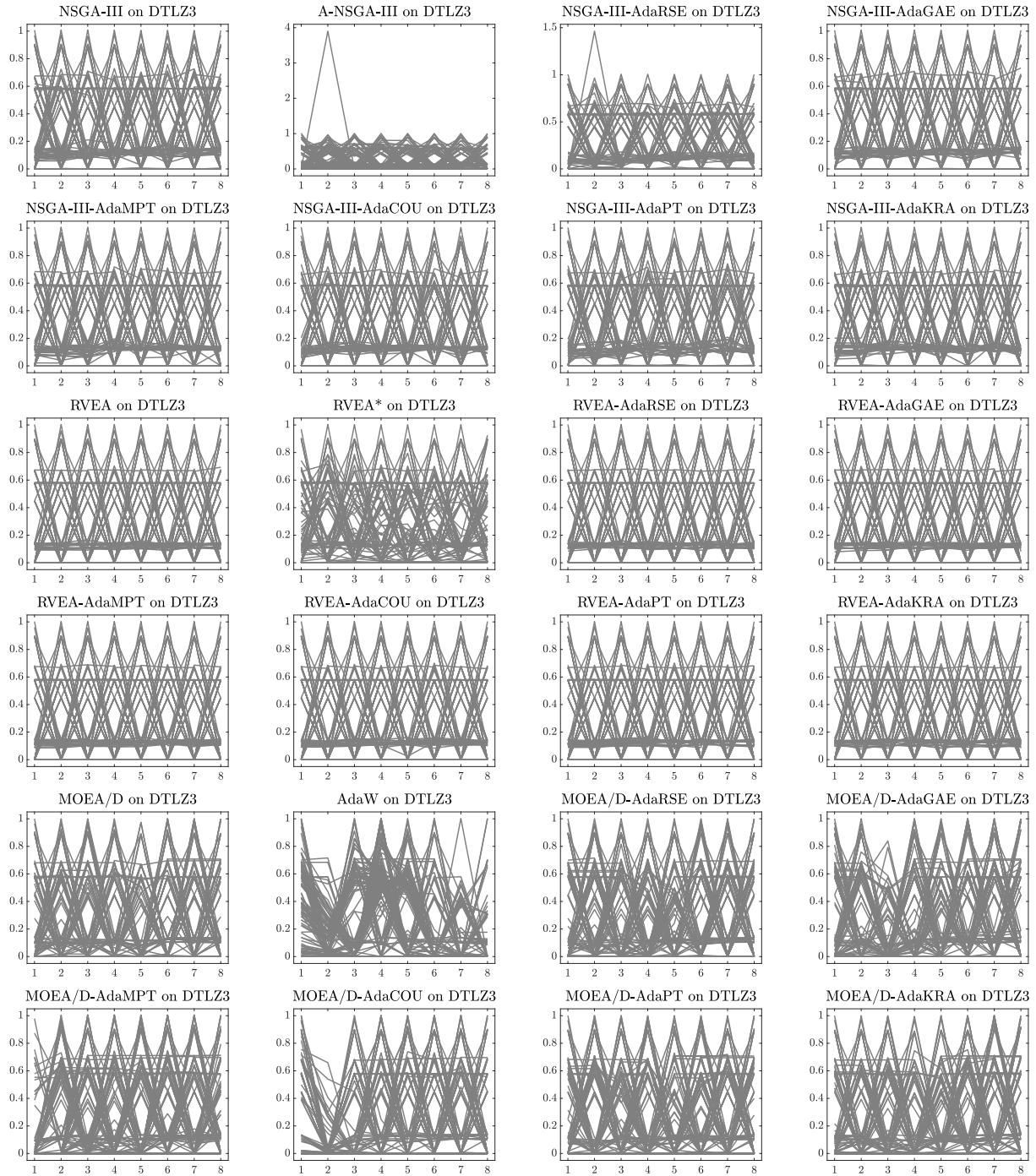


Figure 11: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ3 with 8 objective functions.

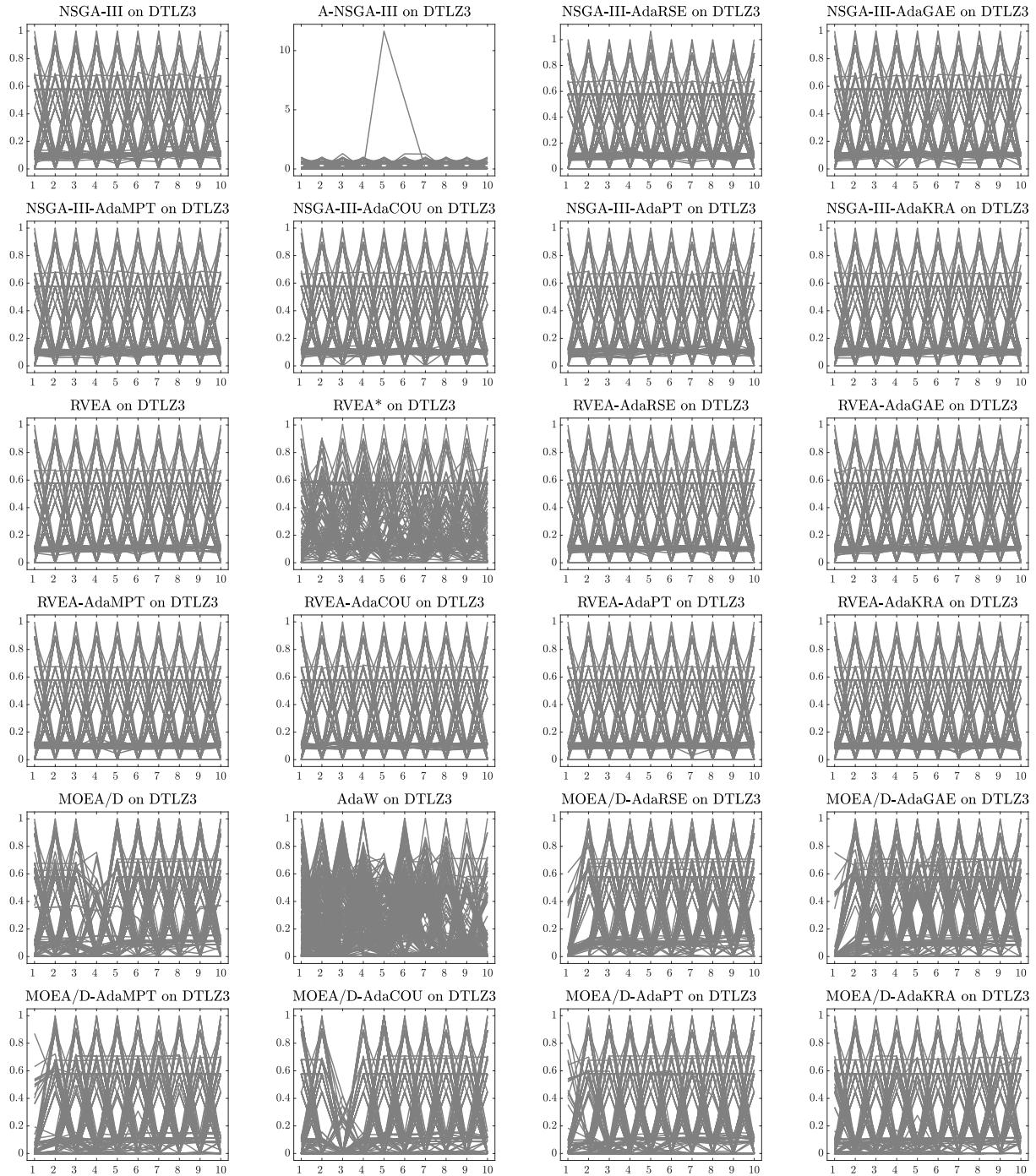


Figure 12: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ3 with 10 objective functions.

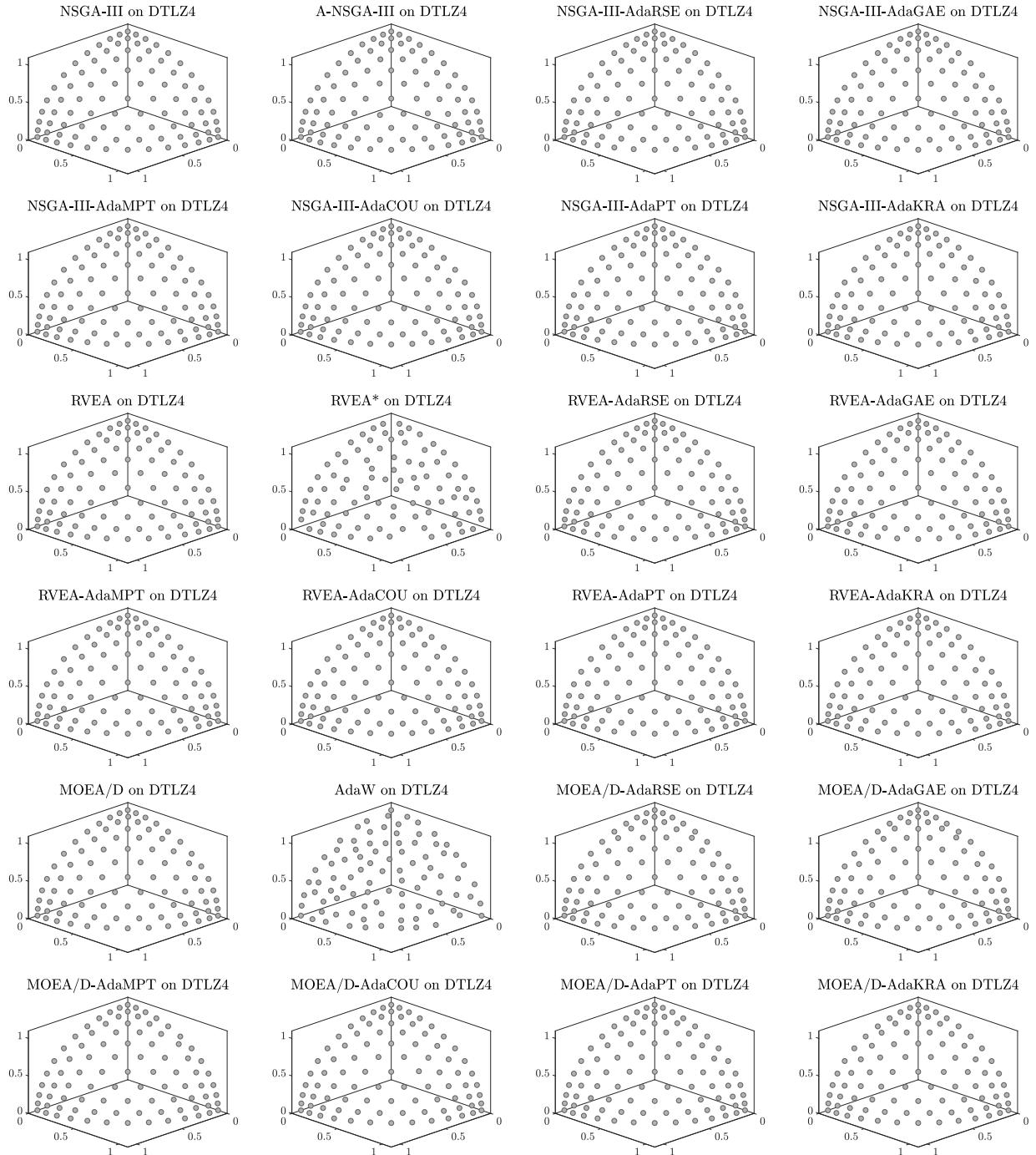


Figure 13: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ4 with 3 objective functions.

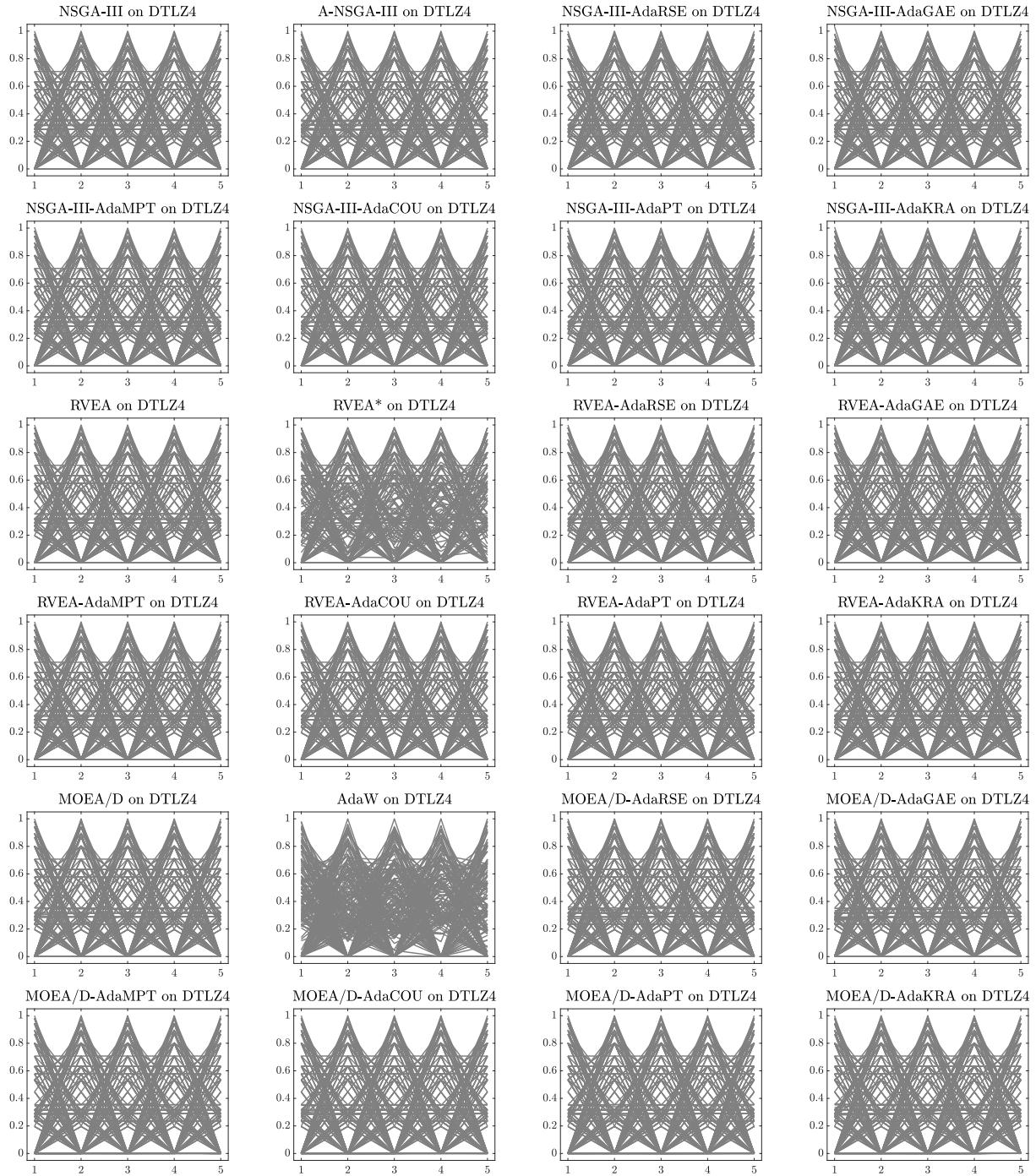


Figure 14: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ4 with 5 objective functions.

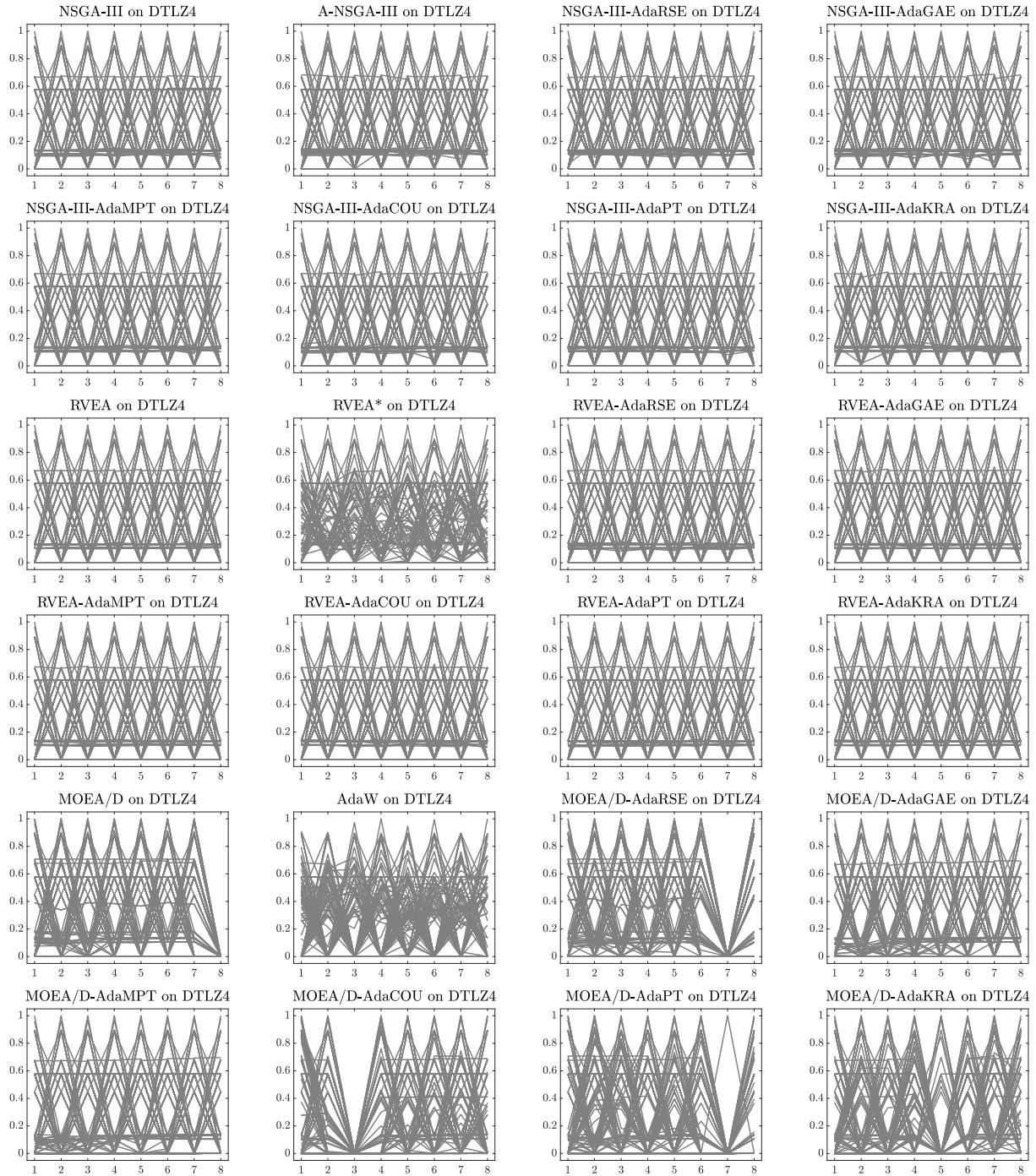


Figure 15: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ4 with 8 objective functions.

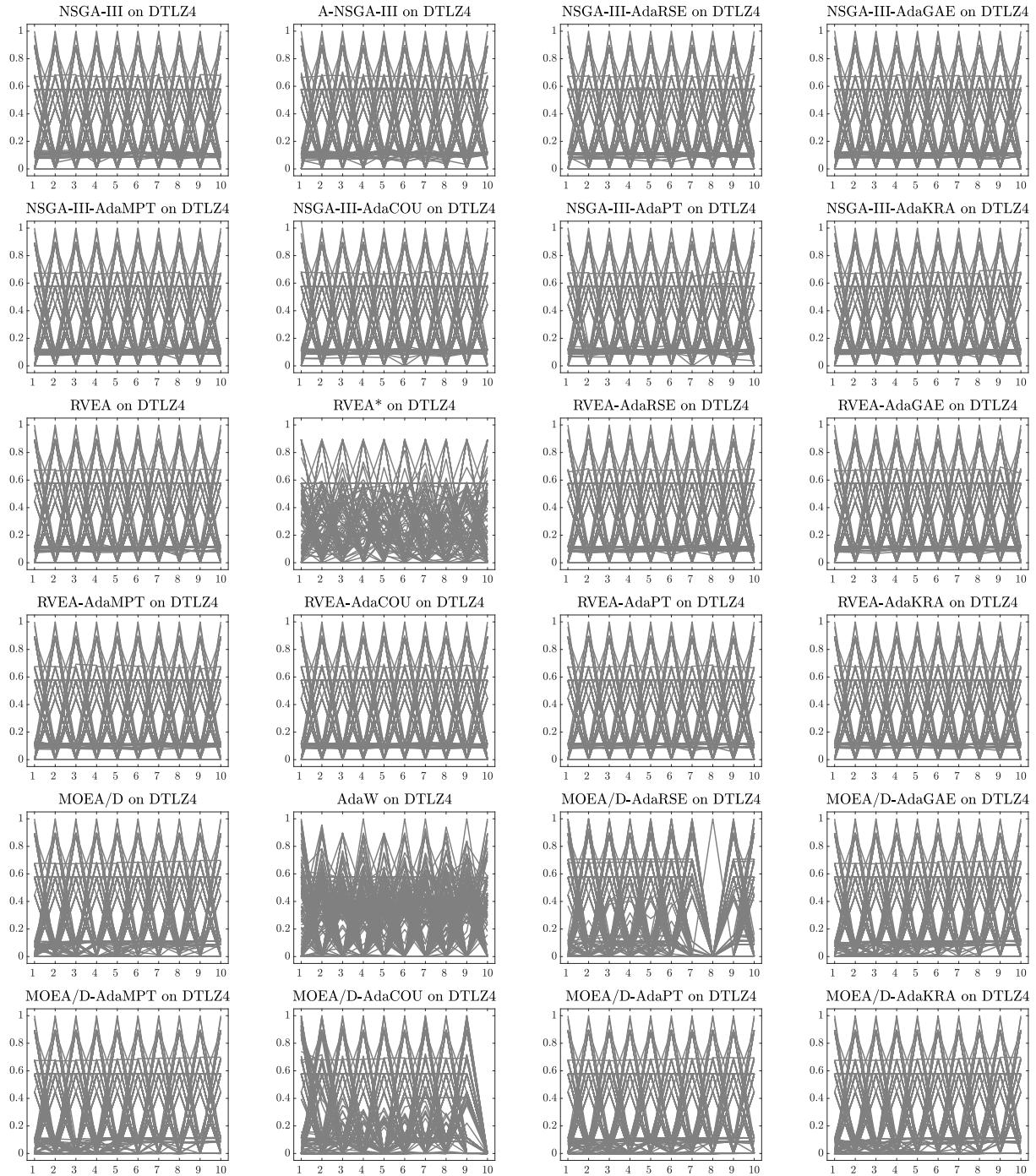


Figure 16: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ4 with 10 objective functions.

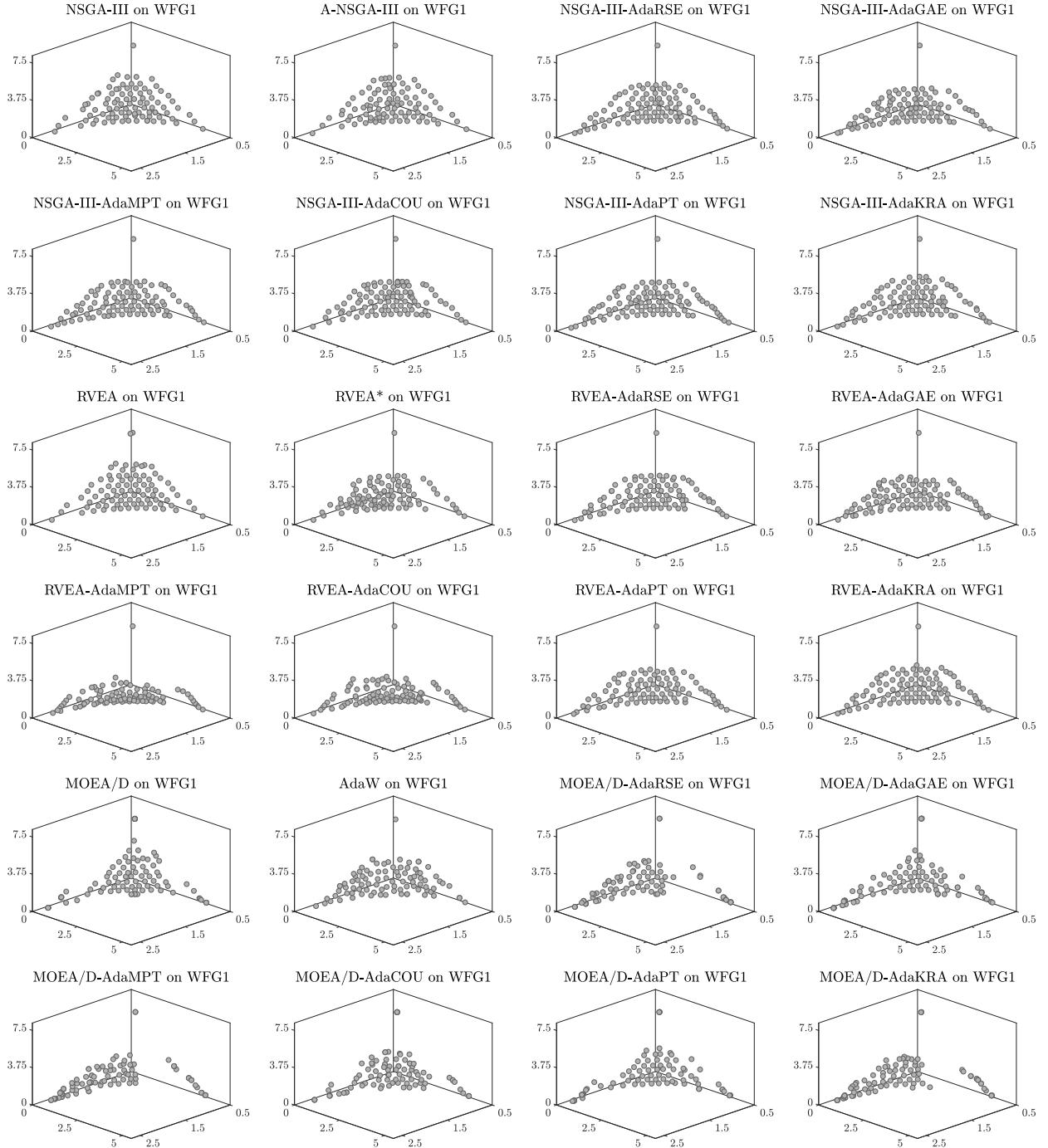


Figure 17: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG1 with 3 objective functions.

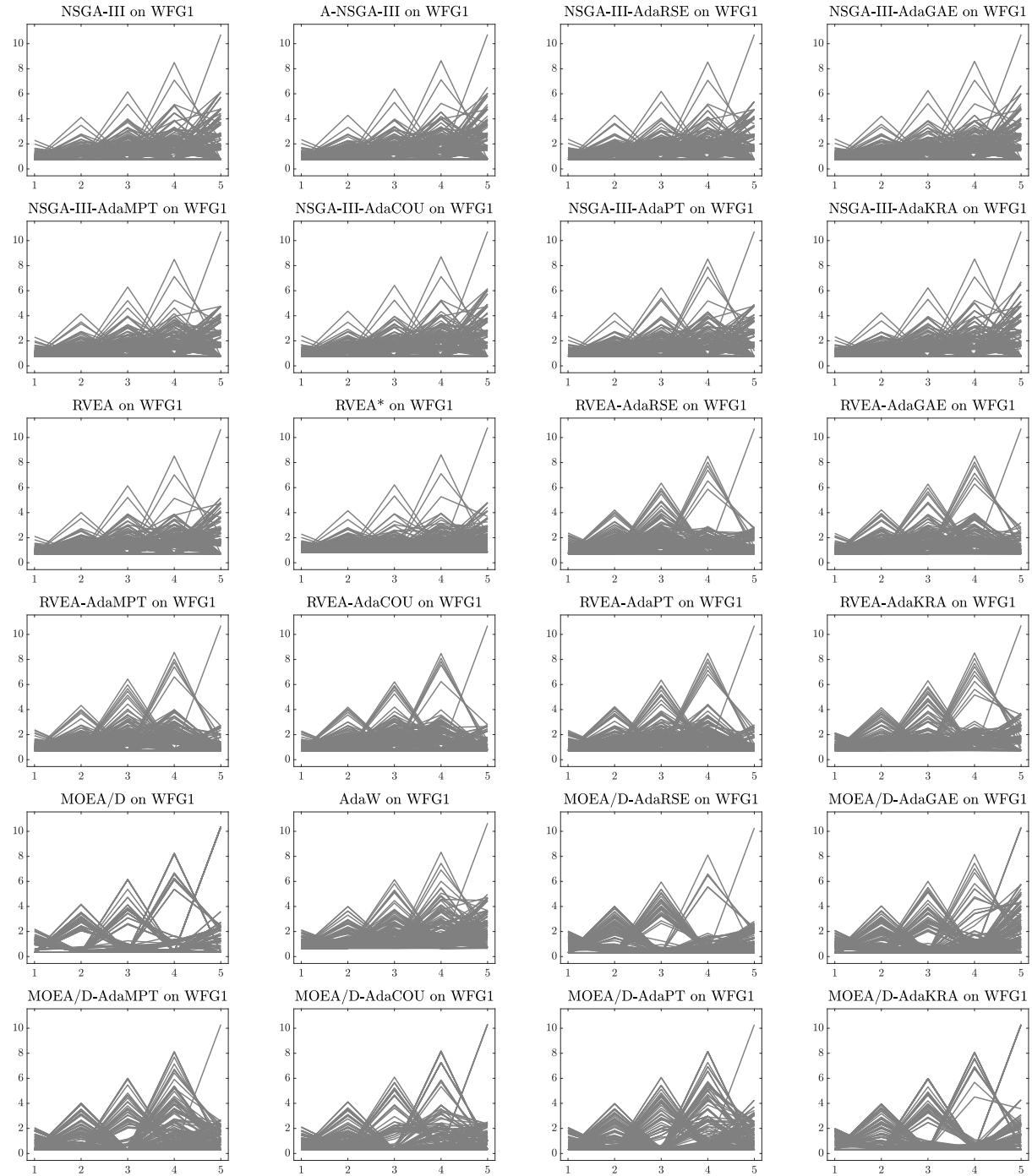


Figure 18: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG1 with 5 objective functions.

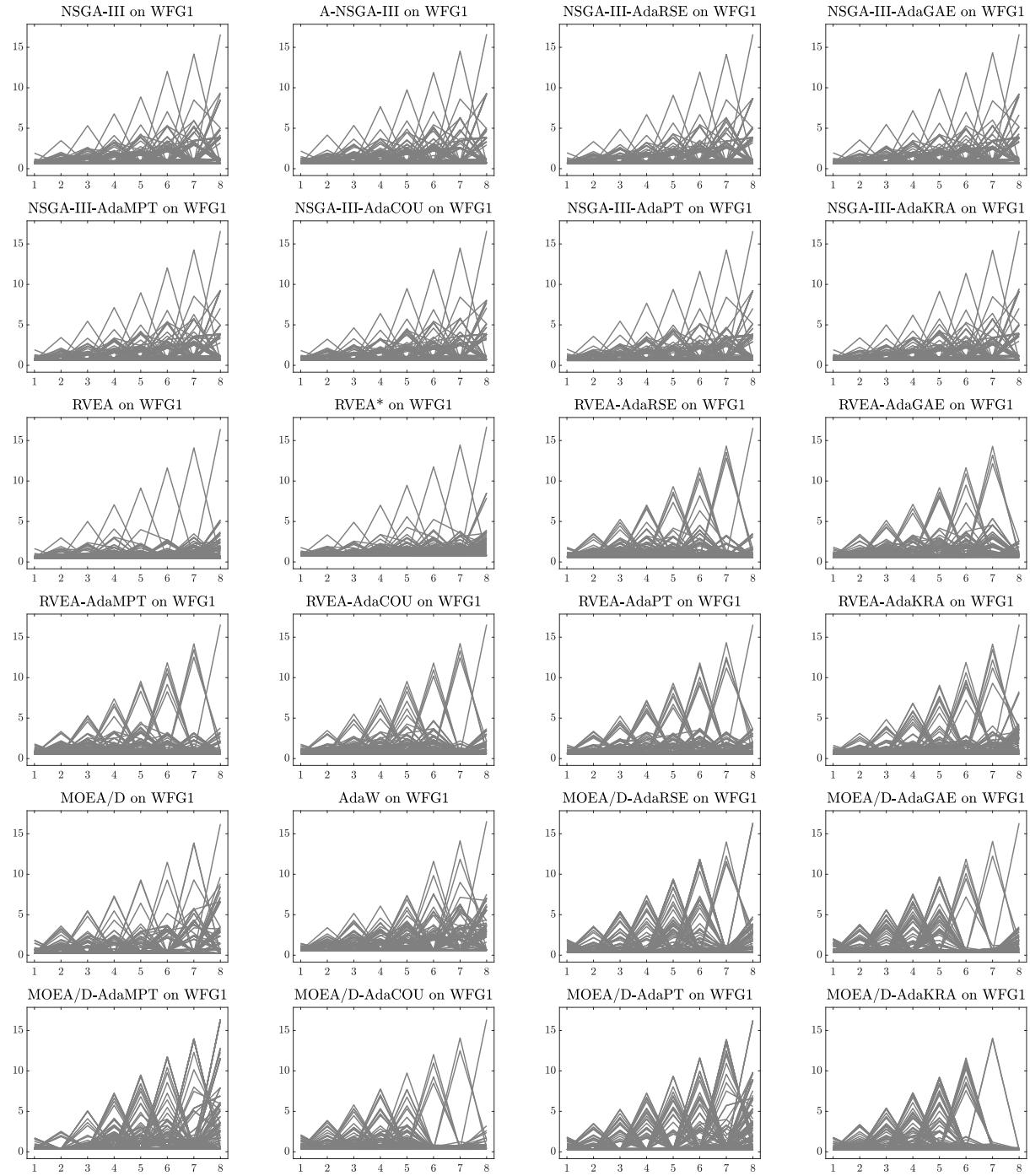


Figure 19: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG1 with 8 objective functions.

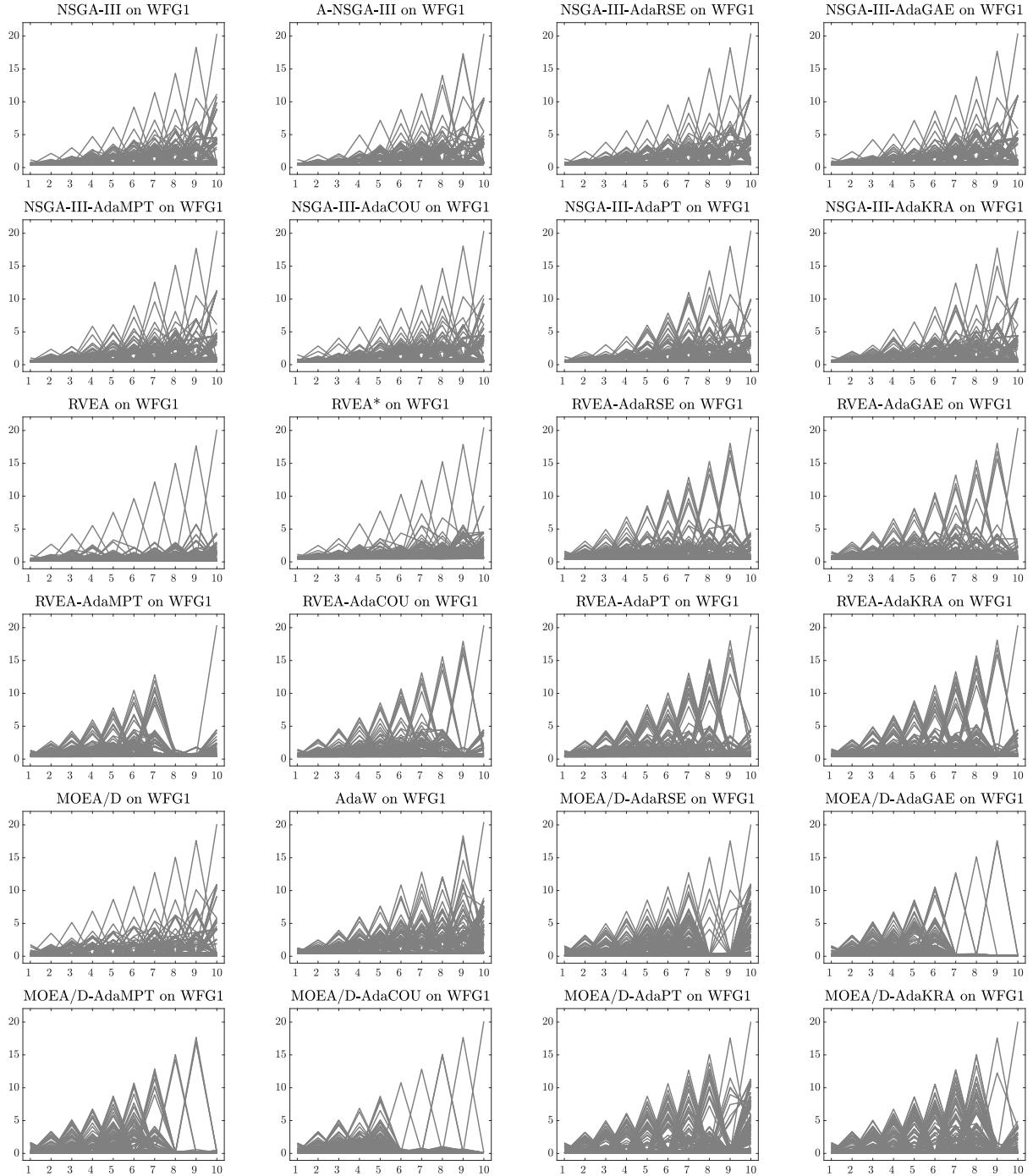


Figure 20: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG1 with 10 objective functions.

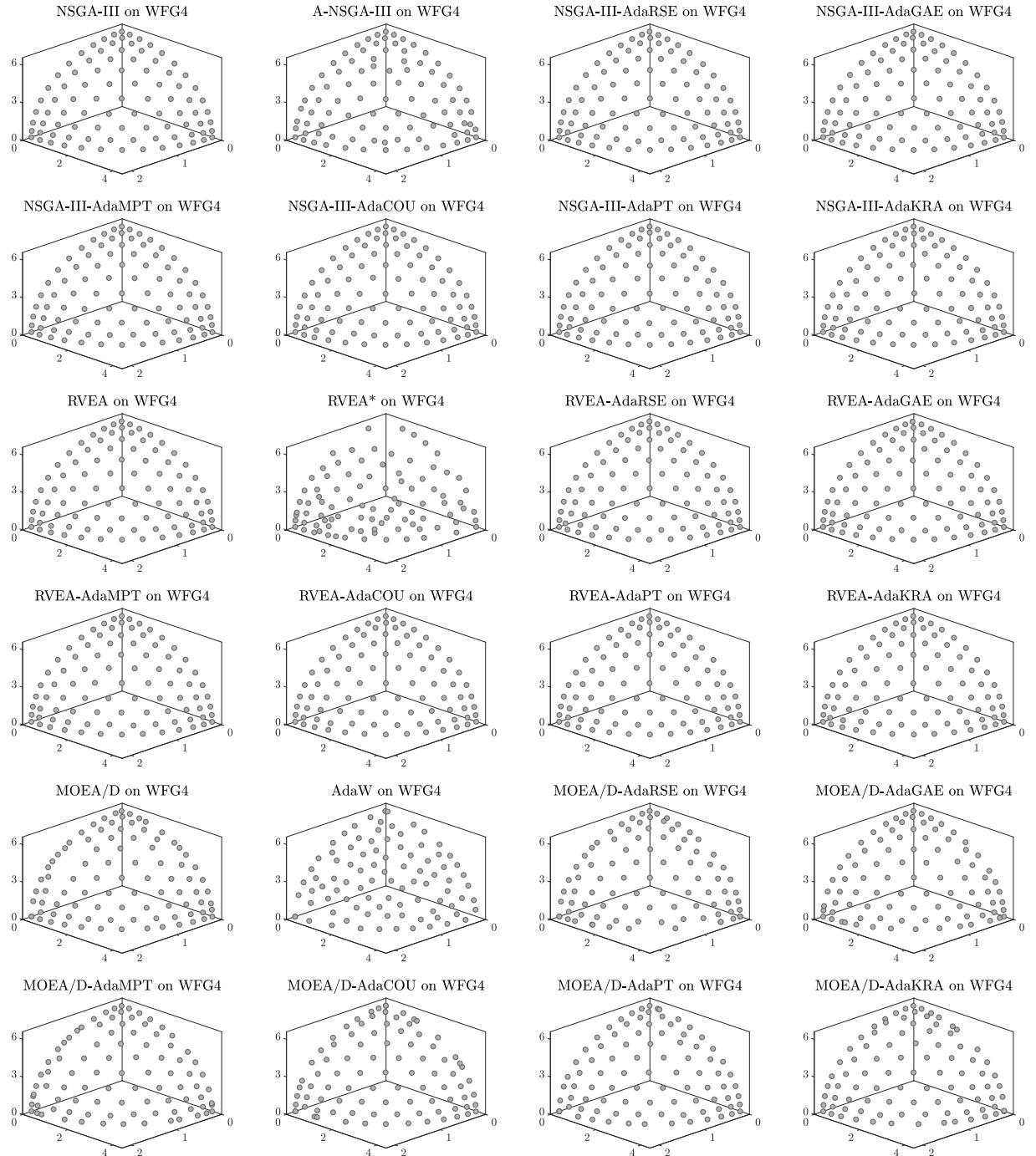


Figure 21: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG4 with 3 objective functions.

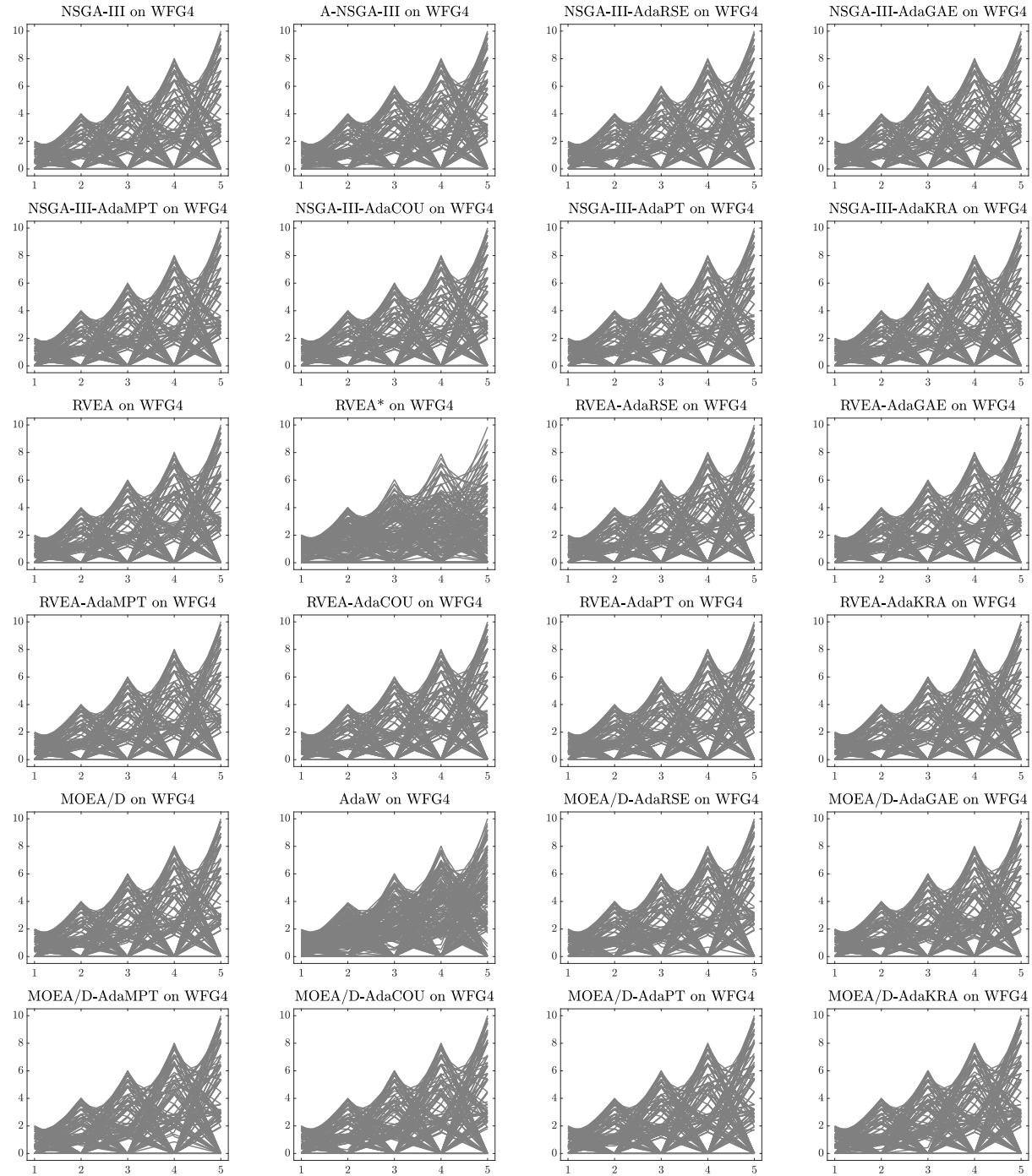


Figure 22: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG4 with 5 objective functions.

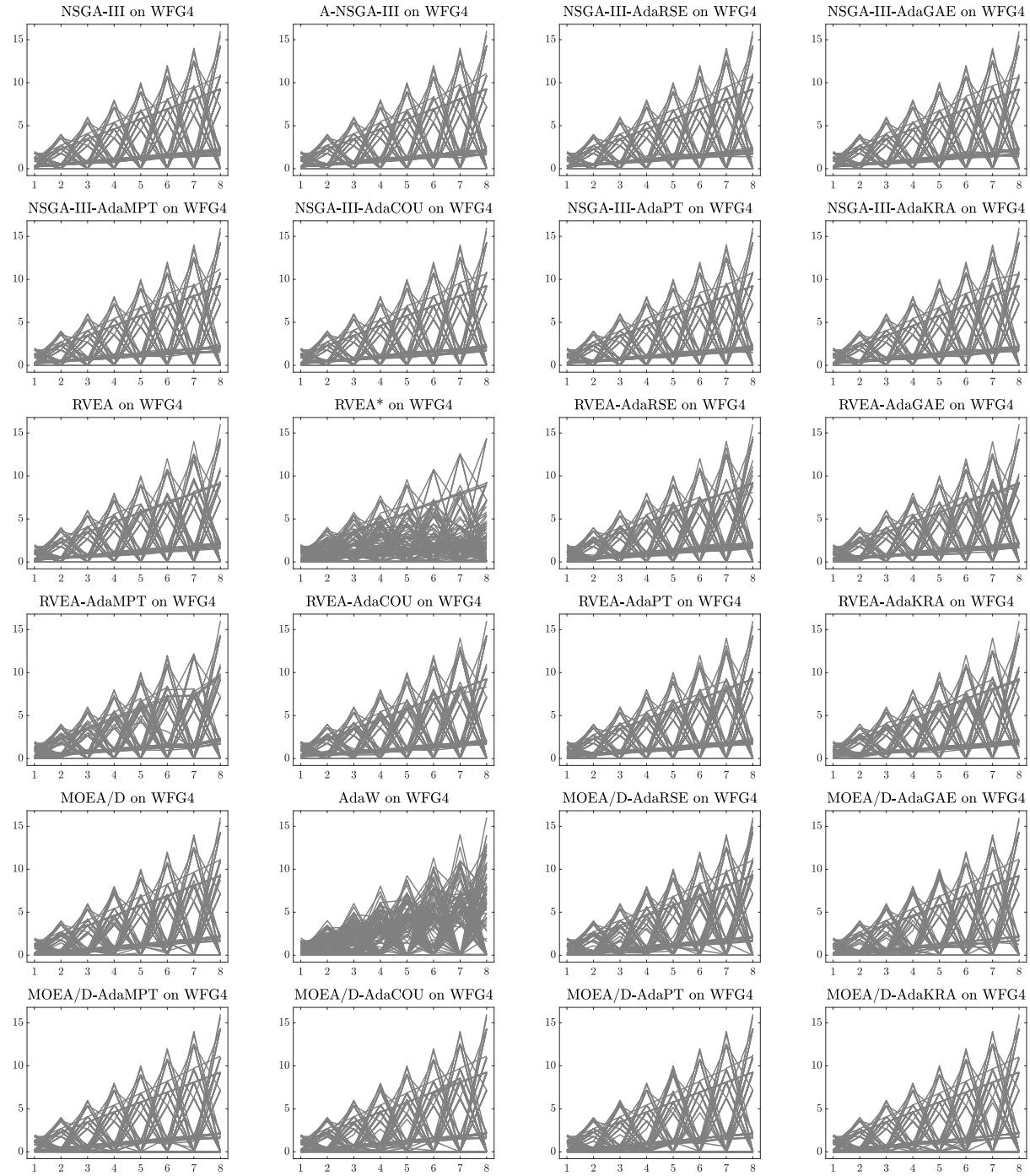


Figure 23: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG4 with 8 objective functions.

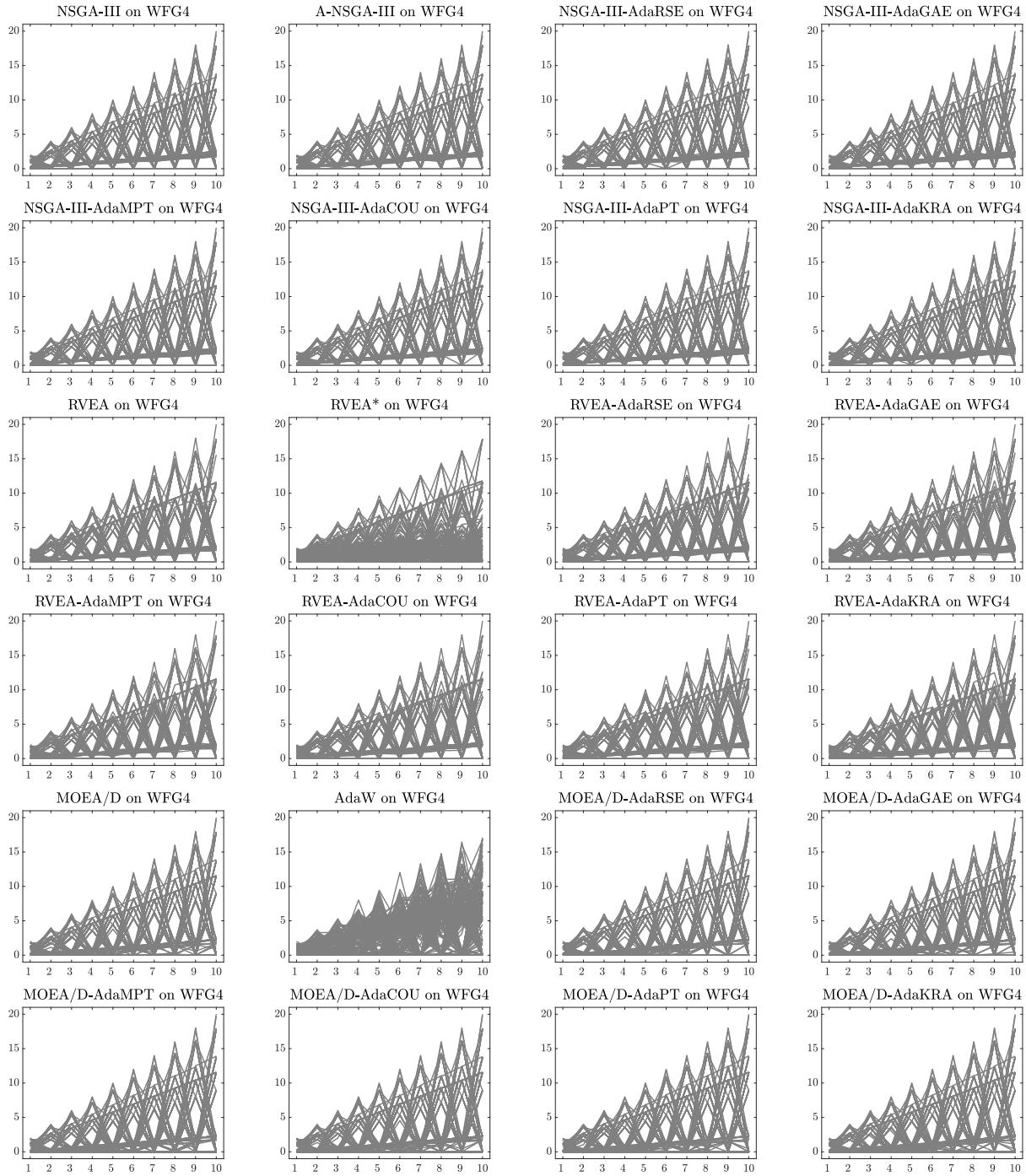


Figure 24: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG4 with 10 objective functions.

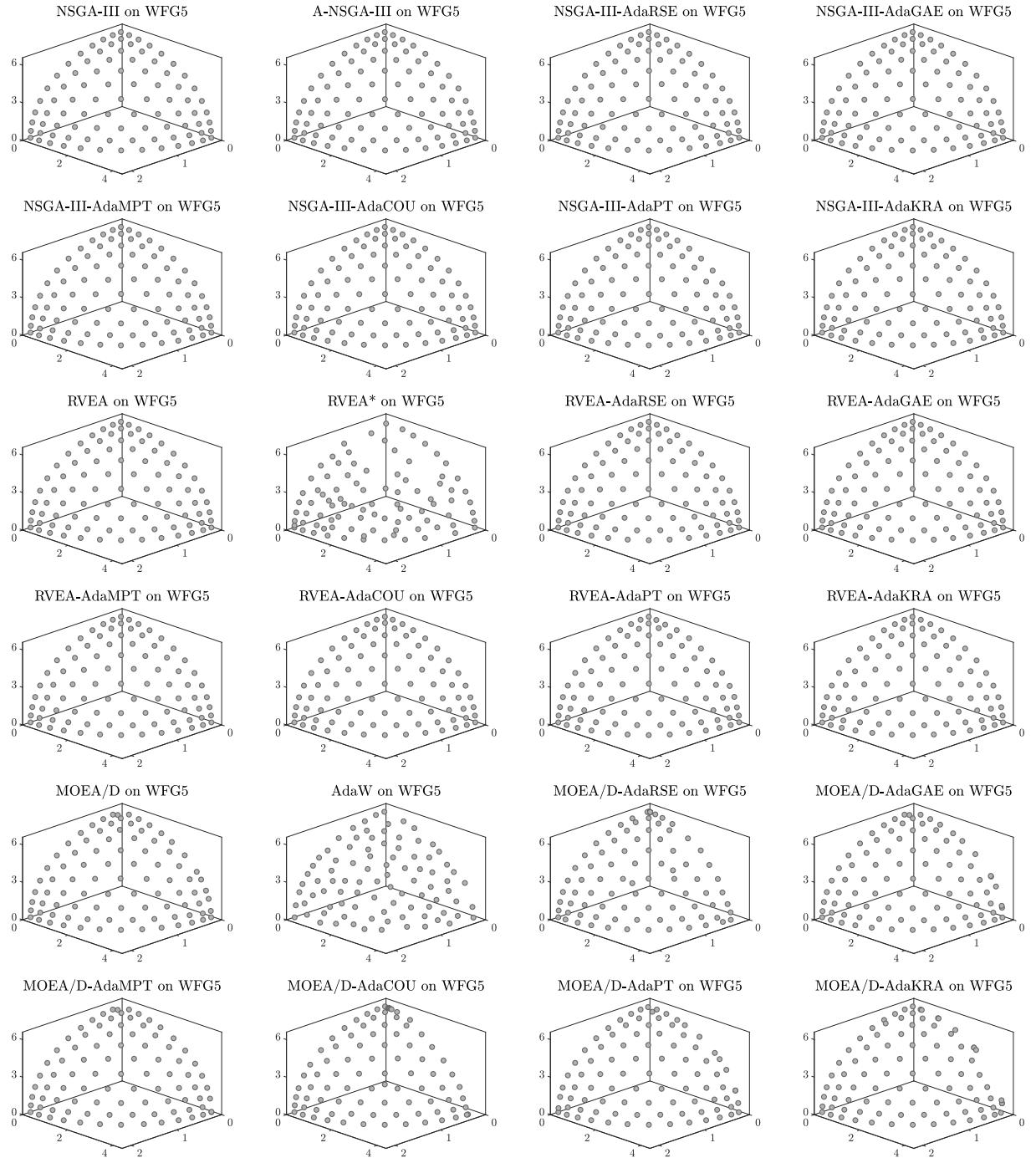


Figure 25: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG5 with 3 objective functions.

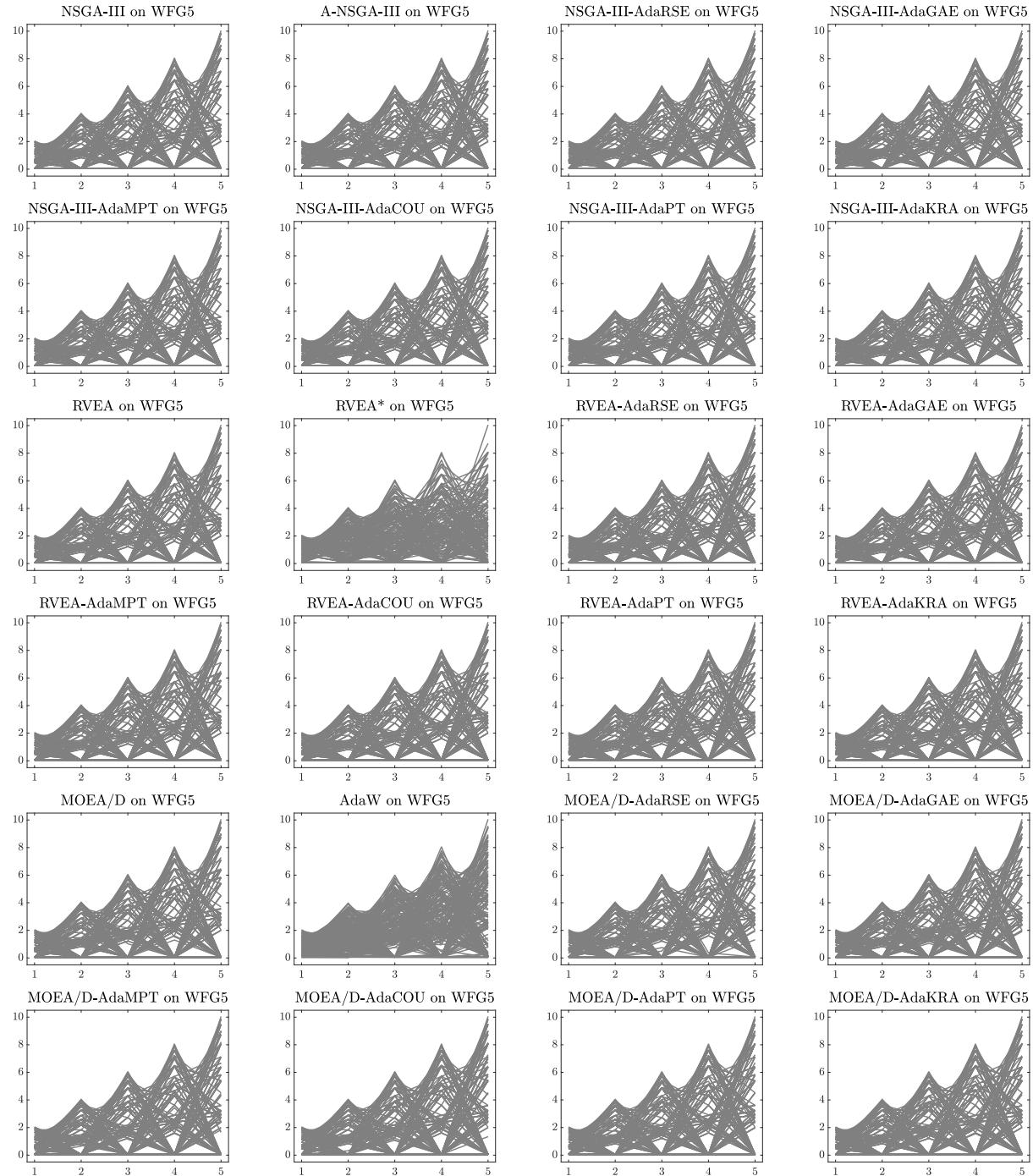


Figure 26: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG5 with 5 objective functions.

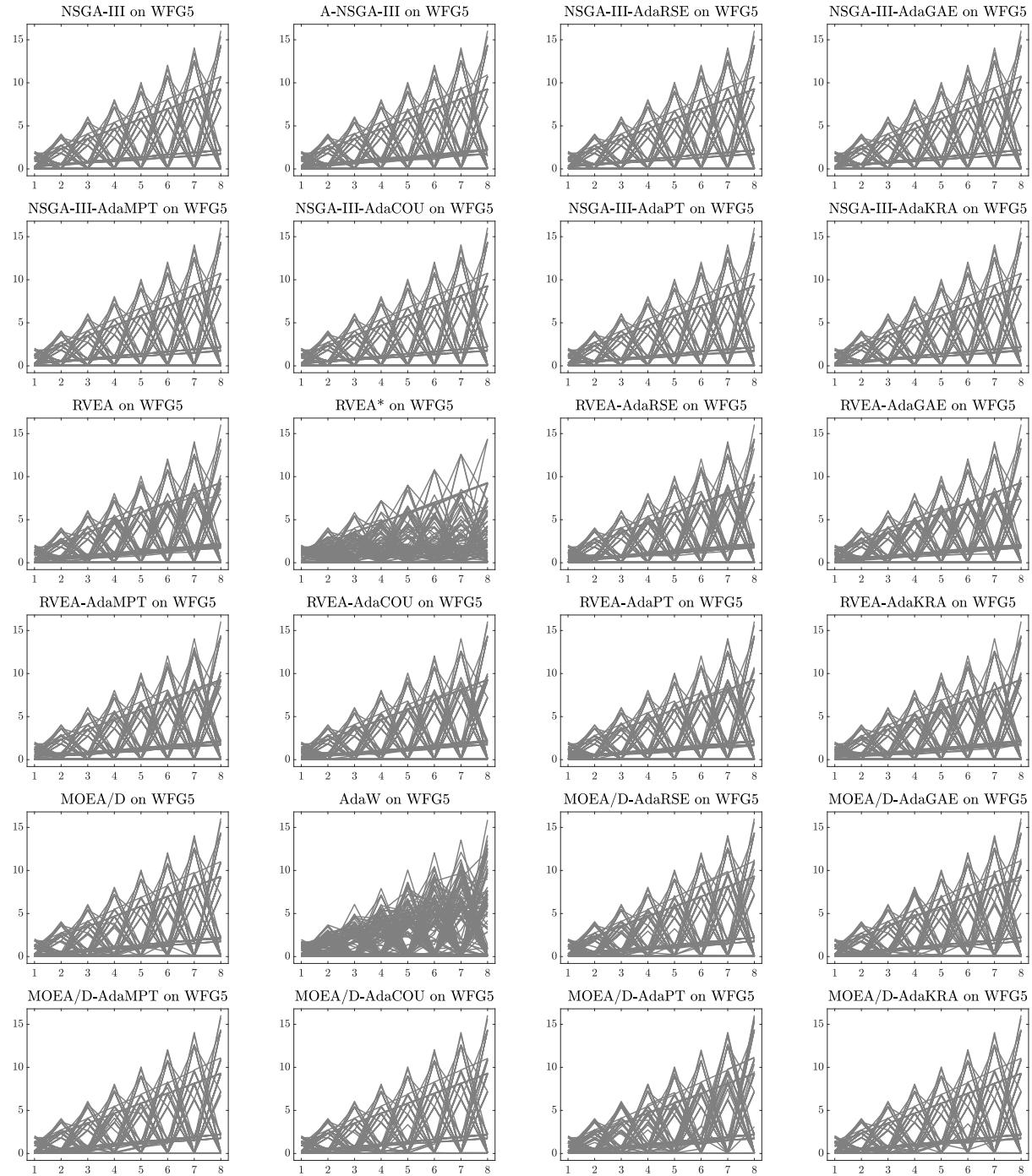


Figure 27: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG5 with 8 objective functions.

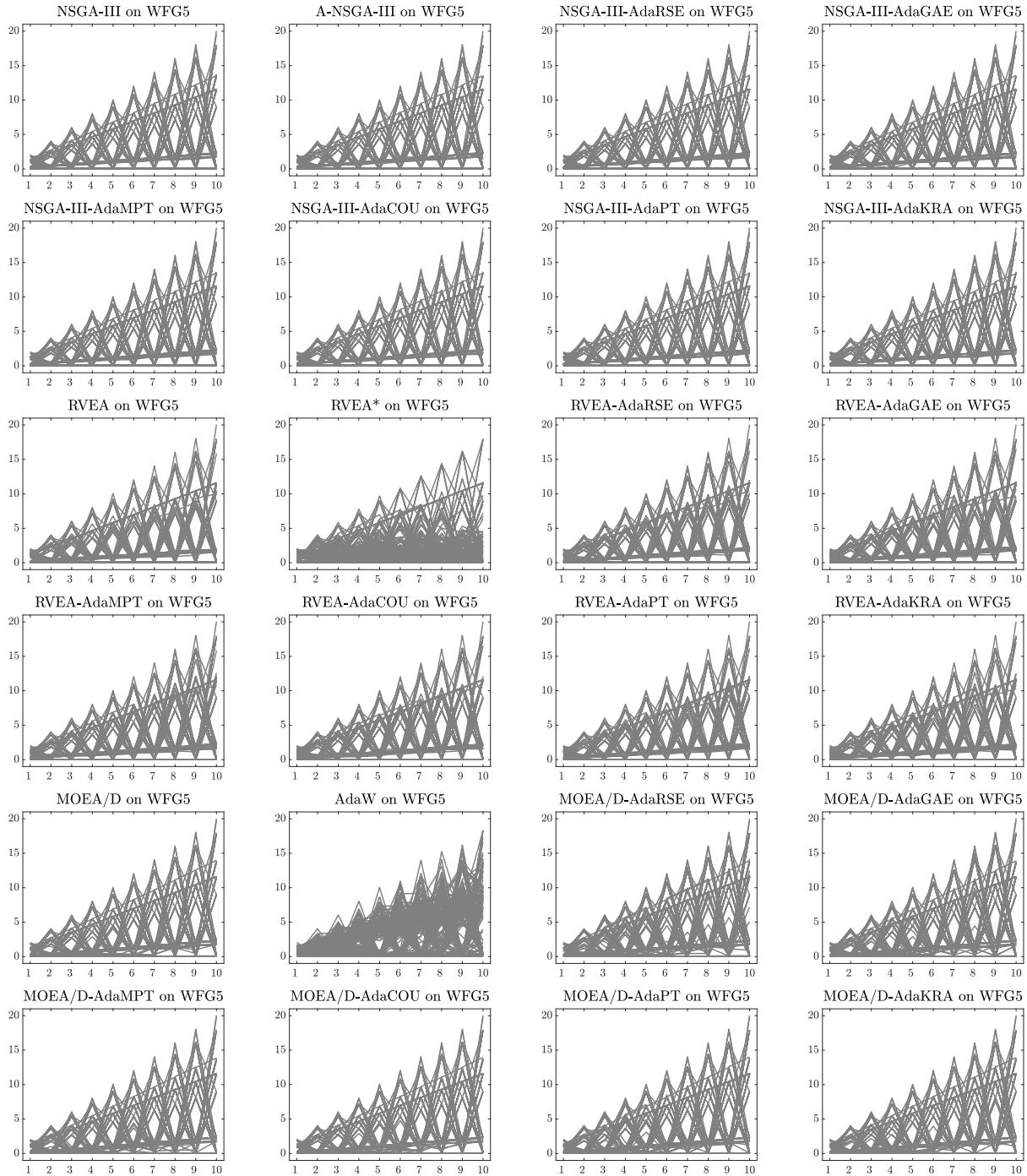


Figure 28: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG5 with 10 objective functions.

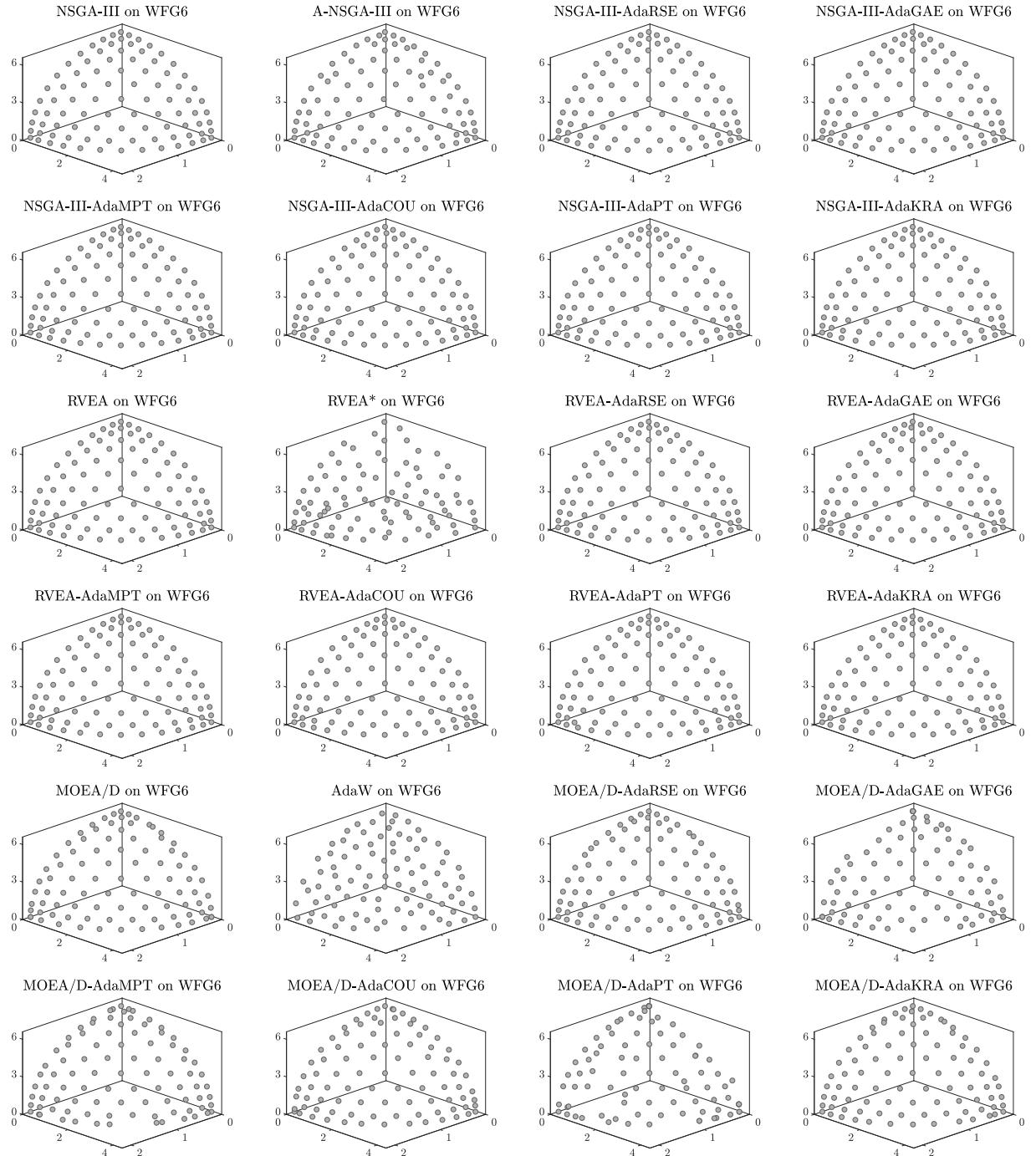


Figure 29: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG6 with 3 objective functions.

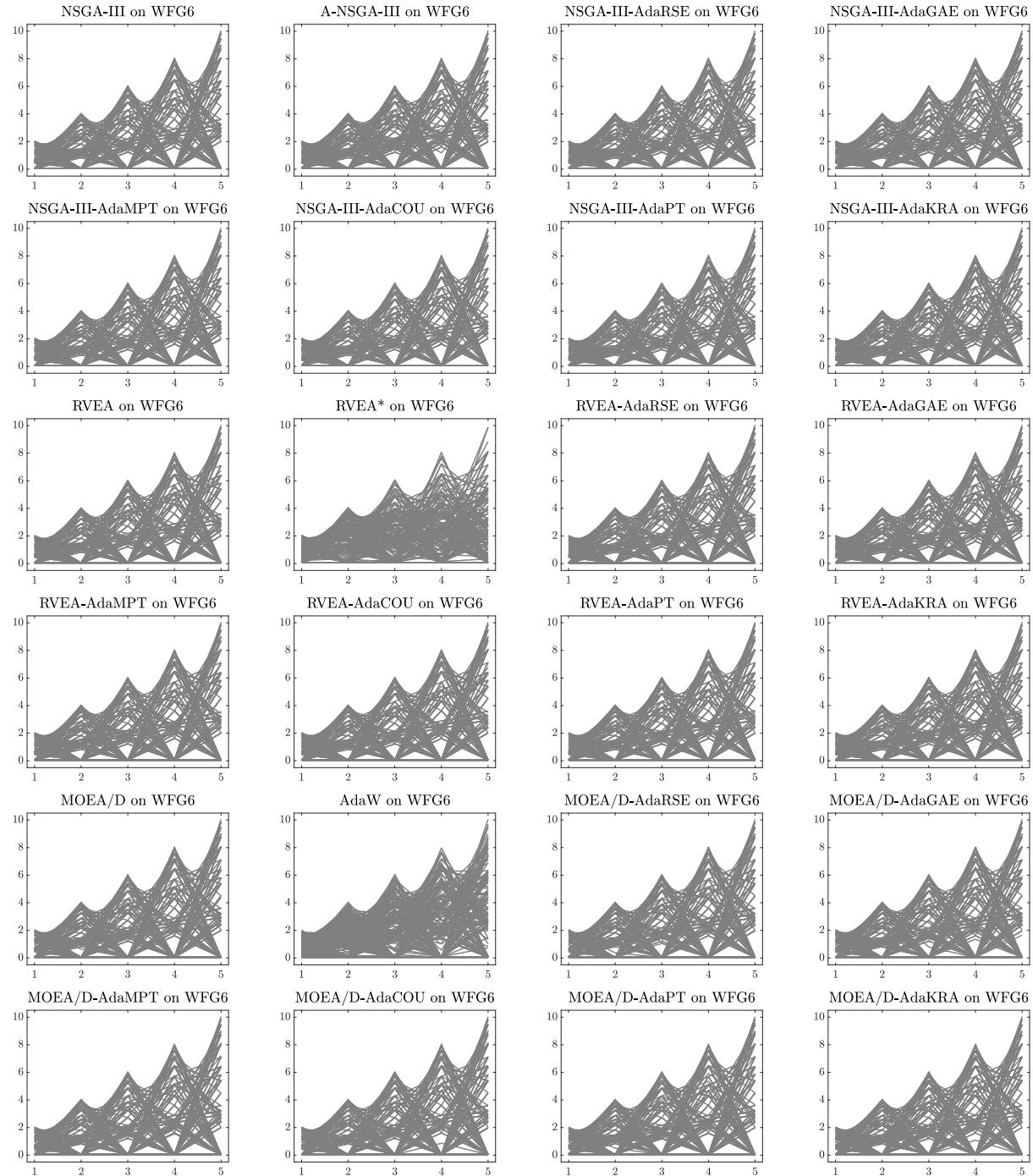


Figure 30: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG6 with 5 objective functions.

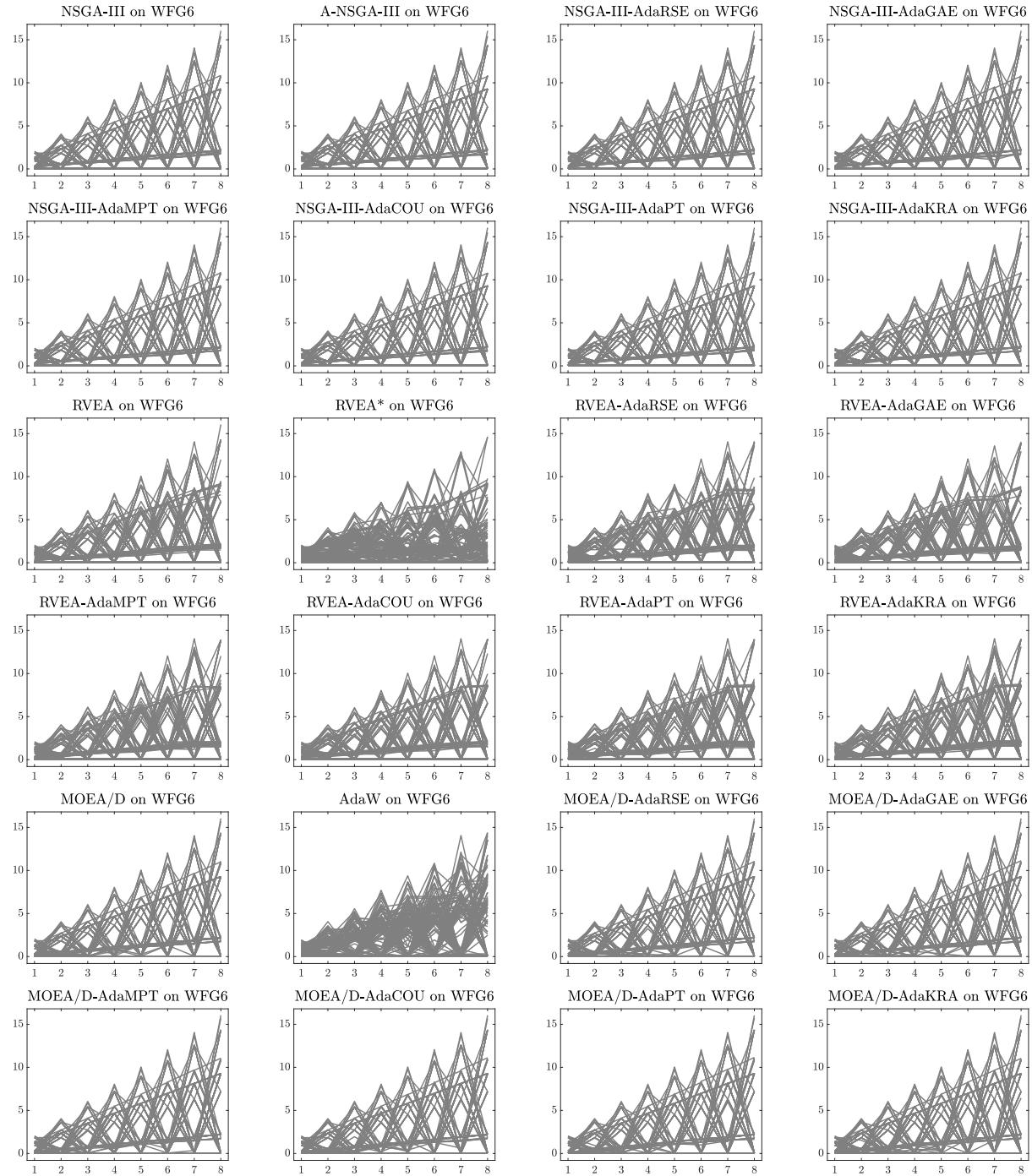


Figure 31: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG6 with 8 objective functions.

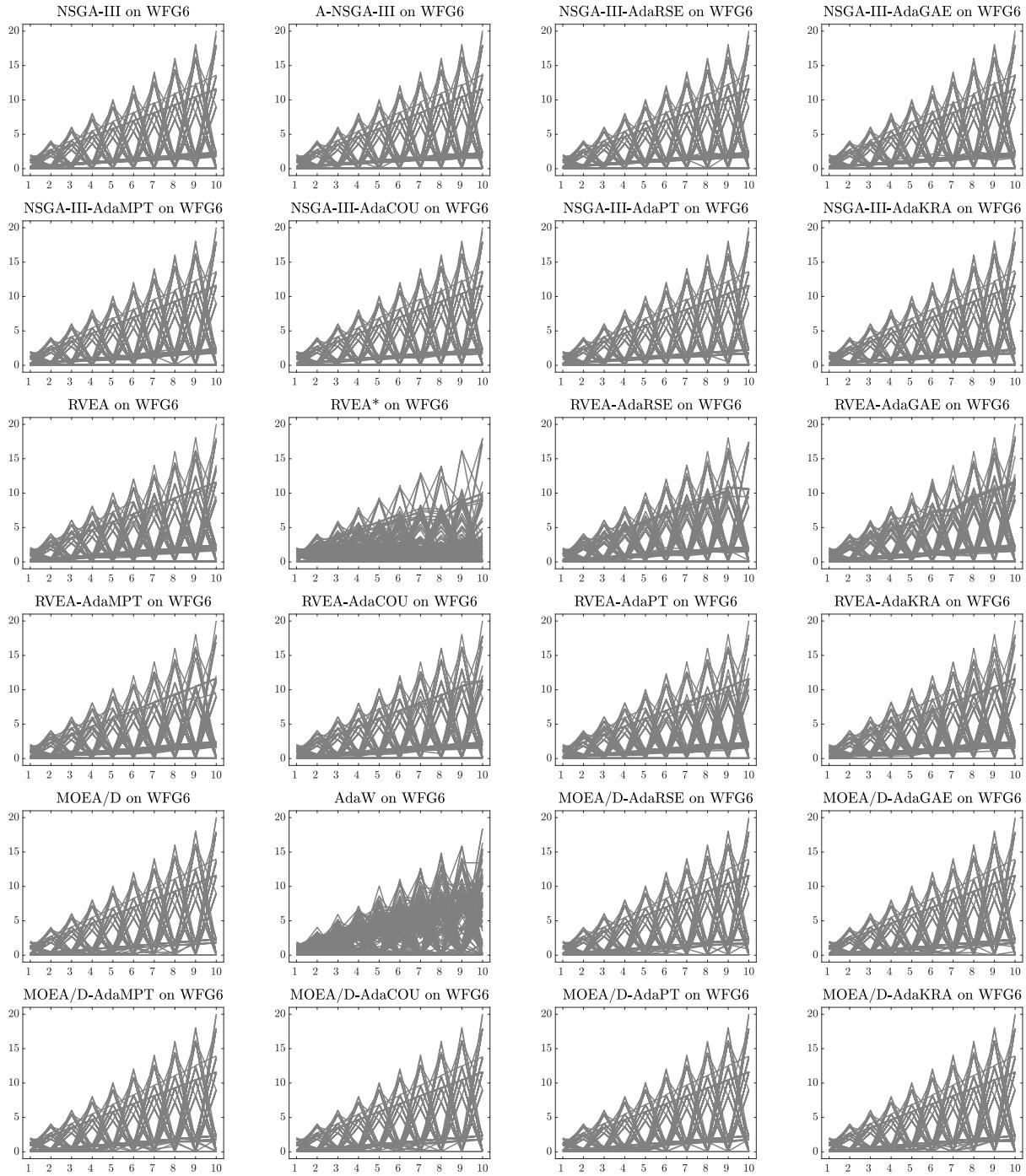


Figure 32: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG6 with 10 objective functions.

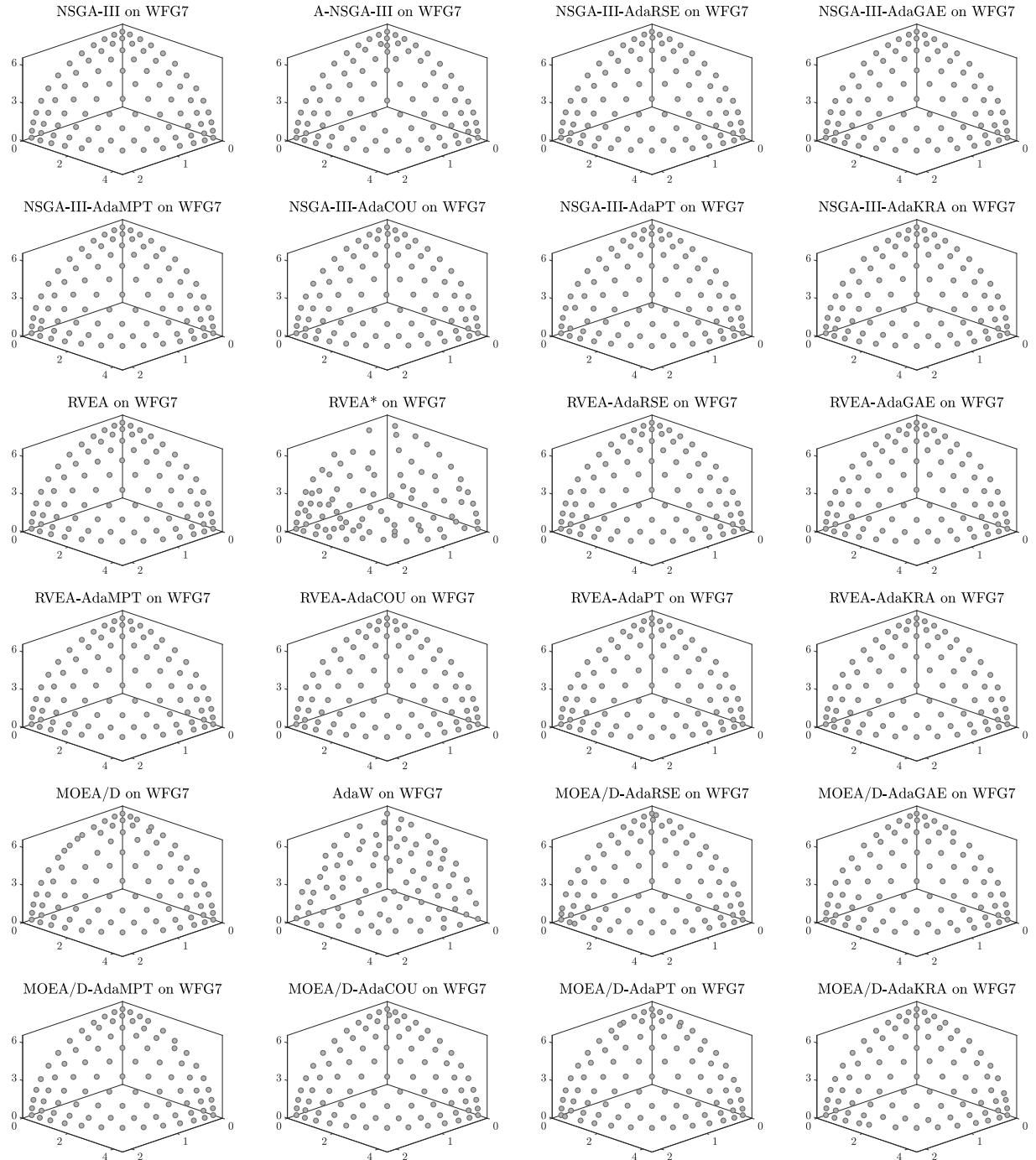


Figure 33: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG7 with 3 objective functions.

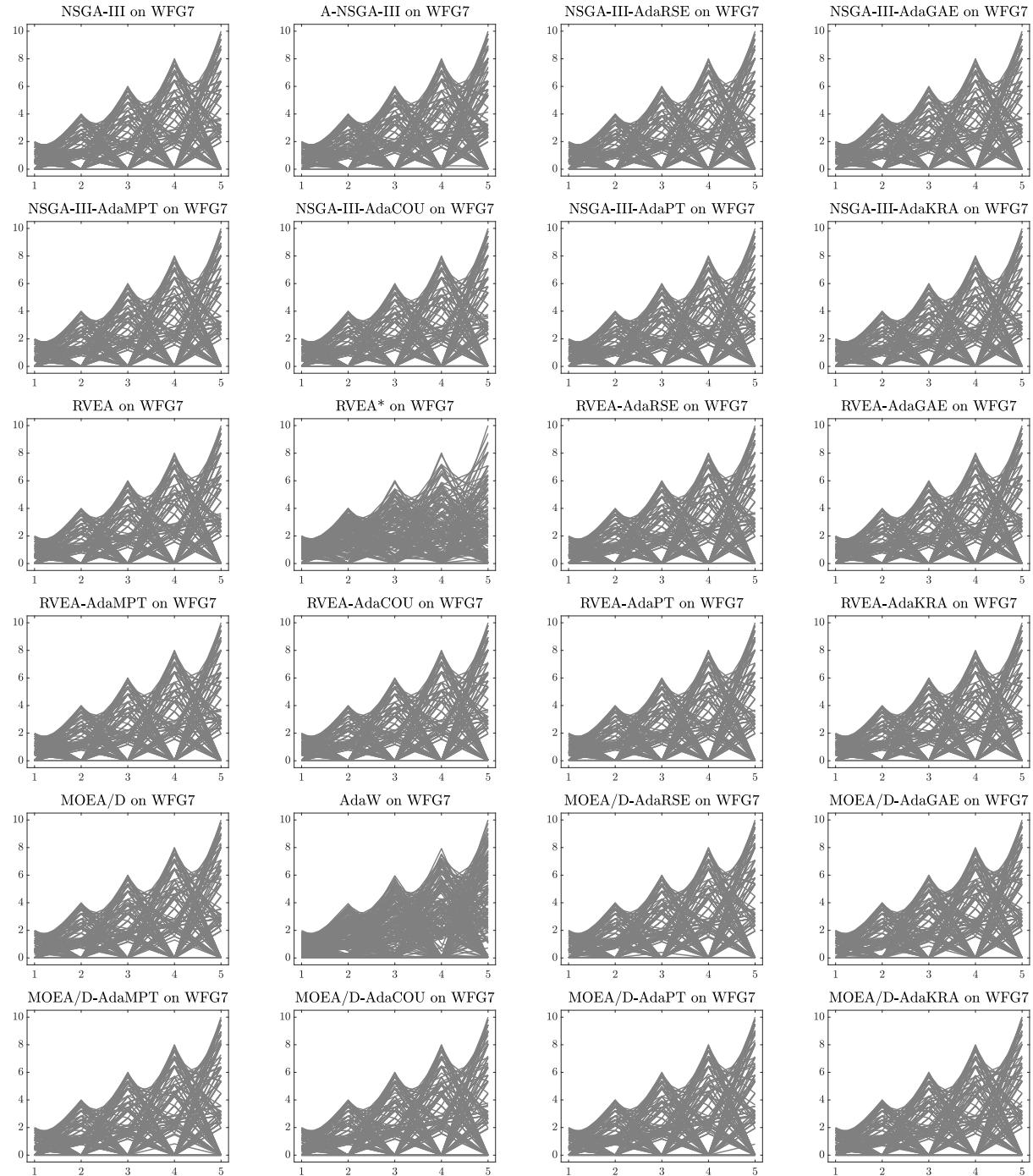


Figure 34: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG7 with 5 objective functions.

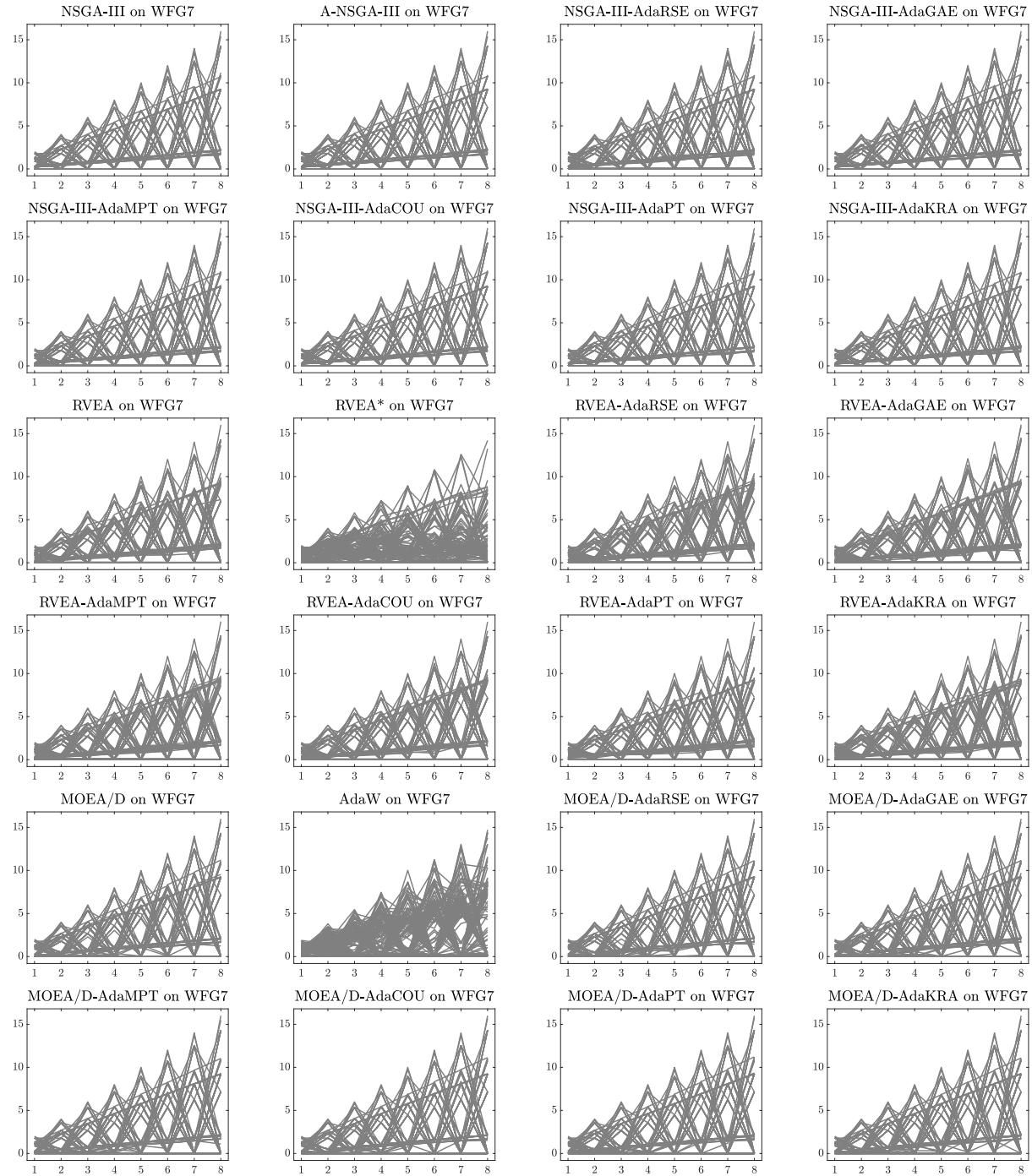


Figure 35: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG7 with 8 objective functions.

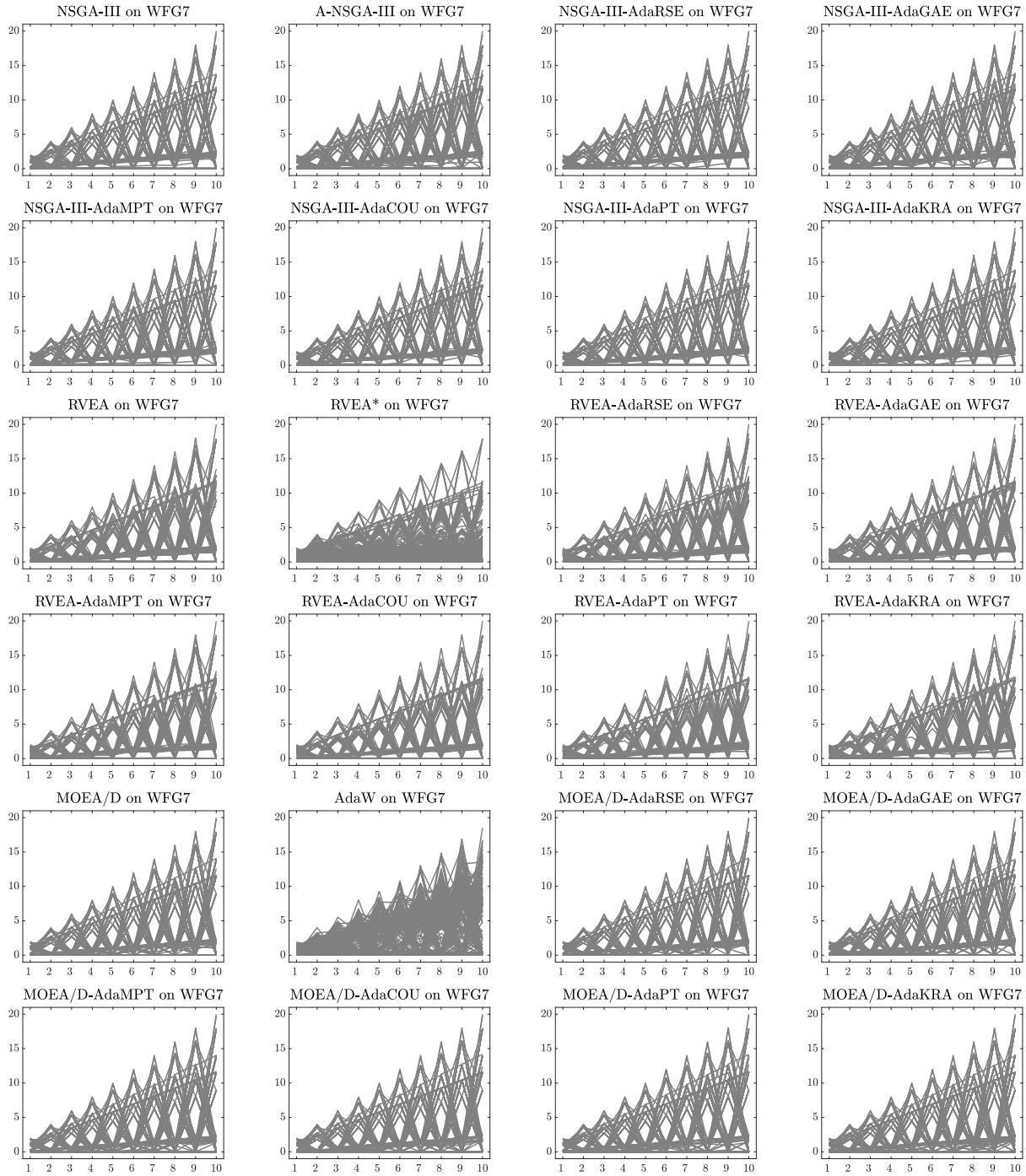


Figure 36: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG7 with 10 objective functions.

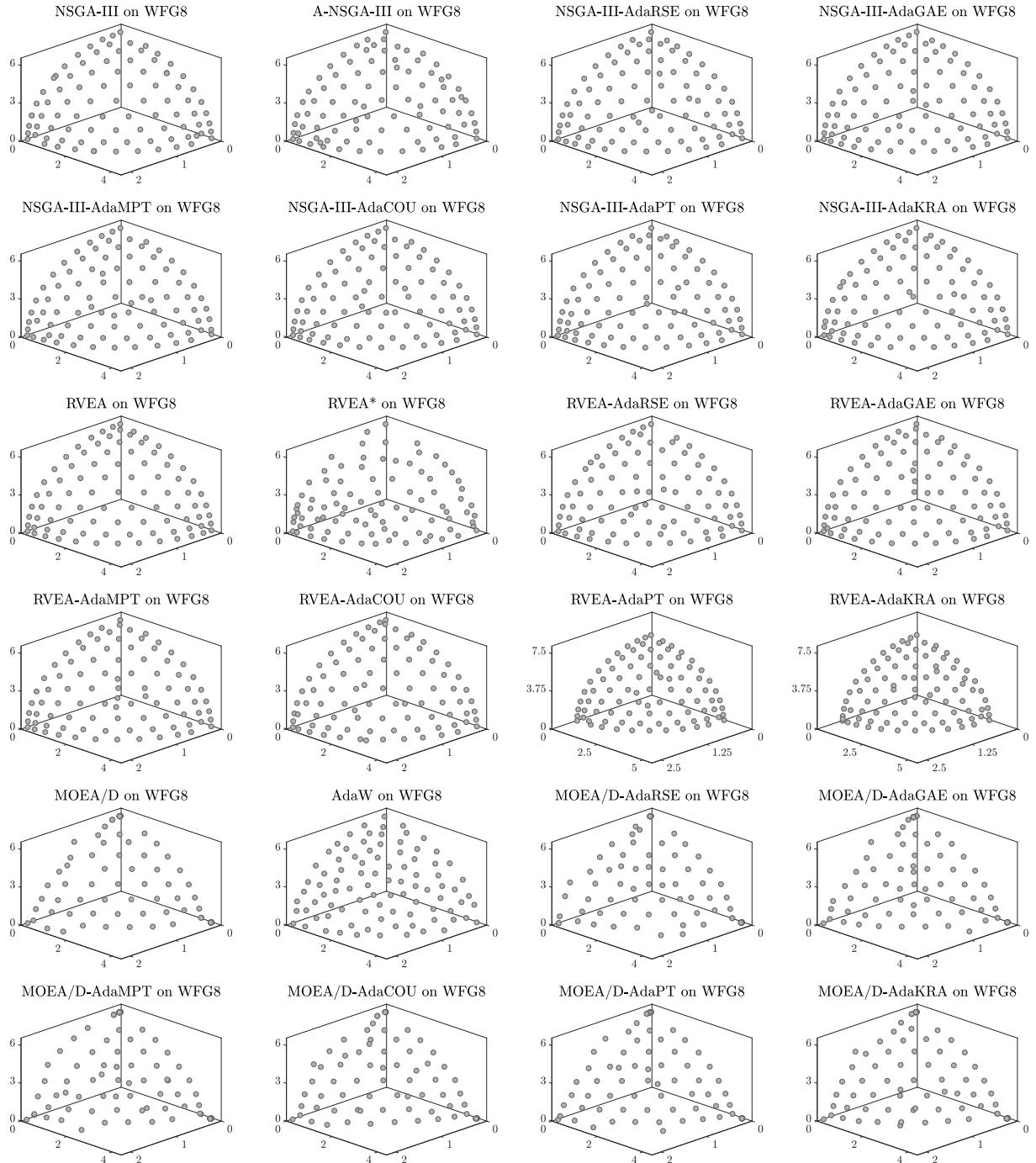


Figure 37: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG8 with 3 objective functions.

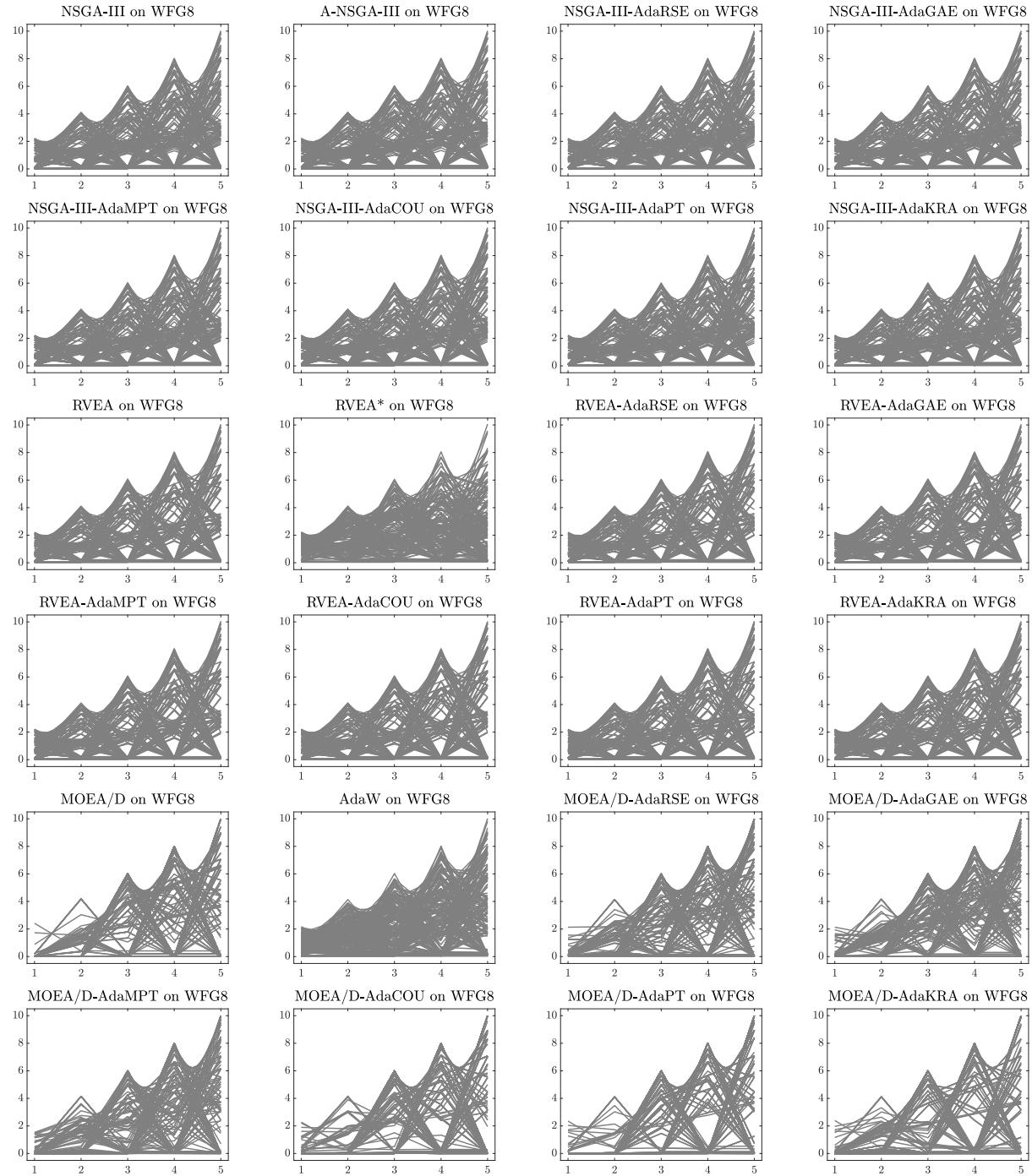


Figure 38: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG8 with 5 objective functions.

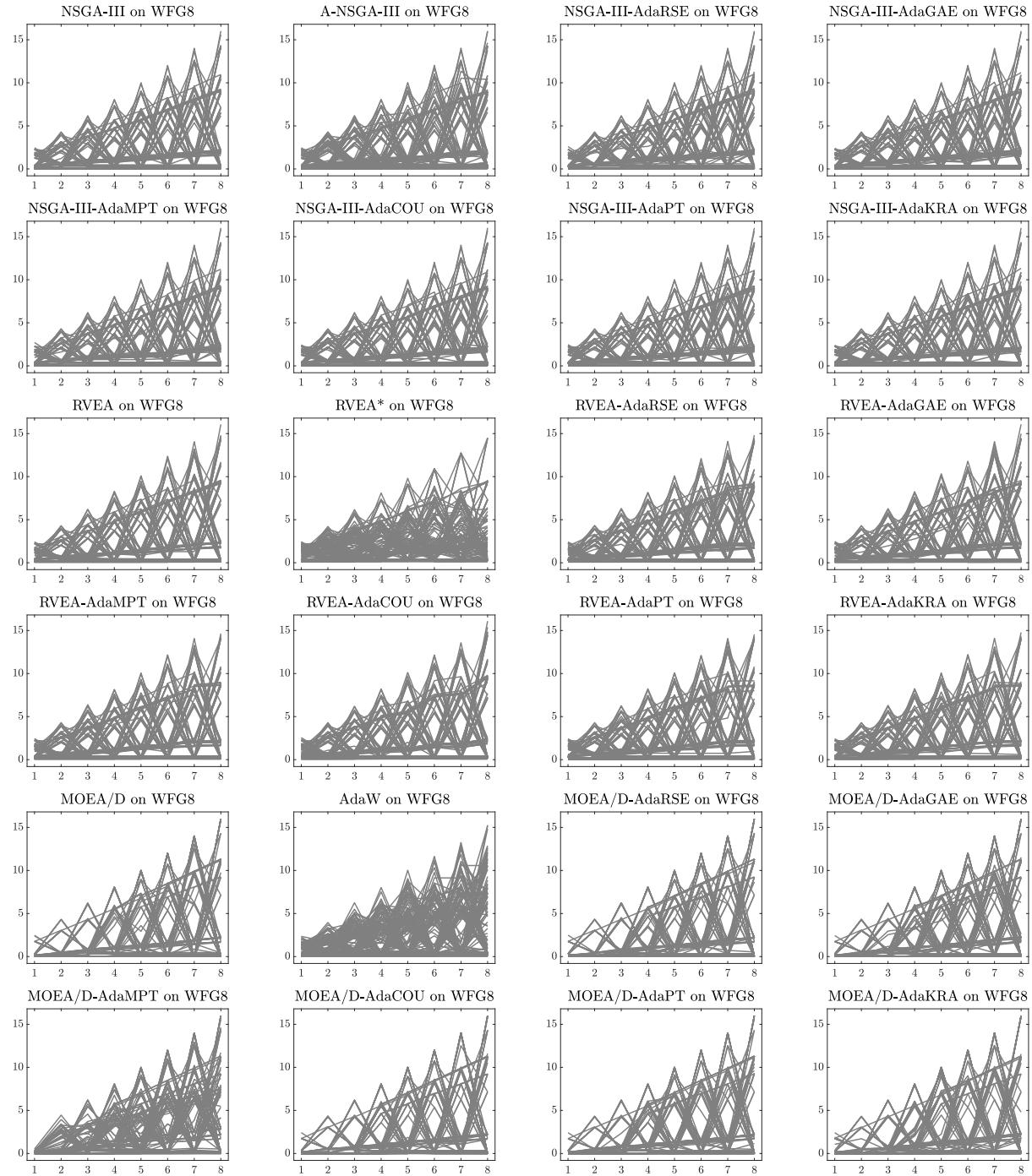


Figure 39: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG8 with 8 objective functions.

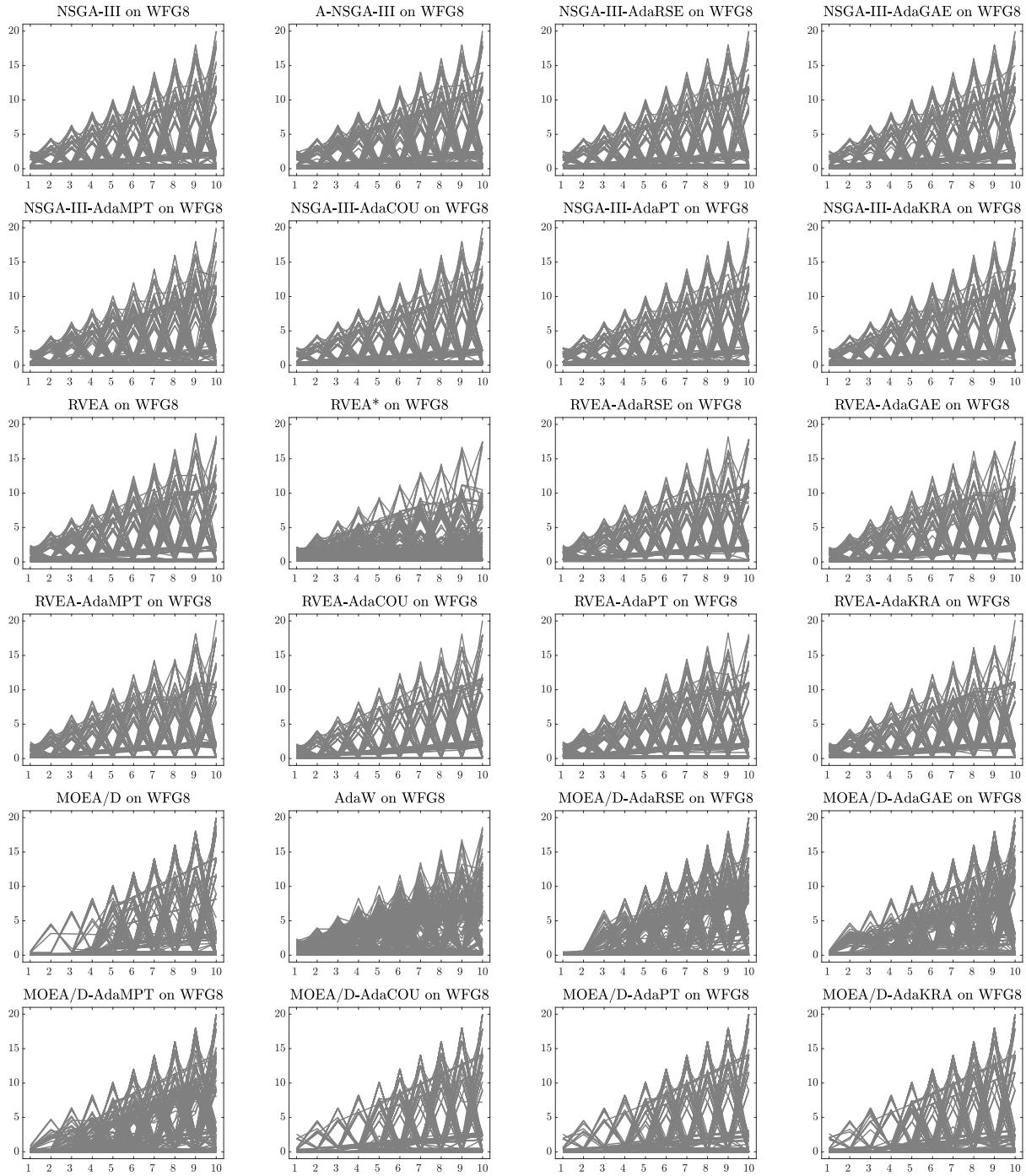


Figure 40: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG8 with 10 objective functions.

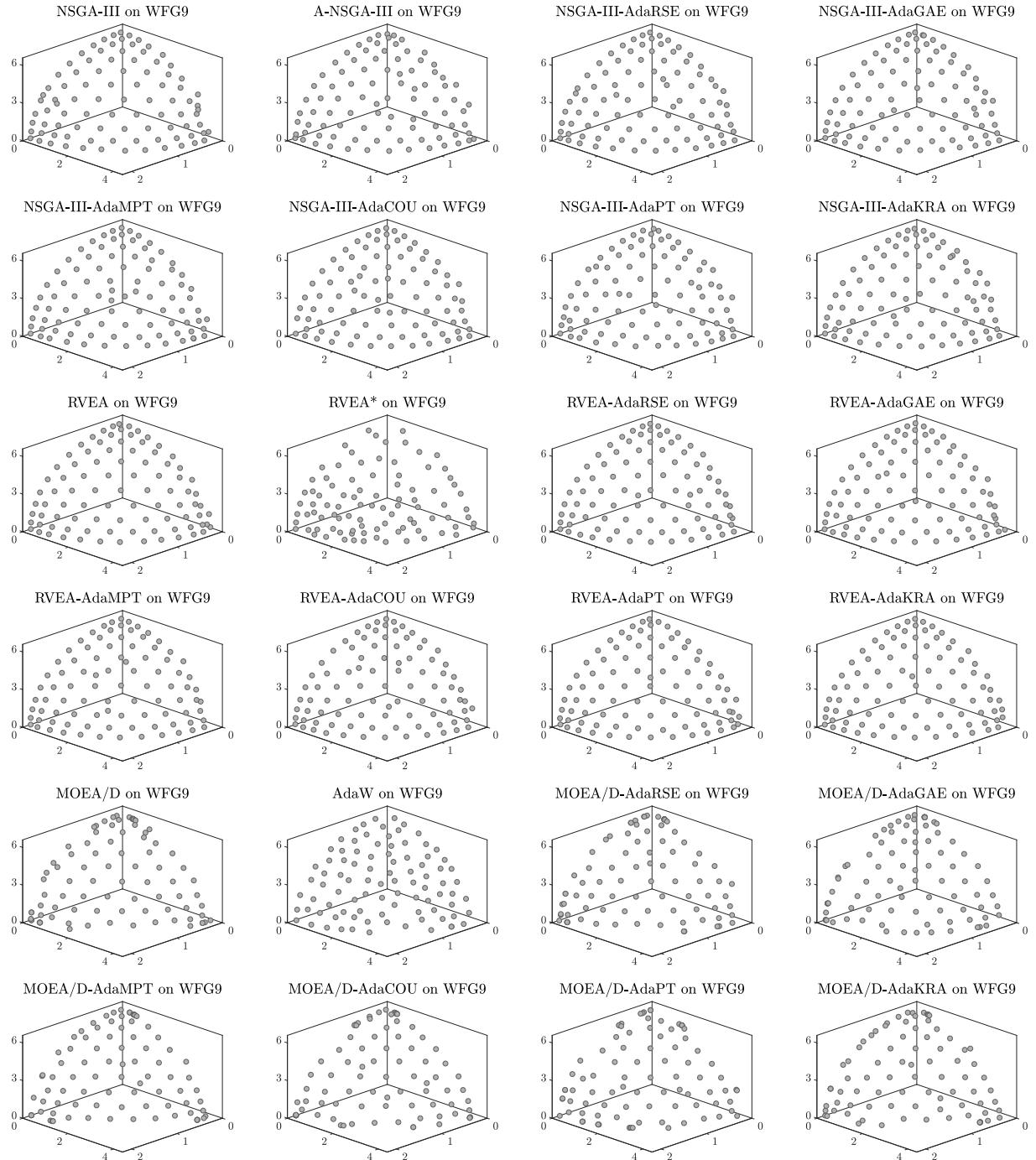


Figure 41: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG9 with 3 objective functions.

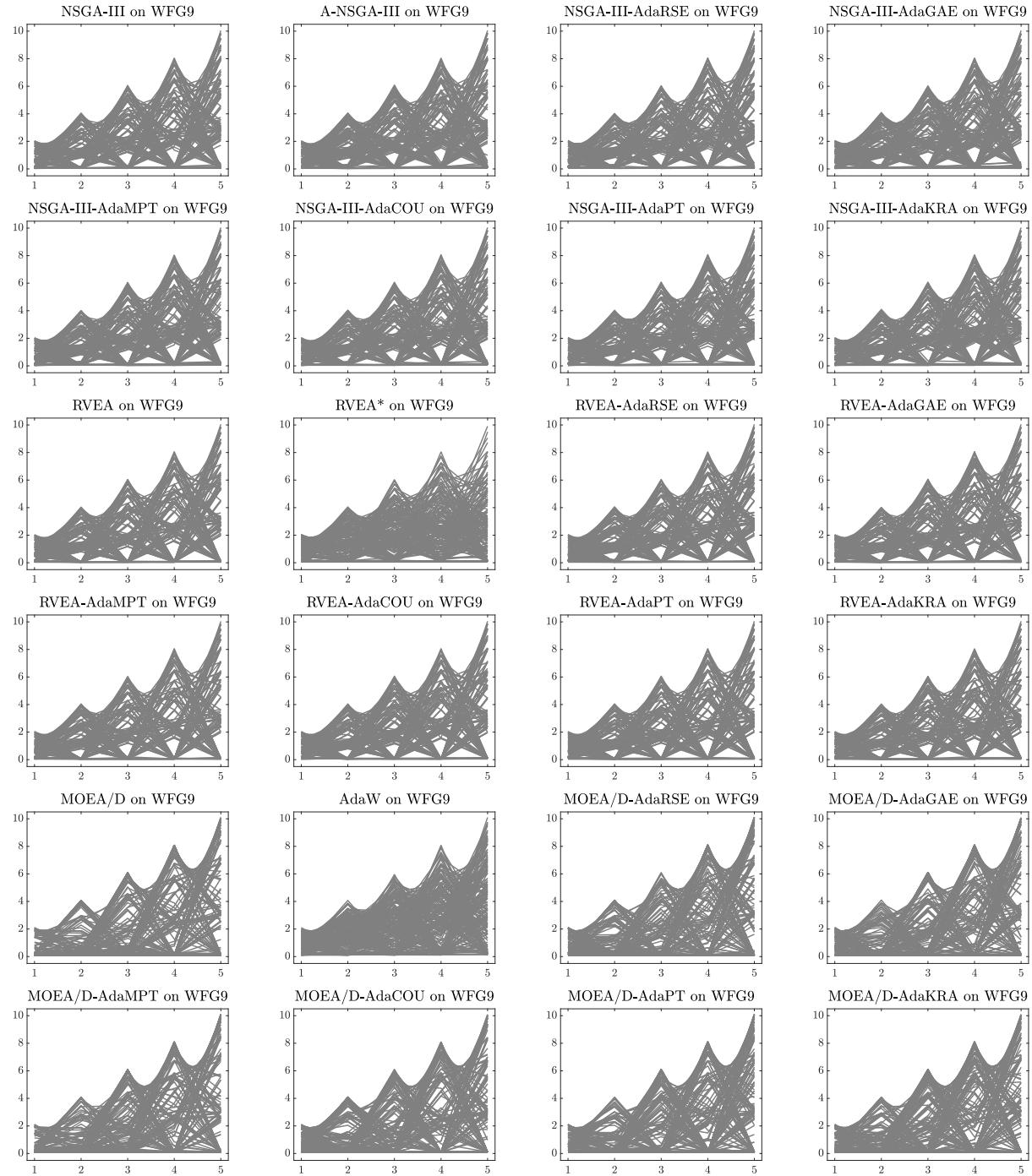


Figure 42: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG9 with 5 objective functions.

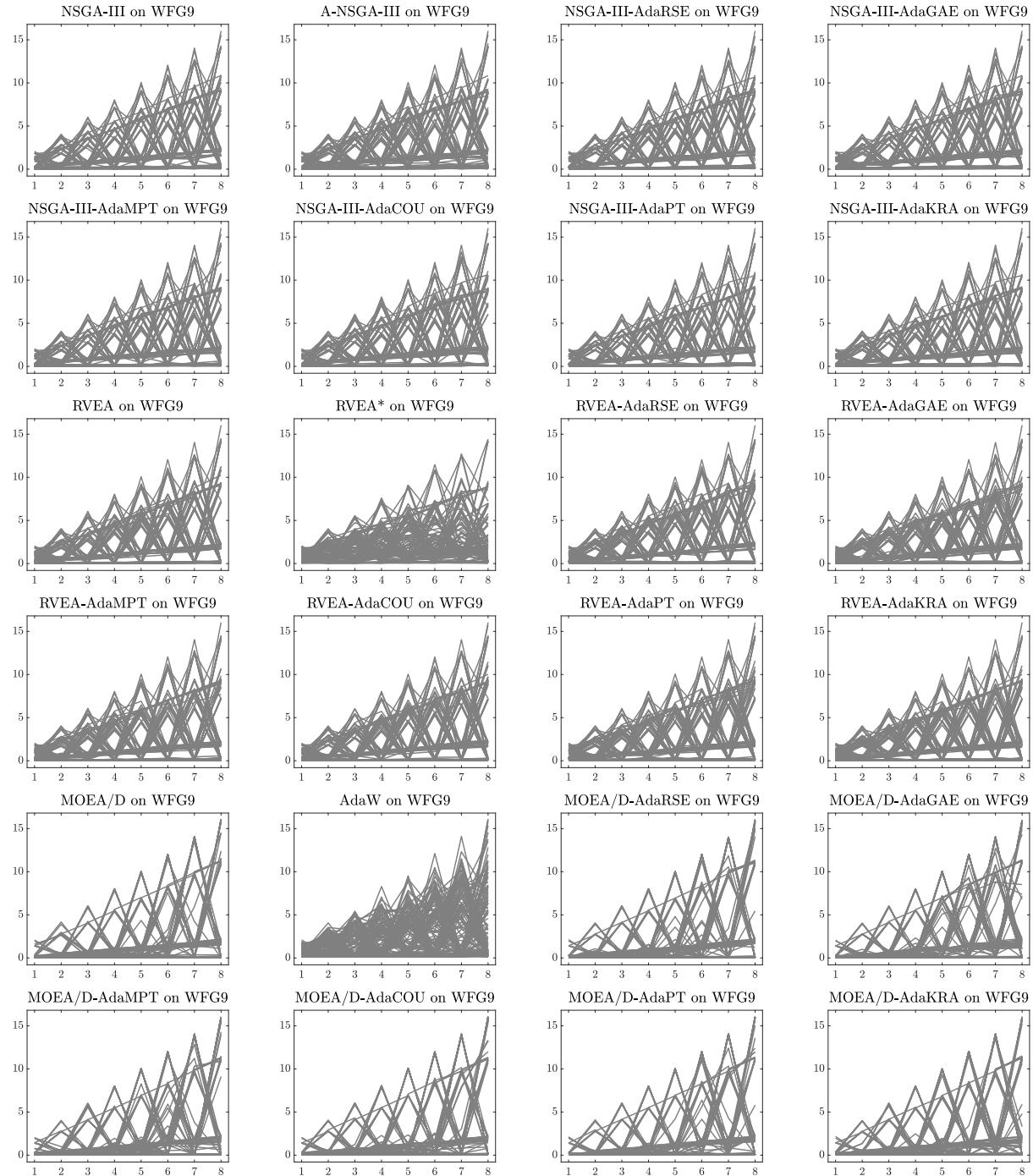


Figure 43: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG9 with 8 objective functions.

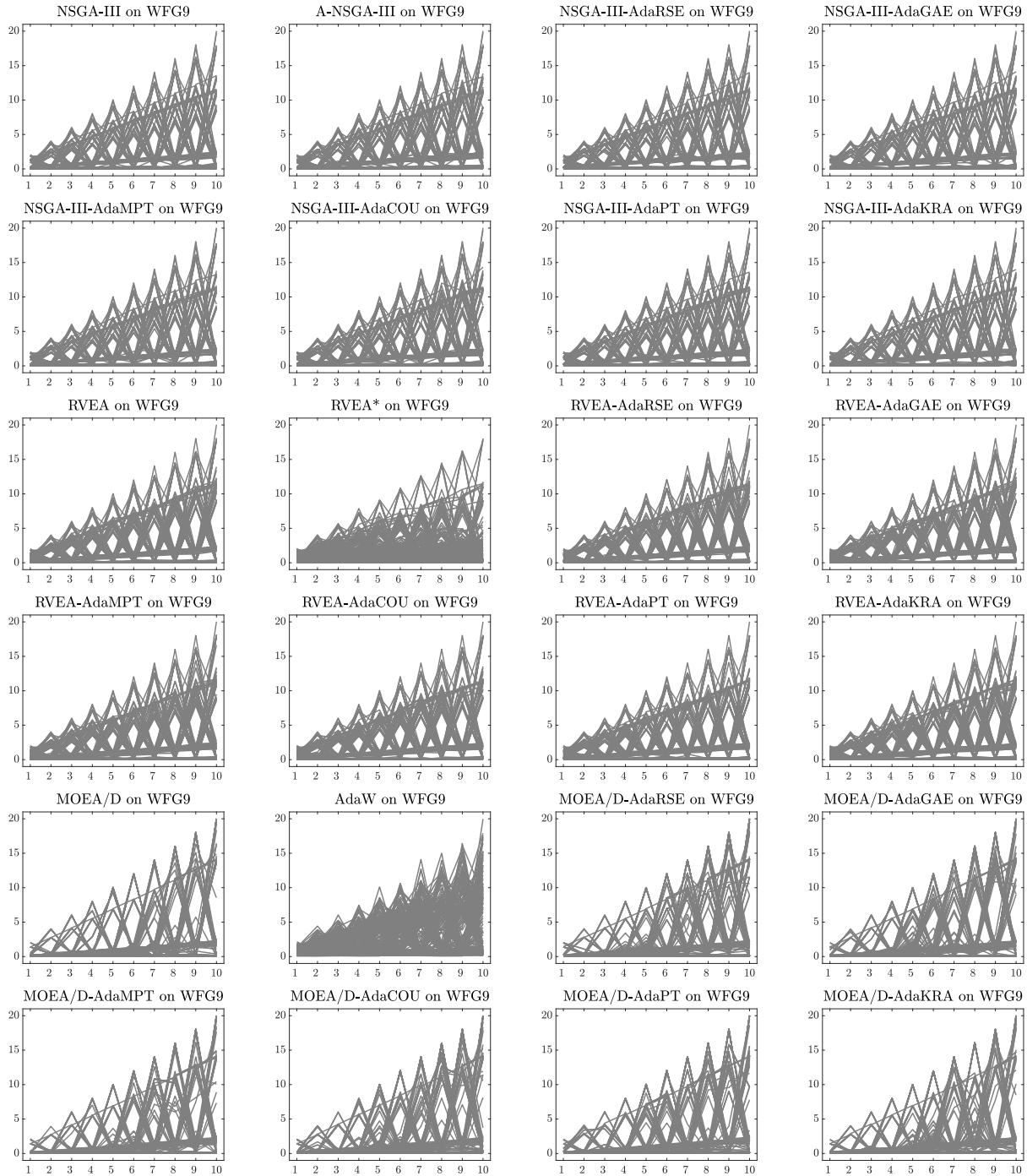


Figure 44: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG9 with 10 objective functions.

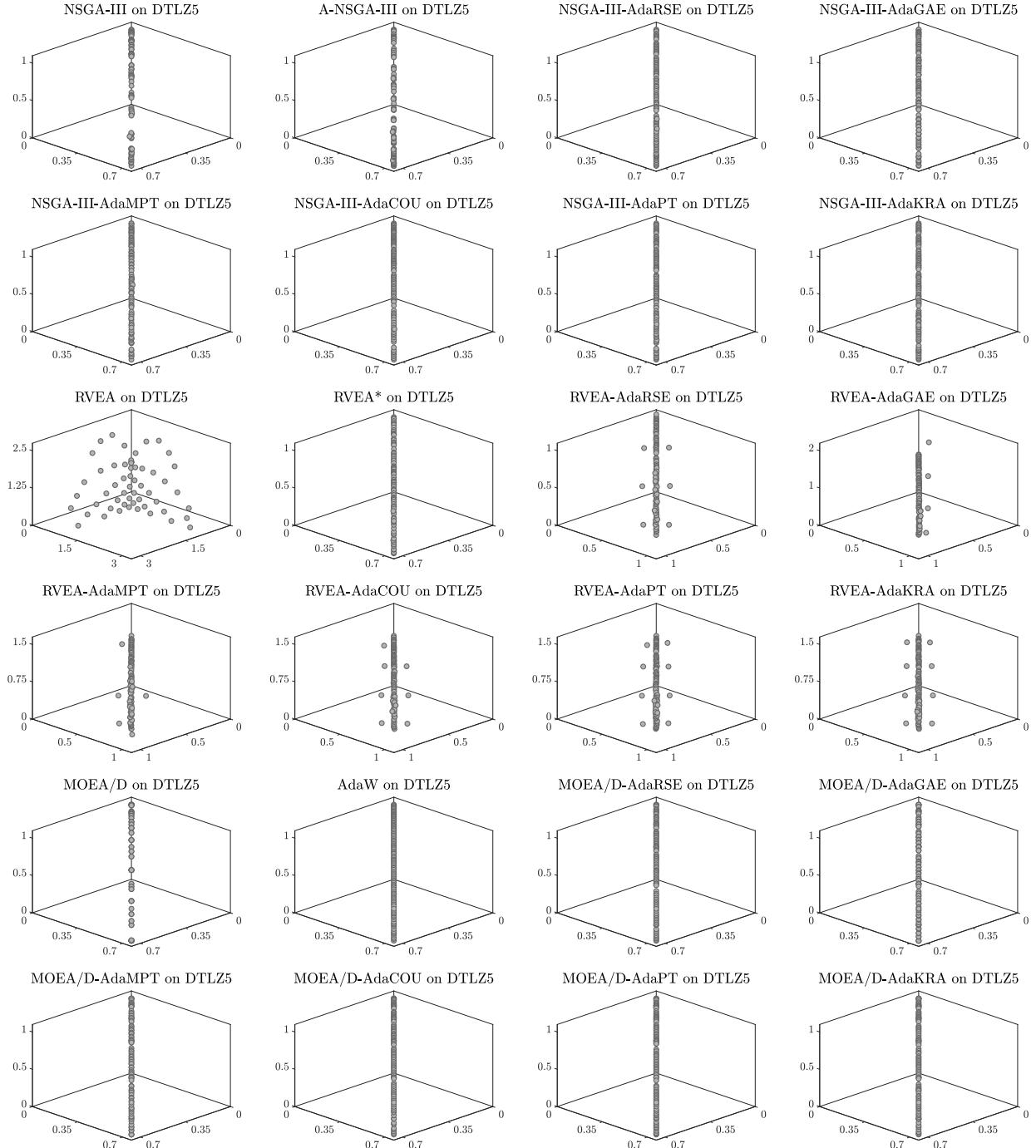


Figure 45: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ5 with 3 objective functions.

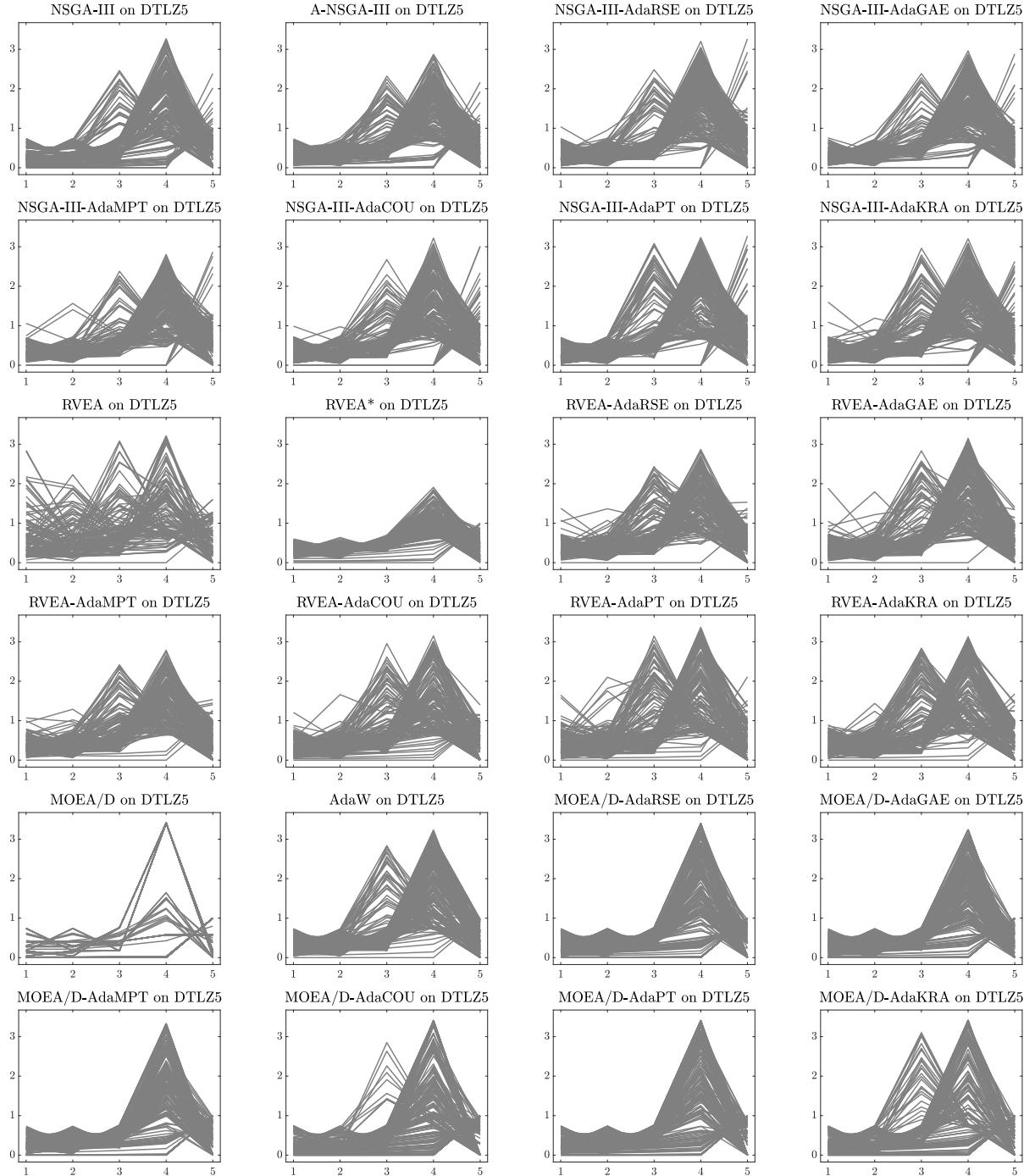


Figure 46: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ5 with 5 objective functions.

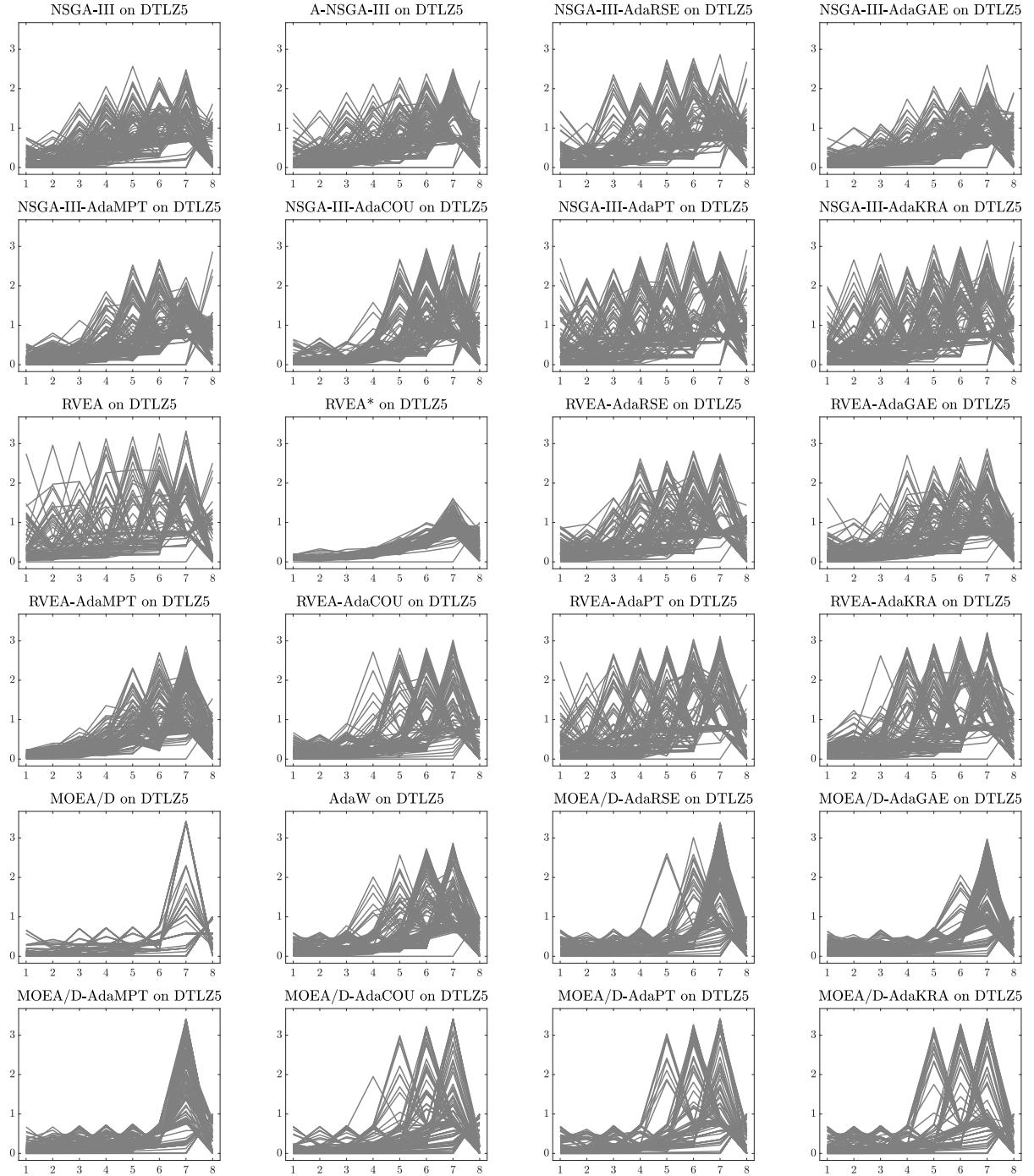


Figure 47: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ5 with 8 objective functions.

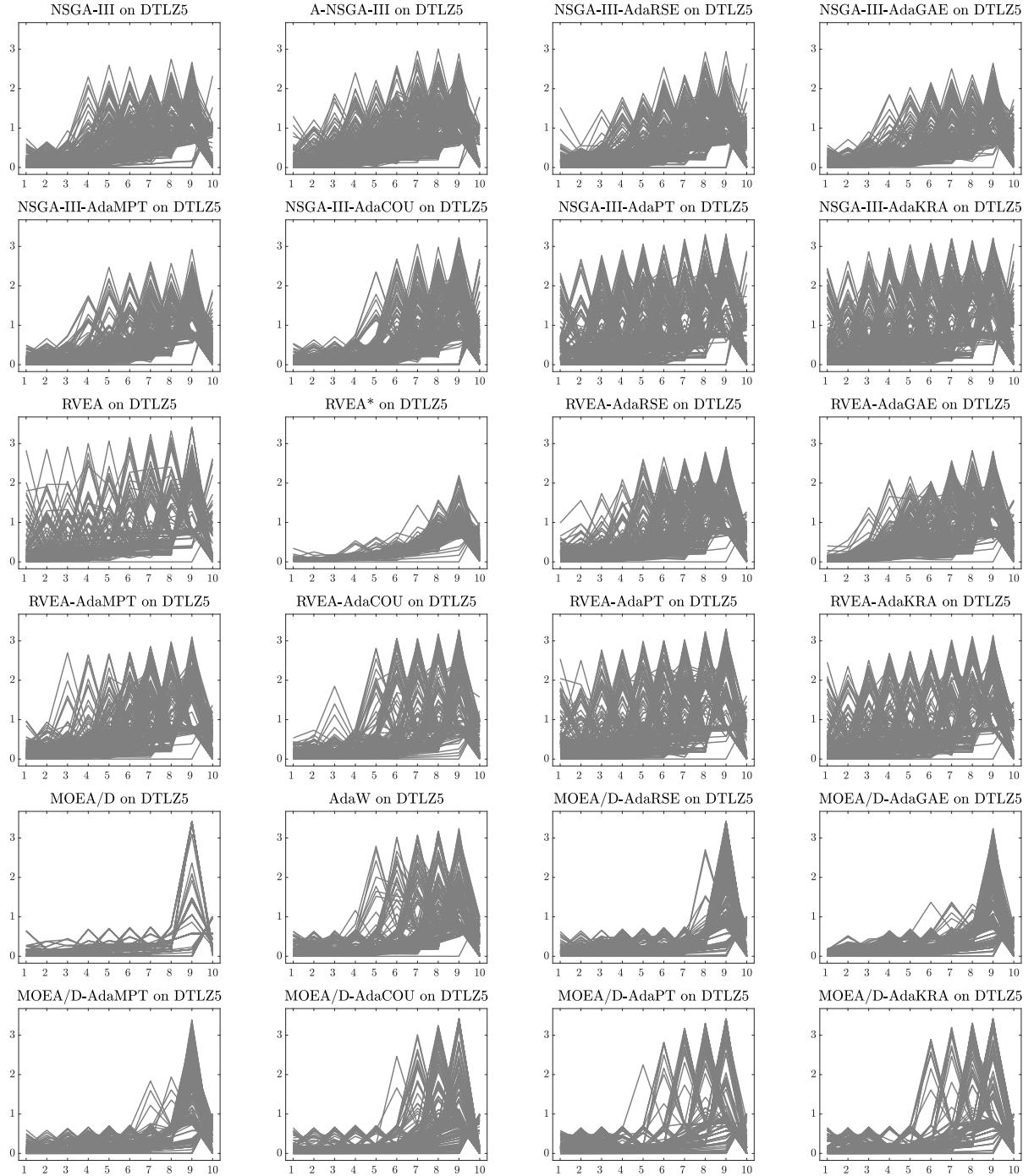


Figure 48: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ5 with 10 objective functions.

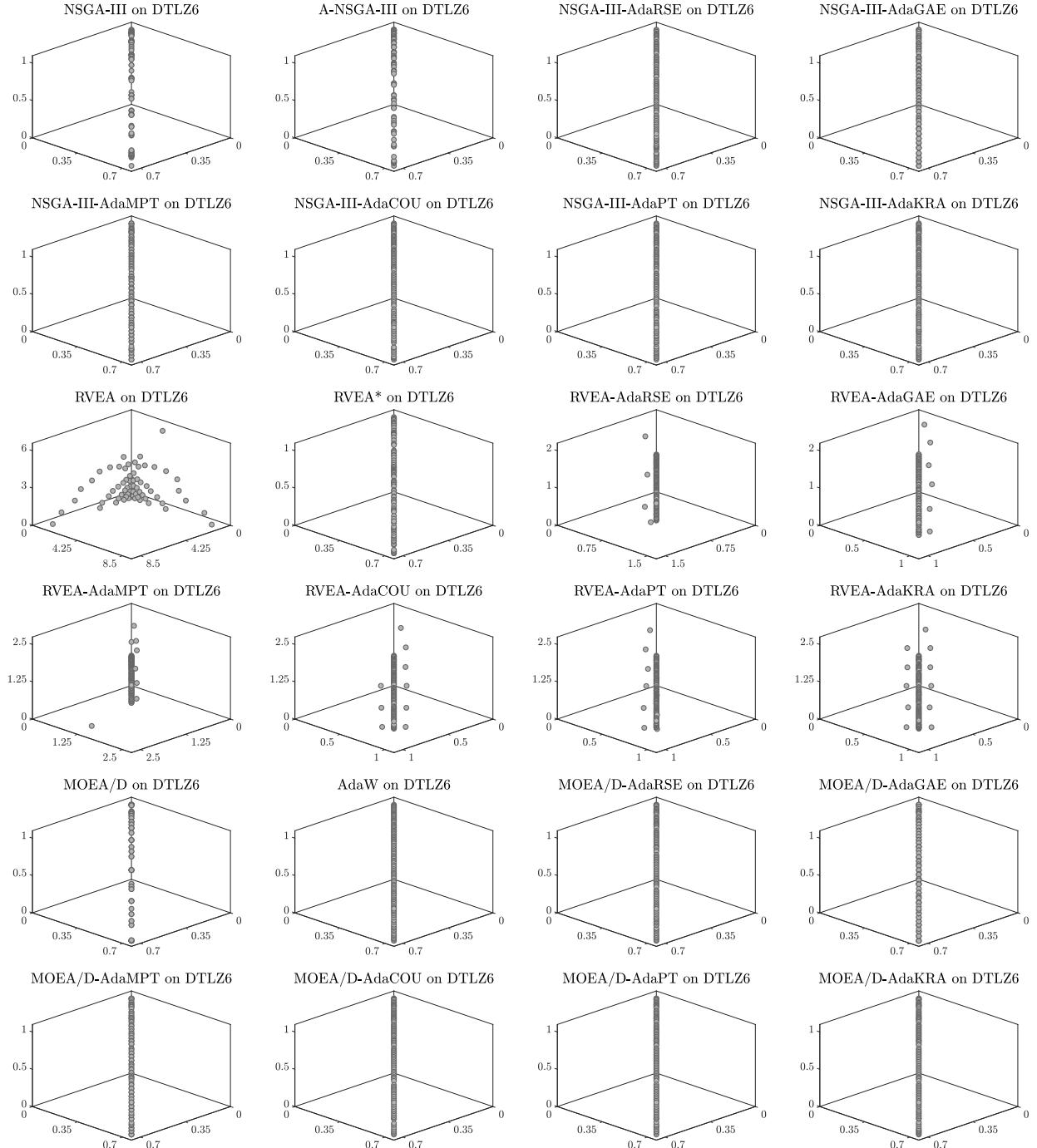


Figure 49: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ6 with 3 objective functions.

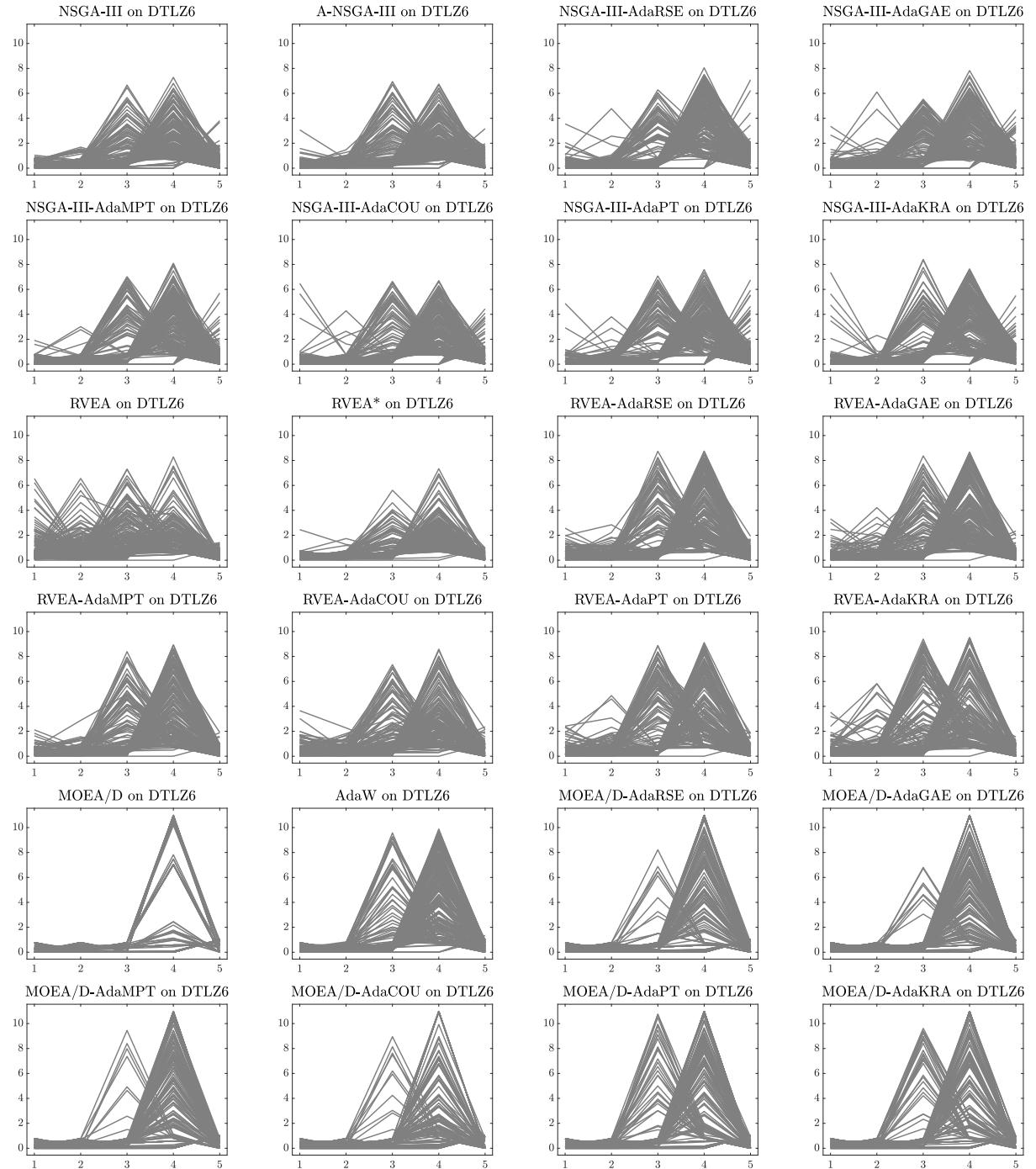


Figure 50: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ6 with 5 objective functions.

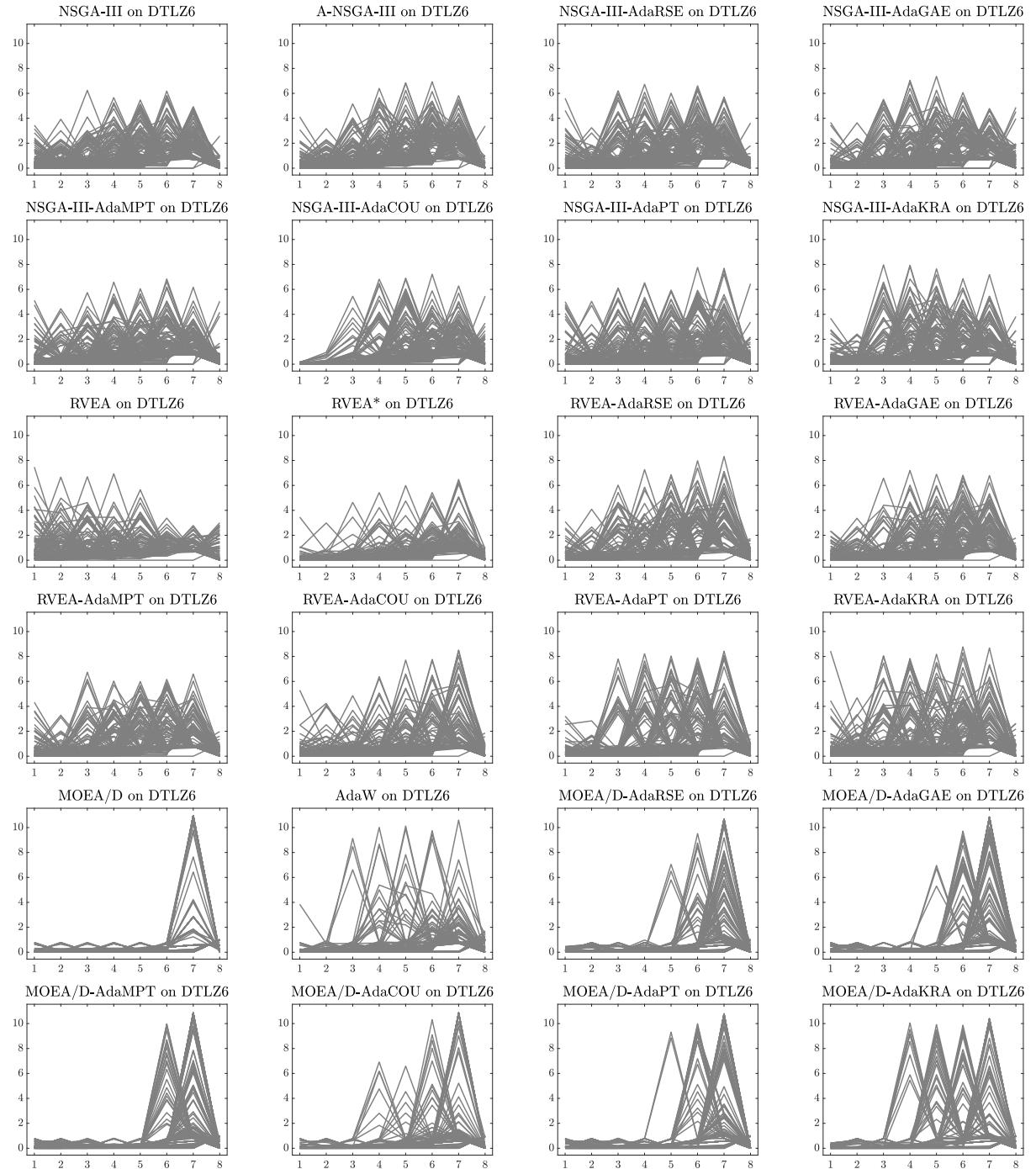


Figure 51: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ6 with 8 objective functions.

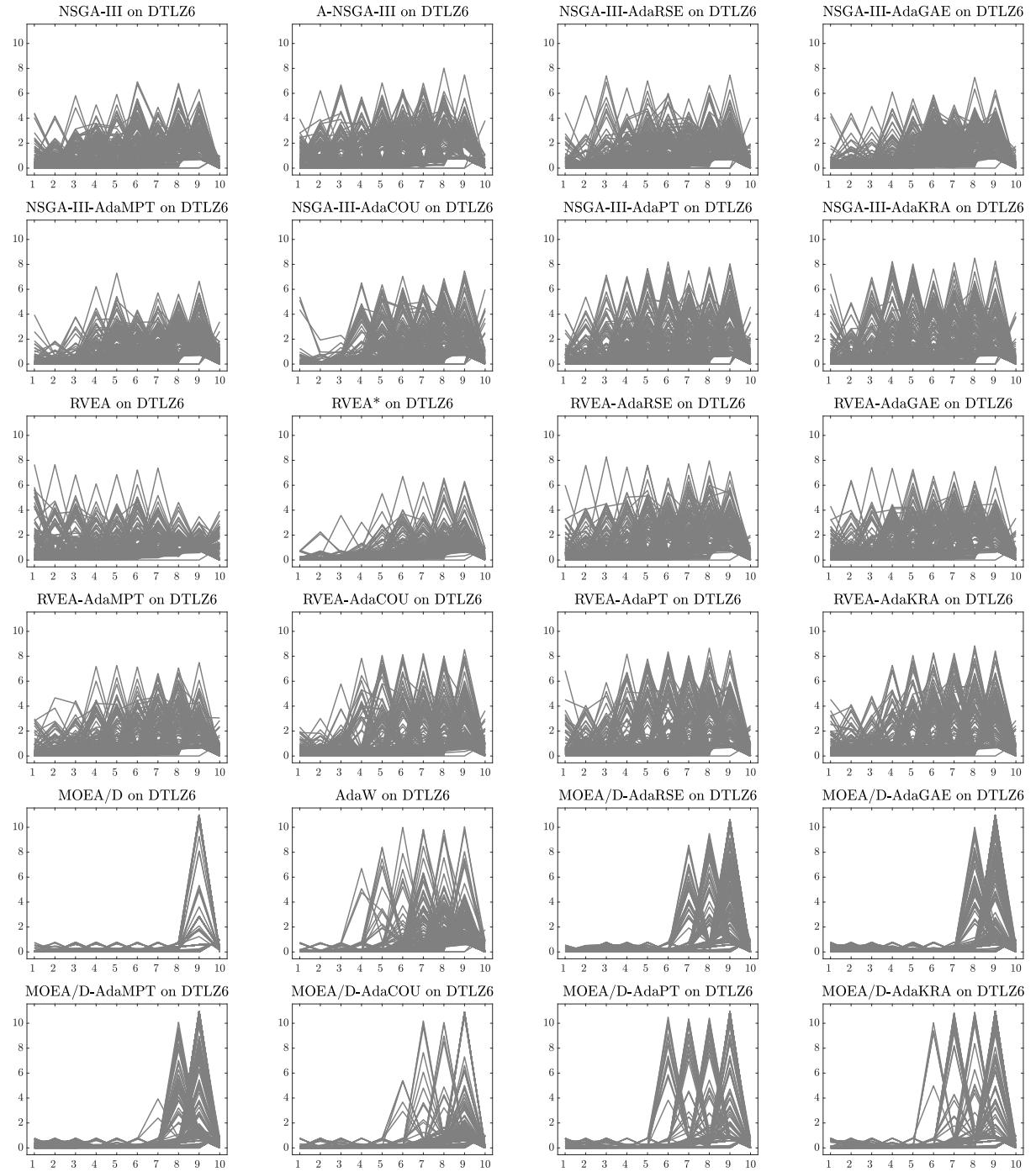


Figure 52: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ6 with 10 objective functions.

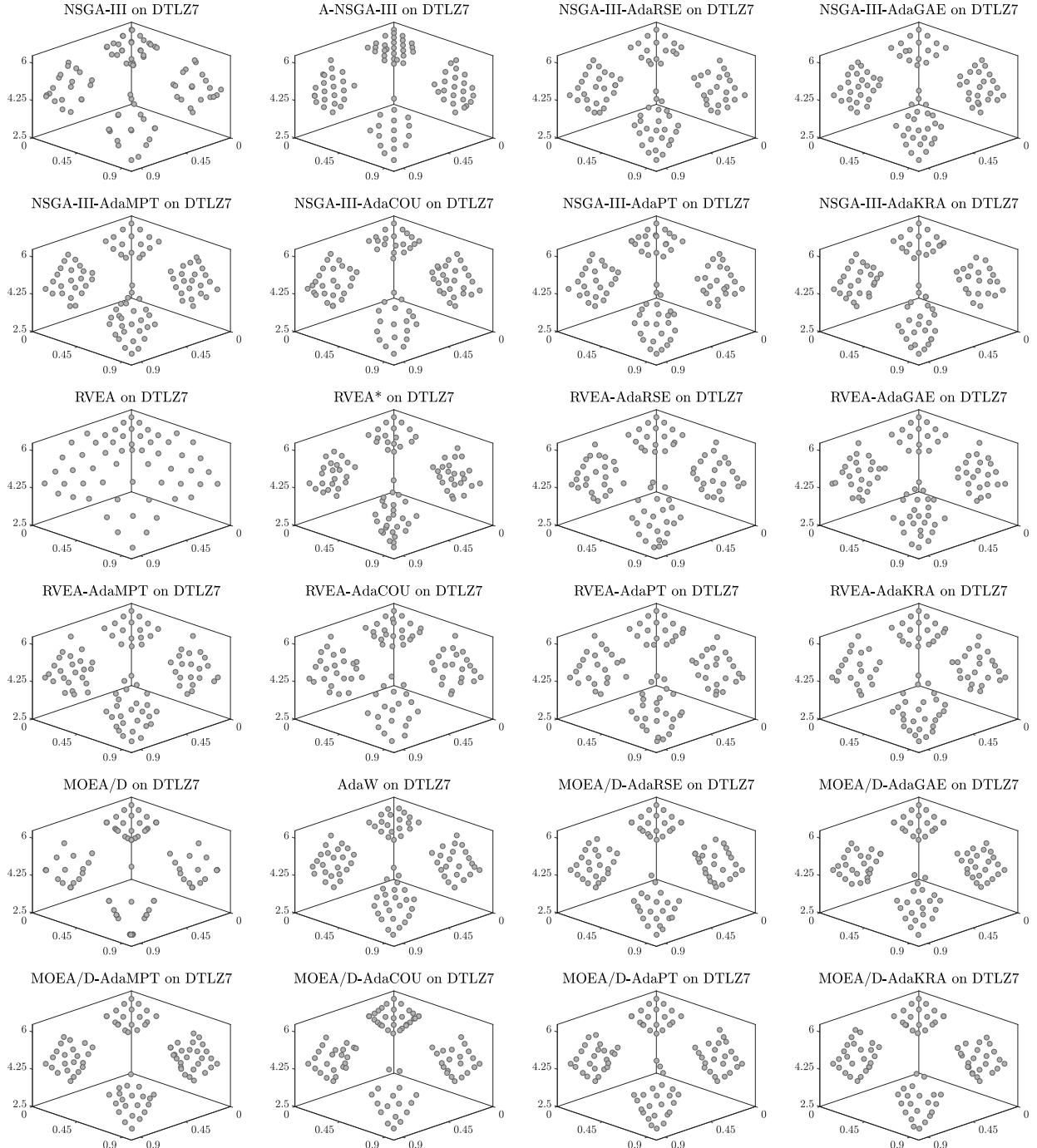


Figure 53: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ7 with 3 objective functions.

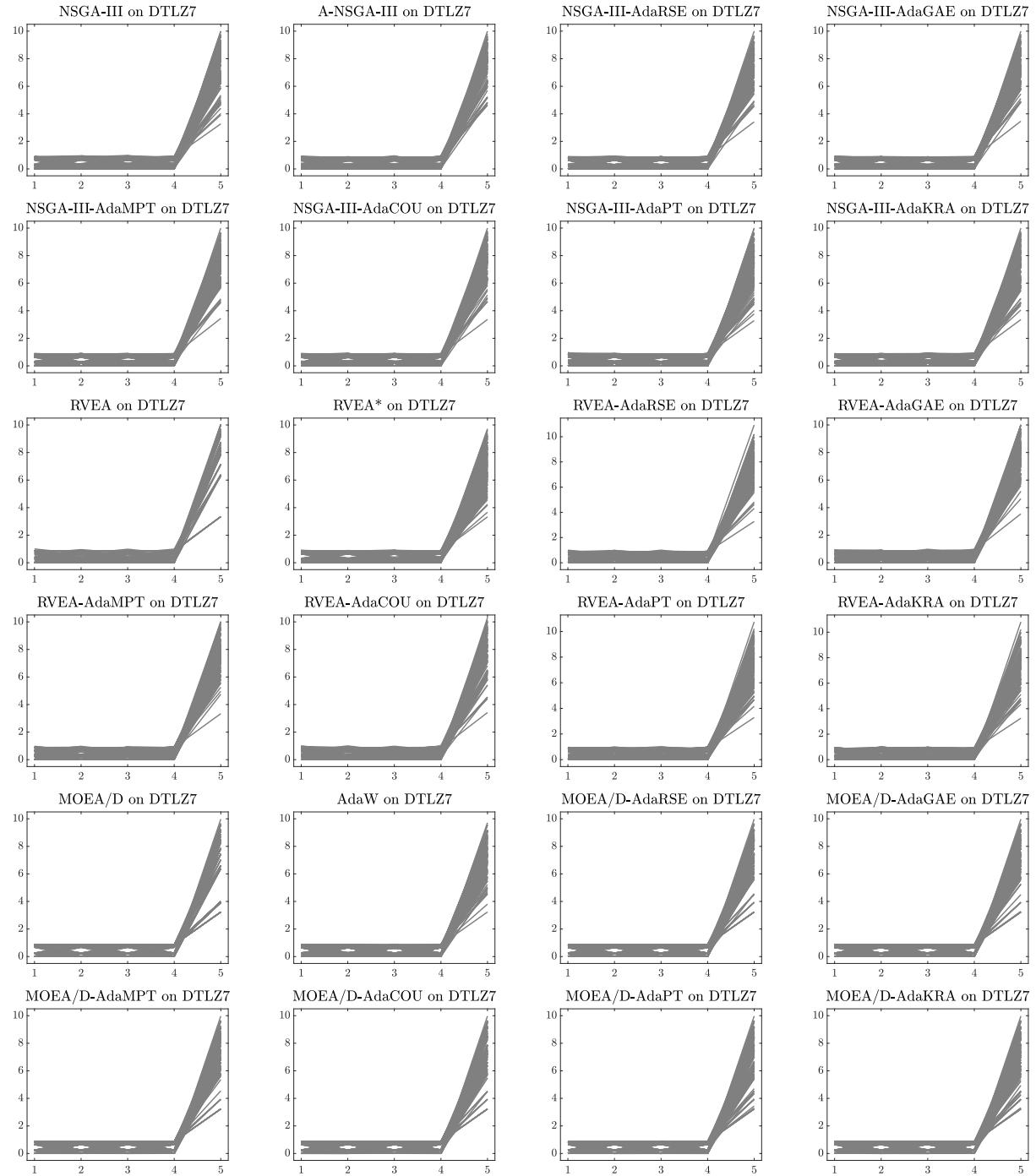


Figure 54: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ7 with 5 objective functions.

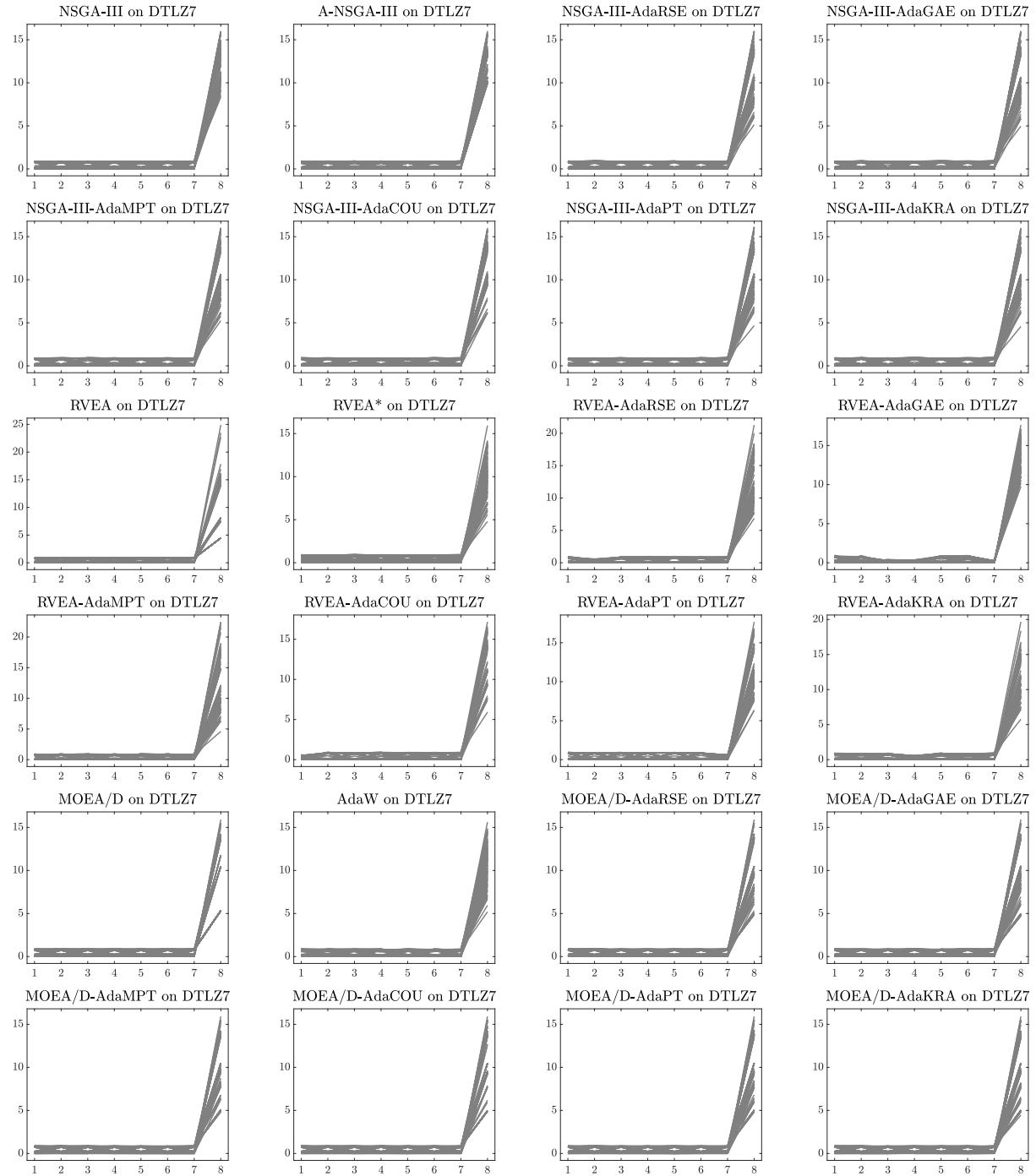


Figure 55: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ7 with 8 objective functions.

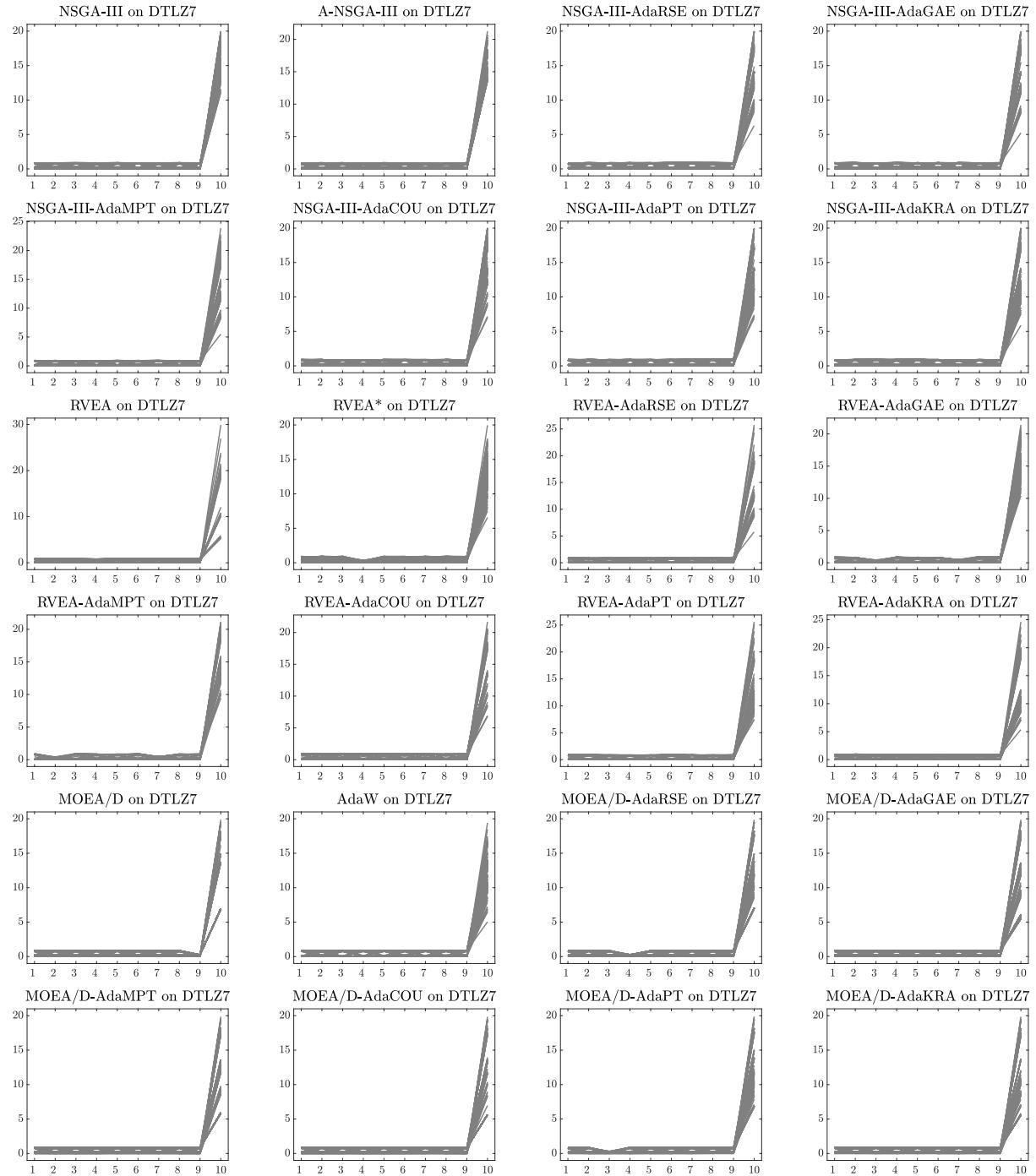


Figure 56: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ7 with 10 objective functions.

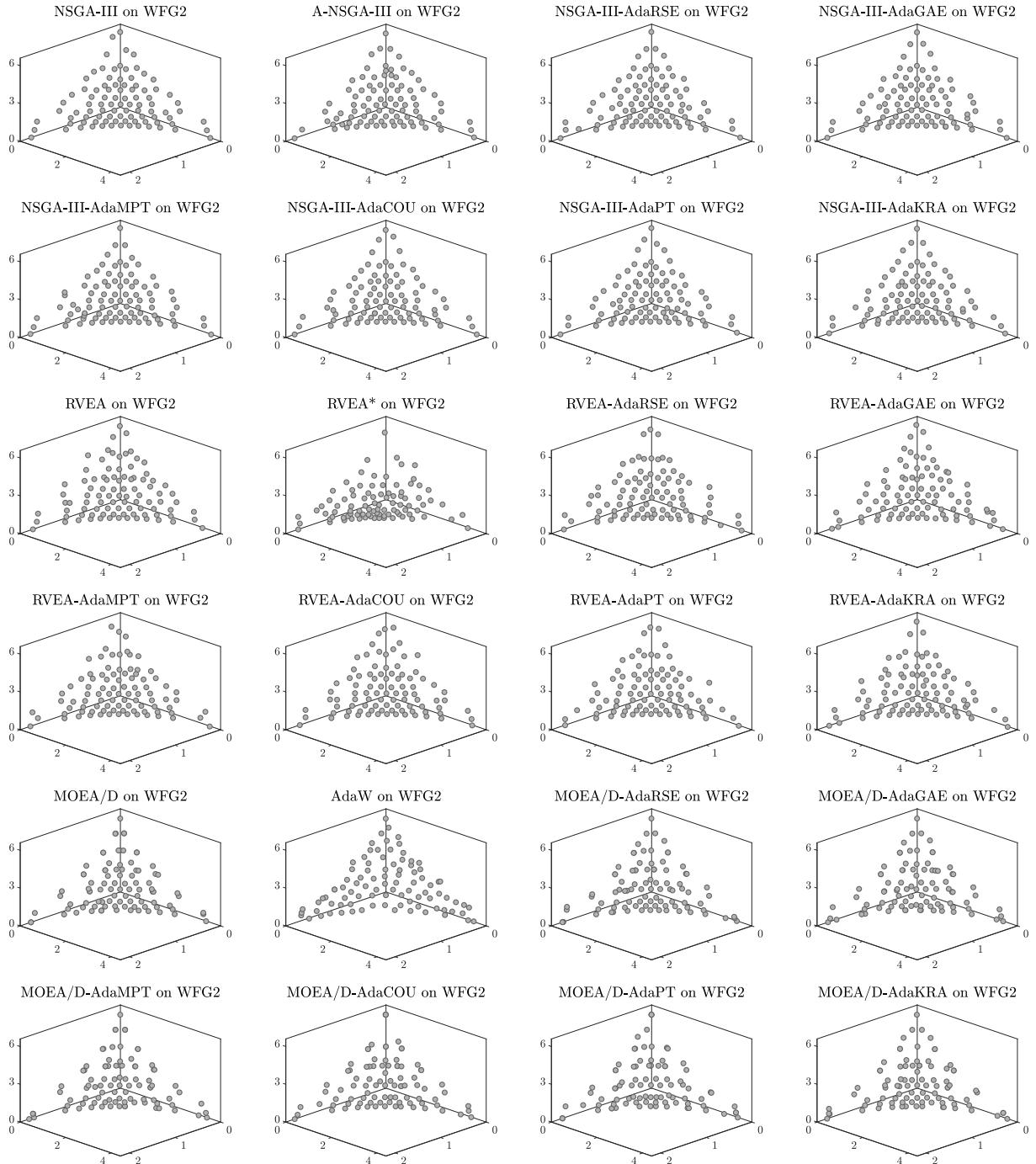


Figure 57: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG2 with 3 objective functions.

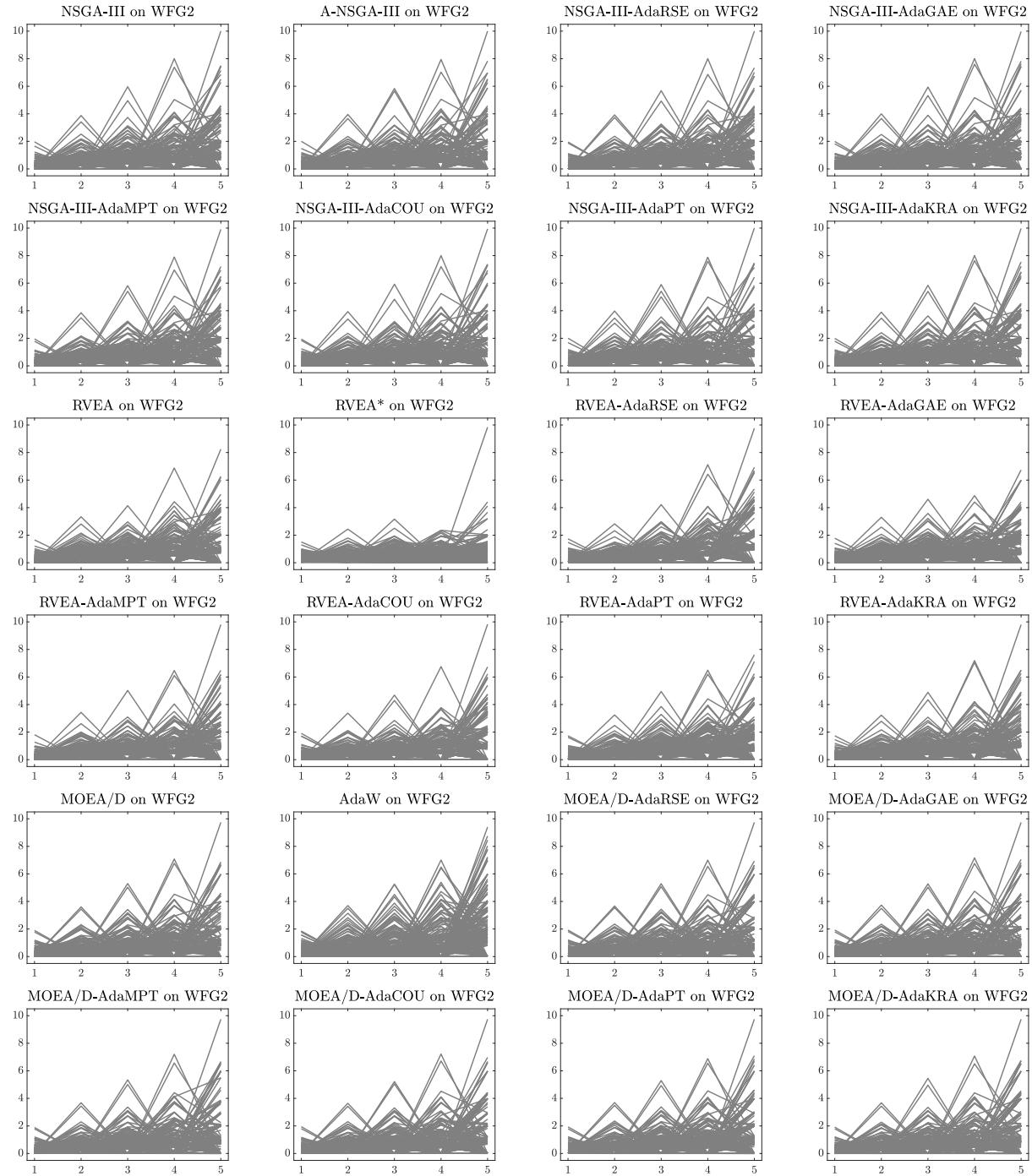


Figure 58: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG2 with 5 objective functions.

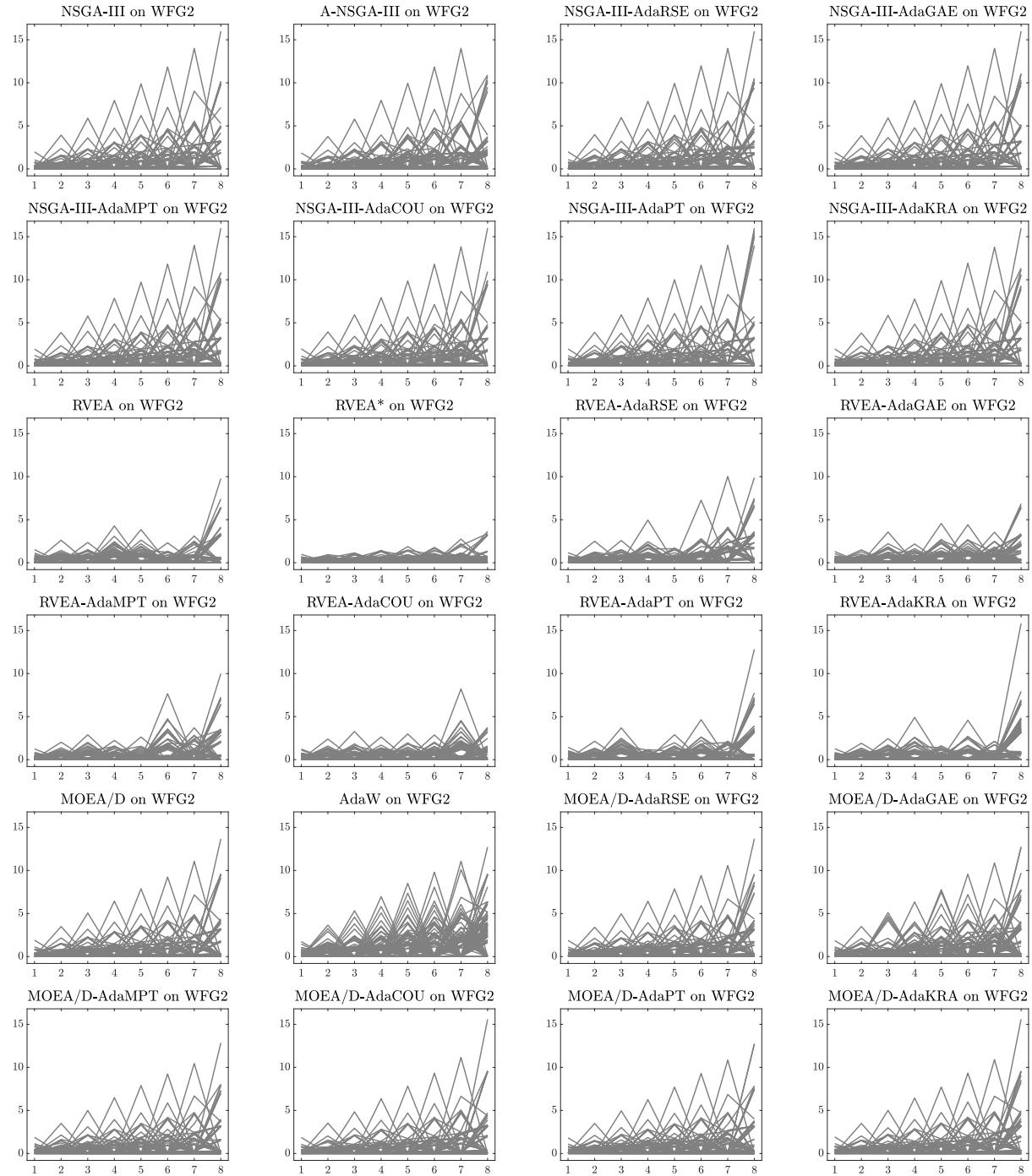


Figure 59: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG2 with 8 objective functions.

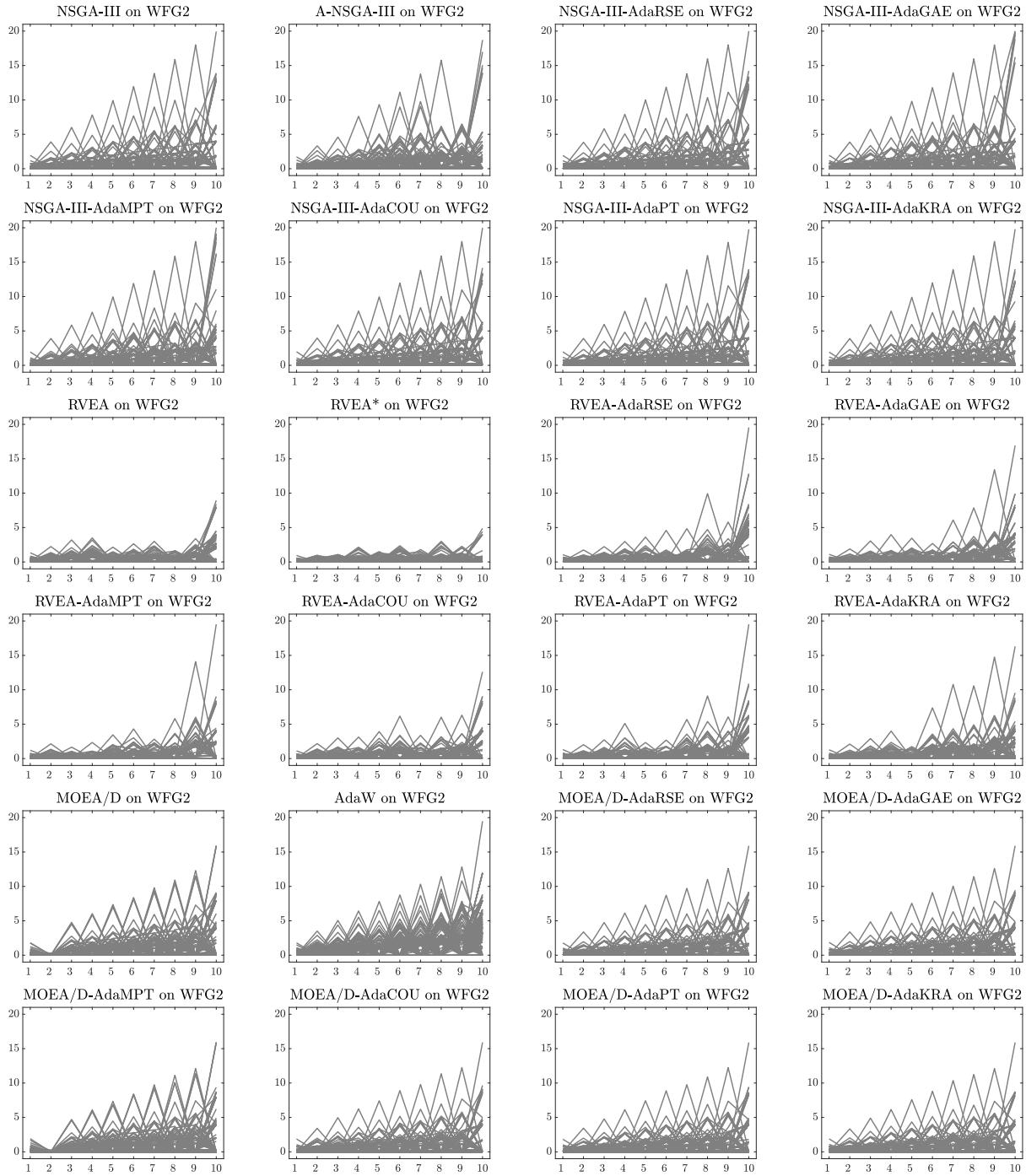


Figure 60: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG2 with 10 objective functions.

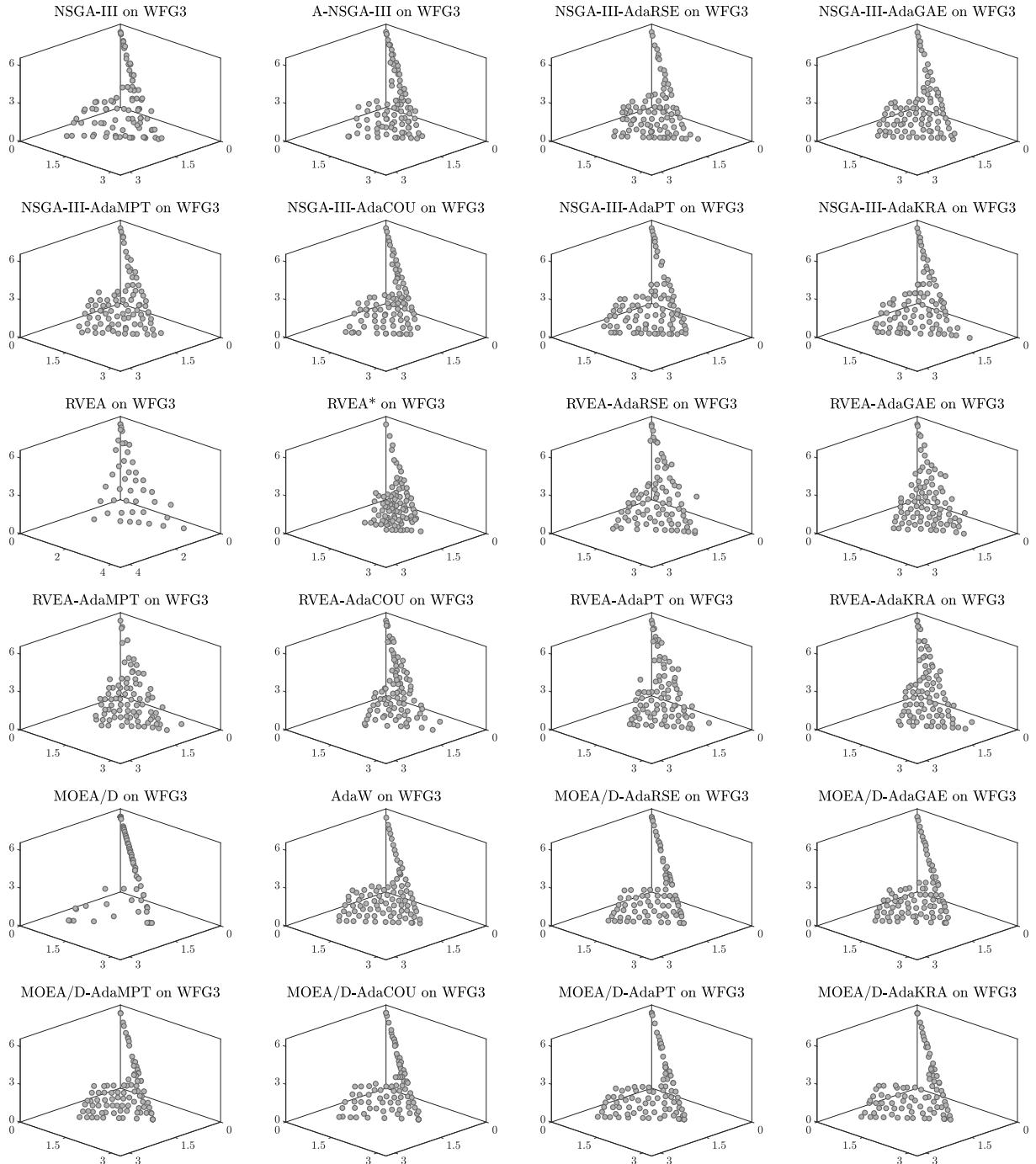


Figure 61: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG3 with 3 objective functions.

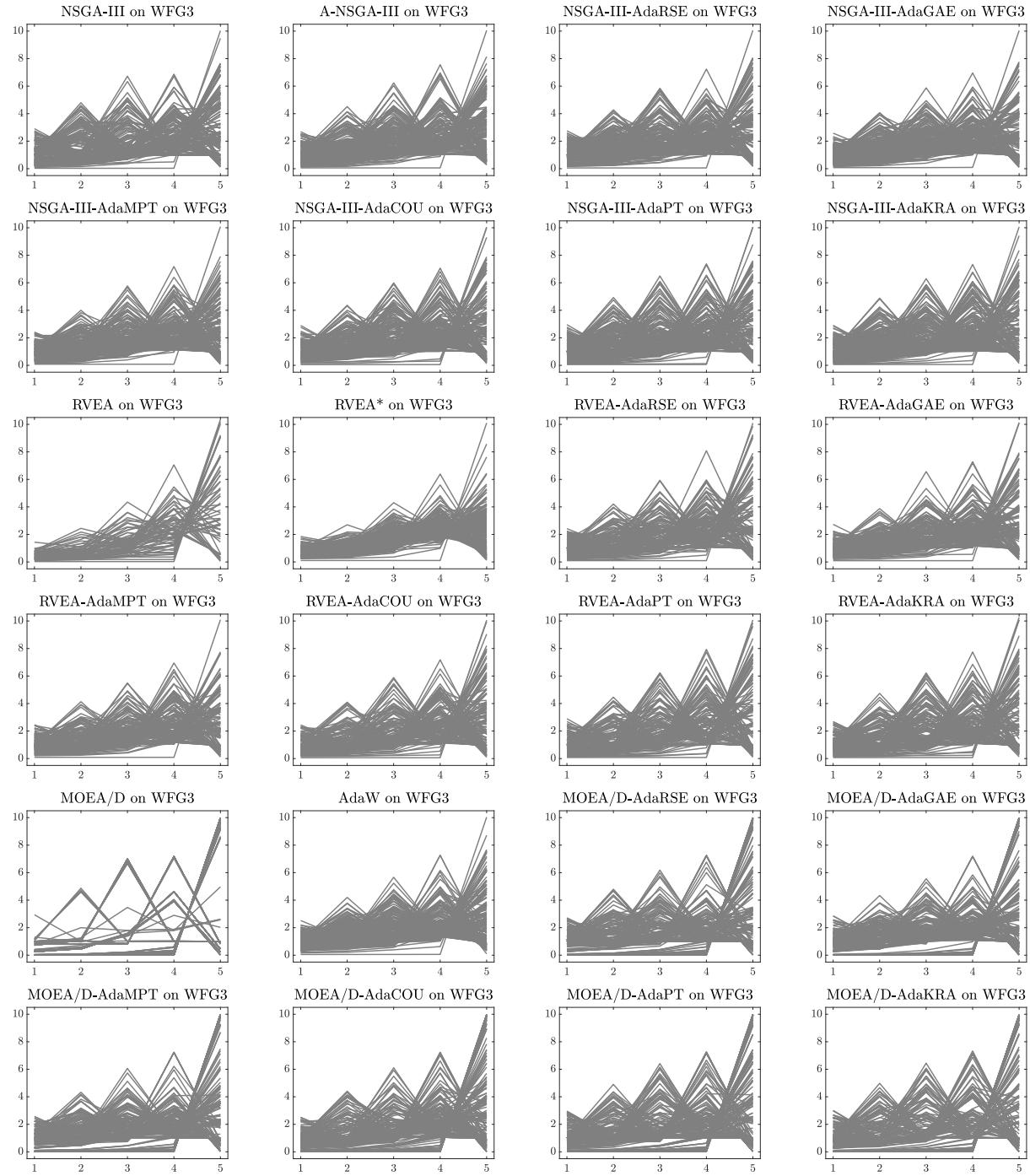


Figure 62: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG3 with 5 objective functions.

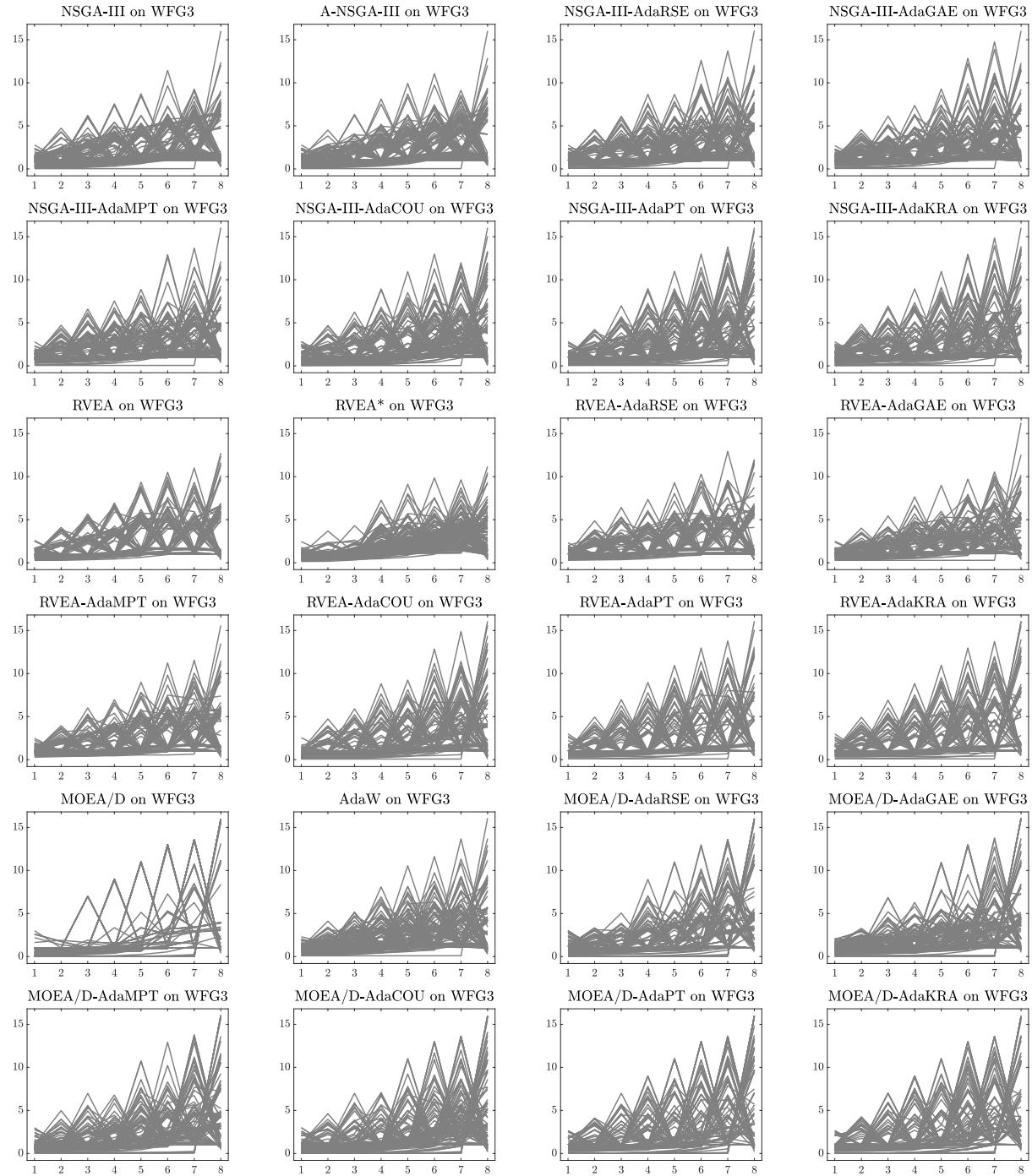


Figure 63: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG3 with 8 objective functions.

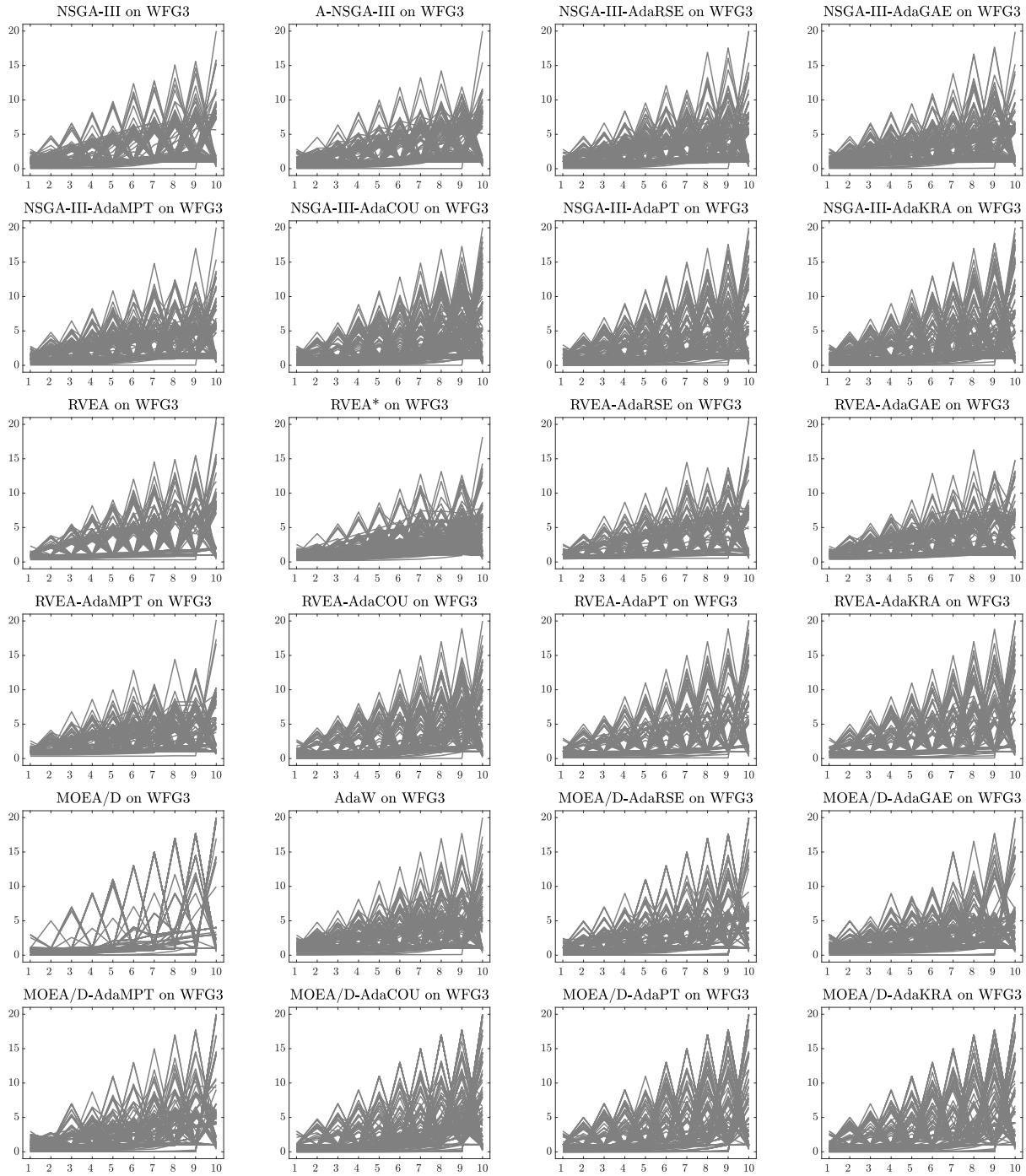


Figure 64: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG3 with 10 objective functions.

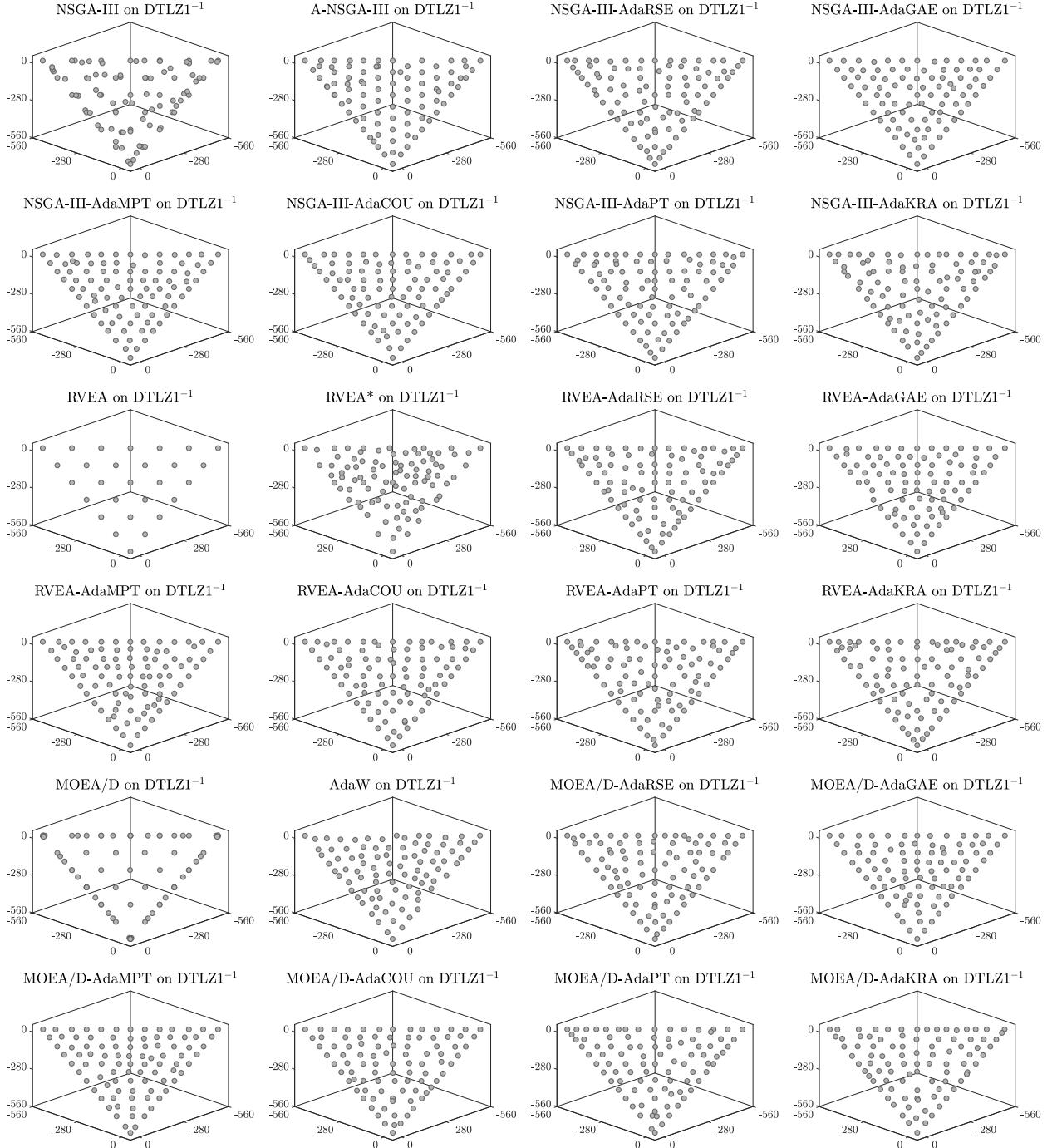


Figure 65: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ1⁻¹ with 3 objective functions.

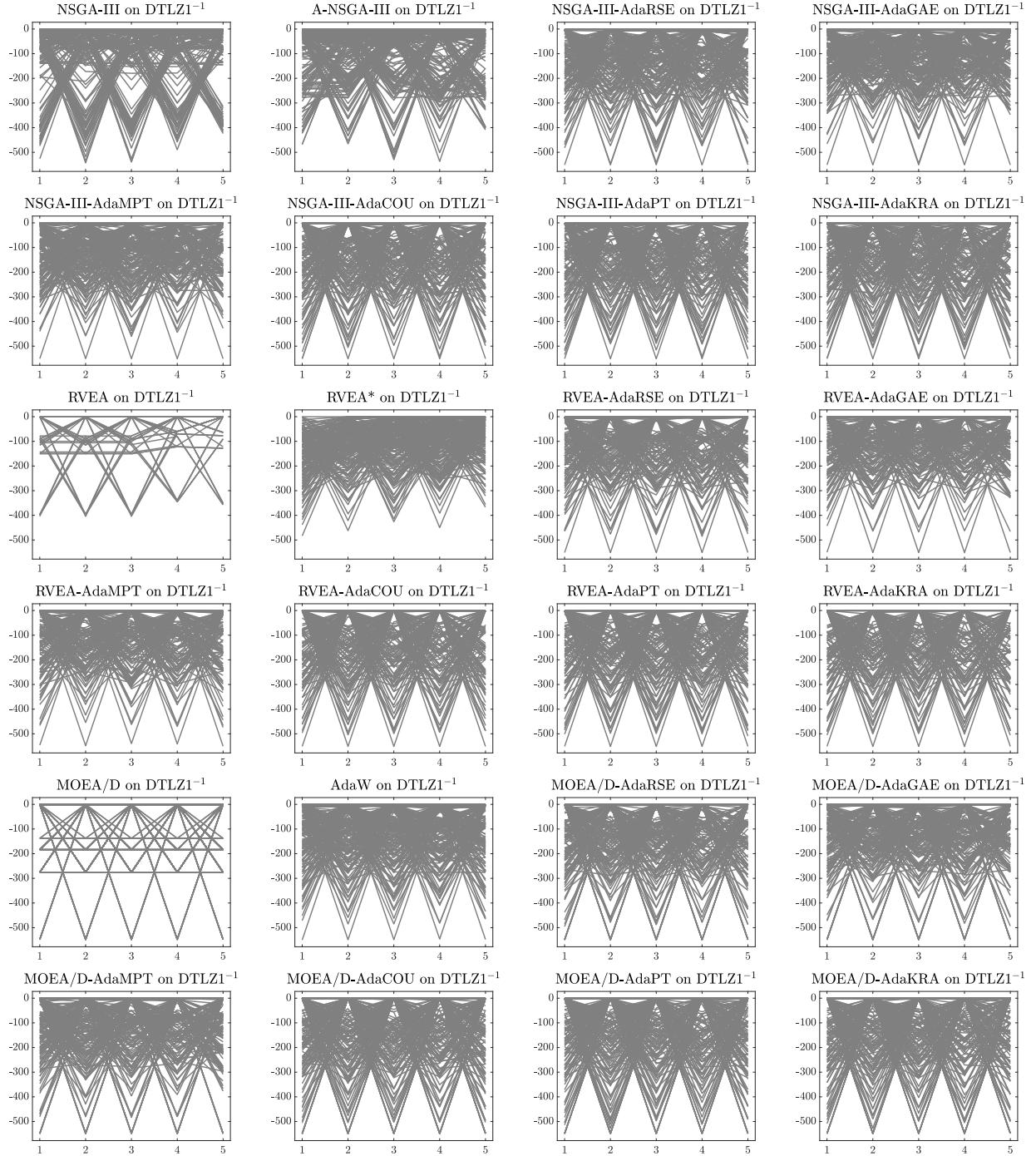


Figure 66: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ1⁻¹ with 5 objective functions.

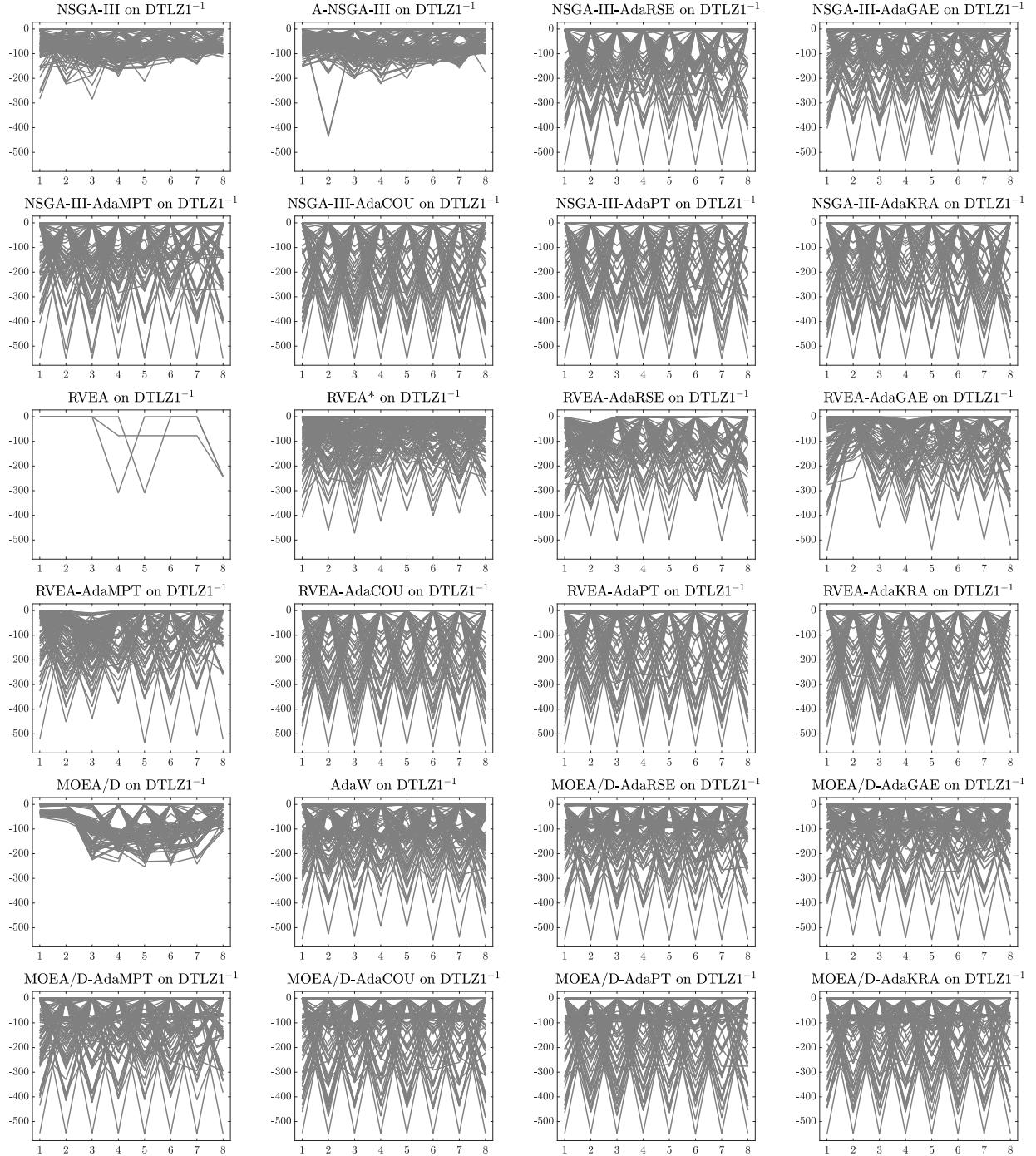


Figure 67: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on $DTLZ1^{-1}$ with 8 objective functions.

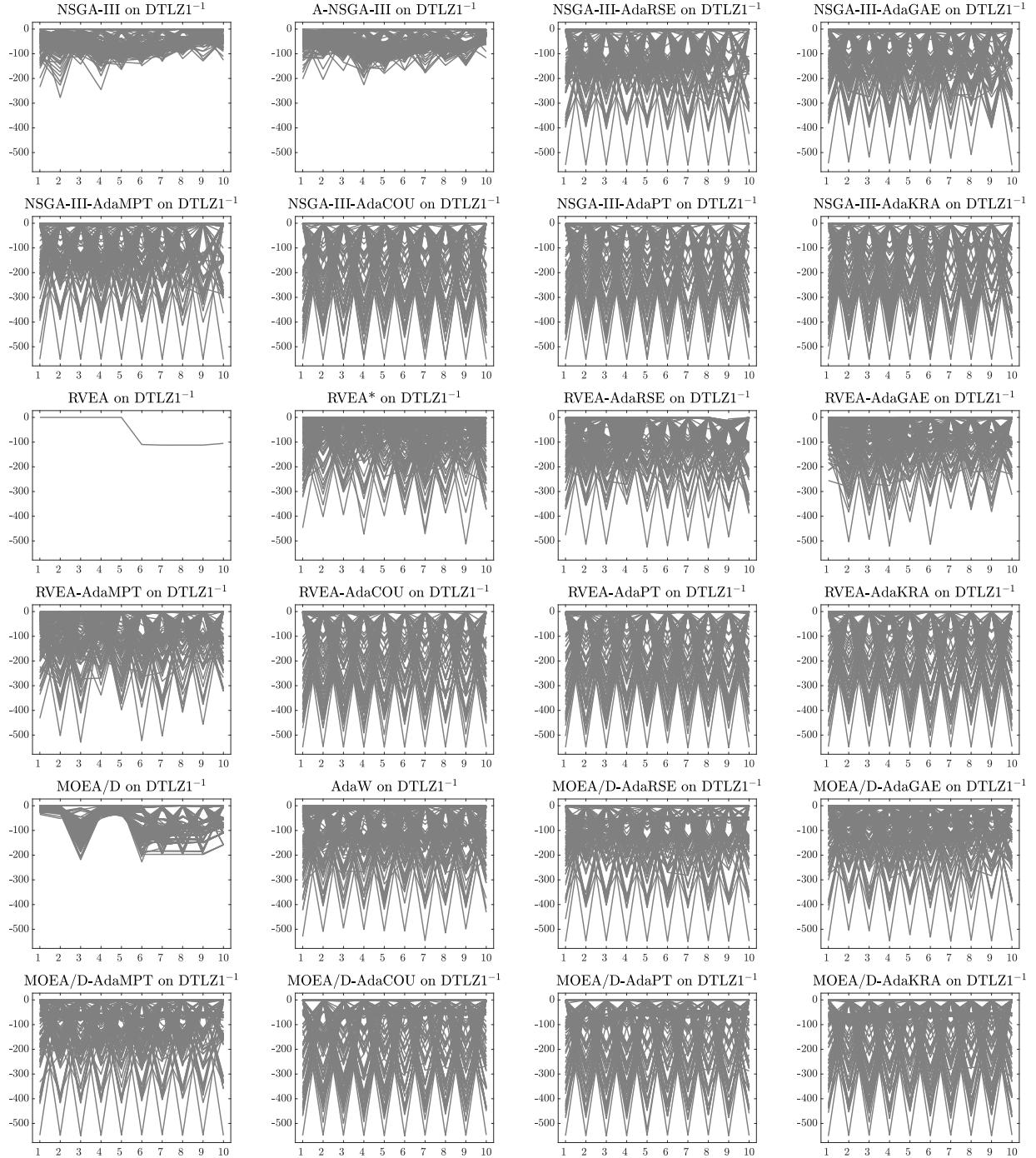


Figure 68: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on $DTLZ1^{-1}$ with 10 objective functions.

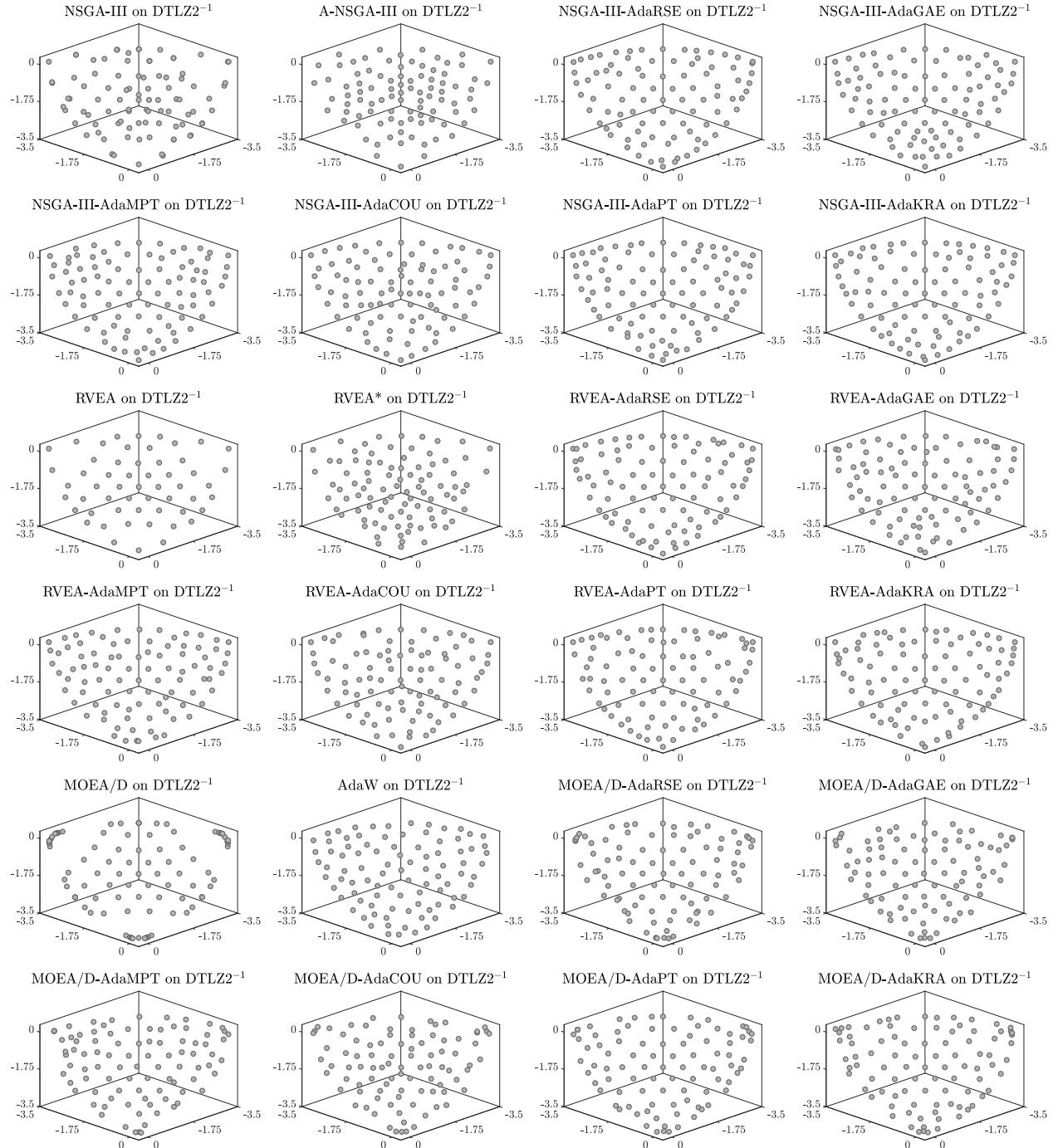


Figure 69: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on $DTLZ2^{-1}$ with 3 objective functions.

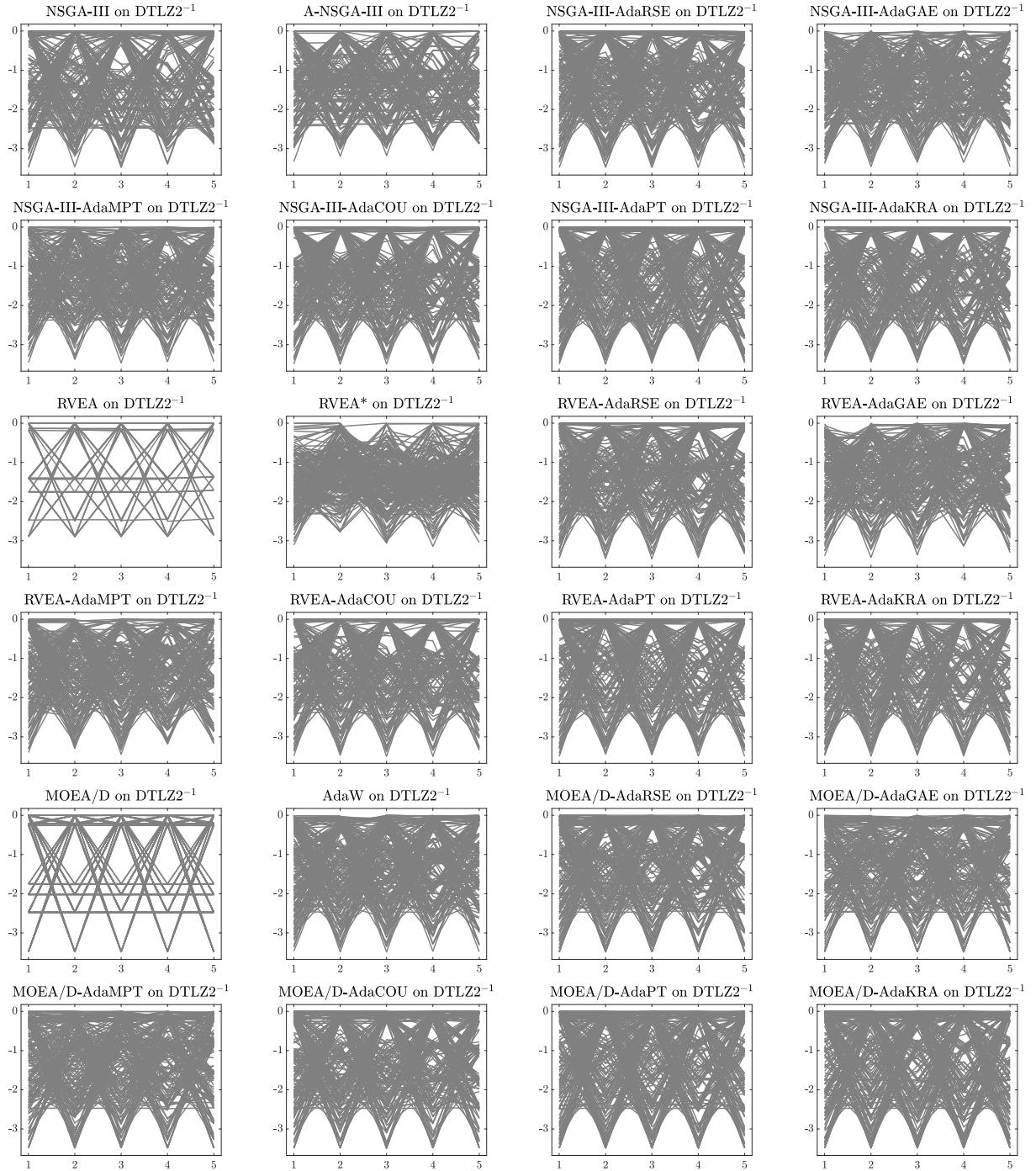


Figure 70: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ2⁻¹ with 5 objective functions.

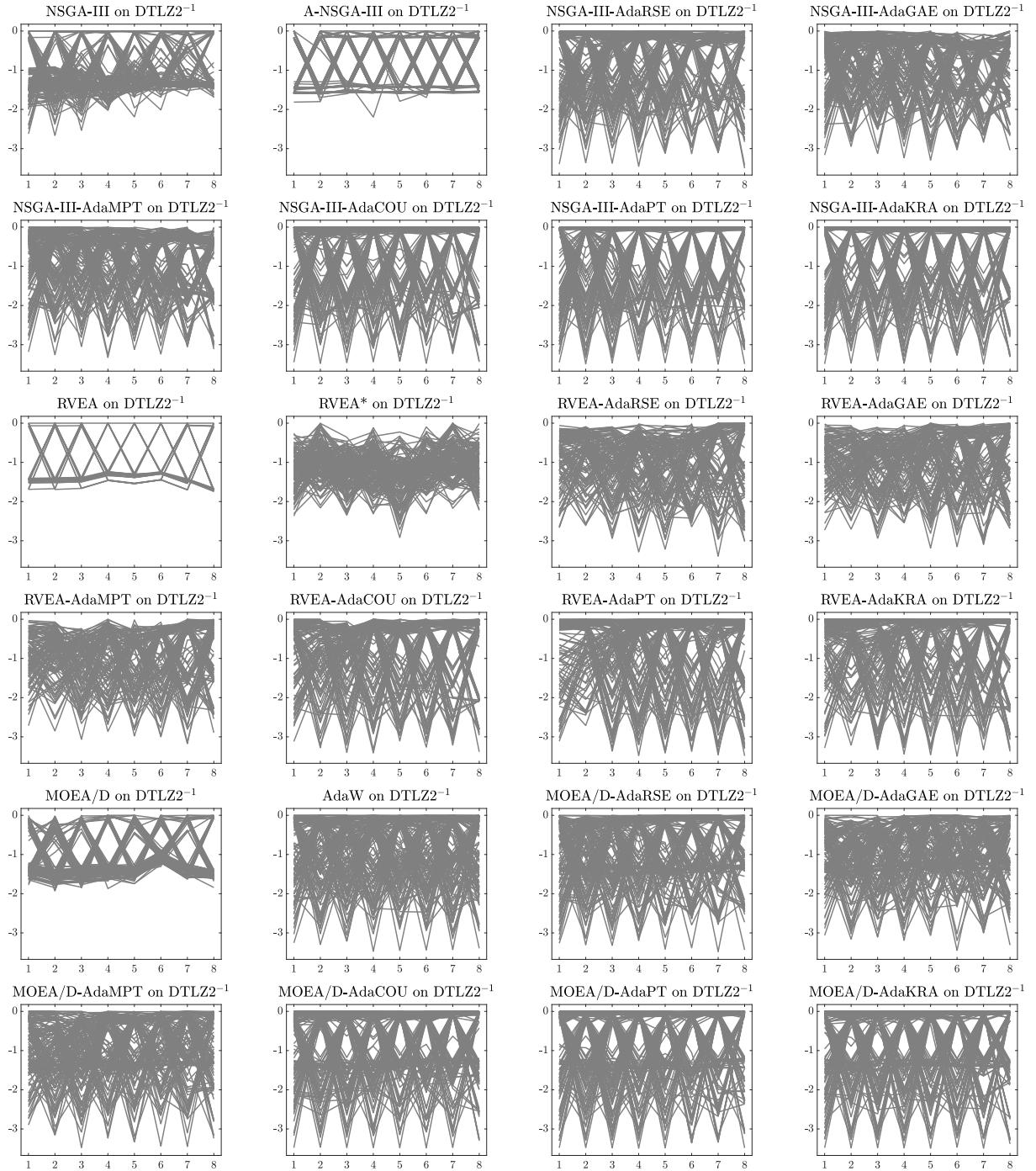


Figure 71: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on $DTLZ2^{-1}$ with 8 objective functions.

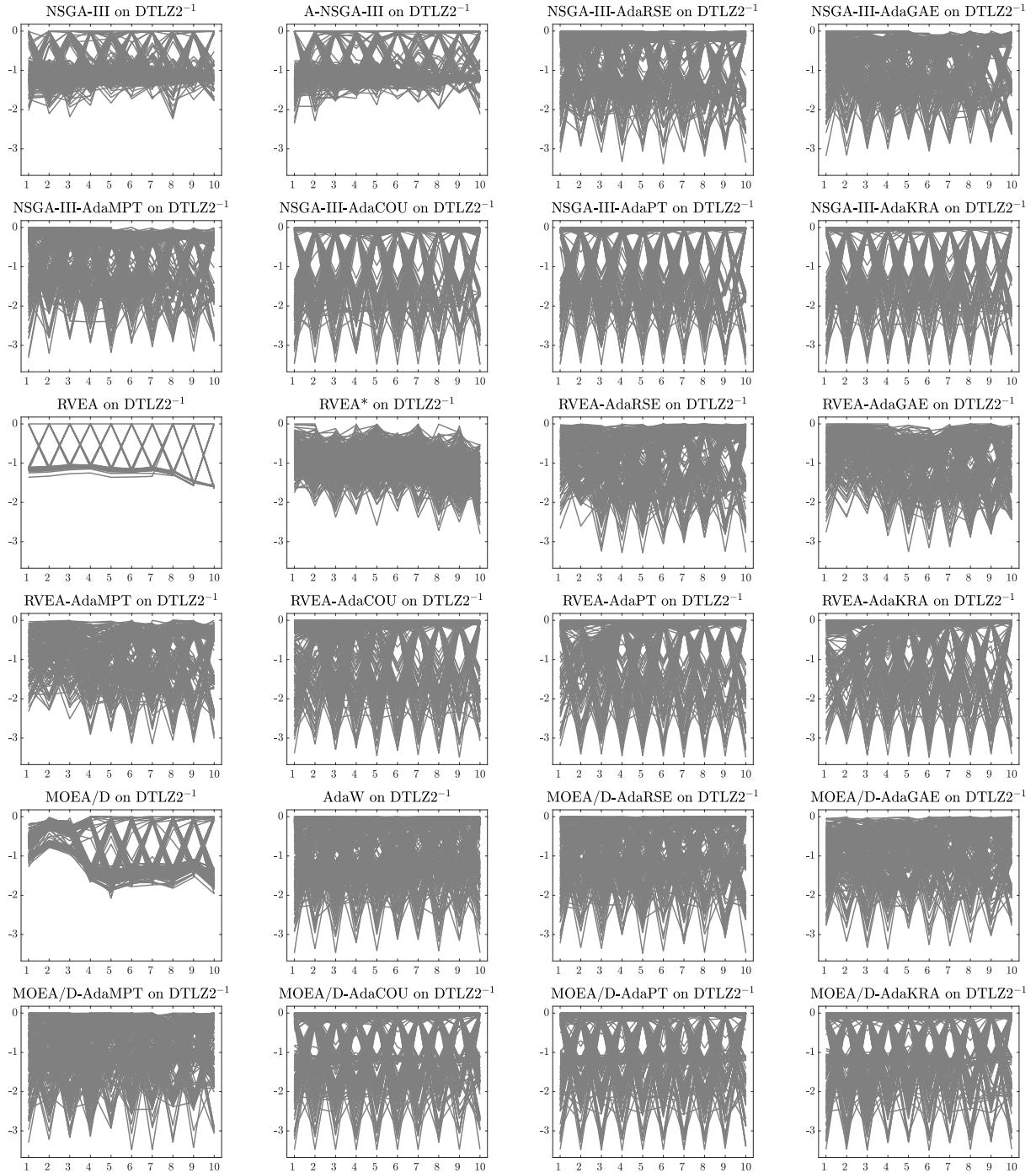


Figure 72: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ2⁻¹ with 10 objective functions.

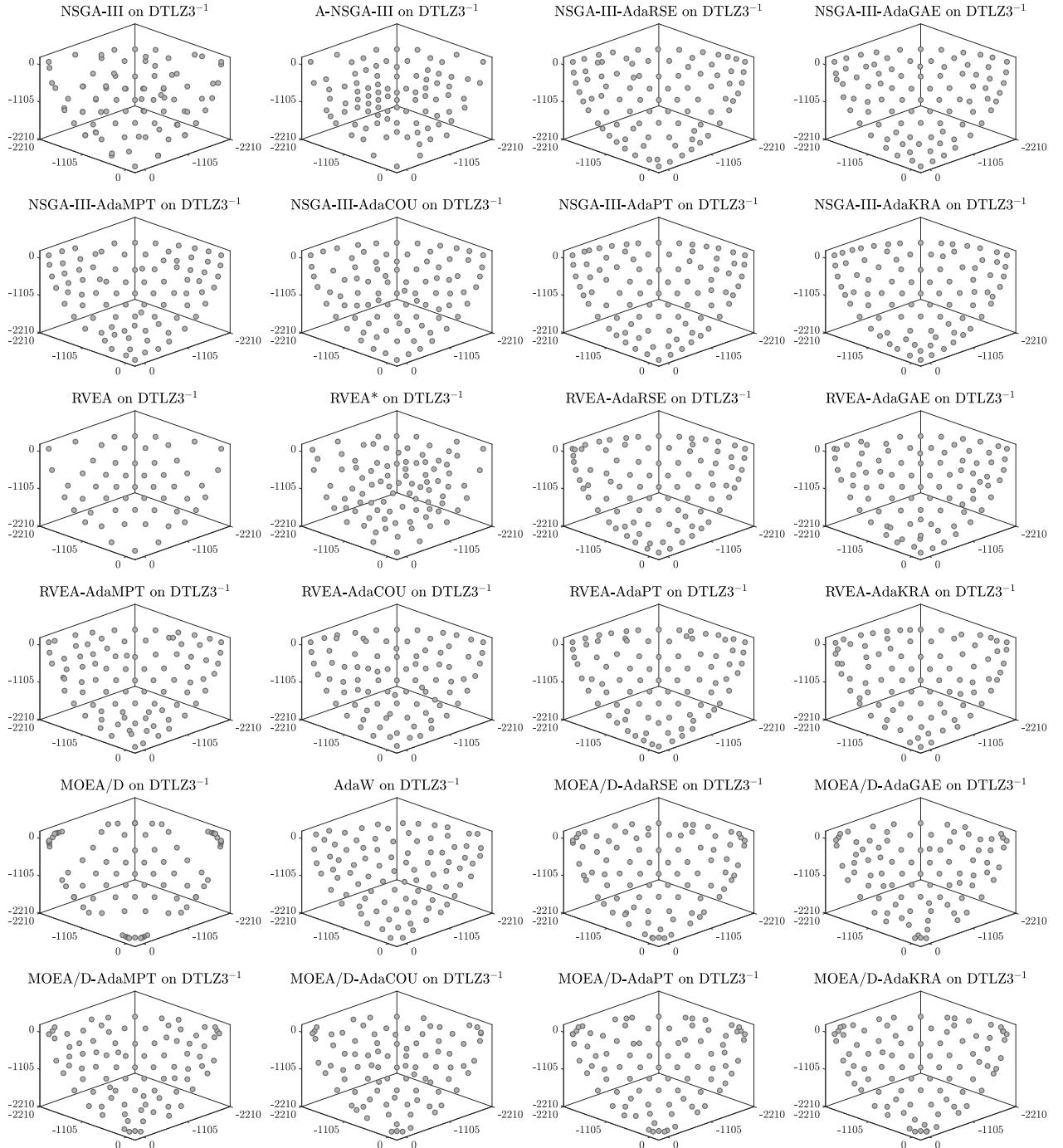


Figure 73: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on $DTLZ3^{-1}$ with 3 objective functions.

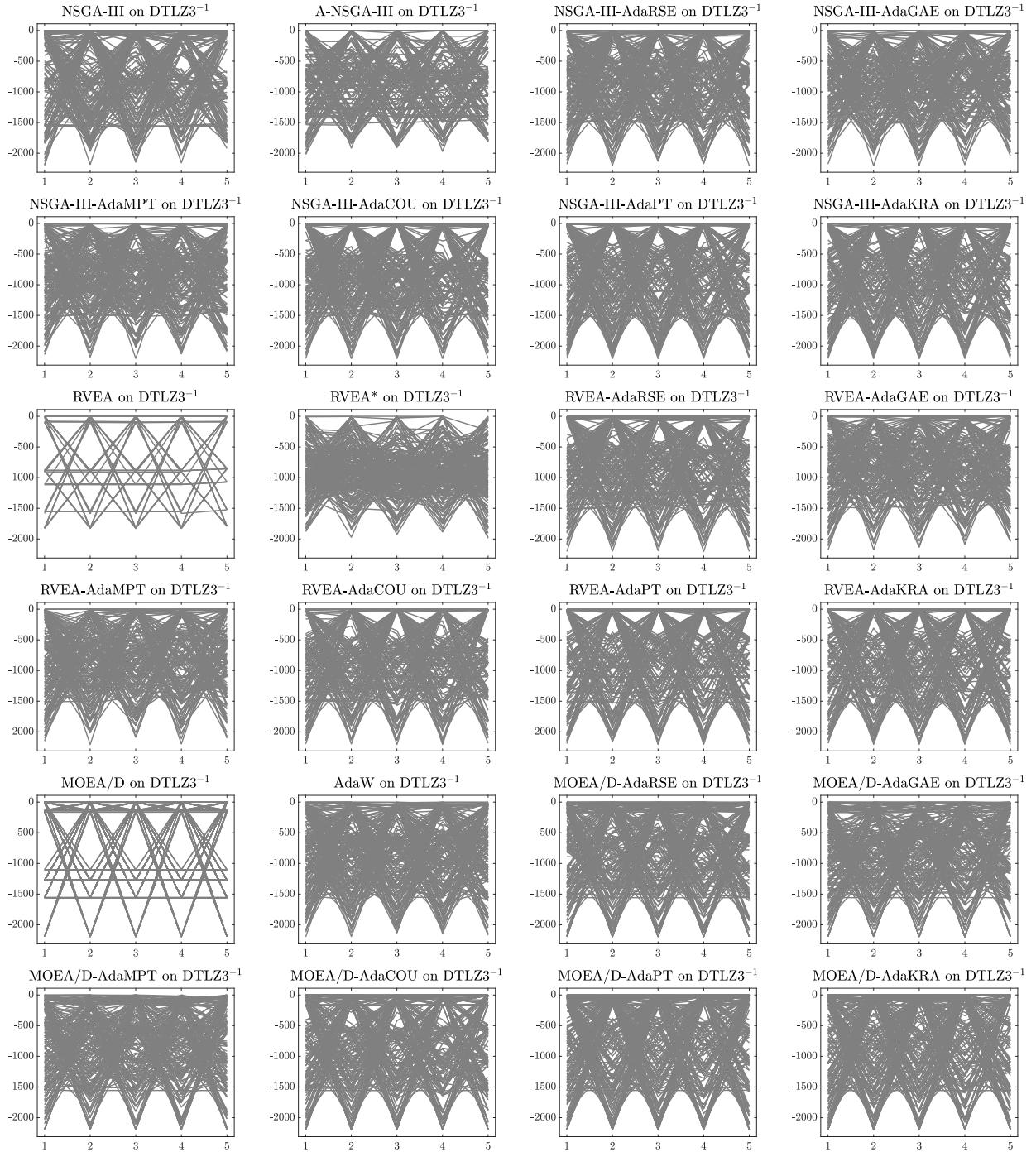


Figure 74: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ3^{-1} with 5 objective functions.

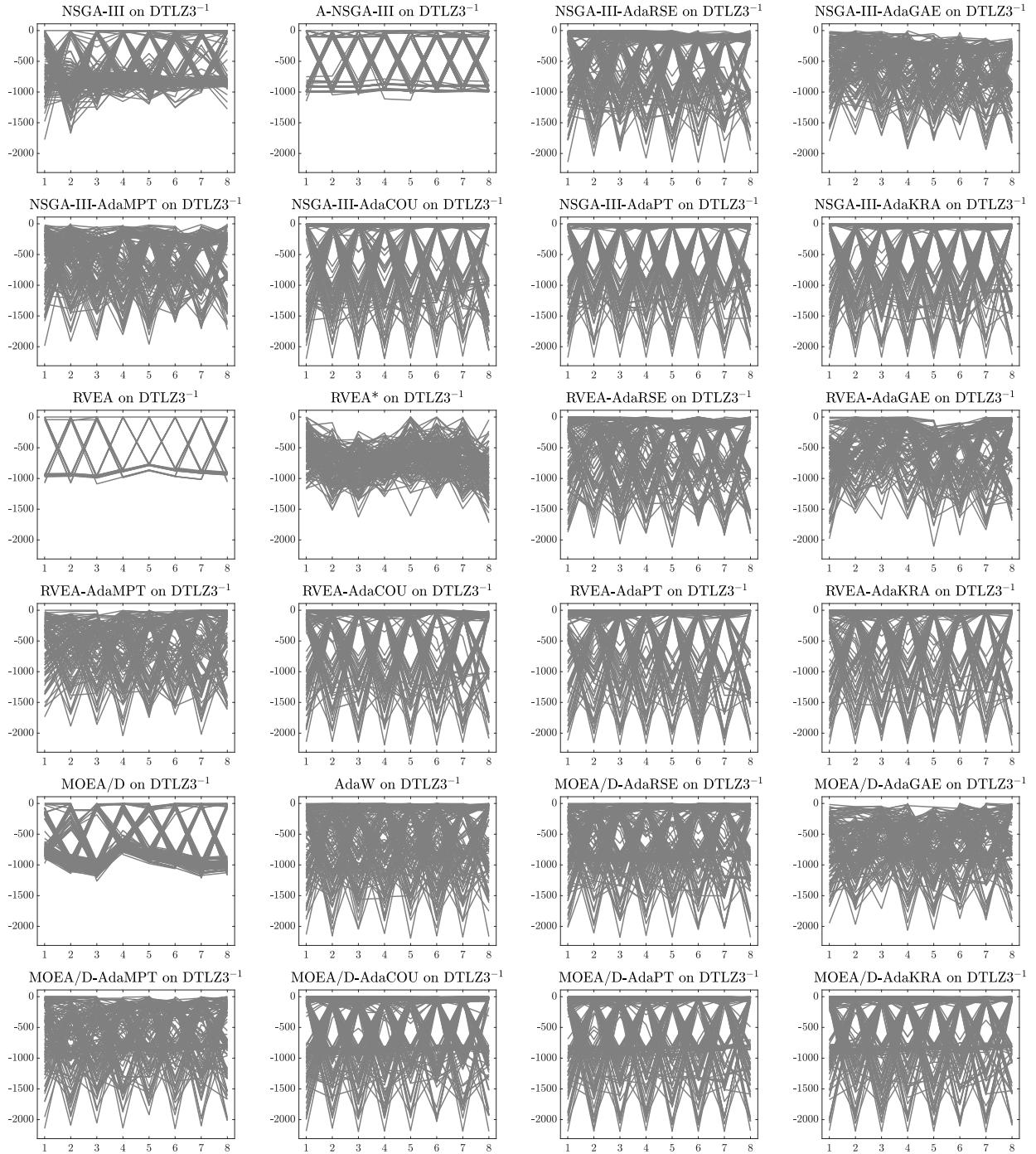


Figure 75: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ3^{-1} with 8 objective functions.

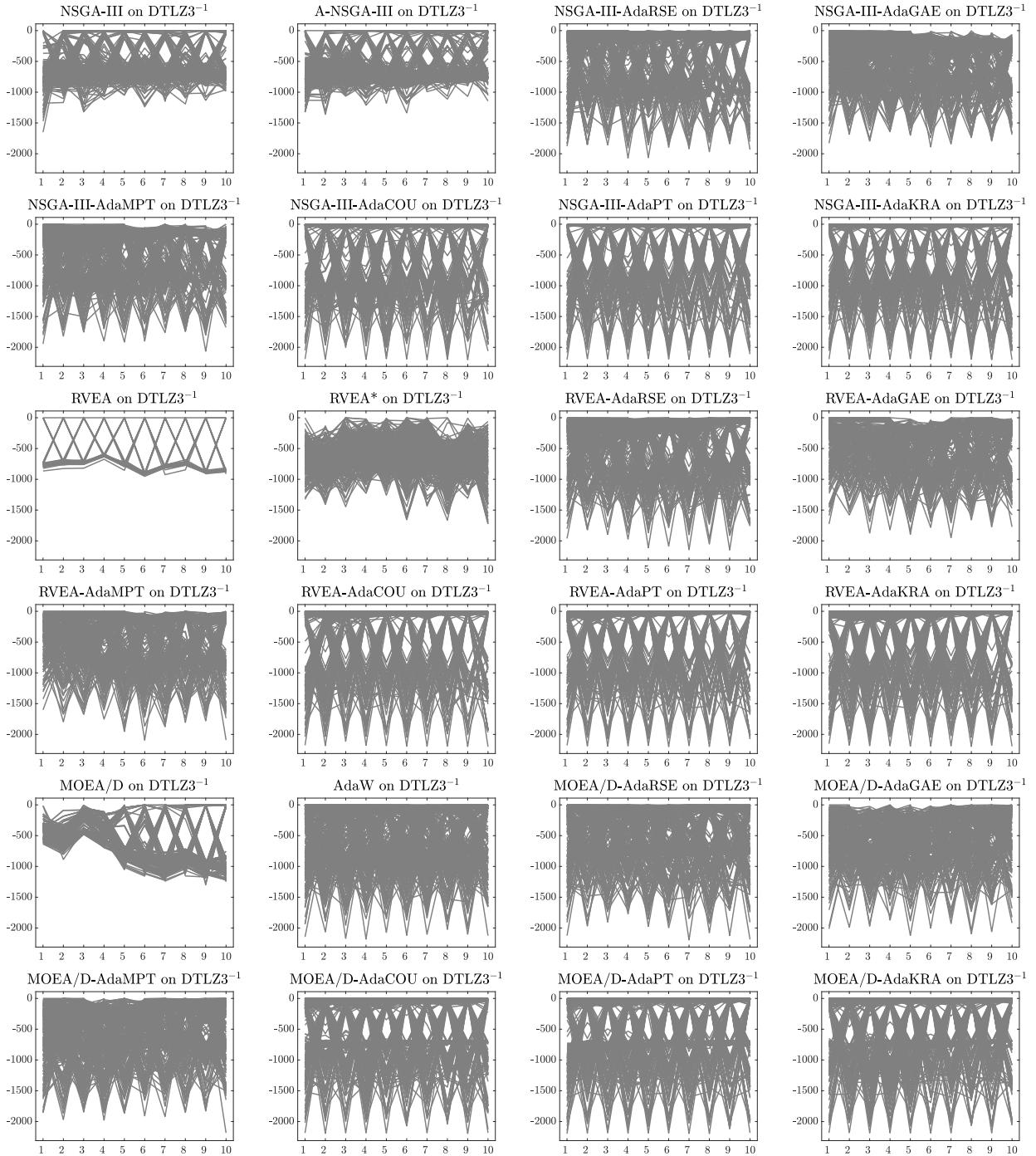


Figure 76: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ3⁻¹ with 10 objective functions.

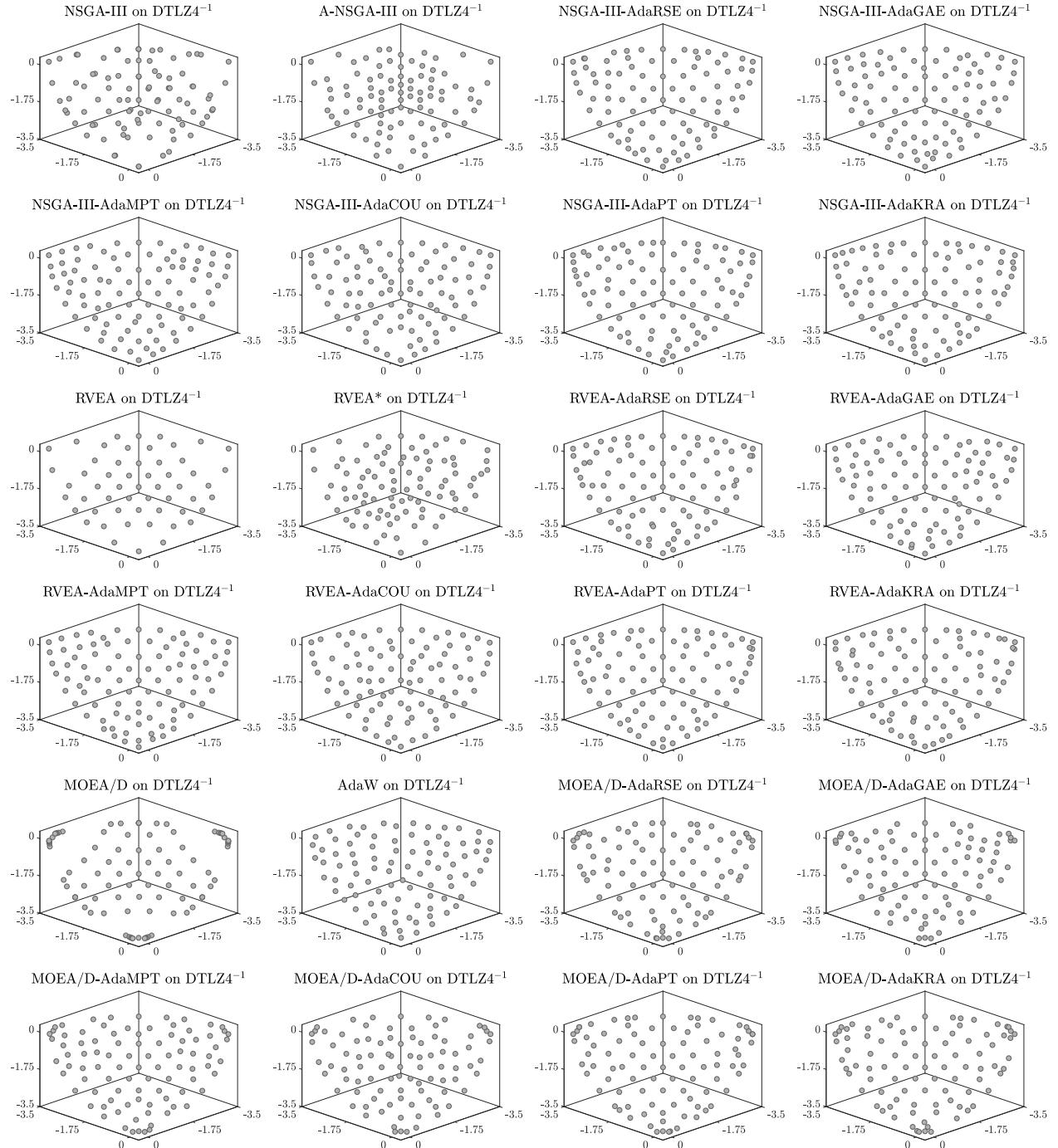


Figure 77: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on $DTLZ4^{-1}$ with 3 objective functions.

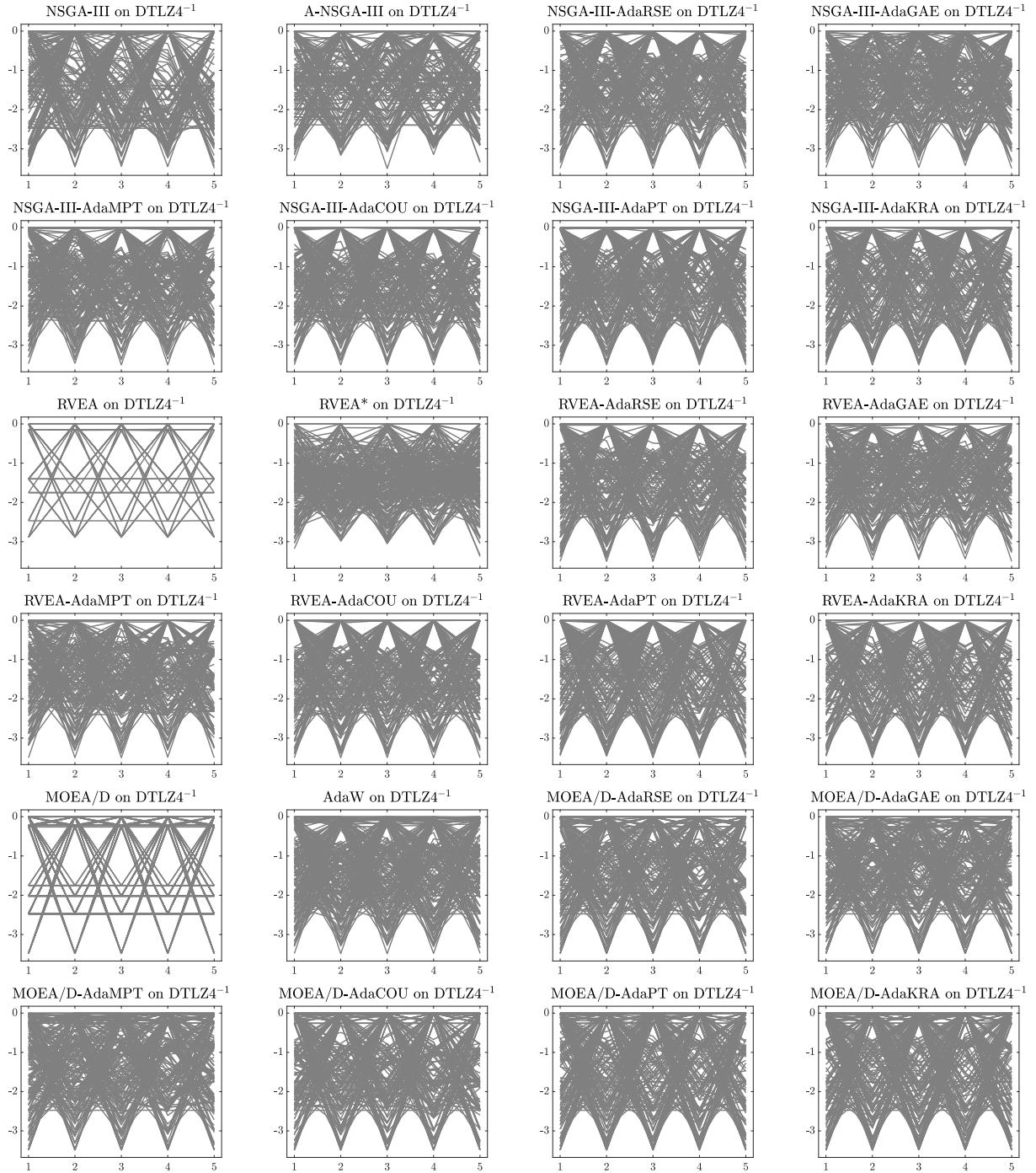


Figure 78: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on $DTLZ4^{-1}$ with 5 objective functions.

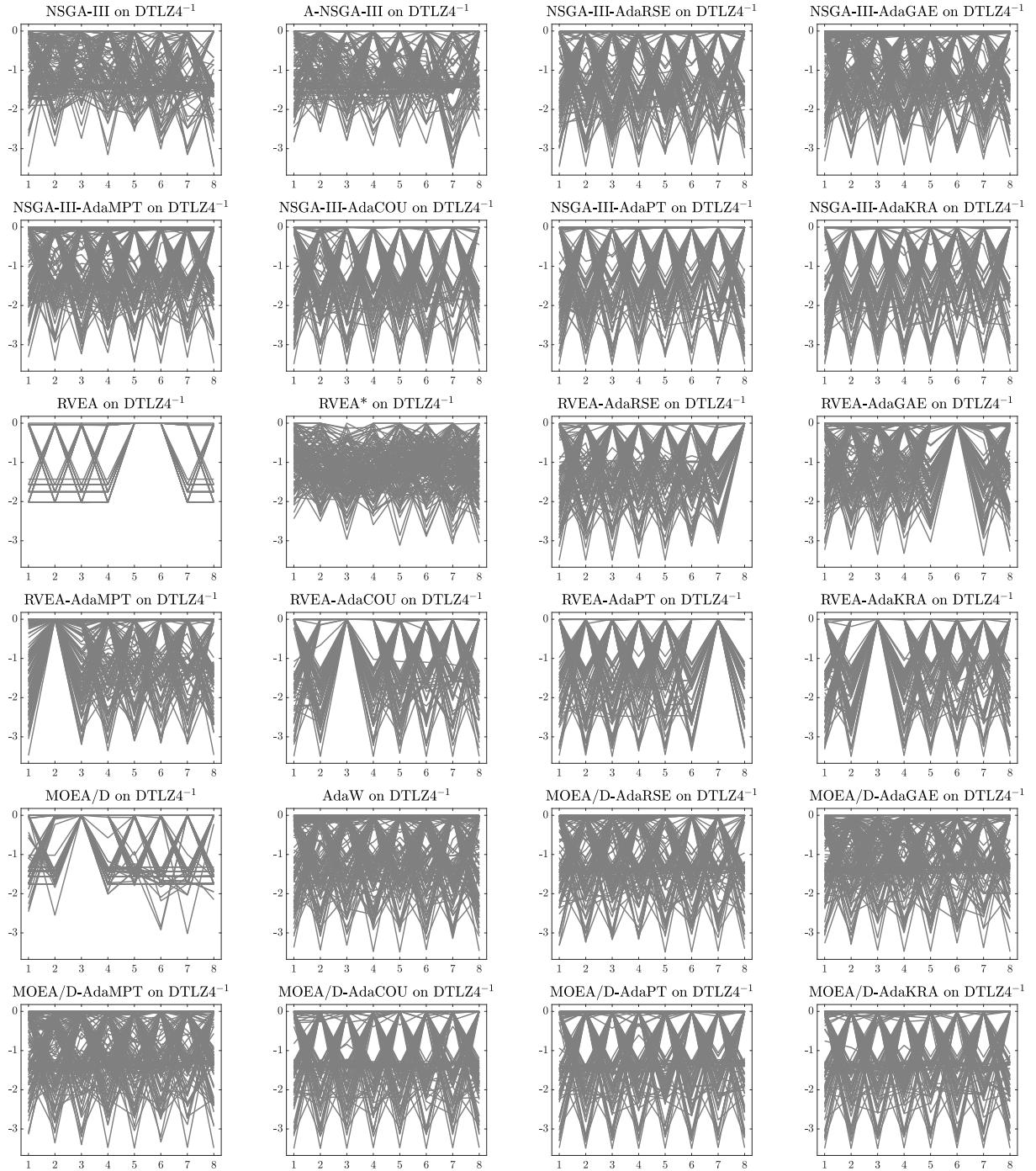


Figure 79: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on $DTLZ4^{-1}$ with 8 objective functions.

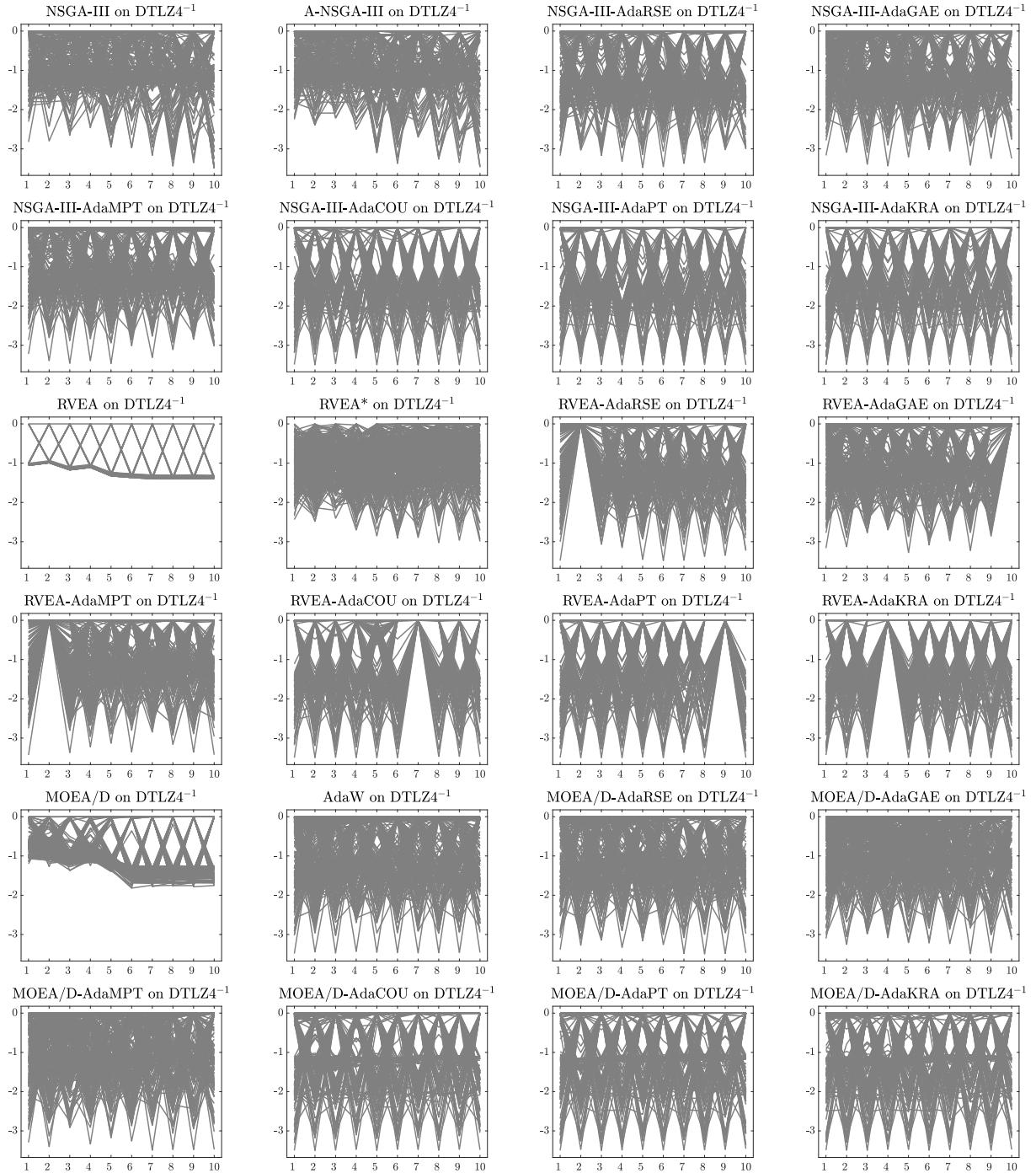


Figure 80: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ4⁻¹ with 10 objective functions.

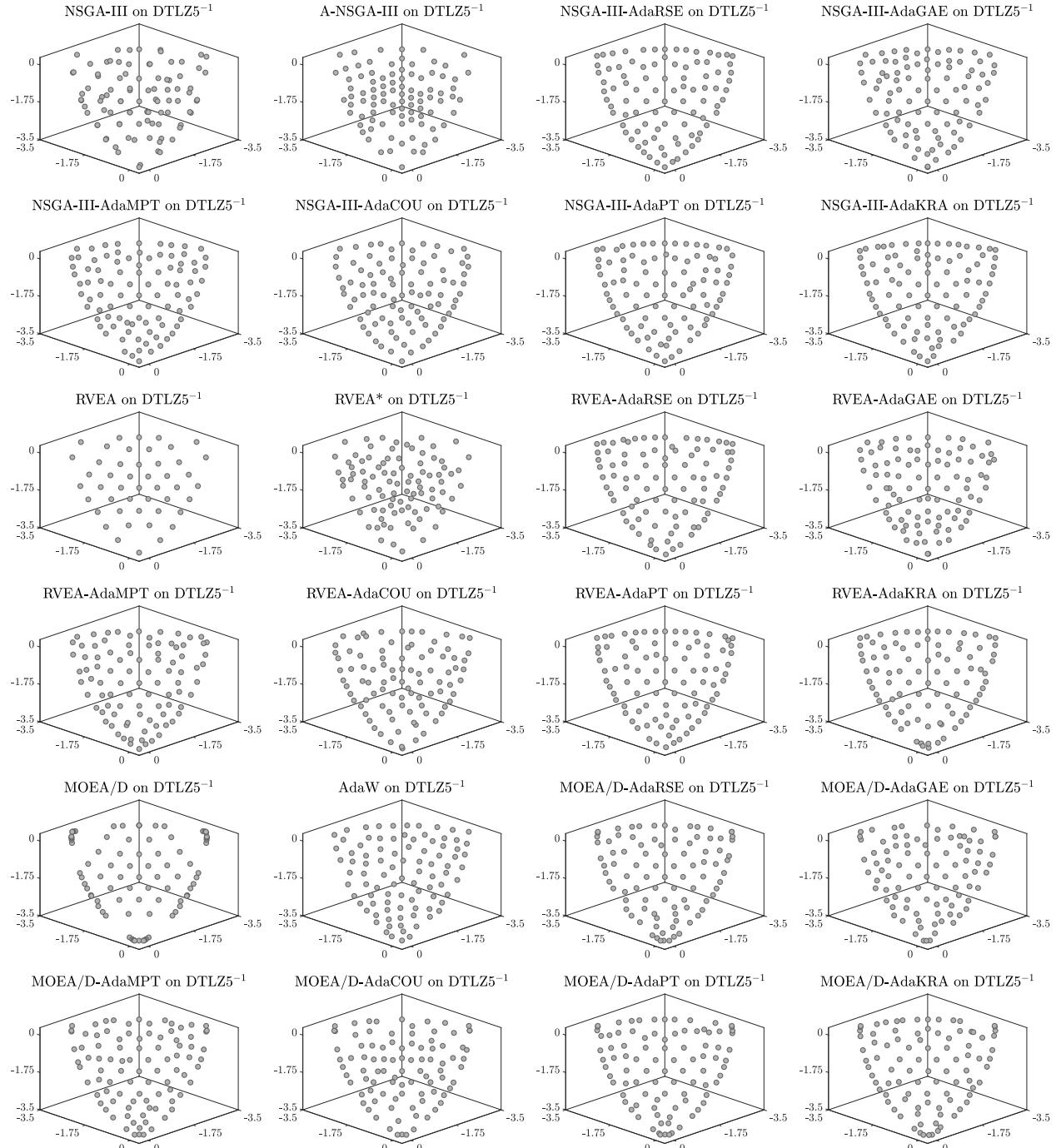


Figure 81: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on $DTLZ5^{-1}$ with 3 objective functions.

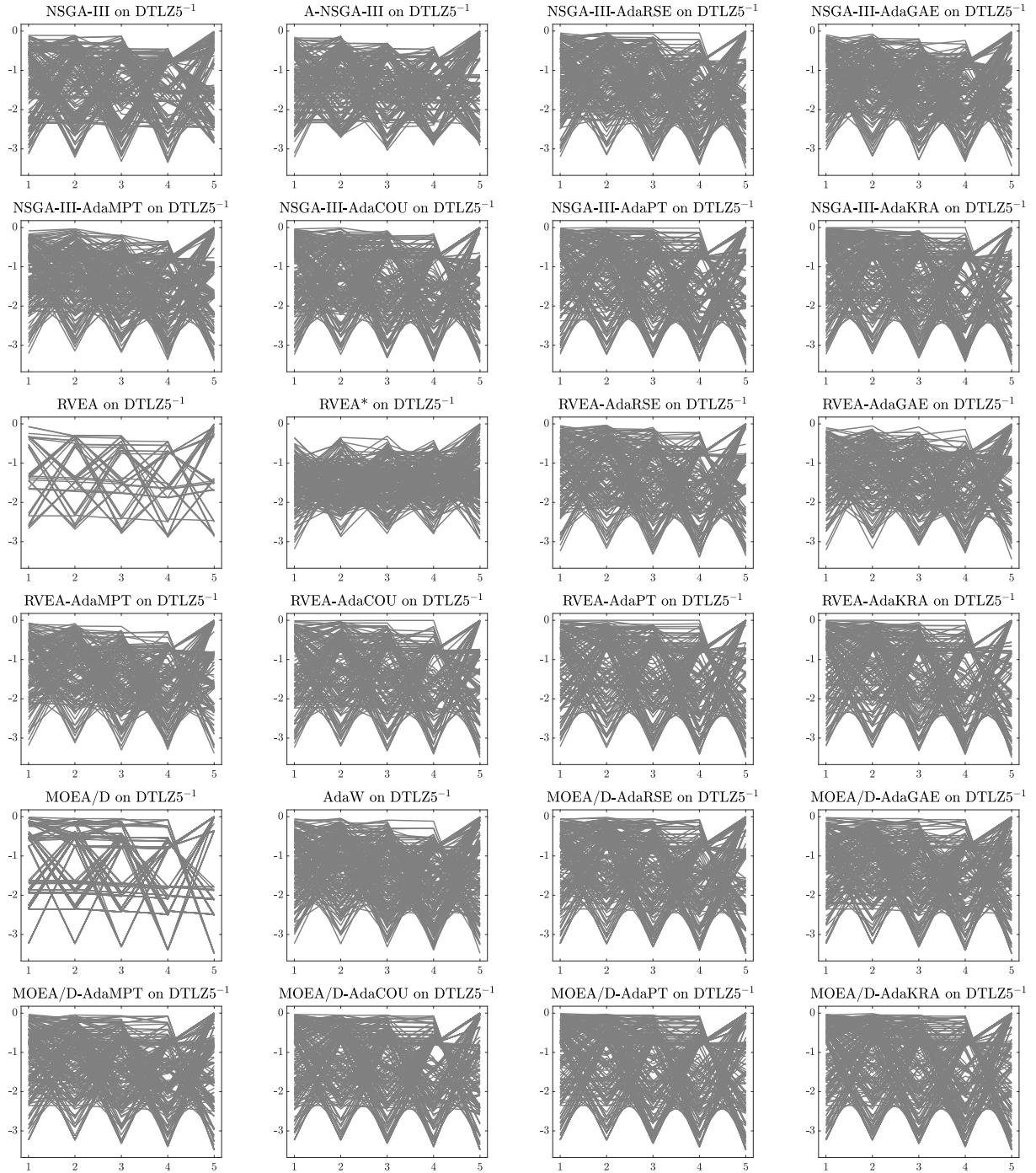


Figure 82: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ5⁻¹ with 5 objective functions.

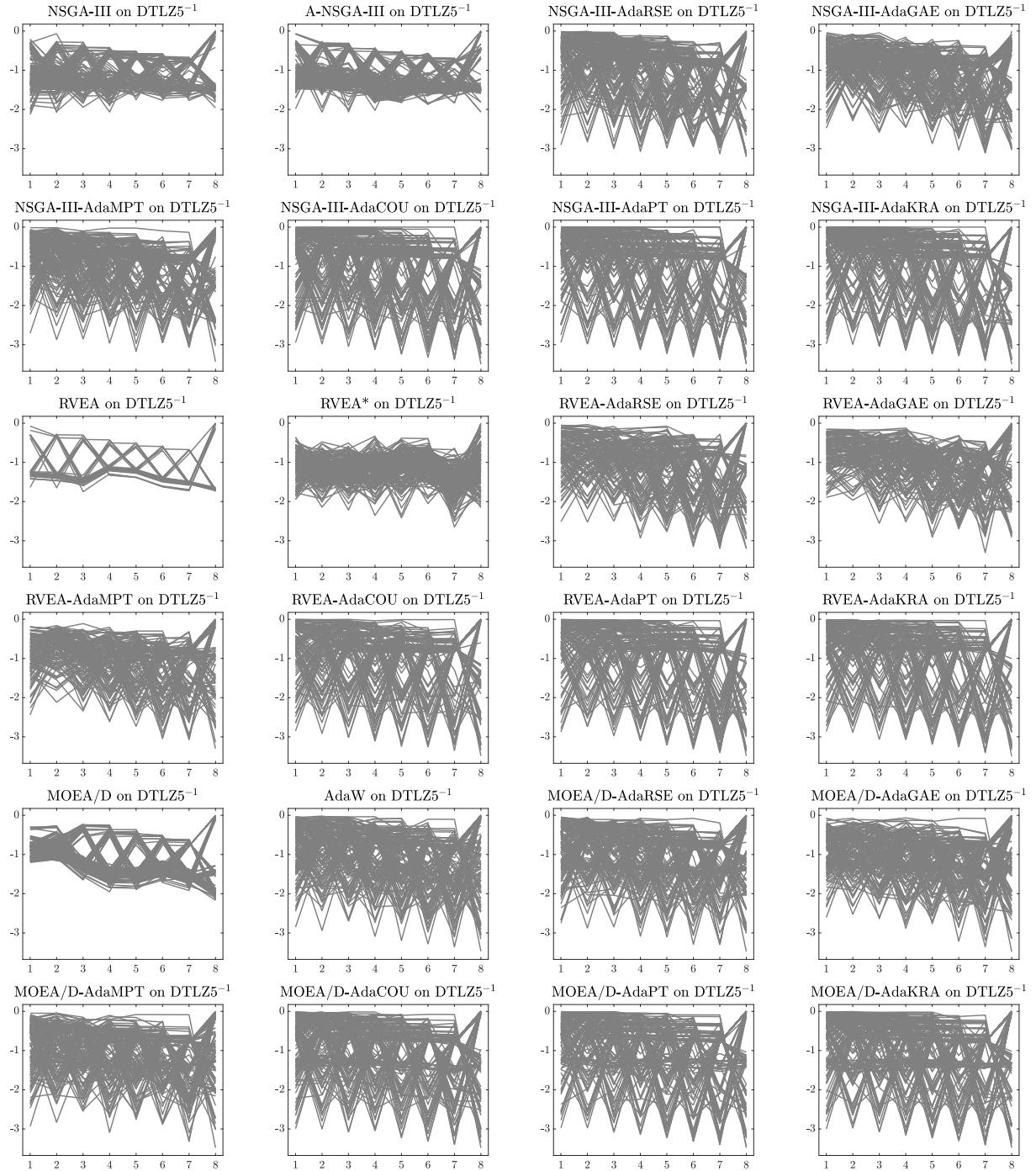


Figure 83: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ5⁻¹ with 8 objective functions.

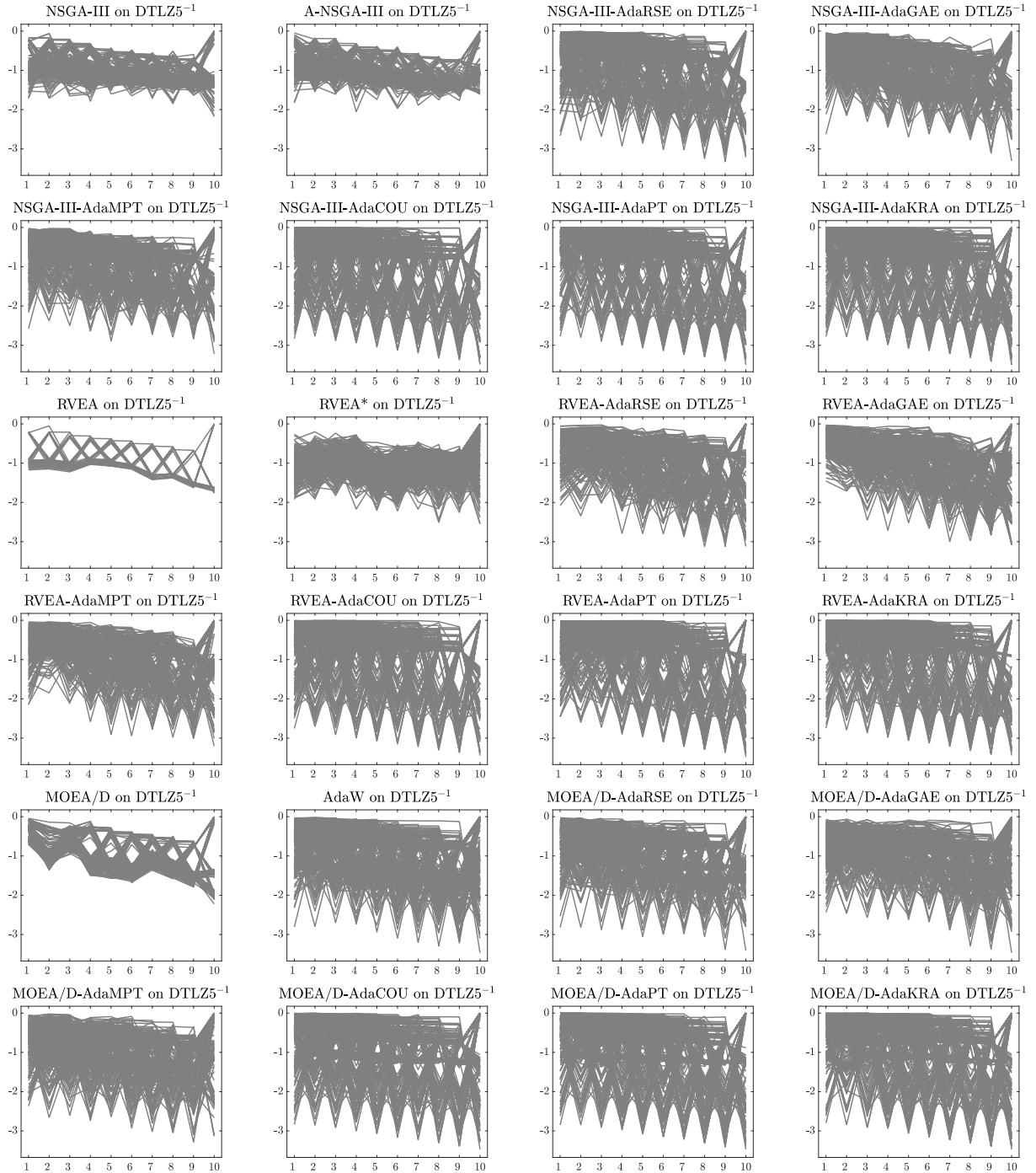


Figure 84: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ5⁻¹ with 10 objective functions.

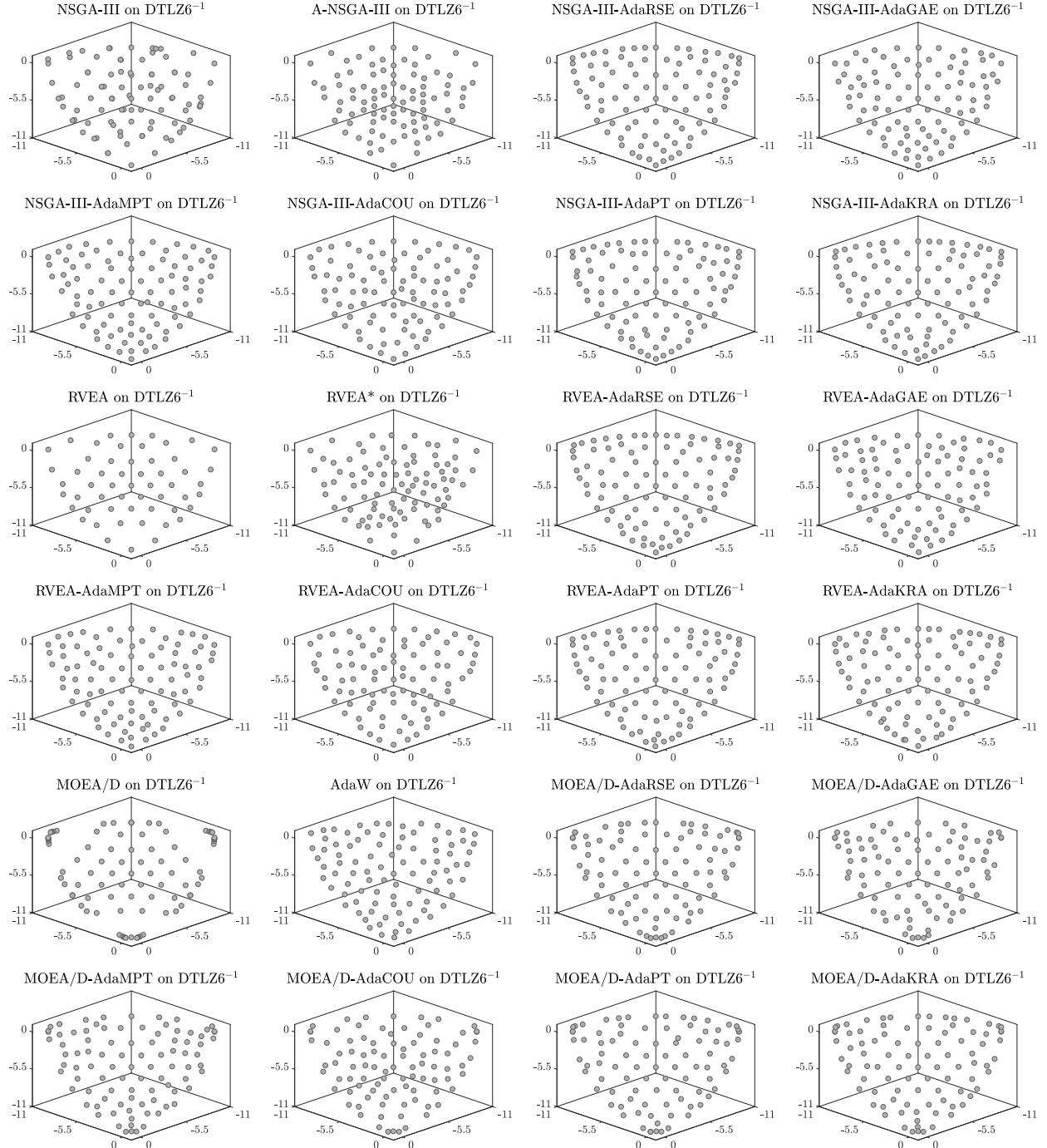


Figure 85: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on $DTLZ6^{-1}$ with 3 objective functions.

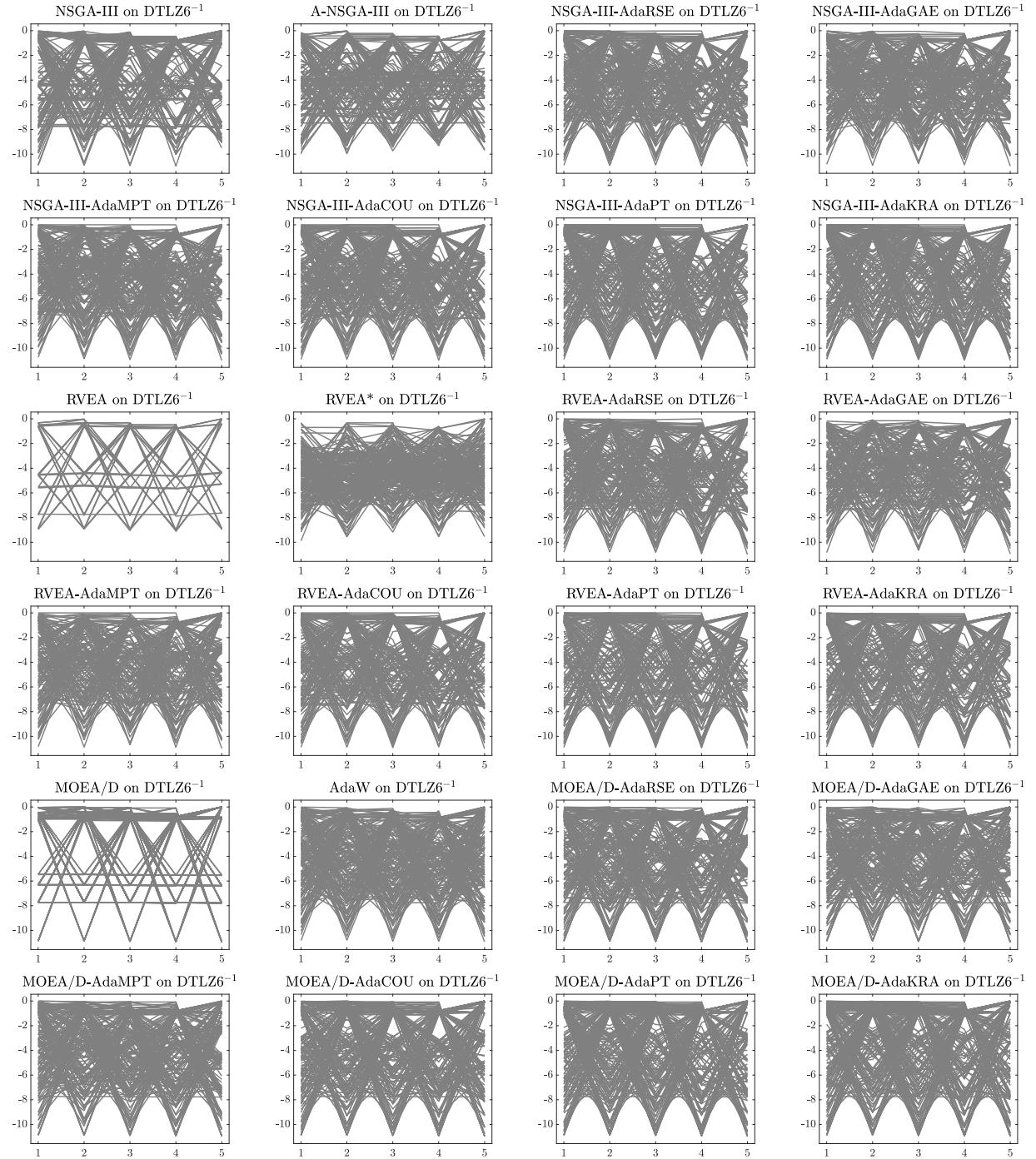


Figure 86: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ6⁻¹ with 5 objective functions.

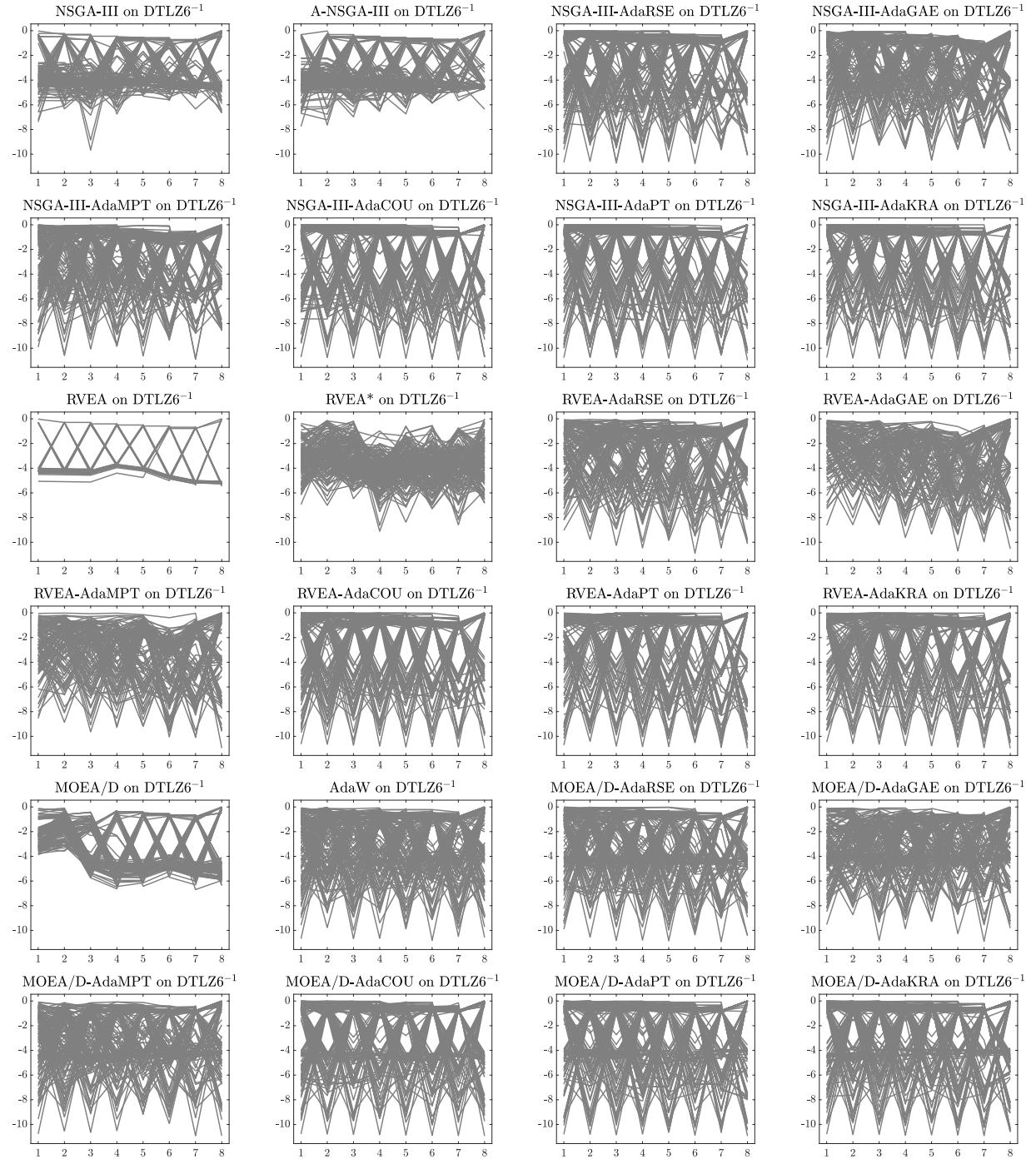


Figure 87: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ6⁻¹ with 8 objective functions.

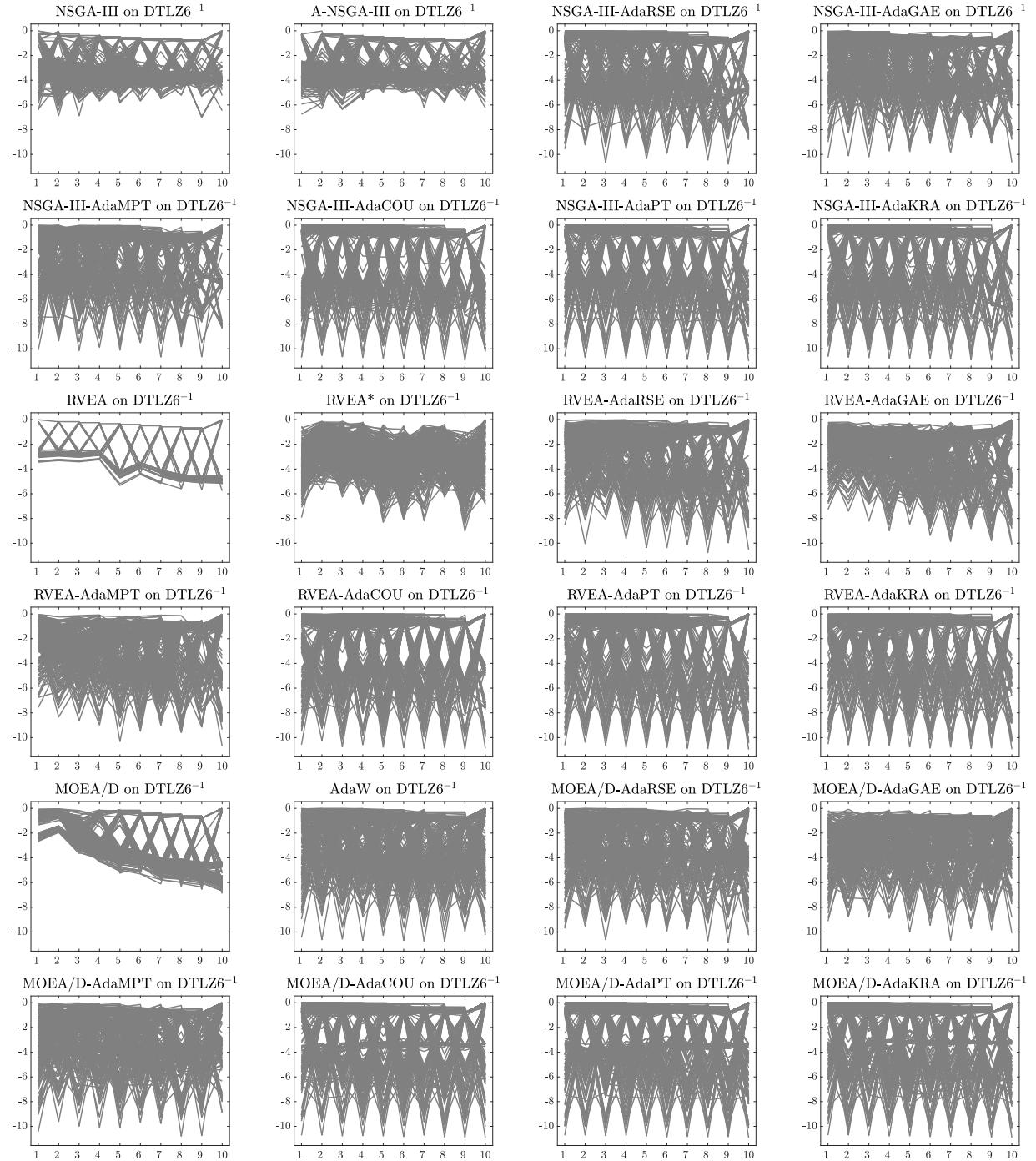


Figure 88: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ6⁻¹ with 10 objective functions.

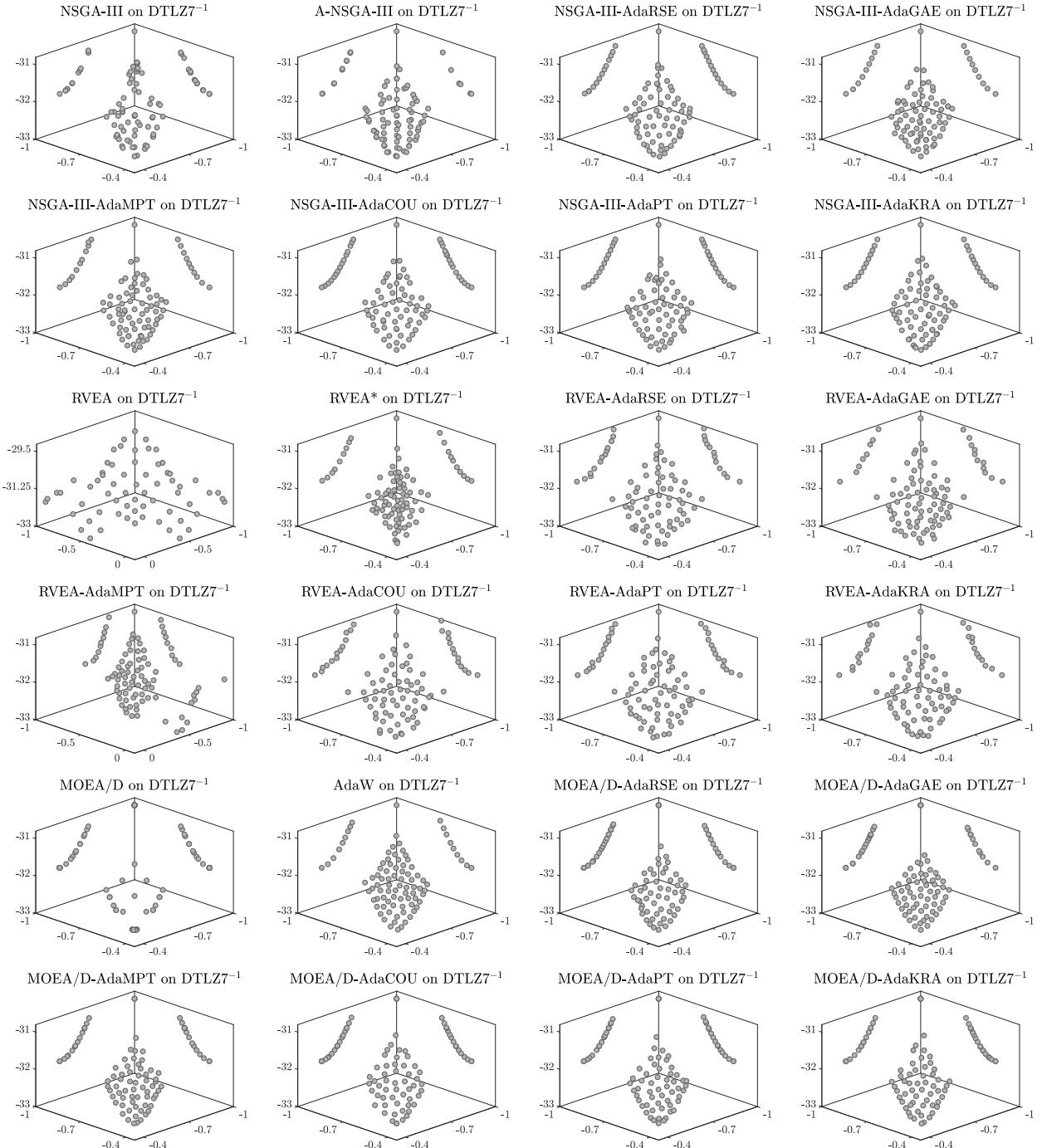


Figure 89: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on $DTLZ7^{-1}$ with 3 objective functions.

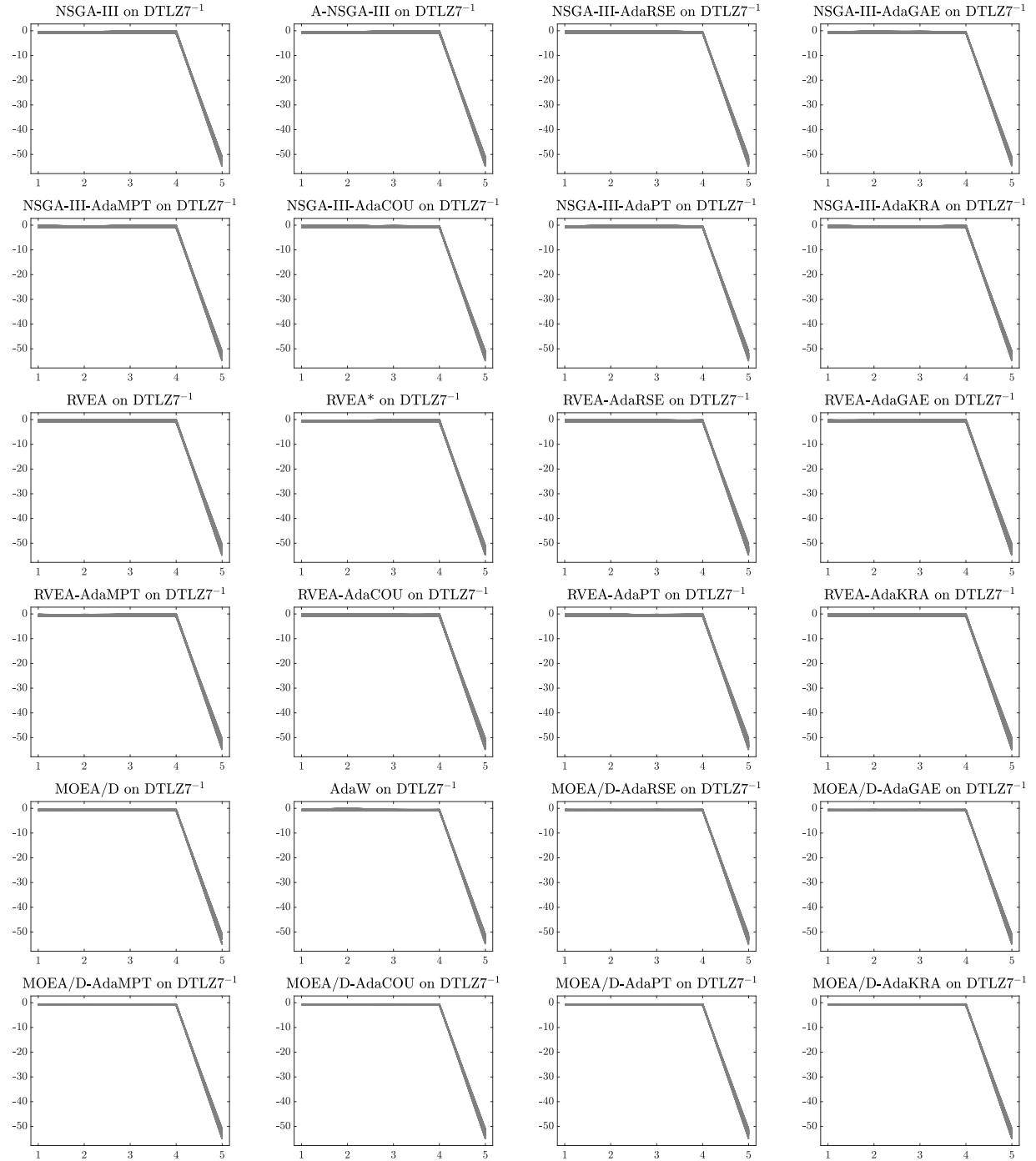


Figure 90: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ7⁻¹ with 5 objective functions.

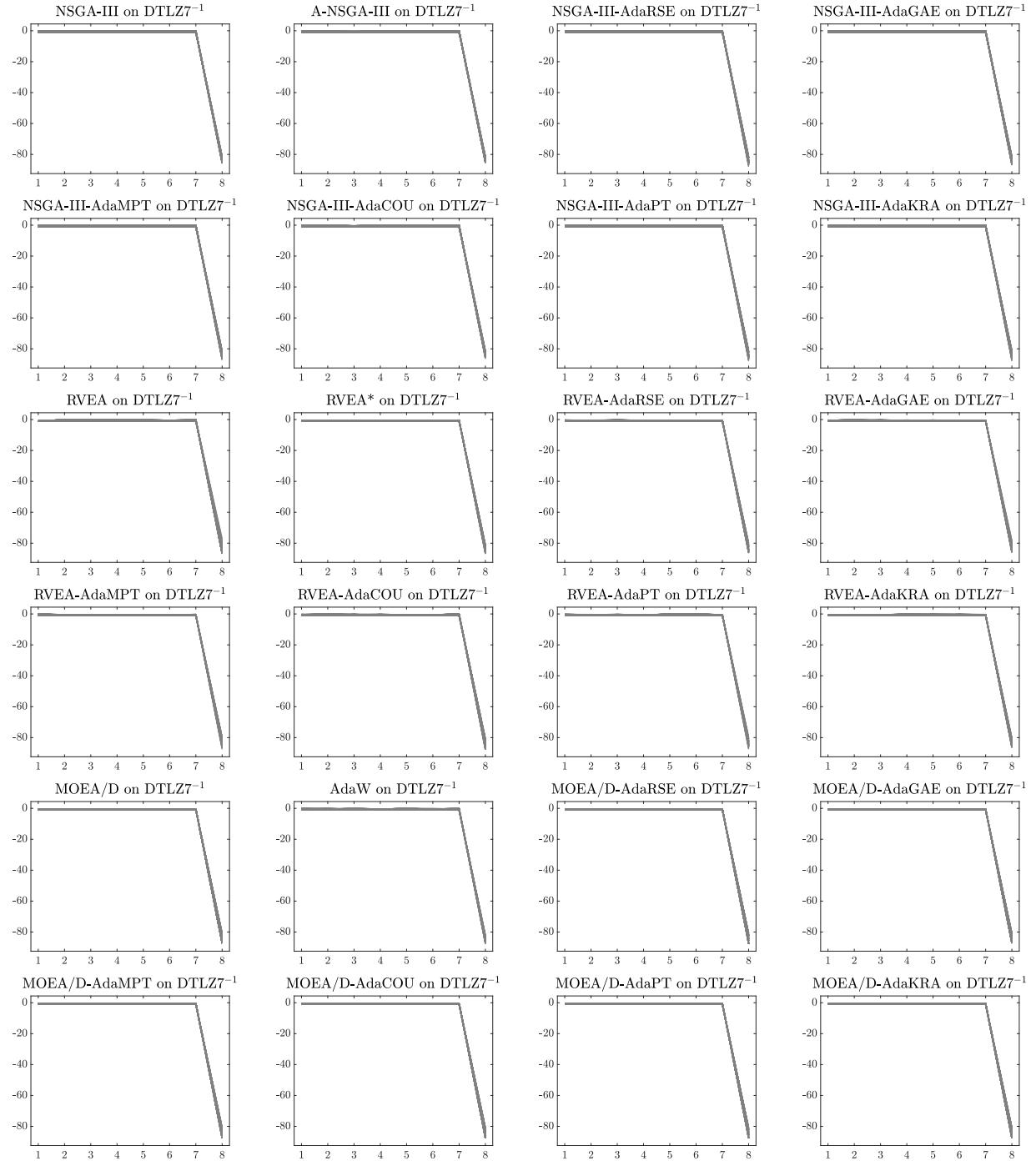


Figure 91: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on $DTLZ7^{-1}$ with 8 objective functions.

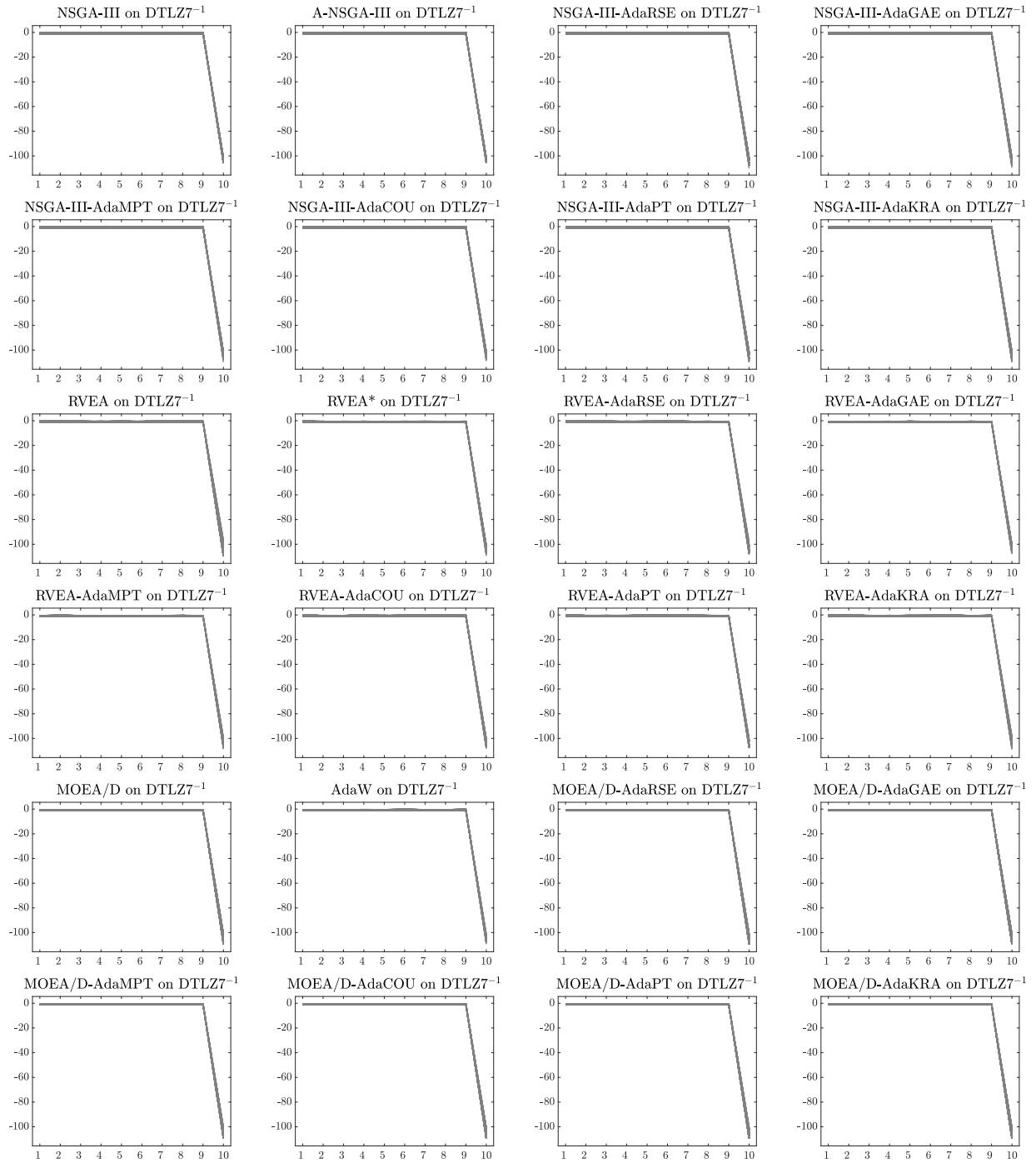


Figure 92: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on $DTLZ7^{-1}$ with 10 objective functions.

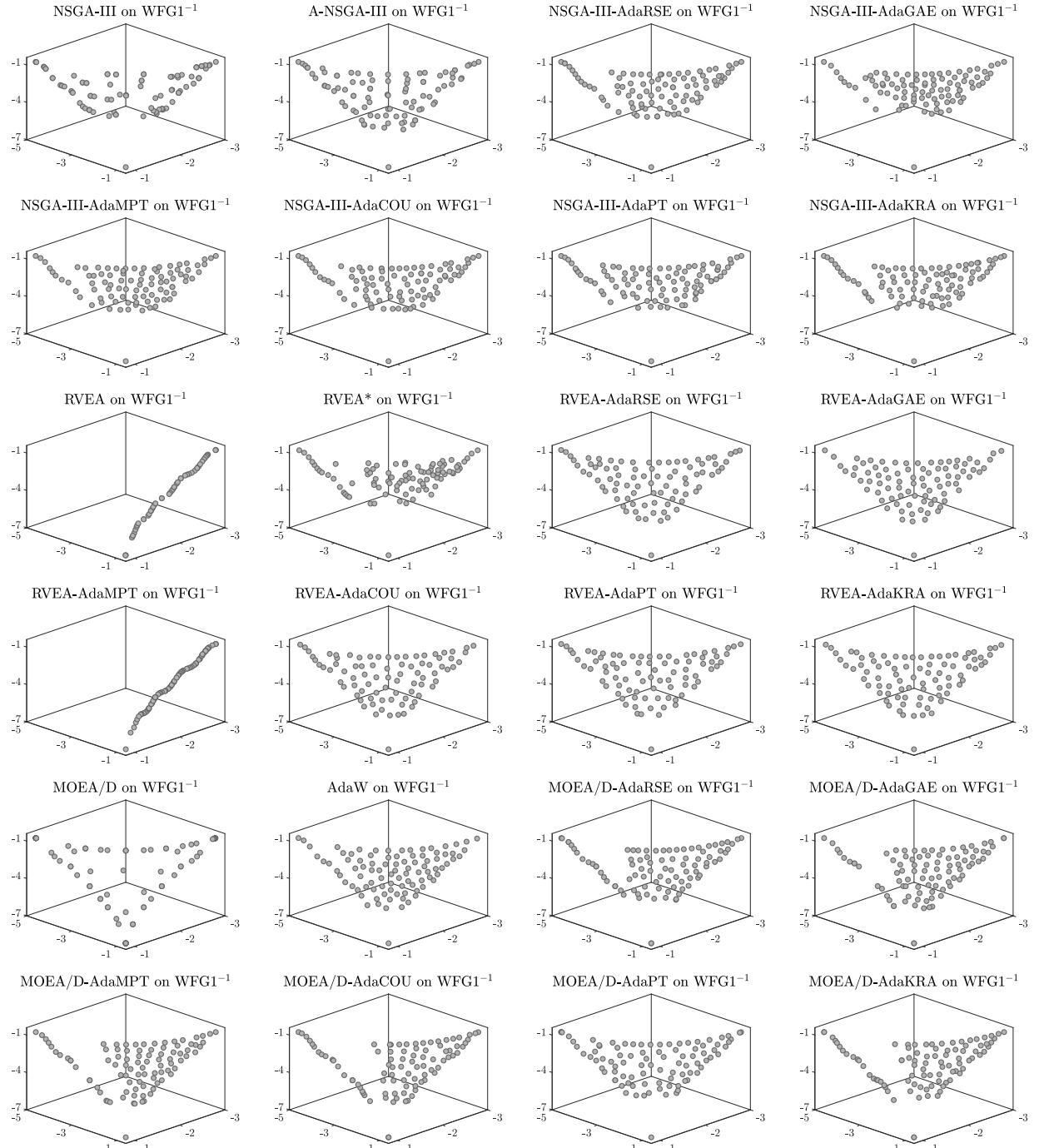


Figure 93: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG1^{-1} with 3 objective functions.

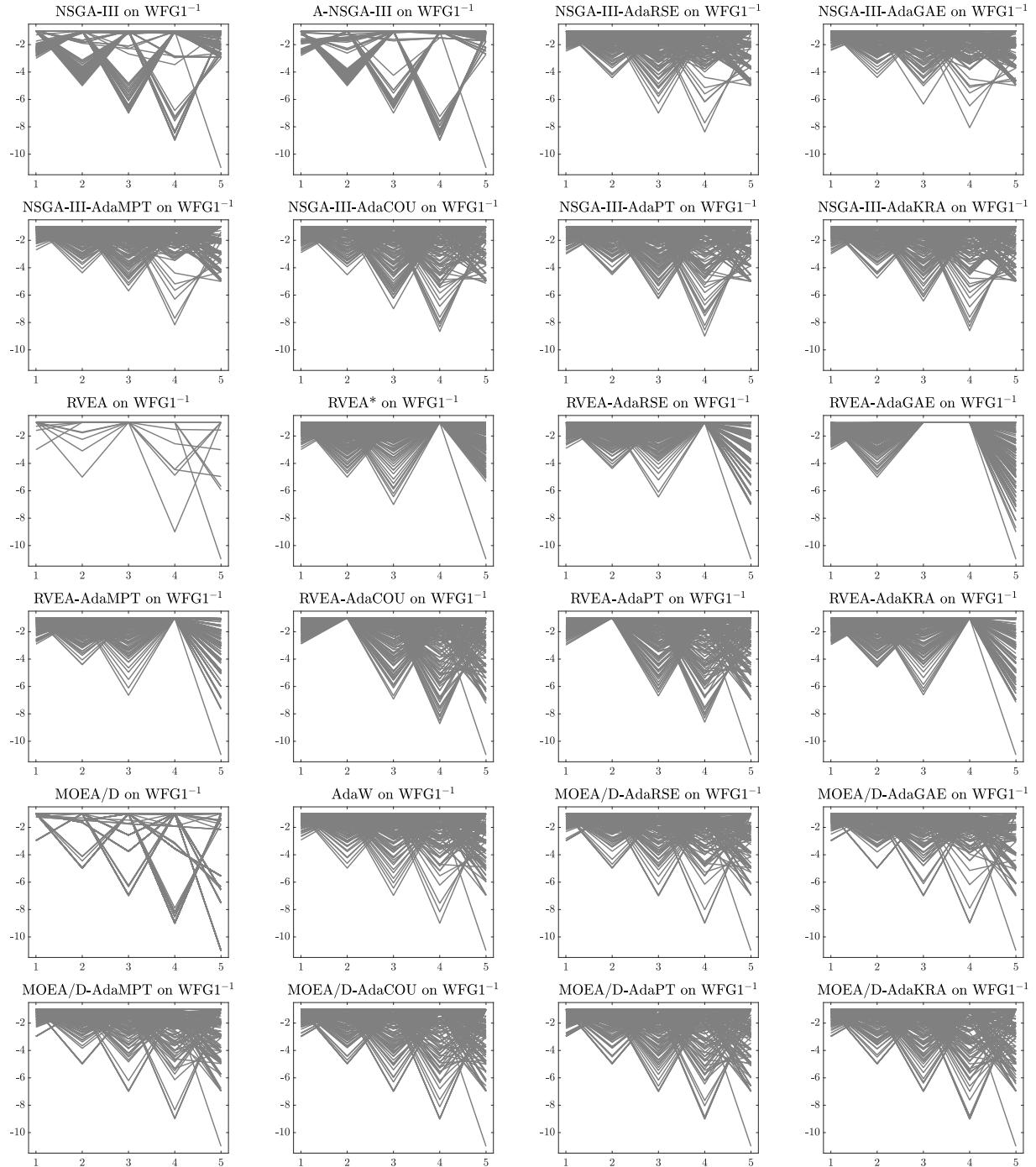


Figure 94: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG1⁻¹ with 5 objective functions.

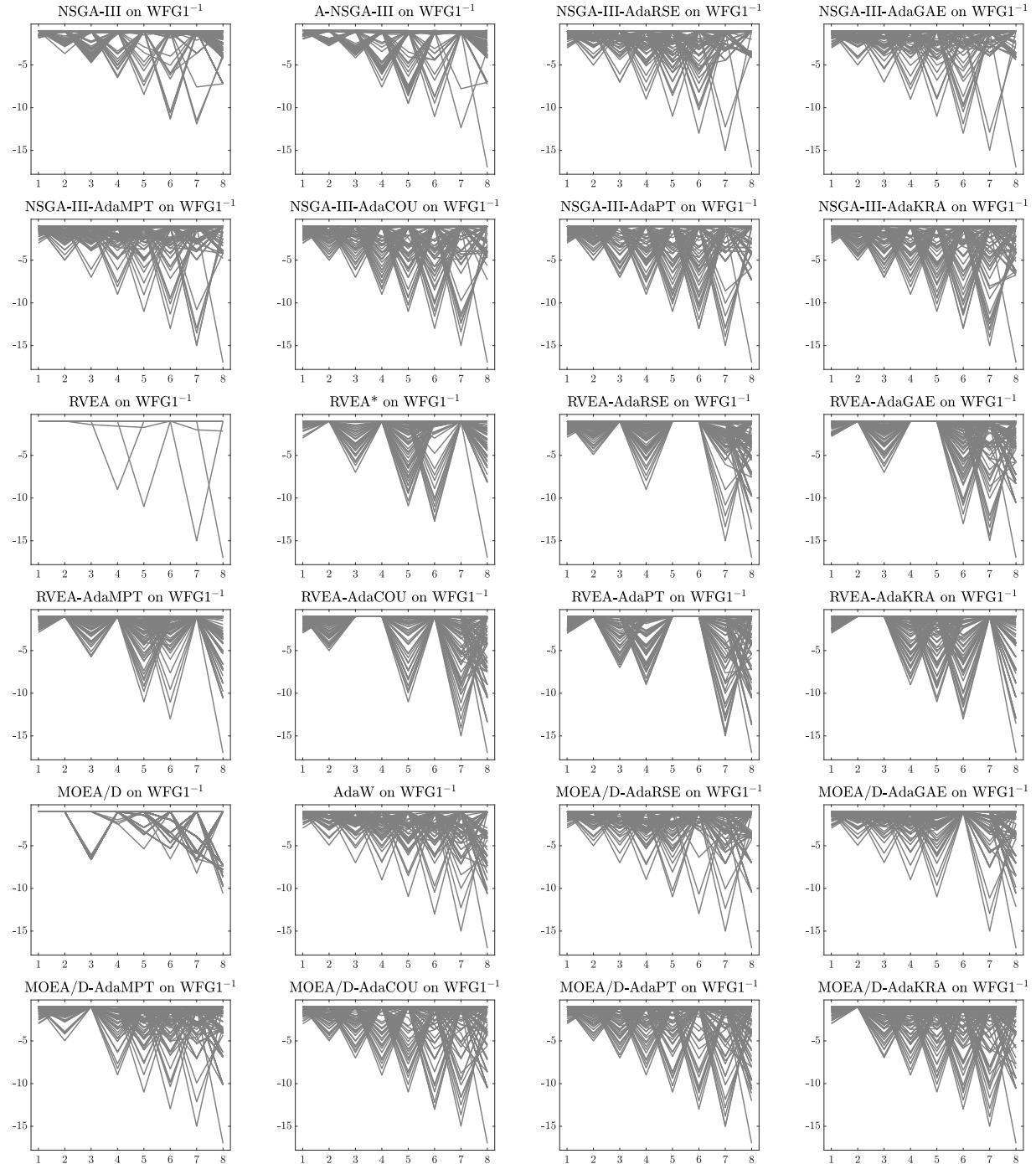


Figure 95: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG1⁻¹ with 8 objective functions.

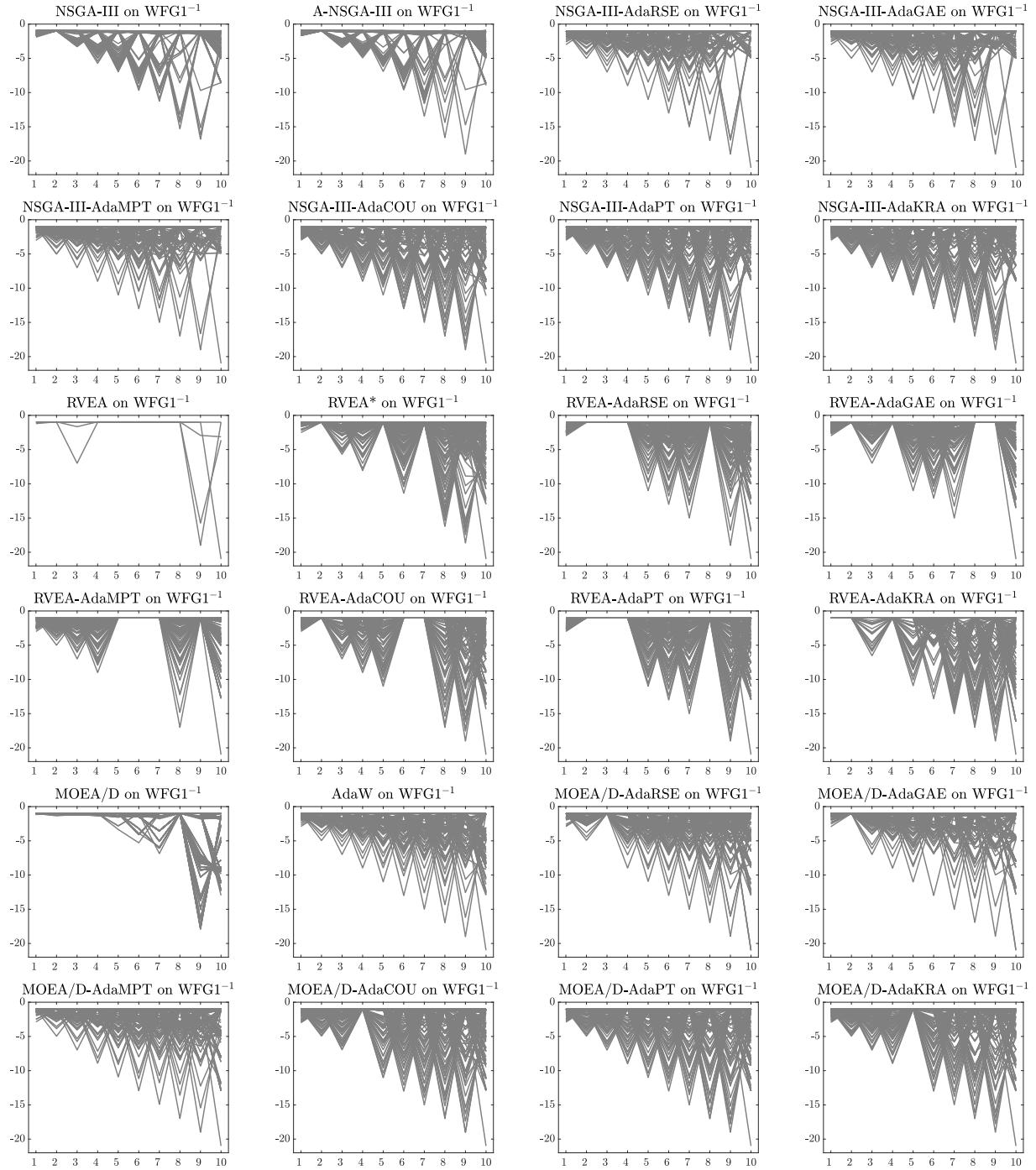


Figure 96: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG1⁻¹ with 10 objective functions.

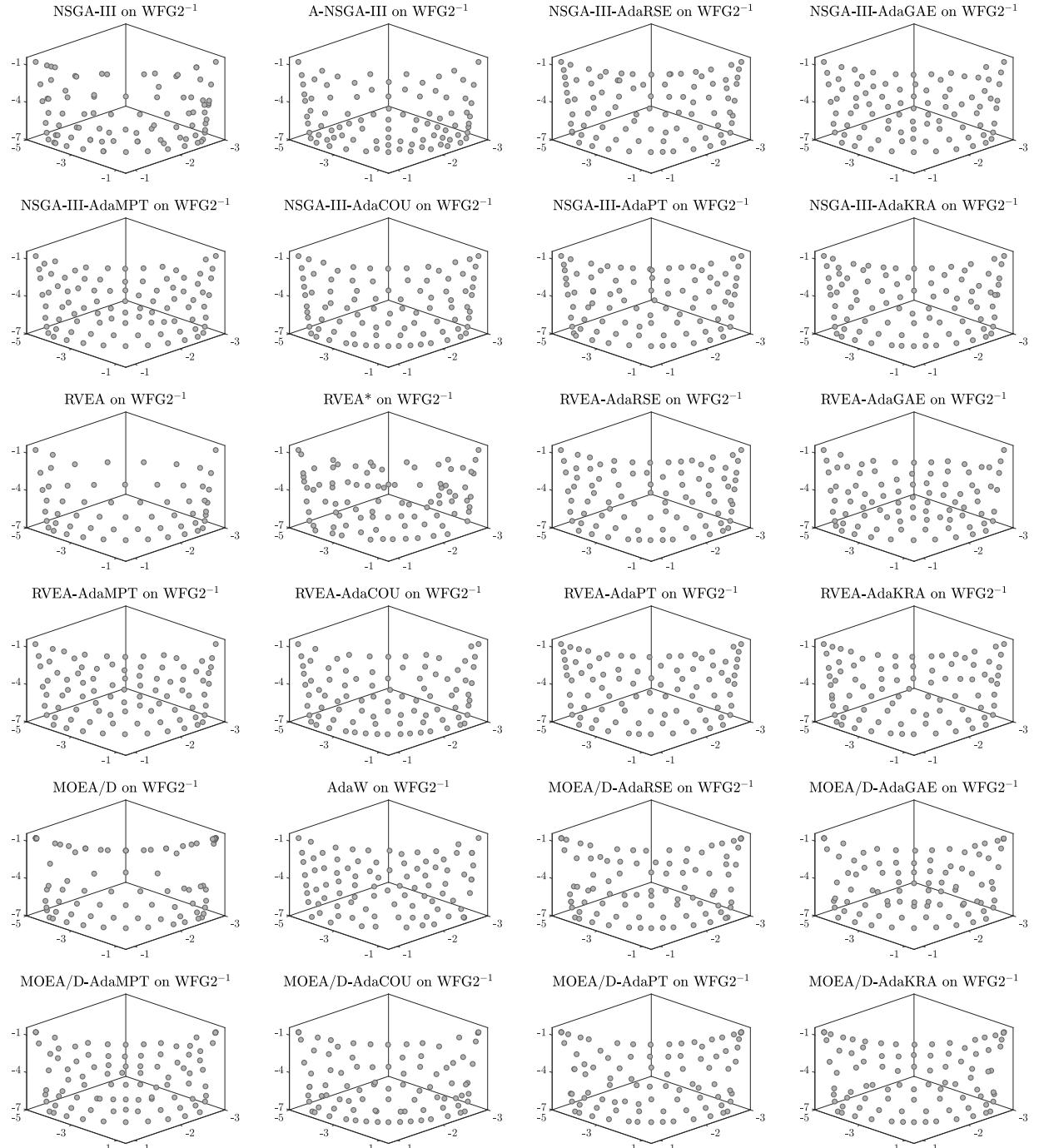


Figure 97: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG2^{-1} with 3 objective functions.

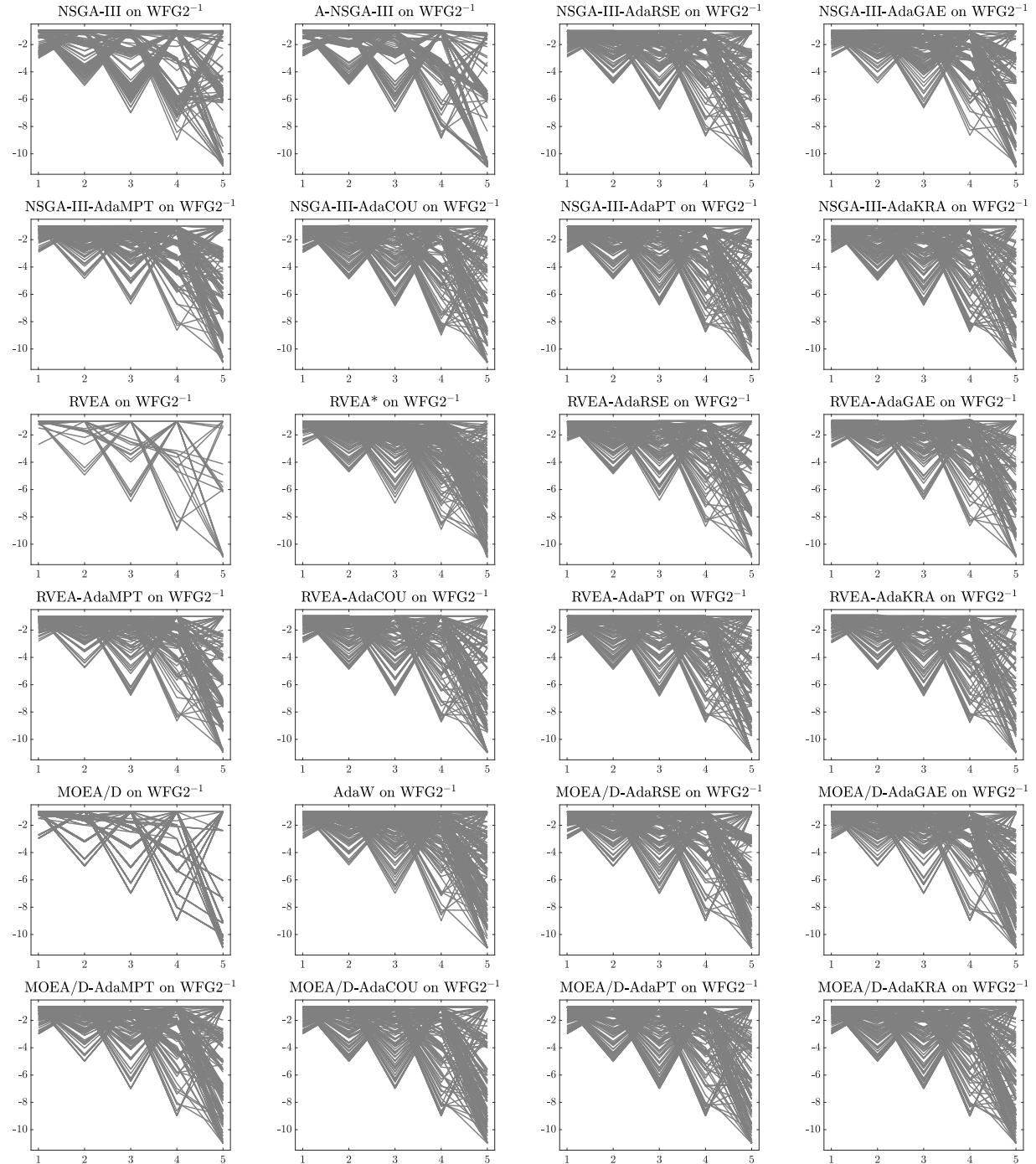


Figure 98: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG2⁻¹ with 5 objective functions.

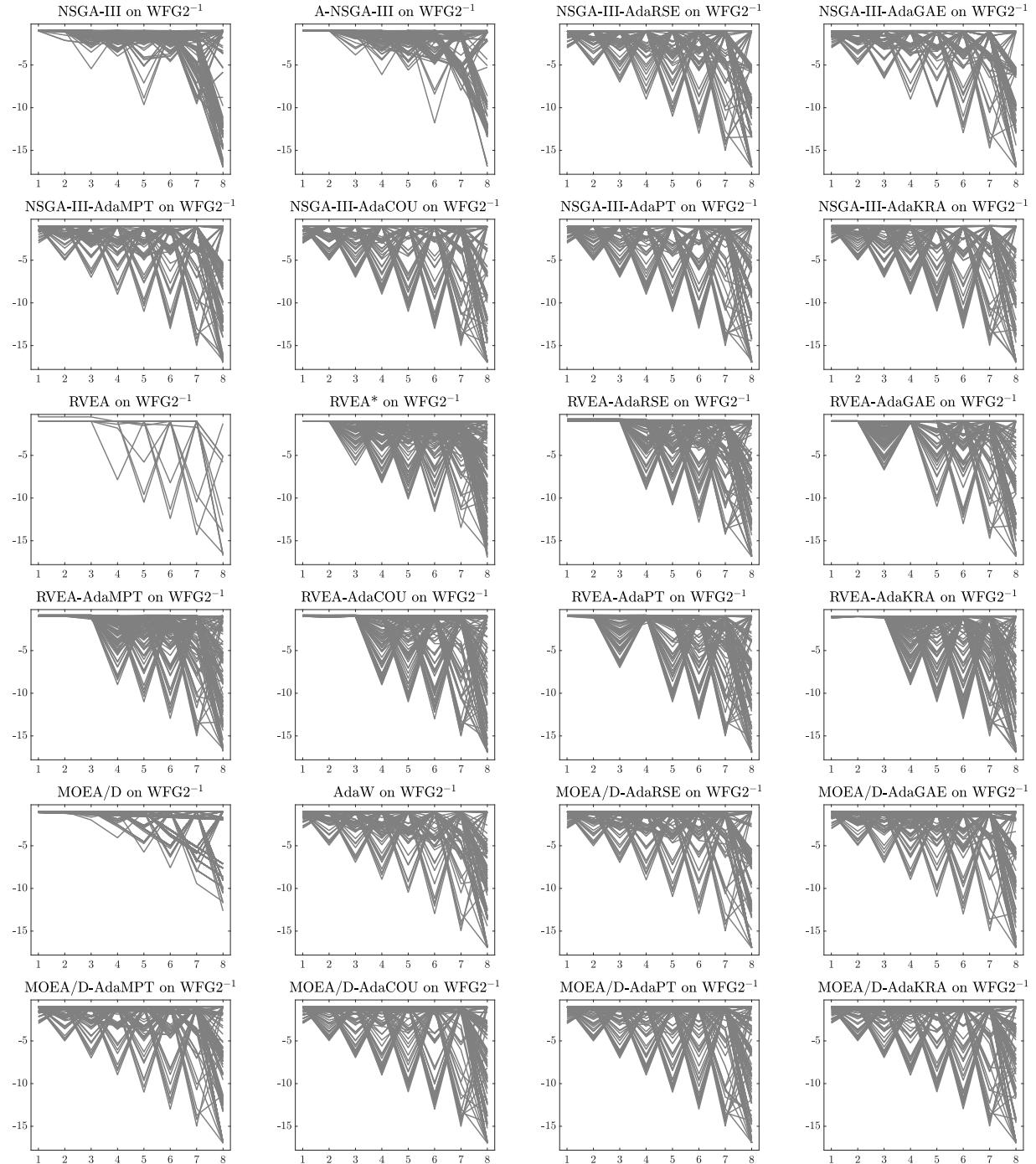


Figure 99: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG2^{-1} with 8 objective functions.

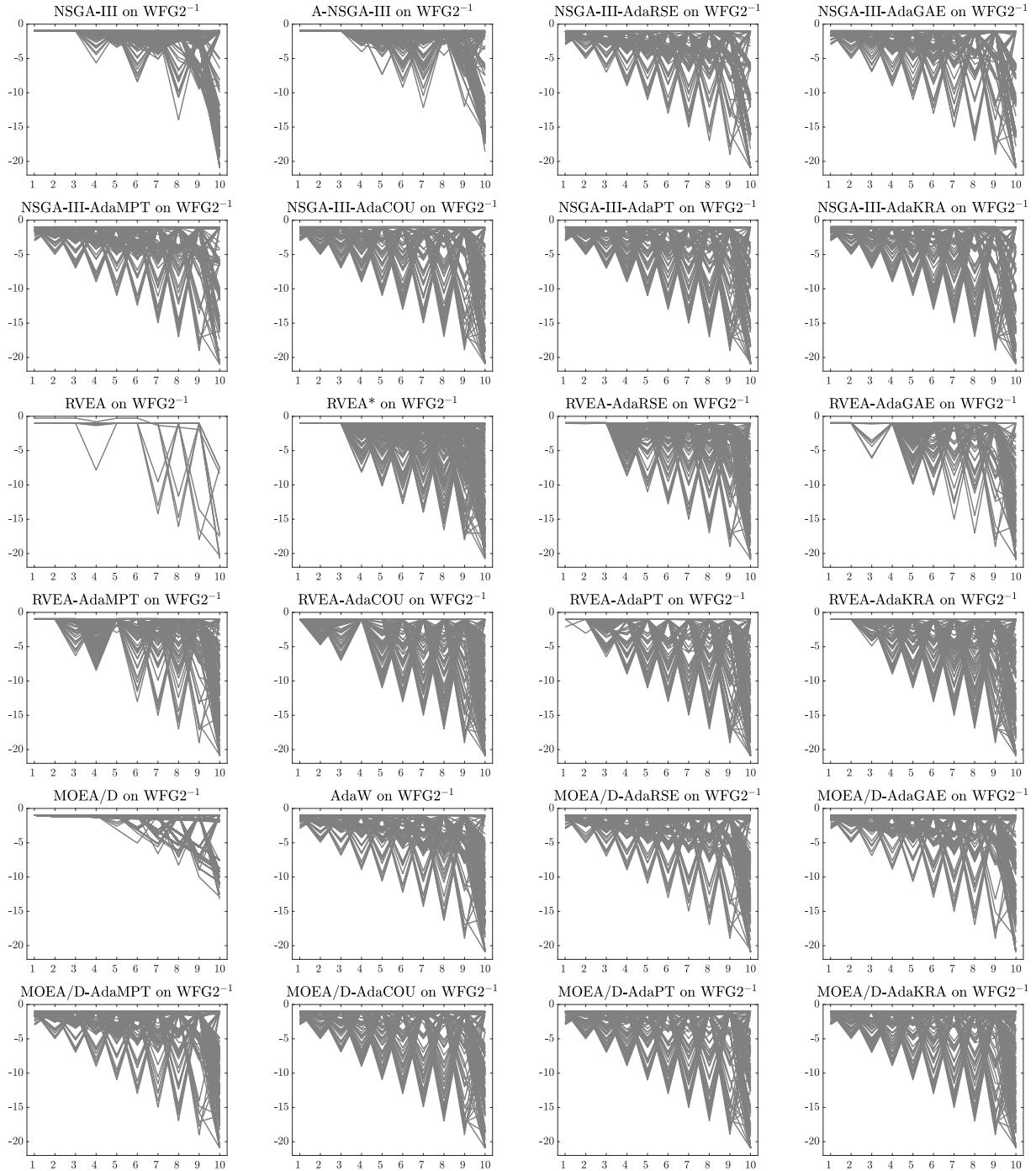


Figure 100: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG2^{-1} with 10 objective functions.

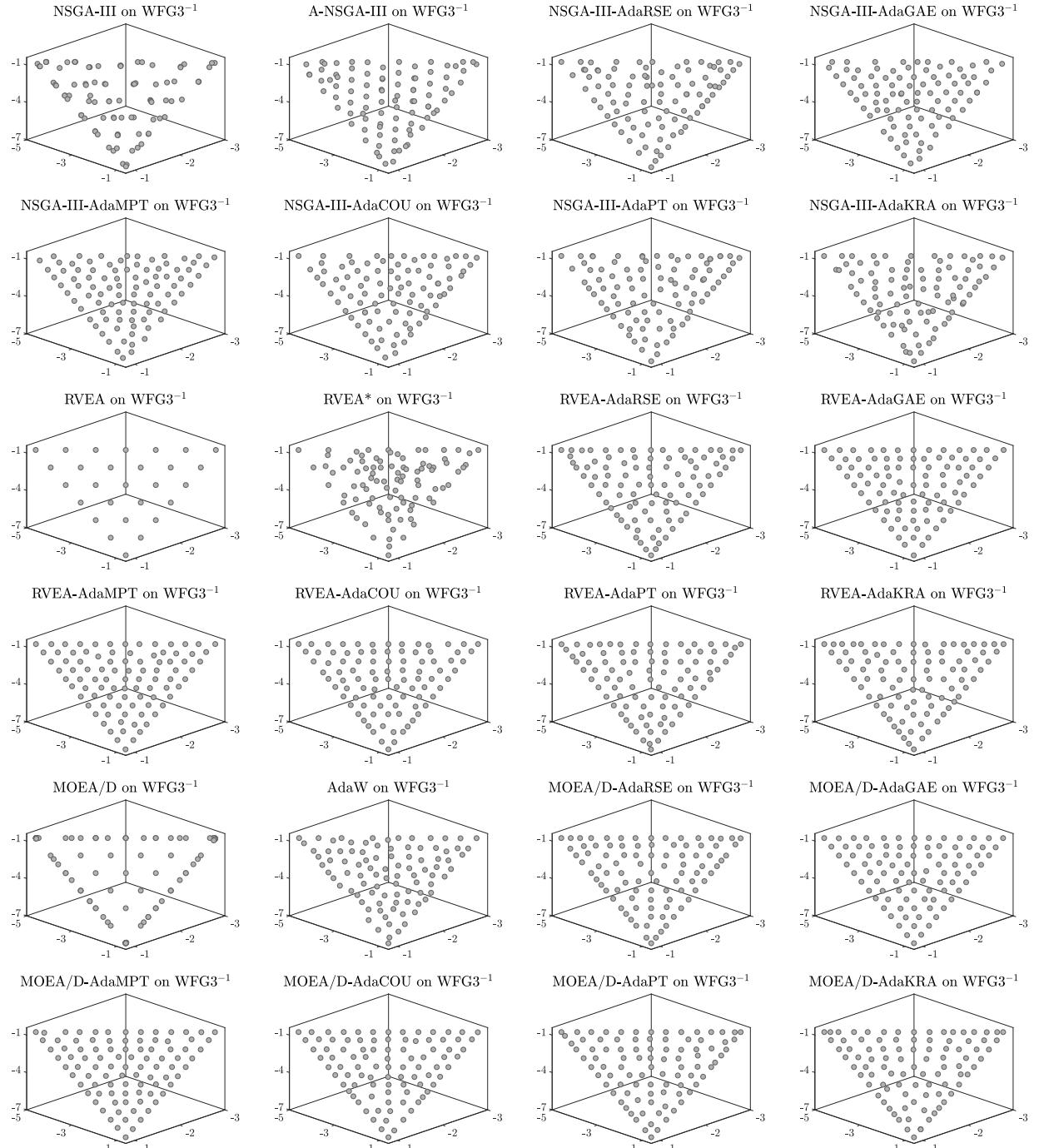


Figure 101: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG3^{-1} with 3 objective functions.

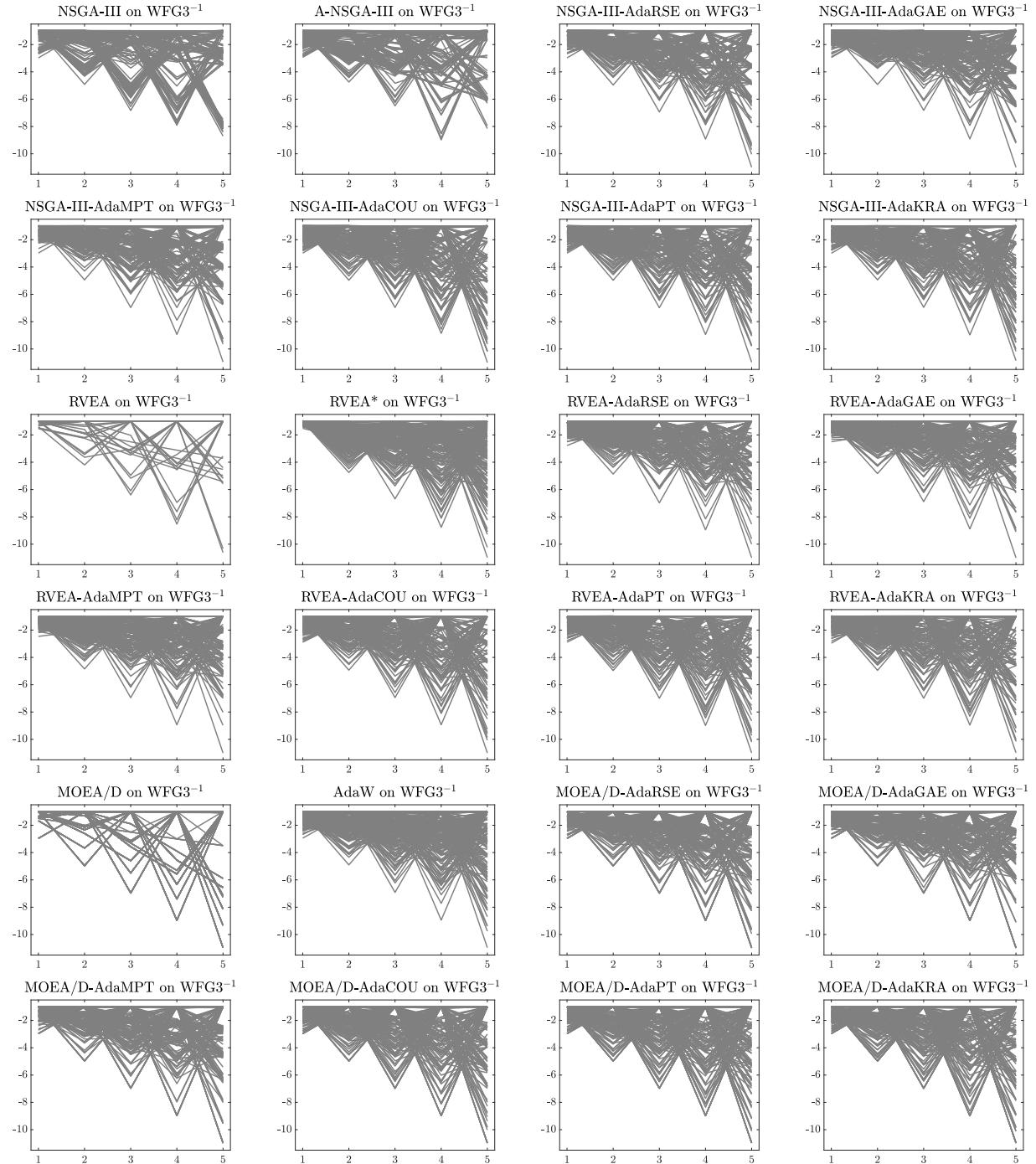


Figure 102: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG3⁻¹ with 5 objective functions.

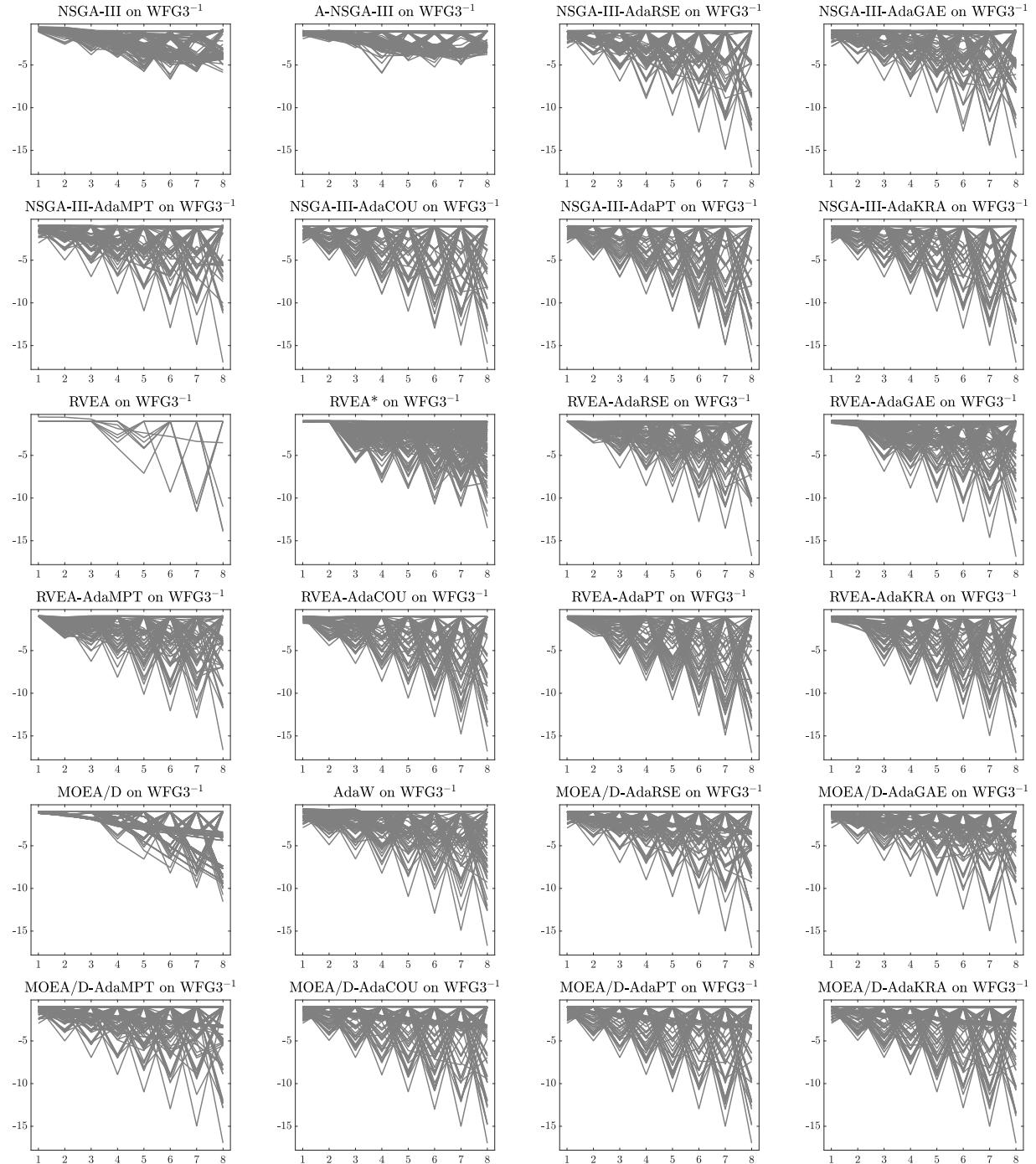


Figure 103: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG3^{-1} with 8 objective functions.

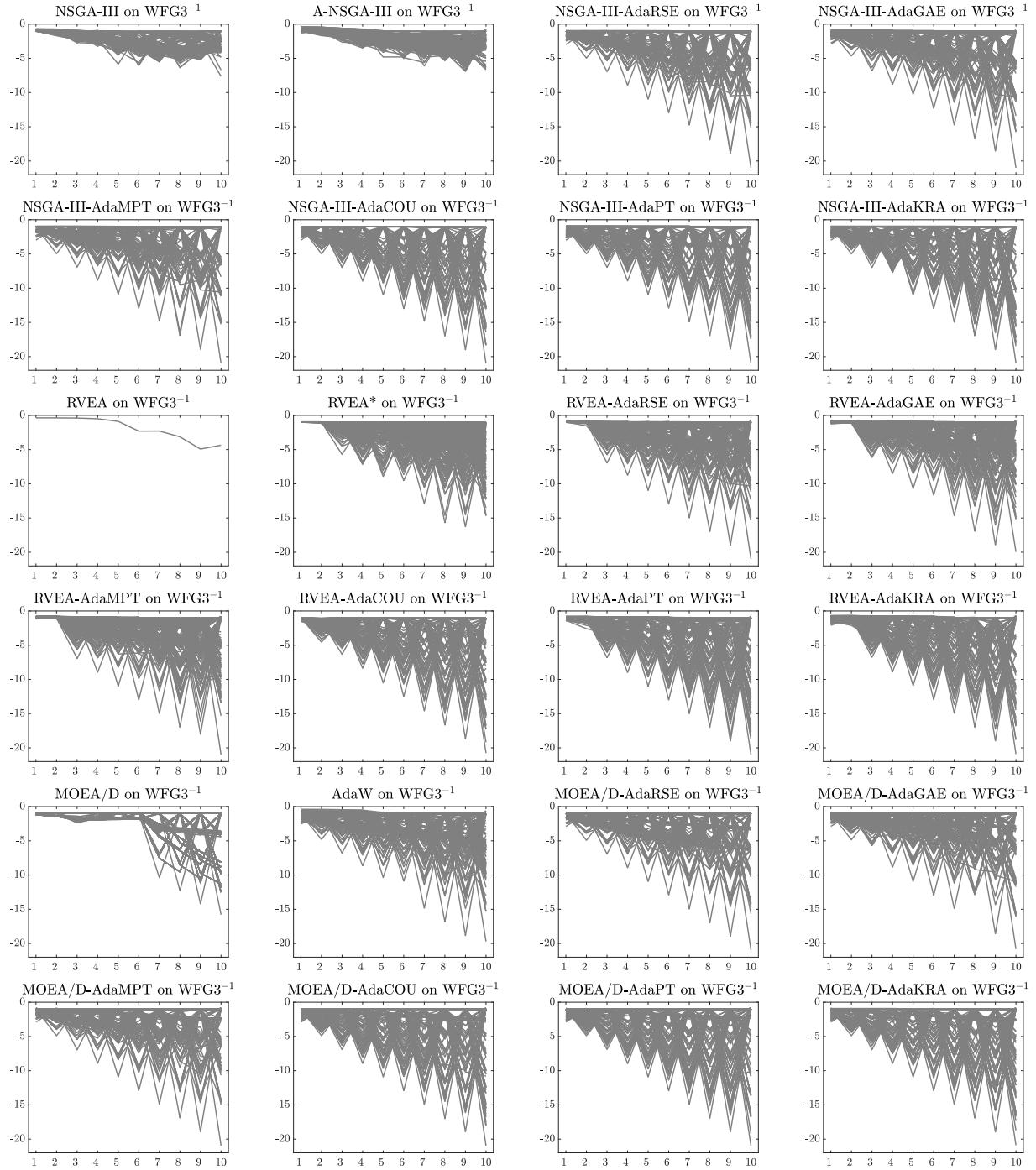


Figure 104: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG3^{-1} with 10 objective functions.

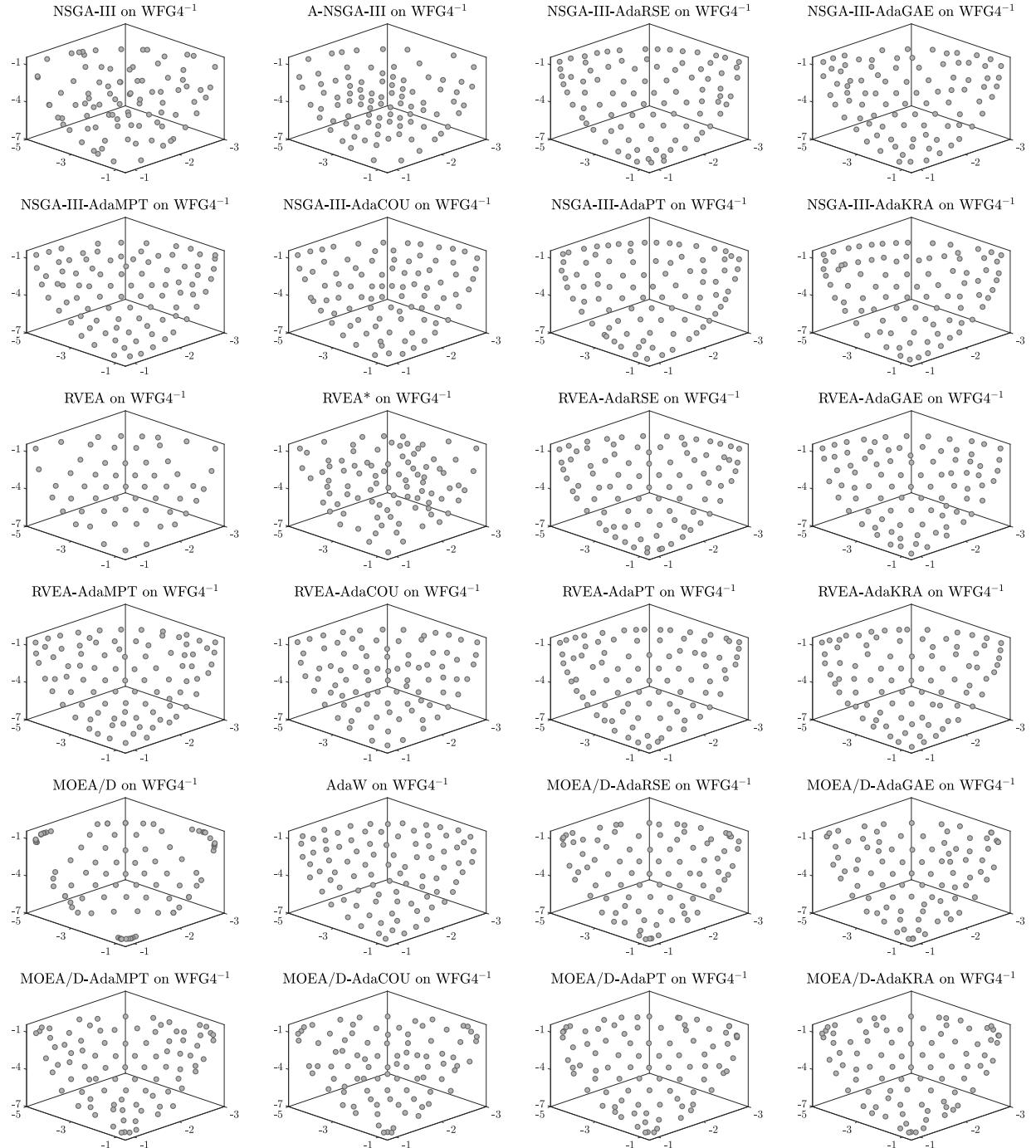


Figure 105: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG4^{-1} with 3 objective functions.

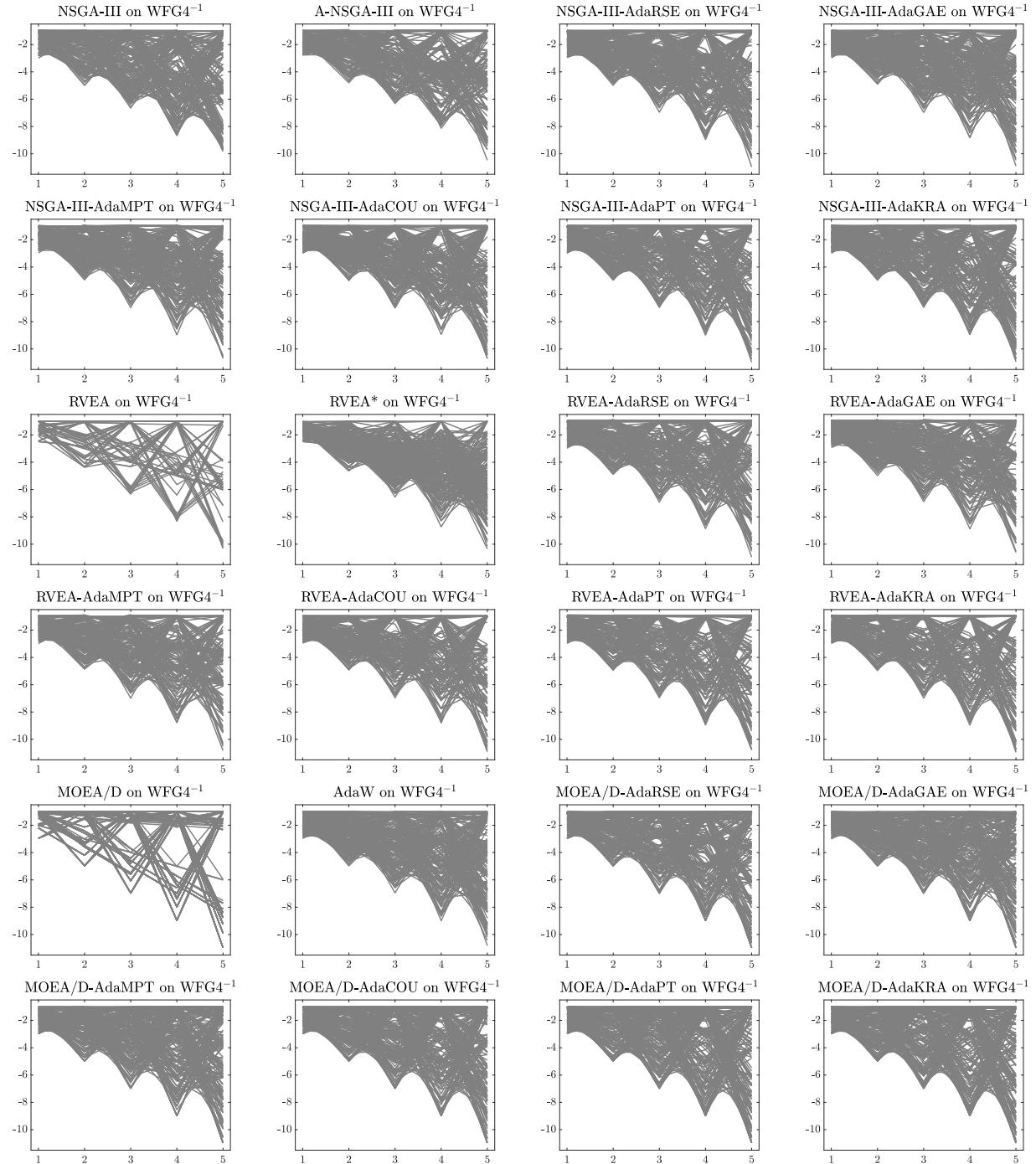


Figure 106: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG4^{-1} with 5 objective functions.

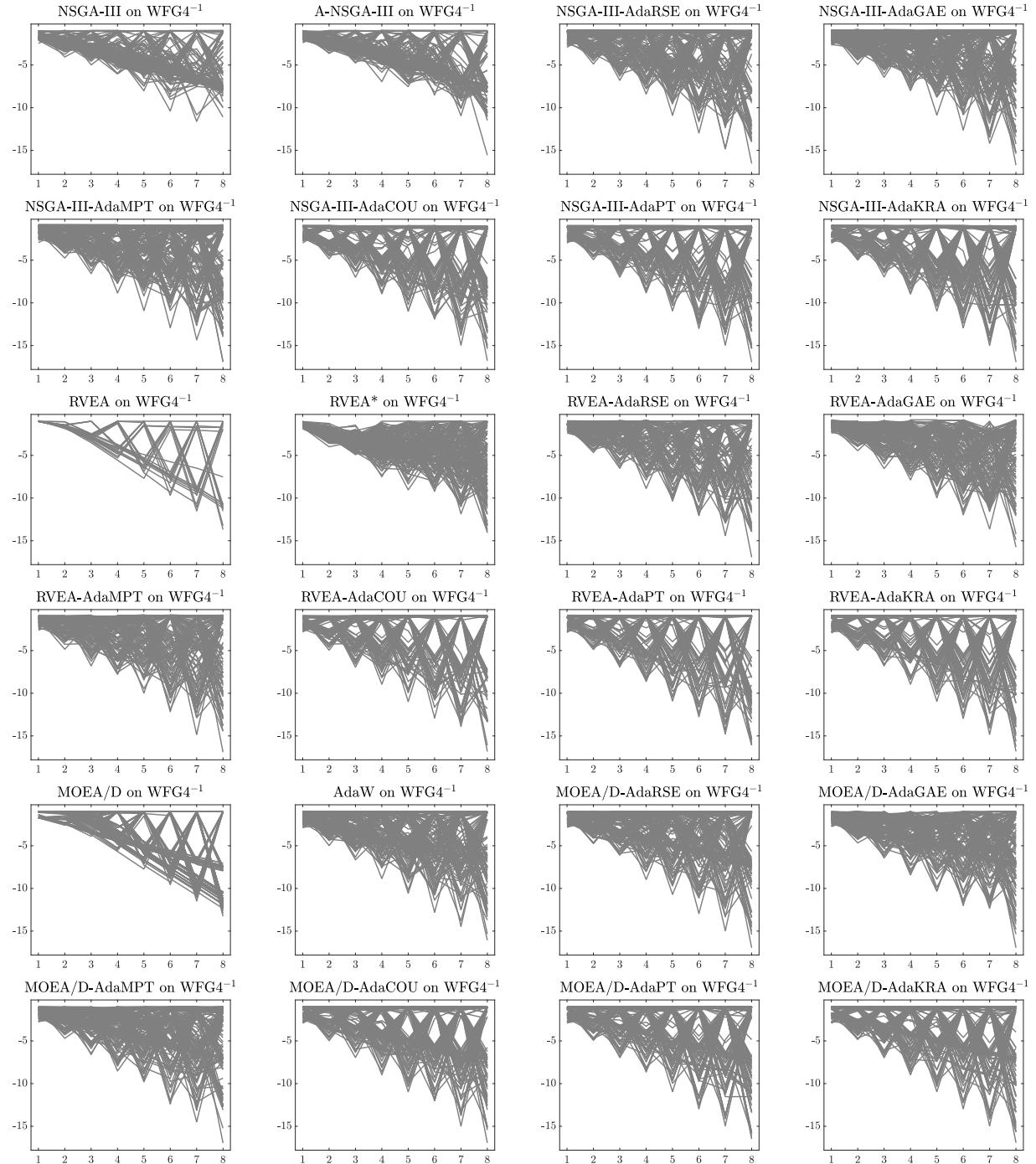


Figure 107: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG4^{-1} with 8 objective functions.

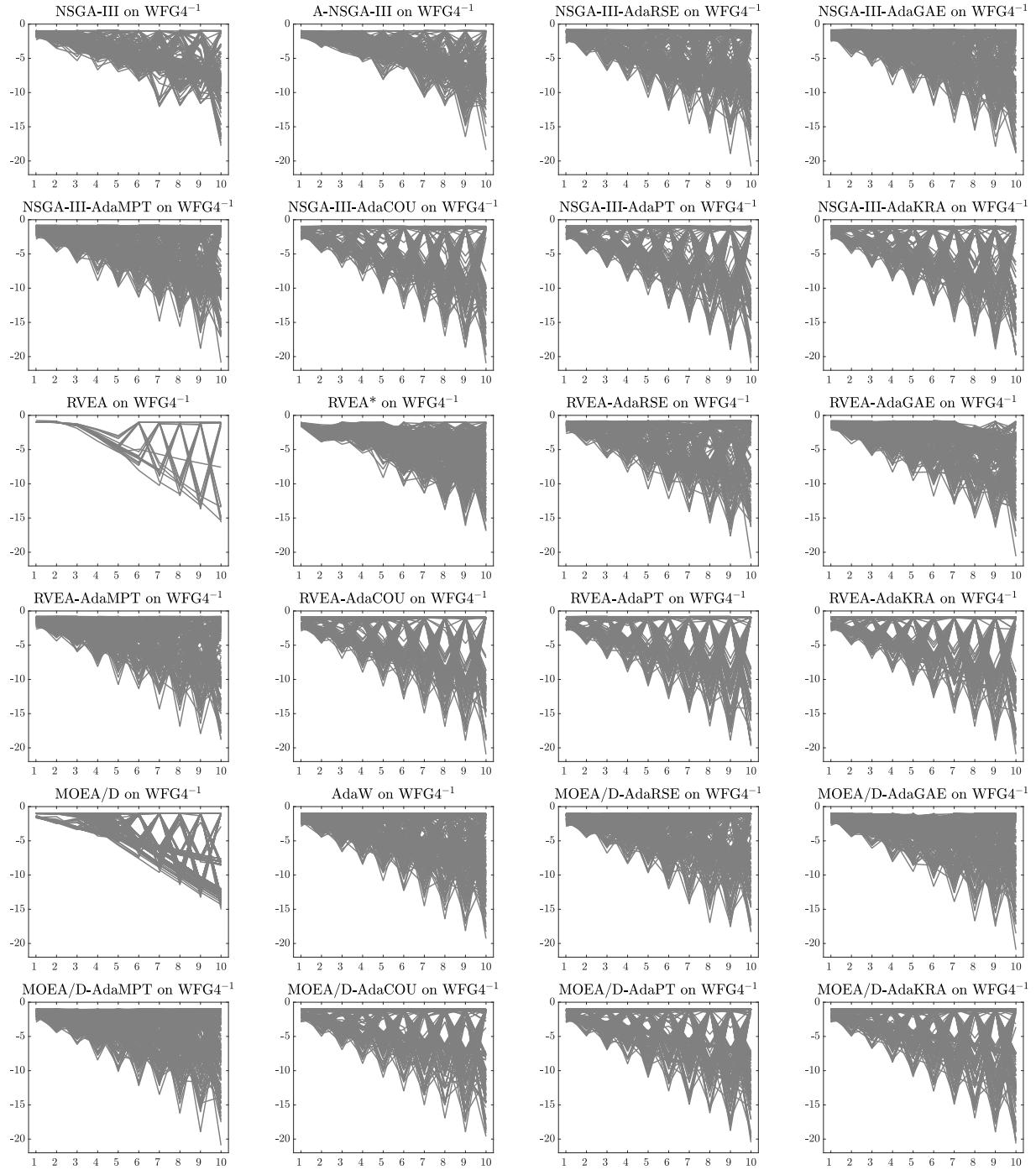


Figure 108: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG4^{-1} with 10 objective functions.

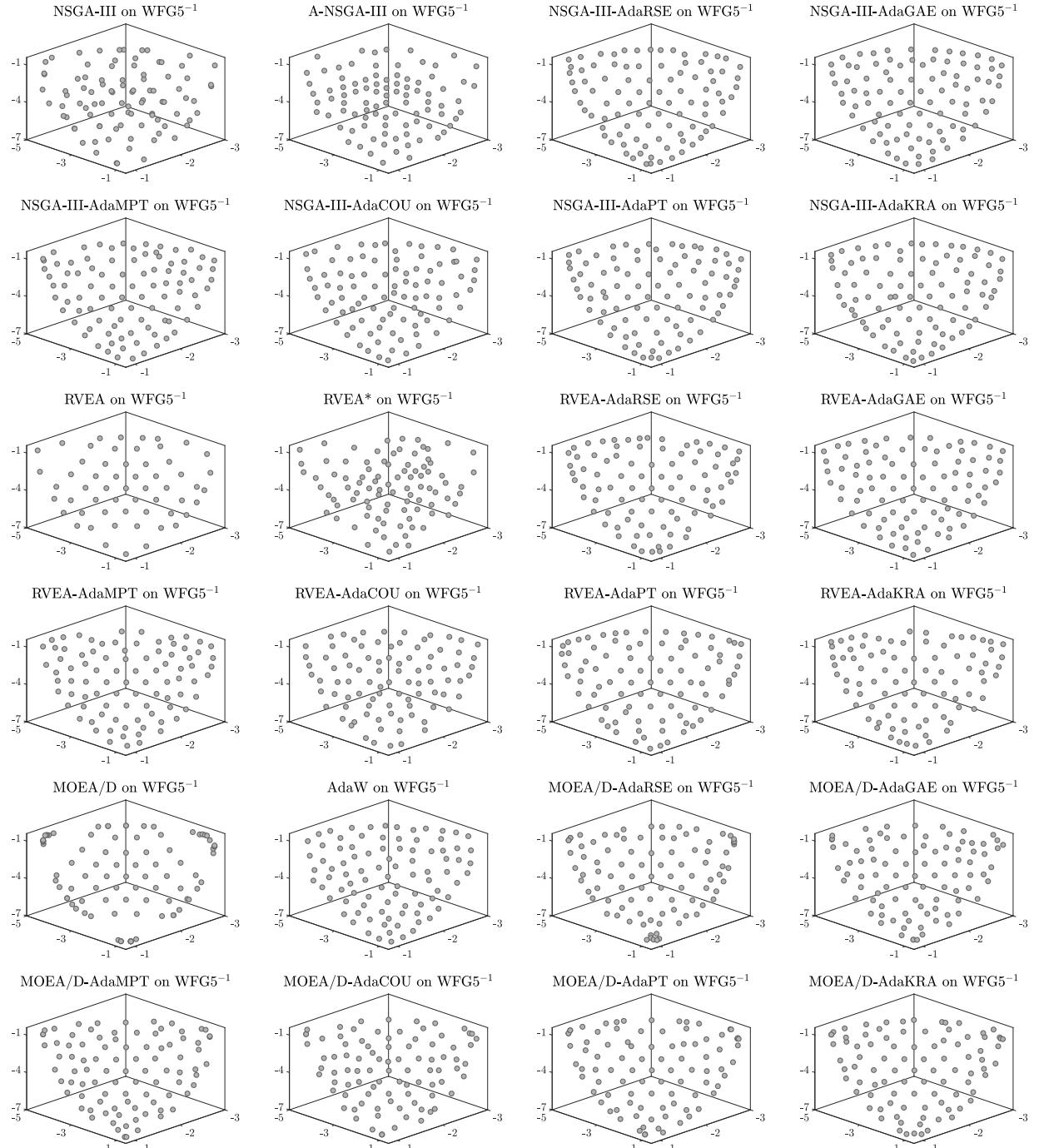


Figure 109: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG5^{-1} with 3 objective functions.

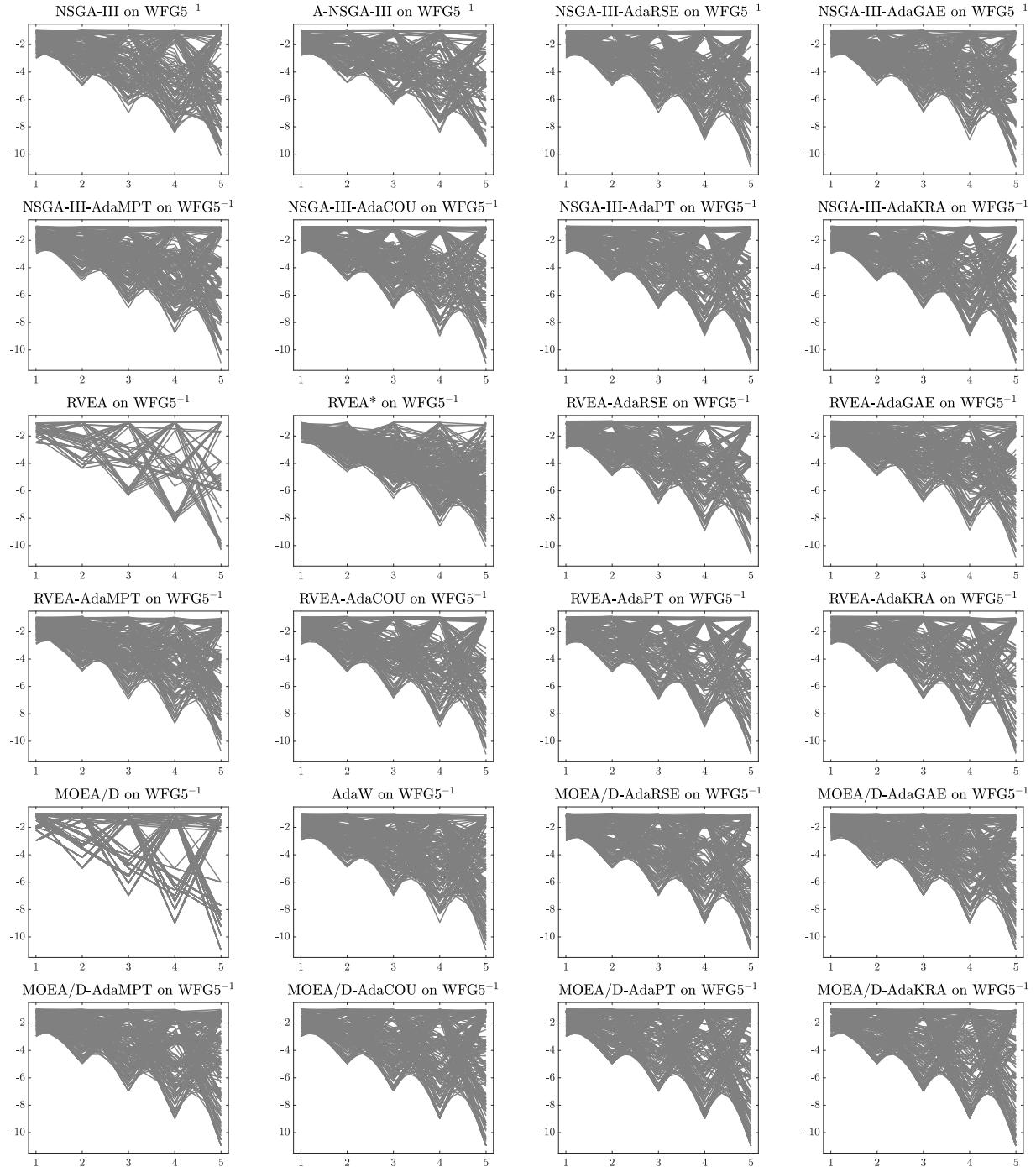


Figure 110: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG5^{-1} with 5 objective functions.

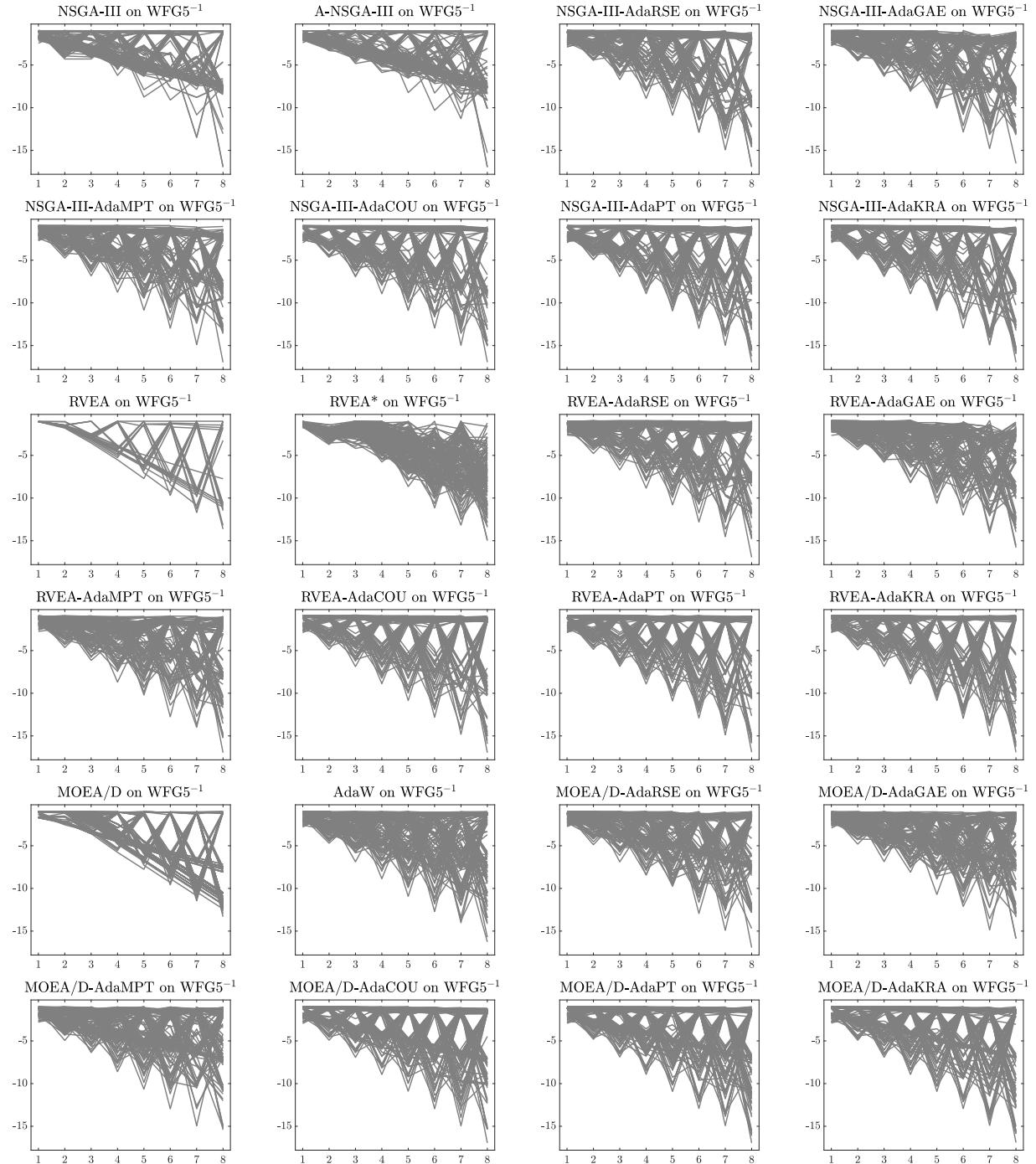


Figure 111: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG5⁻¹ with 8 objective functions.

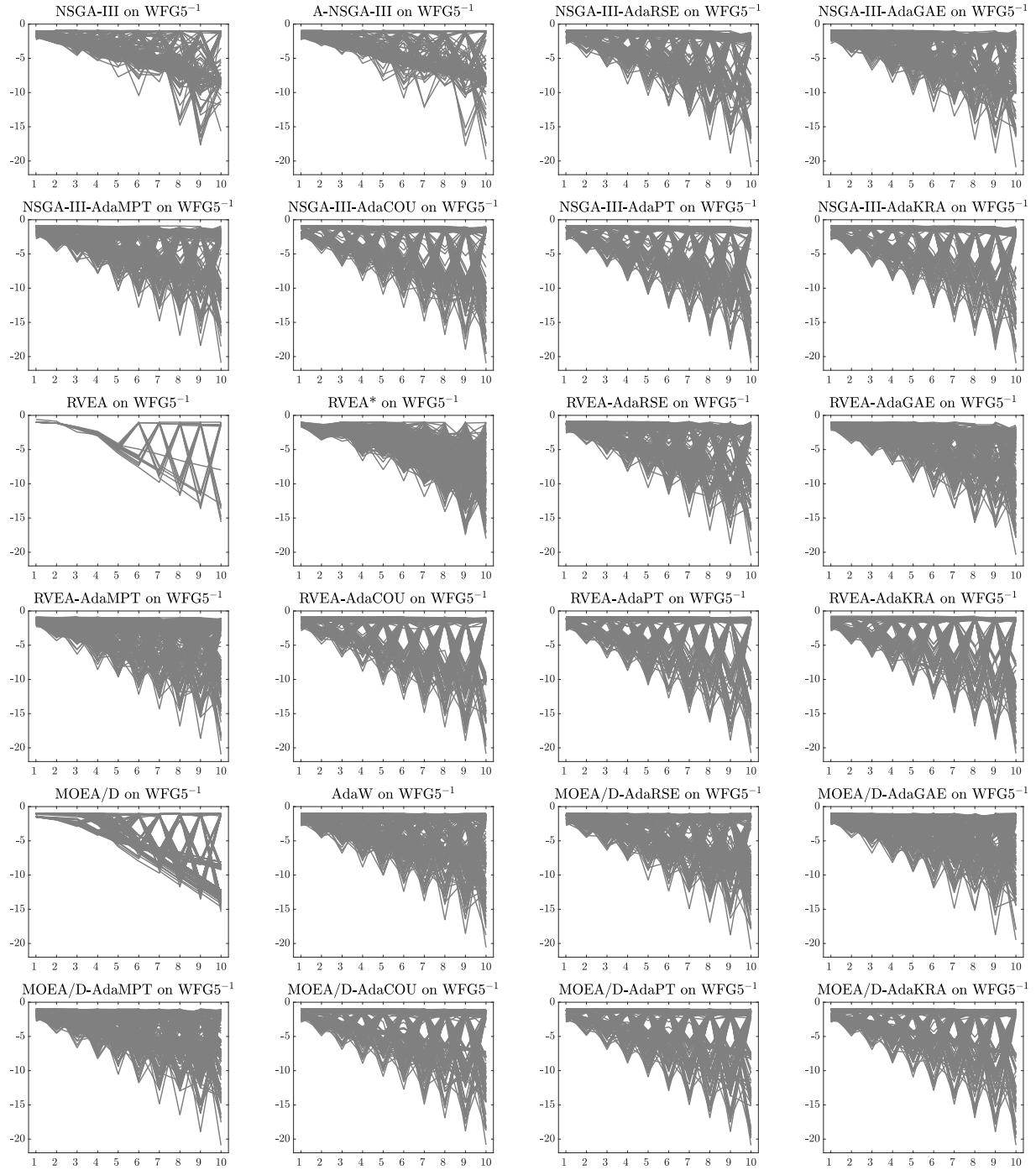


Figure 112: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG5^{-1} with 10 objective functions.

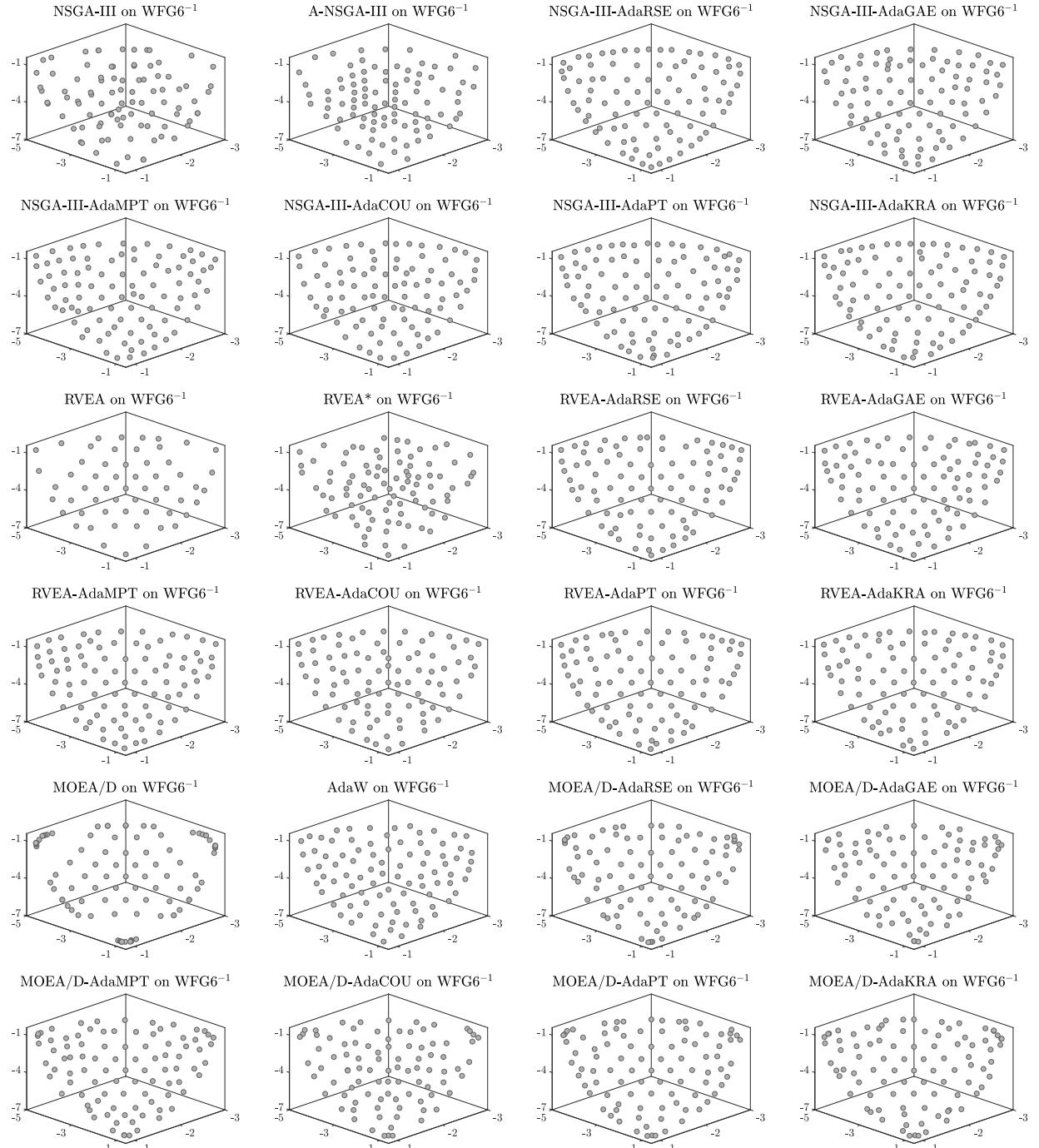


Figure 113: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG6^{-1} with 3 objective functions.

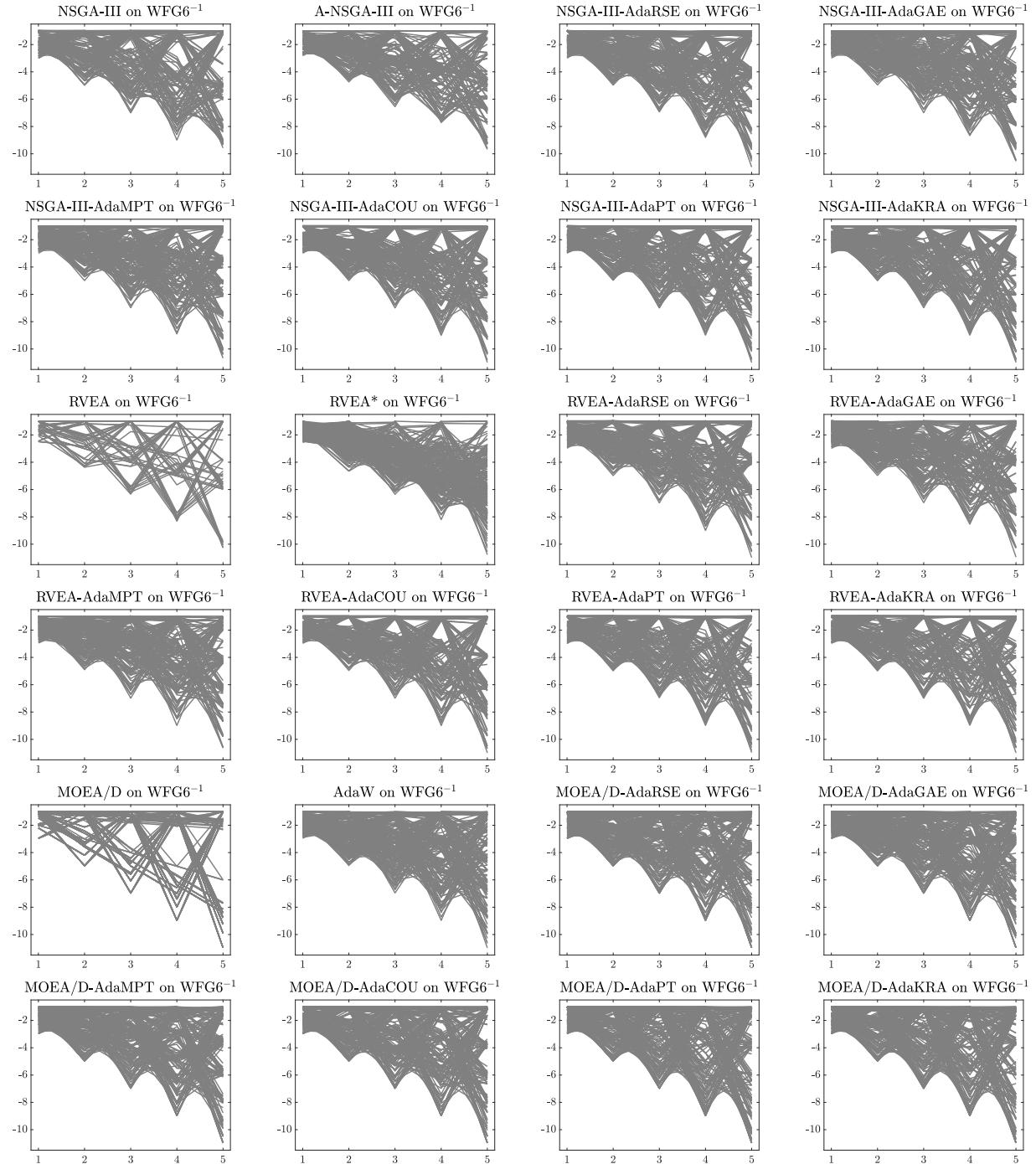


Figure 114: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG6⁻¹ with 5 objective functions.

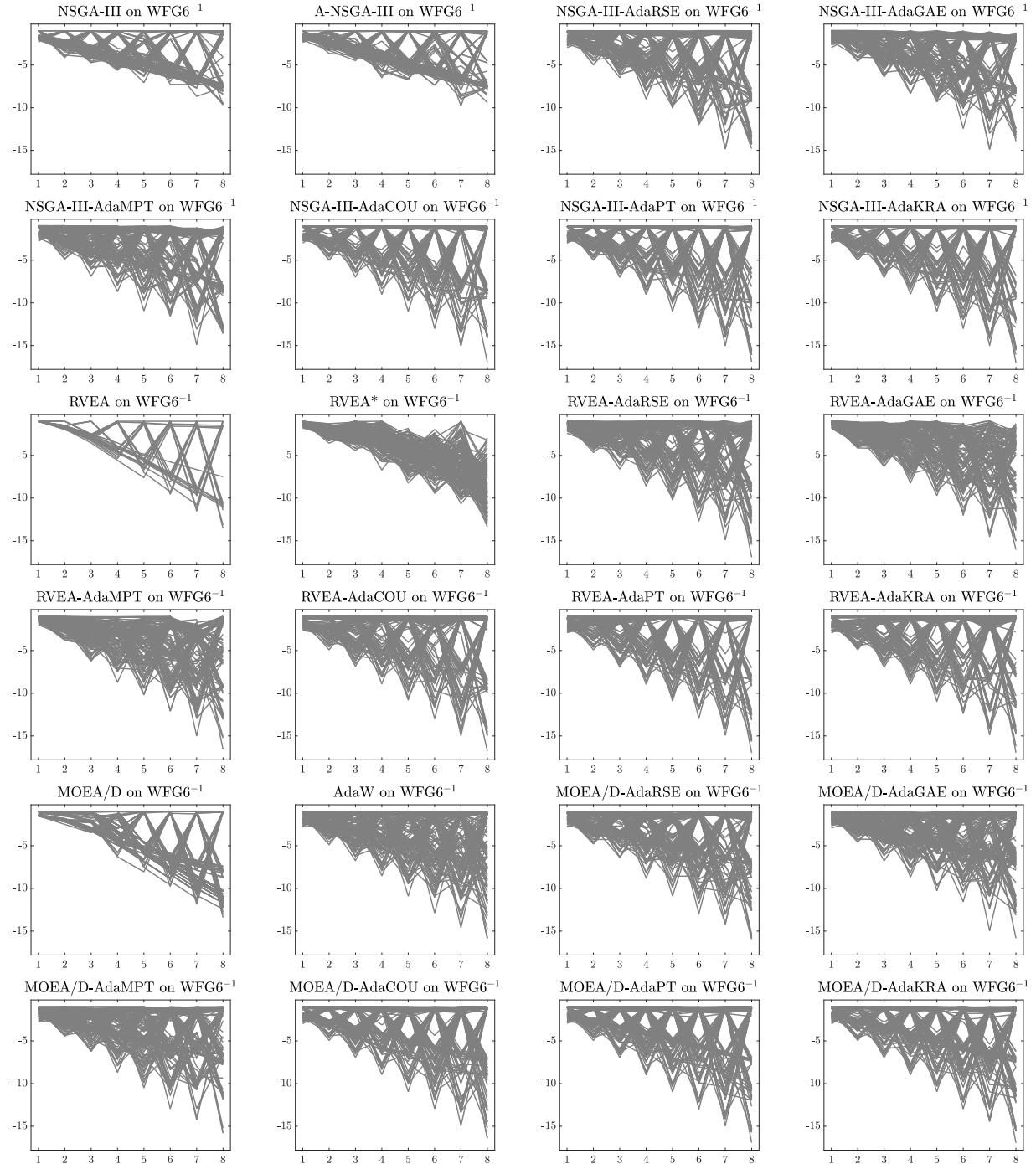


Figure 115: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG6^{-1} with 8 objective functions.

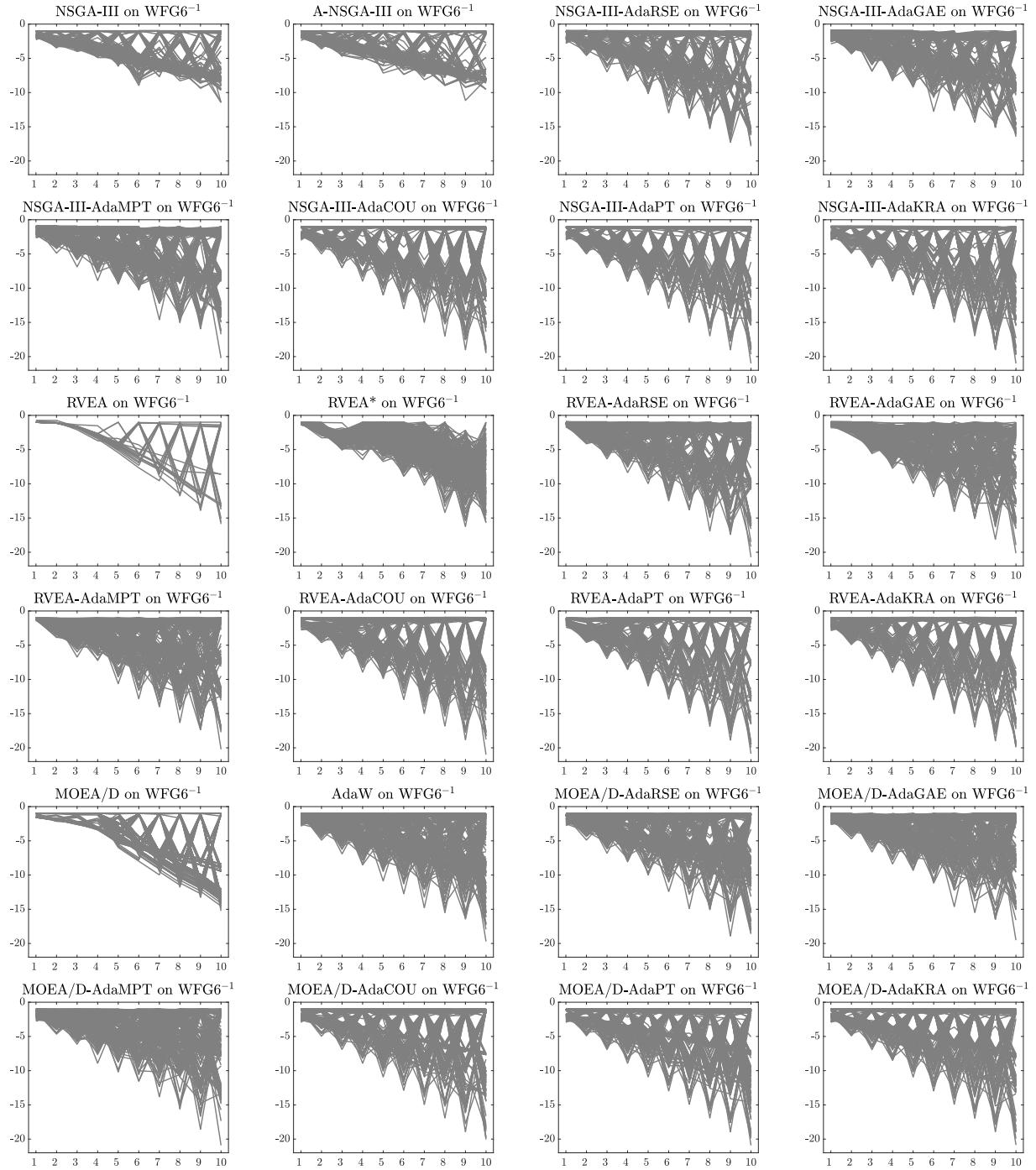


Figure 116: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG6⁻¹ with 10 objective functions.

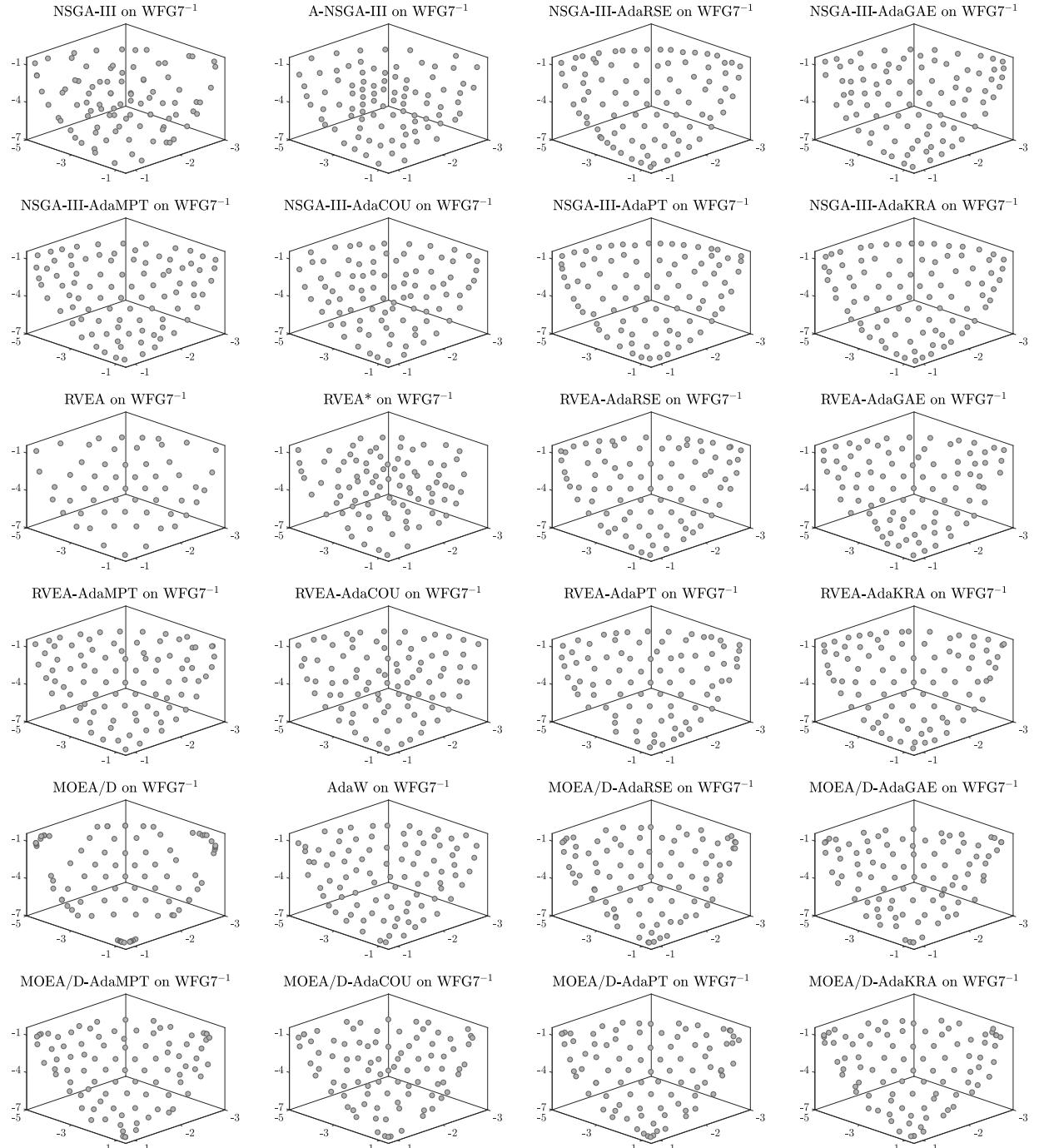


Figure 117: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG7^{-1} with 3 objective functions.

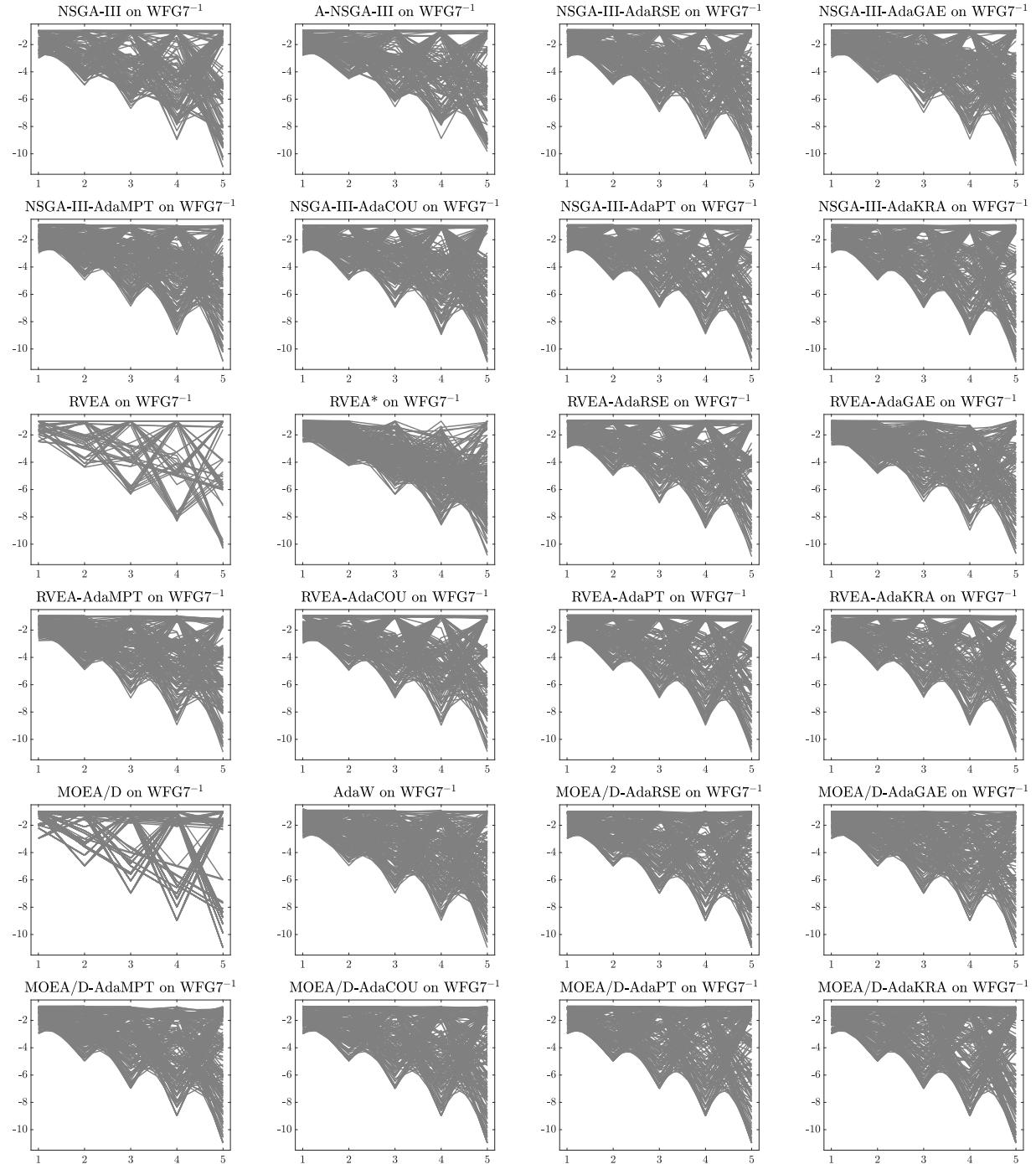


Figure 118: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG7^{-1} with 5 objective functions.

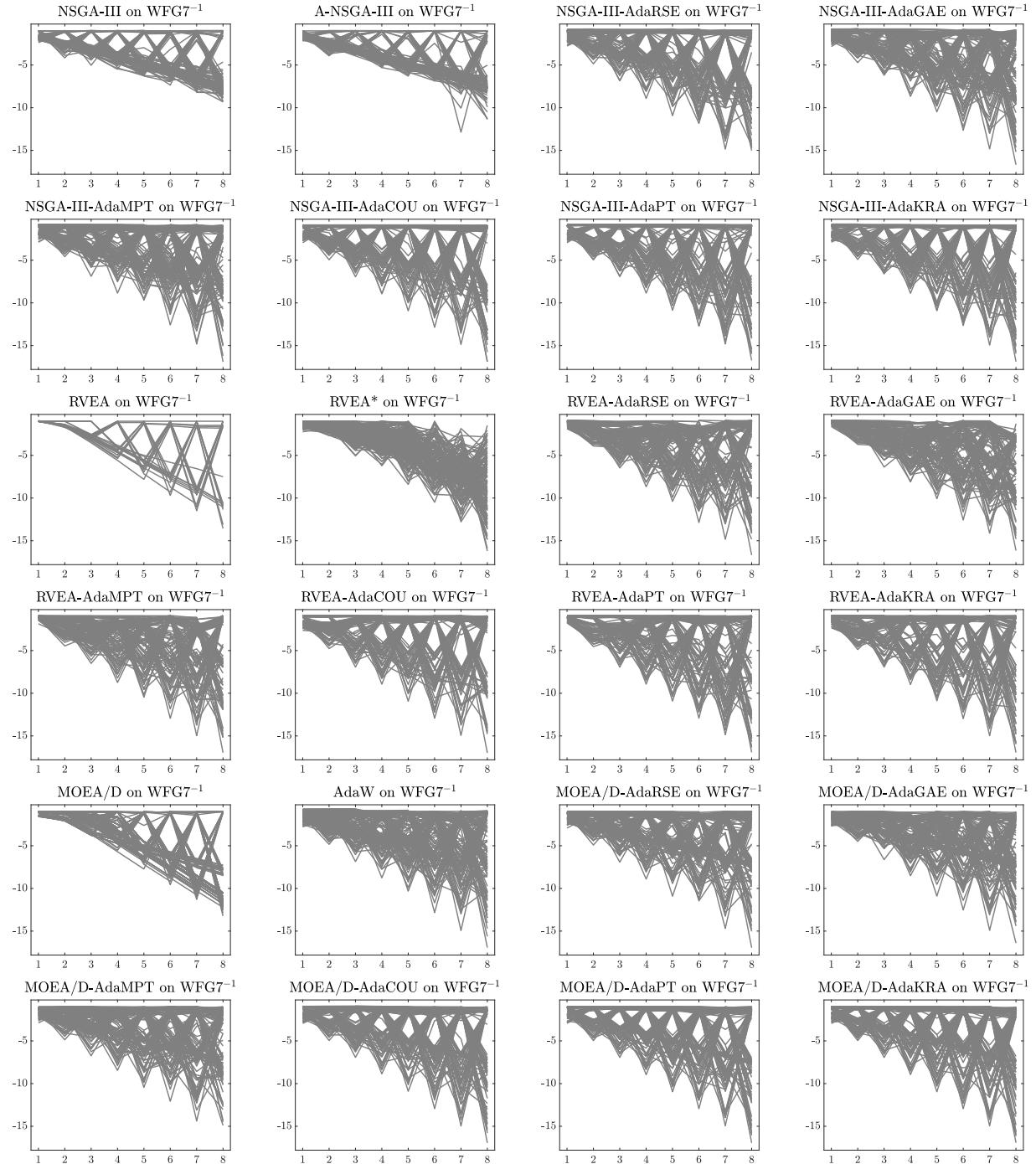


Figure 119: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG7⁻¹ with 8 objective functions.

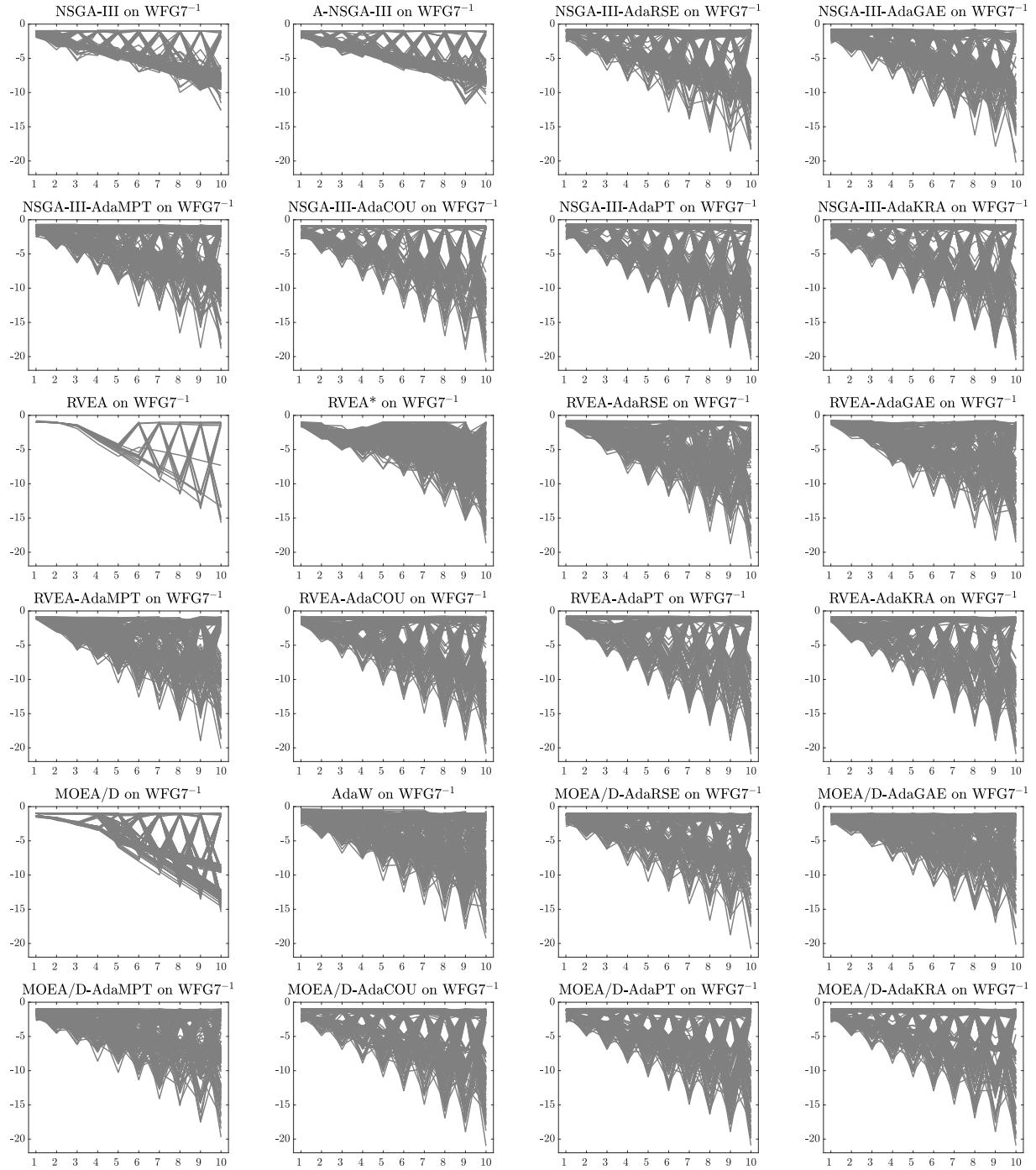


Figure 120: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG7^{-1} with 10 objective functions.

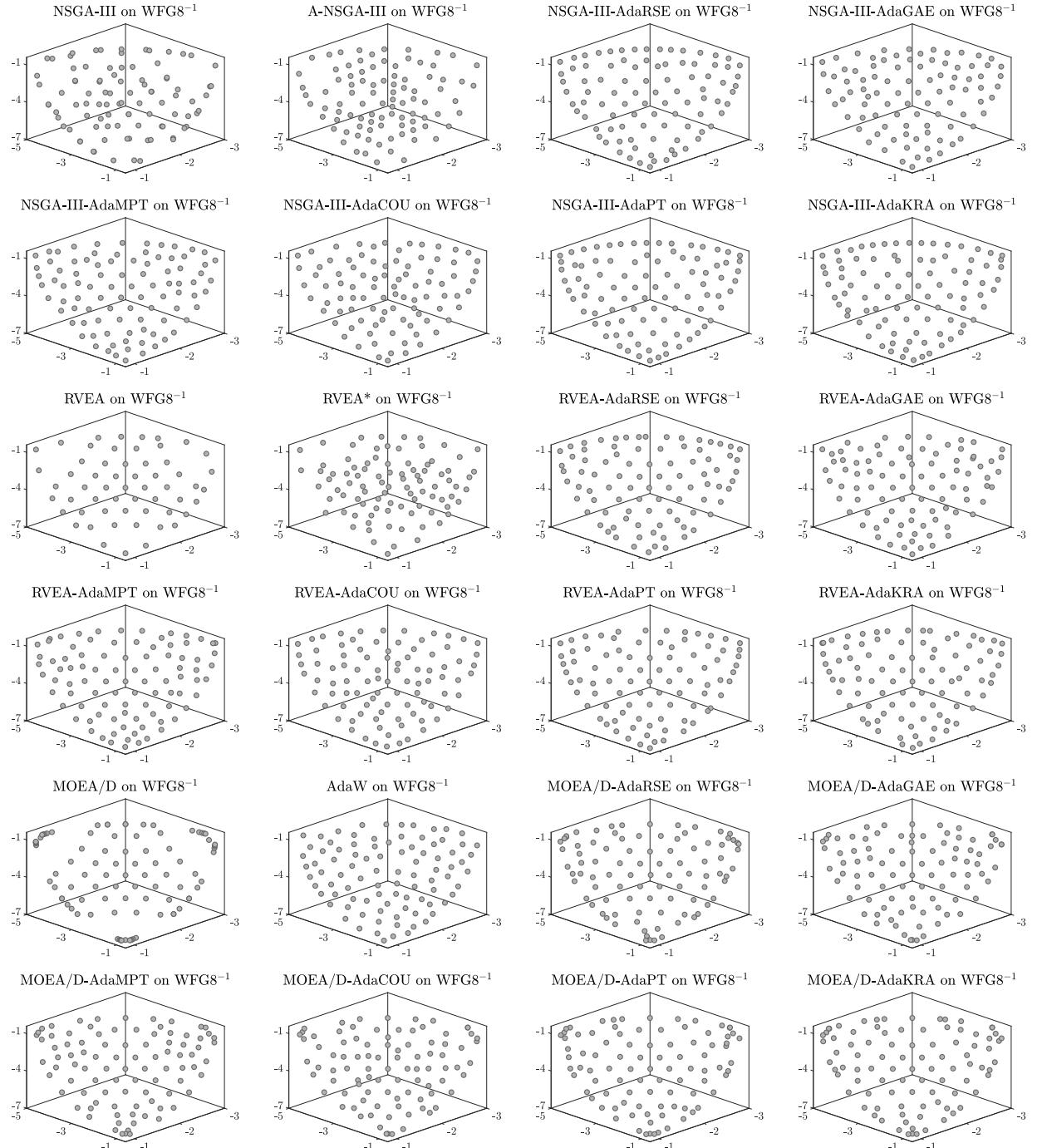


Figure 121: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG8^{-1} with 3 objective functions.

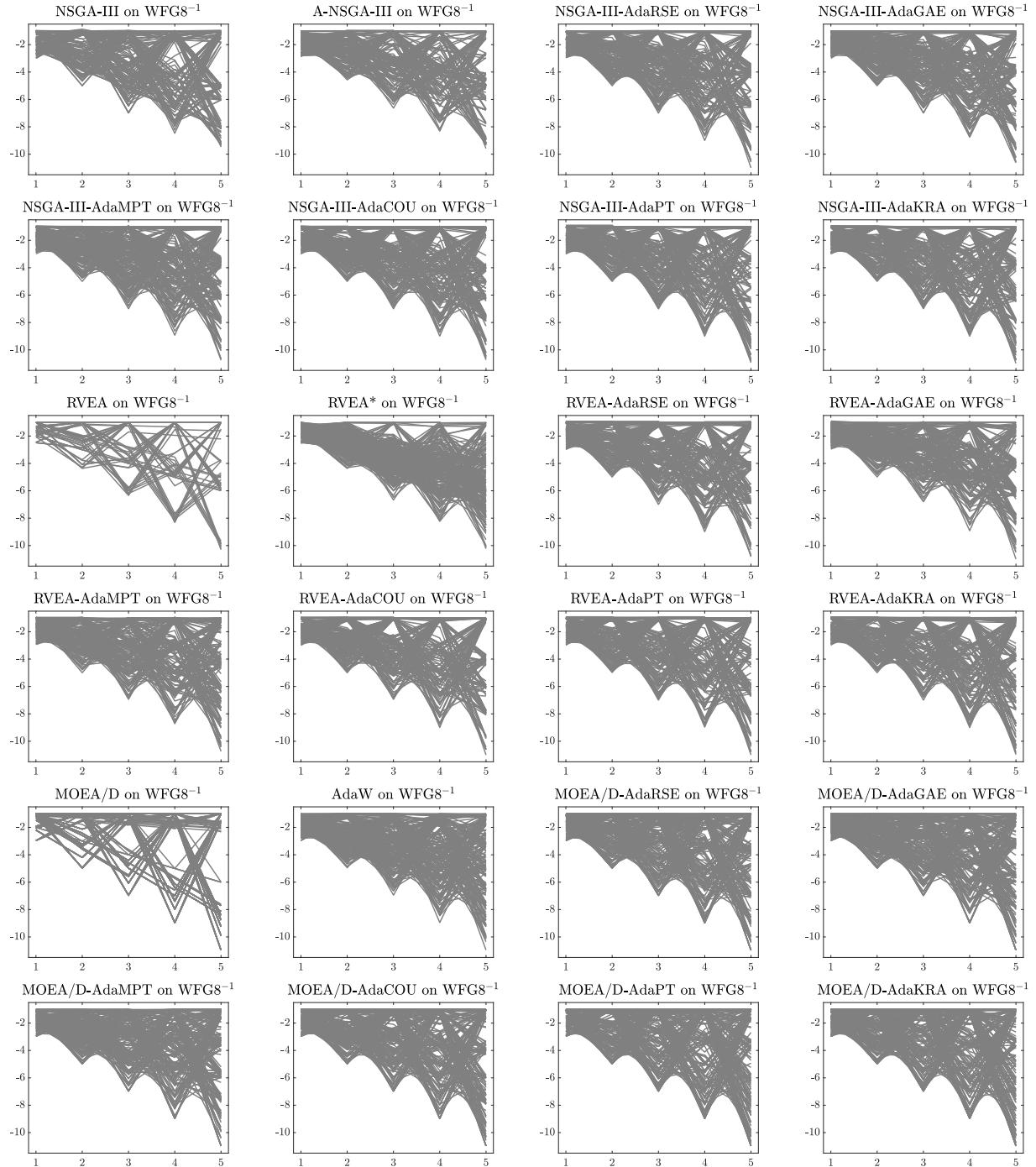


Figure 122: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG8^{-1} with 5 objective functions.

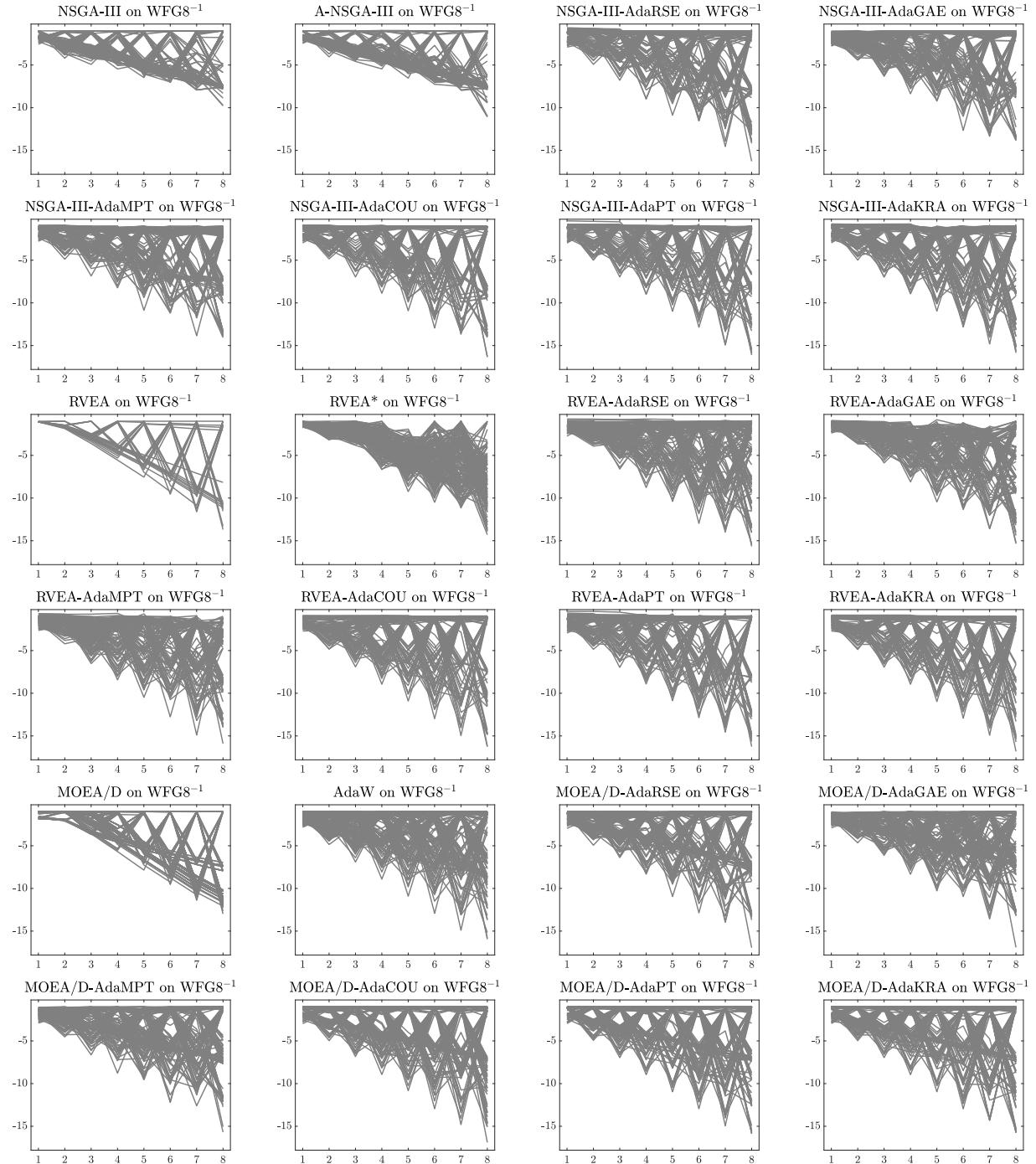


Figure 123: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG8^{-1} with 8 objective functions.

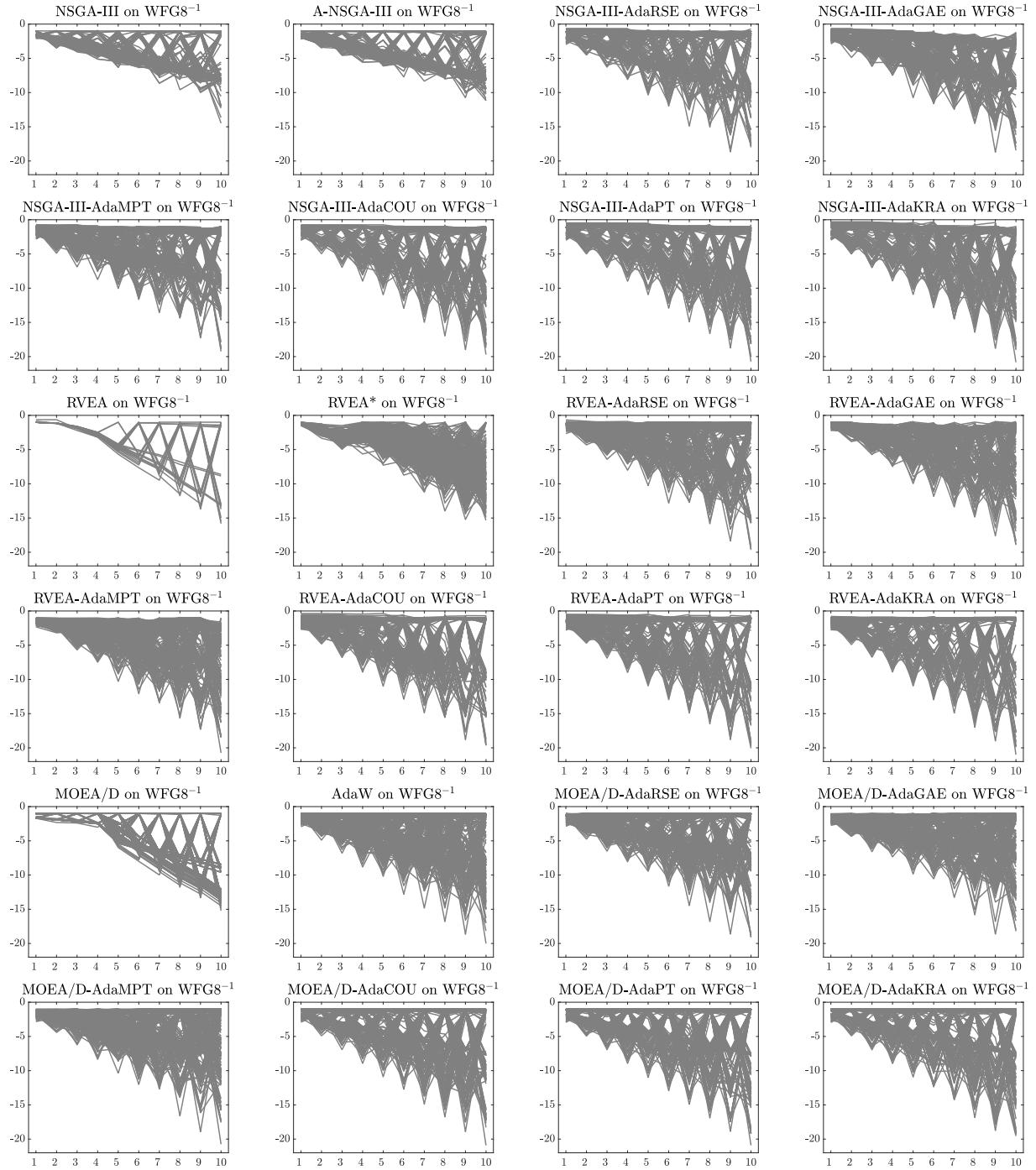


Figure 124: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG8^{-1} with 10 objective functions.

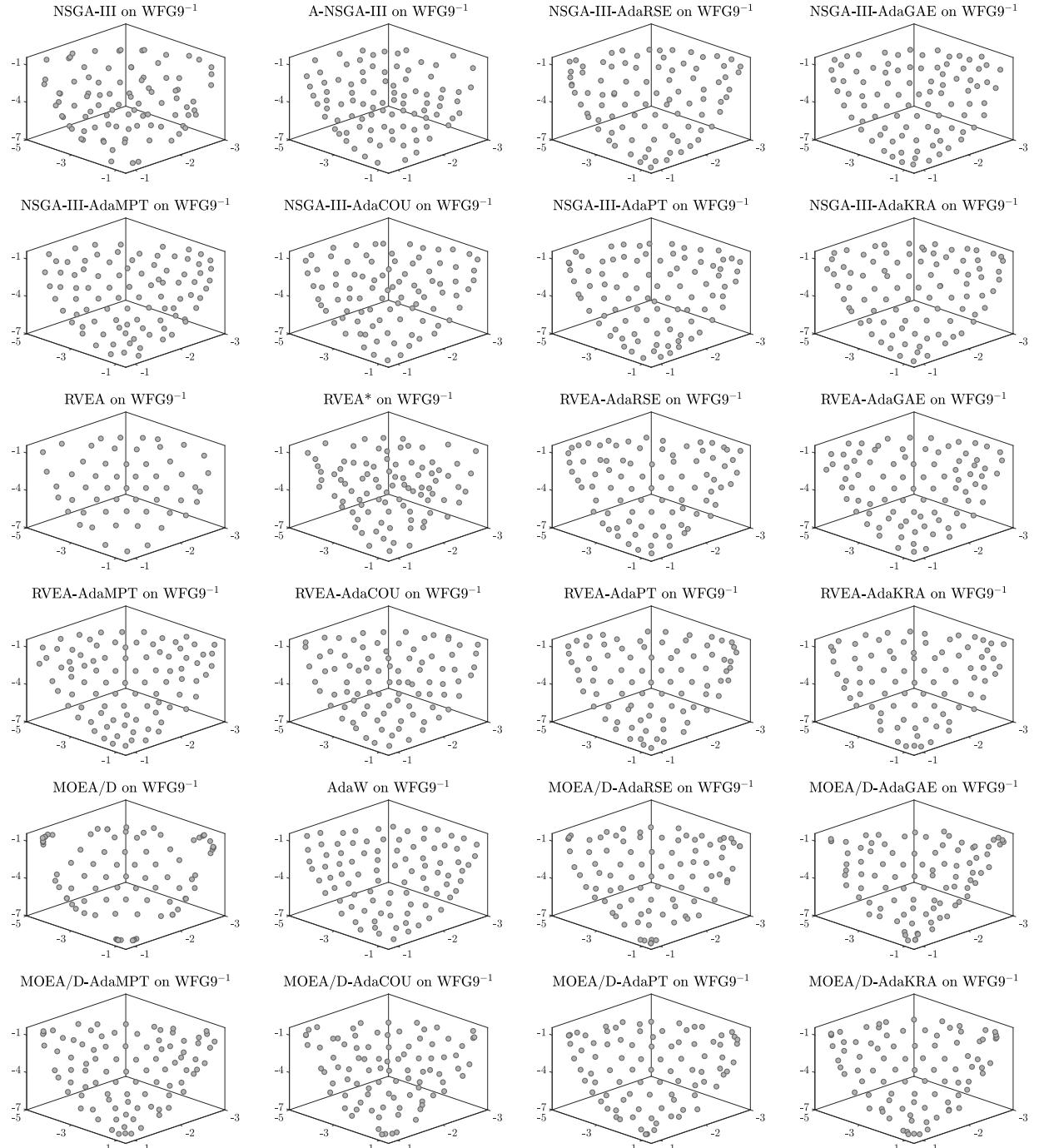


Figure 125: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG9^{-1} with 3 objective functions.

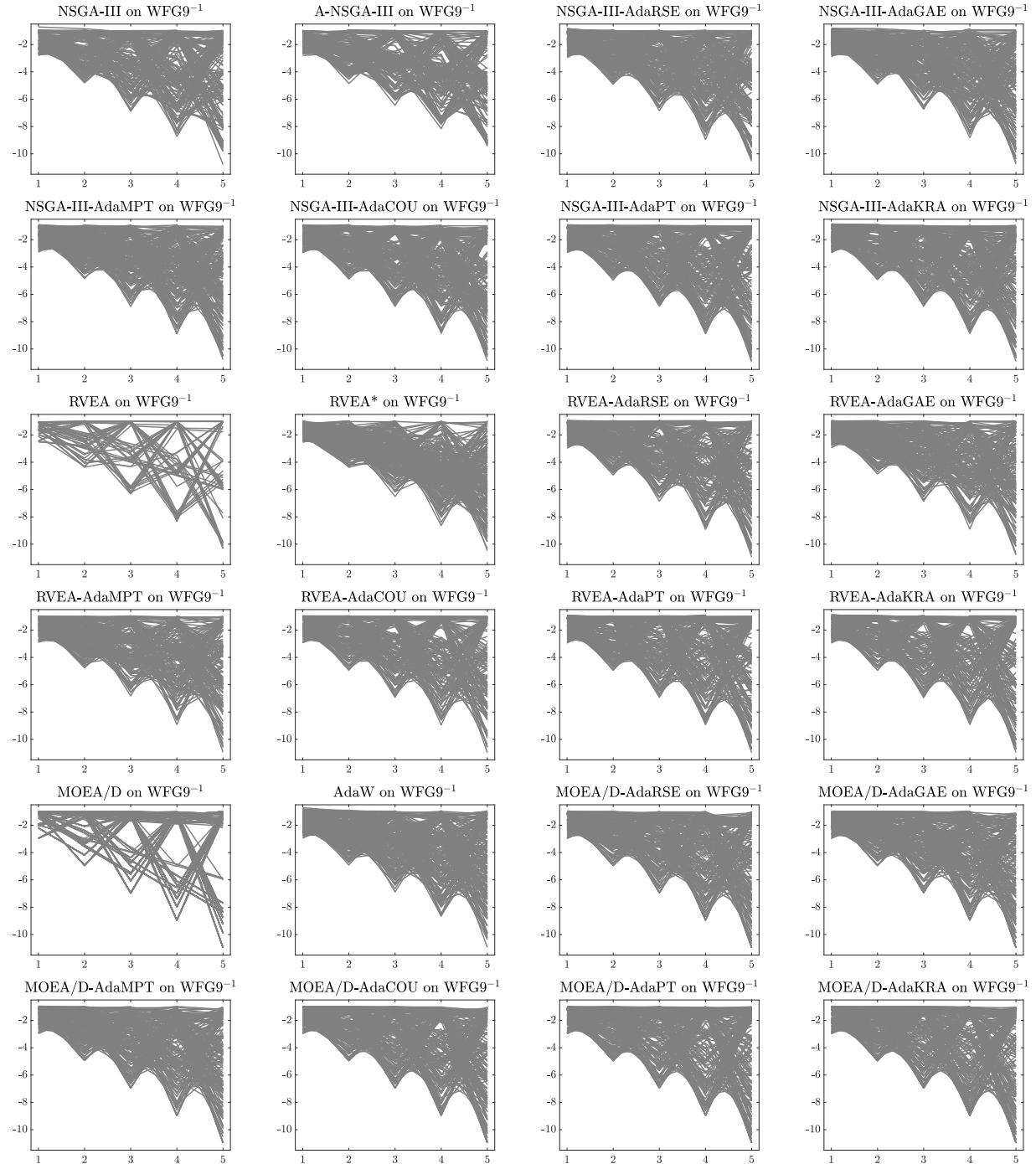


Figure 126: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG9^{-1} with 5 objective functions.

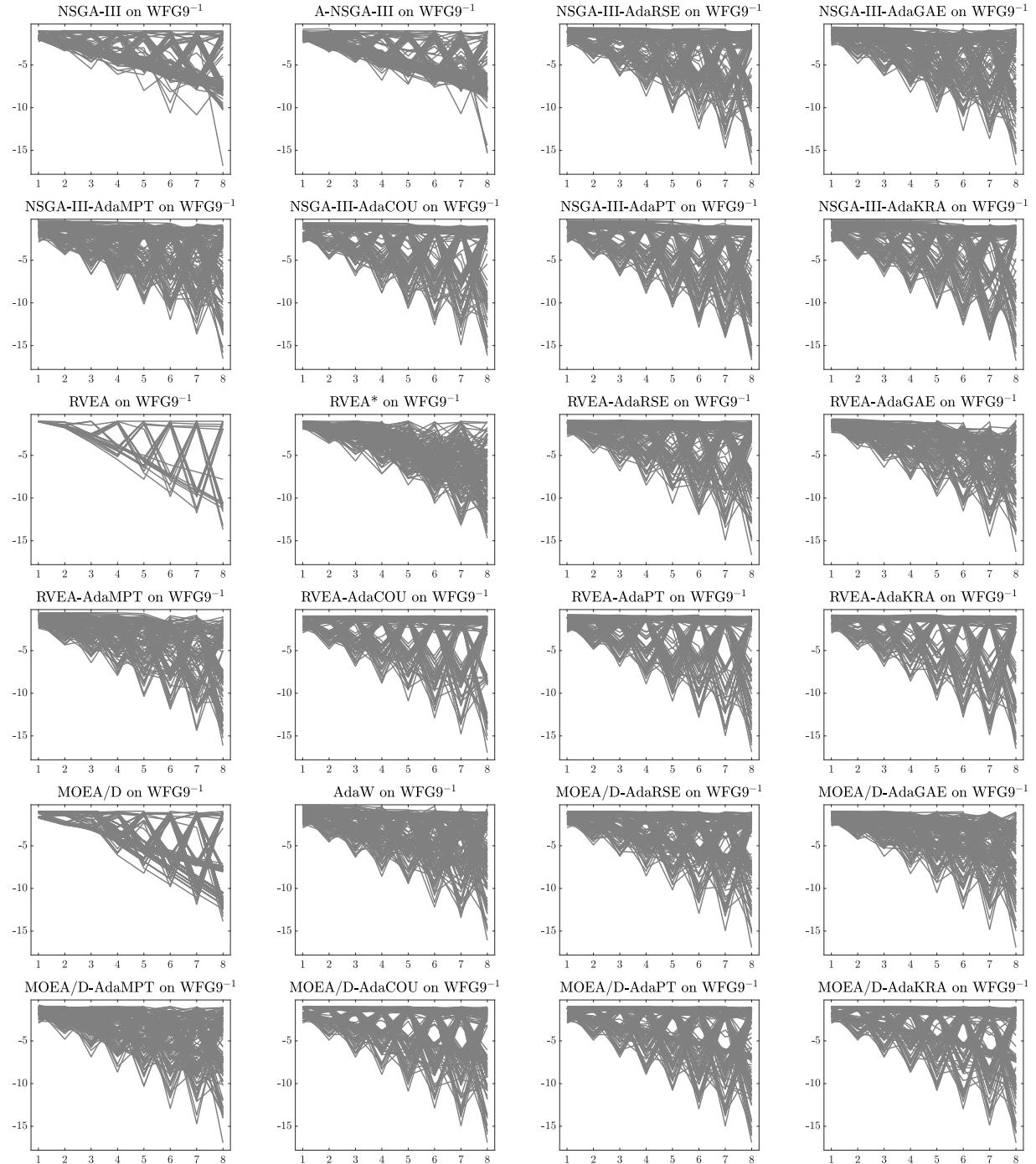


Figure 127: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG9⁻¹ with 8 objective functions.

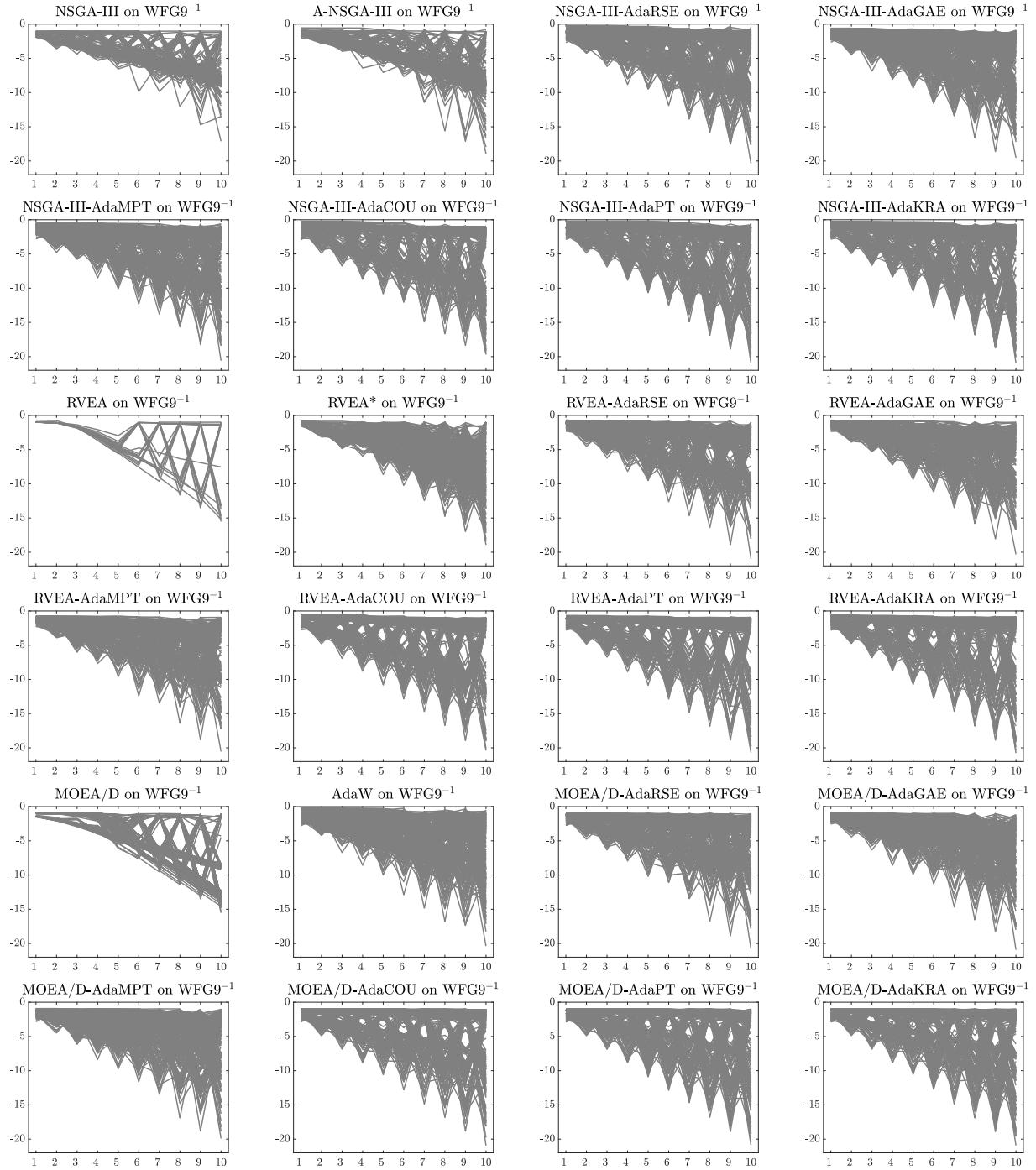


Figure 128: Final populations with the median HV value among 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG9⁻¹ with 10 objective functions.

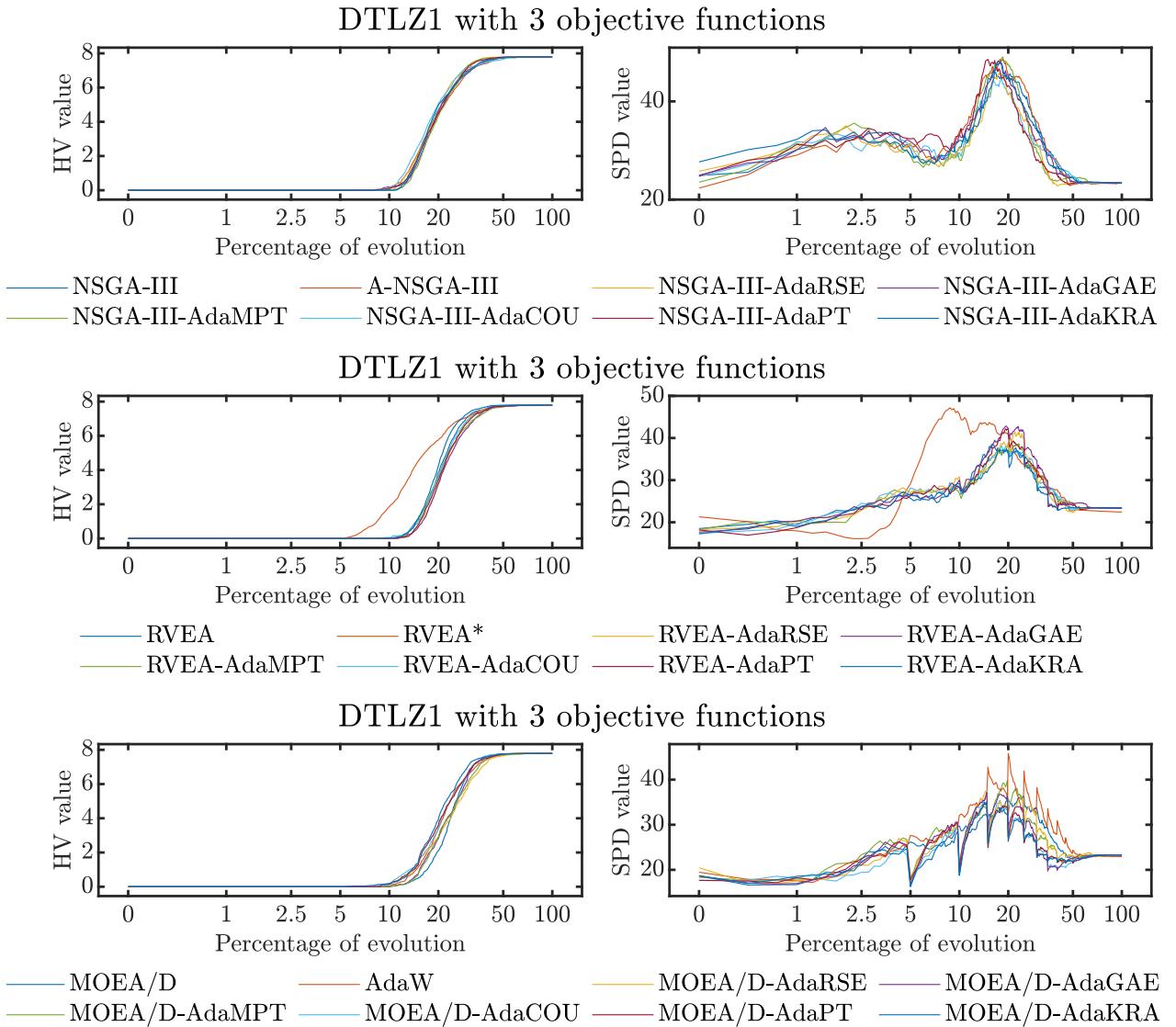


Figure 129: Convergence and diversity graphs with the mean HV value and SPD value of 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ1 with 3 objective functions.

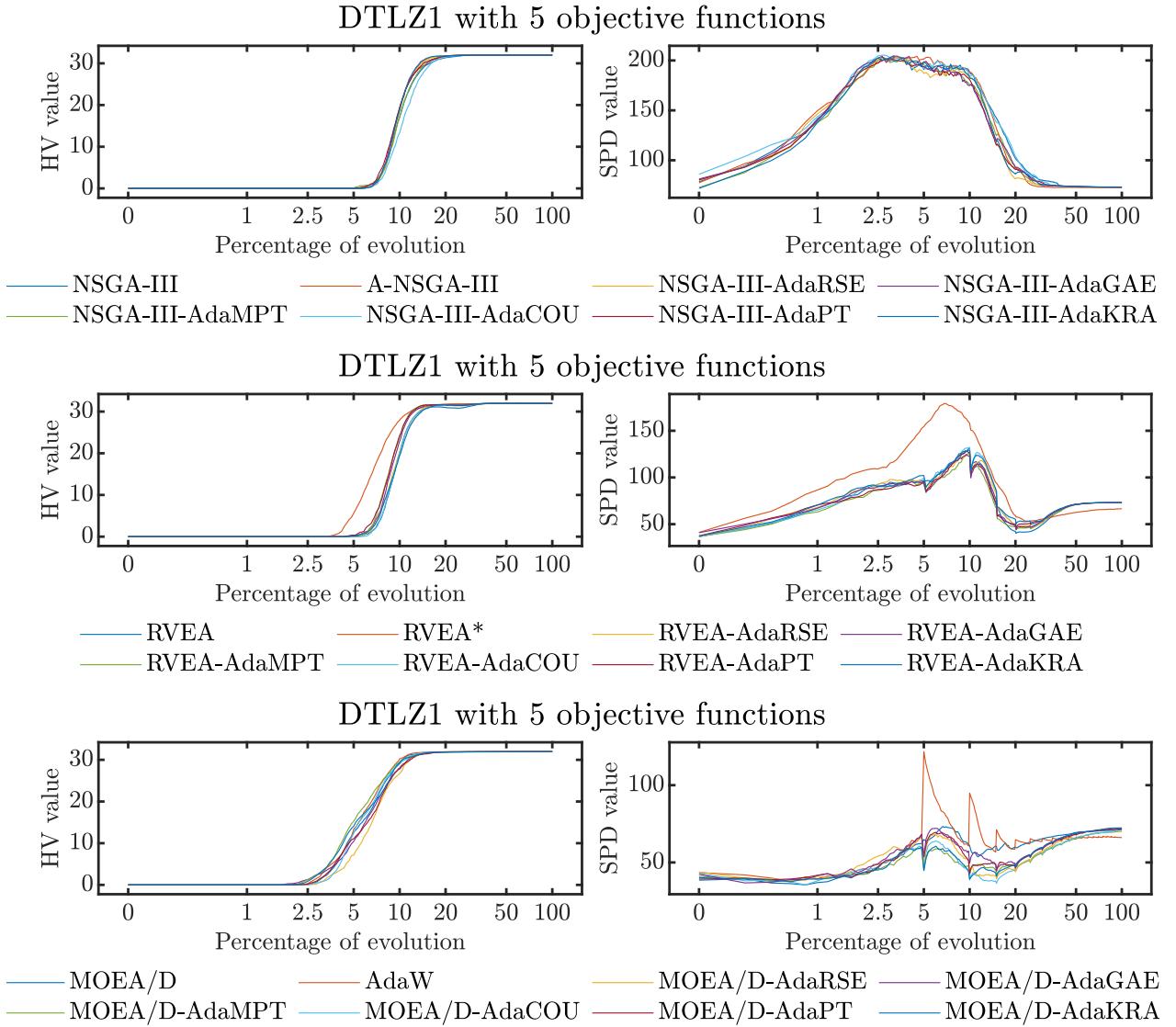


Figure 130: Convergence and diversity graphs with the mean HV value and SPD value of 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ1 with 5 objective functions.

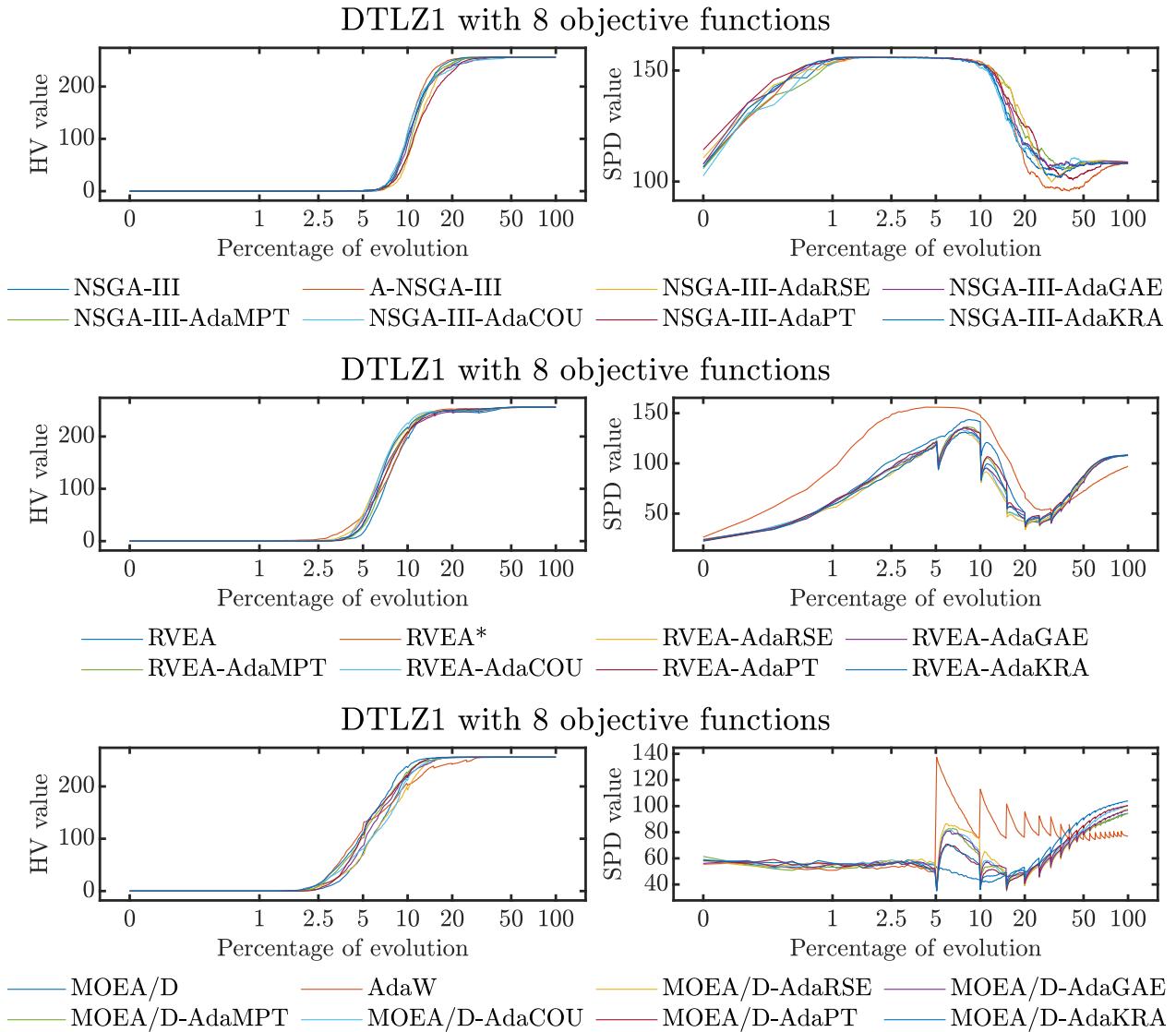


Figure 131: Convergence and diversity graphs with the mean HV value and SPD value of 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ1 with 8 objective functions.

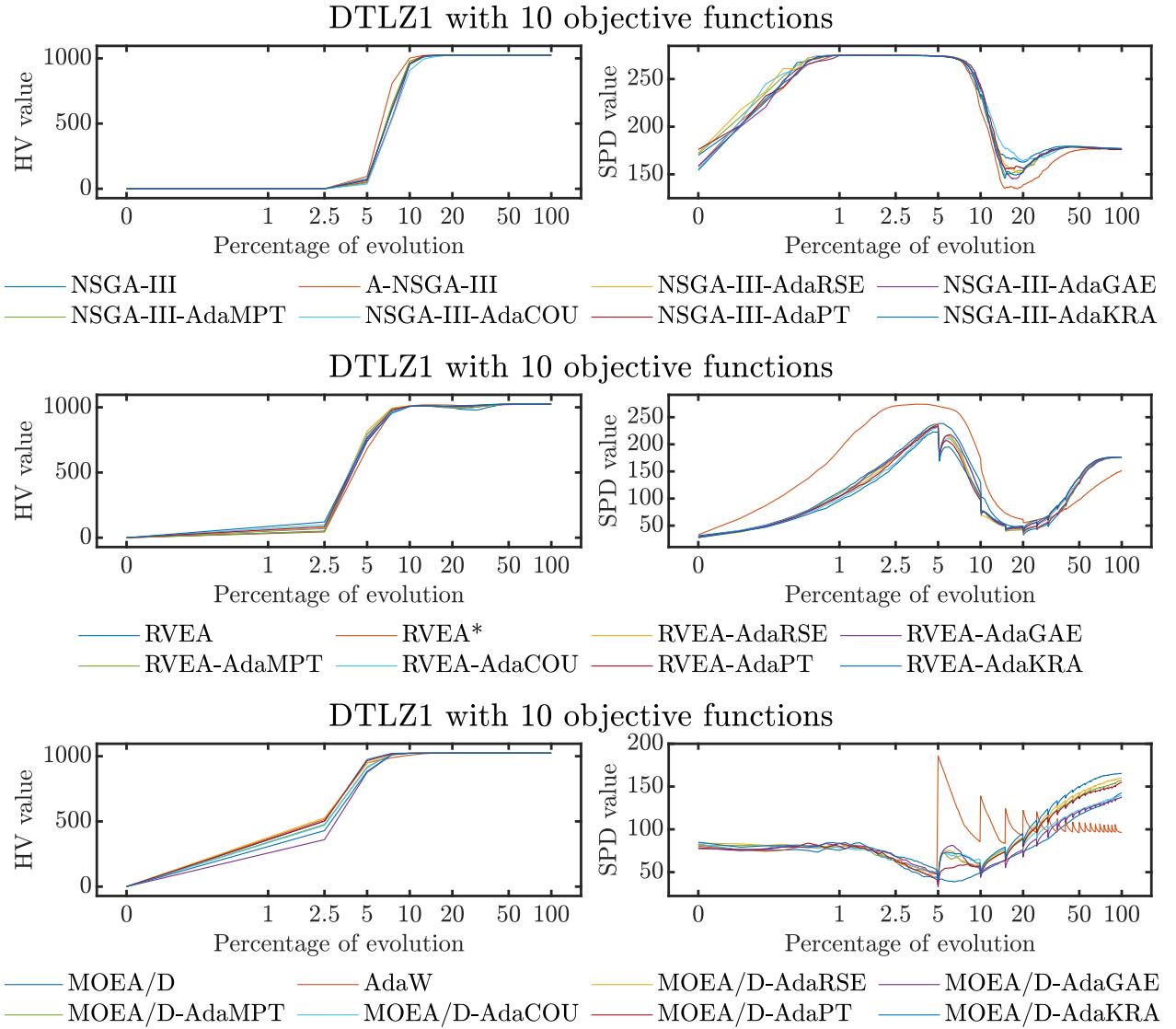


Figure 132: Convergence and diversity graphs with the mean HV value and SPD value of 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ1 with 10 objective functions.

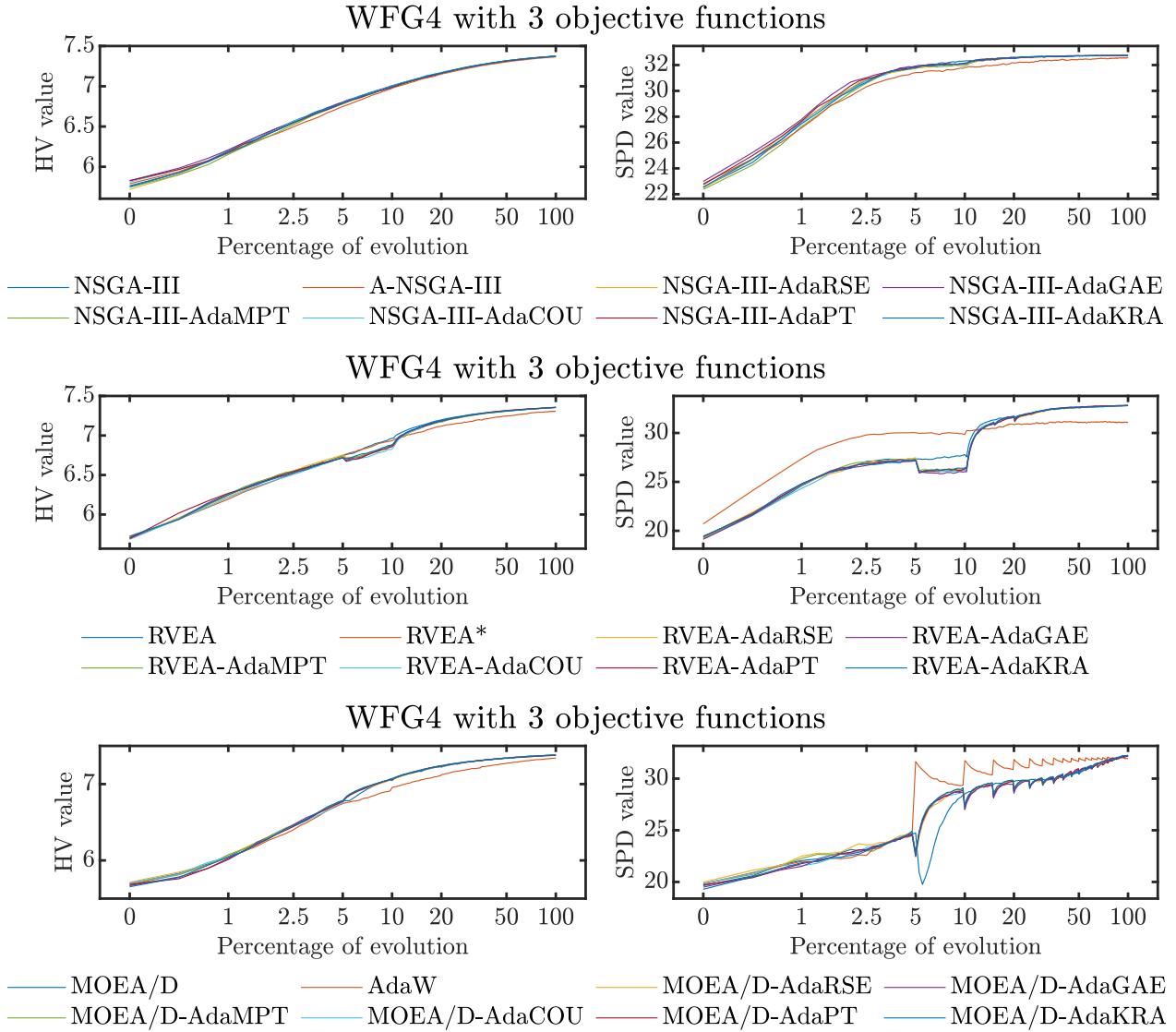


Figure 133: Convergence and diversity graphs with the mean HV value and SPD value of 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG4 with 3 objective functions.

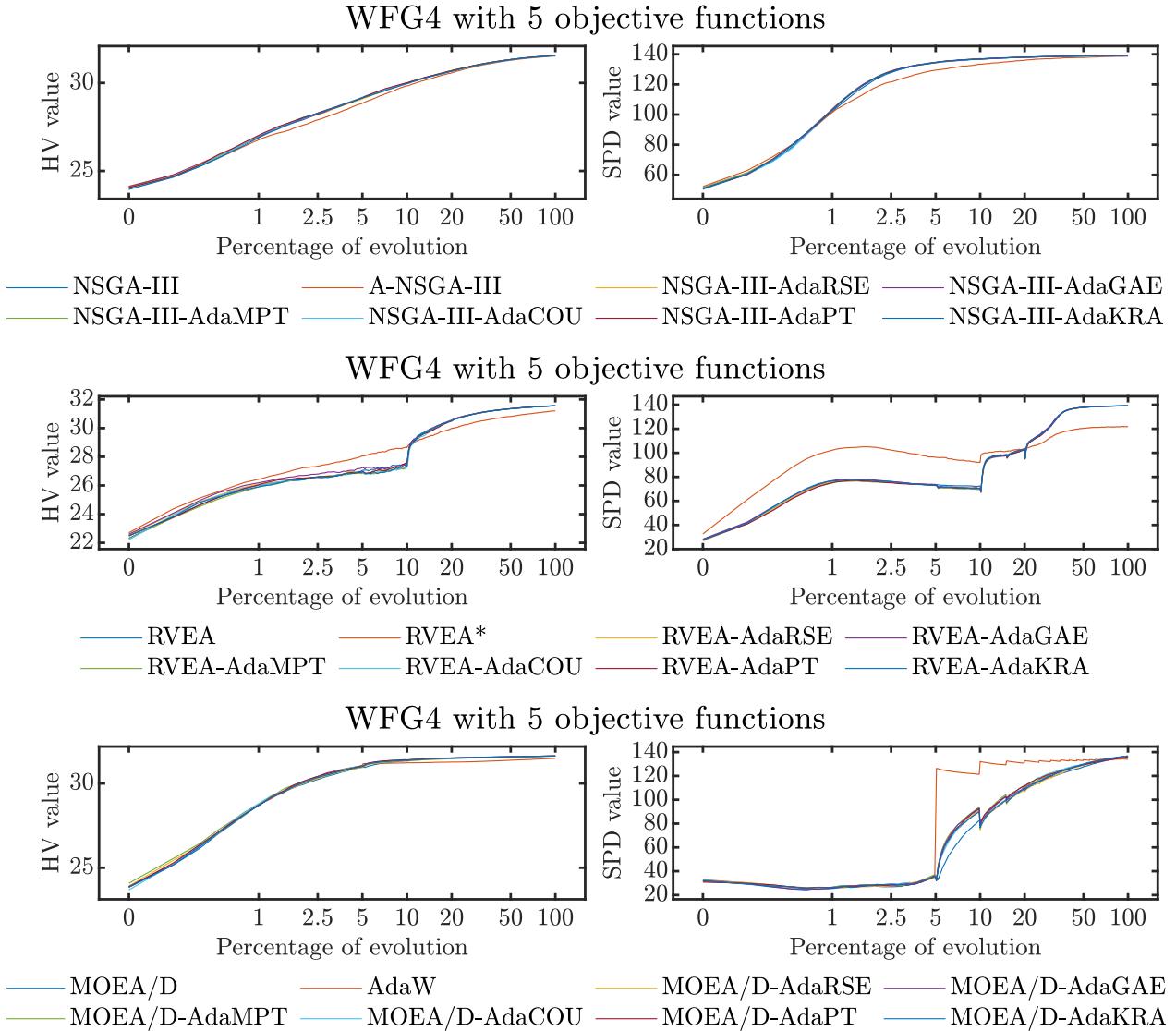


Figure 134: Convergence and diversity graphs with the mean HV value and SPD value of 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG4 with 5 objective functions.

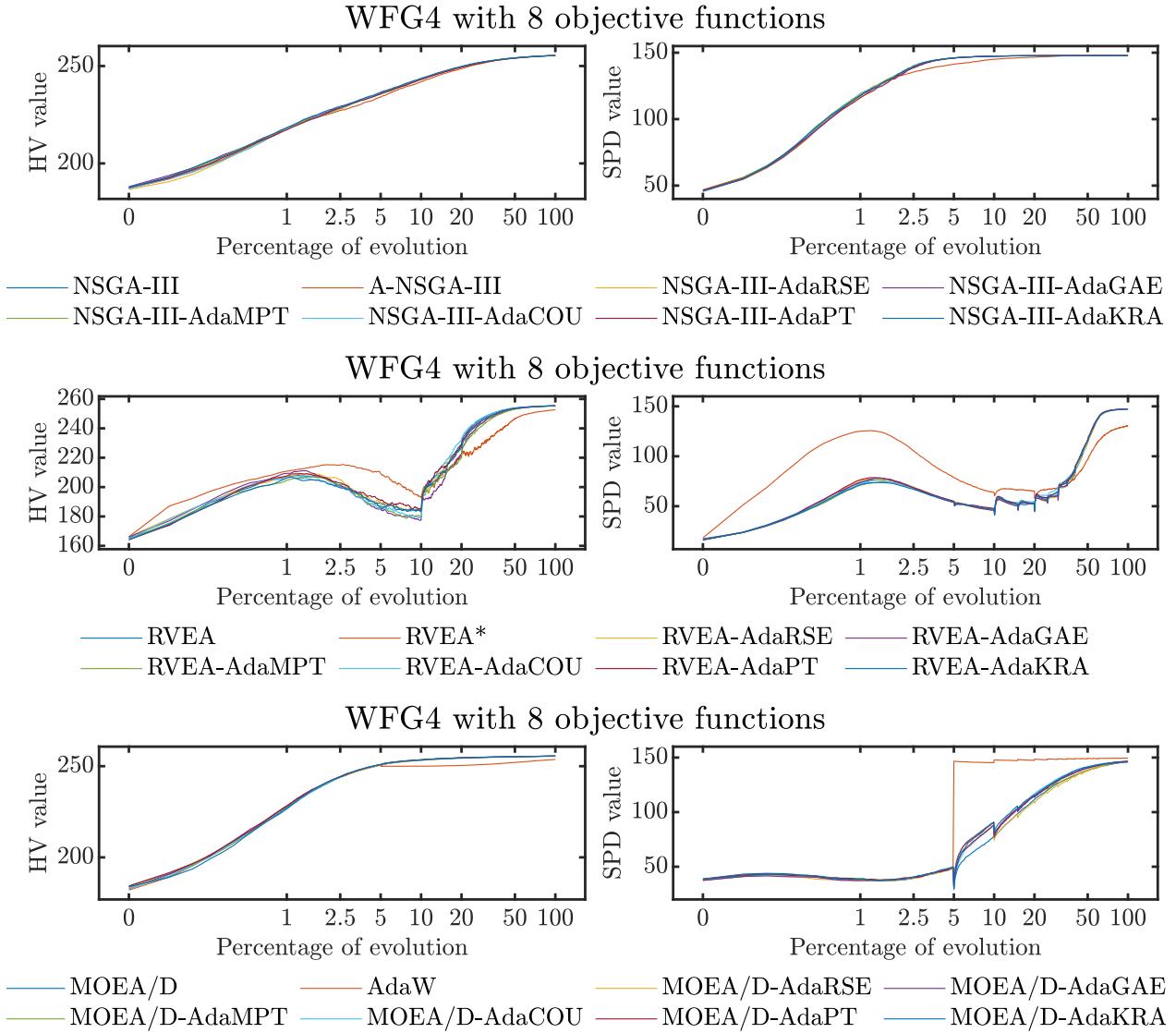


Figure 135: Convergence and diversity graphs with the mean HV value and SPD value of 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG4 with 8 objective functions.

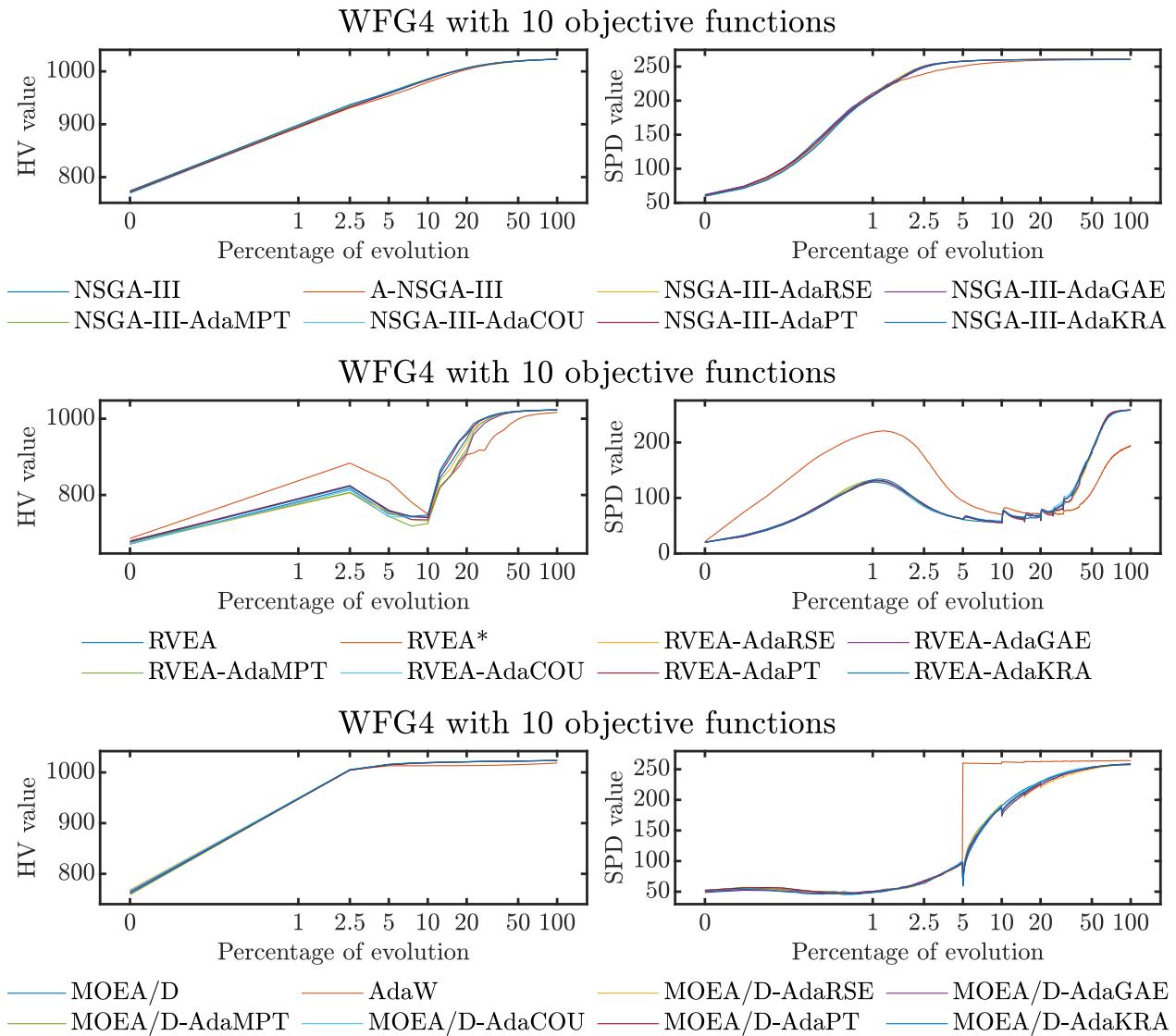


Figure 136: Convergence and diversity graphs with the mean HV value and SPD value of 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG4 with 10 objective functions.

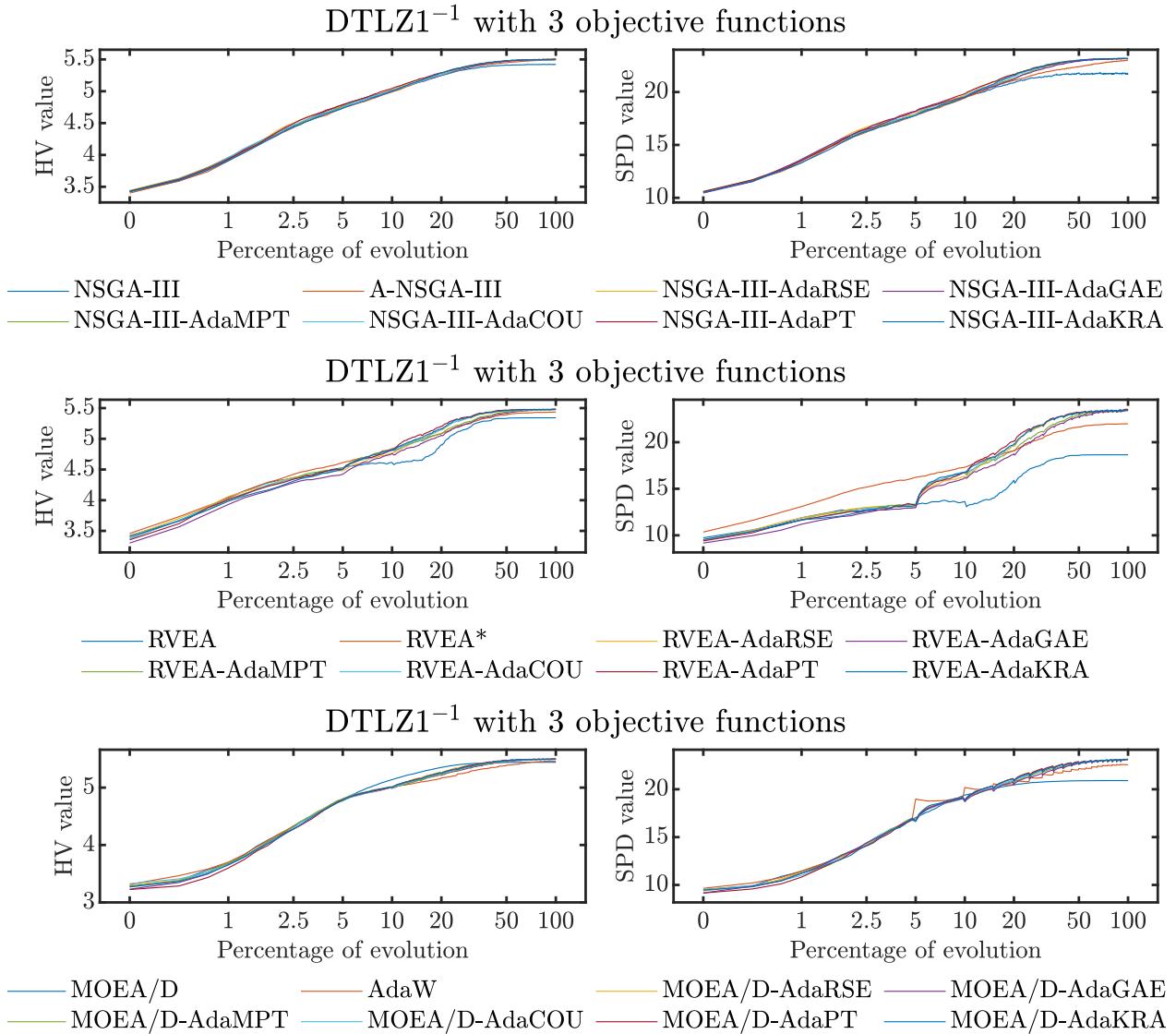


Figure 137: Convergence and diversity graphs with the mean HV value and SPD value of 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ1⁻¹ with 3 objective functions.

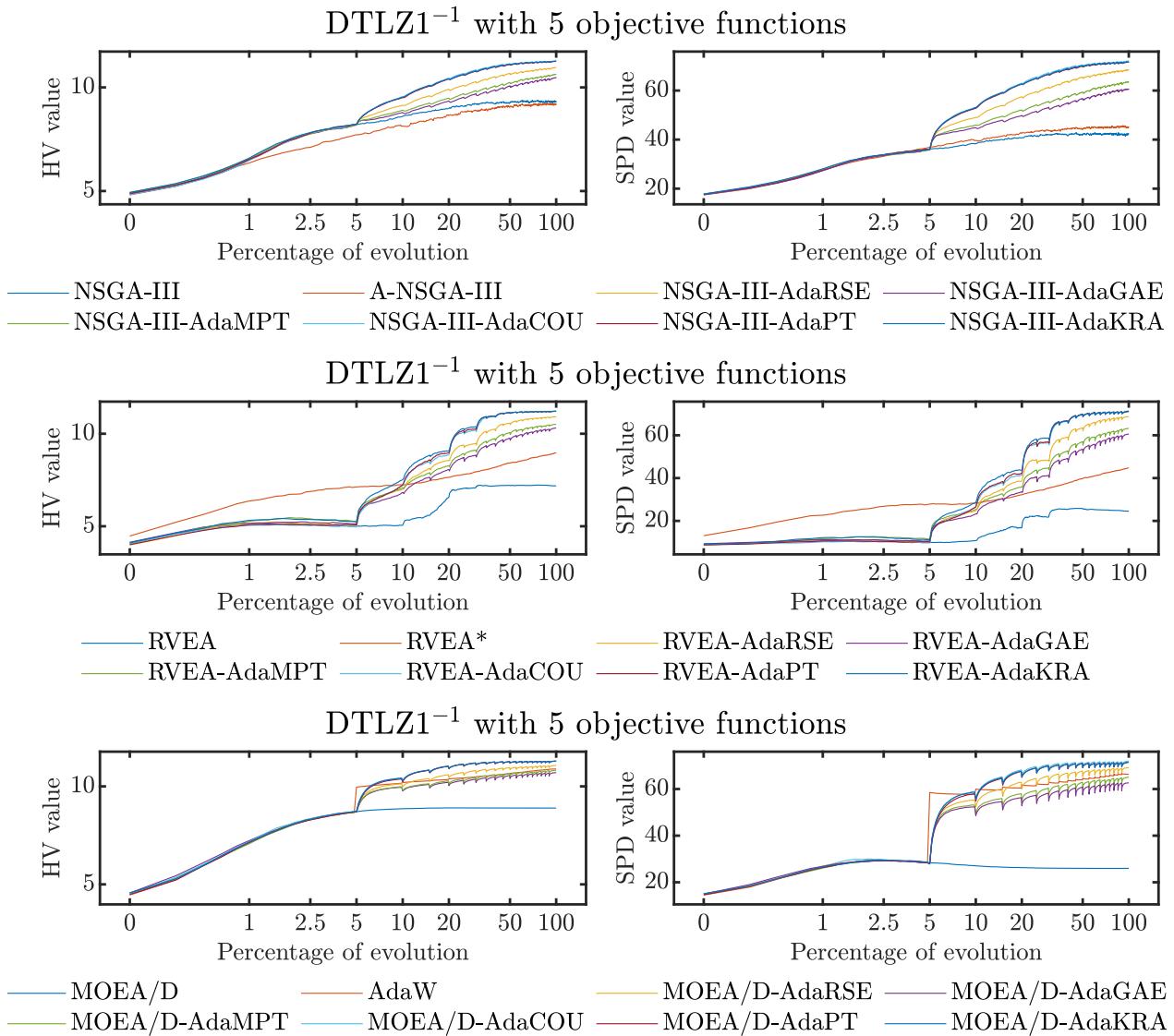


Figure 138: Convergence and diversity graphs with the mean HV value and SPD value of 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ1⁻¹ with 5 objective functions.

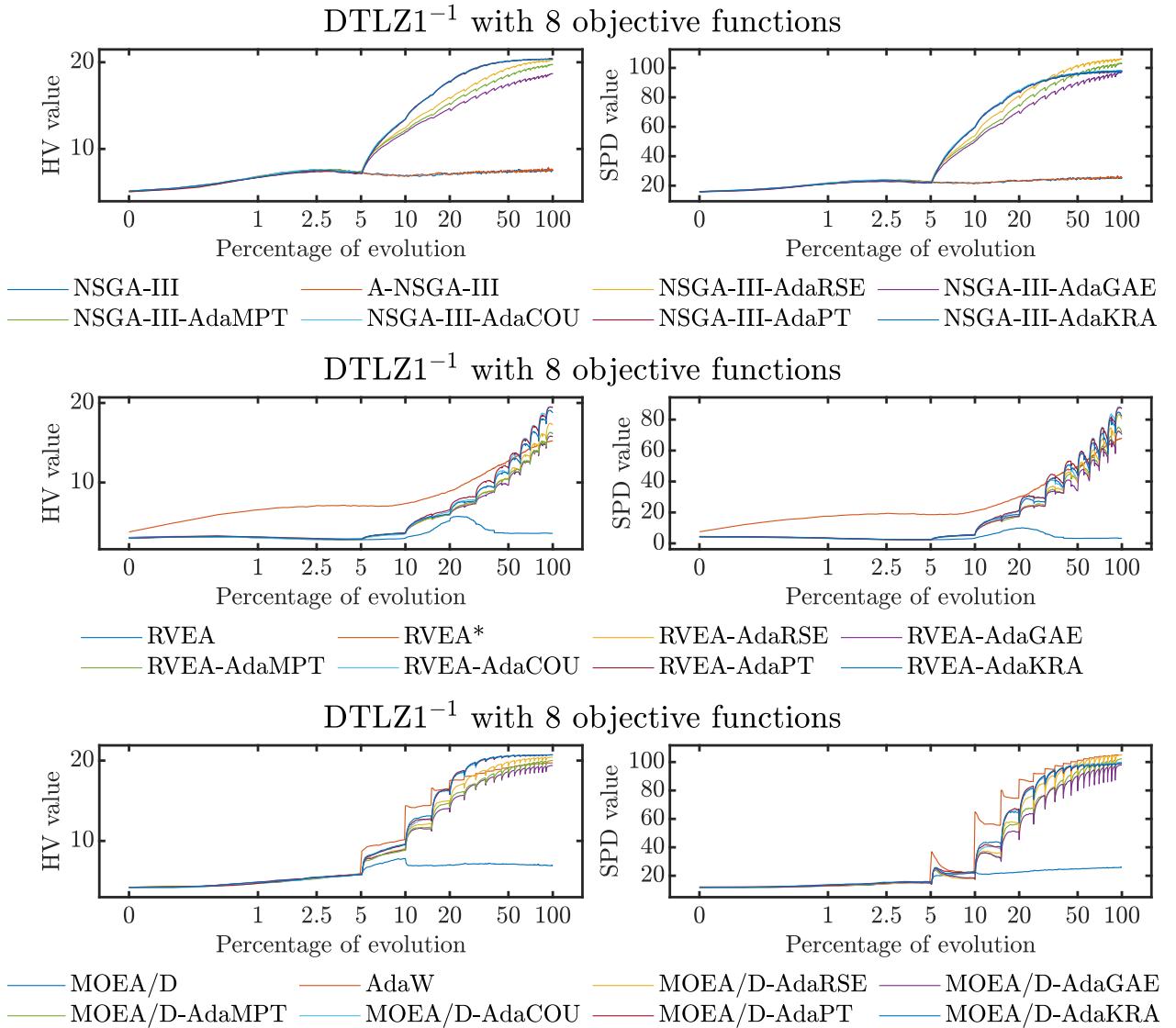


Figure 139: Convergence and diversity graphs with the mean HV value and SPD value of 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ1⁻¹ with 8 objective functions.

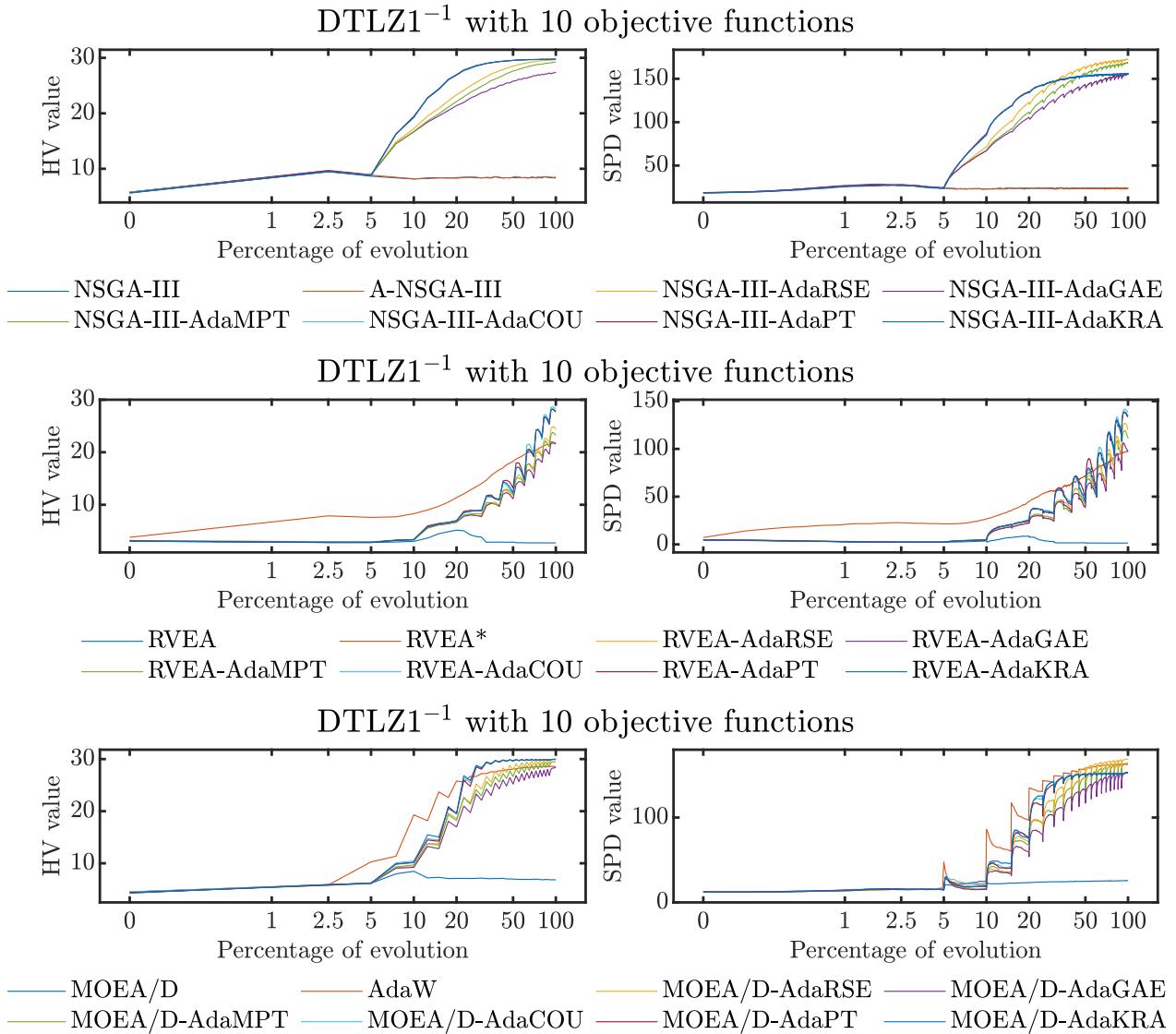


Figure 140: Convergence and diversity graphs with the mean HV value and SPD value of 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on DTLZ1⁻¹ with 10 objective functions.

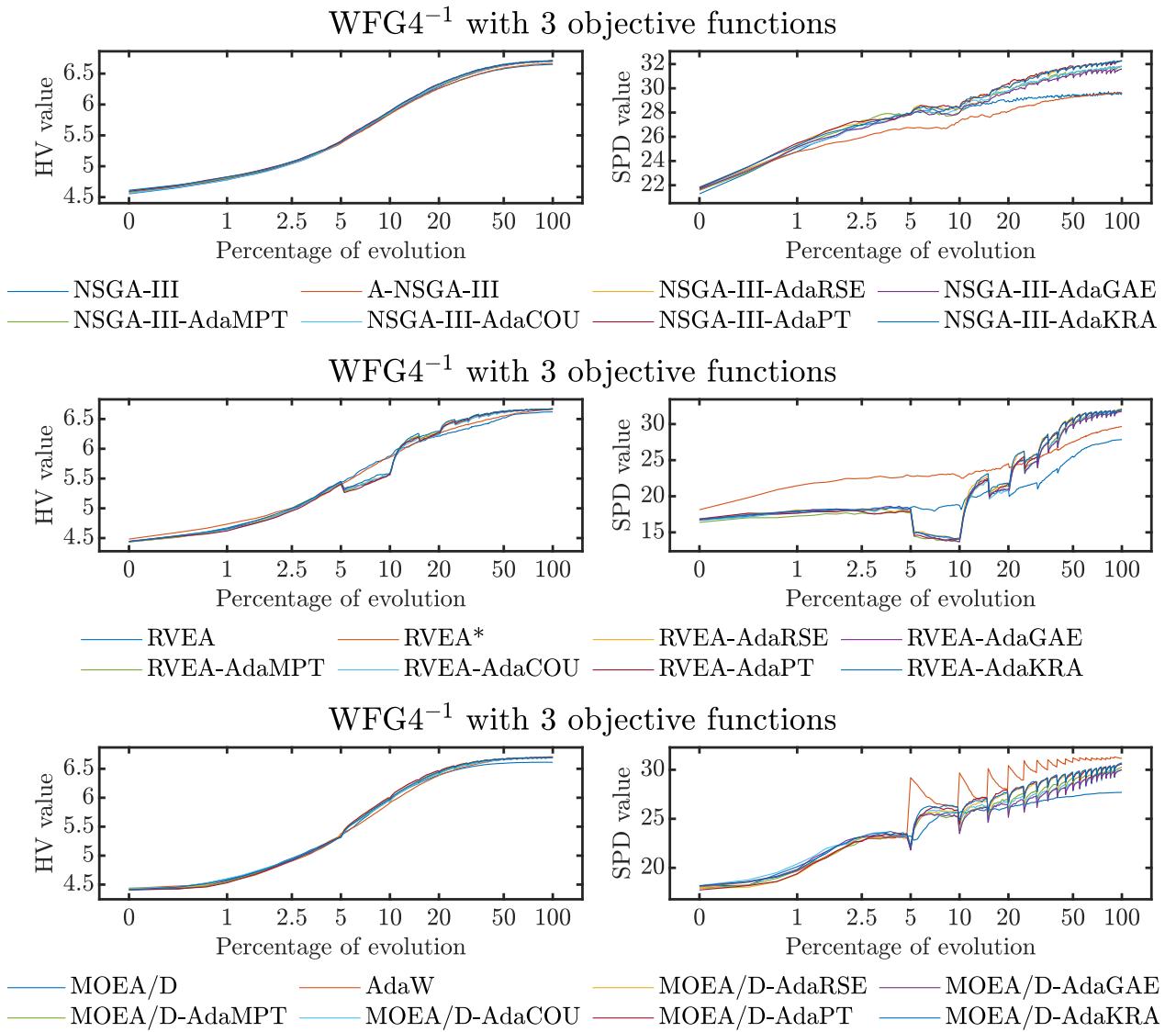


Figure 141: Convergence and diversity graphs with the mean HV value and SPD value of 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG4⁻¹ with 3 objective functions.

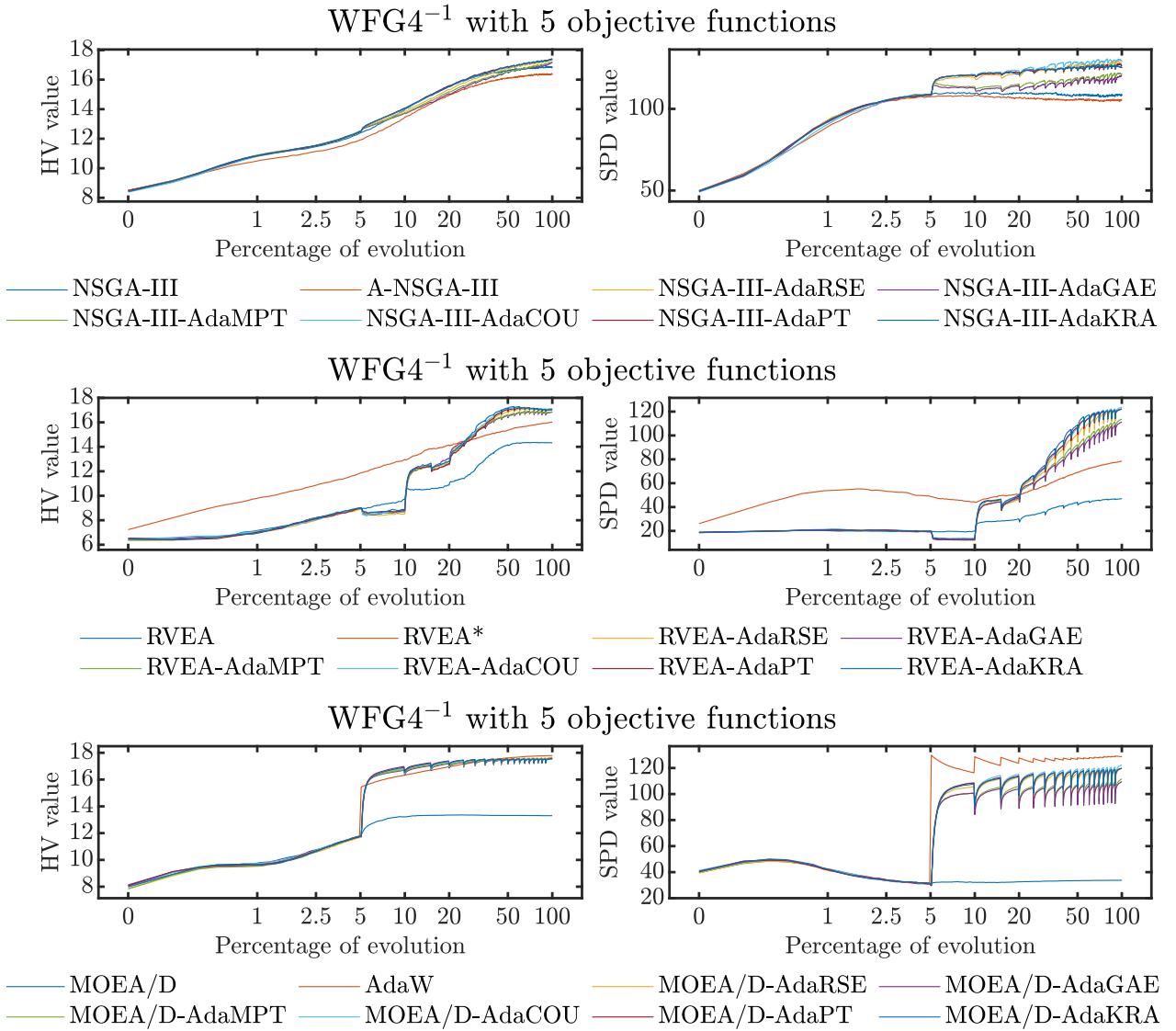


Figure 142: Convergence and diversity graphs with the mean HV value and SPD value of 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG4⁻¹ with 5 objective functions.

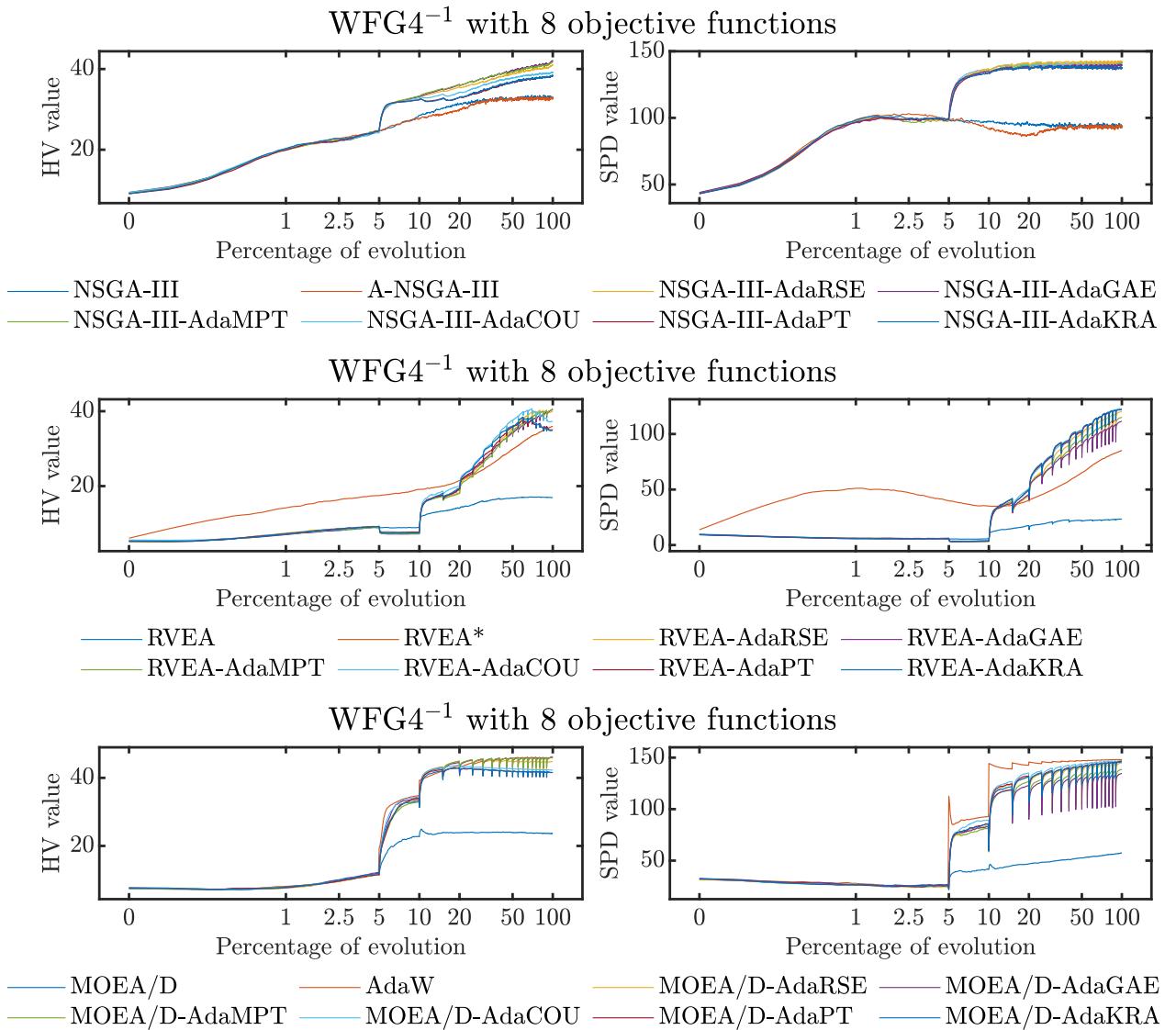


Figure 143: Convergence and diversity graphs with the mean HV value and SPD value of 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG4⁻¹ with 8 objective functions.

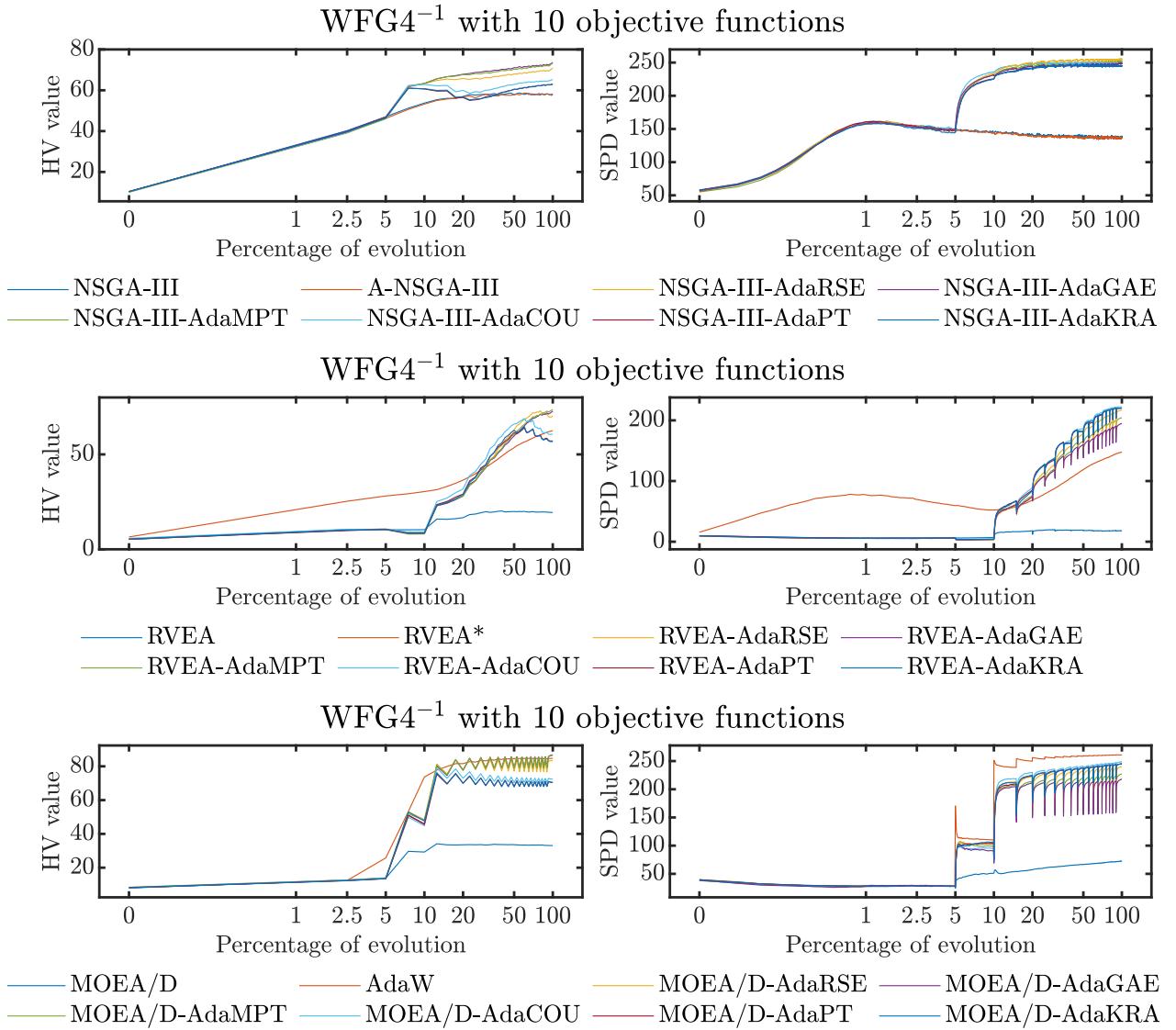


Figure 144: Convergence and diversity graphs with the mean HV value and SPD value of 30 independent runs of MOEAs using the NSGA-III, RVEA, and MOEA/D frameworks on WFG4⁻¹ with 10 objective functions.