

Lecture 10

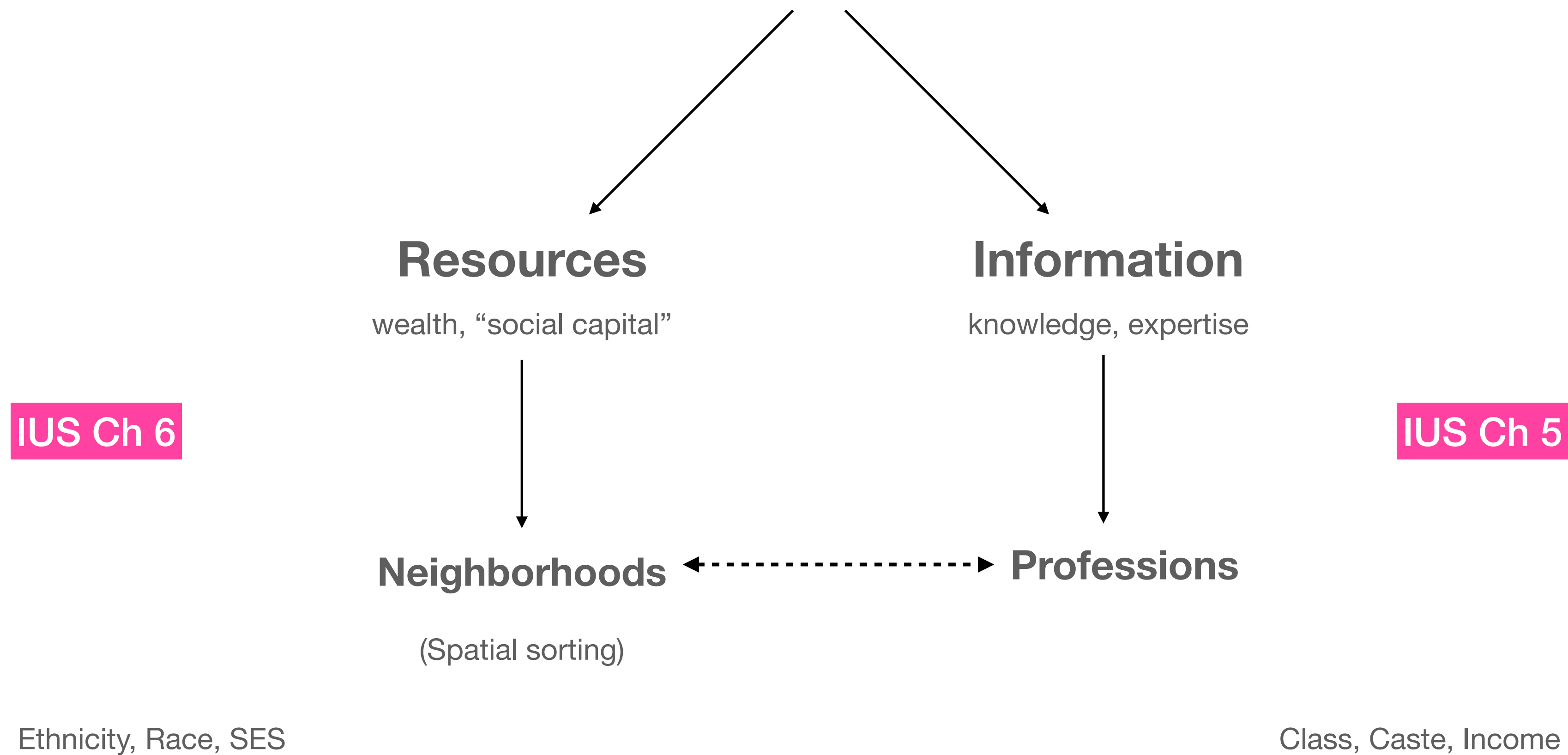
Looking inside Cities: Professional Diversity and Productivity

10.2 Professional and Business Diversity and the Productivity of Cities

IUS 5

@Luís M. A. Bettencourt 2024

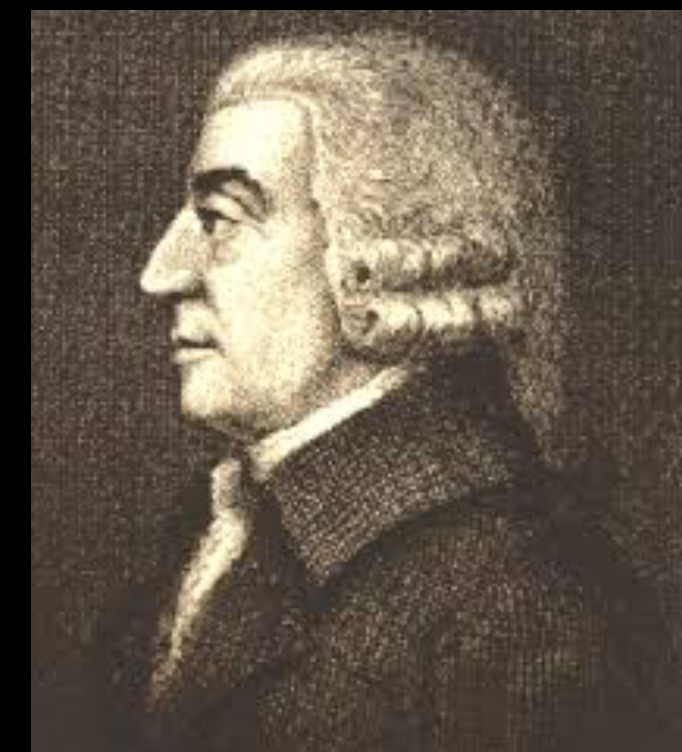
Inequality and statistics of variation in cities



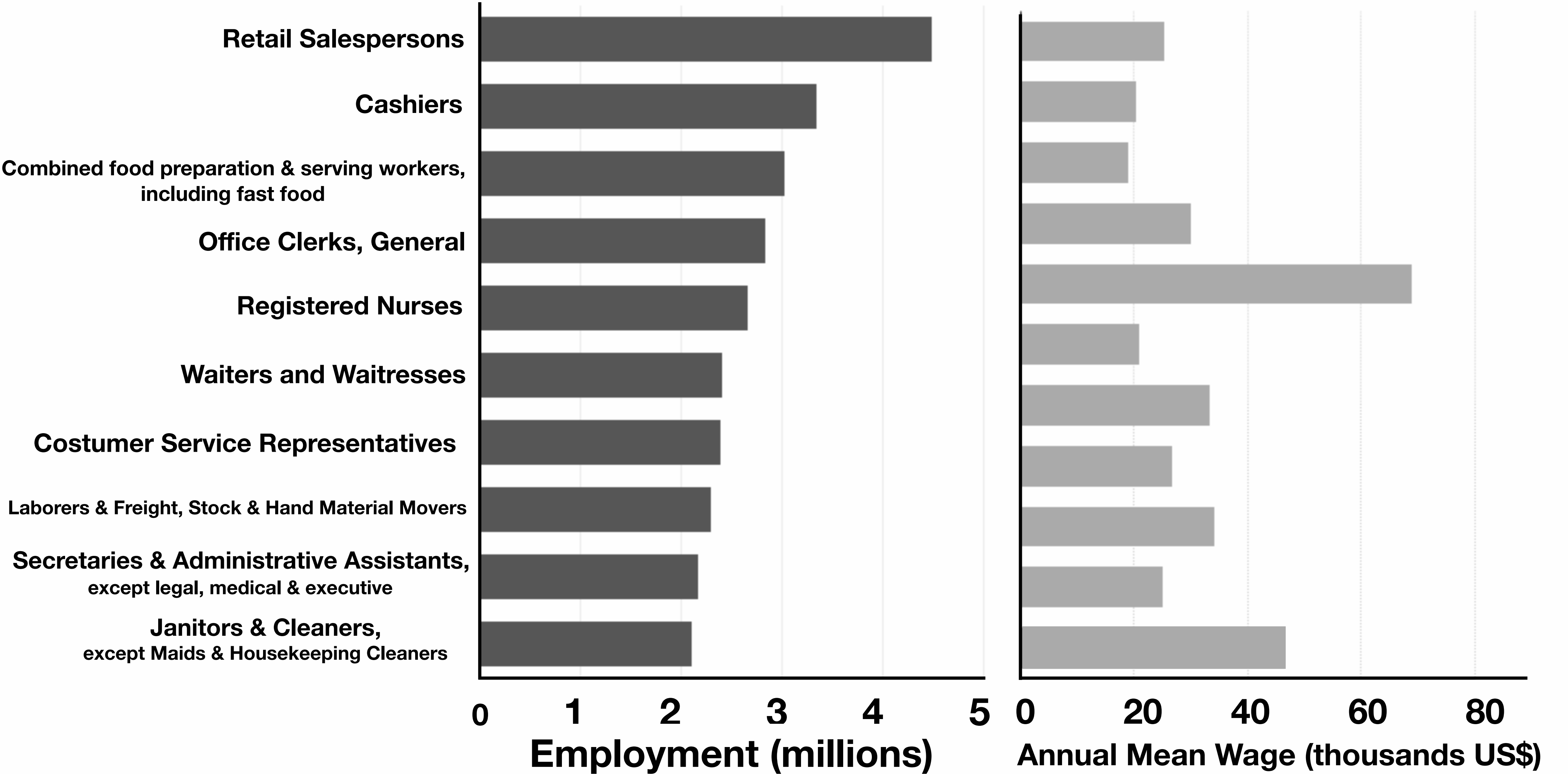
Observe the accommodation of most day laborers in a civilized and thriving country, and you will perceive that the number of people of whose industry a part, though but a small part, has been employed in procuring him this accommodation, exceeds all computation. [...]

if we examine, all these things, and consider what a variety of labour is employed about each of them, we shall be sensible that without the assistance and co-operation of many thousands, the very meanest person in a civilized country could not be provided

Adam Smith (wealth of nations, ch 2)



Occupations with the highest employment, USA 2013



Sector 71 — Arts, Entertainment, and Recreation $r_s = 2$

711 Performing Arts, Spectator Sports, and Related Industries $r_s = 3$

7111 Performing Arts Companies $r_s = 4$

71111 Theater Companies and Dinner Theaters $r_s = 5$

711110 Theater Companies and Dinner Theaters $r_s = 6$

71112 Dance Companies

711120 Dance Companies

71113 Musical Groups and Artists

711130 Musical Groups and Artists

71119 Other Performing Arts Companies

711190 Other Performing Arts Companies

7112 Spectator Sports

71121 Spectator Sports

711211 Sports Teams and Clubs

711212 Racetracks

711219 Other Spectator Sports



resolution

Professional Diversity and Classification Resolution

of different occupations
in US Metropolitan
Statistical Areas

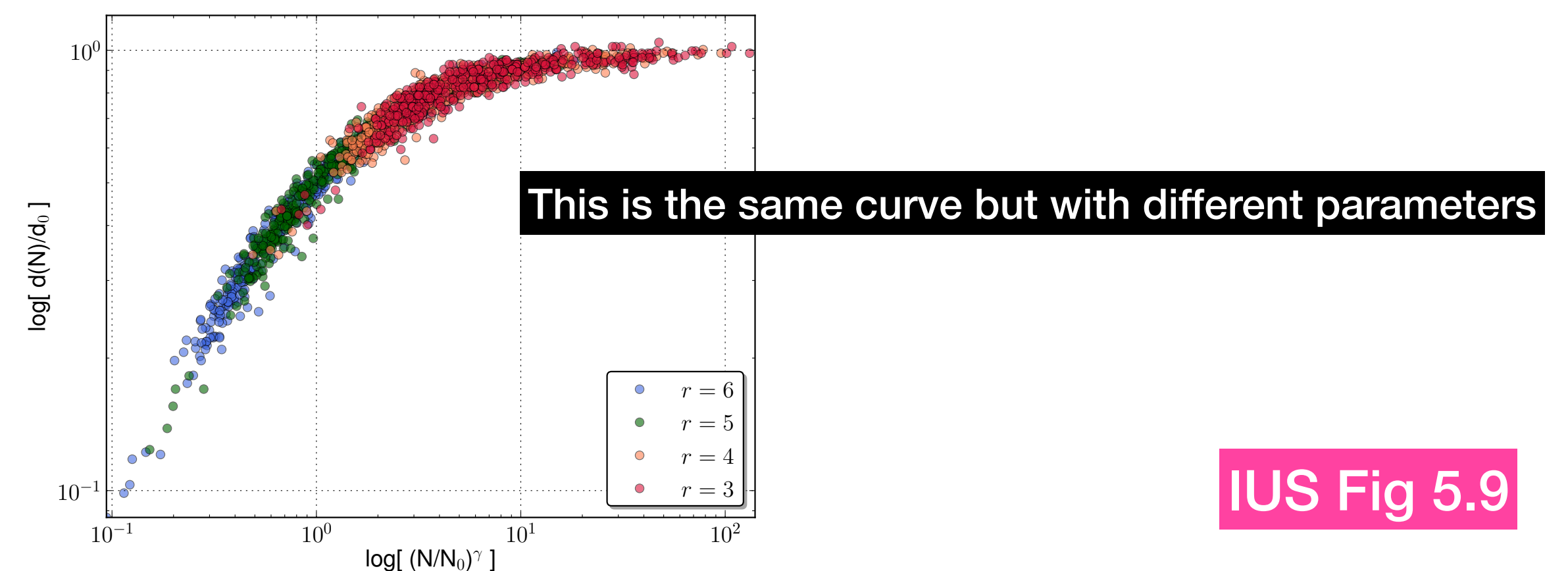
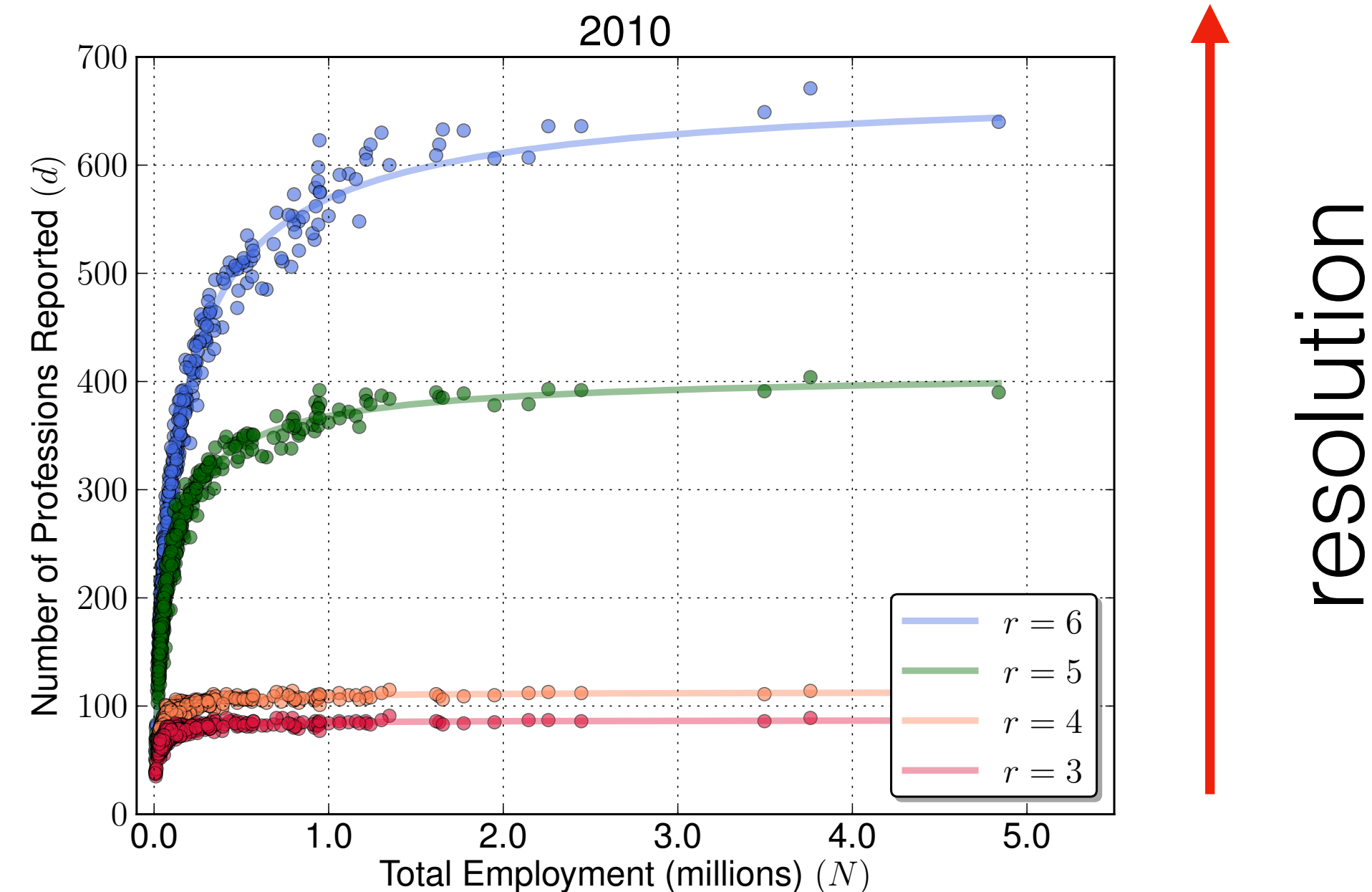
A good fit at all **resolutions**:

$$D(N_e) = d_0 \frac{\left(\frac{N_e}{N_0}\right)^\gamma}{1 + \left(\frac{N_e}{N_0}\right)^\gamma}.$$

↑
occupation richness: count different professions

$$\gamma = 1 - \delta \simeq \frac{5}{6}$$

<https://www.nature.com/articles/srep05393>



IUS Fig 5.9

Inferring actual diversity $D(N)$:

$$D(N) = d_0 h \left(\frac{N}{N_0} \right) \left(\frac{N}{N_0} \right)^\gamma \rightarrow \begin{cases} D_0 N^\gamma, & N \ll N_0, \\ d_0(r), & N \gg N_0, \end{cases}$$

In the limit of no saturation:

$$\frac{N}{N_0} \rightarrow 0; \quad h \rightarrow 1, \quad D_0 \rightarrow \frac{d_0}{N_0^\gamma}$$

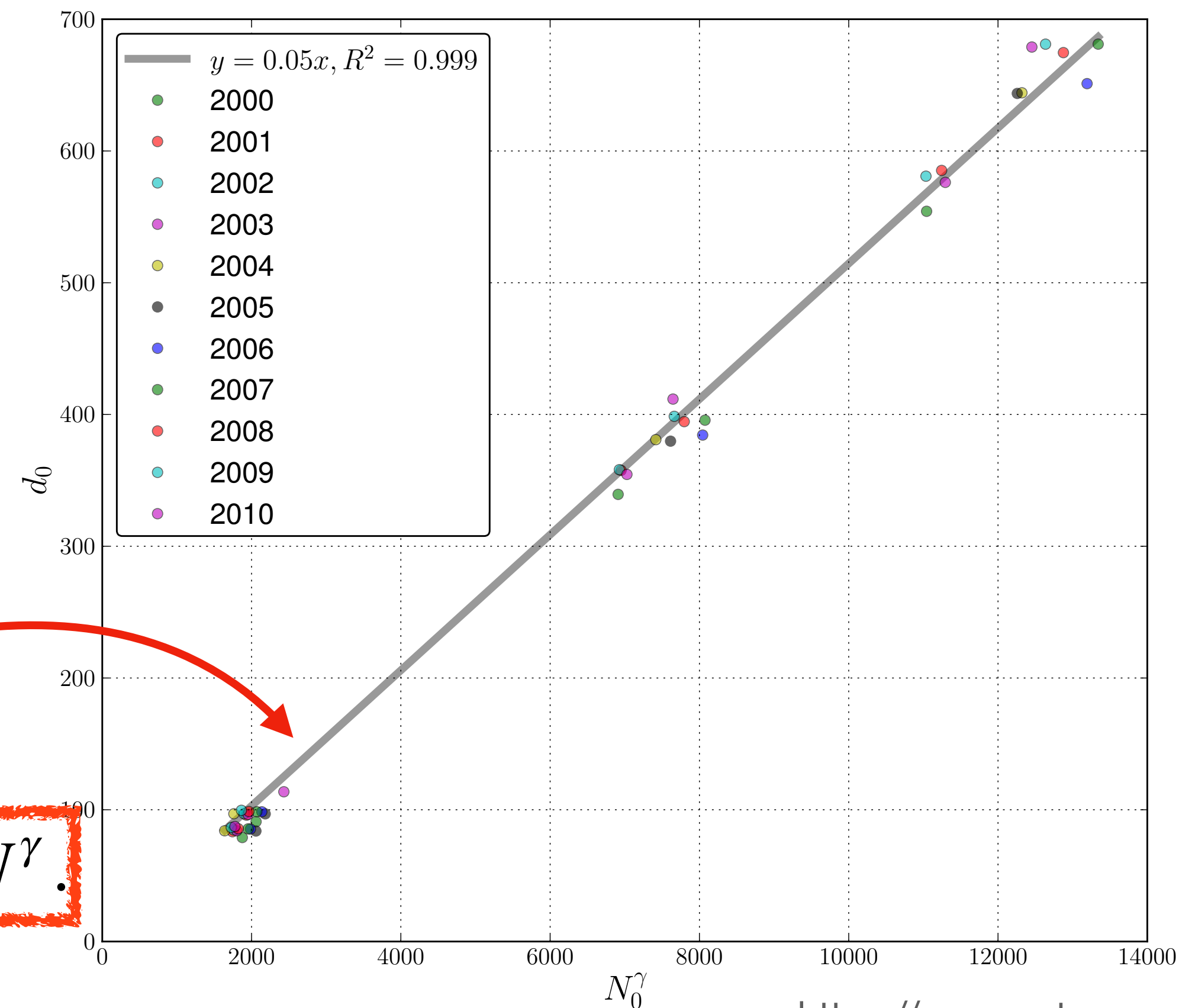
In the limit of full saturation:

$$\frac{N}{N_0} \rightarrow +\infty; \quad h \rightarrow \left(\frac{N_0}{N} \right)^\gamma,$$

A scaling limit exists if:

$$D_0 \rightarrow \frac{d_0}{N_0^\gamma} = \text{const.} \quad \text{with} \quad D(N) = D_0 N^\gamma.$$

Test !



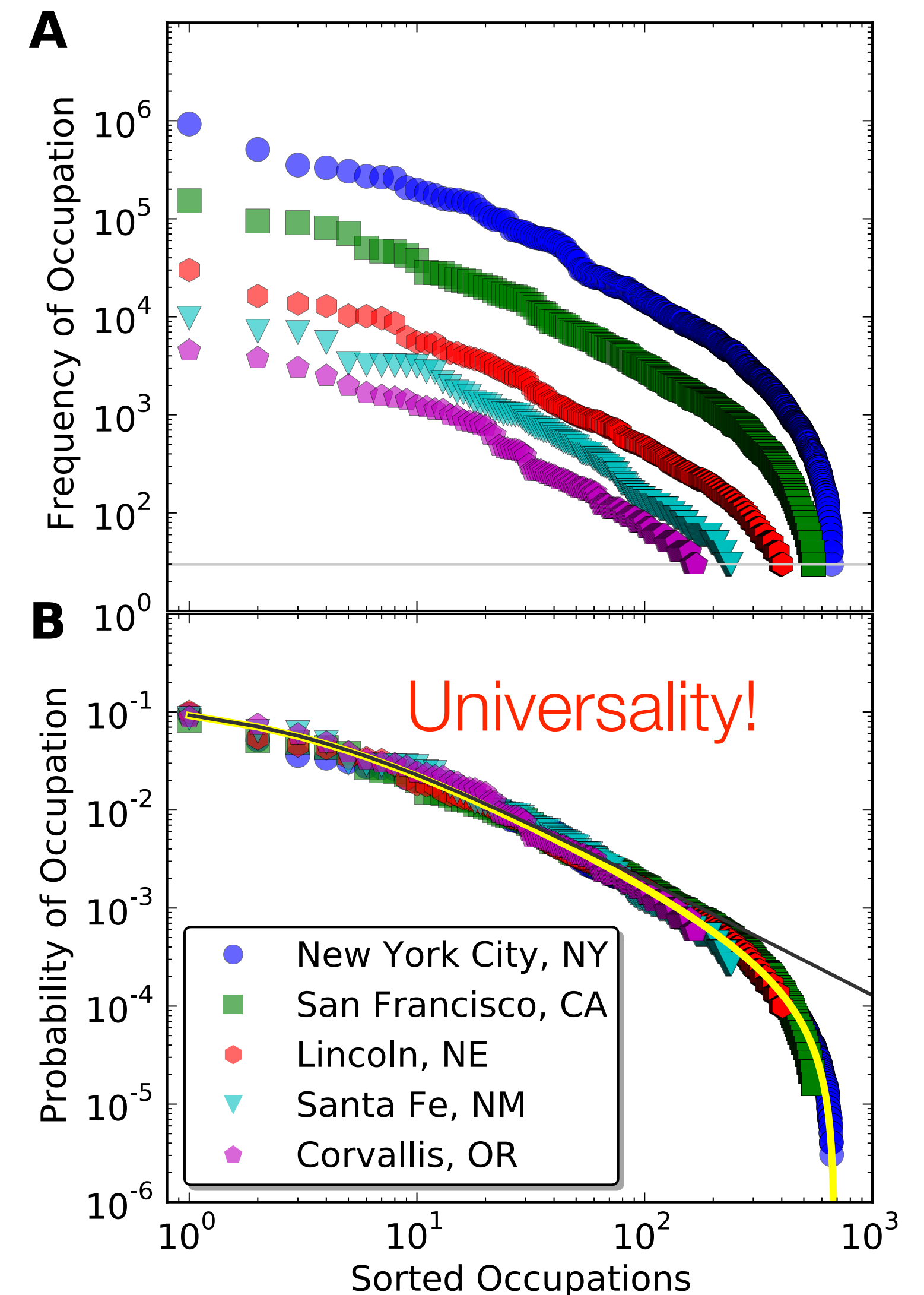
The distribution of professions (more common / less common)

IUS Fig 5.10

From $D(N)$, for all N , derive frequency distribution

$$f(i) = \frac{N_e}{N_0} \left(\frac{d_0 - i}{i} \right)^{1/\gamma}.$$

$$p(i) = \frac{f(i)}{\sum_{j=1}^{D(N)} f(j)} = \frac{1-\gamma}{\gamma} \frac{i^{-1/\gamma}}{1 - D(N)^{-\frac{1-\gamma}{\gamma}}};$$



Professional Diversity and Urban Productivity (back to Adam Smith)

Specialization as the Division of Labor

as sources of increases in urban **productivity**

$$D/N = D_0 N^{-\delta}$$

Diversification comes from specialization

specialization

$$y = Y_0 N^\delta = G I(N)$$

productivity

interactions per capita

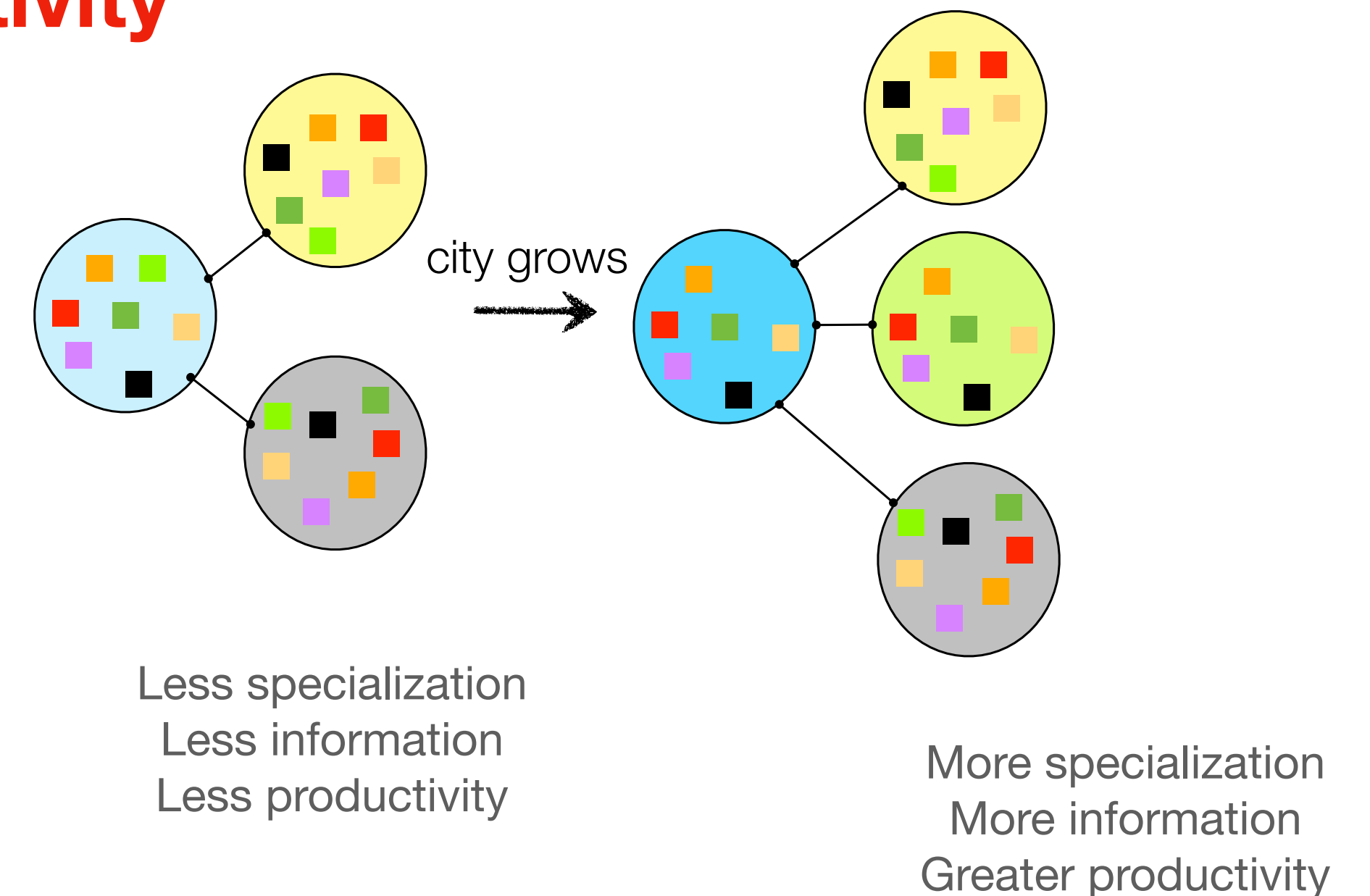
This tells us that there is an invariant quantity (total functions):

$$y(N) * \frac{D(N)}{N} = F$$

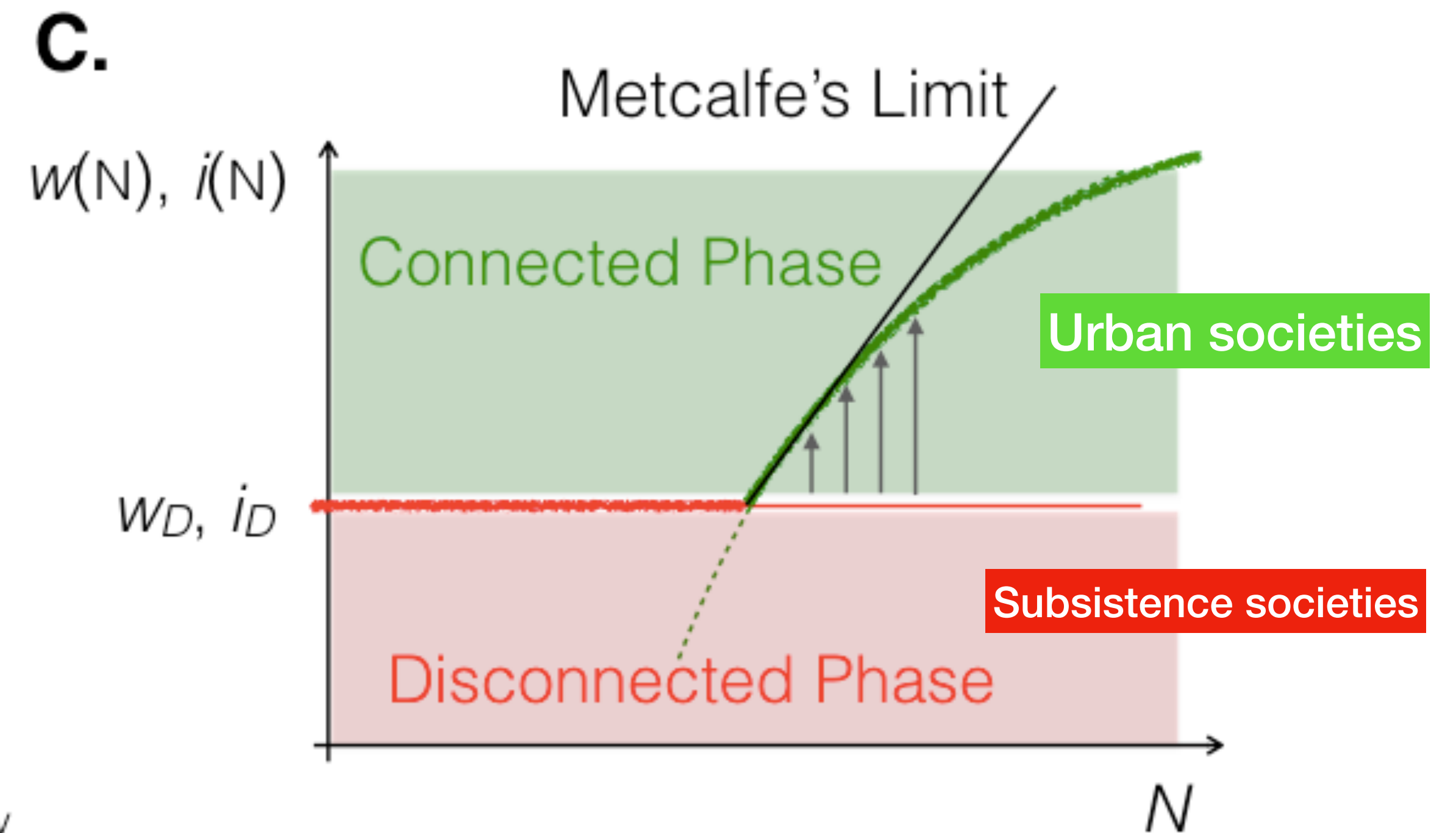
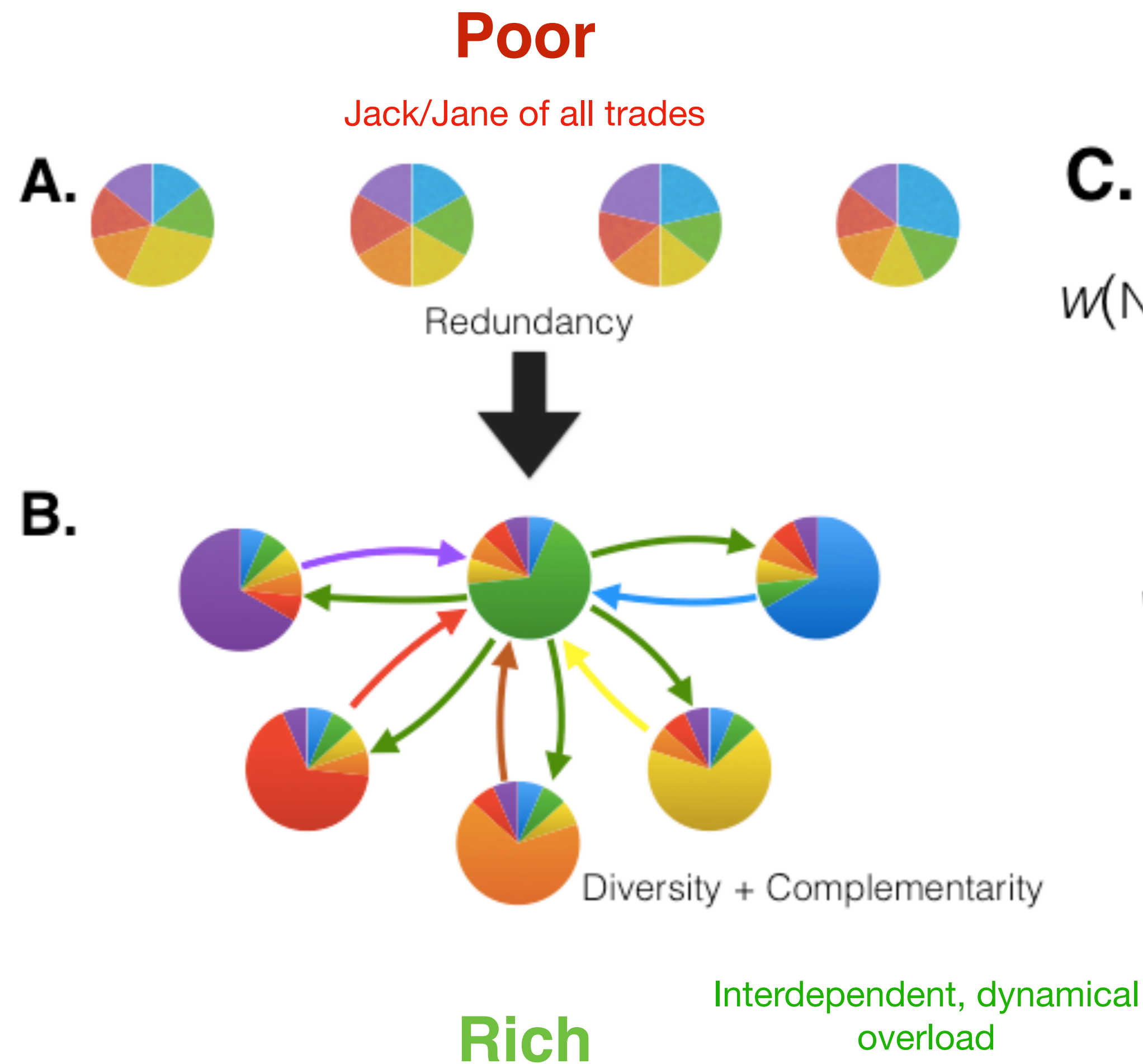
independent of city size

better quality, more segmented functions

**In a larger city I get more different things from more different people,
to satisfy same needs**



Generalizing: Information, Connectivity & Productivity



IUS Fig 5.12

IUS Fig 5.13

A Network Theory of Development:

Interconnected human societies
contain more information at higher connectivity costs

CHARACTERISTICS OF COMPLEX NETWORK PHASES

Symbol	Node Property	Disconnected Phase	Connected Phase
k	connectivity (degree)	k_D (small)	$k(N) = k_c(t)N^\delta$ (increasing)
d	number of functions	d_D (large)	$d(N) = d_c(t)N^{-\delta}$ (decreasing)
i	information	i_D (small)	$i(N) = i_c(t)N^\delta$ (increasing)
w	productivity	w_D (low)	$w(N) = w_c(t)N^\delta$ (increasing)
t	time per function	t_D (small)	$t(N) = t_c(t)N^\delta$ (increasing)
c	cost per connection	c_D (large)	$c(N) = c_c(t)N^\delta$ (increasing)

Metcalf's limit of the connected phase is obtained as $\delta \rightarrow 1$, see Figure 1.

IUS Table 5.3



In a real sense all life is inter-related.

All people are caught in an inescapable network of mutuality, tied in a single garment of destiny.

Whatever affects one directly, affects all indirectly.

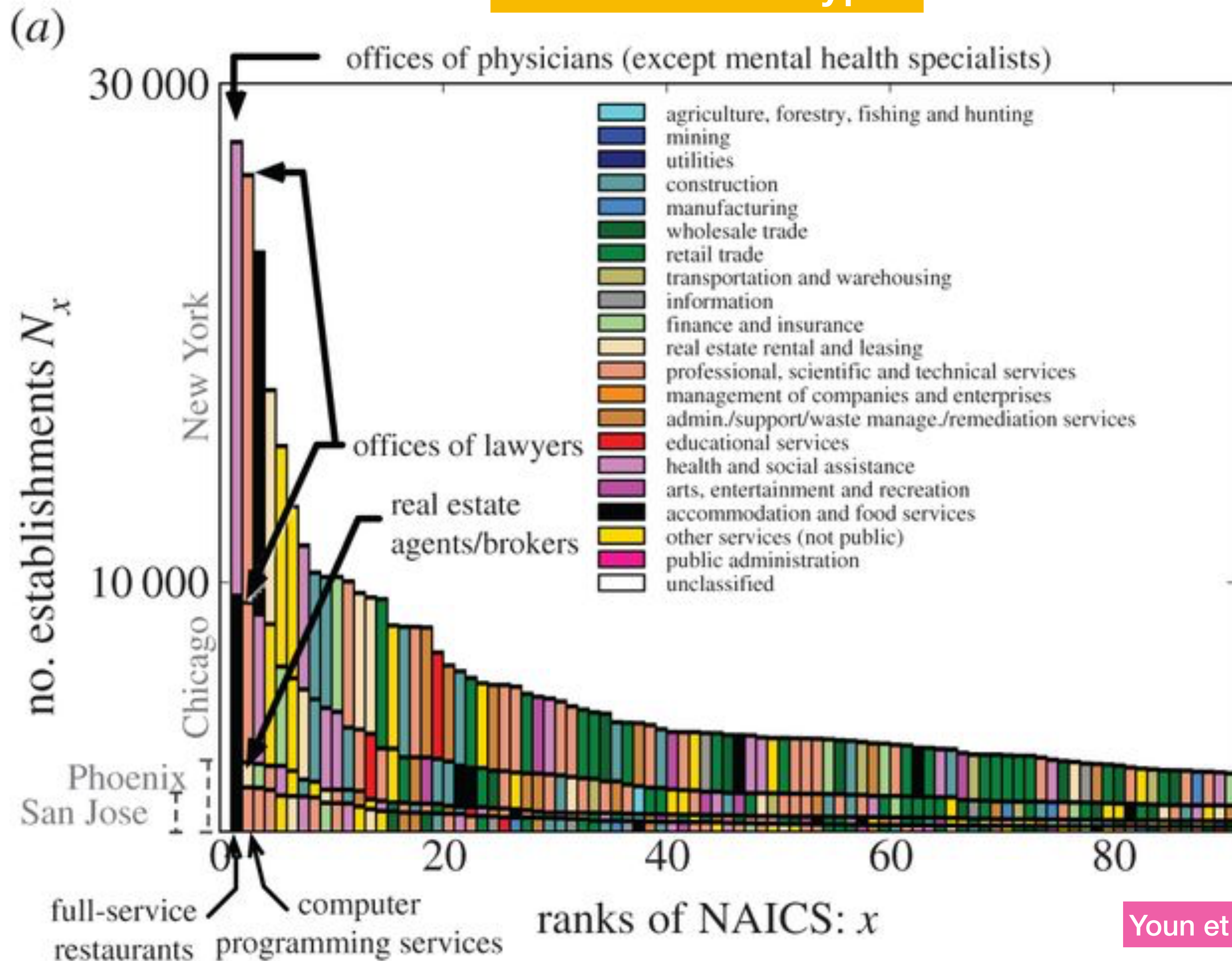
I can never be what I ought to be until you are what you ought to be, and you can never be what you ought to be until I am what I ought to be...

This is the inter-related structure of reality.

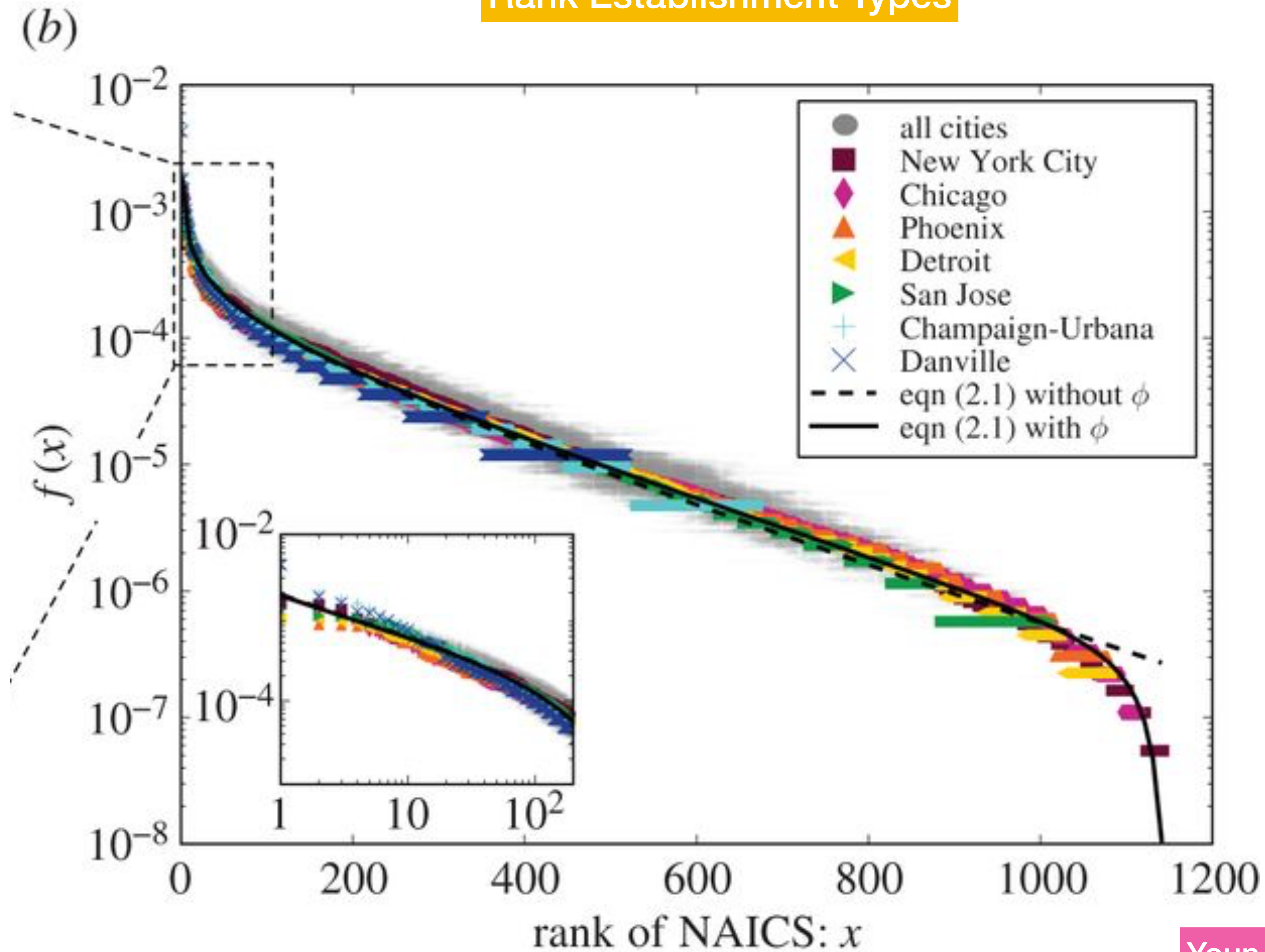
- Martin Luther King Jr, Letter from Birmingham Jail.

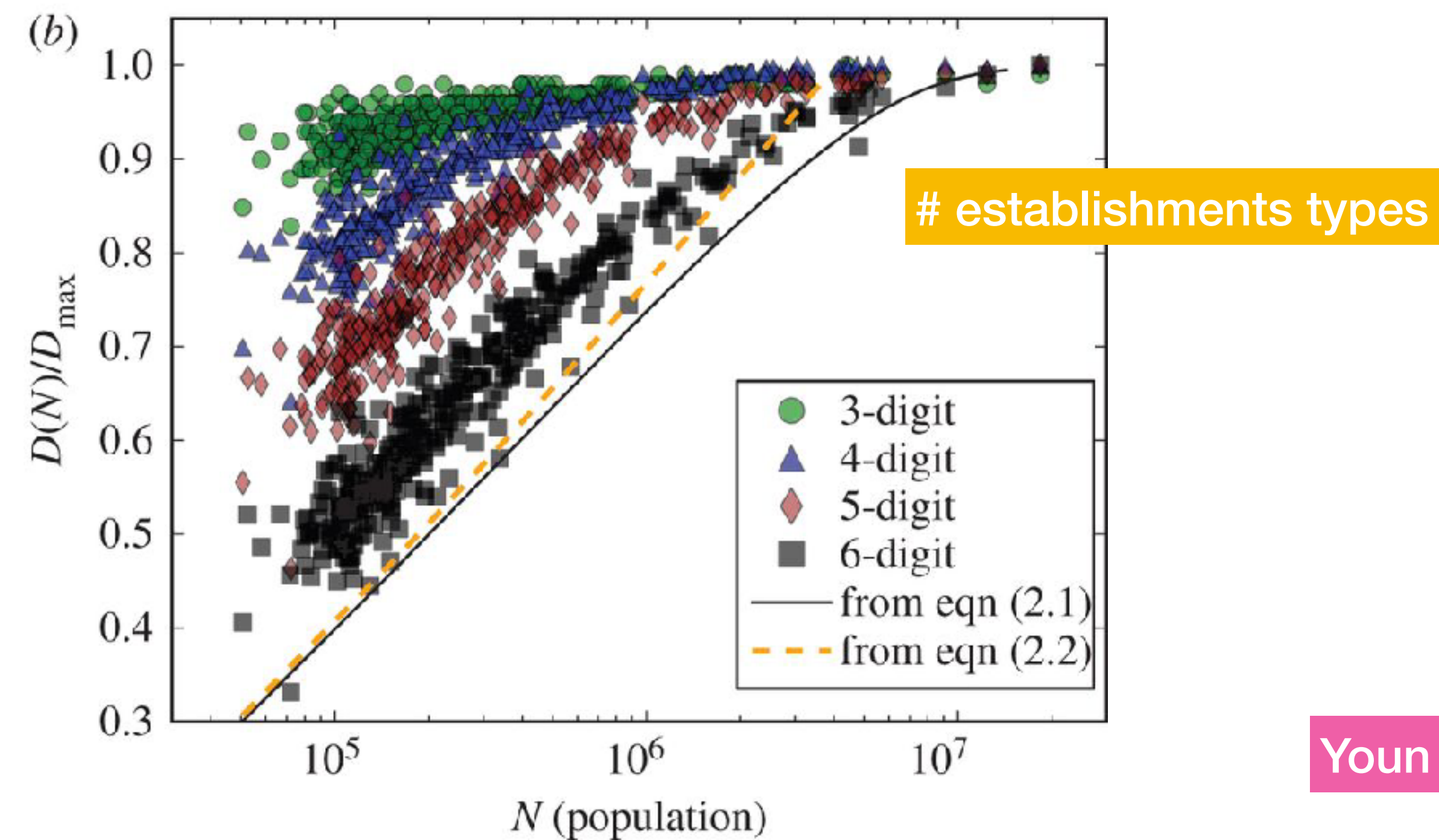
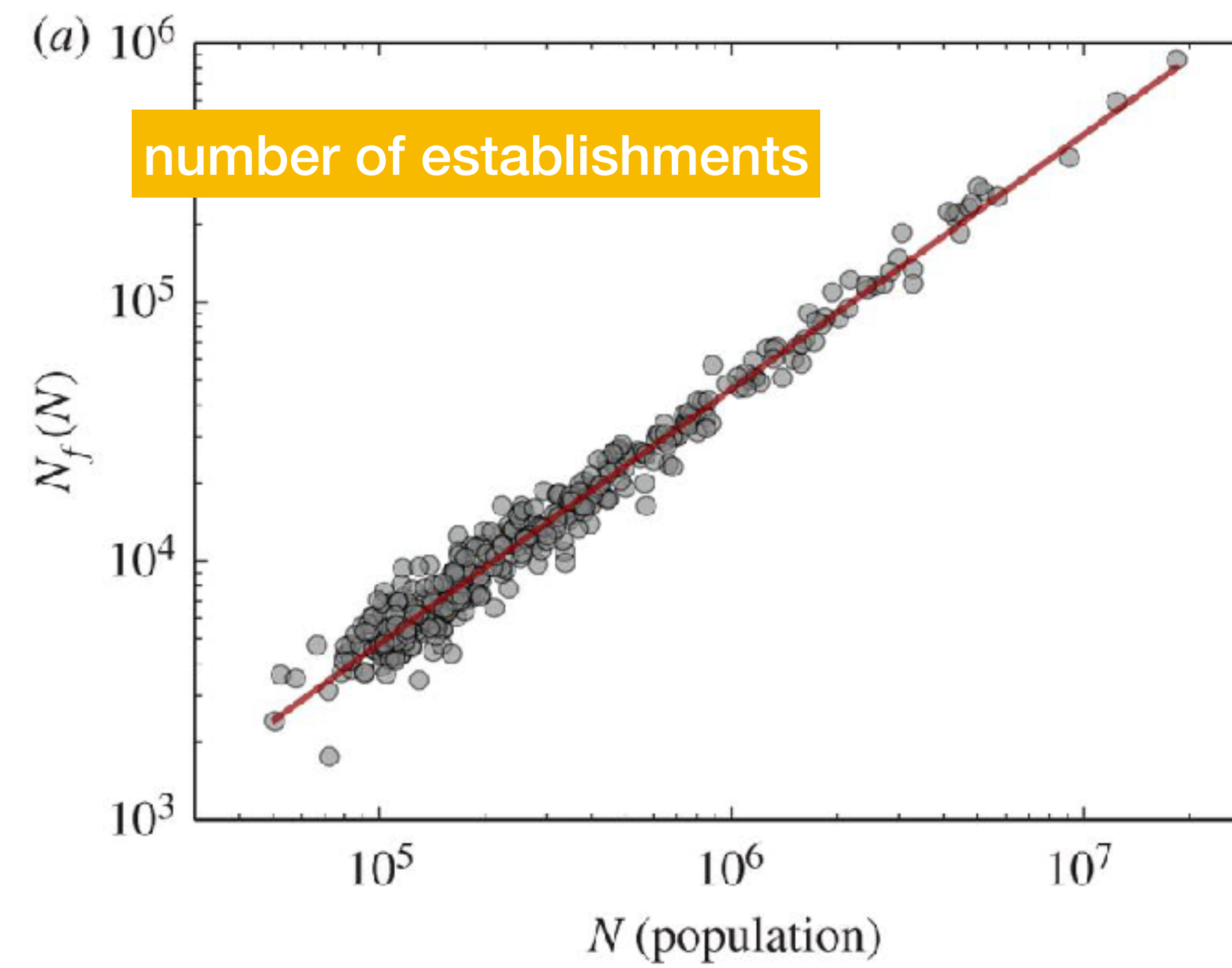
Business Diversity

Establishment Types

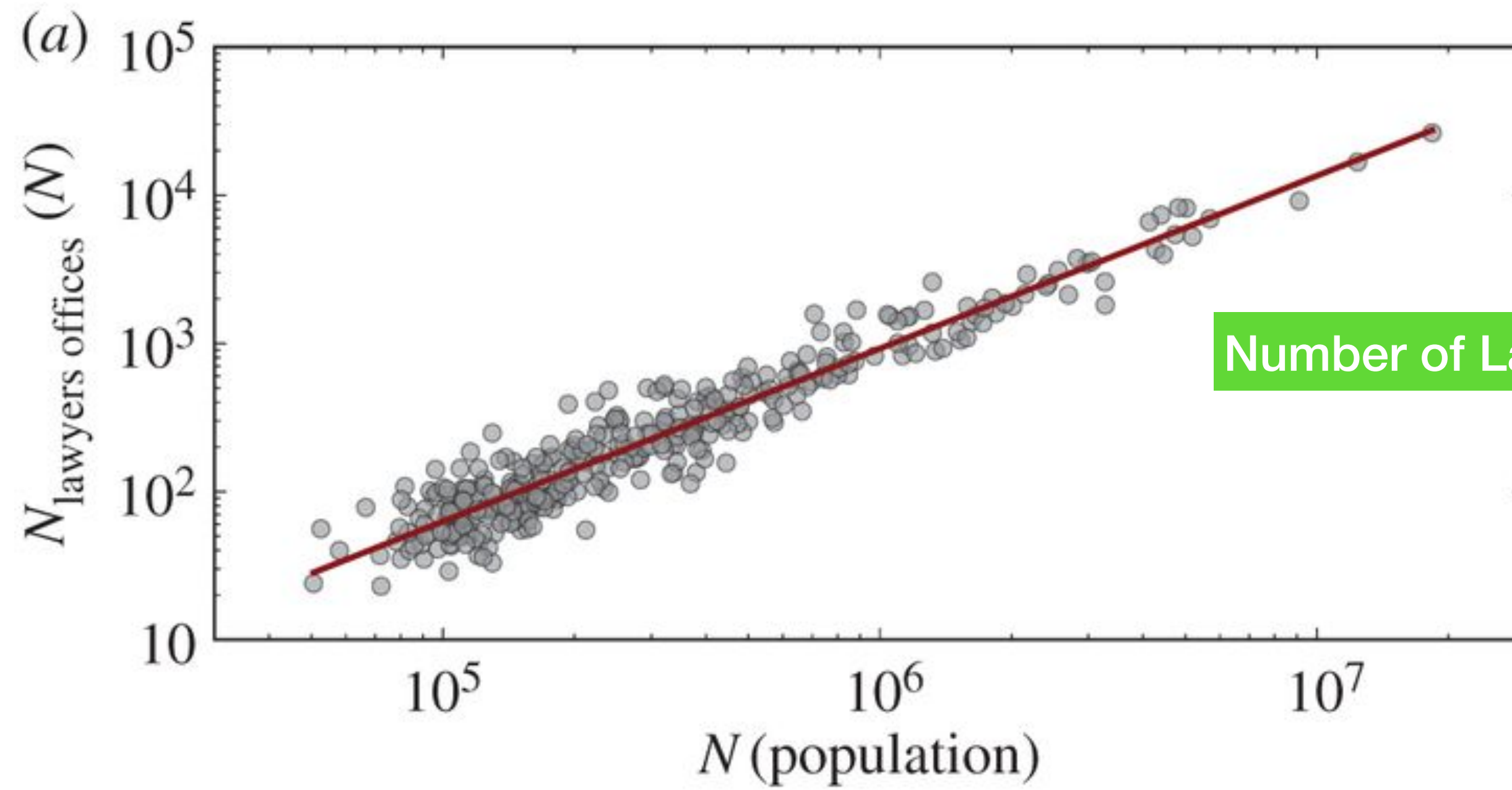


Rank Establishment Types

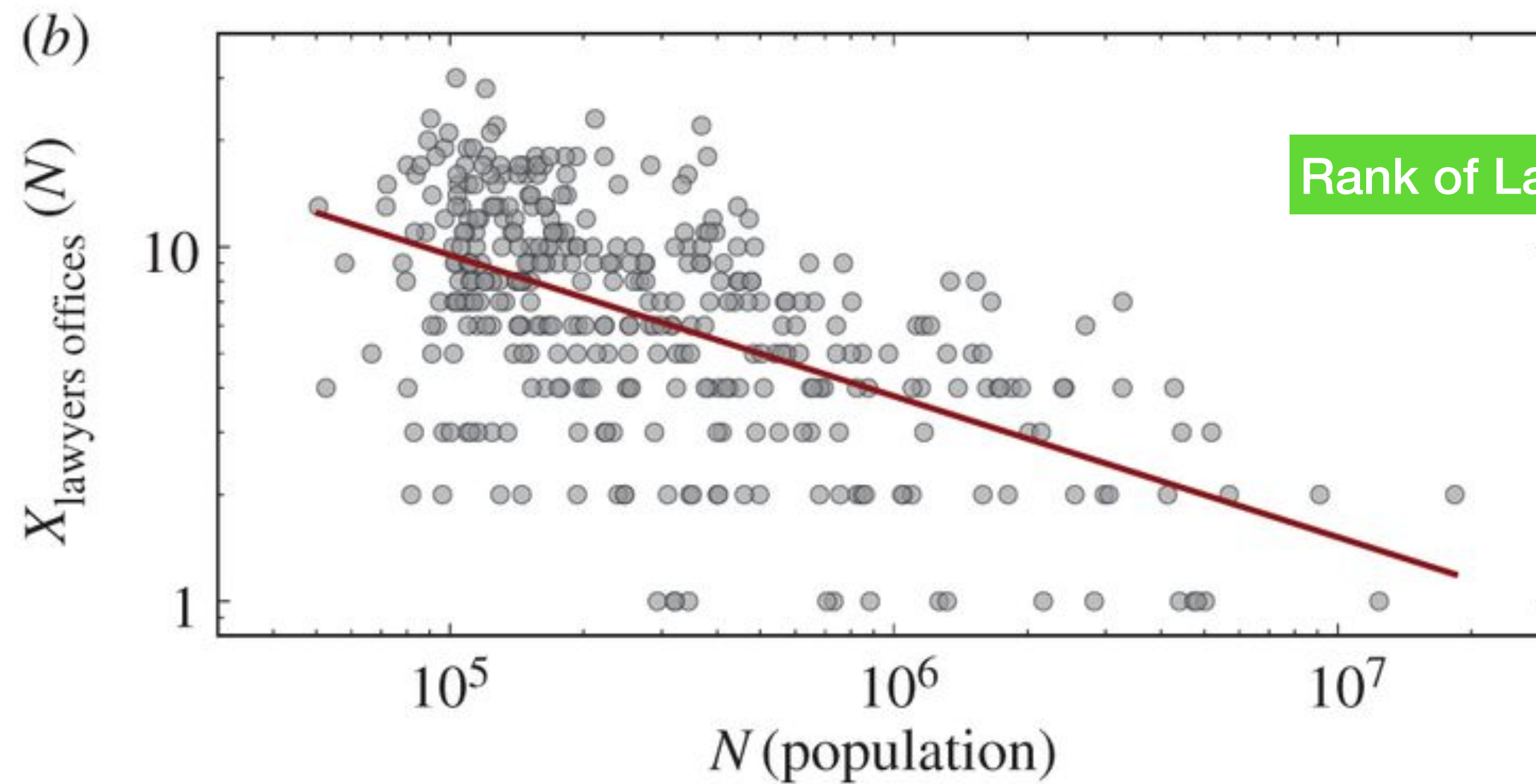




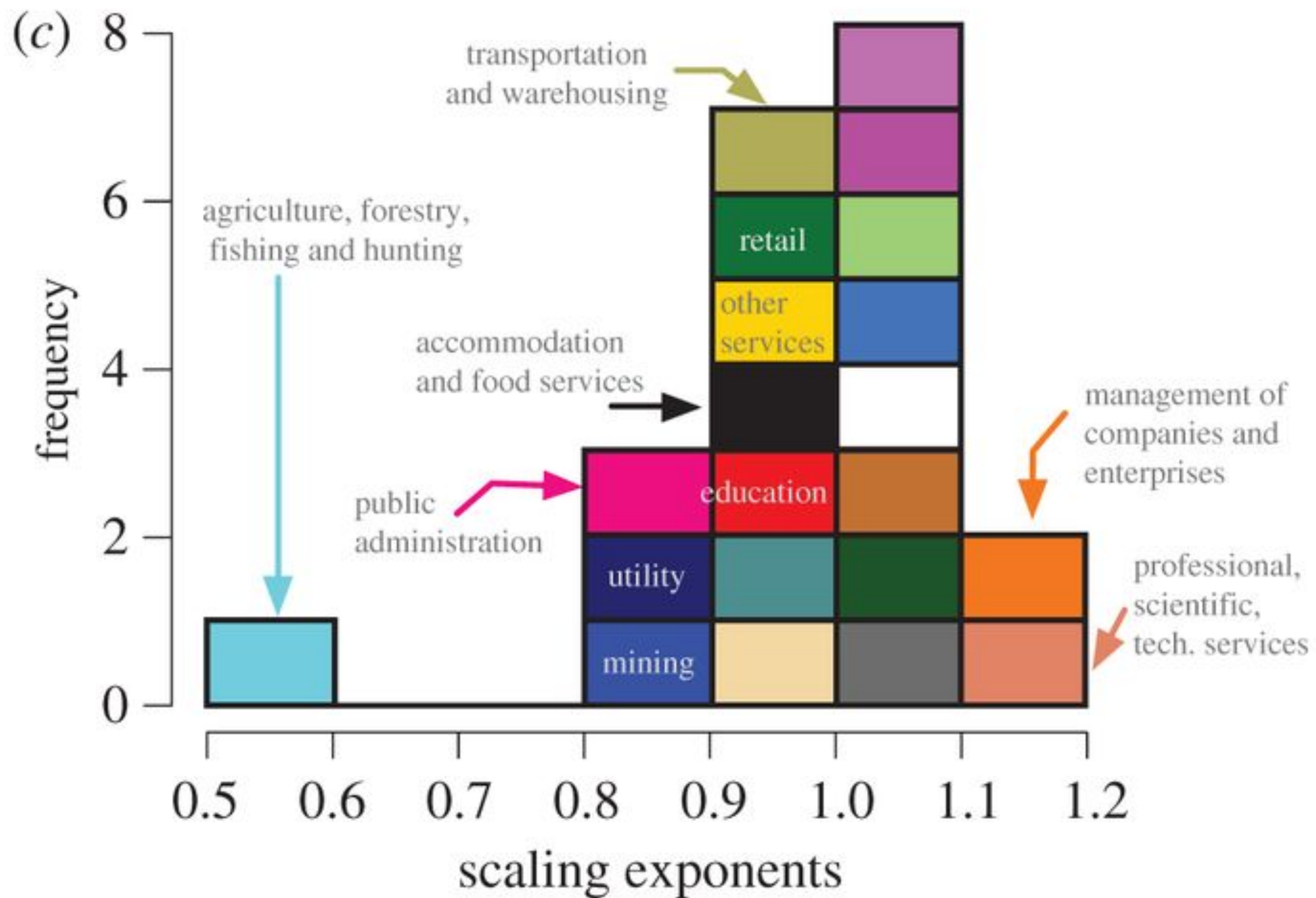
Scale each business type on population



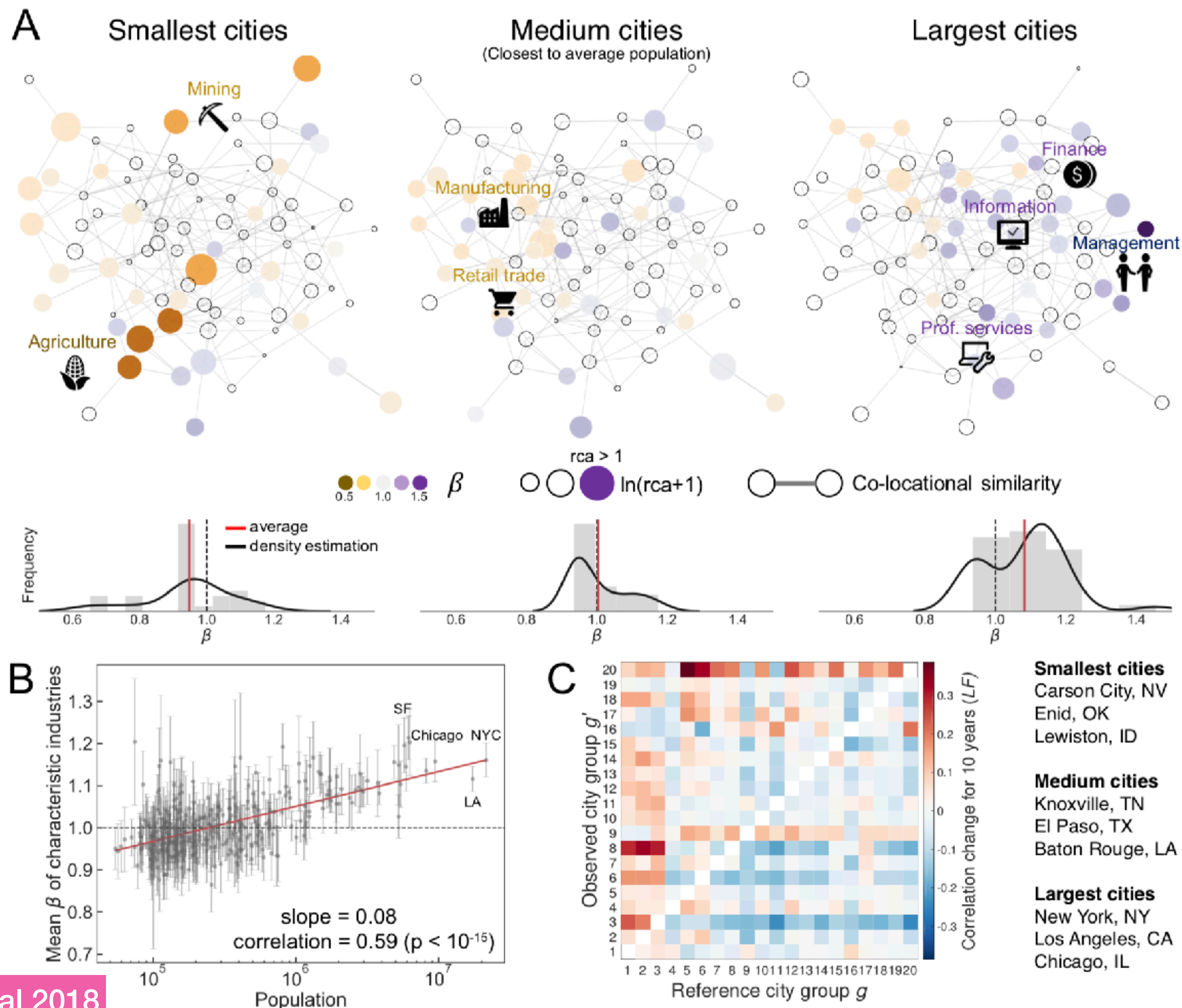
Number of Lawyers Offices



Rank of Lawyers Offices



Recapitulation of Business Sectors



Functional **Diversity** is related to **Complementarities**

Division of labor, knowledge, interdependence

Second reason (Marshall) for agglomeration economies

This creates an “ecology” of functions in cities that is quantitatively predictable,
with small cities disproportionately dedicated to primary sectors
and large cities to informational activities

Interactions, degree of specialization and economic productivity are
facets of a structural transformation predicted by urban scaling