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A Model Checker Using IC3

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Proforma

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Original Aims of the Project

Describe the original aims of the project, i.e. summarize information from the “Substance and Structure” and “Success Criteria” sections of the project proposal.

Work Completed

Describe the work completed as part of project, including extensions.

Special Difficulties

None.

Declaration

I, Lauren Pick of Homerton College, being a candidate for Part II of the Computer Science Tripos, hereby declare that this dissertation and the work described in it are my own work, unaided except as may be specified below, and that the dissertation does not contain material that has already been used to any substantial extent for a comparable purpose.

Signed [signature]

Date [date]

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Chapter 1

Introduction

Model checking attempts to verify that a hardware or software system has certain properties. Given a model of the system and a specified property, a model checker will automatically check whether all reachable states in the system satisfy this property.

All model-checking approaches suffer from limitations on the size of the systems they can model check in practice as a result of the state explosion problem: the number of states in a system can be (and often is) exponential in the number of state variables [7].

The initial approach to the model checking problem involved explicitly considering each reachable state in the model. Symbolic model checking arose as a method of mitigating the effects of the state explosion problem to some extent. By representing states and the transition relation between them as boolean expression, symbolic model checking allows sets of states to be represented efficiently as boolean expressions involving state variables as opposed to an explicit list of each individual state in the set [11].

A brief description symbolic model-checking and SAT-based model-checking follows to provide further context for this project, which focuses on implementing the IC3 algorithm, a SAT-based model-checking algorithm.

1.1 Symbolic Model Checking

Symbolic model checking was originally invented for use with ordered binary decision diagrams (BDDs), which provide an efficient representation of boolean formulas using canonical forms for the formulas. The efficiency of BDDs in storing boolean formulas allowed for the model checking of systems with larger numbers of states than could be handled by explicit-state model checking [11].

The efficiency of BDD representations relies on choosing an appropriate ordering, which can be computationally expensive, and in some cases, there is no such ordering that results in a space-efficient BDD [1].

An alternative to BDD-based symbolic model-checking techniques are SAT-based techniques, which do not use the canonical representations of boolean formulas as BDDs and make use of SAT procedures. Such techniques include bounded model checking (BMC), which proves properties by finding counterexamples of certain lengths [1]; k -induction,

which proves properties inductively [12]; and the IC3 algorithm that is the focus of this project. A brief description and comparison of these techniques follows.

Many modern SAT-based model checkers are based on BMC, which begins at the initial state of the transition system and searches for paths of length k from the initial state that violate the negated property. If no path of length k is found, BMC increments k and searches again. BMC is effective at finding counterexamples, but for some large systems, BMC is incomplete unless it is allowed to reach the point at which k is the maximal path length.

The k -induction algorithm is similar to BMC in its unrolling of the transition relation to consider paths of length k , but it also incorporates induction. At each depth k , the algorithm asserts that the desired property holds at each state before the final state.

1.2 The IC3 Algorithm

The IC3 algorithm (also called PDR [9]) is a SAT-based model-checking algorithm for proving the safety properties (i.e. properties that must hold in all reachable states) of hardware. The first implementation of the algorithm `ic3` placed third in HWMCC'10, and since then, several variants of the algorithm have been developed.

As in k -induction, properties are proved through induction: the algorithm considers reachable sets of states k steps away from the initial state until reaching a fixed point. As with later variants of k -induction, the IC3 algorithm also discovers new invariants if the initial assumptions are not strong enough to prove the desired property, but unlike k -induction, the safety property guides the discovery of the invariants. As a result, the discovered invariants are more relevant for proving the safety property [5].

Furthermore, IC3 does not unroll the transition relation as k -induction or other BMC-based methods do, but instead considers at most one step of the transition relation at a time, leading to smaller, simpler SAT queries. As a result, IC3 requires less memory than BMC-based methods in practice [5].

1.3 Further Work

While IC3 algorithm is for model checking safety properties of hardware, there are applications of the algorithm in model checking LTL and CTL properties and model checking software [5].

The FAIR model-checking algorithm, which model checks ω -regular properties, makes use of a safety model checker such as IC3, and IICTL, which model-checks CTL formulas [10], makes use of both a safety model checker such as IC3 as well as a fair cycle finder such as FAIR.

Other work generalizes IC3 to use an underlying SMT solver rather than a SAT solver, and this generalization has been used to check control-flow graphs of programs [6]. More recently, Johannes Birgmeier, Aaron Bradley, and Georg Weissenbacher have introduced CTIGAR, a method of abstraction-refinement based on IC3's counterexamples to induc-

tion rather than the counterexamples in CEGAR, which experiments suggest is competitive with CEGAR-based techniques for software verification [3].

1.4 Project Aims

This project aims to implement a basic form of the IC3 algorithm in Haskell. The model checker should be able to correctly check several small examples.

Chapter 2

Preparation

2.1 Requirements Analysis

A SAT-based model checker requires a way of taking input models and also requires a way to solve SAT queries. I chose the AIGER format for representing the hardware models and the MiniSat SAT solver for answering SAT queries, resulting in a need for an AIGER parser and an interface to MiniSat in Haskell.

Given that the model checking algorithm deals with transition systems (discussed later), the implementation also requires a representation of transition systems, which should correspond to the input hardware model. A further requirement is the implementation of the IC3 algorithm itself.

In summary, the requirements are as follows:

- AIGER parser
- MiniSat interface
- Transition system representation
- IC3 algorithm implementation

2.2 Tools Used

The tools used in the project and what they were used for are as follows:

- Git was used for version control, with GitHub providing backup storage
- Haddock was used for documentation
- HUnit was used for testing
- Criterion was used for benchmarking
- Cabal was used for package/dependency management
- The `hsc2hs` preprocessor eased writing Haskell interfaces to C code

- The Aiger Utilities' parser for comparison with and as an alternative to the one developed as part of the project
- The `bliftoaig` and `aigtoaig` tools eased the specification of models by converting from human-readable BLIF and ASCII AIG formats to the binary AIG format
- The MiniSat SAT solver was used for handling SAT queries

2.3 Model Specification

I used both the AIGER format and Berkeley Logic Interchange Format (BLIF) to specify some of the example hardware models. Hardware models that the model checker accepts as input are specified using the AIGER format, which is the format used to specify hardware models in the Hardware Model Checking Competitions; however using the AIGER format to specify larger models was cumbersome, so such models were specified using BLIF and converted to AIGER format using the AIGER library's `bliftoaig` tool.

The model checker takes as input models formatted using either the ASCII or binary AIGER formats described below.

2.3.1 AIGER

The AIGER format provides a method of specifying hardware modeled as And-Inverter Graphs with latch elements providing single clock-tick delays: all circuits are modeled as a graph of nodes consisting only of AND gates, NOT gates, and latches.

The AIGER format has both an ASCII and binary version, where the ASCII format is more flexible and human readable, and the binary version is more compact. The Hardware Model Checking Competition's examples are in the latter of the two.

A new version of the AIGER format is currently under development, with examples from HWMCC'14 using the new version.

Old version

All AIGER files begin with a header of the form

`V M I L O A`

where

- `V` can take on values `aag`, specifying that the file is in the ASCII format or `aig`, specifying that the file is in the binary format.
- `M` gives the maximum index of a variable
- `L` gives the number of latches
- `O` gives the number of outputs
- `A` gives the number of two-input AND gates

Variables are represented in AIGER with even integers greater than 1, with 0 representing the constant value *False* and 1 representing *True*. An odd integer value $i + 1$ represents the negated value of the literal represented by i . In other words, a variable named x is represented by $x \times 2$, which gives the positive literal x , and $x \times 2 + 1$ gives the negative literal $\neg x$.

The different components are specified after the header in the order that their counts are given in the header.

In the ASCII version of the format, inputs are specified by giving the index (greater than 2) that represents its corresponding variable name, and outputs are specified similarly as single indices. Latches initially begin with value 0 and are specified by giving the index representing their corresponding variable name followed by the integer that represents the literal giving their next-state value. AND gates are specified by giving their indices and their two inputs literals' integer representations.

```
aag 3 0 2 1 1
2 3
4 2
6
6 2 4
```

Figure 2.1: A circuit specified in the old ASCII AIGER format

For example, figure 2.1 specifies a circuit with no inputs, two latches with indices 2 and 4 and one AND gate 6 that takes the outputs of the two latches as inputs and whose output is the single output of the circuit.

In the binary version of the format, variable indices are assumed to occur in increasing order. Since each literal must be defined, this allows for the omission of the variable indices when defining inputs or latches.

Inputs are not explicitly listed: the input variables are inferred based on the value of **I**. Similarly, latches are specified by only listing their next-state literals' representations.

The binary format also assumes that AND gates occur in order of their variable indices and additionally assumes that inputs to an AND gate will have already been defined before that AND gate. These assumptions allow AND gates to be represented by two differences that tend to be small in practice:

For an AND gate specified in the old format by **lhs rhs0 rhs1**, where inputs **rhs0** and **rhs1** have been ordered such that $\text{rhs0} \geq \text{rhs1}$, define

$$\delta_0 = \text{lhs} - \text{rhs0}$$

and

$$\delta_1 = \text{lhs} - \text{rhs1}$$

The values δ_i are then represented with the following binary encoding, giving a more compact representation for AND gates than the ASCII version of the format:

For 7-bit words w_0, \dots, w_n with

$$\delta_i = w_0 + 2^7 w_1 + \dots + 2^{7n} w_n,$$

δ_i is represented as the sequence of $n + 1$ bytes b_0, \dots, b_n , where

- for $0 \leq k < n$, b_k is the byte obtained by setting the most significant bit to 1 and the rest of the bits to w_k , and
- b_n is the byte obtained by setting the most significant bit to 0 and the rest of the bits to w_n

New version

The new AIGER format begins with a header of the form

V M I L O A B C J F

where V, M, I, L, O, A are as in the old format, and

- B gives the number of “bad state” properties
- C gives the number of invariant constraints
- J gives the number of justice properties
- F gives the number of fairness constraints

Variables are represented in the same manner as the old format and are specified after the header in the same order that the counts are given in the header with the exception of AND gates, which occur at the end of the file. Latches’ initial values can also be specified now with an additional 0 or 1 after the next-state literal’s index. If the initial value is omitted, the initial value is assumed to be 0 as in the old version of the format. The header can also be truncated after giving the number of AND-gates if the remaining counts are all zero, allowing any parser for the new AIGER format to be backwards-compatible.

The new version of the format is otherwise the same as the old format.

2.4 The IC3 Algorithm

Given a hardware model (i.e. a finite-state transition system) and a safety property P , IC3 aims either to prove inductively that P holds at all reachable states from the initial state or to find a $\neg P$ state that can be reached.

2.4.1 Transition Systems

A transition system is a tuple (i, x, I, T) consisting of a set of input variables i , state variables x , next-state variables x' , an initial set of states represented by the boolean expression $I(x)$ and a transition relation represented by the boolean expression $T(i, x, x')$.

A single state of the system (or a singleton set containing that state) is specified through the assignment of all state variables in x .

2.4.2 Frames

As with other inductive approaches to model checking, the IC3 algorithm maintains a set of k frames F_0, \dots, F_k , where each frame F_i is a set of clauses whose conjunction represents an overapproximation of the set of states that reachable by the transition system in i steps (so, for example, F_0 is just the initial state set I).

If $F_i = F_{i+1}$ holds for any i at any point, then a fixed point has been found, and the algorithm terminates.

2.4.3 Checking Properties

The initiation query $I \Rightarrow P$ is used to check that the safety property holds in the initial state I . This query is run once at the start of the algorithm for the desired safety property. If it fails (i.e. if it is false), then the algorithm terminates, as an error state in which $\neg P$ holds is reachable in 0 steps. If the query succeeds, then the algorithm proceeds.

The consecution query $F_k \wedge T \Rightarrow P'$ for a frame F_k is used to check whether the property P necessarily holds in the next frame.

The algorithm extends its set of frames F_0, \dots, F_k with a new frame F_{k+1} by running the consecution query. If the consecution query is successful, then the new frame F_{k+1} with clause $\{P\}$ can be added. All clauses in frame F_k are then propagated to F_{k+1} : For each clause $C \in F_k$, if $F_k \wedge T \Rightarrow C'$ holds, then C' is added to F_{k+1} .

If a consecution query $F_k \wedge T \Rightarrow P'$ fails, then that means that there is an F_k state that is a predecessor of the $\neg P'$ state, i.e. there is an F_k state s and a $\neg P'$ state v with $T(i, s, v')$. The state s is a *counterexample to induction* (CTI) state.

The algorithm aims to refine the approximation F_k of the set of states reachable in at least k steps by finding a clause c that holds at depth k such that $F_k \wedge c \wedge T \Rightarrow P'$ holds:

Such a c must be such that for the counterexample to induction s ,

$$c \Rightarrow \neg s,$$

with an obvious choice being $c = \neg s$, which can be found easily using a SAT solver. In practice, it is better to generalize $\neg s$ and choose a smaller c , which can allow for a set of several states to be eliminated in F_k rather than just eliminating s . In particular, the choice of c that maximises the number of states eliminated in F_k is the minimal inductive subclause of $\neg s$ relative to frame F_k .

2.4.4 Minimal Inductive Subclauses

A minimal inductive subclause for a frame F_k and a clause s that is inductive relative to F_k (i.e. $F_0 \Rightarrow s'$ and $F_k \wedge T \wedge s \Rightarrow s'$) is a clause c whose literals are the smallest subset of the literals in s such that

$$F_k \wedge T \wedge c \Rightarrow c'$$

holds.

The minimal inductive subclause can be found by dropping each literal in s in turn and checking if the resulting clause is inductive relative to F_k :

```

mic (s, k):
  for literal l in s:
    c := s \ {l}
    if c is inductive relative to frame at depth k
      s := c
  return s

```

Finding the minimal inductive subclause can be computationally expensive, so it is often approximated in practice.

An improvement to the generalization provided by finding minimal inductive subclauses in this way incorporates the use of counterexamples to generalization.

2.4.5 Counterexamples to Generalization

Checking if a subclause $c = s/\{l\}$ of a clause s is inductive relative to a frame F_k , involves checking if $F_k \wedge T \wedge c \Rightarrow c'$ holds. If the implication does not hold, then c is not inductive relative to F_k . In the original method of generalization described above, this means that s cannot be generalized to c , and generalization proceeds without dropping l .

It could be the case that the reason that the query $F_k \wedge T \wedge c \Rightarrow c'$ is unsatisfiable because F_k is too broad an approximation, similarly to why a consecution query at F_k might fail. As with consecution queries, discovering a new clause that can be conjoined to F_k may allow the queries that check for relative induction to succeed, and the discovery of this clause can be directed by a counterexample extracted from the SAT-solver after querying $F_k \wedge T \wedge c \Rightarrow c'$.

The counterexample state in this case is called a *counterexample to generalization* (CTG), and proving the negated CTG to be true at frame F_k allows s to be generalized to c .

Chapter 3

Implementation

Briefly mention sections in the chapter and the example models written in AIGER and BLIF formats.

3.1 Parser

The parser component parses both ASCII or binary-formatted AIGER files, assuming the new format is used (because all old format AIGER files are also new instances of the new format). The justice properties and fairness constraints are ignored by the parser, as they are not used by the model checker.

Both the `Parser.AigerParser` module that implements the parser in Haskell and the `Parser.AigerTools` module that calls the Aiger Utilities' parser's functions parse the AIGER file into the `Model` data structure in `Parser.AigModel`, which stores the components specified in the AIGER file.

3.1.1 Model

More specifically, the `Model` data structure stores the number of variables and the number of inputs. It also stores as a list of literals the outputs, bad states, and invariant constraints. The data structure also stores latches and AND gates as lists of lists of literals. I discuss the representation of literals, latches, and AND gates below.

Literals are represented by a `Lit` data structure in `Parser.AigModel`, which instead of representing a positive literal x as $2 \times x$ and negative literal $\neg x$ as $2 \times x + 1$, represents positive literal x as `Lit` $x - 1$ and negative literal $\neg x$ as `Neg` $x - 1$. The subtraction by 1 allows variable indices to start at 0 rather than 1, since starting at 1 is unnecessary because the `Lit` data structure also contains the separate `Bool` constructor for representing the values `True` and `False`.

Latches and AND gates are represented by three-element literal lists. For latches, the first element gives the variable name of the latch (as a positive literal), the second gives the next-state literal, and the final element gives the initial state of the latch. For AND gates, the first element gives the variable name of the AND gate (as a positive literal), and the next two elements give the literals whose values are taken as inputs to the AND gate.

3.2 Minisat Interface

MiniSat serves as the SAT solver for this implementation of the IC3 algorithm. Because the Haskell Foreign Function Interface cannot interface with C++ directly, the interface to the MiniSat SAT solver is composed of a C wrapper for the relevant MiniSat functions and classes and a Haskell interface to the C wrapper.

3.2.1 Relevant MiniSat Functions

To solve a SAT query, MiniSat creates an instance of a `Solver` object, which contains a set of variables, sets of clauses represented by `VecLit` instances that must be satisfied each SAT query, a model and a conflict vector. The `solveWithAssumps` function makes a SAT query that must satisfy all of the clauses in the `Solver` as well as all the literals supplied in the assumption `VecLit`.

If there has been at least one query made of the `Solver` object, and the query was satisfiable, the `Solver`'s `model` variable points to a set of variable assignments for that SAT query. If there has been at least one query made of the `Solver` object, and the query was unsatisfiable, the `Solver`'s `conflict` variable points to a set of literals that contains the assumed literals that caused the query to be unsatisfiable.

This model checker uses instances of `SimpSolver`, a subclass of the `Solver` class that does simplification and returns full assignments.

3.2.2 C Wrapper

Much of the C wrapper is straightforward: every MiniSat class is replaced with a C type, and every MiniSat function is replaced with a function with an `extern C` function that calls the MiniSat C++ function. I also added an additional `result` struct to allow for the results of a SAT query to be returned from a single function call. The struct contains not only the result of the SAT query, but also pointers to the model and conflict vector (if any) of the `Solver`. The wrapper function for `solveWithAssumps` returns a pointer to a `result` struct rather than just whether or not the query was satisfiable.

3.2.3 Haskell Interface

The Haskell interface makes use of the Haskell FFI as well as the `hsc2hs` preprocessor for handling the `result` struct.

Using just the Haskell FFI for calling the C functions does not provide a sufficient abstraction for use by the rest of the model checker. I wrote further functions to allow for a more natural interface to MiniSat, making use of `unsafePerformIO` to have the functions return values outside the `IO` monad.

Many of the functions and datatypes in the interface are analogous to functions and structs in the C wrapper and C++ implementation of MiniSat. For example, the `Solver` datatype is an analogue to the MiniSat `Solver` object, and itself contains a pointer to an instance of a MiniSat `Solver` object. Similarly, functions such as `solveWithAssumps`

work analogously to the C wrapper's `solveWithAssumps`, returning a `Result` that contains whether or not the query was satisfiable and the model or conflict vector (if any).

The information kept in a `Result` is taken directly from the `result` returned by the C Wrapper functions. I used the `hsc2hs` preprocessor to help handle pointer offsets when unmarshalling from the C struct. Beyond straightforward unmarshalling, some additional work to convert from the MiniSat representation of literals to the model checkers representation of literals was necessary.

3.3 Hardware Models

3.3.1 Representation

Literals

The `Lit` data structure in `Model.Model` gives the representation for literals in the model checker. The `Var` constructor gives positive current-state (unprimed) literals, the `Neg` constructor gives negative current-state literals, and the `Var'` and `Neg'` constructors respectively give positive and negative next-state (primed) literals.

Transition Systems and Safety Properties

The representation of transition systems and the safety property for the model checker to check are both encompassed in the `Model` data structure in `Model.Model`. The inputs i and state variables x in the transition system $T(i, x, I, T)$ are not distinguished, and the total count of variables is kept in `vars`. Clauses that specify the initial state I are kept in `initial`. The transition relation T is captured by `transition`, a list of both clauses that specify latches and clauses that specify AND gates. The literal that gives the safety property is given by `safe`.

3.3.2 Construction

The `Model.Model` module contains functions to convert the `Model` data structure in `Parser.AigModel` into the hardware model representation used by the model checker.

3.4 Model Checking

3.4.1 Frames

The data structure `Frame` represents frames in the IC3 algorithm. Along with the set of clauses (represented by a list of literals), a `Frame` also includes a `Solver`, which contains at least all the clauses in the frame's set of clauses. The `Solver` may also contain the `transition` clauses for the hardware model.

3.4.2 Initiation

The initiation query $I \Rightarrow P$ is an implication, but a MiniSat **Solver** can only solve queries given in conjunctive normal form (CNF), where each disjunct is one of the clauses passed to the solver (assumptions passed to the solver can be taken as a set of single-literal clauses that are also part of the conjunction). As a result, the representation for the query $I \Rightarrow P$ for a frame I and a clause P makes use of the logical equivalence between $I \Rightarrow P$ and $\neg(\neg P \wedge I)$.

Using the fact that the formula $\neg(\neg P \wedge I)$ is true iff $\neg P \wedge I$ is unsatisfiable, and deMorgan's laws gives the following implementation of the initiation query:

```
initiation :: Frame -> Clause -> Bool
initiation = not (satisfiable (solveWithAssumps (solver f) (map neg prop)))
```

3.4.3 Consecution

Similarly to how the implication in the initiation query is converted to an equivalent logical expression that renders a CNF query to a MiniSat **Solver** to determine the satisfiability of the query, the consecution query's implementation uses the logical equivalence of $F_k \wedge T \Rightarrow P'$ and $\neg(\neg P' \wedge F_k \wedge T)$. Again, along with deMorgan's laws, this yields the implementation of the consecution query (where it is assumed that the **Frame's Solver** contains the **transition** clauses of the **Model**).

3.4.4 Counterexamples to Induction

When the consecution query $F_k \wedge T \Rightarrow P$ in **prove'** fails, then a call to the function **nextCTI** gives a cube (a conjunction of literals) whose current-state literals give relevant CTI for the query.

Basic

In the most basic implementation of the IC3 algorithm, **negCTI** asks for a model (i.e. the set of true literals) for the satisfiable query $\neg P \wedge F_k \wedge T$. The current-state literals are then extracted from the model in **prove'** and passed as one of the parameters to **proveNegCTI**.

The function **proveNegCTI** begins with a query

3.4.5 Propagation

Basic

Subsumed clauses

3.4.6 Generalization

Simple

Minimal Inductive Subclauses

Counterexamples to Generalization

Chapter 4

Evaluation

4.1 Performance Impact of Improvements

Discuss performance comparison of the naive implementation of the model checker and the final implementation of the model checker.

4.2 Performance Comparison

Discuss performance comparison of final implementation with IC3 reference implementation, taking into account differences between the implementations.

Chapter 5

Conclusion

5.1 Summary

Summarize the project and accomplishments

5.2 Further extensions

Mention further extensions that could be implemented.

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Appendix A

Project Proposal

Introduction and Description of the Work

Model checking is one way of assessing whether or not a hardware or software system has certain properties. For example, model checkers can be used to check systems for safety properties by finding examples of states that violate the properties or by proving that all states have the properties.

Explicit-state model checking can be infeasible for systems with a large number of states, but symbolic model checking, which represents states and the transition relation between them as boolean expressions, can handle more states. Symbolic model checking initially relied on the efficient representation of boolean expressions through binary decision diagrams (BDDs), but BDDs can still consume a large amount of space, and finding an ordering for BDD variables that keeps the BDDs small can become costly [2].

Symbolic model checking techniques that rely on SAT solvers provide an alternative to BDD-based approaches. SAT-based approaches include bounded model checking [2] and k -induction [8], but both of these approaches involve unrolling the transition relation, which can lead to long SAT solver queries.

IC3 [4] is a more recently developed SAT-based algorithm for the symbolic model checking of safety properties. Instead of unrolling the transition relation and considering entire paths, IC3 maintains a set of frames F_0, \dots, F_k , where each frame F_i is an overapproximation of the set of states reachable in at most i steps, and considers at most one step of the transition relation from a particular frame at a time. As a result, IC3 can find inductive strengthenings that tend to be smaller and more convenient than those found by BMC-based techniques such as k -induction, which finds strengthenings that are the negations of spurious counterexample paths [8], and the SAT queries that IC3 makes tend to be simpler [5].

This project focuses on implementing a symbolic model checker for verifying safety properties of hardware. The model checker will include a new implementation of the IC3 algorithm in Haskell, which will make use of an existing SAT solver.

Starting Point

I begin the project with some experience programming in Haskell from a summer internship and no experience with model checking or using a SAT solver. I have informally acquired some knowledge about model checking to formulate this project idea.

Substance and Structure of the Project

The project aims to implement a hardware model checker that takes its inputs in AIGER format and queries the MiniSat SAT solver.

The structure of the project can be broken down into the following components:

1. **Parsing AIGER format** The model checker takes its inputs in AIGER format and will, as a result, require an AIGER parser. The AIGER format is fairly simple and hand-coding a parser for it should be suitable.
2. **Interfacing with MiniSat** The model checker will be using the MiniSat SAT solver, so an API that allows the model checker to query MiniSat will be required.
3. **Implementing the IC3 algorithm** The main aspect of the project is the implementation of the IC3 algorithm. The implementation will largely be based on the algorithm as described in [4, 5].
4. **Evaluating the model checker** The model checker will be evaluated by measuring its performance on checking examples. Though the project does not focus greatly on the efficiency of the implementation, it may still be interesting to see how the performance of this IC3 implementation in Haskell compares with other implementations. As a result, benchmarks taken for the model checker will be compared with further benchmarks taken for Aaron Bradley's reference IC3 implementation, which is implemented in C++. Given that the reference implementation takes its inputs in AIGER format and also uses MiniSat, the benchmarks should provide a means to compare the IC3 implementations specifically.
5. **Writing the dissertation**

Possible Extensions

If the aforementioned aspects of the project are completed, carrying out the following extensions could be possible:

- Interfacing with other SAT solvers, and possibly performing additional benchmarking; comparing the performance of the model checker when used with different SAT solvers may be of interest since the performance of IC3 implementations tend to vary considerably depending on the characteristics of the underlying SAT solver.
- Model checking properties of real hardware as a case study.
- Implementing abstraction-refinement as described in [13].

Success Criteria

The project will be a success if the following have been completed:

- The AIGER parser has been implemented.
- The MiniSat interface has been implemented.
- The IC3 algorithm has been implemented.
- The model checker should be able to solve some small examples.

Timetable: Workplan and Milestones

1. 16 October 2015 – 28 October 2015

Preliminary reading. Get familiar with the AIGER format, MiniSat and relevant Haskell libraries and tools for implementing the components of the project.

2. 29 October 2015 – 4 November 2015

Write an AIGER format parser.

Milestone: Parser completed. Relevant information from AIGER files can be extracted.

3. 5 November 2015 – 18 November 2015

Implement a MiniSat interface.

Milestone: MiniSat interface completed, enabling the model checker to use MiniSat to solve SAT problems.

4. 19 November 2015

Begin implementing the IC3 algorithm.

5. Michaelmas vacation

Continue implementing the IC3 algorithm.

6. 14 January 2016 – 27 January 2016

Write progress report. Finish implementation of the IC3 algorithm.

Milestones: Progress report completed. Working implementation of the model checker completed.

7. 28 January 2016 – 10 February 2016

Measure and compare this IC3 implementation's performance and the reference implementation's performance.

Milestone: Evaluation completed.

8. 11 February 2016 – 11 March 2016

Write the main parts of the dissertation.

Milestone: Finished writing main parts of dissertation: introduction, preparation, implementation and evaluation chapters.

9. Easter vacation

If necessary, use this time for catching up. Otherwise, work on extensions, starting with interfacing with other SAT solvers. Finish writing dissertation.

Milestones: All implementation and evaluation completed. Draft dissertation completed.

10. 21 April 2016 – 4 May 2016

Proofread and edit dissertation as necessary.

Milestone: Dissertation ready for submission.

11. 5 May 2016 – 13 May 2016

Time left for catching up in case any delays have occurred in the completion of any milestones.

Milestone: Dissertation submitted.

Resources Required

For the project I will mostly make use of my laptop, which runs OS X 10.8. I accept full responsibility for this machine and I have made contingency plans to protect myself against hardware and/or software failure. If my main computer fails, I will use MCS computers. I will use GitHub for backup and git for revision control.

I will also be using:

- AIGER utilities, available <http://fmv.jku.at/aiger/>
- MiniSat, available <https://github.com/niklasso/minisat>
- Models from the Hardware Model Checking Competition, such as those available <http://fmv.jku.at/hwmcc10/>
- Aaron Bradley's Reference IC3 implementation, available <https://github.com/arbrad/IC3ref>