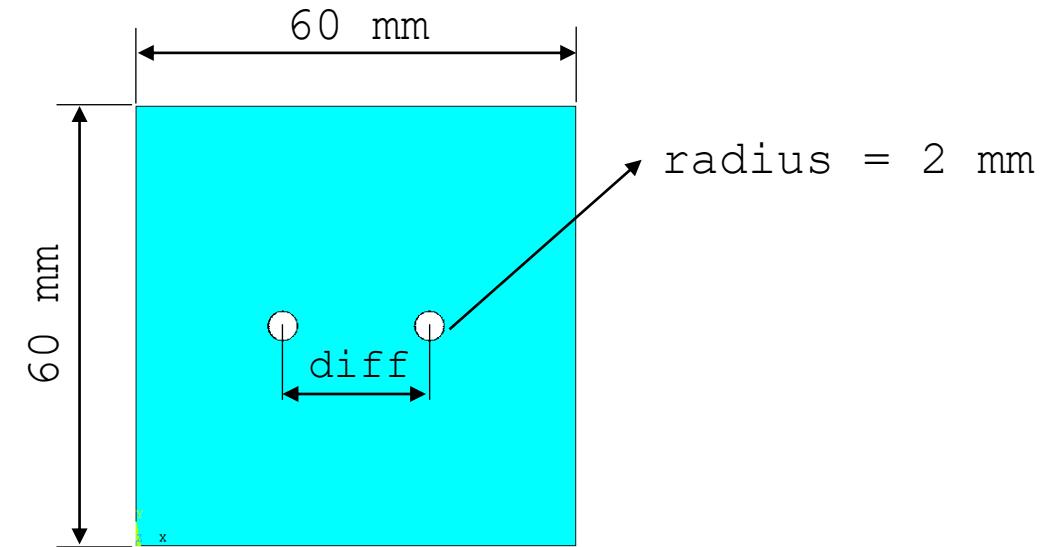
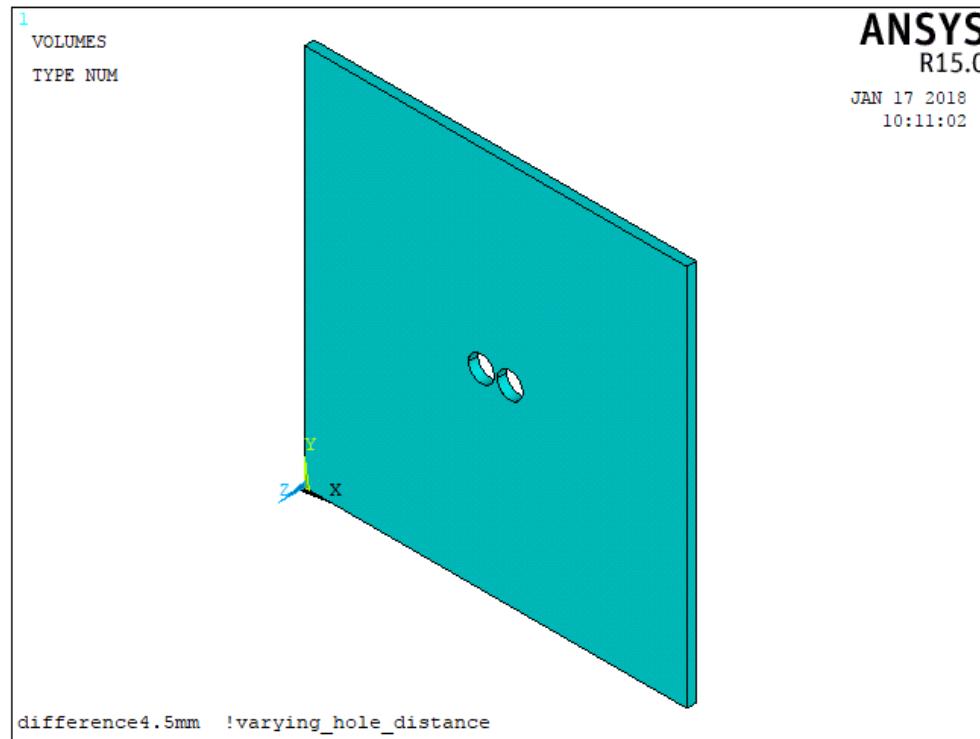


Varying hole distance

problem description

Two Circular Holes in a Plate

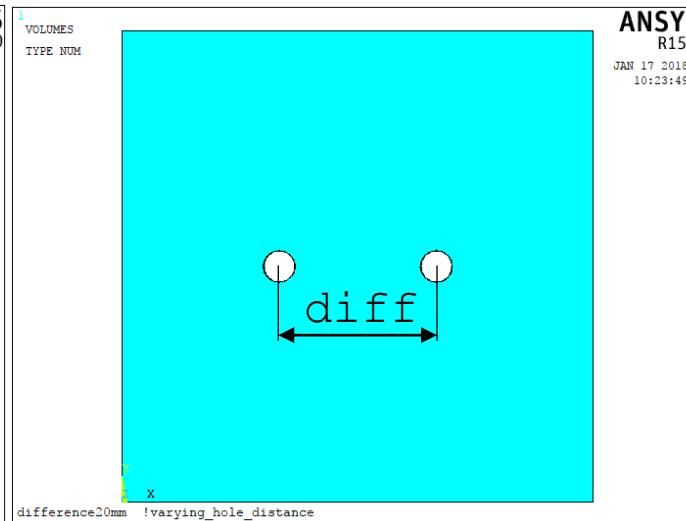
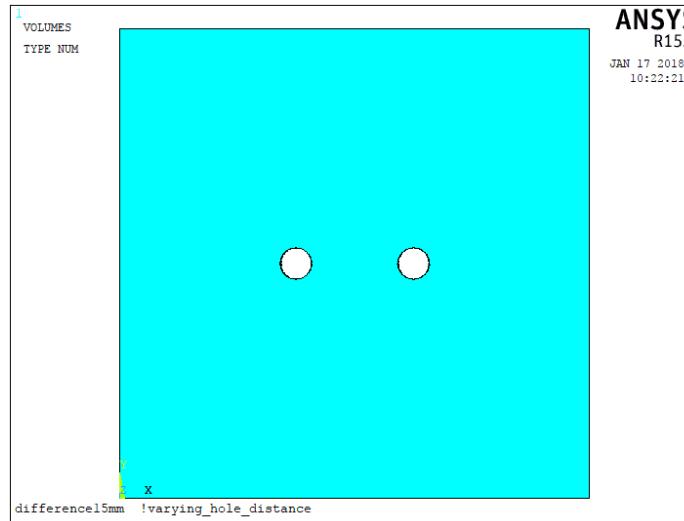
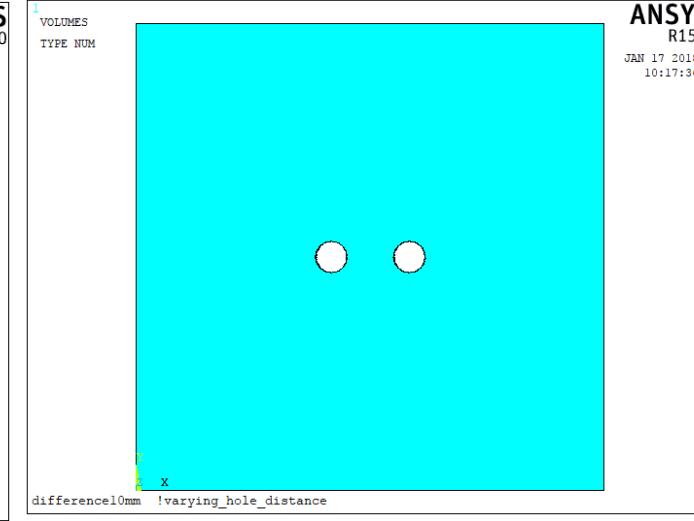
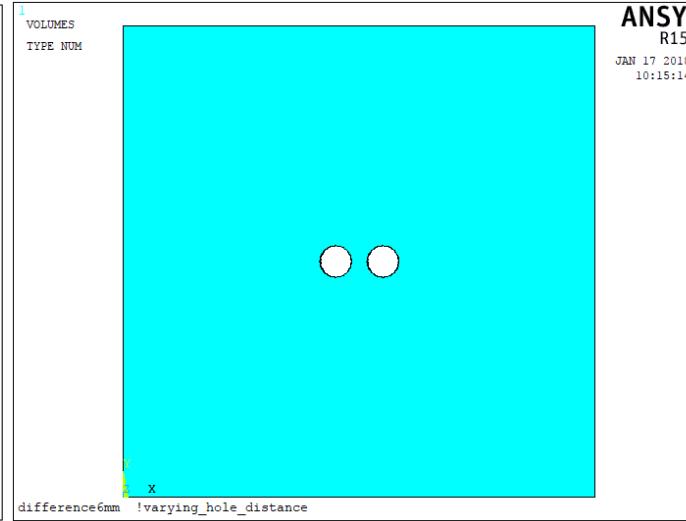
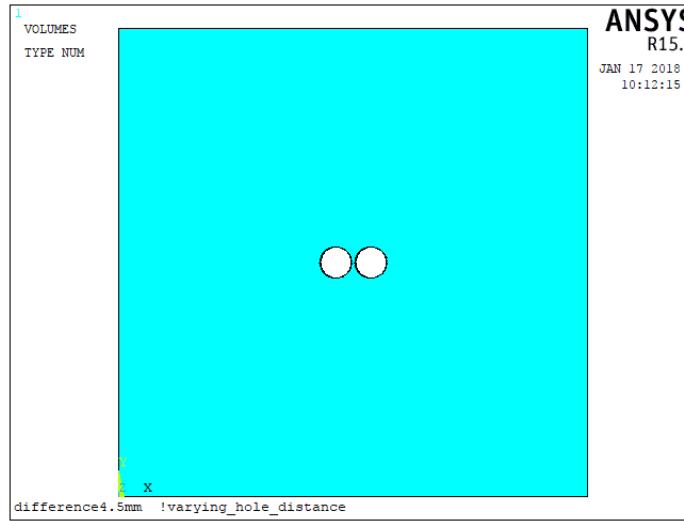


plate_thickness = depth = 1.5 mm

"through hole"

- Varying the hole distance

Simulation Goal



inicial = 4.5 !mm

final = 20 !mm

incr = 0.5 !mm

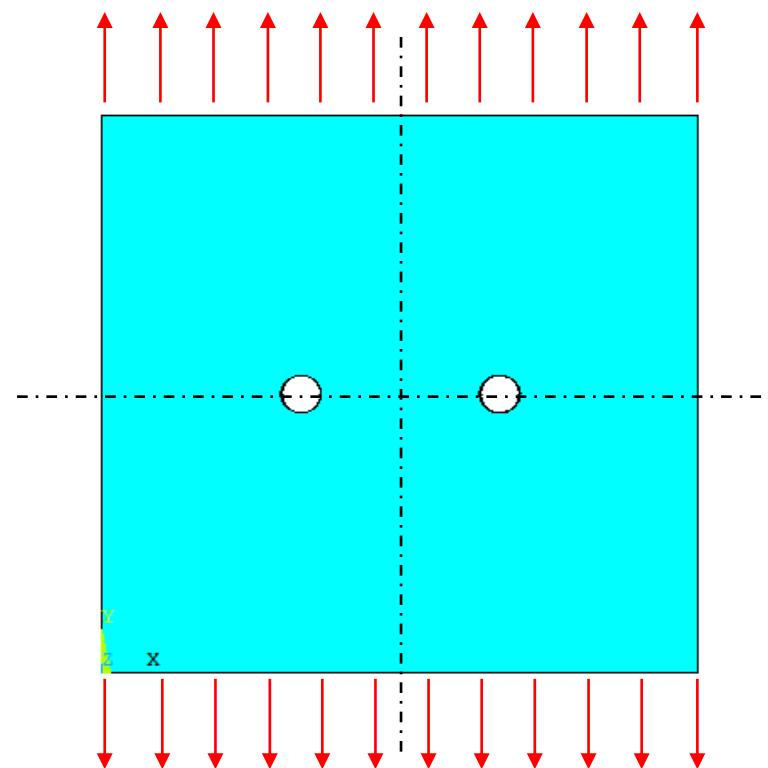
*do,diff,inicial,final,incr

...

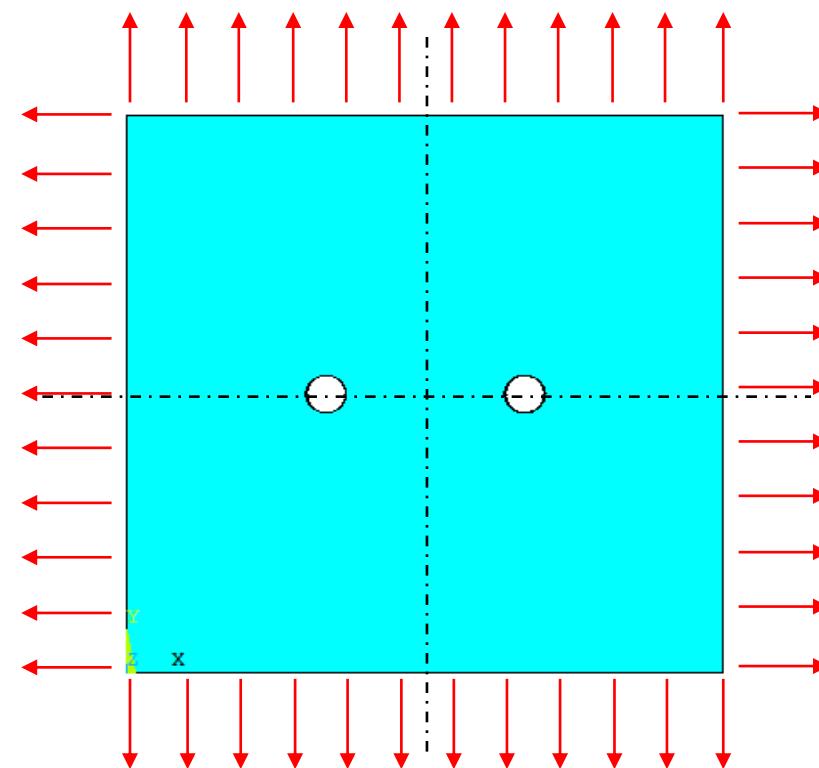
...

*enddo

Types of Loads for simulation

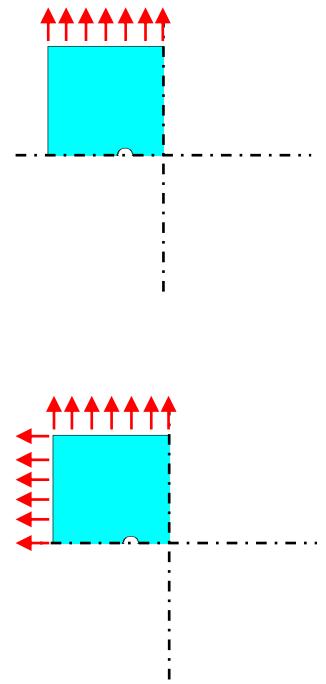
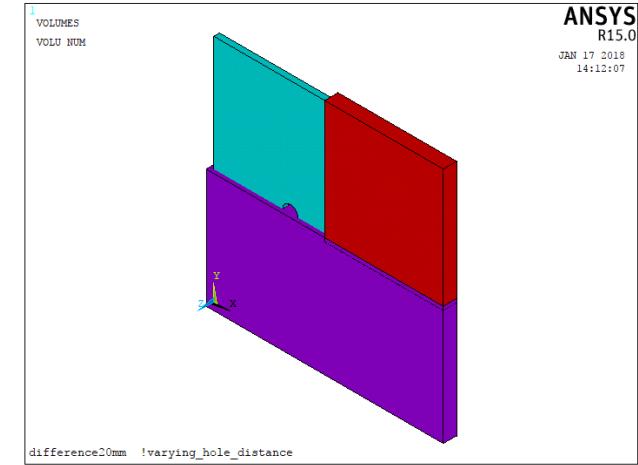
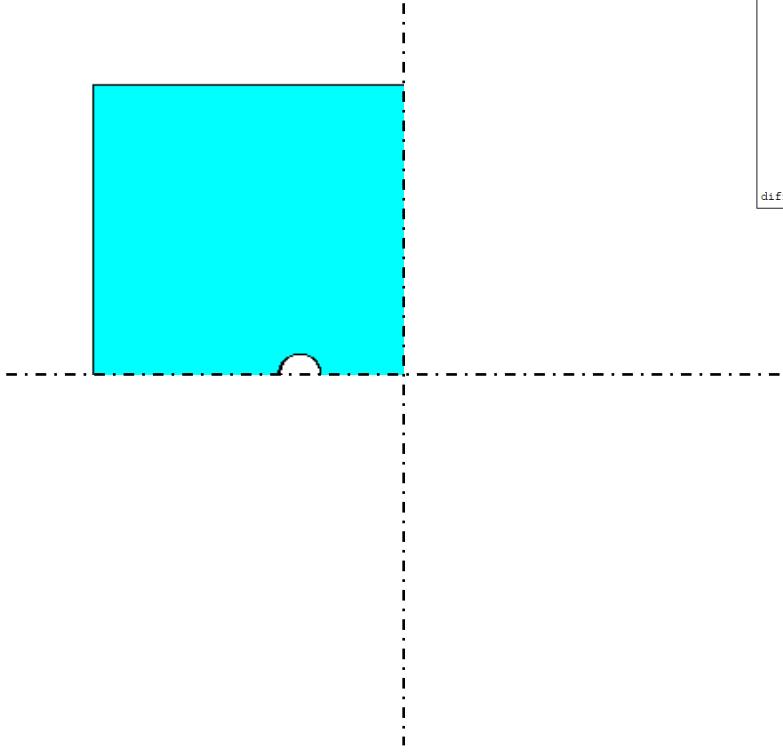
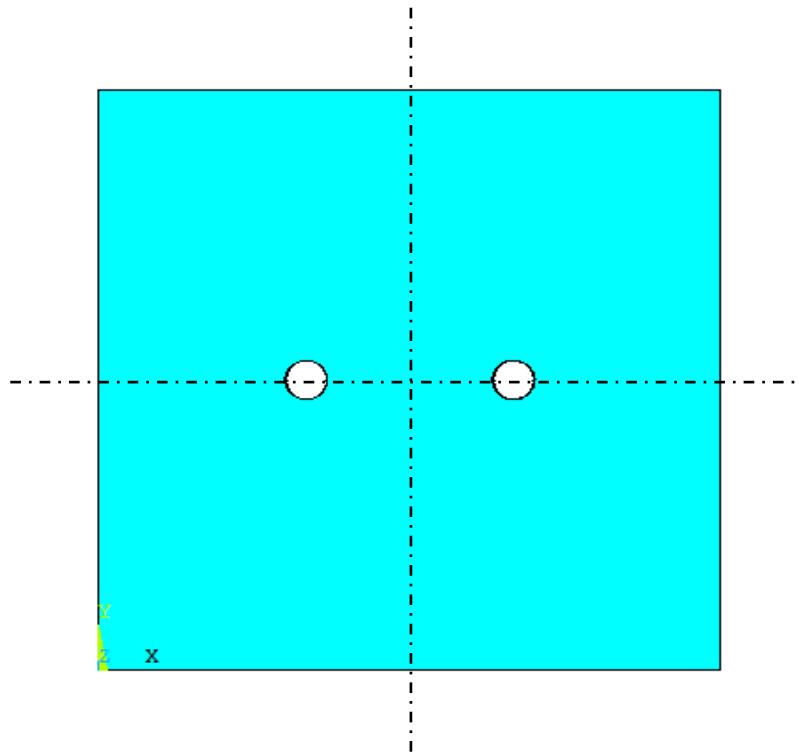


(a) Uniaxial
Transverse load



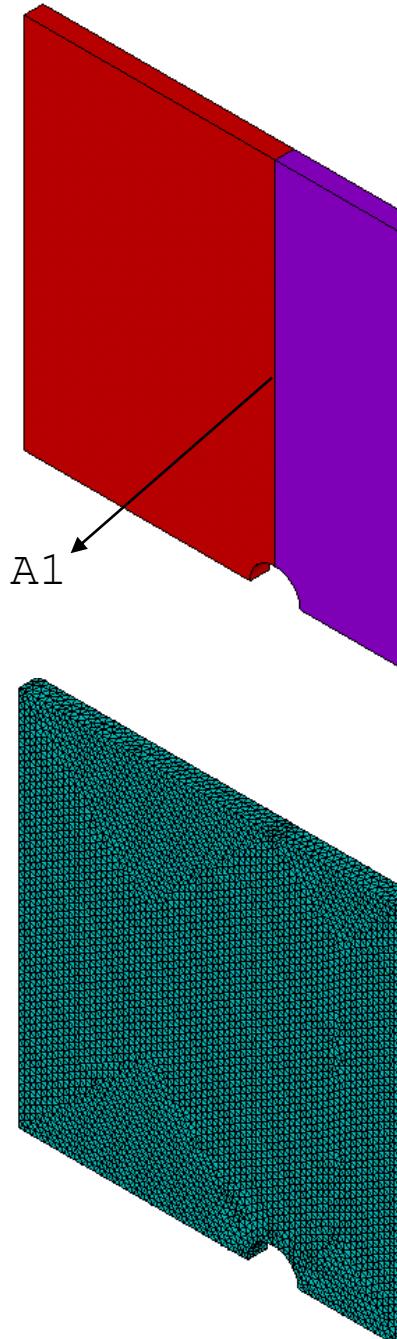
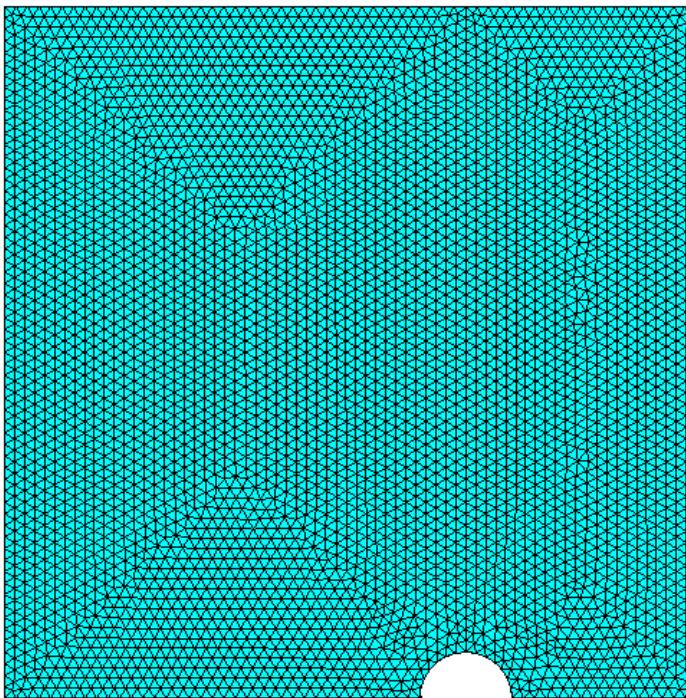
(b) Biaxial load

Symmetry



Mesh

- Due to the interest in the data from the nodes in the common area, A1, two volumes were modeled.



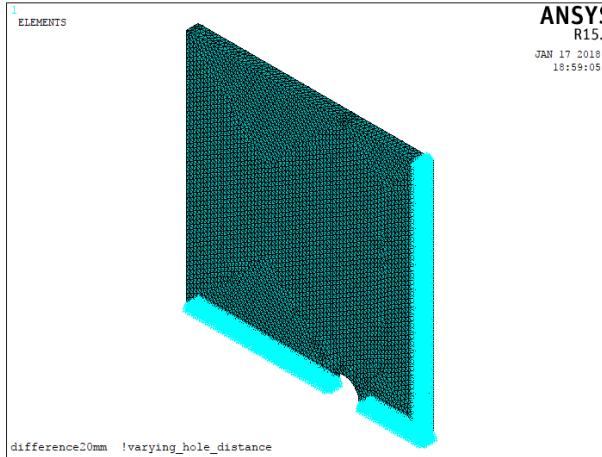
```
! Mesh  
! Selection volumes  
allsel
```

```
! Type element  
et,1,187
```

```
! Element edge  
size= 0.5  
esize,size
```

```
!command  
vmesh,all  
eplot
```

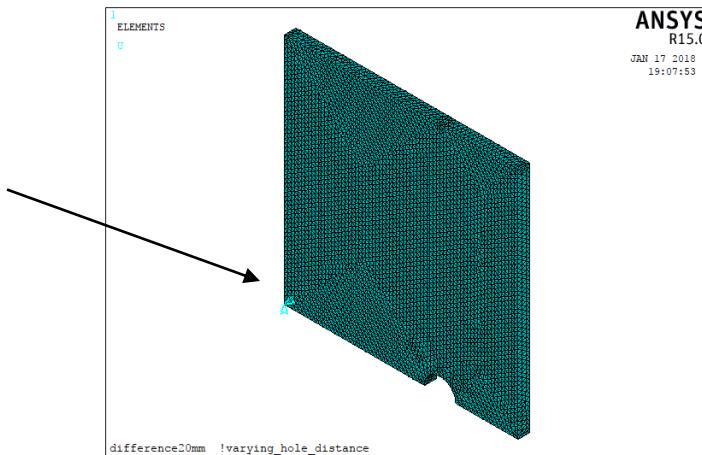
Symmetry and Boundary Conditions



! Symmetry Condition

```
! (cross section X)
asel,s,loc,x,x2/2
nsla,s,1
dsym,symm,x,0
```

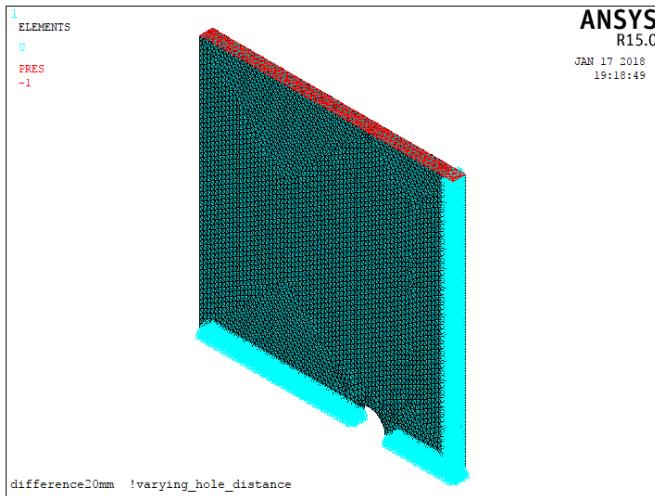
```
! (cross section Y)
asel,s,loc,y,y2/2
nsla,s,1
dsym,symm,y,0
```



! Boundary Condition
allsel

```
ksel,s,loc,x,x1
ksel,r,loc,y,y2/2
ksel,r,loc,z,z1
nslk,s
d,all,uz,0
```

(a) Uniaxial, Transverse load

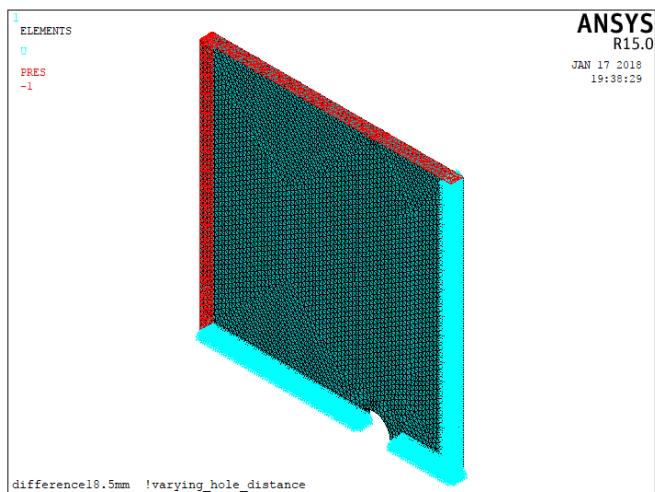


Load Conditions

```
! p = 1 Mpa
```

```
allsel  
asel,s,loc,y,y2  
sfa,all,1,pres,-p  
asel,s,loc,y,y1  
sfa,all,1,pres,-p  
allsel  
lswrite,1
```

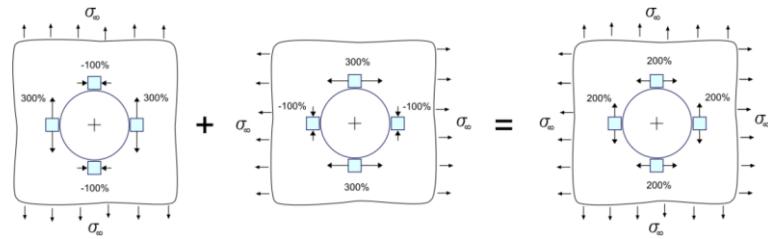
(b) Biaxial load



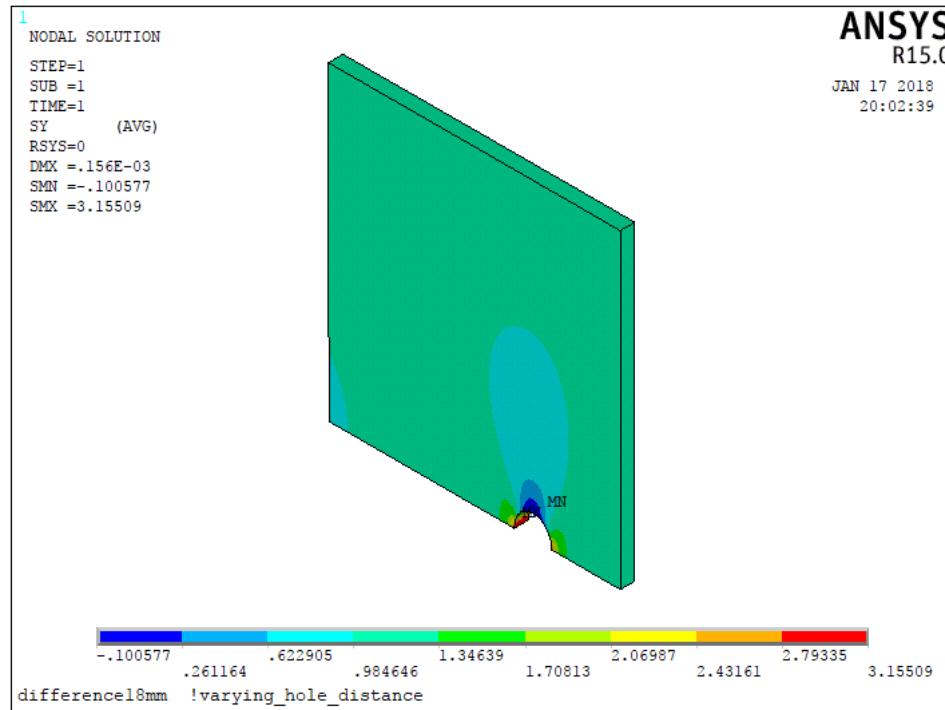
```
allsel  
asel,s,loc,x,x2  
sfa,all,1,pres,-p  
asel,s,loc,x,x1  
sfa,all,1,pres,-p  
allsel  
lswrite,1
```

```
allsel  
asel,s,loc,y,y2  
sfa,all,1,pres,-p  
asel,s,loc,y,y1  
sfa,all,1,pres,-p  
allsel  
lswrite,2
```

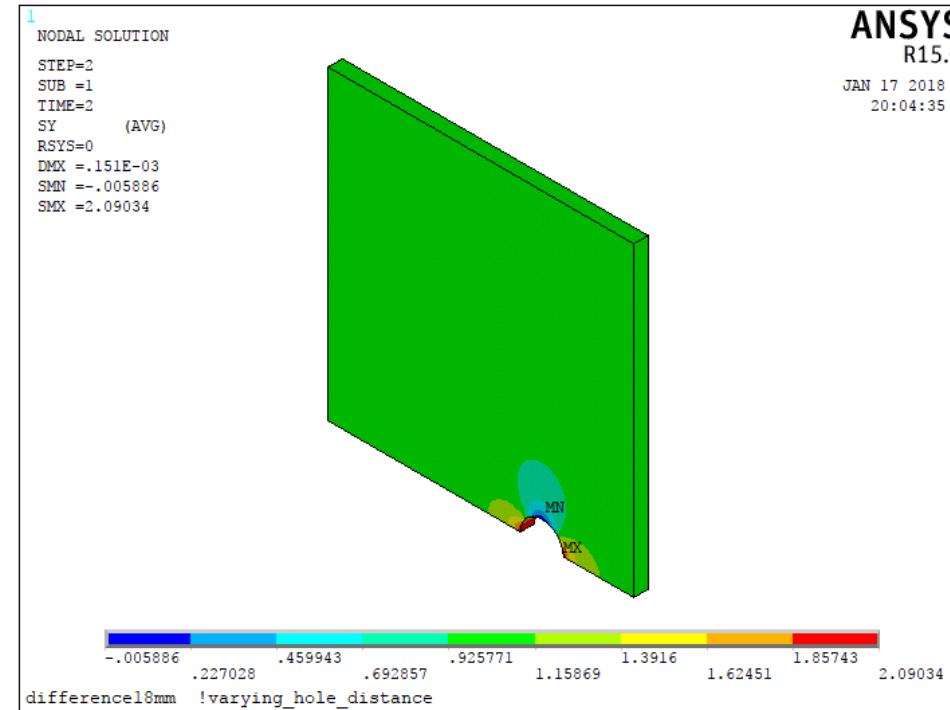
Solution



Theoretical Results



(a) Uniaxial, Transverse load



(b) Biaxial load

```
!cont=1 Uniaxial
!cont=2 Biaxial

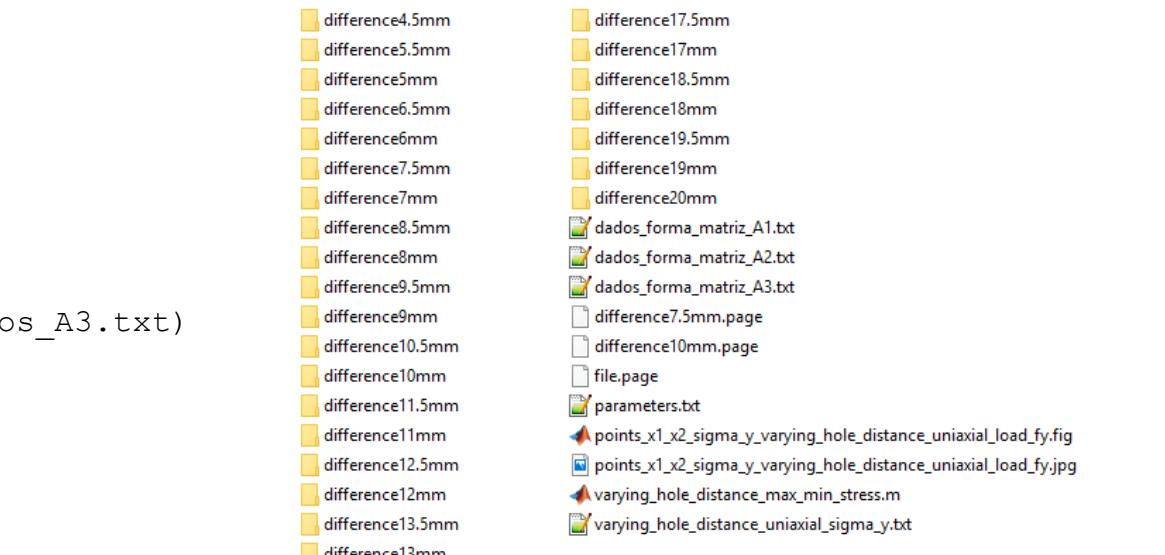
finish
/solu
lssolve,cont
save
/post1
plnsol,s,y
```

Obtaining Data

```
/cwd,wd(1,1)

/input,dados_forma_matriz_A3.txt !(cria arquivo dados_dos_nos_A3.txt)
! ARMAZENAMENTO DE DADOS
*vget,dados_dos_nos_A3(1,1),node,menor_numero_de_nos,loc,x
*vget,dados_dos_nos_A3(1,2),node,menor_numero_de_nos,loc,y
*vget,dados_dos_nos_A3(1,3),node,menor_numero_de_nos,loc,z
*vget,dados_dos_nos_A3(1,4),node,menor_numero_de_nos,u,x
*vget,dados_dos_nos_A3(1,5),node,menor_numero_de_nos,u,y
*vget,dados_dos_nos_A3(1,6),node,menor_numero_de_nos,u,z
*vget,dados_dos_nos_A3(1,7),node,menor_numero_de_nos,s,x
*vget,dados_dos_nos_A3(1,8),node,menor_numero_de_nos,s,y
*vget,dados_dos_nos_A3(1,9),node,menor_numero_de_nos,s,z
*vget,dados_dos_nos_A3(1,10),node,menor_numero_de_nos,s,eqv

/input,dados_forma_matriz_A3.txt
```



The screenshot shows a MATLAB workspace window with several files listed on the right and a preview of a data table on the left.

Files listed on the right:

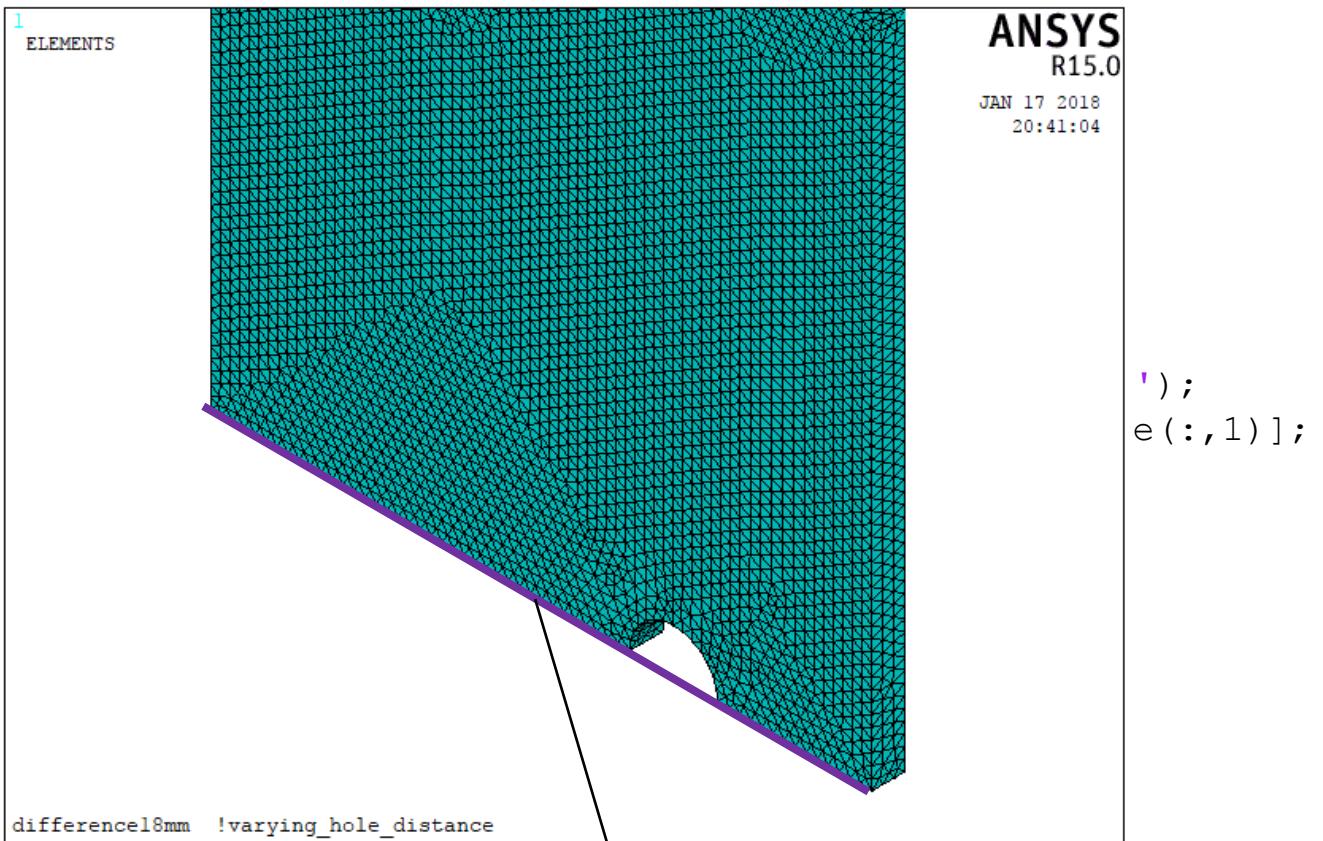
- difference4.5mm
- difference5.5mm
- difference5mm
- difference6.5mm
- difference6mm
- difference7.5mm
- difference7mm
- difference8.5mm
- difference8mm
- difference9.5mm
- difference9mm
- difference10.5mm
- difference10mm
- difference11.5mm
- difference11mm
- difference12.5mm
- difference12mm
- difference13.5mm
- difference13mm
- difference14.5mm
- difference14mm
- difference15.5mm
- difference17.5mm
- difference17mm
- difference18.5mm
- difference18mm
- difference19.5mm
- difference19mm
- difference20mm
- dados_forma_matriz_A1.txt
- dados_forma_matriz_A2.txt
- dados_forma_matriz_A3.txt
- difference7.5mm.page
- difference10mm.page
- file.page
- parameters.txt
- points_x1_x2_sigma_y_varying_hole_distance_uniaxial_load_fy.fig
- points_x1_x2_sigma_y_varying_hole_distance_uniaxial_load_fy.jpg
- varying_hole_distance_max_min_stress.m
- varying_hole_distance_uniaxial_sigma_y.txt

Preview of the data table (dados_dos_nos_A3.txt):

1	1.	23.0000000000	30.0000000000	-1.5000000000	-0.0000135929	0.0000000000	0.0000046365	
2	2.	23.0000000000	30.0000000000	0.0000000000	-0.0000135946	0.0000000000	-0.0000003017	
3	3.	23.0000000000	30.0000000000	-1.2500000000	-0.0000135677	0.0000000000	0.0000038492	
4	4.	23.0000000000	30.0000000000	-1.0000000000	-0.0000135688	0.0000000000	0.0000030711	
5	5.	23.0000000000	30.0000000000	-0.7500000000	-0.0000135642	0.0000000000	0.0000022976	
6	6.	23.0000000000	30.0000000000	-0.5000000000	-0.0000135763	0.0000000000	0.0000015221	
7	7.	23.0000000000	30.0000000000	-0.2500000000	-0.0000135731	0.0000000000	0.0000007464	
8	8.	29.7500000000	30.0000000000	0.0000000000	-0.0000007283	0.0000000000	0.0000000235	
9	9.	29.5000000000	30.0000000000	0.0000000000	-0.00000014559	0.0000000000	0.0000000235	
10	10.	29.2500000000	30.0000000000	0.0000000000	-0.00000021821	0.0000000000	0.0000000233	
11	11.	29.0000000000	30.0000000000	0.0000000000	-0.00000029060	0.0000000000	0.0000000233	
12	12.	28.7500000000	30.0000000000	0.0000000000	-0.00000036268	0.0000000000	0.0000000231	
13	13.	28.5000000000	30.0000000000	0.0000000000	-0.00000043438	0.0000000000	0.0000000230	
14	14.	28.2500000000	30.0000000000	0.0000000000	-0.00000050560	0.0000000000	0.0000000228	
15	15.	28.0000000000	30.0000000000	0.0000000000	-0.00000057625	0.0000000000	0.0000000226	
16	16.	27.7500000000	30.0000000000	0.0000000000	-0.00000064621	0.0000000000	0.0000000223	
17	17.	27.5000000000	30.0000000000	0.0000000000	-0.00000071536	0.0000000000	0.0000000220	
18	18.	27.2500000000	30.0000000000	0.0000000000	-0.00000078355	0.0000000000	0.0000000216	
19	19.	27.0000000000	30.0000000000	0.0000000000	-0.00000085065	0.0000000000	0.0000000211	
20	20.	26.7500000000	30.0000000000	0.0000000000	-0.00000091644	0.0000000000	0.0000000207	
21	21.	26.5000000000	30.0000000000	0.0000000000	-0.00000098074	0.0000000000	0.0000000203	
22	22.	26.2500000000	30.0000000000	0.0000000000	-0.00000104328	0.0000000000	0.0000000195	
23	23.	26.0000000000	30.0000000000	0.0000000000	-0.00000110377	0.0000000000	0.0000000187	
24	24.	25.7500000000	30.0000000000	0.0000000000	-0.00000116187	0.0000000000	0.0000000178	
25	25.	25.5000000000	30.0000000000	0.0000000000	-0.00000121713	0.0000000000	0.0000000165	
26	26.	25.2500000000	30.0000000000	0.0000000000	-0.00000126900	0.0000000000	0.0000000153	
27	27.	25.0000000000	30.0000000000	0.0000000000	-0.00000131680	0.0000000000	0.0000000138	
28	28.	24.7500000000	30.0000000000	0.0000000000	-0.00000135970	0.0000000000	0.0000000115	
29	29.	24.5000000000	30.0000000000	0.0000000000	-0.00000139653	0.0000000000	0.0000000095	

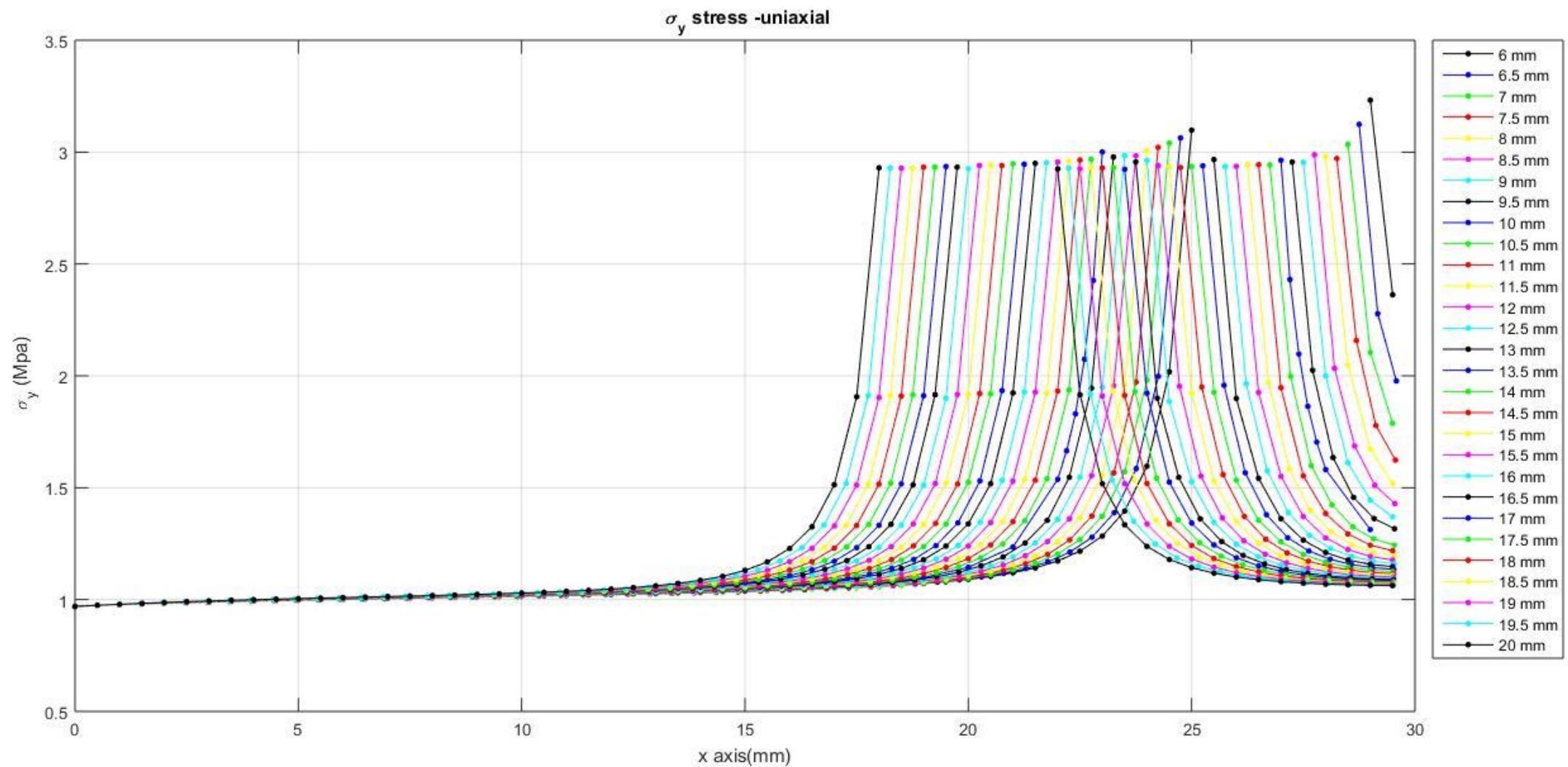
Manipulating Data – Matlab Code

```
diff=[6:0.5:20]; %Point differences to be read
[m n] = size(diff);
r = 2; %hole radius
L = 60;
for a=1:1:n %going through each point difference
    path=['C:\Manasses\varying_hole_distance\',c
    nome='dados_dos_nos_A3.txt';%file name
    [n,xloc,yloc,zloc,ux,uy,uz,sx,sy,sz,se]=tex
    matriz=[n(:,1),xloc(:,1),yloc(:,1),zloc(:,1
    matriz=sortrows(matriz,2); %Deixa os dados
    [i,j]=find(matriz(:,4)~=0.0);%transversal l
    matriz(i,:)=[];%exclui os pontos que não es
    [i,j]=find(matriz(:,9)==0); %finds sigmax v
    matriz(i,:)=[];%exclui os valores de tensão
    [i,j]=size(matriz);
    x1 = ((L-diff(a))/2)-r;
    x2 = ((L-diff(a))/2)+r;
    [i,j]=find(matriz(:,2)==x1|matriz(:,2)==x2)
    [g h] = size(matriz);
    .
    .
    .
```



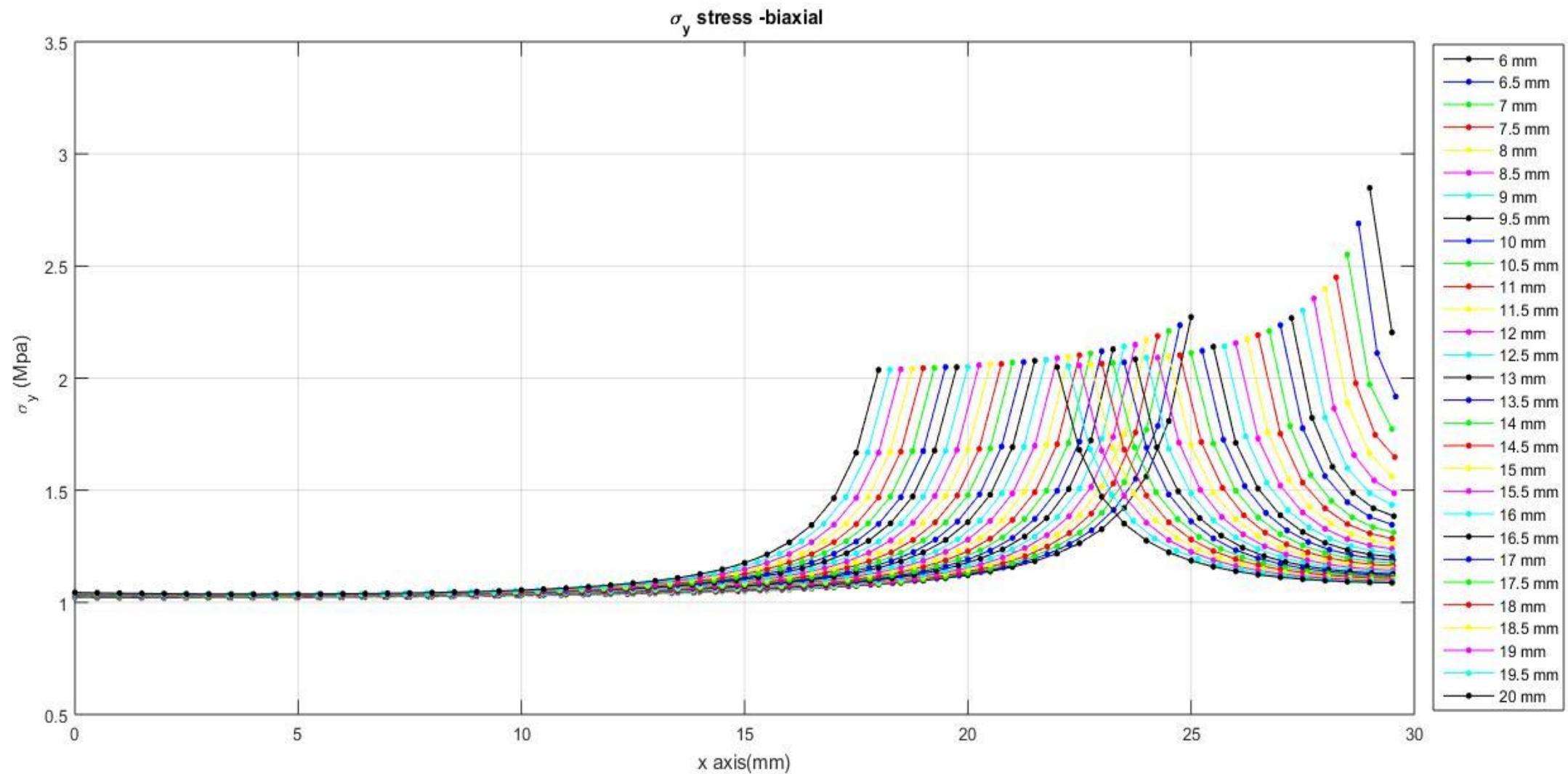
line of interest

Matlab Plots – stress profile



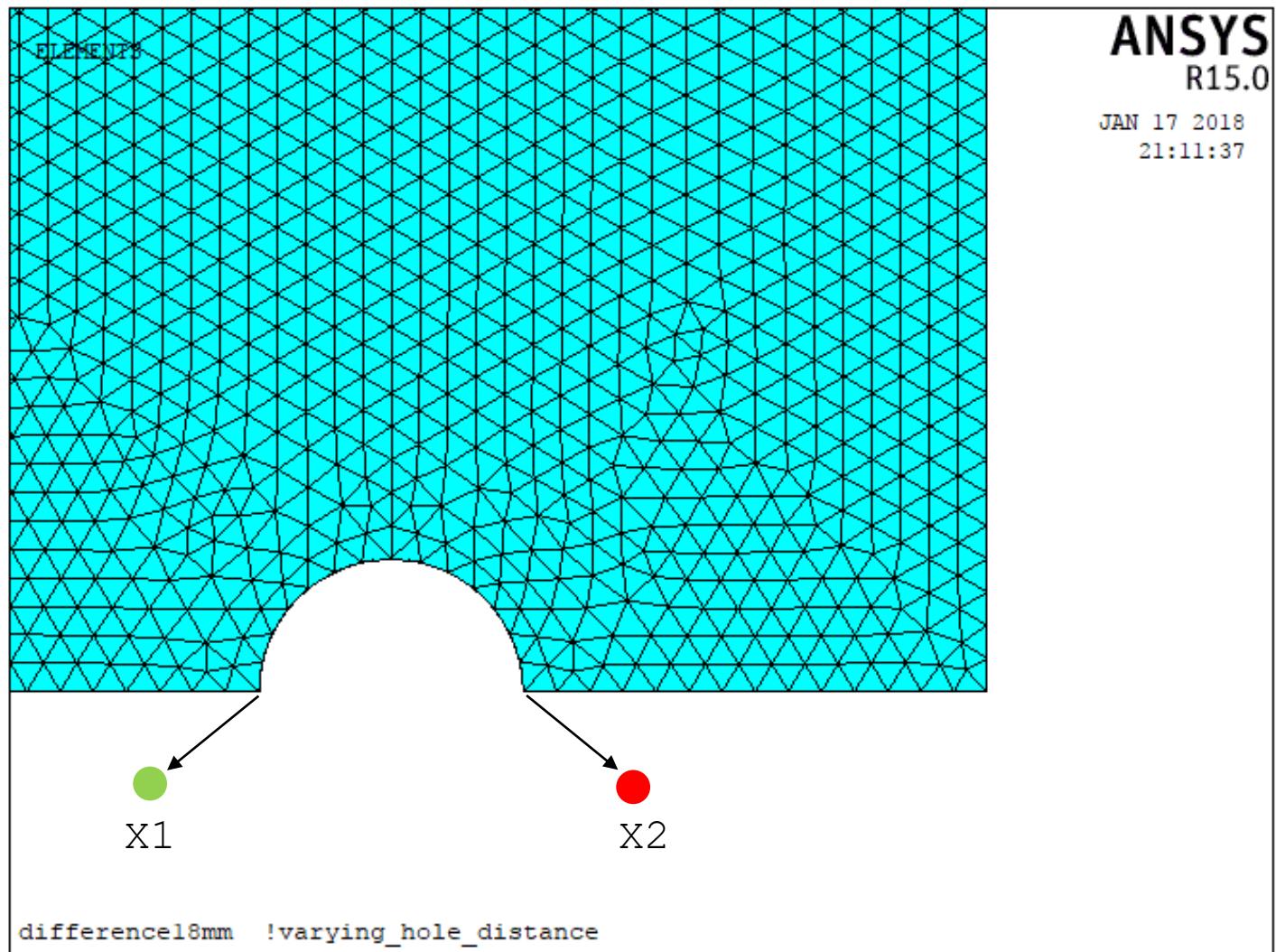
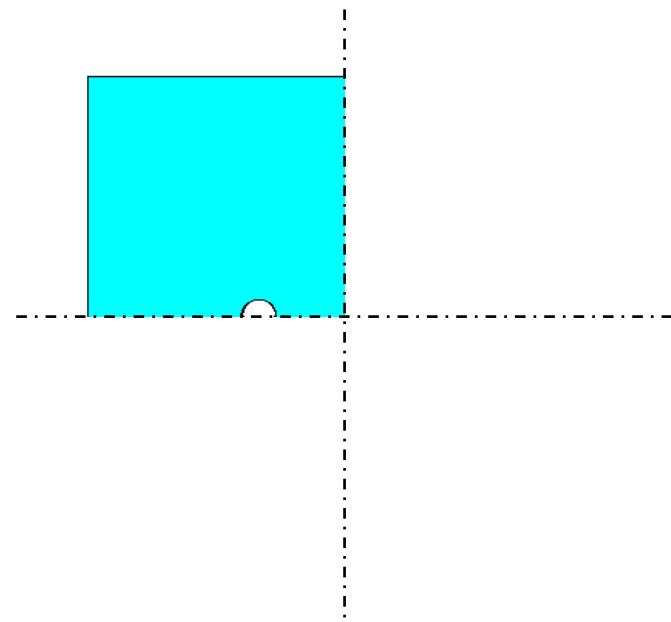
- Varying the hole distance

Matlab Plots – stress profile

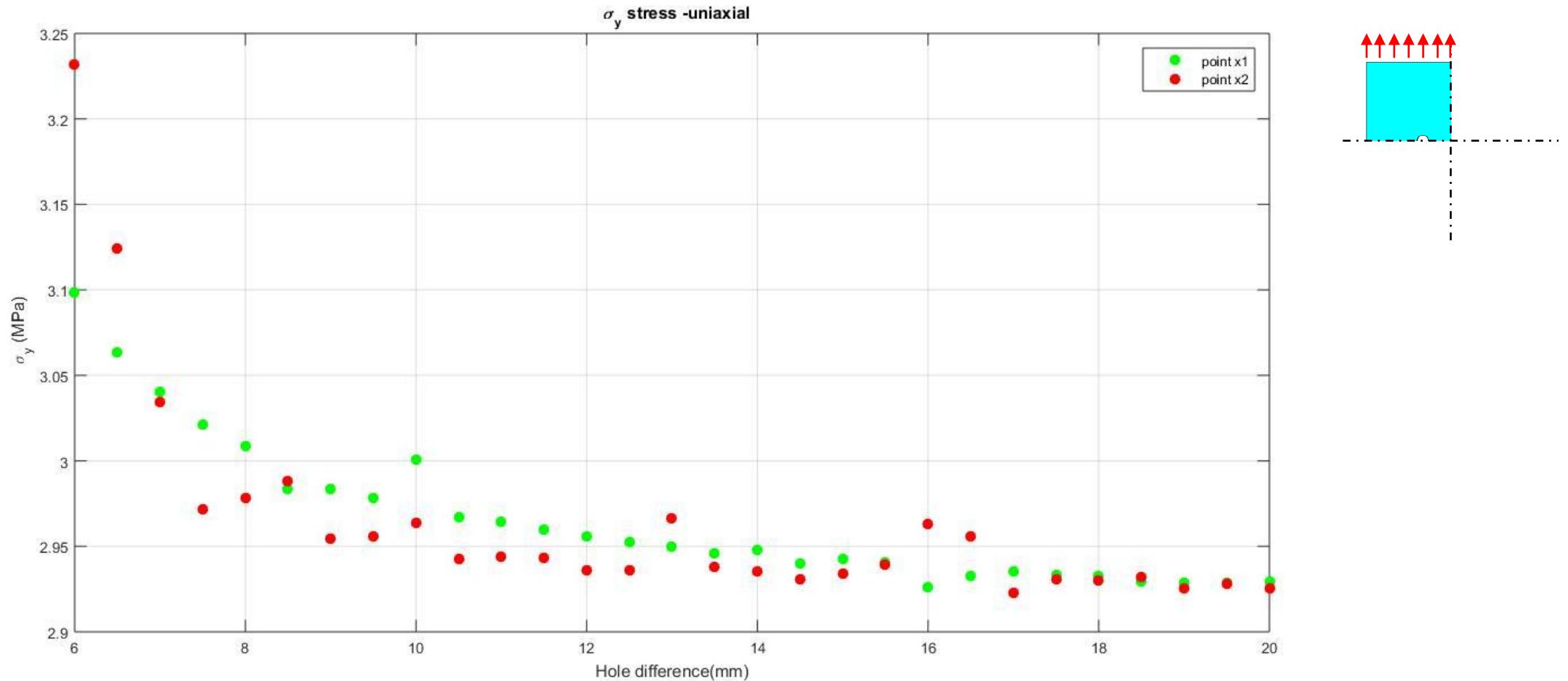


- Varying the hole distance

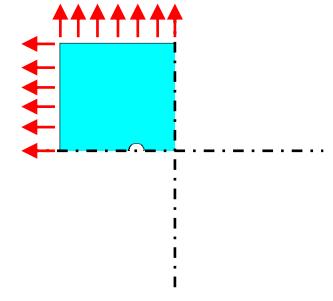
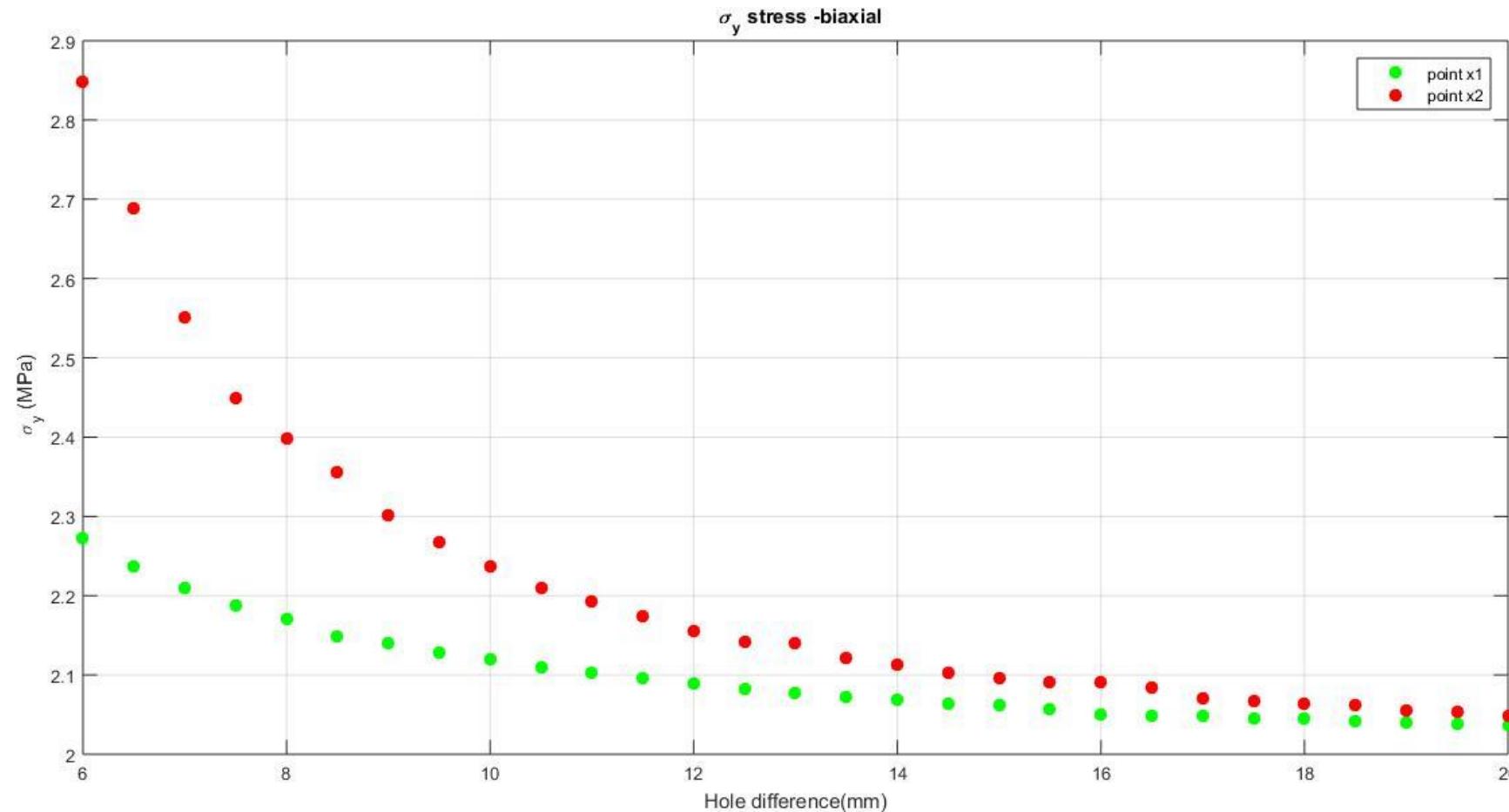
Manipulating Data – Matlab Code



Matlab Plots – stress at points x1, x2

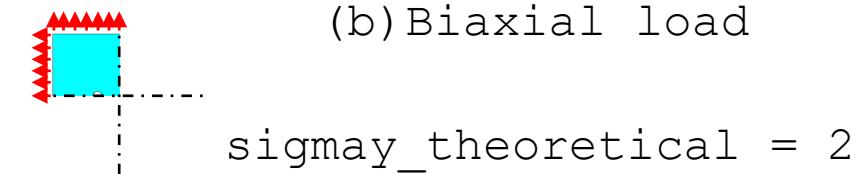
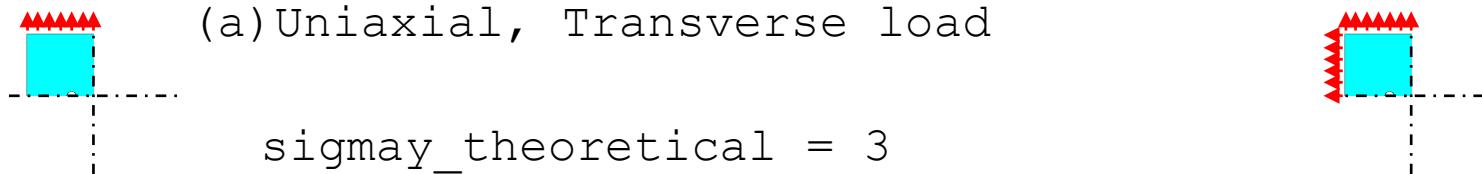
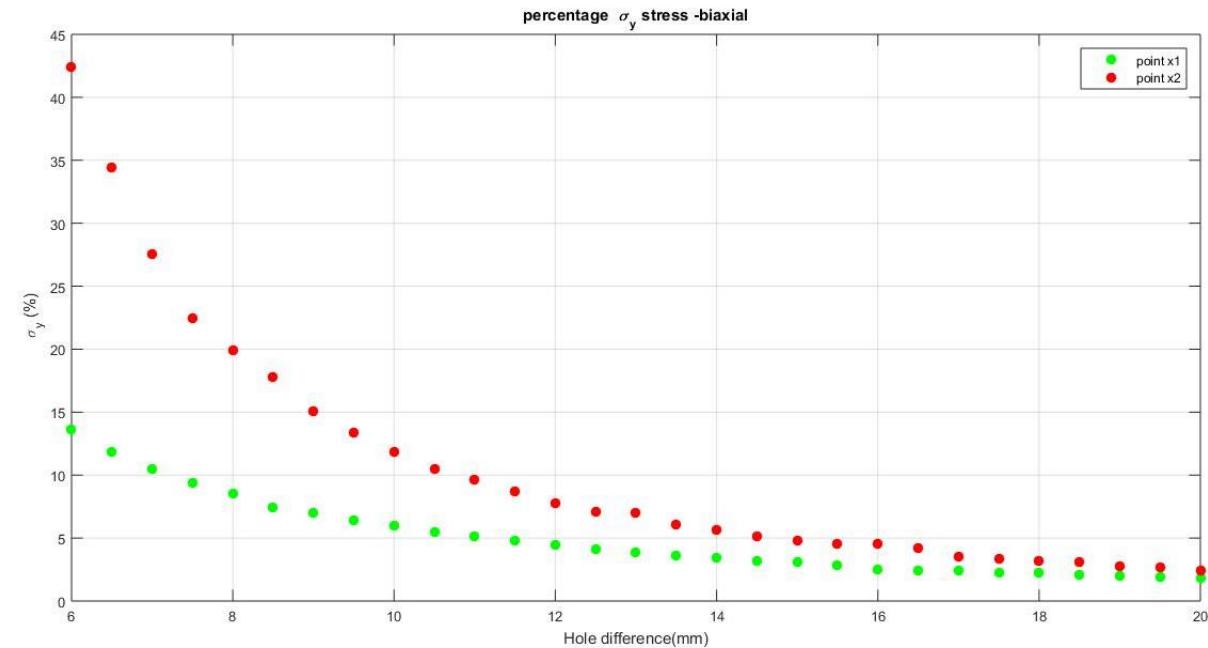
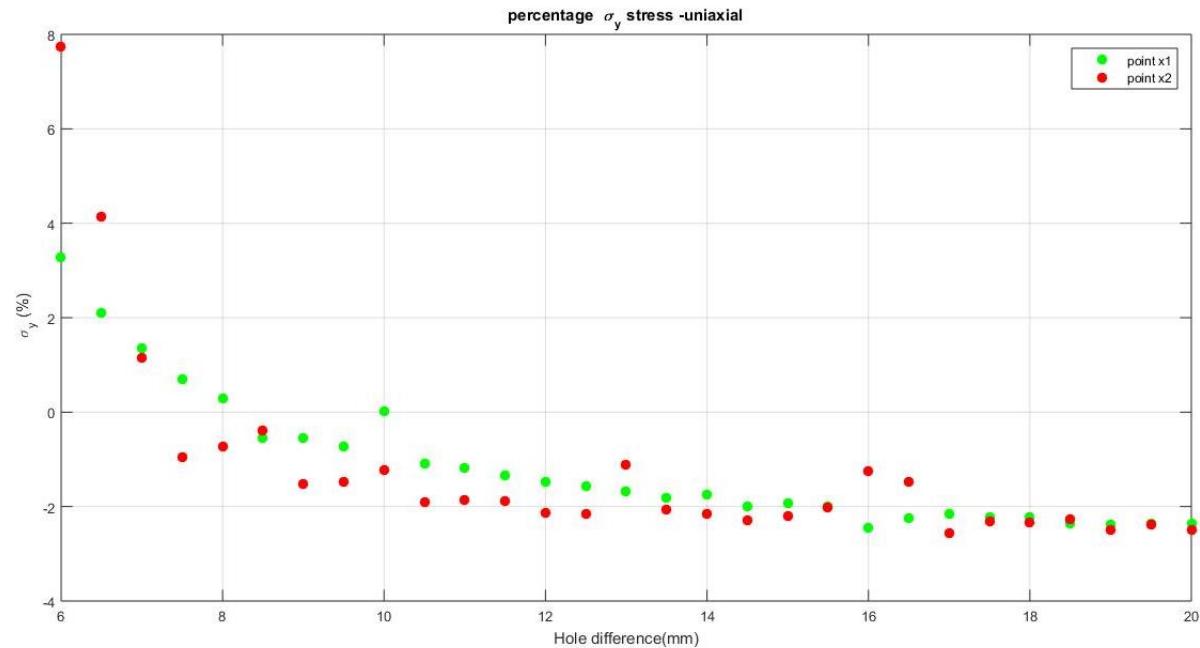


Matlab Plots – stress at points x1, x2

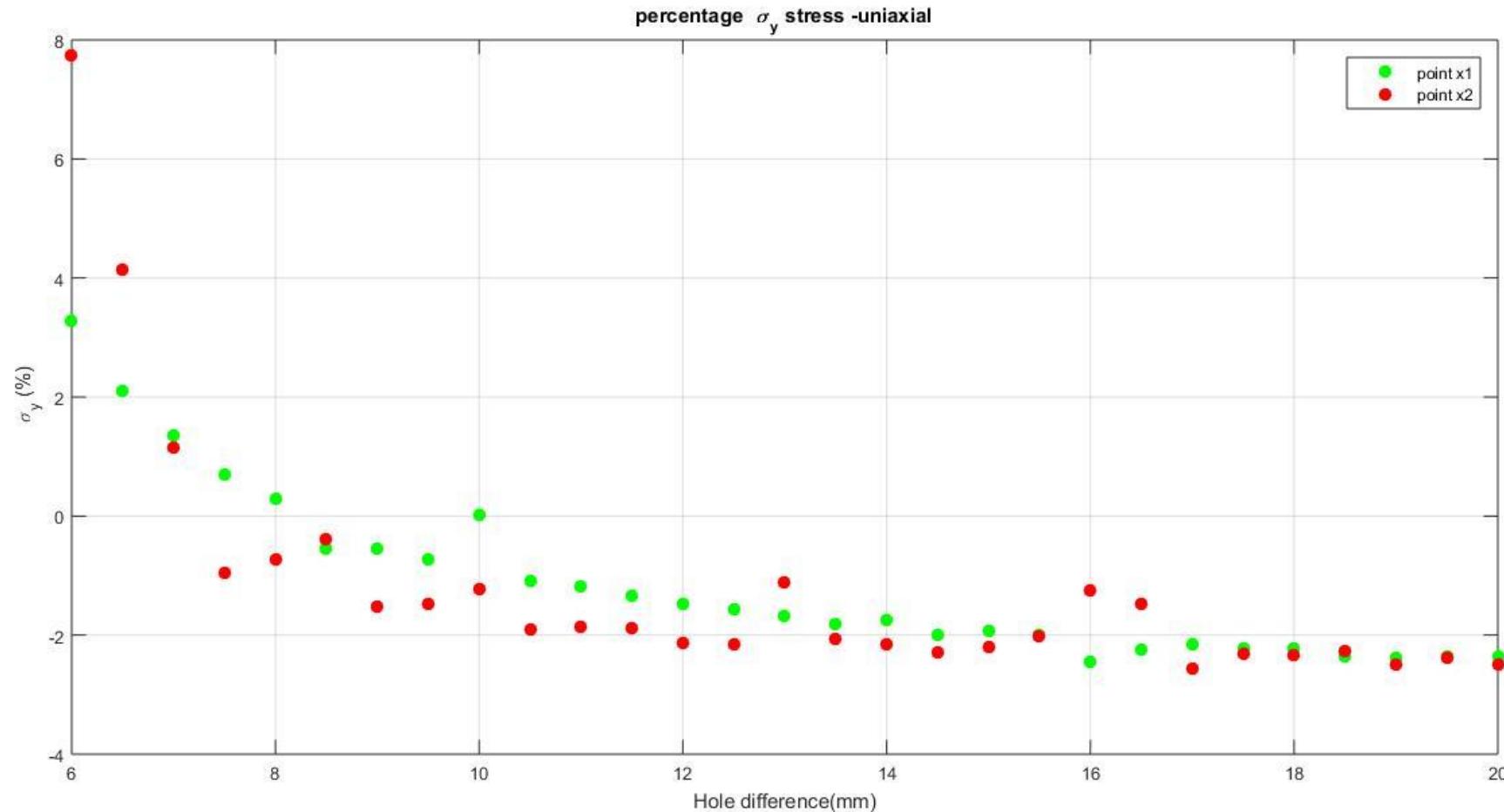


Matlab Plots - percentage, X1, X2

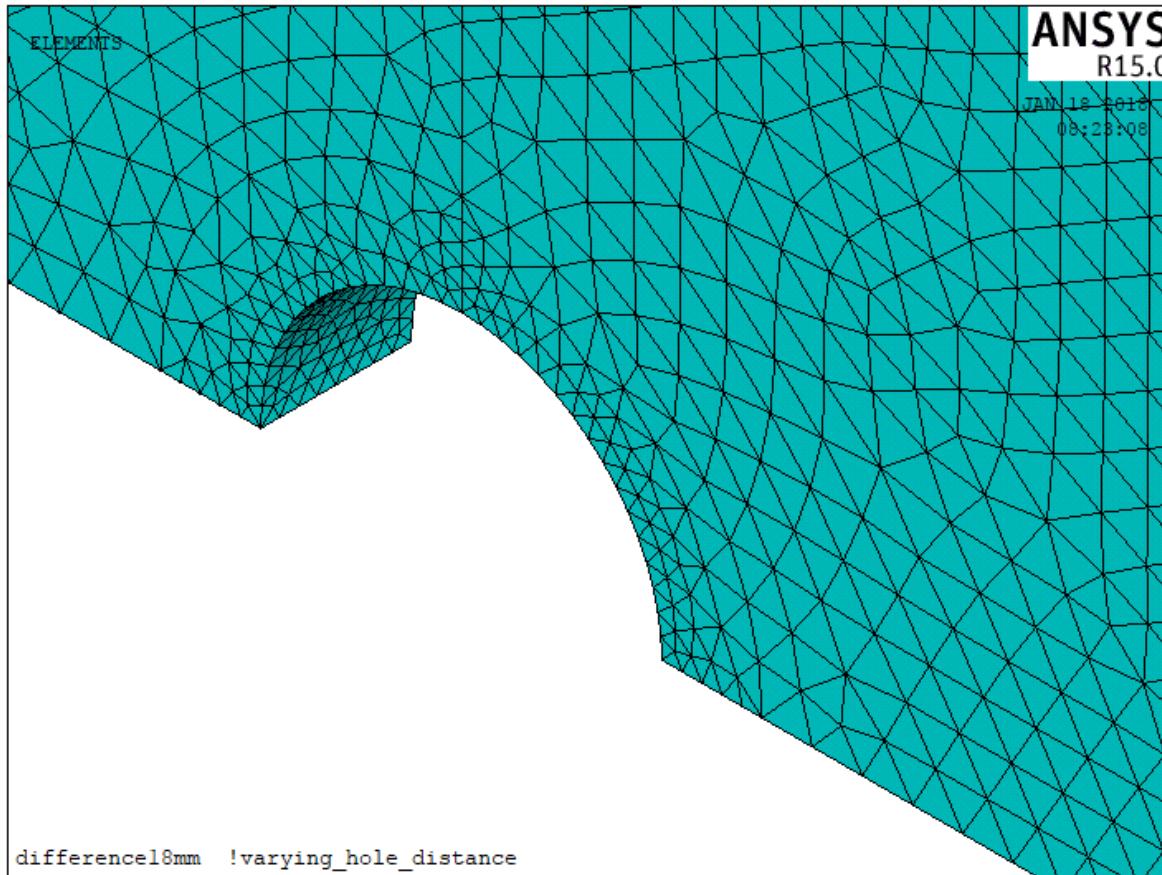
percentage = $100 * (\text{Sigmay}(x1, x2) - \text{sigmay_theoretical}) / (\text{sigmay_theoretical})$



Matlab Plots - points X1, X2



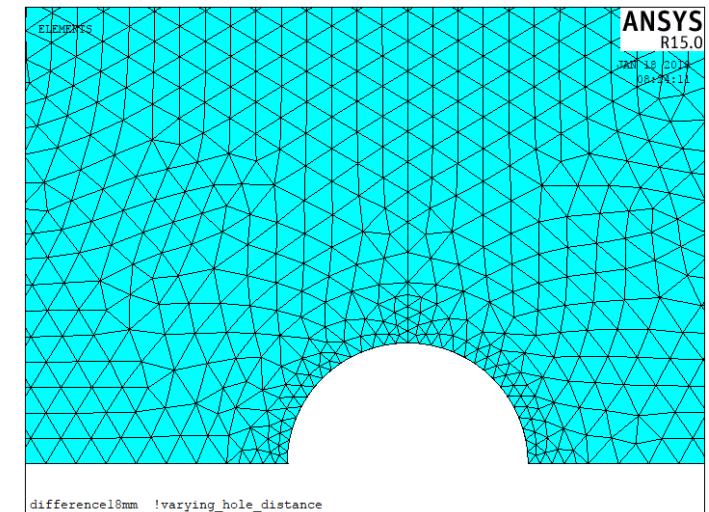
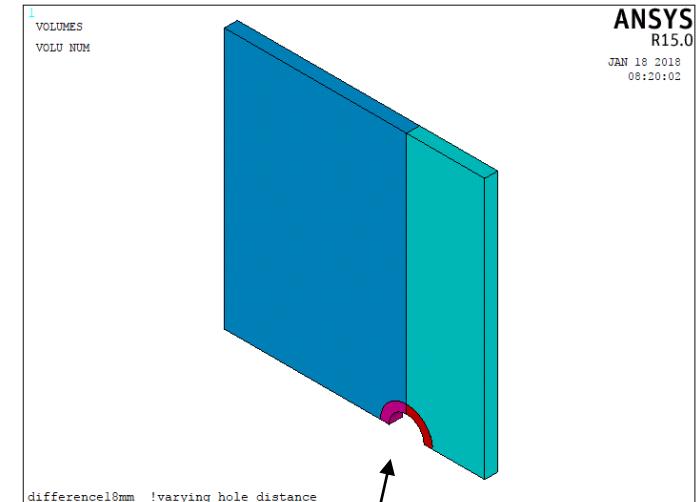
Refined Mesh Region

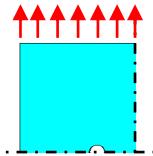


radius_int1=2.0

radius_ext1=3.0

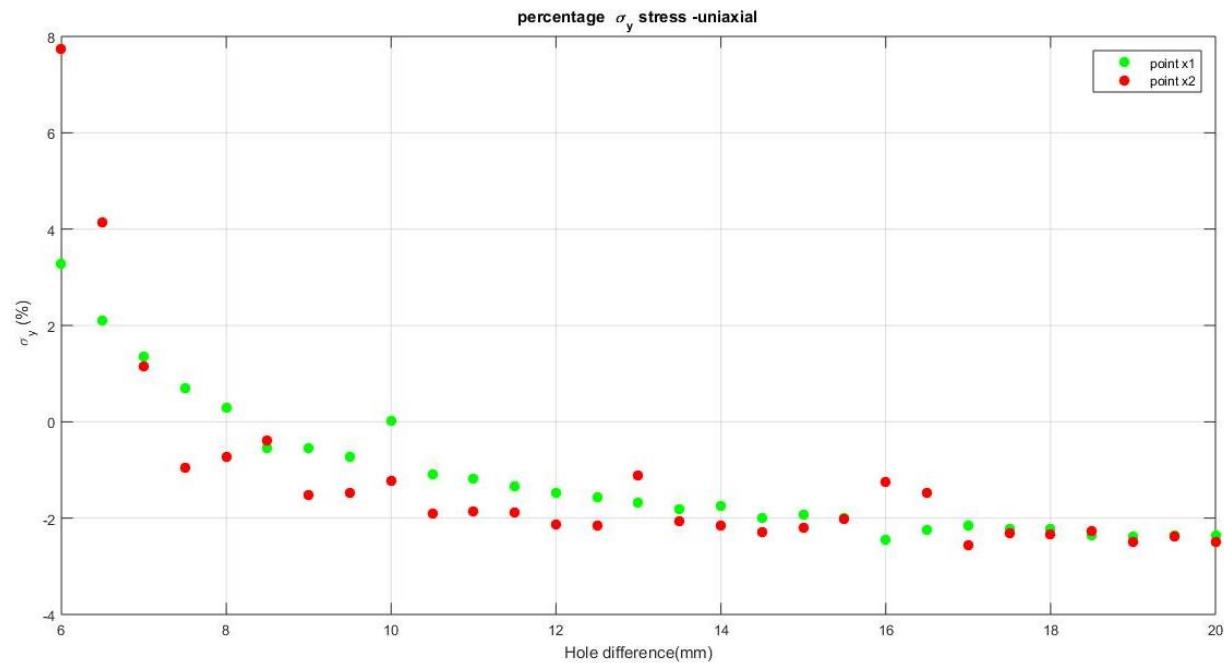
cyl4,xcenter1,ycenter1, radius_int1, angle_int1, radius_ext1, angle_ext1, -depth1



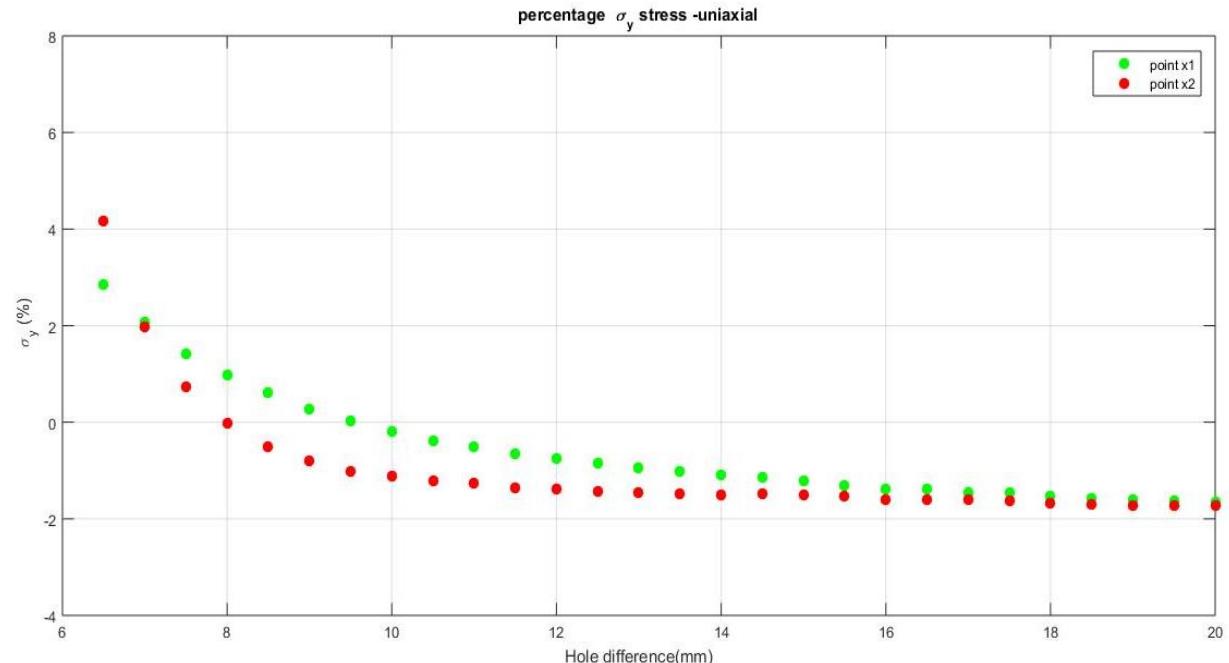


Uniaxial, Transverse load

No Refined Mesh Region



Refined Mesh Region

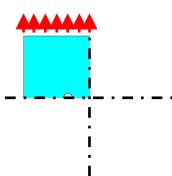
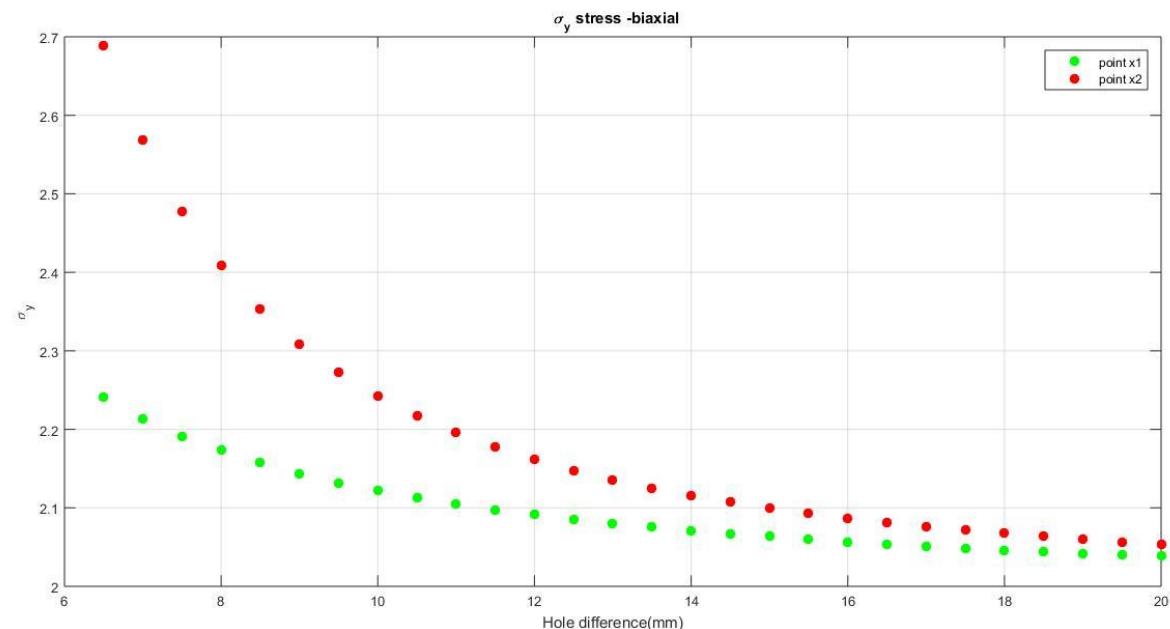
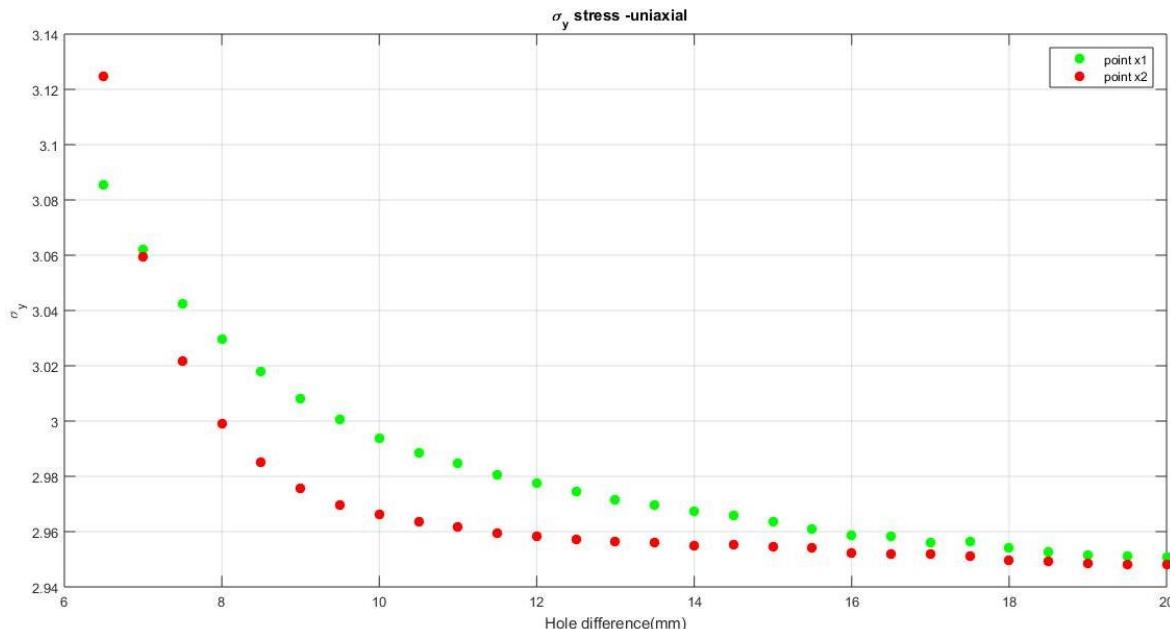


```
!mesh  
esize,0.5
```

```
!coarse mesh  
esize,0.5  
!fine mesh  
esize,0.2
```

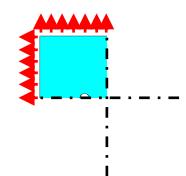
Load Comparison, X1, X2

```
! coarse mesh  
esize,0.5  
! fine mesh  
esize,0.2
```



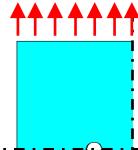
(a) Uniaxial, Transverse load

$\text{sigmay_theoretical} = 3$

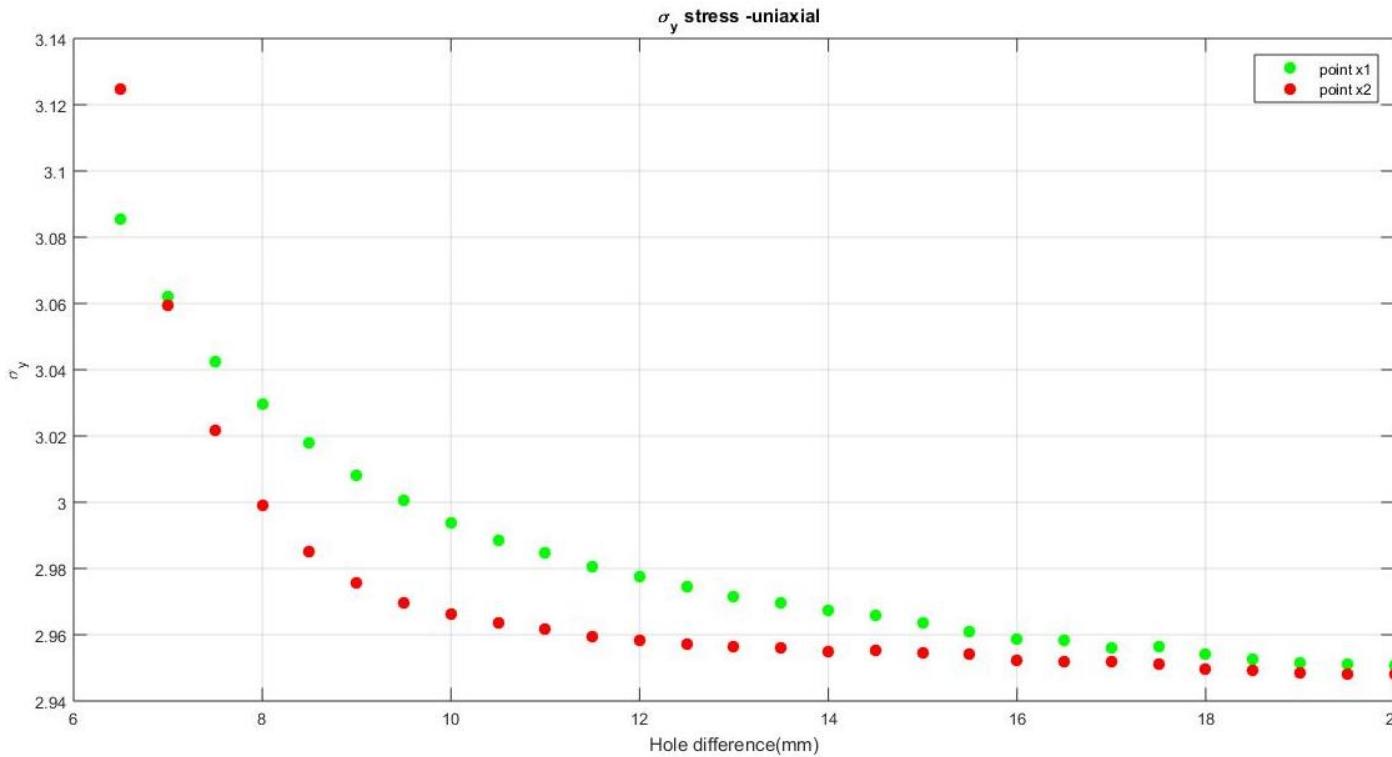


(b) Biaxial load

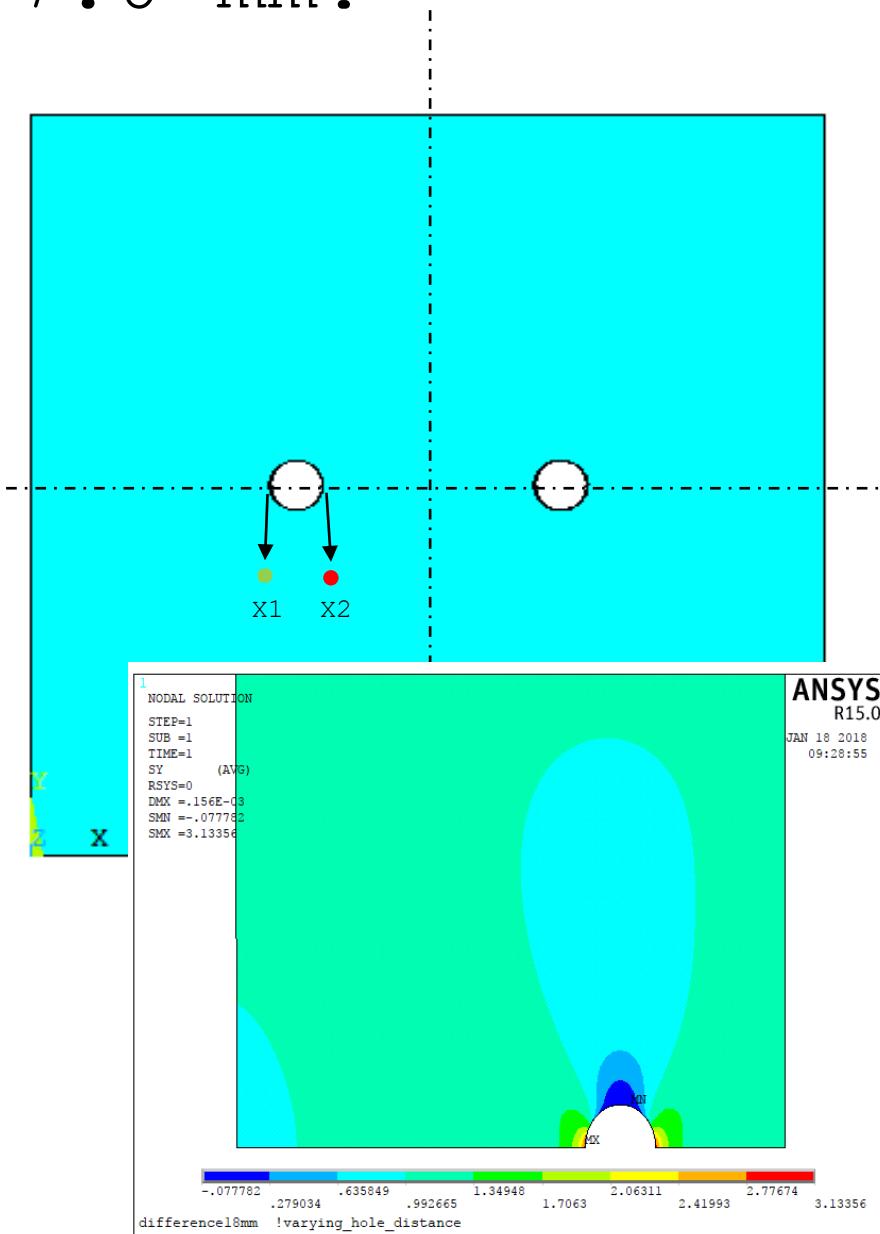
$\text{sigmay_theoretical} = 2$

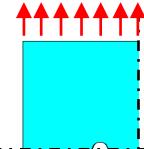


Why $x_1 > x_2$ for $\text{diff} > 7.0 \text{ mm}$?

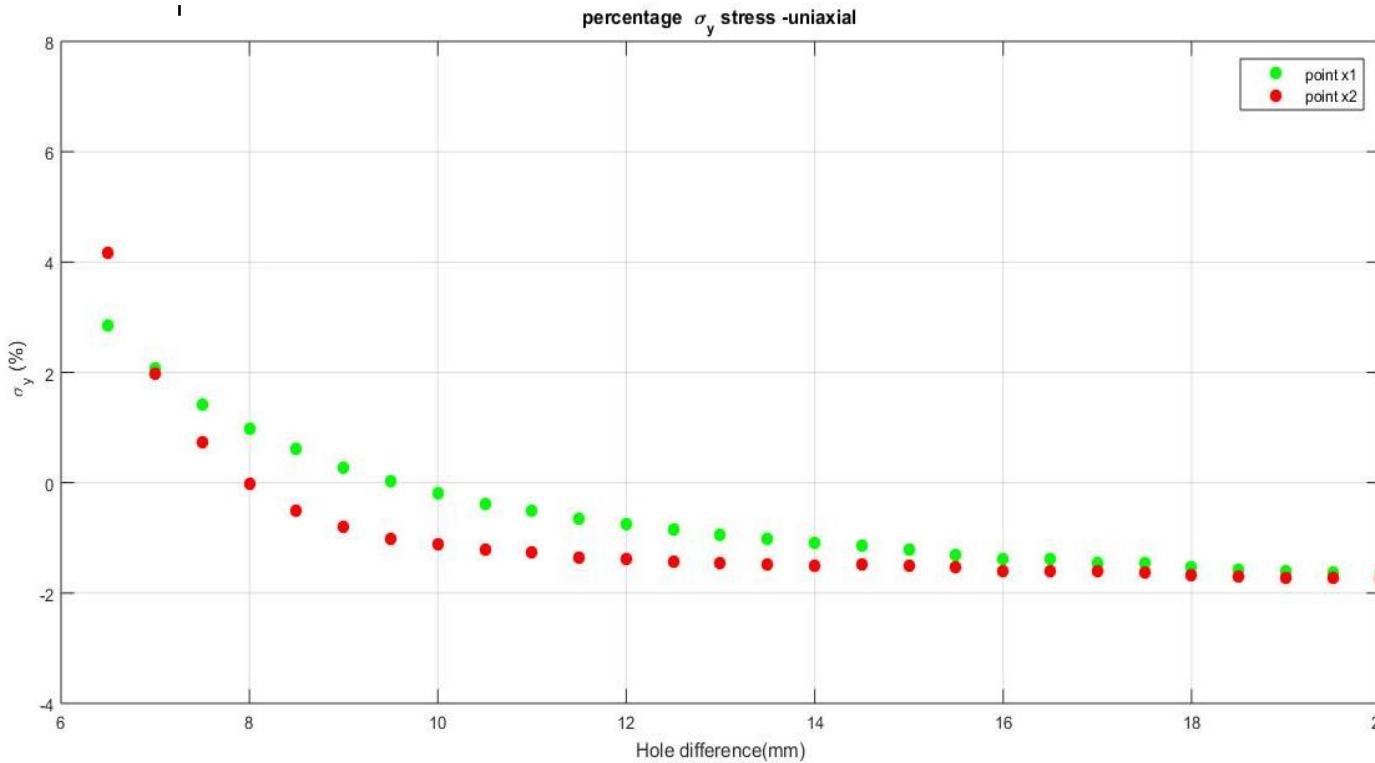


```
inicial = 6.5 !mm, minimum, duo the refined mesh region (cylinder)
final = 20 !mm
incr = 0.5 !mm
*do,diff,inicial,final,incr
    ...
*enddo
```

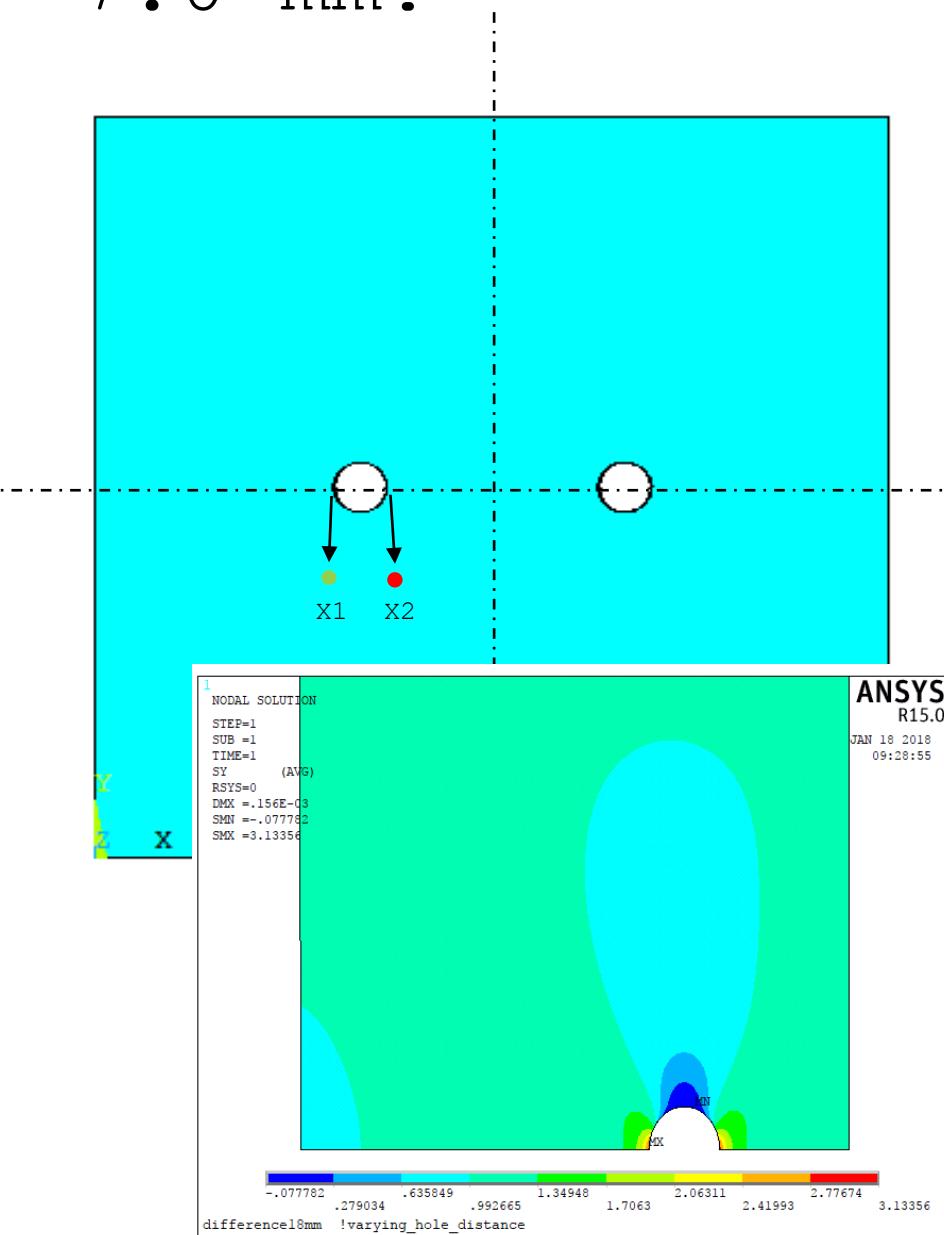




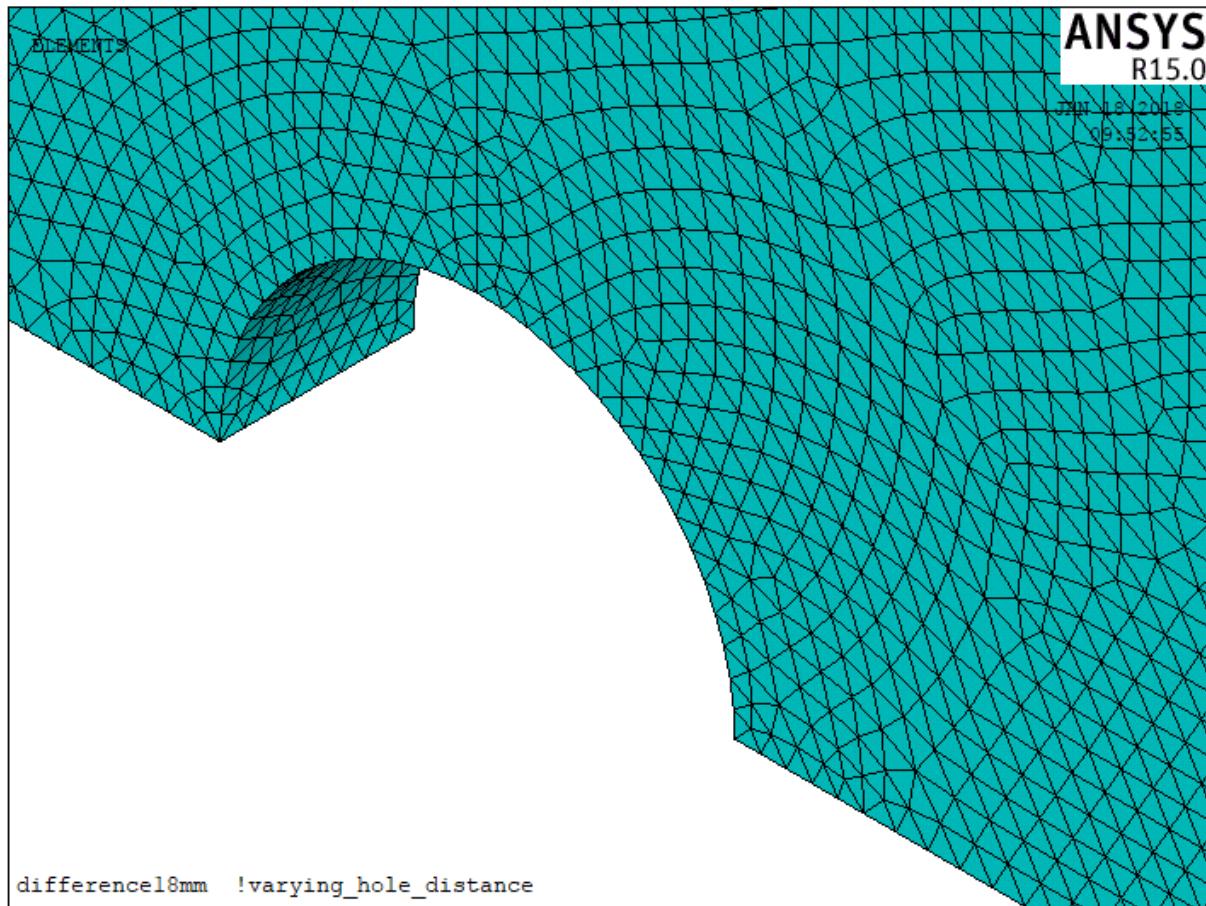
Why $x_1 > x_2$ for $\text{diff} > 7.0 \text{ mm}$?



```
inicial = 6.5 !mm, minimum, duo the refined mesh region (cylinder)
final = 20 !mm
incr = 0.5 !mm
*do,diff,inicial,final,incr
    ...
*enddo
```

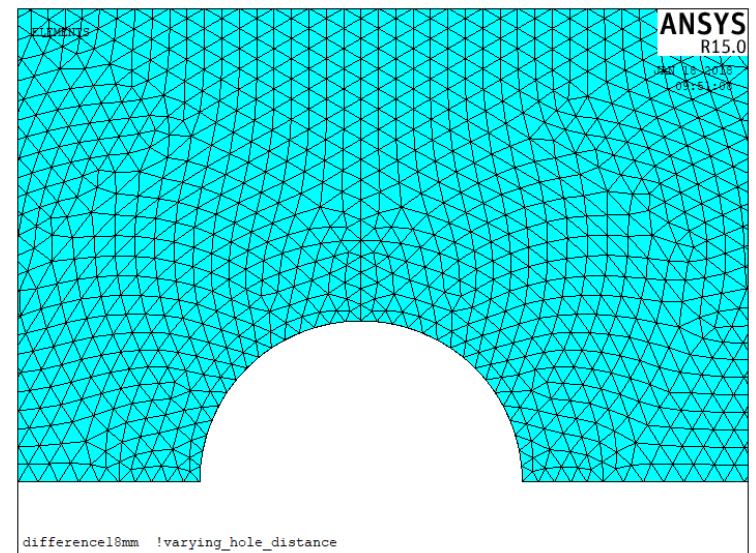
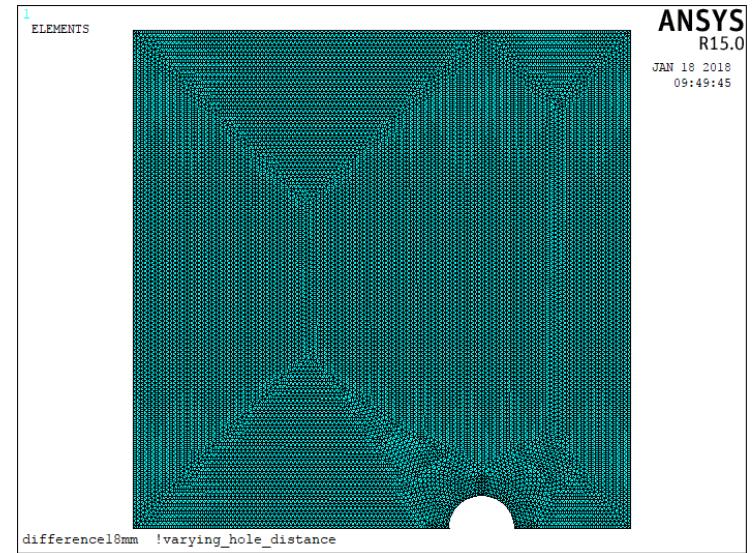


Even Finer Mesh Region



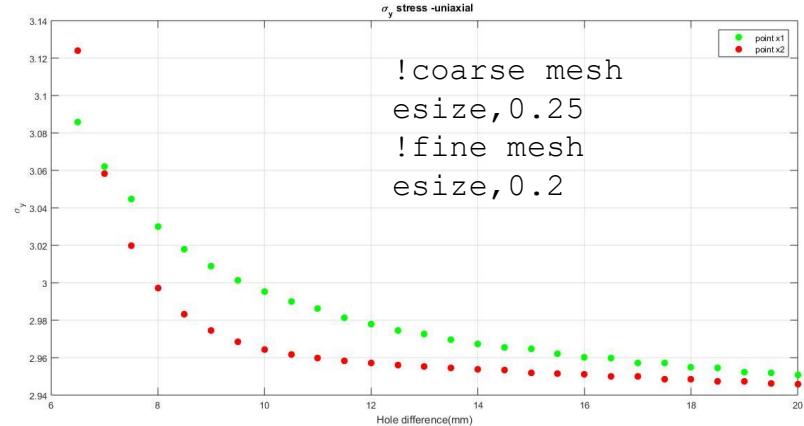
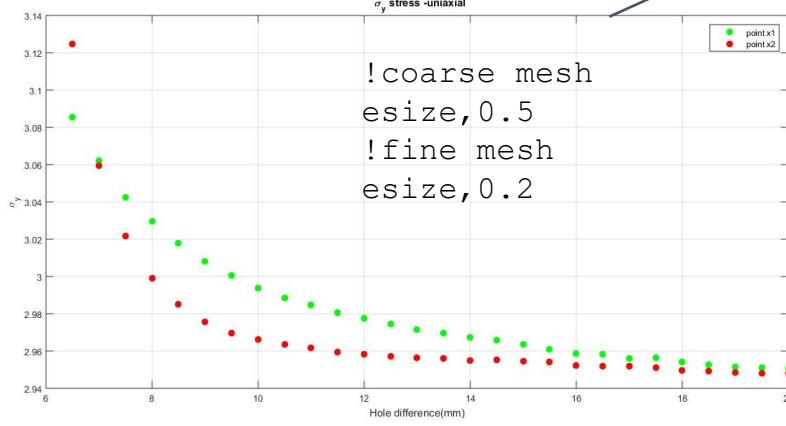
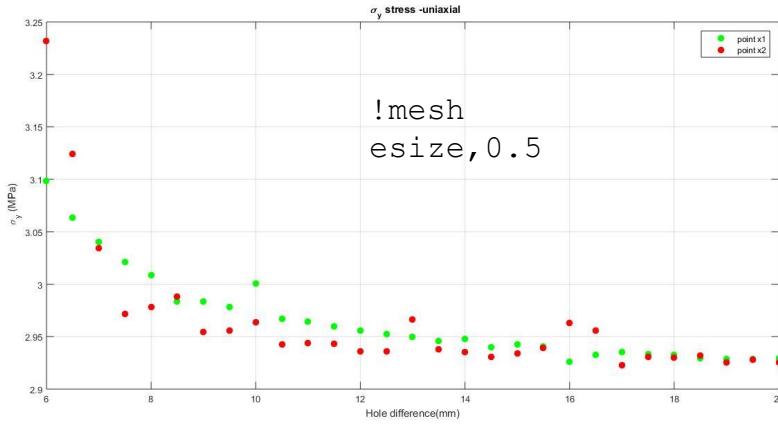
```
!coarse mesh  
esize,0.25  
!fine mesh  
esize,0.2
```

!Cost, just uniaxial simulation
! ~12h processing
! 166 GB files

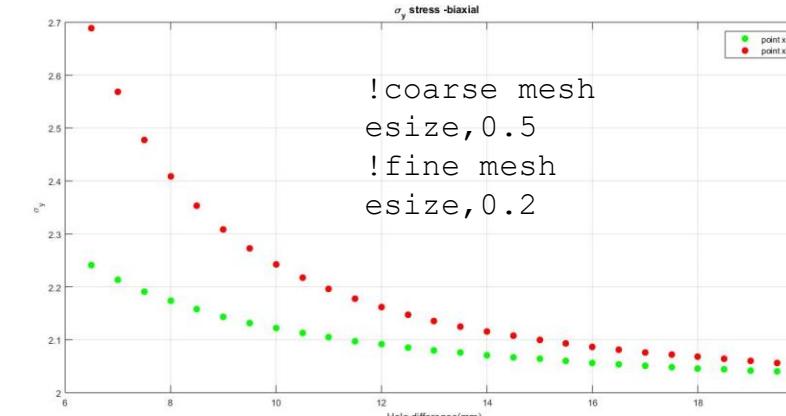
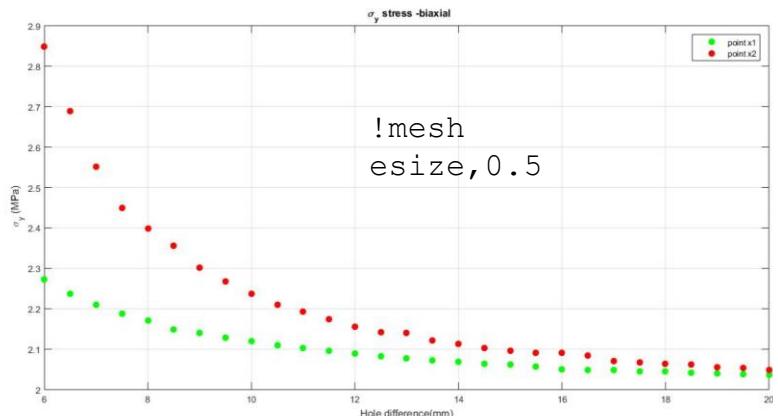


Results

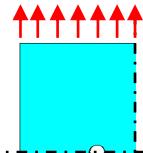
Asked this mesh with 0.5 thickness ring



(a) Uniaxial, Transverse load

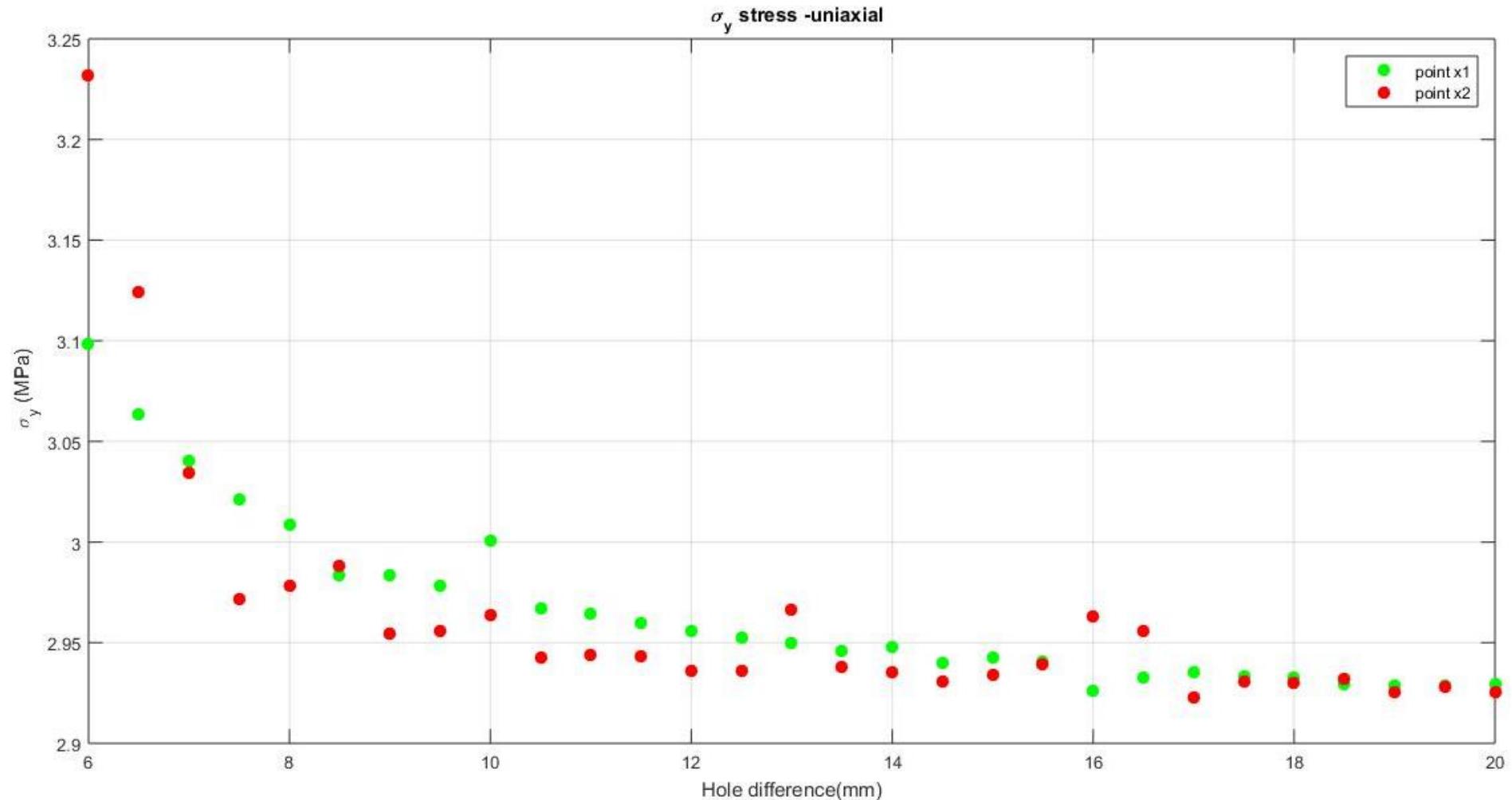


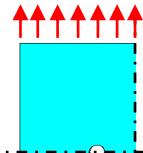
(b) Biaxial load



Uniaxial, Transverse load

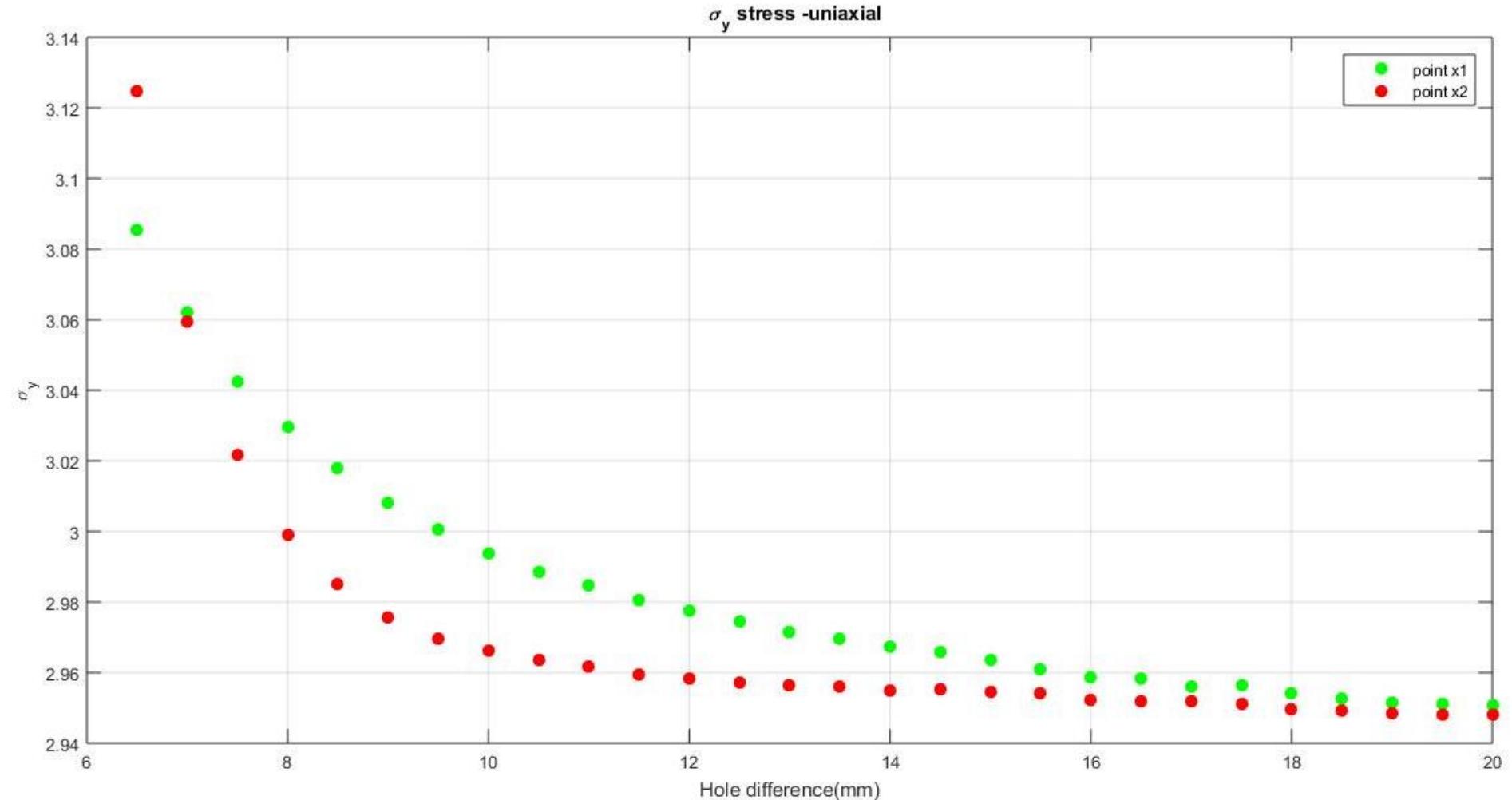
```
!mesh  
esize, 0.5
```

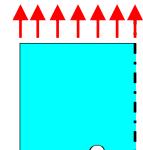




Uniaxial, Transverse load

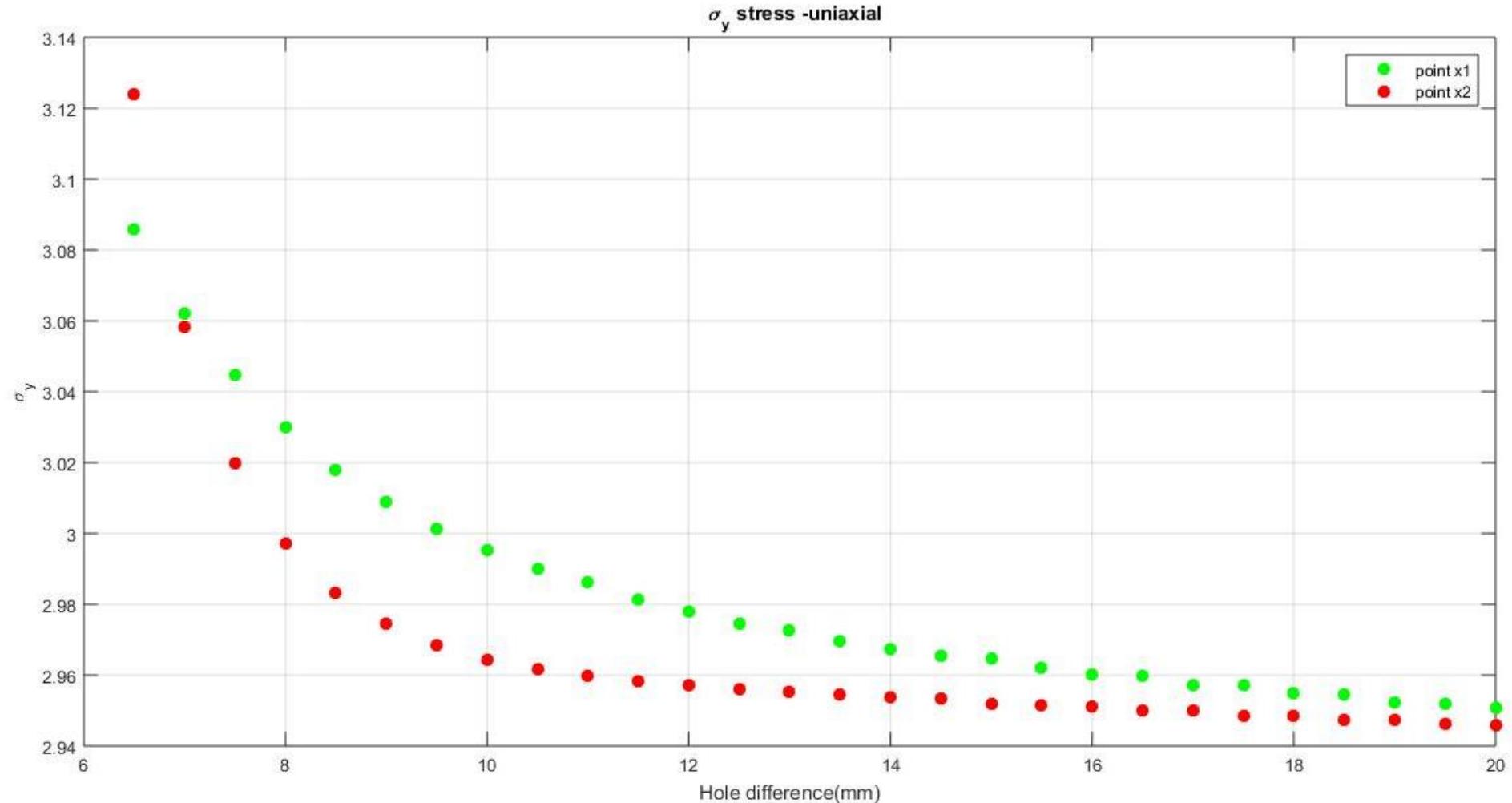
```
!coarse mesh  
esize,0.5  
!fine mesh  
esize,0.2
```





Uniaxial, Transverse load

```
!coarse mesh  
esize,0.25  
!fine mesh  
esize,0.2
```



Theoretical Result

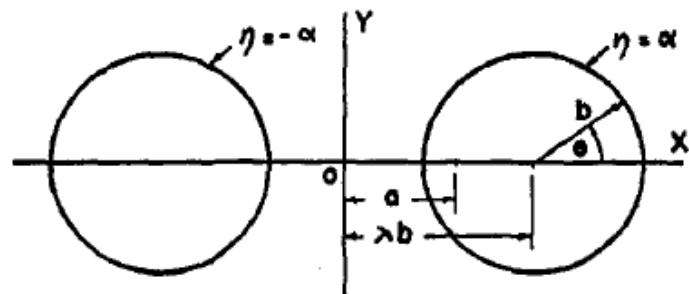


FIG. 1. Two equal holes.

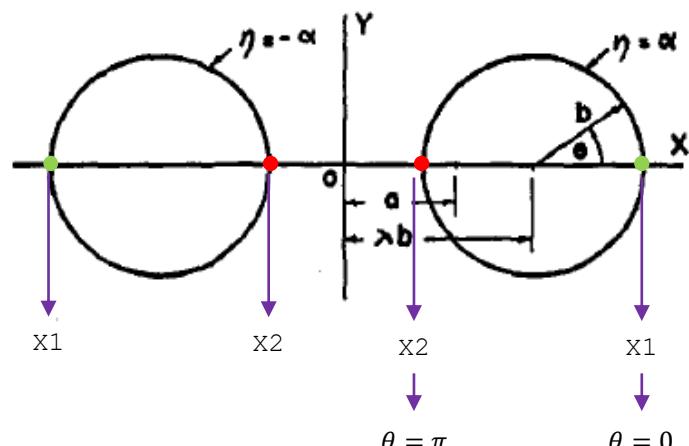


TABLE I. The maximum stresses ($T=1$).

λ	(1) All-around tension $\theta=0$	(1) All-around tension $\theta=\pi$	(2) Longitudinal tension $\theta=\pm\pi/2$	(3) Transverse tension $\theta=0$	(3) Transverse tension $\theta=\pi$
1	2.894	∞	2.569	3.869	∞
1.5	2.255	2.887	2.623	3.151	3.264
2	2.158	2.411	2.703	3.066	3.020
3	2.080	2.155	2.825	3.020	2.992
5	2.033	2.049	2.927	3.004	2.997
8	2.014	2.018	2.970	3.001	2.999
∞	2.000	2.000	3.000	3.000	3.000

On the Stresses in a Plate Containing Two Circular Holes

CHIH-BING LING

Guggenheim Laboratory, California Institute of Technology, Pasadena 4, California

(Received May 29, 1947)

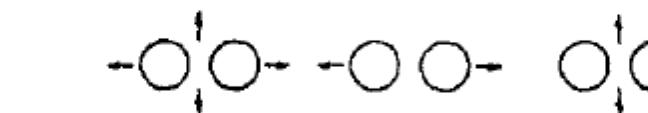
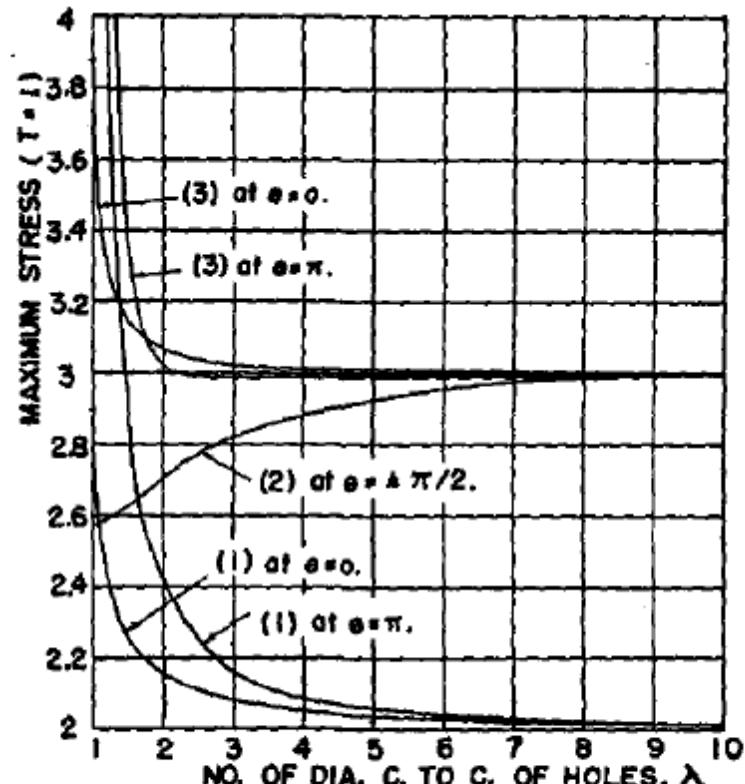
This note gives a theoretical solution to a plate containing two circular holes of equal size. The method of solution is to add to the given stress system a suitable biharmonic function which gives no stress at infinity. The parametric coefficients involved in the solution are adjusted so as to satisfy the boundary conditions at the edges of the holes. Bipolar coordinates are used in the solution, by means of which explicit expressions are obtained for the parametric coefficients. Three fundamental stress systems are discussed in some detail, namely, the all-around tension case, the longitudinal tension case, and the transverse tension case. Formulas of the stress along the edges of holes are derived and, in particular, values of maximum stress are calculated. The limiting case in which the holes are tangential is also discussed.

THE general solution of the stresses in a perforated plate, of infinite size, containing a group of circular holes was obtained by Howland and Knight,¹ and Green.² Naturally, such general solutions do not give much information as to the numerical aspect of the problem unless particular cases are worked out separately. In both solutions, it may be mentioned that the

Jeffery's, will be given, corresponding to several fundamental stress systems acting in the plate. The parametric coefficients involved in the solution are obtained in explicit forms in terms of bipolar coordinates. Finally, the maximum stresses in the plate are calculated and plotted against the distance between the holes.

The bipolar coordinates (ξ, η) will be defined

Theoretical Result

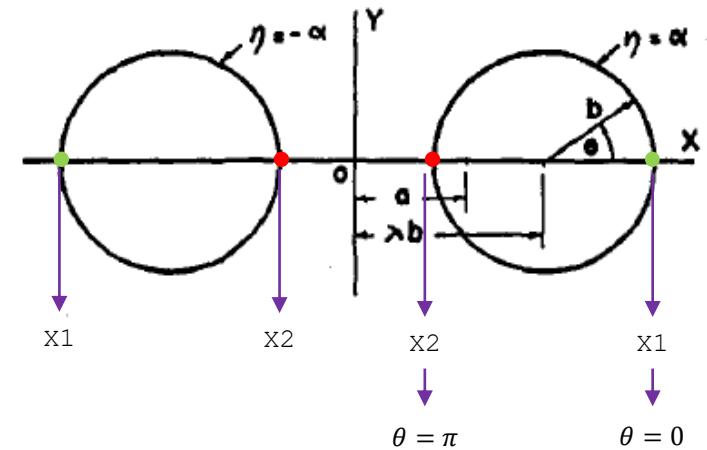


(1) All-around tension case (2) Longitudinal tension case (3) Transverse tension case

FIG. 2. The maximum stress.

TABLE I. The maximum stresses ($T=1$).

λ	(1) All-around tension		(2) Longitudinal tension		(3) Transverse tension	
	$\theta=0$	$\theta=\pi$	$\theta=\pm\pi/2$	$\theta=0$	$\theta=\pi$	
1	2.894	∞	2.569	3.869	∞	
1.5	2.255	2.887	2.623	3.151	3.264	
2	2.158	2.411	2.703	3.066	3.020	
3	2.080	2.155	2.825	3.020	2.992	
5	2.033	2.049	2.927	3.004	2.997	
8	2.014	2.018	2.970	3.001	2.999	
∞	2.000	2.000	3.000	3.000	3.000	



Theoretical Result

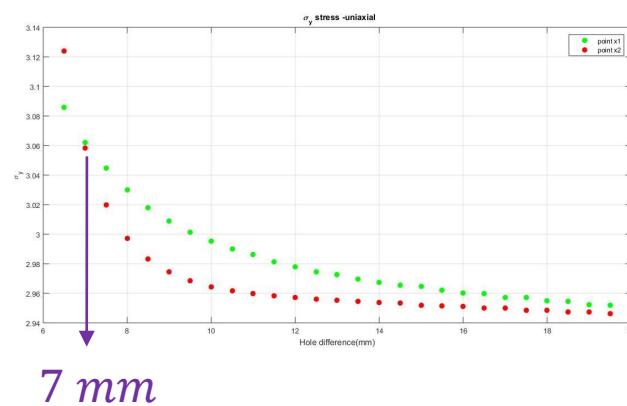
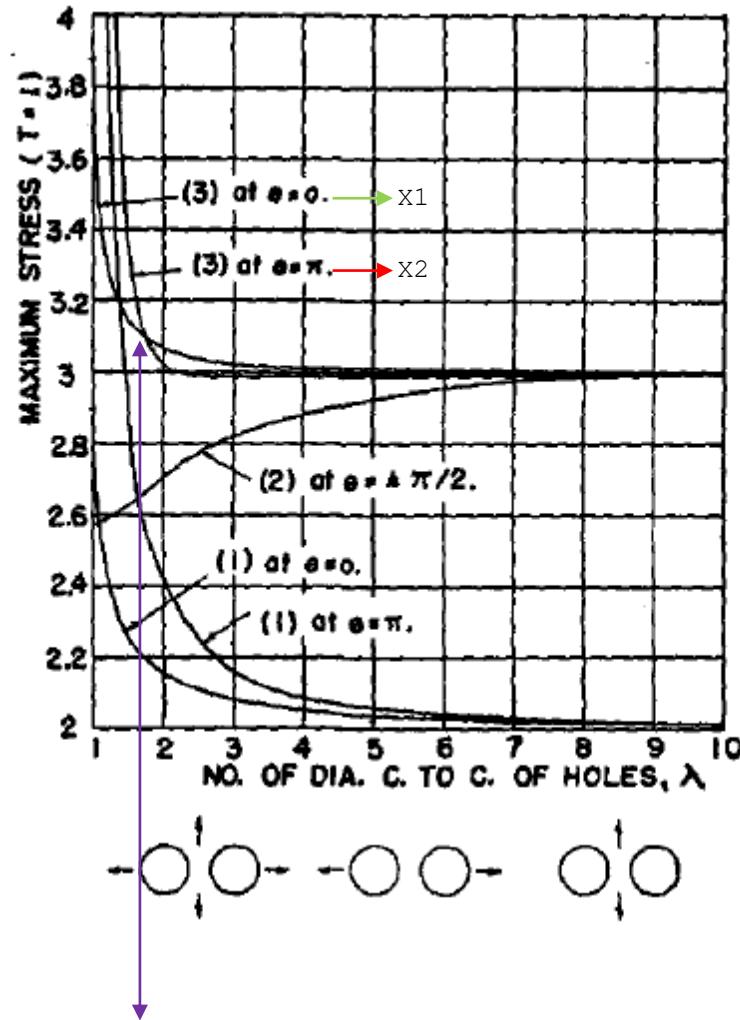
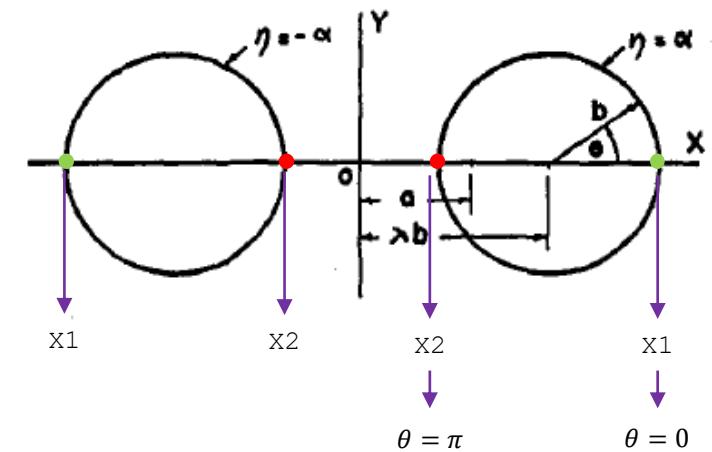


TABLE I. The maximum stresses ($T=1$).

λ	(1) All-around tension		(2) Longitudinal tension		(3) Transverse tension	
	$\theta=0$	$\theta=\pi$	$\theta=\pm\pi/2$	$\theta=0$	$\theta=\pi$	
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1.5	2.255	2.887	2.623	3.151	3.264	
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5	2.033	2.049	2.927	3.004	2.997	
8	2.014	2.018	2.970	3.001	2.999	
∞	2.000	2.000	3.000	3.000	3.000	



How to explain the physical phenomena ?

$$\frac{\xi\xi_\alpha}{T} = 2(\cosh\alpha - \cos\xi) \left\{ K \sinh\alpha \left(1 + 4 \sum_{n=1}^{\infty} \frac{\sinh n\alpha \cos n\xi}{\sinh 2n\alpha + n \sinh 2\alpha} \right) \right. \\ \left. \mp 2 \sum_{n=1}^{\infty} \frac{n(n \sinh n\alpha \sinh\alpha - \cosh n\alpha \cosh\alpha) \cos n\xi}{\sinh 2n\alpha + n \sinh 2\alpha} \right\}. \quad (34)$$

and (3) in the transverse tension case at $\xi=0$,

$$\frac{\xi\xi_0}{T} = 4(\alpha^2 K) \int_0^\infty \frac{\sinh\phi d\phi}{\sinh 2\phi + 2\phi} \\ + 2 \int_0^\infty \frac{\phi(\phi \sinh\phi - \cosh\phi)d\phi}{\sinh 2\phi + 2\phi}. \quad (40)$$

TABLE I. The maximum stresses ($T=1$).

λ	(1) All-around tension		(2) Longitudinal tension		(3) Transverse tension	
	$\theta=0$	$\theta=\pi$	$\theta=\pm\pi/2$	$\theta=0$	$\theta=\pi$	
1	2.894	∞	2.569	3.869	∞	
1.5	2.255	2.887	2.623	3.151	3.264	
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3	2.080	2.155	2.825	3.020	2.992	
5	2.033	2.049	2.927	3.004	2.997	
8	2.014	2.018	2.970	3.001	2.999	
∞	2.000	2.000	3.000	3.000	3.000	

On the Stresses in a Plate Containing Two Circular Holes

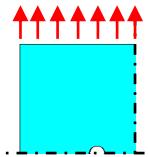
CHIH-BING LING

Guggenheim Laboratory, California Institute of Technology, Pasadena 4, California

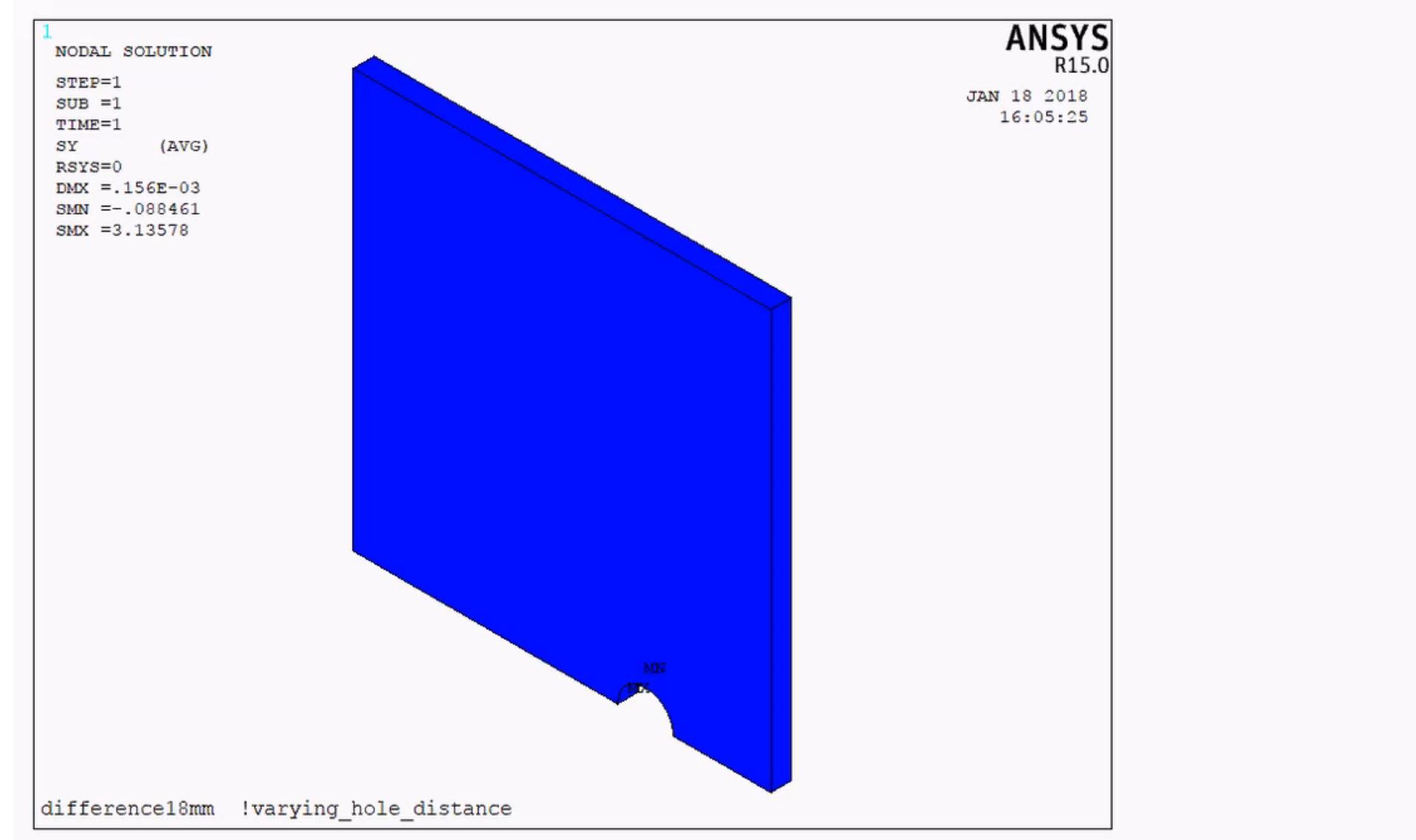
(Received May 29, 1947)

This note gives a theoretical solution to a plate containing two circular holes of equal size. The method of solution is to add to the given stress system a suitable biharmonic function which gives no stress at infinity. The parametric coefficients involved in the solution are adjusted so as to satisfy the boundary conditions at the edges of the holes. Bipolar coordinates are used in the solution, by means of which explicit expressions are obtained for the parametric coefficients. Three fundamental stress systems are discussed in some detail, namely, the all-around tension case, the longitudinal tension case, and the transverse tension case. Formulas of the stress along the edges of holes are derived and, in particular, values of maximum stress are calculated. The limiting case in which the holes are tangential is also discussed.

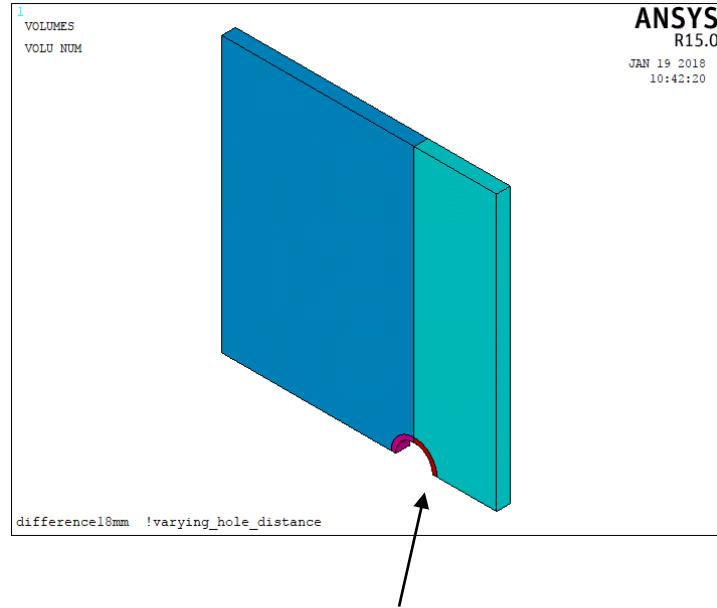
THE general solution of the stresses in a perforated plate, of infinite size, containing a group of circular holes was obtained by Howland and Knight,¹ and Green.² Naturally, such general solutions do not give much information as to the numerical aspect of the problem unless Jeffery's, will be given, corresponding to several fundamental stress systems acting in the plate. The parametric coefficients involved in the solution are obtained in explicit forms in terms of bipolar coordinates. Finally, the maximum stresses in the plate are calculated and plotted against



Uniaxial, Transverse load



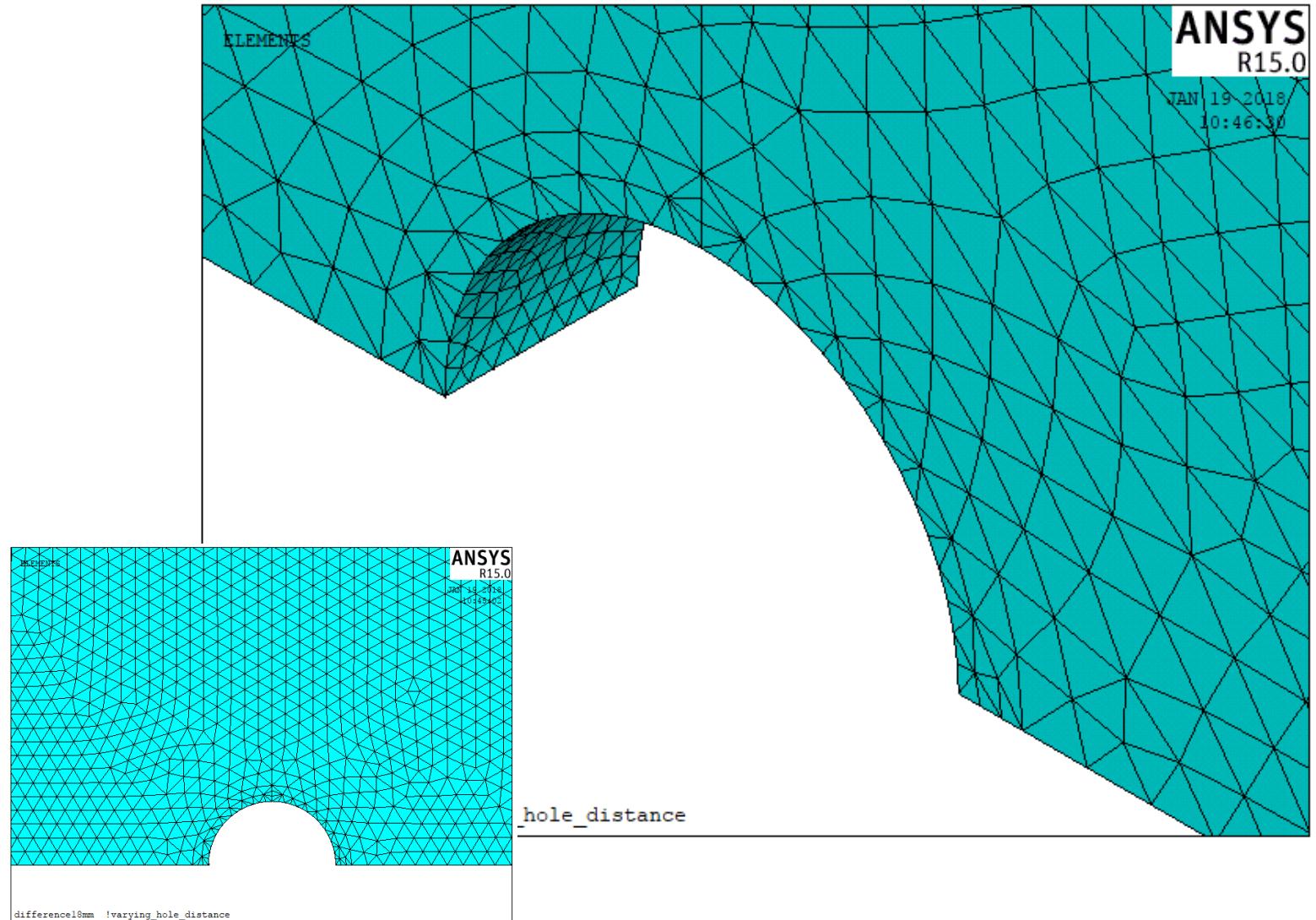
varying_hole_distance_with_refined_mesh_region_and_different_ring_thickness



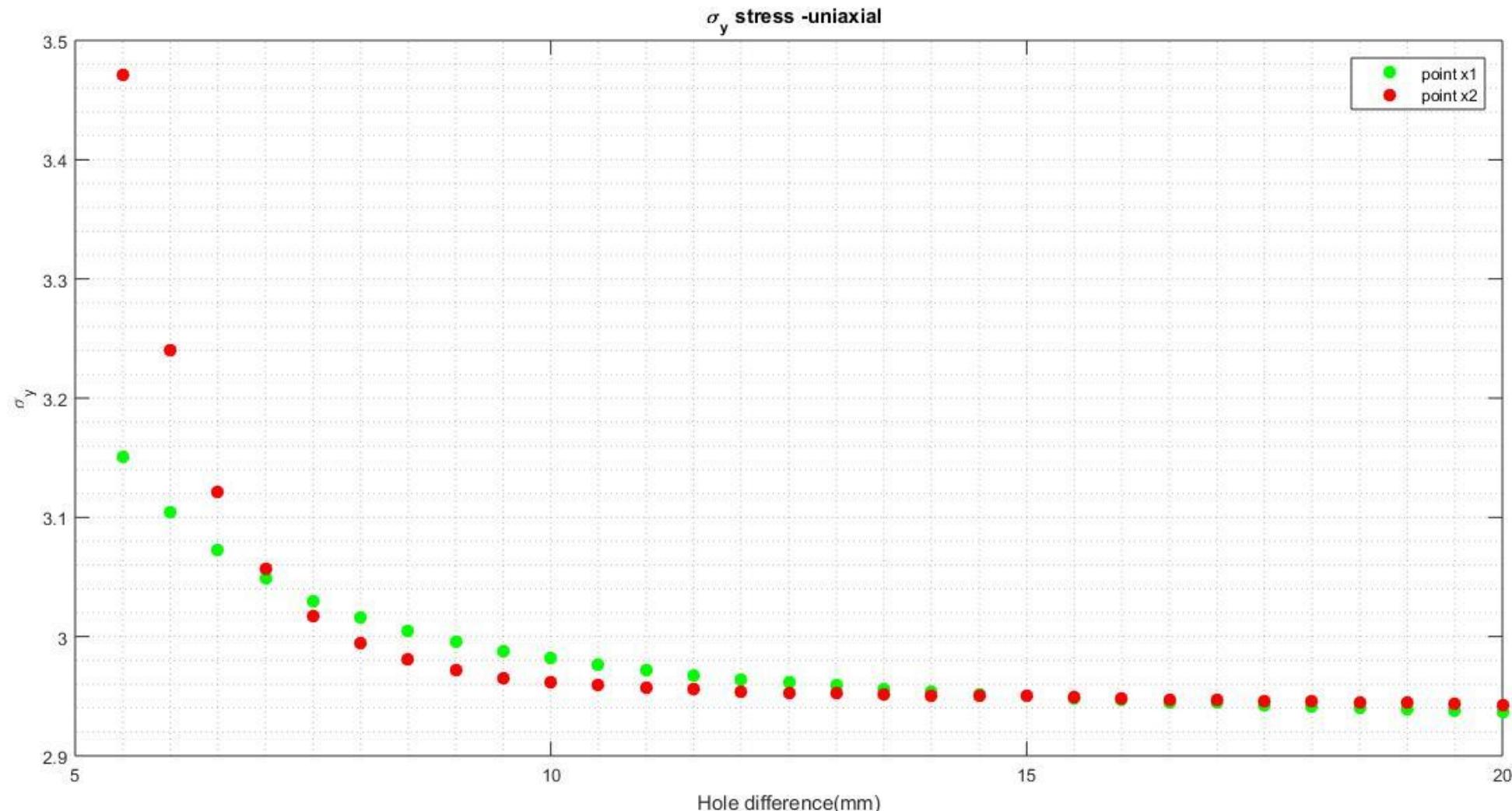
radius_int1=2.0

radius_ext1=2.5

ring_thickness = 0.5

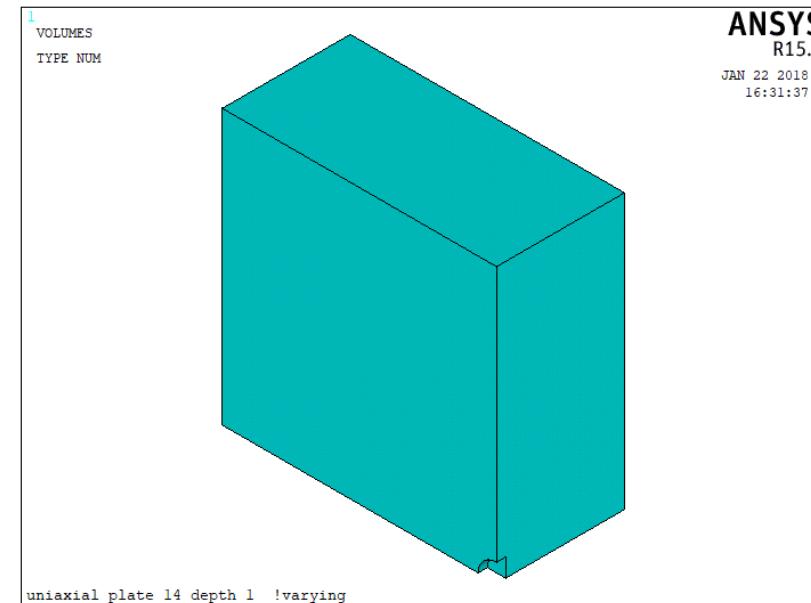
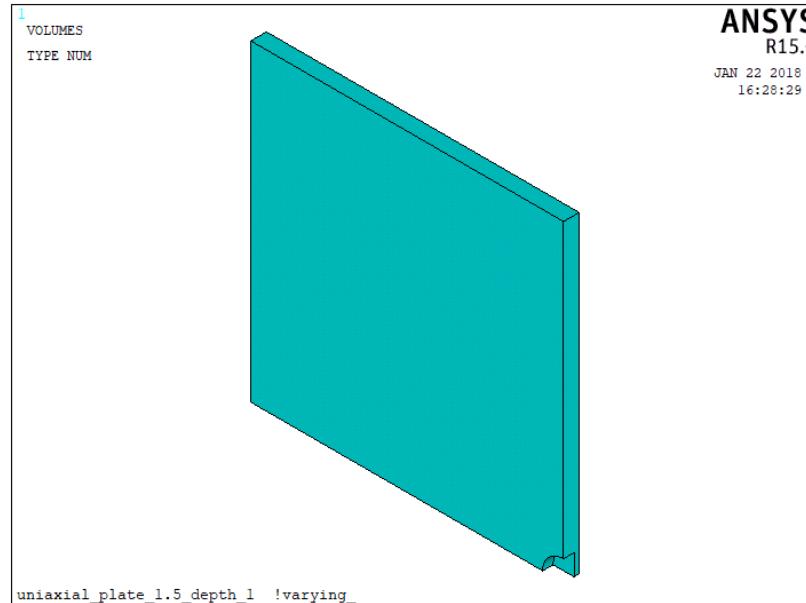
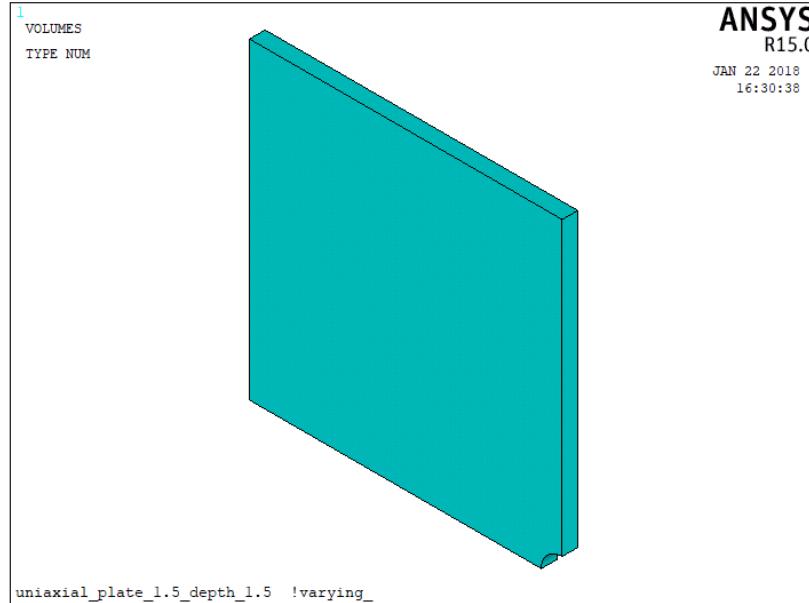


Results for uniaxial (only)



varying_hole_distance_with_refined_mesh_region_and_different_ring_thickness

Center Hole



Uniaxial

```
graph LR; Uniaxial --> plate15d15; Uniaxial --> plate15d1; Uniaxial --> plate14d1
```

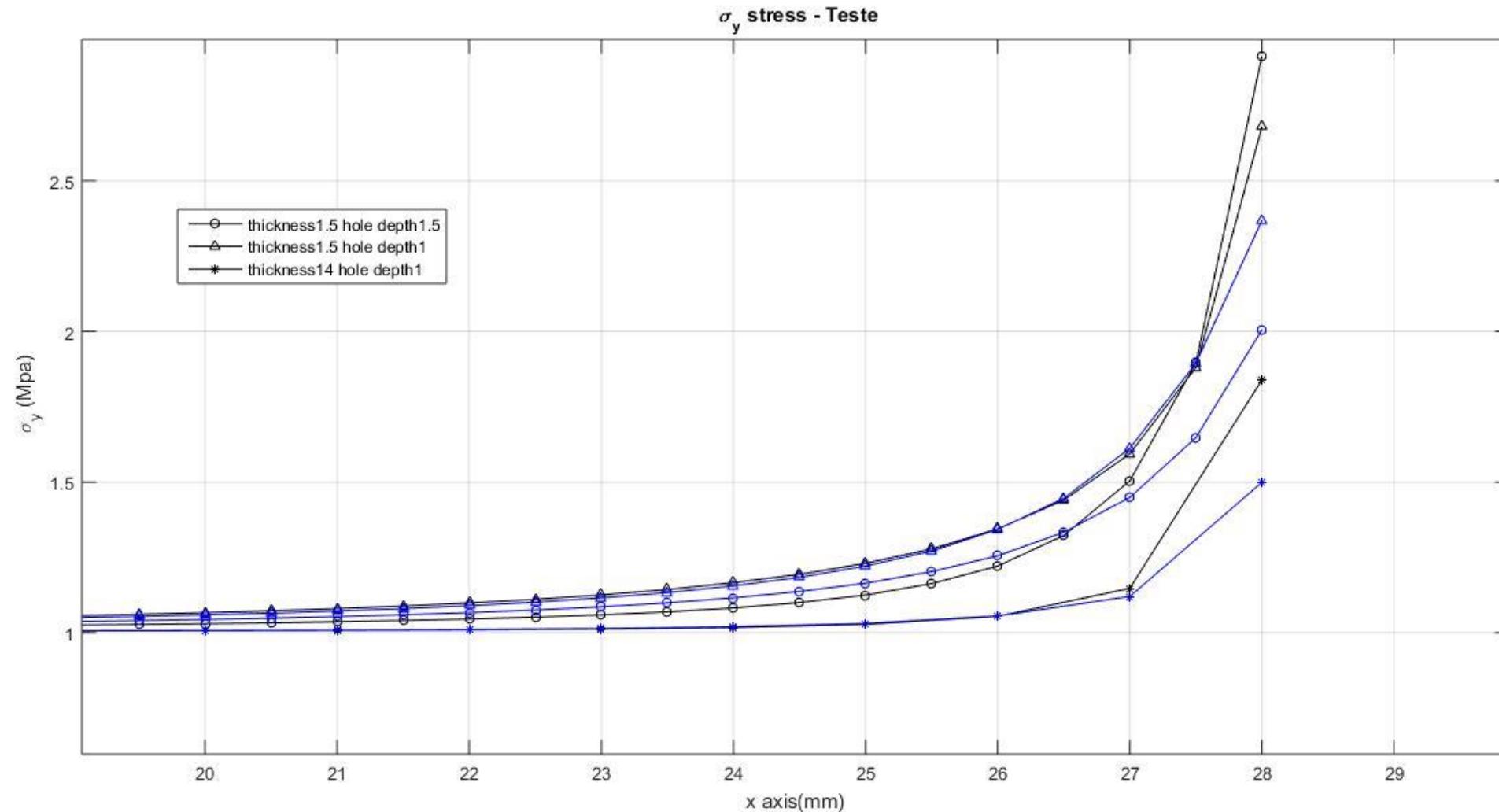
plate_1.5_depth_1.5
plate_1.5_depth_1
plate_14_depth_1

Biaxial

```
graph LR; Biaxial --> plate15d15; Biaxial --> plate15d1; Biaxial --> plate14d1
```

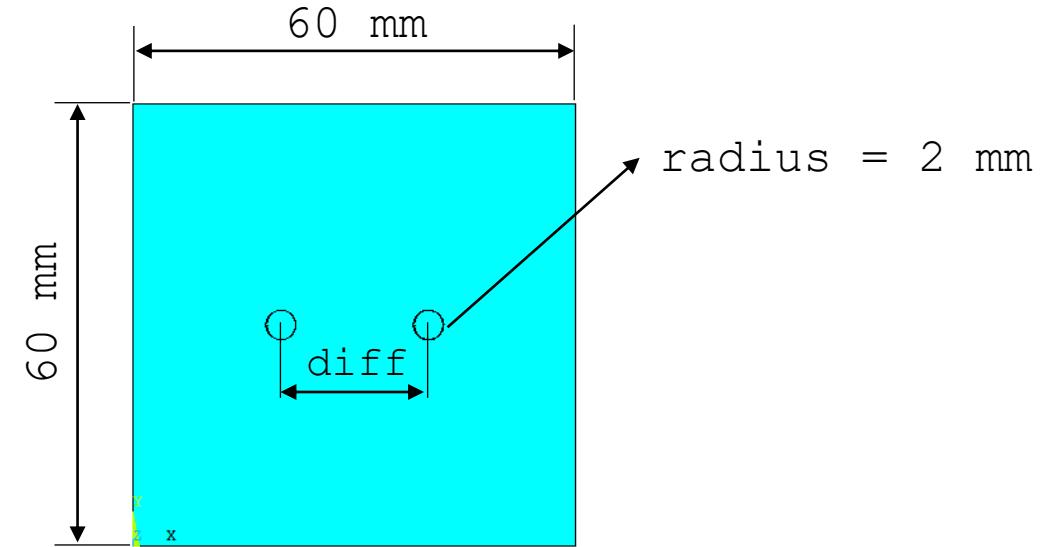
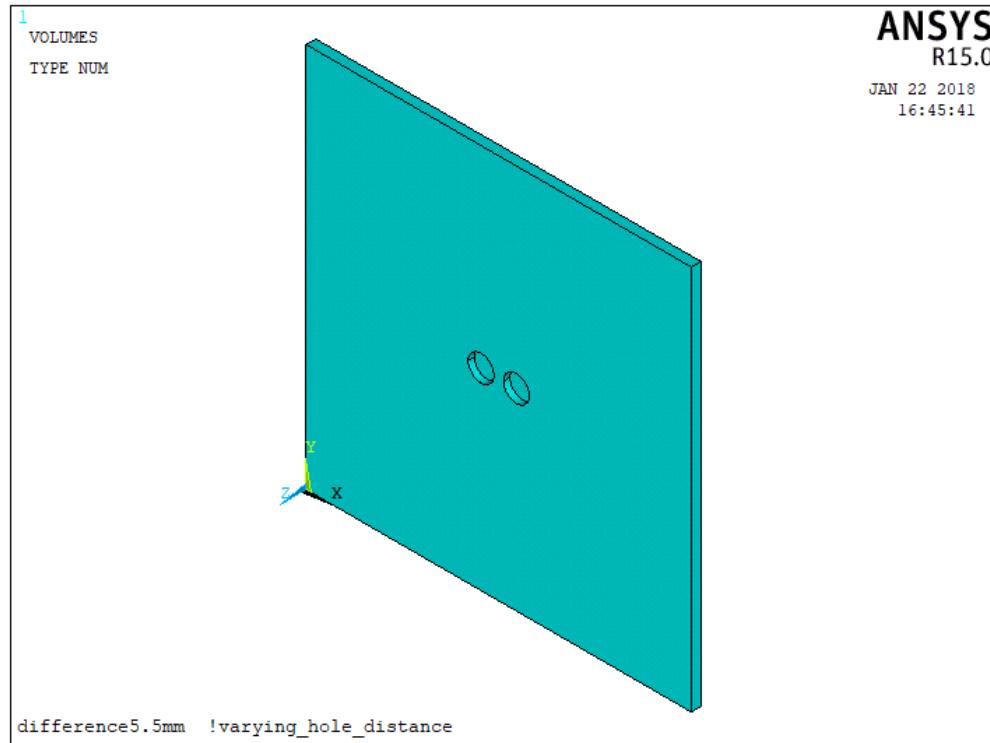
plate_1.5_depth_1.5
plate_1.5_depth_1
plate_14_depth_1

Center Hole



center_hole_uniaxial-black_and_biaxial-blue_three_geometries

A 1.5 mm plate and two Circular Holes with 1 mm depth



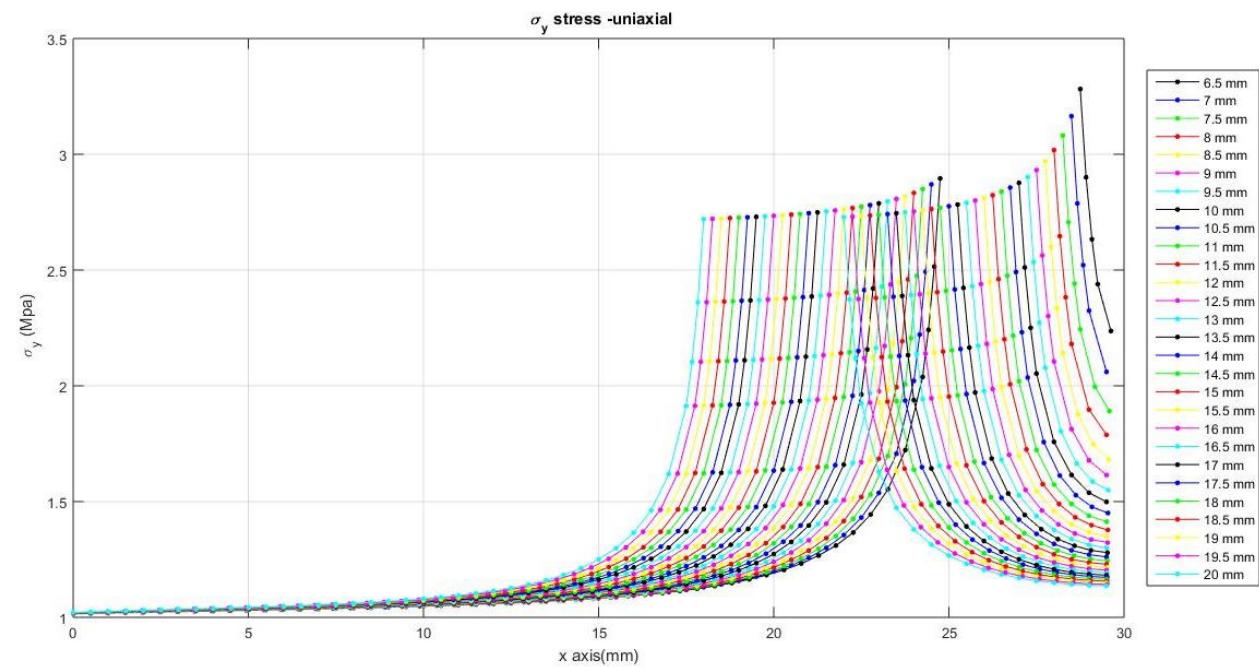
plate_thickness = 1.5 mm

depth = 1.0 mm

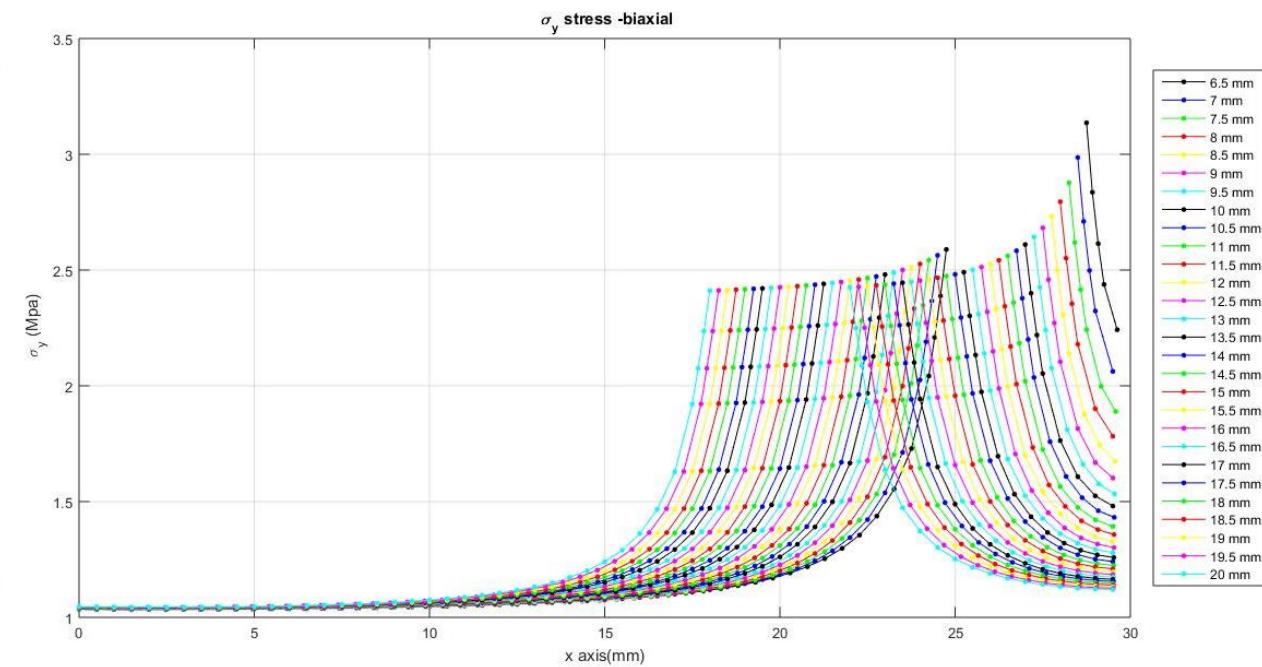
"cylindrical hole"

- Varying the hole distance

A 1.5 mm plate and two Circular Holes with 1 mm depth

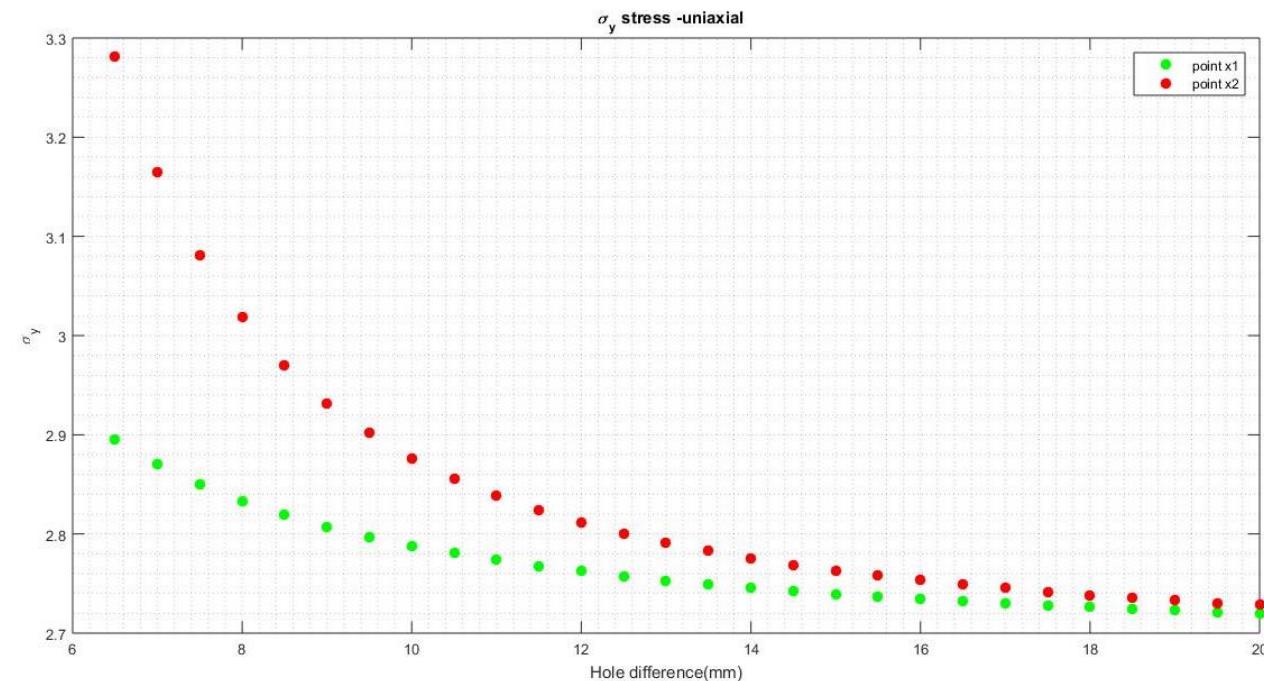


(a) Uniaxial, Transverse load

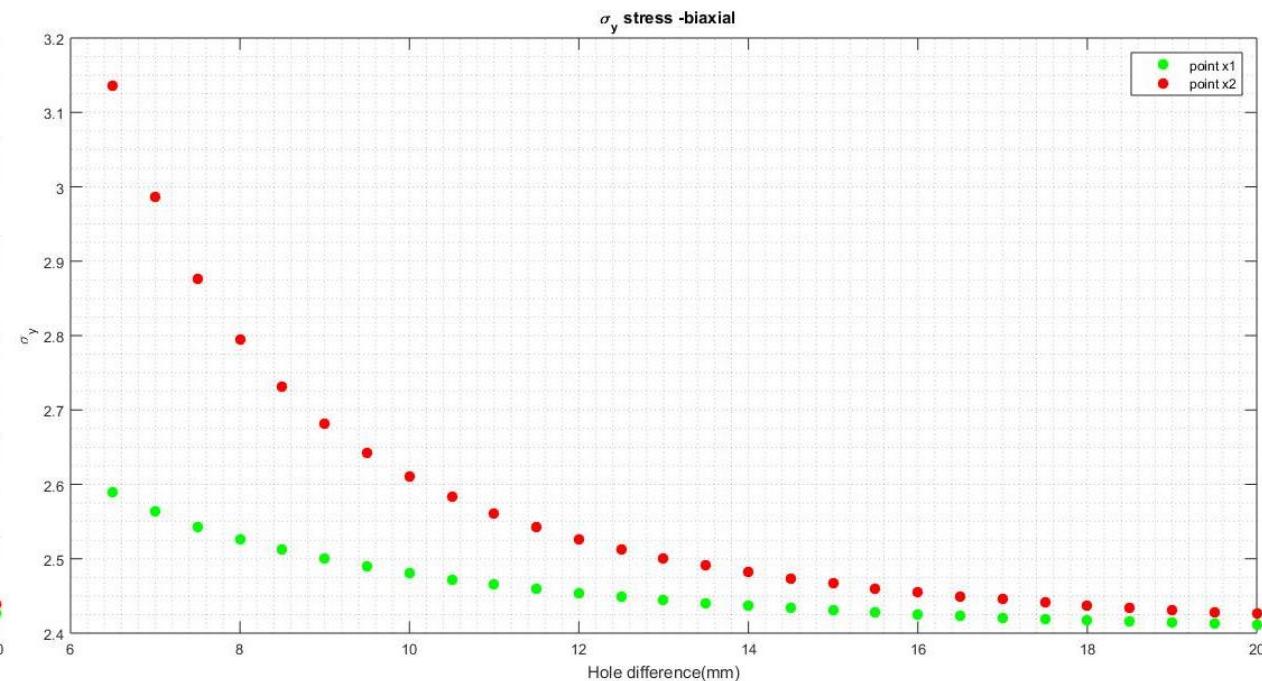
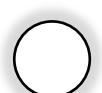


(b) Biaxial load

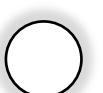
A 1.5 mm plate and two Circular Holes with 1 mm depth



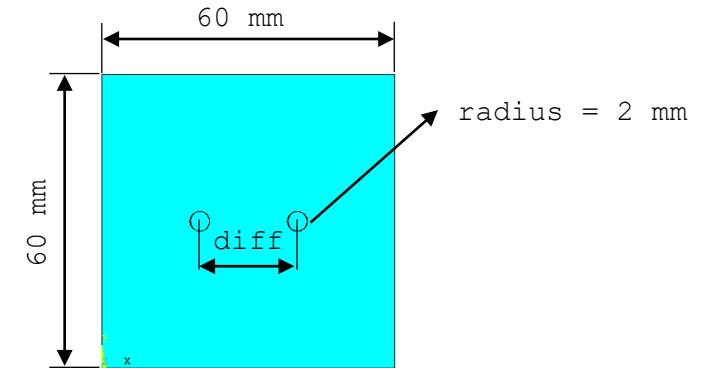
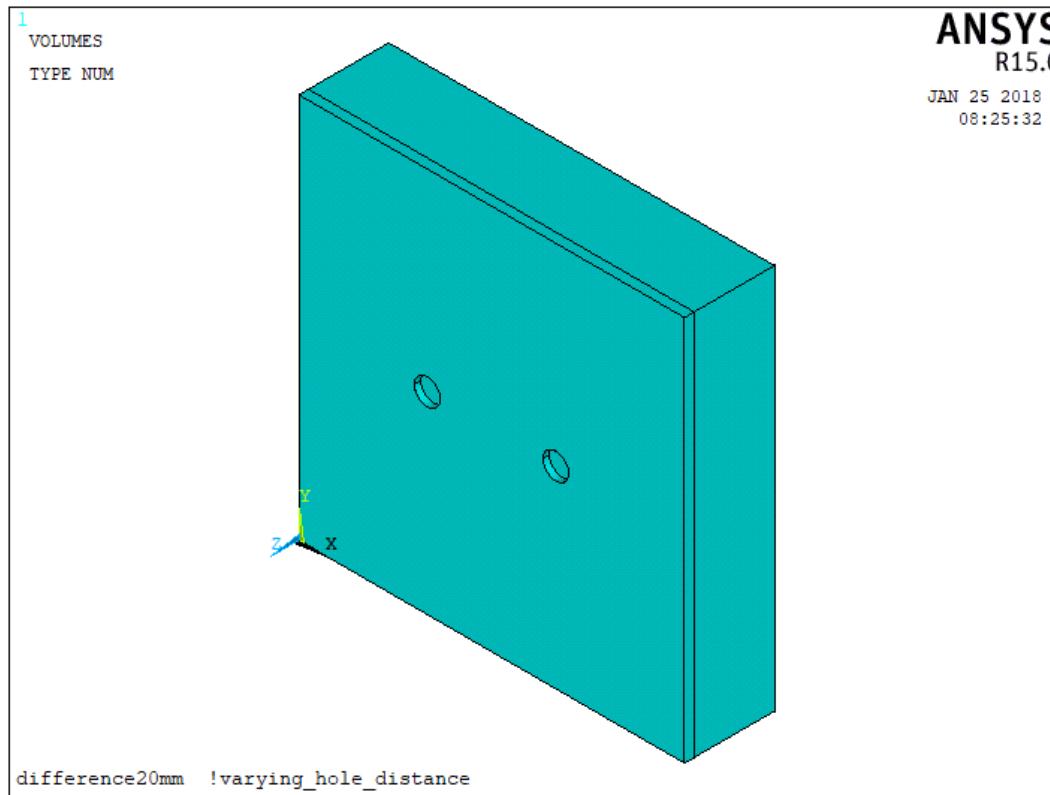
(a) Uniaxial, Transverse load



(b) Biaxial load



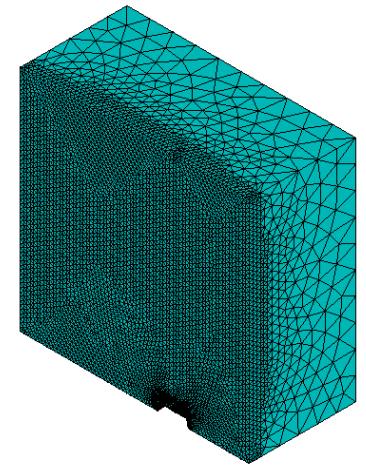
A 14 mm plate and two Circular Holes with 1 mm depth



plate_thickness = 14 mm

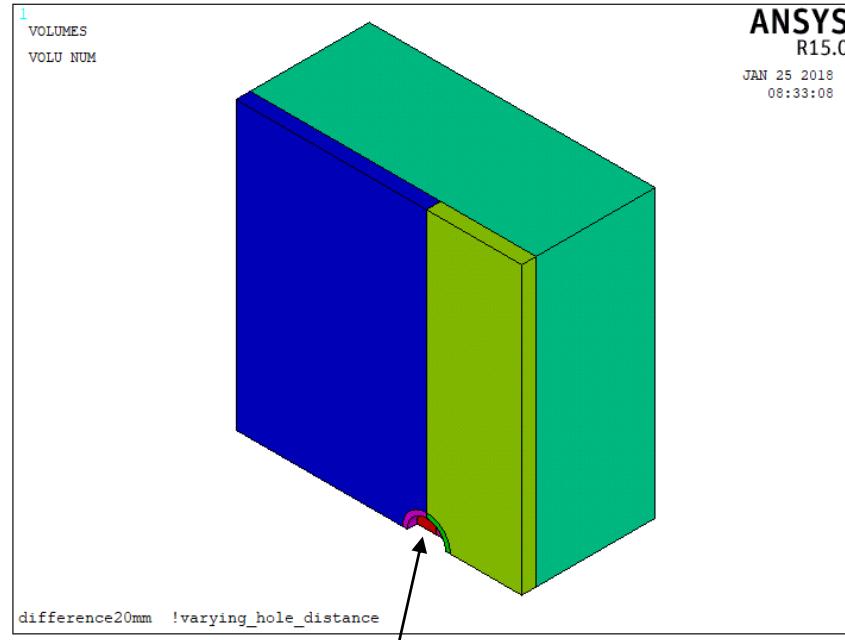
depth = 1.0 mm

"cylindrical hole"



- Varying the hole distance

varying_hole_distance_plate_14_depth_1_refined_mesh_region_ring

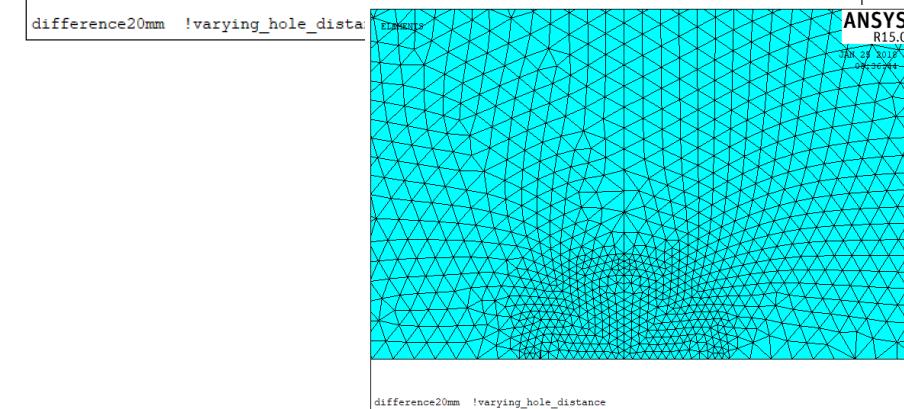
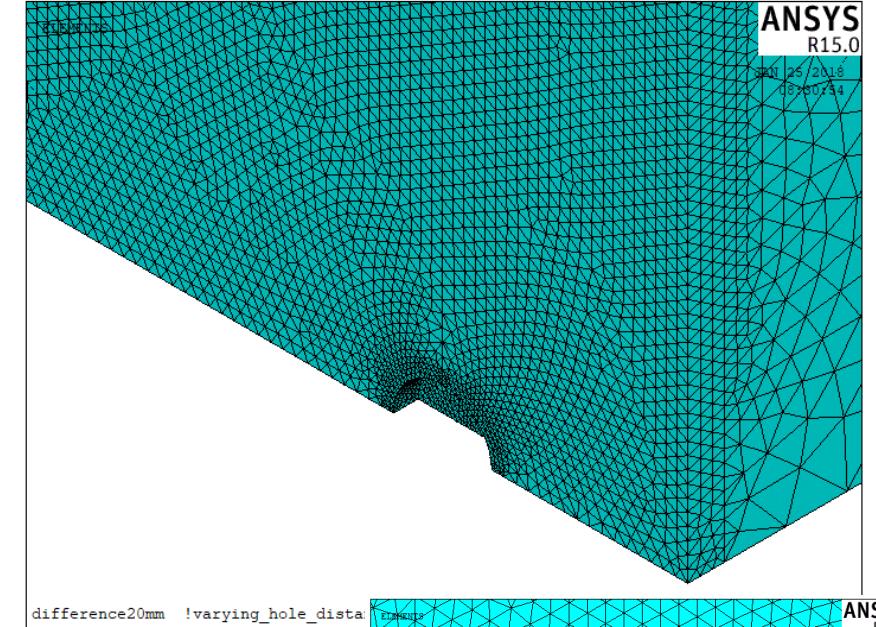
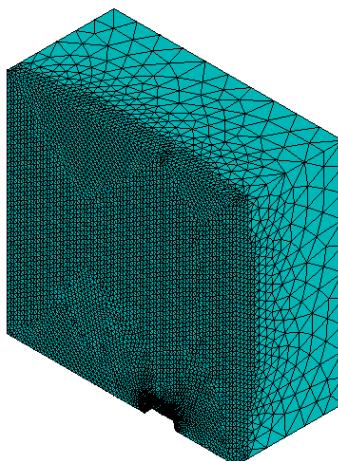


```
radius_int1=2.0
radius_ext1=2.5
ring_thickness = 0.5
```

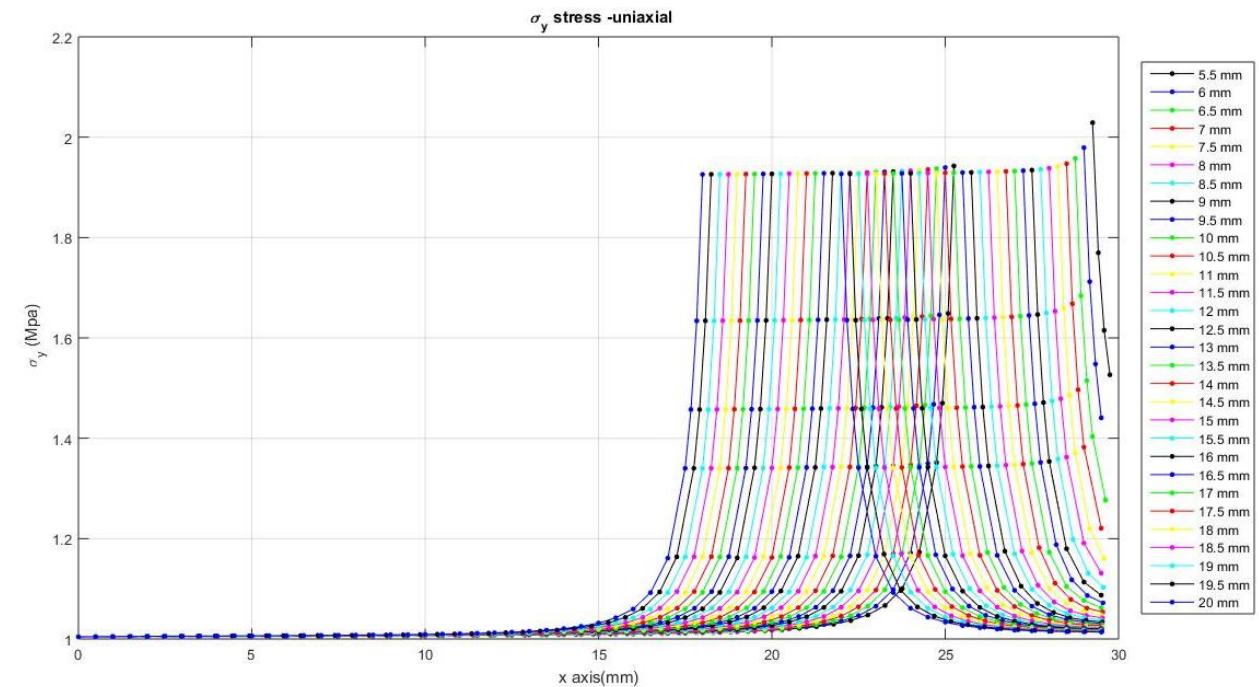
```
size_refined= 0.2
esize,size_refined

size_coarse2= 0.5
esize,size_coarse2

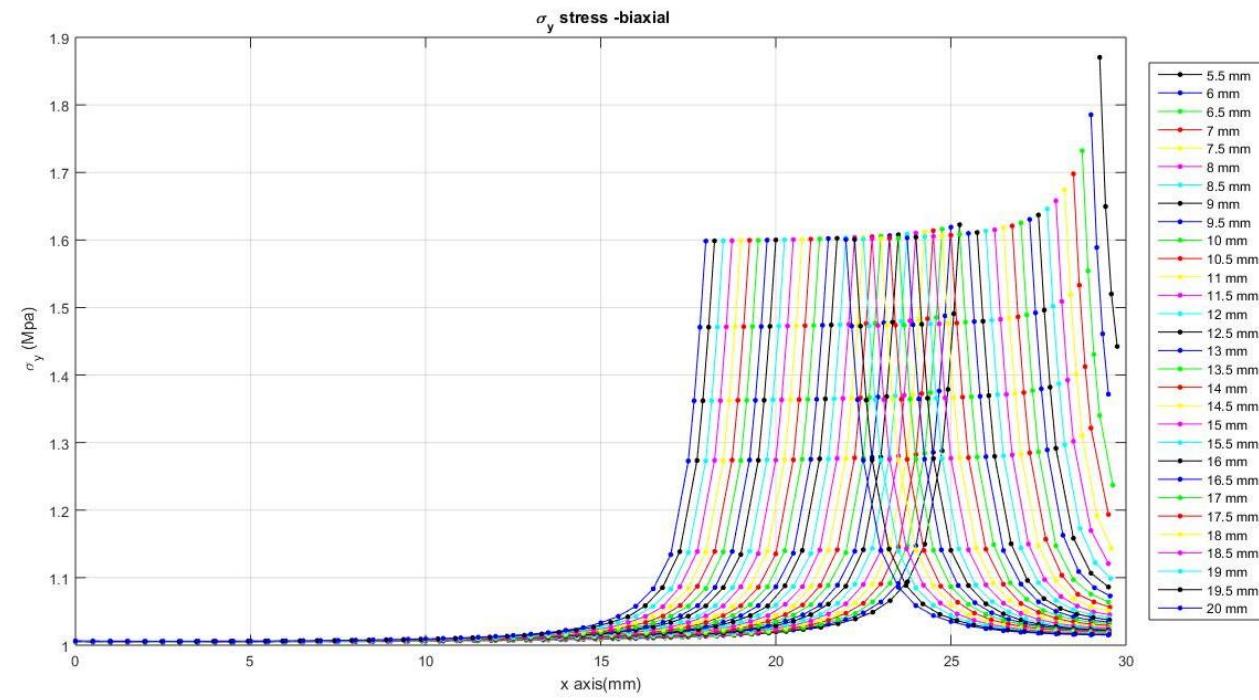
size_coarse1=3.0
esize,size_coarse1
```



A 14 mm plate and two Circular Holes with 1 mm depth

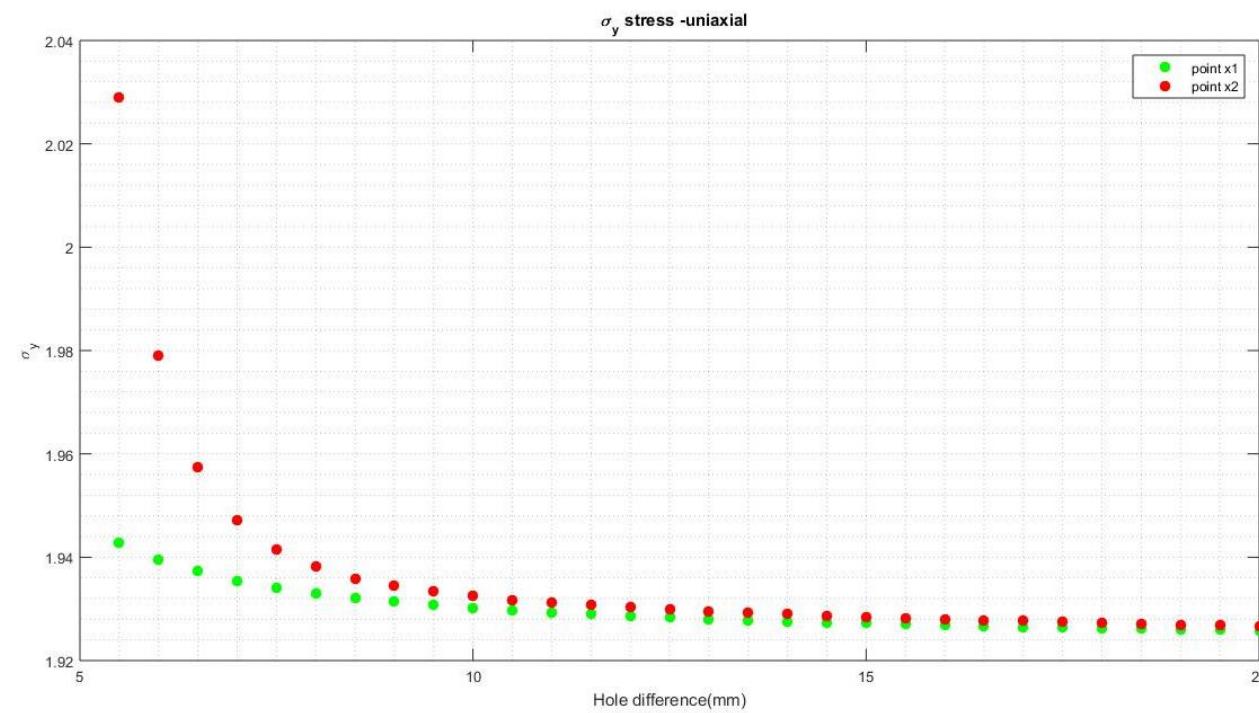


(a) Uniaxial, Transverse load

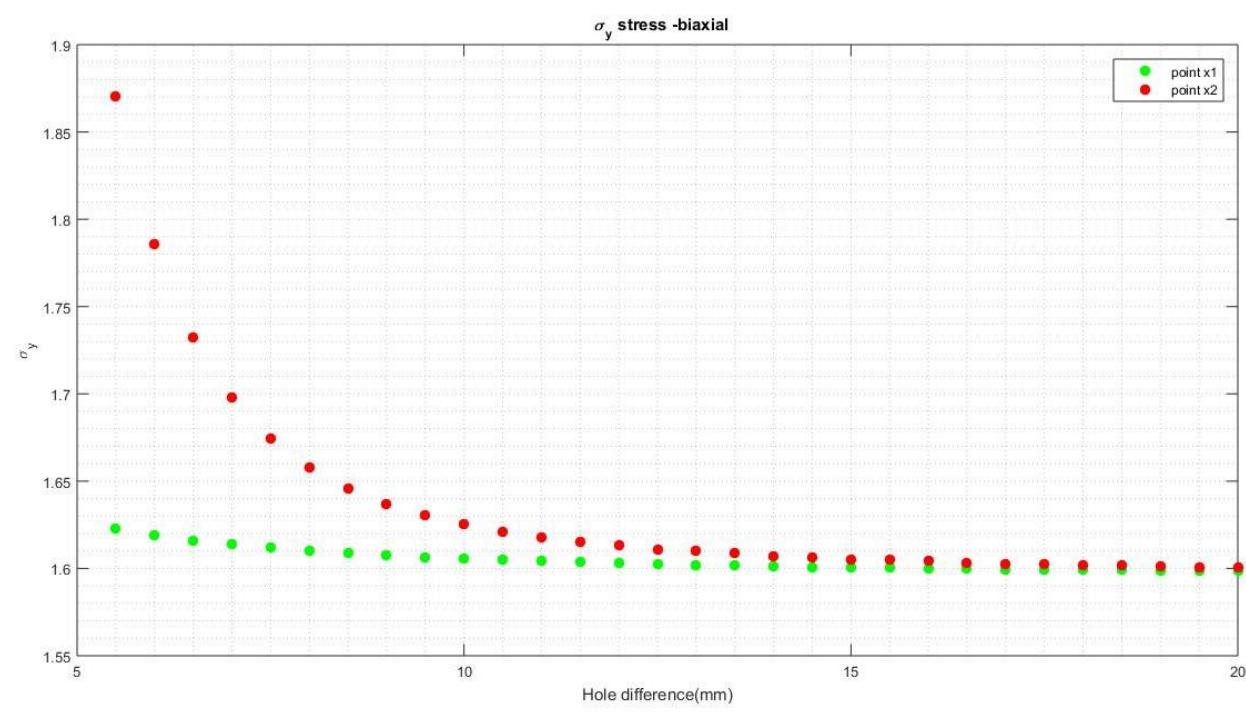


(b) Biaxial load

A 14 mm plate and two Circular Holes with 1 mm depth



(a) Uniaxial, Transverse load



(b) Biaxial load

Identified Problem

plate_1.5_depth_1.5

plate_1.5_depth_1

plate_14_depth_1

they need code repairs

Finished simulation

The problem was identified
in the **plate_14_depth_1** code.
It was repaired.

* The coarse generation
is coming before fine
(ring) mesh generation;

* The node sequence
change is not generic in
one selection command
(inside a loop) :

```
...  
! Section A3(y2/2)  
! changing nodes sequence  
asel,s,loc,y,y2/2  
nsla,s,1  
asel,s,loc,x,x2/4  
nsla,u,1  
asel,s,loc,x,x2/2  
nsla,u,1  
...
```

xcenter1



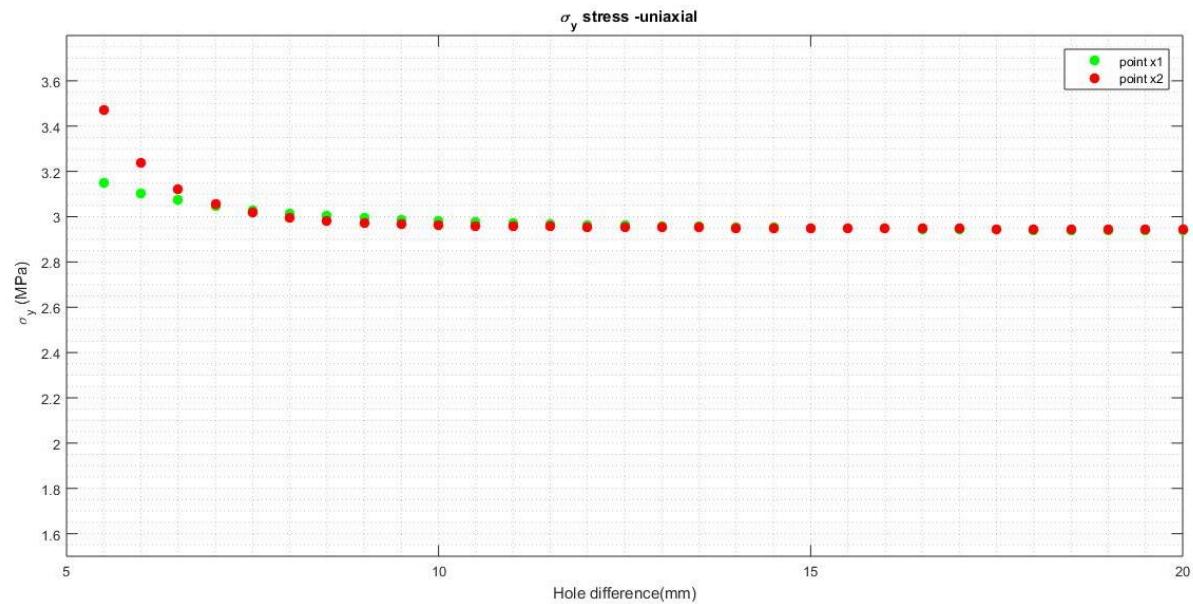
Files -> folders

- plate_1.5_depth_1.5
- plate_1.5_depth_1
- plate_14_depth_1
- **plate_1.5_depth_1.5**
 - varying_hole_distance_with_refined_mesh_region_and_different_ring_thickness
 - C:\Manasses\varying_hole_distance_with_refined_mesh_region_and_different_ring_thickness\uniaxial
 - ?
- **plate_1.5_depth_1**
 - varying_hole_distance_plate_1.5_depth_1_refined_mesh_region_ring
 - C:\Manasses\varying_hole_distance_plate_1.5_depth_1_refined_mesh_region_ring\uniaxial
 - C:\Manasses\varying_hole_distance_plate_1.5_depth_1_refined_mesh_region_ring\biaxial
- **plate_14_depth_1**
 - varying_hole_distance_plate_14_depth_1_refined_mesh_region_ring
 - C:\Manasses\varying_hole_distance_plate_14_depth_1_refined_mesh_region_ring\uniaxial
 - C:\Manasses\varying_hole_distance_plate_14_depth_1_refined_mesh_region_ring\biaxial

three_geometries_comparison_same _scale

- `plate_1.5_depth_1.5`
- `plate_1.5_depth_1`
- `plate_14_depth_1`

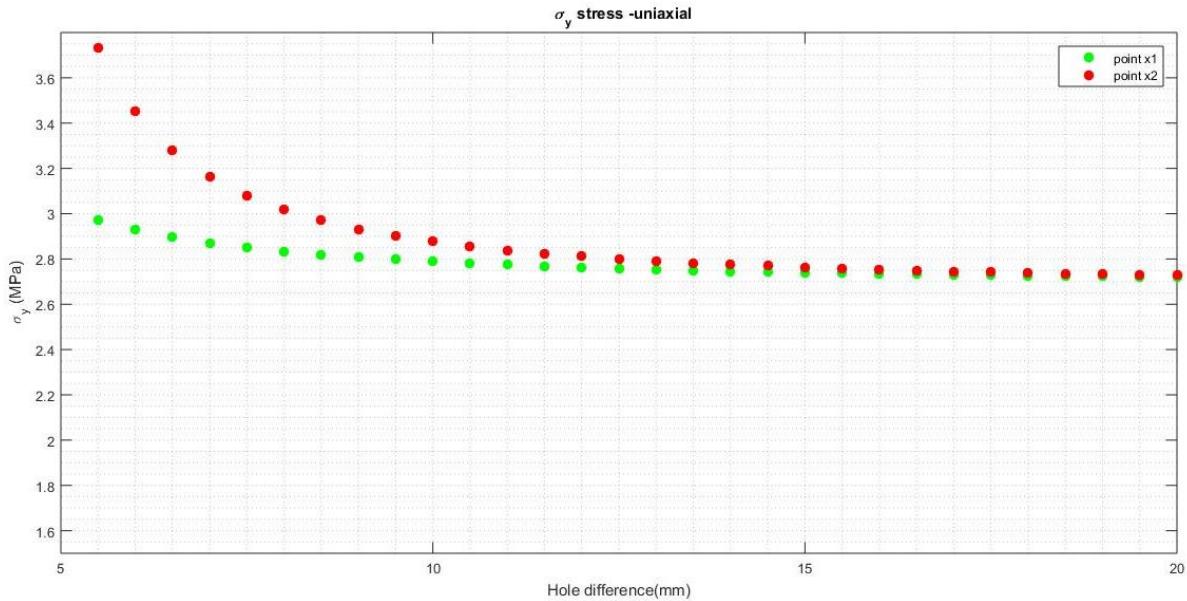
plate_1.5_depth_1.5



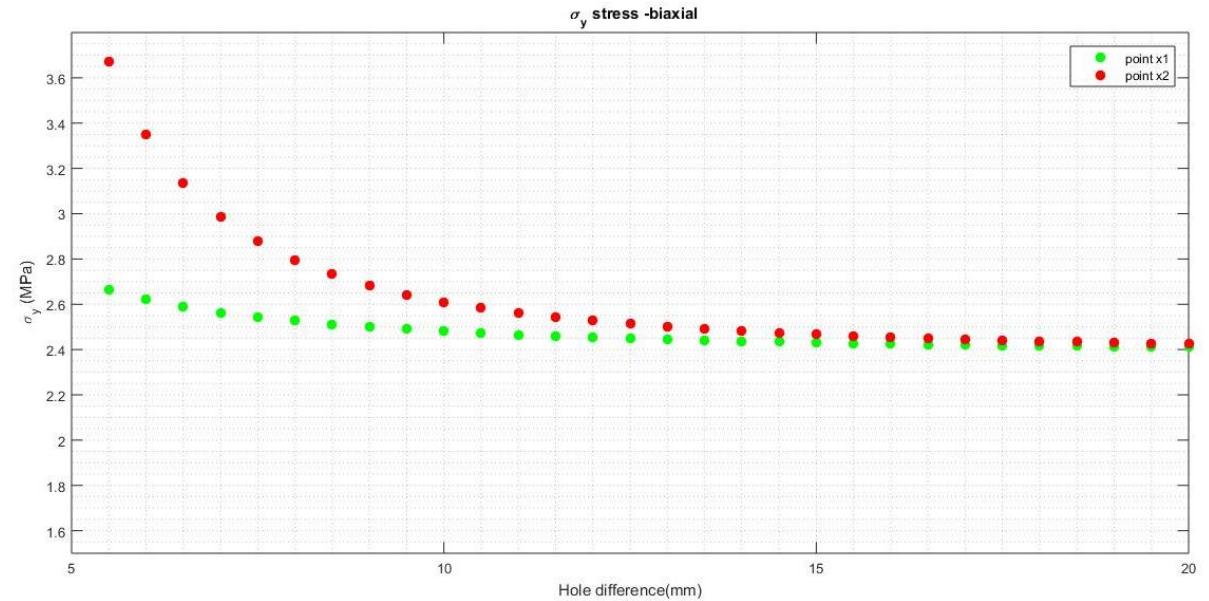
(a) Uniaxial, Transverse load

(b) Biaxial load

plate_1.5_depth_1

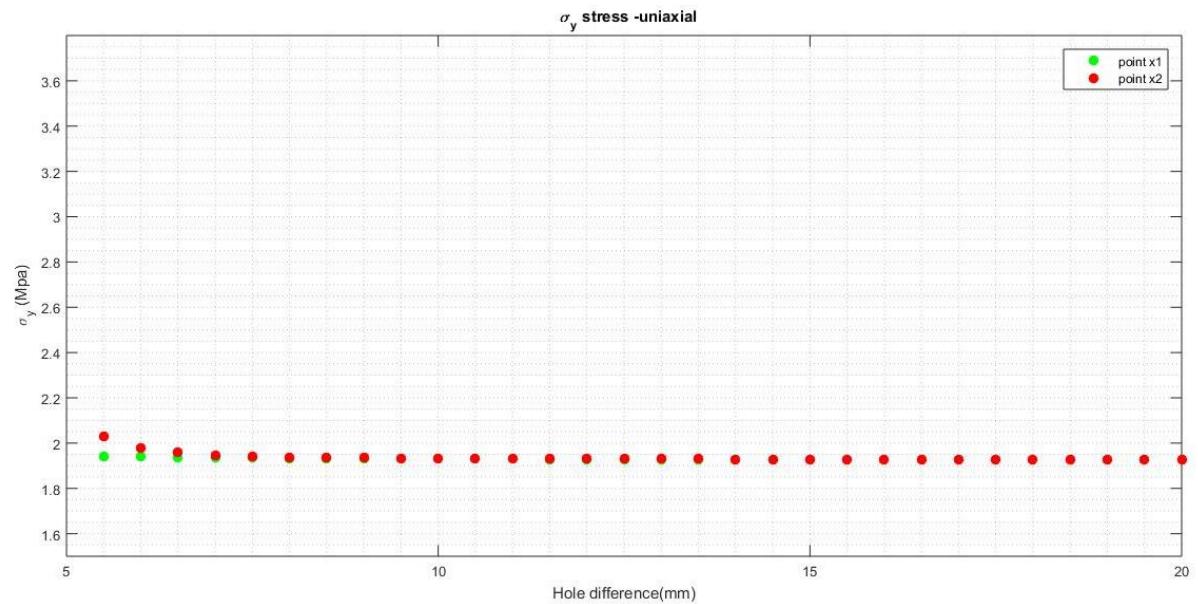


(a) Uniaxial, Transverse load

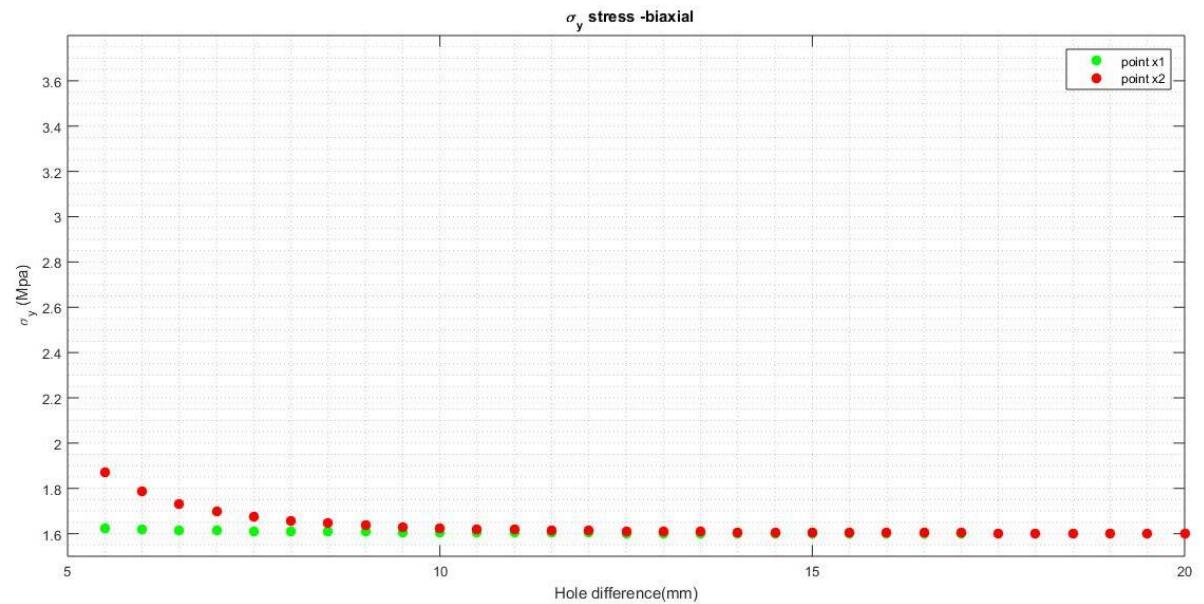


(b) Biaxial load

plate_14_depth_1



(a) Uniaxial, Transverse load



(b) Biaxial load

Repairing the Code Problem

➤ **plate_1.5_depth_1.5 → changing name folder**

varying_hole_distance_with_refined_mesh_region_and_different_ring_thickness

varying_hole_distance_plate_1.5_depth_1.5_refined_mesh_region_ring

C:\Manasses\varying_hole_distance_plate_1.5_de

C:\Manasses\varying_hole_distance_with_refined

?

Identified Problem

plate_1.5_depth_1.5 → they need code repairs
plate_1.5_depth_1 → they need code repairs

plate_14_depth_1 → Finished simulation

The problem was identified
in the **plate_14_depth_1** code.
It was repaired.

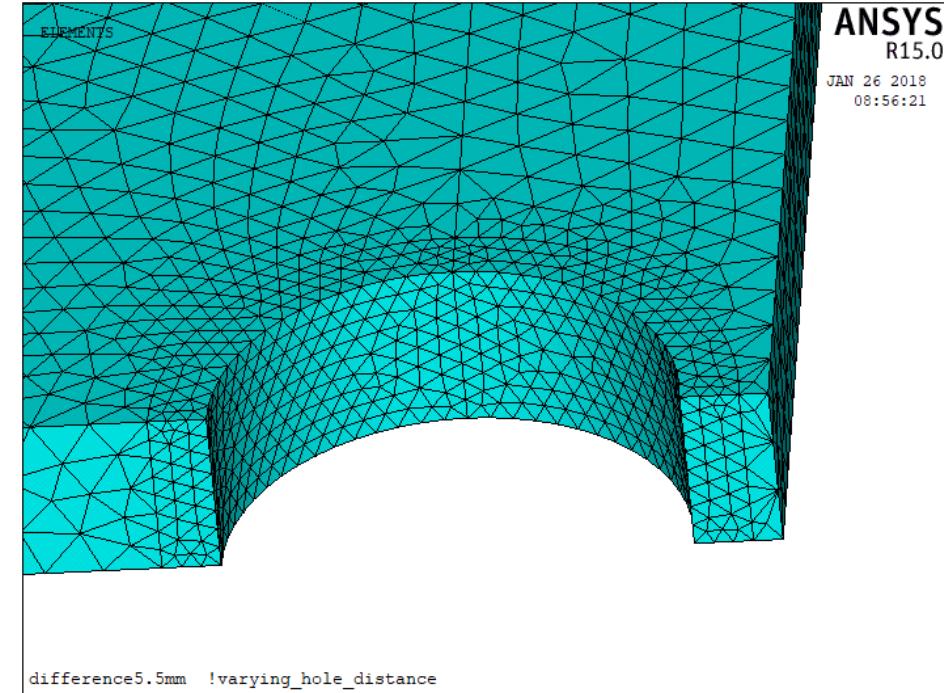
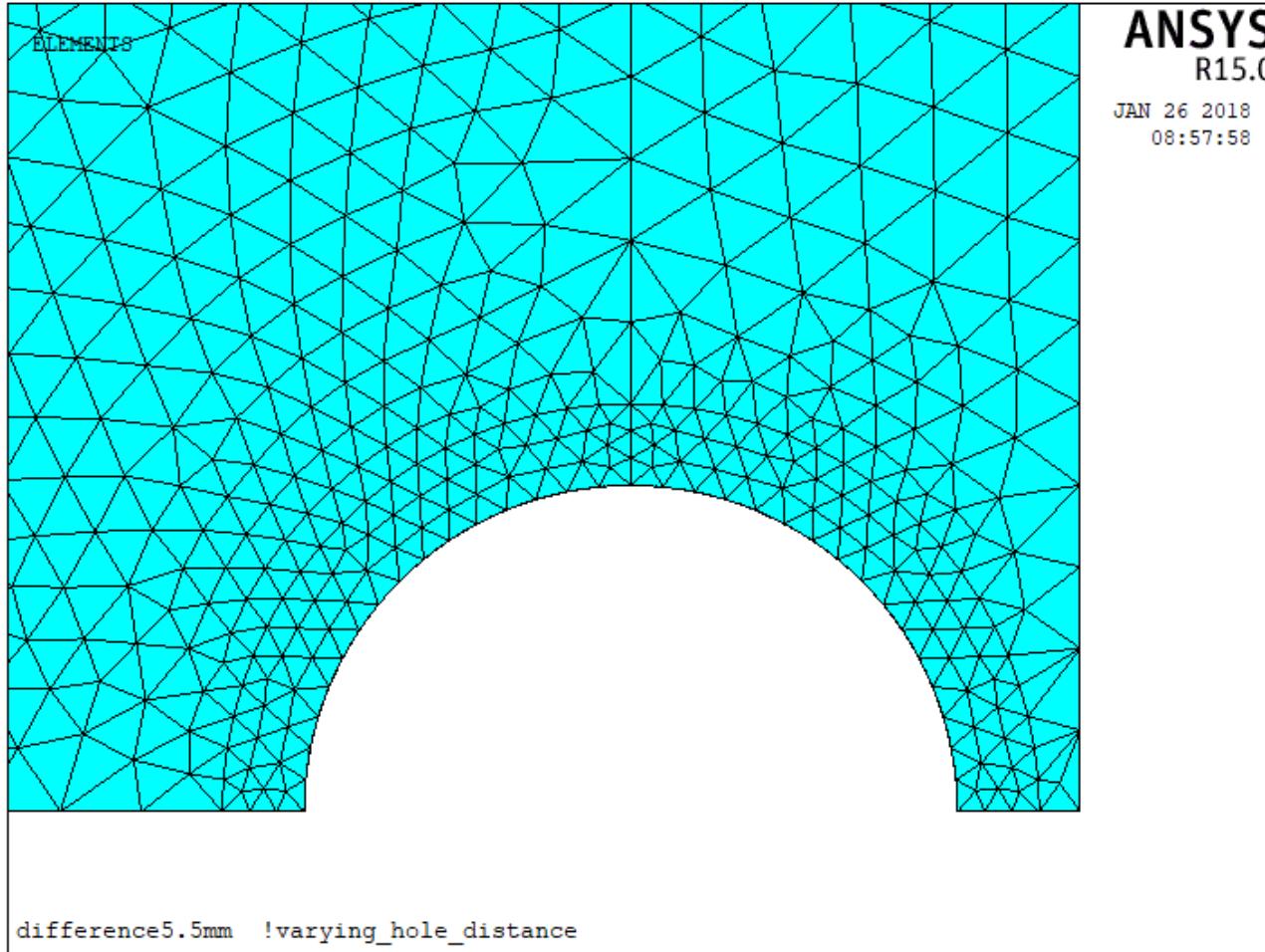
* The coarse generation
is coming before fine
(ring) mesh generation;

* The node sequence
change is not generic in
one selection command
(inside a loop):

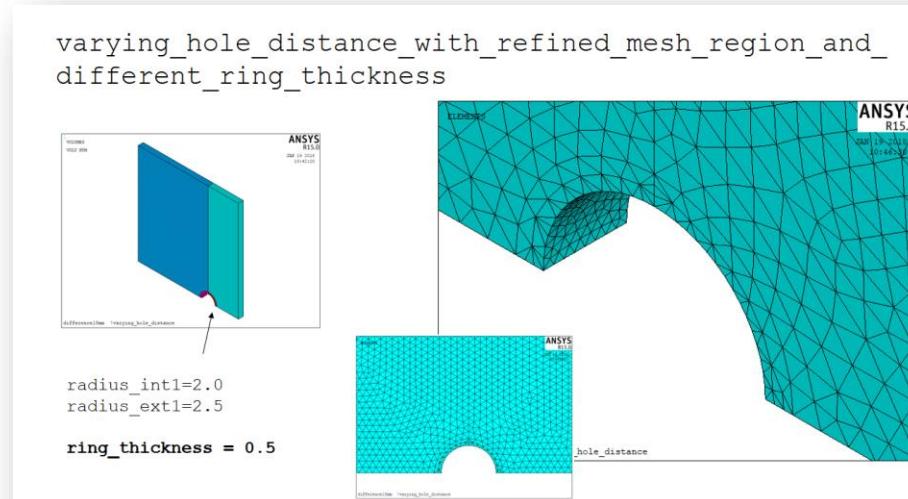
...
! Section A3(y2/2)
!changing nodes sequence
asel,s,loc,y,y2/2
nsla,s,1
asel,s,loc,x,x2/4
nsla,u,1
asel,s,loc,x,x2/2
nsla,u,1
...

xcenter1

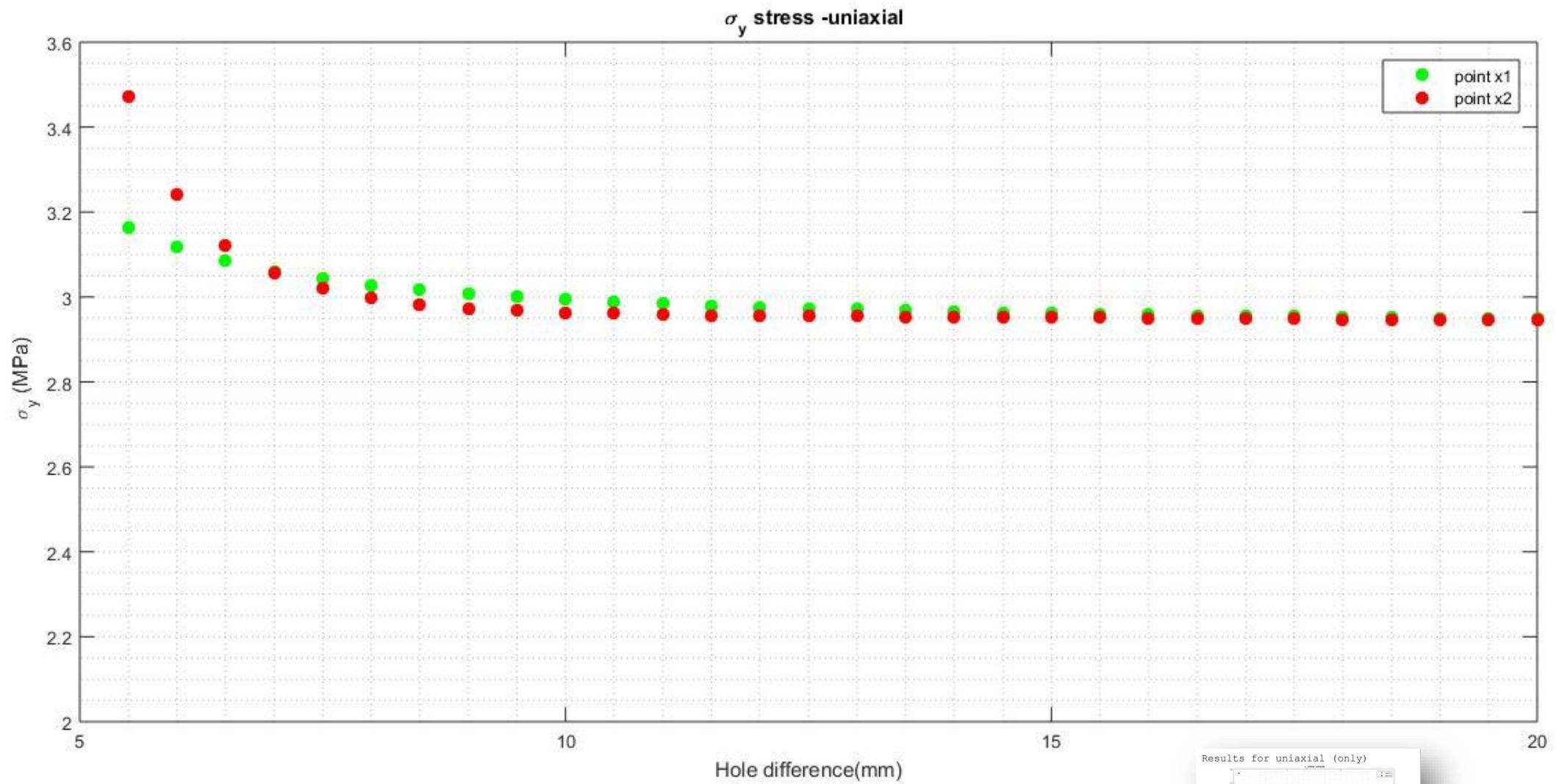
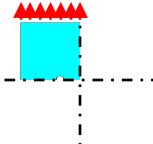
plate_1.5_depth_1.5



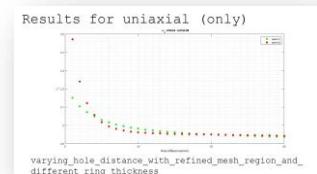
Comparison with the previous geometry code



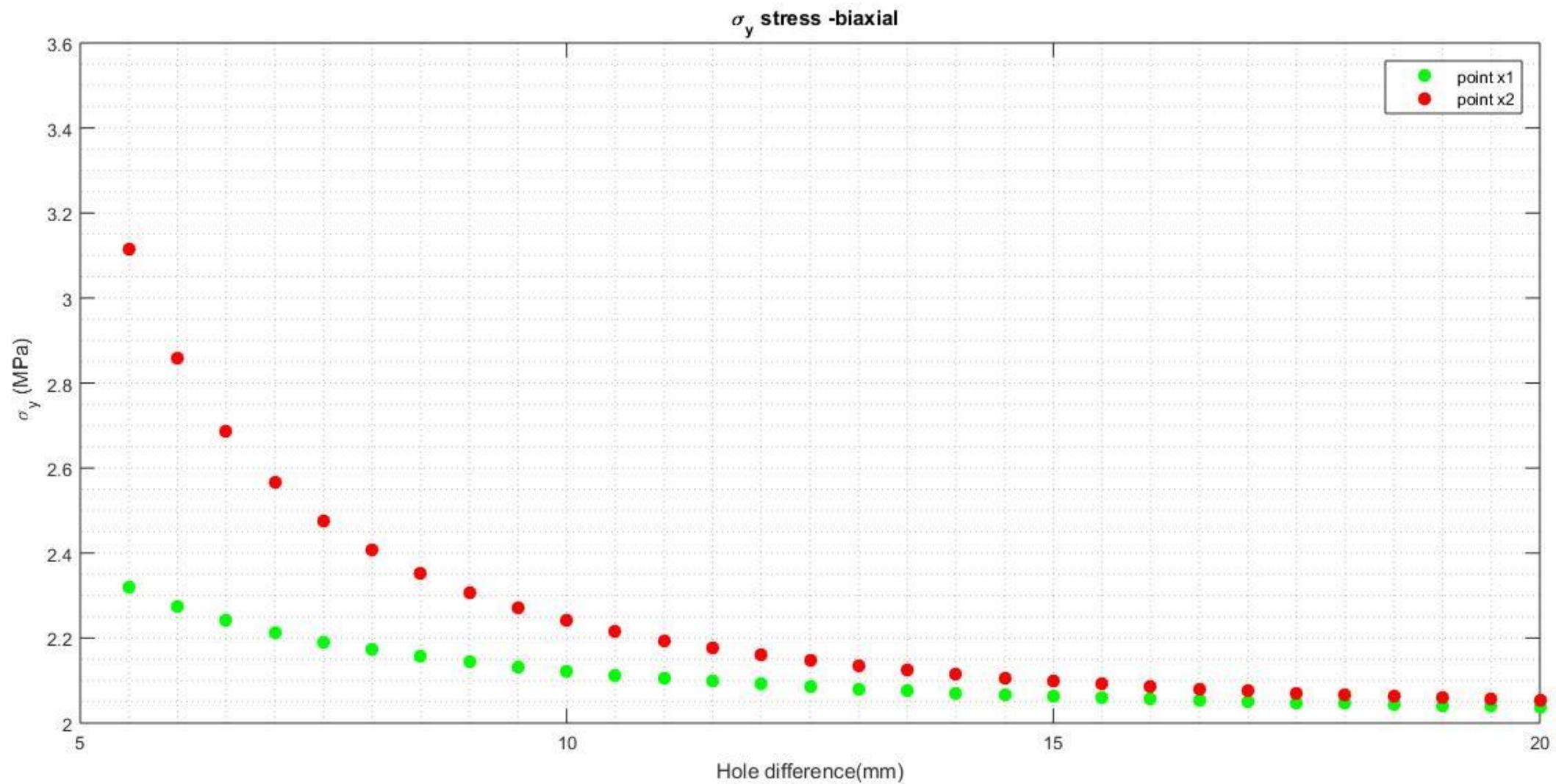
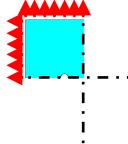
plate_1.5_depth_1.5



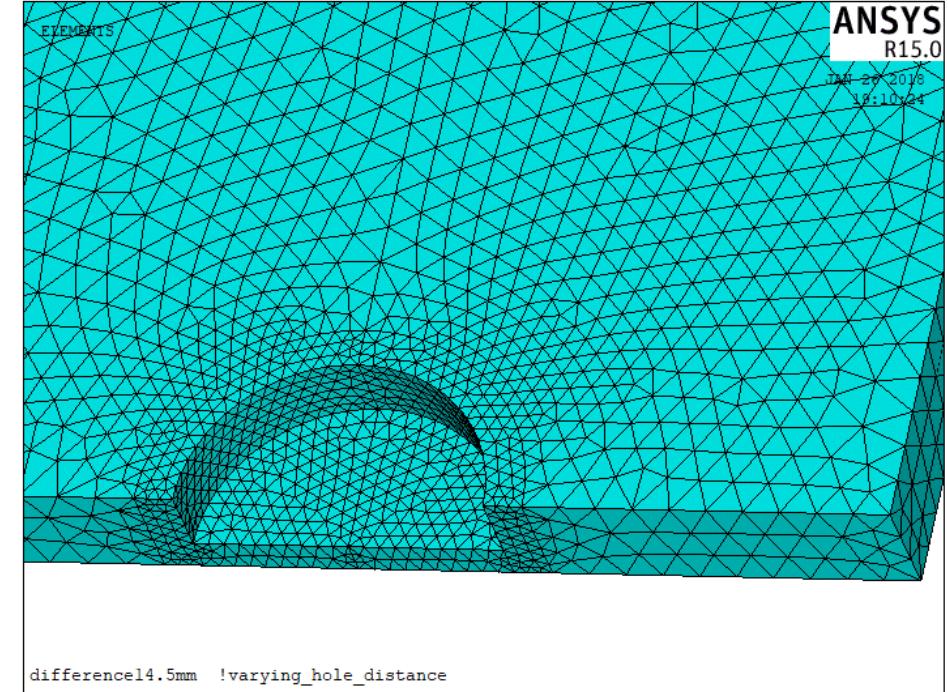
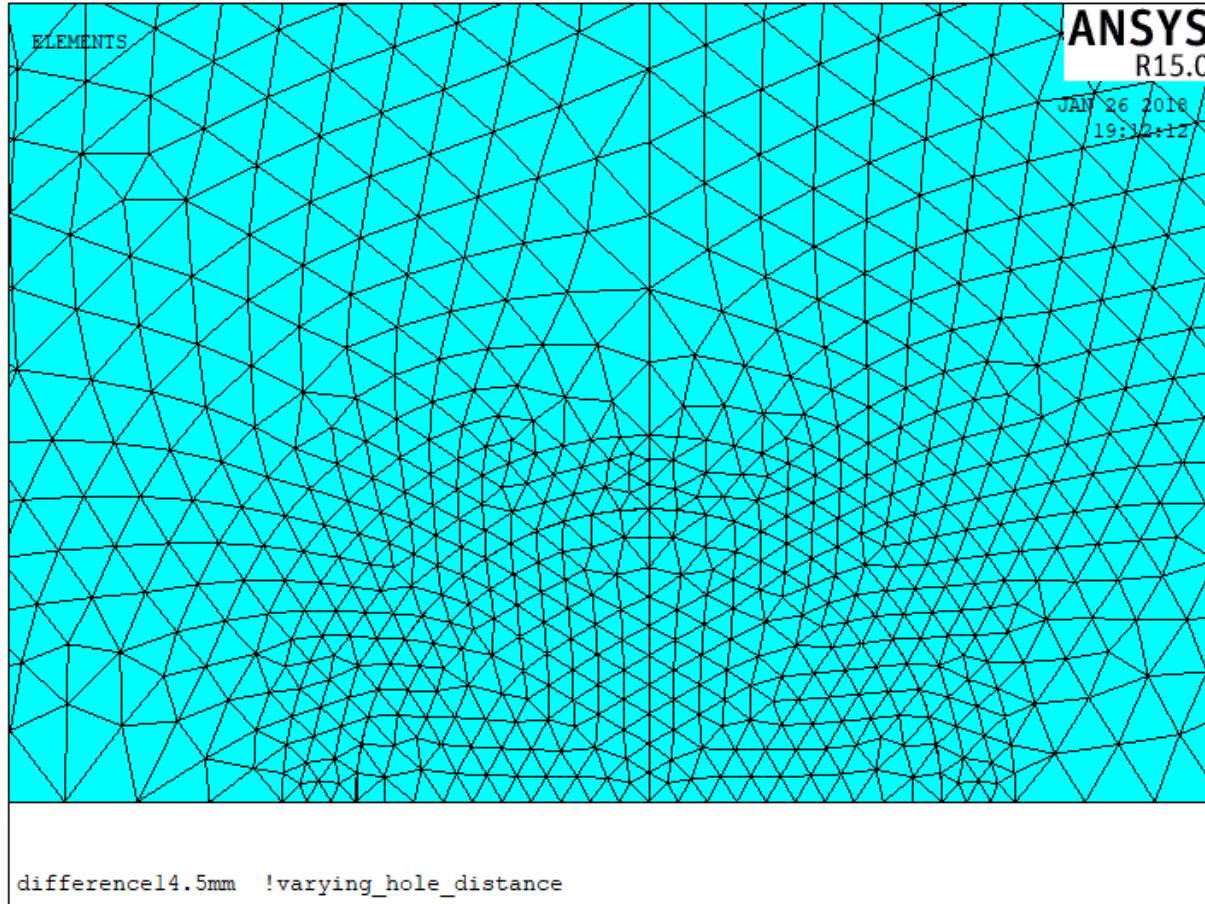
Comparison with the previous geometry code →



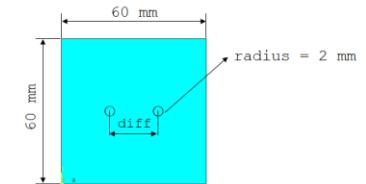
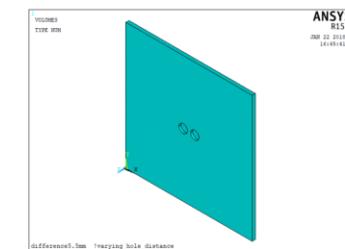
plate_1.5_depth_1.5



plate_1.5_depth_1



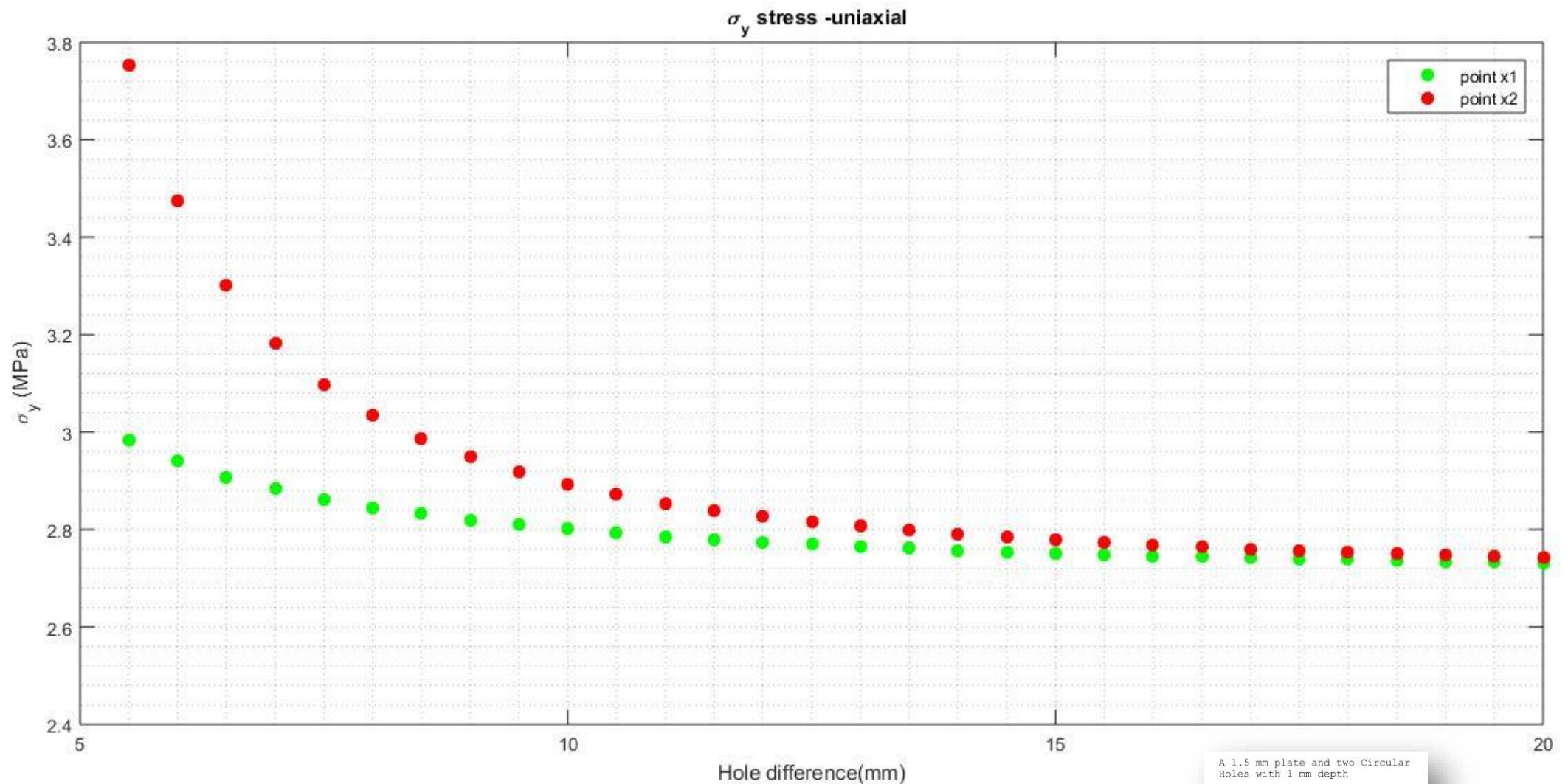
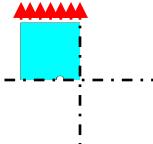
A 1.5 mm plate and two Circular Holes with 1 mm depth



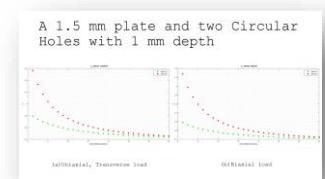
plate_thickness = 1.5 mm
depth = 1.0 mm
"cylindrical hole"

- Varying the hole distance

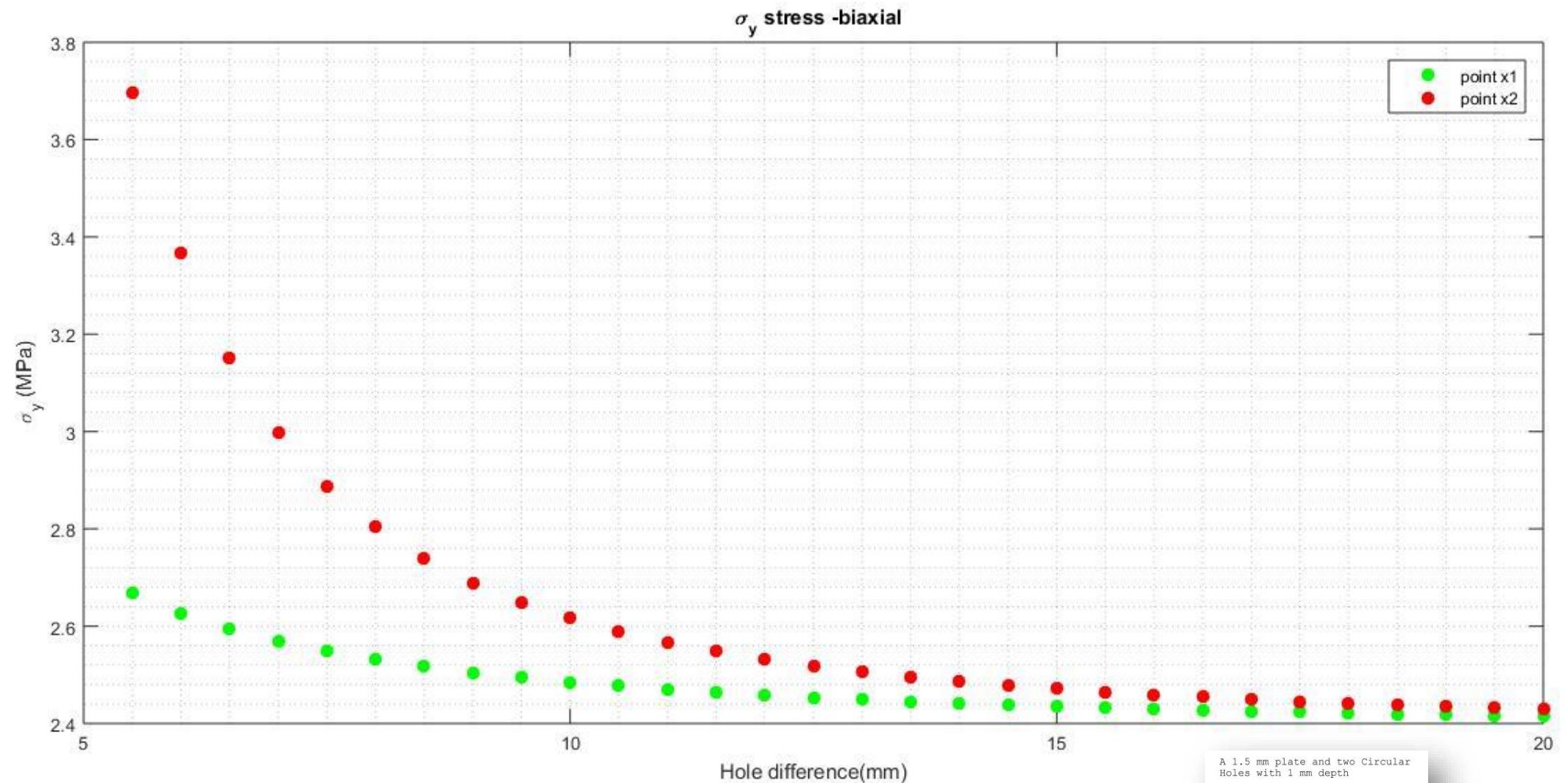
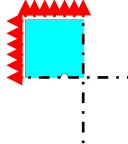
plate_1.5_depth_1



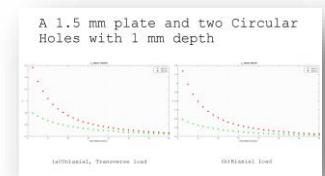
Comparison with the previous geometry code →



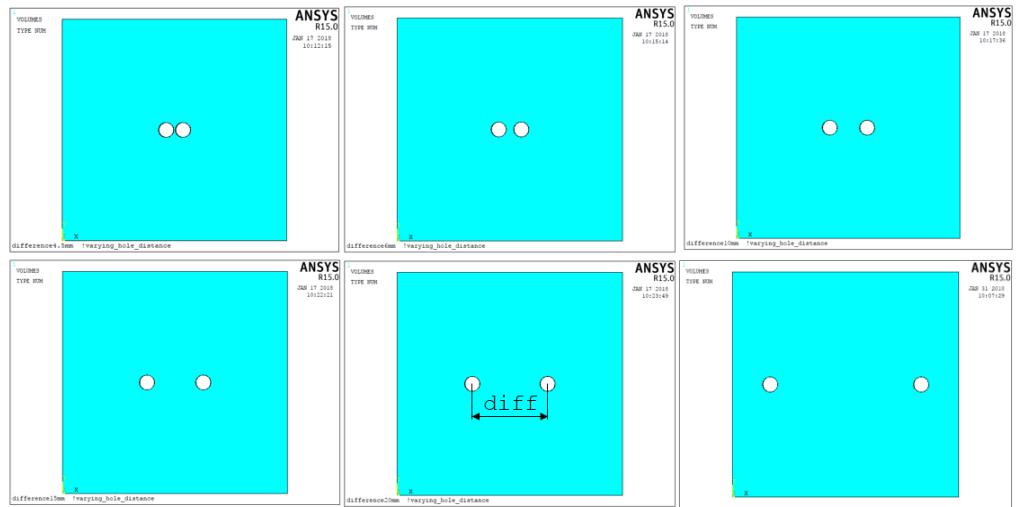
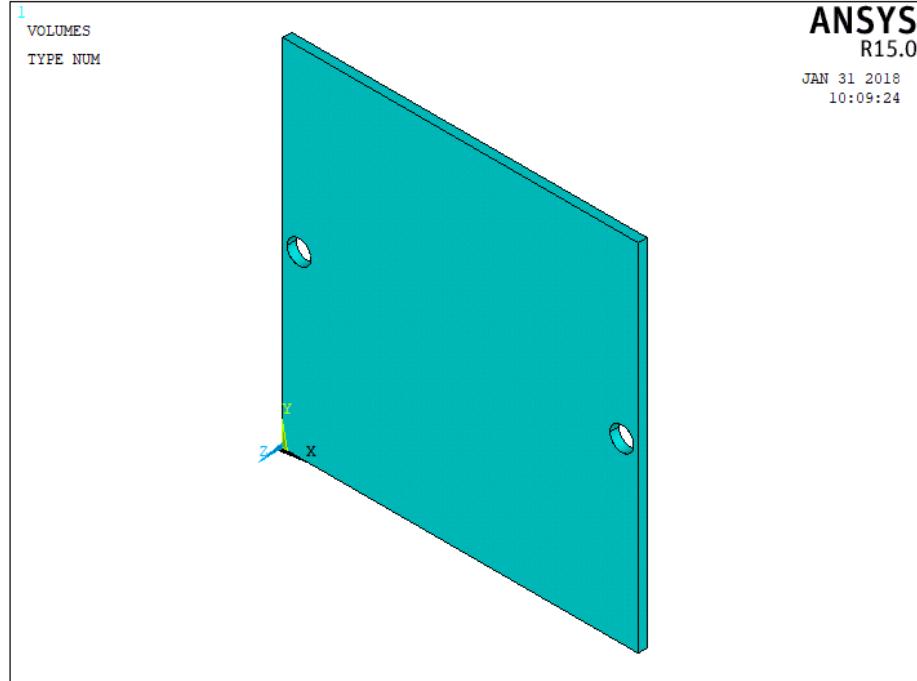
plate_1.5_depth_1



Comparison with the previous geometry code →



Extending Range



```
inicial = 25 !mm  
final = 54.5 !mm  
incr = 5 !mm
```

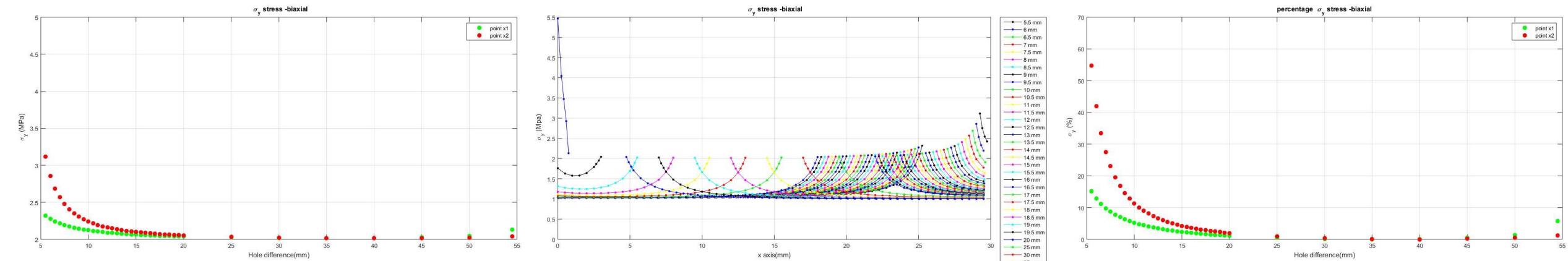
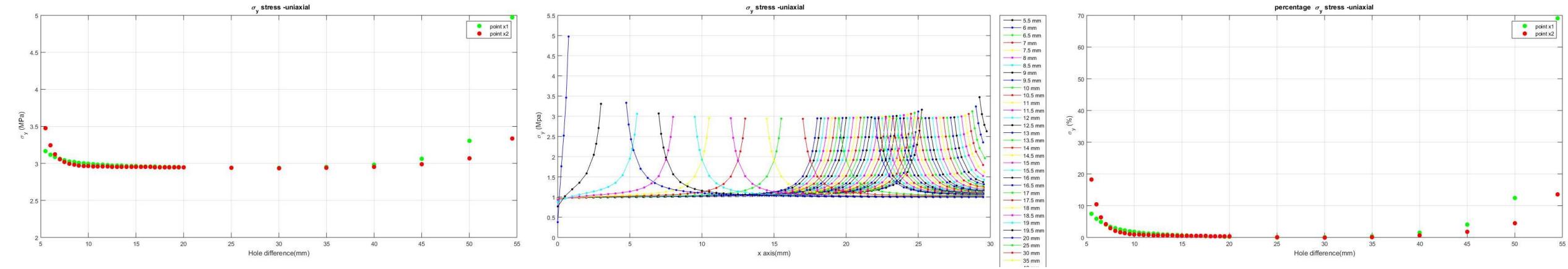
```
*do, diff, inicial, final, incr
```

```
...
```

```
...
```

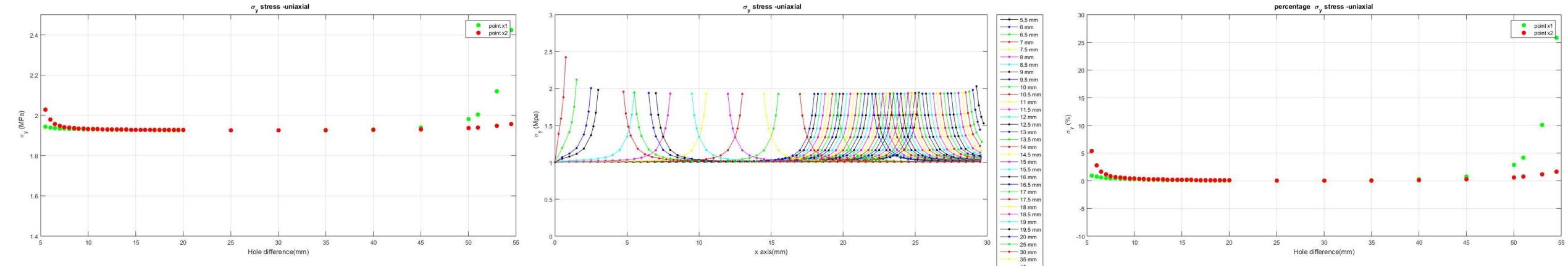
```
*enddo
```

plate_1.5_depth_1.5_through_hole

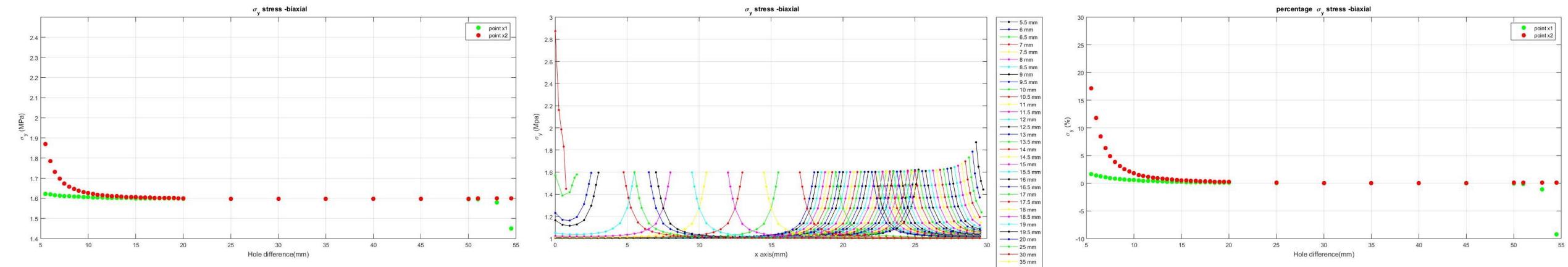


(b) Biaxial load

plate_14_depth_1

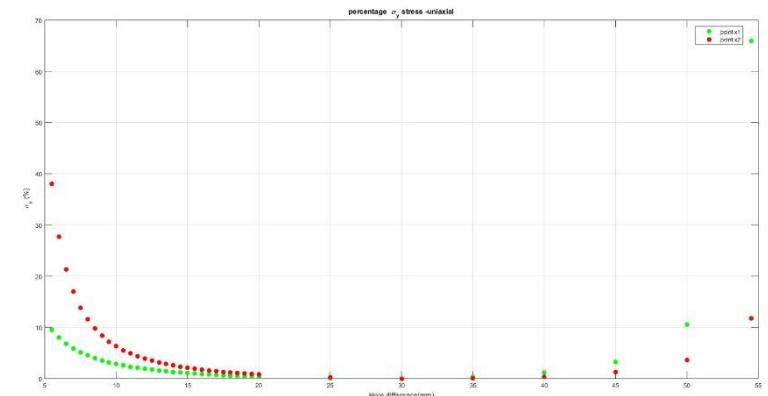
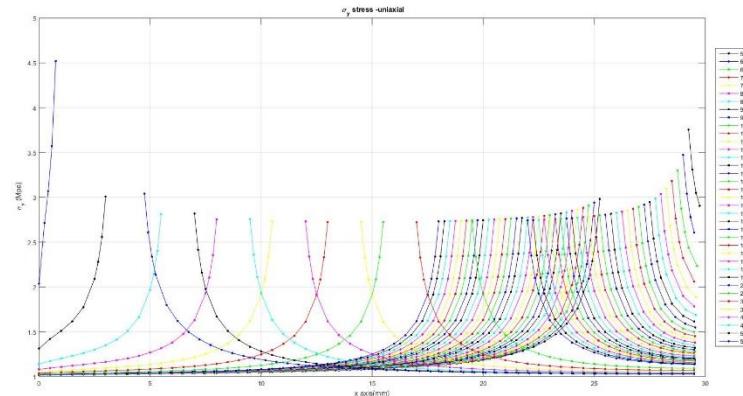
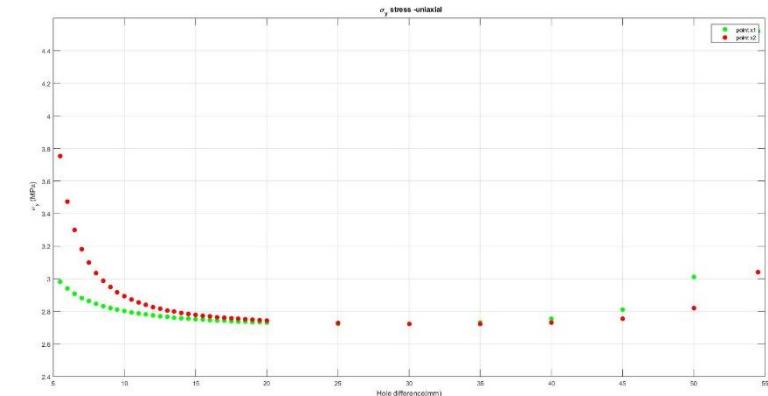


(a) Uniaxial, Transverse load

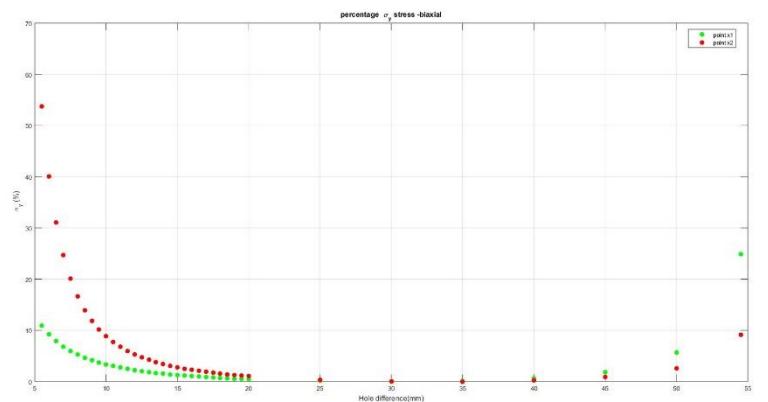
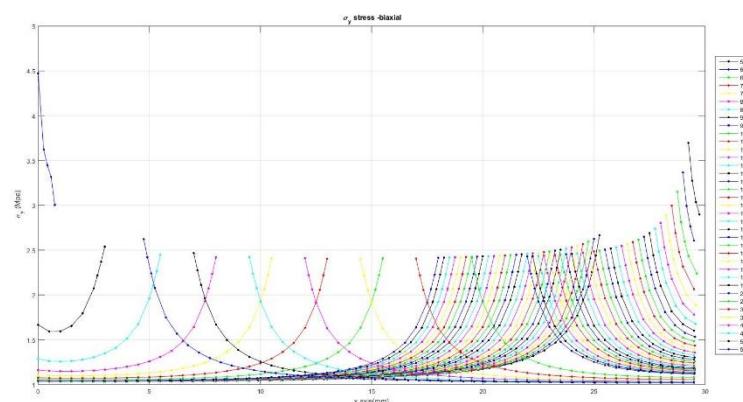
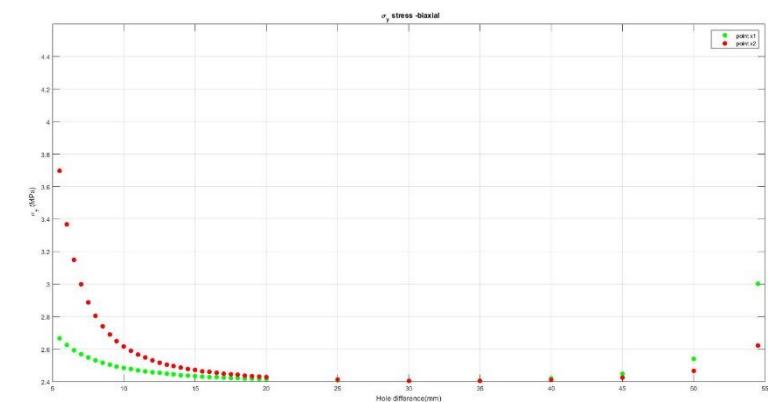


(b) Biaxial load

plate_1.5_depth_1



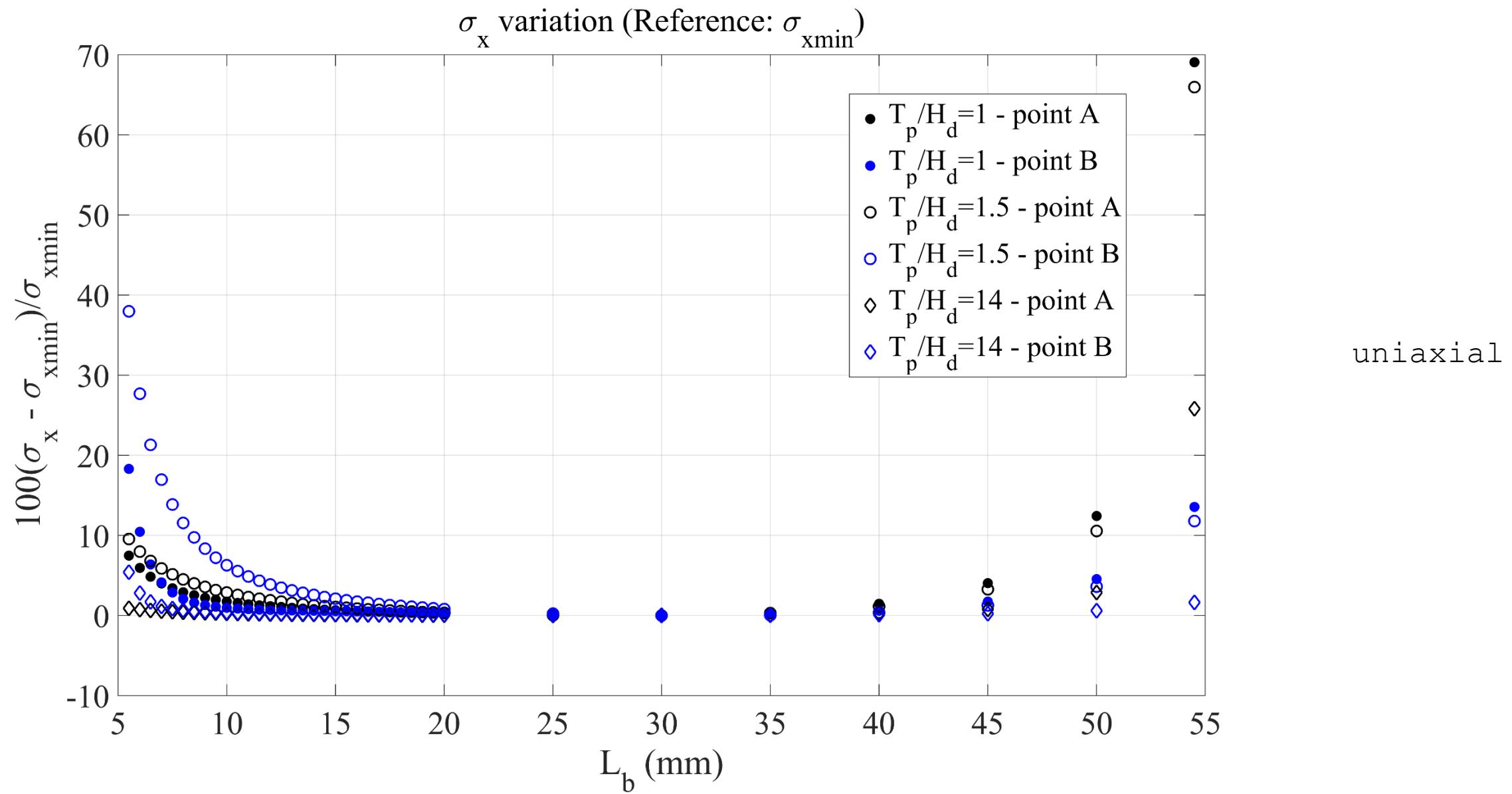
(a) Uniaxial, Transverse load



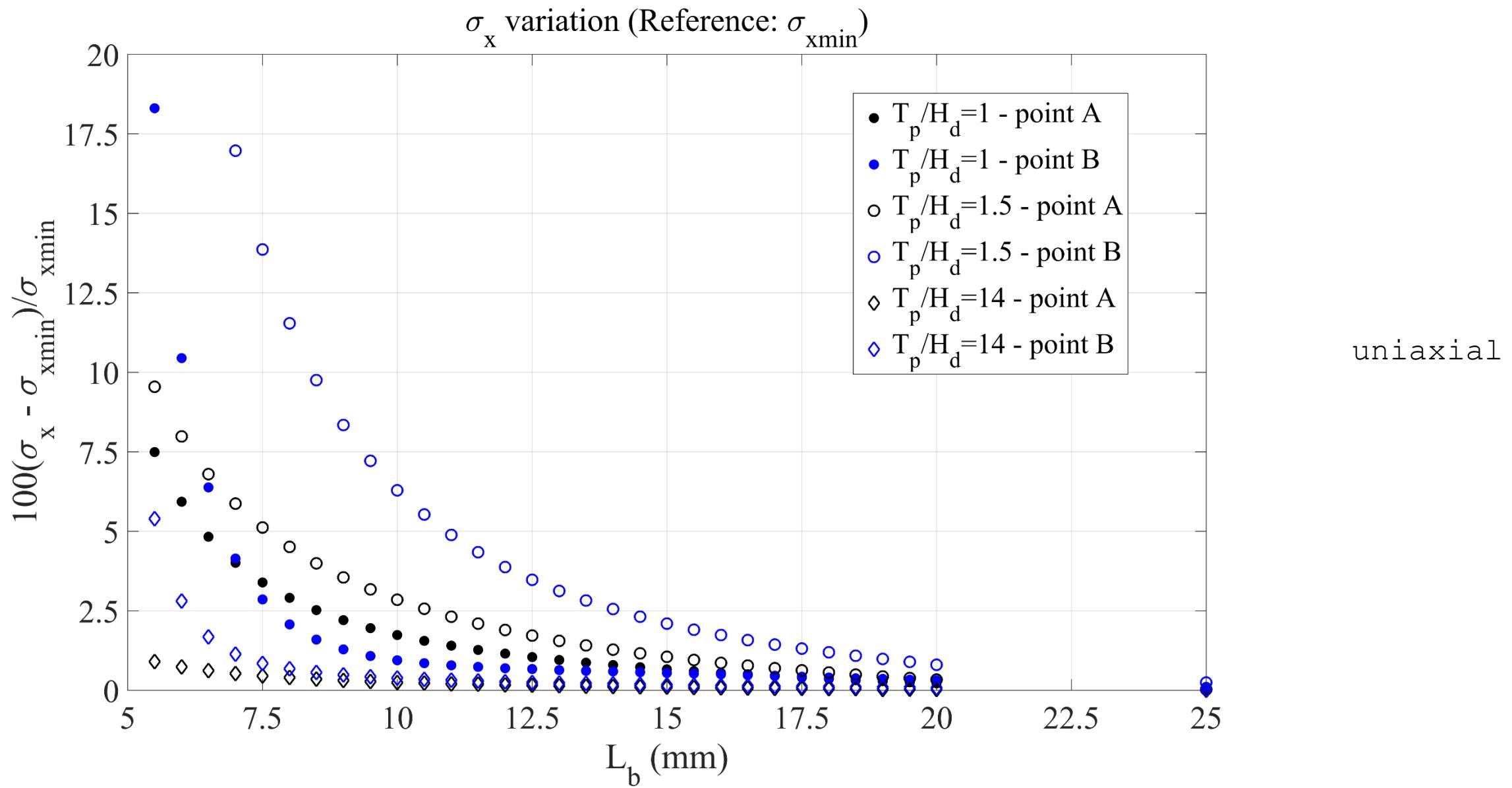
(b) Biaxial load

Prepare slides -> problem
description

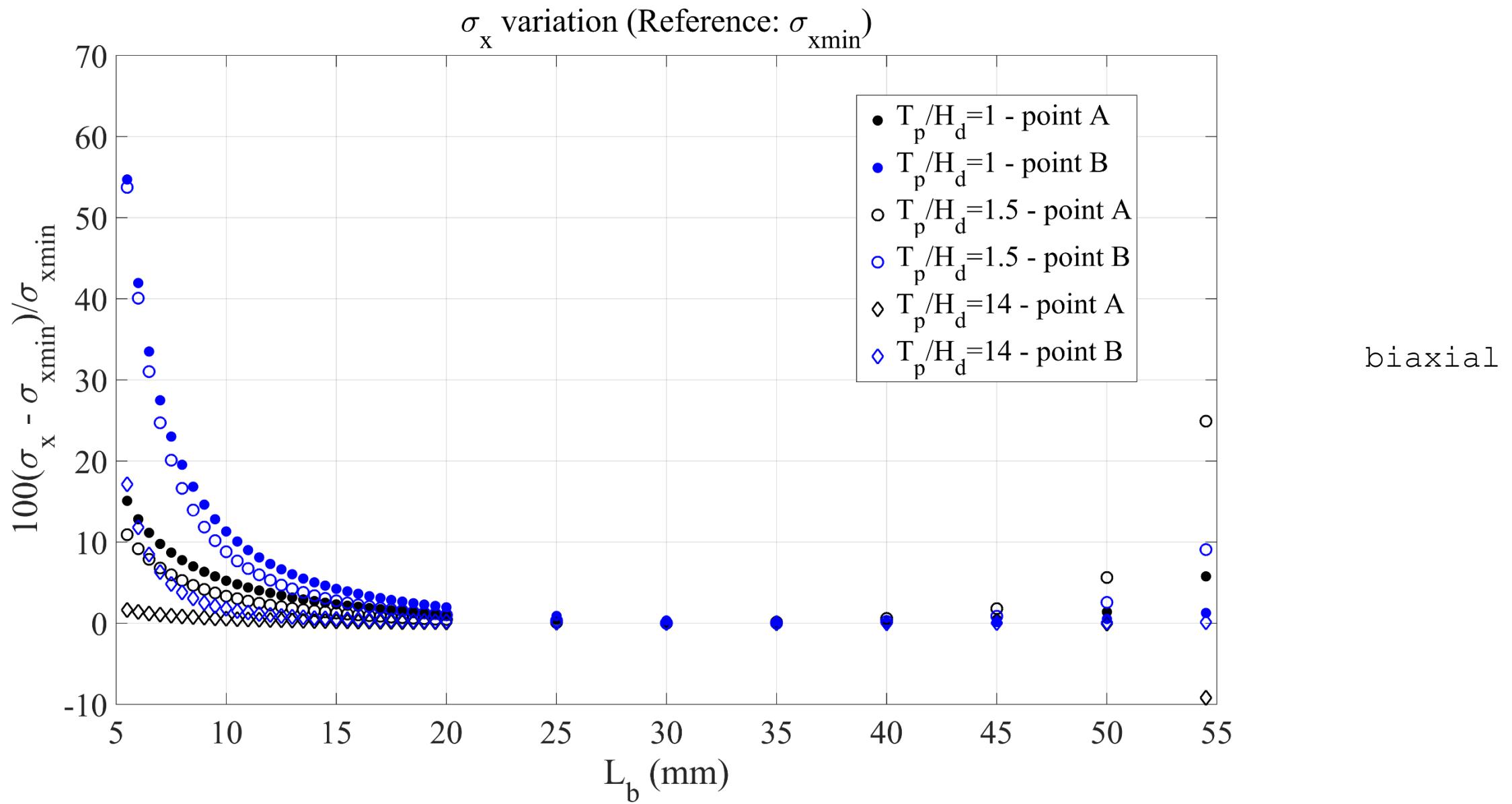
all_uniaxial_biaxial_3_geometries



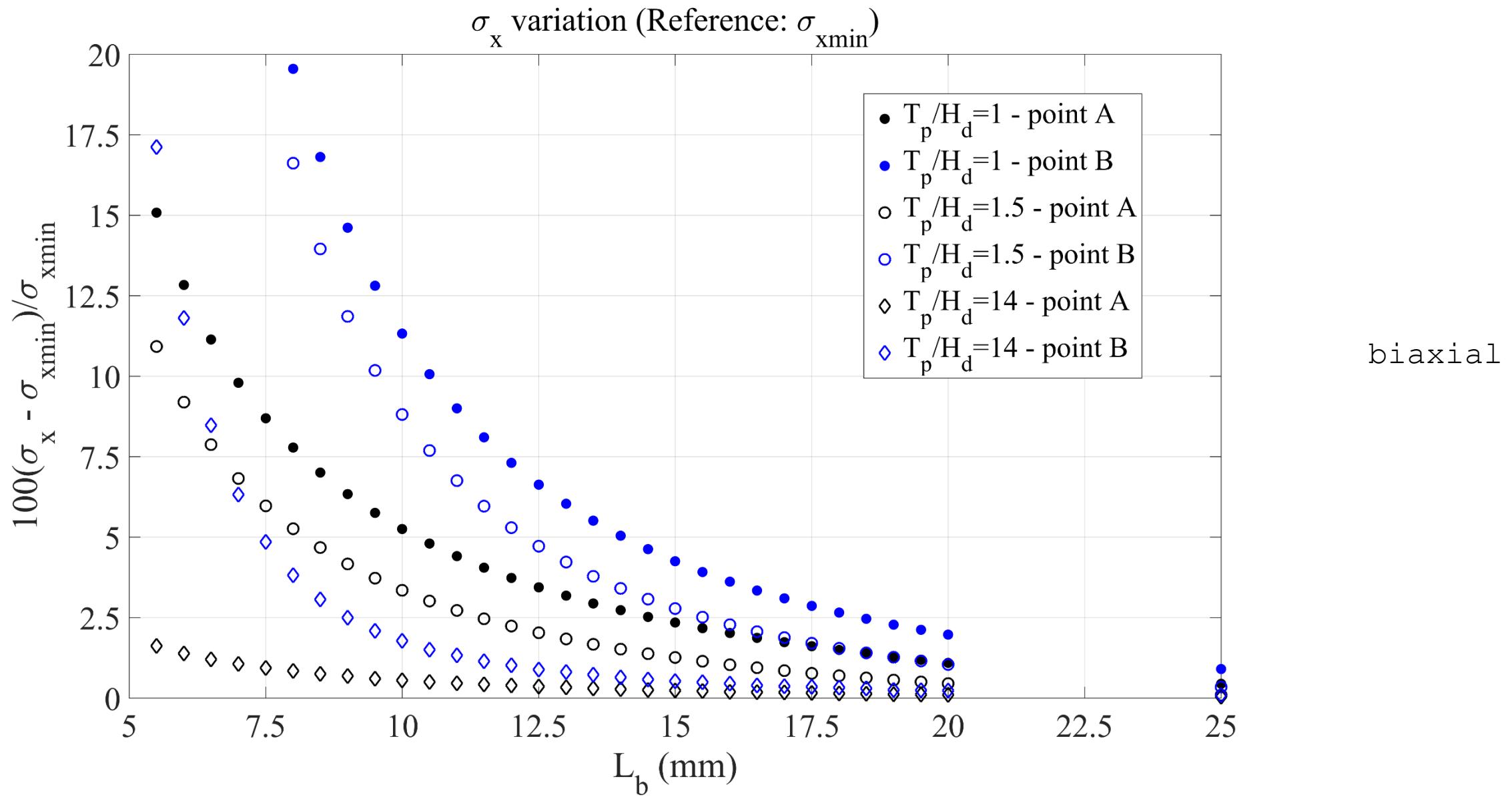
all_uniaxial_biaxial_3_geometries



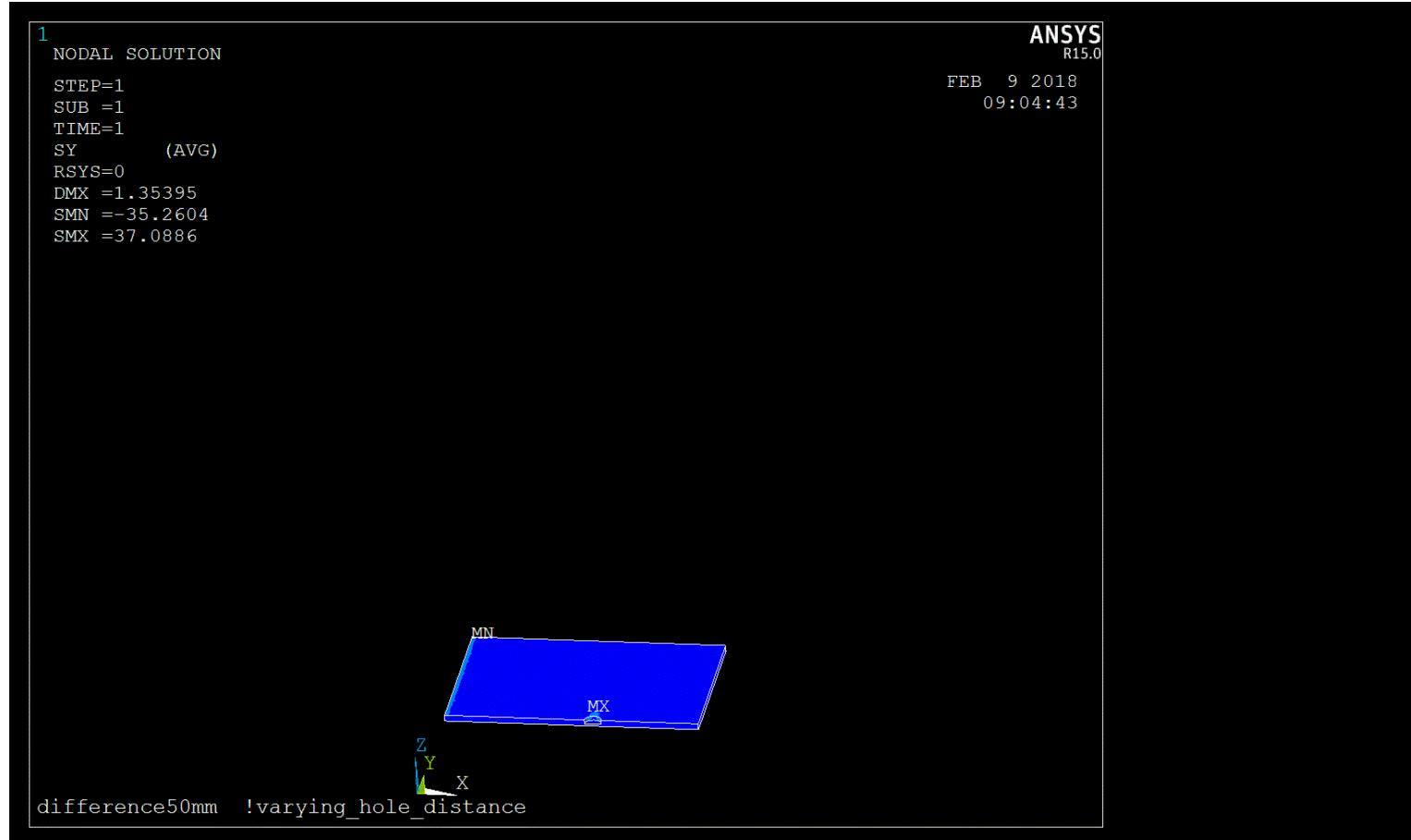
all_uniaxial_biaxial_3_geometries



all_uniaxial_biaxial_3_geometries



<https://convertio.co/pt/avi-converter/>



varying_hole_distance_bending

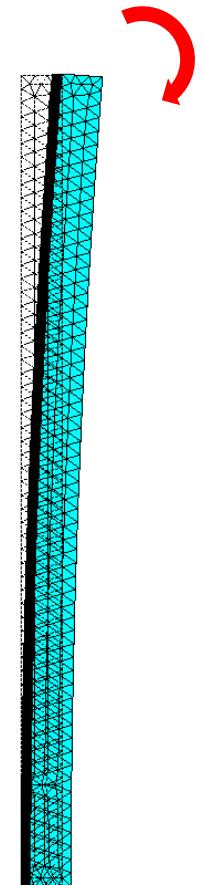
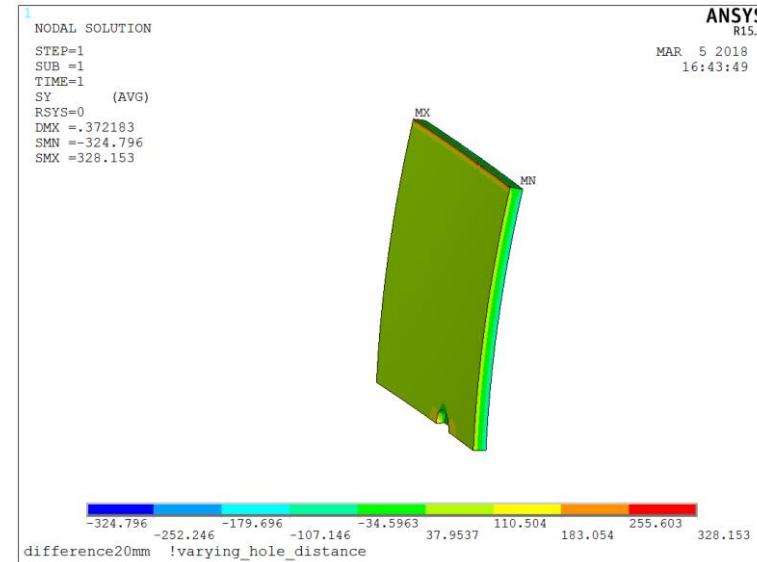
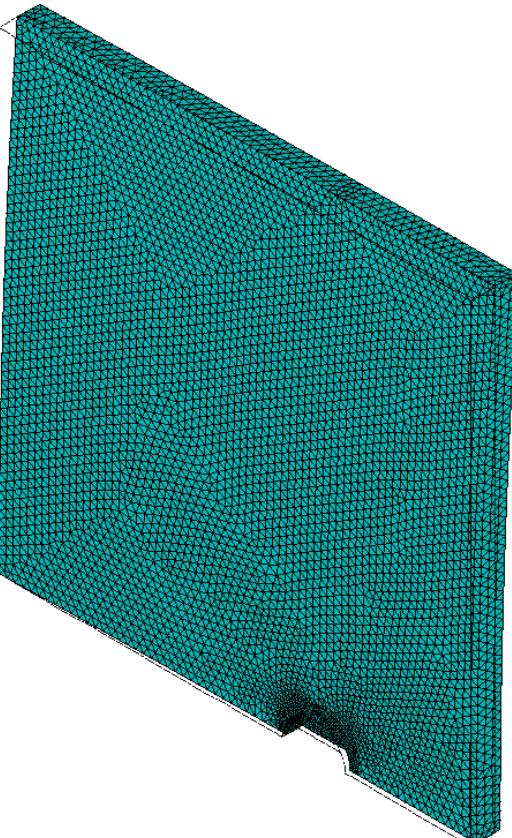
```
! BENDING  
! apply displacements conditions at the nodes of the line:  
! x=0, z=0
```

```
allsel  
lsel,s,loc,y,y2  
lsel,r,loc,z,z1  
nsll,s  
d,all,uy,0.0145
```

```
allsel  
lsel,s,loc,x,x1  
lsel,r,loc,z,z1  
nsll,s  
d,all,ux,-0.0145
```

```
allsel  
lsel,s,loc,y,y2  
lsel,r,loc,z,-z2  
nsll,s  
d,all,uy,-0.0145
```

```
allsel  
lsel,s,loc,x,x1  
lsel,r,loc,z,-z2  
nsll,s  
d,all,ux,0.0145
```



The same CODE for Uniaxial and Biaxial cases, just comment or uncomment some commands
!lines: 17/18 , 55/56 , 315/321 , 327/333

varying_hole_distance_bending

```

! UNIAXIAL BENDING
! apply displacements conditions at the nodes of the line:
! x=0, z=0

```

```

allsel
lsel,s,loc,y,y2
lsel,r,loc,z,z1
nsll,s
d,all,uy,0.0145
!
```

```

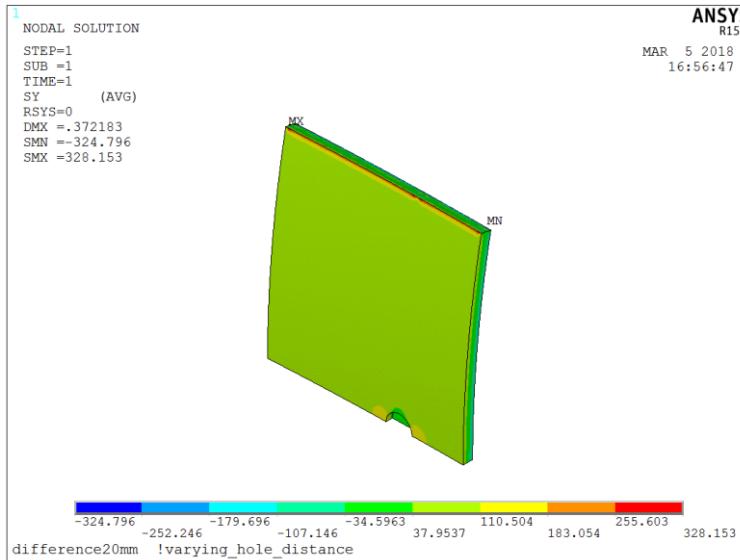
allsel
lsel,s,loc,y,y2
lsel,r,loc,z,-z1
nsll,s
d,all,uy,-0.0145
!
```

```

allsel
lsel,s,loc,y,y2
lsel,r,loc,z,-z2
nsll,s
d,all,uy,-0.0145
!
```

```

allsel
lsel,s,loc,y,y2
lsel,r,loc,z,-z2
nsll,s
d,all,uy,0.0145
!
```



(a) Uniaxial (Transverse) Bending

```

! BIAXIAL BENDING
! apply displacements conditions at the nodes of the line:
! x=0, z=0

```

```

allsel
lsel,s,loc,y,y2
lsel,r,loc,z,z1
nsll,s
d,all,uy,0.0145
!
```

```

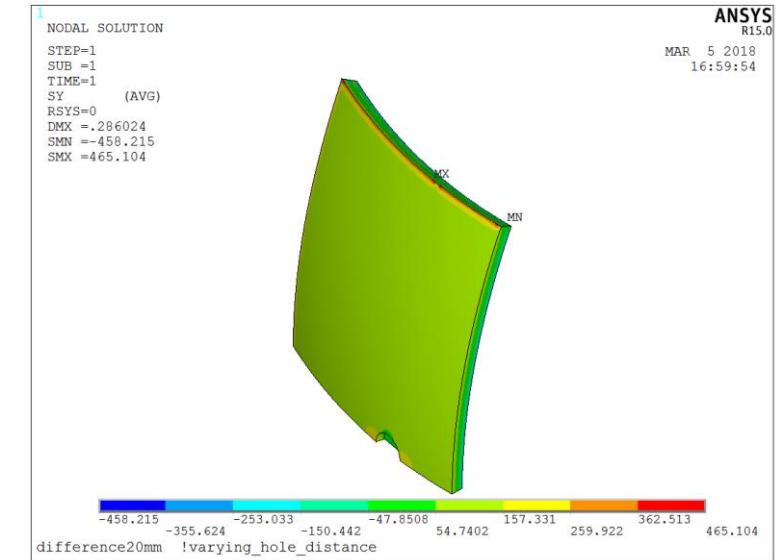
allsel
lsel,s,loc,x,x1
lsel,r,loc,z,z1
nsll,s
d,all,ux,-0.0145
!
```

```

allsel
lsel,s,loc,y,y2
lsel,r,loc,z,-z2
nsll,s
d,all,uy,-0.0145
!
```

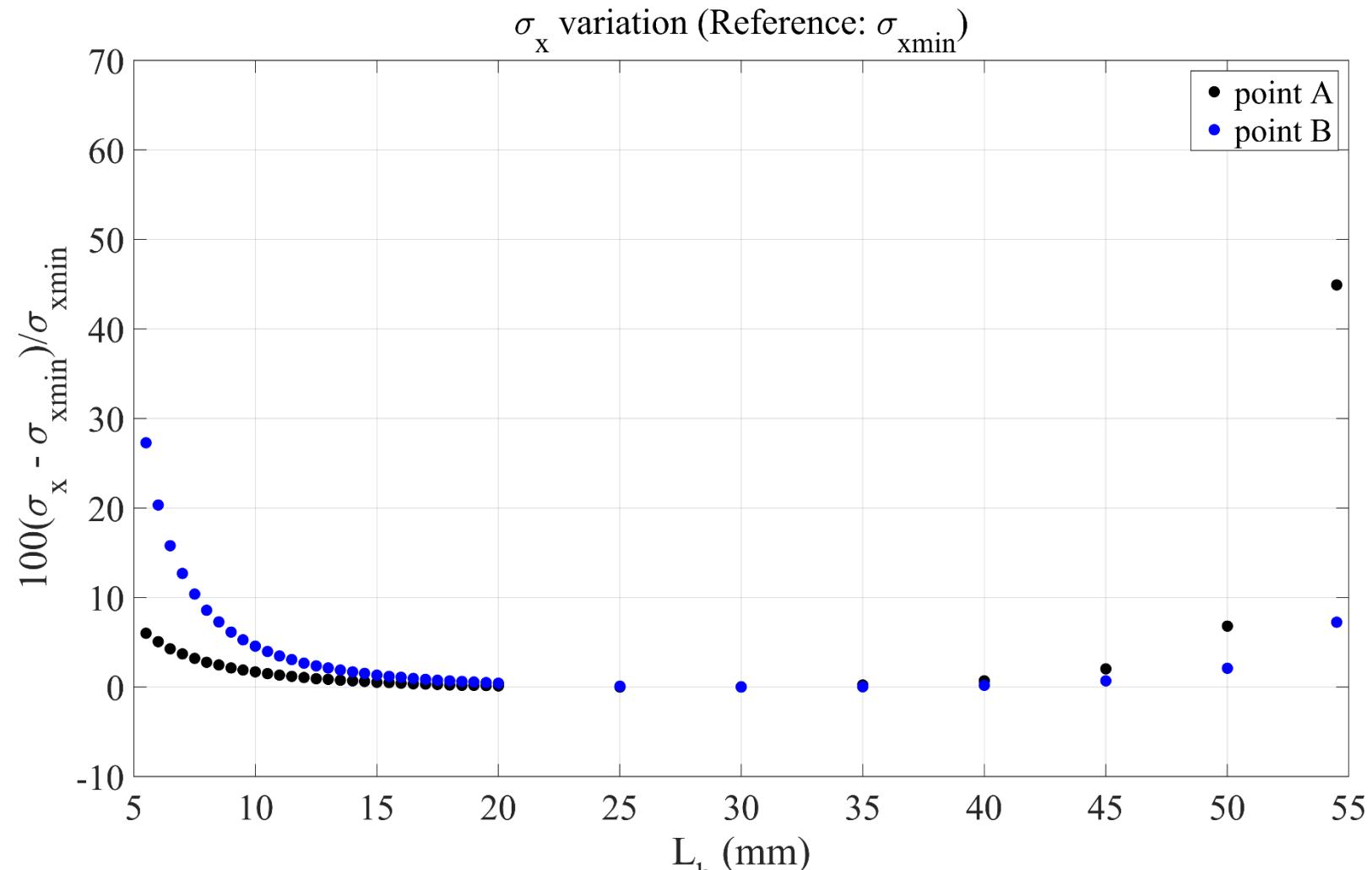
```

allsel
lsel,s,loc,x,x1
lsel,r,loc,z,-z2
nsll,s
d,all,ux,0.0145
!
```



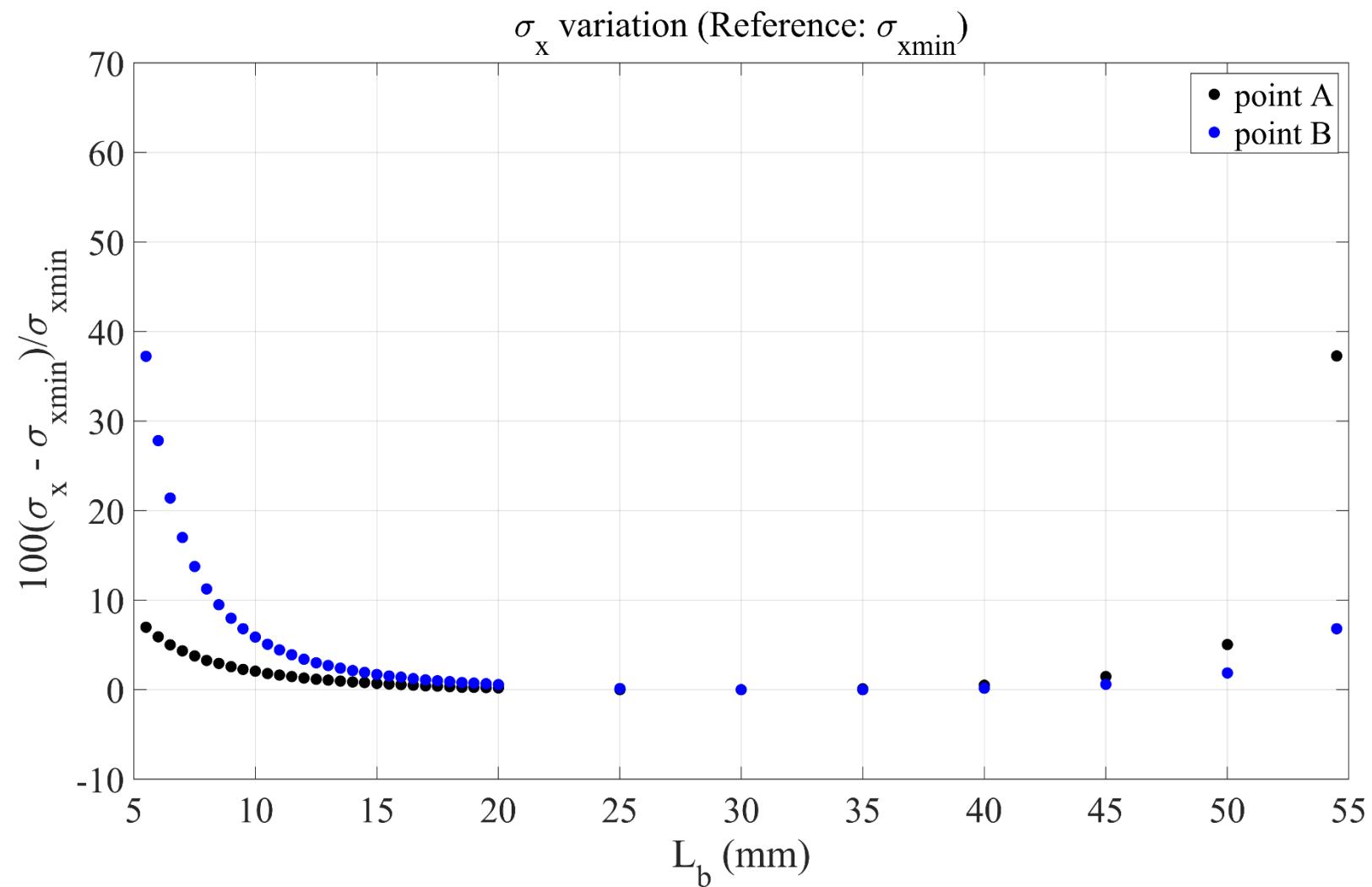
(b) Biaxial Bending

varying_hole_distance_bending



(a) Uniaxial (Transverse) Bending

varying_hole_distance_bending



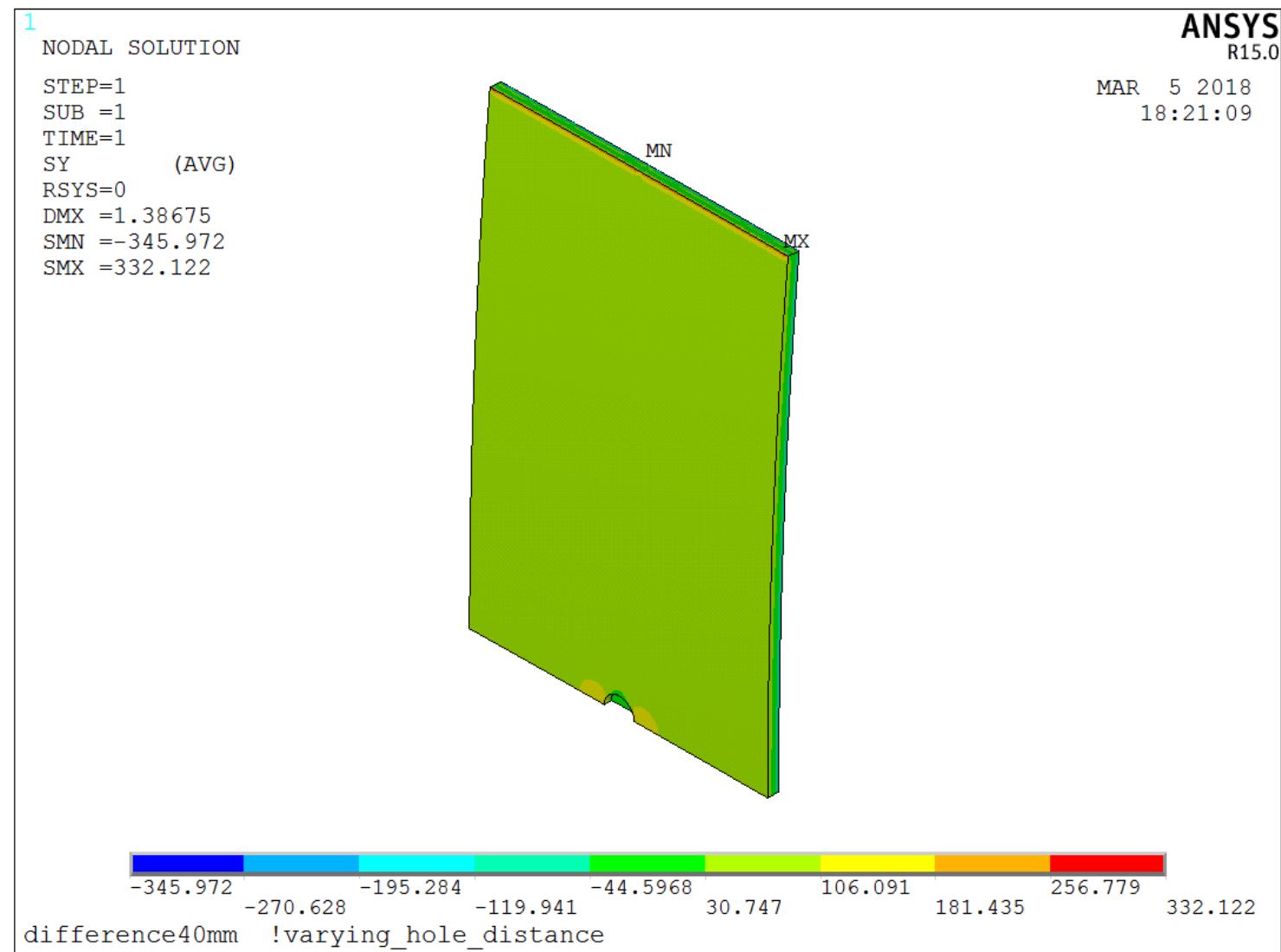
(b) Biaxial Bending

varying_hole_distance_bending_80x124mm

(a) Uniaxial
(Transverse) Bending

```
x1 = 0
x2 = 80
y1 = 0
y2 = 124
z1 = 0
z2 = 1.5
```

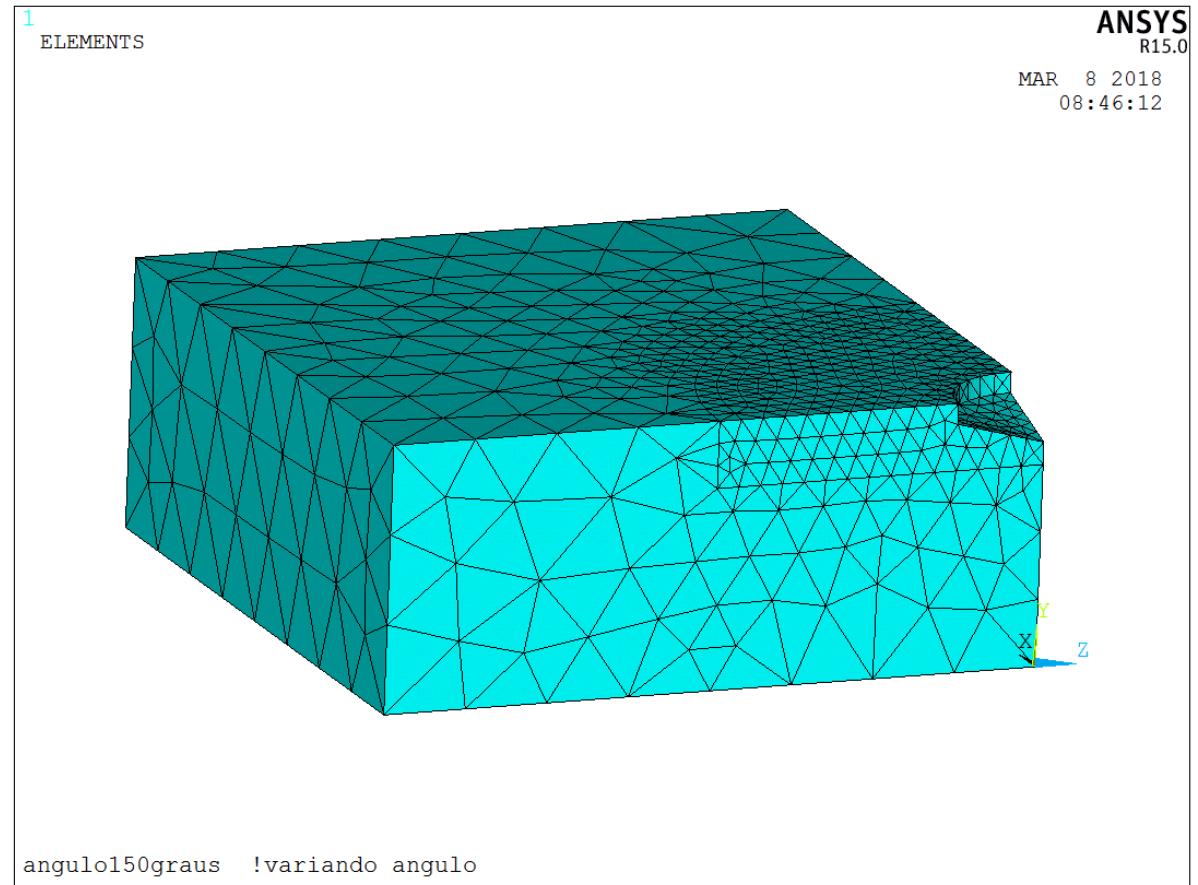
```
inicial = 10
final = 72
incr = 2
```



tarefa_furo_diferente_angulos

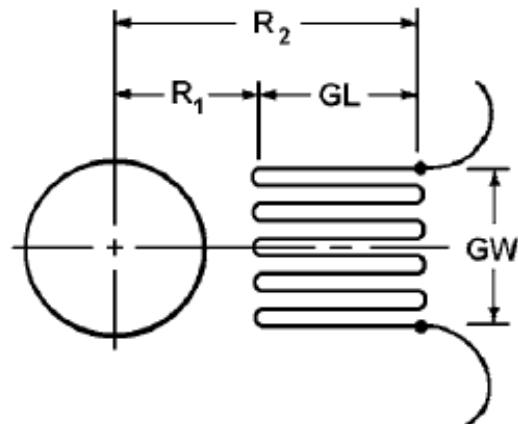
```
inicial = 130
final = 180
incr = 10

*do,angle,inicial,final,
incr
.
.
.
*enddo
```



Result Deformation -> "tarefa_furo_diferente_angulos"

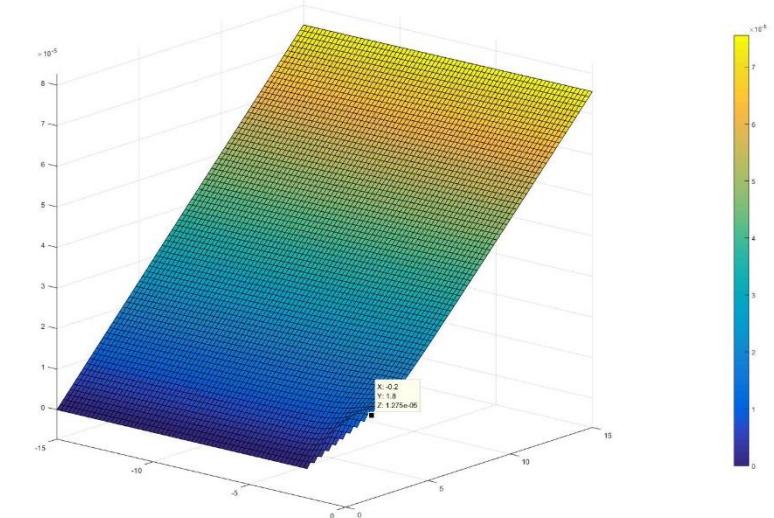
```
F_angle = scatteredInterpolant(xloc,zloc,ux,'linear','none');
```



$$\varepsilon = \sum_{i=1}^n \frac{U_{i2} - U_{i1}}{n(r_2 - r_1)}$$

```
%parameters:  
%take a look at the PDF NORMA  
r1=3.54; %values according to the NORMA [?], distane from the hole to the  
initial position of the strain gauge (x axis)  
r2=6.72; %values according to the NORMA [?], distane from the hole to the  
final position of the strain gauge (x axis)  
D=(r1+r2);  
GL=3.18; %strain gauge length, %values according to the NORMA [?]  
GW=3.18; %strain gauge width, %values according to the NORMA [?]  
ngrid=21; %number of grids -> strain gauge
```

strain_gauge_deformation.m

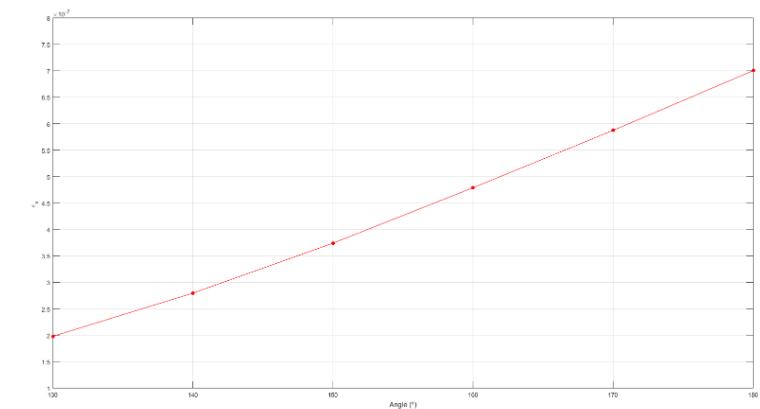


```
matrix_u0 =[n(:,1),xloc(:,1),zloc(:,1),ux(:,1)];  
%matrix with ux data, strain gauge with tetha = 0°  
direction
```

TABLE 1 Rosette Dimensions ^a					
Rosette Type	D	GL ^b	GW ^b	R ₁ ^b	R ₂ ^b
	Type A	0.309D	0.309D	0.3455D	0.6545D
1/16 in. nominal	0.101 (2.57)	0.031 (0.79)	0.031 (0.89)	0.035 (1.68)	0.066 (3.68)
	0.202 (5.13)	0.062 (1.59)	0.062 (1.59)	0.070 (1.77)	0.132 (3.36)
1/16 in. nomininal	0.404 (10.26)	0.125 (3.18)	0.125 (3.18)	0.140 (3.54)	0.264 (6.72)
	0.202 (5.13)	0.062 (1.59)	0.045 (1.14)	0.070 (1.77)	0.132 (3.36)
Conceptual	D	0.309D	0.223D	0.3455D	0.6545D
	Type C	30°	0.412D	0.588D	
1/16 in. nominal	0.170 (4.32)	0.030 (0.76)	30° (30°)	0.070 (1.78)	0.100 (2.54)

^a Dimensions are in inches (mm).

^b Rosette dimensions are defined in Fig. 2.



center_hole uniaxial plate_{1.5} depth_{1.5}
"through hole"

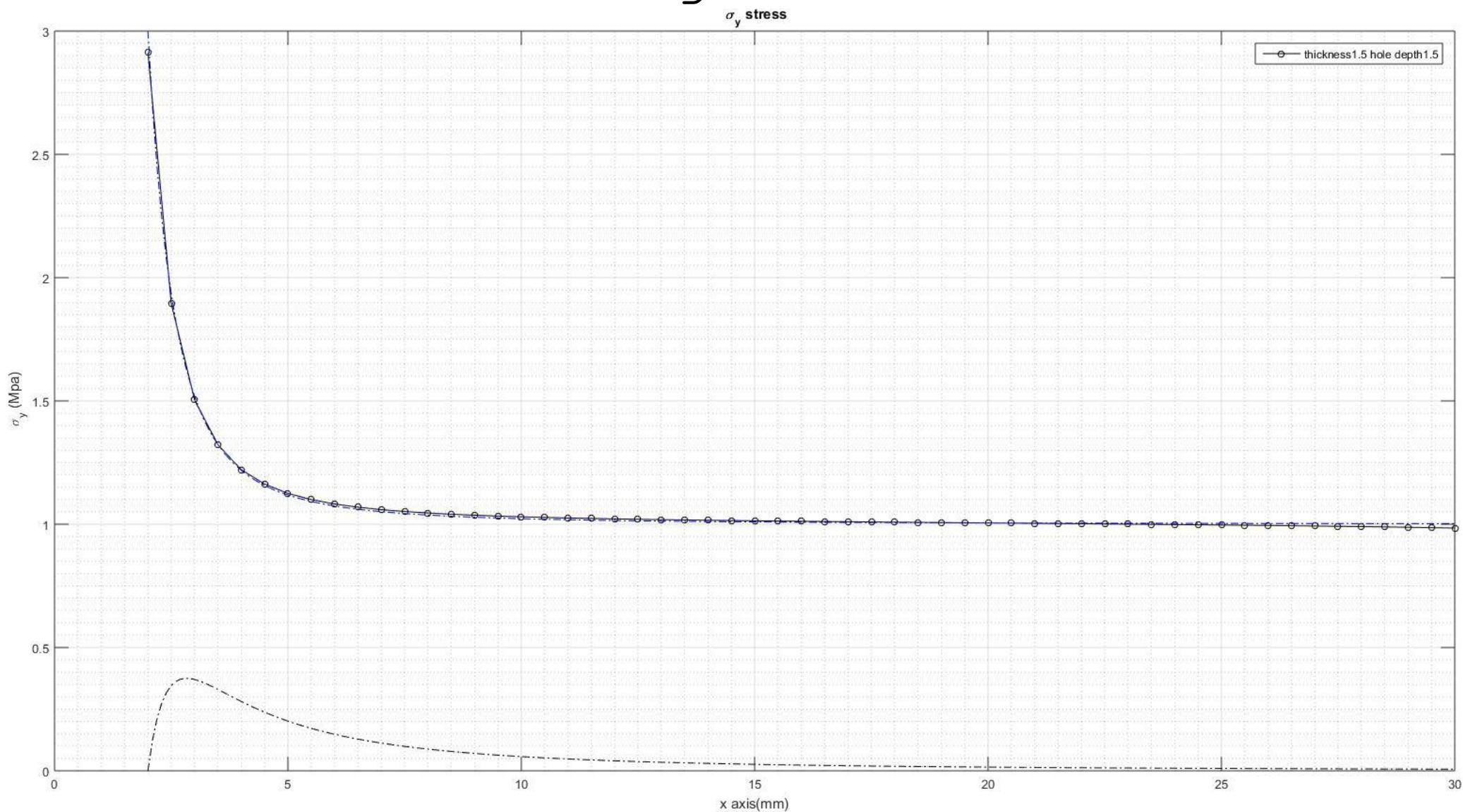
→ tensile_stress_concentration_polar_equations.m



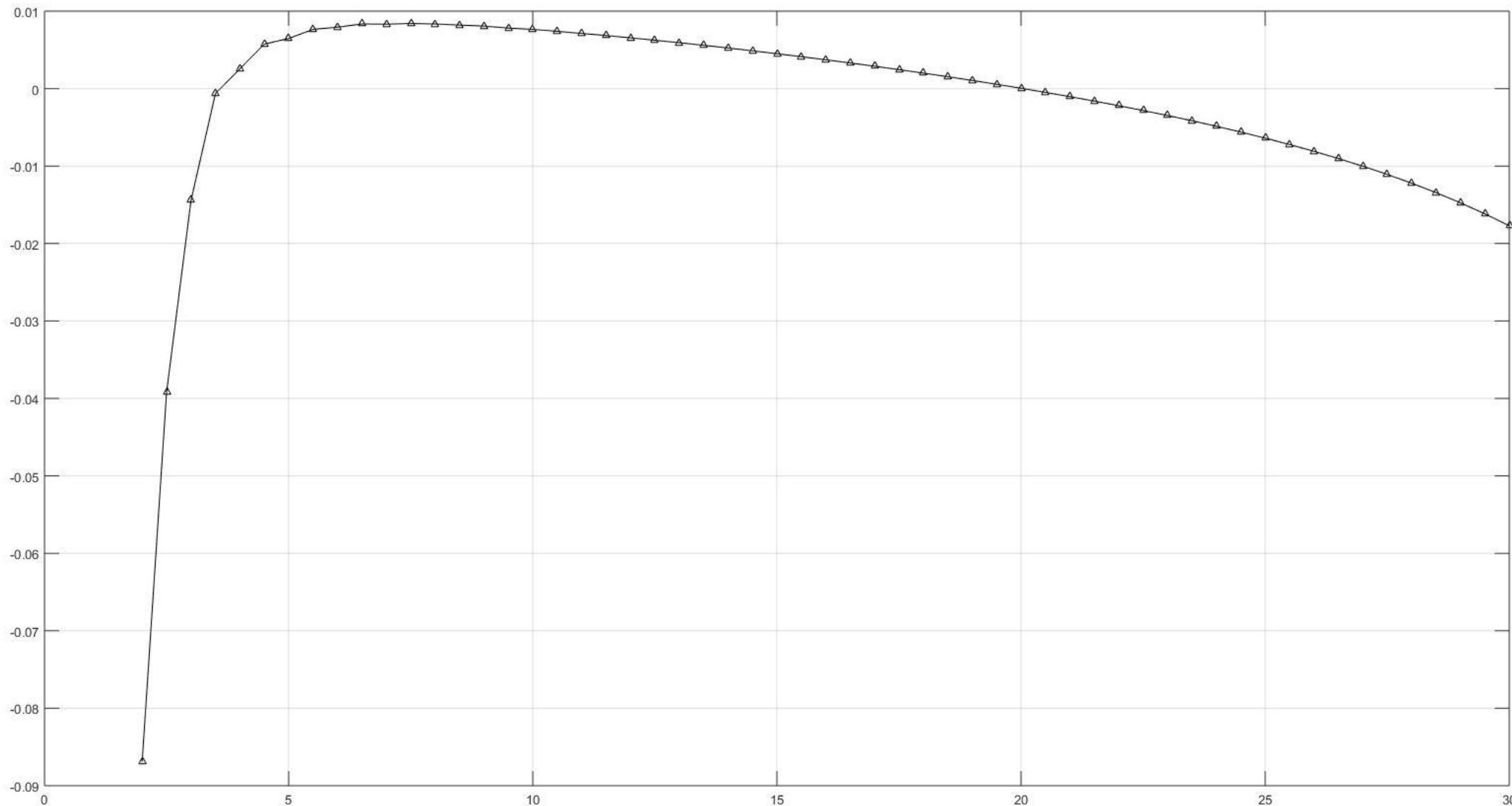
→ uniaxial_biaxial_stress_profile_center_hole.m

t=1 % uniaxial only
m=1 % through hole

center _ hole uniaxial plate 1.5 _ depth _ 1.5
"through hole"



center _ hole uniaxial plate 1.5 _ depth_1.5
"through hole"



center_hole_uniaxial_through_hole_and_kirsch_equations_sigma_theta_diff_K_sim

center_hole with “through hole”

plate_1.5_depth_1.5

radius = 2 mm

1° case

plate_1.5_depth_1.5

radius = 1 mm

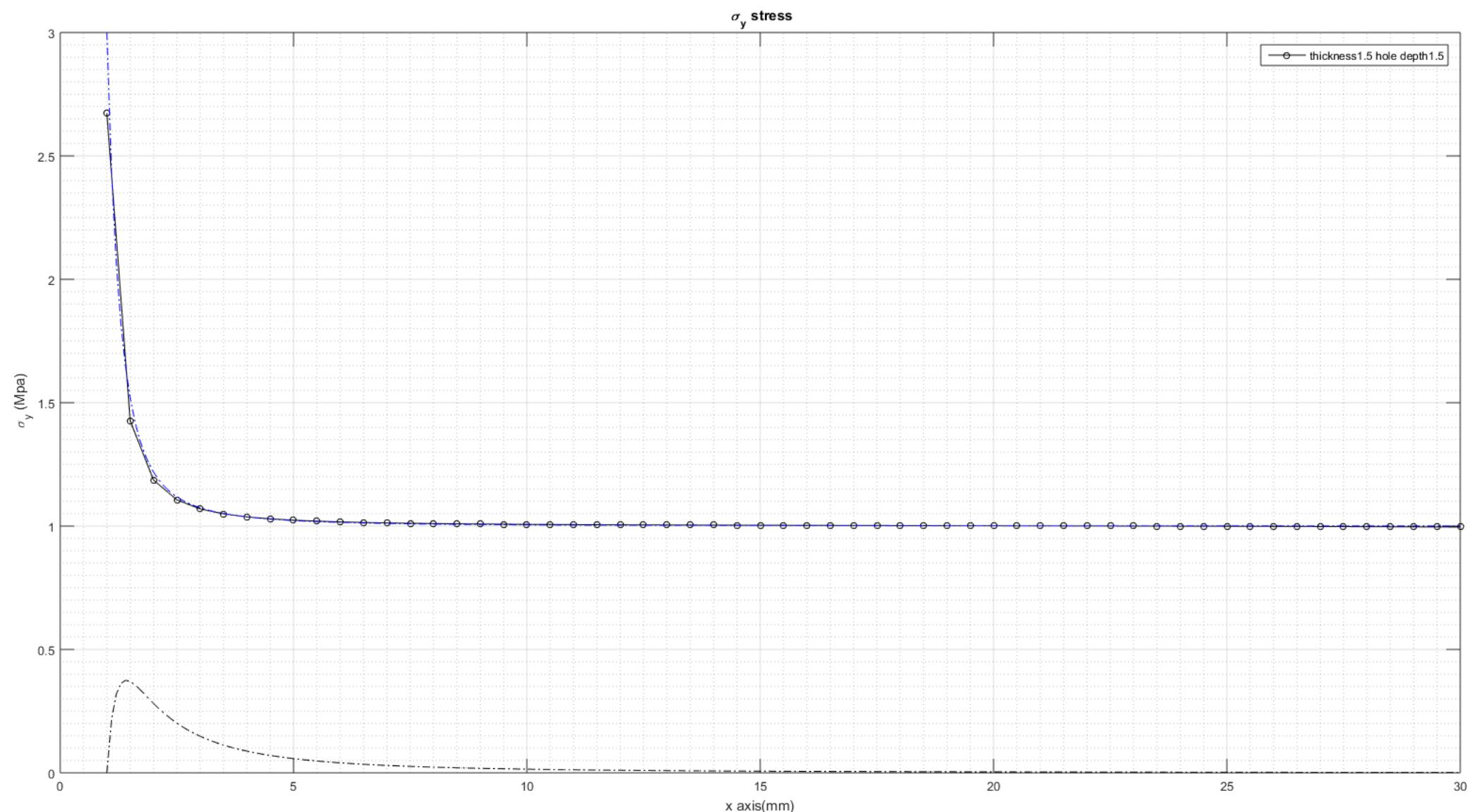
2° case

plate_0.5_depth_0.5

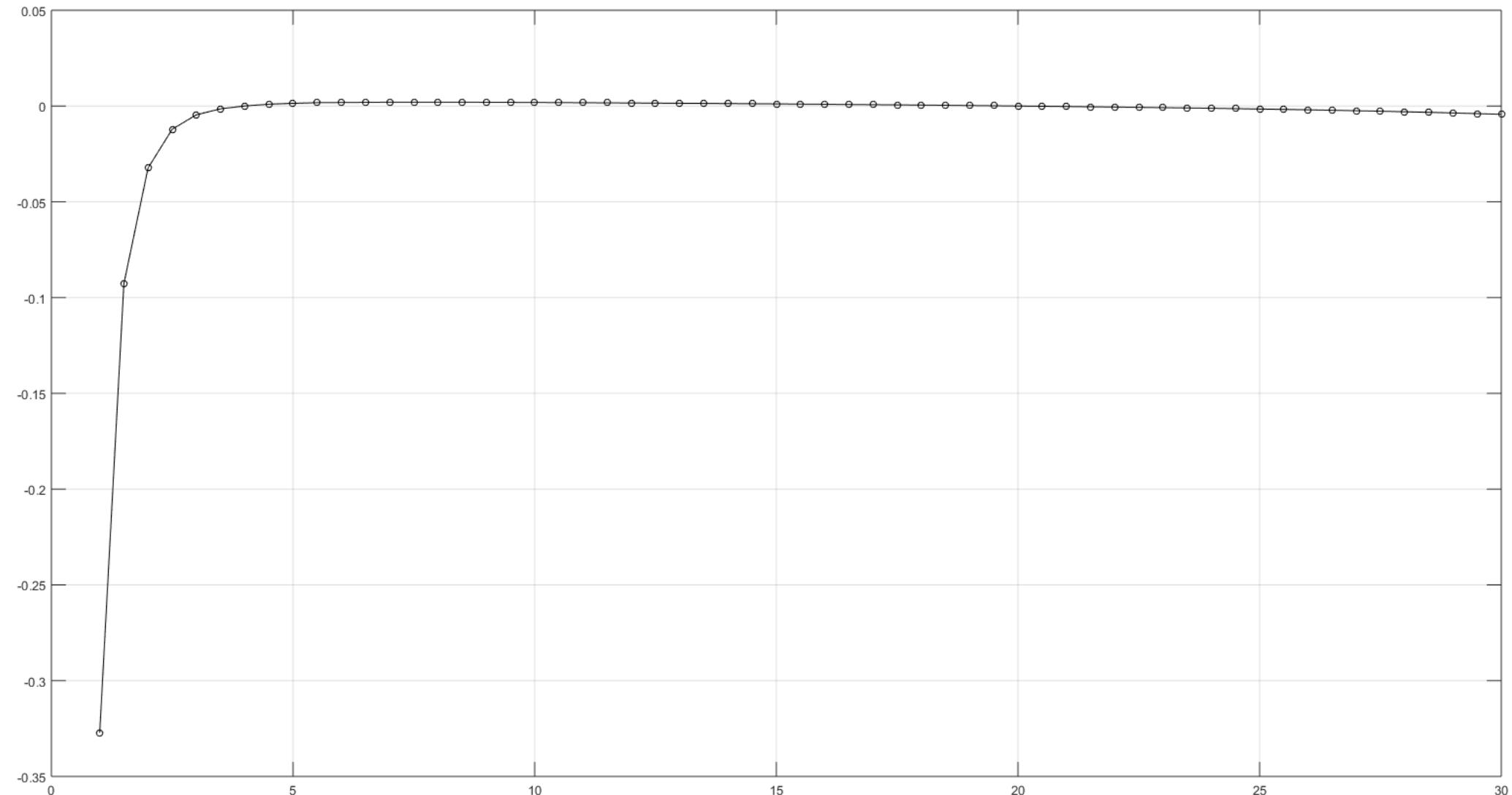
radius = 2 mm

3° case

2°case: plate_1.5_depth_1.5 radius=1mm

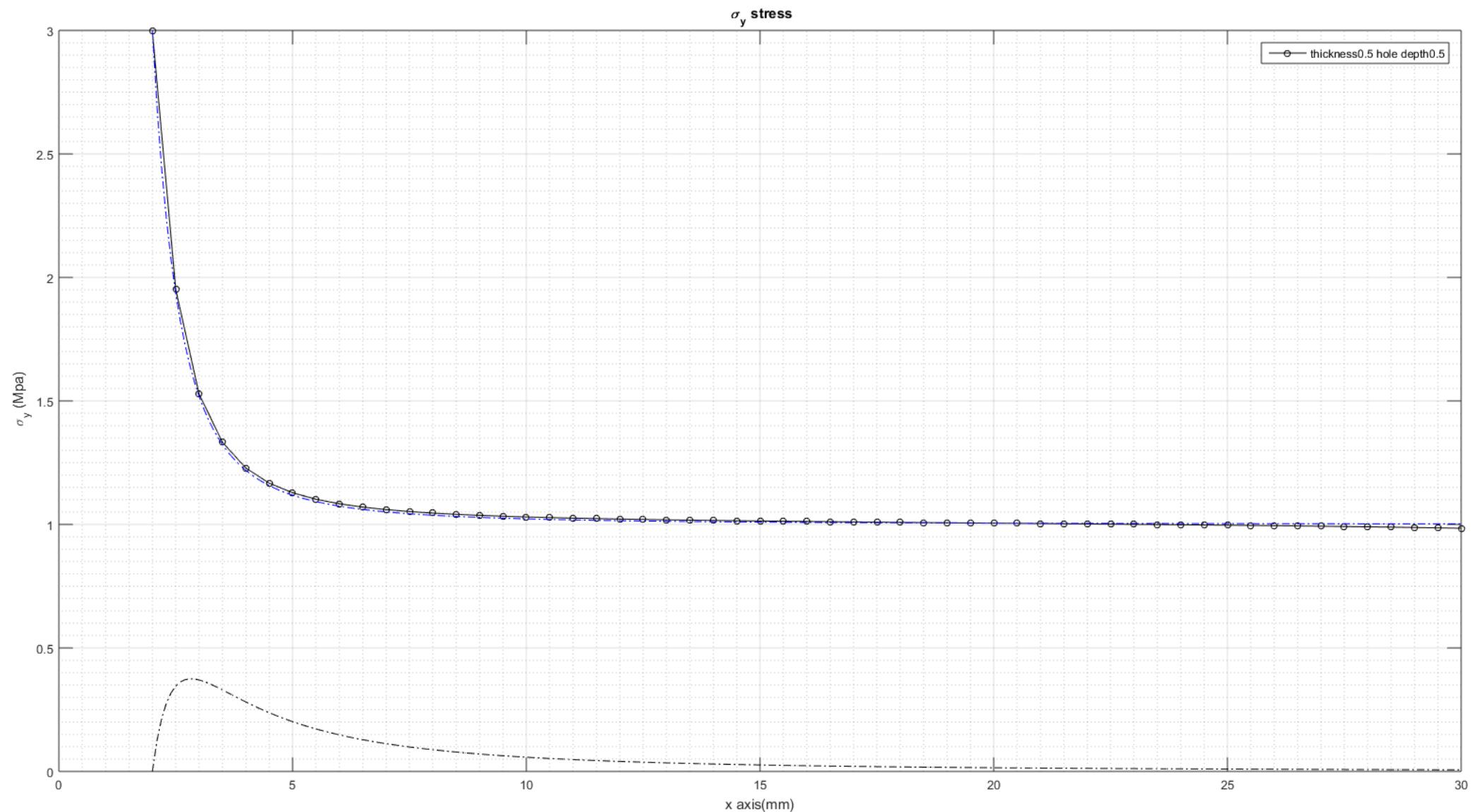


2°case: plate_1.5_depth_1.5 radius=1mm

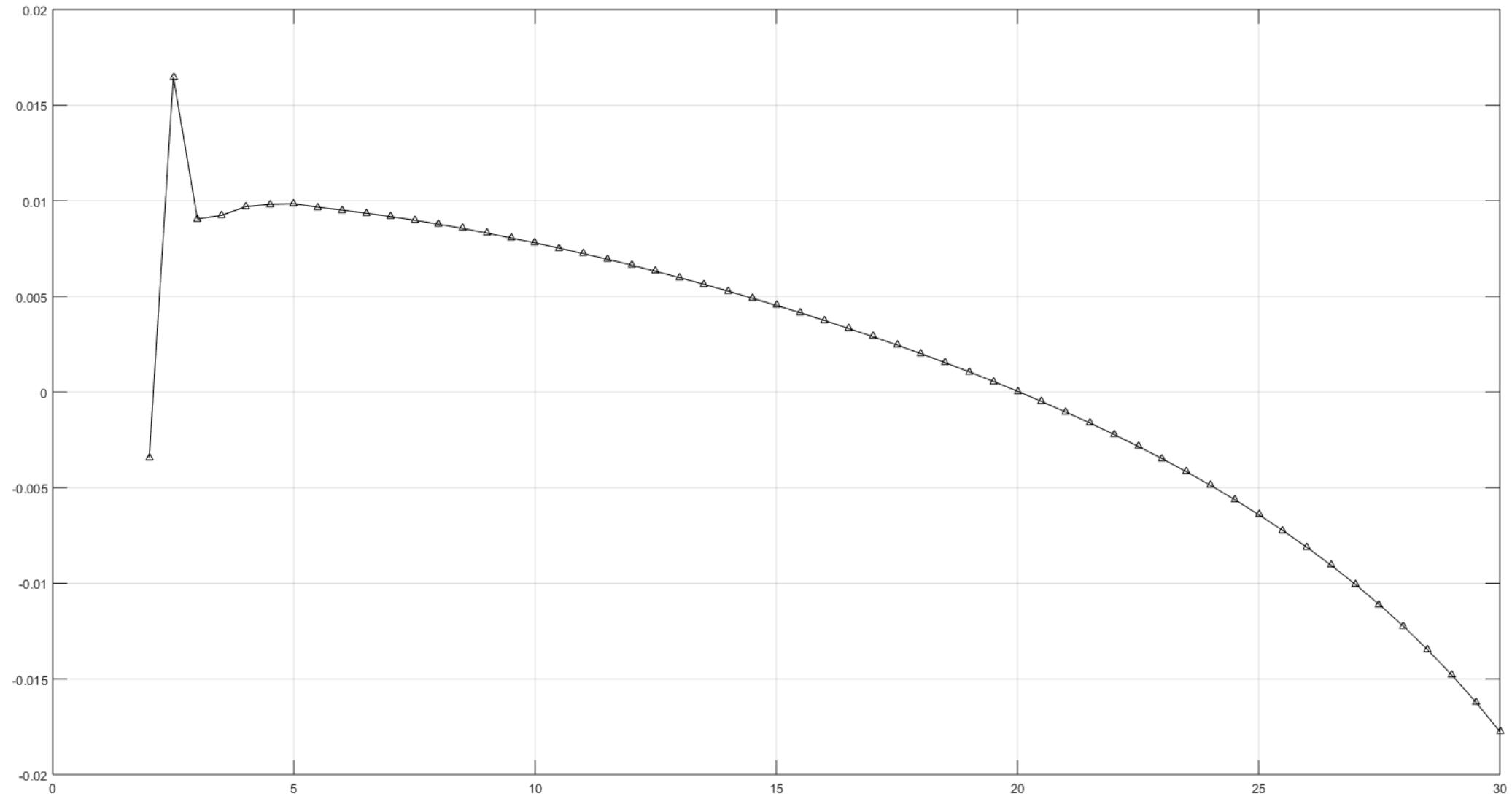


center_hole_uniaxial_through_hole_and_kirsch_equations_sigma_theta_diff_K_sim

3°case: plate_0.5_depth_0.5 radius=2mm

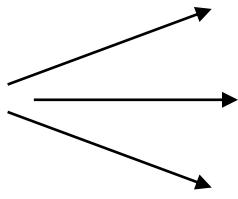


3°case: plate_0.5_depth_0.5 radius=2mm



elements_images

→ Uniaxial



plate_1.5_depth_1.5
plate_1.5_depth_1
plate_14_depth_1

```
! the following code takes images from elements inside the geometry (3  
geometries)
```

```
! Geometries and simulations:  
! -> varying_hole_distance_plate_1.5_depth_1.5_refined_mesh_region_ring  
! -> varying_hole_distance_plate_1.5_depth_1_refined_mesh_region_ring  
! -> varying_hole_distance_plate_14_depth_1_refined_mesh_region_ring
```

```
allsel  
diff = 30
```

```
x1 = 0  
x2 = 60  
y1 = 0  
y2 = 60  
z1 = 0  
z2 = 1.5
```

```
xcenter1 = (x2 - diff)/2
```

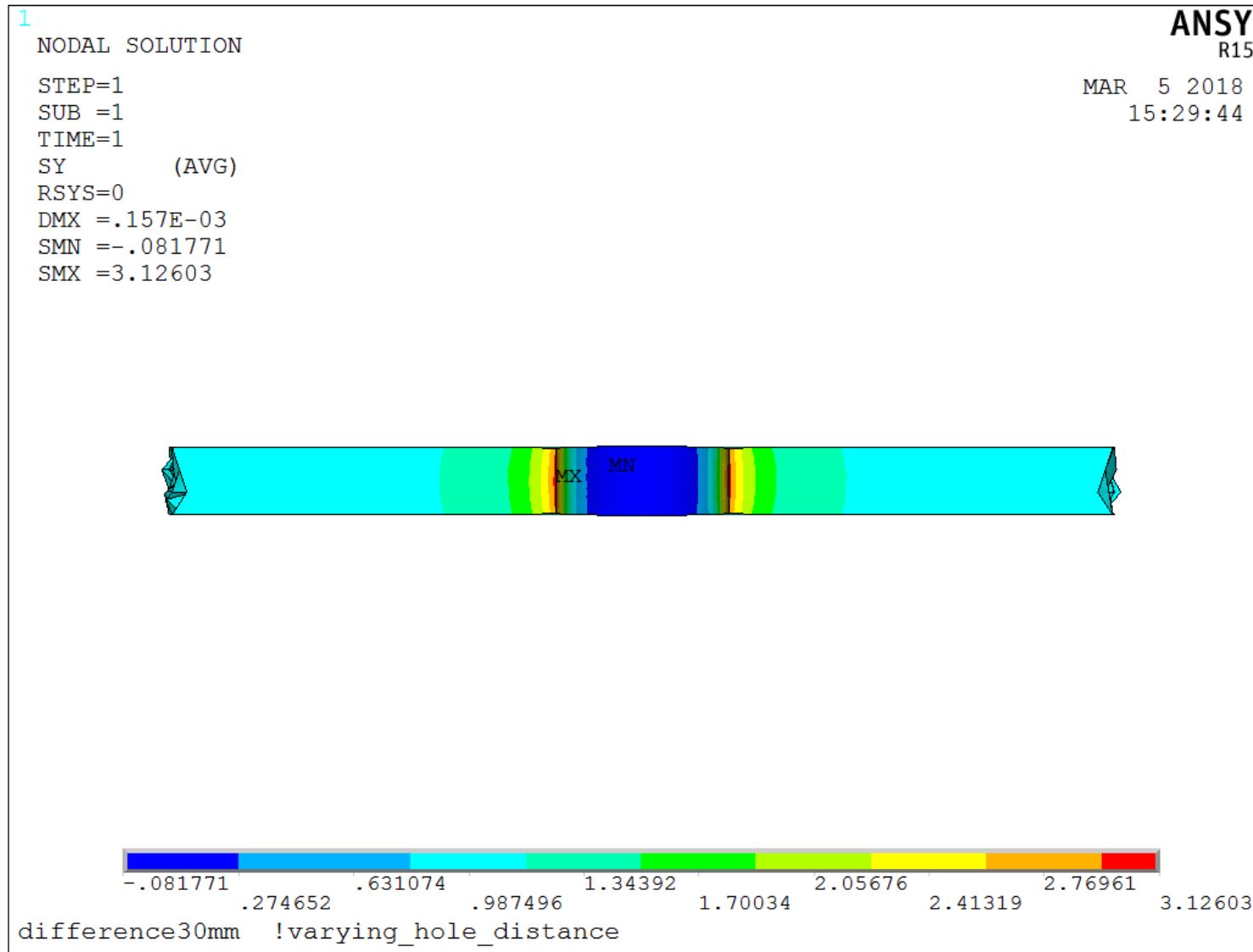
```
allsel  
vplot  
/VIEW,1,0,-1  
/rep  
nsl,s,loc,x,xcenter1-10,xcenter1+10  
nplot  
esln  
/post1  
plnsol,s,y  
!plesol,sy
```

```
/contour,1,, -0.081771,, 3.12603  
/rep
```

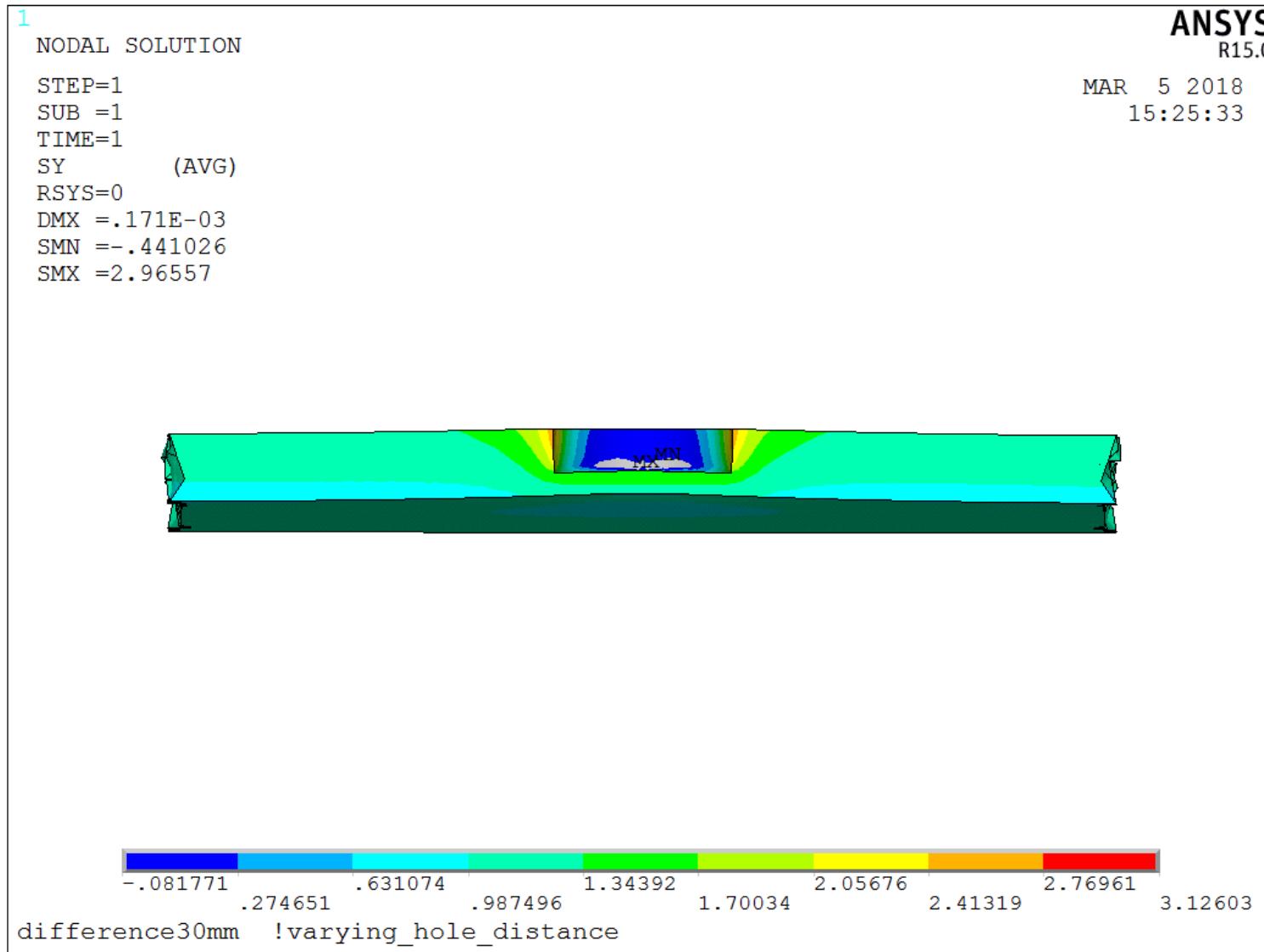
elements_images

→ Uniaxial

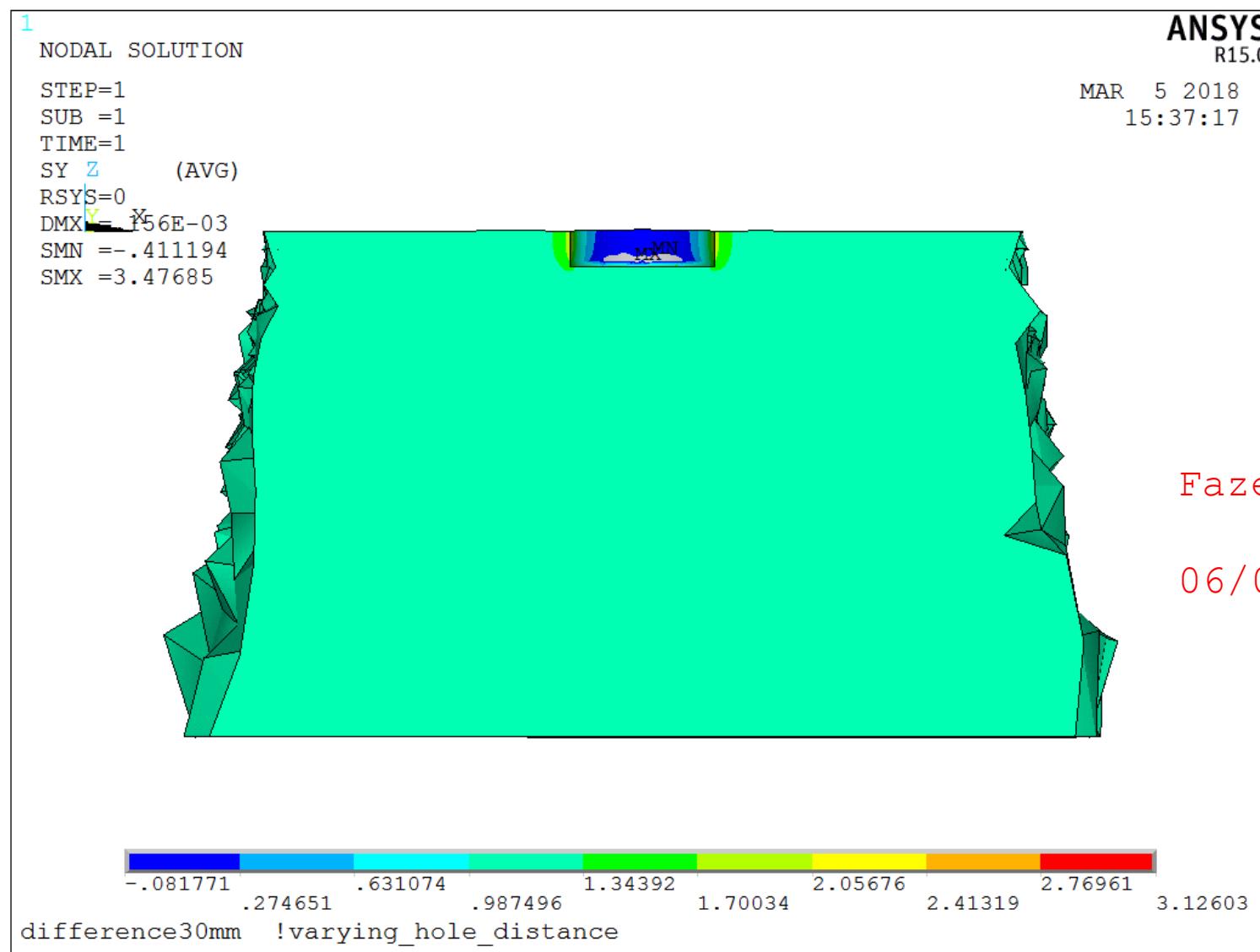
plate_1.5_depth_1.5



elements_images → Uniaxial → plate_1.5_depth_1



elements_images → Uniaxial

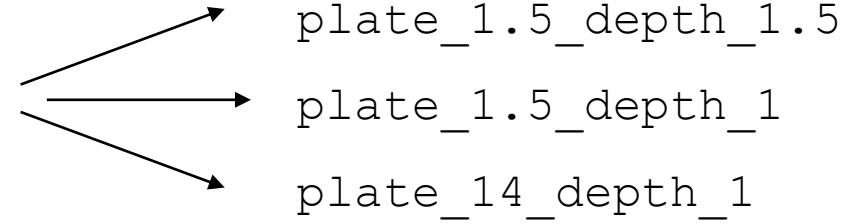


plate_14_depth_1

Fazer para Biaxial
06/03/2018

elements_images

→ Biaxial



```
! the following code takes images from elements inside the geometry (3  
geometries)
```

```
! Geometries and simulations:  
! -> varying_hole_distance_plate_1.5_depth_1.5_refined_mesh_region_ring  
! -> varying_hole_distance_plate_1.5_depth_1_refined_mesh_region_ring  
! -> varying_hole_distance_plate_14_depth_1_refined_mesh_region_ring
```

```
allsel  
diff = 30
```

```
x1 = 0  
x2 = 60  
y1 = 0  
y2 = 60  
z1 = 0  
z2 = 1.5
```

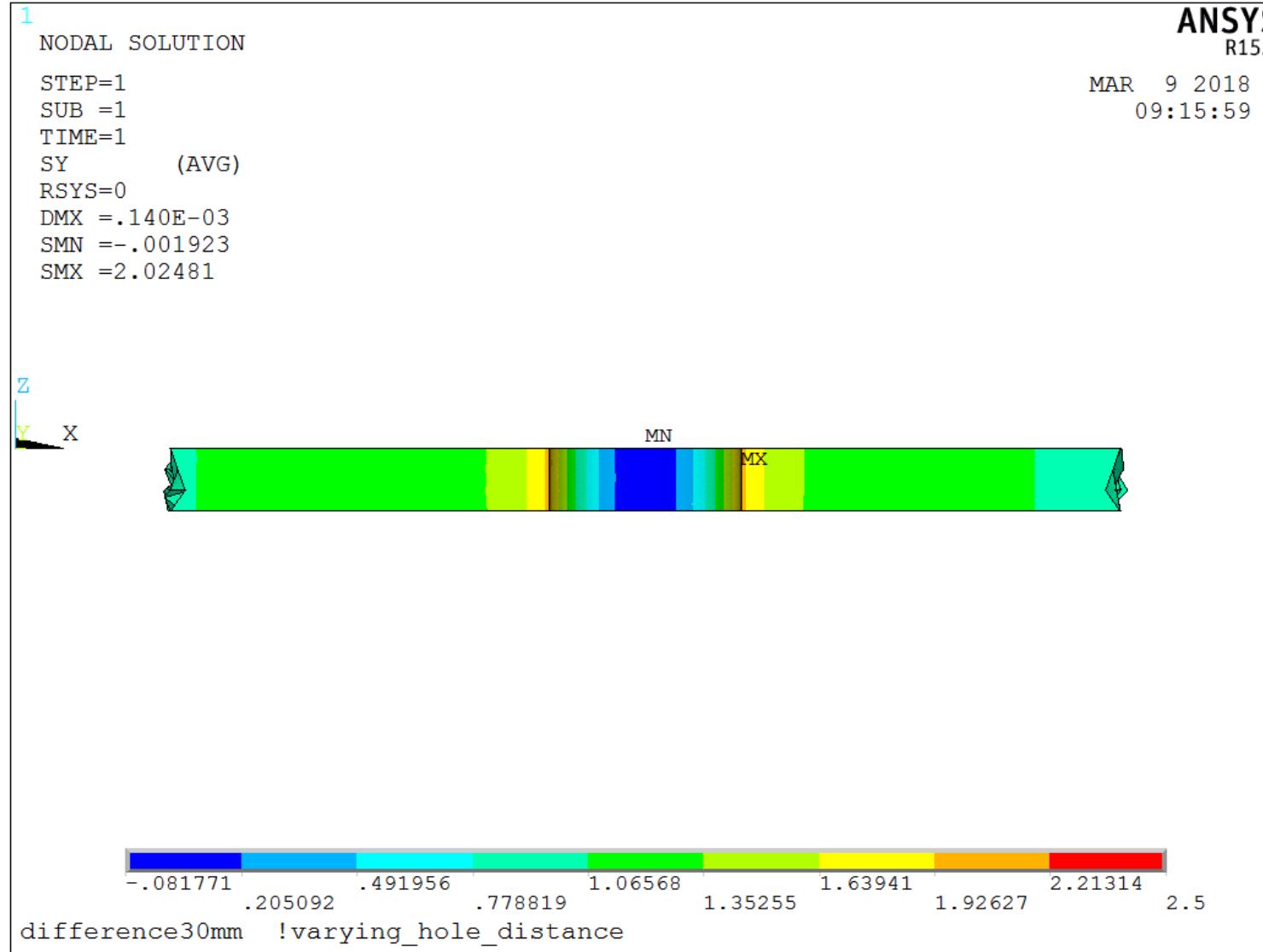
```
xcenter1 = (x2 - diff)/2
```

```
allsel  
vplot  
/VIEW,1,0,-1  
/rep  
nsl,s,loc,x,xcenter1-10,xcenter1+10  
nplot  
esln  
/post1  
plnsol,s,y  
!plesol,sy  
  
/contour,1,, -0.081771,, 3.12603  
/rep
```

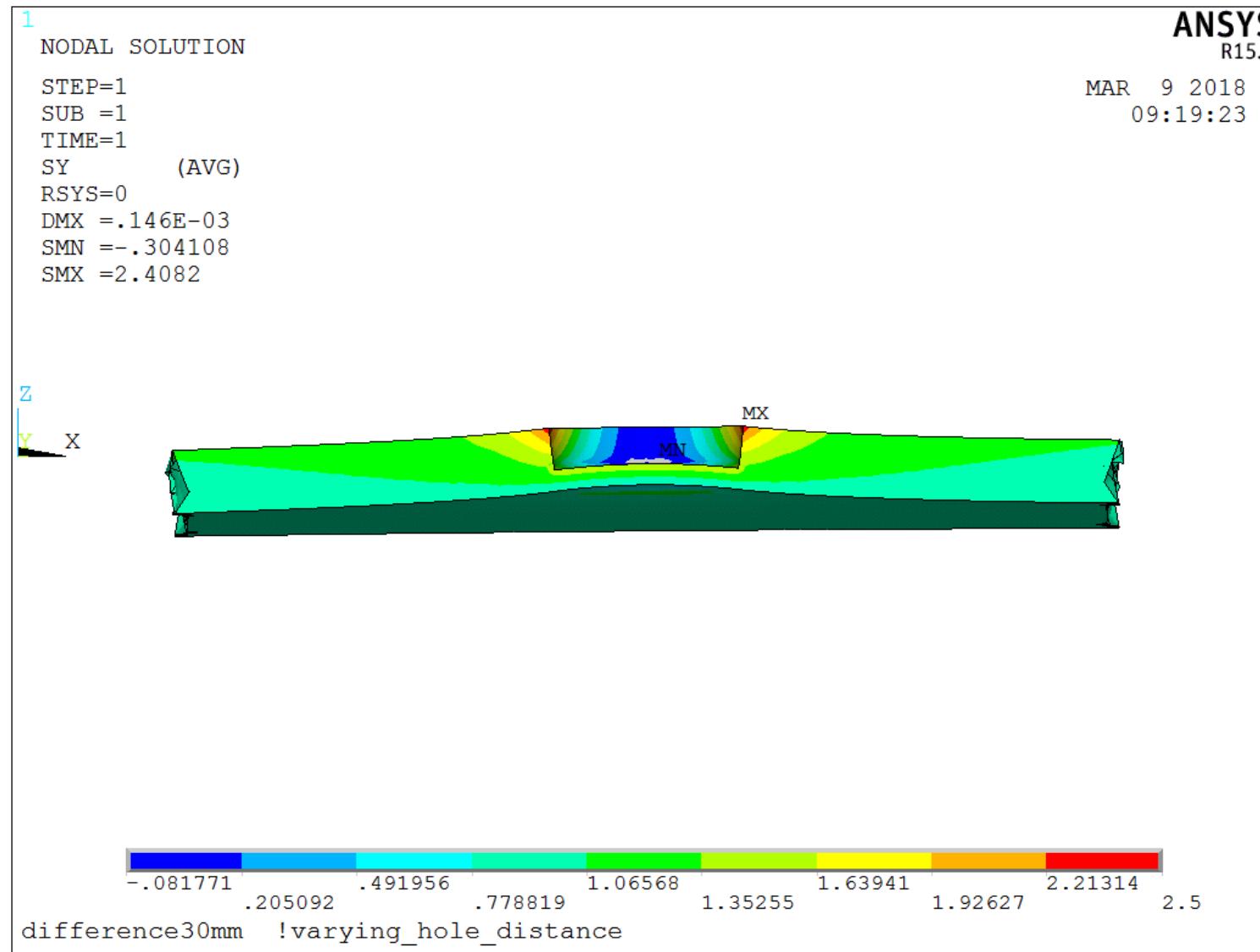
elements_images

→ Biaxial

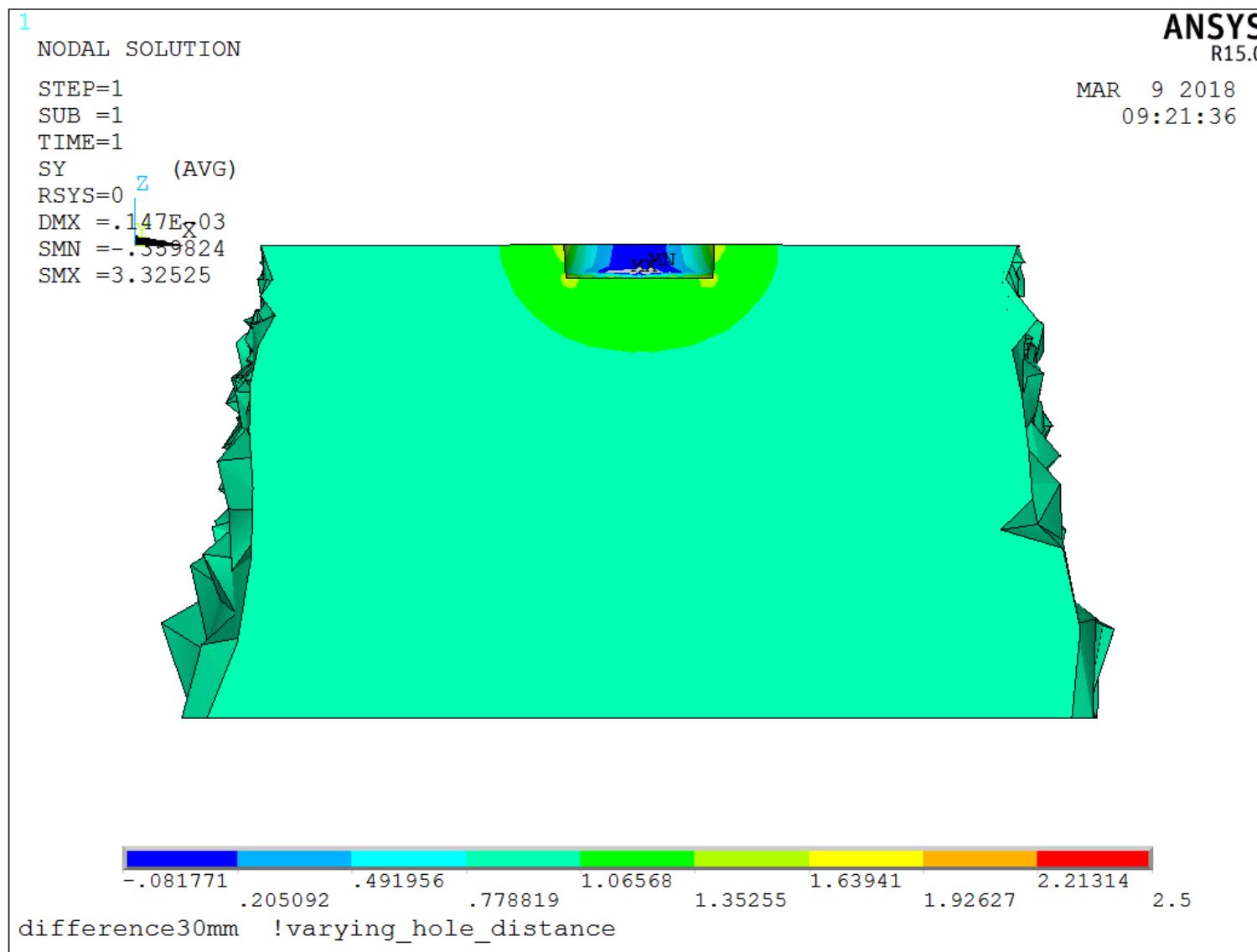
plate_1.5_depth_1.5



elements_images → Biaxial → plate_1.5_depth_1



elements_images → Biaxial



plate_14_depth_1

Sigma_min

	Uniaxial		
	T_p/H_d=1	T_p/H_d=1.5	T_p/H_d=14
Point A (x1)	2.942446768300000	2.722951114200000	1.925316333800000
Point B (x2)	2.935607373700000	2.721057593800000	1.925137460200000
Biaxial			
	T_p/H_d=1	T_p/H_d=1.5	T_p/H_d=14
Point A (x1)	2.015860319100000	2.404486894600000	1.596784085000000
Point B (x2)	2.013187766100000	2.404265463400000	1.596903532700000

Na Geometria T_p/H_d=14,
 Intervalo do Sigma_min {20, 40}

Sigma min calculated via u_b_s_p_center_hole_withou_kirsch.m at

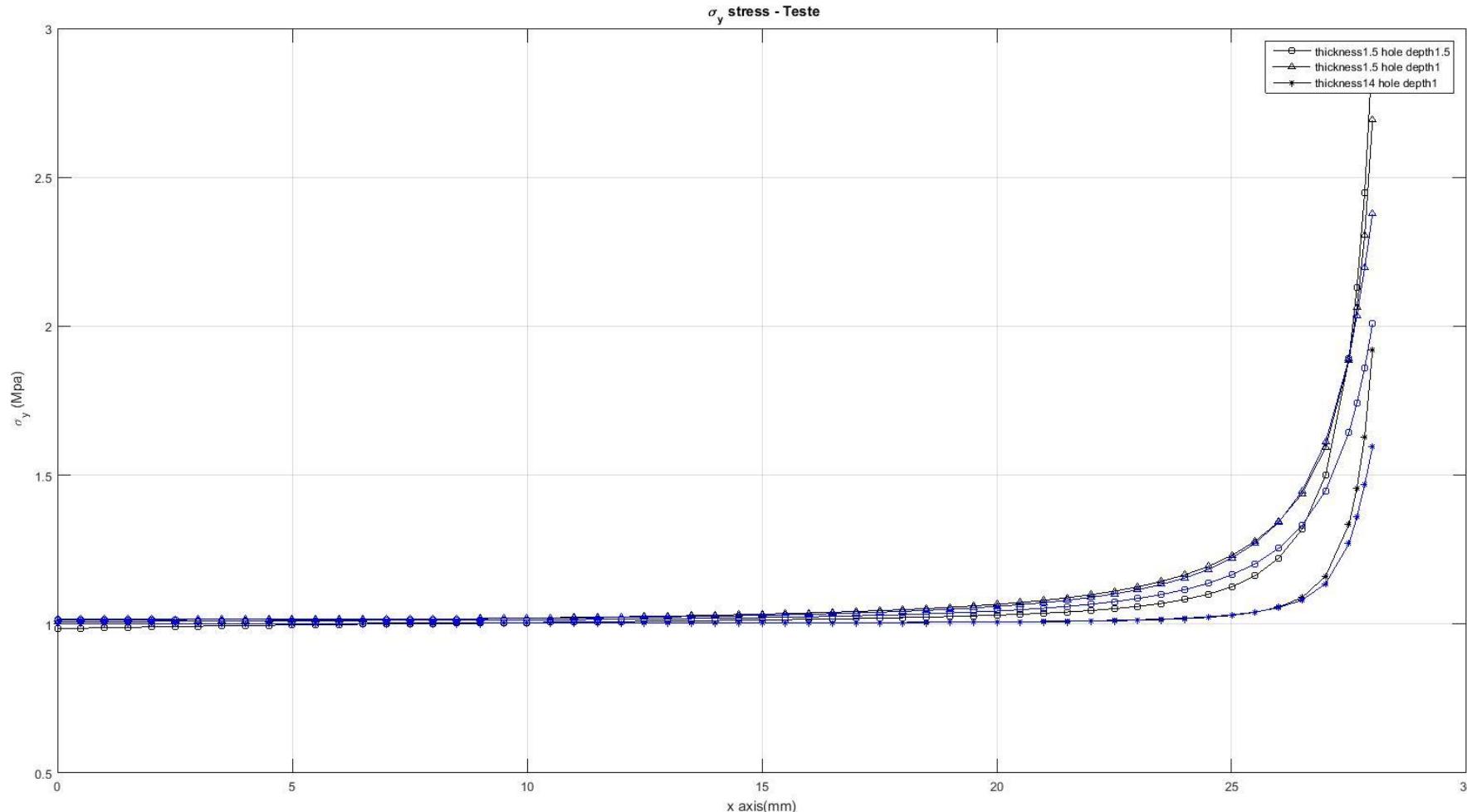
C:\Manasses\center_hole\u_b_s_p_center_hole_withou_kirsch.m

sig_min(cont_min)=matrix(end, 9);

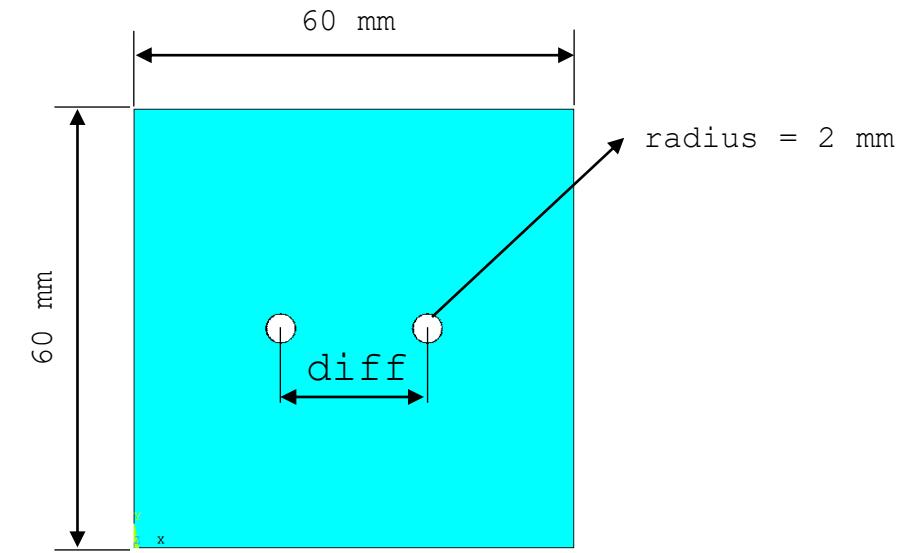
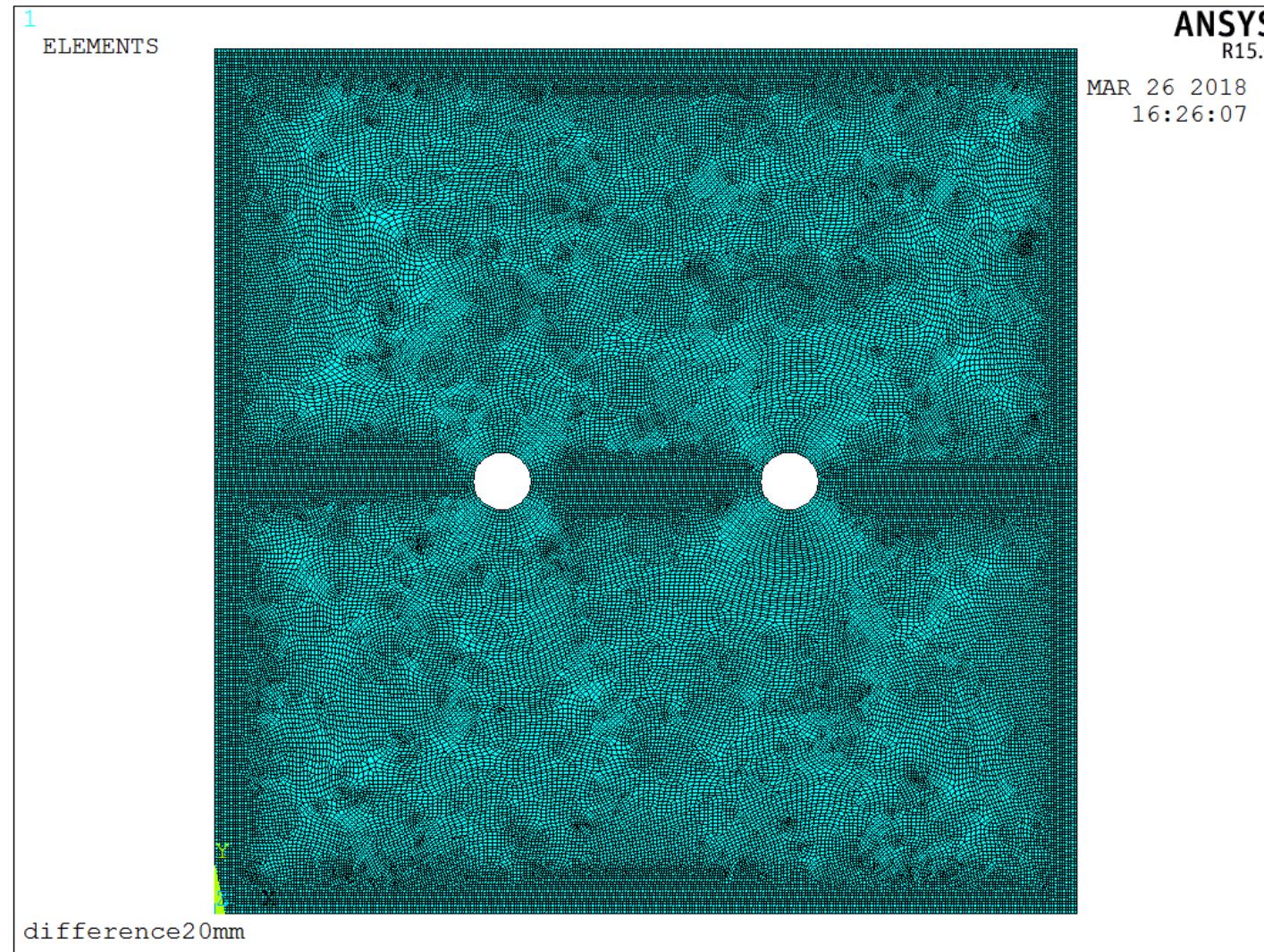
Uniaxial			
	T_p/H_d=1	T_p/H_d=1.5	T_p/H_d=14
Point A (x1)	2.933690130700000	2.692401707200000	1.920085877200000
Point B (x2)	=	=	=
Biaxial			
	T_p/H_d=1	T_p/H_d=1.5	T_p/H_d=14
Point A (x1)	2.008045554200000	2.378486096900000	1.594718247700000
Point B (x2)	=	=	=

Sigma min calculated via u_b_s_p_center_hole_withou_kirsch.m at

C:\Manasses\center_hole\u_b_s_p_center_hole_withou_kirsch.m

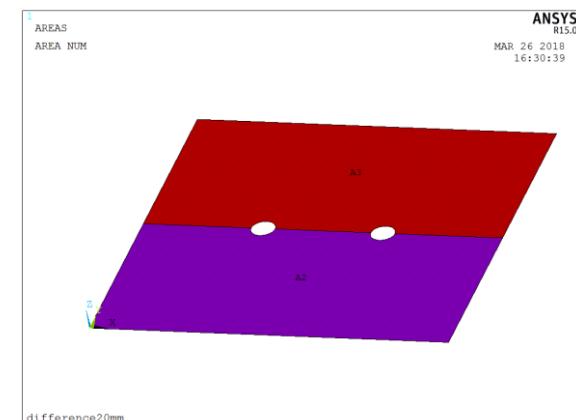


varying_hole_distance_2D diff=20 mm

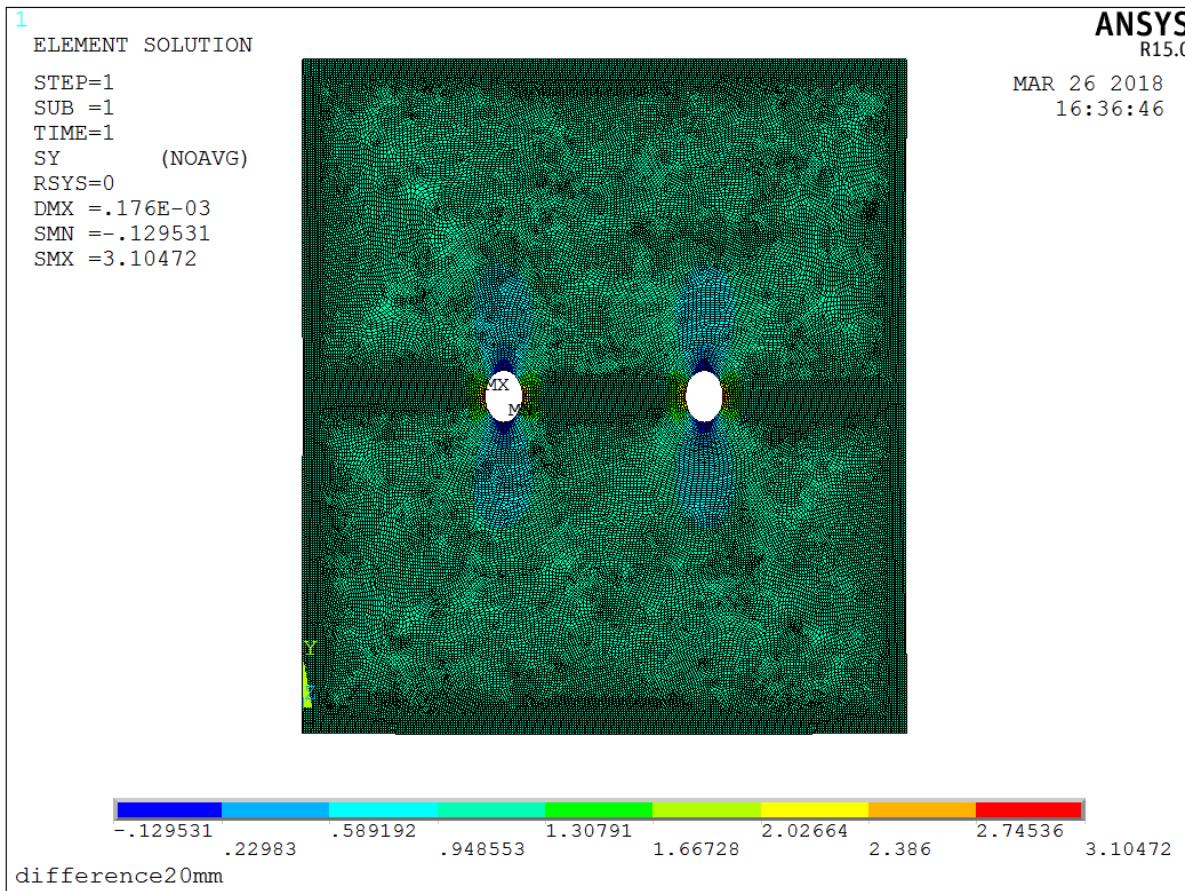


plate_thickness = depth = 0.0 mm

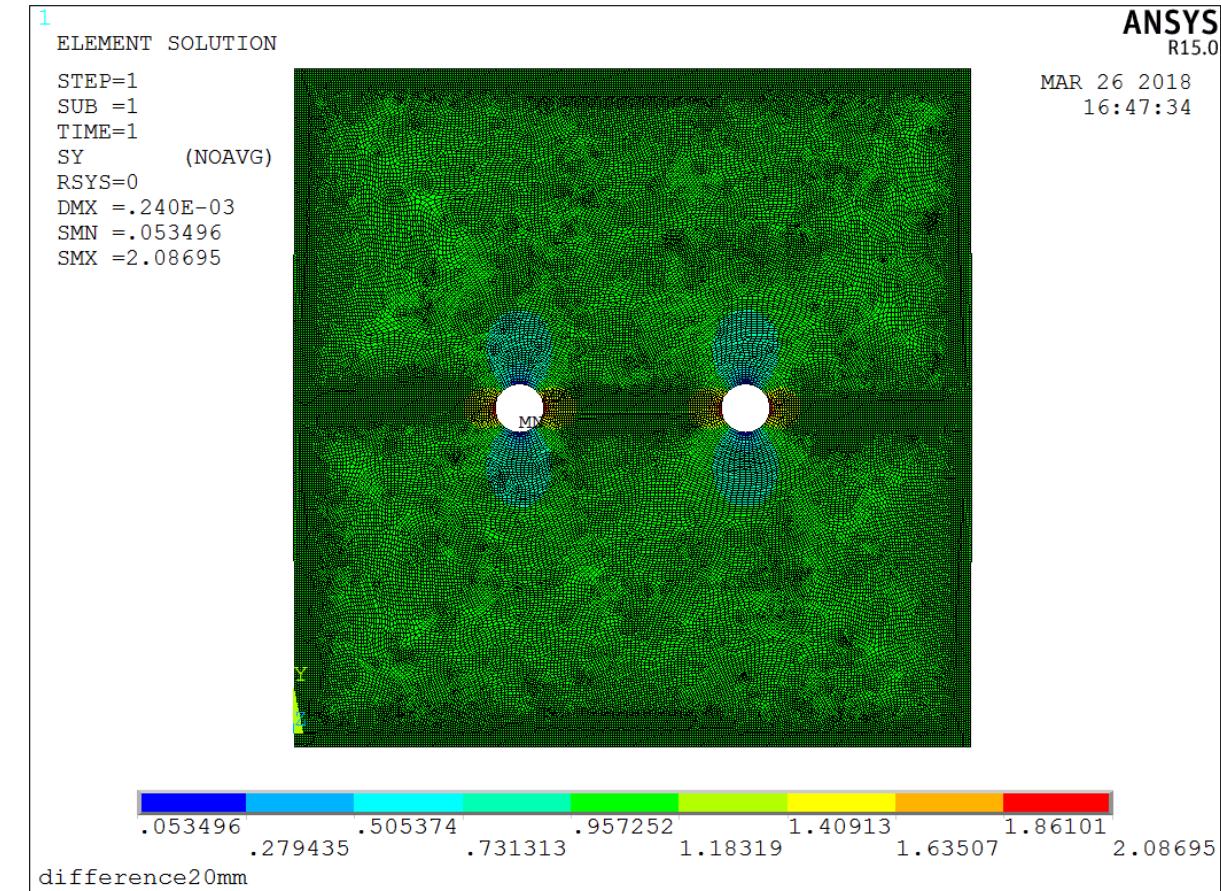
"through hole"



varying_hole_distance_2D diff=20 mm

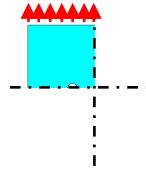


(a) Uniaxial
Transverse load



(b) Biaxial load

varying_hole_distance_2D diff=20 mm



Uniaxial Transverse Load

$$\text{Sigma}_{\max(60 \times 60)}^{\text{diff}=(5*D)=20} = 3.088956714$$

$$\text{Sigma}_{\max(150 \times 150)}^{\text{diff}=\left(\frac{70}{4}*D\right)=70} = 3.024106741$$

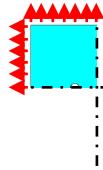
$$\text{Sigma}_{\max(150 \times 150)}^{\text{diff}=(5*D)=20} = 3.037305094$$

$$\text{Error} = \frac{\left| \text{Sigma}_{\max(60 \times 60)}^{\text{diff}=(5*D)=20} - \text{Sigma}_{\max(150 \times 150)}^{\text{diff}=\left(\frac{70}{4}*D\right)=70} \right|}{\text{Sigma}_{\max(150 \times 150)}^{\text{diff}=\left(\frac{70}{4}*D\right)=70}}$$

$$\text{Error} = \frac{|3.088956714 - 3.024106741|}{3.024106741} = 0.02144433995 = 2.14\%$$

$$\text{Error} = \frac{\left| \text{Sigma}_{\max(150 \times 150)}^{\text{diff}=(5*D)=20} - \text{Sigma}_{\max(150 \times 150)}^{\text{diff}=\left(\frac{70}{4}*D\right)=70} \right|}{\text{Sigma}_{\max(150 \times 150)}^{\text{diff}=\left(\frac{70}{4}*D\right)=70}}$$

$$\text{Error} = \frac{|3.037305094 - 3.024106741|}{3.024106741} = 0.00436438066853275798441798453701 = 0.4364\%$$



Biaxial Load

$$\text{Sigma}_{\max(150 \times 150)}^{\text{diff}=(5*D)=20} = 2.085622532$$

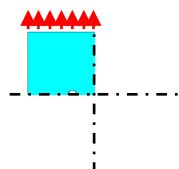
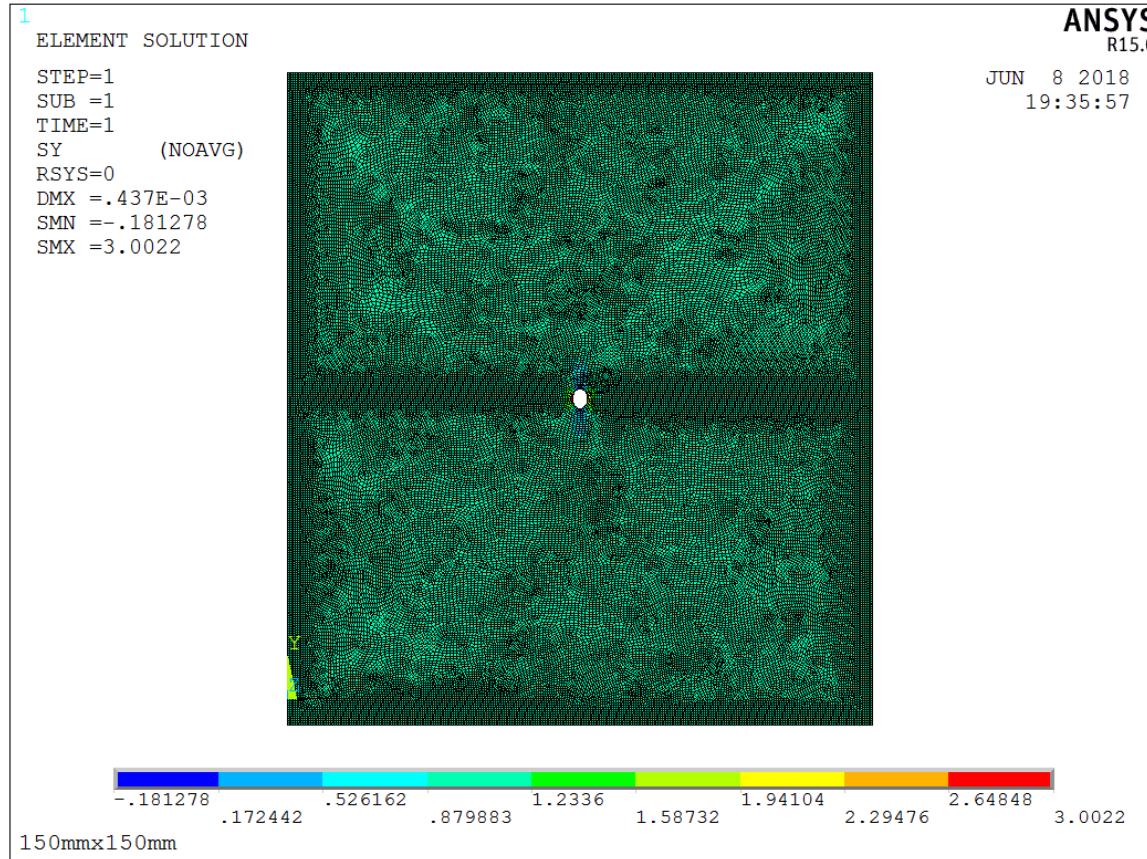
$$\text{Sigma}_{\max(150 \times 150)}^{\text{diff}=\left(\frac{70}{4}*D\right)=70} = 2.030161023$$

$$\text{Error} = \frac{\left| \text{Sigma}_{\max(150 \times 150)}^{\text{diff}=(5*D)=20} - \text{Sigma}_{\max(150 \times 150)}^{\text{diff}=\left(\frac{70}{4}*D\right)=70} \right|}{\text{Sigma}_{\max(150 \times 150)}^{\text{diff}=\left(\frac{70}{4}*D\right)=70}}$$

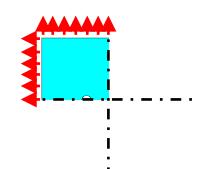
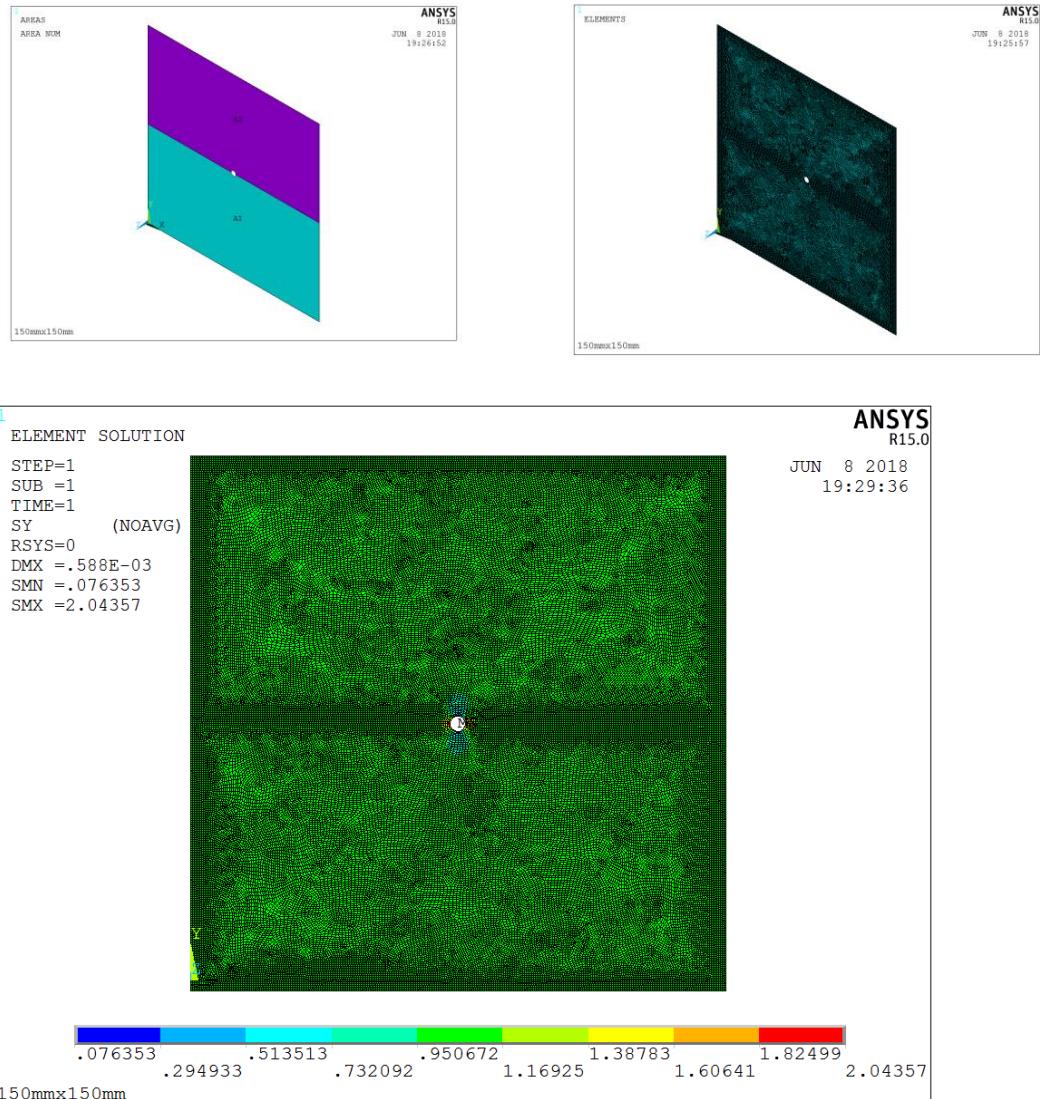
$$\text{Error} = \frac{|2.085622532 - 2.030161023|}{2.030161023} = 0.0273187734232251586282178366893 = 2.7318\%$$

0.4364 %

center_hole_2d



(a) Uniaxial
Transverse load



(b) Biaxial load