

- "It seems that in any realistic scenario, excluding extreme cases, LHCb would reduce the total uncertainty on the LHC average by 20-40%"
- "LHCb has a more ~~large~~ impact than a second GPD"
- Table of values to confirm (Table)

### 5) Uncertainties stemming from the $p_T^W$ modelling.

- source of theoretical uncertainty
- not discussed in paper, suggestion of further study.
- affects templates used to fit data to extract  $m_W$

### 6) Summary

- "LHCb Run II using  $W \rightarrow \mu\nu$  reduces total uncertainty on the LHC average by 20-40%" depending on the assumptions on the experimental uncertainties.
- "It remains to be demonstrated that the  $p_T^W$  model uncertainties can be controlled at the necessary level of precision"

Action: Read 2nd Mika Paper, Eur Phys J C 79, 6, 2 2019  
 → Detailed analysis of PDFs

(Also revise error calculation / correlation) ✓

05/10/20

### Error Revision - Tommasi Book p. Chpt 6 & 7

(aj)

Standard error in a parameter, in terms of CURVATURE of the error surface

$$\downarrow x^2 \quad x_j = \sqrt{\frac{2}{\left(\frac{\partial^2 x^2}{\partial a_j^2}\right)}}$$

(AKA hyper-surface)

$$x^2 = \sum_i \left( \frac{(y_i - y(x_i))^2}{\sigma_i^2} \right)$$

$y(x_i)$  = theoretical model  
 $y_i$  = data    $\sigma_i$  = error bars.

→ Develop matrix methodology for describing the variation of the  $x^2$  surface (around minimum value  $x_{\min}^2$ ) & determining the uncertainties of fit parameters.

"Fit our  $N$  data points  $(x_i, y_i)$  w/ uncertainties  $\alpha_i$  to a nonlinear function w/  $N$  parameters  $f(x; \alpha_1, \alpha_2, \dots, \alpha_N)$ "

- The uncertainty of a parameter  $\alpha_j$  is defined as the extreme of the  $\chi^2_{\text{min}+1}$  contour along the  $\alpha_j$ -axis.
- When the parameter moves away from its optimal value by  $\Delta \alpha = \alpha_j - \bar{\alpha}_j = \alpha_j$ ,  $\chi^2$  evolves to  $\chi^2_{\text{min}+1}$

$\Rightarrow$  CURVATURE MATRIX  $A$

$N \times N$  matrix w/ components  $A_{jk} = \frac{1}{2} \frac{\partial \chi^2}{\partial \alpha_j \partial \alpha_k}$

$$\left( \frac{1}{2} \text{Hessian Matrix}, H_s = H(\alpha_s) = \begin{bmatrix} \frac{\partial^2 \chi^2}{\partial \alpha_1^2} & \dots & \frac{\partial^2 \chi^2}{\partial \alpha_1 \partial \alpha_N} \\ \vdots & \ddots & \vdots \\ \frac{\partial^2 \chi^2}{\partial \alpha_N \partial \alpha_1} & \dots & \frac{\partial^2 \chi^2}{\partial \alpha_N^2} \end{bmatrix} \right)$$

Off angle terms = degree of correlation of uncertainties in parameters

COVARIANCE or ERROR MATRIX  $C$   $[C] = [A]^{-1}$

$$\Rightarrow \alpha_j = \sqrt{C_{jj}} \quad \text{if uncorrelated \& off diagonal = 0}$$

(independent terms)

$C_{jk}$  = correlation coefficients (can be -ve whilst  $C_{jj}$  must be +ve)

Illustration of covariance of 2 variables

$Z = f(A, B)$ ,  $N$  pairs of measurements  $(A_i, B_i)$   
 $\rightarrow$  mean  $\bar{A}$  & standard deviation  $\sigma_A$  etc

$$Z_i = f(A_i, B_i) \approx f(\bar{A}, \bar{B}) + (A_i - \bar{A}) \frac{\partial Z}{\partial A} + (B_i - \bar{B}) \frac{\partial Z}{\partial B}$$

$$\bar{Z} = f(\bar{A}, \bar{B})$$

$$\sigma_Z^2 = \frac{1}{N-1} \sum_{i=1}^N (Z_i - \bar{Z})^2 = \frac{1}{N-1} \sum_{i=1}^N \left( \frac{\partial Z}{\partial A} (A_i - \bar{A}) + \frac{\partial Z}{\partial B} (B_i - \bar{B}) \right)^2$$

$\hookrightarrow N-1$  due to one fewer degree of freedom, as mean is calculated from the data.

$$\Rightarrow \sigma_z^2 = \left( \frac{\partial z}{\partial A} \right)^2 \sigma_A^2 + \left( \frac{\partial z}{\partial B} \right)^2 \sigma_B^2 + 2 \frac{\partial z}{\partial A} \frac{\partial z}{\partial B} \sigma_{AB}$$

$$\sigma_{AB} = \frac{1}{N-1} \sum_{i=1}^N (A_i - \bar{A})(B_i - \bar{B}) \quad \text{COVARIANCE}$$

=  $\rho_{AB}$  measure of correlated variable.

- Variance & covariance do not necessarily have same unit.

**CORRELATION MATRIX** ( $N \times N$ )  $\rightarrow$  dimensionless measure of correlation,  
diagonal elements = 1, off diagonal  $\rho_{AB}$

$$\rho_{AB} = \frac{\sigma_{AB}}{\sigma_A \sigma_B} = \frac{C_{AB}}{\sqrt{C_{AA} C_{BB}}} \quad \text{CORRELATION COEFFICIENT}$$

$-1 \leq \rho_{AB} \leq 1$   $1 = \text{strong tve}, -1 = \text{strong -ve}, 0 = \text{unrelated}$

[Look up table TPAHuge pg 95 for correlated  $Z = A \pm B, A \times B, A/B$ ]

[Eqs 7.23-25 pg 93 = curvature matrix for straight line fit]

### Eur. Phy. J. C (2019) 79:497

Understanding and constraining the PDF uncertainties in a W boson mass measurement with forward muons at the LHC

- $M_W$  predicted with higher precision than measured  $\Rightarrow$  new physics beyond SM
- $M_W = 80354 \pm 7 \text{ MeV}/c^2$   
prediction by gFit collaboration 2018
- Measurements of  $M_W$  @ Hadron colliders made by comparing data to templates of
  - charged lepton transverse momentum
  - missing transverse energy
  - transverse mass
 in  $W \rightarrow l \nu_l$  decays.
- $p\bar{p}$  collider (tevatron)  $\Rightarrow W$  from annihilation of valence quarks & anti- $q$ .
- $p\bar{p}$  collider (LHC)  $\Rightarrow$  gluons & sea quarks play a critical role.

⇒ LHC measurements more susceptible to theoretical uncertainties in the modelling of  $W$  production, particularly in PDFs  
e.g. ATLAS  $M_W = 80370 \pm 13 \pm 14$  MeV/c<sup>2</sup>  
theoretical, PDF dominant.

LHCb is a single-arm spectrometer w/ full charged particle tracking & identification capabilities over the range  $2 < |\eta| < 5$ , which is mostly orthogonal to the acceptance of ATLAS & CMS

$$\begin{aligned} pp \rightarrow W^+ \rightarrow \mu^+ \nu + X \\ pp \rightarrow W^- \rightarrow \mu^- \bar{\nu} + X \end{aligned} \quad \left. \begin{array}{l} \text{decay process to observe} \\ \text{}} \end{array} \right\}$$

- LHCb Run II →  $\sim 6 \text{ fb}^{-1}$  of pp collisions @  $\sqrt{s} = 13 \text{ TeV}$
- Run I →  $3 \text{ fb}^{-1}$  @ lower  $\sqrt{s}$
- Estimates  $M_W$  statistical uncertainty  $\sim 10 \text{ MeV/c}^2$
- Papers given for measurement of forward  $W$  &  $Z$  boson production & future ATLAS measurement prospects

## 2) Simulation of $W$ production

- $10^8$  Monte Carlo events  $pp \rightarrow W \rightarrow \mu\nu + X$   $\sqrt{s} = 13 \text{ TeV}$
- Events are selected  $80 < p_T^M < 50 \text{ GeV/c}$   $2 < |m| < 4.5$  → 10% of event sample

- The invariant mass,  $m$ , of  $W$  decay products is assumed to follow a relativistic Breit-Wigner distribution:

$$\frac{d\sigma}{dm} \propto \frac{m^2}{(m^2 - M_W^2)^2 + m^4 \Gamma_W^2 / M_W^2}$$

$M_W$ ;  $\Gamma_W$  = mass & width of  $W$  boson.

## 3) Fitting Method

## 4) Understanding the PDF uncertainties NNPDF3.1

Figure showing contribution of different partonic subprocesses to the cross-section for  $W$  production as a func of rapidity ( $y$ ).

- Dominant valence u(d) quarks ( $u\bar{u}$  &  $d\bar{d}$ ) ( $g_u, g_d$ )
- Annihilation of sea quarks & gluons  $g g \rightarrow \text{sea}$   $\sim 20\%$

- PDF uncertainty on  $M_W$  measurement arises as the  $p_T^W$  distribution depends on the  $W$  production kinematics, which are characterised by transverse momentum  $p_T^W$ , rapidity, & polarisation.
- Use "distribution of the angle  $\Theta^*$  in the Collins-Soper frame" as a proxy for polarisation
- Biases in  $M_W$  (from replica sets) that bias weight: Replicas (from sets) that bias  $M_W$  upwards (downwards) tend to predict large (smaller)  $\langle y \rangle$  values & smaller (larger)  $\langle p_T^W \rangle$ . Opposite for  $w^-$ .
- Replicas that bias  $M_W$  upwards (downwards) correspond to  $\frac{w^+}{w^-}$  & decrease (increase) in predicted cross-section at high  $p_T^W$  & high  $M_W$

Figures 7 & 8 illustrative of how above statement can be used to constrain PDF uncertainty.

## 5) PDF uncertainty reduction

"Each replica is assigned a weight according to the best-fit  $\chi^2$  ( $\chi^2_{\min}$ ) for a fit with  $n$  degrees of freedom (n):

$$P(\chi^2_{\min}) \propto \chi^2_{\min}^{(n-1)} e^{-\frac{1}{2}\chi^2_{\min}}$$

This has the effect of disregarding replicas that are incompatible with the data."

- Weights reduced widths of  $\chi^2$  vs  $M_W$  distribution to factor of 3x smaller ( $w^+$ ) & factor of 2 ( $w^-$ )
- effective # replicas after reweighting  $N_{\text{eff}} = 113$  (105)  $w^+$  ( $w^-$ ) where initial  $N = 1000$ .

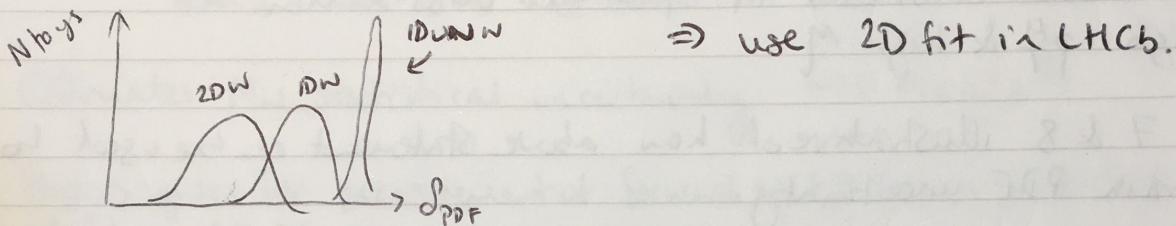
"For a single toy dataset the PDF uncertainty is defined by the RMS of the  $M_W$  values for the 1000 replicas"

- 1D weighting case ( $p_T^M$ ) reduces PDF uncertainty by an average factor of  $10(20)\%$
- 2D weighting ( $p_T^M, \eta$ ) reduces PDF uncertainty by a factor of roughly  $\sim 2(1.5)$

However data fluctuation both fits give a large spread under data fluctuation.

1D unweighted	$0.04(0.07) \text{ MeV}/c^2$
1D weighted	$0.8(1.2) \text{ MeV}/c^2$
2D weighted	$0.9(1.2) \text{ MeV}/c^2$

→ Since PDF replica weighting scheme depends on the data, PDF uncertainty becomes much more sensitive to the statistical fluctuations at the data themselves.



### 5.1) Simultaneous fit of $W^+$ and $W^-$ samples

→ partial cancellation of PDF uncertainty when  $W^+$  &  $W^-$  data combined.

2D weighting has a "large constraining power of the data"

I've assumed that we want  $N_{\text{eff}}$  as small as possible but I'm not sure of this → check.

Ensure understand bias, toy data & replicas. Bins.

### 5.2) Dependence on detector acceptance

→ discussion of the effects of acceptance range of  $p_T^M$  &  $\eta$  on stat uncertainty as range affects statistical uncertainty on  $M_W$

→ although a smaller range may  $\downarrow$  PDF  $\delta$ , may  $\uparrow$  statistical  $\delta$

(CONCLUSION) "With large enough data samples, a 2D fit to the  $p_T^M$  vs  $\eta$  distribution, w/ PDF replica weighting, would allow the PDF uncertainty to be further refined." Factor of 2 improvement for  $W^+$  &  $W^-$  simultaneous data using LHCb Run 2 statistics.

- Research staff, 1<sup>st</sup> MPhys group.  
→ LHCb 10 years
- Run programs outside of the course → probably prefers C++
- Collider - intensive work in C
  - mostly in Python → more efficient for fast bits.
- Start on some initial task, then divide later on to different parts of the project.
- GitHub - share code
  - Miha & Rasmus can discuss.
  - suggestions to use to for electronic record
  - similar to use for actual research
- Set up GitHub account.
- SCRTP username phukjd
- ssh via putty → ssh -X -Y phukjd@godzilla.cse.warwick.ac.uk
  - ↳ method for accessing warwick servers
- Putty for other PC
- Gitlab
- GitHub → copy code for git clone
  - LS MPhys Project 2021 /
  - cd MPhys

emacs -nw is a code editor  
IDE - powerful but more complicated code editor

(Screen shots of command) → python

Tree data - data has collisional events.

- "DATADIR = " location  
Read in code  
Produces histogram.
- "gs plot; pdf" to view plot
- Sample of collision events with one high momentum muon  
Code plots ~~more~~ my distribution  
Bump = 100 GeV boson  $\rightarrow$  at half of 136 GeV M\_W  
Rate vs mom in GeV
- ls Makefile to compile C code , screenshot 3.

git clone git@github.com:mvesteri/MPhysProject2021.git

Data access

commands in chat

ls /storage/ep2/phsogg/MPhysProject2021/  
→ opens data

- Use Mika GitHub , create own fork

## Weekly Meetings

Thursdays 1200

Discuss over GitHub repository  
→ no immediate response in evenings or weekend.

- Office work Risk Assessment
- Ask how to get started on GitHub when all set up.  
, how to send message explaining git & ssh.

## Px 402 Intro Meeting

[www.warwick.ac.uk/finalists/briefing](http://www.warwick.ac.uk/finalists/briefing)

→ sci comp facilities.

→ postgrad & careers.

→ health safety & risk assessment

- David Leadley
- set of live session timetables on UG handbook
  - right of start page
  - can access module pages on handbook.
  - ONLINE OPEN BOOK EXAMS
  - Welcome back :)

SSLC - Aggie Martin, Emily Detke, Grady Beckett, Shameem Golestaneh

Robin Ball - r.c.ball@warwick.ac.uk

## Project Talk

- GET IN TOUCH WITH SUPERVISOR
- Late penalties are 5% per working day.
- Record of work - day-by-day working record
  - NOT a beautified document.
  - keep up to date AND DATED.
  - individual record, but try to cross reference other electronic records
  - BACK UPS
  - suggestion of OneNote, but discuss w/ supervisor
  - ready to share w/ supervisor @ or before meetings.
- Supervisor - regular scheduled weekly progress meetings
  - email supervisor for missed work ASAP (fmu)
  - expect inspection of work done every 2-3 weeks (min 3/term)
- Rooms available to book on Moodle for meetings.
- Interim Report - Intro - aims, lit review & background, objectives
  - T1 achievements 2pg max
  - realistic T2 work plan 1pg max
  - 10 pgs + references

- If using ionizing radiation, contact Jon Duffy.
- Plagiarism example given on powerpoint.
- Contact Robin Ball for mitigation of late work & questions

### John Horstle H&S Presentation

- Review of Risk assessment T2 Thurs W2 → 21/10/121
- Need to complete some tabs, given on doc.

### SCRTP David Quigley

- warwick.ac.uk / scrt
  - Linux system, shared computing space. → CentOS
  - Can be used remotely
  - Distributed computing infrastructure (the CoW)
  - Do not use without EXPLICIT permission from supervisors
  - Centrally stored files & settings
- [
- READ KEY INFO PDF
  - ✗ Apply for desktop account
  - ✗ Read acceptable use policy
    - Sign up for scrt-linux-use email list
- ]
- Remote Desktop Protocol, web browser, or X2Go software.
  - godzilla.csc.warwick.ac.uk
    - DO NOT RUN COMPUTATION
    - editing files, compiling code, plotting simple graphs, submitting computational jobs to the CoW ONLY
  - Access example avocado.csc.warwick.ac.uk in web browser
  - Access programs by command line
    - (~12min in video)
    - module spider ProgramName
    - module load

SCRT USERNAME phukjd

Standard maintenance Wednesday 13:00 - 17:00