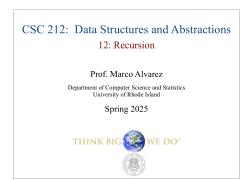
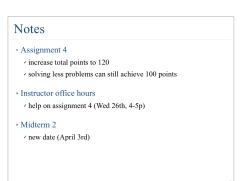
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## Rec

Wednesday, April 2, 2025 12:27 PM







## Recursion Definition method of solving problems that involves breaking a problem down into smaller and smaller subproblems (of the same structure) until you get to a small enough problem that it can be solved trivially Recursive functions technically, a recursive function is one that calls itself must have at least a base case and a recursive case base case: a condition that will eventually be met that will stop the recursive case: a condition that will eventually be met that will

continue the recursion

```
Basic form

function() {
    if (base case) {
        return trivial solution
    } else {
        break task into subtasks
        solve each task recursively
        merge solutions if necessary
        return solution
    }
}
```

```
Why recursion?

Can we live without it?

yes, for every recursive function, there is an iterative solution

However ...

some formulas are explicitly recursive

some problems exhibit a natural recursive solution
```

```
Practice

• Write a recursive function to add all elements in a vector

int sum_array(std::vector<int>& A, int n) {
    // base case
    if (n == 1) {
        return A[0];
    }

    // solve sub-task
    int partial_sum = sum_array(A, n-1);

    // return sum
    return A[n-1] + partial_sum;
}
```

```
Recursion call tree

Definition

a tree that represents the recursive calls of a function

Properties

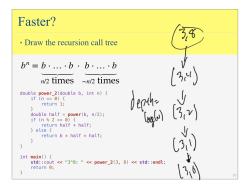
each node in the tree represents a call to the function
the root of the tree represents the initial call
the children of a node represent the recursive calls made by that function call
the leaves of the tree represents the depth of the recursion
the number of nodes in the tree represents the total number of recursive calls made
```

```
Draw the recursion call tree

#include evector-
```

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```
Draw the recursion call tree b^n = b \cdot b \cdot \dots \cdot b
n \text{ times}
double power(double b, int n) { } { } // base case if (n = 0) { } { } return 1; } // recursive call return b * power(b, n-1); } // return b * power(b, n-1); } int main() { } std::cout << "3^8: " << power(3, 8) << std::endl; } return 0; }
```





```
Binary search

Search on a sorted sequence

Ind the position of a target value within a sorted array

binary search is an efficient algorithm for this problem

Binary search algorithm

compare the target value to the middle element of the array

if they are not equal

the half in which the target cannot lie is eliminated and the search continues on the cemaining half

if the target value is equal to the middle element

the search terminates successfully

Recursive approach

base case: the array is empty

recursive case: the array is not empty, apply recursion to the left or right half of the array
```

