Evolution de la population d'Homo Néanderthal

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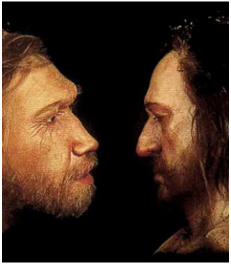


Contexte biologique

Présentation des modèles étudiés
Cadre général

Modèle général

$$\frac{\partial u(t,x)}{\partial t} = f(u(t,x)) + d\Delta u(t,x), \quad t \in \mathbb{R}, x \in \mathbb{R} \tag{1}$$

u(t,x) : Densité de population $\in [0,1]$

d : Constante de diffusion

Présentation des modèles étudiés

Croissance logistique

Croissance Logistique

$$\frac{\partial u(t,x)}{\partial t} = f(u(t,x)) + d\Delta u(t,x)$$

$$f(u(t,x)) = \alpha u(1 - \frac{u}{K})$$

K : Capacité de transport

α : Taux de croissance maximum

Présentation des modèles étudiés
Modèle Allee

Modèle Allee

$$\frac{\partial u(t,x)}{\partial t} = f(u(t,x)) + d\Delta u(t,x)$$

$$f(u(t,x)) = ku(1-u)(u-A)$$

k : Taux de croissance normalisé constant

A : Densité critique

$$k = \frac{4}{(1-A)^2}$$

Présentation des modèles étudiés

Système de Lolkta-Volterra

Modèle de compétition

$$\begin{cases} \frac{\partial u(t,x)}{\partial t} = f(u,v) + d_1 \Delta u \\ \frac{\partial v(t,x)}{\partial t} = g(u,v) + d_2 \Delta v \end{cases}$$

$$f(u,v) = \alpha_1 u \left(1 - \frac{u}{K_1} - \gamma_1 \frac{v}{K_1}\right), g(u,v) = \alpha_2 v \left(1 - \frac{v}{K_2} - \gamma_2 \frac{u}{K_2}\right)$$

u(t,x) : Densité de population des Hommes Modernes

v(t,x) : Densité de population des Hommes de Néanderthal

K_1 et K_2 : Capacités d'accueil du milieu

γ_1 et γ_2 : Coefficients de compétition

α_1 et α_2 : Taux de croissance

Analyse mathématique

Croissance logistique

Analyse mathématique

Effet Allee

Analyse mathématique

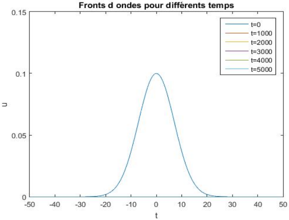
Système de Lolkta Volterra

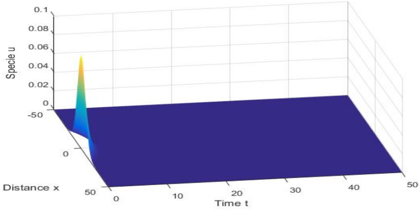
Simulations Numériques

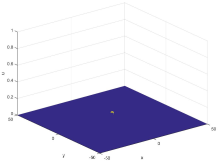
Croissance logistique

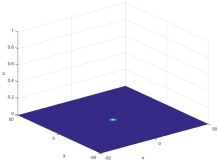
Simulations Numériques

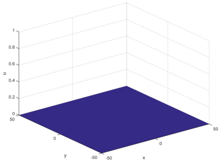
Modèle Allee : $d = 0.5, A = 0.25(k = 64), u_0 = 0.1$





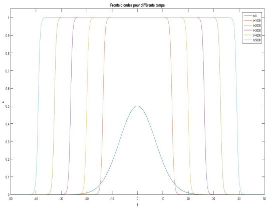


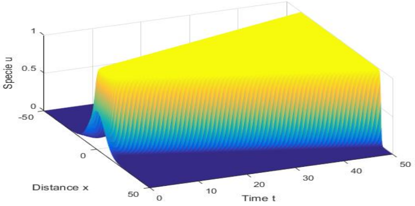


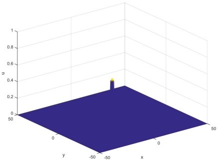


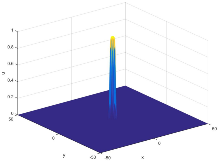
Simulations Numériques

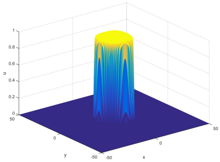
Modèle Allee : $d = 0.5, A = 0.25(k = 64), u_0 = 0.5$





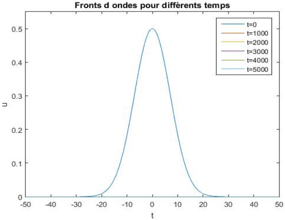


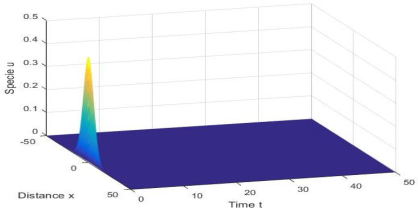


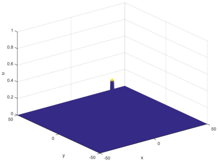


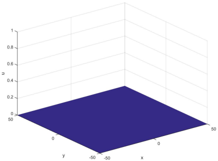
Simulations Numériques

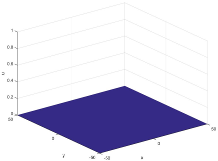
Modèle Allee : $d = 0.5, A = 0.75(k = 7.1), u_0 = 0.5$





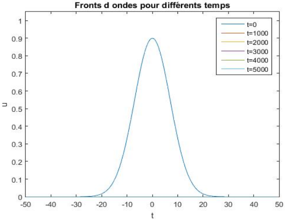


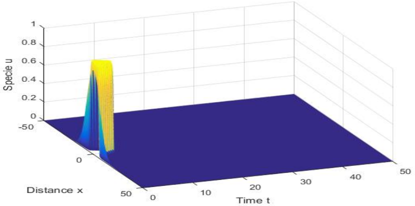


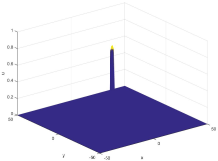


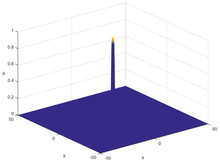
Simulations Numériques

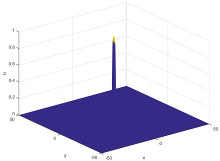
Modèle Allee : $d = 0.5, A = 0.75(k = 7.1), u_0 = 0.9$





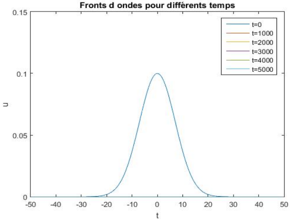


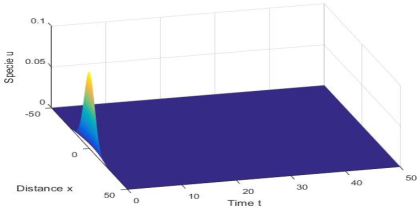


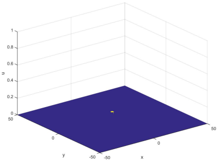


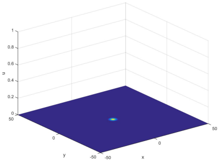
Simulations Numériques

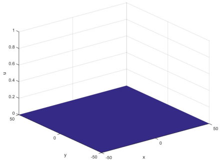
Modèle Allee : $d = 0.5, A = 0.5(k = 16), u_0 = 0.1$





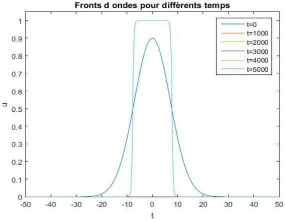


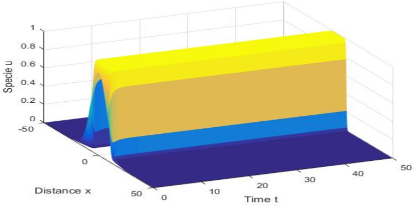


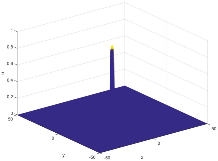


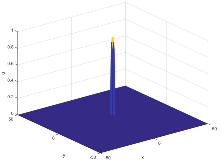
Simulations Numériques

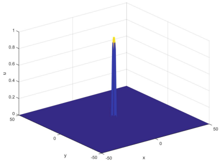
Modèle Allee : $d = 0.5$, $A = 0.5 (k = 16)$, $u_0 = 0.9$











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Système de Lolkta Volterra