

LOGIC FOR NATURAL LANGUAGE, LOGIC IN NATURAL LANGUAGE

WELCOME TO THE COURSE!

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on Logic, Language, and Information
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THIS COURSE PRESENTS LOGICAL SYSTEMS TUNED TO NATURAL LANGUAGE

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- ▶ The raison d'être of logic is the study of inference in language.
- ▶ However, modern logic was developed in connection with the foundations of mathematics.
- ▶ So we have a mismatch, leading to
 - neglect of language in the first place
 - use of first-order logic and no other tools
- ▶ First-order logic is both too big and too small:
 - cannot handle many interesting phenomena
 - is undecidable

NATURAL LOGIC: RESTORE NATURAL LANGUAGE INFERENCE AS A CENTERPIECE OF LOGIC

PROGRAM

Show that significant parts of natural language inference can be carried out in **decidable** logical systems, preferably in “**light**” systems.

To **axiomatize** as much as possible, because the resulting logical systems are likely to be interesting.

To ask how much of language could have been done if the traditional logicians had today's mathematical tools.

WHAT WILL YOU LEARN IN THIS CLASS?

The class will have a lot of technical material connected to the basic notions of topics such as

- ▶ model theory
- ▶ algebraic logic
- ▶ modal logic
- ▶ decidable fragments of first-order logic
- ▶ the typed lambda calculus and its connection to grammar and semantics

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The course will also present a lot of educational material. This could be an introduction to logic or a “bridge to mathematical proofs” course.

MORE ON THE EDUCATIONAL ASPECTS

I comment on educational points in green boxes.

NATURAL LOGIC: PARALLEL STUDIES

I DIDN'T HAVE MUCH TO SAY ON THESE, BUT WE CAN DISCUSS THEM

- ▶ History of logic: reconstruction of original ideas
- ▶ Philosophy of language: proof-theoretic semantics
- ▶ Philosophy of logic: why variables?
- ▶ Cognitive science: models of human reasoning
- ▶ Linguistic semantics:
Are deep structures necessary, or can we just
use surface forms?
And is a complete logic a semantics?
- ▶ Computational linguistics/artificial intelligence:
many precursors and related projects

Given a list of temporary assumptions,
decide whether another sentence **follows** from the given list.

WHAT “FOLLOWS FROM” MEANS

A sentence φ **follows from** a list Γ of other sentences
if whenever we accept the sentences in Γ ,
we could/should also accept φ .

THE STRONGEST FORMULATION OF THIS FORMULATION OF “INFERENCE”

In seeing whether φ follows from Γ in some situation s ,
and ideal human would start with some set
 Δ of **categorical sentences**,
known or believed to be true,
stated in some formal language \mathcal{L} ,
and also some general features of s , again stated in s ,
and then parse φ and turn it into a sentence in \mathcal{L} ,
and then appeal to a general inference procedure.

Such a procedure should exist: this whole account should be effective.

The inference should also match some semantics of \mathcal{L} .

Deviations in performance would be correlated to various features of the ideal account.

WHAT DO VARIOUS FIELDS GIVE UP?

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This is what is done in RTE (see below).

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This is what is done in RTE (see below).

GIVE UP ON COMPLEX INFERENCES

This is what is done in psychological studies of syllogistic inference.

WHAT I AM TRYING TO DO

What I propose to do:

GIVE UP SOMEWHAT ON STATEMENTS IN “REAL LIFE
LANGUAGE”,
BUT NOT ON DECIDABILITY,
AND NOT ON LOGICAL COMPLETENESS

Also:

GIVE UP MORE TO DO MORE

EXAMPLES OF INFERENCES

WHICH WE WILL SEE IN THIS COURSE

THESE ARE THE BASIC DATA THAT THE COURSE WILL ACCOUNT FOR

First, a few examples from the **classical syllogistic**:

$$\frac{\text{All men are mortal} \quad \text{Socrates is a man}}{\text{Socrates is mortal}} \quad (1)$$

$$\frac{\text{All auctioneers are curmudgeons} \quad \text{No bartenders are curmudgeons}}{\text{No auctioneers are bartenders}} \quad (2)$$

Syllogistic logic is under-appreciated!

My aim in the first two days of the course is to convince you that **extended syllogistic logics** are very interesting indeed.

A FIRST LOOK AT SYLLOGISTIC LOGIC

Our “syntax” of sentences will give us

All X are Y

Some X are Y

No X are Y

but no boolean connectives (!), at least not yet

We adopt the evident semantics.

We craft a logical system which has formal proofs using our syntax of sentences and nothing else.

After this, we want to extend the idea of syllogistic logic.

BASIC SYLLOGISTIC LOGIC: ALL, AND SOME

Syntax: *All p are q, Some p are q*

Semantics: A model \mathcal{M} is a set M ,
and for each noun p we have an interpretation $\llbracket p \rrbracket \subseteq M$.

$$\begin{array}{lll} \mathcal{M} \models \textit{All } p \textit{ are } q & \text{iff} & \llbracket p \rrbracket \subseteq \llbracket q \rrbracket \\ \mathcal{M} \models \textit{Some } p \textit{ are } q & \text{iff} & \llbracket p \rrbracket \cap \llbracket q \rrbracket \neq \emptyset \end{array}$$

Proof system:

$$\begin{array}{c} \frac{}{\textit{All } p \textit{ are } p} \\ \frac{\textit{Some } p \textit{ are } q}{\textit{Some } q \textit{ are } p} \quad \frac{\textit{Some } p \textit{ are } q}{\textit{Some } p \textit{ are } p} \quad \frac{\textit{All } q \textit{ are } n \quad \textit{Some } p \textit{ are } q}{\textit{Some } p \textit{ are } n} \end{array}$$
$$\frac{\textit{All } p \textit{ are } n \quad \textit{All } n \textit{ are } q}{\textit{All } p \textit{ are } q}$$

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Proof system:

$$\begin{array}{c} \frac{}{\textit{All } p \textit{ are } p} \qquad \frac{\textit{All } p \textit{ are } n \quad \textit{All } n \textit{ are } q}{\textit{All } p \textit{ are } q} \\[10pt] \frac{\textit{Some } p \textit{ are } q}{\textit{Some } q \textit{ are } p} \quad \frac{\textit{Some } p \textit{ are } q}{\textit{Some } p \textit{ are } p} \quad \frac{\textit{All } q \textit{ are } n \quad \textit{Some } p \textit{ are } q}{\textit{Some } p \textit{ are } n} \end{array}$$

We could also add the word *No*.
What rules do you think we would need?

If Γ is a set of formulas, we write $\mathcal{M} \models \Gamma$ if for all $\varphi \in \Gamma$, $\mathcal{M} \models \varphi$.

$\Gamma \models \varphi$ means that every $\mathcal{M} \models \Gamma$ also has $\mathcal{M} \models \varphi$.

A **proof tree over Γ** is a finite tree \mathcal{T} whose nodes are labeled with sentences and each node is either an element of Γ , or comes from its parent(s) by an application of one of the rules.

$\Gamma \vdash S$ means that there is a proof tree \mathcal{T} for over Γ whose root is labeled S .

English:

If there is an n , and if all ns are ps and also qs , then some p are q .

Semantic assertion:

Some n are n , All n are p , All n are $q \models$ Some p are q .

Proof-theoretic assertion:

Some n are n , All n are p , All n are $q \vdash$ Some p are q .

English:

If there is an n , and if all ns are ps and also qs , then some p are q .

This is something we could check against human intuition and performance.

Semantic assertion:

$\text{Some } n \text{ are } n, \text{ All } n \text{ are } p, \text{ All } n \text{ are } q \models \text{Some } p \text{ are } q.$

The reasoning here would be a mathematical proof.

Proof-theoretic assertion:

$\text{Some } n \text{ are } n, \text{ All } n \text{ are } p, \text{ All } n \text{ are } q \vdash \text{Some } p \text{ are } q.$

The proof tree is

$$\frac{\text{All } n \text{ are } q \quad \frac{\frac{\text{All } n \text{ are } p \quad \text{Some } n \text{ are } n}{\text{Some } n \text{ are } p}}{\text{Some } p \text{ are } n}}{\text{Some } p \text{ are } q}}$$

EXAMPLE OF A CONCLUSION WHICH DOESN'T FOLLOW

All frogs are reptiles.

All frogs are animals.

All reptiles are animals.

EXAMPLE OF A CONCLUSION WHICH DOESN'T FOLLOW

All frogs are reptiles.

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All reptiles are animals.

We can define a model \mathcal{M} by

$$M = \{1, 2, 3, 4, 5, 6\}$$

$$\llbracket \text{frogs} \rrbracket = \{1, 2\}$$

$$\llbracket \text{reptiles} \rrbracket = \{1, 2, 3, 4\}$$

$$\llbracket \text{animals} \rrbracket = \{1, 2, 4, 5, 6\}$$

In this model, the assumptions are true but the conclusion is false.
So the argument is **invalid**.

All frogs are reptiles, All frogs are animals $\not\models$ All reptiles are animals.

SOUNDNESS/COMPLETENESS THEOREM

$$\Gamma \models \varphi \text{ iff } \Gamma \vdash \varphi$$

References to related work:

Łukasiewicz 1951, Westerståhl 1989.

All the logical systems in this course are complete.

If you follow most of the details, you'll learn a lot of technical material.

A first course in logic could contain the completeness results which we'll see in the first few days plus parallel material on propositional logic and also *something* on first-order logic.

MORE EXAMPLES OF INFERENCES

THIS CLASS WILL NOT QUITE TREAT THESE

Every giraffe is taller than every gnu
Some gnu is taller than every lion
Some lion is taller than some zebra
Every giraffe is taller than some zebra

(3)

More students than professors run More professors than deans run
More students than deans run

(4)

At most as many xenophobics as yodelers are zookeepers
At most as many zookeepers as alcoholics are yodelers
At most as many yodelers as xenophobics are alcoholics
At most as many zookeepers as alcoholics are xenophobics

(5)

MORE REASONING ABOUT THE SIZES OF SETS

WE **ARE** GOING TO SEE THE FULL SET OF RULES ON TUESDAY OR WEDNESDAY

EXAMPLE

Assume:

- ① *There are at least as many non-y as y*
- ② *There are at least as many non-z as z*
- ③ *All non-y are z*
- ④ *All x are z*

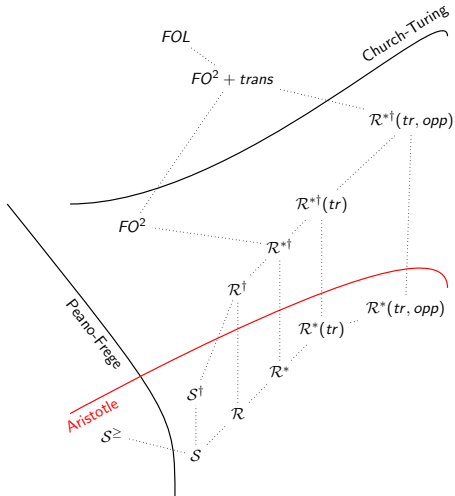
Then prove from these that *No x are y*.

Here is a formal proof in the logical system which we'll see:

$$\frac{\forall(x, z) \quad \frac{\forall(\bar{y}, z) \quad \frac{\exists^{\geq}(\bar{y}, y) \quad \exists^{\geq}(\bar{z}, z)}{\exists^{\geq}(\bar{y}, z)} \text{ (HALF)}}{\forall(z, \bar{y})} \text{ (CARD MIX)}}{\forall(x, \bar{y})} \text{ (BARBARA)}$$

MAP OF SOME NATURAL LOGICS

The **Aristotle boundary** is the dividing line between fragments which are formulated syllogistically and those which are not. Reductio proofs are ok. Infinitely many rules are not.



first-order logic

$FO^2 + \text{"R is trans"}$

2 variable FO logic

\dagger adds full *N*-negation

$\mathcal{R}^*(tr) + \text{opposites}$

$\mathcal{R}^* + (\text{transitive})$

comparative adjs

$\mathcal{R} + \text{relative clauses}$

$S + \text{full } N\text{-negation}$

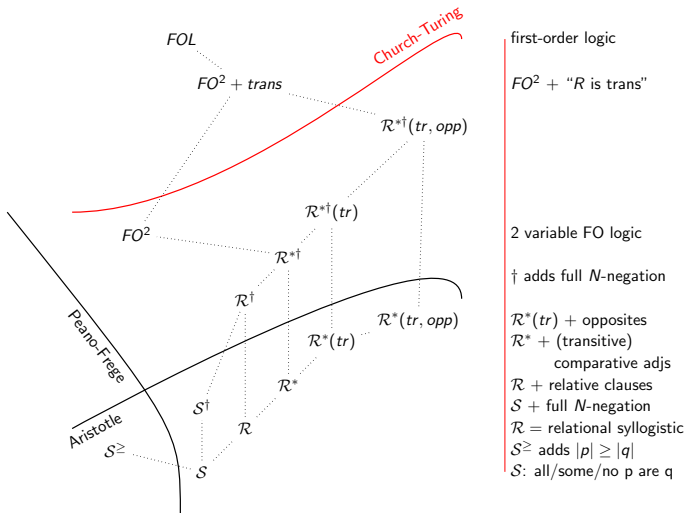
$\mathcal{R} = \text{relational syllogistic}$

$S \geq$ adds $|p| \geq |q|$

S : all/some/no p are q

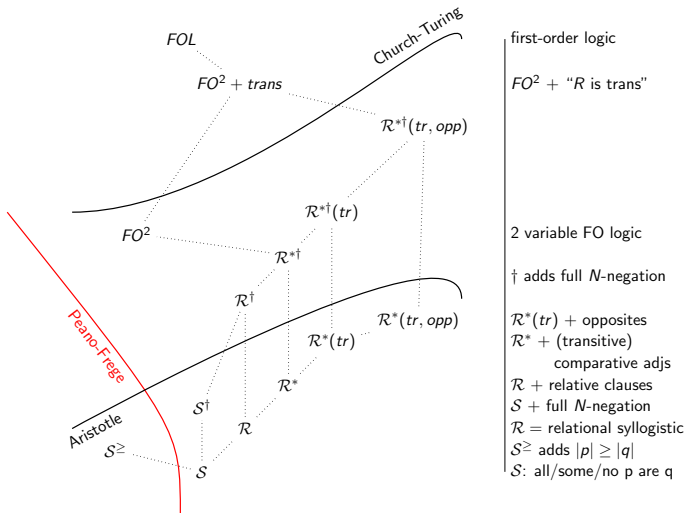
MAP OF SOME NATURAL LOGICS

The **Church-Turing boundary** is the dividing line between decidable and undecidable fragments.



MAP OF SOME NATURAL LOGICS

The **Peano-Frege** boundary divides the fragments according to whether they may be formulated in first-order logic.



EXAMPLE OF WHERE WE WOULD WANT DERIVATIONS WITH VARIABLES

All xenophobics see all astronauts

All yodelers see all zookeepers

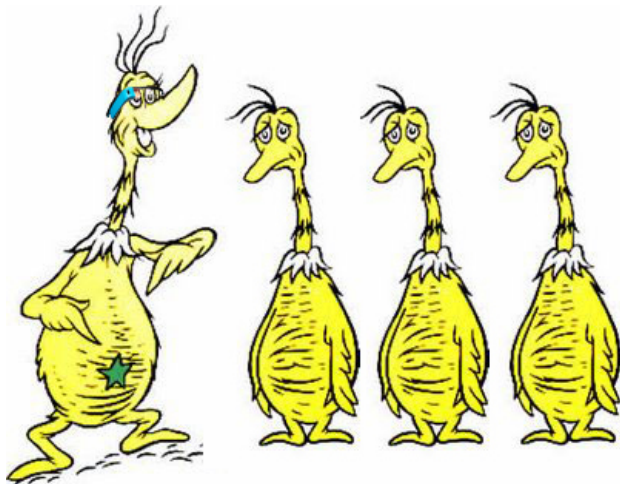
All non-yodelers see all non-astronauts

All wardens are xenophobics

All wardens see all zookeepers

1	<i>All xenophobics see all astronauts</i>	Hyp
2	<i>All yodelers see all zookeepers</i>	Hyp
3	<i>All non-yodelers see all non-astronauts</i>	Hyp
4	<i>All wardens are xenophobics</i>	Hyp
5	Jane <i>Jane is a warden</i>	Hyp
6	<i>All wardens are xenophobics</i>	R, 4
7	<i>Jane is a xenophobic</i>	All Eliim, 6
8	<i>All xenophobics see all astronauts</i>	R, 2
9	<i>Jane sees all astronauts</i>	All Elim, 8
10	<i>Jane is a yodeler</i>	Hyp
11	<i>Jane sees all zookeepers</i>	Easy from 2
12	<i>Jane is not a yodeler</i>	Hyp
13	<i>Jane sees all zookeepers</i>	See below
14	<i>Jane sees all zookeepers</i>	Cases 10-11, 12-13
15	<i>All wardens see all zookeepers</i>	All Intro

1	<i>Jane is not a yodeler</i>	Hyp
2	<i>Jane sees all astronauts</i>	R, above
3	<i>All non-yodelers see all non-astronauts</i>	R, above
4	<i>Jane sees all non-astronauts</i>	All Elim, 1, 3
5	<i>Bob</i> <i>Bob is a zookeeper</i>	Hyp
6	<i>Bob is astronaut</i>	Hyp
7	<i>Jane sees Bob</i>	All Elim, 2
8	<i>Bob is not astronaut</i>	Hyp
9	<i>Jane sees Bob</i>	All Elim, 4
10	<i>Jane sees Bob</i>	Cases
11	<i>Jane sees all zookeepers</i>	All Intro



THE OVERALL TOPIC FOR THE TALK TO KIDS

How can a person or computer
answers questions involving a word which they don't know?

A word like Sneetch.

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answers questions involving a **word which they don't know**?

A word like **Sneetch**.

WHAT “FOLLOWS FROM” MEANS

One sentence, A, **follows from** a second sentence, B,
if every time we use B in a true way,
we also would be committed to A if we asked about it. Day

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WHAT “FOLLOWS FROM” MEANS

One sentence, A, follows from a second sentence, B,
if every time we use B in a true way,
we also would be committed to A if we asked about it.

If we say

B : every animal hops

then it follows that

A : every Sneetch moves



animal
Sneetch
Star-Belly Sneetch



move
dance
waltz





animal
Sneetch
Star-Belly Sneetch



move
dance
waltz

Let's talk about a situation where

all Sneetches dance.

Which one would be true?

- ▶ all Star-Belly Sneetches dance
- ▶ all animals dance



animal
Sneetch
Star-Belly Sneetch



move
dance
waltz

-
- ▶ all Star-Belly Sneetches dance true
 - ▶ all animals dance false

We write

all Sneetches↓ dance



animal
Sneetch
Star-Belly Sneetch



move
dance
waltz

all Sneetches↓ dance

What arrow goes on “dance”?

- ▶ all Sneetches waltz
- ▶ all Sneetches move



animal
Sneetch
Star-Belly Sneetch



move
dance
waltz

We write

all Sneetches↓ dance↑



animal
Sneetch
Star-Belly Sneetch



move
dance
waltz

Let's put the arrows on the words **Sneetches** and **dance**.

- ① No Sneetches dance.
- ② If you play loud enough music, any Sneetch will dance.
- ③ Any Sneetch in Zargonia would prefer to live in Yabistan.
- ④ If any Sneetch dances, McBean will dance, too.



animal
Sneetch
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WHAT GOES UP? WHAT GOES DOWN?

$$f(x, y) = y - x \quad (6)$$

$$g(x, y) = x + \frac{2}{y} \quad (7)$$

$$h(v, w, x, y, z) = \frac{x - y}{2^{z-(v+w)}} \quad (8)$$

WHAT GOES UP? WHAT GOES DOWN?

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$$h(v^{\uparrow}, w^{\uparrow}, x^{\uparrow}, y^{\downarrow}, z^{\downarrow}) = \frac{x - y}{2^{z - (v + w)}} \quad (8)$$

The \uparrow and \downarrow notations have the same meaning in language as in math!

This is not an accident!

LET'S LOOK AT AN (EASY) INFERENCE IN ALGEBRA

Which is bigger, $-(7 + 2^{-3})$ or $-(7 + 2^{-4})$?

LET'S LOOK AT AN (EASY) INFERENCE IN ALGEBRA

Which is bigger, $-(7 + 2^{-3})$ or $-(7 + 2^{-4})$?

$$\begin{array}{rcl} 3 < 4 & & \\ \hline -4 < -3 & -x \text{ is antitone} & \\ \hline 2^{-4} < 2^{-3} & 2^x \text{ is monotone} & \\ \hline 7 + 2^{-4} < 7 + 2^{-3} & 7 + x \text{ is monotone} & \\ \hline -(7 + 2^{-3}) < -(7 + 2^{-4}) & -x \text{ is antitone} & \end{array}$$

$f(x)$ monotone means if $x \leq y$, then $f(x) \leq f(y)$
 $f(x)$ antitone means if $x \leq y$, then $f(y) \leq f(x)$
i.e., $f(x) \geq f(y)$

LET'S LOOK AT AN (EASY) INFERENCE IN ALGEBRA

Which is bigger, $-(7 + 2^{-3})$ or $-(7 + 2^{-4})$?

$$\begin{array}{l} \frac{3 < 4}{-4 < -3} \quad \begin{array}{l} -x \text{ is antitone} \\ 2^x \text{ is monotone} \end{array} \\ \frac{2^{-4} < 2^{-3}}{7 + 2^{-4} < 7 + 2^{-3}} \quad 7 + x \text{ is monotone} \\ \hline -(7 + 2^{-3}) < -(7 + 2^{-4}) \quad -x \text{ is antitone} \end{array}$$

Occasionally in this week's lectures, I'll use

blue for syntax,
and red for semantics.

ANOTHER WAY TO FRAME THIS PROBLEM

$$f(x, y^{\uparrow}) = -(x + 2^{-y})$$

LET'S LOOK AT A PARALLEL INFERENCE IN LANGUAGE

Background: $\text{skunks} \leq \text{mammals}$.

What do you think about this one?

All skunks are mammals

All who fear all who respect all skunks fear all who respect all mammals

Based only on our assumption, which set is bigger?

those who fear all who respect all skunks
or
those who fear all who respect all mammals

LET'S LOOK AT A PARALLEL INFERENCE IN LANGUAGE

Background: $\text{skunks} \leq \text{mammals}$.

Based only on our assumption, which set is bigger?

those who fear all who respect all skunks

or

those who fear all who respect all mammals

$$\frac{\frac{\text{skunks} \leq \text{mammals}}{\text{respect all mammals} \leq \text{respect all skunks}} \quad \lambda x. \text{respect all } x \text{ is antitone}}{\text{fear all who respect all skunks} \leq \text{fear all who respect all mammals}} \quad \lambda x. \text{fear all } x \text{ is antitone}$$

respect all x^\downarrow

fear all who respect all x^\uparrow

DAY-BY-DAY PLAN FOR THIS COURSE

I have arranged the course material in a number of units:

- ▶ overview + examples (today, done) + objections
- ▶ the simplest logic in the world (today)
- ▶ all + verbs + relative clauses (Tuesday)
- ▶ negation, definite descriptions, sizes of sets (Tuesday/Wednesday)
- ▶ basics on monotonicity \uparrow and \downarrow , and connections to categorial grammar and semantics (Wednesday/Thursday)
- ▶ implementations and experience with language models (Friday)

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I can't cover everything without rushing, so there will be times when I mainly mention results without proofs.

There are also some worksheets and/or suggested homework exercises.

I like talking to you on the course topics.

OBJECTIONS TO THE PROGRAM OF NATURAL LOGIC

MOST NATURAL LANGUAGE PHENOMENA ARE NOT
ADDRESSED:

ANYTHING “PRAGMATIC”

VAGUENESS, INTENT OF SPEAKERS, POETIC LANGUAGE

I agree with this objection!

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I agree with this objection!

TO DO LOGIC FULLY, WE NEED RESOURCES TO HANDLE THE
WORST-POSSIBLE PHENOMENA

I don't agree with this; see below.

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VAGUENESS, INTENT OF SPEAKERS, POETIC LANGUAGE

I agree with this objection!

TO DO LOGIC FULLY, WE NEED RESOURCES TO HANDLE THE
WORST-POSSIBLE PHENOMENA

I don't agree with this; see below.

QUINE, FROM *Word and Object*:
IF WE WERE TO DEVISE A LOGIC OF ORDINARY LANGUAGE
FOR DIRECT USE ON SENTENCES AS THEY COME,
WE WOULD HAVE TO COMPLICATE OUR RULES OF INFERENCE
IN SUNDRY UNILLUMINATING WAYS.

This is something we'll talk about throughout the week.

SLOGAN: TREAT “EVERYDAY INFERENCE” IN LIGHT SYSTEMS

YOU DECIDE

Consider three activities:

- A mathematics: prove the Pythagorean Theorem, $a^2 + b^2 = c^2$.
- B syntax: parse John knows his mother saw him at her house.
- C semantics: tell whether a reader of the UW Fight Song should infer that the speaker wants the Carnegie team to win.

A: mathematics

B: syntax

Where would you put C: semantics?

THE UW FIGHT SONG

Bow Down to Washington, Bow Down to Washington.
Mighty are the men who wear the Purple and the Gold,
Joyfully we welcome them within the Victor's fold.
We will carve our name in the Hall of Fame,
To preserve the memory of our Devotion.

So, heaven help the foes of Washington,
They're trembling at the feet of mighty Washington.
Our boys are there with bells, their fighting blood excels,
It's harder to push them over the lines than pass the Dardanelles.
So Victory's the cry of Washington
Our leather lungs together with a Rah! Rah! Rah!
And o'er the land, the loyal band
Will sing the glory of Washington forever!.

YOU DECIDE

Consider three activities:

- A mathematics: prove the Pythagorean Theorem, $a^2 + b^2 = c^2$.
- B syntax: parse John knows his mother saw him at her house.
- C semantics: tell whether a reader of the UW Fight Song should infer that the speaker wants the Washington team to win.

A: mathematics

B: syntax

Where would you put C: semantics?

MY VIEW: B AND C GO TOGETHER; A DOESN'T BELONG

We should not reduce formal linguistic inference to formal inference in standard logical systems.

(Also, we really can't carry out that reduction, for several different reasons.)