## Lecture 16

Economic Growth, Information and Cities

16.2 The link between urbanization and economic growth

IUS 9.2



# **Economic Growth**

where do economic growth rates come from?

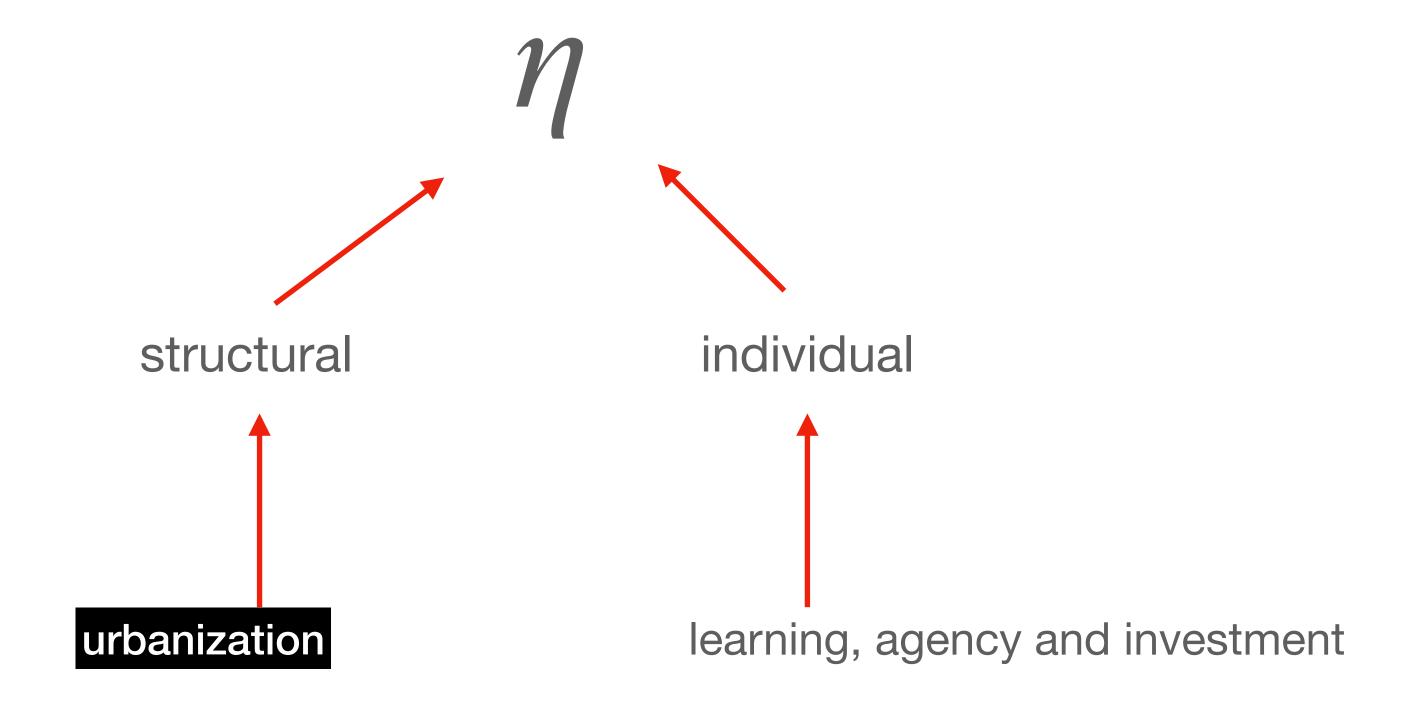
$$\frac{dY}{dt} = \eta Y$$

Exponential Growth: 2-3% a year for USA

noisy, scale dependent, variable



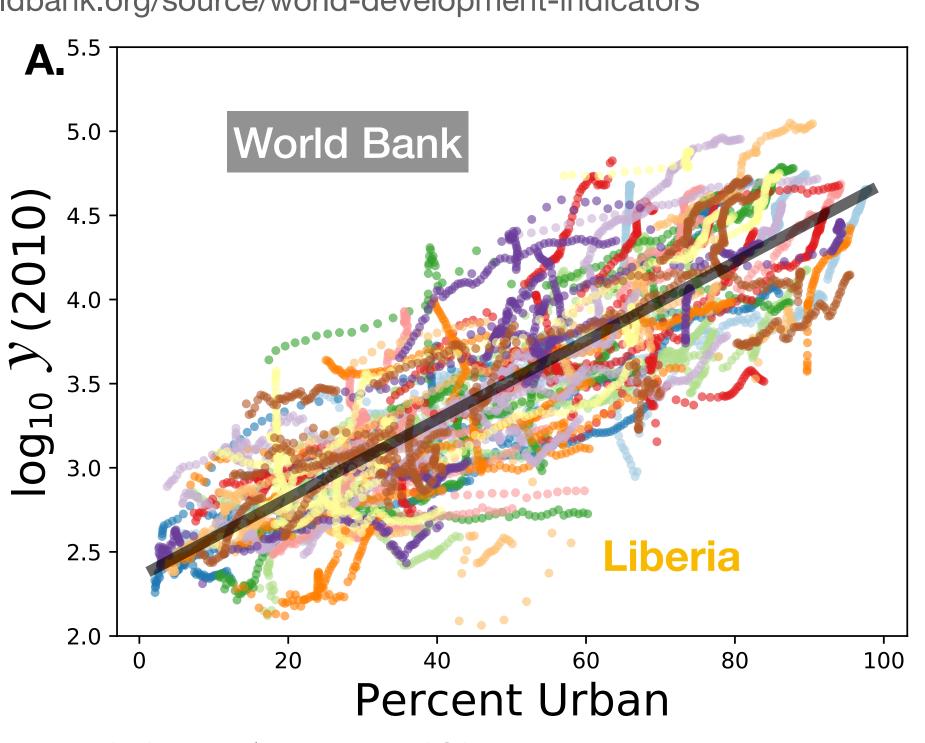
## What creates growth?



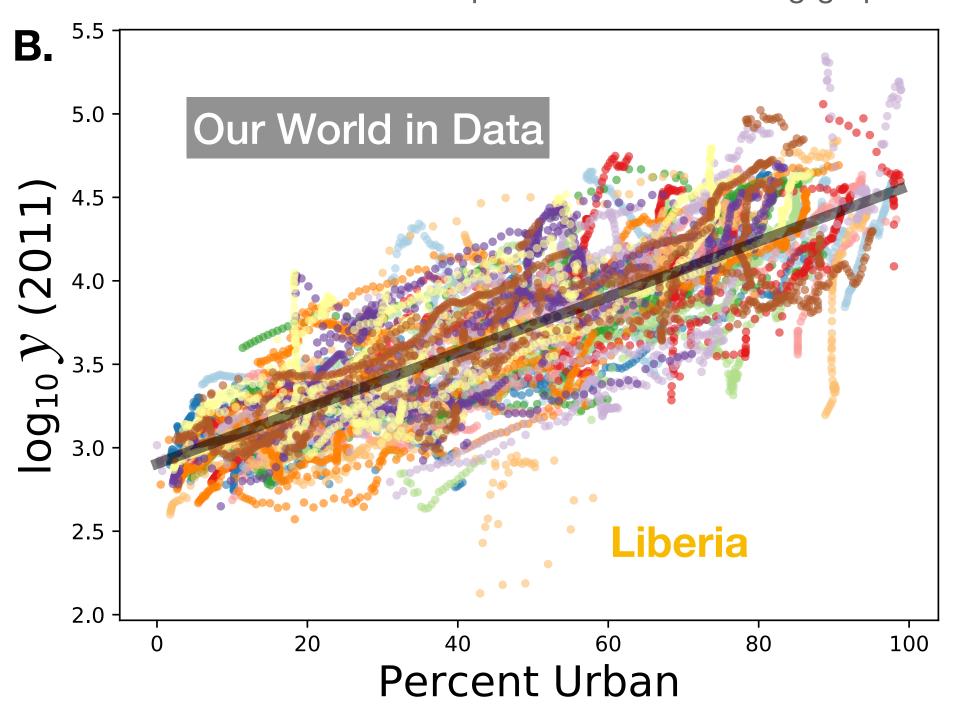
Urbanization and Economic Growth

### How can we explain this association? What does it tell us about economic growth? and Cities?

https://databank.worldbank.org/source/world-development-indicators



https://ourworldindata.org/grapher/urbanization-vs-gdp



Fit:  $\log_{10} y(u) = \log_{10} y(0) + a_y u$  \$235/year  $a_y \simeq 0.02$ 

 $y = y_0 10^{a_y u} = y_0 e^{a_y \ln 10 u}$   $a'_y = a_y \underbrace{\ln 10}_{\approx 2.3} \approx 4 - 5\%$ 

spectacular !!

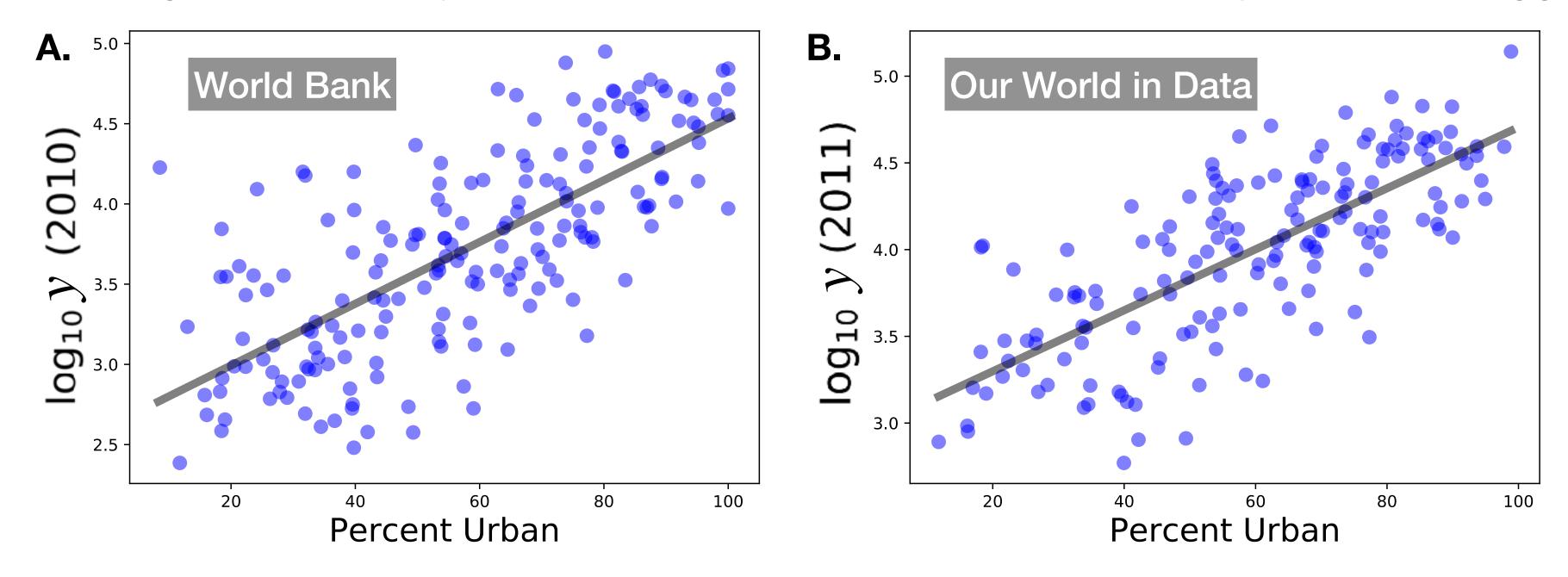
Growth rate of GDP/capita with urbanization is:  $a'_y = a_y \ln 10 \simeq 4 - 5\%$ 

The puzzle here is that there is no "time": this suggests a purely structural transition

### This also holds for each year across nations

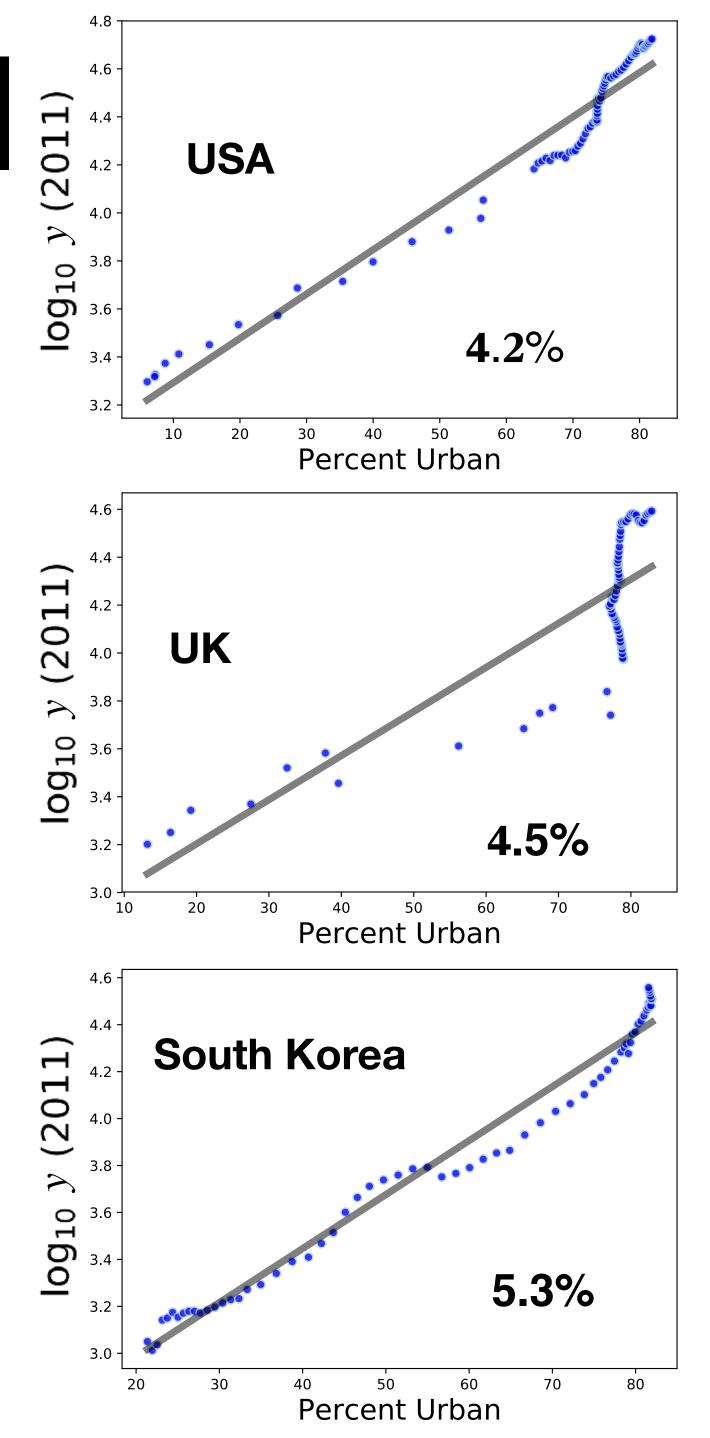
https://databank.worldbank.org/source/world-development-indicators

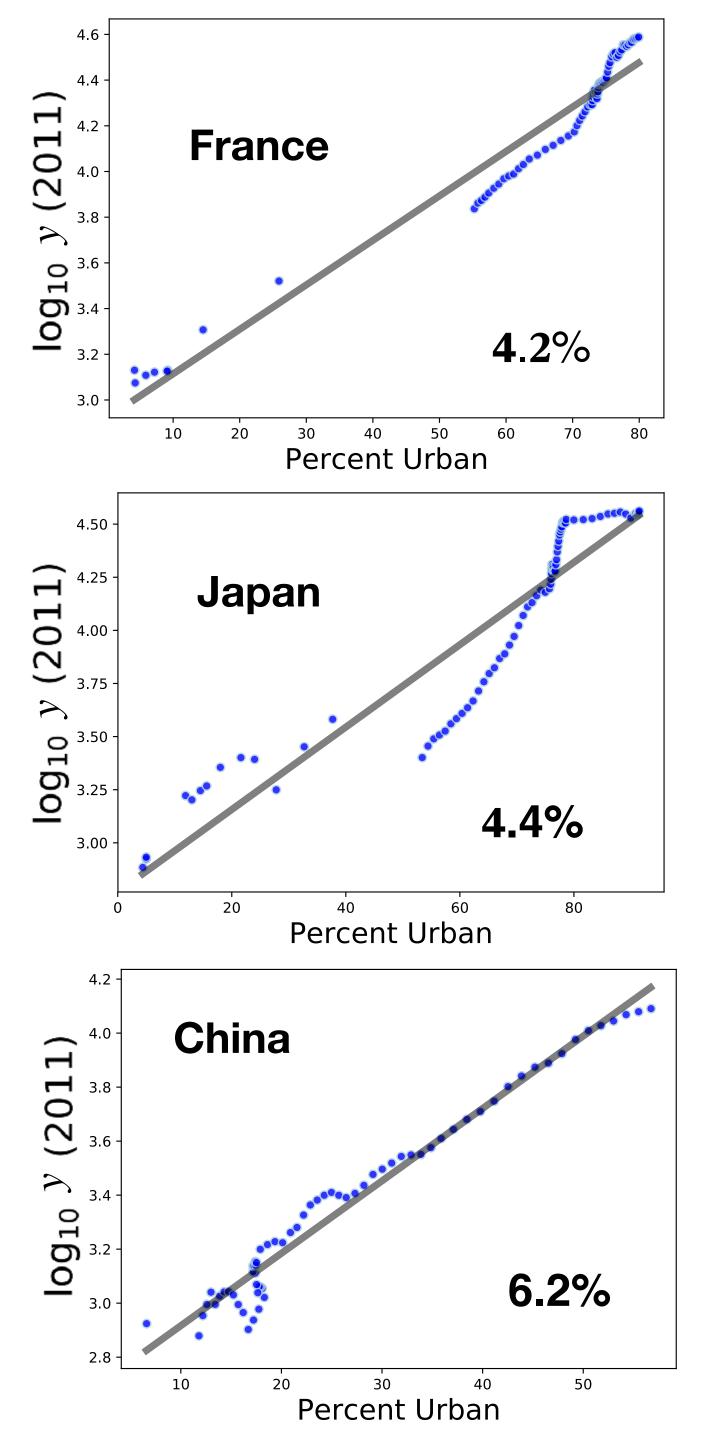
https://ourworldindata.org/grapher/urbanization-vs-gdp



similar fits to that across nations and time

# And more roughly over time in each nation





# How to get rid of time?

$$\log_{10} y = \frac{1}{\ln 10} \int_{0}^{t} dt' \frac{d}{dt'} \ln y(t')$$

$$\ln y \simeq \gamma_{y}(t - t_{0})$$

define the average growth rate of the GDP per capita, averaged over some time period:

$$\gamma_{y} = \frac{1}{t - t_{0}} \int_{t_{0}}^{t} dt' \frac{d}{dt'} \ln y(t') \qquad \longrightarrow \qquad \ln y(t) = \frac{1}{\ln 10} \log_{10} y = \gamma_{y}(t - t_{0})$$

The log of GDP/capita is the average growth rate times time.

need to express both  $\gamma_{\rm v}$  and  $t-t_0$  as functions of urbanization rate, u

Nations urbanize in the same way but at very different speeds

$$u(t) = \frac{u_M}{1 + e^{-s_U(t - t_0)}},$$

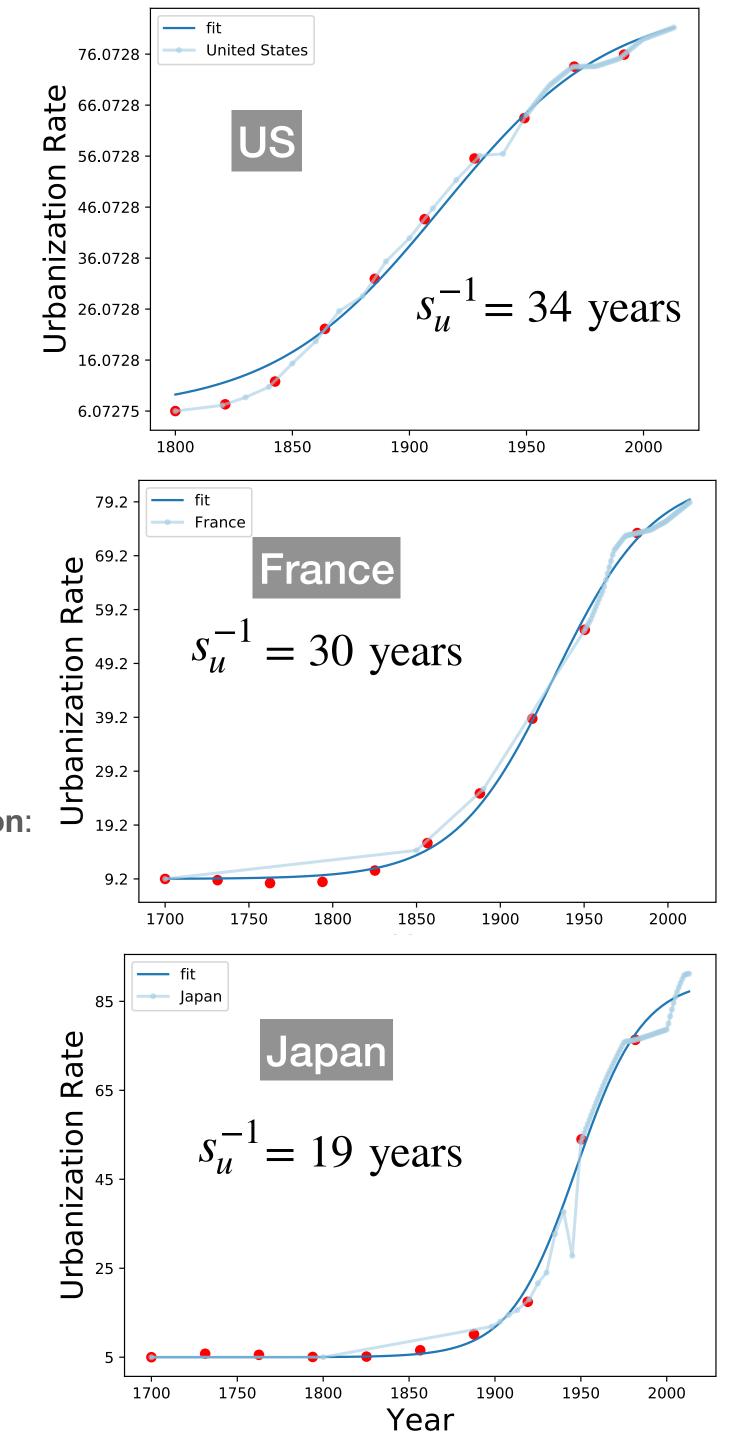
logistical growth

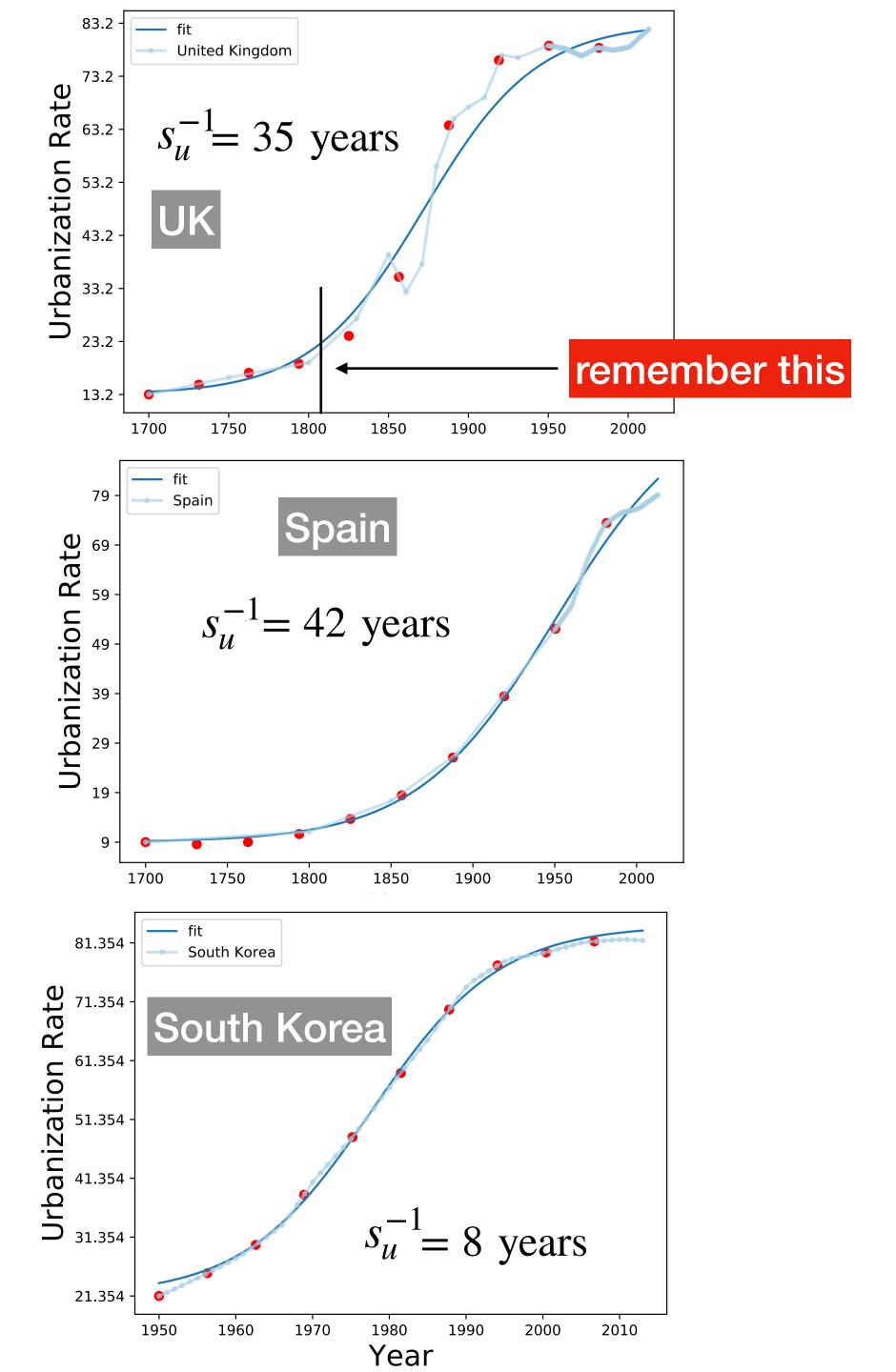
which allows us to **trade time for urbanization**:

$$t = t_0 + \frac{1}{s_U} \ln \frac{u}{u_M - u}$$

This is a very slow function of u

only speeds up near zero or the maximum





# How about $\gamma_{v}$ ?

# Two effects at play

#### selection into more urban environments

differentials in population growth and migration

### endogenous growth

local learning and innovation

divide the population between urban and rural with rates

$$n_U = u, n_R = 1 - u$$

fraction of urban population

fraction of rural population (subsistence)

$$\ln y' = \ln y(t + \Delta t) = n_U(t + \Delta t) \ln y_U(t + \Delta t) + n_R(t + \Delta t) \ln y_R(t + \Delta t) \qquad \qquad \ln y = \ln y(t) = n_U(t) \ln y_U(t) + n_R(t) \ln y_R(t)$$

$$\ln y = \ln y(t) = n_U(t) \ln y_U(t) + n_R(t) \ln y_R(t)$$

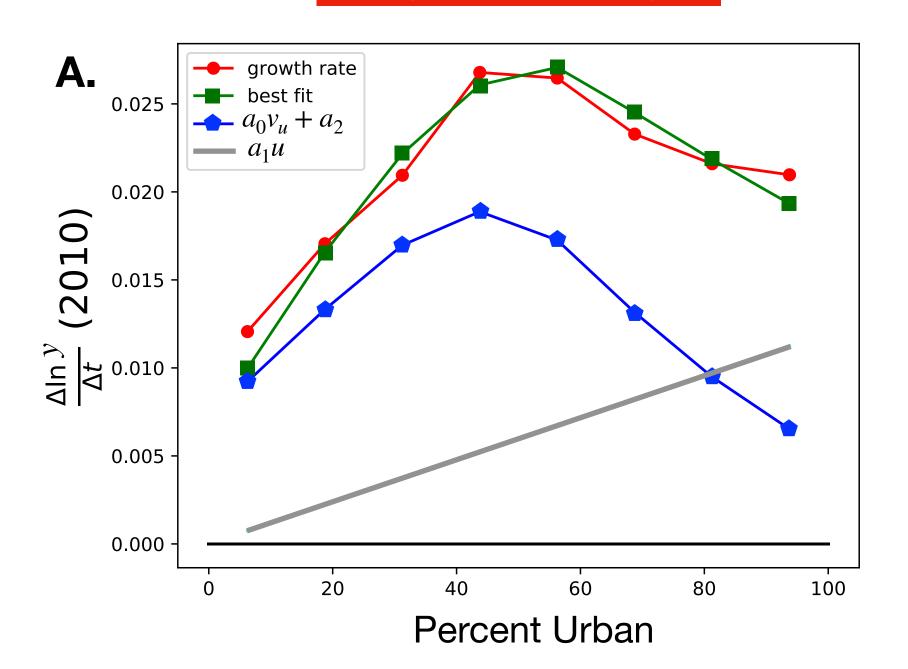
national income is an average of urban and rural

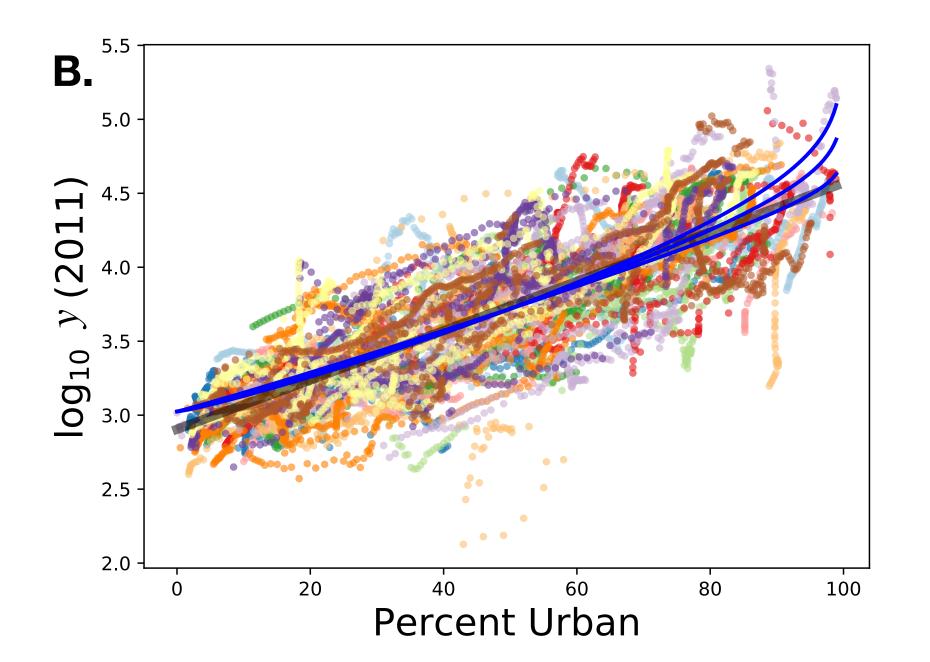
$$\gamma_{y} = \frac{\Delta \ln y}{\Delta t} = \frac{\ln y' - \ln y}{\Delta t} = \sum_{i=U,S} \frac{\Delta n_{i}}{\Delta t} \ln y_{i}(t) + n_{i}(t) \frac{\Delta \ln y_{i}}{\Delta t}$$

selection into/out of urban environments

endogenous growth in urban and rural

#### GDP growth rate per year





urbanization speed boost

$$\frac{\Delta \ln y}{\Delta t} = \frac{\Delta \ln y_S}{\Delta t} + u \left[ \frac{\Delta \ln y_U}{\Delta t} - \frac{\Delta \ln y_S}{\Delta t} \right] + \frac{\Delta u}{\Delta t} \left[ \ln y_U - \ln y_S \right].$$

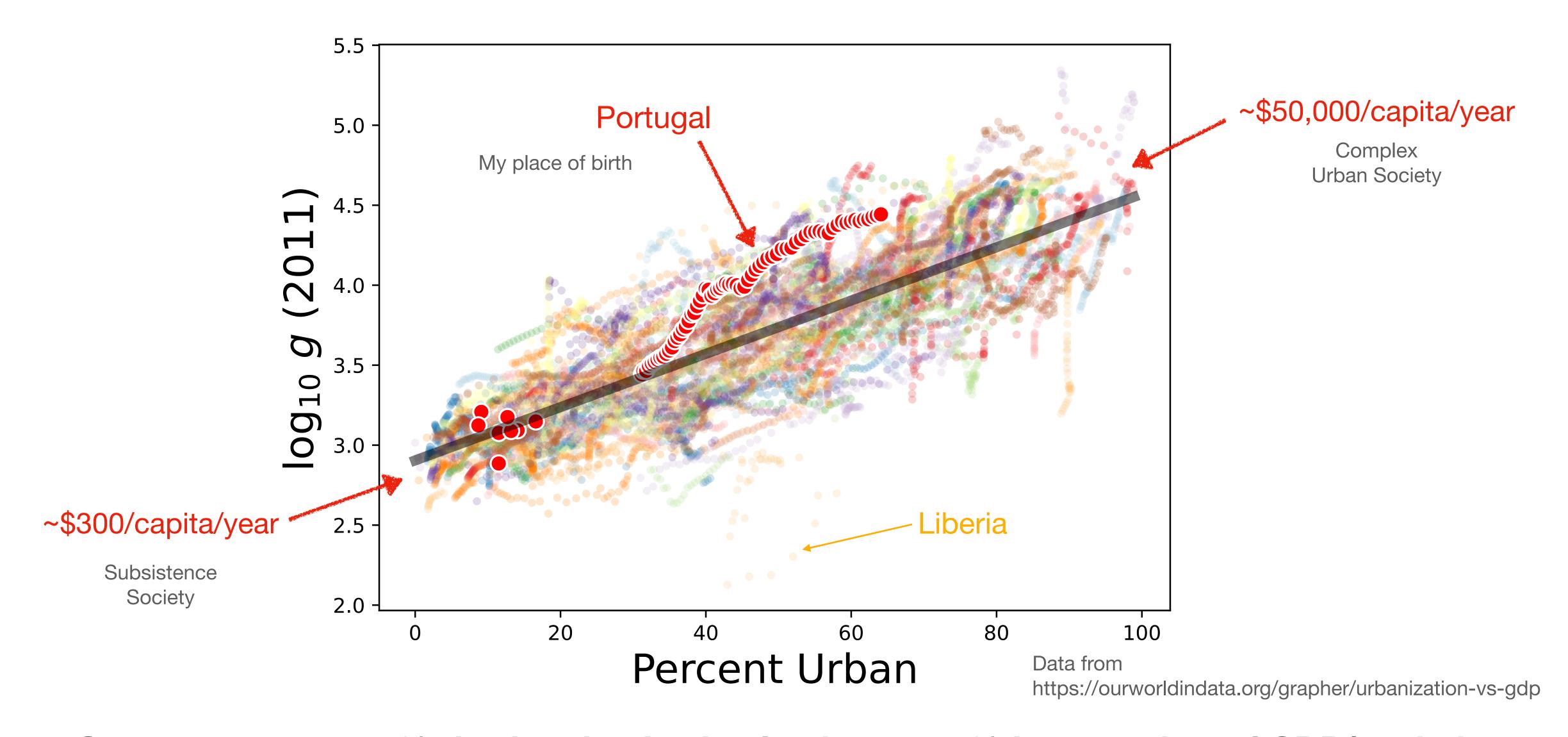
$$\frac{\Delta u}{\Delta t} = v_u$$

$$\frac{\Delta \ln y}{\Delta t}(t) = a_0 v_u(t) + a_1 \left[ u(t) + v_u(t) (t - t_0) \right] + a_2, \quad a_0 = \ln \frac{y_U(t_0)}{y_S(t_0)}, a_1 = \gamma_U - \gamma_S, \ a_2 = \gamma_S \simeq 0$$

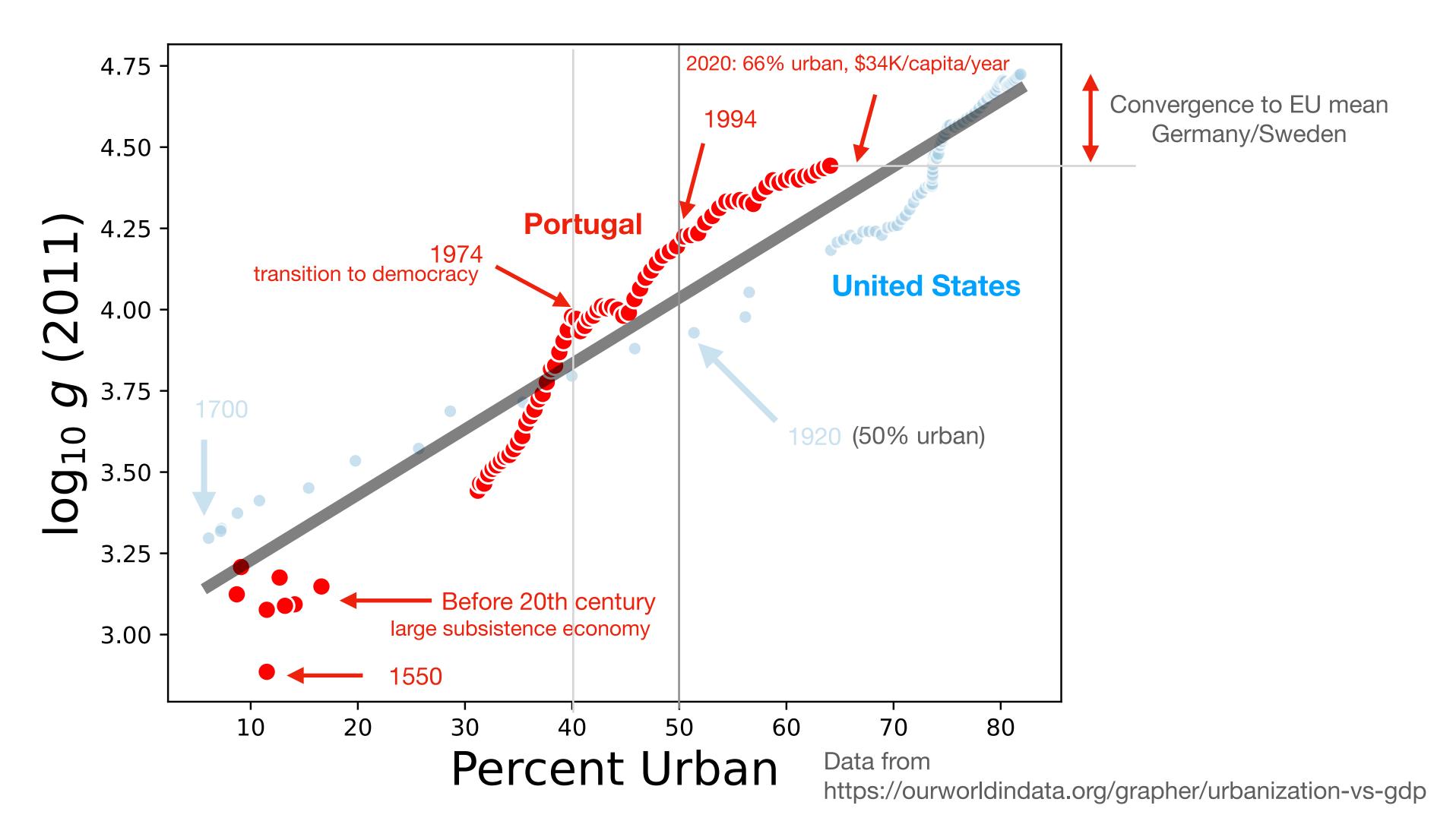
Most of the Effect is due to fast migration from rural environments to larger cities

There is a few percent GDP/capita speed up in annual growth rate around 50% urbanized

## The general connection between urbanization and development:

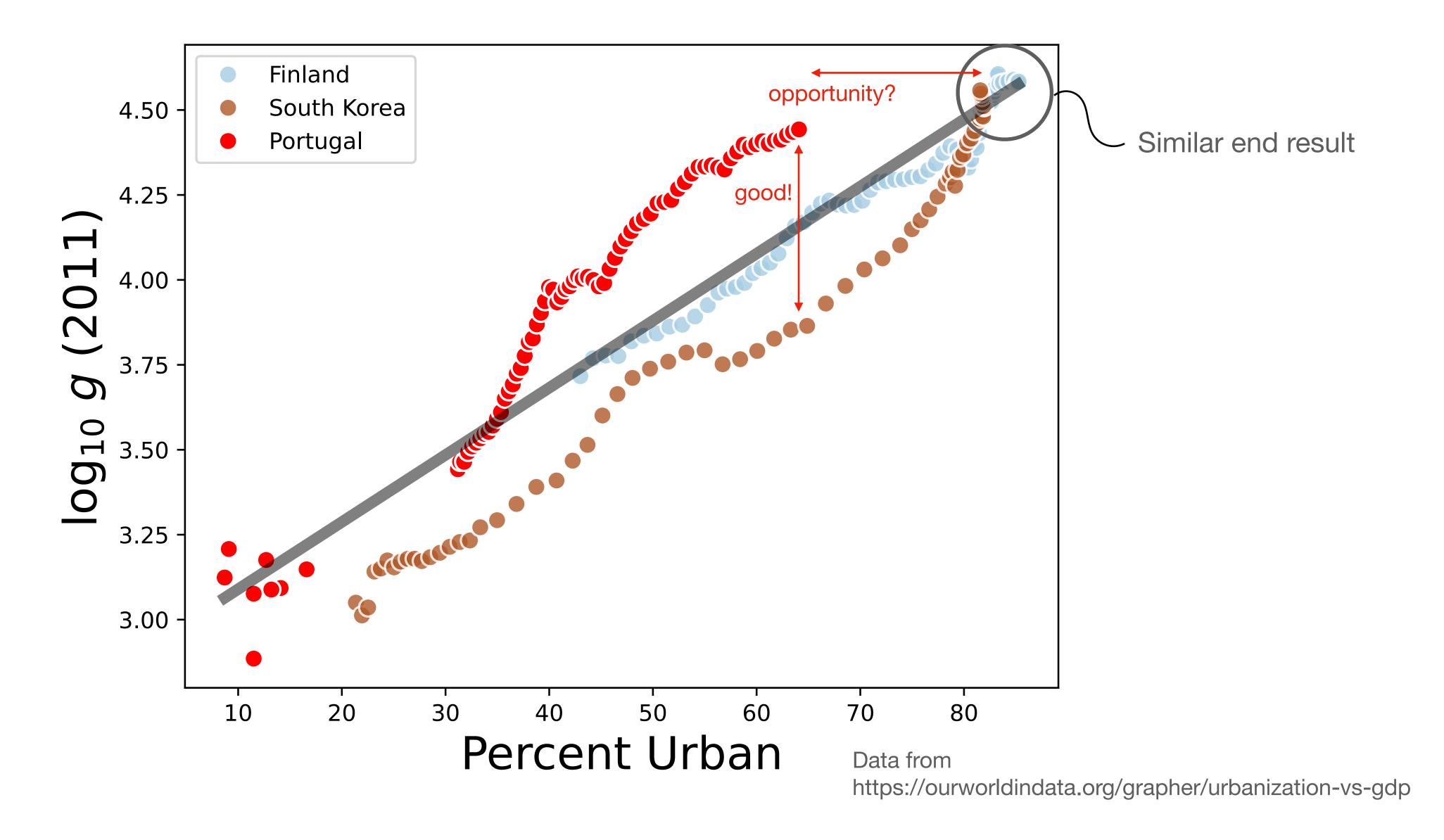


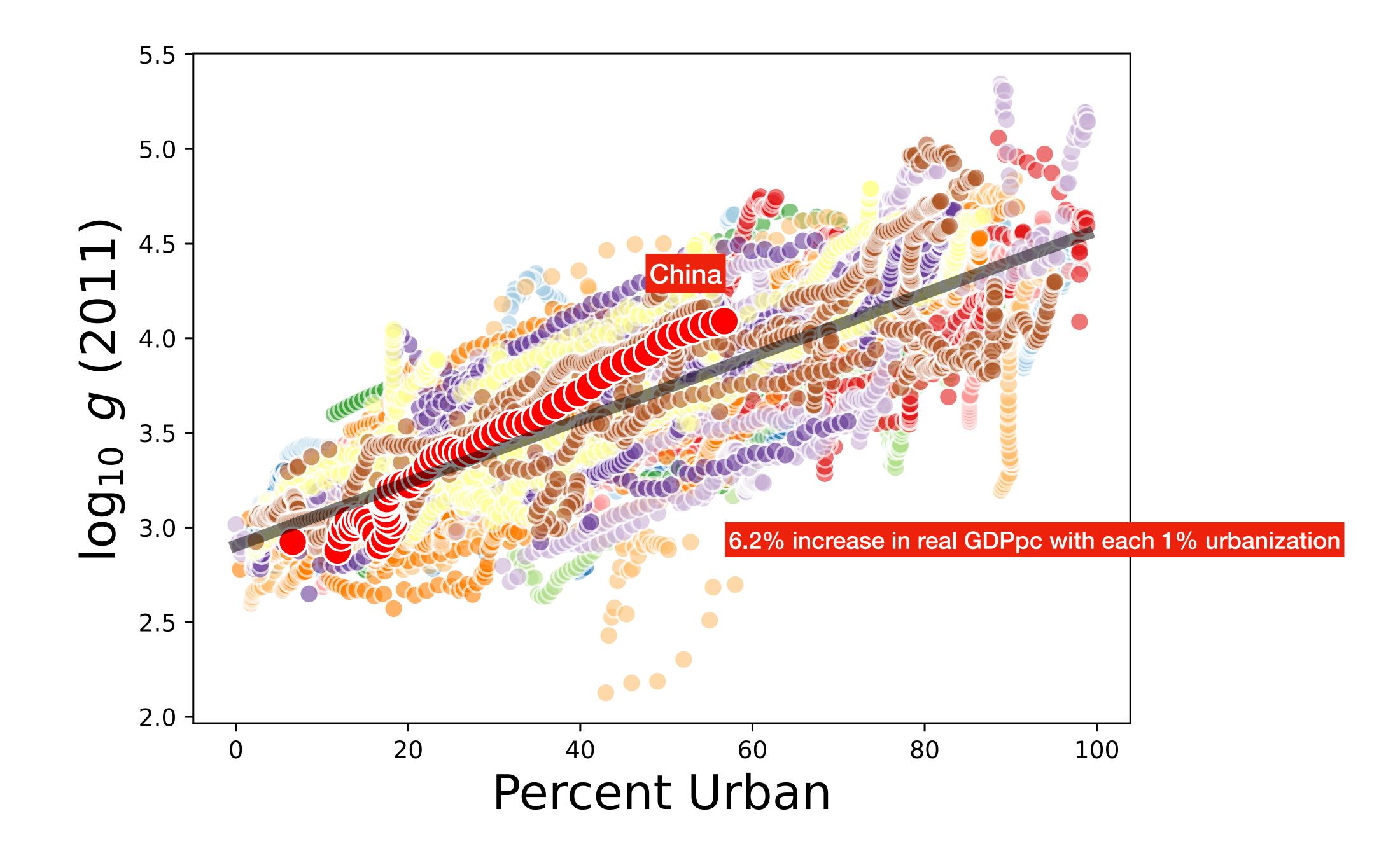
On average, every 1% rise in urbanization leads to a ~4% increase in real GDP/capita!

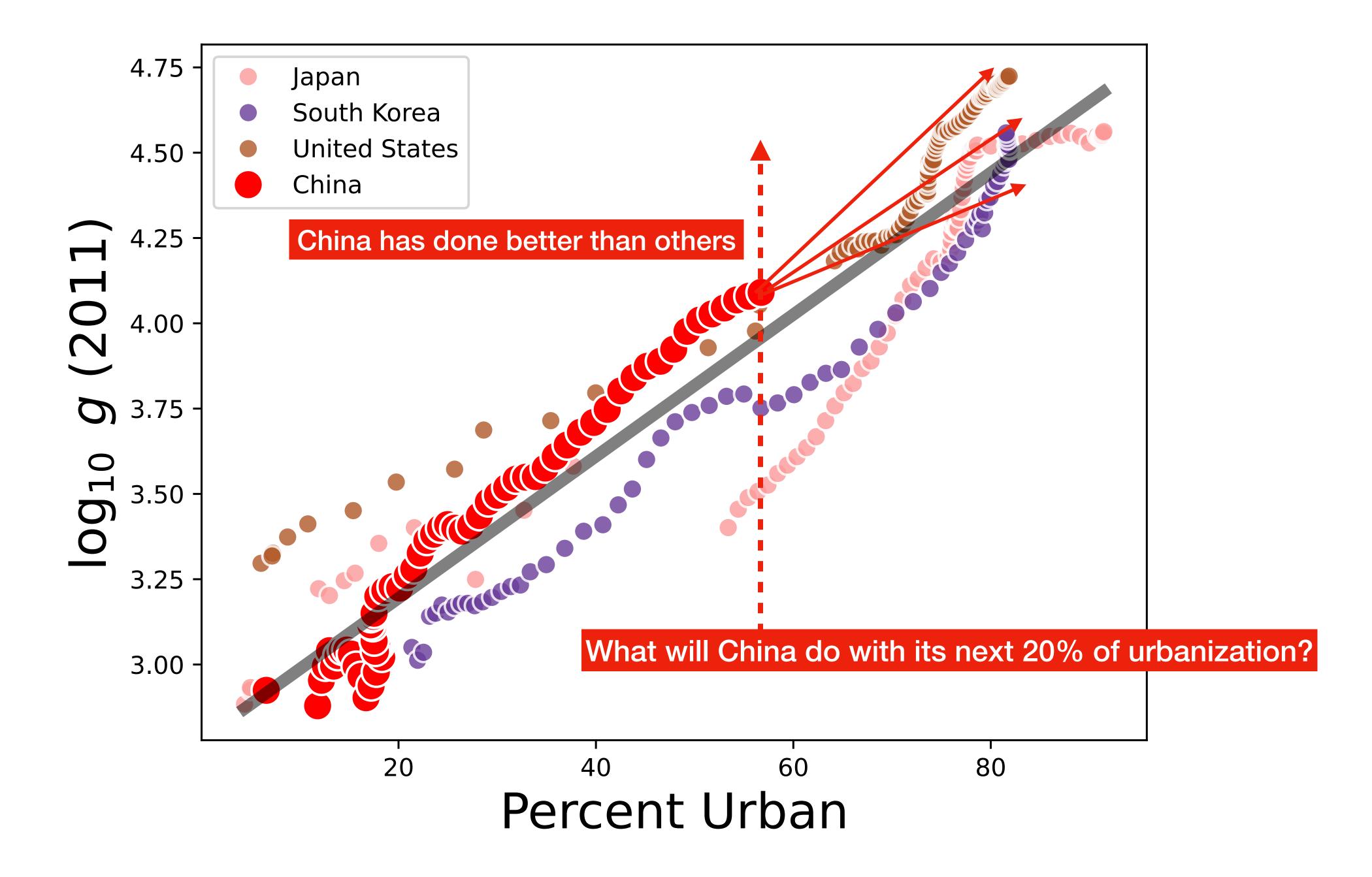


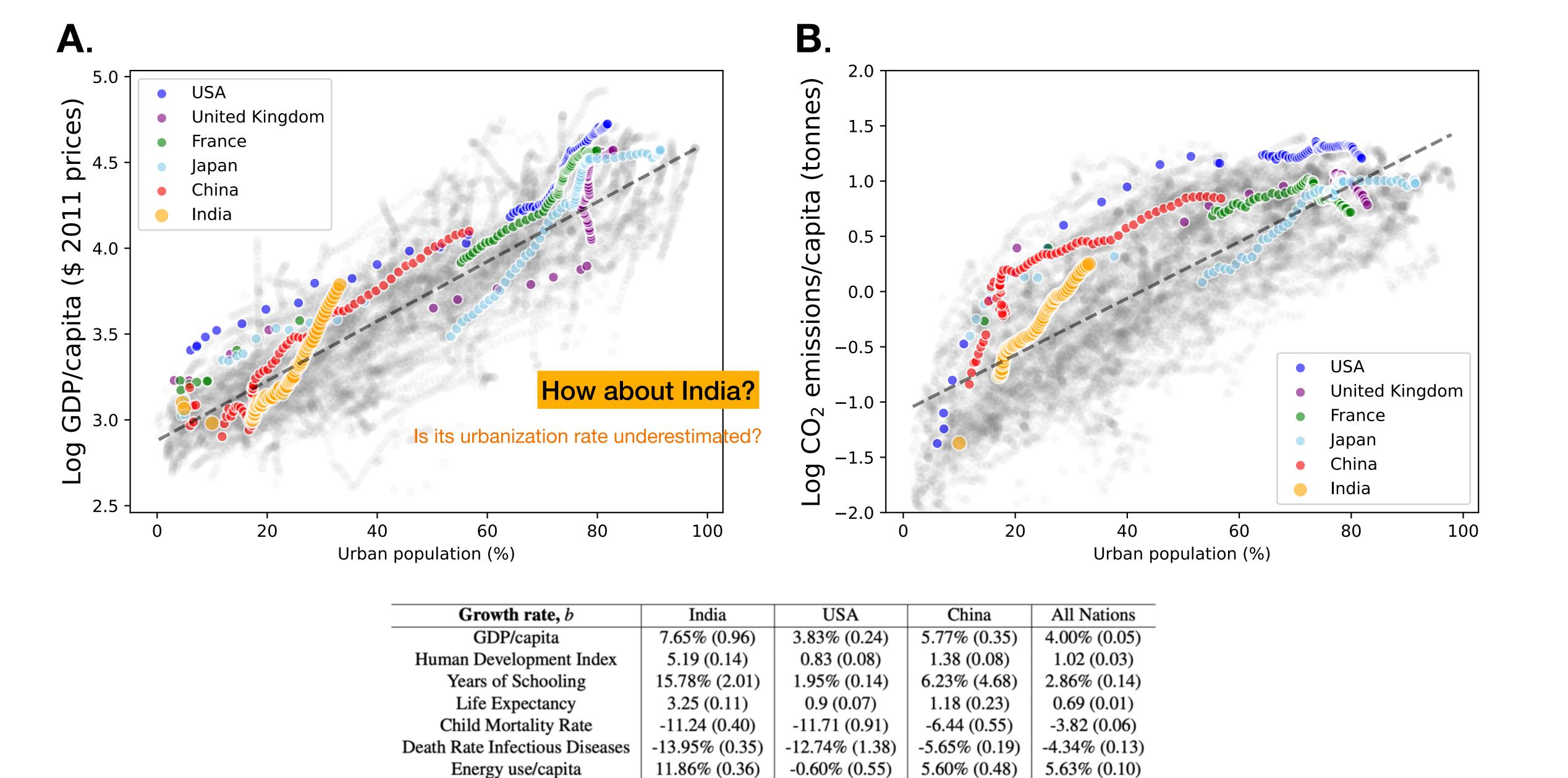
Portugal: every 1% rise in urbanization leads to a ~4.6% increase in real GDP/capita!

## Two other successful "fast urbanizers"









**Table 1.** Growth rate b of various quantities with each 1 % increase in urbanization

14.04% (0.55)

CO<sub>2</sub>/capita

0.06% (0.62)

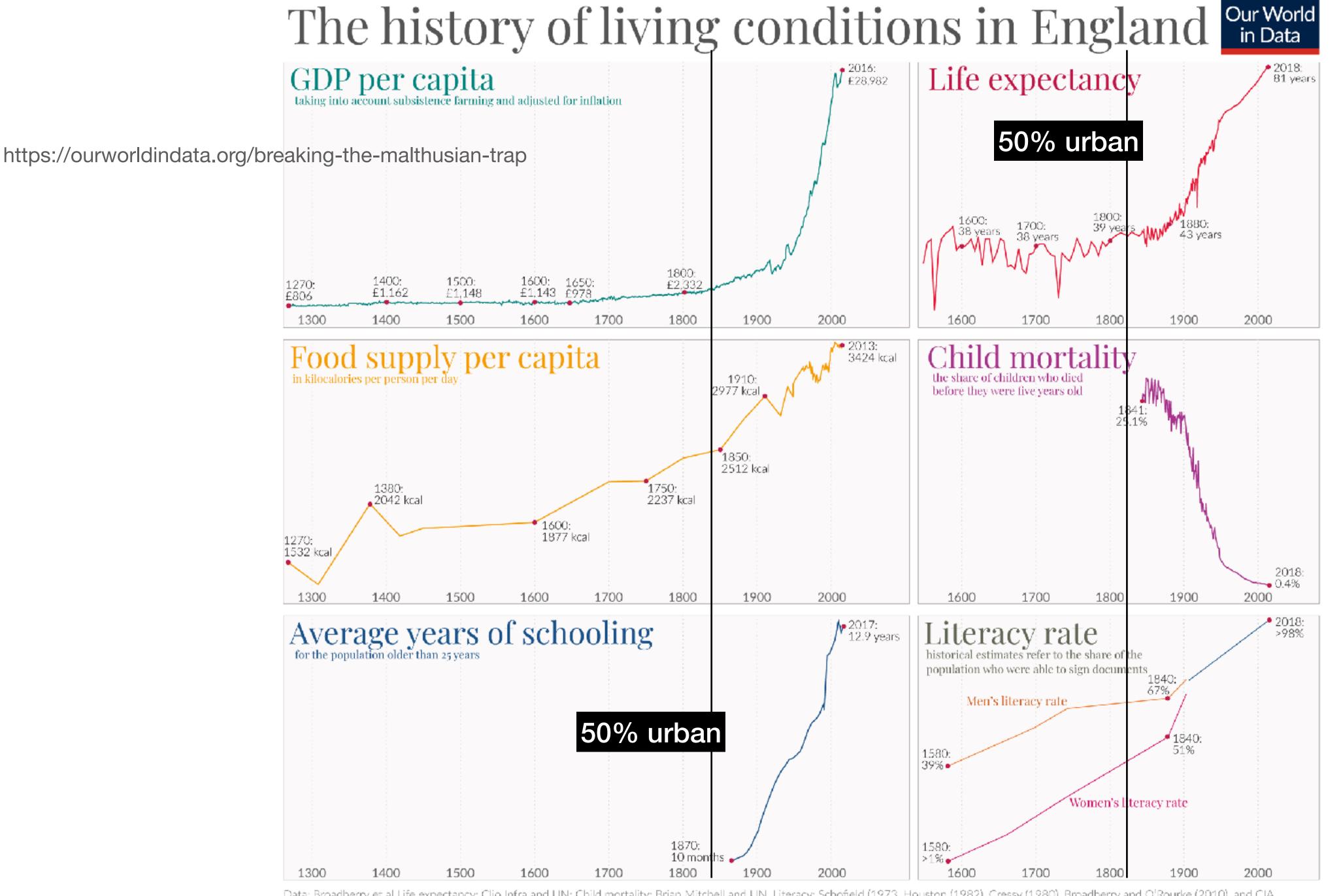
6.73% (0.84)

5.89% (0.09)

Urbanization begets its impact on economic growth per capita by taking people from

low GDP situations (rural subsistence) to high GDP situations (large cities) (structural change)

endogenous economic growth (at the "frontier") is slower

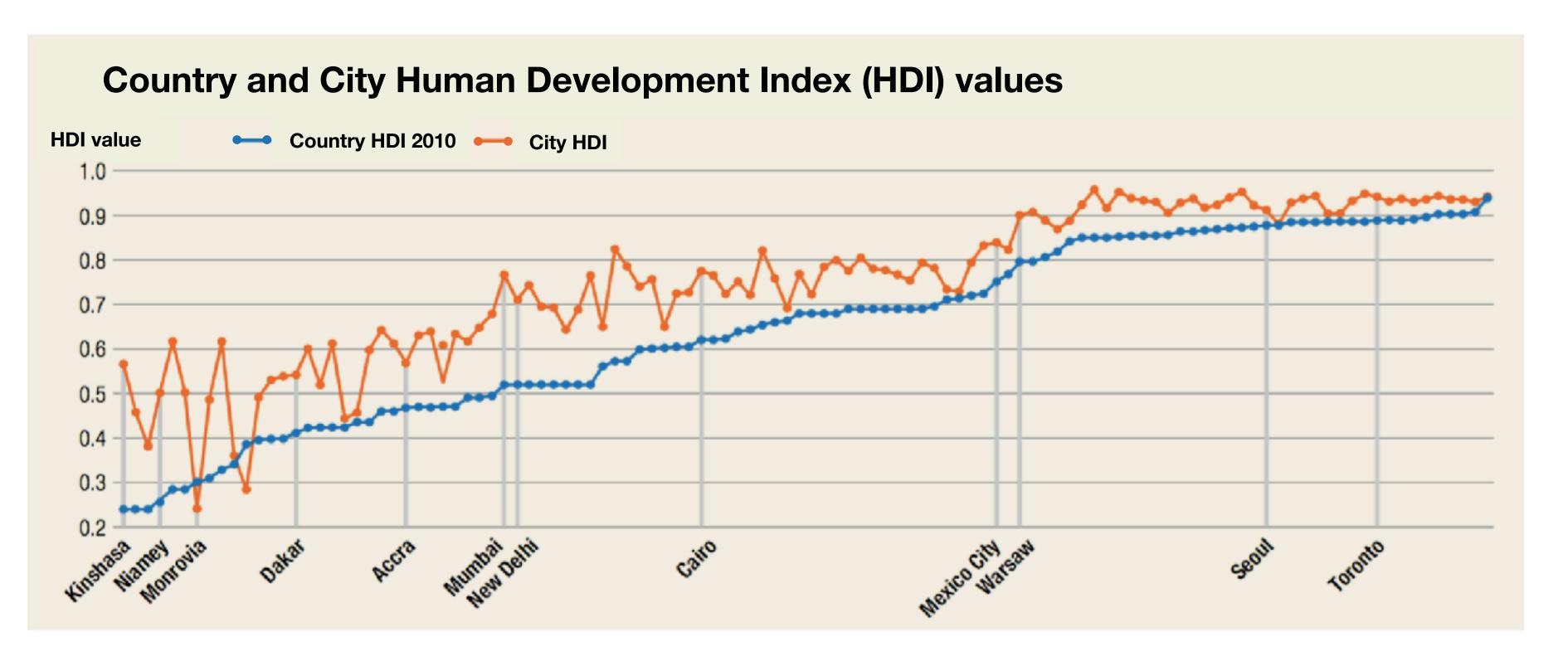


Data: Broadberry et al Life expectancy: Clio Infra and UN; Child mortality: Brian Mitchell and UN, Literacy: Schofield (1973, Houston (1982), Cressy (1980), Broadberry and O'Rourke (2010), and CIA. Food provision: Broadberry et al (2015) and UN; Lee and Lee (2016) and UNDP. All of the shown data relates to England, but some measures relate to the UK (that England is a part of) or England & Wales.

Our World in Data.org – Research and data to make progress against the world's largest problems.

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### **Broad Human Development is a Feature of Larger Cities!**



credit: UNDP Human Development Report 2013

(Led by Pedro Conceição, Director and lead author)