

Branch → edit by adding "commits" → pull request to discuss commits & review,
 → deploy from branch to test → merge w/ main

Distributed version control system → see all edits & changes
 → view history
 → split by user

commits = file history, edits.

Git commands → git clone = create a local copy of an existing project.

WHERE TO START?

- ✗ Analyse example code & make notes
- ✗ Data format → root files

Measure W & Z production cross sections

- These constrain PDFs
- PDF - how likely is it to find an up quark w/ a particular momentum fraction when you probe the proton at a particular energy scale

Data set never looked at → low energy run @ $\sqrt{s} = 5 \text{ TeV}$

→ unique sensitivity to proton structure at large momentum fractions

- Split between as
 - measurement of x-sections
 - calculation of the "hypothesis"
 - theory predictions of x-sections

Next step: Search for Z boson in the dataset

to笨拙wise w/ helper functions for 4-momentum vectors

- Method on comment, one do python, one C

15/10/2020

MIKA MEETING

- Initial set up on top level read me (ESSENTIAL)
ALWAYS:
module use /nwmsch/epc/modules
module load lhuxben
- ROOT is CERN project
ROOT trees are the data format
∴ use to extract data & can create histograms.
- Issues 2 & 3 → ROOT TBrowser
→ pythnic event loop in ROOT
- Rule of thumb python x100 slower than C by TTree is a lot faster
- Going through TTree & TBranches
root [0] → can type C into this
→ use hlt to inspect file
quicker if add "root -l /\$tar"
See says "attaching files -fileθ"
- fileθ → ls()
Better: go directory → ls() lists files

written up
better in
project notes
doc.

pdf for report

INARIANT MASS CALCULATION

$$Z \rightarrow \mu^+ \mu^-$$

- "In the labframe, the charged particle has 3 degrees of freedom" - Miller
- Cartesian, p_x, p_y, p_z
 - Cylindrical (Spherical) $\rightarrow p_T$ transverse momentum (MeV)
 - $\rightarrow \eta$ pseudo rapidity (polar angle)
 - $\rightarrow \phi$ azimuthal angle.
- see
diagrams
overleaf

Use muon mass $M = 0.105 \text{ GeV}$

Particles are relativistic $\Rightarrow 4$ momentum

(I'm assuming natural units)

Standard Model notes, L4

$$p^M = k_R(E, \gamma) \quad p \cdot p = p^M p_M = E^2 - |\vec{p}|^2 = m^2$$

$$M^2 = \left(\sum_i^N E_i\right)^2 - \left(\sum_i^N p_i\right)^2 \text{ for } N \text{ particle system}$$

↳ invariant mass of system

$$\vec{p}_Z^\alpha = \vec{p}_{\mu^+}^\alpha + \vec{p}_{\mu^-}^\alpha$$

$$\begin{aligned} M^2 &= \left(p_{\mu^+} + p_{\mu^-}\right)^2 = \frac{\left(p_{\mu^+} + p_{\mu^-}\right)^\alpha \cdot \left(p_{\mu^+} + p_{\mu^-}\right)_\alpha}{\alpha} \\ &= p_{\mu^+} p_{\mu^+}^\alpha + p_{\mu^-} p_{\mu^-}^\alpha + 2 p_{\mu^+} \cdot p_{\mu^-} \\ &= m_{\mu^+}^2 + m_{\mu^-}^2 + 2(E_{\mu^+} E_{\mu^-} - p_{\mu^+} p_{\mu^-}) \end{aligned}$$

$$m_{\mu^+} = m_{\mu^-} = 0.105 \text{ GeV}$$

$$\Rightarrow M^2 = 2m_\mu^2 + 2E_\mu E_\mu - 2\vec{p}_\mu \cdot \vec{p}_\mu$$

Spherical polars \rightarrow cartesian

$$\begin{aligned}x &= r \sin \theta \cos \varphi \\y &= r \sin \theta \sin \varphi \\z &= r \cos \theta\end{aligned}$$

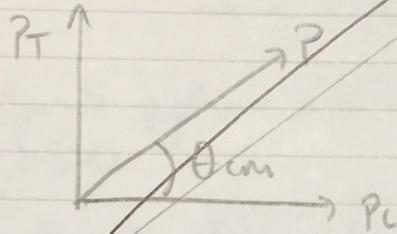
where $r = p_{cm}$
 $\theta = \Theta_{cm}$
 $\varphi = \phi$

$$\eta = -\ln \left[\tan \left(\frac{\theta}{2} \right) \right] \quad \theta = 2 \arctan(e^{-\eta})$$

$$z = r \cos [2 \arctan(e^{-\eta})]$$

$$\cos 2\theta = \frac{1 - \tan^2 \theta}{1 + \tan^2 \theta} \Rightarrow \frac{1 - e^{-2\eta}}{1 + e^{-2\eta}} = \frac{e^{2\eta} - e^{-2\eta}}{e^{2\eta} + e^{-2\eta}} = \tanh(\eta)$$

$$\Rightarrow z = p_{cm} \tanh(\eta)$$



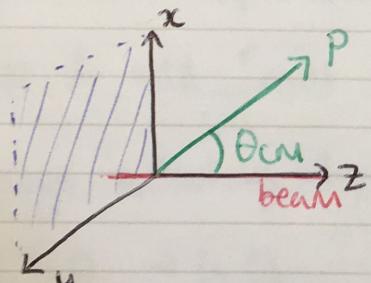
$$p = p_T \sin \theta_{cm}$$

$$p = p_T \sin [\arctan(e^{-\eta})]$$

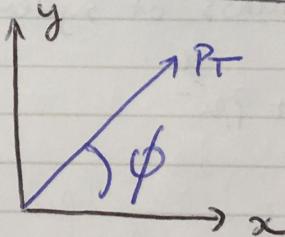
$$p = p_T \frac{2e^{-\eta}}{1 - e^{-2\eta}} = \text{csch}(\eta) = \frac{1}{\sinh(\eta)}$$

$$z = p_T \frac{\tanh(\eta)}{\sinh(\eta)} = \frac{p_T}{\cosh(\eta)} = p_T \operatorname{sech}(\eta)$$

COORDINATE SYSTEM



Transverse
x-y
plane



ϕ = Azimuthal scattering angle

$$\eta = -\ln \left[\tan \left(\frac{\theta_{cm}}{2} \right) \right]$$

$$p_T = p \sin \theta_{cm}$$

θ_{cm} = centre of mass scattering angle.

$$\begin{aligned}\Rightarrow p_x &= p_T \cos \phi \\p_y &= p_T \sin \phi\end{aligned}$$

$$\begin{aligned}p_z &= p \sin \theta_{cm} \\p_z &= p \cos \theta_{cm}\end{aligned}$$

$$\begin{aligned}p &= \frac{p_T}{\sin \theta_{cm}} \Rightarrow p_z = p_T \frac{\cos \theta_{cm}}{\sin \theta_{cm}} \approx \\&\quad p_T \cot \theta_{cm} \\&\theta_{cm} = 2 \arctan(e^{-\eta})\end{aligned}$$

$$\frac{\sin \theta}{\sin 2\theta} = \frac{1 - \tan^2 \theta}{1 + \tan^2 \theta} \times \frac{1 + \tan^2 \theta}{2 \tan \theta}$$

$$= \frac{1 - \tan^2 \theta}{2 \tan \theta}$$

$$\Rightarrow p_Z = p_T \frac{1 - e^{-2\eta}}{2e^{-\eta}} = p_T \sinh(\eta)$$

$p_Z = p_T \sinh(\eta)$

$$M^2 = 2m_\mu^2 + 2E_{\mu^+}E_{\mu^-} - 2\vec{p}_{\mu^+} \cdot \vec{p}_{\mu^-}$$

$$\vec{p}_{\mu^+} \cdot \vec{p}_{\mu^-} = p_T, p_{T_2} \cos \phi, \cos \phi_2 + p_T, p_{T_2} \sin \phi, \sin \phi_2$$

$$+ p_T, p_{T_2} \sinh(\eta_1) \sinh(\eta_2)$$

$$= p_T, p_{T_2} [\cos(\phi_1 - \phi_2) + \sinh(\eta_1) \sinh(\eta_2)]$$

(ROOT : T Lorentz Vector)

$$E^2 = m^2 + |\vec{p}|^2 \Rightarrow E_{\mu^+}^2 = m_\mu^2 + |p_{\mu^+}|^2$$

$$E_\mu^2 = m_\mu^2 + p_x^2 + p_y^2 + p_z^2$$

$$E_\mu^2 = m_\mu^2 + p_T^2 \cos^2 \phi + p_T^2 \sin^2 \phi + p_T^2 \sinh^2 \eta$$

$$= m_\mu^2 + p_T^2 + p_T^2 \sinh^2 \eta$$

$$= m_\mu^2 + p_T^2 \cosh^2 \eta$$

$$M^2 = 2m_\mu^2 + 2\sqrt{m_\mu^2 + p_{T_1}^2 \cosh^2 \eta_1} \sqrt{m_\mu^2 + p_{T_2}^2 \cosh^2 \eta_2} - 2p_T, p_{T_2} [$$

$$\cos(\phi_1 - \phi_2) + \sinh(\eta_1) \sinh(\eta_2)]$$

$$\cancel{M^2 = 2} [\cancel{p_{T\mu}}]$$

16/10/20 & 15/10/20 evening

- Coded manually using R & by using ROOT in python
- REMEMBER to Square root M^2 ! → gave ~~factor~~ 10^2 higher
- Gets expected Z mass ~ 91 GeV
- Originally bins $0 - 150$ GeV
reduced to $30 - 120$ GeV $\rightarrow 40 - 120$ GeV

- Used mix of Spyder & emacs -nw