Cox Library for Lmrpp¹ Version 2.0

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 $^{^{1}} https://github.com/lmxyy/Code-Library-for-Lmxyy$

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Chapter 1

Algorithms

1.1 1D1D Dynamic Programming

```
// noi2009 诗人小 G
    #include<cstring>
    #include<cstdio>
    #include<cstdlib>
    using namespace std;
   #define limit (1e18)
   #define maxn 100010
   #define maxm 40
   int N,L,P,pre[maxn],top;
    char s[maxm];
    long double f[maxn];
    struct node { int l,r,key; }stack[maxn];
13
14
    inline long double qsm(int a,int b)
15
16
        long double ret = 1;
17
        while (b--) ret *= 1.0*a;
18
        return ret;
19
    }
20
    inline long double calc(int a,int b)
22
23
        return f[b]+qsm(abs(pre[a]-pre[b]-L),P);
24
    }
25
    inline int find(int a)
27
28
        int 1 = 1,r = top,mid;
29
        while (1 <= r)
30
31
            mid = (1 + r) >> 1;
32
            if (stack[mid].1 \le a \& \& stack[mid].r > = a) return stack[mid].key;
33
```

```
if (a < stack[mid].1) r = mid - 1;</pre>
34
             else l = mid + 1;
35
         }
36
    }
37
38
    inline void updata(int now)
39
    {
40
         int 1 = 1,r;
41
         while (top)
42
43
             if (calc(stack[top].1,stack[top].key) >= calc(stack[top].1,now))
44
                  --top;
45
             else
46
             {
47
                 1 = stack[top].1,r = stack[top].r;
48
                 while (1 <= r)
49
50
                      int mid = (1 + r) >> 1;
51
                      if (calc(mid,stack[top].key) >= calc(mid,now)) r = mid - 1;
52
                      else l = mid + 1;
53
                  }
54
                  stack[top].r = r;
55
                 break;
56
             }
57
         }
58
         if (1 \le N) stack[++top] = (node){1,N,now};
59
    }
60
61
    inline void dp()
62
63
        f[0] = 0;
64
         stack[top = 1] = (node) \{1,N,0\};
65
        for (int i = 1;i <= N;++i)</pre>
66
67
             int key = find(i);
68
             f[i] = calc(i,key);
69
             updata(i);
70
         }
71
    }
72
73
    int main()
74
    {
75
         freopen("1563.in","r",stdin);
76
        freopen("1563.out","w",stdout);
77
         int T; scanf("%d",&T);
78
        while (T--)
79
         {
80
             scanf("%d %d %d\n",&N,&L,&P);
81
             L++;
82
```

```
for (int i = 1;i <= N;++i)
83
            {
84
                scanf("%s",s);
85
                pre[i] = strlen(s)+1+pre[i-1];
            }
87
            dp();
            if (f[N] > limit) printf("Too hard to arrange\n");
89
            else printf("%.OLf\n",f[N]);
90
            printf("----\n");
91
92
        fclose(stdin); fclose(stdout);
93
        return 0;
94
    }
95
```

1.2 Dynamic Minimal Spanning Tree

```
// 每次修改一条边,每次修改一条边权值,求最小生成树
    #include<algorithm>
   #include<cstring>
    #include<vector>
    #include<iostream>
    #include<cstdio>
    #include<cstdlib>
    using namespace std;
   typedef long long 11;
10
    const int maxn = 100010; const ll inf = 1LL<<40;</pre>
11
    int N,M,Q,father[maxn],cnt[maxn],reid[maxn]; ll ans[maxn];
12
13
    inline int find(int a) { if (father[a] != a) return father[a] = find(father[a]); return
14
       father[a]; }
15
    inline int gi()
16
17
        char ch; int ret = 0,f = 1;
18
        do ch = getchar(); while (!(ch >= '0'&&ch <= '9')&&ch != '-');
19
        if (ch == '-') f = -1,ch = getchar();
20
        do ret = ret*10+ch-'0',ch = getchar(); while (ch >= '0'&&ch <= '9');
21
        return ret*f;
22
   }
23
24
    struct Edge
25
26
        int a,b,id; ll c;
27
        inline Edge() = default;
28
        inline Edge(int _a,int _b,int _id,ll _c):a(_a),b(_b),id(_id),c(_c) {}
29
        inline void read(int i) { a = gi(),b = gi(),c = gi(); id = i; }
30
        friend inline bool operator <(const Edge &x,const Edge &y) { return x.c < y.c; }
31
    }edge[22][maxn],tmp[maxn],bac[maxn];
```

```
33
    struct Operation
34
    {
35
         int x; 11 y;
36
         inline Operation() = default;
37
         inline Operation(int _x,ll _y):x(_x),y(_y) {}
38
         inline void read() { x = gi(),y = gi(); }
39
    }opt[maxn];
40
41
    inline void construct(int &tot,ll &sum)
42
    {
43
         sort(tmp+1,tmp+tot+1);
44
         for (int i = 1;i <= tot;++i)
45
             father[tmp[i].a] = tmp[i].a,father[tmp[i].b] = tmp[i].b;
46
         vector <Edge> vec;
47
         for (int i = 1;i <= tot;++i)</pre>
48
49
             int u = find(tmp[i].a), v = find(tmp[i].b);
50
             if (u != v) father[u] = v,vec.push_back(tmp[i]);
51
52
         for (int i = 0;i < (int)vec.size();++i)</pre>
53
             father[vec[i].a] = vec[i].a,father[vec[i].b] = vec[i].b;
54
         for (int i = 0;i < (int)vec.size();++i)</pre>
55
         {
56
             Edge e = vec[i];
57
             if (e.c != -inf) father[find(e.a)] = find(e.b),sum += e.c;
         }
59
         vec.clear();
60
         for (int i = 1;i <= tot;++i)</pre>
61
62
             int u = find(tmp[i].a), v = find(tmp[i].b);
63
             if (u != v)
64
65
                  tmp[i].a = u,tmp[i].b = v;
66
                  vec.push_back(tmp[i]);
67
             }
68
         }
69
         for (int i = 0;i < (int)vec.size();++i) tmp[i+1] = vec[i];</pre>
70
         for (int i = 1;i <= tot;++i) reid[tmp[i].id] = i;</pre>
71
         tot = (int)vec.size();
72
    }
73
    inline void destruct(int &tot)
75
76
         sort(tmp+1,tmp+tot+1);
77
         for (int i = 1;i <= tot;++i)</pre>
78
             father[tmp[i].a] = tmp[i].a,father[tmp[i].b] = tmp[i].b;
79
         vector <Edge> vec;
80
         for (int i = 1;i <= tot;++i)</pre>
81
```

```
{
82
             int u = find(tmp[i].a),v = find(tmp[i].b);
83
             if (u != v) father[u] = v,vec.push_back(tmp[i]);
84
             else if (tmp[i].c == inf) vec.push_back(tmp[i]);
85
86
         for (int i = 0;i < (int)vec.size();++i) tmp[i+1] = vec[i];</pre>
87
         tot = (int)vec.size();
88
    }
89
90
     inline void work(int 1,int r,int dep,ll sum)
91
92
         int tot = cnt[dep];
93
         for (int i = 1;i <= tot;++i) tmp[i] = edge[dep][i];</pre>
94
         if (1 == r)
95
         {
96
             bac[opt[1].x].c = opt[1].y;
97
             for (int i = 1;i <= tot;++i)
98
             {
99
                  tmp[i].c = bac[tmp[i].id].c;
100
                  father[tmp[i].a] = tmp[i].a;
101
                  father[tmp[i].b] = tmp[i].b;
102
             }
103
             sort(tmp+1,tmp+tot+1);
104
             for (int i = 1;i <= tot;++i)</pre>
105
106
                  int u = find(tmp[i].a),v = find(tmp[i].b);
107
                  if (u != v) sum += tmp[i].c,father[u] = v;
108
             }
109
             ans[1] = sum; return;
110
111
         for (int i = 1;i <= tot;++i)
112
             tmp[i].c = bac[tmp[i].id].c,reid[tmp[i].id] = i;
113
         for (int i = 1;i <= r;++i) tmp[reid[opt[i].x]].c = -inf;</pre>
114
         construct(tot,sum);
115
         for (int i = 1;i <= r;++i)
116
             tmp[reid[opt[i].x]].c = inf;
117
         destruct(tot);
118
         for (int i = 1;i <= tot;++i) edge[dep+1][i] = tmp[i];</pre>
119
         int mid = (1+r)>>1; cnt[dep+1] = tot;
120
         work(1,mid,dep+1,sum); work(mid+1,r,dep+1,sum);
121
    }
122
123
     int main()
124
     {
125
         // freopen("B.in", "r", stdin);
126
         N = gi(), M = gi(), Q = gi();
127
         for (int i = 1;i <= M;++i) bac[i].read(i),edge[0][i] = bac[i];</pre>
128
         for (int i = 1;i <= Q;++i) opt[i].read();</pre>
129
         for (int i = 1;i <= N;++i) father[i] = i;</pre>
130
```

```
cnt[0] = M; work(1,Q,0,0);
for (int i = 1;i <= Q;++i) printf("%lld\n",ans[i]);
return 0;
</pre>
```

1.3 Plug-like Dynamic Programming

```
// ural 1519
    #include<cstdio>
    #include<cstdlib>
    #include<cstring>
    #include<iostream>
    #include<algorithm>
    using namespace std;
    typedef long long 11;
    const int maxn = 14,maxs = 300010;
10
    int mp[maxn] [maxn], N, M, cur, last, total[2];
11
    int size,ex,ey,head[maxs],nxt[maxs],Hash[maxs];
12
    11 f[2][maxs],state[2][maxs];
13
    inline void init()
15
16
        memset(mp,0,sizeof mp); ex = ey = 0;
17
        size = cur = 0; last = 1;
18
        total[cur] = 1;
19
        state[cur][1] = 0;
20
        f[cur][1] = 1;
21
    }
22
23
    inline void calc(ll s,ll inc)
24
25
        int pos = s%maxs;
26
        for (int i = head[pos];i;i = nxt[i])
27
            if (state[cur][Hash[i]] == s)
            {
29
                 f[cur][Hash[i]] += inc;
30
                 return;
31
            }
32
        ++total[cur];
33
        state[cur][total[cur]] = s;
34
        f[cur][total[cur]] = inc;
35
        nxt[++size] = head[pos];
36
        head[pos] = size;
37
        Hash[size] = total[cur];
38
    }
39
40
    inline 11 work()
41
    {
42
```

```
11 \text{ ret} = 0;
43
         for (int i = 1;i <= N;++i)</pre>
44
45
             for (int k = 1;k <= total[cur];++k) state[cur][k] <<= 2;</pre>
46
             for (int j = 1; j \le M; ++j)
47
48
                 memset(head,0,sizeof head);
49
                  size = 0; cur ^= 1,last ^= 1;
50
                  total[cur] = 0;
51
                  for (int k = 1;k <= total[last];++k)</pre>
52
53
                      11 s = state[last][k],num = f[last][k];
54
                      int p = (s>>((j-1)<<1))%4, q = (s>>(j<<1))%4;
55
                      if (!mp[i][j]) { if (!p\&\&!q) calc(s,num); }
56
                      else if (!p&&!q)
57
                      {
58
                           if (mp[i+1][j]\&\&mp[i][j+1])
59
                               calc(s+(1<<((j-1)<<1))+2*(1<<(j<<1)),num);
60
61
                      else if (!p&&q)
62
63
                           if (mp[i][j+1]) calc(s,num);
64
                           if (mp[i+1][j]) calc(s-q*(1<<(j<<1))+q*(1<<((j-1)<<1)),num);
65
                      }
66
                      else if (p\&\&!q)
67
68
                           if (mp[i+1][j]) calc(s,num);
69
                           if (mp[i][j+1]) calc(s-p*(1<<((j-1)<<1))+p*(1<<(j<<1)),num);
70
71
                      else if (p == 1 \& \& q == 1)
72
73
                          int b = 1;
74
                          for (int t = j+1; t \le M; ++t)
75
76
                               int v = (s >> (t << 1)) %4;
77
                               if (v == 1) ++b; else if (v == 2) --b;
78
                               if (b == 0) { s -= 1*(1<<(t<<1)); break; }
79
80
                           calc(s-(1<<((j-1)<<1))-(1<<(j<<1)),num);
81
                      }
82
                      else if (p == 2 \& \& q == 2)
83
                      {
84
                           int b = 1;
85
                          for (int t = j-2;t \ge 0;--t)
86
87
                               int v = (s >> (t << 1)) %4;
88
                               if (v == 2) ++b; else if (v == 1) --b;
89
                               if (b == 0) { s += 1*(1<<(t<1)); break; }
90
                          }
91
```

```
calc(s-2*(1<<((j-1)<<1))-2*(1<<(j<<1)),num);
92
93
                       else if (p == 1 \& q == 2) { if (i == ex \& kj == ey) ret += num; }
94
                       else if (p == 2 \& \& q == 1)
95
                            calc(s-2*(1<<((j-1)<<1))-(1<<(j<<1)),num);
96
                  }
97
              }
98
         }
99
         return ret;
100
     }
101
102
     int main()
103
104
         freopen("1519.in","r",stdin);
105
         while (scanf("%d%d",&N,&M) != EOF)
106
107
              init();
108
              for (int i = 1;i <= N;++i)</pre>
109
                   for (int j = 1; j \le M; ++j)
110
                  {
111
                       char ch; do ch = getchar(); while (ch != '.'&&ch != '*');
112
                       if (ch == '.') ex = i,ey = j,mp[i][j] = 1;
113
114
              cout << work() << endl;</pre>
115
         }
116
         return 0;
117
     }
118
```

1.4 Slop Optimization

```
#include<algorithm>
   #include<cstring>
   #include<iostream>
   #include<cstdio>
   #include<cstdlib>
   using namespace std;
   typedef long long 11;
   const int maxn = 500010; const ll inf = 1LL<<60;</pre>
   int N,K,A[maxn]; ll pre[maxn],f[maxn];
10
11
   struct Point
12
   {
13
       11 x,y;
14
        inline Point() = default;
15
        inline Point(11 _x,11 _y):x(_x),y(_y) {}
16
       friend inline Point operator -(const Point &a,const Point &b) { return
17
    → Point(a.x-b.x,a.y-b.y); }
        friend inline 11 operator /(const Point &a,const Point &b) { return a.x*b.y-a.y*b.x; }
```

```
};
19
20
    inline ll calc(const Point &a,int b) { return -a.x*b+a.y; }
21
22
    struct Queue
23
24
        Point array[maxn]; int h,t;
25
        inline Queue() = default;
26
        inline void init() { h = t = 0; }
27
        inline void pop_front(int i) { while (t-h >= 2&&calc(array[h+1],i) > calc(array[h+2],i))
28
     inline void push(const Point &a,int i) { while (t-h >=
29
        2kk(a-array[t-1])/(array[t]-array[t-1]) >= 0) --t; array[++t] = a; 
        inline Point front() const { return array[h+1]; }
30
31
    }team;
32
    inline int gi()
33
34
        char ch; int ret = 0,f = 1;
35
        do ch = getchar(); while (!(ch >= '0'&&ch <= '9')&&ch != '-');
36
        if (ch == '-') f = -1, ch = getchar();
37
        do ret = ret*10+ch-'0',ch = getchar(); while (ch >= '0'&&ch <= '9');
38
        return ret*f;
39
    }
40
41
    int main()
42
    {
43
        // freopen("E.in", "r", stdin);
44
        for (int T = gi();T--;)
45
46
             N = gi(), K = gi(); team.init();
47
             for (int i = 1;i <= N;++i) A[i] = gi();</pre>
48
             for (int i = 1;i <= N;++i) pre[i] = pre[i-1]+A[i];</pre>
49
             for (int i = 1;i <= N;++i)</pre>
50
             {
51
                 if (i >= K)
52
                 {
53
                     if (f[i-K] != inf)
54
                          team.push(Point(A[i-K+1],f[i-K]-pre[i-K]+(11)(i-K)*A[i-K+1]),i);\\
55
                     team.pop_front(i);
56
                     f[i] = calc(team.front(),i)+pre[i];
57
                 }
58
                 else f[i] = inf;
59
             }
60
             cout << f[N] << endl;</pre>
61
62
        return 0;
63
    }
64
```

1.5 Three-dimension Partial Order

```
//三维偏序, CDQ 分治
    #define lowbit(a) (a&-a)
    int M,N,A,B,tree[maxn];
    inline void ins(int a,int b) { for (;a < maxn;a += lowbit(a)) tree[a] = max(tree[a],b); }</pre>
    inline void clear(int a) { for (;a < maxn;a += lowbit(a)) tree[a] = 0; }</pre>
    inline int calc(int a) { int ret = 0; for (;a;a -= lowbit(a)) ret = max(tree[a],ret); return

   ret; }

    struct Node
10
        int x,y,z,res;
11
        inline Node(int x = 0,int y = 0,int z = 0,int z = 0):x(x),y(y),z(z),res(res) {}
12
        inline void update() { ++x,++y,++z; }
13
    }E[maxn];
14
15
    inline bool cmpx(const Node &a,const Node &b)
16
17
        if (a.x != b.x) return a.x < b.x;</pre>
18
        else if (a.y != b.y) return a.y > b.y;
19
        else return a.z > b.z;
20
    }
21
    inline bool cmpy(const Node &a,const Node &b) { return a.y < b.y; }</pre>
22
23
    inline void work(int l,int r)
24
    {
25
        if (1 == r) { E[1].res = max(E[1].res,1); return; }
26
        int mid = (1+r) >> 1,p = 1;
27
        work(1,mid);
28
        sort(E+1,E+mid+1,cmpy);
29
        sort(E+mid+1,E+r+1,cmpy);
30
        for (int i = mid+1;i <= r;++i)</pre>
31
32
            for (;p <= mid\&\&E[p].y < E[i].y;++p) ins(E[p].z,E[p].res);
33
            E[i].res = max(E[i].res, calc(E[i].z-1)+1);
34
35
        while (p > 1) clear(E[--p].z);
36
        sort(E+mid+1,E+r+1,cmpx);
37
        work(mid+1,r);
38
    }
39
40
    inline int run()
41
42
        for (int i = 1;i <= N+M;++i) E[i].update();</pre>
43
        sort(E+1,E+N+M+1,cmpx); work(1,N+M);
44
        int ret = 0;
45
        for (int i = 1;i <= N+M;++i) ret = max(ret,E[i].res);</pre>
46
        return ret;
47
```

48 }

Chapter 2

Computational Geometry

2.1 Circle Intersection

```
//modified
    const double eps = 1e-7,pi = acos(-1.0);
    int N,M; double area[maxn]; // area[k] \rightarrow area of intersections >= k.
   inline int dcmp(double a)
        if (-eps <= a&&a <= eps) return 0;
        else if (a > 0) return 1; else return -1;
   }
9
10
   struct Point
11
12
        double x,y;
13
        inline Point() = default;
14
        inline Point(double _x,double _y):x(_x),y(_y) {}
15
        inline void read() { x = gi(),y = gi(); }
16
        inline double norm() const { return sqrt(x*x+y*y); }
17
        inline double angle() const { return atan2(y,x); }
        inline Point unit() const { double len = norm(); return Point(x/len,y/len); }
19
        friend inline Point operator-(const Point &a,const Point &b) { return
    → Point(a.x-b.x,a.y-b.y); }
        friend inline Point operator+(const Point &a,const Point &b) { return
21
    → Point(a.x+b.x,a.y+b.y); }
        friend inline Point operator*(const Point &a, double b) { return Point(a.x*b,a.y*b); }
22
        friend inline Point operator*(double b,const Point &a) { return Point(a.x*b,a.y*b); }
23
        friend inline Point operator/(const Point &a,double b) { return Point(a.x/b,a.y/b); }
24
        friend inline double operator/(const Point &a,const Point &b) { return a.x*b.y-a.y*b.x; }
25
   };
26
   struct Circle
27
        Point C; double r; int sgn;
29
        inline Circle() = default;
30
```

```
inline Circle(const Point &_C,double _r,int _sgn):C(_C),r(_r),sgn(_sgn) {}
31
        // sgn 代表该圆的权值, 默认 1
        friend inline bool operator == (const Circle &a, const Circle &b)
32
33
            if (dcmp(a.r-b.r)) return false;
34
            if (dcmp(a.C.x-b.C.x)) return false;
35
            if (dcmp(a.C.y-b.C.y)) return false;
36
            if (a.sgn != b.sgn) return false;
37
            return true;
38
39
        friend inline bool operator!=(const Circle &a,const Circle &b) { return !(a == b); }
40
    }cir[maxn];
41
42
    inline Point rotate(const Point &p,double cost,double sint)
43
44
    {
        double x = p.x, y = p.y;
45
        return Point(x*cost-y*sint,x*sint+y*cost);
46
    }
47
    inline pair <Point,Point> crosspoint(const Point &ap,double ar,const Point &bp,double br)
48
49
        double d = (ap-bp).norm(),cost = (ar*ar+d*d-br*br)/(2*ar*d),sint = sqrt(1-cost*cost);
50
        Point v = ((bp-ap).unit())*ar;
51
        return make_pair(ap+rotate(v,cost,-sint),ap+rotate(v,cost,sint));
52
    }
53
    inline pair <Point,Point> crosspoint(const Circle &a,const Circle &b) { return
54
        crosspoint(a.C,a.r,b.C,b.r); }
55
    inline bool overlap(const Circle &a,const Circle &b) { return dcmp(a.r-b.r-(a.C-b.C).norm()) >=
56
    → 0; } // b 是不是在 a 里面
    inline bool intersect(const Circle &a,const Circle &b)
57
    {
58
        if (overlap(a,b)) return false;
59
        if (overlap(b,a)) return false;
60
        return dcmp((a.C-b.C).norm()-a.r-b.r) < 0;
61
    }
62
63
    struct Event
64
65
        Point p; double a; int d;
66
        inline Event() = default;
67
        in line \  \, Event(const\ Point\ \&\_p, \\ double\ \_a, \\ double\ \_d):p(\_p), \\ a(\_a), \\ d(\_d)\ \{\}
68
        friend inline bool operator <(const Event &a,const Event &b) { return a.a < b.a; }
69
70
    };
71
    inline void solve()
72
73
        for (int i = 1;i <= M;++i) area[i] = 0;</pre>
74
        for (int i = 1;i <= M;++i)</pre>
75
76
```

```
int cnt = cir[i].sgn; if (cnt<0) cnt = 0; vector <Event> event;
77
             for (int j = 1; j < i; ++j) if (cir[i] == cir[j]) cnt += cir[j].sgn;
78
             for (int j = 1; j \le M; ++j)
79
                 if (j != i\&\&cir[i] != cir[j]\&\&overlap(cir[j],cir[i])) cnt += cir[j].sgn;
80
             for (int j = 1; j \le M; ++j)
81
                 if (j != i&&intersect(cir[i],cir[j]))
82
                 ł
83
                      pair <Point,Point> res = crosspoint(cir[i],cir[j]); swap(res.first,res.second);
84
                      double alpha1 = (res.first-cir[i].C).angle(),alpha2 =
85
         (res.second-cir[i].C).angle();
                      event.push_back(Event(res.second,alpha2,cir[j].sgn));
86
                      event.push_back(Event(res.first,alpha1,-cir[j].sgn));
87
                      cnt += (alpha2 > alpha1)*cir[j].sgn;
88
                 }
89
             if (!event.size()) area[cnt] += pi*cir[i].r*cir[i].r*cir[i].sgn;
90
             else
91
             {
92
                 sort(event.begin(),event.end());
93
                 event.push_back(event.front());
94
                 for (int j = 0; j+1 < (int)event.size(); ++j)
95
                 {
96
                      cnt += event[j].d;
97
                      area[cnt] += event[j].p/event[j+1].p/2*cir[i].sgn;
98
                      double alpha = event[j+1].a-event[j].a;
99
                      if (alpha < 0) alpha += 2*pi;</pre>
100
                      if (!dcmp(alpha)) continue;
101
                      area[cnt] += alpha*cir[i].r*cir[i].r/2*cir[i].sgn;
102
                      area[cnt] += -sin(alpha)*cir[i].r*cir[i].r/2*cir[i].sgn;
103
                 }
104
             }
105
         }
106
    }
107
108
    // origin
109
    struct Event {
110
         Point p;
111
         double ang;
112
         int delta;
113
         Event (Point p = Point(0, 0), double ang = 0, double delta = 0) : p(p), ang(ang),
114
         delta(delta) {}
    };
115
    bool operator < (const Event &a, const Event &b) {</pre>
116
         return a.ang < b.ang;
117
    }
118
    void addEvent(const Circle &a, const Circle &b, vector<Event> &evt, int &cnt) {
119
         double d2 = (a.o - b.o).len2(),
120
                dRatio = ((a.r - b.r) * (a.r + b.r) / d2 + 1) / 2,
121
                pRatio = sqrt(-(d2 - sqr(a.r - b.r)) * (d2 - sqr(a.r + b.r)) / (d2 * d2 * 4));
122
         Point d = b.o - a.o, p = d.rotate(PI / 2),
123
```

```
q0 = a.o + d * dRatio + p * pRatio,
124
               q1 = a.o + d * dRatio - p * pRatio;
125
         double ang 0 = (q0 - a.o).ang(),
126
                ang1 = (q1 - a.o).ang();
127
         evt.push_back(Event(q1, ang1, 1));
128
         evt.push_back(Event(q0, ang0, -1));
129
         cnt += ang1 > ang0;
130
    }
131
    bool issame(const Circle &a, const Circle &b) { return sign((a.o - b.o).len()) == 0 && sign(a.r
132
     \hookrightarrow - b.r) == 0; }
    bool overlap(const Circle &a, const Circle &b) { return sign(a.r - b.r - (a.o - b.o).len()) >=
133
     → 0; }
    bool intersect(const Circle &a, const Circle &b) { return sign((a.o - b.o).len() - a.r - b.r) <</pre>
134
     Circle c[N];
135
    double area[N]; // area[k] \rightarrow area of intersections >= k.
136
    Point centroid[N]; //k 次圆的质心
137
    bool keep[N];
138
    void add(int cnt, DB a, Point c) {
139
         area[cnt] += a;
140
         centroid[cnt] = centroid[cnt] + c * a;
141
    }
142
    void solve(int C) {
143
         for (int i = 1; i <= C; ++ i) {
144
             area[i] = 0;
145
             centroid[i] = Point(0, 0);
146
         }
147
         for (int i = 0; i < C; ++i) {
148
             int cnt = 1;
149
             vector<Event> evt;
150
             for (int j = 0; j < i; ++j) if (issame(c[i], c[j])) ++cnt;
151
             for (int j = 0; j < C; ++j) {
152
                 if (j != i \&\& !issame(c[i], c[j]) \&\& overlap(c[j], c[i])) {
153
                      ++cnt;
154
                 }
155
             }
156
             for (int j = 0; j < C; ++j) {
157
                 if (j != i && !overlap(c[j], c[i]) && !overlap(c[i], c[j]) && intersect(c[i], c[j]))
158
         {
                      addEvent(c[i], c[j], evt, cnt);
159
                 }
160
             }
161
             if (evt.size() == Ou) {
162
                 add(cnt, PI * c[i].r * c[i].r, c[i].o);
163
             } else {
164
                 sort(evt.begin(), evt.end());
165
                 evt.push_back(evt.front());
166
                 for (int j = 0; j + 1 < (int)evt.size(); ++j) {</pre>
167
                      cnt += evt[j].delta;
168
```

```
add(cnt, det(evt[j].p, evt[j + 1].p) / 2, (evt[j].p + evt[j + 1].p) / 3);
169
                      double ang = evt[j + 1].ang - evt[j].ang;
170
                      if (ang < 0) {
171
                          ang += PI * 2;
172
173
                      if (sign(ang) == 0) continue;
174
                      double ang0 = evt[j].a,ang1 = evt[j+1].a;
175
                      add(cnt, ang * c[i].r * c[i].r / 2, c[i].o +
176
                          Point(sin(ang1) - sin(ang0), -cos(ang1) + cos(ang0)) * (2 / (3 * ang) *
177
         c[i].r));
                      add(cnt, -sin(ang) * c[i].r * c[i].r / 2, (c[i].o + evt[j].p + evt[j + 1].p) /
178
         3);
                 }
179
             }
180
181
         for (int i = 1; i <= C; ++ i)
182
             if (sign(area[i])) {
183
                 centroid[i] = centroid[i] / area[i];
184
185
    }
186
```

2.2 Common Formulas

```
//计算几何常用公式
    inline int dcmp(double a)
    {
        if (fabs(a) <= eps) return 0;</pre>
        else if (a > 0) return 1;
        else return -1;
    struct Point
9
        double x,y;
10
        inline Point() = default;
11
        inline Point(double _x,double _y):x(_x),y(_y) {}
12
        inline Point unit() const
13
14
            double len = norm();
15
            if (!dcmp(len)) return Point(1,0);
16
            else return *this/len;
17
18
        inline double norm() const { return sqrt(x*x+y*y); }
19
        inline Point reflect(const Point &p) const
20
        {
21
            Point v = *this-p; double len = v.norm();
22
            v = v/len; return p+v*(1/len);
23
        }
24
        inline void read() { scanf("%lf %lf",&x,&y); }
25
        inline Point vertical() const { return Point(y,-x); }
26
```

```
inline double angle() const
27
        {
28
            double ret = atan2(y,x);
29
            if (ret < 0) ret += 2*pi;</pre>
30
            return ret;
31
32
        friend inline bool operator == (const Point &a, const Point &b) { return
33
        !dcmp(a.x-b.x)&&!dcmp(a.y-b.y); }
        friend inline Point operator -(const Point &a,const Point &b) { return
34
        Point(a.x-b.x,a.y-b.y); }
        friend inline Point operator +(const Point &a,const Point &b) { return
35
     → Point(a.x+b.x,a.y+b.y); }
        friend inline Point operator /(const Point &a,double b) { return Point(a.x/b,a.y/b); }
36
        friend inline Point operator *(const Point &a,double b) { return Point(a.x*b,a.y*b); }
37
        friend inline Point operator *(double b,const Point &a) { return Point(a.x*b,a.y*b); }
38
        friend inline double operator /(const Point &a,const Point &b) { return a.x*b.y-a.y*b.x; }
39
    };
40
    struct Line
41
42
    {
        Point p,v; double slop;
43
        inline Line() = default;
44
        inline Line(const Point &_p,const Point &_v):p(_p),v(_v) {}
45
        inline void update() { slop = v.alpha(); }
46
        friend inline bool operator <(const Line &11,const Line &12)
47
        { return l1.slop < l2.slop; }
48
        inline double dis(const Point &a) { fabs((a-p)/v)/(v.len()); } //点到直线距离
49
    };
50
51
    inline bool OnLine(const Line &1,const Point &p) { return !dcmp(1.v/(p-1.p)); } //点在直线上
52
53
    inline Point CrossPoint(const Line &a,const Line &b) //直线交点
54
    {
55
        Point u = a.p - b.p;
56
        double t = (b.v/u)/(a.v/b.v);
57
        return a.p+a.v*t;
58
    }
59
60
    inline bool parallel(const Line &a,const Line &b) { return !dcmp(a.v/b.v); } //直线平行
61
62
    inline Point rotate(const Point &p,double cost,double sint)
63
64
        double x = p.x, y = p.y;
65
        return Point(x*cost-y*sint,x*sint+y*cost);
66
    }
67
68
    inline Point reflect(const Point &a,const Line &1)
69
    {
70
        Point p = 1.p, v = 1.v; v = v.unit();
71
        return (2*v*(a-p))*v-(a-p)+p;
72
```

2.3 Convex Hull

```
struct Point
2
    {
        inline Point() = default;
3
        inline Point(double _x,double _y):x(_x),y(_y) {}
        inline Point unit() const
            double len = norm();
            if (!dcmp(len)) return Point(1,0);
            else return *this/len;
        }
10
        inline double norm() const { return sqrt(x*x+y*y); }
11
        inline Point reflect(const Point &p) const
12
13
            Point v = *this-p; double len = v.norm();
14
            v = v/len; return p+v*(1/len);
15
        }
16
        inline void read() { scanf("%lf %lf",&x,&y); }
17
        inline Point vertical() const { return Point(y,-x); }
18
        inline double angle() const
19
20
            double ret = atan2(y,x);
21
            if (ret < 0) ret += 2*pi;</pre>
22
            return ret;
23
        }
24
        friend inline bool operator ==(const Point &a,const Point &b) { return
25
        !dcmp(a.x-b.x)&&!dcmp(a.y-b.y); }
        friend inline Point operator -(const Point &a,const Point &b) { return
26
     → Point(a.x-b.x,a.y-b.y); }
        friend inline Point operator +(const Point &a,const Point &b) { return
27
     \hookrightarrow Point(a.x+b.x,a.y+b.y); }
        friend inline Point operator /(const Point &a,double b) { return Point(a.x/b,a.y/b); }
28
        friend inline Point operator *(const Point &a,double b) { return Point(a.x*b,a.y*b); }
29
        friend inline Point operator *(double b,const Point &a) { return Point(a.x*b,a.y*b); }
30
        friend inline double operator /(const Point &a,const Point &b) { return a.x*b.y-a.y*b.x; }
31
        friend inline bool operator <(const Point &a,const Point &b)
32
33
            if (a.x != b.x) return a.x < b.x;
34
```

```
else return a.y < b.y;</pre>
35
36
    }P[maxn],convex[maxn];
37
    inline void ConvexHull()
39
40
        sort(P+1,P+N+1); //x 第一关键字, y 第二关键字从小到大排序
41
        for (int i = 1;i <= N;++i)</pre>
42
43
             while (m > 1\&\&(convex[m]-convex[m-1])/(P[i]-convex[m-1]) <= 0) --m;
44
             convex[++m] = P[i];
45
        }
46
        int k = m;
47
        for (int i = N-1;i;--i)
48
49
             while (m > k \&\& (convex[m]-convex[m-1])/(P[i]-convex[m-1]) \le 0) --m;
50
             convex[++m] = P[i];
51
        }
52
        if (N > 1) m--;
53
    }
54
```

2.4 Cross Points of Circles

```
//圆圆求交,需先判定两圆有交
inline Point rotate(const Point &p,double cost,double sint)

{
    double x = p.x,y = p.y;
    return Point(x*cost-y*sint,x*sint+y*cost);
}

inline pair <Point,Point> CrossPoint(const Point &ap,double ar,const Point &bp,double br)

{
    double d = (ap-bp).norm();
    double cost = (ar*ar+d*d-br*br)/(2*ar*d),sint = sqrt(1-cost*cost);
    Point v = ((bp-ap)/(bp-ap).norm())*ar;
    return make_pair(ap+rotate(v,cost,-sint),ap+rotate(v,cost,sint));
}
```

2.5 Cross Points of Line and Circle

```
double A = dx*dx+dy*dy;
9
        double B = 2*dx*(X1-X0)+2*dy*(Y1-Y0);
10
        double C = (X1-X0)*(X1-X0)+(Y1-Y0)*(Y1-Y0)-r*r;
11
        double delta = B*B-4*A*C+eps;
12
        num = 0;
13
        if (delta >= 0)
14
15
            double t1 = (-B-sqrt(delta))/(2*A);
16
            double t2 = (-B+sqrt(delta))/(2*A);
17
            ret[++num] = Point(X1+t1*dx,Y1+t1*dy);
18
            ret[++num] = Point(X1+t2*dx,Y1+t2*dy);
19
        }
20
    }
21
```

2.6 Graham Scanning Algorithm

```
//凸包上最大四边形面积
    #include<cmath>
    #include<algorithm>
    #include<cstring>
    #include<iostream>
    #include<cstdio>
    #include<cstdlib>
    using namespace std;
    const int maxn = 2010;
10
    int N,M; double ans;
11
12
    struct Point
13
    {
14
        double x,y;
15
        Point() = default;
16
        Point(double _x,double _y):x(_x),y(_y) {}
17
        inline void read() { scanf("%lf %lf",&x,&y); }
18
        friend inline Point operator -(const Point &a,const Point &b) { return
19
     → Point(a.x-b.x,a.y-b.y); }
        friend inline double operator /(const Point &a,const Point &b) { return a.x*b.y-a.y*b.x; }
20
        friend inline double operator <(const Point &a,const Point &b)
21
22
            if (a.x != b.x) return a.x < b.x;</pre>
23
            else return a.y < b.y;</pre>
24
25
    }P[maxn],convex[maxn];
26
27
    inline int gi()
28
    {
29
        char ch; int ret = 0, f = 1;
30
        do ch = getchar(); while (!(ch >= '0'&&ch <= '9')&&ch != '-');
31
        if (ch == '-') f = -1, ch = getchar();
32
```

```
do ret = ret*10+ch-'0',ch = getchar(); while (ch >= '0'&&ch <= '9');
33
        return ret*f;
34
    }
35
36
    inline void ConvexHull()
37
38
        int m = 0;
39
        sort(P+1,P+N+1); //x 第一关键字, y 第二关键字从小到大排序
40
        for (int i = 1;i <= N;++i)</pre>
41
42
             while (m > 1\&\&(convex[m]-convex[m-1])/(P[i]-convex[m-1]) \le 0) --m;
43
             convex[++m] = P[i];
44
        }
45
        int k = m;
46
        for (int i = N-1; i; --i)
47
48
             while (m > k \& \& (convex[m]-convex[m-1])/(P[i]-convex[m-1]) <= 0) --m;
49
             convex[++m] = P[i];
50
51
        if (N > 1) m--; M = m;
52
    }
53
54
    inline void Graham()
55
    {
56
        for (int i = 1;i <= M;++i) convex[i+M] = convex[i];</pre>
57
        int p1,p2,p3,p4;
58
        for (p1 = 1;p1 <= M;++p1)
59
60
             p2 = p1+1;
61
             p3 = p2+1;
62
             p4 = p3+1;
63
             for (;p3 < p1+M-1;++p3)
64
65
                 Point v = convex[p3]-convex[p1];
66
                 while (p2 < p3\&\&fabs((convex[p2]-convex[p1])/v) <
67
         fabs((convex[p2+1]-convex[p1])/v)) ++p2;
                 while (p4 < p1+M\&\&fabs((convex[p4]-convex[p1])/v) <
68
         fabs((convex[p4+1]-convex[p1])/v)) ++p4;
                 ans = \max(ans,fabs((convex[p2]-convex[p1])/v)+fabs((convex[p4]-convex[p1])/v));
69
70
        }
71
        ans = ans/2;
72
    }
73
74
    int main()
75
76
        N = gi();
77
        for (int i = 1;i <= N;++i) P[i].read();</pre>
78
        ConvexHull();
79
```

```
Graham();
80
       printf("%.3f\n",ans);
81
       return 0;
82
    }
83
    84
    inline void jam() //凸包上最大四边形面积
    {
86
       for (int i = 1;i <= m;++i) ch[i+m] = ch[i]; //凸包倍长
87
       for (int p1 = 1,p2,p3,p4;p1 <= m;++p1)</pre>
88
89
           p2 = p1 + 1;
90
           p3 = p2 + 1;
91
           p4 = p3 + 1;
92
           for (;p3 < p1 + m - 1;++p3)
93
94
           {
               Line 1 = ((SEG) { ch[p1],ch[p3] }).extend();//枚举对角线,线段变成直线
95
               while (p2 < p3 && 1.dis(ch[p2]) < 1.dis(ch[p2 + 1])) ++p2;//点到直线距离
96
               while (p4 < p1 + m && 1.dis(ch[p4]) < 1.dis(ch[p4 + 1])) ++p4;
97
               ans = max(ans,(1.dis(ch[p2])+1.dis(ch[p4]))*(ch[p1] - ch[p3]).len()/2);//更新答案
98
           }
99
       }
100
    }
101
```

2.7 Half Plane Intersection

```
//半平面交,直线左侧半平面,注意最后是 tail-head <= 0 还是 tail-head <= 1
   inline int dcmp(double a)
3
        if (-eps <= a&&a <= eps) return 0;</pre>
        else if (a > 0) return 1; else return -1;
   }
   struct Point
   {
       double x,y;
        inline Point() = default;
11
        inline Point(double _x,double _y):x(_x),y(_y) {}
        inline void read() { x = gi(),y = gi(); }
13
       inline Point vertical() const { return Point(-y,x); }
       inline Point unit() const
17
           double len = norm();
           if (!dcmp(len)) return Point(1,0);
           else return *this/len;
        inline double norm() const { return sqrt(x*x+y*y); }
21
        inline double angle() const { return atan2(y,x); }
        friend inline Point operator+(const Point &a,const Point &b) { return
       Point(a.x+b.x,a.y+b.y); }
```

```
friend inline Point operator-(const Point &a,const Point &b) { return
24
     → Point(a.x-b.x,a.y-b.y); }
        friend inline Point operator*(const Point &a, double b) { return Point(a.x*b,a.y*b); }
25
        friend inline Point operator*(double b,const Point &a) { return Point(a.x*b,a.y*b); }
26
        friend inline double operator/(const Point &a,const Point &b) { return a.x*b.y-a.y*b.x; }
27
    }P[maxn],pp[maxn],pol[maxn];
28
29
    struct Line
30
31
        Point p,v;
32
        inline Line(const Point _p = Point(),const Point _v = Point()):p(_p),v(_v) {}
33
        inline double slop() const { return v.angle(); }
34
        friend inline bool operator < (const Line &a, const Line &b) { return a.slop() < b.slop(); }
35
    }line[maxn],qq[maxn];
36
37
    inline bool onleft(const Line &L,const Point &p)
38
39
        return dcmp(L.v/(p-L.p)) > 0;
40
    }
41
    inline bool parallel(const Line &a,const Line &b) { return !dcmp(a.v/b.v); }
42
    inline Point crosspoint(const Line &a,const Line &b)
43
44
        Point u = a.p-b.p;
45
        double t = (b.v/u)/(a.v/b.v);
46
        return a.p+(a.v*t);
47
    }
48
49
    inline int half_plane_intersection()
50
51
        sort(lines+1,lines+tot+1); //直线按斜率排序
52
        int head,tail;
53
        qq[head = tail = 1] = lines[1];
54
        for (int i = 2;i <= tot;++i)
55
56
            while (head < tail&&!onleft(lines[i],pp[tail-1])) --tail;</pre>
57
            while (head < tail&&!onleft(lines[i],pp[head])) ++head;</pre>
58
            qq[++tail] = lines[i];
59
            if (parallel(qq[tail],qq[tail-1]))
60
            {
61
                 tail--:
62
                 if (onleft(qq[tail],lines[i].p)) qq[tail] = lines[i];
63
64
            if (head < tail) pp[tail-1] = crosspoint(qq[tail],qq[tail-1]);</pre>
65
        }
66
        while (head < tail && !onleft(qq[head],pp[tail-1])) --tail;</pre>
67
        if (tail-head <= 0) return 0;</pre>
68
        pp[tail] = crosspoint(qq[tail],qq[head]);
69
        for (int i = head;i <= tail;++i) pol[++m] = pp[i]; //半平面交点
70
        pol[0] = pol[m];
71
```

```
72     return m;
73  }
```

2.8 Intersecting Area of Circle and Polygon

```
const int maxn = 510;
    const double eps = 1e-9;
    inline int dcmp(double a)
        if (a > eps) return 1;
        else if (a < -eps) return -1;
        else return 0;
    }
10
    struct Point
11
12
        double x,y;
13
        Point() = default;
14
        Point(double _x,double _y):x(_x),y(_y) {}
15
        inline double norm() const { return sqrt(x*x+y*y); }
16
        inline Point unit() const { double len = norm(); return Point(x/len,y/len); }
17
        friend Point operator +(const Point &a,const Point &b) { return Point(a.x+b.x,a.y+b.y); }
18
        friend Point operator -(const Point &a,const Point &b) { return Point(a.x-b.x,a.y-b.y); }
19
        friend Point operator *(const Point &a,double b) { return Point(a.x*b,a.y*b); }
20
        friend Point operator *(double b,const Point &a) { return Point(a.x*b,a.y*b); }
21
        friend Point operator /(const Point &a,double b) { return Point(a.x/b,a.y/b); }
22
        friend double operator /(const Point &a,const Point &b) { return a.x*b.y-b.x*a.y; }
23
        friend double operator *(const Point &a,const Point &b) { return a.x*b.x+a.y*b.y; }
24
        inline void read() { scanf("%lf %lf",&x,&y); }
25
    }P[maxn],A,B;
    int N; double K;
27
    inline double getSectorArea(const Point &a,const Point &b,double r)
29
30
        double c = (2*r*r-((a-b)*(a-b)))/(2*r*r);
31
        double alpha = acos(c);
32
        return r*r*alpha/2.0;
33
    }
34
35
    inline pair <double, double > getSolution(double a, double b, double c)
36
37
    {
        double delta = b*b-4*a*c;
38
        if (dcmp(delta) < 0) return make_pair(0,0);</pre>
39
        else return make_pair((-b-sqrt(delta))/(2*a),(-b+sqrt(delta))/(2*a));
40
    }
41
42
    inline pair <Point,Point> getIntersection(const Point &a,const Point &b,double r)
43
    {
44
```

```
Point d = b-a;
45
        double A = d*d, B = 2*(d*a), C = (a*a)-r*r;
46
        pair <double, double> s = getSolution(A,B,C);
47
        return make_pair(a+(d*s.first),a+(d*s.second));
48
    }
49
50
    inline double getPointDist(const Point &a,const Point &b)
51
52
        Point d = b-a;
53
        int sA = dcmp(a*d),sB = dcmp(b*d);
54
        if (sA*sB \le 0) return (a/b)/((a-b).norm());
55
        else return min(a.norm(),b.norm());
56
    }
57
    double getArea(const Point &a,const Point &b,double r)
59
60
        double dA = a*a,dB = b*b,dC = getPointDist(a,b),ans = 0;
61
        if (dcmp(dA-r*r) \le 0 \&\&dcmp(dB-r*r) \le 0) return (a/b)/2;
62
        Point tA = a.unit()*r,tB = b.unit()*r;
63
        if (dcmp(dC-r) > 0) return getSectorArea(tA,tB,r);
64
        pair <Point,Point> ret = getIntersection(a,b,r);
65
        if (dcmp(dA-r*r) > 0\&\&dcmp(dB-r*r) > 0)
66
        {
67
            ans += getSectorArea(tA,ret.first,r);
            ans += (ret.first/ret.second)/2;
69
            ans += getSectorArea(ret.second,tB,r);
70
            return ans;
71
        }
72
        if (dcmp(dA-r*r) > 0) return (ret.first/b)/2+getSectorArea(tA,ret.first,r);
73
        else return (a/ret.second)/2.0+getSectorArea(ret.second,tB,r);
74
    }
75
76
    double getArea(int n,Point *p,const Point &c,double r)
77
78
        double ret = 0;
79
        for (int i = 0; i < n; ++i)
80
81
            int sgn = dcmp((p[i]-c)/(p[(i+1)\%n]-c));
            if (sgn > 0) ret += getArea(p[i]-c,p[(i+1)%n]-c,r);
83
            else ret = getArea(p[(i+1)\%n]-c,p[i]-c,r);
84
        }
85
        return fabs(ret);
86
    }
87
```

2.9 Intersection of Line and Convex Hull

```
1 //O(logN)
2 inline double getA(const Node &a)
3 {
```

```
double ret = atan2(a.y,a.x);
4
         if (ret \leftarrow -pi/2) ret += 2*pi;
5
         return ret;
    }
    inline int find(double x)
    {
10
         if (x \le w[1] | |x >= w[m]) return 1;
11
        return upper_bound(w+1,w+m+1,x)-w;
12
    }
13
14
    inline bool intersect(const Node &a,const Node &b)
15
16
         int i = find(getA(b-a)),j = find(getA(a-b));
17
         if (dcmp((b-a)/(hull[i]-a))*dcmp((b-a)/(hull[j]-a)) > 0) return false;
18
         else return true;
19
    }
20
21
    inline void convex()
22
23
        for (int i = 1;i <= N;++i)</pre>
24
25
             while (m > 1\&\&(hull[m]-hull[m-1])/(P[i]-hull[m-1]) <= 0) --m;
26
             hull[++m] = P[i];
27
         }
28
         int k = m;
29
        for (int i = N-1; i; --i)
30
31
             while (m > k\&\&(hull[m]-hull[m-1])/(P[i]-hull[m-1]) \ll 0) --m;
32
             hull[++m] = P[i];
33
         }
34
         if (N > 1) m--;
35
         for (int i = 1;i <= m;++i)</pre>
36
             w[i]= getA(hull[i+1]-hull[i]);
37
    }
38
```

2.10 Minimal Product

```
1  // 最小乘积匹配
2  #include<algorithm>
3  #include<cstring>
4  #include<iostream>
5  #include<cstdio>
6  #include<cstdlib>
7  using namespace std;
8
9  const int maxn = 80,inf = 1<<29;
int N,ans,A[maxn][maxn],B[maxn][maxn];
11</pre>
```

```
inline int gi()
12
13
        char ch; int ret = 0,f = 1;
14
        do ch = getchar(); while (!(ch >= '0'&&ch <= '9')&&ch != '-');
15
        if (ch == '-') f = -1,ch = getchar();
16
        do ret = ret*10+ch-'0', ch = getchar(); while (ch >= '0'&&ch <= '9');
17
        return ret*f;
18
    }
19
20
    struct KM
21
    {
22
        int w[maxn] [maxn],lx[maxn],ly[maxn],match[maxn],way[maxn],slack[maxn]; bool used[maxn];
23
24
        inline void init()
25
        {
26
             for (int i = 1;i <= N;++i)</pre>
27
                 match[i] = lx[i] = ly[i] = way[i] = 0;
28
        }
29
30
        inline void hungary(int x)
31
32
             match[0] = x; int j0 = 0;
33
             for (int j = 0; j \le N; ++j)
34
                 slack[j] = -inf,used[j] = false;
35
             do
36
             {
37
                 used[j0] = true;
38
                 int i0 = match[j0],delta = -inf,j1 = 0;
39
                 for (int j = 1; j \le N; ++j)
40
                     if (!used[j])
41
                      {
42
                          int cur = -w[i0][j]-lx[i0]-ly[j];
43
                          if (cur > slack[j]) slack[j] = cur,way[j] = j0;
44
                          if (slack[j] > delta) delta = slack[j],j1 = j;
45
46
                 for (int j = 0; j \le N; ++j)
47
                 {
48
                      if (used[j]) lx[match[j]] += delta,ly[j] -= delta;
49
                      else slack[j] -= delta;
50
                 }
51
                 j0 = j1;
52
53
             while (match[j0]);
54
             do
55
             {
56
                 int j1 = way[j0];
57
                 match[j0] = match[j1];
58
                 j0 = j1;
59
             }
60
```

```
while (j0);
61
         }
62
 63
         inline void work() { for (int i = 1;i <= N;++i) hungary(i); }</pre>
64
65
         inline int get_ans()
 66
         {
67
              int sum = 0;
 68
              for (int i = 1;i <= N;++i)
 69
 70
                  // if (w[match[i]][i] == inf); // 无解
 71
                  if (match[i] > 0) sum += w[match[i]][i];
 72
              }
73
              return sum;
 74
         }
 75
 76
         inline void getp(int &x,int &y)
77
          {
 78
              x = y = 0;
 79
              for (int i = 1;i <= N;++i)</pre>
 80
                  x += A[match[i]][i],y += B[match[i]][i];
 81
         }
 82
     }km;
 83
 84
     inline void work(int X1,int Y1,int X2,int Y2)
 85
     {
 86
         km.init();
 87
         for (int i = 1;i <= N;++i)</pre>
 88
              for (int j = 1; j \le N; ++j)
 89
                  km.w[i][j] = (X2-X1)*B[i][j]+(Y1-Y2)*A[i][j];
 90
         km.work();
91
         if (km.get_ans() >= X2*Y1-X1*Y2) return;
92
         int x,y; km.getp(x,y);
93
         ans = min(ans,x*y);
94
         work(X1,Y1,x,y); work(x,y,X2,Y2);
95
     }
96
97
     int main()
98
     {
99
         // freopen("B.in", "r", stdin);
100
         for (int T = gi();T--;)
101
          {
102
              N = gi(); ans = inf;
103
              for (int i = 1; i \le N; ++i) for (int j = 1; j \le N; ++j) A[i][j] = gi();
104
              for (int i = 1; i \le N; ++i) for (int j = 1; j \le N; ++j) B[i][j] = gi();
105
              int X1,Y1,X2,Y2;
106
              km.init();
107
              for (int i = 1;i <= N;++i)</pre>
108
                  for (int j = 1; j \le N; ++j)
109
```

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```
km.w[i][j] = A[i][j];
110
              km.work(); km.getp(X1,Y1);
111
              km.init();
112
              for (int i = 1;i <= N;++i)
113
                  for (int j = 1; j \le N; ++j)
114
                       km.w[i][j] = B[i][j];
115
              km.work(); km.getp(X2,Y2);
116
              ans = min(X1*Y1,X2*Y2);
117
              work(X1,Y1,X2,Y2);
118
              cout << ans << endl;</pre>
119
120
         fclose(stdin); fclose(stdout);
121
         return 0;
122
    }
123
```

Planar Graph 2.11

28

```
// 包括平面图转对偶图
    inline int dcmp(double a)
3
        if (fabs(a) <= eps) return 0;</pre>
        else if (a > 0) return 1;
        else return -1;
    }
    struct Point
    {
        double x,y;
10
        inline Point(double _x = 0,double _y = 0):x(_x),y(_y) {}
11
        inline void read() { x = gi(),y = gi(); }
12
        friend inline Point operator-(const Point &a,const Point &b) { return
13
     → Point(a.x-b.x,a.y-b.y); }
        friend inline double operator/(const Point &a,const Point &b) { return a.x*b.y-a.y*b.x; }
14
        inline double angle() { return atan2(y,x); }
15
    }pp[maxn];
16
    struct Segment
17
18
        int from,to,h,id,sur; // from 号点到 to 号点, h 为边权,suf 为这条有向边维出来的平面编号。
19
        inline Segment(int _from = 0,int _to = 0,int _h = 0,int _id = 0,int _sur =
20
     \hookrightarrow 0):from(_from),to(_to),h(_h),id(_id),sur(_sur) {}
        friend inline bool operator<(const Segment &a,const Segment &b) { return
21
    \hookrightarrow (pp[a.to]-pp[a.from]).angle() < (pp[b.to]-pp[b.from]).angle(); }
    }edge[maxm*2];
22
    vector <int> G[maxn];
23
24
    inline void nadd(int u,int v,int h) { ++ncnt; G[u].push_back(ncnt); edge[ncnt] = Segment(u,v,h);
25
       }
    inline void nins(int u,int v,int h) { nadd(u,v,h); nadd(v,u,h); }
26
27
    inline bool cmp(int a,int b) { return edge[a] < edge[b]; }</pre>
```

```
29
    inline void find_surface()
30
31
        for (int i = 1;i <= N;++i) sort(G[i].begin(),G[i].end(),cmp);</pre>
32
        for (int i = 1; i \le N; ++i)
33
34
            int nn = G[i].size();
35
            for (int j = 0; j < nn; ++j)
36
                 edge[G[i][j]].id = j;
37
38
        for (int i = 2;i <= ncnt;++i)</pre>
39
            if (!edge[i].sur)
40
41
                 ++tot; int j = i,p,nn; vector <Point> vec;
42
                 while (!edge[j].sur)
43
                 {
44
                     edge[j].sur = tot; vec.push_back(pp[edge[j].from]);
45
                     p = edge[j].to; nn = G[p].size();
46
                     j ^= 1; j = G[p][(edge[j].id+1)%nn];
47
                 }
48
                 double res = 0; nn = vec.size();
49
                 for (j = 0; j < nn; ++j)
50
                     res += (vec[j]-vec[0])/(vec[(j+1)%nn]-vec[0]);
51
                 res /= 2; space[tot] = res;
52
        // 第 tot 个平面的有向面积, 外面的大平面面积为正, 其余为负, 大平面可能有多个 (平面图不连通)
            }
53
        // 开始建边, 以 mst 为例
54
        // for (int i = 2; i \le cnt; i += 2)
55
        // {
56
        //
                if \ (space[edge[i].sur] < 0 \\ \& \\ \ space[edge[i ^1].sur] < 0)
57
        //
                    arr[++all] = (ARR) { edge[i].sur,edge[i^1].sur,edge[i].h };
58
        //
                else arr[++all] = (ARR) { edge[i].sur,edge[i^1].sur,inf};
59
        // }
60
    }
61
62
    // 点定位
63
    struct Scan
64
65
        double x,y; int bel,sign;
66
        inline Scan(double _x = 0,double _y = 0,int _bel = 0,int _sign =
67
        0):x(_x),y(_y),bel(_bel),sign(_sign) {}
        friend inline bool operator < (const Scan &a,const Scan &b)
68
69
            if (a.x != b.x) return a.x < b.x;</pre>
70
            else return a.sign > b.sign;
71
72
    }bac[maxn*4];
73
74
    struct Splay
75
```

2.11. PLANAR GRAPH

```
{
76
        int num,root,ch[maxn][2],fa[maxn],key[maxn]; queue <int> team;
77
78
        inline int newnode()
79
80
            int ret;
81
            if (team.empty()) ret = ++num;
82
            else ret = team.front(),team.pop();
83
            fa[ret] = ch[ret][0] = ch[ret][1] = 0;
84
            return ret;
85
        }
86
87
        inline void init() { num = 0; root = newnode(); key[root] = cnt; }
88
89
        inline void rotate(int x)
90
91
            int y = fa[x],z = fa[y],l = ch[y][1] == x,r = 1^1;
92
            if (z != 0) ch[z][ch[z][1] == y] = x;
93
            fa[x] = z; fa[y] = x; fa[ch[x][r]] = y;
94
            ch[y][1] = ch[x][r]; ch[x][r] = y;
95
        }
96
97
        inline void splay(int x)
98
99
            while (fa[x] != 0)
100
101
                 int y = fa[x],z = fa[y];
102
                if (fa[y] != 0)
103
104
                     if ((ch[y][0] == x)^(ch[z][0] == y)) rotate(x);
105
                     else rotate(y);
106
                }
107
                 rotate(x);
108
            }
109
            root = x;
110
        }
111
112
        inline int lower_bound(const Point &p)
113
        {
114
            int now = root,ret = 0;
115
            while (now)
116
            {
117
                 int k = key[now];
118
                 119
                     ret = k,now = ch[now][0];
120
                 else now = ch[now][1];
121
122
            return ret;
123
        }
124
```

```
125
          inline int find(int w)
126
127
              int now = root;
128
              double x = pp[edge[w].to].x,y = pp[edge[w].to].y;
129
              double ang = (pp[edge[w].to] - pp[edge[w].from]).angle();
130
              while (now)
131
              {
132
                   int k = key[now];
133
                   if (k == w) return now;
134
                   \label{eq:node_p} \mbox{NODE } p = \mbox{pp[edge[k].to]} - \mbox{pp[edge[k].from],} q = \mbox{pp[edge[k].from];}
135
                   double xx = x - q.x,yy = q.y+xx/p.x*p.y;
136
                   if (equal(yy,y))
137
138
                        double t = p.angle();
139
                       now = ch[now][ang < t];</pre>
140
                   }
141
                   else now = ch[now][y > yy];
142
              }
143
         }
144
145
          inline void erase(int w)
146
          {
147
              int p = find(w);
148
              while (ch[p][0] || ch[p][1])
149
150
                   if (ch[p][0])
151
                   {
152
                       rotate(ch[p][0]);
153
                        if (p == root) root = fa[p];
154
                   }
155
                   else
156
                   {
157
                       rotate(ch[p][1]);
158
                        if (p == root) root = fa[p];
159
                   }
160
              }
161
              team.push(p);
162
              ch[fa[p]][ch[fa[p]][1] == p] = 0;
163
              fa[p] = 0;
164
          }
165
166
          inline void insert(int w)
167
          {
168
              int now = root,pre;
169
              double x = pp[edge[w].from].x,y = pp[edge[w].from].y;
170
              double ang = (pp[edge[w].to] - pp[edge[w].from]).angle();
171
              double xx,yy;
172
              while (true)
173
```

2.11. PLANAR GRAPH

```
{
174
                  int k = key[now];
175
                  NODE p = pp[edge[k].to] - pp[edge[k].from],q = pp[edge[k].from];
176
                  xx = x - q.x,yy = q.y+xx/p.x*p.y;
177
                  if (equal(yy,y))
178
179
                      double t = p.angle();
180
                      pre = now,now = ch[now][ang > t];
181
                      if (!now)
182
                      {
183
                           now = newnode();
184
                           fa[now] = pre; ch[pre][ang > t] = now; key[now] = w;
185
                           break;
186
                      }
187
                  }
188
                  else
189
                  {
190
                      pre = now,now = ch[now][y > yy];
191
                      if (!now)
192
                      {
193
                           now = newnode();
194
                           fa[now] = pre; ch[pre][y>yy] = now; key[now] = w;
195
                           break;
196
                      }
197
                  }
198
199
             splay(now);
200
         }
201
     }S;
202
203
     inline void locate()
204
     {
205
         int nn = 0;
206
         for (int i = 2; i \le cnt; i += 2)
207
208
             if (!dcmp(pp[edge[i].from].x-pp[edge[i].to].x)) continue;
209
             bac[++nn] = Scan(pp[edge[i].from].x,pp[edge[i].from].y,i,2);
210
             bac[++nn] = Scan(pp[edge[i].to].x,pp[edge[i].to].y,i,3);
211
         }
212
         scanf("%d",&T); double x,y;
213
         // 查询 (x,y) 所在平面
214
         for (int i = 1;i <= T;++i)
215
         {
216
             scanf("%lf %lf",&x,&y);
217
             bac[++nn] = Scan(x,y,i,0);
218
             scanf("%lf %lf",&x,&y);
219
             bac[++nn] = Scan(x,y,i,1);
220
         }
221
         sort(bac+1,bac+nn+1);
222
```

```
pp[++n] = Point(-oo,-oo); pp[++n] = (oo,-oo);
223
         edge[++cnt] = Edge(n-1,n);
224
         S.init(); int p;
225
         for (int i = 1;i <= nn;++i)</pre>
226
227
              if (bac[i].sign == 2||bac[i].sign == 3)
228
              {
229
                  if (bac[i].sign == 2) S.insert(bac[i].bel);
230
                  else S.erase(bac[i].bel);
231
              }
232
              else
233
              {
234
                  p = S.lower_bound(Point(bac[i].x,bac[i].y));
235
                  query[bac[i].bel][bac[i].sign] = edge[p].sur;
236
237
         }
238
     }
239
```

2.12 Polygon Class

```
inline bool PointOnSegment(const Point &t,const Point &a,const Point &b)
   {
        if (dcmp((t-a)/(b-a))) return false;
        if (dcmp((t-a)*(t-b)) > 0) return false;
        return true;
   }
    inline bool in(const Point &a,const Point &b,const Point &c)
        double alpha = a.angle(),beta = b.angle(),gamma = c.angle(); // angle 返回 [0,2pi]
10
        if (alpha <= beta) return dcmp(gamma-alpha) > 0&&dcmp(beta-gamma) > 0;
11
        else return dcmp(gamma-alpha) > 0||dcmp(beta-gamma) > 0;
12
   }
13
14
   struct Polygon
15
16
        int n; Point a[maxn];
17
        inline Polygon() {}
18
        inline void read()
19
20
            n = gi();
21
            for (int i = 0;i < n;++i) a[i].read();</pre>
22
            a[n] = a[0];
23
        }
24
        // 点是否在多边形内部,内部为 1,外部为 0,边界为 2,不管顺逆时针
25
        inline int Point_In(const Point &t) const
26
        {
27
            int num = 0;
28
            for (int i = 0; i < n; ++i)
29
```

```
{
30
                 if (PointOnSegment(t,a[i],a[i+1])) return 2;
31
                int k = dcmp((a[i+1]-a[i])/(t-a[i]));
32
                 int d1 = dcmp(a[i].y-t.y),d2 = dcmp(a[i+1].y-t.y);
33
                 if (k > 0 \& \& d1 \le 0 \& \& d2 > 0) ++num;
34
                 if (k < 0 \&\&d2 <= 0 \&\&d1 > 0) --num;
35
36
            return num != 0;
37
        }
38
        // 判断多边形的方向, true 为逆时针, false 为顺时针, 用叉积判断哪个多
39
        inline bool CalculateClockDirection()
40
        {
41
            int res = 0;
42
            for (int i = 0; i < n; ++i)
43
            {
44
                int p = i-1,s = i+1,sgn;
45
                if (p < 0) p += n; if (s >= n) s -= n;
46
                sgn = dcmp((a[i]-a[p])/(a[s]-a[i]));
47
                 if (sgn) { if (sgn > 0) ++res; else --res; }
48
49
            return res > 0;
50
51
        // 判断多边形方向, true 为逆时针, false 为顺时针, 用 Green 公式
52
        inline bool CalculateClockDirection()
53
54
            double res = 0;
55
            for (int i = 0; i < n; ++i)
56
                res -= 0.5*(a[i+1].y+a[i].y)*(a[i+1].x-a[i].x);
57
            return res > 0;
58
        }
59
60
        // 线段 ab 是否有点严格在多边形内部,先判断线段是否与多边形边界有交,再判断 ab 是否与多边形有交,内部 false, 外
61
        inline bool can(int ia,int ib)
62
        {
63
            Point a = P[ia],b = P[ib],v = b-a;
64
             \  \  \text{if } (in(P[ia+1]-a,P[ia-1]-a,b-a) \mid | in(P[ib+1]-b,P[ib-1]-b,a-b)) \  \, \text{return false}; \\
65
            for (register int i = 0;i < N;++i)</pre>
66
67
                 if (dcmp(v/(P[i]-a))*dcmp(v/(P[i+1]-a)) <
68
         0\&\&dcmp(vec[i]/(a-P[i]))*dcmp(vec[i]/(b-P[i])) < 0)
                     return false;
69
                 if (PointOnSegment(a,P[i],P[i+1])||PointOnSegment(b,P[i],P[i+1])) return false;
70
                 if (PointOnSegment(P[i],a,b)||PointOnSegment(P[i+1],a,b)) return false;
71
            }
72
            return true;
73
74
    }poly;
75
```

2.13 Union Area of Circles

```
//N 为开始圆的个数, M 为离散化后圆的个数, cnt 为去包含后圆的个数
    int N,M,cnt;
   struct Node
    {
        double x,y;
6
        inline Node(double _x = 0, double _y = 0):x(_x),y(_y) {}
        inline void read() { x = gi(),y = gi(); }
        inline double norm() const { return sqrt(x*x+y*y); }
        inline double angle() const { return atan2(y,x); }
10
        inline Node unit() const { double len = norm(); return Node(x/len,y/len); }
11
        friend inline Node operator-(const Node &a,const Node &b) { return Node(a.x-b.x,a.y-b.y); }
12
        friend inline Node operator+(const Node &a,const Node &b) { return Node(a.x+b.x,a.y+b.y); }
13
        friend inline Node operator*(const Node &a,double b) { return Node(a.x*b,a.y*b); }
14
        friend inline Node operator*(double b,const Node &a) { return Node(a.x*b,a.y*b); }
15
        friend inline double operator/(const Node &a,const Node &b) { return a.x*b.y-a.y*b.x; }
16
   };
17
    struct Circle
18
19
        Node C; double r;
20
        inline Circle(const Node &_C = Node(),double _r = 0):C(_C),r(_r) {}
21
        friend inline bool operator<(const Circle &a,const Circle &b)
22
23
            if (dcmp(a.r-b.r)) return dcmp(a.r-b.r) < 0;</pre>
24
            else if (dcmp(a.C.x-b.C.x)) return dcmp(a.C.x-b.C.x) < 0;</pre>
25
            else return dcmp(a.C.y-b.C.y) < 0;</pre>
26
27
        friend inline bool operator == (const Circle &a, const Circle &b)
28
        ł
29
            if (dcmp(a.r-b.r)) return false;
30
            if (dcmp(a.C.x-b.C.x)) return false;
31
            if (dcmp(a.C.y-b.C.y)) return false;
32
            return true;
33
        }
34
    }tc[maxn],cir[maxn];
35
36
    inline Node rotate(const Node &p,double cost,double sint)
37
38
        double x = p.x, y = p.y;
39
        return Node(x*cost-y*sint,x*sint+y*cost);
40
   }
41
    inline pair <Node, Node> crosspoint(const Node &ap,double ar,const Node &bp,double br)
42
43
        double d = (ap-bp).norm(),cost = (ar*ar+d*d-br*br)/(2*ar*d),sint = sqrt(1-cost*cost);
44
        Node v = ((bp-ap).unit())*ar;
45
        return make_pair(ap+rotate(v,cost,-sint),ap+rotate(v,cost,sint));
46
   }
47
```

```
inline pair <Node, Node> crosspoint(const Circle &a,const Circle &b) { return
48
        crosspoint(a.C,a.r,b.C,b.r); }
49
    struct Event
50
51
        Node p; double a; int d;
52
        inline Event(const Node &_p = Node(),double _a = 0,double _d = 0):p(_p),a(_a),d(_d) {}
53
        friend inline bool operator <(const Event &a,const Event &b) { return a.a < b.a; }
54
    };
55
    inline double work()
57
58
        sort(tc+1,tc+M+1); M = unique(tc+1,tc+M+1)-tc-1;
59
        for (int i = M; i; --i)
60
        {
61
            bool ok = true;
62
            for (int j = i+1; j \le M; ++j)
63
            {
64
                 double d = (tc[i].C-tc[j].C).norm();
65
                 if (dcmp(d-fabs(tc[i].r-tc[j].r)) \le 0) \{ ok = false; break; \}
66
            }
67
            if (ok) cir[++cnt] = tc[i];
68
69
        // for (int i = M; i; --i) cir[++cnt] = tc[i];
70
        double ret = 0;
71
        for (int i = 1;i <= cnt;++i)
72
        {
73
            vector <Event> event;
74
            Node boundary = cir[i].C+Node(cir[i].r,0);
75
            event.push_back(Event(boundary,-pi,0));
76
            event.push_back(Event(boundary,pi,0));
77
            for (int j = 1; j <= cnt; ++ j)</pre>
79
                 if (i == j) continue;
80
                 double d = (cir[i].C-cir[j].C).norm();
81
                 if (dcmp(d-(cir[i].r+cir[j].r)) < 0)</pre>
82
                 {
83
                     pair <Node, Node> res = crosspoint(cir[i],cir[j]);
84
                     double x = (res.first-cir[i].C).angle(),y = (res.second-cir[i].C).angle();
85
                     if (dcmp(x-y) > 0)
86
                     {
87
                          event.push_back(Event(res.first,x,1));
                         event.push_back(Event(boundary,pi,-1));
89
                         event.push_back(Event(boundary,-pi,1));
90
                         event.push_back(Event(res.second,y,-1));
91
                     }
92
                     else
93
                     {
94
                         event.push_back(Event(res.first,x,1));
95
```

```
event.push_back(Event(res.second,y,-1));
96
                      }
97
                 }
98
             }
99
             sort(event.begin(),event.end());
100
             int sum = event[0].d;
101
             for (int j = 1; j < (int)event.size(); ++j)
102
             {
103
                 if (!sum)
104
                 {
105
                      ret += (event[j-1].p/event[j].p)/2;
106
                      double x = event[j-1].a,y = event[j].a;
107
                      double area = cir[i].r*cir[i].r*(y-x)/2;
108
                      Node v1 = event[j-1].p-cir[i].C,v2 = event[j].p-cir[i].C;
109
                      area -= (v1/v2)/2; ret += area;
110
                 }
111
                 sum += event[j].d;
112
             }
113
         }
114
         return ret;
115
    }
116
```

Chapter 3

Data Structure

3.1 Divide and Conquer on Tree

```
#include<cstring>
    #include<iostream>
    #include<cstdio>
    #include<cstdlib>
    using namespace std;
    #define maxn (100010)
    int best,cnt = 1,side[maxn],toit[maxn],next[maxn],large[maxn];
    int sd[maxn],d[maxn],ns,nd,ans,N,K,size[maxn]; bool vis[maxn];
10
    inline void add(int a,int b)
11
    { next[++cnt] = side[a]; side[a] = cnt; toit[cnt] = b; }
12
    inline void ins(int a,int b)
13
    { add(a,b); add(b,a); }
14
15
    inline void getroot(int now,int fa,int rest)
16
17
        size[now] = 1; large[now] = 0;
18
        for (int i = side[now];i;i = next[i])
19
20
            if (toit[i] == fa||vis[toit[i]]) continue;
21
            getroot(toit[i],now,rest);
22
            size[now] += size[toit[i]];
23
            large[now] = max(large[now], size[toit[i]]);
24
25
        large[now] = max(large[now],rest-size[now]);
26
        if (large[now] < large[best]) best = now;</pre>
27
28
    inline int find_root(int now,int rest)
29
    { best = 0; getroot(now,0,rest); return best; }
30
31
    inline void dfs(int now,int fa,int dep)
32
    {
33
```

```
size[now] = 1; nd = max(dep,nd); ++d[dep];
34
        for (int i = side[now];i;i = next[i])
35
             if (toit[i] != fa&&!vis[toit[i]])
36
                 dfs(toit[i],now,dep+1),size[now] += size[toit[i]];
37
38
39
    inline void subdivide(int now)
40
41
        vis[now] = true;
42
        for (int i = side[now];i;i = next[i])
43
44
             if (vis[toit[i]]) continue;
45
             dfs(toit[i],now,1); ans += d[K];
46
             for (int j = 1; j < K; ++ j) ans += d[j] *sd[K-j];</pre>
             for (int j = 1; j \le nd; ++j) sd[j] += d[j], d[j] = 0;
48
             ns = max(nd,ns); nd = 0;
49
        }
50
        memset(sd,0,4*(ns+1)); ns = 0;
51
        for (int i = side[now];i;i = next[i])
52
             if (!vis[toit[i]])
53
                 subdivide(find_root(toit[i],size[toit[i]]));
54
    }
55
56
    int main()
57
58
        freopen("D.in", "r", stdin);
59
        freopen("D.out", "w", stdout);
60
         scanf("%d %d",&N,&K);
61
        for (int i = 1,a,b;i < N;++i) scanf("%d %d",&a,&b),ins(a,b);
62
        large[0] = 1<<30; subdivide(find_root(1,N));</pre>
63
        printf("%d",ans);
64
        fclose(stdin); fclose(stdout);
65
        return 0;
66
    }
67
```

3.2 Dynamicly Divide and Conquer on Tree

```
1 // N 个点的树,每个点点权 O/1, 询问两个 O 点之间最远距离,每次可以 flip 一个点的点权
2 #include<set>
3 #include<vector>
4 #include<algorithm>
5 #include<cstring>
6 #include<cstring>
7 #include<cstdio>
8 #include<cstdlib>
9 using namespace std;

10 const int maxn = 200010, inf = 1<<29, lhh = 4000037;
```

```
int
12
    \hspace*{0.5cm} \hookrightarrow \hspace*{0.5cm} \texttt{N,cnt,nlight,tot,best,Root,side[maxn],toit[maxn],nxt[maxn],size[maxn],large[maxn],optimal[maxn];} \\
    int father[maxn],L[maxn],R[maxn],leaf[maxn],rechain[lhh],depth[lhh]; bool off[maxn],vis[maxn];
13
    vector <int> son[maxn]; pair <int,int> Hash[lhh]; multiset <int> mx[maxn],S[maxn];
14
15
    struct Value
16
    {
17
        int a,b;
18
        inline Value() {}
19
        inline Value(int _a,int _b):a(_a),b(_b) {}
20
        friend inline Value operator +(const Value &x,const Value &y)
21
22
             Value ret;
23
             if (x.a > y.a)
24
             {
25
                 ret.a = x.a;
26
                 if (x.b > y.a) ret.b = x.b;
27
                 else ret.b = y.a;
28
             }
29
             else
30
             {
31
                 ret.a = y.a;
32
                 if (y.b > x.a) ret.b = y.b;
33
                 else ret.b = x.a;
34
             }
35
             return ret;
36
37
    }tree[maxn*2];
38
39
    inline void add(int a,int b) { nxt[++cnt] = side[a]; side[a] = cnt; toit[cnt] = b; }
40
    inline void ins(int a,int b) { add(a,b); add(b,a); }
41
42
    inline int gi()
43
44
         char ch; int ret = 0,f = 1;
45
        do ch = getchar(); while (!(ch >= '0'&&ch <= '9')&&ch != '-');
46
        if (ch == '-') f = -1, ch = getchar();
47
        do ret = ret*10+ch-'0',ch = getchar(); while (ch >= '0'&&ch <= '9');
48
        return ret*f;
49
    }
50
51
    inline int find(const pair <int,int> &key)
52
53
    {
        int now = (2333*key.first+5003*key.second)%lhh;
54
        while (true)
55
56
             if (Hash[now].first == 0||Hash[now] == key) return now;
57
             else ++now;
             if (now >= lhh) now -= lhh;
59
```

```
}
60
    }
61
62
    inline void getroot(int now,int rest,int fa)
63
64
         size[now] = 1; large[now] = 0;
65
         for (int i = side[now];i;i = nxt[i])
66
67
             if (vis[toit[i]]||toit[i] == fa) continue;
68
             getroot(toit[i],rest,now);
69
             size[now] += size[toit[i]];
70
             large[now] = max(large[now], size[toit[i]]);
72
         large[now] = max(large[now],rest-size[now]);
73
         if (large[now] < large[best]) best = now;</pre>
74
    }
75
    inline int find_root(int rest,int now) { best = 0; getroot(now,rest,0); return best; }
76
    inline void dfs(int id,int root,int now,int fa,int dep)
78
    {
79
         S[id].insert(dep);
80
         pair <int,int> key = make_pair(root,now); int pos = find(key);
81
         rechain[pos] = id; depth[pos] = dep; Hash[pos] = key;
82
         size[now] = 1;
83
         for (int i = side[now];i;i = nxt[i])
84
85
             if (vis[toit[i]] | | toit[i] == fa) continue;
86
             dfs(id,root,toit[i],now,dep+1);
                                                   size[now] += size[toit[i]];
87
         }
88
    }
89
90
    inline void subdivide(int root)
91
92
         optimal[root] = -inf; mx[root].insert(-inf);
93
         L[root] = tot+1;
94
         for (int i = side[root];i;i = nxt[i])
95
96
             if (vis[toit[i]]) continue;
97
             ++tot; dfs(tot,root,toit[i],root,1);
98
             S[tot].insert(-inf);
99
100
         R[root] = tot; vis[root] = true;
101
         for (int i = side[root];i;i = nxt[i])
102
         {
103
             if (vis[toit[i]]) continue;
104
             int tmp = find_root(size[toit[i]],toit[i]);
105
             father[tmp] = root; son[root].push_back(tmp);
106
             subdivide(tmp);
107
         }
108
```

```
}
109
110
     inline void build(int now,int 1,int r)
111
112
         if (1 == r)
113
114
             tree[now] = Value(*S[1].rbegin(),-inf);
115
             leaf[1] = now; return;
116
         }
117
         int mid = (1+r)>>1;
118
         build(now<<1,1,mid); build(now<<1|1,mid+1,r);
119
         tree[now] = tree[now<<1]+tree[now<<1|1];</pre>
120
    }
121
122
     inline Value query(int now,int 1,int r,int ql,int qr)
123
124
         if (1 == ql&&r == qr) return tree[now];
125
         int mid = (1+r)>>1;
126
         if (qr <= mid) return query(now<<1,1,mid,q1,qr);</pre>
127
         else if (ql > mid) return query(now<<1|1,mid+1,r,ql,qr);</pre>
128
         else return query(now<<1,1,mid,q1,mid)+query(now<<1|1,mid+1,r,mid+1,qr);</pre>
129
    }
130
131
     inline void upd(int &a,int b) { if (a < b) a = b; }</pre>
132
133
     inline void modify(int pos,int dep,bool sign)
134
     {
135
         if (sign) S[pos].insert(dep); else S[pos].erase(S[pos].find(dep));
136
         tree[leaf[pos]] = Value(*S[pos].rbegin(),-inf);
137
         for (int now = leaf[pos]>>1;now;now >>= 1)
138
             tree[now] = tree[now<<1]+tree[now<<1|1];</pre>
139
    }
140
     inline void modify(int pos)
141
142
         int c = 0;
143
         if (father[pos]) mx[father[pos]].erase(mx[father[pos]].find(optimal[pos]));
144
         off[pos] ^= 1; if (off[pos]) nlight++; else nlight--;
145
         if (L[pos] <= R[pos])</pre>
146
         {
147
             Value res = query(1,1,tot,L[pos],R[pos]);
148
             optimal[pos] = max(res.a+res.b,*mx[pos].rbegin());
149
             if (off[pos]) upd(optimal[pos],res.a);
150
151
         if (father[pos]) mx[father[pos]].insert(optimal[pos]);
152
         for (int now = father[pos];now;now = father[now])
153
154
             int t = find(make_pair(now,pos));
155
             int id = rechain[t],dep = depth[t];
156
             modify(id,dep,off[pos]);
157
```

```
if (father[now]) mx[father[now]].erase(mx[father[now]].find(optimal[now]));
158
             Value res = query(1,1,tot,L[now],R[now]);
159
             optimal[now] = max(res.a+res.b,*mx[now].rbegin());
160
             if (off[now]) upd(optimal[now],res.a);
161
             if (father[now]) mx[father[now]].insert(optimal[now]);
162
             ++c;
163
         }
164
    }
165
166
     inline void redfs(int now)
167
168
         for (int i = 0;i < (int)son[now].size();++i)</pre>
169
             redfs(son[now][i]),mx[now].insert(optimal[son[now][i]]);
170
         if (L[now] <= R[now])</pre>
171
         {
172
             Value res = query(1,1,tot,L[now],R[now]);
173
             optimal[now] = max(res.a+res.b,*mx[now].rbegin());
174
             if (off[now]) upd(optimal[now],res.a);
175
         }
176
    }
177
178
     int main()
179
     {
180
         // freopen("A.in", "r", stdin);
181
         memset(off,true,sizeof off);
182
         nlight = N = gi();
183
         for (int i = 1;i < N;++i) ins(gi(),gi());</pre>
184
         large[0] = inf;
185
         subdivide(Root = find_root(N,1));
186
         build(1,1,tot); redfs(Root);
187
         for (int Q = gi();Q--;)
188
189
             char opt; do opt = getchar(); while (opt != 'G'&&opt != 'C');
190
             if (opt == 'G')
191
             {
192
                  if (!nlight) puts("-1");
193
                  else if (nlight == 1) puts("0");
194
                  else printf("%d\n",optimal[Root]);
195
196
             else modify(gi());
197
         }
198
         return 0;
199
    }
200
```

3.3 Heavy Path Decomposition

```
int side[maxn],toit[maxn<<1],nxt[maxn<<1];
int timestamp,father[maxn],dfn[maxn],redfn[maxn],top[maxn],size[maxn];</pre>
```

```
void decompose(int now,int tp)
    {
5
        redfn[dfn[now] = ++timestamp] = now;
        top[now] = tp; int heavy = 0;
        for (int i = side[now];i;i = nxt[i])
            if (toit[i] != father[now]&&size[toit[i]] > size[heavy]) heavy = toit[i];
        if (!heavy) return; decompose(heavy,tp);
10
        for (int i = side[now];i;i = nxt[i])
11
            if (toit[i] != father[now]&&toit[i] != heavy) decompose(toit[i],toit[i]);
12
    }
13
14
    void dfs(int now)
15
16
        size[now] = 1;
17
        for (int i = side[now];i;i = nxt[i])
18
            if (toit[i] != father[now])
19
20
                 father[toit[i]] = now,con[toit[i]] = i;
21
                 dep[toit[i]] = dep[now]+1,dfs(toit[i]);
22
                 size[now] += size[toit[i]] ;
23
            }
24
    }
25
26
    // 对点操作
27
    inline int query(int a,int b)
28
29
        int ret = -inf;
30
        while (top[a] != top[b])
31
32
            if (dep[top[a]] < dep[top[b]]) swap(a,b);</pre>
33
            ret = max(ret,ask(1,1,N,dfn[top[a]],dfn[a]));
34
            a = father[top[a]];
35
        }
36
        if (dep[a] < dep[b]) swap(a,b);</pre>
37
        ret = max(ret,query(1,1,N,dfn[b],dfn[a]));
38
        return ret;
39
    }
40
    // 对边操作
42
    inline int query(int a,int b)
43
44
        int ret = -inf;
45
        while (top[a] != top[b])
46
47
            if (dep[top[a]] < dep[top[b]]) swap(a,b);</pre>
48
            ret = max(ret,ask(1,1,N,dfn[top[a]],dfn[a]));
49
            a = father[top[a]];
50
        }
51
        if (a == b) return ret;
52
```

```
if (dep[a] < dep[b]) swap(a,b);
ret = max(ret,ask(1,1,N,dfn[b]+1,dfn[a]));
return ret;
}</pre>
```

3.4 K-Dimension Tree

```
struct Point
    {
2
        double x,y; int id;
        inline Point() = default;
        inline Point(double _x,double _y,int _id):x(_x),y(_y),id(_id) {}
5
        inline void read(int i = 0) { scanf("%lf %lf",&x,&y); id = i; }
        inline double norm() { return sqrt(x*x+y*y); }
        friend inline Point operator+(const Point &a,const Point &b) { return
    → Point(a.x+b.x,a.y+b.y); }
        friend inline Point operator-(const Point &a,const Point &b) { return
    → Point(a.x-b.x,a.y-b.y); }
        friend inline double operator*(const Point &a,const Point &b) { return a.x*b.x+a.y*b.y; }
10
        friend inline double operator/(const Point &a,const Point &b) { return a.x*b.y-a.y*b.x; }
11
    }P[maxn];
12
13
    struct Rectangle
14
15
        double lx,rx,ly,ry;
16
        inline Rectangle() = default;
17
        inline Rectangle(double _lx,double _rx,double _ly,double
18
        _ry):lx(_lx),rx(_rx),ly(_ly),ry(_ry) {}
        inline void set(const Point &p) { lx = rx = p.x; ly = ry = p.y; }
19
        inline void merge(const Point &p)
20
21
            lx = min(lx,p.x); rx = max(rx,p.x);
22
            ly = min(ly,p.y); ry = max(ry,p.y);
23
24
        inline void merge(const Rectangle &r)
25
26
            lx = min(lx,r.lx); rx = max(rx,r.rx);
27
            ly = min(ly,r.ly); ry = max(ry,r.ry);
28
29
        // 最小距离, 到 4 个角和 4 条边距离
30
        inline double dist(const Point &p)
31
32
            if (p.x \le lx \& p.y \le ly) return (p-Point(lx,ly)).norm();
33
            else if (p.x <= rx&&p.y <= ly) return p.y-ly;
34
            else if (p.x >= rx&&p.y <= ly) return (p-Point(rx,ly)).norm();
35
            else if (p.x >= rx&&p.y <= ry) return p.x-rx;
36
            else if (p.x \ge rx \& p.y \ge ry) return (p-Point(rx,ry)).norm();
37
            else if (p.x \ge lx\&\&p.y \ge ry) return p.y-ry;
38
            else if (p.x \le lx \& p.y \ge ry) return (p-Point(lx,ry)).norm();
39
```

```
else if (p.x \le lx \& p.y \ge ly) return p.x-lx;
40
            return 0;
41
        }
42
        // 最大距离, 到 4 个角的距离
43
        inline double dist(const Point &p)
44
45
            double ret = 0;
46
            ret += max((rx-p.x)*(rx-p.x),(lx-p.x)*(lx-p.x));
47
            ret += max((ry-p.y)*(ry-p.y),(ly-p.y)*(ly-p.y));
48
            return ret;
49
        }
50
    };
51
52
    struct Node
53
54
    {
        int child[2]; Point p; Rectangle r;
55
        inline Node() = default;
56
        inline Node(const Point &_p,const Rectangle &_r):p(_p),r(_r) { r.set(p); memset(child,0,8);
57
        inline void set(const Point &_p) { p = _p; r.set(p); memset(child,0,8); }
58
    }tree[maxn];
59
    inline bool cmpx(const Point &a,const Point &b)
61
    {
62
        if (a.x != b.x) return a.x < b.x;</pre>
63
        else return a.y < b.y;</pre>
64
    }
65
    inline bool cmpy(const Point &a,const Point &b)
66
67
        if (a.y != b.y) return a.y < b.y;</pre>
68
        else return a.x < b.x;</pre>
69
    }
70
71
    inline bool cmp(pair <double,int> a,pair <double,int> b)
72
    {
73
        int sgn = dcmp(a.first-b.first);
74
        if (sgn) return sgn < 0;
75
        else return a.second < b.second;</pre>
76
    }
77
78
    // 查询 k 大/小
79
    inline void query(int now, const Point &p,int k,pair <double,int> ret[],bool dim = false)
80
81
        if (dcmp(tree[now].r.dist(p)-ret[k].first) > 0) return;
82
        pair <double,int> val = make_pair((p-tree[now].p).norm(),tree[now].p.id);
83
        for (int i = 1;i <= k;++i)
84
            if (cmp(val,ret[i]))
85
            {
86
                 for (int j = k+1; j > i; --j) ret[j] = ret[j-1];
87
```

```
ret[i] = val; break;
88
89
         if ((dim&&cmpx(p,tree[now].p))||(!dim&&cmpy(p,tree[now].p)))
90
         {
91
             if (tree[now].child[0]) query(tree[now].child[0],p,k,ret,dim^1);
92
             if (tree[now].child[1]) query(tree[now].child[1],p,k,ret,dim^1);
93
         }
94
         else
95
         {
96
             if (tree[now].child[1]) query(tree[now].child[1],p,k,ret,dim^1);
97
             if (tree[now].child[0]) query(tree[now].child[0],p,k,ret,dim^1);
98
         }
99
    }
100
101
    // 查询最小/大
102
    inline void query(int x,const Point &p,pair <double,int> ret,bool dim = false)
103
104
         if (dcmp(tree[now].r.disp(p)-ret.first) > 0) return;
105
         pair <double,int> val = make_pair((p-tree[now].p).norm(),tree[now].p.id);
106
         if (cmp(val,ret)) ret = val;
107
         if ((dim&&cmpx(p,tree[now].p))||(!dim&&cmpy(p,tree[now].p)))
108
109
             if (tree[now].child[0]) query(tree[now].child[0],p,ret,dim^1);
110
             if (tree[now].child[1]) query(tree[now].child[1],p,ret,dim^1);
111
         }
112
         else
113
         {
114
             if (tree[now].child[1]) query(tree[now].child[1],p,ret,dim^1);
115
             if (tree[now].child[0]) query(tree[now].child[0],p,ret,dim^1);
116
         }
117
    }
118
119
    inline int build(int l,int r,bool dim)
120
    {
121
         int now = ++size,mid = (1+r)>>1;
122
         nth_element(vec.begin()+l-1,vec.begin()+mid-1,vec.begin()+r,dim?cmpx:cmpy);
123
         tree[now].set(vec[mid-1]);
124
         if (1 < mid)
125
         {
126
             tree[now].child[0] = build(1,mid-1,dim^1);
127
             tree[now].r.merge(tree[tree[now].child[0]].r);
128
         }
129
         if (r > mid)
130
         {
131
             tree[now].child[1] = build(mid+1,r,dim^1);
132
             tree[now].r.merge(tree[tree[now].child[1]].r);
133
134
         return now;
135
    }
136
```

3.5. LEFTLIST TREE 53

3.5 Leftlist Tree

```
// It's correct, but it needs be rewritten.
    #include<iostream>
    #include<cstdio>
    #include<cstdlib>
    using namespace std;
    #define maxn (600010)
    int N,M,root[maxn],size[maxn],v[maxn],dep[maxn],l[maxn],r[maxn],tot;
    inline int Merge(int x,int y)
10
11
        if (!x||!y) return x+y;
12
        if (v[x]>v[y]) swap(x,y);
13
        r[x] = Merge(r[x],y);
14
        if (dep[l[x]] < dep[r[x]]) swap(l[x],r[x]);</pre>
15
        dep[x] = dep[r[x]]+1;
16
        return x;
17
    }
18
    inline int Init(int x) { v[++tot] = x; 1[tot] = r[tot] = dep[tot] = 0; return tot;}
19
    inline int Insert(int x,int y) { return Merge(x,Init(y)); }
20
    inline int pop(int x) { return Merge(l[x],r[x]); }
21
22
    inline int read()
23
24
        char ch; int f = 1, ret = 0;
25
        do ch = getchar(); while (!(ch >= '0'&&ch <= '9')&&ch != '-');
26
        if (ch == '-') f = -1, ch = getchar();
27
        do ret = ret*10+ch-^{'}0',ch = getchar(); while (ch >= ^{'}0'&&ch <= ^{'}9');
28
        return ret*f;
29
    }
30
31
    int main()
32
    {
33
        freopen("1050.in","r",stdin);
34
        freopen("1050.out","w",stdout);
35
        scanf("%d %d",&N,&M);
36
        for (int i = 1;i <= N;++i) root[i] = Init(read()),size[i] = 1;</pre>
37
        while (M--)
38
39
            int opt = read();
40
            if (!opt)
41
            {
42
                 int a = read()+1,b = read()+1;
43
                 if (size[b]) root[a] = Merge(root[a],root[b]);
44
                 size[a] += size[b]; size[b] = 0;
45
            }
46
            else if (opt == 1)
47
            {
48
```

```
int a = read()+1;
49
                 if (!size[a]) puts("-1");
50
                 else printf("%d\n",v[root[a]]),root[a] = pop(root[a]),--size[a];
51
             }
52
             else
53
             {
54
                 int a = read()+1; ++size[a];
55
                 root[a] = Insert(root[a],read());
57
58
        fclose(stdin); fclose(stdout);
59
        return 0;
60
    }
61
```

3.6 Link Cut Tree

```
inline bool isroot(int a) { return ch[fa[a]][0] != a&&ch[fa[a]][1] != a; }
    inline void update(int x) { val[x] = (val[ch[x][0]]+val[ch[x][1]]).merge(x); }
    inline void pushdown(int x)
        if (rev[x])
        {
            int &lc = ch[x][0],&rc = ch[x][1];
            swap(lc,rc);
            if (lc) rev[lc] ^= 1;
10
            if (rc) rev[rc] ^= 1;
11
            rev[x] = false;
12
        }
13
    }
14
15
    inline void rotate(int x)
16
17
        int y = fa[x],z = fa[y],l = ch[y][1] == x,r = l^1;
18
        if (!isroot(y)) ch[z][ch[z][1] == y] = x; fa[x] = z;
19
        if (ch[x][r]) fa[ch[x][r]] = y; ch[y][1] = ch[x][r];
20
        fa[y] = x; ch[x][r] = y; update(y); update(x);
21
    }
22
    inline void splay(int x)
23
24
        int top = 0,i;
25
        for (i = x;!isroot(i);i = fa[i]) stk[++top] = i; stk[++top] = i;
26
        while (top) pushdown(stk[top--]);
27
        while (!isroot(x))
28
29
            int y = fa[x], z = fa[y];
30
            if (!isroot(y))
31
32
                 if ((ch[y][0] == x)^(ch[z][0] == y)) rotate(x);
33
```

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```
else rotate(y);
34
             }
35
             rotate(x);
36
        }
37
    }
38
39
    inline int access(int x)
40
41
        int t = 0;
42
        for (t = 0;x;t = x,x = fa[x])
43
             splay(x),ch[x][1] = t,update(x);
44
        return t;
45
    }
46
    inline int evert(int x) { int t; rev[t = access(x)] ^= 1; return t; }
47
    inline int find(int x)
48
49
        x = access(x);
50
        while (pushdown(x),ch[x][0]) x = ch[x][0];
51
        return x;
52
    }
53
    inline void cut(int x,int y)
54
55
         evert(x); access(y); splay(y);
56
        if (ch[y][0] != x||ch[x][1] != 0) return;
57
         ch[y][0] = fa[x] = 0; update(x); update(y);
58
    }
59
    inline void link(int x,int y) { fa[evert(x)] = y; }
60
61
62
    // Magic Forest
63
    #include<algorithm>
64
    #include<cstring>
65
    #include<iostream>
66
    #include<cstdio>
67
    #include<cstdlib>
68
    using namespace std;
69
70
    const int maxn = 200010,inf = 1<<29;</pre>
71
    int N,M,A[maxn],B[maxn],fa[maxn],ch[maxn][2];
72
    int stk[maxn],ans = inf; bool rev[maxn];
73
74
    struct Value
75
76
    {
        int ma,mb,id;
77
        inline Value(int _ma = 0,int _mb = 0,int _id = 0):ma(_ma),mb(_mb),id(_id) {}
78
        friend inline Value operator +(const Value &a,const Value &b)
79
        {
80
             Value ret = Value(max(a.ma,b.ma),max(a.mb,b.mb),a.id);
81
             if (B[a.id] < B[b.id]) ret.id = b.id;</pre>
82
```

```
return ret;
83
         }
84
         inline Value merge(int i)
85
         {
86
             Value ret = Value(max(ma,A[i]),max(mb,B[i]),id);
87
             if (B[i] > B[id]) ret.id = i;
88
             return ret;
89
         }
90
    }val[maxn];
91
92
    inline int gi()
93
    {
94
         char ch; int ret = 0,f = 1;
95
         do ch = getchar(); while (!(ch >= '0'&&ch <= '9')&&ch != '-');
96
         if (ch == '-') f = -1, ch = getchar();
97
         do ret = ret*10+ch-'0',ch = getchar(); while (ch >= '0'&&ch <= '9');
98
         return ret*f;
99
    }
100
101
    struct Edge
102
103
         int x,y,a,b;
104
         inline Edge(int x = 0,int y = 0,int a = 0,int b = 0):x(x),y(y),a(a),b(b) {}
105
         inline void read() { x = gi(), y = gi(), a = gi(), b = gi(); }
106
         friend inline bool operator <(const Edge &s,const Edge &t) { return s.a < t.a; }
107
    }edge[maxn];
108
109
    inline bool isroot(int a) { return ch[fa[a]][0] != a&&ch[fa[a]][1] != a; }
110
111
    inline void update(int x) { val[x] = (val[ch[x][0]]+val[ch[x][1]]).merge(x); }
112
    inline void pushdown(int x)
113
    {
114
         if (rev[x])
115
         {
116
             int &lc = ch[x][0],&rc = ch[x][1];
117
             swap(lc,rc);
118
             if (lc) rev[lc] ^= 1;
119
             if (rc) rev[rc] ^= 1;
120
             rev[x] = false;
121
         }
122
    }
123
124
    inline void rotate(int x)
125
126
         int y = fa[x],z = fa[y],1 = ch[y][1] == x,r = 1^1;
127
         if (!isroot(y)) ch[z][ch[z][1] == y] = x; fa[x] = z;
128
         if (ch[x][r]) fa[ch[x][r]] = y; ch[y][1] = ch[x][r];
129
         fa[y] = x; ch[x][r] = y; update(y); update(x);
130
    }
131
```

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```
inline void splay(int x)
132
133
         int top = 0,i;
134
         for (i = x;!isroot(i);i = fa[i]) stk[++top] = i; stk[++top] = i;
135
         while (top) pushdown(stk[top--]);
136
         while (!isroot(x))
137
         {
138
              int y = fa[x],z = fa[y];
139
              if (!isroot(y))
140
              {
141
                  if ((ch[y][0] == x)^(ch[z][0] == y)) rotate(x);
142
                  else rotate(y);
143
              }
144
              rotate(x);
145
         }
146
     }
147
148
     inline int access(int x)
149
150
         int t = 0;
151
         for (t = 0;x;t = x,x = fa[x])
152
              splay(x),ch[x][1] = t,update(x);
153
         return t;
154
     }
155
     inline int evert(int x) { int t; rev[t = access(x)] ^= 1; return t; }
156
     inline int find(int x)
157
158
         x = access(x);
159
         while (pushdown(x), ch[x][0]) x = ch[x][0];
160
         return x;
161
     }
162
     inline void cut(int x,int y)
163
164
         evert(x); access(y); splay(y);
165
         if (ch[y][0] != x||ch[x][1] != 0) return;
166
         ch[y][0] = fa[x] = 0; update(x); update(y);
167
     }
168
     inline void link(int x,int y) { fa[evert(x)] = y; }
169
170
     inline Value query(int x,int y) { evert(x); return val[access(y)]; }
171
172
     int main()
173
     {
174
         // freopen("D.in", "r", stdin);
175
         N = gi(), M = gi();
176
         for (int i = 1;i <= M;++i) edge[i].read();</pre>
177
         sort(edge+1,edge+M+1);
178
         for (int i = 0;i <= N;++i)</pre>
179
              A[i] = B[i] = -inf, val[i] = Value(A[i], B[i], i);
180
```

```
for (int i = 1;i <= M;++i)</pre>
181
              A[i+N] = edge[i].a,B[i+N] = edge[i].b,val[i+N] = Value(A[i+N],B[i+N],i+N);
182
         for (int i = 1;i <= M;++i)
183
184
              if (edge[i].x == edge[i].y) continue;
185
              if (find(edge[i].x) == find(edge[i].y))
186
              {
187
                  Value res = query(edge[i].x,edge[i].y); int id = res.id-N;
188
                  if (edge[i].b < edge[id].b)</pre>
189
190
                      cut(edge[id].x,id+N),cut(edge[id].y,id+N);
191
                      link(edge[i].x,i+N),link(edge[i].y,i+N);
192
                  }
193
              }
194
              else link(edge[i].x,i+N),link(i+N,edge[i].y);
195
              if (find(1) == find(N))
196
197
                  Value res = query(1,N);
198
                  ans = min(ans,res.ma+res.mb);
199
200
         }
201
         if (ans == inf) ans = -1;
202
         printf("%d\n",ans);
203
         return 0;
204
     }
205
```

3.7 Merge Split Treap

```
// jisuanke17123
   // Warning: 给指针赋值时, 不要赋 this, 因为 this 是临时变量的地址
    #include<sys/timeb.h>
    #include<queue>
    #include<algorithm>
    #include<cstring>
    #include<iostream>
    #include<cstdio>
    #include<cstdlib>
    #include<set>
10
   using namespace std;
11
12
    typedef long long ll;
13
    const int maxn = 1000010;
14
    int N;
15
16
    inline int rand(int n) { int x = rand(); if (x < 0) x = -x; return x\%n+1; }
17
   struct Node
19
20
        int size,key,val; Node *mn,*ch[2];
21
```

```
inline Node *update()
22
23
            mn = this; size = 1;
24
            if (ch[0])
25
26
                 size += ch[0]->size;
27
                 if (ch[0]->mn->val < mn->val) mn = ch[0]->mn;
28
            }
29
            if (ch[1])
30
            {
31
                 size += ch[1]->size;
32
                 if (ch[1]->mn->val < mn->val) mn = ch[1]->mn;
33
            }
34
            return this;
35
        }
36
        inline Node() = default;
37
        inline Node(int v,Node *_mn):size(1),key(rand()),val(v),mn(_mn) { ch[0] = ch[1] = NULL; }
38
    }pool[maxn*100/4],*root[maxn],*cur;
39
    struct Status
40
    {
41
        int 1,r; 11 val;
42
        inline Status() = default;
43
        inline Status(int _1,int _r,ll _val):1(_1),r(_r),val(_val) {}
44
        friend inline bool operator <(const Status &a,const Status &b) { return a.val > b.val; }
45
    };
46
47
    inline int sz(const Node *x) { if (x == NULL) return 0; else return x->size; }
48
49
    inline Node *newnode(int v = 0) { *cur = Node(v,cur); return cur++; }
50
51
    Node *insert(Node *p,Node *q)
52
53
        if (p == NULL&&q == NULL) return NULL;
54
        if (p == NULL||q == NULL) return p?p:q;
55
        Node *u = NULL;
56
        if (rand(sz(p)+sz(q)) < sz(p))
57
            u = p,u->ch[1] = insert(u->ch[1],q);
58
        else u = q,u->ch[0] = insert(p,u->ch[0]);
59
        return u->update();
60
    }
61
62
    Node *merge(Node *p,Node *q)
63
64
    {
        if (p == NULL&&q == NULL) return NULL;
65
        if (p == NULL||q == NULL) return p?p:q;
66
        Node *u = newnode();
67
        if (rand(sz(p)+sz(q)) < sz(p))
68
            *u = *p,u->ch[1] = merge(u->ch[1],q);
69
        else *u = *q,u->ch[0] = merge(p,u->ch[0]);
70
```

```
return u->update();
71
    }
72
73
    Node *split(Node *u,int l,int r)
74
75
         if (1 > r | | u == NULL) return 0;
76
         Node *x = NULL;
77
         if (1 == 1 \&\&r == sz(u))
78
79
             x = newnode(); *x = *u;
80
             return x->update();
81
         }
82
         int lsz = sz(u->ch[0]);
83
         if (r <= lsz) return split(u->ch[0],1,r);
84
         if (l > lsz+1) return split(u->ch[1],l-lsz-1,r-lsz-1);
85
         x = newnode(); *x = *u;
86
         x->ch[0] = split(u->ch[0],1,lsz);
87
         x->ch[1] = split(u->ch[1],1,r-lsz-1);
         return x->update();
89
    }
90
91
    inline int gi()
92
    {
93
         char ch; int ret = 0,f = 1;
94
         do ch = getchar(); while (!(ch >= '0'&&ch <= '9')&&ch != '-');
95
         if (ch == '-') f = -1,ch = getchar();
96
         do ret = ret*10+ch-'0',ch = getchar(); while (ch >= '0'&&ch <= '9');
97
         return ret*f;
98
    }
99
100
    int get_pos(Node *rt,Node *mn)
101
    {
102
         if (rt == mn) return sz(rt->ch[0]);
103
         else if (rt->ch[0]\&\&rt->ch[0]->mn == mn)
104
             return get_pos(rt->ch[0],mn);
105
         else return sz(rt->ch[0])+1+get_pos(rt->ch[1],mn);
106
    }
107
    inline pair <int,int> Qmin(Node *rt,int 1,int r)
108
109
         if (1 > r) return make_pair(-1,-1);
110
         Node *v = split(rt,1,r);
111
         auto ret = make_pair(v->mn->val,get_pos(v,v->mn)+1);
112
         return ret;
113
    }
114
    inline int get(Node *u,int x) { return split(u,x,x)->val; }
115
116
    inline void work(Node *rt,int k)
117
    {
118
         int n = sz(rt);
119
```

```
set <int> S; S.insert(0); S.insert(n+1);
120
         priority_queue <Status> heap;
121
         auto tmp = Qmin(rt,1,n);
122
         heap.push(Status(tmp.second,tmp.second,tmp.first));
123
         while (k--)
124
125
             auto now = heap.top(); heap.pop();
126
             printf("%lld\n",now.val);
127
             if (now.l == now.r)
128
             {
129
                  S.insert(now.1);
130
                  auto it = S.find(now.1);
131
                  int pre = *(--it);
132
                  int nxt = *++(++it);
133
                  auto ls = Qmin(rt,pre+1,now.l-1);
134
                  auto rs = Qmin(rt,now.l+1,nxt-1);
135
                  if (ls.first !=-1)
136
                      heap.push(Status(ls.second,ls.second,ls.first));
137
                  if (rs.first != -1)
138
                      heap.push(Status(rs.second,rs.second,rs.first));
139
             }
140
             if (now.r < n)
141
             {
142
                  int inc = get(rt,now.r+1);
143
                  ++now.r; now.val += (11)inc;
144
                  heap.push(now);
145
             }
146
         }
147
     }
148
149
     inline void init() { N = 0; cur = pool; }
150
151
     int main()
152
153
         struct timeb ttt; ftime(&ttt);
154
         srand(ttt.millitm+ttt.time*1000);
155
         for (int T = gi();T--;)
156
157
             init();
158
             for (int Q = gi();Q--;)
159
160
                  int opt = gi();
161
                  if (opt == 1)
162
163
                      root[++N] = NULL;
164
                      for (int n = gi();n--;)
165
                          root[N] = insert(root[N],newnode(gi()));
166
                  }
167
                  else if (opt == 2)
168
```

```
{
169
                      root[++N] = NULL;
170
                      int x = gi(),11 = gi(),r1 = gi(),y = gi(),12 = gi(),r2 = gi();
171
                      Node *ls = split(root[x],11,r1);
172
                      Node *rs = split(root[y],12,r2);
173
                      root[N] = merge(ls,rs);
174
                  }
175
                  else
176
                  {
177
                      int x = gi(),k = gi();
178
                      work(root[x],k);
179
                  }
180
              }
181
              // cerr << cur - pool << endl;
182
         }
183
         return 0;
184
     }
185
186
     // By zky. To be rewritten.
187
     const int mo=1e9+7;
188
     int rnd(){
189
         static int x=1;
190
         return x=(x*23333+233);
191
     }
192
     int rnd(int n){
193
         int x=rnd();
194
         if(x<0)x=-x;
195
         return x\%n+1;
196
     }
197
     struct node{
198
         int siz,key;
199
         int val;
200
         LL sum;
201
         node *c[2];
202
         node* rz(){
203
              sum=val;siz=1;
204
              if(c[0])sum+=c[0]->sum,siz+=c[0]->siz;
205
              if(c[1])sum+=c[1]->sum,siz+=c[1]->siz;
206
              return this;
207
         }
208
         node(){}
209
         node(int v){
210
              siz=1;key=rnd();
211
              val=v;sum=v;
212
              c[0]=c[1]=0;
213
         }
214
215
     }pool[maxn*8],*root,*cur=pool,*old_root,*stop;
216
     node *newnode(int v=0){
217
```

```
*cur=node(v);
218
         return cur++;
219
     }
220
     node *old_merge(node *p,node *q){
221
         if(!p&&!q)return 0;
222
         node *u=0;
223
         if(!p||!q)return u=p?p->rz():(q?q->rz():0);
224
         if(rnd(sz(p)+sz(q)) < sz(p)){
225
              u=p;
226
              u - c[1] = old_merge(u - c[1],q);
227
         }else{
228
              u=q;
229
              u->c[0]=old_merge(p,u->c[0]);
230
231
         return u->rz();
232
     }
233
     node *merge(node *p,node *q){
234
         if(!p&&!q)return 0;
235
         node *u=newnode();
236
         if(!p||!q)return u=p?p->rz():(q?q->rz():0);
237
         if(rnd(sz(p)+sz(q)) < sz(p)) \{
238
              *u=*p;
239
              u-c[1]=merge(u-c[1],q);
240
         }else{
241
              *u=*q;
242
              u->c[0]=merge(p,u->c[0]);
243
244
         return u->rz();
245
     }
246
     node *split(node *u,int l,int r){
247
         if(1>r||!u)return 0;
248
         node *x=0;
249
         if(l==1\&\&r==sz(u)){}
250
              x=newnode();
251
              *x=*u;
252
              return x->rz();
253
         }
254
         int lsz=sz(u->c[0]);
255
         if(r<=lsz)</pre>
256
              return split(u->c[0],1,r);
257
         if(l>lsz+1)
258
              return split(u->c[1],l-lsz-1,r-lsz-1);
259
         x=newnode();
260
         *x=*u;
261
         x->c[0]=split(u->c[0],1,lsz);
262
         x->c[1]=split(u->c[1],1,r-lsz-1);
263
         return x->rz();
264
     }
265
```

3.8 Modui Algorithm on Tree

```
// 询问树上路径元素 mex, inc dec 复杂度不对,需要用线段树/set(带 log) 或者分块 (修改 O(1))
   // 若包括 lca, 每组询问需要把 lca 补 (inc) 上去。
    #include<cstdio>
    #include < cstdlib>
    #include<algorithm>
   #include<cstring>
    #include<iostream>
   using namespace std;
    const int Size = 337,maxn = 200010;
10
    int N,Q,cnt,nxt[maxn],side[maxn],len[maxn],toit[maxn],f[maxn][20],key[maxn],timestamp;
11
    int dep[maxn],L[maxn],R[maxn],dfn[maxn],ans[maxn],exist[maxn],show[maxn],res;
12
13
    inline void add(int a,int b,int c) { nxt[++cnt] = side[a]; side[a] = cnt; toit[cnt] = b;
14

    len[cnt] = c; }

    inline void ins(int a,int b,int c) { add(a,b,c); add(b,a,c); }
15
16
   void dfs(int now)
17
18
        dfn[L[now] = ++timestamp] = now;
19
        for (int i = 1; (1<<i) <= dep[now]; ++i) f[now][i] = f[f[now][i-1]][i-1];
20
        for (int i = side[now];i;i = nxt[i])
21
22
            if (toit[i] == f[now][0]) continue;
23
            f[toit[i]][0] = now; key[toit[i]] = len[i];
24
            dep[toit[i]] = dep[now]+1;
25
            dfs(toit[i]);
26
27
        dfn[R[now] = ++timestamp] = now;
28
   }
29
30
    inline int jump(int a, int b) { for (int i = 0; b; b >>= 1, ++i) if (b\&1) a = f[a][i]; return a; }
31
    inline int lca(int a,int b)
32
33
        if (dep[a] < dep[b]) swap(a,b);</pre>
34
        a = jump(a,dep[a]-dep[b]);
35
        if (a == b) return a;
36
        for (int i = 0;i >= 0;)
37
38
            if (f[a][i] == f[b][i]) --i;
39
            else a = f[a][i], b = f[b][i], ++i;
40
        }
41
        return f[a][0];
42
   }
43
44
   struct Node
45
46
        int a,b,c,id;
47
```

```
Node() = default;
48
        Node(int _a,int _b,int _c = 0,int _id = 0):a(_a),b(_b),c(_c),id(_id) {}
49
        inline void read(int i)
50
        {
51
             id = i; scanf("%d %d", \&a, \&b); c = lca(a,b);
52
             if (c == a | | c == b) { if (a != c) swap(a,b); a = L[c]+1; b = L[b]; }
53
             else { if (L[a] > L[b]) swap(a,b); a = R[a]; b = L[b]; }
54
55
        friend inline bool operator <(const Node &x,const Node &y) { return x.b < y.b; }
56
    }query[maxn];
57
58
    inline bool cmp(const Node &x,const Node &y) { return x.a < y.a; }
59
60
    inline void inc(int id)
61
62
    {
        if (key[id] >= maxn) return;
63
        ++exist[key[id]];
64
        while (exist[res]) ++res;
65
    }
66
    inline void dec(int id)
67
68
        if (key[id] >= maxn) return;
69
        --exist[key[id]];
70
        if (key[id] < res&&!exist[key[id]]) res = key[id];</pre>
71
    }
72
73
    inline void work()
74
75
        int 1 = 1,r = 0;
76
        for (int i = 1;i <= Q;++i)</pre>
77
78
             while (r < query[i].b)</pre>
79
80
                 show[dfn[++r]]++;
                 if (show[dfn[r]] == 2) dec(dfn[r]); else inc(dfn[r]);
82
             }
83
             while (1 > query[i].a)
84
85
                 show[dfn[--1]]++;
86
                 if (show[dfn[1]] == 2) dec(dfn[1]); else inc(dfn[1]);
87
             }
88
             while (r > query[i].b)
89
90
                 if (show[dfn[r]] == 1) dec(dfn[r]); else inc(dfn[r]);
91
                 show[dfn[r--]]--;
92
93
             while (1 < query[i].a)
94
             {
95
                 if (show[dfn[1]] == 1) dec(dfn[1]); else inc(dfn[1]);
96
```

```
show[dfn[l++]]--;
97
98
              ans[query[i].id] = res;
99
          }
100
     }
101
102
     int main()
103
     {
104
          freopen("F.in","r",stdin);
105
          scanf("%d %d",&N,&Q);
106
          for (int i = 1; i < N; ++i)
107
108
              int a,b,c;
109
              scanf("%d %d %d",&a,&b,&c);
110
              ins(a,b,c);
111
          }
112
         dfs(1);
113
          for (int i = 1;i <= Q;++i) query[i].read(i);</pre>
114
          sort(query+1,query+Q+1,cmp);
115
         for (int i = 1, j; i \le Q; i = j)
116
117
              for (j = i; j \le Q\&\&query[j].a-query[i].a \le Size;++j);
118
              sort(query+i+1,query+j);
119
          }
120
          work();
121
          for (int i = 1;i <= Q;++i) printf("%d\n",ans[i]);</pre>
122
          return 0;
123
     }
124
```

3.9 Modui Algorithm without Deletion

```
//r 单调右移, l 只会在 sqrt(N) 中移动, 保证每次 undo 的复杂度可行即可。
   // CodeForces 620F
   #include<vector>
   #include<algorithm>
   #include<cstring>
   #include<iostream>
   #include<cstdio>
   #include < cstdlib>
   using namespace std;
10
   const int maxn = 1000010,len = 200,inf = 1<<29;</pre>
11
   int N,M,pre[maxn],A[maxn],ans[maxn];
12
13
   inline int gi()
14
   {
15
       char ch; int ret = 0,f = 1;
16
       do ch = getchar(); while (!(ch >= 0'&&ch <= 9')&&ch != -1);
17
       if (ch == '-') f = -1, ch = getchar();
18
```

```
do ret = ret*10+ch-'0',ch = getchar(); while (ch >= '0'&&ch <= '9');
19
        return ret*f;
20
    }
21
22
    inline void upd(int &a,int b) { if (a < b) a = b; }</pre>
23
24
    struct Trie
25
    {
26
        int nxt[maxn][2],val[maxn],root,cnt; vector < pair<int,int> > vec;
27
        inline int newnode() { val[++cnt] = inf; memset(nxt[cnt],0,8); return cnt; }
28
        inline void init() { val[0] = inf; cnt = 0; root = newnode(); }
29
        inline int query(int key,int num)
31
32
33
            int now = root,ret = 0;
            for (int i = 19; i >= 0; --i)
34
35
                 int dir = !(num&(1<<i));</pre>
36
                 if (val[nxt[now][dir]] <= key)</pre>
37
                     ret |= (1<<i),now = nxt[now][dir];</pre>
38
                 else now = nxt[now][dir^1];
39
            }
40
41
            return ret;
        }
42
43
        inline void insert(int key,int num,int mode) { insert(root,19,key,num,mode); }
44
        inline void insert(int &now,int dep,int key,int num,int mode)
45
46
            if (!now) now = newnode();
47
            if (dep < 0)
48
            {
49
                 if (mode) vec.push_back(make_pair(num,val[now]));
50
                 val[now] = min(val[now],key); return;
51
            }
52
            insert(nxt[now][(num&(1<<dep)) > 0],dep-1,key,num,mode);
53
            val[now] = min(val[nxt[now][0]],val[nxt[now][1]]);
        }
55
        inline void change(int now,int dep,int num,int v)
57
        {
            if (dep < 0) { val[now] = v; return; }</pre>
59
            change(nxt[now][(num&(1<<dep)) > 0],dep-1,num,v);
60
            val[now] = min(val[nxt[now][0]],val[nxt[now][1]]);
61
        }
62
63
        inline void undo()
64
        {
65
            reverse(vec.begin(),vec.end());
66
            for (auto x:vec) change(root,19,x.first,x.second);
67
```

```
vec.clear();
68
69
    }tree1,tree2;
70
     struct Query
72
73
         int 1,r,id;
74
         inline void read(int i) { 1 = gi(),r = gi(),id = i; }
75
         friend inline bool operator <(const Query &a,const Query &b) { return a.1 < b.1; }
76
     }query[maxn];
77
     inline bool cmp(const Query &a,const Query &b) { return a.r < b.r; }</pre>
78
79
     inline void work(int l,int r)
80
81
         int lim = query[r].1;
82
         sort(query+1,query+r+1,cmp);
83
         tree1.init(); tree2.init();
84
         for (int i = 1;i <= r;++i)
85
86
             if (query[i].r <= lim)</pre>
87
             Ł
88
                  for (int j = query[i].1; j <= query[i].r; ++ j)</pre>
89
                  {
90
                      tree1.insert(A[j],pre[A[j]-1],false);
91
                      tree2.insert(-A[j],pre[A[j]],false);
92
                      upd(ans[query[i].id],tree1.query(A[j],pre[A[j]]));
93
                      upd(ans[query[i].id],tree2.query(-A[j],pre[A[j]-1]));
94
                 }
95
                  tree1.init(),tree2.init();
96
             }
97
             else
98
             {
99
                  int pos = lim,mx = 0;
100
                 for (;i <= r;++i)
101
                  {
102
                      while (pos < query[i].r)</pre>
103
                      {
104
                           ++pos;
105
                           tree1.insert(A[pos],pre[A[pos]-1],false);
106
                           tree2.insert(-A[pos],pre[A[pos]],false);
107
                           upd(mx,tree1.query(A[pos],pre[A[pos]]));
108
                           upd(mx,tree2.query(-A[pos],pre[A[pos]-1]));
109
110
                      upd(ans[query[i].id],mx);
111
                      for (int j = lim; j >= query[i].1;--j)
112
113
                           tree1.insert(A[j],pre[A[j]-1],true);
114
                           tree2.insert(-A[j],pre[A[j]],true);
115
                           upd(ans[query[i].id],tree1.query(A[j],pre[A[j]]));
116
```

```
upd(ans[query[i].id],tree2.query(-A[j],pre[A[j]-1]));
117
                       }
118
                       tree1.undo(); tree2.undo();
119
                  }
120
                   break;
121
              }
122
          }
123
     }
124
125
     int main()
126
     {
127
         // freopen("A.in", "r", stdin);
128
         for (int i = 1;i <= 1000000;++i) pre[i] = pre[i-1]^i;
129
         N = gi(); M = gi();
130
         for (int i = 1;i <= N;++i) A[i] = gi();</pre>
131
         for (int i = 1;i <= M;++i) query[i].read(i);</pre>
132
         sort(query+1,query+M+1);
133
         for (int i = 1,j;i <= M;i = j)
134
135
              for (j = i; j <= M&&query[j].l-query[i].l <= len;++j);</pre>
136
              work(i,j-1);
137
138
         for (int i = 1;i <= M;++i) printf("%d\n",ans[i]);</pre>
139
         return 0;
140
     }
141
```

3.10 President Tree

```
inline void build(int &now,int l,int r)
        now = ++cnt; if (1 == r) return;
        int mid = (1+r) >> 1;
        build(tree[now].ch[0],1,mid); build(tree[now].ch[1],mid+1,r);
   }
   inline void ins(int &now,int ref,int l,int r,int key)
        now = ++cnt; tree[now] = tree[ref];
10
        if (1 == r) { ++tree[now].sum; return; }
        int mid = (1+r) >> 1;
        if (key <= mid) ins(tree[now].ch[0],tree[ref].ch[0],1,mid,key);</pre>
        else ins(tree[now].ch[1],tree[ref].ch[1],mid+1,r,key);
        tree[now].sum = tree[tree[now].ch[0]].sum+tree[tree[now].ch[1]].sum;
15
   }
16
```

3.11 Splay

```
1 //splay
```

```
inline int find(int rk)
4
        for (int now = root;;)
5
            if (rk == size[ch[now][0]]+1) return now;
            else if (rk > size[ch[now][0]]+1)
                 rk -= size[ch[now][1]]+1,now = ch[now][1];
            else now = ch[now][0];
10
        }
11
        return 0;
12
    }
13
14
    inline int upperbound(int x)
15
16
        int ret = 0;
17
        for (int now = root;now;)
18
19
            if (key[now] > x) ret = now,now = ch[now][0];
20
            else now = ch[now][1];
21
        }
22
        return ret;
23
    }
24
    inline int lowerbound(int x)
25
    {
26
        int ret = 0;
27
        for (int now = root;now;)
28
29
            if (key[now] >= x) ret = now,now = ch[now][0];
30
            else now = ch[now][1];
31
        }
32
        return ret;
33
    }
34
35
    inline void rotate(int x)
36
37
        int y = fa[x],z = fa[y],l = ch[y][0] != x,r = l^1;
38
        if (z) ch[z][ch[z][0] != y] = x; fa[x] = z;
39
        if (ch[x][r]) fa[ch[x][r]] = y;
40
        ch[y][1] = ch[x][r]; fa[y] = x; ch[x][r] = y;
41
        update(y); update(x);
42
    }
43
    inline void splay(int x,int aim) //aim is x's father.
44
    {
45
        int top = 0;
46
        for (int i = x;i;i = fa[i]) stack[++top] = i;
47
        while (top) pushdown(stack[top--]);
48
        while (fa[x] != aim)
49
50
            int y = fa[x],z = fa[y];
51
```

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```
if (z != aim)
52
53
                  if ((ch[y][0] == x)^(ch[z][0] == y)) rotate(x);
54
                  else rotate(y);
55
             }
56
             rotate(x);
57
         }
58
         if (!aim) root = x;
59
    }
60
61
    // 维修数列
62
    #include<cassert>
63
    #include<queue>
64
    #include<algorithm>
65
    #include<cstring>
66
    #include<iostream>
67
     #include<cstdio>
68
    #include<cstdlib>
69
    using namespace std;
70
71
    const int maxn = 500010,inf = 1<<29;</pre>
72
    int N,M,root,cnt,arr[maxn],tag[maxn],key[maxn],fa[maxn],ch[maxn][2],lb[maxn],rb[maxn];
73
    int wb[maxn],sum[maxn],size[maxn],stk[maxn]; bool rev[maxn]; char cmd[20]; queue <int> team;
74
75
    inline int gi()
76
77
         char ch; int ret = 0,f = 1;
78
         do ch = getchar(); while (!(ch >= '0'&&ch <= '9')&&ch != '-');
79
         if (ch == '-') f = -1,ch = getchar();
80
         do ret = ret*10+ch-'0',ch = getchar(); while (ch >= '0'&&ch <= '9');
81
         return ret*f;
82
    }
83
84
    inline int newnode(int x = 0)
85
    {
86
         int ret;
87
         if (!team.empty())
88
             ret = team.front(),team.pop();
89
         else ret = ++cnt;
90
         key[ret] = sum[ret] = lb[ret] = rb[ret] = wb[ret] = x;
91
         rev[ret] = false; tag[ret] = inf; size[ret] = 1;
92
         return ret;
93
    }
94
95
    inline void pushdown(int now)
96
97
         int lc = ch[now][0],rc = ch[now][1];
98
         if (rev[now])
99
100
```

```
if (lc)
101
             {
102
                  swap(ch[lc][0],ch[lc][1]);
103
                  swap(lb[lc],rb[lc]); rev[lc] ^= 1;
104
             }
105
             if (rc)
106
             {
107
                  swap(ch[rc][0],ch[rc][1]);
108
                  swap(lb[rc],rb[rc]); rev[rc] ^= 1;
109
             }
110
             rev[now] = false;
111
         }
112
         if (tag[now] != inf)
113
114
             if (lc)
115
             {
116
                  key[lc] = tag[lc] = tag[now]; sum[lc] = tag[lc]*size[lc];
117
                  if (tag[lc] > 0) lb[lc] = rb[lc] = wb[lc] = sum[lc];
118
                  else lb[lc] = rb[lc] = wb[lc] = tag[lc];
119
             }
120
             if (rc)
121
             {
122
                  key[rc] = tag[rc] = tag[now]; sum[rc] = tag[rc]*size[rc];
123
                  if (tag[rc] > 0) lb[rc] = rb[rc] = wb[rc] = sum[rc];
124
                  else lb[rc] = rb[rc] = wb[rc] = tag[rc];
125
126
             tag[now] = inf;
127
         }
128
     }
129
130
     inline void update(int now)
131
     {
132
         // pushdown(now);
133
         int lc = ch[now][0],rc = ch[now][1];
134
         size[now] = size[lc]+size[rc]+1;
135
         sum[now] = sum[lc]+sum[rc]+key[now];
136
         if (lc&&rc)
137
138
             lb[now] = max(lb[lc],max(sum[lc]+key[now],sum[lc]+key[now]+lb[rc]));
139
             rb[now] = max(rb[rc], max(sum[rc]+key[now], sum[rc]+key[now]+rb[lc]));
140
             wb[now] = max(wb[lc],wb[rc]); wb[now] = max(wb[now],key[now]);
141
             wb[now] = max(wb[now],rb[lc]+key[now]); wb[now] = max(wb[now],lb[rc]+key[now]);
142
             wb[now] = max(wb[now],rb[lc]+key[now]+lb[rc]);
143
         }
144
         else if (lc)
145
146
             lb[now] = max(lb[lc],sum[lc]+key[now]);
147
             rb[now] = max(key[now],key[now]+rb[lc]);
148
             wb[now] = max(wb[lc],key[now]);
149
```

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```
wb[now] = max(wb[now],rb[lc]+key[now]);
150
151
         else if (rc)
152
         {
153
             rb[now] = max(rb[rc],sum[rc]+key[now]);
154
             lb[now] = max(key[now],key[now]+lb[rc]);
155
             wb[now] = max(wb[rc],key[now]);
156
             wb[now] = max(wb[now],lb[rc]+key[now]);
157
158
         else sum[now] = lb[now] = rb[now] = wb[now] = key[now];
159
    }
160
161
    inline int build(int 1,int r)
162
163
         int mid = (l+r) >> 1,ret = newnode(arr[mid]);
164
         if (1 < mid) ch[ret][0] = build(1,mid-1),fa[ch[ret][0]] = ret;</pre>
165
         if (r > mid) ch[ret][1] = build(mid+1,r),fa[ch[ret][1]] = ret;
166
         update(ret); return ret;
167
    }
168
169
    inline void init()
170
171
         root = newnode(); ch[root][1] = newnode(); fa[2] = 1;
172
         for (int i = 1;i <= N;++i) arr[i] = gi();</pre>
173
         ch[2][0] = build(1,N); fa[ch[2][0]] = 2;
174
         update(2); update(1);
175
    }
176
177
    inline int find(int rk)
178
179
         for (int now = root;;)
180
         {
181
             pushdown(now);
182
             if (rk == size[ch[now][0]]+1) return now;
183
             else if (rk > size[ch[now][0]]+1)
184
                 rk -= size[ch[now][0]]+1,now = ch[now][1];
185
             else now = ch[now][0];
186
         }
187
         return 0;
188
    }
189
190
    inline void rotate(int x)
191
192
    {
         int y = fa[x],z = fa[y],l = ch[y][0] != x,r = 1^1;
193
         if (z) ch[z][ch[z][0] != y] = x;
194
         fa[x] = z; fa[y] = x; fa[ch[x][r]] = y;
195
         ch[y][1] = ch[x][r]; ch[x][r] = y;
196
         update(y); update(x);
197
    }
198
```

```
inline void splay(int x,int aim)
199
200
         int top = 0;
201
         for (int i = x;i;i = fa[i]) stk[++top] = i;
202
         while (top) pushdown(stk[top--]);
203
         while (fa[x] != aim)
204
205
              int y = fa[x],z = fa[y];
206
              if (z != aim)
207
208
                  if ((ch[y][0] == x)^(ch[z][0] == y)) rotate(x);
209
                  else rotate(y);
210
              }
211
              rotate(x);
212
213
         if (!aim) root = x;
214
     }
215
216
     inline void Delete(int &now)
217
218
         if (!now) return;
219
         Delete(ch[now][0]);
220
         Delete(ch[now][1]);
221
         team.push(now); now = 0;
222
     }
223
224
     inline void print()
225
226
         for (int i = 1;i <= cnt;++i)
227
              printf("%d:%d %d\n",i,ch[i][0],ch[i][1]);
228
         for (int i = 1;i <= cnt;++i)</pre>
229
              printf("%d:%d\n",i,fa[i]);
230
231
     }
232
233
     inline void laydown(int now)
234
235
         if (!now) return;
236
         pushdown(now);
237
         laydown(ch[now][0]);
238
         printf("%d ",key[now]);
239
         laydown(ch[now][1]);
240
         update(now);
241
     }
242
243
     int main()
244
     {
245
         //freopen("C.in", "r", stdin);
246
         N = gi(); M = gi(); init();
247
```

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```
while (M--)
248
         {
249
             scanf("%s",cmd);
250
             if (cmd[0] == 'I')
251
             {
252
                  int pos = gi(),a = find(pos+1),b = find(pos+2); N = gi();
253
                  for (int i = 1;i <= N;++i) arr[i] = gi();</pre>
254
                  splay(a,0); splay(b,a);
255
                  ch[b][0] = build(1,N); fa[ch[b][0]] = b;
256
                  update(b); update(a);
257
258
             else if (cmd[0] == 'D')
259
             {
260
                  int pos = gi(); N = gi();
261
                  int a = find(pos),b = find(pos+N+1);
262
                  splay(a,0); splay(b,a);
263
                  Delete(ch[b][0]); update(b); update(a);
264
             }
265
             else if (cmd[0] == 'M'\&\&cmd[2] == 'K')
266
             {
267
                  int pos = gi(); N = gi();
268
                  int a = find(pos),b = find(pos+N+1);
269
                  splay(a,0); splay(b,a);
270
                  key[ch[b][0]] = tag[ch[b][0]] = gi(); sum[ch[b][0]] = tag[ch[b][0]]*size[ch[b][0]];
271
                  if (tag[ch[b][0]] > 0) lb[ch[b][0]] = rb[ch[b][0]] = wb[ch[b][0]] = sum[ch[b][0]];
272
                  else lb[ch[b][0]] = rb[ch[b][0]] = wb[ch[b][0]] = tag[ch[b][0]];
273
                  update(b); update(a);
274
             }
275
             else if (cmd[0] == 'R')
276
277
                  int pos = gi(); N = gi();
278
                  int a = find(pos),b = find(pos+N+1);
279
                  splay(a,0); splay(b,a);
280
                  rev[ch[b][0]] ^= 1;
281
                  swap(ch[ch[b][0]][0],ch[ch[b][0]][1]);
282
                  swap(lb[ch[b][0]],rb[ch[b][0]]);
283
                  update(b); update(a);
284
             }
285
             else if (cmd[0] == 'G')
286
             {
287
                  int pos = gi(); N = gi();
288
                  int a = find(pos),b = find(pos+N+1);
289
                  splay(a,0); splay(b,a);
290
                 printf("%d\n",sum[ch[b][0]]);
291
             }
292
             else
293
             {
294
                  splay(1,0); splay(2,1);
295
                  printf("%d\n", wb[ch[2][0]]);
296
```

```
297 }
298 }
299 return 0;
300 }
```

Chapter 4

Graph Theory

4.1 2-Sat

```
// bzoj 1823
    #include<stack>
    #include<iostream>
    #include<cstring>
    #include<cstdio>
    #include<cstdlib>
    using namespace std;
    #define maxn 210
    #define maxm 2010
10
    int n,m,cnt,side[maxn],next[maxm],toit[maxm],dfn[maxn],id[maxn];
    int tot,low[maxn],d[maxn],DFN;
    stack <int> S; bool vis[maxn];
13
14
    inline void init()
15
16
        DFN = tot = cnt = 0; memset(vis,false,2*(n+4));
17
        memset(side,0,8*(n+4)); memset(dfn,0,8*(n+4));
18
    }
19
20
    inline void add(int a,int b) { next[++cnt] = side[a]; side[a] = cnt; toit[cnt] = b; }
21
22
    inline void dfs(int now)
23
24
        S.push(now); dfn[now] = low[now] = ++DFN;
25
        for (int i = side[now];i;i = next[i])
26
27
            if (vis[toit[i]]) continue;
28
            if (!dfn[toit[i]]) dfs(toit[i]);
29
            low[now] = min(low[toit[i]],low[now]);
30
31
        if (low[now] == dfn[now])
32
        {
33
```

```
++tot;
34
             while (S.top() != now) id[S.top()] = tot,vis[S.top()] = true,S.pop();
35
             id[S.top()] = tot,vis[S.top()] = true,S.pop();
36
        }
37
    }
38
39
    int main()
40
    {
41
        freopen("1823.in","r",stdin);
42
        freopen("1823.out","w",stdout);
43
        int T; scanf("%d",&T);
44
        while (T--)
45
46
             scanf("%d %d\n",&n,&m);
47
             init();
48
             while (m--)
49
50
                 char c1,c2; int a,b; bool o1,o2;
51
                 scanf("%c%d %c%d\n",&c1,&a,&c2,&b);
52
                 o1 = c1 == 'h'; o2 = c2 == 'h';
53
                 add((o1^1)*n+a,o2*n+b);
54
                 add((o2^1)*n+b,o1*n+a);
55
             }
56
             int i;
57
             for (i = 1;i <= n<<1;++i) if (!dfn[i]) dfs(i);
58
             for (i = 1; i <= n; ++i) if (id[i] == id[i+n]) { printf("BAD\n"); break; }
             if (i <= n) continue;</pre>
60
             printf("GOOD\n");
61
62
        fclose(stdin); fclose(stdout);
63
        return 0;
64
    }
65
```

4.2 Bridges and Cut Vertices

```
// 求割边和割点
   const int maxn = 200010;
   int N,M,cnt,Ts,dfn[maxn],low[maxn],nxt[maxn];
   int toit[maxn], side[maxn];
   bool bridge[maxn], cut[maxn];
   inline void dfs(int now,int fa)
       dfn[now] = low[now] = ++Ts; int child = 0;
        for (int i = side[now];i;i = nxt[i])
10
11
            if (toit[i] == fa) continue;
12
            if (!dfn[toit[i]])
13
            {
14
```

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```
dfs(toit[i],now); ++child;
15
                low[now] = min(low[now],low[toit[i]]);
16
                 if (low[toit[i]] > dfn[now]) bridge[i] = true;
17
                 if (low[toit[i]] >= dfn[now]) cut[now] = true;
18
19
            else low[now] = min(low[now],dfn[toit[i]]);
20
21
        if (!fa&&child == 1) cut[now] = false;
22
    }
23
```

4.3 Cost Flow

return true;

36

```
int side[maxv],nxt[maxe],toit[maxe],cost[maxe],pre[maxv];
    int cap[maxv],arr[maxv],dis[maxv]; bool in[maxv];
    int source,sink;
    inline void add(int a,int b,int c,int d) { nxt[++cnt] = side[a]; side[a] = cnt; toit[cnt] = b;

    cap[cnt] = c; cost[cnt] = d; }

    inline void ins(int a,int b,int c,int d) { add(a,b,c,d); add(b,a,0,-d); }
    inline bool spfa(int &Flow,int &Cost)
    {
        queue <int> team; team.push(source);
10
        memset(dis,0x7,4*(sink+5));
11
        dis[source] = 0; in[source] = true;
12
        arr[source] = inf; arr[sink] = 0;
13
        while (!team.empty())
14
15
            int now = team.front(); team.pop();
16
            for (int i = side[now];i;i = nxt[i])
17
            {
18
                if (!cap[i]) continue;
19
                if (dis[toit[i]] > dis[now]+cost[i])
20
                {
21
                     arr[toit[i]] = min(cap[i],arr[now]); pre[toit[i]] = i;
22
                     dis[toit[i]] = dis[now]+cost[i];
23
                     if (!in[toit[i]]) in[toit[i]] = true,team.push(toit[i]);
24
                }
25
            }
26
            in[now] = false;
27
28
        if (!arr[sink]) return false;
29
        Flow += arr[sink];
30
        for (int now = sink,i;now != source;now = toit[i^1])
31
32
            i = pre[now]; Cost += cost[pre[now]]*arr[sink];
33
            cap[i] -= arr[sink]; cap[i^1] += arr[sink];
34
        }
35
```

37 }

4.4 Difference Constraints

```
// DFS 判负环,相当于用栈跑 SPFA,只判负环比队列快
    inline bool SPFA(int n,int source)
        for(int i = 1;i <= n; i++)
4
            dis[i] = inf,vis[i] = false,arr[i] = 0;
        arr[source] = 1; dis[source] = 0; vis[source] = true;
        stack <int> stk; stk.push(source);
        while(!stk.empty())
            int now = stk.top(); stk.pop(); vis[now] = false;
10
            for (int i = side[now];i;i = nxt[i])
11
                if (dis[toit[i]] > dis[now]+len[i])
12
                {
13
                    dis[toit[i]] = dis[now]+len[i];
14
                    if (!vis[toit[i]])
15
16
                         if (++arr[toit[i]] > N) return false;
17
                         vis[toit[i]] = true;
18
                         team.push(toit[i]);
19
                    }
20
                }
21
22
        return true;
23
   }
24
25
    // bzoj2330
26
    #include<iostream>
27
    #include<stack>
28
    #include<queue>
29
    #include<cstdio>
30
    #include<cstdlib>
31
    using namespace std;
32
33
    #define maxn 100010
34
    #define maxm 200010
35
    int cnt,side[maxn],next[maxm],toit[maxm],cost[maxm],d[maxn];
36
    int nside[maxn],nnext[maxm],ntoit[maxm],ncost[maxm],m,tot;
37
    int dfn[maxn],low[maxn],sum[maxn],id[maxn],arr[maxn],n;
38
    bool vis[maxn]; stack <int> S;
39
40
    inline void add(int a,int b,int c)
41
   {
42
        next[++cnt] = side[a]; side[a] = cnt;
43
        toit[cnt] = b; cost[cnt] = c;
44
   }
45
```

```
46
    inline void ins(int a,int b,int c)
47
48
        nnext[++cnt] = nside[a]; nside[a] = cnt;
49
        ntoit[cnt] = b; ncost[cnt] = c; ++d[b];
50
    }
51
52
    inline void dfs(int now)
53
54
        S.push(now); dfn[now] = low[now] = ++cnt;
55
        for (int i = side[now];i;i = next[i])
56
             if (!vis[toit[i]])
57
58
                 if (!dfn[toit[i]]) dfs(toit[i]);
59
                 low[now] = min(low[toit[i]],low[now]);
60
61
        if (low[now] == dfn[now])
62
        {
63
             ++tot;
64
             while (S.top() != now) id[S.top()] = tot,vis[S.top()] = true,S.pop();
65
             id[S.top()] = tot,vis[S.top()] = true,S.pop();
66
        }
67
    }
68
69
    inline bool rebuild()
70
71
        cnt = 0;
72
        for (int i = 1;i <= n;++i)
73
             for (int j = side[i]; j; j = next[j])
74
75
                 if (id[toit[j]] == id[i]) sum[id[i]] += cost[j];
76
                 else ins(id[i],id[toit[j]],cost[j]);
77
78
        for (int i = 1;i <= tot;++i) if (sum[i]) return false;</pre>
79
        return true;
80
    }
81
82
    inline void topsort()
83
    {
84
        queue <int> team;
85
        for (int i = 1;i <= tot;++i) if (!d[i]) team.push(i),arr[i] = 1;</pre>
86
        while (!team.empty())
87
88
             int now = team.front(); team.pop();
89
             for (int i = nside[now];i;i = nnext[i])
90
91
                 arr[ntoit[i]] = max(arr[now]+ncost[i],arr[ntoit[i]]);
92
                 if (!--d[ntoit[i]]) team.push(ntoit[i]);
93
             }
94
```

```
}
95
    }
96
97
    int main()
99
         freopen("2330.in", "r", stdin);
100
         freopen("2330.out","w",stdout);
101
         scanf("%d %d",&n,&m);
102
         for (int i = 1;i <= m;++i)
103
104
             int x,a,b; scanf("%d %d %d",&x,&a,&b);
105
             if (x == 1) add(a,b,0),add(b,a,0);
106
             else if (x == 2) add(a,b,1);
107
             else if (x == 3) add(b,a,0);
108
             else if (x == 4) add(b,a,1);
109
             else add(a,b,0);
110
         }
111
         cnt = 0; for (int i = n;i;--i) if (!dfn[i]) dfs(i);
112
         if (!rebuild()) printf("-1"),exit(0);
113
         topsort();
114
         long long ans = 0;
115
         for (int i = 1;i <= n;++i) ans += (long long)arr[id[i]];</pre>
116
         printf("%lld",ans);
117
         fclose(stdin); fclose(stdout);
118
         return 0;
119
    }
120
```

4.5 Dinic Algorithm

```
// dinic
   int source,sink,cnt = 1;
   int d[maxv], side[maxv], cur[maxv], nxt[maxe], toit[maxe], cap[maxe]; bool in[maxv];
   inline void add(int a,int b,int c) { nxt[++cnt] = side[a]; side[a] = cnt; toit[cnt] = b;

    cap[cnt] = c; }

   inline void ins(int a,int b,int c) { add(a,b,c); add(b,a,0); }
   inline bool bfs()
   {
        queue <int> team; team.push(source); d[source] = 0;
10
        memset(in,false,tot+10); in[source] = true; team.push(source);
11
        while (!team.empty())
12
13
            int now = team.front(); team.pop(); cur[now] = side[now];
14
            for (int i = side[now];i;i = nxt[i])
15
            {
16
                if (!cap[i]) continue;
                if (!in[toit[i]])
18
                    in[toit[i]] = true,d[toit[i]] = d[now]+1,team.push(toit[i]);
19
```

```
}
20
21
        return in[sink];
22
    }
23
24
    inline int dfs(int now,int f)
25
26
        if (now == sink||!f) return f;
27
        int used = 0,w;
28
        for (int &i = cur[now];i;i = nxt[i])
29
             if (cap[i]&&d[toit[i]] == d[now]+1)
30
31
                 w = dfs(toit[i],min(cap[i],f-used));
32
                 used += w; cap[i] -= w; cap[i^1] += w;
33
                 if (used == f) break;
34
35
        return used;
36
    }
37
38
    inline int dinic(int S,int T)
39
40
         source = S; sink = T; int ret = 0;
41
        while (bfs()) ret += dfs(source,inf);
42
        return ret;
43
    }
44
```

4.6 Dominator Tree

```
//建出来的树点的编号 i 在原图中是 redfn[i]
   int
        N,M,Ts,cnt,side[maxn],nxt[maxn],toit[maxn],dfn[maxn],redfn[maxn],idom[maxn],best[maxn],semi[maxn];
   int ans[maxn],anc[maxn],fa[maxn],child[maxn],size[maxn]; vector <int>
        prod[maxn],bucket[maxn],son[maxn];
   inline void init()
        cnt = 1; memset(side,0,sizeof side); memset(ans,0,sizeof ans);
        for (int i = 0;i <= N;++i) prod[i].clear(),bucket[i].clear(),son[i].clear();</pre>
   }
10
   inline void add(int a,int b) { nxt[++cnt] = side[a]; side[a] = cnt; toit[cnt] = b; }
11
12
   inline int gi()
13
14
        char ch; int ret = 0,f = 1;
15
        do ch = getchar(); while (!(ch >= '0'&&ch <= '9')&&ch != '-');
16
        if (ch == '-') f = -1, ch = getchar();
       do ret = ret*10+ch-^{'0'},ch = getchar(); while (ch >= ^{'0'}&&ch <= ^{'9'});
18
       return ret*f;
19
```

```
}
20
21
    inline void dfs(int now)
22
    {
23
        dfn[now] = ++Ts; redfn[Ts] = now;
24
        anc[Ts] = idom[Ts] = child[Ts] = size[Ts] = 0;
25
        semi[Ts] = best[Ts] = Ts;
26
        for (int i = side[now];i;i = nxt[i])
27
28
             if (!dfn[toit[i]])
29
                 dfs(toit[i]),fa[dfn[toit[i]]] = dfn[now];
30
             prod[dfn[toit[i]]].push_back(dfn[now]);
31
        }
32
    }
33
34
    inline void compress(int now)
35
36
        if (anc[anc[now]] != 0)
37
        {
38
             compress(anc[now]);
39
             if (semi[best[now]] > semi[best[anc[now]]])
40
                 best[now] = best[anc[now]];
41
             anc[now] = anc[anc[now]];
42
        }
43
    }
44
45
    inline int eval(int now)
46
47
        if (!anc[now]) return now;
48
        else
49
        {
50
             compress(now);
51
             return semi[best[anc[now]]] >= semi[best[now]]?best[now]:best[anc[now]];
52
        }
53
    }
54
55
    inline void link(int v,int w)
56
57
        int s = w;
58
        while (semi[best[w]] < semi[best[child[w]]])</pre>
59
60
             if (size[s]+size[child[child[s]]] >= 2*size[child[s]])
61
                 anc[child[s]] = s,child[s] = child[child[s]];
62
             else size[child[s]] = size[s],s = anc[s] = child[s];
63
        }
64
        best[s] = best[w]; size[v] += size[w];
65
        if (size[v] < 2*size[w]) swap(s,child[v]);</pre>
66
        while (s) anc[s] = v,s = child[s];
67
    }
68
```

```
69
     inline void lengauer_tarjan()
70
 71
         memset(dfn,0,sizeof dfn); memset(fa,-1,sizeof fa); Ts = 0;
 72
         dfs(N); fa[1] = 0;
 73
         for (int w = Ts; w > 1; --w)
 74
         {
 75
             for (auto x:prod[w])
 76
 77
                  int u = eval(x);
                  if (semi[w] > semi[u]) semi[w] = semi[u];
 79
             }
 80
             bucket[semi[w]].push_back(w);
 81
             link(fa[w],w); if (!fa[w]) continue;
 82
             for (auto x:bucket[fa[w]])
 83
             {
 84
                  int u = eval(x);
 85
                  if (semi[u] < fa[w]) idom[x] = u;</pre>
 86
                  else idom[x] = fa[w];
 87
 88
             bucket[fa[w]].clear();
 89
 90
         for (int w = 2; w \le Ts; ++w)
91
             if (idom[w] != semi[w])
92
                  idom[w] = idom[idom[w]];
93
         idom[1] = 0;
 94
         for (int i = Ts; i > 1; --i)
95
         {
96
             if (fa[i] == -1) continue;
97
             son[idom[i]].push_back(i);
98
         }
99
     }
100
101
     // 例题: 询问 i 号点到 N 号点所有必经点编号和
102
     #include<algorithm>
103
     #include<cstring>
104
     #include<iostream>
105
     #include<cstdio>
106
     #include<cstdlib>
107
     using namespace std;
108
109
     const int maxn = 100010;
110
111
     int
          \verb|N,M,Ts,cnt,side[maxn],nxt[maxn],toit[maxn],dfn[maxn],redfn[maxn],idom[maxn],best[maxn],semi[maxn];\\
     int ans[maxn],anc[maxn],fa[maxn],child[maxn],size[maxn]; vector <int>
112
          prod[maxn],bucket[maxn],son[maxn];
113
     inline void init()
114
115
```

```
cnt = 1; memset(side,0,sizeof side); memset(ans,0,sizeof ans);
116
         for (int i = 0;i <= N;++i) prod[i].clear(),bucket[i].clear(),son[i].clear();</pre>
117
     }
118
119
     inline void add(int a,int b) { nxt[++cnt] = side[a]; side[a] = cnt; toit[cnt] = b; }
120
121
     inline int gi()
122
     {
123
         char ch; int ret = 0,f = 1;
124
         do ch = getchar(); while (!(ch >= '0'&&ch <= '9')&&ch != '-');
125
         if (ch == '-') f = -1,ch = getchar();
126
         do ret = ret*10+ch-'0',ch = getchar(); while (ch >= '0'&&ch <= '9');
127
         return ret*f;
128
     }
129
130
     inline void dfs(int now)
131
132
         dfn[now] = ++Ts; redfn[Ts] = now;
133
         anc[Ts] = idom[Ts] = child[Ts] = size[Ts] = 0;
134
         semi[Ts] = best[Ts] = Ts;
135
         for (int i = side[now];i;i = nxt[i])
136
137
             if (!dfn[toit[i]])
138
                  dfs(toit[i]),fa[dfn[toit[i]]] = dfn[now];
139
             prod[dfn[toit[i]]].push_back(dfn[now]);
140
         }
141
     }
142
143
     inline void compress(int now)
144
145
         if (anc[anc[now]] != 0)
146
         {
147
             compress(anc[now]);
148
             if (semi[best[now]] > semi[best[anc[now]]])
149
                  best[now] = best[anc[now]];
150
             anc[now] = anc[anc[now]];
151
         }
152
     }
153
154
     inline int eval(int now)
155
156
         if (!anc[now]) return now;
157
         else
158
         {
159
             compress(now);
160
             return semi[best[anc[now]]] >= semi[best[now]]?best[now]:best[anc[now]];
161
         }
162
     }
163
164
```

```
inline void link(int v,int w)
165
166
         int s = w;
167
         while (semi[best[w]] < semi[best[child[w]]])</pre>
168
169
              if (size[s]+size[child[child[s]]] >= 2*size[child[s]])
170
                  anc[child[s]] = s,child[s] = child[child[s]];
171
              else size[child[s]] = size[s],s = anc[s] = child[s];
172
         }
173
         best[s] = best[w]; size[v] += size[w];
174
         if (size[v] < 2*size[w]) swap(s,child[v]);</pre>
175
         while (s) anc[s] = v,s = child[s];
176
     }
177
178
     inline void lengauer_tarjan()
179
180
         memset(dfn,0,sizeof dfn); memset(fa,-1,sizeof fa); Ts = 0;
181
         dfs(N); fa[1] = 0;
182
         for (int w = Ts; w > 1; --w)
183
184
              for (auto x:prod[w])
185
              {
186
                  int u = eval(x);
187
                  if (semi[w] > semi[u]) semi[w] = semi[u];
188
              }
189
              bucket[semi[w]].push_back(w);
190
              link(fa[w],w); if (!fa[w]) continue;
191
              for (auto x:bucket[fa[w]])
192
193
                  int u = eval(x);
194
                  if (semi[u] < fa[w]) idom[x] = u;</pre>
195
                  else idom[x] = fa[w];
196
              }
197
              bucket[fa[w]].clear();
198
199
         for (int w = 2; w \le Ts; ++w)
200
              if (idom[w] != semi[w])
201
                  idom[w] = idom[idom[w]];
202
         idom[1] = 0;
203
         for (int i = Ts; i > 1; --i)
204
205
              if (fa[i] == -1) continue;
206
              son[idom[i]].push_back(i);
207
         }
208
     }
209
210
     inline void get_ans(int now)
211
     {
212
         ans[redfn[now]] += redfn[now];
213
```

```
for (auto x:son[now])
214
              ans[redfn[x]] += ans[redfn[now]],get_ans(x);
215
     }
216
217
     int main()
218
219
          //freopen("I.in", "r", stdin);
220
         while (scanf("%d %d", &N, &M) != EOF)
221
222
              init();
223
              for (int i = 1,a,b;i <= M;++i)</pre>
224
                  a = gi(),b = gi(),add(a,b);
225
              lengauer_tarjan(); get_ans(1);
226
              for (int i = 1;i <= N;++i)</pre>
227
                  printf("%d%c",ans[i]," \n"[i == N]);
228
         }
229
         return 0;
230
     }
231
```

4.7 Hungary

```
//匈牙利算法
    //Version1
    inline bool find(int x)
    {
4
        if (cor[x]) return false;
        for (int i = side[x];i;i = next[i]) if (!used[toit[i]])
             used[toit[i]] = true;
             if (!cho[toit[i]]||find(cho[toit[i]]))
             {
10
                 cho[toit[i]] = x; map[x] = toit[i];
11
                  return true;
12
             }
13
        }
14
        return false;
15
    }
16
17
    inline void hungry()
18
19
        for (int i = 1;i <= p;++i)</pre>
20
             memset(used,false,sizeof(used)),find(i);
21
        for (int i = 1;i <= m;++i)</pre>
22
23
             memset(used,false,sizeof(used)),cho[map[i]] = 0;
24
             find(i),cor[i] = true;
25
        }
26
    }
27
    //Version2
```

```
inline int find(int x)
29
30
         for (int i = 1;i <= n;++i)
31
             if (f[x][i]&&!used[i])
32
33
                 used[i] = true;
34
                  if (!cho[i]||find(cho[i])) { cho[i] = x; return true; }
35
36
        return false;
37
    }
38
39
    inline int hungry()
40
41
         int ret = 0;
42
         for (int i = 1;i <= n;++i)
43
44
             memset(used,false,sizeof(used));
45
             if (find(i)) ret++;
46
47
        return ret;
48
    }
49
```

4.8 Isap Algorithm

```
// isap: 有毒
    inline void bfs()
        queue <int> team; memcpy(cur,side,4*(N+1));
        team.push(sink); d[sink] = 1; in[sink] = true;
        while (!team.empty())
            int now = team.front(); team.pop(); nd[d[now]]++;
            for (int i = side[now];i;i = nxt[i])
                 if (cap[i^1] && !in[toit[i]])
10
                     in[toit[i]] = true,d[toit[i]] = d[now]+1,team.push(toit[i]);
11
12
        for (int i = 1;i <= N;++i) if (!in[i]) nd[d[i] = N+1]++;
13
14
    inline int isap()
15
16
        int res = 0,now = source,ca = inf;
17
        bfs();
18
        while (d[source] <= N)</pre>
19
20
            if (now == sink)
21
22
                while (now != source)
23
24
                     cap[pre[now]] -= ca; cap[pre[now]^1] += ca;
25
```

```
now = toit[pre[now]^1];
26
                }
27
                res += ca; ca = inf;
28
            }
29
            bool flag = false; arr[now] = ca;
30
            for (int i = cur[now];i;i = nxt[i])
31
                if (cap[i] &&d[toit[i]] ==d[now] -1)
32
33
                    cur[now] = pre[toit[i]] = i; ca = min(ca,cap[i]);
34
                    now = toit[i]; flag = true; break;
35
36
            if (flag) continue; if (!--nd[d[now]]) break; int arg = N;
37
            for (int i = side[now];i;i = nxt[i])
38
                if (cap[i]&&d[toit[i]] < arg) arg = d[toit[i]];</pre>
39
            ++nd[d[now]=arg+1]; cur[now] = side[now];
40
            if (now != source) ca = arr[now = toit[pre[now]^1]];
41
        }
42
        return res;
43
    }
44
45
                        // 源点
    int source;
46
    int sink;
                         // 汇点
47
                        // 可增广路上的上一条弧的编号
    int p[max_nodes];
48
    int num[max_nodes]; // 和 t 的最短距离等于 i 的节点数量
49
    int cur[max_nodes]; // 当前弧下标
50
    int d[max_nodes]; // 残量网络中节点 i 到汇点 t 的最短距离
    bool visited[max_nodes];
52
53
    // 预处理, 反向 BFS 构造 d 数组
54
    bool bfs()
55
    {
56
        memset(visited, 0, sizeof(visited));
57
        queue<int> Q;
58
        Q.push(sink);
59
        visited[sink] = 1;
60
        d[sink] = 0;
61
        while (!Q.empty()) {
62
            int u = Q.front();
63
            Q.pop();
64
            for (iterator_t ix = G[u].begin(); ix != G[u].end(); ++ix) {
65
                Edge &e = edges[(*ix)^1];
66
                if (!visited[e.from] && e.capacity > e.flow) {
67
                    visited[e.from] = true;
68
                    d[e.from] = d[u] + 1;
69
                    Q.push(e.from);
70
                }
71
            }
72
        }
73
        return visited[source];
74
```

```
}
75
76
    // 增广
77
    int augment()
79
         int u = sink, df = __inf;
 80
         // 从汇点到源点通过 p 追踪增广路径, df 为一路上最小的残量
 81
         while (u != source) {
 82
             Edge &e = edges[p[u]];
 83
             df = min(df, e.capacity - e.flow);
 84
             u = edges[p[u]].from;
 85
         }
 86
         u = sink;
 87
         // 从汇点到源点更新流量
 88
         while (u != source) {
 89
             edges[p[u]].flow += df;
90
             edges[p[u]^1].flow -= df;
91
             u = edges[p[u]].from;
92
93
         return df;
94
    }
95
96
    int max_flow()
97
     {
98
         int flow = 0;
99
         bfs();
100
         memset(num, 0, sizeof(num));
101
         for (int i = 0; i < num_nodes; i++) num[d[i]]++;</pre>
102
         int u = source;
103
         memset(cur, 0, sizeof(cur));
104
         while (d[source] < num_nodes) {</pre>
105
             if (u == sink) {
106
                 flow += augment();
107
                 u = source;
108
109
             bool advanced = false;
110
             for (int i = cur[u]; i < G[u].size(); i++) {</pre>
111
                 Edge& e = edges[G[u][i]];
112
                  if (e.capacity > e.flow && d[u] == d[e.to] + 1) {
113
                      advanced = true;
114
                      p[e.to] = G[u][i];
115
                      cur[u] = i;
116
                      u = e.to;
117
                      break;
118
                 }
119
120
             if (!advanced) { // retreat
121
                 int m = num_nodes - 1;
122
                  for (iterator_t ix = G[u].begin(); ix != G[u].end(); ++ix)
123
```

```
if (edges[*ix].capacity > edges[*ix].flow)
124
                           m = min(m, d[edges[*ix].to]);
125
                  if (--num[d[u]] == 0) break; // gap 优化
126
                  num[d[u] = m+1]++;
127
                  cur[u] = 0;
128
                  if (u != source)
129
                       u = edges[p[u]].from;
130
              }
131
         }
132
         return flow;
133
     }
134
     //By mxh
135
     #define maxn 1010
136
     const int INF=1<<30;</pre>
137
     int n,m;
138
     int S,T;
139
     struct Edge
140
141
         int v,flow,next;
142
          e[510010];
     }
143
     int g[maxn],tot=1;//tot 初值必须赋为 1
144
     void addedge(int x,int y,int flow)
145
     {
146
         e[++tot].v=y;e[tot].flow=flow;e[tot].next=g[x];g[x]=tot;
147
         e[++tot].v=x;e[tot].flow=0;e[tot].next=g[y];g[y]=tot;
148
     }
149
     int w[maxn],hash[maxn],d[maxn];
150
     int que[maxn],pre1[maxn],pre2[maxn],p[maxn];
151
     bool vis[maxn];
152
     int maxflow()
153
     {
154
         for (int i=1;i<=n;i++)</pre>
                                      hash[i]=0,d[i]=0,vis[i]=false;
155
         for (int i=1;i<=n;i++)</pre>
                                      p[i]=g[i];
156
         //hash[0]=n;
157
         int 1,r;
158
         1=r=1;
159
         que[1]=T;hash[0]=1;vis[T]=true;
160
         while (1<=r)
161
         {
162
              int u=que[1++];
163
              for (int i=g[u];i;i=e[i].next)
164
              if ((i&1) && !vis[e[i].v])
165
              {
166
                  que[++r]=e[i].v;
167
                  vis[e[i].v]=true;
168
                  d[e[i].v]=d[u]+1;
169
                  hash[d[e[i].v]]++;
170
              }
171
         }
172
```

```
for (int i=1;i<=n;i++)</pre>
173
                           d[i]=n,hash[n]++;
         if (!vis[i])
174
         int flow=INF;
175
         int ans=0;
176
         int u=S;
177
         while (d[S]<n)
178
          {
179
              w[u]=flow;
180
              bool bo=true;
181
              for (int i=p[u];i;i=e[i].next)
182
              if (e[i].flow && d[e[i].v]==d[u]-1)
183
184
                  flow=min(flow,e[i].flow);
185
                  p[u]=i;
186
                  pre1[e[i].v]=u;
187
                  pre2[e[i].v]=i;
188
                  u=e[i].v;
189
                  bo=false;
190
                   if (u==T)
191
192
                       ans+=flow;
193
                       while (u!=S)
194
                       {
195
                            e[pre2[u]].flow-=flow;
196
                            e[pre2[u]^1].flow+=flow;
197
                            u=pre1[u];
198
                       }
199
                       flow=INF;
200
                  }
201
                  break;
202
203
              if (!bo)
                            continue;
204
              int minx=n,pos=0;
205
              for (int i=g[u];i;i=e[i].next)
206
              if (e[i].flow && d[e[i].v]<minx)
                                                      minx=d[e[i].v],pos=i;
207
              p[u]=pos;
208
              hash[d[u]]--;
209
              if (hash[d[u]]==0)
                                       break;
210
              d[u]=minx+1;
211
              hash[d[u]]++;
212
              if (u!=S)
                             u=pre1[u],flow=w[u];
213
214
215
         return ans;
     }
216
```

4.9 Kuhn-Munkres Algorithm

```
// Truly O(n^3), 最大权匹配
```

^{2 //} 邻接矩阵,不能连的边设为-INF,求最小权匹配时边权取负,但不能连的还是 -INF,使用时先对 1 -> n 调用 hungary(),再

```
struct KM
3
    {
4
         int w[maxn] [maxn], lx[maxn], ly[maxn], match[maxn], way[maxn], slack[maxn];
5
         bool used[maxn];
         inline void init()
         {
             for (int i = 1;i <= N;++i)</pre>
10
                  match[i] = lx[i] = ly[i] = way[i] = 0;
11
         }
12
13
         inline void hungary(int x)
14
15
             match[0] = x; int j0 = 0;
16
             for (int j = 0; j \leftarrow N; ++j)
17
                  slack[j] = inf,used[j] = false;
18
             do
19
             {
20
                  used[j0] = true;
21
                  int i0 = match[j0],delta = inf,j1 = 0;
22
                  for (int j = 1; j \le N; ++j)
23
                      if (!used[j])
24
                       {
25
                           int cur = -w[i0][j]-lx[i0]-ly[j];
26
                           if (cur < slack[j])</pre>
27
                                slack[j] = cur, way[j] = j0;
                           if (slack[j] < delta)</pre>
29
                               delta = slack[j],j1 = j;
30
31
                  for (int j = 0; j \le N; ++j)
32
                  {
33
                       if (used[j]) lx[match[j]] += delta,ly[j] -= delta;
34
                       else slack[j] -= delta;
35
                  }
36
                  j0 = j1;
37
             }
38
             while (match[j0]);
39
             do
40
             {
41
                  int j1 = way[j0];
42
                  match[j0] = match[j1];
43
                  j0 = j1;
44
45
             while (j0);
46
         }
47
48
         inline void work() { for (int i = 1;i <= N;++i) hungary(i); }</pre>
49
50
         inline int get_ans()
51
```

```
{
52
             int sum = 0;
53
             for (int i = 1;i <= N;++i)</pre>
54
55
                  // if (w[match[i]][i] == -inf); //无解
56
                  if (match[i] > 0) sum += w[match[i]][i];
57
58
             return sum;
59
         }
60
    }km;
61
     //最小权匹配
62
     struct KM
63
64
         int w[maxn] [maxn],lx[maxn],ly[maxn],match[maxn],way[maxn],slack[maxn]; bool used[maxn];
65
66
         inline void init()
67
68
             for (int i = 1;i <= N;++i)</pre>
69
                  match[i] = lx[i] = ly[i] = way[i] = 0;
70
         }
71
72
         inline void hungary(int x)
73
         {
74
             match[0] = x; int j0 = 0;
75
             for (int j = 0; j \le N; ++j)
76
                  slack[j] = -inf,used[j] = false;
             do
78
             {
79
                  used[j0] = true;
80
                  int i0 = match[j0],delta = -inf,j1 = 0;
81
                  for (int j = 1; j \le N; ++j)
82
                      if (!used[j])
83
84
                           int cur = -w[i0][j]-lx[i0]-ly[j];
85
                           if (cur > slack[j]) slack[j] = cur,way[j] = j0;
86
                           if (slack[j] > delta) delta = slack[j],j1 = j;
87
88
                  for (int j = 0; j \le N; ++j)
89
                  {
90
                      if (used[j]) lx[match[j]] += delta,ly[j] -= delta;
91
                      else slack[j] -= delta;
92
                  }
93
                  j0 = j1;
94
             }
95
             while (match[j0]);
96
             do
97
             {
98
                  int j1 = way[j0];
99
                  match[j0] = match[j1];
100
```

```
j0 = j1;
101
102
              while (j0);
103
          }
104
105
          inline void work() { for (int i = 1;i <= N;++i) hungary(i); }</pre>
106
107
          inline int get_ans()
108
109
              int sum = 0;
110
              for (int i = 1;i <= N;++i)</pre>
111
112
                   // if (w[match[i]][i] == inf); // 无解
113
                   if (match[i] > 0) sum += w[match[i]][i];
114
115
              return sum;
116
          }
117
     }km;
118
```

4.10 Maximal Matching in General Graphs

```
// 接口 int matching(), 返回最大匹配数,G 为邻接矩阵
    inline void push(int x)
        team.push(x); check[x] = true;
        if (!treec[x]) tra[++cnt] = x,treec[x] = true;
    inline int root(int x) { return f[x]?f[x] = root(f[x]):x; }
    inline void clear()
10
        for (int i = 1,j;i <= cnt;++i)</pre>
11
12
            j = tra[i]; father[j] = 0,f[j] = 0;
13
            check[j] = treec[j] = false;
14
        }
15
    }
16
17
    inline int lca(int u,int v)
18
19
        int len = 0;
20
        for (;u;u = father[match[u]])
21
            pathc[path[++len] = u = root(u)] = true;
22
        for (;;v = father[match[v]])
23
            if (pathc[v = root(v)]) break;
24
        for (int i = 1;i <= len;++i)</pre>
25
            pathc[path[i]] = false;
26
        return v;
27
    }
28
```

```
29
    inline void reset(int u,int p)
30
31
        for (int v;root(u) != p;)
32
33
             if (!check[v = match[u]]) push(v);
34
             if (!f[u]) f[u] = p; if (!f[v]) f[v] = p;
35
             u = father[v]; if (root(u) != p) father[u] = v;
36
        }
37
    }
38
39
    inline void flower(int u,int v)
40
41
        int p = lca(u,v);
42
         if (root(u) != p) father[u] = v;
43
        if (root(v) != p) father[v] = u;
44
        reset(u,p); reset(v,p);
45
    }
46
47
    inline bool find(int x)
48
49
        while (!team.empty()) team.pop();
50
         cnt = 0; push(x);
51
        while (!team.empty())
52
53
             int i = team.front(); team.pop();
54
             for (int j = 1; j \le N; ++j)
55
                 if (G[i][j]&&root(i) != root(j)&&match[j] != i)
56
57
                      if (match[j]&&father[match[j]]) flower(i,j);
58
                      else if (!father[j])
59
                      {
60
                          father[tra[++cnt] = j] = i; treec[j] = true;
61
                          if (match[j]) push(match[j]);
62
                          else
63
                          {
64
                              for (int k = i,l = j,p;k;l = p,k = father[1])
65
                                   p = match[k], match[k] = 1, match[l] = k;
66
                              return true;
67
                          }
68
                     }
69
                 }
70
71
        return false;
72
    }
73
74
    inline int matching()
75
    {
76
        memset(father,0,sizeof father); memset(f,0,sizeof f); memset(path,0,sizeof path);
77
```

```
memset(tra,0,sizeof tra); memset(match,0,sizeof match); memset(check,false,sizeof check);
78
        memset(treec,false,sizeof treec); memset(pathc,false,sizeof pathc);
79
        int ret = cnt = 0;
80
        for (int i = 1;i <= N;++i)
82
            if (match[i]) continue;
83
            if (find(i)) ++ret; clear();
84
85
        return ret;
86
    }
87
```

4.11 Maximal Weighted Matching in General Graphs

```
// 接口 int matching(), 返回最大匹配数,G 为邻接矩阵
    inline void push(int x)
        team.push(x); check[x] = true;
        if (!treec[x]) tra[++cnt] = x,treec[x] = true;
    inline int root(int x) { return f[x]?f[x] = root(f[x]):x; }
    inline void clear()
10
        for (int i = 1,j;i <= cnt;++i)
11
12
            j = tra[i]; father[j] = 0,f[j] = 0;
13
            check[j] = treec[j] = false;
14
        }
15
    }
16
17
    inline int lca(int u,int v)
18
19
        int len = 0;
20
        for (;u;u = father[match[u]])
21
            pathc[path[++len] = u = root(u)] = true;
22
        for (;;v = father[match[v]])
23
            if (pathc[v = root(v)]) break;
24
        for (int i = 1;i <= len;++i)
25
            pathc[path[i]] = false;
        return v;
27
    }
28
29
    inline void reset(int u,int p)
30
31
        for (int v;root(u) != p;)
32
33
            if (!check[v = match[u]]) push(v);
34
            if (!f[u]) f[u] = p; if (!f[v]) f[v] = p;
35
            u = father[v]; if (root(u) != p) father[u] = v;
36
```

```
}
37
    }
38
39
    inline void flower(int u,int v)
40
41
        int p = lca(u,v);
42
         if (root(u) != p) father[u] = v;
43
        if (root(v) != p) father[v] = u;
44
        reset(u,p); reset(v,p);
45
    }
46
47
    inline bool find(int x)
48
49
        while (!team.empty()) team.pop();
50
         cnt = 0; push(x);
51
        while (!team.empty())
52
53
             int i = team.front(); team.pop();
54
             for (int j = 1; j \le N; ++j)
55
                 if (G[i][j]&&root(i) != root(j)&&match[j] != i)
56
                 {
57
                      if (match[j]&&father[match[j]]) flower(i,j);
58
                      else if (!father[j])
59
                      {
60
                          father[tra[++cnt] = j] = i; treec[j] = true;
61
                          if (match[j]) push(match[j]);
62
                          else
63
                          {
64
                              for (int k = i, l = j, p; k; l = p, k = father[1])
65
                                   p = match[k], match[k] = 1, match[l] = k;
66
                              return true;
67
                          }
68
                      }
69
                 }
70
        }
71
        return false;
72
    }
73
74
    inline int matching()
75
    {
76
        memset(father,0,sizeof father); memset(f,0,sizeof f); memset(path,0,sizeof path);
77
        memset(tra,0,sizeof tra); memset(match,0,sizeof match); memset(check,false,sizeof check);
78
        memset(treec,false,sizeof treec); memset(pathc,false,sizeof pathc);
79
        int ret = cnt = 0;
80
        for (int i = 1;i <= N;++i)</pre>
81
82
             if (match[i]) continue;
83
             if (find(i)) ++ret; clear();
84
        }
85
```

```
86 return ret;
87 }
```

4.12 Maximum Cardinality Search

```
// BZOJ 1006
    #include<algorithm>
    #include<queue>
    #include<cstdio>
    #include<cstdlib>
    #include<set>
    using namespace std;
    #define maxn 10010
    #define maxc 510
10
    #define maxm 1000010
11
    int tot,n,m,cnt,color[maxn][maxc],label[maxn],all;
12
    int side[maxn],next[maxm*2],toit[maxm*2],per[maxn];
13
    bool in[maxn];
    struct node
15
16
        int key,ord;
17
        friend bool operator < (node a,node b) {return a.key > b.key; }
18
    };
19
    multiset <node> S;
20
21
    inline void add(int a,int b)
22
23
        next[++cnt] = side[a]; side[a] = cnt; toit[cnt] = b;
24
    }
25
26
    inline void ins(int a,int b){add(a,b); add(b,a);}
27
    inline void mcs()
29
30
        int i,u;
31
        for (i = 1;i <= n;++i) S.insert((node){0,i});</pre>
32
        while (all < n)
33
34
            u = (*S.begin()).ord; S.erase(S.begin()); if (in[u]) continue;
35
            in[u] = true; per[++all] = u;
36
            for (i = side[u];i;i = next[i])
37
                if (!in[toit[i]])
                 {
39
                     label[toit[i]]++;
40
                     S.insert((node){label[toit[i]],toit[i]});
41
                }
42
        }
43
    }
44
```

```
45
    inline void paint()
46
47
        int p,i,j,t;
48
        for (p = 1; p \le n; ++p)
49
50
             i = per[p];
51
             for (j = 1; j \le tot; ++j)
52
                 if (!color[i][j]) {t = j; break; }
53
             if (j == tot + 1) t = ++tot;
54
             for (j = side[i]; j; j = next[j])
55
                 color[toit[j]][t] = true;
56
        }
57
    }
58
59
    int main()
60
61
        freopen("1006.in", "r", stdin);
62
        freopen("1006.out","w",stdout);
63
        scanf("%d %d",&n,&m);
64
        for (int i = 1;i <= m;++i)
65
        { int a,b; scanf("%d %d",&a,&b); ins(a,b); }
66
        mcs();
67
        paint();
        printf("%d",tot);
69
        fclose(stdin); fclose(stdout);
70
        return 0;
71
    }
72
```

4.13 Network Flow with Lower Bound

1. 无源汇有上下界可行流

设原来源点为 Source, 汇点是 Sink。新建一个超级源 SuperSource 和超级汇 SuperSink。对于原网络中的每一条边 $u \rightarrow v$,上界 U,下界 L,将它拆分为三条边:

- (1) $u \to SuperSink$, 容量为 L。
- (2) $SuperSource \rightarrow v$, 容量为 L。
- (3) $u \rightarrow v$, 容量为 U L。

最后添加边 $Sink \to Source$,容量为 $+\infty$ 。在新建的网络上,计算从 SuperSource 到 SuperSink 的最大流。若每条从 SuperSource 发出的边都满流,说明存在可行流,否则不。每条边实际流量为容量下界 + 附加流中它的流量。

2. 有源汇有上下界可行流

在 "无源汇有上下界可行流" 建图上,新增一条 $Sink \to Source$ 的边,容量为 $+\infty$ 即可。

3. 有源汇有上下界最大流

在"有源汇有上下界可行流"建图上,先判断是否存在可行流,若存在可行流,拆掉 $Sink \rightarrow Source$ 的边后,接着在图中 $Source \rightarrow Sink$ 最大流增广加上原可行流即为最大流答案。(若存在可行流,去掉下界后最大流即为原图有源汇有上下界最大流)

4. 有源汇有上下界最小流

在"有源汇有上下界可行流"建图上,先判断是否存在可行流,若存在可行流,拆掉 $Sink \rightarrow Source$ 的边后,用可行流减去在图中 $Sink \rightarrow Source$ 增广的最大流即为最小流答案。

在实现时,可以吧 SuperSource 连向同一节点的多条边合成一条(容量合并。从同一节点指向 SuperSink 的多条边也应合并。

对于费用流,只需要改变将网络流算法改成费用流算法。对于原网络中的每一条边 $u \to v$,上界 U,下界 L,费用 c,将它拆分为三条边:

- (1) $u \to SuperSink$, 容量为 L, 费用 c。
- (2) $SuperSource \rightarrow v$, 容量为 L, 费用 0。
- (3) $u \rightarrow v$, 容量为 U L, 费用 c。

4.14 Point Biconnected Component

```
// Source: HackerRank - bonnie-and-clyde
   #include<algorithm>
   #include<vector>
   #include<stack>
   #include<iostream>
   #include<cstdio>
   #include<cstdlib>
   using namespace std;
   const int maxn = 400010;
10
   int N,M,Q,cnt = 1,side[maxn],toit[maxn],nxt[maxn],f[maxn][25],father[maxn],low[maxn];
11
    int tot,dep[maxn],dfn[maxn],nside[maxn],ntoit[maxn],nnxt[maxn]; bool cut[maxn];
    stack <int> S; vector <int> bel[maxn],bcc[maxn]; bool vis[maxn];
13
14
    inline int find(int a) { if (father[a] != a) father[a] = find(father[a]); return father[a]; }
15
16
    inline void add(int a,int b) { nxt[++cnt] = side[a]; side[a] = cnt; toit[cnt] = b; }
17
    inline void ins(int a,int b) { add(a,b); add(b,a); }
    inline void nadd(int a,int b) { nnxt[++cnt] = nside[a]; nside[a] = cnt; ntoit[cnt] = b; }
19
    inline void nins(int a,int b) { nadd(a,b); nadd(b,a); }
20
21
   inline int gi()
22
23
        char ch; int ret = 0,f = 1;
24
        do ch = getchar(); while (!(ch >= '0'&&ch <= '9')&&ch != '-');
25
        if (ch == '-') f = -1, ch = getchar();
26
        do ret = ret*10+ch-^{\circ}', ch = getchar(); while (ch >= ^{\circ}0'&&ch <= ^{\circ}9');
27
        return ret*f;
```

```
}
29
30
    inline void tj(int now,int fa)
31
    {
32
        dfn[now] = low[now] = ++cnt; int child = 0;
33
        for (int i = side[now];i;i = nxt[i])
34
35
             if (toit[i] == fa) continue;
36
             if (!dfn[toit[i]])
37
             {
38
                 S.push(i>>1); tj(toit[i],now); ++child;
39
                 low[now] = min(low[now],low[toit[i]]);
40
                 if (low[toit[i]] >= dfn[now])
41
42
                      cut[now] = true; ++tot;
43
                      while (true)
44
45
                          int t = S.top(); S.pop();
46
                          bel[toit[t<<1]].push_back(tot);</pre>
                                                                 bel[toit[t<<1|1]].push_back(tot);</pre>
47
                          bcc[tot].push_back(toit[t<<1]); bcc[tot].push_back(toit[t<<1|1]);</pre>
48
                          if (t == (i>>1)) break;
49
                      }
50
                 }
51
52
             else low[now] = min(low[now],dfn[toit[i]]);
53
54
        if (!fa&&child == 1) cut[now] = false;
55
    }
56
57
    inline void build()
58
    {
59
        vector <int> cuts; cnt = 1;
60
        for (int i = 1;i <= tot;++i)</pre>
61
62
             sort(bcc[i].begin(),bcc[i].end());
63
             bcc[i].erase(unique(bcc[i].begin(),bcc[i].end()),bcc[i].end());
64
        }
65
        for (int i = 1;i <= N;++i) if (cut[i]) cuts.push_back(i);</pre>
66
        for (auto x:cuts)
67
         {
68
             sort(bel[x].begin(),bel[x].end());
69
             bel[x].erase(unique(bel[x].begin(),bel[x].end()),bel[x].end());
70
             ++tot; for (auto y:bel[x]) nins(tot,y);
71
             bel[x].clear(); bel[x].push_back(tot); bcc[tot].push_back(x);
72
        }
73
    }
74
75
    inline void dfs(int now)
76
    {
77
```

```
vis[now] = true;
78
         for (int i = 1;(1<<i) <= dep[now];++i) f[now][i] = f[f[now][i-1]][i-1];
79
         for (int i = nside[now];i;i = nnxt[i])
80
         {
81
             if (vis[ntoit[i]]) continue; f[ntoit[i]][0] = now;
82
             dep[ntoit[i]] = dep[now]+1; dfs(ntoit[i]);
83
         }
84
    }
85
86
    inline int jump(int a, int b) { for (int i = 0; b; ++i, b >>= 1) if (b\&1) a = f[a][i]; return a; }
87
    inline int lca(int a,int b)
88
    {
89
         if (dep[a] < dep[b]) swap(a,b);</pre>
90
         a = jump(a,dep[a]-dep[b]); if (a == b) return a;
91
         for (int i = 0;i >= 0;)
92
93
             if (f[a][i] != f[b][i]) a = f[a][i],b = f[b][i],++i;
94
             else --i;
95
         }
96
         return f[a][0];
97
    }
98
99
    inline bool check(int u,int v,int w)
100
    {
101
         if (find(u) != find(v) | |find(v) != find(w)) return false;
102
         if (u == w | | v == w) return true; if (u == v) return false;
103
         int uu = bel[u][0],vv = bel[v][0],ww = bel[w][0],su,sv;
104
         if (uu == ww||vv == ww) return true;
105
         if (lca(uu,ww) == ww) su = jump(uu,dep[uu]-dep[ww]-1); else su = f[ww][0];
106
         if (lca(vv,ww) == ww) sv = jump(vv,dep[vv]-dep[ww]-1); else sv = f[ww][0];
107
         if (su == sv)
108
         {
109
             if (!cut[w]) return false;
110
             else
111
             {
112
                 if (su == uu||sv == vv) return true; int ssu,ssv;
113
                 if (lca(su,uu) == su) ssu = jump(uu,dep[uu]-dep[su]-1); else ssu = f[su][0];
114
                 if (lca(sv,vv) == sv) ssv = jump(vv,dep[vv]-dep[sv]-1); else ssv = f[sv][0];
115
                 if (ssu == ssv) return false; else return true;
116
             }
117
         }
118
         else return true;
119
    }
120
121
    int main()
122
123
         freopen("J.in", "r", stdin);
124
         freopen("J.out","w",stdout);
125
         N = gi(); M = gi(); Q = gi();
126
```

4.15. STEINER TREE

```
for (int i = 1;i <= N;++i) father[i] = i;</pre>
127
         for (int i = 1,a,b;i <= M;++i)</pre>
128
129
              ins(a = gi(),b = gi());
130
              a = find(a),b = find(b);
131
              if (a != b) father[a] = b;
132
133
         cnt = 0; for (int i = 1;i <= N;++i) if (!dfn[i]) tj(i,0);</pre>
134
         build(); for (int i = 1;i <= N;++i) if (!vis[i]) dfs(i);
135
         while (Q--)
136
         {
137
              int u = gi(), v = gi(), w = gi();
138
              if (check(u,v,w)) puts("YES"); else puts("NO");
139
140
141
         return 0;
     }
142
```

4.15 Steiner Tree

```
* Steiner Tree: 求, 使得指定 K 个点连通的生成树的最小总权值
    * st[i] 表示顶点 i 的标记值,如果 i 是指定集合内第 m(O<=m<K) 个点,则 st[i]=1<<m
    * endSt=1<<K
      dptree[i][state] 表示以 i 为根,连通状态为 state 的生成树值
    */
   inline void update(int &x,int y) { if (x == -1) x = y; else if (x > y) x = y; }
   inline void spfa(int state)
9
       while (!team.empty())
10
       {
11
          int now = team.front(); team.pop();
12
          for (int i = side[now];i;i = nxt[i])
13
          {
14
              int v = toit[i];
15
              16
              {
17
                  f[v][st[v]|state] = f[now][state]+len[i];
18
                  if ((st[v]|state) != state||vis[v][state]) continue;
19
                  vis[v][state] = true; team.push(v);
20
              }
21
22
          vis[now][state] = false;
23
       }
24
   }
25
   inline int work()
26
   {
27
       endSt = 1<<(K<<1);
28
       memset(f,-1,sizeof(f)); memset(st,0,sizeof(st)); memset(dp,-1,sizeof(dp));
29
       memset(vis,false,sizeof(vis)); memset(side,0,sizeof(side));
30
```

```
for (int i = 1;i <= K;++i) st[i] = 1<<(i-1);
31
         for (int i = 1;i <= K;++i) st[N-K+i] = 1<<(i+K-1);</pre>
32
         for (int i = 1;i <= N;++i) f[i][st[i]] = 0;</pre>
33
         for (int j = 1; j < endSt; ++j)
34
35
             for (int i = 1;i <= N;++i)
36
             {
37
                  if (!st[i]||(st[i]&j))
                      for (int sub = (j-1)\&j; sub; sub = (sub-1)\&j)
39
40
                           int x = sub|st[i],y = (j-sub)|st[i];
41
                           if (f[i][x] != -1 \&\&f[i][y] != -1)
42
                               update(f[i][j],f[i][x]+f[i][y]);
43
44
                  if (f[i][j] != -1) team.push(i),vis[i][j] = true;
45
46
             spfa(j);
47
         }
48
    }
49
```

4.16 Stoer Wagner Algorithm

```
int G[maxn] [maxn], node [maxn], dis[maxn]; bool visit[maxn];
    inline int solve(int n)
        if (n == 1) return inf;
        int answer = inf;
        for (int i = 0;i < n;++i) node[i] = i;</pre>
        while (n > 1)
        {
            int mx = 1;
10
            for (int i = 0; i < n; ++i)
            {
12
                 dis[node[i]] = G[node[0]][node[i]];
13
                 if (dis[node[i]] > dis[node[mx]]) mx = i;
14
            }
15
            int prev = 0;
16
            memset(visit,false,sizeof visit);
            visit[node[0]] = true;
18
            for (int i = 1; i < n; ++i)
19
20
                 if (i == n-1)
22
                     answer = min(answer,dis[node[mx]]);
23
                     for (int k = 0; k < n; ++k)
24
                         G[node[k]][node[prev]] = (G[node[prev]][node[k]] += G[node[k]][node[mx]]);
25
                     node[mx] = node[--n];
26
                 }
27
```

```
visit[node[mx]] = true; prev = mx; mx = -1;
28
                 for (int j = 1; j < n; ++j)
29
                      if (!visit[node[j]])
30
                      {
31
                          dis[node[j]] += G[node[prev]][node[j]];
32
                           if (mx == -1 | dis[node[mx]] < dis[node[j]]) mx = j;
33
                      }
34
             }
35
         }
36
         return answer;
37
    }
38
```

4.17 Strongly Connected Component

```
int dfn[maxn],low[maxn],timestamp;
   stack <int> stk; vector <int> scc[maxn];
   void tarjan(int now)
        dfn[now] = low[now] = ++timestamp;
        stk.push(now);
        for (int i = side[now];i;i = nxt[i])
            if (!dfn[toit[i]])
                tarjan(toit[i]),low[now] = min(low[now],low[toit[i]]);
            else if (!bel[toit[i]]) low[now] = min(low[now],dfn[toit[i]]);
        }
13
        if (dfn[now] == low[now])
            ++tot;
            while (stk.top() != now)
16
                scc[tot].push_back(stk.top());
                bel[stk.top()] = tot; stk.pop();
20
            scc[tot].push_back(stk.top());
21
            bel[stk.top()] = tot; stk.pop();
23
   }
24
```

4.18 Virtual Tree

```
inline void nadd(int a,int b,int idc)
9
        if (a == b) return;
10
        if (last[a] != idc) side[a] = 0,last[a] = idc;
11
        if (last[b] != idc) side[b] = 0,last[b] = idc;
12
        nxt[++cnt] = side[a]; side[a] = cnt; toit[cnt] = b;
13
    }
14
15
    inline bool cmp(int a,int b) { return dfn[a] < dfn[b]; }</pre>
16
17
    inline void dfs(int now)
18
    {
19
        dfn[now] = ++timestamp;
20
        for (int i = 1; (1<<i) <= dep[now]; ++i)
21
             f[now][i] = f[f[now][i-1]][i-1];
22
        for (int i = side[now];i;i = nxt[i])
23
             if (toit[i] != f[now][0])
24
             {
25
                 best[toit[i]] = min(best[now],(ll)cost[i]);
26
                 dep[toit[i]] = dep[now]+1;
27
                 f[toit[i]][0] = now; dfs(toit[i]);
28
             }
29
    }
30
31
    inline int jump(int a,int step) { for (int i = 0; step; step >>= 1,++i) if (step&1) a = f[a][i];
32

    return a; }

    inline int lca(int a,int b)
33
34
        if (dep[a] < dep[b]) swap(a,b);</pre>
35
        a = jump(a,dep[a]-dep[b]);
36
        if (a == b) return a;
37
        for (int i = 0;i >= 0;)
38
39
             if (f[a][i] != f[b][i])
40
                 a = f[a][i], b = f[b][i], ++i;
41
             else --i;
42
        }
43
        return f[a][0];
44
    }
45
46
    inline void work(int idc)
47
    {
48
        cnt = 0; int K = gi(),tot,top;
49
        for (int i = 1;i <= K;++i) H[i] = gi();
50
        sort(H+1,H+K+1,cmp); H[tot = 1] = H[1];
51
        for (int i = 2;i <= K;++i) if (lca(H[tot],H[i]) != H[tot]) H[++tot] = H[i];</pre>
52
        stk[top = 1] = 1;
53
        for (int i = 1;i <= tot;++i)</pre>
54
55
```

```
int ans = lca(H[i],stk[top]);
56
            while (true)
57
            {
58
                 if (dep[ans] >= dep[stk[top-1]]) { nadd(ans,stk[top--],idc); break; }
                nadd(stk[top-1],stk[top],idc); --top;
60
            }
61
            if (stk[top] != ans) stk[++top] = ans;
62
            if (stk[top] != H[i]) stk[++top] = H[i];
63
        }
64
        while (--top) nadd(stk[top],stk[top+1],idc);
65
        // dp(1); printf("%lld\n",g[1]);
66
    }
67
```

4.19 Zhu-Liu Algorithm

```
struct Directed_MT
    {
2
        struct Edge
3
        {
4
            int u,v,w;
5
            inline Edge() = default;
            inline Edge(int _u,int _v,int _w):u(_u),v(_v),w(_w) {}
        int n,m,vis[maxn],pre[maxn],id[maxn],in[maxn]; Edge edges[maxm];
10
        inline void init(int _n) { n = _n; m = 0; }
11
        inline void AddEdge(int u,int v,int w) { edges[m++] = Edge(u,v,w); }
12
        inline int work(int root)
13
14
            int ret = 0;
15
            while (true)
16
17
                // 初始化
                for (int i = 0;i < n;++i) in[i] = inf+1;</pre>
19
                for (int i = 0;i < m;++i)</pre>
21
                    int u = edges[i].u,v = edges[i].v;
22
                    // 找寻最小入边, 删除自环
23
                    if (edges[i].w < in[v] \&\&u != v)
24
                        in[v] = edges[i].w,pre[v] = u;
25
                }
26
                // 如果没有最小入边,表示该点不连通,则最小树形图形成失败
27
                for (int i = 0; i < n; ++i)
29
                    if (i == root) continue;
30
                    if (in[i] == inf+1) return inf;
31
                }
32
                int cnt = 0; // 记录缩点
33
                memset(id,-1,sizeof id); memset(vis,-1,sizeof vis);
34
```

```
in[root] = 0;
35
               for (int i = 0; i < n; ++i)
36
37
                   ret += in[i]; int v = i;
38
                    // 找寻自环
39
                   while (vis[v] != i&&id[v] == -1&&v != root)
40
                        vis[v] = i, v = pre[v];
41
                    if (v != root&&id[v] == -1)
42
43
                        // 这里不能从 i 开始找, 因为 i 有可能不在自环内
44
                       for (int u = pre[v];u != v;u = pre[u]) id[u] = cnt;
45
                        id[v] = cnt++;
46
                   }
47
               }
48
               // 如果没有自环了,表示最小树形图成功了
49
               if (!cnt) break;
50
               // 找到那些不是自环的, 重新给那些点进行标记
51
               for (int i = 0; i < n; ++i)
52
                    if (id[i] == -1) id[i] = cnt++;
53
               for (int i = 0;i < m;++i)
54
55
                    int u = edges[i].u,v = edges[i].v;
56
                    edges[i].v = id[v]; edges[i].u = id[u];
57
                    if (id[u] != id[v]) edges[i].w -= in[v];
58
               }
59
                // 缩点完后,点的数量就变了
60
               n = cnt; root = id[root];
61
            }
62
            return ret;
63
        }
64
   }MT:
65
```

4.20 ZKW Cost Flow

```
// To be written
   bool spfa()
   {
3
        memset(mark,0,sizeof(mark));
4
        memset(d,0x7,sizeof(d));
        d[T] = 0; mark[T] = 1;
        queue <int> team;
        team.push(T);
        while (!team.empty())
10
            int now = team.front();
11
            team.pop();
12
            for (int i = head[now];i;i = e[i].next)
13
                if (e[i^1].v\&\&d[e[i].to] > d[now]-e[i].c)
14
                {
15
```

```
d[e[i].to] = d[now]-e[i].c;
16
                      if (!mark[e[i].to])
17
                      {
18
                          mark[e[i].to] = true;
19
                          team.push(e[i].to);
20
                      }
21
22
             mark[now] = false;
23
         }
24
         if (d[0] > 10000000) return false;
25
         return true;
26
    }
27
28
    int dfs(int x,int f)
29
    {
30
        if (x == T)
31
32
             mark[T] = 1;
33
             return f;
34
        }
35
        int used = 0,w;
36
        mark[x] = true;
37
        for (int i = head[x];i;i = e[i].next)
38
             if (!mark[e[i].to]\&\&e[i].v\&\&d[x]-e[i].c==d[e[i].to])
39
40
                 w = f - used;
41
                 w = dfs(e[i].to,small(e[i].v,w));
42
                 ans += w*e[i].c;
43
                 e[i].v -= w;
44
                 e[i^1].v += w;
45
                 used += w;
46
                 if (used == f) return f;
47
             }
48
        return used;
49
    }
50
51
    void zkw()
52
53
         while (spfa())
54
         {
55
             mark[T] = 1;
56
             while (mark[T])
57
             {
58
                 memset(mark,0,sizeof(mark));
                 dfs(0,inf);
60
             }
61
         }
62
    }
63
```

Chapter 5

Number Theory

5.1 Baby Step Giant Step

```
// To Be Verified
   // 求出最小的 t 使得 X^{-}t = Y \mod mod
   inline int bsgs(int X,int Y,int mod)
        int m = ceil(sqrt(mod+0.5)),mul = 1,res = 1;
        if (Y == 1) return 0;
        hash.clear(); hash[Y] = 0;
        for (int i = 1;i <= m;++i)</pre>
            mul = ((11)mul*(11)X)%mod;
            if (mul == Y) return i;
            hash[(11)Y*(11)mul\%mod] = i;
12
13
        res = mul;
14
        for (int i = 2; (i-1)*m <= mod; ++i)
16
            res = (11)res*(11)mul%mod;
            if (hash.find(res) != hash.end()) return i*m-hash[res];
18
        return -1;
20
   }
21
```

5.2 Chinese Remainder Theorem

```
1 //快速乘
2 inline ll qsc(ll a,ll b,ll mod)
3 {
4     ll ret = 0; a %= mod,b %= mod;
5     for (;b;b >>= 1)
6     {
7         if (b&1)
8     {
```

```
ret += a;
9
                 if (ret >= mod) ret -= mod;
10
11
             a += a; if (a >= mod) a -= mod;
12
13
        return ret;
14
    }
15
16
    inline 11 msm(11 a,11 b,11 mod)
17
18
        11 \text{ ret} = 1;
19
        for (;b;b >>= 1,a = qsc(a,a,mod)) if (b%1) ret = qsc(ret,a,mod);
20
        return ret;
21
    }
22
23
    inline 11 crt()
24
25
        11 lcm = 1,ret = 0;
26
        for (int i = 1;i <= K;++i) lcm *= (ll)P[i];
27
        for (int i = 1;i <= K;++i)
28
29
             11 tm = lcm/P[i];
30
             11 inv = msm(tm,P[i]-2,P[i]);
31
             ret = (ret+qsj(qsj(tm,inv,lcm),res[i],lcm))%lcm;
32
        }
33
        return ret;
34
    }
35
```

Extended Euclidean Algorithm

```
//By yxj
   inline ll exgcd(ll a, ll b, ll c) //ax mod b = c
3
        if (a == 0) return -1;
        else if (c \% a == 0) return c/a;
        11 t = exgcd(b \% a,a,((-c \% a)+a)\%a);
        if (t == -1) return -1;
        return (t*b+c)/a;
   }
10
   //Input:a,b,&x,&y,ax+by = gcd(a,b)
11
   //Output:gcd(a,b)
12
   inline int exgcd(int a,int b,int &x,int &y)
13
14
        if (!b) { x = 1,y = 0; return a; }
15
        else
16
        {
17
            int r = exgcd(b,a%b,y,x);
18
            y = x*(a/b); return r;
```

19

```
20 }
```

5.4 Linearly Sieve

```
//欧拉函数
   inline void ready()
        phi[1] = 1;
        for (int i = 2;i < maxn;++i)</pre>
            if (!exist[i]) phi[i] = i-1,prime[++tot] = i;
            for (int j = 1; j \le tot; ++j)
                if (i*prime[j] >= maxn) break;
10
                exist[i*prime[j]] = true;
                if (i % prime[j] == 0)
12
                     { phi[i*prime[j]] = phi[i]*prime[j]; break; }
                else phi[i*prime[j]] = phi[i]*phi[prime[j]];
        }
   }
    //莫比乌斯函数
    inline void ready()
19
        mu[1] = 1;
21
        for (int i = 2; i \le 50000; ++i)
22
23
            if (!exist[i]) { prime[++tot] = i; mu[i] = -1; }
            for (int j = 1; j \le tot \&\&prime[j]*i \le 50000; ++j)
25
26
                exist[i*prime[j]] = true;
                if (i % prime[j] == 0) { mu[i*prime[j]] = 0; break; }
                mu[i*prime[j]] = -mu[i];
29
            }
30
        }
   }
```

5.5 N-Power Residue

```
//Input:p,N,a p is a prime
//Output:the solutions to equation x^N=a(mod p) in [O,p-1]
inline vector <int> residue(int p,int N,int a)
{
   int g = PrimitiveRoot(p); ll m = bsgs(g,a,p);
   vector <int> ret;
   if (!a) { ret.push_back(0); return ret; }
   if (m == -1) return ret;
}
A = N,B = p-1,C = m,x,y,d = exgcd(A,B,x,y);
```

```
if (C % d) return ret;
10
        x *= (C / d)\%B;
11
        11 delta = B / d;
12
        for (int i = 0; i < d; ++i)
13
14
             x += delta; if (x >= B) x -= B;
15
             ret.push_back((int)qsm(g,x,p));
16
17
        sort(ret.begin(),ret.end());
18
        ret.erase(unique(ret.begin(),ret.end()),ret.end());
19
        return ret;
20
    }
21
```

5.6 Number Theoretic Transformation

```
// The First Version
    struct node
        int a[maxn*2],len;
        inline void NTT(int loglen,int len,int on)
5
            for (int i = 0,j,t,p;i < len;++i)
            {
                 for (j = 0,t = i,p = 0;j < loglen;++j,t >>= 1)
                     p <<= 1,p |= t&1;
10
                 if (p > i) swap(a[p],a[i]);
11
            }
12
            for (int s = 1,k = 2;s <= loglen;++s,k <<= 1)
13
14
                 int wn; if (on) wn = e[s]; else wn = ine[s];
15
                 for (int i = 0;i < len;i += k)</pre>
16
17
                     int w = 1;
18
                     for (int j = 0; j < (k >> 1); ++j, w = (ll)wn*w%rhl)
19
20
                          int u = a[i+j],v = (ll)w*a[i+j+(k>>1)]%rhl;
21
                          a[i+j] = u+v; if (a[i+j] >= rhl) a[i+j] -= rhl;
22
                          a[i+j+(k>>1)] = u-v;
23
                          if (a[i+j+(k>>1)] < 0) a[i+j+(k>>1)] += rhl;
24
                     }
25
                 }
26
27
            if (!on)
28
            {
29
                 int inv = qsm(len,rhl-2,rhl);
30
                 for (int i = 0;i < len;++i) a[i] = (ll)a[i]*inv%rhl;</pre>
31
            }
32
        }
33
        friend inline bool operator *(node x,node y)
34
```

```
{
35
             int loglen = 0,len;
36
             for (;(1<<loglen)<x.len+y.len;++loglen); len = 1<<loglen;</pre>
37
             x.NTT(loglen,len,1); y.NTT(loglen,len,1);
38
             for (int i = 0;i < (1<<loglen);++i) x.a[i] = (11)x.a[i]*y.a[i]%rhl;</pre>
39
             x.NTT(loglen,len,0);
40
        }
41
    };
42
43
    int main()
44
    {
45
        for (int i = 1; i < 20; ++i)
46
             e[i] = qsm(gg,(rhl-1)>>i,rhl),ine[i] = qsm(e[i],rhl-2,rhl);
47
    }
48
49
    // The Second Version
50
    typedef long long 11;
51
    ll e[20], ine[20];
52
53
    inline ll qsm(ll a,int b,int c)
54
55
        11 \text{ ret} = 1;
56
        for (;b;b >>= 1,(a *= a) %= c) if (b&1) (ret *= a) %= c;
57
        return ret;
58
    }
59
60
    inline void NTT(ll *a,int loglen,int len,int on)
61
62
        for (int i = 0, j, t, p; i < len; ++i)
63
64
             for (j = 0,t = i,p = 0;j < loglen;++j,t >>= 1)
65
                 p <<= 1,p |= t&1;
66
             if (p > i) swap(a[p],a[i]);
67
68
        for (int s = 1,k = 2;s <= loglen;++s,k <<= 1)
69
70
             int wn; if (on) wn = e[s]; else wn = ine[s];
71
             for (int i = 0; i < len; i += k)
72
             {
73
                 int w = 1;
74
                 for (int j = 0; j < (k >> 1); ++j, w = (ll)wn*w%lhh)
75
                 {
76
                      int u = a[i+j], v = (ll)w*a[i+j+(k>>1)]%lhh;
77
                      a[i+j] = u+v; if (a[i+j] >= lhh) a[i+j] -= lhh;
78
                      a[i+j+(k>>1)] = u-v;
79
                      if (a[i+j+(k>>1)] < 0) a[i+j+(k>>1)] += lhh;
80
81
             }
82
        }
83
```

```
if (!on)
84
         {
85
             int inv = qsm(len,lhh-2,lhh);
86
             for (int i = 0;i < len;++i) a[i] = a[i]*inv%lhh;</pre>
87
         }
88
    }
89
90
     struct Polynomial
91
92
         int len; ll array[maxn<<2];</pre>
93
         inline Polynomial(int _len = 0):len(_len) {}
94
         inline Polynomial(ll a[],int n):len(n) { for (int i = 0; i < n; ++i) array[i] = a[i]; }</pre>
95
         inline ll operator [](int n) const { return array[n]; }
96
         inline ll &operator [](int n) { return array[n]; }
97
         inline void set(int n) { len = n; }
98
         inline void set(int n,ll a[]) { len = n; for (int i = 0; i < n; ++i) array[i] = a[i]; }
99
         inline void extend(int key)
100
101
             for (int i = len;i < (1<<key);++i)</pre>
102
                  array[i] = 0;
103
         }
104
         inline void cut(int key) { len = key; }
105
         inline void transform(int loglen,int on) { NTT(array,loglen,1<<loglen,on); }</pre>
106
     }; //变量只能定义在全局, 不然会 re
107
108
     inline Polynomial multiply(Polynomial &pa,Polynomial &ret) // self-multiply
109
     {
110
         int loglen = 0;
111
         while ((1<<loglen) < (pa.len<<1)-1) ++loglen;
112
         pa.extend(1<<loglen); pa.transform(loglen,1);</pre>
113
         for (int i = 0;i < (1<<loglen);++i) ret[i] = pa[i]*pa[i]%lhh;</pre>
114
         ret.transform(loglen,0); ret.cut((pa.len<<1)-1);</pre>
115
         return ret;
116
    }
117
     inline Polynomial multiply(Polynomial &pa,Polynomial &pb,Polynomial &ret)
118
119
         int loglen = 0;
120
         while ((1<<loglen) < (pa.len+pb.len-1)) ++loglen;
121
         pa.extend(1<<loglen); pa.transform(loglen,1);</pre>
122
         pb.extend(1<<loglen); pb.transform(loglen,1);</pre>
123
         for (int i = 0;i < (1<<loglen);++i) ret[i] = pa[i]*pb[i]%lhh;</pre>
124
         ret.transform(loglen,0); ret.cut(pa.len+pb.len-1);
125
         return ret;
126
    }
127
128
    int main()
129
     {
130
         for (int i = 1; i < 20; ++i)
131
             e[i] = qsm(g,(lhh-1)>>i,lhh),ine[i] = qsm(e[i],lhh-2,lhh);
132
```

133 }

5.7 Pollard Rho Algorithm

```
const int prime[] = {0,2,3,5,7,11,13,17,19,23,29,31};
    inline 11 mul(11 a,11 b,11 p) { return (a*b-((11)((1d)a/p*b+1e-3)*p)+p)%p; }
    inline bool check(ll m)
        if (m <= 2) return m == 2;</pre>
        11 tmp = m-1; int t = 0;
        while (!(tmp&1)) ++t,tmp >>= 1;
        for (int i = 1;i <= 10;++i)
10
11
             int a = prime[i];
12
             if (a == m) return true;
13
             ll w = qsm(a,tmp,m);
14
             for (int it = 1;it <= t;++it)</pre>
15
16
                 11 pf = mul(w,w,m);
17
                 if (pf == 1\&\&(w != 1\&\&w != m-1)) return false;
18
                 w = pf;
19
20
             if (w != 1) return false;
21
22
        return true;
23
    }
24
    inline void rho(ll m)
25
26
        if (check(m)) { fac[++nn] = m; return; }
27
        while (true)
28
             11 X = (11) rand() * rand() % (m-1) + 1, Y = X;
30
             11 c = (11)rand()*rand()%(m-1)+1; int i,j;
31
             for (i = j = 2;;++i)
32
33
                 X = (mul(X,X,m)+c) \% m;
34
                 11 d = \_gcd(abs(X-Y),m);
35
                 if (1 < d \& \& d < m) \{ rho(d), rho(m/d); return; }
36
                 if (X == Y) break; if (i == j) Y = X, j <<= 1;
37
38
        }
39
40
    inline void factor(ll m) { nn = 0; if (m > 1) rho(m); sort(fac+1,fac+nn+1); }
41
42
43
    //_int128 Version
44
    typedef __int128 int128;
```

```
inline int128 mul(int128 a,int128 b,int128 mod)
46
47
        int128 ret = 0; a %= mod,b %= mod;
48
        for (;b;b >>= 1)
49
50
             if (b&1)
51
             {
52
                 ret += a;
53
                 if (ret >= mod) ret -= mod;
54
55
             a += a; if (a >= mod) a -= mod;
56
        }
57
        return ret;
58
    }
59
60
    inline int128 qsm(int128 a,int128 b,int128 mod)
61
62
        int128 ret = 1;
63
        for (;b;b >>= 1,a = mul(a,a,mod)) if (b&1) ret = mul(ret,a,mod);
64
        return ret;
65
    }
66
67
    inline void ready()
68
69
        for (int i = 2; i \le 100; ++i)
70
71
             if (prime[i]) continue; prime[++tot] = i;
72
             for (int j = i*i; j \le 100; j += i) prime[j] = 1;
73
        }
74
    }
75
76
    inline int128 gi()
77
78
        int128 ret = 0; char ch;
79
        do ch = getchar(); while (!(ch >= '0'&&ch <= '9'));
80
        do ret = ret*10+ch-'0',ch = getchar(); while (ch >= '0'&&ch <= '9');
81
        return ret;
82
    }
83
84
    inline int128 gcd(int128 a,int128 b) { if (b == 0) return a; return gcd(b,a%b); }
85
86
    inline int128 Abs(int128 a) { if (a < 0) return -a; return a; }</pre>
87
88
    inline bool check(int128 m)
89
90
        if (m <= 2) return m == 2;</pre>
91
        int128 tmp = m-1; int t = 0;
92
        while (!(tmp\&1)) ++t,tmp >>= 1;
93
        for (int i = 1;i <= tot;++i)</pre>
94
```

```
{
95
              int a = prime[i];
96
              if (a == m) return true;
97
              int128 w = qsm(a,tmp,m);
98
              for (int it = 1;it <= t;++it)</pre>
99
100
                  int128 pf = mul(w,w,m);
101
                  if (pf == 1\&\&(w != 1\&\&w != m-1)) return false;
102
                  w = pf;
103
              }
104
              if (w != 1) return false;
105
         }
106
         return true;
107
     }
108
     inline void rho(int128 m)
109
110
         if (check(m)) { fac[++nn] = m; return; }
111
         while (true)
112
113
              int128 X = (int128)rand()*(int128)rand()%(m-1)+1,Y = X;
114
              int128 c = (int128)rand()*(int128)rand()%(m-1)+1; int i,j;
115
              for (i = j = 2;;++i)
116
              {
117
                  X = (mul(X,X,m)+c)\%m;
118
                  int128 d = gcd(Abs(X-Y),m);
119
                  if (1 < d \& \& d < m) \{ rho(d), rho(m/d); return; }
120
                  if (X == Y) break; if (i == j) Y = X, j <<= 1;
121
              }
122
         }
123
     }
124
125
     inline void factor(int128 m) { nn = 0; if (m > 1) rho(m); sort(fac+1,fac+nn+1); }
126
```

5.8 Primitive Root

```
_{1} //Input:A prime p
   //Output:p's primitive root
    vector <11> a;
    inline g_test(ll g,ll p)
5
    {
6
        for (ll i = a.size()-1;i >= 0;--i)
            if (qsm(g,(p-1)/a[i],p) == 1) return 0;
        return 1;
9
    }
10
11
    inline 11 PrimitiveRoot(11 p)
12
13
        11 \text{ tmp} = p - 1;
14
```

```
for (11 i = 2; i \le tmp/i; ++i)
15
16
             if (!(tmp % i))
17
             {
                 a.push_back(i);
19
                 while (!(tmp\%i)) tmp /= i;
20
21
             if (tmp != 1) a.push_back(tmp);
22
        }
23
        for (ll g = 1;;++g) if (g_test(g,p)) return g;
24
    }
25
```

5.9 Quadratic Residue

```
//判断是否存在 x, 使得 x^2=a \mod n, 存在返回最小 x, 否则返回-1
    inline int modsqr(int a,int n)
        int b,k,i,x;
        if (n == 2) return a & 1;
        if (qsm(a,(n-1)>>1,n) == 1)
            if (n \% 4 == 3) x = qsm(a,(n+1)>>2,n);
            else
10
                for (b = 1; qsm(b, (n-1)>>1, n) == 1; ++b);
                i = (n-1) >> 1; k = 0;
12
13
                do
14
                    i >>= 1,k >>= 1;
                    if (!((qsm(a,i,n)*(ll)qsm(b,k,n)+1)%n)) k += ((n-1)>>1);
16
                while (!(i&1));
                x = (qsm(a,(i+1)>>1,n)*(11)qsm(b,k>>1,n)) % n;
            }
20
            if ((x << 1) > n) x = n-x;
21
            return x;
23
        return -1;
24
   }
25
```

5.10 Single Variable Modulus Linear Equation

```
//Input:a,b,n
//Output:All the solutions in [0,n) to the equation ax=b(mod n)
inline vector <1l> LineModEquation(ll a,ll b,ll n)
{
    ll x,y,d = exgcd(a,n,x,y); vector <1l> ans;
    if (!(b % d))
}
```

Chapter 6

Numerical Algorithms

6.1 Counting Integral Points under Straight Line

```
1  //\sum_{{i = 0}^{n-1} (a+bi)/m}
2  inline ll count(ll n,ll a,ll b,ll m)
3  {
4    if (!b) return n*(a/m);
5    else if (a >= m) return n*(a/m)+count(n,a%m,b,m);
6    else if (b >= m) return (n-1)*n/2*(b/m)+count(n,a,b%m,m);
7    else return count((a+b*n)/m,(a+b*n)%m,m,b);
8  }
```

6.2 Evaluation of Expression

```
#include<bitset>
   #include<stack>
   #include<iostream>
   #include<cstdio>
   #include<cstdlib>
    using namespace std;
   const int maxn = 200010;
    int T,N,M,pri[256],match[maxn]; bitset <maxn> A,B; char s[maxn];
10
   inline int gi()
11
12
        char ch; int ret = 0,f = 1;
13
        do ch = getchar(); while (!(ch >= '0'&&ch <= '9')&&ch != '-');
14
        if (ch == '-') f = -1,ch = getchar();
15
        do ret = ret*10+ch-'0', ch = getchar(); while (ch >= '0'&&ch <= '9');
16
        return ret*f;
17
18
19
   inline bitset <maxn> calc(int 1,int r)
20
    {
21
```

```
if (1 > r) return bitset <maxn>();
22
        while (match[1] == r) ++1,r--;
23
        if (1 == r) \{ if (s[1] == 'A') return A; else return B; \}
24
        int cur = 0; pair <int,int> mn(1<<30,0);</pre>
25
        for (int i = 1;i <= r;++i)
26
27
             if (s[i] == '(') cur += 10;
28
             else if (s[i] == '|)') cur -= 10;
             else if (pri[s[i]])
30
                 if (make_pair(cur+pri[s[i]],i) < mn)</pre>
                     mn = make_pair(cur+pri[s[i]],i);
32
        }
        int pos = mn.second; auto L = calc(1,pos-1),R = calc(pos+1,r);
34
        if (s[pos] == '+') return L|R;
        else if (s[pos] == '*') return L&R;
36
        else return ~R;
    }
38
40
    int main()
    {
41
        freopen("H.in", "r", stdin);
42
        freopen("H.out","w",stdout);
43
        pri['+'] = 1; pri['*'] = 2; pri['-'] = 3;
        while (++T)
45
             N = gi(), M = gi(); if (!N) break;
             A.reset(); B.reset(); printf("Case %d: ",T);
             for (int K = gi();K--;) A[gi()] = 1;
             for (int K = gi();K--;) B[gi()] = 1;
             scanf("%s",s+1); stack <int> S;
             for (int i = 1;i <= M;++i) match[i] = -1;
52
             for (int i = 1;i <= M;++i)</pre>
                 if (s[i] == '(') S.push(i);
                 else if (s[i] == |'|)|')
57
                     int t = S.top(); S.pop();
58
                     match[match[t] = i] = t;
59
                 }
60
             }
61
             int tot = 0; auto ans = calc(1,M);
62
             for (int i = 1;i <= N;++i) tot += ans[i]; printf("%d",tot);
63
             for (int i = 1; i \le N; ++i) if (ans[i]) printf(" %d",i); putchar('\n');
64
        }
65
        return 0;
66
67
```

6.3 Fast Fourier Transformation

```
// The First Version
    struct Vir
        double re,im;
        inline Vir(double _re = 0,double _im = 0):re(_re),im(_im) {}
        friend inline Vir operator*(const Vir &a,const Vir &b) { return
        Vir(a.re*b.re-a.im*b.im,a.re*b.im+a.im*b.re); }
        friend inline Vir operator+(const Vir &a,const Vir &b) { return Vir(a.re+b.re,a.im+b.im); }
        friend inline Vir operator-(const Vir &a,const Vir &b) { return Vir(a.re-b.re,a.im-b.im); }
        friend inline Vir operator/(const Vir &a,double r) { return Vir(a.re/r,a.im/r); }
    }pa[maxn],pb[maxn];
10
12
    inline void fft(Vir *a,int loglen,int len,int on)
13
        for (register int i = 0,j,t,p;i < len;++i)</pre>
14
        {
15
            for (p = j = 0, t = i; j < loglen; ++j, t >>= 1)
16
                p <<= 1,p |= (t&1);
17
            if (p > i) swap(a[p],a[i]);
18
19
        for (register int m = 2,s = 1;s <= loglen;++s,m <<= 1)
20
21
            register Vir w(cos(2*pi*on/m),sin(2*pi*on/m));
22
            for (int i = 0; i < len; i += m)
23
24
                register Vir wn(1,0);
25
                for (register int j = 0; j < (m>>1); ++j, wn = wn*w)
26
27
                     register Vir u = a[i+j], v = wn*a[i+j+(m>>1)];
28
                     a[i+j] = u+v; a[i+j+(m>>1)] = u-v;
29
                }
30
            }
31
32
        if (on == -1) for (int i = 0; i < len; i = a[i]/len;
33
    }
34
35
    inline void work()
36
    {
37
        int loglen = 0,len;
38
        while ((1<<loglen) < 1) ++loglen; len = 1 << loglen;
39
        fft(pa,loglen,len,1); fft(pb,loglen,len,1);
40
        for (int i = 0;i < len;++i) pa[i] = pa[i]*pb[i];</pre>
41
        fft(pa,loglen,len,-1);
42
    }
43
44
    //The Second Version
45
    const double pi = acos(-1.0);
46
    struct Complex
```

```
{
48
        double re,im;
49
        inline Complex() = default;
50
        inline Complex(double _re,double _im):re(_re),im(_im) {}
51
        friend inline Complex operator*(const Complex &a,const Complex &b) { return
52
    friend inline Complex operator+(const Complex &a,const Complex &b) { return
53
    friend inline Complex operator-(const Complex &a,const Complex &b) { return
54
       Complex(a.re-b.re,a.im-b.im); }
        friend inline Complex operator/(const Complex &a, double r) { return Complex(a.re/r,a.im/r);
55
        }
   };
56
58
    inline void FFT(Complex *a,int loglen,int len,int on)
59
        for (register int i = 0,j,t,p;i < len;++i)</pre>
60
        {
61
            for (p = j = 0,t = i;j < loglen;++j,t >>= 1)
62
               p <<= 1,p |= (t&1);
63
            if (p > i) swap(a[p],a[i]);
64
65
        for (register int m = 2,s = 1;s <= loglen;++s,m <<= 1)
66
67
            register Complex w(cos(2*pi*on/m),sin(2*pi*on/m));
68
            for (int i = 0; i < len; i += m)
69
            {
70
                register Complex wn(1,0);
                for (register int j = 0; j < (m>>1); ++j, wn = wn*w)
72
73
                    register Complex u = a[i+j],v = wn*a[i+j+(m>>1)];
74
                    a[i+j] = u+v; a[i+j+(m>>1)] = u-v;
75
               }
76
            }
77
78
        if (on == -1) for (int i = 0; i < len; i = a[i]/len;
79
   }
80
    struct Polynomial
82
    {
83
        int len; Complex array[maxn<<2];</pre>
84
        inline Polynomial(int _len = 0):len(_len) {}
85
        inline Polynomial(Complex a[],int n):len(n) { for (int i = 0;i < n;++i) array[i] = a[i]; }</pre>
86
        inline Complex operator [](int n) const { return array[n]; }
87
        inline Complex &operator [](int n) { return array[n]; }
88
        inline void set(int n) { len = n; }
89
        inline void set(int n,Complex a[]) { len = n; for (int i = 0;i < n;++i) array[i] = a[i]; }</pre>
90
        inline void extend(int key)
91
92
```

```
for (int i = len;i < (1<<key);++i)</pre>
93
                  array[i] = Complex(0,0);
94
95
         inline void cut(int key) { len = key; }
         inline void transform(int loglen,int on) { FFT(array,loglen,1<<loglen,on); }</pre>
97
     }; //变量只能定义在全局, 不然会 re
98
     inline Polynomial multiply(Polynomial &pa,Polynomial &ret) // self-multiply
100
101
         int loglen = 0;
102
         while ((1<<loglen) < (pa.len<<1)-1) ++loglen;
103
         pa.extend(1<<loglen); pa.transform(loglen,1);</pre>
104
         for (int i = 0;i < (1<<loglen);++i) ret[i] = pa[i]*pa[i];</pre>
105
         ret.transform(loglen,-1); ret.cut((pa.len<<1)-1);</pre>
106
         return ret;
107
    }
108
    inline Polynomial multiply(Polynomial &pa,Polynomial &pb,Polynomial &ret)
109
110
         int loglen = 0;
111
         while ((1<<loglen) < (pa.len+pb.len-1)) ++loglen;
112
         pa.extend(1<<loglen); pa.transform(loglen,1);</pre>
113
         pb.extend(1<<loglen); pb.transform(loglen,1);</pre>
114
         for (int i = 0;i < (1<<loglen);++i) ret[i] = pa[i]*pb[i];</pre>
115
         ret.transform(loglen,-1); ret.cut(pa.len+pb.len-1);
116
         return ret;
117
118
    }
```

6.4 Fast Input and Output

```
// Input and Output of Int
   // Be careful of Max_Int and Min_Int
   inline int gi()
    {
        char ch; int ret = 0,f = 1;
        do ch = getchar(); while (!(ch >= '0'&&ch <= '9')&&ch != '-');
        if (ch == '-') f = -1,ch = getchar();
        do ret = ret*10+ch-'0',ch = getchar(); while (ch >= '0'&&ch <= '9');
        return ret*f;
   }
10
11
   inline void pi(int a)
12
13
        if (!a) putchar('0');
14
        if (a < 0) a = -a,putchar('-');</pre>
15
        int num[10],n = 0;
16
        while (a) num[n++] = a\%10, a /= 10;
        for (int i = n-1; i >= 0; --i) putchar('0'+num[i]);
18
   }
19
```

6.5 Fraction Class

```
typedef long long 11;
   struct Fraction
        11 num,den;
4
        inline Fraction(ll a = 0,ll b = 1)
            if (den < 0) a = -a,b = -b;
            assert(b != 0); ll g = gcd(abs(a),b);
            num = a/g; den = b/g;
10
       friend inline Fraction operator +(const Fraction &a,const Fraction &b) const { return
11

    Fraction(a.num*b.den+b.num*a.den,a.den*b.den); }

        friend inline Fraction operator -(const Fraction &a,const Fraction &b) const { return
12

    Fraction(a.num*b.den-b.num*a.den,a*den*b.den); }

       friend inline Fraction operator *(const Fraction &a,const Fraction &b) const { return
13
    → Fraction(a.num*b.num,a*den*b.den); }
        friend inline Fraction operator /(const Fraction &a,const Fraction &b) const { return

    Fraction(a.num*b.den,a*den*b.num); }

       friend inline bool operator <(const Fraction &a,const Fraction &b) const { return
15

    a.num*b.den < a.den*b.num; }
</pre>
       friend inline bool operator <(const Fraction &a,const Fraction &b) const { return
       a.num==b.num&&a.den==b.den; }
   };
17
```

6.6 Gray Code

```
1  //O-2^n-1 的格雷码
2  inline vector <int> GrayCreat(int n)
3  {
4     vector <int> res;
5     for (int i = 0;i < (1<<n);++i) res.push_back(i^(i>>1));
6     return res;
7  }
```

6.7 Numerical Integration

6.8. SIMPLEX 129

```
10
    //romberg---To Be Verified
11
    template <class T>
12
    inline double romberg(const T &f, double a, double b, double eps = 1e-8)
13
14
        vector <double> t; double h = b-a,last,cur;
15
        int k = 1, i = 1;
16
        t.push_back(h*(f(a)+f(b))/2);
17
18
        {
19
            last = t.back(); cur = 0; double x = a+h/2;
20
            for (int j = 0; j < k; ++j) cur += f(x), x += h;
21
            cur = (t[0]+h*cur)/2;
22
            double k1 = 4.0/3, k2 = 1.0/3;
23
            for (int j = 0; j < i; ++j)
24
            {
25
                 double temp = k1*cur-k2*t[j];
26
                 t[j] = cur; cur = temp; k2 /= 4*k1-k2; k1 = k2+1;
27
28
            t.push_back(cur); k *= 2; h /= 2; ++i;
29
30
        while (fabs(last - cur) > eps);
31
        return t.back();
32
   }
33
```

6.8 Simplex

6.8.1 Description

有 n 个实数变量 x_1, x_2, \ldots, x_n 和 m 条约束,其中第 i 条约束形如 $\sum_{i=1}^n a_{i,j} x_j \leq b_i$ 。 此外这 n 个变量需要满足非负性限制, $x_i \geq 0$ 。

在满足上述所有条件的情况下,你需要指定每个变量 x_j 的取值,使得目标函数 $F = \sum_{j=1}^n c_j x_j$ 的值最大。

6.8.2 Input

第一行三个正整数 n, m, t。其中 $t \in \{0, 1\}$ 。

第二行有 n 个整数 c_1, c_2, \ldots, c_n , 整数间均用一个空格分隔。

接下来 m 行,每行代表一条约束,其中第 i 行有 n+1 个整数 $a_{i1}, a_{i2}, \ldots, a_{in}, b_i$,整数间均用一个空格分隔。

6.8.3 Output

如果不存在满足所有约束的解,仅输出一行"Infeasible"。

如果对于任意的 M,都存在一组解使得目标函数的值大于 M,仅输出一行 "Unbounded"。 否则,第一行输出一个实数,表示目标函数的最大值 F。 如果 t = 1,那么你还需要输出第二行,用空格隔开的 n 个非负实数,表示此时 $x_1, x_2, ..., x_n$ 的取值,如有多组方案请任意输出其中一个。

6.8.4 Code

```
1 // uoj 179
          #include<iostream>
          #include<cstdio>
          #include<cstdlib>
          using namespace std;
          #define maxn (30)
          #define eps (1e-8)
          int N,M,op,tot,q[maxn],idx[maxn],idy[maxn]; double a[maxn][maxn],A[maxn];
10
11
          inline void pivot(int x,int y)
12
13
                      swap(idy[x],idx[y]);
14
                     double tmp = a[x][y]; a[x][y] = 1/a[x][y];
15
                     for (int i = 0;i <= N;++i) if (y != i) a[x][i] /= tmp;
16
                     tot = 0; for (int i = 0; i \le N; ++i) if (i != y&&(a[x][i] > eps | |a[x][i] < -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] < -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] < -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] < -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] < -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] < -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] < -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] < -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] < -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] < -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] > -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] > -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] > -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] > -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] > -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] > -eps)) q[++tot] = (int i = 0; i := y&(a[x][i] > eps | |a[x][i] > -eps)) q[++tot] = (int i = 0; i := y&(a[x][i] > eps | |a[x][i] > -eps)) q[++tot] = (int i = 0; i := y&(a[x][i] > eps | |a[x][i] > -eps)) q[++tot] = (int i = y&(a[x][i] > eps | |a[x][i] > -eps)) q[++tot] = (int i = y&(a[x][i] > eps | |a[x][i] > -eps)) q[++tot] = (int i = y&(a[x][i] > eps | |a[x][i] > -eps)) q[++tot] = (int i = y&(a[x][i] > eps | |a[x][i] > -eps | 
             \hookrightarrow i;
                     for (int i = 0;i <= M;++i)</pre>
18
                                if ((x == i) | | (a[i][y] < eps&&a[i][y] > -eps)) continue;
                                for (int j = 1; j \le tot; ++j) a[i][q[j]] -= a[x][q[j]]*a[i][y];
21
                                a[i][y] = -a[i][y]/tmp;
                     }
23
          }
24
25
          int main()
27
                     freopen("179.in", "r", stdin);
29
                     freopen("179.out", "w", stdout);
                      scanf("%d %d %d",&N,&M,&op); srand(233);
                     for (int i = 1;i <= N;++i) scanf("%lf",a[0]+i);</pre>
31
                     for (int i = 1;i <= M;++i)</pre>
                     {
33
                                for (int j = 1; j <= N; ++j) scanf("%lf", a[i]+j);</pre>
                                scanf("%lf",a[i]);
35
                     }
37
                     for (int i = 1;i <= N;++i) idx[i] = i;
                     for (int i = 1;i <= M;++i) idy[i] = i+N;</pre>
                     while (true)
                                int x = 0, y = 0;
                                for (int i = 1; i <= M; ++i) if (a[i][0] < -eps&&((!x)||(rand()&1))) x = i; if (!x) break;
42
                                for (int i = 1; i <= N; ++i) if (a[x][i] < -eps&&((!y)||(rand()&1))) y = i; if (!y) return
                    puts("Infeasible"),0;
```

```
pivot(x,y);
44
45
        while (true)
46
47
             int x = 0, y = 0; double mn = 1e15;
48
             for (int i = 1; i \le N; ++i) if (a[0][i] > eps) { y = i; break; } if (!y) break;
49
             for (int i = 1; i \le M; ++i) if (a[i][y] > eps && a[i][0]/a[i][y] < mn) mn = 1
50
        a[i][0]/a[i][y],x = i; if (!x) return puts("Unbounded"),0;
             pivot(x,y);
51
52
        printf("%.81f\n",-a[0][0]); if (!op) return 0;
53
        for (int i = 1;i <= M;++i) if (idy[i] <= N) A[idy[i]] = a[i][0];</pre>
        for (int i = 1;i <= N;++i) printf("%.81f ",A[i]);</pre>
55
        fclose(stdin); fclose(stdout);
56
        return 0;
57
   }
58
```

6.9 Solutions of Equation of Higher Order

```
// vector <double> solve(vector <double> coef,int n)
    // coef 方程的系数; n 方程的系数
    // 输出所有实数解
    const double EPS = 1e-15,inf = 1e12;
    inline int sign(double x) { return x < -EPS?-1:x > EPS; }
    inline double get(const vector <double> &coef,double x)
9
        double e = 1, s = 0;
10
        for (int i = 0;i < coef.size();++i) s += coef[i]*e,e *= x;</pre>
11
        return s;
12
    }
13
    inline double find(const vector <double> &coef,int n,double lo,double hi)
15
16
        double sign_lo,sign_hi;
17
        if ((sign_lo = sign(get(coef,lo)))== 0) return lo;
18
        if ((sign_hi = sign(get(coef,hi)))== 0) return hi;
19
        if (sign_lo*sign_hi > 0) return inf;
20
        for (int step = 0; step < 100&&hi-lo > EPS; ++step)
21
22
            double m = (lo+hi)/2; int sign_mid = sign(get(coef,m));
23
            if (sign_mid == 0) return m;
24
            else if (sign_lo*sign_mid < 0) hi = m;</pre>
25
            else lo = m;
26
27
        return (lo+hi)/2;
28
    }
29
30
```

```
inline vector <double> solve(const vector <double> &coef,int n)
31
32
        vector <double> ret;
33
        if (n == 1)
34
35
             if (sign(coef[1])) ret.push_back(-coef[0]/coef[1]);
36
             return ret;
37
        }
38
        vector <double> dcoef(n);
39
        for (int i = 0;i < n;++i) dcoef[i] = coef[i+1]*(i+1);</pre>
40
        vector <double> droot = solve(dcoef,n-1);
41
        droot.insert(droot.begin(),-inf);
42
        droot.push_back(inf);
43
        for (int i = 0;i+1 < droot.size();++i)</pre>
44
        {
45
             double tmp = find(coef,n,droot[i],droot[i+1]);
46
             if (tmp < inf) ret.push_back(tmp);</pre>
47
48
        return ret;
49
   }
50
```

Chapter 7

String Algorithms

7.1 Aho-Corasick Automaton

```
// ac 自动机
    inline int newnode()
        memset(nxt[L],-1,sizeof(nxt[L]));
        return ++L-1;
    inline void init() { L = 0; root = newnode(); }
    inline void insert()
        int len = strlen(buf),now = root;
10
        for (int i = 0; i < len; ++i)
11
12
            if (nxt[now][buf[i]-'0'] == -1)
13
                nxt[now][buf[i]-'0'] = newnode();
14
            now = nxt[now][buf[i]-'0'];
15
        }
16
        end[now] = true;
18
    inline void build()
19
20
        int now = root; queue <int> team;
21
        fail[root] = root;
22
        for (int i = 0; i < 10; ++i)
23
24
            if (nxt[now][i] == -1) nxt[now][i] = root;
25
            else fail[nxt[now][i]] = root,team.push(nxt[now][i]);
26
        }
27
        while (!team.empty())
28
29
            now = team.front(); team.pop();
30
            for (int i = 0; i < 10; ++i)
31
32
                 if (nxt[now][i] == -1)
33
```

```
nxt[now][i] = nxt[fail[now]][i];
34
                  else
35
                  {
36
                      fail[nxt[now][i]] = nxt[fail[now]][i];
37
                      team.push(nxt[now][i]);
38
                  }
39
             }
40
         }
41
42
```

7.2 Extended Knuth-Morris-Pratt Algorithm

```
// To Be Rewritten
   // extend[i] 表示 T 与 S[i,n-1] 的最长公共前缀
   const int maxn=100010; //字符串长度最大值
   int next[maxn], ex[maxn]; //ex 数组即为 extend 数组
   //预处理计算 next 数组
   void GETNEXT(char *str)
       int i=0,j,po,len=strlen(str);
       next[0]=len;//初始化 next[0]
       while(str[i]==str[i+1]&&i+1<len)//计算 next[1]
10
       i++:
11
       next[1]=i;
12
       po=1;//初始化 po 的位置
13
       for(i=2;i<len;i++)
14
15
           if(next[i-po]+i<next[po]+po)//第一种情况, 可以直接得到 next[i] 的值
16
           next[i]=next[i-po];
           else//第二种情况,要继续匹配才能得到 next[i] 的值
18
           {
19
               j=next[po]+po-i;
20
               if(j<0)j=0;//如果 i>po+next[po],则要从头开始匹配
               while(i+j<len&&str[j]==str[j+i])//计算 next[i]
22
               j++;
23
              next[i]=j;
24
              po=i;//更新 po 的位置
25
           }
26
       }
27
28
   //计算 extend 数组
   void EXKMP(char *s1,char *s2)
                                    // s1 is S, s2 is T
30
31
       int i=0,j,po,len=strlen(s1),l2=strlen(s2);
32
       GETNEXT(s2);//计算 T 串的 next 数组
33
       while(s1[i]==s2[i]&&i<12&&i<len)//计算 ex[0]
34
       i++;
35
       ex[0]=i;
36
       po=0;//初始化 po 的位置
37
```

```
for(i=1;i<len;i++)
38
39
           if(next[i-po]+i<ex[po]+po)//第一种情况,直接可以得到 ex[i] 的值
40
           ex[i]=next[i-po];
41
           else//第二种情况,要继续匹配才能得到 ex[i] 的值
42
43
               j=ex[po]+po-i;
44
               if(j<0)j=0;//如果 i>ex[po]+po 则要从头开始匹配
45
               while(i+j<len&&j<l2&&s1[j+i]==s2[j])//计算 ex[i]
46
               j++;
47
               ex[i]=j;
48
               po=i;//更新 po 的位置
49
           }
50
       }
51
   }
52
```

7.3 Knuth-Morris-Pratt Algorithm

```
// To Be Verified
    void cal_next(char *str, int *next, int len)
        int i,j;
4
        next[0] = -1;
        for (int i = 1; i < len; i++)
             j = next[i - 1];
             while (str[j+1] != str[i] \&\&(j >= 0)) j = next[j];
             if (str[i] == str[j+1]) next[i] = j + 1;
10
             else next[i] = -1;
11
        }
12
    }
13
14
    int KMP(char *str,int slen, char *ptr,int plen,int *next)
15
16
        int s_i = 0,p_i = 0;
17
        while (s_i < slen \& p_i < plen)
18
19
             if (str[s_i] == ptr[p_i]) s_i++,p_i++;
20
             else
21
             {
22
                 if (!p_i) s_i++;
23
                 else p_i = next[p_i-1] + 1;
24
25
26
        return (p_i == plen)?(s_i - plen):-1;
27
    }
28
```

7.4 Manacher Algorithm

```
// Correct but to Be Rewritten
    inline void ready()
        for (int i = 1;i <= 2*11+1;++i)
            { if (i & 1) bac[i] = '#'; else bac[i] = s[i>>1]; }
        bin[0] = 1;
        for (int i = 1;i <= 11;++i)
            hash[i] = hash[i-1]*37+s[i]-'A'+1,bin[i] = 37*bin[i-1];
10
    inline void manacher()
11
12
        rad[1] = 1; int best = 1;
13
        for (int i = 2;i <= 2*11+1;++i)
14
15
            int j;
            if (best+rad[best]-1 < i) j = 1;
            else j = min(rad[2*best-i],best+rad[best]-i)+1;
18
            while (i-j+1\&\&i+j-1<=2*11+1\&\&bac[i-j+1]==bac[i+j-1])
19
20
                 if (bac[i+j-1] != '#')
21
                 {
22
                     ull h = (hash[(i+j-1)>>1]-hash[((i-j+1)>>1)-1]*bin[j]);
23
                     if (!exist1[h%rhl1]||!exist2[h%rhl2]||!exist3[h%rhl3])
24
25
                         exist1[h%rhl1]=exist2[h%rhl2]=exist3[h%rhl3] = true;
26
                         ++tot, have [tot] [0] = (i-j+1)>>1;
27
                         have[tot][1] = (i+j-1)>>1;
28
29
                 }
30
                 ++j;
31
            }
32
            rad[i] = j-1;
33
            if (i+rad[i]>best+rad[best]) best = i;
34
        }
35
   }
36
```

7.5 Palindrome Automaton

```
// Correct but to Be Rewritten
struct pat
{
    int next[maxn][26],fail[maxn],cnt[maxn],len[maxn],s[maxn],last,n,p;
    inline int newnode(int l) { cnt[p] = 0; len[p] = 1; return p++; }
    inline void init() { last = n = p = 0; newnode(0); newnode(-1); s[0] = -1; fail[0] = 1; }
    inline int getfail(int x) { while (s[n-len[x]-1] != s[n]) x = fail[x]; return x; }
    inline void add(int c)
```

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```
{
9
            c -= 'a'; s[++n] = c; int cur = getfail(last);
10
            if (!next[cur][c])
11
            {
12
                 int now = newnode(len[cur]+2);
13
                 fail[now] = next[getfail(fail[cur])][c];
14
                next[cur][c] = now;
15
16
            last = next[cur][c]; cnt[last]++;
17
        }
18
   }
19
```

7.6 Suffix Array

```
// 记得最后填一个字符集中没有的字符
    inline void build(char *buf,int *Sa,int *Rank,int *Height,int n,int now,int m)
        int i,j,k,*x = t1,*y = t2;
4
        memset(c,0,4*m);
        for (i = 0; i < n; ++i) c[x[i] = buf[i]-'A']++;
        for (i = 1; i < m; ++i) c[i] += c[i-1];
        for (i = n-1; i \ge 0; --i) Sa[--c[x[i]]] = i;
        for (k = 1; k < n; k <<= 1)
10
            int p = 0;
            for (i = n-k; i < n; ++i) y[p++] = i;
12
            for (i = 0; i < n; ++i) if (Sa[i] >= k) y[p++] = Sa[i] - k;
13
            memset(c,0,4*m);
14
            for (i = 0; i < n; ++i) c[x[y[i]]] ++;
15
            for (i = 1; i < m; ++i) c[i] += c[i-1];
16
            for (i = n-1; i \ge 0; --i) Sa[--c[x[y[i]]]] = y[i];
17
            swap(x,y); p = 1; x[Sa[0]] = 0;
18
            for (i = 1; i < n; ++i)
19
                 x[Sa[i]] = y[Sa[i-1]] == y[Sa[i]] & & y[Sa[i-1]+k] == y[Sa[i]+k]?p-1:p++;
20
            if (p \ge n) break; m = p;
21
        }
22
        for (i = 0;i < n;++i) Rank[Sa[i]] = i;</pre>
23
        for (i = k = 0; i < n; ++i)
24
25
            if (k) --k; if (!Rank[i]) continue;
26
            j = Sa[Rank[i]-1];
27
            while (i+k< n\&\&j+k< n\&\&buf[i+k] == buf[j+k]) ++k;
28
            Height[Rank[i]] = k;
        }
30
    }
31
```

7.7 Suffix Automaton

```
// Correct but to Be Rewritten
    struct SAM
3
        int tot,tail,cnt,p,np,q,nq,sz[maxn],arr[maxn],step[maxn],tran[maxn][26],parent[maxn];
        inline SAM() { tail = tot = 1; }
        inline void insert(int c)
            p = tail; np = tail = ++tot; step[np] = step[p]+1;
            for (;!tran[p][c];p = parent[p]) tran[p][c] = np;
            if (!p) parent[np] = 1;
10
            else
11
            {
12
                 q = tran[p][c];
13
                 if (step[p]+1 == step[q]) parent[np] = q;
14
                 else
15
                 {
16
                     nq = ++tot; step[nq] = step[p]+1;
17
                     memcpy(tran[nq],tran[q],104);
18
                     parent[nq] = parent[q]; parent[np] = parent[q] = nq;
19
                     for (;tran[p][c] == q;p = parent[p]) tran[p][c] = nq;
20
                }
21
            }
22
            sz[np] = 1;
23
        }
24
25
        inline void dfs(int now)
26
27
            if (vis[now]) return; vis[now] = true;
            for (int i = 0; i < 26; ++i)
29
                 if (tran[now][i]) dfs(tran[now][i]),arr[now] += arr[tran[now][i]];
            arr[now] += sz[now];
31
        }
32
33
        inline void build()
34
35
            if (!mode) for (int i = 1; i \le tot; ++i) sz[i] = 1;
36
            else
37
            {
                 for (int i = 2;i <= tot;++i) ++d[parent[i]];</pre>
39
                 queue <int> team; for (int i = 1;i <= tot;++i) if (!d[i]) team.push(i);
40
                 while (!team.empty())
41
42
                     int now = team.front(); team.pop();
43
                     sz[parent[now]] += sz[now];
44
                     if (!--d[parent[now]]) team.push(parent[now]);
45
                 }
46
            }
47
            sz[1] = 0; dfs(1);
48
```

```
}
49
        inline void work()
50
51
             int now = 1,1 = 0,rank = 0; memset(s,0,N+1);
52
            if (K > arr[1]) puts("-1");
53
             else
54
             {
55
                 while (true)
57
                     rank += sz[now]; if (rank >= K) break;
                     for (int i = 0; i < 26; ++i)
59
                     {
60
                          if (rank+arr[tran[now][i]] < K) rank += arr[tran[now][i]];</pre>
61
                          else { s[++1] = 'a'+i; now = tran[now][i]; break; }
62
                     }
63
                 }
64
                 printf("%s",s+1);
65
            }
66
        }
67
    }sam;
68
```

Chapter 8

Others

8.1 Calculation of Date

```
//ya 年 ma 月 da 日与 yb 年 mb 月 db 日相差几天
    const int days = 365,s[] = {0,31,28,31,30,31,30,31,30,31,30,31};
    inline bool isleap(int y)
        if ((!(y\%400)||y\%100)\&\&!(y\%4)) return true;
        return false;
    inline int leap(int y)
10
        if (!y) return 0;
11
        return y/4-y/100+y/400;
12
    }
13
14
    inline int calc(int day,int mon,int year)
15
16
        int res = (year-1)*days+leap(year-1);
17
        for (int i = 1;i < mon;++i) res += s[i];</pre>
18
        if (isleap(year)&&mon > 2) res++;
19
        res += day; return res;
20
    }
21
22
    inline int count_day(int da,int ma,int ya,int db,int mb,int yb)
23
24
        int resa = calc(da,ma,ya);
25
        int resb = calc(db,mb,yb);
26
        return abs(resa-resb);
27
    }
28
```

8.2. JAVA HINTS

8.2 Java Hints

8.2.1 Code Example

```
// Code 1
    import java.io.*;
    import java.math.*;
    import java.util.*;
    public class Main
    {
        final static int lhh = 998244353,maxn = 1655;
        static long jc[] = new long [maxn];
9
10
        static int calc(BigInteger N)
11
12
             if (N.compareTo(BigInteger.ONE) <= 0) return 0;</pre>
13
             // System.out.println(N);
14
             int 1 = 2,r = 1650,mid;
15
             while (1 \le r)
16
17
                 mid = (l+r)>>1;
18
                  \  \  \text{if } \  (((BigInteger.valueOf(mid)).pow(mid)).compareTo(N) <= 0) \ 1 = mid + 1; \\
19
                 else r = mid-1;
20
             }
21
             // System.out.println(l+" "+r);
22
              int ret = (int)jc[r]-1,d = 1; if (ret < 0) ret += lhh;</pre>
23
             int digit[] = new int[d]; BigInteger _d = BigInteger.valueOf(1);
24
             for (int i = 0; i < d; ++i)
25
26
                 digit[i] = N.mod(_d).intValue();
27
                 N = N.divide(_d);
28
             }
29
             // for (int i = d-1; i \ge 0; --i) System.out.print(digit[i]);
30
             // System.out.println();
31
             boolean cho[] = new boolean[d],safe = false,exist = true;
32
             Arrays.fill(cho,false);
33
             int per[] = new int [d];
34
             for (int i = d-1; i >= 0;--i)
35
             {
36
                 int cur = -1;
37
                 if (safe)
38
39
                      int down = i == d-1?1:0;
40
                     for (int j = d-1; j >= down; --j)
41
42
                          if (cho[j] == true) continue;
43
                          cur = j; break;
44
45
                      if (cur == -1) { exist = false; break; }
46
```

```
cho[cur] = true; per[i] = cur;
47
                 }
48
                 else
49
                 {
50
                     if (cho[digit[i]] == true)
51
52
                          // System.out.println(i+":"+digit[i]);
53
                          while (i < d)
54
55
                              cur = -1;
56
                              int down = i == d-1?1:0;
57
                              for (int j = digit[i]-1; j >= down; --j)
58
59
                                   if (cho[j] == true) continue;
60
                                   cur = j; break;
61
                              }
62
                              // System.out.println(cur+":"+i);
63
                              if (cur == -1) { ++i; if (i < d) cho[per[i]] = false; }</pre>
64
                              else { cho[cur] = true; per[i] = cur; break; }
65
                          }
66
67
                          if (cur == -1) { exist = false; break; }
68
                          safe = true;
69
                     }
70
                     else
71
                      {
72
                          if (digit[i] == 0&&i == d-1) { exist = false; break; }
73
                          per[i] = digit[i];
74
                          cho[digit[i]] = true;
75
                     }
76
                 }
77
78
             // for (int i = d-1; i \ge 0; --i) System.out.print(per[i]);
79
             // System.out.println();
80
             if (!exist) return ret;
81
             for (int i = d-1; i >= 0; --i)
82
             {
83
                 int tmp = per[i];
84
                 for (int j = d-1; j > i; --j)
85
                     if (per[j] < per[i]) --tmp;</pre>
86
                 ret += jc[i]*tmp%lhh;
87
                 if (ret >= lhh) ret -= lhh;
88
89
             ret++; if (ret >= lhh) ret -= lhh;
90
             ret -= jc[d-1]; if (ret < 0) ret += lhh;
91
             // System.out.println(ret);
92
             return ret;
93
        }
94
95
```

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```
public static void main(String args[])
96
         {
97
             jc[0] = 1;
98
             for (int i = 1; i \le 1650; ++i)
99
                  jc[i] = jc[i-1]*(long)i%lhh;
100
             Scanner cin = new Scanner(System.in);
101
             int T = cin.nextInt();
102
103
             while (T-- > 0)
104
             {
105
                  BigInteger 1 = cin.nextBigInteger(),r = cin.nextBigInteger();
106
                  int ans = calc(r)-calc(l.subtract(BigInteger.ONE));
107
                  if (ans < 0) ans += lhh; System.out.println(ans);</pre>
108
109
              // calc(BigInteger.valueOf(123455));
110
         }
111
    }
112
113
    //Code 2
114
    import java.io.*;
115
     import java.util.*;
116
     import java.math.*;
117
    public class Main
118
119
         static BigDecimal ratio[] = new BigDecimal[110];
120
         public static void main(String[] args)
121
         {
122
             Scanner cin = new Scanner(System.in);
123
             int T = cin.nextInt();
124
             for (int Case = 1;Case <= T;++Case)</pre>
125
             {
126
                  int N = cin.nextInt();
127
                  for (int i = 1; i \le N; ++i)
128
129
                      String S = cin.next();
130
                      String[] str = S.split(":");
131
                      BigDecimal a = new BigDecimal(str[0]),b = new BigDecimal(str[1]);
132
                      ratio[i] = a.divide(a.add(b),30,BigDecimal.ROUND_HALF_EVEN);
133
134
                  Arrays.sort(ratio,1,N+1);
135
                  BigDecimal res = new BigDecimal(0), 1 = new BigDecimal(1); int ans = 0;
136
                  for (int i = 1; i \le N; ++i)
137
138
                      res = res.add(ratio[i]);
139
                      if (res.compareTo(_1) < 0) ans = i;</pre>
140
                      else break;
141
142
                  System.out.println("Case #"+Case+": "+ans);
143
             }
144
```

```
}
145
     }
146
147
     // Code 3
148
     import java.math.*;
149
     import java.util.*;
150
     public class Main
151
152
         static BigInteger d,ret,temp,yy;
153
         static int n,dd;
154
         static boolean mark = true;
155
         static BigInteger[] a = new BigInteger[20];
156
         public static void main(String[] args)
157
158
             Scanner in = new Scanner (System.in);
159
             n = in.nextInt();
160
             temp = BigInteger.ONE;
161
             ret = BigInteger.ZERO;
162
             for (int i = 0; i < n; ++i)
163
164
                  int k = in.nextInt();
165
                  a[i] = BigInteger.valueOf(k);
166
                  d = temp.gcd(a[i]);
167
                  temp = temp.multiply(a[i]).divide(d);
168
             }
169
             for (int i = 1; i < (1 << n); ++i)
170
171
                  mark = false; yy = BigInteger.ONE;
172
                  for (int j = 0; j < n; ++j) if (((1 << j) & i) > 0) { mark = !mark; d = a[j].gcd(yy);
173
         yy = yy.multiply(a[j]).divide(d); }
                  if (mark) ret = ret.add(temp.divide(yy));
174
                  else ret = ret.subtract(temp.divide(yy));
175
             }
176
             d = ret.gcd(temp);
177
             System.out.println(ret.divide(d));
178
             System.out.println(temp.divide(d));
179
         }
180
     }
181
182
     // Code 4
183
     import java.io.*;
184
     import java.math.*;
185
     import java.util.*;
186
187
     public class Main
188
189
         public static String reverse(String str) { return new
190
         StringBuffer(str).reverse().toString(); }
191
```

```
public static void main(String args[])
192
193
             Scanner cin = new Scanner(System.in);
194
             int T = cin.nextInt(); BigInteger zero = BigInteger.valueOf(0);
195
             while (T-- > 0)
196
             {
197
                  int base1 = cin.nextInt(),base2 = cin.nextInt();
198
                  String S = cin.next(); int len = S.length();
199
                  System.out.println(base1+" "+S);
200
                  BigInteger res = BigInteger.valueOf(0),b1 = BigInteger.valueOf(base1),b2 =
201
         BigInteger.valueOf(base2);
                  for (int i = 0; i < len; ++i)
202
203
                      res = res.multiply(b1);
204
                      int rep = 0;
205
                      if (S.charAt(i) \ge '0'\&\&S.charAt(i) \le '9') rep = S.charAt(i)-'0';
206
                      else if (S.charAt(i) \ge 'A'\&\&S.charAt(i) \le 'Z') rep = 10+S.charAt(i)-'A';
207
                      else rep = 36+S.charAt(i)-'a';
208
                      res = res.add(BigInteger.valueOf(rep));
209
                 }
210
                  String ret = new String();
211
                  // System.out.println(res);
212
                  if (res.compareTo(zero) == 0) ret += '0';
213
                  else
214
                      while (res.compareTo(zero) > 0)
215
                      {
216
                          long val = res.remainder(b2).longValue();
217
                          // System.out.println(val);
218
                          if (val < 10) ret += (char)(val+'0');</pre>
219
                          else if (val < 36) ret += (char)(val+'A'-10);</pre>
220
                          else ret += (char)(val+'a'-36);
221
                          res = res.divide(b2);
222
223
                  System.out.println(base2+" "+reverse(ret)+"\n");
224
225
         }
226
    }
227
```

8.2.2 Class Reference

BigDecimal Class

2017/11/2 BigDecimal (Java Platform SE 7)

Overview Package Class Use Tree Deprecated Index Help

Java™ Platform Standard Ed. 7

Prev Class Next Class Frames No Frames All Classes

Summary: Nested | Field | Constr | Method Detail: Field | Constr | Method

iava.math

Class BigDecimal

java.lang.Object java.lang.Number java.math.BigDecimal

All Implemented Interfaces:

Serializable, Comparable<BigDecimal>

public class BigDecimal
extends Number
implements Comparable<BigDecimal>

Immutable, arbitrary-precision signed decimal numbers. A BigDecimal consists of an arbitrary precision integer *unscaled value* and a 32-bit integer *scale*. If zero or positive, the scale is the number of digits to the right of the decimal point. If negative, the unscaled value of the number is multiplied by ten to the power of the negation of the scale. The value of the number represented by the BigDecimal is therefore (unscaledValue \times 10^{-scale}).

The BigDecimal class provides operations for arithmetic, scale manipulation, rounding, comparison, hashing, and format conversion. The toString() method provides a canonical representation of a BigDecimal.

The BigDecimal class gives its user complete control over rounding behavior. If no rounding mode is specified and the exact result cannot be represented, an exception is thrown; otherwise, calculations can be carried out to a chosen precision and rounding mode by supplying an appropriate MathContext object to the operation. In either case, eight rounding modes are provided for the control of rounding. Using the integer fields in this class (such as ROUND_HALF_UP) to represent rounding mode is largely obsolete; the enumeration values of the RoundingMode enum, (such as RoundingMode.HALF_UP) should be used instead.

When a MathContext object is supplied with a precision setting of 0 (for example, MathContext.UNLIMITED), arithmetic operations are exact, as are the arithmetic methods which take no MathContext object. (This is the only behavior that was supported in releases prior to 5.) As a corollary of computing the exact result, the rounding mode setting of a MathContext object with a precision setting of 0 is not used and thus irrelevant. In the case of divide, the exact quotient could have an infinitely long decimal expansion; for example, 1 divided by 3. If the quotient has a nonterminating decimal expansion and the operation is specified to return an exact result, an ArithmeticException is thrown. Otherwise, the exact result of the division is returned, as done for other operations

When the precision setting is not 0, the rules of BigDecimal arithmetic are broadly compatible with selected modes of operation of the arithmetic defined in ANSI X3.274-1996 and ANSI X3.274-1996/AM 1-2000 (section 7.4). Unlike those standards, BigDecimal includes many rounding modes, which were mandatory for division in BigDecimal releases prior to 5. Any conflicts between these ANSI standards and the BigDecimal specification are resolved in favor of BigDecimal.

Since the same numerical value can have different representations (with different scales), the rules of arithmetic and rounding must specify both the numerical result and the scale used in the result's representation.

In general the rounding modes and precision setting determine how operations return results with a limited number of digits when the exact result has more digits (perhaps infinitely many in the case of division) than the number of digits returned. First, the total number of digits to return is specified by the MathContext's precision setting; this determines the result's precision. The digit count starts from the leftmost nonzero digit of the exact result. The rounding mode determines how any discarded trailing digits affect the returned result.

For all arithmetic operators , the operation is carried out as though an exact intermediate result were first calculated and then rounded to the number of digits specified by the precision setting (if necessary), using the selected rounding mode. If the exact result is not returned, some digit positions of the exact result are discarded. When rounding increases the magnitude of the returned result, it is possible for a new digit position to be created by a carry propagating to a leading "9" digit. For example, rounding the value 999.9 to three digits rounding up would be numerically equal to one thousand, represented as 100×10^{1} . In such cases, the new "1" is the leading digit position of the returned result.

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BigDecimal (Java Platform SE 7)

Besides a logical exact result, each arithmetic operation has a preferred scale for representing a result. The preferred scale for each operation is listed in the table below.

Preferred Scales for Results of Arithmetic Operations

Operation	referred Scale of Result				
Add	ddend.scale(), augend.scale())				
Subtract	max(minuend.scale(), subtrahend.scale())				
Multiply	multiplier.scale() + multiplicand.scale()				
Divide	dividend.scale() - divisor.scale()				

These scales are the ones used by the methods which return exact arithmetic results; except that an exact divide may have to use a larger scale since the exact result may have more digits. For example, 1/32 is 0.03125.

Before rounding, the scale of the logical exact intermediate result is the preferred scale for that operation. If the exact numerical result cannot be represented in precision digits, rounding selects the set of digits to return and the scale of the result is reduced from the scale of the intermediate result to the least scale which can represent the precision digits actually returned. If the exact result can be represented with at most precision digits, the representation of the result with the scale closest to the preferred scale is returned. In particular, an exactly representable quotient may be represented in fewer than precision digits by removing trailing zeros and decreasing the scale. For example, rounding to three digits using the floor rounding mode, 19/100 = 0.19 // integer=19, scale=2

but 21/110 = 0.190 // integer=190, scale=3

Note that for add, subtract, and multiply, the reduction in scale will equal the number of digit positions of the exact result which are discarded. If the rounding causes a carry propagation to create a new high-order digit position, an additional digit of the result is discarded than when no new digit position is created.

Other methods may have slightly different rounding semantics. For example, the result of the pow method using the specified algorithm can occasionally differ from the rounded mathematical result by more than one unit in the last place, one ulp.

Two types of operations are provided for manipulating the scale of a BigDecimal: scaling/rounding operations and decimal point motion operations. Scaling/rounding operations (setScale and round) return a BigDecimal whose value is approximately (or exactly) equal to that of the operand, but whose scale or precision is the specified value; that is, they increase or decrease the precision of the stored number with minimal effect on its value. Decimal point motion operations (movePointLeft and movePointRight) return a BigDecimal created from the operand by moving the decimal point a specified distance in the specified direction

For the sake of brevity and clarity, pseudo-code is used throughout the descriptions of BigDecimal methods. The pseudo-code expression (i+j) is shorthand for "a BigDecimal whose value is that of the BigDecimal i added to that of the BigDecimal j." The pseudo-code expression (i==j) is shorthand for "true if and only if the BigDecimal i represents the same value as the BigDecimal j." Other pseudo-code expressions are interpreted similarly. Square brackets are used to represent the particular BigInteger and scale pair defining a BigDecimal value; for example [19, 2] is the BigDecimal numerically equal to 0.19 having a scale of 2.

Note: care should be exercised if BigDecimal objects are used as keys in a SortedMap or elements in a SortedSet since BigDecimal's natural ordering is inconsistent with equals. See Comparable, SortedMap or SortedSet for more information.

All methods and constructors for this class throw NullPointerException when passed a null object reference for any input parameter.

See Also:

BigInteger, MathContext, RoundingMode, SortedMap, SortedSet, Serialized Form

Field Summary					
Fields					
Modifier and Type	Field and Description				
static BigDecimal	ONE				
	The value 1, with a scale of 0.				
static int	ROUND_CEILING				
	Rounding mode to round towards positive infinity.				
static int	ROUND DOWN				

https://docs.oracle.com/javase/7/docs/api/java/math/BigDecimal.html

ecimal (Java Platform SE 7)

	Rounding mode to round towards zero.
static int	ROUND_FLOOR
	Rounding mode to round towards negative infinity.
static int	ROUND_HALF_DOWN
	Rounding mode to round towards "nearest neighbor" unless both neighbors are equidistant, in which case round down.
static int	ROUND_HALF_EVEN
	Rounding mode to round towards the "nearest neighbor" unless both neighbors are equidistant, in which case, round towards the even neighbor.
static int	ROUND_HALF_UP
	Rounding mode to round towards "nearest neighbor" unless both neighbors are equidistant, in which case round up.
static int	ROUND_UNNECESSARY
	Rounding mode to assert that the requested operation has an exact result, hence no rounding is necessary.
static int	ROUND_UP
	Rounding mode to round away from zero.
static BigDecimal	TEN
	The value 10, with a scale of 0.
static BigDecimal	ZER0
	The value 0, with a scale of 0.

Constructor Summary

Constructors

Constructor and Description

BigDecimal(BigInteger val)

Translates a BigInteger into a BigDecimal.

 ${\bf BigDecimal}({\bf BigInteger}\ {\tt unscaledVal},\ {\tt int}\ {\tt scale})$

Translates a BigInteger unscaled value and an int scale into a BigDecimal.

BigDecimal(BigInteger unscaledVal, int scale, MathContext mc)

Translates a BigInteger unscaled value and an int scale into a BigDecimal, with rounding according to the context settings.

BigDecimal(BigInteger val, MathContext mc)

Translates a BigInteger into a BigDecimal rounding according to the context settings.

BigDecimal(char[] in)

Translates a character array representation of a BigDecimal into a BigDecimal, accepting the same sequence of characters as the BigDecimal(String) constructor.

BigDecimal(char[] in, int offset, int len)

Translates a character array representation of a BigDecimal into a BigDecimal, accepting the same sequence of characters as the **BigDecimal(String)** constructor, while allowing a sub-array to be specified.

BigDecimal(char[] in, int offset, int len, MathContext mc)

Translates a character array representation of a BigDecimal into a BigDecimal, accepting the same sequence of characters as the **BigDecimal(String)** constructor, while allowing a sub-array to be specified and with rounding according to the context settings.

BigDecimal(char[] in, MathContext mc)

Translates a character array representation of a BigDecimal into a BigDecimal, accepting the same sequence of characters as the **BigDecimal(String)** constructor and with rounding according to the context settings.

BigDecimal(double val)

Translates a double into a BigDecimal which is the exact decimal representation of the double's binary floating-point value.

BigDecimal(double val, MathContext mc)

Translates a double into a BigDecimal, with rounding according to the context settings.

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BigDecimal (Java Platform SE 7)

BigDecimal(int val)

Translates an int into a BigDecimal.

BigDecimal(int val, MathContext mc)

 $\label{thm:continuous} \mbox{Translates an int into a BigDecimal}, \mbox{with rounding according to the context settings}.$

BigDecimal(long val)

Translates a long into a BigDecimal.

BigDecimal(long val, MathContext mc)

Translates a long into a BigDecimal, with rounding according to the context settings.

BigDecimal(String val)

 $Translates \ the \ string \ representation \ of \ a \ BigDecimal \ into \ a \ BigDecimal.$

BigDecimal(String val, MathContext mc)

Translates the string representation of a BigDecimal into a BigDecimal, accepting the same strings as the BigDecimal(String) constructor, with rounding according to the context settings.

Method Summary

Methods

Wellious							
Modifier and Type	Method and Description						
BigDecimal	abs()						
	Returns a BigDecimal whose value is the absolute value of this BigDecimal, and whose scale is this.scale().						
BigDecimal	abs(MathContext mc)						
	Returns a BigDecimal whose value is the absolute value of this BigDecimal, with rounding according to the context settings.						
BigDecimal	<pre>add(BigDecimal augend)</pre>						
	Returns a BigDecimal whose value is (this + augend), and whose scale is max(this.scale(), augend.scale()).						
BigDecimal	<pre>add(BigDecimal augend, MathContext mc)</pre>						
	Returns a $BigDecimal$ whose value is (this + augend), with rounding according to the context settings.						
byte	byteValueExact()						
	Converts this BigDecimal to a byte, checking for lost information.						
int	compareTo(BigDecimal val)						
	Compares this BigDecimal with the specified BigDecimal.						
BigDecimal	<pre>divide(BigDecimal divisor)</pre>						
	Returns a BigDecimal whose value is (this / divisor), and whose preferred scale is (this.scale() - divisor.scale()); if the exact quotient cannot be represented (because it has a non-terminating decimal expansion) an ArithmeticException is thrown.						
BigDecimal	<pre>divide(BigDecimal divisor, int roundingMode)</pre>						
	Returns a BigDecimal whose value is (this / divisor), and whose scale is this.scale().						
BigDecimal	<pre>divide(BigDecimal divisor, int scale, int roundingMode)</pre>						
	Returns a BigDecimal whose value is (this / divisor), and whose scale is as specified.						
BigDecimal	<pre>divide(BigDecimal divisor, int scale, RoundingMode roundingMode)</pre>						
	Returns a BigDecimal whose value is (this / divisor), and whose scale is as specified.						
BigDecimal	<pre>divide(BigDecimal divisor, MathContext mc)</pre>						
	Returns a BigDecimal whose value is (this $/$ divisor), with rounding according to the context settings.						
BigDecimal	<pre>divide(BigDecimal divisor, RoundingMode roundingMode)</pre>						

2017/11/2 BigDecimal (Java Platform SE 7)

Returns a BigDecimal whose value is (this / divisor), and whose scale is

this.scale().

BigDecimal[] divideAndRemainder(BigDecimal divisor)

Returns a two-element BigDecimal array containing the result of

divideToIntegralValue followed by the result of remainder on the two operands.

BigDecimal[] divideAndRemainder(BigDecimal divisor, MathContext mc)

Returns a two-element BigDecimal array containing the result of

divideToIntegralValue followed by the result of remainder on the two operands

calculated with rounding according to the context settings.

BigDecimal divideToIntegralValue(BigDecimal divisor)

Returns a BigDecimal whose value is the integer part of the quotient (this /

divisor) rounded down.

BigDecimal divideToIntegralValue(BigDecimal divisor, MathContext mc)

Returns a BigDecimal whose value is the integer part of (this / divisor).

double
doubleValue()

Converts this BigDecimal to a double.

boolean equals(Object x)

Compares this BigDecimal with the specified Object for equality.

float floatValue()

Converts this BigDecimal to a float.

int hashCode()

Returns the hash code for this BigDecimal.

int intValue()

Converts this BigDecimal to an int.

int
 intValueExact()

Converts this BigDecimal to an int, checking for lost information.

long
longValue()

Converts this BigDecimal to a long.

long
longValueExact()

Converts this BigDecimal to a long, checking for lost information.

BigDecimal max(BigDecimal val)

Returns the maximum of this BigDecimal and val.

BigDecimal min(BigDecimal val)

Returns the minimum of this ${\tt BigDecimal}$ and ${\tt val}.$

BigDecimal movePointLeft(int n)

Returns a BigDecimal which is equivalent to this one with the decimal point moved n

places to the left.

BigDecimal movePointRight(int n)

Returns a BigDecimal which is equivalent to this one with the decimal point moved n

places to the right.

BigDecimal multiply(BigDecimal multiplicand)

Returns a BigDecimal whose value is (this \times multiplicand), and whose scale is

(this.scale() + multiplicand.scale()).

BigDecimal multiply(BigDecimal multiplicand, MathContext mc)

Returns a BigDecimal whose value is (this \times multiplicand), with rounding

according to the context settings.

BigDecimal negate()

Returns a BigDecimal whose value is (-this), and whose scale is this. scale().

BigDecimal negate(MathContext mc)

Returns a BigDecimal whose value is (-this), with rounding according to the context

settings.

BigDecimal plus()

Returns a BigDecimal whose value is (+this), and whose scale is this.scale().

BigDecimal plus(MathContext mc)

2017/11/2 BigDecimal (Java Platform SE 7)

Returns a BigDecimal whose value is (+this), with rounding according to the context

settings.

BigDecimal pow(int n)

Returns a BigDecimal whose value is $(this^n)$, The power is computed exactly, to

unlimited precision.

BigDecimal pow(int n, MathContext mc)

Returns a BigDecimal whose value is $(this^n)$.

int precision()

Returns the *precision* of this BigDecimal.

BigDecimal remainder(BigDecimal divisor)

Returns a BigDecimal whose value is (this % divisor).

BigDecimal remainder(BigDecimal divisor, MathContext mc)

Returns a BigDecimal whose value is (this $\,\%\,$ divisor), with rounding according to

the context settings.

BigDecimal round(MathContext mc)

Returns a BigDecimal rounded according to the MathContext settings.

int scale()

Returns the scale of this BigDecimal.

BigDecimal scaleByPowerOfTen(int n)

Returns a BigDecimal whose numerical value is equal to (this * 10ⁿ).

BigDecimal setScale(int newScale)

Returns a BigDecimal whose scale is the specified value, and whose value is numerically

equal to this BigDecimal's.

BigDecimal setScale(int newScale, int roundingMode)

Returns a BigDecimal whose scale is the specified value, and whose unscaled value is determined by multiplying or dividing this BigDecimal's unscaled value by the appropriate

power of ten to maintain its overall value.

BigDecimal setScale(int newScale, RoundingMode roundingMode)

Returns a BigDecimal whose scale is the specified value, and whose unscaled value is

 $\label{lem:determined} \mbox{ determined by multiplying or dividing this $\tt BigDecimal$'s unscaled value by the appropriate}$

power of ten to maintain its overall value.

short shortValueExact()

Converts this ${\tt BigDecimal}$ to a short, checking for lost information.

int signum()

Returns the signum function of this ${\tt BigDecimal}.$

BigDecimal stripTrailingZeros()

Returns a BigDecimal which is numerically equal to this one but with any trailing zeros removed from the representation

removed from the representation.

BigDecimal subtract(BigDecimal subtrahend)

Returns a BigDecimal whose value is (this - subtrahend), and whose scale is

 $\max(\text{this.scale()}, \, \text{subtrahend.scale()}).$

BigDecimal subtract(BigDecimal subtrahend, MathContext mc)

Returns a BigDecimal whose value is (this - subtrahend), with rounding according

to the context settings.

BigInteger toBigInteger()

Converts this BigDecimal to a BigInteger.

BigInteger toBigIntegerExact()

 $\label{lem:converts} \textbf{Converts this BigDecimal to a BigInteger, checking for lost information.}$

String toEngineeringString()

Returns a string representation of this BigDecimal, using engineering notation if an

exponent is needed.

String toPlainString()

Returns a string representation of this BigDecimal without an exponent field.

String toString()

2017/11/2 BigDecimal (Java Platform SE 7)

Returns the string representation of this BigDecimal, using scientific notation if an

exponent is needed.

BigDecimal ulp()

Returns the size of an ulp, a unit in the last place, of this BigDecimal.

BigInteger unscaledValue()

Returns a BigInteger whose value is the *unscaled value* of this BigDecimal.

static BigDecimal valueOf(double val)

Translates a double into a BigDecimal, using the double's canonical string

representation provided by the **Double.toString(double)** method.

static BigDecimal valueOf(long val)

Translates a long value into a BigDecimal with a scale of zero.

static BigDecimal valueOf(long unscaledVal, int scale)

Translates a long unscaled value and an int scale into a BigDecimal.

Methods inherited from class java.lang.Number

byteValue, shortValue

Methods inherited from class java.lang.Object

clone, finalize, getClass, notify, notifyAll, wait, wait, wait

Field Detail

ZERO

public static final BigDecimal ZERO

The value 0, with a scale of 0.

Since:

1.5

ONE

public static final BigDecimal ONE

The value 1, with a scale of 0.

Since:

1.5

TEN

public static final BigDecimal TEN

The value 10, with a scale of 0.

Since:

1.5

BigInteger Class

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Summary: Nested | Field | Constr | Method Detail: Field | Constr | Method

iava.math

Class BigInteger

java.lang.Object java.lang.Number java.math.BigInteger

All Implemented Interfaces:

Serializable, Comparable<BigInteger>

public class BigInteger
extends Number
implements Comparable<BigInteger>

Immutable arbitrary-precision integers. All operations behave as if BigIntegers were represented in two's-complement notation (like Java's primitive integer types). BigInteger provides analogues to all of Java's primitive integer operators, and all relevant methods from java.lang.Math. Additionally, BigInteger provides operations for modular arithmetic, GCD calculation, primality testing, prime generation, bit manipulation, and a few other miscellaneous operations.

Semantics of arithmetic operations exactly mimic those of Java's integer arithmetic operators, as defined in *The Java Language Specification*. For example, division by zero throws an ArithmeticException, and division of a negative by a positive yields a negative (or zero) remainder. All of the details in the Spec concerning overflow are ignored, as BigIntegers are made as large as necessary to accommodate the results of an operation.

Semantics of shift operations extend those of Java's shift operators to allow for negative shift distances. A right-shift with a negative shift distance results in a left shift, and vice-versa. The unsigned right shift operator (>>>) is omitted, as this operation makes little sense in combination with the "infinite word size" abstraction provided by this class.

Semantics of bitwise logical operations exactly mimic those of Java's bitwise integer operators. The binary operators (and, or, xor) implicitly perform sign extension on the shorter of the two operands prior to performing the operation.

Comparison operations perform signed integer comparisons, analogous to those performed by Java's relational and equality operators.

Modular arithmetic operations are provided to compute residues, perform exponentiation, and compute multiplicative inverses. These methods always return a non-negative result, between θ and (modulus - 1), inclusive.

Bit operations operate on a single bit of the two's-complement representation of their operand. If necessary, the operand is sign-extended so that it contains the designated bit. None of the single-bit operations can produce a BigInteger with a different sign from the BigInteger being operated on, as they affect only a single bit, and the "infinite word size" abstraction provided by this class ensures that there are infinitely many "virtual sign bits" preceding each BigInteger.

For the sake of brevity and clarity, pseudo-code is used throughout the descriptions of BigInteger methods. The pseudo-code expression (i + j) is shorthand for "a BigInteger whose value is that of the BigInteger i plus that of the BigInteger j." The pseudo-code expression (i == j) is shorthand for "t rue if and only if the BigInteger i represents the same value as the BigInteger j." Other pseudo-code expressions are interpreted similarly.

All methods and constructors in this class throw NullPointerException when passed a null object reference for any input parameter.

Since:

JDK1 1

See Also:

BigDecimal, Serialized Form

BigInteger (Java Platform SE 7)

Field Summary

Fields

Modifier and Type	Field and Description
static BigInteger	ONE
	The BigInteger constant one.
static BigInteger	TEN
	The BigInteger constant ten.
static BigInteger	ZERO
	The BigInteger constant zero.

Constructor Summary

Constructors

Constructor and Description

BigInteger(byte[] val)

Translates a byte array containing the two's-complement binary representation of a BigInteger into a BigInteger.

BigInteger(int signum, byte[] magnitude)

Translates the sign-magnitude representation of a BigInteger into a BigInteger.

BigInteger(int bitLength, int certainty, Random rnd)

Constructs a randomly generated positive BigInteger that is probably prime, with the specified bitLength.

BigInteger(int numBits, Random rnd)

Constructs a randomly generated BigInteger, uniformly distributed over the range 0 to (2^{numBits} - 1), inclusive.

BigInteger(String val)

Translates the decimal String representation of a BigInteger into a BigInteger.

BigInteger(String val, int radix)

Translates the String representation of a BigInteger in the specified radix into a BigInteger.

Method Summary

Methods

Modifier and Type	Method and Description
BigInteger	abs()
	Returns a BigInteger whose value is the absolute value of this BigInteger.
BigInteger	<pre>add(BigInteger val)</pre>
	Returns a BigInteger whose value is (this + val).
BigInteger	<pre>and(BigInteger val)</pre>
	Returns a BigInteger whose value is (this & val).
BigInteger	<pre>andNot(BigInteger val)</pre>
	Returns a BigInteger whose value is (this & ~val).
int	<pre>bitCount()</pre>
	Returns the number of bits in the two's complement representation of this BigInteger that differ from its sign bit.
int	<pre>bitLength()</pre>
	Returns the number of bits in the minimal two's-complement representation of this BigInteger, excluding a sign bit.
BigInteger	<pre>clearBit(int n)</pre>

2017/11/2 BigInteger (Java Platform SE 7)

Returns a BigInteger whose value is equivalent to this BigInteger with the designated bit

cleared.

int compareTo(BigInteger val)

Compares this BigInteger with the specified BigInteger.

BigInteger divide(BigInteger val)

Returns a BigInteger whose value is (this / val).

BigInteger[] divideAndRemainder(BigInteger val)

Returns an array of two BigIntegers containing (this \prime val) followed by (this %

val).

double doubleValue()

Converts this BigInteger to a double.

boolean equals(Object x)

Compares this BigInteger with the specified Object for equality.

BigInteger flipBit(int n)

Returns a BigInteger whose value is equivalent to this BigInteger with the designated bit

flipped.

float
floatValue()

Converts this BigInteger to a float.

BigInteger gcd(BigInteger val)

Returns a BigInteger whose value is the greatest common divisor of abs(this) and

abs(val).

int getLowestSetBit()

Returns the index of the rightmost (lowest-order) one bit in this BigInteger (the number of

zero bits to the right of the rightmost one bit).

int hashCode()

Returns the hash code for this BigInteger.

int intValue()

Converts this BigInteger to an int.

boolean isProbablePrime(int certainty)

Returns true if this BigInteger is probably prime, false if it's definitely composite.

long longValue()

Converts this BigInteger to a long.

BigInteger wat max(BigInteger val)

Returns the maximum of this BigInteger and val.

BigInteger min(BigInteger val)

Returns the minimum of this BigInteger and val.

BigInteger mod(BigInteger m)

Returns a BigInteger whose value is (this $\mbox{mod}\mbox{ m}$).

BigInteger modInverse(BigInteger m)

Returns a BigInteger whose value is $(this^{-1} mod m)$.

BigInteger modPow(BigInteger exponent, BigInteger m)

Returns a BigInteger whose value is (this exponent mod m).

BigInteger multiply(BigInteger val)

Returns a BigInteger whose value is (this * val).

BigInteger negate()

Returns a BigInteger whose value is (-this).

BigInteger nextProbablePrime()

Returns the first integer greater than this BigInteger that is probably prime.

BigInteger not()

Returns a BigInteger whose value is (~this).

BigInteger or(BigInteger val)

Returns a BigInteger whose value is (this \mid val).

BigInteger pow(int exponent)

BigInteger (Java Platform SE 7)

Returns a BigInteger whose value is (this^{exponent}).

static BigInteger probablePrime(int bitLength, Random rnd)

Returns a positive BigInteger that is probably prime, with the specified bitLength.

BigInteger remainder(BigInteger val)

Returns a BigInteger whose value is (this % val).

BigInteger setBit(int n)

Returns a BigInteger whose value is equivalent to this BigInteger with the designated bit

set.

BigInteger shiftLeft(int n)

Returns a BigInteger whose value is (this << n).

BigInteger shiftRight(int n)

Returns a BigInteger whose value is (this >> n).

int signum()

Returns the signum function of this BigInteger.

BigInteger subtract(BigInteger val)

Returns a BigInteger whose value is (this - val).

boolean testBit(int n)

Returns true if and only if the designated bit is set.

byte[] toByteArray()

Returns a byte array containing the two's-complement representation of this BigInteger.

String toString()

Returns the decimal String representation of this BigInteger.

String toString(int radix)

Returns the String representation of this BigInteger in the given radix.

static BigInteger valueOf(long val)

Returns a BigInteger whose value is equal to that of the specified long.

BigInteger xor(BigInteger val)

Returns a BigInteger whose value is (this $\, \hat{} \,$ val).

Methods inherited from class java.lang.Number

byteValue, shortValue

Methods inherited from class java.lang.Object

clone, finalize, getClass, notify, notifyAll, wait, wait, wait

Field Detail

ZERO

public static final BigInteger ZERO

The BigInteger constant zero.

Since:

1.2

ONE

MathContext Class

2017/11/2 MathContext (Java Platform SE 7)

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Summary: Nested | Field | Constr | Method Detail: Field | Constr | Method

iava math

Class MathContext

java.lang.Object

java.math.MathContext

All Implemented Interfaces:

Serializable

public final class MathContext
extends Object
implements Serializable

Immutable objects which encapsulate the context settings which describe certain rules for numerical operators, such as those implemented by the BigDecimal class.

The base-independent settings are:

- 1. precision: the number of digits to be used for an operation; results are rounded to this precision
- 2. roundingMode: a RoundingMode object which specifies the algorithm to be used for rounding.

Since:

1.5

See Also:

BigDecimal, RoundingMode, Serialized Form

ield Summary	
Fields	
Modifier and Type	Field and Description
static MathContext	DECIMAL128
	A MathContext object with a precision setting matching the IEEE 754R Decimal128 format, 34 digits, and a rounding mode of HALF_EVEN, the IEEE 754R default.
static MathContext	DECIMAL32
	A MathContext object with a precision setting matching the IEEE 754R Decimal32 format, 7 digits, and a rounding mode of HALF_EVEN, the IEEE 754R default.
static MathContext	DECIMAL64
	A MathContext object with a precision setting matching the IEEE 754R Decimal64 format, 16 digits, and a rounding mode of HALF_EVEN, the IEEE 754R default.
static MathContext	UNLIMITED
	A MathContext object whose settings have the values required for unlimited precision arithmetic.

Constructor Summary

Constructors

MathContext (Java Platform SE 7)

Constructor and Description

MathContext(int setPrecision)

Constructs a new MathContext with the specified precision and the HALF_UP rounding mode.

MathContext(int setPrecision, RoundingMode setRoundingMode)

Constructs a new MathContext with a specified precision and rounding mode.

MathContext(String val)

Constructs a new MathContext from a string.

Method Summary

Methods

Modifier and Type	Method and Description
boolean	equals(Object x)
	Compares this MathContext with the specified Object for equality.
int	<pre>getPrecision()</pre>
	Returns the precision setting.
RoundingMode	<pre>getRoundingMode()</pre>
	Returns the roundingMode setting.
int	hashCode()
	Returns the hash code for this MathContext.
String	toString()
	Returns the string representation of this MathContext.

Methods inherited from class java.lang.Object

clone, finalize, getClass, notify, notifyAll, wait, wait, wait

Field Detail

UNLIMITED

public static final MathContext UNLIMITED

A MathContext object whose settings have the values required for unlimited precision arithmetic. The values of the settings are: precision=0 roundingMode=HALF_UP

DECIMAL32

public static final MathContext DECIMAL32

A MathContext object with a precision setting matching the IEEE 754R Decimal 32 format, 7 digits, and a rounding mode of HALF_EVEN, the IEEE 754R default.

DECIMAL64

public static final MathContext DECIMAL64

A MathContext object with a precision setting matching the IEEE 754R Decimal64 format, 16 digits, and a rounding mode of $HALF_EVEN$, the IEEE 754R default.

2017/11/2

MathContext (Java Platform SE 7)

DECIMAL128

public static final MathContext DECIMAL128

A MathContext object with a precision setting matching the IEEE 754R Decimal128 format, 34 digits, and a rounding mode of HALF_EVEN, the IEEE 754R default.

Constructor Detail

MathContext

public MathContext(int setPrecision)

 ${\tt Constructs\ a\ new\ MathContext\ with\ the\ specified\ precision\ and\ the\ HALF_UP\ rounding\ mode.}$

Parameters:

setPrecision - The non-negative int precision setting.

Throws:

 ${\tt IllegalArgumentException-if}\ the\ {\tt setPrecision}\ parameter\ is\ less\ than\ zero.$

MathContext

Constructs a new MathContext with a specified precision and rounding mode.

Parameters:

 $\verb|setPrecision-The| non-negative int| precision setting.$

 $\verb|setRounding| Mode - The rounding mode to use.$

Throws:

IllegalArgumentException - if the setPrecision parameter is less than zero.

 ${\bf NullPointerException - if the \ rounding \ mode \ argument \ is \ null}$

MathContext

public MathContext(String val)

Constructs a new MathContext from a string. The string must be in the same format as that produced by the toString() method.

An IllegalArgumentException is thrown if the precision section of the string is out of range (< θ) or the string is not in the format created by the toString() method.

Parameters:

val - The string to be parsed

Throws:

IllegalArgumentException - if the precision section is out of range or of incorrect format

NullPointerException - if the argument is null

MathContext (Java Platform SE 7)

Method Detail

getPrecision

public int getPrecision()

Returns the precision setting. This value is always non-negative.

Returns:

an int which is the value of the precision setting

getRoundingMode

public RoundingMode getRoundingMode()

Returns the roundingMode setting. This will be one of RoundingMode.CEILING, RoundingMode.DOWN, RoundingMode.FLOOR, RoundingMode.HALF_DOWN, RoundingMode.HALF_EVEN, RoundingMode.HALF_UP, RoundingMode.UNNECESSARY, or RoundingMode.UP.

Returns:

a RoundingMode object which is the value of the roundingMode setting

equals

public boolean equals(Object x)

 $\label{lem:compares} \textbf{Compares this MathContext} \ \ \textbf{with the specified Object for equality}.$

Overrides:

equals in class Object

Parameters:

x - Object to which this MathContext is to be compared.

Returns

true if and only if the specified Object is a MathContext object which has exactly the same settings as this object

See Also:

Object.hashCode(),HashMap

hashCode

public int hashCode()

Returns the hash code for this MathContext.

Overrides:

 $\verb|hashCode| in class Object|$

Returns:

2017/11/2

MathContext (Java Platform SE 7)

hash code for this MathContext

See Also:

Object.equals(java.lang.Object), System.identityHashCode(java.lang.Object)

toString

public String toString()

Returns the string representation of this MathContext. The String returned represents the settings of the MathContext object as two space-delimited words (separated by a single space character, '\u0020', and with no leading or trailing white space), as follows:

- The string "precision=", immediately followed by the value of the precision setting as a numeric string as if generated by the Integer.toString method.
 The string "roundingMode=", immediately followed by the value of the roundingMode setting as a word. This
- word will be the same as the name of the corresponding public constant in the RoundingMode enum.

For example:

precision=9 roundingMode=HALF_UP

Additional words may be appended to the result of toString in the future if more properties are added to this class.

Overrides:

toString in class Object

Returns:

a String representing the context settings

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Submit a bug or feature

For further API reference and developer documentation, see Java SE Documentation. That documentation contains more detailed, developer-targeted descriptions, with conceptual overviews, definitions of terms, workarounds, and working code

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RoundingMode Class

2017/11/2 RoundingMode (Java Platform SE 7)

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Summary: Nested | Enum Constants | Field | Method Detail: Enum Constants | Field | Method

iava math

Enum RoundingMode

java.lang.Object java.lang.Enum<RoundingMode> java.math.RoundingMode

All Implemented Interfaces:

Serializable, Comparable<RoundingMode>

public enum RoundingMode
extends Enum<RoundingMode>

Specifies a *rounding behavior* for numerical operations capable of discarding precision. Each rounding mode indicates how the least significant returned digit of a rounded result is to be calculated. If fewer digits are returned than the digits needed to represent the exact numerical result, the discarded digits will be referred to as the *discarded fraction* regardless the digits' contribution to the value of the number. In other words, considered as a numerical value, the discarded fraction could have an absolute value greater than one.

Each rounding mode description includes a table listing how different two-digit decimal values would round to a one digit decimal value under the rounding mode in question. The result column in the tables could be gotten by creating a BigDecimal number with the specified value, forming a MathContext object with the proper settings (precision set to 1, and the roundingMode set to the rounding mode in question), and calling round on this number with the proper MathContext. A summary table showing the results of these rounding operations for all rounding modes appears below.

Summary of Rounding Operations Under Different Rounding Modes

	Res	Result of rounding input to one digit with the given rounding mode						
Input Number	UP	DOWN	CEILING	FL00R	HALF_UP	HALF_DOWN	HALF_EVEN	UNNECESSARY
5.5	6	5	6	5	6	5	6	throw ArithmeticException
2.5	3	2	3	2	3	2	2	throw ArithmeticException
1.6	2	1	2	1	2	2	2	throw ArithmeticException
1.1	2	1	2	1	1	1	1	throw ArithmeticException
1.0	1	1	1	1	1	1	1	1
-1.0	-1	-1	-1	-1	-1	-1	-1	-1
-1.1	-2	-1	-1	-2	-1	-1	-1	throw ArithmeticException
-1.6	-2	-1	-1	-2	-2	-2	-2	throw ArithmeticException
-2.5	-3	-2	-2	-3	-3	-2	-2	throw ArithmeticException
-5.5	-6	-5	-5	-6	-6	-5	-6	throw ArithmeticException

This enum is intended to replace the integer-based enumeration of rounding mode constants in $BigDecimal(BigDecimal.ROUND_UP, BigDecimal.ROUND_DOWN, etc.)$.

Since:

1.5

See Also:

BigDecimal, MathContext

2017/11/2

RoundingMode (Java Platform SE 7)

Enum Constant Summary

Enum Constants

Enum Constant and Description

CEILING

Rounding mode to round towards positive infinity.

DOM

Rounding mode to round towards zero.

FL00R

Rounding mode to round towards negative infinity.

HALF_DOWN

Rounding mode to round towards "nearest neighbor" unless both neighbors are equidistant, in which case round down.

HALF EVEN

Rounding mode to round towards the "nearest neighbor" unless both neighbors are equidistant, in which case, round towards the even neighbor.

HALF UP

Rounding mode to round towards "nearest neighbor" unless both neighbors are equidistant, in which case round up.

UNNECESSARY

Rounding mode to assert that the requested operation has an exact result, hence no rounding is necessary.

ПP

Rounding mode to round away from zero.

Method Summary

Methods

Modifier and Type	Method and Description
static RoundingMode	<pre>valueOf(int rm)</pre>
	Returns the RoundingMode object corresponding to a legacy integer rounding mode constant in BigDecimal .
static RoundingMode	<pre>valueOf(String name)</pre>
	Returns the enum constant of this type with the specified name.
<pre>static RoundingMode[]</pre>	values()
	Returns an array containing the constants of this enum type, in the order they are declared

Methods inherited from class java.lang.Enum

clone, compareTo, equals, finalize, getDeclaringClass, hashCode, name, ordinal, toString, valueOf

Methods inherited from class java.lang.Object

getClass, notify, notifyAll, wait, wait, wait

Enum Constant Detail

UP

public static final RoundingMode UP

RoundingMode (Java Platform SE 7)

Rounding mode to round away from zero. Always increments the digit prior to a non-zero discarded fraction. Note that this rounding mode never decreases the magnitude of the calculated value.

Example:

Input Number	Input rounded to one digit with UP rounding
5.5	6
2.5	3
1.6	2
1.1	2
1.0	1
-1.0	-1
-1.1	-2
-1.6	-2
-2.5	-3
-5.5	-6

DOWN

public static final RoundingMode DOWN

Rounding mode to round towards zero. Never increments the digit prior to a discarded fraction (i.e., truncates). Note that this rounding mode never increases the magnitude of the calculated value.

Example:

Input Number	Input rounded to one digit with DOWN rounding
5.5	5
2.5	2
1.6	1
1.1	1
1.0	1
-1.0	-1
-1.1	-1
-1.6	-1
-2.5	-2
-5.5	-5

CEILING

${\tt public static final Rounding Mode CEILING}$

Rounding mode to round towards positive infinity. If the result is positive, behaves as for RoundingMode.UP; if negative, behaves as for RoundingMode.DOWN. Note that this rounding mode never decreases the calculated value.

Example:

2017/11/2

RoundingMode (Java Platform SE 7)

1/2		Nounding Mode (Sava Flactorin SE 7)
	Input Number	Input rounded to one digit with CEILING rounding
	5.5	6
	2.5	3
	1.6	2
	1.1	2
	1.0	1
	-1.0	-1
	-1.1	-1
	-1.6	-1
	-2.5	-2
	-5.5	-5
П	1	'

FLOOR

public static final RoundingMode FLOOR

Rounding mode to round towards negative infinity. If the result is positive, behave as for RoundingMode.DOWN; if negative, behave as for RoundingMode.UP. Note that this rounding mode never increases the calculated value.

Example:

Input Number	Input rounded to one digit with FL00R rounding
5.5	5
2.5	2
1.6	1
1.1	1
1.0	1
-1.0	-1
-1.1	-2
-1.6	-2
-2.5	-3
-5.5	-6

HALF_UP

public static final RoundingMode HALF_UP

Rounding mode to round towards "nearest neighbor" unless both neighbors are equidistant, in which case round up. Behaves as for RoundingMode.UP if the discarded fraction is \geq 0.5; otherwise, behaves as for RoundingMode.DOWN. Note that this is the rounding mode commonly taught at school.

Example:

	Input rounded to one digit with HALF_UP rounding
5.5	6

https://docs.oracle.com/javase/7/docs/api/java/math/RoundingMode.html

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	2.5	3
	1.6	2
	1.1	1
	1.0	1
	-1.0	-1
	-1.1	-1
	-1.6	-2
	-2.5	-3
	-5.5	-6
П		

HALF_DOWN

public static final RoundingMode HALF_DOWN

Rounding mode to round towards "nearest neighbor" unless both neighbors are equidistant, in which case round down. Behaves as for RoundingMode.UP if the discarded fraction is > 0.5; otherwise, behaves as for RoundingMode.DOWN.

Example:

Input Number	Input rounded to one digit with HALF_DOWN rounding
5.5	5
2.5	2
1.6	2
1.1	1
1.0	1
-1.0	-1
-1.1	-1
-1.6	-2
-2.5	-2
-5.5	-5

HALF_EVEN

 $\verb"public static final Rounding Mode HALF_EVEN"$

Rounding mode to round towards the "nearest neighbor" unless both neighbors are equidistant, in which case, round towards the even neighbor. Behaves as for RoundingMode.HALF_UP if the digit to the left of the discarded fraction is odd; behaves as for RoundingMode.HALF_DOWN if it's even. Note that this is the rounding mode that statistically minimizes cumulative error when applied repeatedly over a sequence of calculations. It is sometimes known as "Banker's rounding," and is chiefly used in the USA. This rounding mode is analogous to the rounding policy used for float and double arithmetic in Java.

Example:

	Input rounded to one digit with HALF_EVEN rounding
5.5	6
2.5	2

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1.6	2
1.1	1
1.0	1
-1.0	-1
-1.1	-1
-1.6	-2
-2.5	-2
-5.5	-6

UNNECESSARY

public static final RoundingMode UNNECESSARY

Rounding mode to assert that the requested operation has an exact result, hence no rounding is necessary. If this rounding mode is specified on an operation that yields an inexact result, an ArithmeticException is thrown.

Example:

Input Number	Input rounded to one digit with UNNECESSARY rounding
5.5	throw ArithmeticException
2.5	throw ArithmeticException
1.6	throw ArithmeticException
1.1	throw ArithmeticException
1.0	1
-1.0	-1
-1.1	throw ArithmeticException
-1.6	throw ArithmeticException
-2.5	throw ArithmeticException
-5.5	throw ArithmeticException

Method Detail

values

public static RoundingMode[] values()

Returns an array containing the constants of this enum type, in the order they are declared. This method may be used to iterate over the constants as follows:

for (RoundingMode c : RoundingMode.values())
 System.out.println(c);

Returns:

an array containing the constants of this enum type, in the order they are declared

RoundingMode (Java Platform SE 7)

valueOf

public static RoundingMode valueOf(String name)

Returns the enum constant of this type with the specified name. The string must match *exactly* an identifier used to declare an enum constant in this type. (Extraneous whitespace characters are not permitted.)

Parameters:

name - the name of the enum constant to be returned.

Returns:

the enum constant with the specified name

Throws:

IllegalArgumentException - if this enum type has no constant with the specified name

NullPointerException - if the argument is null

valueOf

public static RoundingMode valueOf(int rm)

Returns the RoundingMode object corresponding to a legacy integer rounding mode constant in BigDecimal.

Parameters:

rm - legacy integer rounding mode to convert

Returns:

 $Rounding Mode\ corresponding\ to\ the\ given\ integer.$

Throws:

IllegalArgumentException - integer is out of range

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Frames No Frames All Classes

Summary: Nested | Enum Constants | Field | Method Detail: Enum Constants | Field | Method

Submit a bug or feature

For further API reference and developer documentation, see Java SE Documentation. That documentation contains more detailed, developer-targeted descriptions, with conceptual overviews, definitions of terms, workarounds, and working code examples.

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String-Class

2017/11/2 String (Java Platform SE 7)

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Summary: Nested | Field | Constr | Method Detail: Field | Constr | Method

iava.lang

Class String

java.lang.Object java.lang.String

All Implemented Interfaces:

Serializable, CharSequence, Comparable<String>

```
public final class String
extends Object
implements Serializable, Comparable<String>, CharSequence
```

The String class represents character strings. All string literals in Java programs, such as "abc", are implemented as instances of this class.

Strings are constant; their values cannot be changed after they are created. String buffers support mutable strings. Because String objects are immutable they can be shared. For example:

```
String str = "abc";
```

is equivalent to:

```
char data[] = {'a', 'b', 'c'};
String str = new String(data);
```

Here are some more examples of how strings can be used:

```
System.out.println("abc");
String cde = "cde";
System.out.println("abc" + cde);
String c = "abc".substring(2,3);
String d = cde.substring(1, 2);
```

The class String includes methods for examining individual characters of the sequence, for comparing strings, for searching strings, for extracting substrings, and for creating a copy of a string with all characters translated to uppercase or to lowercase. Case mapping is based on the Unicode Standard version specified by the Character class.

The Java language provides special support for the string concatenation operator (+), and for conversion of other objects to strings. String concatenation is implemented through the StringBuilder(or StringBuffer) class and its append method. String conversions are implemented through the method toString, defined by Object and inherited by all classes in Java. For additional information on string concatenation and conversion, see Gosling, Joy, and Steele, *The Java Language Specification*.

Unless otherwise noted, passing a null argument to a constructor or method in this class will cause a NullPointerException to be thrown.

A String represents a string in the UTF-16 format in which *supplementary characters* are represented by *surrogate pairs* (see the section Unicode Character Representations in the Character class for more information). Index values refer to char code units, so a supplementary character uses two positions in a String.

The String class provides methods for dealing with Unicode code points (i.e., characters), in addition to those for dealing with Unicode code units (i.e., char values).

Since:

JDK1.0

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See Also:

Object.toString(), StringBuffer, StringBuilder, Charset, Serialized Form

Field Summary

Fields

Modifier and Type	Field and Description
static Comparator <string></string>	CASE_INSENSITIVE_ORDER
	A Comparator that orders String objects as by compareToIgnoreCase.

Constructor Summary

Constructors

Constructor and Description

String()

Initializes a newly created String object so that it represents an empty character sequence.

String(byte[] bytes)

Constructs a new String by decoding the specified array of bytes using the platform's default charset.

String(byte[] bytes, Charset charset)

Constructs a new String by decoding the specified array of bytes using the specified charset.

String(byte[] ascii, int hibyte)

Deprecated.

This method does not properly convert bytes into characters. As of JDK 1.1, the preferred way to do this is via the String constructors that take a **Charset**, charset name, or that use the platform's default charset.

 $\textbf{String}(\texttt{byte}[] \ \texttt{bytes}, \ \texttt{int offset}, \ \texttt{int length})$

Constructs a new String by decoding the specified subarray of bytes using the platform's default charset.

String(byte[] bytes, int offset, int length, Charset charset)

Constructs a new String by decoding the specified subarray of bytes using the specified charset.

String(byte[] ascii, int hibyte, int offset, int count)

Deprecated.

This method does not properly convert bytes into characters. As of JDK 1.1, the preferred way to do this is via the String constructors that take a Charset, charset name, or that use the platform's default charset.

String(byte[] bytes, int offset, int length, String charsetName)

 ${\tt Constructs\ a\ new\ String\ by\ decoding\ the\ specified\ subarray\ of\ bytes\ using\ the\ specified\ charset.}$

String(byte[] bytes, String charsetName)

Constructs a new String by decoding the specified array of bytes using the specified charset.

String(char[] value)

Allocates a new String so that it represents the sequence of characters currently contained in the character array argument.

String(char[] value, int offset, int count)

Allocates a new String that contains characters from a subarray of the character array argument.

String(int[] codePoints, int offset, int count)

 $Allocates \ a \ new \ String \ that \ contains \ characters \ from \ a \ subarray \ of \ the \ Unicode \ code \ point \ array \ argument.$

String(String original)

Initializes a newly created String object so that it represents the same sequence of characters as the argument; in other words, the newly created string is a copy of the argument string.

String(StringBuffer buffer)

Allocates a new string that contains the sequence of characters currently contained in the string buffer argument.

String(StringBuilder builder)

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Allocates a new string that contains the sequence of characters currently contained in the string builder argument.

Method Summary

Methods	
Modifier and Type	Method and Description
char	<pre>charAt(int index)</pre>
	Returns the char value at the specified index.
int	<pre>codePointAt(int index)</pre>
	Returns the character (Unicode code point) at the specified index.
int	codePointBefore(int index)
	Returns the character (Unicode code point) before the specified index.
int	<pre>codePointCount(int beginIndex, int endIndex) Returns the number of Unicode code points in the specified text range of this String.</pre>
int	compareTo(String anotherString) Compares two strings lexicographically.
int	<pre>compareToIgnoreCase(String str) Compares two strings lexicographically, ignoring case differences.</pre>
String	<pre>concat(String str) Concatenates the specified string to the end of this string.</pre>
boolean	contains(CharSequence s)
	Returns true if and only if this string contains the specified sequence of char values.
boolean	<pre>contentEquals(CharSequence cs)</pre>
	Compares this string to the specified CharSequence.
boolean	<pre>contentEquals(StringBuffer sb)</pre>
	Compares this string to the specified StringBuffer.
static String	<pre>copyValueOf(char[] data)</pre>
	Returns a String that represents the character sequence in the array specified.
static String	<pre>copyValue0f(char[] data, int offset, int count) Returns a String that represents the character sequence in the array specified.</pre>
boolean	<pre>endsWith(String suffix) Tests if this string ends with the specified suffix.</pre>
boolean	<pre>equals(Object anObject)</pre>
	Compares this string to the specified object.
boolean	equalsIgnoreCase(String anotherString)
service Cautum	Compares this String to another String, ignoring case considerations.
static String	<pre>format(Locale l, String format, Object args) Returns a formatted string using the specified locale, format string, and arguments.</pre>
static String	format(String format, Object args)
Static String	Returns a formatted string using the specified format string and arguments.
byte[]	getBytes()
	Encodes this String into a sequence of bytes using the platform's default charset, storing the result into a new byte array.
byte[]	<pre>getBytes(Charset charset) Encodes this String into a sequence of bytes using the given charset, storing the result into a new byte array.</pre>
void	<pre>getBytes(int srcBegin, int srcEnd, byte[] dst, int dstBegin) Deprecated.</pre>
	This method does not properly convert characters into bytes. As of JDK 1.1, the preferred way to do this is via the <code>getBytes()</code> method, which uses the platform's default charset.
byte[]	<pre>getBytes(String charsetName)</pre>

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		Encodes this String into a sequence of bytes using the named charset, storing the result into a new byte array.
	void	<pre>getChars(int srcBegin, int srcEnd, char[] dst, int dstBegin) Copies characters from this string into the destination character array.</pre>
	int	hashCode() Returns a hash code for this string.
	int	<pre>indexOf(int ch) Returns the index within this string of the first occurrence of the specified character.</pre>
	int	<pre>indexOf(int ch, int fromIndex) Returns the index within this string of the first occurrence of the specified character, starting the search at the specified index.</pre>
	int	indexOf(String str) Returns the index within this string of the first occurrence of the specified substring.
	int	<pre>indexOf(String str, int fromIndex) Returns the index within this string of the first occurrence of the specified substring, starting at the specified index.</pre>
	String	intern() Returns a canonical representation for the string object.
	boolean	isEmpty() Returns true if, and only if, length() is 0.
	int	lastIndexOf(int ch) Returns the index within this string of the last occurrence of the specified character.
	int	lastIndexOf(int ch, int fromIndex) Returns the index within this string of the last occurrence of the specified character, searching backward starting at the specified index.
	int	lastIndexOf(String str) Returns the index within this string of the last occurrence of the specified substring.
	int	lastIndexOf(String str, int fromIndex) Returns the index within this string of the last occurrence of the specified substring, searching backward starting at the specified index.
	int	length() Returns the length of this string.
	boolean	matches(String regex) Tells whether or not this string matches the given regular expression.
	int	<pre>offsetByCodePoints(int index, int codePointOffset) Returns the index within this String that is offset from the given index by codePointOffset code points.</pre>
	boolean	<pre>regionMatches(boolean ignoreCase, int toffset, String other, int ooffset, int len) Tests if two string regions are equal.</pre>
	boolean	regionMatches(int toffset, String other, int ooffset, int len) Tests if two string regions are equal.
	String	replace(char oldChar, char newChar) Returns a new string resulting from replacing all occurrences of oldChar in this string with newChar.
	String	replace(CharSequence target, CharSequence replacement) Replaces each substring of this string that matches the literal target sequence with the specified literal replacement sequence.
	String	replaceAll(String regex, String replacement) Replaces each substring of this string that matches the given regular expression with the given replacement.
	String	replaceFirst(String regex, String replacement) Replaces the first substring of this string that matches the given regular expression with the given replacement.
	String[]	<pre>split(String regex)</pre>

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,, - 	Splits this string around matches of the given regular expression .
String[]	<pre>split(String regex, int limit)</pre>
	Splits this string around matches of the given regular expression.
boolean	<pre>startsWith(String prefix)</pre>
	Tests if this string starts with the specified prefix.
boolean	<pre>startsWith(String prefix, int toffset)</pre>
	Tests if the substring of this string beginning at the specified index starts with the specified prefix.
CharSequence	<pre>subSequence(int beginIndex, int endIndex) Returns a new character sequence that is a subsequence of this sequence.</pre>
String	<pre>substring(int beginIndex) Returns a new string that is a substring of this string.</pre>
String	<pre>substring(int beginIndex, int endIndex) Returns a new string that is a substring of this string.</pre>
char[]	toCharArray()
	Converts this string to a new character array.
String	toLowerCase()
	Converts all of the characters in this String to lower case using the rules of the default locale.
String	toLowerCase(Locale locale)
	Converts all of the characters in this String to lower case using the rules of the given Locale.
String	toString()
	This object (which is already a string!) is itself returned.
String	toUpperCase() Converts all of the characters in this String to upper case using the rules of the default locale.
String	toUpperCase(Locale locale)
	Converts all of the characters in this String to upper case using the rules of the given Locale.
String	trim()
	Returns a copy of the string, with leading and trailing whitespace omitted.
static String static String static String	<pre>valueOf(boolean b)</pre>
	Returns the string representation of the boolean argument.
	valueOf(char c)
	Returns the string representation of the char argument.
	value0f(char[] data)
static String	Returns the string representation of the char array argument. value0f(char[] data, int offset, int count)
	Returns the string representation of a specific subarray of the char array argument.
static String	<pre>valueOf(double d)</pre>
	Returns the string representation of the double argument.
static String	<pre>valueOf(float f)</pre>
	Returns the string representation of the float argument.
static String	<pre>valueOf(int i)</pre>
	Returns the string representation of the int argument.
static String	<pre>valueOf(long l)</pre>
	Returns the string representation of the long argument.
static String	<pre>valueOf(Object obj) Returns the string representation of the Object argument.</pre>

Methods inherited from class java.lang.Object

clone, finalize, getClass, notify, notifyAll, wait, wait, wait

8.3 Emacs Configuration-Competition

```
;; Default Font: Courier 10 Pitch Bold
   ;; Remember to set CUA-mode and save your options.
  (global-set-key (kbd "M-n") 'forward-paragraph)
  (global-set-key (kbd "M-p") 'backward-paragraph)
  (global-linum-mode t)
  (defun compile-cpp ()
    (interactive)
    (compile (format "g++ -o %s %s -g -lm -Wall -std=c++11" (file-name-sans-extension
   (global-set-key (kbd "<f9>") 'compile-cpp)
   (global-set-key (kbd "<f8>") 'gud-gdb)
10
   (setq default-tab-width 4)
11
  (setq c-basic-offset 4)
12
  (global-set-key (kbd "RET") 'newline-and-indent)
```