# Cox Library for Lmrpp

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# Chapter 1

# Algorithms

## 1.1 1D1D Dynamic Programming

```
// noi2009 诗人小 G
    #include<cstring>
    #include<cstdio>
    #include<cstdlib>
    using namespace std;
   #define limit (1e18)
   #define maxn 100010
   #define maxm 40
   int N,L,P,pre[maxn],top;
    char s[maxm];
    long double f[maxn];
    struct node { int l,r,key; }stack[maxn];
13
14
    inline long double qsm(int a,int b)
15
16
        long double ret = 1;
17
        while (b--) ret *= 1.0*a;
18
        return ret;
19
    }
20
    inline long double calc(int a,int b)
22
23
        return f[b]+qsm(abs(pre[a]-pre[b]-L),P);
24
    }
25
    inline int find(int a)
27
28
        int 1 = 1,r = top,mid;
29
        while (1 <= r)
30
31
            mid = (1 + r) >> 1;
32
            if (stack[mid].1 \le a \& \& stack[mid].r > = a) return stack[mid].key;
33
```

```
if (a < stack[mid].1) r = mid - 1;</pre>
34
             else l = mid + 1;
35
         }
36
    }
37
38
    inline void updata(int now)
39
    {
40
         int 1 = 1,r;
41
         while (top)
42
43
             if (calc(stack[top].1,stack[top].key) >= calc(stack[top].1,now))
44
                  --top;
45
             else
46
             {
47
                 1 = stack[top].1,r = stack[top].r;
48
                 while (1 <= r)
49
50
                      int mid = (1 + r) >> 1;
51
                      if (calc(mid,stack[top].key) >= calc(mid,now)) r = mid - 1;
52
                      else l = mid + 1;
53
                  }
54
                  stack[top].r = r;
55
                 break;
56
             }
57
         }
58
         if (1 \le N) stack[++top] = (node){1,N,now};
59
    }
60
61
    inline void dp()
62
63
        f[0] = 0;
64
         stack[top = 1] = (node) \{1,N,0\};
65
        for (int i = 1;i <= N;++i)</pre>
66
67
             int key = find(i);
68
             f[i] = calc(i,key);
69
             updata(i);
70
         }
71
    }
72
73
    int main()
74
    {
75
         freopen("1563.in","r",stdin);
76
        freopen("1563.out","w",stdout);
77
         int T; scanf("%d",&T);
78
        while (T--)
79
         {
80
             scanf("%d %d %d\n",&N,&L,&P);
81
             L++;
82
```

```
for (int i = 1;i <= N;++i)
83
            {
84
                scanf("%s",s);
85
                pre[i] = strlen(s)+1+pre[i-1];
            }
87
            dp();
            if (f[N] > limit) printf("Too hard to arrange\n");
89
            else printf("%.OLf\n",f[N]);
90
            printf("----\n");
91
92
        fclose(stdin); fclose(stdout);
93
        return 0;
94
    }
95
```

### 1.2 Dynamic Minimal Spanning Tree

```
// 每次修改一条边,每次修改一条边权值,求最小生成树
    #include<algorithm>
   #include<cstring>
    #include<vector>
    #include<iostream>
    #include<cstdio>
    #include<cstdlib>
    using namespace std;
   typedef long long 11;
10
    const int maxn = 100010; const ll inf = 1LL<<40;</pre>
11
    int N,M,Q,father[maxn],cnt[maxn],reid[maxn]; ll ans[maxn];
12
13
    inline int find(int a) { if (father[a] != a) return father[a] = find(father[a]); return
14
       father[a]; }
15
    inline int gi()
16
17
        char ch; int ret = 0,f = 1;
18
        do ch = getchar(); while (!(ch >= '0'&&ch <= '9')&&ch != '-');
19
        if (ch == '-') f = -1,ch = getchar();
20
        do ret = ret*10+ch-'0',ch = getchar(); while (ch >= '0'&&ch <= '9');
21
        return ret*f;
22
   }
23
24
    struct Edge
25
26
        int a,b,id; ll c;
27
        inline Edge() = default;
28
        inline Edge(int _a,int _b,int _id,ll _c):a(_a),b(_b),id(_id),c(_c) {}
29
        inline void read(int i) { a = gi(),b = gi(),c = gi(); id = i; }
30
        friend inline bool operator <(const Edge &x,const Edge &y) { return x.c < y.c; }
31
    }edge[22][maxn],tmp[maxn],bac[maxn];
```

```
33
    struct Operation
34
    {
35
         int x; 11 y;
36
         inline Operation() = default;
37
         inline Operation(int _x,ll _y):x(_x),y(_y) {}
38
         inline void read() { x = gi(),y = gi(); }
39
    }opt[maxn];
40
41
    inline void construct(int &tot,ll &sum)
42
    {
43
         sort(tmp+1,tmp+tot+1);
44
         for (int i = 1;i <= tot;++i)
45
             father[tmp[i].a] = tmp[i].a,father[tmp[i].b] = tmp[i].b;
46
         vector <Edge> vec;
47
         for (int i = 1;i <= tot;++i)</pre>
48
49
             int u = find(tmp[i].a), v = find(tmp[i].b);
50
             if (u != v) father[u] = v,vec.push_back(tmp[i]);
51
52
         for (int i = 0;i < (int)vec.size();++i)</pre>
53
             father[vec[i].a] = vec[i].a,father[vec[i].b] = vec[i].b;
54
         for (int i = 0;i < (int)vec.size();++i)</pre>
55
         {
56
             Edge e = vec[i];
57
             if (e.c != -inf) father[find(e.a)] = find(e.b),sum += e.c;
         }
59
         vec.clear();
60
         for (int i = 1;i <= tot;++i)</pre>
61
62
             int u = find(tmp[i].a), v = find(tmp[i].b);
63
             if (u != v)
64
65
                  tmp[i].a = u,tmp[i].b = v;
66
                  vec.push_back(tmp[i]);
67
             }
68
         }
69
         for (int i = 0;i < (int)vec.size();++i) tmp[i+1] = vec[i];</pre>
70
         for (int i = 1;i <= tot;++i) reid[tmp[i].id] = i;</pre>
71
         tot = (int)vec.size();
72
    }
73
    inline void destruct(int &tot)
75
76
         sort(tmp+1,tmp+tot+1);
77
         for (int i = 1;i <= tot;++i)</pre>
78
             father[tmp[i].a] = tmp[i].a,father[tmp[i].b] = tmp[i].b;
79
         vector <Edge> vec;
80
         for (int i = 1;i <= tot;++i)</pre>
81
```

```
{
82
             int u = find(tmp[i].a),v = find(tmp[i].b);
83
             if (u != v) father[u] = v,vec.push_back(tmp[i]);
84
             else if (tmp[i].c == inf) vec.push_back(tmp[i]);
85
86
         for (int i = 0;i < (int)vec.size();++i) tmp[i+1] = vec[i];</pre>
87
         tot = (int)vec.size();
88
    }
89
90
     inline void work(int l,int r,int dep,ll sum)
91
92
         int tot = cnt[dep];
93
         for (int i = 1;i <= tot;++i) tmp[i] = edge[dep][i];</pre>
94
         if (1 == r)
95
         {
96
             bac[opt[1].x].c = opt[1].y;
97
             for (int i = 1;i <= tot;++i)
98
             {
99
                  tmp[i].c = bac[tmp[i].id].c;
100
                  father[tmp[i].a] = tmp[i].a;
101
                  father[tmp[i].b] = tmp[i].b;
102
             }
103
             sort(tmp+1,tmp+tot+1);
104
             for (int i = 1;i <= tot;++i)</pre>
105
106
                  int u = find(tmp[i].a),v = find(tmp[i].b);
107
                  if (u != v) sum += tmp[i].c,father[u] = v;
108
             }
109
             ans[1] = sum; return;
110
111
         for (int i = 1;i <= tot;++i)
112
             tmp[i].c = bac[tmp[i].id].c,reid[tmp[i].id] = i;
113
         for (int i = 1;i <= r;++i) tmp[reid[opt[i].x]].c = -inf;</pre>
114
         construct(tot,sum);
115
         for (int i = 1;i <= r;++i)
116
             tmp[reid[opt[i].x]].c = inf;
117
         destruct(tot);
118
         for (int i = 1;i <= tot;++i) edge[dep+1][i] = tmp[i];</pre>
119
         int mid = (1+r)>>1; cnt[dep+1] = tot;
120
         work(1,mid,dep+1,sum); work(mid+1,r,dep+1,sum);
121
    }
122
123
     int main()
124
     {
125
         // freopen("B.in", "r", stdin);
126
         N = gi(), M = gi(), Q = gi();
127
         for (int i = 1;i <= M;++i) bac[i].read(i),edge[0][i] = bac[i];</pre>
128
         for (int i = 1;i <= Q;++i) opt[i].read();</pre>
129
         for (int i = 1;i <= N;++i) father[i] = i;</pre>
130
```

```
cnt[0] = M; work(1,Q,0,0);
for (int i = 1;i <= Q;++i) printf("%lld\n",ans[i]);
return 0;
</pre>
```

# 1.3 Plug-like Dynamic Programming

```
// ural 1519
    #include<cstdio>
    #include<cstdlib>
    #include<cstring>
    #include<iostream>
    #include<algorithm>
    using namespace std;
    typedef long long 11;
    const int maxn = 14,maxs = 300010;
10
    int mp[maxn] [maxn], N, M, cur, last, total[2];
11
    int size,ex,ey,head[maxs],nxt[maxs],Hash[maxs];
12
    11 f[2][maxs],state[2][maxs];
13
    inline void init()
15
16
        memset(mp,0,sizeof mp); ex = ey = 0;
17
        size = cur = 0; last = 1;
18
        total[cur] = 1;
19
        state[cur][1] = 0;
20
        f[cur][1] = 1;
21
    }
22
23
    inline void calc(ll s,ll inc)
24
25
        int pos = s%maxs;
26
        for (int i = head[pos];i;i = nxt[i])
27
            if (state[cur][Hash[i]] == s)
            {
29
                 f[cur][Hash[i]] += inc;
30
                 return;
31
            }
32
        ++total[cur];
33
        state[cur][total[cur]] = s;
34
        f[cur][total[cur]] = inc;
35
        nxt[++size] = head[pos];
36
        head[pos] = size;
37
        Hash[size] = total[cur];
38
    }
39
40
    inline 11 work()
41
    {
42
```

```
11 \text{ ret} = 0;
43
         for (int i = 1;i <= N;++i)</pre>
44
45
             for (int k = 1;k <= total[cur];++k) state[cur][k] <<= 2;</pre>
46
             for (int j = 1; j \le M; ++j)
47
48
                 memset(head,0,sizeof head);
49
                  size = 0; cur ^= 1,last ^= 1;
50
                  total[cur] = 0;
51
                  for (int k = 1;k <= total[last];++k)</pre>
52
53
                      11 s = state[last][k],num = f[last][k];
54
                      int p = (s>>((j-1)<<1))%4, q = (s>>(j<<1))%4;
55
                      if (!mp[i][j]) { if (!p\&\&!q) calc(s,num); }
56
                      else if (!p&&!q)
57
                      {
58
                           if (mp[i+1][j]\&\&mp[i][j+1])
59
                               calc(s+(1<<((j-1)<<1))+2*(1<<(j<<1)),num);
60
61
                      else if (!p&&q)
62
63
                           if (mp[i][j+1]) calc(s,num);
64
                           if (mp[i+1][j]) calc(s-q*(1<<(j<<1))+q*(1<<((j-1)<<1)),num);
65
                      }
66
                      else if (p\&\&!q)
67
68
                           if (mp[i+1][j]) calc(s,num);
69
                           if (mp[i][j+1]) calc(s-p*(1<<((j-1)<<1))+p*(1<<(j<<1)),num);
70
71
                      else if (p == 1 \& \& q == 1)
72
73
                          int b = 1;
74
                          for (int t = j+1; t \le M; ++t)
75
76
                               int v = (s >> (t << 1)) %4;
77
                               if (v == 1) ++b; else if (v == 2) --b;
78
                               if (b == 0) { s -= 1*(1<<(t<<1)); break; }
79
80
                           calc(s-(1<<((j-1)<<1))-(1<<(j<<1)),num);
81
                      }
82
                      else if (p == 2 \& \& q == 2)
83
                      {
84
                           int b = 1;
85
                          for (int t = j-2;t \ge 0;--t)
86
87
                               int v = (s >> (t << 1)) %4;
88
                               if (v == 2) ++b; else if (v == 1) --b;
89
                               if (b == 0) { s += 1*(1<<(t<1)); break; }
90
                          }
91
```

```
calc(s-2*(1<<((j-1)<<1))-2*(1<<(j<<1)),num);
92
93
                       else if (p == 1 \& q == 2) { if (i == ex \& kj == ey) ret += num; }
94
                       else if (p == 2 \& \& q == 1)
95
                            calc(s-2*(1<<((j-1)<<1))-(1<<(j<<1)),num);
96
                  }
97
              }
98
         }
99
         return ret;
100
     }
101
102
     int main()
103
104
         freopen("1519.in","r",stdin);
105
         while (scanf("%d%d",&N,&M) != EOF)
106
107
              init();
108
              for (int i = 1;i <= N;++i)</pre>
109
                   for (int j = 1; j \le M; ++j)
110
                  {
111
                       char ch; do ch = getchar(); while (ch != '.'&&ch != '*');
112
                       if (ch == '.') ex = i,ey = j,mp[i][j] = 1;
113
114
              cout << work() << endl;</pre>
115
         }
116
         return 0;
117
     }
118
```

## 1.4 Slop Optimization

```
#include<algorithm>
   #include<cstring>
   #include<iostream>
   #include<cstdio>
   #include<cstdlib>
   using namespace std;
   typedef long long 11;
   const int maxn = 500010; const ll inf = 1LL<<60;</pre>
   int N,K,A[maxn]; ll pre[maxn],f[maxn];
10
11
   struct Point
12
   {
13
       11 x,y;
14
        inline Point() = default;
15
        inline Point(11 _x,11 _y):x(_x),y(_y) {}
16
       friend inline Point operator -(const Point &a,const Point &b) { return
17
    → Point(a.x-b.x,a.y-b.y); }
        friend inline 11 operator /(const Point &a,const Point &b) { return a.x*b.y-a.y*b.x; }
```

```
};
19
20
    inline ll calc(const Point &a,int b) { return -a.x*b+a.y; }
21
22
    struct Queue
23
24
        Point array[maxn]; int h,t;
25
        inline Queue() = default;
26
        inline void init() { h = t = 0; }
27
        inline void pop_front(int i) { while (t-h >= 2&&calc(array[h+1],i) > calc(array[h+2],i))
28
     inline void push(const Point &a,int i) { while (t-h >=
29
        2kk(a-array[t-1])/(array[t]-array[t-1]) >= 0) --t; array[++t] = a; 
        inline Point front() const { return array[h+1]; }
30
31
    }team;
32
    inline int gi()
33
34
        char ch; int ret = 0,f = 1;
35
        do ch = getchar(); while (!(ch >= '0'&&ch <= '9')&&ch != '-');
36
        if (ch == '-') f = -1, ch = getchar();
37
        do ret = ret*10+ch-'0',ch = getchar(); while (ch >= '0'&&ch <= '9');
38
        return ret*f;
39
    }
40
41
    int main()
42
    {
43
        // freopen("E.in", "r", stdin);
44
        for (int T = gi();T--;)
45
46
             N = gi(), K = gi(); team.init();
47
             for (int i = 1;i <= N;++i) A[i] = gi();</pre>
48
             for (int i = 1;i <= N;++i) pre[i] = pre[i-1]+A[i];</pre>
49
             for (int i = 1;i <= N;++i)</pre>
50
             {
51
                 if (i >= K)
52
                 {
53
                     if (f[i-K] != inf)
54
                          team.push(Point(A[i-K+1],f[i-K]-pre[i-K]+(11)(i-K)*A[i-K+1]),i);\\
55
                     team.pop_front(i);
56
                     f[i] = calc(team.front(),i)+pre[i];
57
                 }
58
                 else f[i] = inf;
59
             }
60
             cout << f[N] << endl;</pre>
61
62
        return 0;
63
    }
64
```

#### 1.5 Three-dimension Partial Order

```
//三维偏序, CDQ 分治
    #define lowbit(a) (a&-a)
    int M,N,A,B,tree[maxn];
    inline void ins(int a,int b) { for (;a < maxn;a += lowbit(a)) tree[a] = max(tree[a],b); }</pre>
    inline void clear(int a) { for (;a < maxn;a += lowbit(a)) tree[a] = 0; }</pre>
    inline int calc(int a) { int ret = 0; for (;a;a -= lowbit(a)) ret = max(tree[a],ret); return

    ret; }

    struct Node
10
        int x,y,z,res;
11
        inline Node(int x = 0,int y = 0,int z = 0,int z = 0):x(x),y(y),z(z),res(res) {}
12
        inline void update() { ++x,++y,++z; }
13
    }E[maxn];
14
15
    inline bool cmpx(const Node &a,const Node &b)
16
17
        if (a.x != b.x) return a.x < b.x;</pre>
18
        else if (a.y != b.y) return a.y > b.y;
19
        else return a.z > b.z;
20
    }
21
    inline bool cmpy(const Node &a,const Node &b) { return a.y < b.y; }</pre>
22
23
    inline void work(int l,int r)
24
    {
25
        if (1 == r) { E[1].res = max(E[1].res,1); return; }
26
        int mid = (1+r) >> 1,p = 1;
27
        work(1,mid);
28
        sort(E+1,E+mid+1,cmpy);
29
        sort(E+mid+1,E+r+1,cmpy);
30
        for (int i = mid+1;i <= r;++i)</pre>
31
32
            for (;p <= mid\&\&E[p].y < E[i].y;++p) ins(E[p].z,E[p].res);
33
            E[i].res = max(E[i].res, calc(E[i].z-1)+1);
34
35
        while (p > 1) clear(E[--p].z);
36
        sort(E+mid+1,E+r+1,cmpx);
37
        work(mid+1,r);
38
    }
39
40
    inline int run()
41
42
        for (int i = 1;i <= N+M;++i) E[i].update();</pre>
43
        sort(E+1,E+N+M+1,cmpx); work(1,N+M);
44
        int ret = 0;
45
        for (int i = 1;i <= N+M;++i) ret = max(ret,E[i].res);</pre>
46
        return ret;
47
```

48 }

# Chapter 2

# Computational Geometry

#### 2.1 Circle Intersection

```
//modified
    const double eps = 1e-7,pi = acos(-1.0);
    int N,M; double area[maxn]; // area[k] \rightarrow area of intersections >= k.
   inline int dcmp(double a)
        if (-eps <= a&&a <= eps) return 0;
        else if (a > 0) return 1; else return -1;
   }
9
10
   struct Point
11
12
        double x,y;
13
        inline Point() = default;
14
        inline Point(double _x,double _y):x(_x),y(_y) {}
15
        inline void read() { x = gi(),y = gi(); }
16
        inline double norm() const { return sqrt(x*x+y*y); }
17
        inline double angle() const { return atan2(y,x); }
        inline Point unit() const { double len = norm(); return Point(x/len,y/len); }
19
        friend inline Point operator-(const Point &a,const Point &b) { return
    → Point(a.x-b.x,a.y-b.y); }
        friend inline Point operator+(const Point &a,const Point &b) { return
21
    → Point(a.x+b.x,a.y+b.y); }
        friend inline Point operator*(const Point &a, double b) { return Point(a.x*b,a.y*b); }
22
        friend inline Point operator*(double b,const Point &a) { return Point(a.x*b,a.y*b); }
23
        friend inline Point operator/(const Point &a,double b) { return Point(a.x/b,a.y/b); }
24
        friend inline double operator/(const Point &a,const Point &b) { return a.x*b.y-a.y*b.x; }
25
   };
26
   struct Circle
27
        Point C; double r; int sgn;
29
        inline Circle() = default;
30
```

```
inline Circle(const Point &_C,double _r,int _sgn):C(_C),r(_r),sgn(_sgn) {}
31
        // sgn 代表该圆的权值, 默认 1
        friend inline bool operator == (const Circle &a, const Circle &b)
32
33
            if (dcmp(a.r-b.r)) return false;
34
            if (dcmp(a.C.x-b.C.x)) return false;
35
            if (dcmp(a.C.y-b.C.y)) return false;
36
            if (a.sgn != b.sgn) return false;
37
            return true;
38
39
        friend inline bool operator!=(const Circle &a,const Circle &b) { return !(a == b); }
40
    }cir[maxn];
41
42
    inline Point rotate(const Point &p,double cost,double sint)
43
44
    {
        double x = p.x, y = p.y;
45
        return Point(x*cost-y*sint,x*sint+y*cost);
46
    }
47
    inline pair <Point,Point> crosspoint(const Point &ap,double ar,const Point &bp,double br)
48
49
        double d = (ap-bp).norm(),cost = (ar*ar+d*d-br*br)/(2*ar*d),sint = sqrt(1-cost*cost);
50
        Point v = ((bp-ap).unit())*ar;
51
        return make_pair(ap+rotate(v,cost,-sint),ap+rotate(v,cost,sint));
52
    }
53
    inline pair <Point,Point> crosspoint(const Circle &a,const Circle &b) { return
54
        crosspoint(a.C,a.r,b.C,b.r); }
55
    inline bool overlap(const Circle &a,const Circle &b) { return dcmp(a.r-b.r-(a.C-b.C).norm()) >=
56
    → 0; } // b 是不是在 a 里面
    inline bool intersect(const Circle &a,const Circle &b)
57
    {
58
        if (overlap(a,b)) return false;
59
        if (overlap(b,a)) return false;
60
        return dcmp((a.C-b.C).norm()-a.r-b.r) < 0;
61
    }
62
63
    struct Event
64
65
        Point p; double a; int d;
66
        inline Event() = default;
67
        in line \ \ Event(const \ Point \ \&\_p, \\ double \ \_a, \\ double \ \_d): p(\_p), a(\_a), d(\_d) \ \{\}
68
        friend inline bool operator <(const Event &a,const Event &b) { return a.a < b.a; }
69
70
    };
71
    inline void solve()
72
73
        for (int i = 1;i <= M;++i) area[i] = 0;</pre>
74
        for (int i = 1;i <= M;++i)</pre>
75
76
```

```
int cnt = cir[i].sgn; if (cnt<0) cnt = 0; vector <Event> event;
77
             for (int j = 1; j < i; ++j) if (cir[i] == cir[j]) cnt += cir[j].sgn;
78
             for (int j = 1; j \le M; ++j)
79
                 if (j != i\&\&cir[i] != cir[j]\&\&overlap(cir[j],cir[i])) cnt += cir[j].sgn;
80
             for (int j = 1; j \le M; ++j)
81
                 if (j != i&&intersect(cir[i],cir[j]))
82
                 ł
83
                      pair <Point,Point> res = crosspoint(cir[i],cir[j]); swap(res.first,res.second);
84
                      double alpha1 = (res.first-cir[i].C).angle(),alpha2 =
85
         (res.second-cir[i].C).angle();
                      event.push_back(Event(res.second,alpha2,cir[j].sgn));
86
                      event.push_back(Event(res.first,alpha1,-cir[j].sgn));
87
                      cnt += (alpha2 > alpha1)*cir[j].sgn;
88
                 }
89
             if (!event.size()) area[cnt] += pi*cir[i].r*cir[i].r*cir[i].sgn;
90
             else
91
             {
92
                 sort(event.begin(),event.end());
93
                 event.push_back(event.front());
94
                 for (int j = 0; j+1 < (int)event.size(); ++j)
95
                 {
96
                      cnt += event[j].d;
97
                      area[cnt] += event[j].p/event[j+1].p/2*cir[i].sgn;
98
                      double alpha = event[j+1].a-event[j].a;
99
                      if (alpha < 0) alpha += 2*pi;</pre>
100
                      if (!dcmp(alpha)) continue;
101
                      area[cnt] += alpha*cir[i].r*cir[i].r/2*cir[i].sgn;
102
                      area[cnt] += -sin(alpha)*cir[i].r*cir[i].r/2*cir[i].sgn;
103
                 }
104
             }
105
         }
106
    }
107
108
    // origin
109
    struct Event {
110
         Point p;
111
         double ang;
112
         int delta;
113
         Event (Point p = Point(0, 0), double ang = 0, double delta = 0) : p(p), ang(ang),
114
         delta(delta) {}
    };
115
    bool operator < (const Event &a, const Event &b) {</pre>
116
         return a.ang < b.ang;
117
    }
118
    void addEvent(const Circle &a, const Circle &b, vector<Event> &evt, int &cnt) {
119
         double d2 = (a.o - b.o).len2(),
120
                dRatio = ((a.r - b.r) * (a.r + b.r) / d2 + 1) / 2,
121
                pRatio = sqrt(-(d2 - sqr(a.r - b.r)) * (d2 - sqr(a.r + b.r)) / (d2 * d2 * 4));
122
         Point d = b.o - a.o, p = d.rotate(PI / 2),
123
```

```
q0 = a.o + d * dRatio + p * pRatio,
124
               q1 = a.o + d * dRatio - p * pRatio;
125
         double ang 0 = (q0 - a.o).ang(),
126
                ang1 = (q1 - a.o).ang();
127
         evt.push_back(Event(q1, ang1, 1));
128
         evt.push_back(Event(q0, ang0, -1));
129
         cnt += ang1 > ang0;
130
    }
131
    bool issame(const Circle &a, const Circle &b) { return sign((a.o - b.o).len()) == 0 && sign(a.r
132
     \hookrightarrow - b.r) == 0; }
    bool overlap(const Circle &a, const Circle &b) { return sign(a.r - b.r - (a.o - b.o).len()) >=
133
     → 0; }
    bool intersect(const Circle &a, const Circle &b) { return sign((a.o - b.o).len() - a.r - b.r) <</pre>
134
     Circle c[N];
135
    double area[N]; // area[k] \rightarrow area of intersections >= k.
136
    Point centroid[N]; //k 次圆的质心
137
    bool keep[N];
138
    void add(int cnt, DB a, Point c) {
139
         area[cnt] += a;
140
         centroid[cnt] = centroid[cnt] + c * a;
141
    }
142
    void solve(int C) {
143
         for (int i = 1; i <= C; ++ i) {
144
             area[i] = 0;
145
             centroid[i] = Point(0, 0);
146
         }
147
         for (int i = 0; i < C; ++i) {
148
             int cnt = 1;
149
             vector<Event> evt;
150
             for (int j = 0; j < i; ++j) if (issame(c[i], c[j])) ++cnt;
151
             for (int j = 0; j < C; ++j) {
152
                 if (j != i \&\& !issame(c[i], c[j]) \&\& overlap(c[j], c[i])) {
153
                      ++cnt;
154
                 }
155
             }
156
             for (int j = 0; j < C; ++j) {
157
                 if (j != i && !overlap(c[j], c[i]) && !overlap(c[i], c[j]) && intersect(c[i], c[j]))
158
         {
                      addEvent(c[i], c[j], evt, cnt);
159
                 }
160
             }
161
             if (evt.size() == Ou) {
162
                 add(cnt, PI * c[i].r * c[i].r, c[i].o);
163
             } else {
164
                 sort(evt.begin(), evt.end());
165
                 evt.push_back(evt.front());
166
                 for (int j = 0; j + 1 < (int)evt.size(); ++j) {</pre>
167
                      cnt += evt[j].delta;
168
```

```
add(cnt, det(evt[j].p, evt[j + 1].p) / 2, (evt[j].p + evt[j + 1].p) / 3);
169
                      double ang = evt[j + 1].ang - evt[j].ang;
170
                      if (ang < 0) {
171
                          ang += PI * 2;
172
173
                      if (sign(ang) == 0) continue;
174
                      double ang0 = evt[j].a,ang1 = evt[j+1].a;
175
                      add(cnt, ang * c[i].r * c[i].r / 2, c[i].o +
176
                          Point(sin(ang1) - sin(ang0), -cos(ang1) + cos(ang0)) * (2 / (3 * ang) *
177
         c[i].r));
                      add(cnt, -sin(ang) * c[i].r * c[i].r / 2, (c[i].o + evt[j].p + evt[j + 1].p) /
178
         3);
                 }
179
             }
180
181
         for (int i = 1; i <= C; ++ i)
182
             if (sign(area[i])) {
183
                 centroid[i] = centroid[i] / area[i];
184
185
    }
186
```

#### 2.2 Common Formulas

```
//计算几何常用公式
    inline int dcmp(double a)
    {
        if (fabs(a) <= eps) return 0;</pre>
        else if (a > 0) return 1;
        else return -1;
    struct Point
9
        double x,y;
10
        inline Point() = default;
11
        inline Point(double _x,double _y):x(_x),y(_y) {}
12
        inline Point unit() const
13
14
            double len = norm();
15
            if (!dcmp(len)) return Point(1,0);
16
            else return *this/len;
17
18
        inline double norm() const { return sqrt(x*x+y*y); }
19
        inline Point reflect(const Point &p) const
20
        {
21
            Point v = *this-p; double len = v.norm();
22
            v = v/len; return p+v*(1/len);
23
        }
24
        inline void read() { scanf("%lf %lf",&x,&y); }
25
        inline Point vertical() const { return Point(y,-x); }
26
```

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```
inline double angle() const
27
        {
28
            double ret = atan2(y,x);
29
            if (ret < 0) ret += 2*pi;</pre>
30
            return ret;
31
32
        friend inline bool operator == (const Point &a, const Point &b) { return
33
        !dcmp(a.x-b.x)&&!dcmp(a.y-b.y); }
        friend inline Point operator -(const Point &a,const Point &b) { return
34
       Point(a.x-b.x,a.y-b.y); }
        friend inline Point operator +(const Point &a,const Point &b) { return
35
    → Point(a.x+b.x,a.y+b.y); }
        friend inline Point operator /(const Point &a,double b) { return Point(a.x/b,a.y/b); }
36
        friend inline Point operator *(const Point &a,double b) { return Point(a.x*b,a.y*b); }
37
        friend inline Point operator *(double b,const Point &a) { return Point(a.x*b,a.y*b); }
38
        friend inline double operator /(const Point &a,const Point &b) { return a.x*b.y-a.y*b.x; }
39
   };
40
   struct Line
41
42
    {
        Point p,v; double slop;
43
        inline Line() = default;
44
        inline Line(const Point &_p,const Point &_v):p(_p),v(_v) \{\}
45
        inline void update() { slop = v.alpha(); }
46
        friend inline bool operator <(const Line &11,const Line &12)
47
        { return l1.slop < l2.slop; }
48
        inline double dis(const Point &a) { fabs((a-p)/v)/(v.len()); } //点到直线距离
49
50
   };
51
    inline bool OnLine(const Line &1,const Point &p) { return !dcmp(1.v/(p-1.p)); } //点在直线上
52
53
    inline Point CrossPoint(const Line &a,const Line &b) //直线交点
54
    {
55
        Point u = a.p - b.p;
56
        double t = (b.v/u)/(a.v/b.v);
57
        return a.p+a.v*t;
58
   }
59
60
    inline bool parallel(const Line &a,const Line &b) { return !dcmp(a.v/b.v); } //直线平行
61
```

#### 2.3 Convex Hull

```
struct Point

find in the point in the
```

```
else return *this/len;
9
10
        inline double norm() const { return sqrt(x*x+y*y); }
11
        inline Point reflect(const Point &p) const
12
13
            Point v = *this-p; double len = v.norm();
14
            v = v/len; return p+v*(1/len);
15
16
        inline void read() { scanf("%lf %lf",&x,&y); }
17
        inline Point vertical() const { return Point(y,-x); }
18
        inline double angle() const
19
        {
20
            double ret = atan2(y,x);
21
            if (ret < 0) ret += 2*pi;</pre>
22
            return ret;
23
24
        friend inline bool operator ==(const Point &a,const Point &b) { return
25
        !dcmp(a.x-b.x)&&!dcmp(a.y-b.y); }
        friend inline Point operator -(const Point &a,const Point &b) { return
26
     → Point(a.x-b.x,a.y-b.y); }
        friend inline Point operator +(const Point &a,const Point &b) { return
27
     → Point(a.x+b.x,a.y+b.y); }
        friend inline Point operator /(const Point &a,double b) { return Point(a.x/b,a.y/b); }
28
        friend inline Point operator *(const Point &a,double b) { return Point(a.x*b,a.y*b); }
29
        friend inline Point operator *(double b,const Point &a) { return Point(a.x*b,a.y*b); }
30
        friend inline double operator /(const Point &a,const Point &b) { return a.x*b.y-a.y*b.x; }
31
        friend inline bool operator <(const Point &a,const Point &b)
32
33
            if (a.x != b.x) return a.x < b.x;</pre>
34
            else return a.y < b.y;</pre>
35
36
    }P[maxn],convex[maxn];
37
38
    inline void ConvexHull()
39
    {
40
        sort(P+1,P+N+1); //x 第一关键字, y 第二关键字从小到大排序
41
        for (int i = 1;i <= N;++i)</pre>
42
43
            while (m > 1\&\&(convex[m]-convex[m-1])/(P[i]-convex[m-1]) <= 0) --m;
44
            convex[++m] = P[i];
45
        }
46
        int k = m;
47
        for (int i = N-1; i; --i)
48
49
            while (m > k \& \& (convex[m] - convex[m-1]) / (P[i] - convex[m-1]) <= 0) --m;
50
            convex[++m] = P[i];
51
        }
52
        if (N > 1) m--;
53
    }
54
```

#### 2.4 Cross Points of Circles

```
//圆圆求交,需先判定两圆有交
   inline Point rotate(const Point &p,double cost,double sint)
       double x = p.x,y = p.y;
       return Point(x*cost-y*sint,x*sint+y*cost);
   }
   inline pair <Point,Point> CrossPoint(const Point &ap,double ar,const Point &bp,double br)
       double d = (ap-bp).norm();
10
       double cost = (ar*ar+d*d-br*br)/(2*ar*d),sint = sqrt(1-cost*cost);
11
       Point v = ((bp-ap)/(bp-ap).norm())*ar;
12
       return make_pair(ap+rotate(v,cost,-sint),ap+rotate(v,cost,sint));
13
   }
14
```

### 2.5 Cross Points of Line and Circle

```
//a b 直线两点, o 圆心
   //若 a b 为线段,则 0 <= t1,t2 <= 1
   inline void CrossPoint(const Point &a,const Point &b,const Point &o,double r,Point *ret,int
        &num)
   {
        double XO = o.x, YO = o.y;
        double X1 = a.x,Y1 = a.y;
        double X2 = b.x, Y2 = b.y;
        double dx = X2-X1, dy = Y2-Y1;
        double A = dx*dx+dy*dy;
        double B = 2*dx*(X1-X0)+2*dy*(Y1-Y0);
10
        double C = (X1-X0)*(X1-X0)+(Y1-Y0)*(Y1-Y0)-r*r;
11
        double delta = B*B-4*A*C+eps;
12
        num = 0;
13
        if (delta >= 0)
14
15
            double t1 = (-B-sqrt(delta))/(2*A);
16
            double t2 = (-B+sqrt(delta))/(2*A);
17
            ret[++num] = Point(X1+t1*dx,Y1+t1*dy);
            ret[++num] = Point(X1+t2*dx,Y1+t2*dy);
19
        }
20
   }
21
```

# 2.6 Graham Scanning Algorithm

```
1 //凸包上最大四边形面积
2 #include<cmath>
3 #include<algorithm>
4 #include<cstring>
5 #include<iostream>
```

```
#include<cstdio>
    #include<cstdlib>
    using namespace std;
    const int maxn = 2010;
10
    int N,M; double ans;
11
12
    struct Point
13
14
        double x,y;
15
        Point() = default;
16
        Point(double _x,double _y):x(_x),y(_y) {}
17
        inline void read() { scanf("%lf %lf",&x,&y); }
18
        friend inline Point operator -(const Point &a,const Point &b) { return
19
     → Point(a.x-b.x,a.y-b.y); }
        friend inline double operator /(const Point &a,const Point &b) { return a.x*b.y-a.y*b.x; }
20
        friend inline double operator <(const Point &a,const Point &b)
21
22
            if (a.x != b.x) return a.x < b.x;</pre>
23
            else return a.y < b.y;</pre>
24
25
    }P[maxn],convex[maxn];
26
27
    inline int gi()
28
29
        char ch; int ret = 0,f = 1;
30
        do ch = getchar(); while (!(ch >= '0'&&ch <= '9')&&ch != '-');
31
        if (ch == '-') f = -1,ch = getchar();
32
        do ret = ret*10+ch-'0',ch = getchar(); while (ch >= '0'&&ch <= '9');
33
        return ret*f;
34
    }
35
36
    inline void ConvexHull()
37
    {
38
        int m = 0;
39
        sort(P+1,P+N+1); //x 第一关键字, y 第二关键字从小到大排序
40
        for (int i = 1;i <= N;++i)</pre>
41
42
            while (m > 1\&\&(convex[m]-convex[m-1])/(P[i]-convex[m-1]) <= 0) --m;
43
            convex[++m] = P[i];
44
        }
45
        int k = m;
46
        for (int i = N-1; i; --i)
47
48
            while (m > k \& \& (convex[m]-convex[m-1])/(P[i]-convex[m-1]) \le 0) --m;
49
            convex[++m] = P[i];
50
51
        if (N > 1) m--; M = m;
52
    }
53
```

```
54
    inline void Graham()
55
56
        for (int i = 1;i <= M;++i) convex[i+M] = convex[i];</pre>
57
        int p1,p2,p3,p4;
58
        for (p1 = 1;p1 <= M;++p1)
59
60
            p2 = p1+1;
61
            p3 = p2+1;
62
            p4 = p3+1;
63
            for (;p3 < p1+M-1;++p3)
64
65
                Point v = convex[p3]-convex[p1];
66
                while (p2 < p3\&\&fabs((convex[p2]-convex[p1])/v) <
67
         fabs((convex[p2+1]-convex[p1])/v)) ++p2;
                while (p4 < p1+M\&\&fabs((convex[p4]-convex[p1])/v) <
68
         fabs((convex[p4+1]-convex[p1])/v)) ++p4;
                ans = max(ans,fabs((convex[p2]-convex[p1])/v)+fabs((convex[p4]-convex[p1])/v));
69
            }
70
        }
71
        ans = ans/2;
72
    }
73
74
    int main()
75
76
        N = gi();
77
        for (int i = 1;i <= N;++i) P[i].read();</pre>
78
        ConvexHull();
79
        Graham();
80
        printf("%.3f\n",ans);
81
        return 0;
82
    }
83
    84
    inline void jam() //凸包上最大四边形面积
85
    {
86
        for (int i = 1;i <= m;++i) ch[i+m] = ch[i]; //凸包倍长
87
        for (int p1 = 1,p2,p3,p4;p1 <= m;++p1)</pre>
88
89
            p2 = p1 + 1;
90
            p3 = p2 + 1;
91
            p4 = p3 + 1;
92
            for (;p3 < p1 + m - 1;++p3)
93
            {
94
                Line 1 = ((SEG) { ch[p1],ch[p3] }).extend();//枚举对角线,线段变成直线
95
                while (p2 < p3 && 1.dis(ch[p2]) < 1.dis(ch[p2 + 1])) ++p2;//点到直线距离
96
                while (p4 < p1 + m \&\& 1.dis(ch[p4]) < 1.dis(ch[p4 + 1])) ++p4;
97
                ans = max(ans,(1.dis(ch[p2])+1.dis(ch[p4]))*(ch[p1] - ch[p3]).len()/2);//更新答案
98
            }
99
        }
100
```

101 }

#### 2.7 Half Plane Intersection

```
//半平面交,直线左侧半平面,注意最后是 tail-head <= 0 还是 tail-head <= 1
   inline int dcmp(double a)
   ₹
        if (-eps <= a&&a <= eps) return 0;</pre>
        else if (a > 0) return 1; else return -1;
   }
   struct Point
9
10
        double x,y;
        inline Point() = default;
11
        inline Point(double _x,double _y):x(_x),y(_y) {}
12
        inline void read() { x = gi(),y = gi(); }
13
        inline Point vertical() const { return Point(-y,x); }
14
        inline Point unit() const
15
16
            double len = norm();
17
            if (!dcmp(len)) return Point(1,0);
18
            else return *this/len:
19
        }
20
        inline double norm() const { return sqrt(x*x+y*y); }
21
        inline double angle() const { return atan2(y,x); }
22
        friend inline Point operator+(const Point &a,const Point &b) { return
23
    → Point(a.x+b.x,a.y+b.y); }
        friend inline Point operator-(const Point &a,const Point &b) { return
24
    → Point(a.x-b.x,a.y-b.y); }
        friend inline Point operator*(const Point &a, double b) { return Point(a.x*b,a.y*b); }
25
        friend inline Point operator*(double b,const Point &a) { return Point(a.x*b,a.y*b); }
26
        friend inline double operator/(const Point &a,const Point &b) { return a.x*b.y-a.y*b.x; }
27
    }P[maxn],pp[maxn],pol[maxn];
28
29
    struct Line
30
31
        Point p,v;
32
        inline Line(const Point _p = Point(),const Point _v = Point()):p(_p),v(_v) {}
33
        inline double slop() const { return v.angle(); }
34
        friend inline bool operator < (const Line &a, const Line &b) { return a.slop() < b.slop(); }
35
    }line[maxn],qq[maxn];
36
37
   inline bool onleft(const Line &L,const Point &p)
38
39
        return dcmp(L.v/(p-L.p)) > 0;
40
   }
41
    inline bool parallel(const Line &a,const Line &b) { return !dcmp(a.v/b.v); }
42
    inline Point crosspoint(const Line &a,const Line &b)
43
```

```
{
44
        Point u = a.p-b.p;
45
        double t = (b.v/u)/(a.v/b.v);
46
        return a.p+(a.v*t);
47
48
49
    inline int half_plane_intersection()
50
51
        sort(lines+1,lines+tot+1); //直线按斜率排序
52
        int head,tail;
53
        qq[head = tail = 1] = lines[1];
54
        for (int i = 2;i <= tot;++i)</pre>
55
56
             while (head < tail&&!onleft(lines[i],pp[tail-1])) --tail;</pre>
57
             while (head < tail&&!onleft(lines[i],pp[head])) ++head;</pre>
58
             qq[++tail] = lines[i];
59
             if (parallel(qq[tail],qq[tail-1]))
60
             {
61
                 tail--;
62
                 if (onleft(qq[tail],lines[i].p)) qq[tail] = lines[i];
63
64
             if (head < tail) pp[tail-1] = crosspoint(qq[tail],qq[tail-1]);</pre>
65
66
        while (head < tail && !onleft(qq[head],pp[tail-1])) --tail;</pre>
67
        if (tail-head <= 0) return 0;</pre>
68
        pp[tail] = crosspoint(qq[tail],qq[head]);
69
        for (int i = head;i <= tail;++i) pol[++m] = pp[i]; //半平面交点
70
        pol[0] = pol[m];
        return m;
72
    }
73
```

# 2.8 Intersecting Area of Circle and Polygon

```
const int maxn = 510;
    const double eps = 1e-9;
   inline int dcmp(double a)
        if (a > eps) return 1;
        else if (a < -eps) return -1;
        else return 0;
   }
9
10
   struct Point
11
12
        double x,y;
13
        Point() = default;
14
        Point(double _x,double _y):x(_x),y(_y) {}
15
        inline double norm() const { return sqrt(x*x+y*y); }
16
```

```
inline Point unit() const { double len = norm(); return Point(x/len,y/len); }
17
        friend Point operator +(const Point &a,const Point &b) { return Point(a.x+b.x,a.y+b.y); }
18
        friend Point operator -(const Point &a,const Point &b) { return Point(a.x-b.x,a.y-b.y); }
19
        friend Point operator *(const Point &a,double b) { return Point(a.x*b,a.y*b); }
20
        friend Point operator *(double b,const Point &a) { return Point(a.x*b,a.y*b); }
21
        friend Point operator /(const Point &a,double b) { return Point(a.x/b,a.y/b); }
22
        friend double operator /(const Point &a,const Point &b) { return a.x*b.y-b.x*a.y; }
23
        friend double operator *(const Point &a,const Point &b) { return a.x*b.x+a.y*b.y; }
24
        inline void read() { scanf("%lf %lf",&x,&y); }
25
    }P[maxn].A.B:
26
    int N; double K;
27
28
    inline double getSectorArea(const Point &a,const Point &b,double r)
29
30
        double c = (2*r*r-((a-b)*(a-b)))/(2*r*r);
31
        double alpha = acos(c);
32
        return r*r*alpha/2.0;
33
    }
34
35
    inline pair <double, double > getSolution(double a, double b, double c)
36
37
        double delta = b*b-4*a*c;
38
        if (dcmp(delta) < 0) return make_pair(0,0);</pre>
39
        else return make_pair((-b-sqrt(delta))/(2*a),(-b+sqrt(delta))/(2*a));
40
    }
41
42
    inline pair <Point, Point > getIntersection(const Point &a,const Point &b,double r)
43
44
        Point d = b-a;
45
        double A = d*d, B = 2*(d*a), C = (a*a)-r*r;
46
        pair <double, double> s = getSolution(A,B,C);
47
        return make_pair(a+(d*s.first),a+(d*s.second));
48
    }
49
    inline double getPointDist(const Point &a,const Point &b)
51
52
        Point d = b-a;
53
        int sA = dcmp(a*d),sB = dcmp(b*d);
54
        if (sA*sB \le 0) return (a/b)/((a-b).norm());
55
        else return min(a.norm(),b.norm());
56
    }
57
    double getArea(const Point &a,const Point &b,double r)
59
60
        double dA = a*a,dB = b*b,dC = getPointDist(a,b),ans = 0;
61
        if (dcmp(dA-r*r) \le 0 \& \& dcmp(dB-r*r) \le 0) return (a/b)/2;
62
        Point tA = a.unit()*r,tB = b.unit()*r;
63
        if (dcmp(dC-r) > 0) return getSectorArea(tA,tB,r);
64
        pair <Point,Point> ret = getIntersection(a,b,r);
65
```

```
if (dcmp(dA-r*r) > 0\&\&dcmp(dB-r*r) > 0)
66
67
            ans += getSectorArea(tA,ret.first,r);
68
            ans += (ret.first/ret.second)/2;
69
            ans += getSectorArea(ret.second,tB,r);
70
            return ans;
71
        }
72
        if (dcmp(dA-r*r) > 0) return (ret.first/b)/2+getSectorArea(tA,ret.first,r);
73
        else return (a/ret.second)/2.0+getSectorArea(ret.second,tB,r);
74
    }
75
76
    double getArea(int n,Point *p,const Point &c,double r)
78
        double ret = 0;
79
        for (int i = 0; i < n; ++i)
80
81
            int sgn = dcmp((p[i]-c)/(p[(i+1)\%n]-c));
82
            if (sgn > 0) ret += getArea(p[i]-c,p[(i+1)%n]-c,r);
83
            else ret -= getArea(p[(i+1)%n]-c,p[i]-c,r);
84
85
        return fabs(ret);
86
    }
87
```

### 2.9 Intersection of Line and Convex Hull

```
//O(logN)
    inline double getA(const Node &a)
        double ret = atan2(a.y,a.x);
         if (ret \leftarrow -pi/2) ret += 2*pi;
        return ret;
    }
    inline int find(double x)
10
        if (x \le w[1] | |x >= w[m]) return 1;
11
        return upper_bound(w+1,w+m+1,x)-w;
12
    }
13
14
    inline bool intersect(const Node &a,const Node &b)
15
16
         int i = find(getA(b-a)),j = find(getA(a-b));
17
        if (dcmp((b-a)/(hull[i]-a))*dcmp((b-a)/(hull[j]-a)) > 0) return false;
18
         else return true;
19
    }
20
21
    inline void convex()
22
23
        for (int i = 1;i <= N;++i)</pre>
24
```

```
{
25
             while (m > 1\&\&(hull[m]-hull[m-1])/(P[i]-hull[m-1]) <= 0) --m;
26
             hull[++m] = P[i];
27
         }
28
         int k = m;
29
        for (int i = N-1; i; --i)
30
31
             while (m > k\&\&(hull[m]-hull[m-1])/(P[i]-hull[m-1]) \ll 0) --m;
32
             hull[++m] = P[i];
33
         }
34
         if (N > 1) m--;
35
         for (int i = 1;i <= m;++i)</pre>
36
             w[i]= getA(hull[i+1]-hull[i]);
37
    }
38
```

#### 2.10 Minimal Product

```
// 最小乘积匹配
    #include<algorithm>
    #include<cstring>
    #include<iostream>
    #include<cstdio>
    #include<cstdlib>
    using namespace std;
    const int maxn = 80,inf = 1<<29;</pre>
    int N,ans,A[maxn][maxn],B[maxn][maxn];
10
11
    inline int gi()
12
    {
13
        char ch; int ret = 0,f = 1;
14
        do ch = getchar(); while (!(ch >= '0'&&ch <= '9')&&ch != '-');
15
        if (ch == '-') f = -1,ch = getchar();
16
        do ret = ret*10+ch-'0',ch = getchar(); while (ch >= '0'&&ch <= '9');
17
        return ret*f;
18
    }
19
20
    struct KM
21
22
        int w[maxn] [maxn], lx[maxn], ly[maxn], match[maxn], way[maxn], slack[maxn]; bool used[maxn];
23
24
        inline void init()
25
        {
26
            for (int i = 1;i <= N;++i)</pre>
27
                match[i] = lx[i] = ly[i] = way[i] = 0;
        }
29
30
        inline void hungary(int x)
31
        {
32
```

```
match[0] = x; int j0 = 0;
33
             for (int j = 0; j \le N; ++j)
34
                  slack[j] = -inf,used[j] = false;
35
             do
36
             {
37
                 used[j0] = true;
38
                  int i0 = match[j0], delta = -inf, j1 = 0;
39
                  for (int j = 1; j \leftarrow N; ++j)
40
                      if (!used[j])
41
                      {
42
                           int cur = -w[i0][j]-lx[i0]-ly[j];
43
                           if (cur > slack[j]) slack[j] = cur,way[j] = j0;
44
                           if (slack[j] > delta) delta = slack[j],j1 = j;
45
                      }
46
                  for (int j = 0; j \le N; ++j)
47
                  {
48
                      if (used[j]) lx[match[j]] += delta,ly[j] -= delta;
49
                      else slack[j] -= delta;
50
                 }
51
                  j0 = j1;
52
             }
53
             while (match[j0]);
54
             do
55
             {
56
                  int j1 = way[j0];
57
                 match[j0] = match[j1];
58
                  j0 = j1;
59
             }
60
             while (j0);
61
         }
62
63
         inline void work() { for (int i = 1;i <= N;++i) hungary(i); }</pre>
64
65
        inline int get_ans()
66
67
             int sum = 0;
68
             for (int i = 1;i <= N;++i)
69
70
                  // if (w[match[i]][i] == inf); // 无解
71
                  if (match[i] > 0) sum += w[match[i]][i];
72
             }
73
             return sum;
74
         }
75
76
         inline void getp(int &x,int &y)
77
78
             x = y = 0;
79
             for (int i = 1;i <= N;++i)</pre>
80
                  x += A[match[i]][i],y += B[match[i]][i];
81
```

```
}
82
     }km;
83
 84
     inline void work(int X1,int Y1,int X2,int Y2)
 86
         km.init();
 87
         for (int i = 1;i <= N;++i)</pre>
 88
              for (int j = 1; j \le N; ++j)
 89
                  km.w[i][j] = (X2-X1)*B[i][j]+(Y1-Y2)*A[i][j];
90
         km.work();
91
         if (km.get_ans() >= X2*Y1-X1*Y2) return;
92
         int x,y; km.getp(x,y);
93
         ans = min(ans,x*y);
94
         work(X1,Y1,x,y); work(x,y,X2,Y2);
95
96
     }
97
     int main()
98
99
         // freopen("B.in", "r", stdin);
100
         for (int T = gi(); T--;)
101
102
              N = gi(); ans = inf;
103
              for (int i = 1; i \le N; ++i) for (int j = 1; j \le N; ++j) A[i][j] = gi();
104
              for (int i = 1; i \le N; ++i) for (int j = 1; j \le N; ++j) B[i][j] = gi();
105
              int X1,Y1,X2,Y2;
106
              km.init();
107
              for (int i = 1;i <= N;++i)</pre>
108
                  for (int j = 1; j \le N; ++j)
109
                       km.w[i][j] = A[i][j];
110
              km.work(); km.getp(X1,Y1);
111
              km.init();
112
              for (int i = 1;i <= N;++i)</pre>
113
                  for (int j = 1; j \le N; ++j)
114
                       km.w[i][j] = B[i][j];
115
              km.work(); km.getp(X2,Y2);
116
              ans = min(X1*Y1,X2*Y2);
117
              work(X1,Y1,X2,Y2);
118
              cout << ans << endl;</pre>
119
120
         fclose(stdin); fclose(stdout);
121
         return 0;
122
     }
123
```

# 2.11 Planar Graph

```
1 //包括平面图转对偶图
2 inline int dcmp(double a)
3 {
4 if (fabs(a) <= eps) return 0;</pre>
```

2.11. PLANAR GRAPH

33

```
else if (a > 0) return 1;
5
        else return -1;
6
    }
    struct Point
9
        double x,y;
10
        inline Point(double _x = 0,double _y = 0):x(_x),y(_y) {}
11
        inline void read() { x = gi(),y = gi(); }
12
        friend inline Point operator-(const Point &a,const Point &b) { return
13
     → Point(a.x-b.x,a.y-b.y); }
        friend inline double operator/(const Point &a,const Point &b) { return a.x*b.y-a.y*b.x; }
14
        inline double angle() { return atan2(y,x); }
15
    }pp[maxn];
16
    struct Segment
17
18
    {
        int from,to,h,id,sur; // from 号点到 to 号点, h 为边权,suf 为这条有向边维出来的平面编号。
19
        inline Segment(int _from = 0,int _to = 0,int _h = 0,int _id = 0,int _sur =
20
     \hookrightarrow 0):from(_from),to(_to),h(_h),id(_id),sur(_sur) {}
        friend inline bool operator<(const Segment &a,const Segment &b) { return
21
        (pp[a.to]-pp[a.from]).angle() < (pp[b.to]-pp[b.from]).angle(); }</pre>
    }edge[maxm*2];
22
    vector <int> G[maxn];
23
24
    inline void nadd(int u,int v,int h) { ++ncnt; G[u].push_back(ncnt); edge[ncnt] = Segment(u,v,h);
25
    inline void nins(int u,int v,int h) { nadd(u,v,h); nadd(v,u,h); }
26
27
    inline bool cmp(int a,int b) { return edge[a] < edge[b]; }</pre>
28
29
    inline void find_surface()
30
    {
31
        for (int i = 1;i <= N;++i) sort(G[i].begin(),G[i].end(),cmp);</pre>
32
        for (int i = 1;i <= N;++i)</pre>
33
        {
34
            int nn = G[i].size();
35
            for (int j = 0; j < nn; ++j)
36
                 edge[G[i][j]].id = j;
37
38
        for (int i = 2;i <= ncnt;++i)</pre>
39
            if (!edge[i].sur)
40
41
                 ++tot; int j = i,p,nn; vector <Point> vec;
42
                 while (!edge[j].sur)
43
                 {
44
                     edge[j].sur = tot; vec.push_back(pp[edge[j].from]);
45
                     p = edge[j].to; nn = G[p].size();
46
                     j ^= 1; j = G[p][(edge[j].id+1)%nn];
47
                 }
48
                 double res = 0; nn = vec.size();
49
```

```
for (j = 0; j < nn; ++j)
50
                    res += (vec[j]-vec[0])/(vec[(j+1)%nn]-vec[0]);
51
                res /= 2; space[tot] = res;
52
         // 第 tot 个平面的有向面积,外面的大平面面积为正,其余为负,大平面可能有多个 (平面图不连通)
            }
53
        // 开始建边, 以 mst 为例
54
        // for (int i = 2; i \le cnt; i += 2)
55
        // {
56
                if \ (space[edge[i].sur] < 0 \\ \& space[edge[i^1].sur] < 0)
        //
57
        //
                    arr[++all] = (ARR) { edge[i].sur,edge[i^1].sur,edge[i].h };
58
                else arr[++all] = (ARR) { edge[i].sur,edge[i^1].sur,inf};
        //
59
        // }
60
    }
61
62
    // 点定位
63
    struct Scan
64
65
        double x,y; int bel,sign;
66
        inline Scan(double _x = 0,double _y = 0,int _bel = 0,int _sign =
67
       0):x(_x),y(_y),bel(_bel),sign(_sign) {}
        friend inline bool operator < (const Scan &a,const Scan &b)
68
69
            if (a.x != b.x) return a.x < b.x;</pre>
70
            else return a.sign > b.sign;
71
        }
72
    }bac[maxn*4];
73
74
    struct Splay
75
76
        int num,root,ch[maxn][2],fa[maxn],key[maxn]; queue <int> team;
77
78
        inline int newnode()
79
80
            int ret;
            if (team.empty()) ret = ++num;
82
            else ret = team.front(),team.pop();
83
            fa[ret] = ch[ret][0] = ch[ret][1] = 0;
84
            return ret;
85
        }
86
87
        inline void init() { num = 0; root = newnode(); key[root] = cnt; }
88
89
        inline void rotate(int x)
90
        {
91
            int y = fa[x],z = fa[y],l = ch[y][1] == x,r = 1^1;
92
            if (z != 0) ch[z][ch[z][1] == y] = x;
93
            fa[x] = z; fa[y] = x; fa[ch[x][r]] = y;
94
            ch[y][1] = ch[x][r]; ch[x][r] = y;
95
        }
96
```

2.11. PLANAR GRAPH

```
97
          inline void splay(int x)
98
99
               while (fa[x] != 0)
100
101
                    int y = fa[x],z = fa[y];
102
                    if (fa[y] != 0)
103
104
                         if ((ch[y][0] == x)^(ch[z][0] == y)) rotate(x);
105
                         else rotate(y);
106
                    }
107
                    rotate(x);
108
               }
109
               root = x;
110
          }
111
112
          inline int lower_bound(const Point &p)
113
114
               int now = root,ret = 0;
115
               while (now)
116
117
                    int k = key[now];
118
                     \  \  \text{if } \  ((p-pp[edge[k].from])/(pp[edge[k].to]-pp[edge[k].from]) \ >= \ 0) \\
119
                        ret = k,now = ch[now][0];
120
                    else now = ch[now][1];
121
               }
122
               return ret;
123
          }
124
125
          inline int find(int w)
126
          {
127
               int now = root;
128
               double x = pp[edge[w].to].x,y = pp[edge[w].to].y;
129
               double ang = (pp[edge[w].to] - pp[edge[w].from]).angle();
130
               while (now)
131
               {
132
                    int k = key[now];
133
                    if (k == w) return now;
134
                    \label{eq:node_power_power} \texttt{NODE}\ p\ =\ pp[\texttt{edge[k].to}]\ -\ pp[\texttt{edge[k].from}]\ , q\ =\ pp[\texttt{edge[k].from}]\ ;
135
                    double xx = x - q.x,yy = q.y+xx/p.x*p.y;
136
                    if (equal(yy,y))
137
                    {
138
                         double t = p.angle();
139
                         now = ch[now][ang < t];</pre>
140
                    }
141
                    else now = ch[now][y > yy];
142
               }
143
          }
144
145
```

```
inline void erase(int w)
146
147
              int p = find(w);
148
              while (ch[p][0] || ch[p][1])
149
150
                  if (ch[p][0])
151
                  {
152
                      rotate(ch[p][0]);
153
                      if (p == root) root = fa[p];
154
                  }
155
                  else
156
                  {
157
                      rotate(ch[p][1]);
158
                      if (p == root) root = fa[p];
159
                  }
160
              }
161
              team.push(p);
162
              ch[fa[p]][ch[fa[p]][1] == p] = 0;
163
              fa[p] = 0;
164
         }
165
166
         inline void insert(int w)
167
         {
168
              int now = root,pre;
169
              double x = pp[edge[w].from].x,y = pp[edge[w].from].y;
170
              double ang = (pp[edge[w].to] - pp[edge[w].from]).angle();
171
              double xx,yy;
172
              while (true)
173
              {
174
                  int k = key[now];
175
                  NODE p = pp[edge[k].to] - pp[edge[k].from],q = pp[edge[k].from];
176
                  xx = x - q.x,yy = q.y+xx/p.x*p.y;
177
                  if (equal(yy,y))
178
                  {
179
                      double t = p.angle();
180
                      pre = now,now = ch[now][ang > t];
181
                      if (!now)
182
183
                           now = newnode();
184
                           fa[now] = pre; ch[pre][ang > t] = now; key[now] = w;
185
                           break;
186
                      }
187
                  }
188
                  else
189
                  {
190
                      pre = now,now = ch[now][y > yy];
191
                      if (!now)
192
                      {
193
                           now = newnode();
194
```

```
fa[now] = pre; ch[pre][y>yy] = now; key[now] = w;
195
                          break;
196
                      }
197
                 }
198
             }
199
             splay(now);
200
         }
201
     }S;
202
203
     inline void locate()
204
     {
205
         int nn = 0;
206
         for (int i = 2; i \le cnt; i += 2)
207
208
             if (!dcmp(pp[edge[i].from].x-pp[edge[i].to].x)) continue;
209
             bac[++nn] = Scan(pp[edge[i].from].x,pp[edge[i].from].y,i,2);
210
             bac[++nn] = Scan(pp[edge[i].to].x,pp[edge[i].to].y,i,3);
211
212
         scanf("%d",&T); double x,y;
213
         // 查询 (x,y) 所在平面
214
         for (int i = 1;i <= T;++i)
215
216
             scanf("%lf %lf",&x,&y);
217
             bac[++nn] = Scan(x,y,i,0);
218
             scanf("%lf %lf",&x,&y);
219
             bac[++nn] = Scan(x,y,i,1);
220
         }
221
         sort(bac+1,bac+nn+1);
222
         pp[++n] = Point(-oo,-oo); pp[++n] = (oo,-oo);
223
         edge[++cnt] = Edge(n-1,n);
224
         S.init(); int p;
225
         for (int i = 1;i <= nn;++i)
226
227
             if (bac[i].sign == 2||bac[i].sign == 3)
228
             {
229
                  if (bac[i].sign == 2) S.insert(bac[i].bel);
230
                  else S.erase(bac[i].bel);
231
             }
232
             else
233
             {
234
                  p = S.lower_bound(Point(bac[i].x,bac[i].y));
235
                  query[bac[i].bel][bac[i].sign] = edge[p].sur;
236
             }
237
         }
238
    }
239
```

## 2.12 Polygon Class

```
inline bool PointOnSegment(const Point &t,const Point &a,const Point &b)
        if (dcmp((t-a)/(b-a))) return false;
        if (dcmp((t-a)*(t-b)) > 0) return false;
        return true;
   }
   inline bool in(const Point &a,const Point &b,const Point &c)
        double alpha = a.angle(),beta = b.angle(),gamma = c.angle(); // angle 返回 [0,2pi]
10
        if (alpha <= beta) return dcmp(gamma-alpha) > 0&&dcmp(beta-gamma) > 0;
11
        else return dcmp(gamma-alpha) > 0||dcmp(beta-gamma) > 0;
12
13
   }
14
   struct Polygon
15
16
        int n; Point a[maxn];
17
        inline Polygon() {}
18
        inline void read()
19
20
            n = gi();
21
            for (int i = 0;i < n;++i) a[i].read();</pre>
22
            a[n] = a[0];
23
24
        // 点是否在多边形内部,内部为 1,外部为 0,边界为 2,不管顺逆时针
25
        inline int Point_In(const Point &t) const
26
27
            int num = 0;
            for (int i = 0; i < n; ++i)
29
            {
                if (PointOnSegment(t,a[i],a[i+1])) return 2;
31
                int k = dcmp((a[i+1]-a[i])/(t-a[i]));
32
                int d1 = dcmp(a[i].y-t.y),d2 = dcmp(a[i+1].y-t.y);
33
                if (k > 0 \& \& d1 \le 0 \& \& d2 > 0) ++num;
34
                if (k < 0 \&\&d2 <= 0 \&\&d1 > 0) --num;
35
36
            return num != 0;
37
        }
38
        // 判断多边形的方向, true 为逆时针, false 为顺时针, 用叉积判断哪个多
39
        inline bool CalculateClockDirection()
40
41
            int res = 0;
42
            for (int i = 0; i < n; ++i)
43
44
                int p = i-1, s = i+1, sgn;
45
                if (p < 0) p += n; if (s >= n) s -= n;
46
                sgn = dcmp((a[i]-a[p])/(a[s]-a[i]));
47
                if (sgn) { if (sgn > 0) ++res; else --res; }
48
```

```
}
49
            return res > 0;
50
51
        // 判断多边形方向, true 为逆时针, false 为顺时针, 用 Green 公式
52
        inline bool CalculateClockDirection()
53
54
            double res = 0;
55
            for (int i = 0; i < n; ++i)
56
                res -= 0.5*(a[i+1].y+a[i].y)*(a[i+1].x-a[i].x);
57
            return res > 0;
        }
59
60
        // 线段 ab 是否有点严格在多边形内部,先判断线段是否与多边形边界有交,再判断 ab 是否与多边形有交,内部 false,外
61
        inline bool can(int ia,int ib)
62
        {
63
            Point a = P[ia],b = P[ib],v = b-a;
64
            if (in(P[ia+1]-a,P[ia-1]-a,b-a)||in(P[ib+1]-b,P[ib-1]-b,a-b)) return false;
65
            for (register int i = 0;i < N;++i)</pre>
66
67
                 if (dcmp(v/(P[i]-a))*dcmp(v/(P[i+1]-a)) <
68
         \label{eq:condition} \begin{center} $0 \& \& dcmp(vec[i]/(a-P[i])) * dcmp(vec[i]/(b-P[i])) < 0$ \end{center}
                     return false;
69
                 if (PointOnSegment(a,P[i],P[i+1])||PointOnSegment(b,P[i],P[i+1])) return false;
70
                 if (PointOnSegment(P[i],a,b)||PointOnSegment(P[i+1],a,b)) return false;
71
            }
72
            return true;
73
74
   }poly;
75
```

#### Union Area of Circles 2.13

18

```
//N 为开始圆的个数, M 为离散化后圆的个数, cnt 为去包含后圆的个数
   int N,M,cnt;
   struct Node
5
       double x,y;
6
       inline Node(double _x = 0, double _y = 0):x(_x),y(_y) {}
       inline void read() { x = gi(),y = gi(); }
       inline double norm() const { return sqrt(x*x+y*y); }
       inline double angle() const { return atan2(y,x); }
10
       inline Node unit() const { double len = norm(); return Node(x/len,y/len); }
11
       friend inline Node operator-(const Node &a,const Node &b) { return Node(a.x-b.x,a.y-b.y); }
12
       friend inline Node operator+(const Node &a,const Node &b) { return Node(a.x+b.x,a.y+b.y); }
13
       friend inline Node operator*(const Node &a,double b) { return Node(a.x*b,a.y*b); }
14
       friend inline Node operator*(double b,const Node &a) { return Node(a.x*b,a.y*b); }
15
       friend inline double operator/(const Node &a,const Node &b) { return a.x*b.y-a.y*b.x; }
16
   };
17
   struct Circle
```

```
{
19
        Node C; double r;
20
        inline Circle(const Node &_C = Node(),double _r = 0):C(_C),r(_r) {}
21
        friend inline bool operator<(const Circle &a,const Circle &b)
22
23
            if (dcmp(a.r-b.r)) return dcmp(a.r-b.r) < 0;</pre>
24
            else if (dcmp(a.C.x-b.C.x)) return dcmp(a.C.x-b.C.x) < 0;</pre>
25
            else return dcmp(a.C.y-b.C.y) < 0;</pre>
26
        }
27
        friend inline bool operator == (const Circle &a, const Circle &b)
28
29
            if (dcmp(a.r-b.r)) return false;
30
            if (dcmp(a.C.x-b.C.x)) return false;
31
            if (dcmp(a.C.y-b.C.y)) return false;
32
            return true;
33
34
    }tc[maxn],cir[maxn];
35
36
    inline Node rotate(const Node &p,double cost,double sint)
37
    {
38
        double x = p.x, y = p.y;
39
        return Node(x*cost-y*sint,x*sint+y*cost);
40
    }
41
    inline pair <Node, Node> crosspoint(const Node &ap,double ar,const Node &bp,double br)
42
43
        double d = (ap-bp).norm(),cost = (ar*ar+d*d-br*br)/(2*ar*d),sint = sqrt(1-cost*cost);
44
        Node v = ((bp-ap).unit())*ar;
45
        return make_pair(ap+rotate(v,cost,-sint),ap+rotate(v,cost,sint));
46
    }
47
    inline pair <Node, Node> crosspoint(const Circle &a,const Circle &b) { return
48
        crosspoint(a.C,a.r,b.C,b.r); }
49
    struct Event
50
51
        Node p; double a; int d;
52
        inline Event(const Node &_p = Node(),double _a = 0,double _d = 0):p(_p),a(_a),d(_d) {}
53
        friend inline bool operator <(const Event &a,const Event &b) { return a.a < b.a; }
54
    };
55
56
    inline double work()
57
58
        sort(tc+1,tc+M+1); M = unique(tc+1,tc+M+1)-tc-1;
59
        for (int i = M; i; --i)
60
        {
61
            bool ok = true;
62
            for (int j = i+1; j \le M; ++j)
63
            {
64
                 double d = (tc[i].C-tc[j].C).norm();
65
                 if (dcmp(d-fabs(tc[i].r-tc[j].r)) \le 0) \{ ok = false; break; \}
66
```

```
}
67
             if (ok) cir[++cnt] = tc[i];
68
69
         // for (int i = M; i; --i) cir[++cnt] = tc[i];
70
         double ret = 0;
71
         for (int i = 1;i <= cnt;++i)
72
         {
73
             vector <Event> event;
74
             Node boundary = cir[i].C+Node(cir[i].r,0);
75
             event.push_back(Event(boundary,-pi,0));
76
             event.push_back(Event(boundary,pi,0));
77
             for (int j = 1; j \le cnt; ++j)
             {
79
                  if (i == j) continue;
80
                 double d = (cir[i].C-cir[j].C).norm();
81
                 if (dcmp(d-(cir[i].r+cir[j].r)) < 0)</pre>
82
83
                      pair <Node, Node> res = crosspoint(cir[i],cir[j]);
84
                      double x = (res.first-cir[i].C).angle(),y = (res.second-cir[i].C).angle();
85
                      if (dcmp(x-y) > 0)
86
                      {
87
                          event.push_back(Event(res.first,x,1));
                          event.push_back(Event(boundary,pi,-1));
89
                          event.push_back(Event(boundary,-pi,1));
90
                          event.push_back(Event(res.second,y,-1));
91
                      }
92
                      else
93
                      {
94
                          event.push_back(Event(res.first,x,1));
95
                          event.push_back(Event(res.second,y,-1));
96
                      }
97
                 }
98
             }
99
             sort(event.begin(),event.end());
100
             int sum = event[0].d;
101
             for (int j = 1; j < (int)event.size(); ++j)
102
             {
103
                  if (!sum)
104
                  {
105
                      ret += (event[j-1].p/event[j].p)/2;
106
                      double x = event[j-1].a,y = event[j].a;
107
                      double area = cir[i].r*cir[i].r*(y-x)/2;
108
                      Node v1 = event[j-1].p-cir[i].C,v2 = event[j].p-cir[i].C;
109
                      area -= (v1/v2)/2; ret += area;
110
                 }
111
                  sum += event[j].d;
112
             }
113
         }
114
         return ret;
115
```

116 }

# Chapter 3

## **Data Structure**

## 3.1 Divide and Conquer on Tree

```
#include<cstring>
    #include<iostream>
    #include<cstdio>
    #include<cstdlib>
    using namespace std;
    #define maxn (100010)
    int best,cnt = 1,side[maxn],toit[maxn],next[maxn],large[maxn];
    int sd[maxn],d[maxn],ns,nd,ans,N,K,size[maxn]; bool vis[maxn];
10
    inline void add(int a,int b)
11
    { next[++cnt] = side[a]; side[a] = cnt; toit[cnt] = b; }
12
    inline void ins(int a,int b)
13
    { add(a,b); add(b,a); }
14
15
    inline void getroot(int now,int fa,int rest)
16
17
        size[now] = 1; large[now] = 0;
18
        for (int i = side[now];i;i = next[i])
19
20
            if (toit[i] == fa||vis[toit[i]]) continue;
21
            getroot(toit[i],now,rest);
22
            size[now] += size[toit[i]];
23
            large[now] = max(large[now], size[toit[i]]);
24
25
        large[now] = max(large[now],rest-size[now]);
26
        if (large[now] < large[best]) best = now;</pre>
27
28
    inline int find_root(int now,int rest)
29
    { best = 0; getroot(now,0,rest); return best; }
30
31
    inline void dfs(int now,int fa,int dep)
32
    {
33
```

```
size[now] = 1; nd = max(dep,nd); ++d[dep];
34
        for (int i = side[now];i;i = next[i])
35
             if (toit[i] != fa&&!vis[toit[i]])
36
                 dfs(toit[i],now,dep+1),size[now] += size[toit[i]];
37
38
39
    inline void subdivide(int now)
40
41
        vis[now] = true;
42
        for (int i = side[now];i;i = next[i])
43
44
             if (vis[toit[i]]) continue;
45
             dfs(toit[i],now,1); ans += d[K];
46
             for (int j = 1; j < K; ++ j) ans += d[j] *sd[K-j];</pre>
             for (int j = 1; j \le nd; ++j) sd[j] += d[j], d[j] = 0;
48
             ns = max(nd,ns); nd = 0;
49
        }
50
        memset(sd,0,4*(ns+1)); ns = 0;
51
        for (int i = side[now];i;i = next[i])
52
             if (!vis[toit[i]])
53
                 subdivide(find_root(toit[i],size[toit[i]]));
54
    }
55
56
    int main()
57
58
        freopen("D.in", "r", stdin);
59
        freopen("D.out", "w", stdout);
60
         scanf("%d %d",&N,&K);
61
        for (int i = 1,a,b;i < N;++i) scanf("%d %d",&a,&b),ins(a,b);
62
        large[0] = 1<<30; subdivide(find_root(1,N));</pre>
63
        printf("%d",ans);
64
        fclose(stdin); fclose(stdout);
65
        return 0;
66
    }
67
```

## 3.2 Dynamicly Divide and Conquer on Tree

```
1 // N 个点的树,每个点点权 O/1, 询问两个 O 点之间最远距离,每次可以 flip 一个点的点权
2 #include<set>
3 #include<vector>
4 #include<algorithm>
5 #include<cstring>
6 #include<cstring>
7 #include<cstdio>
8 #include<cstdlib>
9 using namespace std;

10 const int maxn = 200010, inf = 1<<29, lhh = 4000037;
```

```
int
12
    \hspace*{0.5cm} \hookrightarrow \hspace*{0.5cm} \texttt{N,cnt,nlight,tot,best,Root,side[maxn],toit[maxn],nxt[maxn],size[maxn],large[maxn],optimal[maxn];} \\
    int father[maxn],L[maxn],R[maxn],leaf[maxn],rechain[lhh],depth[lhh]; bool off[maxn],vis[maxn];
13
    vector <int> son[maxn]; pair <int,int> Hash[lhh]; multiset <int> mx[maxn],S[maxn];
14
15
    struct Value
16
    {
17
        int a,b;
18
        inline Value() {}
19
        inline Value(int _a,int _b):a(_a),b(_b) {}
20
        friend inline Value operator +(const Value &x,const Value &y)
21
22
             Value ret;
23
             if (x.a > y.a)
24
             {
25
                 ret.a = x.a;
26
                 if (x.b > y.a) ret.b = x.b;
27
                 else ret.b = y.a;
28
             }
29
             else
30
             {
31
                 ret.a = y.a;
32
                 if (y.b > x.a) ret.b = y.b;
33
                 else ret.b = x.a;
34
             }
35
             return ret;
36
37
    }tree[maxn*2];
38
39
    inline void add(int a,int b) { nxt[++cnt] = side[a]; side[a] = cnt; toit[cnt] = b; }
40
    inline void ins(int a,int b) { add(a,b); add(b,a); }
41
42
    inline int gi()
43
44
         char ch; int ret = 0,f = 1;
45
        do ch = getchar(); while (!(ch >= '0'&&ch <= '9')&&ch != '-');
46
        if (ch == '-') f = -1,ch = getchar();
47
        do ret = ret*10+ch-'0',ch = getchar(); while (ch >= '0'&&ch <= '9');
48
        return ret*f;
49
    }
50
51
    inline int find(const pair <int,int> &key)
52
53
    {
        int now = (2333*key.first+5003*key.second)%lhh;
54
        while (true)
55
56
             if (Hash[now].first == 0||Hash[now] == key) return now;
57
             else ++now;
             if (now >= lhh) now -= lhh;
59
```

```
}
60
    }
61
62
    inline void getroot(int now,int rest,int fa)
63
64
         size[now] = 1; large[now] = 0;
65
         for (int i = side[now];i;i = nxt[i])
66
67
             if (vis[toit[i]]||toit[i] == fa) continue;
68
             getroot(toit[i],rest,now);
69
             size[now] += size[toit[i]];
70
             large[now] = max(large[now], size[toit[i]]);
72
         large[now] = max(large[now],rest-size[now]);
73
         if (large[now] < large[best]) best = now;</pre>
74
    }
75
    inline int find_root(int rest,int now) { best = 0; getroot(now,rest,0); return best; }
76
    inline void dfs(int id,int root,int now,int fa,int dep)
78
    {
79
         S[id].insert(dep);
80
         pair <int,int> key = make_pair(root,now); int pos = find(key);
81
         rechain[pos] = id; depth[pos] = dep; Hash[pos] = key;
82
         size[now] = 1;
83
         for (int i = side[now];i;i = nxt[i])
84
85
             if (vis[toit[i]] | | toit[i] == fa) continue;
86
             dfs(id,root,toit[i],now,dep+1);
                                                   size[now] += size[toit[i]];
87
         }
88
    }
89
90
    inline void subdivide(int root)
91
92
         optimal[root] = -inf; mx[root].insert(-inf);
93
         L[root] = tot+1;
94
         for (int i = side[root];i;i = nxt[i])
95
96
             if (vis[toit[i]]) continue;
97
             ++tot; dfs(tot,root,toit[i],root,1);
98
             S[tot].insert(-inf);
99
100
         R[root] = tot; vis[root] = true;
101
         for (int i = side[root];i;i = nxt[i])
102
         {
103
             if (vis[toit[i]]) continue;
104
             int tmp = find_root(size[toit[i]],toit[i]);
105
             father[tmp] = root; son[root].push_back(tmp);
106
             subdivide(tmp);
107
         }
108
```

```
}
109
110
     inline void build(int now,int 1,int r)
111
112
         if (1 == r)
113
114
             tree[now] = Value(*S[1].rbegin(),-inf);
115
             leaf[1] = now; return;
116
         }
117
         int mid = (1+r)>>1;
118
         build(now<<1,1,mid); build(now<<1|1,mid+1,r);
119
         tree[now] = tree[now<<1]+tree[now<<1|1];</pre>
120
    }
121
122
     inline Value query(int now,int 1,int r,int ql,int qr)
123
124
         if (1 == ql&&r == qr) return tree[now];
125
         int mid = (1+r)>>1;
126
         if (qr <= mid) return query(now<<1,1,mid,q1,qr);</pre>
127
         else if (ql > mid) return query(now<<1|1,mid+1,r,ql,qr);</pre>
128
         else return query(now<<1,1,mid,q1,mid)+query(now<<1|1,mid+1,r,mid+1,qr);</pre>
129
    }
130
131
     inline void upd(int &a,int b) { if (a < b) a = b; }</pre>
132
133
     inline void modify(int pos,int dep,bool sign)
134
     {
135
         if (sign) S[pos].insert(dep); else S[pos].erase(S[pos].find(dep));
136
         tree[leaf[pos]] = Value(*S[pos].rbegin(),-inf);
137
         for (int now = leaf[pos]>>1;now;now >>= 1)
138
             tree[now] = tree[now<<1]+tree[now<<1|1];</pre>
139
    }
140
     inline void modify(int pos)
141
142
         int c = 0;
143
         if (father[pos]) mx[father[pos]].erase(mx[father[pos]].find(optimal[pos]));
144
         off[pos] ^= 1; if (off[pos]) nlight++; else nlight--;
145
         if (L[pos] <= R[pos])</pre>
146
         {
147
             Value res = query(1,1,tot,L[pos],R[pos]);
148
             optimal[pos] = max(res.a+res.b,*mx[pos].rbegin());
149
             if (off[pos]) upd(optimal[pos],res.a);
150
151
         if (father[pos]) mx[father[pos]].insert(optimal[pos]);
152
         for (int now = father[pos];now;now = father[now])
153
154
             int t = find(make_pair(now,pos));
155
             int id = rechain[t],dep = depth[t];
156
             modify(id,dep,off[pos]);
157
```

```
if (father[now]) mx[father[now]].erase(mx[father[now]].find(optimal[now]));
158
             Value res = query(1,1,tot,L[now],R[now]);
159
             optimal[now] = max(res.a+res.b,*mx[now].rbegin());
160
             if (off[now]) upd(optimal[now],res.a);
161
             if (father[now]) mx[father[now]].insert(optimal[now]);
162
             ++c;
163
         }
164
    }
165
166
     inline void redfs(int now)
167
168
         for (int i = 0;i < (int)son[now].size();++i)</pre>
169
             redfs(son[now][i]),mx[now].insert(optimal[son[now][i]]);
170
         if (L[now] <= R[now])</pre>
171
         {
172
             Value res = query(1,1,tot,L[now],R[now]);
173
             optimal[now] = max(res.a+res.b,*mx[now].rbegin());
174
             if (off[now]) upd(optimal[now],res.a);
175
         }
176
    }
177
178
     int main()
179
     {
180
         // freopen("A.in", "r", stdin);
181
         memset(off,true,sizeof off);
182
         nlight = N = gi();
183
         for (int i = 1;i < N;++i) ins(gi(),gi());</pre>
184
         large[0] = inf;
185
         subdivide(Root = find_root(N,1));
186
         build(1,1,tot); redfs(Root);
187
         for (int Q = gi();Q--;)
188
189
             char opt; do opt = getchar(); while (opt != 'G'&&opt != 'C');
190
             if (opt == 'G')
191
             {
192
                  if (!nlight) puts("-1");
193
                  else if (nlight == 1) puts("0");
194
                  else printf("%d\n",optimal[Root]);
195
196
             else modify(gi());
197
         }
198
         return 0;
199
    }
200
```

## 3.3 Heavy Path Decomposition

```
int side[maxn],toit[maxn<<1],nxt[maxn<<1];
int timestamp,father[maxn],dfn[maxn],redfn[maxn],top[maxn],size[maxn];</pre>
```

```
void decompose(int now,int tp)
    {
5
        redfn[dfn[now] = ++timestamp] = now;
        top[now] = tp; int heavy = 0;
        for (int i = side[now];i;i = nxt[i])
            if (toit[i] != father[now]&&size[toit[i]] > size[heavy]) heavy = toit[i];
        if (!heavy) return; decompose(heavy,tp);
10
        for (int i = side[now];i;i = nxt[i])
11
            if (toit[i] != father[now]&&toit[i] != heavy) decompose(toit[i],toit[i]);
12
    }
13
14
    void dfs(int now)
15
16
        size[now] = 1;
17
        for (int i = side[now];i;i = nxt[i])
18
            if (toit[i] != father[now])
19
20
                 father[toit[i]] = now,con[toit[i]] = i;
21
                 dep[toit[i]] = dep[now]+1,dfs(toit[i]);
22
                 size[now] += size[toit[i]] ;
23
            }
24
    }
25
26
    // 对点操作
27
    inline int query(int a,int b)
28
29
        int ret = -inf;
30
        while (top[a] != top[b])
31
32
            if (dep[top[a]] < dep[top[b]]) swap(a,b);</pre>
33
            ret = max(ret,ask(1,1,N,dfn[top[a]],dfn[a]));
34
            a = father[top[a]];
35
        }
36
        if (dep[a] < dep[b]) swap(a,b);</pre>
37
        ret = max(ret,query(1,1,N,dfn[b],dfn[a]));
38
        return ret;
39
    }
40
    // 对边操作
42
    inline int query(int a,int b)
43
44
        int ret = -inf;
45
        while (top[a] != top[b])
46
47
            if (dep[top[a]] < dep[top[b]]) swap(a,b);</pre>
48
            ret = max(ret,ask(1,1,N,dfn[top[a]],dfn[a]));
49
            a = father[top[a]];
50
        }
51
        if (a == b) return ret;
52
```

```
if (dep[a] < dep[b]) swap(a,b);
ret = max(ret,ask(1,1,N,dfn[b]+1,dfn[a]));
return ret;
}</pre>
```

#### 3.4 K-Dimension Tree

```
struct Point
    {
2
        double x,y; int id;
        inline Point() = default;
        inline Point(double _x,double _y,int _id):x(_x),y(_y),id(_id) {}
5
        inline void read(int i = 0) { scanf("%lf %lf",&x,&y); id = i; }
        inline double norm() { return sqrt(x*x+y*y); }
        friend inline Point operator+(const Point &a,const Point &b) { return
    → Point(a.x+b.x,a.y+b.y); }
        friend inline Point operator-(const Point &a,const Point &b) { return
    → Point(a.x-b.x,a.y-b.y); }
        friend inline double operator*(const Point &a,const Point &b) { return a.x*b.x+a.y*b.y; }
10
        friend inline double operator/(const Point &a,const Point &b) { return a.x*b.y-a.y*b.x; }
11
    }P[maxn];
12
13
    struct Rectangle
14
15
        double lx,rx,ly,ry;
16
        inline Rectangle() = default;
17
        inline Rectangle(double _lx,double _rx,double _ly,double
18
        _ry):lx(_lx),rx(_rx),ly(_ly),ry(_ry) {}
        inline void set(const Point &p) { lx = rx = p.x; ly = ry = p.y; }
19
        inline void merge(const Point &p)
20
21
            lx = min(lx,p.x); rx = max(rx,p.x);
22
            ly = min(ly,p.y); ry = max(ry,p.y);
23
24
        inline void merge(const Rectangle &r)
25
26
            lx = min(lx,r.lx); rx = max(rx,r.rx);
27
            ly = min(ly,r.ly); ry = max(ry,r.ry);
28
29
        // 最小距离, 到 4 个角和 4 条边距离
30
        inline double dist(const Point &p)
31
32
            if (p.x \le lx \& p.y \le ly) return (p-Point(lx,ly)).norm();
33
            else if (p.x <= rx&&p.y <= ly) return p.y-ly;
34
            else if (p.x >= rx&&p.y <= ly) return (p-Point(rx,ly)).norm();
35
            else if (p.x >= rx&&p.y <= ry) return p.x-rx;
36
            else if (p.x \ge rx \& p.y \ge ry) return (p-Point(rx,ry)).norm();
37
            else if (p.x \ge lx\&\&p.y \ge ry) return p.y-ry;
38
            else if (p.x \le lx \& p.y \ge ry) return (p-Point(lx,ry)).norm();
39
```

```
else if (p.x \le lx \& p.y \ge ly) return p.x-lx;
40
            return 0;
41
        }
42
        // 最大距离, 到 4 个角的距离
43
        inline double dist(const Point &p)
44
45
            double ret = 0;
46
            ret += max((rx-p.x)*(rx-p.x),(lx-p.x)*(lx-p.x));
47
            ret += max((ry-p.y)*(ry-p.y),(ly-p.y)*(ly-p.y));
48
            return ret;
49
        }
50
    };
51
52
    struct Node
53
54
    {
        int child[2]; Point p; Rectangle r;
55
        inline Node() = default;
56
        inline Node(const Point &_p,const Rectangle &_r):p(_p),r(_r) { r.set(p); memset(child,0,8);
57
        inline void set(const Point &_p) { p = _p; r.set(p); memset(child,0,8); }
58
    }tree[maxn];
59
    inline bool cmpx(const Point &a,const Point &b)
61
    {
62
        if (a.x != b.x) return a.x < b.x;</pre>
63
        else return a.y < b.y;</pre>
64
    }
65
    inline bool cmpy(const Point &a,const Point &b)
66
67
        if (a.y != b.y) return a.y < b.y;</pre>
68
        else return a.x < b.x;</pre>
69
    }
70
71
    inline bool cmp(pair <double,int> a,pair <double,int> b)
72
    {
73
        int sgn = dcmp(a.first-b.first);
74
        if (sgn) return sgn < 0;
75
        else return a.second < b.second;</pre>
76
    }
77
78
    // 查询 k 大/小
79
    inline void query(int now, const Point &p,int k,pair <double,int> ret[],bool dim = false)
80
81
        if (dcmp(tree[now].r.dist(p)-ret[k].first) > 0) return;
82
        pair <double,int> val = make_pair((p-tree[now].p).norm(),tree[now].p.id);
83
        for (int i = 1;i <= k;++i)
84
            if (cmp(val,ret[i]))
85
            {
86
                 for (int j = k+1; j > i; --j) ret[j] = ret[j-1];
87
```

```
ret[i] = val; break;
88
89
         if ((dim&&cmpx(p,tree[now].p))||(!dim&&cmpy(p,tree[now].p)))
90
         {
91
             if (tree[now].child[0]) query(tree[now].child[0],p,k,ret,dim^1);
92
             if (tree[now].child[1]) query(tree[now].child[1],p,k,ret,dim^1);
93
         }
94
         else
95
         {
96
             if (tree[now].child[1]) query(tree[now].child[1],p,k,ret,dim^1);
97
             if (tree[now].child[0]) query(tree[now].child[0],p,k,ret,dim^1);
98
         }
99
    }
100
101
    // 查询最小/大
102
    inline void query(int x,const Point &p,pair <double,int> ret,bool dim = false)
103
104
         if (dcmp(tree[now].r.disp(p)-ret.first) > 0) return;
105
         pair <double,int> val = make_pair((p-tree[now].p).norm(),tree[now].p.id);
106
         if (cmp(val,ret)) ret = val;
107
         if ((dim&&cmpx(p,tree[now].p))||(!dim&&cmpy(p,tree[now].p)))
108
109
             if (tree[now].child[0]) query(tree[now].child[0],p,ret,dim^1);
110
             if (tree[now].child[1]) query(tree[now].child[1],p,ret,dim^1);
111
         }
112
         else
113
         {
114
             if (tree[now].child[1]) query(tree[now].child[1],p,ret,dim^1);
115
             if (tree[now].child[0]) query(tree[now].child[0],p,ret,dim^1);
116
         }
117
    }
118
119
    inline int build(int l,int r,bool dim)
120
    {
121
         int now = ++size,mid = (1+r)>>1;
122
         nth_element(vec.begin()+l-1,vec.begin()+mid-1,vec.begin()+r,dim?cmpx:cmpy);
123
         tree[now].set(vec[mid-1]);
124
         if (1 < mid)
125
         {
126
             tree[now].child[0] = build(1,mid-1,dim^1);
127
             tree[now].r.merge(tree[tree[now].child[0]].r);
128
         }
129
         if (r > mid)
130
         {
131
             tree[now].child[1] = build(mid+1,r,dim^1);
132
             tree[now].r.merge(tree[tree[now].child[1]].r);
133
134
         return now;
135
    }
136
```

3.5. LEFTLIST TREE 53

#### 3.5 Leftlist Tree

```
// It's correct, but it needs be rewritten.
    #include<iostream>
    #include<cstdio>
    #include<cstdlib>
    using namespace std;
    #define maxn (600010)
    int N,M,root[maxn],size[maxn],v[maxn],dep[maxn],l[maxn],r[maxn],tot;
    inline int Merge(int x,int y)
10
11
        if (!x||!y) return x+y;
12
        if (v[x]>v[y]) swap(x,y);
13
        r[x] = Merge(r[x],y);
14
        if (dep[l[x]] < dep[r[x]]) swap(l[x],r[x]);</pre>
15
        dep[x] = dep[r[x]]+1;
16
        return x;
17
    }
18
    inline int Init(int x) { v[++tot] = x; 1[tot] = r[tot] = dep[tot] = 0; return tot;}
19
    inline int Insert(int x,int y) { return Merge(x,Init(y)); }
20
    inline int pop(int x) { return Merge(l[x],r[x]); }
21
22
    inline int read()
23
24
        char ch; int f = 1, ret = 0;
25
        do ch = getchar(); while (!(ch >= '0'&&ch <= '9')&&ch != '-');
26
        if (ch == '-') f = -1, ch = getchar();
27
        do ret = ret*10+ch-^{'}0',ch = getchar(); while (ch >= ^{'}0'&&ch <= ^{'}9');
28
        return ret*f;
29
    }
30
31
    int main()
32
    {
33
        freopen("1050.in","r",stdin);
34
        freopen("1050.out","w",stdout);
35
        scanf("%d %d",&N,&M);
36
        for (int i = 1;i <= N;++i) root[i] = Init(read()),size[i] = 1;</pre>
37
        while (M--)
38
39
            int opt = read();
40
            if (!opt)
41
            {
42
                 int a = read()+1,b = read()+1;
43
                 if (size[b]) root[a] = Merge(root[a],root[b]);
44
                 size[a] += size[b]; size[b] = 0;
45
            }
46
            else if (opt == 1)
47
            {
48
```

```
int a = read()+1;
49
                 if (!size[a]) puts("-1");
50
                 else printf("%d\n",v[root[a]]),root[a] = pop(root[a]),--size[a];
51
             }
52
             else
53
             {
54
                 int a = read()+1; ++size[a];
55
                 root[a] = Insert(root[a],read());
57
58
        fclose(stdin); fclose(stdout);
59
        return 0;
60
    }
61
```

#### 3.6 Link Cut Tree

```
inline bool isroot(int a) { return ch[fa[a]][0] != a&&ch[fa[a]][1] != a; }
    inline void update(int x) { val[x] = (val[ch[x][0]]+val[ch[x][1]]).merge(x); }
    inline void pushdown(int x)
        if (rev[x])
        {
            int &lc = ch[x][0],&rc = ch[x][1];
            swap(lc,rc);
            if (lc) rev[lc] ^= 1;
10
            if (rc) rev[rc] ^= 1;
11
            rev[x] = false;
12
        }
13
    }
14
15
    inline void rotate(int x)
16
17
        int y = fa[x],z = fa[y],l = ch[y][1] == x,r = l^1;
18
        if (!isroot(y)) ch[z][ch[z][1] == y] = x; fa[x] = z;
19
        if (ch[x][r]) fa[ch[x][r]] = y; ch[y][1] = ch[x][r];
20
        fa[y] = x; ch[x][r] = y; update(y); update(x);
21
    }
22
    inline void splay(int x)
23
24
        int top = 0,i;
25
        for (i = x;!isroot(i);i = fa[i]) stk[++top] = i; stk[++top] = i;
26
        while (top) pushdown(stk[top--]);
27
        while (!isroot(x))
28
29
            int y = fa[x], z = fa[y];
30
            if (!isroot(y))
31
32
                 if ((ch[y][0] == x)^(ch[z][0] == y)) rotate(x);
33
```

3.6. LINK CUT TREE 55

```
else rotate(y);
34
             }
35
             rotate(x);
36
        }
37
    }
38
39
    inline int access(int x)
40
41
        int t = 0;
42
        for (t = 0;x;t = x,x = fa[x])
43
             splay(x),ch[x][1] = t,update(x);
44
        return t;
45
    }
46
    inline int evert(int x) { int t; rev[t = access(x)] ^= 1; return t; }
47
    inline int find(int x)
48
49
        x = access(x);
50
        while (pushdown(x),ch[x][0]) x = ch[x][0];
51
        return x;
52
    }
53
    inline void cut(int x,int y)
54
55
         evert(x); access(y); splay(y);
56
        if (ch[y][0] != x||ch[x][1] != 0) return;
57
         ch[y][0] = fa[x] = 0; update(x); update(y);
58
    }
59
    inline void link(int x,int y) { fa[evert(x)] = y; }
60
61
62
    // Magic Forest
63
    #include<algorithm>
64
    #include<cstring>
65
    #include<iostream>
66
    #include<cstdio>
67
    #include<cstdlib>
68
    using namespace std;
69
70
    const int maxn = 200010,inf = 1<<29;</pre>
71
    int N,M,A[maxn],B[maxn],fa[maxn],ch[maxn][2];
72
    int stk[maxn],ans = inf; bool rev[maxn];
73
74
    struct Value
75
76
    {
        int ma,mb,id;
77
        inline Value(int _ma = 0,int _mb = 0,int _id = 0):ma(_ma),mb(_mb),id(_id) {}
78
        friend inline Value operator +(const Value &a,const Value &b)
79
        {
80
             Value ret = Value(max(a.ma,b.ma),max(a.mb,b.mb),a.id);
81
             if (B[a.id] < B[b.id]) ret.id = b.id;</pre>
82
```

```
return ret;
83
         }
84
         inline Value merge(int i)
85
         {
86
             Value ret = Value(max(ma,A[i]),max(mb,B[i]),id);
87
             if (B[i] > B[id]) ret.id = i;
88
             return ret;
89
         }
90
    }val[maxn];
91
92
    inline int gi()
93
    {
94
         char ch; int ret = 0,f = 1;
95
         do ch = getchar(); while (!(ch >= '0'&&ch <= '9')&&ch != '-');
96
         if (ch == '-') f = -1, ch = getchar();
97
         do ret = ret*10+ch-'0',ch = getchar(); while (ch >= '0'&&ch <= '9');
98
         return ret*f;
99
    }
100
101
    struct Edge
102
103
         int x,y,a,b;
104
         inline Edge(int x = 0,int y = 0,int a = 0,int b = 0):x(x),y(y),a(a),b(b) {}
105
         inline void read() { x = gi(), y = gi(), a = gi(), b = gi(); }
106
         friend inline bool operator <(const Edge &s,const Edge &t) { return s.a < t.a; }
107
    }edge[maxn];
108
109
    inline bool isroot(int a) { return ch[fa[a]][0] != a&&ch[fa[a]][1] != a; }
110
111
    inline void update(int x) { val[x] = (val[ch[x][0]]+val[ch[x][1]]).merge(x); }
112
    inline void pushdown(int x)
113
    {
114
         if (rev[x])
115
         {
116
             int &lc = ch[x][0],&rc = ch[x][1];
117
             swap(lc,rc);
118
             if (lc) rev[lc] ^= 1;
119
             if (rc) rev[rc] ^= 1;
120
             rev[x] = false;
121
         }
122
    }
123
124
    inline void rotate(int x)
125
126
         int y = fa[x],z = fa[y],1 = ch[y][1] == x,r = 1^1;
127
         if (!isroot(y)) ch[z][ch[z][1] == y] = x; fa[x] = z;
128
         if (ch[x][r]) fa[ch[x][r]] = y; ch[y][1] = ch[x][r];
129
         fa[y] = x; ch[x][r] = y; update(y); update(x);
130
    }
131
```

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```
inline void splay(int x)
132
133
         int top = 0,i;
134
         for (i = x;!isroot(i);i = fa[i]) stk[++top] = i; stk[++top] = i;
135
         while (top) pushdown(stk[top--]);
136
         while (!isroot(x))
137
         {
138
             int y = fa[x],z = fa[y];
139
             if (!isroot(y))
140
             {
141
                  if ((ch[y][0] == x)^(ch[z][0] == y)) rotate(x);
142
                  else rotate(y);
143
             }
144
             rotate(x);
145
         }
146
     }
147
148
     inline int access(int x)
149
150
         int t = 0;
151
         for (t = 0;x;t = x,x = fa[x])
152
             splay(x),ch[x][1] = t,update(x);
153
         return t;
154
     }
155
     inline int evert(int x) { int t; rev[t = access(x)] ^= 1; return t; }
156
     inline int find(int x)
157
158
         x = access(x);
159
         while (pushdown(x),ch[x][0]) x = ch[x][0];
160
         return x;
161
     }
162
     inline void cut(int x,int y)
163
164
         evert(x); access(y); splay(y);
165
         if (ch[y][0] != x||ch[x][1] != 0) return;
166
         ch[y][0] = fa[x] = 0; update(x); update(y);
167
     }
168
     inline void link(int x,int y) { fa[evert(x)] = y; }
169
170
     inline Value query(int x,int y) { evert(x); return val[access(y)]; }
171
172
     int main()
173
     {
174
         // freopen("D.in", "r", stdin);
175
         N = gi(), M = gi();
176
         for (int i = 1;i <= M;++i) edge[i].read();</pre>
177
         sort(edge+1,edge+M+1);
178
         for (int i = 0;i <= N;++i)</pre>
179
             A[i] = B[i] = -inf, val[i] = Value(A[i], B[i], i);
180
```

```
for (int i = 1;i <= M;++i)</pre>
181
             A[i+N] = edge[i].a,B[i+N] = edge[i].b,val[i+N] = Value(A[i+N],B[i+N],i+N);
182
         for (int i = 1;i <= M;++i)
183
184
             if (edge[i].x == edge[i].y) continue;
185
             if (find(edge[i].x) == find(edge[i].y))
186
             {
187
                  Value res = query(edge[i].x,edge[i].y); int id = res.id-N;
188
                  if (edge[i].b < edge[id].b)</pre>
189
190
                      cut(edge[id].x,id+N),cut(edge[id].y,id+N);
191
                      link(edge[i].x,i+N),link(edge[i].y,i+N);
192
                  }
193
             }
194
             else link(edge[i].x,i+N),link(i+N,edge[i].y);
195
             if (find(1) == find(N))
196
197
                  Value res = query(1,N);
198
                  ans = min(ans,res.ma+res.mb);
199
200
         }
201
         if (ans == inf) ans = -1;
202
         printf("%d\n",ans);
203
         return 0;
204
     }
205
```

## 3.7 Merge Split Treap

```
// By zky. To be rewritten.
    const int mo=1e9+7;
    int rnd(){
        static int x=1;
        return x=(x*23333+233);
    int rnd(int n){
        int x=rnd();
        if (x<0)x=-x;
9
        return x%n+1;
10
    }
11
    struct node{
12
        int siz,key;
13
        int val;
14
        LL sum;
15
        node *c[2];
16
        node* rz(){
17
            sum=val;siz=1;
18
            if(c[0])sum+=c[0]->sum,siz+=c[0]->siz;
19
            if(c[1])sum+=c[1]->sum,siz+=c[1]->siz;
20
            return this;
21
```

```
}
22
        node(){}
23
        node(int v){
24
             siz=1;key=rnd();
25
             val=v;sum=v;
26
             c[0]=c[1]=0;
27
         }
28
29
    }pool[maxn*8],*root,*cur=pool,*old_root,*stop;
30
    node *newnode(int v=0){
31
         *cur=node(v);
32
        return cur++;
33
34
    node *old_merge(node *p,node *q){
35
         if(!p&&!q)return 0;
36
        node *u=0;
37
         if(!p||!q)return u=p?p->rz():(q?q->rz():0);
38
         if(rnd(sz(p)+sz(q)) < sz(p)){
39
40
             u - c[1] = old_merge(u - c[1],q);
41
         }else{
42
             u=q;
43
             u - c[0] = old_merge(p, u - c[0]);
44
45
         return u->rz();
46
    }
47
    node *merge(node *p,node *q){
48
         if(!p&&!q)return 0;
49
        node *u=newnode();
50
         if(!p||!q)return u=p?p->rz():(q?q->rz():0);
51
         if(rnd(sz(p)+sz(q)) < sz(p)){
52
             *u=*p;
53
             u - c[1] = merge(u - c[1], q);
54
        }else{
55
             *u=*q;
56
             u->c[0]=merge(p,u->c[0]);
57
58
         return u->rz();
59
    }
60
    node *split(node *u,int 1,int r){
61
         if(1>r||!u)return 0;
62
        node *x=0;
63
         if(l==1&&r==sz(u)){
64
             x=newnode();
65
             *x=*u;
66
             return x->rz();
67
         }
68
         int lsz=sz(u->c[0]);
69
         if(r<=lsz)
70
```

```
return split(u->c[0],1,r);
71
        if(l>lsz+1)
72
            return split(u->c[1],l-lsz-1,r-lsz-1);
73
        x=newnode();
74
        *x=*u;
75
        x->c[0]=split(u->c[0],1,lsz);
76
        x->c[1]=split(u->c[1],1,r-lsz-1);
        return x->rz();
78
79
```

### 3.8 Modui Algorithm on Tree

```
// 询问树上路径元素 mex, inc dec 复杂度不对,需要用线段树/set(带 log) 或者分块 (修改 O(1))
   // 若包括 lca, 每组询问需要把 lca 补 (inc) 上去。
   #include<cstdio>
    #include<cstdlib>
   #include < algorithm>
   #include<cstring>
    #include<iostream>
   using namespace std;
    const int Size = 337,maxn = 200010;
10
    int N,Q,cnt,nxt[maxn],side[maxn],len[maxn],toit[maxn],f[maxn][20],key[maxn],timestamp;
    int dep[maxn],L[maxn],R[maxn],dfn[maxn],ans[maxn],exist[maxn],show[maxn],res;
12
13
    inline void add(int a,int b,int c) { nxt[++cnt] = side[a]; side[a] = cnt; toit[cnt] = b;
14

    len[cnt] = c; }

    inline void ins(int a,int b,int c) { add(a,b,c); add(b,a,c); }
15
    void dfs(int now)
17
18
        dfn[L[now] = ++timestamp] = now;
19
        for (int i = 1; (1<<i) <= dep[now]; ++i) f[now][i] = f[f[now][i-1]][i-1];
20
        for (int i = side[now];i;i = nxt[i])
21
22
            if (toit[i] == f[now][0]) continue;
23
            f[toit[i]][0] = now; key[toit[i]] = len[i];
24
            dep[toit[i]] = dep[now]+1;
25
            dfs(toit[i]);
26
27
        dfn[R[now] = ++timestamp] = now;
28
   }
29
30
    inline int jump(int a,int b) { for (int i = 0;b;b >>= 1,++i) if (b&1) a = f[a][i]; return a; }
31
    inline int lca(int a,int b)
32
33
        if (dep[a] < dep[b]) swap(a,b);</pre>
34
        a = jump(a,dep[a]-dep[b]);
35
        if (a == b) return a;
36
```

```
for (int i = 0;i >= 0;)
37
38
             if (f[a][i] == f[b][i]) --i;
39
             else a = f[a][i], b = f[b][i], ++i;
40
41
        return f[a][0];
42
    }
43
44
    struct Node
45
46
        int a,b,c,id;
47
        Node() = default;
48
        Node(int _a,int _b,int _c = 0,int _id = 0):a(_a),b(_b),c(_c),id(_id) {}
49
        inline void read(int i)
50
        {
51
             id = i; scanf("%d %d",&a,&b); c = lca(a,b);
52
             if (c == a | | c == b) { if (a != c) swap(a,b); a = L[c]+1; b = L[b]; }
53
             else { if (L[a] > L[b]) swap(a,b); a = R[a]; b = L[b]; }
54
55
        friend inline bool operator <(const Node &x,const Node &y) { return x.b < y.b; }
56
    }query[maxn];
57
    inline bool cmp(const Node &x,const Node &y) { return x.a < y.a; }
59
60
    inline void inc(int id)
61
62
        if (key[id] >= maxn) return;
63
        ++exist[key[id]];
64
        while (exist[res]) ++res;
65
    }
66
    inline void dec(int id)
67
68
        if (key[id] >= maxn) return;
69
        --exist[key[id]];
70
         if (key[id] < res&&!exist[key[id]]) res = key[id];</pre>
71
    }
72
73
    inline void work()
74
    {
75
        int 1 = 1, r = 0;
76
        for (int i = 1;i <= Q;++i)</pre>
77
78
             while (r < query[i].b)
79
             {
80
                 show[dfn[++r]]++;
81
                 if (show[dfn[r]] == 2) dec(dfn[r]); else inc(dfn[r]);
82
83
             while (1 > query[i].a)
84
85
```

```
show[dfn[--1]]++;
86
                  if (show[dfn[1]] == 2) dec(dfn[1]); else inc(dfn[1]);
 87
 88
              while (r > query[i].b)
90
                  if (show[dfn[r]] == 1) dec(dfn[r]); else inc(dfn[r]);
91
                  show[dfn[r--]]--;
92
              }
 93
              while (1 < query[i].a)
94
95
                  if (show[dfn[1]] == 1) dec(dfn[1]); else inc(dfn[1]);
96
                  show[dfn[l++]]--;
97
98
              ans[query[i].id] = res;
99
         }
100
     }
101
102
     int main()
103
     {
104
         freopen("F.in","r",stdin);
105
          scanf("%d %d",&N,&Q);
106
         for (int i = 1; i < N; ++i)
107
          {
108
              int a,b,c;
109
              scanf("%d %d %d",&a,&b,&c);
110
              ins(a,b,c);
111
         }
112
         dfs(1);
113
         for (int i = 1;i <= Q;++i) query[i].read(i);</pre>
114
         sort(query+1,query+Q+1,cmp);
115
         for (int i = 1,j;i <= Q;i = j)</pre>
116
117
              for (j = i; j \le Q\&\&query[j].a-query[i].a \le Size;++j);
118
              sort(query+i+1,query+j);
119
         }
120
         work();
121
         for (int i = 1;i <= Q;++i) printf("%d\n",ans[i]);</pre>
122
         return 0;
123
     }
124
```

## 3.9 Modui Algorithm without Deletion

```
1 // r 单调右移, l 只会在 sqrt(N) 中移动, 保证每次 undo 的复杂度可行即可。
2 // CodeForces 620F
3 #include<vector>
4 #include<algorithm>
5 #include<cstring>
6 #include<iostream>
7 #include<cstdio>
```

```
#include<cstdlib>
    using namespace std;
10
    const int maxn = 1000010,len = 200,inf = 1<<29;</pre>
11
    int N,M,pre[maxn],A[maxn],ans[maxn];
12
13
    inline int gi()
14
    {
15
         char ch; int ret = 0,f = 1;
16
        do ch = getchar(); while (!(ch >= '0'&&ch <= '9')&&ch != '-');
17
        if (ch == '-') f = -1, ch = getchar();
18
        do ret = ret*10+ch-'0',ch = getchar(); while (ch >= '0'&&ch <= '9');
19
        return ret*f;
20
    }
21
22
    inline void upd(int &a,int b) { if (a < b) a = b; }</pre>
23
24
    struct Trie
25
26
    {
         int nxt[maxn][2],val[maxn],root,cnt; vector < pair<int,int> > vec;
27
         inline int newnode() { val[++cnt] = inf; memset(nxt[cnt],0,8); return cnt; }
28
         inline void init() { val[0] = inf; cnt = 0; root = newnode(); }
29
30
        inline int query(int key,int num)
31
32
             int now = root,ret = 0;
33
             for (int i = 19; i >= 0; --i)
34
35
                 int dir = !(num&(1<<i));</pre>
36
                 if (val[nxt[now][dir]] <= key)</pre>
37
                     ret |= (1<<i),now = nxt[now][dir];</pre>
38
                 else now = nxt[now][dir^1];
39
             }
40
             return ret;
41
        }
42
43
        inline void insert(int key,int num,int mode) { insert(root,19,key,num,mode); }
44
        inline void insert(int &now,int dep,int key,int num,int mode)
45
         {
46
             if (!now) now = newnode();
47
             if (dep < 0)
48
             {
49
                 if (mode) vec.push_back(make_pair(num,val[now]));
50
                 val[now] = min(val[now], key); return;
51
             }
52
             insert(nxt[now][(num&(1<<dep)) > 0],dep-1,key,num,mode);
53
             val[now] = min(val[nxt[now][0]],val[nxt[now][1]]);
54
        }
55
56
```

```
inline void change(int now,int dep,int num,int v)
57
58
              if (dep < 0) { val[now] = v; return; }</pre>
59
              \label{eq:change_norm} \begin{split} & \texttt{change(nxt[now][(num\&(1<<\texttt{dep})) > 0],dep-1,num,v);} \end{split}
60
              val[now] = min(val[nxt[now][0]],val[nxt[now][1]]);
61
          }
62
63
          inline void undo()
64
65
              reverse(vec.begin(),vec.end());
66
              for (auto x:vec) change(root,19,x.first,x.second);
67
              vec.clear();
68
69
     }tree1,tree2;
70
71
     struct Query
72
73
          int 1,r,id;
74
          inline void read(int i) { 1 = gi(),r = gi(),id = i; }
75
          friend inline bool operator <(const Query &a,const Query &b) { return a.1 < b.1; }
76
     }query[maxn];
77
     inline bool cmp(const Query &a,const Query &b) { return a.r < b.r; }</pre>
79
     inline void work(int l,int r)
80
81
          int lim = query[r].1;
82
          sort(query+1,query+r+1,cmp);
83
          tree1.init(); tree2.init();
84
          for (int i = 1;i <= r;++i)
85
86
              if (query[i].r <= lim)</pre>
87
              {
                   for (int j = query[i].1; j <= query[i].r; ++ j)</pre>
89
                   {
90
                        tree1.insert(A[j],pre[A[j]-1],false);
91
                        tree2.insert(-A[j],pre[A[j]],false);
92
                        upd(ans[query[i].id],tree1.query(A[j],pre[A[j]]));
93
                        upd(ans[query[i].id],tree2.query(-A[j],pre[A[j]-1]));
94
                   }
95
                   tree1.init(),tree2.init();
96
              }
97
              else
98
              {
99
                   int pos = lim,mx = 0;
100
                   for (;i <= r;++i)
101
102
                        while (pos < query[i].r)</pre>
103
                        {
104
                            ++pos;
105
```

```
tree1.insert(A[pos],pre[A[pos]-1],false);
106
                            tree2.insert(-A[pos],pre[A[pos]],false);
107
                            upd(mx,tree1.query(A[pos],pre[A[pos]]));
108
                            upd(mx,tree2.query(-A[pos],pre[A[pos]-1]));
109
110
                       upd(ans[query[i].id],mx);
111
                       for (int j = lim; j >= query[i].1;--j)
112
113
                            tree1.insert(A[j],pre[A[j]-1],true);
114
                            tree2.insert(-A[j],pre[A[j]],true);
115
                            upd(ans[query[i].id],tree1.query(A[j],pre[A[j]]));
116
                            \verb"upd(ans[query[i].id]", tree2.query(-A[j]", pre[A[j]-1]"));
117
                       }
118
                       tree1.undo(); tree2.undo();
119
                  }
120
                  break:
121
              }
122
         }
123
     }
124
125
     int main()
126
127
         // freopen("A.in", "r", stdin);
128
         for (int i = 1;i <= 1000000;++i) pre[i] = pre[i-1]^i;
129
         N = gi(); M = gi();
130
         for (int i = 1;i <= N;++i) A[i] = gi();</pre>
131
         for (int i = 1;i <= M;++i) query[i].read(i);</pre>
132
          sort(query+1,query+M+1);
133
         for (int i = 1,j;i <= M;i = j)</pre>
134
135
              for (j = i; j \le M\&\&query[j].l-query[i].l \le len; ++j);
136
              work(i,j-1);
137
138
         for (int i = 1;i <= M;++i) printf("%d\n",ans[i]);</pre>
139
         return 0;
140
     }
141
```

### 3.10 President Tree

```
inline void build(int &now,int l,int r)

{
    now = ++cnt; if (l == r) return;
    int mid = (l+r)>>1;
    build(tree[now].ch[0],l,mid); build(tree[now].ch[1],mid+1,r);
}

inline void ins(int &now,int ref,int l,int r,int key)

now = ++cnt; tree[now] = tree[ref];
```

```
if (1 == r) { ++tree[now].sum; return; }
int mid = (1+r) >> 1;
if (key <= mid) ins(tree[now].ch[0],tree[ref].ch[0],1,mid,key);
else ins(tree[now].ch[1],tree[ref].ch[1],mid+1,r,key);
tree[now].sum = tree[tree[now].ch[0]].sum+tree[tree[now].ch[1]].sum;
}</pre>
```

## 3.11 Splay

```
//splay
    inline int find(int rk)
4
        for (int now = root;;)
5
            if (rk == size[ch[now][0]]+1) return now;
            else if (rk > size[ch[now][0]]+1)
                 rk -= size[ch[now][1]]+1,now = ch[now][1];
            else now = ch[now][0];
10
        }
11
        return 0;
12
    }
13
14
    inline int upperbound(int x)
15
16
        int ret = 0;
17
        for (int now = root;now;)
18
19
            if (key[now] > x) ret = now,now = ch[now][0];
20
            else now = ch[now][1];
21
        }
22
        return ret;
23
    }
24
    inline int lowerbound(int x)
25
26
        int ret = 0;
27
        for (int now = root;now;)
28
29
            if (key[now] >= x) ret = now,now = ch[now][0];
30
            else now = ch[now][1];
31
32
        return ret;
33
    }
34
35
    inline void rotate(int x)
36
37
        int y = fa[x],z = fa[y],1 = ch[y][0] != x,r = 1^1;
38
        if (z) ch[z][ch[z][0] != y] = x; fa[x] = z;
39
        if (ch[x][r]) fa[ch[x][r]] = y;
40
```

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```
ch[y][1] = ch[x][r]; fa[y] = x; ch[x][r] = y;
41
        update(y); update(x);
42
    }
43
    inline void splay(int x,int aim) //aim is x's father.
44
45
        int top = 0;
46
        for (int i = x;i;i = fa[i]) stack[++top] = i;
47
        while (top) pushdown(stack[top--]);
48
        while (fa[x] != aim)
49
50
            int y = fa[x],z = fa[y];
51
            if (z != aim)
52
53
                 if ((ch[y][0] == x)^(ch[z][0] == y)) rotate(x);
54
                 else rotate(y);
55
            }
56
            rotate(x);
57
58
        if (!aim) root = x;
59
    }
60
61
    // 维修数列
62
    #include<cassert>
63
    #include<queue>
64
    #include<algorithm>
65
    #include<cstring>
66
    #include<iostream>
67
    #include<cstdio>
    #include<cstdlib>
69
    using namespace std;
70
71
    const int maxn = 500010,inf = 1<<29;</pre>
72
    int N,M,root,cnt,arr[maxn],tag[maxn],key[maxn],fa[maxn],ch[maxn][2],lb[maxn],rb[maxn];
73
    int wb[maxn],sum[maxn],size[maxn],stk[maxn]; bool rev[maxn]; char cmd[20]; queue <int> team;
74
75
    inline int gi()
76
77
        char ch; int ret = 0,f = 1;
78
        do ch = getchar(); while (!(ch >= '0'&&ch <= '9')&&ch != '-');
79
        if (ch == '-') f = -1,ch = getchar();
80
        do ret = ret*10+ch-'0',ch = getchar(); while (ch >= '0'&&ch <= '9');
81
        return ret*f;
82
    }
83
84
    inline int newnode(int x = 0)
85
86
        int ret;
87
        if (!team.empty())
88
            ret = team.front(),team.pop();
89
```

```
else ret = ++cnt;
90
         key[ret] = sum[ret] = lb[ret] = rb[ret] = wb[ret] = x;
91
         rev[ret] = false; tag[ret] = inf; size[ret] = 1;
92
         return ret;
93
     }
94
95
     inline void pushdown(int now)
96
97
         int lc = ch[now][0],rc = ch[now][1];
98
         if (rev[now])
99
100
             if (lc)
101
             {
102
                  swap(ch[lc][0],ch[lc][1]);
103
                  swap(lb[lc],rb[lc]); rev[lc] ^= 1;
104
             }
105
             if (rc)
106
             {
107
                  swap(ch[rc][0],ch[rc][1]);
108
                  swap(lb[rc],rb[rc]); rev[rc] ^= 1;
109
             }
110
             rev[now] = false;
111
         }
112
         if (tag[now] != inf)
113
114
             if (lc)
115
             {
116
                  key[lc] = tag[lc] = tag[now]; sum[lc] = tag[lc]*size[lc];
117
                  if (tag[lc] > 0) lb[lc] = rb[lc] = wb[lc] = sum[lc];
118
                  else lb[lc] = rb[lc] = wb[lc] = tag[lc];
119
             }
120
             if (rc)
121
             {
122
                  key[rc] = tag[rc] = tag[now]; sum[rc] = tag[rc]*size[rc];
123
                  if (tag[rc] > 0) lb[rc] = rb[rc] = wb[rc] = sum[rc];
124
                  else lb[rc] = rb[rc] = wb[rc] = tag[rc];
125
126
             tag[now] = inf;
127
         }
128
     }
129
130
     inline void update(int now)
131
     {
132
         // pushdown(now);
133
         int lc = ch[now][0],rc = ch[now][1];
134
         size[now] = size[lc]+size[rc]+1;
135
         sum[now] = sum[lc]+sum[rc]+key[now];
136
         if (lc&&rc)
137
         {
138
```

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```
lb[now] = max(lb[lc],max(sum[lc]+key[now],sum[lc]+key[now]+lb[rc]));
139
             rb[now] = max(rb[rc],max(sum[rc]+key[now],sum[rc]+key[now]+rb[lc]));
140
             wb[now] = max(wb[lc],wb[rc]); wb[now] = max(wb[now],key[now]);
141
             wb[now] = max(wb[now],rb[lc]+key[now]); wb[now] = max(wb[now],lb[rc]+key[now]);
142
             wb[now] = max(wb[now],rb[lc]+key[now]+lb[rc]);
143
         }
144
         else if (lc)
145
         {
146
             lb[now] = max(lb[lc],sum[lc]+key[now]);
147
             rb[now] = max(key[now],key[now]+rb[lc]);
148
             wb[now] = max(wb[lc],key[now]);
149
             wb[now] = max(wb[now],rb[lc]+key[now]);
150
         }
151
         else if (rc)
152
153
         ₹
             rb[now] = max(rb[rc],sum[rc]+key[now]);
154
             lb[now] = max(key[now],key[now]+lb[rc]);
155
             wb[now] = max(wb[rc],key[now]);
156
             wb[now] = max(wb[now],lb[rc]+key[now]);
157
         }
158
         else sum[now] = lb[now] = rb[now] = wb[now] = key[now];
159
    }
160
161
    inline int build(int 1,int r)
162
163
         int mid = (l+r) >> 1,ret = newnode(arr[mid]);
164
         if (1 < mid) ch[ret][0] = build(1,mid-1),fa[ch[ret][0]] = ret;</pre>
165
         if (r > mid) ch[ret][1] = build(mid+1,r),fa[ch[ret][1]] = ret;
166
         update(ret); return ret;
167
    }
168
169
    inline void init()
170
171
         root = newnode(); ch[root][1] = newnode(); fa[2] = 1;
172
         for (int i = 1;i <= N;++i) arr[i] = gi();</pre>
173
         ch[2][0] = build(1,N); fa[ch[2][0]] = 2;
174
         update(2); update(1);
175
    }
176
177
    inline int find(int rk)
178
179
         for (int now = root;;)
180
         {
181
             pushdown(now);
182
             if (rk == size[ch[now][0]]+1) return now;
183
             else if (rk > size[ch[now][0]]+1)
184
                  rk -= size[ch[now][0]]+1,now = ch[now][1];
185
             else now = ch[now][0];
186
         }
187
```

```
return 0;
188
     }
189
190
     inline void rotate(int x)
191
192
         int y = fa[x],z = fa[y],l = ch[y][0] != x,r = 1^1;
193
         if (z) ch[z][ch[z][0] != y] = x;
194
         fa[x] = z; fa[y] = x; fa[ch[x][r]] = y;
195
         ch[y][1] = ch[x][r]; ch[x][r] = y;
196
         update(y); update(x);
197
     }
198
     inline void splay(int x,int aim)
199
200
         int top = 0;
201
         for (int i = x;i;i = fa[i]) stk[++top] = i;
202
         while (top) pushdown(stk[top--]);
203
         while (fa[x] != aim)
204
205
              int y = fa[x],z = fa[y];
206
              if (z != aim)
207
208
                  if ((ch[y][0] == x)^(ch[z][0] == y)) rotate(x);
209
                  else rotate(y);
210
211
              rotate(x);
212
213
         if (!aim) root = x;
214
     }
215
216
     inline void Delete(int &now)
217
     {
218
         if (!now) return;
219
         Delete(ch[now][0]);
220
         Delete(ch[now][1]);
221
         team.push(now); now = 0;
222
     }
223
224
     inline void print()
225
     {
226
         for (int i = 1;i <= cnt;++i)</pre>
227
              printf("%d:%d %d\n",i,ch[i][0],ch[i][1]);
228
         for (int i = 1;i <= cnt;++i)
229
              printf("%d:%d\n",i,fa[i]);
230
231
     }
232
233
     inline void laydown(int now)
234
     {
235
         if (!now) return;
236
```

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```
pushdown(now);
237
         laydown(ch[now][0]);
238
         printf("%d ",key[now]);
239
         laydown(ch[now][1]);
240
         update(now);
241
     }
242
243
     int main()
244
245
         //freopen("C.in", "r", stdin);
246
         N = gi(); M = gi(); init();
247
         while (M--)
248
249
             scanf("%s",cmd);
250
             if (cmd[0] == 'I')
251
             {
252
                  int pos = gi(),a = find(pos+1),b = find(pos+2); N = gi();
253
                  for (int i = 1;i <= N;++i) arr[i] = gi();</pre>
254
                  splay(a,0); splay(b,a);
255
                  ch[b][0] = build(1,N); fa[ch[b][0]] = b;
256
                  update(b); update(a);
257
             }
258
             else if (cmd[0] == 'D')
259
             {
260
                  int pos = gi(); N = gi();
261
                  int a = find(pos),b = find(pos+N+1);
262
                  splay(a,0); splay(b,a);
263
                  Delete(ch[b][0]); update(b); update(a);
264
             }
265
             else if (cmd[0] == 'M' \&\&cmd[2] == 'K')
266
             {
267
                  int pos = gi(); N = gi();
268
                  int a = find(pos),b = find(pos+N+1);
269
                  splay(a,0); splay(b,a);
270
                  key[ch[b][0]] = tag[ch[b][0]] = gi(); sum[ch[b][0]] = tag[ch[b][0]]*size[ch[b][0]];
271
                  if (tag[ch[b][0]] > 0) lb[ch[b][0]] = rb[ch[b][0]] = wb[ch[b][0]] = sum[ch[b][0]];
272
                  else lb[ch[b][0]] = rb[ch[b][0]] = wb[ch[b][0]] = tag[ch[b][0]];
273
                  update(b); update(a);
274
275
             else if (cmd[0] == 'R')
276
277
                  int pos = gi(); N = gi();
278
                  int a = find(pos),b = find(pos+N+1);
279
                  splay(a,0); splay(b,a);
280
                  rev[ch[b][0]] ^= 1;
281
                  swap(ch[ch[b][0]][0],ch[ch[b][0]][1]);
282
                  swap(lb[ch[b][0]],rb[ch[b][0]]);
283
                  update(b); update(a);
284
             }
285
```

```
else if (cmd[0] == 'G')
286
             {
287
                 int pos = gi(); N = gi();
288
                 int a = find(pos),b = find(pos+N+1);
289
                 splay(a,0); splay(b,a);
290
                 printf("%d\n",sum[ch[b][0]]);
291
             }
292
             else
293
             {
294
                 splay(1,0); splay(2,1);
295
                 printf("%d\n", wb[ch[2][0]]);
296
             }
297
         }
298
         return 0;
299
    }
300
```

# Chapter 4

# Graph Theory

#### 4.1 2-Sat

```
// bzoj 1823
    #include<stack>
    #include<iostream>
    #include<cstring>
    #include<cstdio>
    #include<cstdlib>
    using namespace std;
    #define maxn 210
    #define maxm 2010
10
    int n,m,cnt,side[maxn],next[maxm],toit[maxm],dfn[maxn],id[maxn];
    int tot,low[maxn],d[maxn],DFN;
    stack <int> S; bool vis[maxn];
13
14
    inline void init()
15
16
        DFN = tot = cnt = 0; memset(vis,false,2*(n+4));
17
        memset(side,0,8*(n+4)); memset(dfn,0,8*(n+4));
18
    }
19
20
    inline void add(int a,int b) { next[++cnt] = side[a]; side[a] = cnt; toit[cnt] = b; }
21
22
    inline void dfs(int now)
23
24
        S.push(now); dfn[now] = low[now] = ++DFN;
25
        for (int i = side[now];i;i = next[i])
26
27
            if (vis[toit[i]]) continue;
28
            if (!dfn[toit[i]]) dfs(toit[i]);
29
            low[now] = min(low[toit[i]],low[now]);
30
31
        if (low[now] == dfn[now])
32
        {
33
```

```
++tot;
34
             while (S.top() != now) id[S.top()] = tot,vis[S.top()] = true,S.pop();
35
             id[S.top()] = tot,vis[S.top()] = true,S.pop();
36
        }
37
    }
38
39
    int main()
40
    {
41
        freopen("1823.in","r",stdin);
42
        freopen("1823.out","w",stdout);
43
        int T; scanf("%d",&T);
44
        while (T--)
45
46
             scanf("%d %d\n",&n,&m);
47
             init();
48
             while (m--)
49
50
                 char c1,c2; int a,b; bool o1,o2;
51
                 scanf("%c%d %c%d\n",&c1,&a,&c2,&b);
52
                 o1 = c1 == 'h'; o2 = c2 == 'h';
53
                 add((o1^1)*n+a,o2*n+b);
54
                 add((o2^1)*n+b,o1*n+a);
55
             }
56
             int i;
57
             for (i = 1;i <= n<<1;++i) if (!dfn[i]) dfs(i);
58
             for (i = 1; i <= n; ++i) if (id[i] == id[i+n]) { printf("BAD\n"); break; }
             if (i <= n) continue;</pre>
60
             printf("GOOD\n");
61
62
        fclose(stdin); fclose(stdout);
63
        return 0;
64
    }
65
```

## 4.2 Bridges and Cut Vertices

```
// 求割边和割点
   const int maxn = 200010;
   int N,M,cnt,Ts,dfn[maxn],low[maxn],nxt[maxn];
   int toit[maxn], side[maxn];
   bool bridge[maxn], cut[maxn];
   inline void dfs(int now,int fa)
       dfn[now] = low[now] = ++Ts; int child = 0;
9
        for (int i = side[now];i;i = nxt[i])
10
11
            if (toit[i] == fa) continue;
12
            if (!dfn[toit[i]])
13
            {
14
```

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```
dfs(toit[i],now); ++child;
15
                low[now] = min(low[now],low[toit[i]]);
16
                 if (low[toit[i]] > dfn[now]) bridge[i] = true;
17
                 if (low[toit[i]] >= dfn[now]) cut[now] = true;
18
19
            else low[now] = min(low[now],dfn[toit[i]]);
20
21
        if (!fa&&child == 1) cut[now] = false;
22
    }
23
```

#### 4.3 Cost Flow

```
int side[maxv],nxt[maxe],toit[maxe],cost[maxe],pre[maxv];
    int cap[maxv],arr[maxv],dis[maxv]; bool in[maxv];
    int source,sink;
    inline void add(int a,int b,int c,int d) { nxt[++cnt] = side[a]; side[a] = cnt; toit[cnt] = b;

    cap[cnt] = c; cost[cnt] = d; }

    inline void ins(int a,int b,int c,int d) { add(a,b,c,d); add(b,a,0,-d); }
    inline bool spfa(int &Flow,int &Cost)
    {
        queue <int> team; team.push(source);
10
        memset(dis,0x7,4*(sink+5));
11
        dis[source] = 0; in[source] = true;
12
        arr[source] = inf; arr[sink] = 0;
13
        while (!team.empty())
14
15
            int now = team.front(); team.pop();
16
            for (int i = side[now];i;i = nxt[i])
17
            {
18
                if (!cap[i]) continue;
19
                if (dis[toit[i]] > dis[now]+cost[i])
20
                {
21
                     arr[toit[i]] = min(cap[i],arr[now]); pre[toit[i]] = i;
22
                     dis[toit[i]] = dis[now]+cost[i];
23
                     if (!in[toit[i]]) in[toit[i]] = true,team.push(toit[i]);
24
                }
25
            }
26
            in[now] = false;
27
28
        if (!arr[sink]) return false;
29
        Flow += arr[sink];
30
        for (int now = sink,i;now != source;now = toit[i^1])
31
32
            i = pre[now]; Cost += cost[pre[now]]*arr[sink];
33
            cap[i] -= arr[sink]; cap[i^1] += arr[sink];
34
        }
35
        return true;
36
```

37 }

#### 4.4 Difference Constraints

```
// bzoj2330
    #include<iostream>
    #include<stack>
    #include<queue>
    #include<cstdio>
    #include<cstdlib>
    using namespace std;
    #define maxn 100010
9
    #define maxm 200010
10
    int cnt,side[maxn],next[maxm],toit[maxm],cost[maxm],d[maxn];
11
    int nside[maxn],nnext[maxm],ntoit[maxm],ncost[maxm],m,tot;
12
    int dfn[maxn],low[maxn],sum[maxn],id[maxn],arr[maxn],n;
13
    bool vis[maxn]; stack <int> S;
14
15
    inline void add(int a,int b,int c)
16
17
        next[++cnt] = side[a]; side[a] = cnt;
18
        toit[cnt] = b; cost[cnt] = c;
19
    }
20
    inline void ins(int a,int b,int c)
22
    {
23
        nnext[++cnt] = nside[a]; nside[a] = cnt;
24
        ntoit[cnt] = b; ncost[cnt] = c; ++d[b];
25
    }
26
27
    inline void dfs(int now)
28
29
        S.push(now); dfn[now] = low[now] = ++cnt;
30
        for (int i = side[now];i;i = next[i])
31
            if (!vis[toit[i]])
32
33
                 if (!dfn[toit[i]]) dfs(toit[i]);
34
                low[now] = min(low[toit[i]],low[now]);
35
36
        if (low[now] == dfn[now])
37
        {
38
            ++tot;
39
            while (S.top() != now) id[S.top()] = tot,vis[S.top()] = true,S.pop();
40
            id[S.top()] = tot,vis[S.top()] = true,S.pop();
41
        }
42
    }
43
44
    inline bool rebuild()
45
```

```
{
46
        cnt = 0;
47
        for (int i = 1;i <= n;++i)
48
             for (int j = side[i];j;j = next[j])
49
50
                 if (id[toit[j]] == id[i]) sum[id[i]] += cost[j];
51
                 else ins(id[i],id[toit[j]],cost[j]);
52
53
        for (int i = 1;i <= tot;++i) if (sum[i]) return false;</pre>
54
        return true;
55
    }
56
57
    inline void topsort()
58
59
60
        queue <int> team;
        for (int i = 1;i <= tot;++i) if (!d[i]) team.push(i),arr[i] = 1;</pre>
61
        while (!team.empty())
62
63
             int now = team.front(); team.pop();
64
             for (int i = nside[now];i;i = nnext[i])
65
66
                 arr[ntoit[i]] = max(arr[now]+ncost[i],arr[ntoit[i]]);
67
                 if (!--d[ntoit[i]]) team.push(ntoit[i]);
68
             }
69
        }
70
    }
71
72
    int main()
73
74
        freopen("2330.in", "r", stdin);
75
        freopen("2330.out","w",stdout);
76
         scanf("%d %d",&n,&m);
77
        for (int i = 1;i <= m;++i)
78
79
             int x,a,b; scanf("%d %d %d",&x,&a,&b);
80
             if (x == 1) add(a,b,0),add(b,a,0);
81
             else if (x == 2) add(a,b,1);
82
             else if (x == 3) add(b,a,0);
83
             else if (x == 4) add(b,a,1);
84
             else add(a,b,0);
85
        }
86
         cnt = 0; for (int i = n;i;--i) if (!dfn[i]) dfs(i);
87
         if (!rebuild()) printf("-1"),exit(0);
88
        topsort();
89
        long long ans = 0;
90
        for (int i = 1;i <= n;++i) ans += (long long)arr[id[i]];</pre>
91
        printf("%lld",ans);
92
        fclose(stdin); fclose(stdout);
93
        return 0;
94
```

95 }

### 4.5 Dinic Algorithm

```
// dinic
    int source,sink,cnt = 1;
    int d[maxv], side[maxv], cur[maxv], side[maxe], nxt[maxe], toit[maxe]; bool in[maxv];
    inline void add(int a,int b,int c) { nxt[++cnt] = side[a]; side[a] = cnt; toit[cnt] = b;
    \hookrightarrow cap[cnt] = c; }
    inline void ins(int a,int b,int c) { add(a,b,c); add(b,a,0); }
    inline bool bfs()
    {
        queue <int> team; team.push(source); d[source] = 0;
10
        memset(in,false,tot+10); in[source] = true; team.push(source);
11
        while (!team.empty())
12
13
            int now = team.front(); team.pop(); cur[now] = side[now];
14
            for (int i = side[now];i;i = nxt[i])
15
16
                 if (!cap[i]) continue;
17
                 if (!in[toit[i]])
                     in[toit[i]] = true,d[toit[i]] = d[now]+1,team.push(toit[i]);
19
20
21
        return in[sink];
22
    }
23
    inline int dfs(int now,int f)
25
26
        if (now == sink||!f) return f;
27
        int used = 0,w;
        for (int &i = cur[now];i;i = nxt[i])
29
            if (cap[i]&&d[toit[i]] == d[now]+1)
31
                 w = dfs(toit[i],min(cap[i],f-used));
32
                used += w; cap[i] -= w; cap[i^1] += w;
33
                 if (used == f) break;
34
35
        return used;
36
    }
37
38
    inline int dinic(int S,int T)
39
40
        source = S; sink = T; int ret = 0;
41
        while (bfs()) ret += dfs(source,inf);
42
        return ret;
43
    }
44
```

#### 4.6 Dominator Tree

```
//建出来的树点的编号 i 在原图中是 redfn[i]
    int
        N,M,Ts,cnt,side[maxn],nxt[maxn],toit[maxn],dfn[maxn],redfn[maxn],idom[maxn],best[maxn],semi[maxn];
    int ans[maxn], anc[maxn], fa[maxn], child[maxn], size[maxn]; vector <int>
         prod[maxn],bucket[maxn],son[maxn];
    inline void init()
    {
        cnt = 1; memset(side,0,sizeof side); memset(ans,0,sizeof ans);
        for (int i = 0;i <= N;++i) prod[i].clear(),bucket[i].clear(),son[i].clear();</pre>
9
10
    inline void add(int a,int b) { nxt[++cnt] = side[a]; side[a] = cnt; toit[cnt] = b; }
11
12
    inline int gi()
13
14
        char ch; int ret = 0,f = 1;
15
        do ch = getchar(); while (!(ch >= '0'&&ch <= '9')&&ch != '-');
16
        if (ch == '-') f = -1, ch = getchar();
17
        do ret = ret*10+ch-'0',ch = getchar(); while (ch >= '0'&&ch <= '9');
18
        return ret*f;
19
    }
20
21
    inline void dfs(int now)
22
    {
23
        dfn[now] = ++Ts; redfn[Ts] = now;
24
        anc[Ts] = idom[Ts] = child[Ts] = size[Ts] = 0;
25
        semi[Ts] = best[Ts] = Ts;
26
        for (int i = side[now];i;i = nxt[i])
27
        Ł
            if (!dfn[toit[i]])
29
                dfs(toit[i]),fa[dfn[toit[i]]] = dfn[now];
30
            prod[dfn[toit[i]]].push_back(dfn[now]);
31
        }
32
    }
33
34
    inline void compress(int now)
35
36
        if (anc[anc[now]] != 0)
37
        {
38
            compress(anc[now]);
39
            if (semi[best[now]] > semi[best[anc[now]]])
40
                best[now] = best[anc[now]];
41
            anc[now] = anc[anc[now]];
42
        }
43
    }
44
45
    inline int eval(int now)
46
```

```
{
47
        if (!anc[now]) return now;
48
        else
49
        {
50
             compress(now);
51
             return semi[best[anc[now]]] >= semi[best[now]]?best[now]:best[anc[now]];
52
        }
53
    }
54
55
    inline void link(int v,int w)
56
    {
57
        int s = w;
58
        while (semi[best[w]] < semi[best[child[w]]])</pre>
59
60
             if (size[s]+size[child[child[s]]] >= 2*size[child[s]])
61
                 anc[child[s]] = s,child[s] = child[child[s]];
62
             else size[child[s]] = size[s],s = anc[s] = child[s];
63
64
        best[s] = best[w]; size[v] += size[w];
65
        if (size[v] < 2*size[w]) swap(s,child[v]);</pre>
66
        while (s) anc[s] = v,s = child[s];
67
    }
68
69
    inline void lengauer_tarjan()
70
71
        memset(dfn,0,sizeof dfn); memset(fa,-1,sizeof fa); Ts = 0;
72
        dfs(N); fa[1] = 0;
73
        for (int w = Ts; w > 1; --w)
74
75
             for (auto x:prod[w])
76
             {
77
                 int u = eval(x);
                 if (semi[w] > semi[u]) semi[w] = semi[u];
79
             }
80
             bucket[semi[w]].push_back(w);
81
             link(fa[w],w); if (!fa[w]) continue;
82
             for (auto x:bucket[fa[w]])
83
84
                 int u = eval(x);
85
                 if (semi[u] < fa[w]) idom[x] = u;</pre>
86
                 else idom[x] = fa[w];
87
88
             bucket[fa[w]].clear();
89
        }
90
        for (int w = 2; w \le Ts; ++w)
91
             if (idom[w] != semi[w])
92
                 idom[w] = idom[idom[w]];
93
        idom[1] = 0;
94
        for (int i = Ts; i > 1; --i)
95
```

```
{
96
             if (fa[i] == -1) continue;
97
             son[idom[i]].push_back(i);
98
         }
99
    }
100
101
    // 例题: 询问 i 号点到 N 号点所有必经点编号和
102
    #include<algorithm>
103
     #include<cstring>
104
     #include<iostream>
105
    #include<cstdio>
106
    #include<cstdlib>
107
    using namespace std;
108
109
    const int maxn = 100010;
110
    int
111
         N,M,Ts,cnt,side[maxn],nxt[maxn],toit[maxn],dfn[maxn],redfn[maxn],idom[maxn],best[maxn],semi[maxn];
    int ans[maxn],anc[maxn],fa[maxn],child[maxn],size[maxn]; vector <int>
112
         prod[maxn],bucket[maxn],son[maxn];
113
    inline void init()
114
115
         cnt = 1; memset(side,0,sizeof side); memset(ans,0,sizeof ans);
116
         for (int i = 0;i <= N;++i) prod[i].clear(),bucket[i].clear(),son[i].clear();</pre>
117
    }
118
119
    inline void add(int a,int b) { nxt[++cnt] = side[a]; side[a] = cnt; toit[cnt] = b; }
120
121
    inline int gi()
122
123
         char ch; int ret = 0,f = 1;
124
         do ch = getchar(); while (!(ch >= '0'&&ch <= '9')&&ch != '-');
125
         if (ch == '-') f = -1,ch = getchar();
126
         do ret = ret*10+ch-'0',ch = getchar(); while (ch >= '0'&&ch <= '9');
127
        return ret*f;
128
    }
129
130
    inline void dfs(int now)
131
    {
132
         dfn[now] = ++Ts; redfn[Ts] = now;
133
         anc[Ts] = idom[Ts] = child[Ts] = size[Ts] = 0;
134
         semi[Ts] = best[Ts] = Ts;
135
         for (int i = side[now];i;i = nxt[i])
136
137
             if (!dfn[toit[i]])
138
                 dfs(toit[i]),fa[dfn[toit[i]]] = dfn[now];
139
             prod[dfn[toit[i]]].push_back(dfn[now]);
140
         }
141
    }
142
```

```
143
     inline void compress(int now)
144
145
         if (anc[anc[now]] != 0)
146
147
              compress(anc[now]);
148
              if (semi[best[now]] > semi[best[anc[now]]])
149
                  best[now] = best[anc[now]];
150
              anc[now] = anc[anc[now]];
151
         }
152
     }
153
154
     inline int eval(int now)
155
156
         if (!anc[now]) return now;
157
         else
158
159
              compress(now);
160
              return semi[best[anc[now]]] >= semi[best[now]]?best[now]:best[anc[now]];
161
         }
162
     }
163
164
     inline void link(int v,int w)
165
     {
166
         int s = w;
167
         while (semi[best[w]] < semi[best[child[w]]])</pre>
168
169
              if (size[s]+size[child[child[s]]] >= 2*size[child[s]])
170
                  anc[child[s]] = s,child[s] = child[child[s]];
171
              else size[child[s]] = size[s],s = anc[s] = child[s];
172
173
         best[s] = best[w]; size[v] += size[w];
174
         if (size[v] < 2*size[w]) swap(s,child[v]);</pre>
175
         while (s) anc[s] = v,s = child[s];
176
     }
177
178
     inline void lengauer_tarjan()
179
180
         memset(dfn,0,sizeof dfn); memset(fa,-1,sizeof fa); Ts = 0;
181
         dfs(N); fa[1] = 0;
182
         for (int w = Ts; w > 1; --w)
183
184
              for (auto x:prod[w])
185
              {
186
                  int u = eval(x);
187
                  if (semi[w] > semi[u]) semi[w] = semi[u];
188
189
              bucket[semi[w]].push_back(w);
190
              link(fa[w],w); if (!fa[w]) continue;
191
```

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```
for (auto x:bucket[fa[w]])
192
193
                   int u = eval(x);
194
                   if (semi[u] < fa[w]) idom[x] = u;</pre>
195
                   else idom[x] = fa[w];
196
197
              bucket[fa[w]].clear();
198
199
         for (int w = 2; w \le Ts; ++w)
200
              if (idom[w] != semi[w])
201
                   idom[w] = idom[idom[w]];
202
         idom[1] = 0;
203
         for (int i = Ts;i > 1;--i)
204
205
              if (fa[i] == -1) continue;
206
              son[idom[i]].push_back(i);
207
         }
208
     }
209
210
     inline void get_ans(int now)
211
212
         ans[redfn[now]] += redfn[now];
213
         for (auto x:son[now])
214
              ans[redfn[x]] += ans[redfn[now]],get_ans(x);
215
     }
216
217
     int main()
218
     {
219
         //freopen("I.in", "r", stdin);
220
         while (scanf("%d %d", &N, &M) != EOF)
221
         {
222
              init();
223
              for (int i = 1,a,b;i <= M;++i)</pre>
224
                  a = gi(),b = gi(),add(a,b);
225
              lengauer_tarjan(); get_ans(1);
226
              for (int i = 1;i <= N;++i)</pre>
227
                  printf("%d%c",ans[i]," \n"[i == N]);
228
         }
229
         return 0;
230
     }
231
```

# 4.7 Hungary

```
1 //匈牙利算法
2 //Version1
3 inline bool find(int x)
4 {
5    if (cor[x]) return false;
6    for (int i = side[x];i;i = next[i]) if (!used[toit[i]])
```

```
{
             used[toit[i]] = true;
             if (!cho[toit[i]]||find(cho[toit[i]]))
10
                 cho[toit[i]] = x; map[x] = toit[i];
11
                  return true;
12
13
        }
14
        return false;
15
    }
16
17
    inline void hungry()
18
19
        for (int i = 1;i <= p;++i)</pre>
20
             memset(used,false,sizeof(used)),find(i);
21
        for (int i = 1;i <= m;++i)</pre>
22
23
             memset(used,false,sizeof(used)),cho[map[i]] = 0;
24
             find(i),cor[i] = true;
25
        }
26
27
    //Version2
    inline int find(int x)
29
30
        for (int i = 1;i <= n;++i)
31
             if (f[x][i]&&!used[i])
32
             {
33
                 used[i] = true;
34
                 if (!cho[i]||find(cho[i])) { cho[i] = x; return true; }
35
             }
36
        return false;
37
    }
38
39
    inline int hungry()
40
41
        int ret = 0;
42
        for (int i = 1;i <= n;++i)
43
44
             memset(used,false,sizeof(used));
45
             if (find(i)) ret++;
46
        }
47
        return ret;
48
    }
49
```

## 4.8 Isap Algorithm

```
1 // isap: 有毒
2 inline void bfs()
3 {
```

```
queue <int> team; memcpy(cur,side,4*(N+1));
4
        team.push(sink); d[sink] = 1; in[sink] = true;
5
        while (!team.empty())
        {
            int now = team.front(); team.pop(); nd[d[now]]++;
            for (int i = side[now];i;i = nxt[i])
                if (cap[i^1] && !in[toit[i]])
10
                    in[toit[i]] = true,d[toit[i]] = d[now]+1,team.push(toit[i]);
11
        }
12
        for (int i = 1; i <= N; ++i) if (!in[i]) nd[d[i] = N+1]++;
13
   }
14
   inline int isap()
15
16
        int res = 0,now = source,ca = inf;
17
        bfs();
18
        while (d[source] <= N)</pre>
19
20
            if (now == sink)
21
            {
22
                while (now != source)
23
24
                    cap[pre[now]] -= ca; cap[pre[now]^1] += ca;
25
                    now = toit[pre[now]^1];
26
                }
27
                res += ca; ca = inf;
28
            }
29
            bool flag = false; arr[now] = ca;
30
            for (int i = cur[now];i;i = nxt[i])
31
                if (cap[i]&&d[toit[i]]==d[now]-1)
32
33
                    cur[now] = pre[toit[i]] = i; ca = min(ca,cap[i]);
34
                    now = toit[i]; flag = true; break;
35
                }
36
            if (flag) continue; if (!--nd[d[now]]) break; int arg = N;
37
            for (int i = side[now];i;i = nxt[i])
38
                if (cap[i]&&d[toit[i]] < arg) arg = d[toit[i]];</pre>
39
            ++nd[d[now]=arg+1]; cur[now] = side[now];
40
            if (now != source) ca = arr[now = toit[pre[now]^1]];
41
42
        return res;
43
   }
44
45
                        // 源点
46
   int source:
                        // 汇点
   int sink;
47
                        // 可增广路上的上一条弧的编号
    int p[max_nodes];
48
    int num[max_nodes]; // 和 t 的最短距离等于 i 的节点数量
49
    int cur[max_nodes]; // 当前弧下标
50
   int d[max_nodes];
                       // 残量网络中节点 i 到汇点 t 的最短距离
   bool visited[max_nodes];
```

```
53
    // 预处理, 反向 BFS 构造 d 数组
54
    bool bfs()
55
    {
56
        memset(visited, 0, sizeof(visited));
57
         queue<int> Q;
58
         Q.push(sink);
59
         visited[sink] = 1;
60
         d[sink] = 0;
61
         while (!Q.empty()) {
62
             int u = Q.front();
63
             Q.pop();
64
             for (iterator_t ix = G[u].begin(); ix != G[u].end(); ++ix) {
65
                 Edge &e = edges[(*ix)^1];
66
                 if (!visited[e.from] && e.capacity > e.flow) {
67
                     visited[e.from] = true;
68
                     d[e.from] = d[u] + 1;
69
                     Q.push(e.from);
70
                 }
71
             }
72
         }
73
         return visited[source];
74
    }
75
76
    // 增广
77
    int augment()
    {
79
         int u = sink, df = __inf;
80
         // 从汇点到源点通过 p 追踪增广路径, df 为一路上最小的残量
81
         while (u != source) {
82
             Edge &e = edges[p[u]];
83
             df = min(df, e.capacity - e.flow);
84
             u = edges[p[u]].from;
85
        }
86
        u = sink;
87
         // 从汇点到源点更新流量
88
         while (u != source) {
89
             edges[p[u]].flow += df;
90
             edges[p[u]^1].flow -= df;
91
             u = edges[p[u]].from;
92
         }
93
         return df;
94
    }
95
96
    int max_flow()
97
98
         int flow = 0;
99
        bfs();
100
        memset(num, 0, sizeof(num));
101
```

```
for (int i = 0; i < num_nodes; i++) num[d[i]]++;</pre>
102
         int u = source;
103
         memset(cur, 0, sizeof(cur));
104
         while (d[source] < num_nodes) {</pre>
105
              if (u == sink) {
106
                  flow += augment();
107
                  u = source;
108
              }
109
              bool advanced = false;
110
              for (int i = cur[u]; i < G[u].size(); i++) {</pre>
111
                  Edge& e = edges[G[u][i]];
112
                  if (e.capacity > e.flow && d[u] == d[e.to] + 1) {
113
                      advanced = true;
114
                      p[e.to] = G[u][i];
115
                      cur[u] = i;
116
                      u = e.to;
117
                      break;
118
                  }
119
120
              if (!advanced) { // retreat
121
                  int m = num_nodes - 1;
122
                  for (iterator_t ix = G[u].begin(); ix != G[u].end(); ++ix)
123
                      if (edges[*ix].capacity > edges[*ix].flow)
124
                           m = min(m, d[edges[*ix].to]);
125
                  if (--num[d[u]] == 0) break; // gap 优化
126
                  num[d[u] = m+1]++;
127
                  cur[u] = 0;
128
                  if (u != source)
129
                      u = edges[p[u]].from;
130
              }
131
132
         return flow;
133
     }
134
     //By mxh
135
     #define maxn 1010
136
     const int INF=1<<30;</pre>
137
     int n,m;
138
     int S,T;
139
     struct Edge
140
     {
141
         int v,flow,next;
142
     }
          e[510010];
143
     int g[maxn],tot=1;//tot 初值必须赋为 1
144
     void addedge(int x,int y,int flow)
145
146
         e[++tot].v=y;e[tot].flow=flow;e[tot].next=g[x];g[x]=tot;
147
         e[++tot].v=x;e[tot].flow=0;e[tot].next=g[y];g[y]=tot;
148
     }
149
     int w[maxn],hash[maxn],d[maxn];
150
```

```
int que[maxn],pre1[maxn],pre2[maxn],p[maxn];
151
     bool vis[maxn];
152
     int maxflow()
153
     {
154
         for (int i=1;i<=n;i++)</pre>
                                       hash[i]=0,d[i]=0,vis[i]=false;
155
         for (int i=1;i<=n;i++)</pre>
                                       p[i]=g[i];
156
         //hash[0]=n;
157
         int 1,r;
158
         l=r=1;
159
         que[1]=T;hash[0]=1;vis[T]=true;
160
         while (1 \le r)
161
         {
162
              int u=que[1++];
163
              for (int i=g[u];i;i=e[i].next)
164
              if ((i&1) && !vis[e[i].v])
165
              {
166
                   que[++r]=e[i].v;
167
                  vis[e[i].v]=true;
168
                  d[e[i].v]=d[u]+1;
169
                  hash[d[e[i].v]]++;
170
              }
171
         }
172
         for (int i=1;i<=n;i++)</pre>
173
         if (!vis[i])
                           d[i]=n,hash[n]++;
174
         int flow=INF;
175
         int ans=0;
176
         int u=S;
177
         while (d[S]<n)
178
179
              w[u]=flow;
180
              bool bo=true;
181
              for (int i=p[u];i;i=e[i].next)
182
              if (e[i].flow && d[e[i].v]==d[u]-1)
183
              {
184
                  flow=min(flow,e[i].flow);
185
                  p[u]=i;
186
                  pre1[e[i].v]=u;
187
                  pre2[e[i].v]=i;
188
                  u=e[i].v;
189
                  bo=false;
190
                  if (u==T)
191
                   {
192
                       ans+=flow;
193
                       while (u!=S)
194
                       {
195
                            e[pre2[u]].flow-=flow;
196
                            e[pre2[u]^1].flow+=flow;
197
                            u=pre1[u];
198
                       }
199
```

```
flow=INF;
200
                  }
201
                  break;
202
              }
203
              if (!bo)
                            continue;
204
              int minx=n,pos=0;
205
              for (int i=g[u];i;i=e[i].next)
206
              if (e[i].flow && d[e[i].v]<minx)</pre>
                                                       minx=d[e[i].v],pos=i;
207
              p[u]=pos;
208
              hash[d[u]]--;
209
              if (hash[d[u]]==0)
                                       break;
210
              d[u]=minx+1;
211
              hash[d[u]]++;
212
              if (u!=S)
                            u=pre1[u],flow=w[u];
213
214
         return ans;
215
     }
216
```

### Kuhn-Munkres Algorithm

29

```
// Truly O(n^3), 最大权匹配
   // 邻接矩阵,不能连的边设为-INF,求最小权匹配时边权取负,但不能连的还是 -INF,使用时先对 1 -> n 调用 hungary(),再
   struct KM
4
        int w[maxn],lx[maxn],ly[maxn],match[maxn],way[maxn],slack[maxn];
        bool used[maxn];
        inline void init()
            for (int i = 1;i <= N;++i)
10
                match[i] = lx[i] = ly[i] = way[i] = 0;
11
        }
12
13
        inline void hungary(int x)
14
15
            match[0] = x; int j0 = 0;
16
            for (int j = 0; j \le N; ++j)
17
                slack[j] = inf,used[j] = false;
18
            do
19
            {
20
                used[j0] = true;
21
                int i0 = match[j0],delta = inf,j1 = 0;
22
                for (int j = 1; j \leftarrow N; ++j)
23
                    if (!used[j])
24
25
                        int cur = -w[i0][j]-lx[i0]-ly[j];
26
                        if (cur < slack[j])</pre>
27
                            slack[j] = cur,way[j] = j0;
28
                        if (slack[j] < delta)</pre>
```

```
delta = slack[j], j1 = j;
30
31
                  for (int j = 0; j \le N; ++j)
32
33
                      if (used[j]) lx[match[j]] += delta, ly[j] -= delta;
34
                      else slack[j] -= delta;
35
                 }
36
                  j0 = j1;
37
             }
38
             while (match[j0]);
39
             do
40
             {
41
                  int j1 = way[j0];
42
                 match[j0] = match[j1];
43
                  j0 = j1;
44
45
             while (j0);
46
         }
47
48
         inline void work() { for (int i = 1;i <= N;++i) hungary(i); }</pre>
49
50
         inline int get_ans()
51
         {
52
             int sum = 0;
53
             for (int i = 1;i <= N;++i)</pre>
54
55
                  // if (w[match[i]][i] == -inf); //无解
56
                  if (match[i] > 0) sum += w[match[i]][i];
57
             }
58
             return sum;
59
         }
60
    }km;
61
    //最小权匹配
62
    struct KM
63
    {
64
         int w[maxn] [maxn], lx[maxn], ly[maxn], match[maxn], way[maxn], slack[maxn]; bool used[maxn];
65
66
         inline void init()
67
         {
68
             for (int i = 1;i <= N;++i)</pre>
69
                 match[i] = lx[i] = ly[i] = way[i] = 0;
70
         }
71
72
         inline void hungary(int x)
73
74
             match[0] = x; int j0 = 0;
75
             for (int j = 0; j \le N; ++j)
76
                  slack[j] = -inf,used[j] = false;
77
             do
78
```

```
{
79
                  used[j0] = true;
 80
                  int i0 = match[j0],delta = -inf,j1 = 0;
 81
                  for (int j = 1; j \le N; ++j)
 82
                       if (!used[j])
 83
 84
                            int cur = -w[i0][j]-lx[i0]-ly[j];
 85
                            if (cur > slack[j]) slack[j] = cur,way[j] = j0;
 86
                            if (slack[j] > delta) delta = slack[j],j1 = j;
 87
 88
                  for (int j = 0; j \leftarrow N; ++j)
 89
 90
                       if (used[j]) lx[match[j]] += delta,ly[j] -= delta;
91
                       else slack[j] -= delta;
92
93
                  j0 = j1;
94
              }
95
              while (match[j0]);
96
              do
97
              {
98
                   int j1 = way[j0];
99
                  match[j0] = match[j1];
100
                   j0 = j1;
101
102
              while (j0);
103
         }
104
105
         inline void work() { for (int i = 1;i <= N;++i) hungary(i); }</pre>
106
107
         inline int get_ans()
108
         {
109
              int sum = 0;
110
              for (int i = 1;i <= N;++i)</pre>
111
112
                   // if (w[match[i]][i] == inf); // 无解
113
                   if (match[i] > 0) sum += w[match[i]][i];
114
              }
115
              return sum;
116
         }
117
     }km;
118
```

# 4.10 Maximal Matching in General Graphs

```
1  //接口 int matching(), 返回最大匹配数,G 为邻接矩阵
2  inline void push(int x)
3  {
4    team.push(x); check[x] = true;
5    if (!treec[x]) tra[++cnt] = x,treec[x] = true;
6  }
```

```
inline int root(int x) { return f[x]?f[x] = root(f[x]):x; }
    inline void clear()
10
        for (int i = 1,j;i <= cnt;++i)</pre>
11
12
             j = tra[i]; father[j] = 0,f[j] = 0;
13
             check[j] = treec[j] = false;
14
        }
15
    }
16
17
    inline int lca(int u,int v)
18
19
        int len = 0;
20
        for (;u;u = father[match[u]])
21
             pathc[path[++len] = u = root(u)] = true;
22
        for (;;v = father[match[v]])
23
             if (pathc[v = root(v)]) break;
24
        for (int i = 1;i <= len;++i)</pre>
25
             pathc[path[i]] = false;
26
        return v;
27
    }
28
29
    inline void reset(int u,int p)
30
31
        for (int v;root(u) != p;)
32
33
             if (!check[v = match[u]]) push(v);
34
             if (!f[u]) f[u] = p; if (!f[v]) f[v] = p;
35
             u = father[v]; if (root(u) != p) father[u] = v;
36
        }
37
    }
38
39
    inline void flower(int u,int v)
40
    {
41
        int p = lca(u,v);
42
        if (root(u) != p) father[u] = v;
43
        if (root(v) != p) father[v] = u;
44
        reset(u,p); reset(v,p);
45
    }
46
47
    inline bool find(int x)
48
    {
49
        while (!team.empty()) team.pop();
50
        cnt = 0; push(x);
51
        while (!team.empty())
52
53
             int i = team.front(); team.pop();
54
             for (int j = 1; j \le N; ++j)
55
```

```
if (G[i][j]&&root(i) != root(j)&&match[j] != i)
56
57
                     if (match[j]&&father[match[j]]) flower(i,j);
58
                     else if (!father[j])
59
60
                          father[tra[++cnt] = j] = i; treec[j] = true;
61
                          if (match[j]) push(match[j]);
62
                          else
63
                          {
64
                              for (int k = i,l = j,p;k;l = p,k = father[1])
65
                                  p = match[k],match[k] = 1,match[l] = k;
66
                              return true;
67
                          }
68
                     }
69
                 }
70
71
        return false;
72
    }
73
74
    inline int matching()
75
76
        memset(father,0,sizeof father); memset(f,0,sizeof f); memset(path,0,sizeof path);
77
        memset(tra,0,sizeof tra); memset(match,0,sizeof match); memset(check,false,sizeof check);
78
        memset(treec,false,sizeof treec); memset(pathc,false,sizeof pathc);
79
        int ret = cnt = 0;
80
        for (int i = 1;i <= N;++i)</pre>
82
             if (match[i]) continue;
83
             if (find(i)) ++ret; clear();
84
        }
85
        return ret;
86
    }
87
```

### 4.11 Maximal Weighted Matching in General Graphs

```
// 接口 int matching(), 返回最大匹配数,G 为邻接矩阵
   inline void push(int x)
   {
3
       team.push(x); check[x] = true;
       if (!treec[x]) tra[++cnt] = x,treec[x] = true;
   }
   inline int root(int x) { return f[x]?f[x] = root(f[x]):x; }
   inline void clear()
10
       for (int i = 1,j;i <= cnt;++i)
11
12
           j = tra[i]; father[j] = 0,f[j] = 0;
13
           check[j] = treec[j] = false;
14
```

```
}
15
    }
16
17
    inline int lca(int u,int v)
19
        int len = 0;
20
        for (;u;u = father[match[u]])
21
             pathc[path[++len] = u = root(u)] = true;
22
        for (;;v = father[match[v]])
23
             if (pathc[v = root(v)]) break;
24
        for (int i = 1;i <= len;++i)</pre>
25
             pathc[path[i]] = false;
26
        return v;
27
    }
28
29
    inline void reset(int u,int p)
30
31
        for (int v;root(u) != p;)
32
33
             if (!check[v = match[u]]) push(v);
34
             if (!f[u]) f[u] = p; if (!f[v]) f[v] = p;
35
             u = father[v]; if (root(u) != p) father[u] = v;
36
        }
37
    }
38
39
    inline void flower(int u,int v)
40
41
        int p = lca(u,v);
42
        if (root(u) != p) father[u] = v;
43
        if (root(v) != p) father[v] = u;
44
        reset(u,p); reset(v,p);
45
    }
46
47
    inline bool find(int x)
48
    {
49
        while (!team.empty()) team.pop();
50
        cnt = 0; push(x);
51
        while (!team.empty())
52
        {
53
             int i = team.front(); team.pop();
54
             for (int j = 1; j \le N; ++j)
55
                 if (G[i][j]&&root(i) != root(j)&&match[j] != i)
56
                 {
57
                     if (match[j]&&father[match[j]]) flower(i,j);
58
                     else if (!father[j])
59
60
                          father[tra[++cnt] = j] = i; treec[j] = true;
61
                          if (match[j]) push(match[j]);
62
                          else
63
```

```
{
64
                              for (int k = i,l = j,p;k;l = p,k = father[1])
65
                                  p = match[k],match[k] = 1,match[l] = k;
66
                             return true;
67
                         }
68
                     }
69
                 }
70
71
        return false;
72
    }
73
74
    inline int matching()
75
76
        memset(father,0,sizeof father); memset(f,0,sizeof f); memset(path,0,sizeof path);
77
        memset(tra,0,sizeof tra); memset(match,0,sizeof match); memset(check,false,sizeof check);
78
        memset(treec,false,sizeof treec); memset(pathc,false,sizeof pathc);
79
        int ret = cnt = 0;
80
        for (int i = 1;i <= N;++i)
82
            if (match[i]) continue;
83
            if (find(i)) ++ret; clear();
84
85
        return ret;
86
    }
87
```

### 4.12 Maximum Cardinality Search

```
// BZOJ 1006
    #include<algorithm>
    #include<queue>
    #include<cstdio>
    #include<cstdlib>
    #include<set>
    using namespace std;
    #define maxn 10010
    #define maxc 510
10
    #define maxm 1000010
11
    int tot,n,m,cnt,color[maxn][maxc],label[maxn],all;
12
    int side[maxn],next[maxm*2],toit[maxm*2],per[maxn];
13
    bool in[maxn];
    struct node
15
16
        int key,ord;
17
        friend bool operator < (node a,node b) {return a.key > b.key; }
18
    };
19
    multiset <node> S;
20
21
    inline void add(int a,int b)
22
```

```
{
23
        next[++cnt] = side[a]; side[a] = cnt; toit[cnt] = b;
24
    }
25
26
    inline void ins(int a,int b){add(a,b); add(b,a);}
27
28
    inline void mcs()
29
    {
30
         int i,u;
31
         for (i = 1;i <= n;++i) S.insert((node){0,i});</pre>
32
         while (all < n)
33
         {
34
             u = (*S.begin()).ord; S.erase(S.begin()); if (in[u]) continue;
35
             in[u] = true; per[++all] = u;
36
             for (i = side[u];i;i = next[i])
37
                 if (!in[toit[i]])
38
                 {
39
                      label[toit[i]]++;
40
                      S.insert((node){label[toit[i]],toit[i]});
41
                 }
42
         }
43
    }
44
45
    inline void paint()
46
47
         int p,i,j,t;
48
         for (p = 1; p \le n; ++p)
49
50
             i = per[p];
51
             for (j = 1; j \le tot; ++j)
52
                  if (!color[i][j]) {t = j; break; }
53
             if (j == tot + 1) t = ++tot;
54
             for (j = side[i]; j; j = next[j])
55
                 color[toit[j]][t] = true;
56
         }
57
    }
58
59
    int main()
60
    {
61
         freopen("1006.in","r",stdin);
62
         freopen("1006.out","w",stdout);
63
         scanf("%d %d",&n,&m);
64
         for (int i = 1;i <= m;++i)</pre>
65
         { int a,b; scanf("%d %d",&a,&b); ins(a,b); }
66
        mcs();
67
        paint();
68
         printf("%d",tot);
69
         fclose(stdin); fclose(stdout);
70
         return 0;
71
```

72 }

#### 4.13 Network Flow with Lower Bound

#### 1. 无源汇有上下界可行流

设原来源点为 Source, 汇点是 Sink。新建一个超级源 SuperSource 和超级汇 SuperSink。对于原网络中的每一条边  $u \rightarrow v$ ,上界 U,下界 L,将它拆分为三条边:

- (1)  $u \to SuperSink$ , 容量为 L。
- (2)  $SuperSource \rightarrow v$ , 容量为 L。
- (3)  $u \rightarrow v$ , 容量为 U L。

最后添加边  $Sink \to Source$ , 容量为  $+\infty$ 。在新建的网络上, 计算从 SuperSource 到 SuperSink 的最大流。若每条从 SuperSource 发出的边都满流,说明存在可行流,否则不。每条边实际流量为容量下界 + 附加流中它的流量。

#### 2. 有源汇有上下界可行流

在"无源汇有上下界可行流"建图上,新增一条  $Sink \rightarrow Source$  的边,容量为  $+\infty$  即可。

#### 3. 有源汇有上下界最大流

在"有源汇有上下界可行流"建图上,先判断是否存在可行流,若存在可行流,拆掉  $Sink \rightarrow Source$  的边后,接着在图中  $Source \rightarrow Sink$  最大流增广加上原可行流即为最大流答案。(若存在可行流,去掉下界后最大流即为原图有源汇有上下界最大流)

#### 4. 有源汇有上下界最小流

在"有源汇有上下界可行流"建图上,先判断是否存在可行流,若存在可行流,拆掉  $Sink \rightarrow Source$  的边后,用可行流减去在图中  $Sink \rightarrow Source$  增广的最大流即为最小流答案。

在实现时,可以吧 SuperSource 连向同一节点的多条边合成一条(容量合并。从同一节点指向 SuperSink 的多条边也应合并。

对于费用流,只需要改变将网络流算法改成费用流算法。对于原网络中的每一条边  $u \to v$ ,上界 U,下界 L,费用 c,将它拆分为三条边:

- (1)  $u \to SuperSink$ , 容量为 L, 费用 c。
- (2)  $SuperSource \rightarrow v$ , 容量为 L, 费用 0。
- (3)  $u \rightarrow v$ , 容量为 U L, 费用 c。

### 4.14 Point Biconnected Component

```
1 // Source: HackerRank - bonnie-and-clyde
```

- 2 #include<algorithm>
- 3 #include<vector>
- 4 #include<stack>
- 5 #include<iostream>
- 6 #include < cstdio >

```
#include<cstdlib>
    using namespace std;
    const int maxn = 400010;
10
    int N,M,Q,cnt = 1,side[maxn],toit[maxn],nxt[maxn],f[maxn][25],father[maxn],low[maxn];
11
    int tot,dep[maxn],dfn[maxn],nside[maxn],ntoit[maxn],nnxt[maxn]; bool cut[maxn];
12
    stack <int> S; vector <int> bel[maxn],bcc[maxn]; bool vis[maxn];
13
    inline int find(int a) { if (father[a] != a) father[a] = find(father[a]); return father[a]; }
15
16
    inline void add(int a,int b) { nxt[++cnt] = side[a]; side[a] = cnt; toit[cnt] = b; }
17
    inline void ins(int a,int b) { add(a,b); add(b,a); }
18
    inline void nadd(int a,int b) { nnxt[++cnt] = nside[a]; nside[a] = cnt; ntoit[cnt] = b; }
19
    inline void nins(int a,int b) { nadd(a,b); nadd(b,a); }
20
21
    inline int gi()
22
23
        char ch; int ret = 0, f = 1;
24
        do ch = getchar(); while (!(ch >= '0'&&ch <= '9')&&ch != '-');
25
        if (ch == '-') f = -1, ch = getchar();
26
        do ret = ret*10+ch-'0',ch = getchar(); while (ch >= '0'&&ch <= '9');
27
        return ret*f;
29
    }
30
    inline void tj(int now,int fa)
31
    {
32
        dfn[now] = low[now] = ++cnt; int child = 0;
33
        for (int i = side[now];i;i = nxt[i])
34
35
            if (toit[i] == fa) continue;
36
            if (!dfn[toit[i]])
37
            {
38
                S.push(i>>1); tj(toit[i],now); ++child;
39
                low[now] = min(low[now],low[toit[i]]);
40
                 if (low[toit[i]] >= dfn[now])
41
42
                     cut[now] = true; ++tot;
43
                     while (true)
44
                     {
45
                         int t = S.top(); S.pop();
46
                         bel[toit[t<<1]].push_back(tot);</pre>
                                                              bel[toit[t<<1|1]].push_back(tot);</pre>
47
                         bcc[tot].push_back(toit[t<<1]); bcc[tot].push_back(toit[t<<1|1]);</pre>
48
                         if (t == (i>>1)) break;
49
                     }
50
                }
51
52
            else low[now] = min(low[now],dfn[toit[i]]);
53
54
        if (!fa&&child == 1) cut[now] = false;
55
```

```
}
56
57
    inline void build()
58
    {
59
         vector <int> cuts; cnt = 1;
60
         for (int i = 1;i <= tot;++i)
61
         {
62
             sort(bcc[i].begin(),bcc[i].end());
63
             bcc[i].erase(unique(bcc[i].begin(),bcc[i].end()),bcc[i].end());
64
65
         for (int i = 1;i <= N;++i) if (cut[i]) cuts.push_back(i);</pre>
66
         for (auto x:cuts)
67
68
             sort(bel[x].begin(),bel[x].end());
69
             bel[x].erase(unique(bel[x].begin(),bel[x].end()),bel[x].end());
70
             ++tot; for (auto y:bel[x]) nins(tot,y);
71
             bel[x].clear(); bel[x].push_back(tot); bcc[tot].push_back(x);
72
         }
73
    }
74
75
    inline void dfs(int now)
76
77
         vis[now] = true;
78
         for (int i = 1; (1<<i) <= dep[now]; ++i) f[now][i] = f[f[now][i-1]][i-1];
79
         for (int i = nside[now];i;i = nnxt[i])
80
         {
             if (vis[ntoit[i]]) continue; f[ntoit[i]][0] = now;
82
             dep[ntoit[i]] = dep[now]+1; dfs(ntoit[i]);
83
         }
84
    }
85
86
    inline int jump(int a, int b) { for (int i = 0;b;++i,b >>= 1) if (b&1) a = f[a][i]; return a; }
87
    inline int lca(int a,int b)
88
89
         if (dep[a] < dep[b]) swap(a,b);</pre>
90
         a = jump(a,dep[a]-dep[b]); if (a == b) return a;
91
         for (int i = 0;i >= 0;)
92
93
             if (f[a][i] != f[b][i]) a = f[a][i],b = f[b][i],++i;
94
             else --i;
95
         }
96
         return f[a][0];
97
    }
98
99
    inline bool check(int u,int v,int w)
100
101
         if (find(u) != find(v) | |find(v) != find(w)) return false;
102
         if (u == w | | v == w) return true; if (u == v) return false;
103
         int uu = bel[u][0],vv = bel[v][0],ww = bel[w][0],su,sv;
104
```

```
if (uu == ww||vv == ww) return true;
105
         if (lca(uu,ww) == ww) su = jump(uu,dep[uu]-dep[ww]-1); else su = f[ww][0];
106
         if (lca(vv,ww) == ww) sv = jump(vv,dep[vv]-dep[ww]-1); else sv = f[ww][0];
107
         if (su == sv)
108
109
             if (!cut[w]) return false;
110
             else
111
             {
112
                  if (su == uu||sv == vv) return true; int ssu,ssv;
113
                 if (lca(su,uu) == su) ssu = jump(uu,dep[uu]-dep[su]-1); else ssu = f[su][0];
114
                 if (lca(sv,vv) == sv) ssv = jump(vv,dep[vv]-dep[sv]-1); else ssv = f[sv][0];
115
                  if (ssu == ssv) return false; else return true;
116
             }
117
         }
118
         else return true;
119
    }
120
121
    int main()
122
    {
123
         freopen("J.in", "r", stdin);
124
         freopen("J.out","w",stdout);
125
         N = gi(); M = gi(); Q = gi();
126
         for (int i = 1;i <= N;++i) father[i] = i;</pre>
127
         for (int i = 1,a,b;i <= M;++i)
128
129
             ins(a = gi(),b = gi());
130
             a = find(a),b = find(b);
131
             if (a != b) father[a] = b;
132
133
         cnt = 0; for (int i = 1;i <= N;++i) if (!dfn[i]) tj(i,0);</pre>
134
         build(); for (int i = 1;i <= N;++i) if (!vis[i]) dfs(i);
135
         while (Q--)
136
137
             int u = gi(), v = gi(), w = gi();
138
             if (check(u,v,w)) puts("YES"); else puts("NO");
139
         }
140
         return 0;
141
    }
142
```

#### 4.15 Steiner Tree

```
1    /*
2    * Steiner Tree: 求,使得指定 K 个点连通的生成树的最小总权值
3    * st[i] 表示顶点 i 的标记值,如果 i 是指定集合内第 m(O<=m<K) 个点,则 st[i]=1<<m
4    * endSt=1<<K
5    * dptree[i][state] 表示以 i 为根,连通状态为 state 的生成树值
6    */
7    inline void update(int &x,int y) { if (x == -1) x = y; else if (x > y) x = y; }
8    inline void spfa(int state)
```

```
{
9
        while (!team.empty())
10
11
             int now = team.front(); team.pop();
12
             for (int i = side[now];i;i = nxt[i])
13
14
                 int v = toit[i];
15
                 if (f[v][st[v]|state] == -1||f[v][st[v]|state] > f[now][state]+len[i])
16
17
                      f[v][st[v]|state] = f[now][state]+len[i];
18
                      if ((st[v]|state) != state||vis[v][state]) continue;
19
                      vis[v][state] = true; team.push(v);
20
                 }
21
             }
22
             vis[now][state] = false;
23
        }
24
    }
25
    inline int work()
26
    {
27
        endSt = 1 << (K << 1);
28
        memset(f,-1,sizeof(f)); memset(st,0,sizeof(st)); memset(dp,-1,sizeof(dp));
29
        memset(vis,false,sizeof(vis)); memset(side,0,sizeof(side));
30
        for (int i = 1;i <= K;++i) st[i] = 1<<(i-1);
31
        for (int i = 1;i <= K;++i) st[N-K+i] = 1<<(i+K-1);
32
        for (int i = 1;i <= N;++i) f[i][st[i]] = 0;</pre>
33
        for (int j = 1; j < endSt; ++j)
34
35
             for (int i = 1;i <= N;++i)</pre>
36
             {
37
                 if (!st[i]||(st[i]&j))
                      for (int sub = (j-1)\&j; sub; sub = (sub-1)\&j)
39
                      {
40
                          int x = sub|st[i],y = (j-sub)|st[i];
41
                          if (f[i][x] != -1 \&\&f[i][y] != -1)
42
                              update(f[i][j],f[i][x]+f[i][y]);
43
                     }
44
                 if (f[i][j] != -1) team.push(i),vis[i][j] = true;
45
             }
46
             spfa(j);
47
        }
48
    }
49
```

## 4.16 Stoer Wagner Algorithm

```
int G[maxn][maxn],node[maxn],dis[maxn]; bool visit[maxn];
inline int solve(int n)
{
    if (n == 1) return inf;
```

```
int answer = inf;
        for (int i = 0;i < n;++i) node[i] = i;</pre>
        while (n > 1)
        {
             int mx = 1;
10
             for (int i = 0; i < n; ++i)
11
             {
12
                 dis[node[i]] = G[node[0]][node[i]];
13
                 if (dis[node[i]] > dis[node[mx]]) mx = i;
14
             }
15
             int prev = 0;
16
             memset(visit,false,sizeof visit);
             visit[node[0]] = true;
18
             for (int i = 1; i < n; ++i)
19
20
                 if (i == n-1)
21
22
                      answer = min(answer, dis[node[mx]]);
23
                      for (int k = 0; k < n; ++k)
24
                          G[node[k]][node[prev]] = (G[node[prev]][node[k]] += G[node[k]][node[mx]]);
25
                     node[mx] = node[--n];
26
                 }
27
                 visit[node[mx]] = true; prev = mx; mx = -1;
28
                 for (int j = 1; j < n; ++j)
29
                      if (!visit[node[j]])
30
                      {
31
                          dis[node[j]] += G[node[prev]][node[j]];
32
                          if (mx == -1 | dis[node[mx]] < dis[node[j]]) mx = j;
33
                     }
34
             }
35
36
        return answer;
37
    }
38
```

# 4.17 Strongly Connected Component

```
int dfn[maxn],low[maxn],timestamp;
   stack <int> stk; vector <int> scc[maxn];
   void tarjan(int now)
4
        dfn[now] = low[now] = ++timestamp;
        stk.push(now);
        for (int i = side[now];i;i = nxt[i])
            if (!dfn[toit[i]])
                tarjan(toit[i]),low[now] = min(low[now],low[toit[i]]);
10
            else if (!bel[toit[i]]) low[now] = min(low[now],dfn[toit[i]]);
11
        }
12
        if (dfn[now] == low[now])
13
```

4.18. VIRTUAL TREE

```
{
14
             ++tot;
15
             while (stk.top() != now)
16
             {
17
                 scc[tot].push_back(stk.top());
18
                 bel[stk.top()] = tot; stk.pop();
19
20
             scc[tot].push_back(stk.top());
21
             bel[stk.top()] = tot; stk.pop();
22
         }
23
    }
24
```

#### 4.18 Virtual Tree

```
int N,cnt,timestamp,dfn[maxn],f[maxn][25],side[maxn],H[maxn];
    int dep[maxn],toit[maxn],nxt[maxn],last[maxn],cost[maxn],stk[maxn];
    11 best[maxn],g[maxn];
    inline void add(int a,int b,int c) { nxt[++cnt] = side[a]; side[a] = cnt; toit[cnt] = b;
        cost[cnt] = c; }
    inline void ins(int a,int b,int c) { add(a,b,c); add(b,a,c); }
    inline void nadd(int a,int b,int idc)
9
        if (a == b) return;
10
        if (last[a] != idc) side[a] = 0,last[a] = idc;
11
        if (last[b] != idc) side[b] = 0,last[b] = idc;
12
        nxt[++cnt] = side[a]; side[a] = cnt; toit[cnt] = b;
13
    }
14
15
    inline bool cmp(int a,int b) { return dfn[a] < dfn[b]; }</pre>
16
17
    inline void dfs(int now)
18
    {
19
        dfn[now] = ++timestamp;
20
        for (int i = 1;(1<<i) <= dep[now];++i)
21
            f[now][i] = f[f[now][i-1]][i-1];
22
        for (int i = side[now];i;i = nxt[i])
23
            if (toit[i] != f[now][0])
24
25
                best[toit[i]] = min(best[now],(11)cost[i]);
26
                dep[toit[i]] = dep[now]+1;
27
                f[toit[i]][0] = now; dfs(toit[i]);
28
            }
29
    }
30
31
    inline int jump(int a,int step) { for (int i = 0; step; step >>= 1,++i) if (step&1) a = f[a][i];
32

    return a; }

    inline int lca(int a,int b)
```

```
{
34
        if (dep[a] < dep[b]) swap(a,b);</pre>
35
        a = jump(a,dep[a]-dep[b]);
36
        if (a == b) return a;
37
        for (int i = 0;i >= 0;)
38
39
             if (f[a][i] != f[b][i])
40
                 a = f[a][i], b = f[b][i], ++i;
             else --i;
42
43
        return f[a][0];
44
    }
45
46
    inline void work(int idc)
47
48
    {
        cnt = 0; int K = gi(),tot,top;
49
        for (int i = 1;i <= K;++i) H[i] = gi();
50
        sort(H+1,H+K+1,cmp); H[tot = 1] = H[1];
51
        for (int i = 2;i <= K;++i) if (lca(H[tot],H[i]) != H[tot]) H[++tot] = H[i];
52
        stk[top = 1] = 1;
53
        for (int i = 1;i <= tot;++i)
54
55
             int ans = lca(H[i],stk[top]);
56
             while (true)
58
                 if (dep[ans] >= dep[stk[top-1]]) { nadd(ans,stk[top--],idc); break; }
                 nadd(stk[top-1],stk[top],idc); --top;
60
             }
61
             if (stk[top] != ans) stk[++top] = ans;
62
             if (stk[top] != H[i]) stk[++top] = H[i];
63
64
        while (--top) nadd(stk[top],stk[top+1],idc);
65
        // dp(1); printf("%lld\n",g[1]);
66
    }
67
```

## 4.19 Zhu-Liu Algorithm

```
struct Directed_MT

{
    struct Edge
    {
        int u,v,w;
        inline Edge() = default;
        inline Edge(int _u,int _v,int _w):u(_u),v(_v),w(_w) {}
    };

int n,m,vis[maxn],pre[maxn],id[maxn],in[maxn]; Edge edges[maxm];

inline void init(int _n) { n = _n; m = 0; }

inline void AddEdge(int u,int v,int w) { edges[m++] = Edge(u,v,w); }
```

```
inline int work(int root)
13
14
           int ret = 0;
15
           while (true)
16
17
               // 初始化
18
               for (int i = 0;i < n;++i) in[i] = inf+1;</pre>
19
               for (int i = 0; i < m; ++i)
20
21
                   int u = edges[i].u,v = edges[i].v;
22
                   // 找寻最小入边, 删除自环
23
                   if (edges[i].w < in[v] \&\&u != v)
24
                       in[v] = edges[i].w,pre[v] = u;
25
               }
26
               // 如果没有最小入边,表示该点不连通,则最小树形图形成失败
27
               for (int i = 0; i < n; ++i)
28
29
                   if (i == root) continue;
30
                   if (in[i] == inf+1) return inf;
31
               }
32
               int cnt = 0; // 记录缩点
33
               memset(id,-1,sizeof id); memset(vis,-1,sizeof vis);
34
               in[root] = 0;
35
               for (int i = 0; i < n; ++i)
36
37
                   38
                   // 找寻自环
39
                   while (vis[v] != i\&\&id[v] == -1\&\&v != root)
40
                       vis[v] = i,v = pre[v];
41
                   if (v != root&&id[v] == -1)
42
43
                       // 这里不能从 i 开始找, 因为 i 有可能不在自环内
44
                       for (int u = pre[v];u != v;u = pre[u]) id[u] = cnt;
45
                       id[v] = cnt++;
46
                   }
47
               }
48
               // 如果没有自环了,表示最小树形图成功了
49
               if (!cnt) break;
50
               // 找到那些不是自环的, 重新给那些点进行标记
51
               for (int i = 0; i < n; ++i)
52
                   if (id[i] == -1) id[i] = cnt++;
53
               for (int i = 0;i < m;++i)</pre>
54
               {
55
                   int u = edges[i].u,v = edges[i].v;
                   edges[i].v = id[v]; edges[i].u = id[u];
57
                   if (id[u] != id[v]) edges[i].w -= in[v];
58
               }
59
               // 缩点完后,点的数量就变了
60
               n = cnt; root = id[root];
61
```

```
62 }
63 return ret;
64 }
65 }MT;
```

### 4.20 ZKW Cost Flow

```
// To be written
    bool spfa()
    {
        memset(mark,0,sizeof(mark));
        memset(d,0x7,sizeof(d));
5
        d[T] = 0; mark[T] = 1;
        queue <int> team;
        team.push(T);
        while (!team.empty())
10
             int now = team.front();
11
             team.pop();
12
             for (int i = head[now];i;i = e[i].next)
13
                  if (e[i^1].v&&d[e[i].to] > d[now]-e[i].c)
14
                 {
15
                      d[e[i].to] = d[now]-e[i].c;
16
                      if (!mark[e[i].to])
17
                      {
18
                          mark[e[i].to] = true;
19
                          team.push(e[i].to);
20
                      }
21
                 }
22
             mark[now] = false;
23
        }
24
        if (d[0] > 10000000) return false;
25
        return true;
26
    }
27
28
    int dfs(int x,int f)
29
30
        if (x == T)
31
         {
32
             mark[T] = 1;
33
             return f;
34
        }
35
        int used = 0,w;
36
        mark[x] = true;
37
        for (int i = head[x];i;i = e[i].next)
38
              \  \  \text{if } \  (!mark[e[i].to]\&\&e[i].v\&\&d[x]-e[i].c==d[e[i].to]) \\
39
             {
40
                  w = f - used;
41
                 w = dfs(e[i].to,small(e[i].v,w));
42
```

```
ans += w*e[i].c;
43
                 e[i].v -= w;
44
                 e[i^1].v += w;
45
                 used += w;
46
                 if (used == f) return f;
47
            }
48
        return used;
49
   }
50
51
    void zkw()
52
    {
53
        while (spfa())
54
55
            mark[T] = 1;
56
            while (mark[T])
57
            {
58
                 memset(mark,0,sizeof(mark));
59
                 dfs(0,inf);
60
            }
61
        }
62
   }
63
```

# Chapter 5

# Number Theory

### 5.1 Baby Step Giant Step

```
// To Be Verified
   // 求出最小的 t 使得 X^{-}t = Y \mod mod
    inline int bsgs(int X,int Y,int mod)
        int m = ceil(sqrt(mod+0.5)),mul = 1,res = 1;
        if (Y == 1) return 0;
        hash.clear(); hash[Y] = 0;
        for (int i = 1;i <= m;++i)</pre>
            mul = ((11)mul*(11)X)%mod;
            if (mul == Y) return i;
            hash[(11)Y*(11)mul\%mod] = i;
12
13
        res = mul;
14
        for (int i = 2; (i-1)*m <= mod; ++i)
16
            res = (11)res*(11)mul%mod;
            if (hash.find(res) != hash.end()) return i*m-hash[res];
18
        return -1;
20
   }
21
```

#### 5.2 Chinese Remainder Theorem

```
1  //快速乘
2  inline ll qsc(ll a,ll b,ll mod)
3  {
4          ll ret = 0; a %= mod,b %= mod;
5          for (;b;b >>= 1)
6          {
7                if (b&1)
8          {
```

```
ret += a;
9
                 if (ret >= mod) ret -= mod;
10
11
             a += a; if (a >= mod) a -= mod;
12
13
        return ret;
14
    }
15
16
    inline 11 msm(11 a,11 b,11 mod)
17
18
        11 \text{ ret} = 1;
19
        for (;b;b >>= 1,a = qsc(a,a,mod)) if (b%1) ret = qsc(ret,a,mod);
20
        return ret;
21
    }
22
23
    inline 11 crt()
24
25
        11 lcm = 1,ret = 0;
26
        for (int i = 1;i <= K;++i) lcm *= (ll)P[i];
27
        for (int i = 1;i <= K;++i)
28
29
             11 tm = lcm/P[i];
30
             11 inv = msm(tm,P[i]-2,P[i]);
31
             ret = (ret+qsj(qsj(tm,inv,lcm),res[i],lcm))%lcm;
32
        }
33
        return ret;
34
    }
35
```

# 5.3 Extended Euclidean Algorithm

```
//By yxj
   inline ll exgcd(ll a, ll b, ll c) //ax mod b = c
3
        if (a == 0) return -1;
        else if (c \% a == 0) return c/a;
        11 t = exgcd(b \% a,a,((-c \% a)+a)\%a);
        if (t == -1) return -1;
        return (t*b+c)/a;
   }
10
   //Input:a,b,&x,&y,ax+by = gcd(a,b)
11
    //Output:gcd(a,b)
12
   inline int exgcd(int a,int b,int &x,int &y)
13
14
        if (!b) { x = 1,y = 0; return a; }
15
        else
16
        {
17
            int r = exgcd(b,a%b,y,x);
18
            y = x*(a/b); return r;
19
```

```
20 }
```

# 5.4 Linearly Sieve

```
//欧拉函数
   inline void ready()
        phi[1] = 1;
        for (int i = 2;i < maxn;++i)</pre>
            if (!exist[i]) phi[i] = i-1,prime[++tot] = i;
            for (int j = 1; j \le tot; ++j)
                if (i*prime[j] >= maxn) break;
10
                exist[i*prime[j]] = true;
                if (i % prime[j] == 0)
12
                     { phi[i*prime[j]] = phi[i]*prime[j]; break; }
                else phi[i*prime[j]] = phi[i]*phi[prime[j]];
        }
   }
    //莫比乌斯函数
    inline void ready()
19
        mu[1] = 1;
21
        for (int i = 2; i \le 50000; ++i)
22
23
            if (!exist[i]) { prime[++tot] = i; mu[i] = -1; }
            for (int j = 1; j \le tot \&\&prime[j]*i \le 50000; ++j)
25
26
                exist[i*prime[j]] = true;
                if (i % prime[j] == 0) { mu[i*prime[j]] = 0; break; }
                mu[i*prime[j]] = -mu[i];
29
            }
30
        }
   }
```

#### 5.5 N-Power Residue

```
//Input:p,N,a p is a prime
//Output:the solutions to equation x^N=a(mod p) in [O,p-1]
inline vector <int> residue(int p,int N,int a)
{
   int g = PrimitiveRoot(p); ll m = bsgs(g,a,p);
   vector <int> ret;
   if (!a) { ret.push_back(0); return ret; }
   if (m == -1) return ret;
}
A = N,B = p-1,C = m,x,y,d = exgcd(A,B,x,y);
```

```
if (C % d) return ret;
10
        x *= (C / d)\%B;
11
        11 delta = B / d;
12
        for (int i = 0; i < d; ++i)
13
14
             x += delta; if (x >= B) x -= B;
15
             ret.push_back((int)qsm(g,x,p));
16
17
        sort(ret.begin(),ret.end());
18
        ret.erase(unique(ret.begin(),ret.end()),ret.end());
19
        return ret;
20
    }
21
```

#### 5.6 Number Theoretic Transformation

```
// The First Version
    struct node
        int a[maxn*2],len;
        inline void NTT(int loglen,int len,int on)
5
            for (int i = 0,j,t,p;i < len;++i)</pre>
            {
                 for (j = 0,t = i,p = 0;j < loglen;++j,t >>= 1)
                     p <<= 1,p |= t&1;
10
                 if (p > i) swap(a[p],a[i]);
11
            }
12
            for (int s = 1,k = 2;s <= loglen;++s,k <<= 1)
13
14
                 int wn; if (on) wn = e[s]; else wn = ine[s];
15
                 for (int i = 0; i < len; i += k)
16
17
                     int w = 1;
18
                     for (int j = 0; j < (k >> 1); ++j, w = (ll)wn*w%rhl)
19
20
                          int u = a[i+j],v = (ll)w*a[i+j+(k>>1)]%rhl;
21
                          a[i+j] = u+v; if (a[i+j] >= rhl) a[i+j] -= rhl;
22
                          a[i+j+(k>>1)] = u-v;
23
                          if (a[i+j+(k>>1)] < 0) a[i+j+(k>>1)] += rhl;
24
                     }
25
                 }
26
27
            if (!on)
28
            {
29
                 int inv = qsm(len,rhl-2,rhl);
30
                 for (int i = 0;i < len;++i) a[i] = (ll)a[i]*inv%rhl;</pre>
31
            }
32
        }
33
        friend inline bool operator *(node x,node y)
34
```

```
{
35
             int loglen = 0,len;
36
             for (;(1<<loglen)<x.len+y.len;++loglen); len = 1<<loglen;</pre>
37
             x.NTT(loglen,len,1); y.NTT(loglen,len,1);
38
             for (int i = 0;i < (1<<loglen);++i) x.a[i] = (11)x.a[i]*y.a[i]%rhl;</pre>
39
             x.NTT(loglen,len,0);
40
        }
41
    };
42
43
    int main()
44
    {
45
        for (int i = 1; i < 20; ++i)
46
             e[i] = qsm(gg,(rhl-1)>>i,rhl),ine[i] = qsm(e[i],rhl-2,rhl);
47
    }
48
49
    // The Second Version
50
    typedef long long 11;
51
    ll e[20], ine[20];
52
53
    inline ll qsm(ll a,int b,int c)
54
55
        11 \text{ ret} = 1;
56
        for (;b;b >>= 1,(a *= a) %= c) if (b&1) (ret *= a) %= c;
57
        return ret;
58
    }
59
60
    inline void NTT(ll *a,int loglen,int len,int on)
61
62
        for (int i = 0, j, t, p; i < len; ++i)
63
64
             for (j = 0,t = i,p = 0;j < loglen;++j,t >>= 1)
65
                 p <<= 1,p |= t&1;
66
             if (p > i) swap(a[p],a[i]);
67
68
        for (int s = 1,k = 2;s <= loglen;++s,k <<= 1)
69
70
             int wn; if (on) wn = e[s]; else wn = ine[s];
71
             for (int i = 0; i < len; i += k)
72
             {
73
                 int w = 1;
74
                 for (int j = 0; j < (k >> 1); ++j, w = (ll)wn*w%lhh)
75
                 {
76
                      int u = a[i+j], v = (ll)w*a[i+j+(k>>1)]%lhh;
77
                      a[i+j] = u+v; if (a[i+j] >= lhh) a[i+j] -= lhh;
78
                      a[i+j+(k>>1)] = u-v;
79
                      if (a[i+j+(k>>1)] < 0) a[i+j+(k>>1)] += lhh;
80
81
             }
82
        }
83
```

```
if (!on)
84
         {
85
             int inv = qsm(len,lhh-2,lhh);
86
             for (int i = 0;i < len;++i) a[i] = a[i]*inv%lhh;</pre>
87
         }
88
    }
89
90
     struct Polynomial
91
92
         int len; ll array[maxn<<2];</pre>
93
         inline Polynomial(int _len = 0):len(_len) {}
94
         inline Polynomial(ll a[],int n):len(n) { for (int i = 0; i < n; ++i) array[i] = a[i]; }</pre>
95
         inline ll operator [](int n) const { return array[n]; }
96
         inline ll &operator [](int n) { return array[n]; }
97
         inline void set(int n) { len = n; }
98
         inline void set(int n,ll a[]) { len = n; for (int i = 0; i < n; ++i) array[i] = a[i]; }
99
         inline void extend(int key)
100
101
             for (int i = len;i < (1<<key);++i)</pre>
102
                  array[i] = 0;
103
         }
104
         inline void cut(int key) { len = key; }
105
         inline void transform(int loglen,int on) { NTT(array,loglen,1<<loglen,on); }</pre>
106
     }; //变量只能定义在全局, 不然会 re
107
108
     inline Polynomial multiply(Polynomial &pa,Polynomial &ret) // self-multiply
109
     {
110
         int loglen = 0;
111
         while ((1<<loglen) < (pa.len<<1)-1) ++loglen;
112
         pa.extend(1<<loglen); pa.transform(loglen,1);</pre>
113
         for (int i = 0;i < (1<<loglen);++i) ret[i] = pa[i]*pa[i]%lhh;</pre>
114
         ret.transform(loglen,0); ret.cut((pa.len<<1)-1);</pre>
115
         return ret;
116
    }
117
     inline Polynomial multiply(Polynomial &pa,Polynomial &pb,Polynomial &ret)
118
119
         int loglen = 0;
120
         while ((1<<loglen) < (pa.len+pb.len-1)) ++loglen;
121
         pa.extend(1<<loglen); pa.transform(loglen,1);</pre>
122
         pb.extend(1<<loglen); pb.transform(loglen,1);</pre>
123
         for (int i = 0;i < (1<<loglen);++i) ret[i] = pa[i]*pb[i]%lhh;</pre>
124
         ret.transform(loglen,0); ret.cut(pa.len+pb.len-1);
125
         return ret;
126
    }
127
128
    int main()
129
     {
130
         for (int i = 1; i < 20; ++i)
131
             e[i] = qsm(g,(lhh-1)>>i,lhh),ine[i] = qsm(e[i],lhh-2,lhh);
132
```

133 }

# 5.7 Pollard Rho Algorithm

```
const int prime[] = {0,2,3,5,7,11,13,17,19,23,29,31};
    inline 11 mul(11 a,11 b,11 p) { return (a*b-((11)((1d)a/p*b+1e-3)*p)+p)%p; }
    inline bool check(ll m)
        if (m <= 2) return m == 2;</pre>
        11 tmp = m-1; int t = 0;
        while (!(tmp&1)) ++t,tmp >>= 1;
        for (int i = 1; i \le 10; ++i)
10
11
             int a = prime[i];
12
             if (a == m) return true;
13
             ll w = qsm(a,tmp,m);
14
             for (int it = 1;it <= t;++it)</pre>
15
16
                 11 pf = mul(w,w,m);
17
                 if (pf == 1\&\&(w != 1\&\&w != m-1)) return false;
18
                 w = pf;
19
20
             if (w != 1) return false;
21
22
        return true;
23
    }
24
    inline void rho(ll m)
25
26
        if (check(m)) { fac[++nn] = m; return; }
27
        while (true)
28
             11 X = (11) rand() * rand() % (m-1) + 1, Y = X;
30
             11 c = (11)rand()*rand()%(m-1)+1; int i,j;
31
             for (i = j = 2;;++i)
32
33
                 X = (mul(X,X,m)+c) \% m;
34
                 11 d = \_gcd(abs(X-Y),m);
35
                 if (1 < d \& \& d < m) \{ rho(d), rho(m/d); return; }
36
                 if (X == Y) break; if (i == j) Y = X, j <<= 1;
37
38
        }
39
40
    inline void factor(ll m) { nn = 0; if (m > 1) rho(m); sort(fac+1,fac+nn+1); }
41
42
43
    //_int128 Version
44
    typedef __int128 int128;
```

```
inline int128 mul(int128 a,int128 b,int128 mod)
46
47
        int128 ret = 0; a %= mod,b %= mod;
48
        for (;b;b >>= 1)
49
50
             if (b&1)
51
             {
52
                 ret += a;
53
                 if (ret >= mod) ret -= mod;
54
55
             a += a; if (a >= mod) a -= mod;
56
        }
57
        return ret;
58
    }
59
60
    inline int128 qsm(int128 a,int128 b,int128 mod)
61
62
        int128 ret = 1;
63
        for (;b;b >>= 1,a = mul(a,a,mod)) if (b&1) ret = mul(ret,a,mod);
64
        return ret;
65
    }
66
67
    inline void ready()
68
69
        for (int i = 2; i \le 100; ++i)
70
71
             if (prime[i]) continue; prime[++tot] = i;
72
             for (int j = i*i; j \le 100; j += i) prime[j] = 1;
73
        }
74
    }
75
76
    inline int128 gi()
77
78
        int128 ret = 0; char ch;
79
        do ch = getchar(); while (!(ch >= '0'&&ch <= '9'));
80
        do ret = ret*10+ch-'0',ch = getchar(); while (ch >= '0'&&ch <= '9');
81
        return ret;
82
    }
83
84
    inline int128 gcd(int128 a,int128 b) { if (b == 0) return a; return gcd(b,a%b); }
85
86
    inline int128 Abs(int128 a) { if (a < 0) return -a; return a; }</pre>
87
88
    inline bool check(int128 m)
89
90
        if (m <= 2) return m == 2;</pre>
91
        int128 tmp = m-1; int t = 0;
92
        while (!(tmp\&1)) ++t,tmp >>= 1;
93
        for (int i = 1;i <= tot;++i)</pre>
94
```

```
{
95
              int a = prime[i];
96
              if (a == m) return true;
97
              int128 w = qsm(a,tmp,m);
98
              for (int it = 1;it <= t;++it)</pre>
99
100
                  int128 pf = mul(w,w,m);
101
                  if (pf == 1\&\&(w != 1\&\&w != m-1)) return false;
102
                  w = pf;
103
              }
104
              if (w != 1) return false;
105
         }
106
         return true;
107
     }
108
     inline void rho(int128 m)
109
110
         if (check(m)) { fac[++nn] = m; return; }
111
         while (true)
112
113
              int128 X = (int128)rand()*(int128)rand()%(m-1)+1,Y = X;
114
              int128 c = (int128)rand()*(int128)rand()%(m-1)+1; int i,j;
115
              for (i = j = 2;;++i)
116
              {
117
                  X = (mul(X,X,m)+c)\%m;
118
                  int128 d = gcd(Abs(X-Y),m);
119
                  if (1 < d \& \& d < m) \{ rho(d), rho(m/d); return; }
120
                  if (X == Y) break; if (i == j) Y = X, j <<= 1;
121
              }
122
         }
123
     }
124
125
     inline void factor(int128 m) { nn = 0; if (m > 1) rho(m); sort(fac+1,fac+nn+1); }
126
```

## 5.8 Primitive Root

```
_{1} //Input:A prime p
   //Output:p's primitive root
    vector <11> a;
    inline g_test(ll g,ll p)
5
    {
6
        for (ll i = a.size()-1;i >= 0;--i)
            if (qsm(g,(p-1)/a[i],p) == 1) return 0;
        return 1;
9
    }
10
11
    inline 11 PrimitiveRoot(11 p)
12
13
        11 \text{ tmp} = p - 1;
14
```

```
for (11 i = 2; i \le tmp/i; ++i)
15
16
             if (!(tmp % i))
17
             {
                 a.push_back(i);
19
                 while (!(tmp\%i)) tmp /= i;
20
21
             if (tmp != 1) a.push_back(tmp);
22
        }
23
        for (ll g = 1;;++g) if (g_test(g,p)) return g;
24
    }
25
```

# 5.9 Quadratic Residue

```
//判断是否存在 x, 使得 x^2=a \mod n, 存在返回最小 x, 否则返回-1
    inline int modsqr(int a,int n)
        int b,k,i,x;
        if (n == 2) return a & 1;
        if (qsm(a,(n-1)>>1,n) == 1)
            if (n \% 4 == 3) x = qsm(a,(n+1)>>2,n);
            else
10
                for (b = 1; qsm(b, (n-1)>>1, n) == 1; ++b);
                i = (n-1) >> 1; k = 0;
12
13
                do
14
                    i >>= 1,k >>= 1;
                    if (!((qsm(a,i,n)*(ll)qsm(b,k,n)+1)%n)) k += ((n-1)>>1);
16
                while (!(i&1));
                x = (qsm(a,(i+1)>>1,n)*(11)qsm(b,k>>1,n)) % n;
            }
20
            if ((x << 1) > n) x = n-x;
21
            return x;
23
        return -1;
24
   }
25
```

# 5.10 Single Variable Modulus Linear Equation

```
//Input:a,b,n
//Output:All the solutions in [0,n) to the equation ax=b(mod n)
inline vector <1l> LineModEquation(ll a,ll b,ll n)
{
    ll x,y,d = exgcd(a,n,x,y); vector <1l> ans;
    if (!(b % d))
}
```

# Chapter 6

# Numerical Algorithms

### 6.1 Counting Integral Points under Straight Line

```
1  //\sum_{{i = 0}^{n-1} (a+bi)/m}
2  inline ll count(ll n,ll a,ll b,ll m)
3  {
4    if (!b) return n*(a/m);
5    else if (a >= m) return n*(a/m)+count(n,a%m,b,m);
6    else if (b >= m) return (n-1)*n/2*(b/m)+count(n,a,b%m,m);
7    else return count((a+b*n)/m,(a+b*n)%m,m,b);
8  }
```

# 6.2 Evaluation of Expression

```
#include<bitset>
   #include<stack>
   #include<iostream>
   #include<cstdio>
   #include<cstdlib>
    using namespace std;
   const int maxn = 200010;
    int T,N,M,pri[256],match[maxn]; bitset <maxn> A,B; char s[maxn];
10
   inline int gi()
11
12
        char ch; int ret = 0,f = 1;
13
        do ch = getchar(); while (!(ch >= '0'&&ch <= '9')&&ch != '-');
14
        if (ch == '-') f = -1,ch = getchar();
15
        do ret = ret*10+ch-'0', ch = getchar(); while (ch >= '0'&&ch <= '9');
16
        return ret*f;
17
18
19
   inline bitset <maxn> calc(int 1,int r)
20
    {
21
```

```
if (1 > r) return bitset <maxn>();
22
        while (match[1] == r) ++1,r--;
23
        if (1 == r) \{ if (s[1] == 'A') return A; else return B; \}
24
        int cur = 0; pair <int, int> mn(1<<30,0);</pre>
25
        for (int i = 1;i <= r;++i)
26
27
             if (s[i] == '(') cur += 10;
28
             else if (s[i] == '|)') cur -= 10;
             else if (pri[s[i]])
30
                 if (make_pair(cur+pri[s[i]],i) < mn)</pre>
                     mn = make_pair(cur+pri[s[i]],i);
32
        }
        int pos = mn.second; auto L = calc(1,pos-1),R = calc(pos+1,r);
34
        if (s[pos] == '+') return L|R;
        else if (s[pos] == '*') return L&R;
36
        else return ~R;
    }
38
40
    int main()
    {
41
        freopen("H.in", "r", stdin);
42
        freopen("H.out","w",stdout);
43
        pri['+'] = 1; pri['*'] = 2; pri['-'] = 3;
        while (++T)
45
             N = gi(), M = gi(); if (!N) break;
             A.reset(); B.reset(); printf("Case %d: ",T);
             for (int K = gi();K--;) A[gi()] = 1;
             for (int K = gi();K--;) B[gi()] = 1;
             scanf("%s",s+1); stack <int> S;
             for (int i = 1;i <= M;++i) match[i] = -1;
52
             for (int i = 1;i <= M;++i)</pre>
                 if (s[i] == '(') S.push(i);
                 else if (s[i] == |'|)|')
57
                     int t = S.top(); S.pop();
58
                     match[match[t] = i] = t;
59
                 }
60
             }
61
             int tot = 0; auto ans = calc(1,M);
62
             for (int i = 1;i <= N;++i) tot += ans[i]; printf("%d",tot);
63
             for (int i = 1; i \le N; ++i) if (ans[i]) printf(" %d",i); putchar('\n');
64
        }
65
        return 0;
66
67
```

#### 6.3 Fast Fourier Transformation

```
// The First Version
    struct Vir
        double re,im;
        inline Vir(double _re = 0,double _im = 0):re(_re),im(_im) {}
        friend inline Vir operator*(const Vir &a,const Vir &b) { return
        Vir(a.re*b.re-a.im*b.im,a.re*b.im+a.im*b.re); }
        friend inline Vir operator+(const Vir &a,const Vir &b) { return Vir(a.re+b.re,a.im+b.im); }
        friend inline Vir operator-(const Vir &a,const Vir &b) { return Vir(a.re-b.re,a.im-b.im); }
        friend inline Vir operator/(const Vir &a,double r) { return Vir(a.re/r,a.im/r); }
    }pa[maxn],pb[maxn];
10
    inline void fft(Vir *a,int loglen,int len,int on)
12
13
        for (register int i = 0,j,t,p;i < len;++i)</pre>
14
        {
15
            for (p = j = 0, t = i; j < loglen; ++j, t >>= 1)
16
                p <<= 1,p |= (t&1);
17
            if (p > i) swap(a[p],a[i]);
18
19
        for (register int m = 2,s = 1;s <= loglen;++s,m <<= 1)
20
21
            register Vir w(cos(2*pi*on/m),sin(2*pi*on/m));
22
            for (int i = 0; i < len; i += m)
23
24
                register Vir wn(1,0);
25
                for (register int j = 0; j < (m>>1); ++j, wn = wn*w)
26
27
                     register Vir u = a[i+j], v = wn*a[i+j+(m>>1)];
28
                     a[i+j] = u+v; a[i+j+(m>>1)] = u-v;
29
                }
30
            }
31
32
        if (on == -1) for (int i = 0; i < len; i = a[i]/len;
33
    }
34
35
    inline void work()
36
    {
37
        int loglen = 0,len;
38
        while ((1<<loglen) < 1) ++loglen; len = 1 << loglen;
39
        fft(pa,loglen,len,1); fft(pb,loglen,len,1);
40
        for (int i = 0;i < len;++i) pa[i] = pa[i]*pb[i];</pre>
41
        fft(pa,loglen,len,-1);
42
    }
43
44
    //The Second Version
45
    const double pi = acos(-1.0);
46
    struct Complex
```

```
{
48
        double re,im;
49
        inline Complex() = default;
50
        inline Complex(double _re,double _im):re(_re),im(_im) {}
51
        friend inline Complex operator*(const Complex &a,const Complex &b) { return
52
    friend inline Complex operator+(const Complex &a,const Complex &b) { return
53
    friend inline Complex operator-(const Complex &a,const Complex &b) { return
54
       Complex(a.re-b.re,a.im-b.im); }
        friend inline Complex operator/(const Complex &a, double r) { return Complex(a.re/r,a.im/r);
55
        }
   };
56
58
    inline void FFT(Complex *a,int loglen,int len,int on)
59
        for (register int i = 0,j,t,p;i < len;++i)</pre>
60
        {
61
            for (p = j = 0,t = i;j < loglen;++j,t >>= 1)
62
               p <<= 1,p |= (t&1);
63
            if (p > i) swap(a[p],a[i]);
64
65
        for (register int m = 2,s = 1;s <= loglen;++s,m <<= 1)
66
67
            register Complex w(cos(2*pi*on/m),sin(2*pi*on/m));
68
            for (int i = 0; i < len; i += m)
69
            {
70
                register Complex wn(1,0);
                for (register int j = 0; j < (m>>1); ++j, wn = wn*w)
72
73
                    register Complex u = a[i+j],v = wn*a[i+j+(m>>1)];
74
                    a[i+j] = u+v; a[i+j+(m>>1)] = u-v;
75
               }
76
            }
77
78
        if (on == -1) for (int i = 0; i < len; i = a[i]/len;
79
   }
80
    struct Polynomial
82
    {
83
        int len; Complex array[maxn<<2];</pre>
84
        inline Polynomial(int _len = 0):len(_len) {}
85
        inline Polynomial(Complex a[],int n):len(n) { for (int i = 0;i < n;++i) array[i] = a[i]; }</pre>
86
        inline Complex operator [](int n) const { return array[n]; }
87
        inline Complex &operator [](int n) { return array[n]; }
88
        inline void set(int n) { len = n; }
89
        inline void set(int n,Complex a[]) { len = n; for (int i = 0;i < n;++i) array[i] = a[i]; }</pre>
90
        inline void extend(int key)
91
92
```

```
for (int i = len;i < (1<<key);++i)</pre>
93
                  array[i] = Complex(0,0);
94
95
         inline void cut(int key) { len = key; }
         inline void transform(int loglen,int on) { FFT(array,loglen,1<<loglen,on); }</pre>
97
     }; //变量只能定义在全局, 不然会 re
98
     inline Polynomial multiply(Polynomial &pa,Polynomial &ret) // self-multiply
100
101
         int loglen = 0;
102
         while ((1<<loglen) < (pa.len<<1)-1) ++loglen;
103
         pa.extend(1<<loglen); pa.transform(loglen,1);</pre>
104
         for (int i = 0;i < (1<<loglen);++i) ret[i] = pa[i]*pa[i];</pre>
105
         ret.transform(loglen,-1); ret.cut((pa.len<<1)-1);</pre>
106
         return ret;
107
    }
108
    inline Polynomial multiply(Polynomial &pa,Polynomial &pb,Polynomial &ret)
109
110
         int loglen = 0;
111
         while ((1<<loglen) < (pa.len+pb.len-1)) ++loglen;
112
         pa.extend(1<<loglen); pa.transform(loglen,1);</pre>
113
         pb.extend(1<<loglen); pb.transform(loglen,1);</pre>
114
         for (int i = 0;i < (1<<loglen);++i) ret[i] = pa[i]*pb[i];</pre>
115
         ret.transform(loglen,-1); ret.cut(pa.len+pb.len-1);
116
         return ret;
117
118
    }
```

# 6.4 Fast Input and Output

```
// Input and Output of Int
   // Be careful of Max_Int and Min_Int
   inline int gi()
    {
        char ch; int ret = 0,f = 1;
        do ch = getchar(); while (!(ch >= '0'&&ch <= '9')&&ch != '-');
        if (ch == '-') f = -1,ch = getchar();
        do ret = ret*10+ch-'0',ch = getchar(); while (ch >= '0'&&ch <= '9');
        return ret*f;
   }
10
11
   inline void pi(int a)
12
13
        if (!a) putchar('0');
14
        if (a < 0) a = -a,putchar('-');</pre>
15
        int num[10],n = 0;
16
        while (a) num[n++] = a\%10, a /= 10;
        for (int i = n-1; i >= 0; --i) putchar('0'+num[i]);
18
   }
19
```

#### 6.5 Fraction Class

```
typedef long long 11;
   struct Fraction
        11 num,den;
4
        inline Fraction(ll a = 0,ll b = 1)
            if (den < 0) a = -a,b = -b;
            assert(b != 0); ll g = gcd(abs(a),b);
            num = a/g; den = b/g;
10
       friend inline Fraction operator +(const Fraction &a,const Fraction &b) const { return
11

    Fraction(a.num*b.den+b.num*a.den,a.den*b.den); }

        friend inline Fraction operator -(const Fraction &a,const Fraction &b) const { return
12

    Fraction(a.num*b.den-b.num*a.den,a*den*b.den); }

       friend inline Fraction operator *(const Fraction &a,const Fraction &b) const { return
13
    → Fraction(a.num*b.num,a*den*b.den); }
        friend inline Fraction operator /(const Fraction &a,const Fraction &b) const { return

    Fraction(a.num*b.den,a*den*b.num); }

       friend inline bool operator <(const Fraction &a,const Fraction &b) const { return
15

    a.num*b.den < a.den*b.num; }
</pre>
       friend inline bool operator <(const Fraction &a,const Fraction &b) const { return
       a.num==b.num&&a.den==b.den; }
   };
17
```

# 6.6 Gray Code

```
1  //O-2^n-1 的格雷码
2  inline vector <int> GrayCreat(int n)
3  {
4     vector <int> res;
5     for (int i = 0;i < (1<<n);++i) res.push_back(i^(i>>1));
6     return res;
7  }
```

# 6.7 Numerical Integration

6.8. SIMPLEX 125

```
10
    //romberg---To Be Verified
11
    template <class T>
12
    inline double romberg(const T &f, double a, double b, double eps = 1e-8)
13
14
        vector <double> t; double h = b-a,last,cur;
15
        int k = 1, i = 1;
16
        t.push_back(h*(f(a)+f(b))/2);
17
18
        {
19
            last = t.back(); cur = 0; double x = a+h/2;
20
            for (int j = 0; j < k; ++j) cur += f(x), x += h;
21
            cur = (t[0]+h*cur)/2;
22
            double k1 = 4.0/3, k2 = 1.0/3;
23
            for (int j = 0; j < i; ++j)
24
            {
25
                 double temp = k1*cur-k2*t[j];
26
                 t[j] = cur; cur = temp; k2 /= 4*k1-k2; k1 = k2+1;
27
28
            t.push_back(cur); k *= 2; h /= 2; ++i;
29
30
        while (fabs(last - cur) > eps);
31
        return t.back();
32
   }
33
```

## 6.8 Simplex

#### 6.8.1 Description

有 n 个实数变量  $x_1, x_2, \ldots, x_n$  和 m 条约束,其中第 i 条约束形如  $\sum_{i=1}^n a_{i,j} x_j \leq b_i$ 。 此外这 n 个变量需要满足非负性限制, $x_i \geq 0$ 。

在满足上述所有条件的情况下,你需要指定每个变量  $x_j$  的取值,使得目标函数  $F = \sum_{j=1}^n c_j x_j$  的值最大。

#### 6.8.2 Input

第一行三个正整数 n, m, t。其中  $t \in \{0, 1\}$ 。

第二行有 n 个整数  $c_1, c_2, \ldots, c_n$ , 整数间均用一个空格分隔。

接下来 m 行,每行代表一条约束,其中第 i 行有 n+1 个整数  $a_{i1}, a_{i2}, \ldots, a_{in}, b_i$ ,整数间均用一个空格分隔。

#### **6.8.3** Output

如果不存在满足所有约束的解,仅输出一行"Infeasible"。

如果对于任意的 M,都存在一组解使得目标函数的值大于 M,仅输出一行 "Unbounded"。 否则,第一行输出一个实数,表示目标函数的最大值 F。 如果 t = 1,那么你还需要输出第二行,用空格隔开的 n 个非负实数,表示此时  $x_1, x_2, ..., x_n$  的取值,如有多组方案请任意输出其中一个。

#### 6.8.4 Code

```
1 // uoj 179
          #include<iostream>
          #include<cstdio>
          #include<cstdlib>
          using namespace std;
          #define maxn (30)
          #define eps (1e-8)
          int N,M,op,tot,q[maxn],idx[maxn],idy[maxn]; double a[maxn][maxn],A[maxn];
10
11
          inline void pivot(int x,int y)
12
13
                      swap(idy[x],idx[y]);
14
                     double tmp = a[x][y]; a[x][y] = 1/a[x][y];
15
                     for (int i = 0;i <= N;++i) if (y != i) a[x][i] /= tmp;
16
                     tot = 0; for (int i = 0; i \le N; ++i) if (i != y&&(a[x][i] > eps | |a[x][i] < -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] < -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] < -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] < -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] < -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] < -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] < -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] < -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] < -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] < -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] > -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] > -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] > -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] > -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] > -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] > -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] > -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] > -eps)) q[++tot] = (int i = 0; i \le N; ++i) if (i != y&(a[x][i] > eps | |a[x][i] > -eps)) q[++tot] = (int i = 0; i := 0;
             \hookrightarrow i;
                     for (int i = 0;i <= M;++i)</pre>
18
                                if ((x == i) | | (a[i][y] < eps&&a[i][y] > -eps)) continue;
                                for (int j = 1; j \le tot; ++j) a[i][q[j]] -= a[x][q[j]]*a[i][y];
21
                                a[i][y] = -a[i][y]/tmp;
                     }
23
          }
24
25
          int main()
27
                     freopen("179.in", "r", stdin);
29
                     freopen("179.out", "w", stdout);
                      scanf("%d %d %d",&N,&M,&op); srand(233);
                     for (int i = 1;i <= N;++i) scanf("%lf",a[0]+i);</pre>
31
                     for (int i = 1;i <= M;++i)</pre>
                     {
33
                                for (int j = 1; j <= N;++j) scanf("%lf",a[i]+j);</pre>
                                scanf("%lf",a[i]);
35
                     }
37
                     for (int i = 1;i <= N;++i) idx[i] = i;
                     for (int i = 1;i <= M;++i) idy[i] = i+N;</pre>
                     while (true)
                                int x = 0, y = 0;
                                for (int i = 1; i <= M; ++i) if (a[i][0] < -eps&&((!x)||(rand()&1))) x = i; if (!x) break;
42
                                for (int i = 1; i <= N; ++i) if (a[x][i] < -eps&&((!y)||(rand()&1))) y = i; if (!y) return
                    puts("Infeasible"),0;
```

```
pivot(x,y);
44
45
        while (true)
46
47
            int x = 0, y = 0; double mn = 1e15;
48
            for (int i = 1; i \le N; ++i) if (a[0][i] > eps) { y = i; break; } if (!y) break;
49
            for (int i = 1; i <= M; ++i) if (a[i][y] > eps && a[i][0]/a[i][y] < mn) mn =
50
        a[i][0]/a[i][y],x = i; if (!x) return puts("Unbounded"),0;
            pivot(x,y);
51
52
        printf("%.81f\n",-a[0][0]); if (!op) return 0;
53
        for (int i = 1;i <= M;++i) if (idy[i] <= N) A[idy[i]] = a[i][0];</pre>
        for (int i = 1;i <= N;++i) printf("%.8lf ",A[i]);</pre>
55
        fclose(stdin); fclose(stdout);
56
        return 0;
57
   }
58
```

## 6.9 Solutions of Equation of Higher Order

```
// vector <double> solve(vector <double> coef,int n)
    // coef 方程的系数; n 方程的系数
    // 输出所有实数解
    const double EPS = 1e-15,inf = 1e12;
    inline int sign(double x) { return x < -EPS?-1:x > EPS; }
    inline double get(const vector <double> &coef,double x)
9
        double e = 1, s = 0;
10
        for (int i = 0;i < coef.size();++i) s += coef[i]*e,e *= x;</pre>
11
        return s;
12
    }
13
    inline double find(const vector <double> &coef,int n,double lo,double hi)
15
16
        double sign_lo,sign_hi;
17
        if ((sign_lo = sign(get(coef,lo)))== 0) return lo;
18
        if ((sign_hi = sign(get(coef,hi)))== 0) return hi;
19
        if (sign_lo*sign_hi > 0) return inf;
20
        for (int step = 0; step < 100&&hi-lo > EPS; ++step)
21
22
            double m = (lo+hi)/2; int sign_mid = sign(get(coef,m));
23
            if (sign_mid == 0) return m;
24
            else if (sign_lo*sign_mid < 0) hi = m;</pre>
25
            else lo = m;
26
27
        return (lo+hi)/2;
28
    }
29
30
```

```
inline vector <double> solve(const vector <double> &coef,int n)
31
32
        vector <double> ret;
33
        if (n == 1)
34
35
             if (sign(coef[1])) ret.push_back(-coef[0]/coef[1]);
36
             return ret;
37
        }
38
        vector <double> dcoef(n);
39
        for (int i = 0;i < n;++i) dcoef[i] = coef[i+1]*(i+1);</pre>
40
        vector <double> droot = solve(dcoef,n-1);
41
        droot.insert(droot.begin(),-inf);
42
        droot.push_back(inf);
43
        for (int i = 0;i+1 < droot.size();++i)</pre>
44
        {
45
             double tmp = find(coef,n,droot[i],droot[i+1]);
46
             if (tmp < inf) ret.push_back(tmp);</pre>
47
48
        return ret;
49
   }
50
```

# Chapter 7

# String Algorithms

#### 7.1 Aho-Corasick Automaton

```
// ac 自动机
    inline int newnode()
        memset(nxt[L],-1,sizeof(nxt[L]));
        return ++L-1;
    inline void init() { L = 0; root = newnode(); }
    inline void insert()
        int len = strlen(buf),now = root;
10
        for (int i = 0; i < len; ++i)
11
12
            if (nxt[now][buf[i]-'0'] == -1)
13
                nxt[now][buf[i]-'0'] = newnode();
14
            now = nxt[now][buf[i]-'0'];
15
        }
16
        end[now] = true;
18
    inline void build()
19
20
        int now = root; queue <int> team;
21
        fail[root] = root;
22
        for (int i = 0; i < 10; ++i)
23
24
            if (nxt[now][i] == -1) nxt[now][i] = root;
25
            else fail[nxt[now][i]] = root,team.push(nxt[now][i]);
26
        }
27
        while (!team.empty())
28
29
            now = team.front(); team.pop();
30
            for (int i = 0; i < 10; ++i)
31
32
                 if (nxt[now][i] == -1)
33
```

```
nxt[now][i] = nxt[fail[now]][i];
34
                 else
35
                  {
36
                      fail[nxt[now][i]] = nxt[fail[now]][i];
37
                      team.push(nxt[now][i]);
38
                 }
39
             }
40
        }
41
42
```

# 7.2 Knuth-Morris-Pratt Algorithm

```
// To Be Verified
   void cal_next(char *str, int *next, int len)
        int i,j;
        next[0] = -1;
        for (int i = 1; i < len; i++)
            j = next[i - 1];
            while (str[j+1] != str[i] \&\&(j >= 0)) j = next[j];
            if (str[i] == str[j+1]) next[i] = j + 1;
            else next[i] = -1;
        }
12
   }
14
    int KMP(char *str,int slen, char *ptr,int plen,int *next)
16
        int s_i = 0,p_i = 0;
        while (s_i < slen&&p_i < plen)
18
19
            if (str[s_i] == ptr[p_i]) s_i++,p_i++;
            else
22
                if (!p_i) s_i++;
                else p_i = next[p_i-1] + 1;
        return (p_i == plen)?(s_i - plen):-1;
27
   }
```

# 7.3 Manacher Algorithm

```
for (int i = 1;i <= 11;++i)
             hash[i] = hash[i-1]*37+s[i]-'A'+1,bin[i] = 37*bin[i-1];
    }
9
10
    inline void manacher()
11
12
        rad[1] = 1; int best = 1;
13
        for (int i = 2;i <= 2*11+1;++i)
14
15
             int j;
16
             if (best+rad[best]-1 < i) j = 1;
17
             else j = min(rad[2*best-i],best+rad[best]-i)+1;
18
             while (i-j+1&&i+j-1 \le 2*11+1&&bac[i-j+1] ==bac[i+j-1])
19
20
                 if (bac[i+j-1] != '#')
21
                 {
22
                     ull h = (hash[(i+j-1)>>1]-hash[((i-j+1)>>1)-1]*bin[j]);
23
                     if (!exist1[h\%rhl1]||!exist2[h\%rhl2]||!exist3[h\%rhl3])
24
25
                          exist1[h%rhl1]=exist2[h%rhl2]=exist3[h%rhl3] = true;
26
                          ++tot, have [tot] [0] = (i-j+1)>>1;
27
                          have[tot][1] = (i+j-1)>>1;
28
                     }
29
                 }
30
                 ++j;
31
             }
32
             rad[i] = j-1;
33
             if (i+rad[i]>best+rad[best]) best = i;
34
        }
35
    }
36
```

#### 7.4 Palindrome Automaton

```
// Correct but to Be Rewritten
   struct pat
3
        int next[maxn] [26],fail[maxn],cnt[maxn],len[maxn],s[maxn],last,n,p;
4
        inline int newnode(int 1) { cnt[p] = 0; len[p] = 1; return p++; }
        inline void init() { last = n = p = 0; newnode(0); newnode(-1); s[0] = -1; fail[0] = 1; }
        inline int getfail(int x) { while (s[n-len[x]-1] != s[n]) x = fail[x]; return x; }
       inline void add(int c)
            c -= 'a'; s[++n] = c; int cur = getfail(last);
10
            if (!next[cur][c])
11
12
                int now = newnode(len[cur]+2);
13
                fail[now] = next[getfail(fail[cur])][c];
14
                next[cur][c] = now;
15
            }
16
```

# 7.5 Suffix Array

```
// 记得最后填一个字符集中没有的字符
   inline void build(char *buf,int *Sa,int *Rank,int *Height,int n,int now,int m)
        int i,j,k,*x = t1,*y = t2;
       memset(c,0,4*m);
        for (i = 0; i < n; ++i) c[x[i] = buf[i]-'A']++;
        for (i = 1; i < m; ++i) c[i] += c[i-1];
        for (i = n-1; i \ge 0; --i) Sa[--c[x[i]]] = i;
        for (k = 1; k < n; k <<= 1)
            int p = 0;
            for (i = n-k; i < n; ++i) y[p++] = i;
            for (i = 0; i < n; ++i) if (Sa[i] >= k) y[p++] = Sa[i] - k;
13
            memset(c,0,4*m);
            for (i = 0; i < n; ++i) c[x[y[i]]] ++;
            for (i = 1; i < m; ++i) c[i] += c[i-1];
16
            for (i = n-1;i >= 0;--i) Sa[--c[x[y[i]]]] = y[i];
            swap(x,y); p = 1; x[Sa[0]] = 0;
18
            for (i = 1; i < n; ++i)
                x[Sa[i]] = y[Sa[i-1]] == y[Sa[i]] \& y[Sa[i-1]+k] == y[Sa[i]+k]?p-1:p++;
20
            if (p >= n) break; m = p;
        for (i = 0;i < n;++i) Rank[Sa[i]] = i;
        for (i = k = 0; i < n; ++i)
24
            if (k) --k; if (!Rank[i]) continue;
            j = Sa[Rank[i]-1];
            while (i+k< n\&\&j+k< n\&\&buf[i+k] == buf[j+k]) ++k;
28
            Height[Rank[i]] = k;
   }
```

#### 7.6 Suffix Automaton

```
// Correct but to Be Rewritten
struct SAM
{
    int tot,tail,cnt,p,np,q,nq,sz[maxn],arr[maxn],step[maxn],tran[maxn][26],parent[maxn];
    inline SAM() { tail = tot = 1; }
    inline void insert(int c)
    {
        p = tail; np = tail = ++tot; step[np] = step[p]+1;
        for (;!tran[p][c];p = parent[p]) tran[p][c] = np;
```

```
if (!p) parent[np] = 1;
10
             else
11
             {
12
                 q = tran[p][c];
13
                 if (step[p]+1 == step[q]) parent[np] = q;
14
                 else
15
                 {
16
                     nq = ++tot; step[nq] = step[p]+1;
                     memcpy(tran[nq],tran[q],104);
18
                      parent[nq] = parent[q]; parent[np] = parent[q] = nq;
19
                      for (;tran[p][c] == q;p = parent[p]) tran[p][c] = nq;
20
                 }
21
             }
22
             sz[np] = 1;
23
        }
24
25
        inline void dfs(int now)
26
27
             if (vis[now]) return; vis[now] = true;
28
             for (int i = 0; i < 26; ++i)
29
                 if (tran[now][i]) dfs(tran[now][i]),arr[now] += arr[tran[now][i]];
30
             arr[now] += sz[now];
31
        }
32
33
        inline void build()
34
35
             if (!mode) for (int i = 1; i \le tot; ++i) sz[i] = 1;
36
             else
37
             {
38
                 for (int i = 2;i <= tot;++i) ++d[parent[i]];</pre>
39
                 queue <int> team; for (int i = 1;i <= tot;++i) if (!d[i]) team.push(i);</pre>
40
                 while (!team.empty())
41
42
                      int now = team.front(); team.pop();
43
                      sz[parent[now]] += sz[now];
44
                      if (!--d[parent[now]]) team.push(parent[now]);
45
                 }
46
             }
47
             sz[1] = 0; dfs(1);
48
        }
49
        inline void work()
50
51
             int now = 1,1 = 0,rank = 0; memset(s,0,N+1);
52
             if (K > arr[1]) puts("-1");
53
             else
54
             {
                 while (true)
56
                 {
57
                     rank += sz[now]; if (rank >= K) break;
58
```

```
for (int i = 0; i < 26; ++i)
59
60
                          if (rank+arr[tran[now][i]] < K) rank += arr[tran[now][i]];</pre>
61
                          else { s[++1] = 'a'+i; now = tran[now][i]; break; }
62
                      }
63
                 }
64
                 printf("%s",s+1);
65
             }
66
        }
67
    }sam;
68
```

# Chapter 8

# Others

## 8.1 Calculation of Date

```
//ya 年 ma 月 da 日与 yb 年 mb 月 db 日相差几天
    const int days = 365,s[] = {0,31,28,31,30,31,30,31,30,31,30,31};
    inline bool isleap(int y)
        if ((!(y\%400)||y\%100)\&\&!(y\%4)) return true;
        return false;
    inline int leap(int y)
10
        if (!y) return 0;
11
        return y/4-y/100+y/400;
12
    }
13
14
    inline int calc(int day,int mon,int year)
15
16
        int res = (year-1)*days+leap(year-1);
17
        for (int i = 1;i < mon;++i) res += s[i];</pre>
18
        if (isleap(year)&&mon > 2) res++;
19
        res += day; return res;
20
    }
21
22
    inline int count_day(int da,int ma,int ya,int db,int mb,int yb)
23
24
        int resa = calc(da,ma,ya);
25
        int resb = calc(db,mb,yb);
26
        return abs(resa-resb);
27
    }
28
```

#### 8.2 Java Hints

```
// Code 1
   import java.io.*;
    import java.math.*;
    import java.util.*;
   public class Main
        final static int lhh = 998244353,maxn = 1655;
        static long jc[] = new long [maxn];
10
        static int calc(BigInteger N)
11
12
             if (N.compareTo(BigInteger.ONE) <= 0) return 0;</pre>
13
             // System.out.println(N);
14
             int 1 = 2,r = 1650,mid;
15
             while (1 \le r)
16
17
                 mid = (l+r)>>1;
18
                 if (((BigInteger.valueOf(mid)).pow(mid)).compareTo(N) <= 0) 1 = mid+1;</pre>
19
                 else r = mid-1;
20
21
             // System.out.println(l+" "+r);
22
             int ret = (int) jc[r]-1,d = 1; if (ret < 0) ret += lhh;</pre>
23
             int digit[] = new int[d]; BigInteger _d = BigInteger.valueOf(1);
24
             for (int i = 0; i < d; ++i)
25
             {
26
                 digit[i] = N.mod(_d).intValue();
27
                 N = N.divide(_d);
28
29
             // for (int i = d-1; i \ge 0; --i) System.out.print(digit[i]);
30
             // System.out.println();
31
             boolean cho[] = new boolean[d],safe = false,exist = true;
32
             Arrays.fill(cho,false);
33
             int per[] = new int [d];
34
             for (int i = d-1; i >= 0;--i)
35
36
                 int cur = -1;
37
                 if (safe)
38
39
                     int down = i == d-1?1:0;
40
                     for (int j = d-1; j \ge down; --j)
41
42
                          if (cho[j] == true) continue;
43
                          cur = j; break;
44
45
                     if (cur == -1) { exist = false; break; }
46
                     cho[cur] = true; per[i] = cur;
47
                 }
48
```

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```
else
49
                 {
50
                      if (cho[digit[i]] == true)
51
                      {
52
                          // System.out.println(i+":"+digit[i]);
53
                          while (i < d)
54
55
                              cur = -1;
56
                              int down = i == d-1?1:0;
57
                              for (int j = digit[i]-1; j \ge down; --j)
58
59
                                   if (cho[j] == true) continue;
60
                                   cur = j; break;
61
62
                              // System.out.println(cur+":"+i);
63
                              if (cur == -1) { ++i; if (i < d) cho[per[i]] = false; }
64
                              else { cho[cur] = true; per[i] = cur; break; }
65
                          }
66
67
                          if (cur == -1) { exist = false; break; }
68
                          safe = true;
69
                      }
70
                      else
71
                      {
72
                          if (digit[i] == 0 \&\&i == d-1)  { exist = false; break; }
73
                          per[i] = digit[i];
74
                          cho[digit[i]] = true;
75
                      }
76
                 }
77
             }
78
             // for (int i = d-1; i \ge 0; --i) System.out.print(per[i]);
79
             // System.out.println();
80
             if (!exist) return ret;
81
             for (int i = d-1; i >= 0; --i)
82
             {
83
                 int tmp = per[i];
84
                 for (int j = d-1; j > i; --j)
85
                      if (per[j] < per[i]) --tmp;</pre>
86
                 ret += jc[i]*tmp%lhh;
87
                 if (ret >= lhh) ret -= lhh;
88
89
             ret++; if (ret >= lhh) ret -= lhh;
90
             ret -= jc[d-1]; if (ret < 0) ret += lhh;
91
             // System.out.println(ret);
92
             return ret;
93
        }
94
95
        public static void main(String args[])
96
97
```

```
jc[0] = 1;
98
              for (int i = 1; i \le 1650; ++i)
99
                  jc[i] = jc[i-1]*(long)i%lhh;
100
              Scanner cin = new Scanner(System.in);
101
              int T = cin.nextInt();
102
103
              while (T-- > 0)
104
105
                  BigInteger 1 = cin.nextBigInteger(),r = cin.nextBigInteger();
106
                  int ans = calc(r)-calc(l.subtract(BigInteger.ONE));
107
                  if (ans < 0) ans += lhh; System.out.println(ans);</pre>
108
109
              // calc(BigInteger.valueOf(123455));
110
         }
111
     }
112
113
     //Code 2
114
     import java.io.*;
115
     import java.util.*;
116
     import java.math.*;
117
     public class Main
118
119
         static BigDecimal ratio[] = new BigDecimal[110];
120
         public static void main(String[] args)
121
122
              Scanner cin = new Scanner(System.in);
123
              int T = cin.nextInt();
124
              for (int Case = 1;Case <= T;++Case)</pre>
125
126
                  int N = cin.nextInt();
127
                  for (int i = 1;i <= N;++i)</pre>
128
129
                      String S = cin.next();
130
                       String[] str = S.split(":");
131
                       BigDecimal a = new BigDecimal(str[0]),b = new BigDecimal(str[1]);
132
                       ratio[i] = a.divide(a.add(b),30,BigDecimal.ROUND_HALF_EVEN);
133
                  }
134
                  Arrays.sort(ratio,1,N+1);
135
                  BigDecimal res = new BigDecimal(0), 1 = new BigDecimal(1); int ans = 0;
136
                  for (int i = 1; i \le N; ++i)
137
138
                       res = res.add(ratio[i]);
139
                       if (res.compareTo(_1) < 0) ans = i;</pre>
140
                       else break;
141
142
                  System.out.println("Case #"+Case+": "+ans);
143
144
         }
145
     }
146
```

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```
147
     // Code 3
148
     import java.math.*;
149
     import java.util.*;
150
     public class Main
151
152
         static BigInteger d,ret,temp,yy;
153
         static int n,dd;
154
         static boolean mark = true;
155
         static BigInteger[] a = new BigInteger[20];
156
         public static void main(String[] args)
157
158
             Scanner in = new Scanner (System.in);
159
             n = in.nextInt();
160
             temp = BigInteger.ONE;
161
             ret = BigInteger.ZERO;
162
             for (int i = 0; i < n; ++i)
163
             {
164
                  int k = in.nextInt();
165
                  a[i] = BigInteger.valueOf(k);
166
                  d = temp.gcd(a[i]);
167
                  temp = temp.multiply(a[i]).divide(d);
168
169
             for (int i = 1;i < (1<<n);++i)
170
171
                 mark = false; yy = BigInteger.ONE;
172
                  for (int j = 0; j < n; ++j) if (((1 << j) & i) > 0) { mark = !mark; d = a[j].gcd(yy);
173
          yy = yy.multiply(a[j]).divide(d); }
                  if (mark) ret = ret.add(temp.divide(yy));
174
                  else ret = ret.subtract(temp.divide(yy));
175
176
             d = ret.gcd(temp);
177
             System.out.println(ret.divide(d));
178
             System.out.println(temp.divide(d));
179
         }
180
     }
181
182
     // Code 4
183
     import java.io.*;
184
     import java.math.*;
185
     import java.util.*;
186
187
     public class Main
188
189
         public static String reverse(String str) { return new
190
         StringBuffer(str).reverse().toString(); }
191
         public static void main(String args[])
192
193
```

```
Scanner cin = new Scanner(System.in);
194
             int T = cin.nextInt(); BigInteger zero = BigInteger.valueOf(0);
195
             while (T-- > 0)
196
             {
197
                  int base1 = cin.nextInt(),base2 = cin.nextInt();
198
                  String S = cin.next(); int len = S.length();
199
                  System.out.println(base1+" "+S);
200
                  BigInteger res = BigInteger.valueOf(0),b1 = BigInteger.valueOf(base1),b2 =
201
          BigInteger.valueOf(base2);
                  for (int i = 0; i < len; ++i)
202
203
                      res = res.multiply(b1);
204
                      int rep = 0;
205
                      if (S.charAt(i) >= '0'&&S.charAt(i) <= '9') rep = S.charAt(i)-'0';</pre>
206
                      else if (S.charAt(i) \ge 'A'\&\&S.charAt(i) \le 'Z') rep = 10+S.charAt(i)-'A';
207
                      else rep = 36+S.charAt(i)-'a';
208
                      res = res.add(BigInteger.valueOf(rep));
209
                  }
210
                  String ret = new String();
211
                  // System.out.println(res);
212
                  if (res.compareTo(zero) == 0) ret += '0';
213
                  else
214
                      while (res.compareTo(zero) > 0)
215
216
                          long val = res.remainder(b2).longValue();
217
                          // System.out.println(val);
218
                          if (val < 10) ret += (char)(val+'0');</pre>
219
                          else if (val < 36) ret += (char)(val+'A'-10);</pre>
220
                          else ret += (char)(val+'a'-36);
221
                          res = res.divide(b2);
222
223
                  System.out.println(base2+" "+reverse(ret)+"\n");
224
225
         }
226
     }
227
```

# 8.3 Emacs Configuration-Full

```
;; comment-dwim
12
   (defun strong-comment-dwim-line (&optional arg)
13
14
    → "Replacement for the comment-dwim command. If no region is selected and current line is not blank and we a
     (interactive "*P")
15
     (comment-normalize-vars)
16
     (if (and (not (region-active-p)) (not (looking-at "[\t]*$")))
17
         (comment-or-uncomment-region (line-beginning-position) (line-end-position))
18
       (comment-dwim arg)))
19
    (global-set-key (kbd "M-;") 'strong-comment-dwim-line)
20
    ;; Remove tool bar
21
   (tool-bar-mode -1)
22
   ;;不要滚动栏,现在都用滚轴鼠标了,可以不用滚动栏了
23
   (scroll-bar-mode -1)
24
   ;;设置行号
25
   (global-linum-mode t)
26
   ;; Change the Title
27
   (setq frame-title-format "%b@lmxyy'-emacs")
28
   ;;滚动页面时比较舒服,不要整页的滚动
29
   (setq scroll-step 1
30
           scroll-margin 3
31
           scroll-conservatively 10000)
32
   ;; 设置界面 start
33
   (if window-system
34
       (setq default-frame-alist
35
             (append
36
              '( (top . 0)
37
                 (left . 0)
38
                 (width . 300)
39
                 (height . 300))
40
              default-frame-alist))
41
42
   ;; 允许 emacs 和外部其他程序的粘贴
43
   (setq x-select-enable-clipboard t)
44
   ;; 去掉菜单栏, 我将 F10 绑定为显示菜单栏, 万一什么东西忘了, 需要菜单栏了可以摁 F10 调出, 再摁 F10 就去掉菜单
45
   (menu-bar-mode -1)
46
   ;;显示列号
47
   (setq column-number-mode t)
48
   ;; 开启语法高亮。
49
   (global-font-lock-mode 1)
50
   ;; Auto Indent
51
   (global-set-key (kbd "RET") 'newline-and-indent)
52
53
54
   :: -----Tex Mode-----
55
   ;; Emacs 加载 Auctex
56
   (load "auctex.el" nil t t)
57
   (load "preview-latex.el" nil t t)
   (setq Tex-auto-save t)
```

```
(setq Tex-parse-self t)
60
    (setq-default Tex-master nil)
61
    ;;设置编译信息
62
    (defun compile-xelatex ()
63
      (interactive)
64
      (compile (format "xelatex -shell-escape %s" (buffer-name))))
65
    (global-set-key (kbd "<f6>") 'compile-xelatex)
66
    (defun compile-latex ()
67
      (interactive)
68
      (compile (format "latex -shell-escape %s" (buffer-name))))
69
    (global-set-key (kbd "C-<f6>") 'compile-latex)
70
71
    ;; -----C++ Mode-----
72
    ;;设置编译信息
73
    (defun compile-cpp ()
74
      (interactive)
75
      (compile (format "g++ -o %s %s -g -lm -Wall -std=c++11" (file-name-sans-extension
76
    (global-set-key (kbd "<f9>") 'compile-cpp)
77
    (defun compile-cpp-02 ()
78
     (interactive)
79
      (compile (format "g++ -o %s %s -g -lm -Wall -std=c++11 -02" (file-name-sans-extension
80
    (global-set-key (kbd "C-<f9>") 'compile-cpp-02)
81
    ;;设置一键调试
82
    (global-set-key (kbd "<f8>") 'gud-gdb)
83
    ;; 设置 tab 为 4 个空格的宽度
84
    (setq c-basic-offset 4)
85
    (setq default-tab-width 4)
86
87
    ;; -----Java Mode-----
88
    ;;设置编译信息
89
    (defun compile-java ()
90
      (interactive)
91
      (compile (format "javac %s" (buffer-name))))
92
    (global-set-key (kbd "<f7>") 'compile-java)
93
94
    ;; -----Org Mode-----
95
    (setq org-startup-indented t)
96
    ;; The following lines are always needed. Choose your own keys.
97
    (add-to-list 'auto-mode-alist '("\\.org\\'" . org-mode))
98
    (add-hook 'org-mode-hook 'turn-on-font-lock); not needed when global-font-lock-mode is on
99
    (global-set-key "\C-cl" 'org-store-link)
100
    (global-set-key "\C-ca" 'org-agenda)
101
    (global-set-key "\C-cb" 'org-iswitchb)
102
103
    ;; -----Ido Mode-----
104
    ;; 启用 ido 模式
105
    (ido-mode t)
106
```

```
107
    ;; -----Custon Sets-----
108
    (custom-set-variables
109
     ;; custom-set-variables was added by Custom.
110
     ;; If you edit it by hand, you could mess it up, so be careful.
111
     ;; Your init file should contain only one such instance.
112
     ;; If there is more than one, they won't work right.
113
     '(column-number-mode t)
114
     '(cua-mode t nil (cua-base))
115
     '(inhibit-startup-screen t)
116
     '(menu-bar-mode nil)
117
     '(tool-bar-mode nil))
118
    (custom-set-faces
119
     ;; custom-set-faces was added by Custom.
120
     ;; If you edit it by hand, you could mess it up, so be careful.
121
     ;; Your init file should contain only one such instance.
122
     ;; If there is more than one, they won't work right.
123
     '(default ((t (:family "Courier 10 Pitch" :foundry "bitstream" :slant normal :weight bold
124
```

# 8.4 Emacs Configuration-Competition

```
;; Default Font: Courier 10 Pitch Bold
                                              Size: 15
   ;; Remember to set CUA-mode and save your options.
   (global-set-key (kbd "M-n") 'forward-paragraph)
   (global-set-key (kbd "M-p") 'backward-paragraph)
   (global-linum-mode t)
   (defun compile-cpp ()
     (interactive)
     (compile (format "g++ -o %s %s -g -lm -Wall -std=c++11" (file-name-sans-extension

    (buffer-name))(buffer-name))))
    (global-set-key (kbd "<f9>") 'compile-cpp)
   (global-set-key (kbd "<f8>") 'gud-gdb)
10
   (setq default-tab-width 4)
11
   (setq c-basic-offset 4)
12
   (global-set-key (kbd "RET") 'newline-and-indent)
```