

# Convergence rate of $X^N - X$ for McKean equations

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## 1 What is this?

An adaptation of [1, Proposition 3.1] for the case of McKean SDEs proposed in [2].

The proof builds on a number of results presented in the sections below.

**Definition 1** *For any real-valued continuous semi-martingale, the local time at zero  $L_t^0(\bar{Y})$  is defined as*

$$L_t^0(\bar{Y}) = \lim_{\epsilon \rightarrow 0} \frac{1}{2\epsilon} \int_0^t \mathbb{1}_{\{|\bar{Y}| \leq \epsilon\}} d\langle \bar{Y} \rangle_s, \mathbb{P}\text{-a.s.} \quad (1)$$

For all  $t \geq 0$ .

## 2 Lemma 5.1

The first result, [1, Lemma 5.1], is not necessary to prove for this particular setting since the result holds for any semi-martingale, I include it here for self-containment reasons.

**Lemma 1 (Lemma 5.1)** *For any  $\epsilon \in (0, 1)$  and any real-valued, continuous semi-martingale*

### **3 Lemma 5.2**

### **4 Lemma 5.3**

### **5 Proposition 5.4**

### **6 Proposition 3.1 (main result)**

## **References**

- [1] Tiziano De Angelis, Maximilien Germain, and Elena Issoglio. “A Numerical Scheme for Stochastic Differential Equations with Distributional Drift”. In: *arXiv:1906.11026 [cs, math]* (Oct. 22, 2020). arXiv: 1906.11026.
- [2] Elena Issoglio and Francesco Russo. “McKean SDEs with singular coefficients”. In: *arXiv:2107.14453 [math]* (July 30, 2021). arXiv: 2107.14453.