

Modelling M/EEG data with Bayesian multilevel generalised additive models

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Abstract

Time-resolved electrophysiological measurements such as those offered by magneto- or electro-encephalography (M/EEG) provide a unique window onto neural activity underlying cognitive process and how they unfold over time. Typically, we are interested in testing whether such measures differ across conditions and/or groups. The conventional approach consists in conducting mass-univariate statistics through followed by some form of multiplicity correction (e.g., FDR, FWER) or cluster-based inference. However, these cluster-based methods have an important downside: they shift the focus of inference from the timepoint to the cluster level, thus preventing any conclusion to be made about the onset and offset of effects (e.g., differences across conditions). Here, we introduce a novel *model-based approach* for analysing one-dimensional M/EEG timeseries such as ERPs or decoding timecourses and their differences across conditions or group. This approach relies on Bayesian nonparametric multilevel modelling (multilevel generalised additive models or Gaussian processes), which outputs the posterior probability of the effect being different than 0 (or above chance) at every timestep, while naturally taking into account the temporal dependencies and between-subject variability present in such data.

Keywords: EEG, MEG, generalised additive models, gaussian processes, mixed-effects models, Bayesian statistics, brms

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Introduction (in progress)

Here are some useful references to be discussed (Combrisson & Jerbi, 2015; Ehinger & Dimigen, 2019; Frossard & Renaud, 2021, 2022; Gramfort, 2013; Hayasaka, 2003; Luck & Gaspelin, 2017; Maris & Oostenveld, 2007; E. J. Pedersen et al., 2019; C. R. Pernet et al., 2015; Riutort-Mayol et al., 2023; Rousselet, 2025)... See also (Maris, 2011)... and (Rosenblatt et al., 2018) (history of cluster-based approaches and using a data split?)... Cluster failure (Eklund et al., 2016)...

In the following, we consider two approaches to modelling the non-linear timecourse of M/EEG ERPs or decoding performance: i) generalised additive models (GAMs) with thin-plate smoothing splines (Wood, 2003; Wood, 2004) and ii) Gaussian processes (GPs) with a smooth covariance kernel (Rasmussen & Williams, 2005) and low-rank approximation (Riutort-Mayol et al., 2023).

Previous modelling work

From Dimigen & Ehinger (2021): “Recently, spline regression has been applied to ERPs (Hendrix, Baayen, & Bolger, 2017; Kryuchkova, Tucker, Wurm, & Baayen, 2012; Tremblay & Baayen, 2010; Tremblay & Newman, 2015)”...

Disentangling overlapping processes (Skukies et al., 2024; Skukies & Ehinger, 2021)... Using Bayes factors (Teichmann, 2022)... Weighting single trials (C. Pernet, 2022)...

See <https://www.let.rug.nl/nerbonne/teach/rema-stats-meth-seminar/presentations/Wieling-2014-GAMs.pdf> and <https://www.let.rug.nl/wieling/Statistics/GAM-EEG/lab/>, <https://www.let.rug.nl/wieling/Statistics/GAM-EEG/GAM-EEG.pdf> (Abugaber et al., 2023; Meulman et al., 2015)...

Recent example of GLM for EEG (Fischer & Ullsperger, 2013; Wüllhorst et al., 2025)... “Similar approaches have been successfully applied to EEG time- (Rousselet et al., 2008) and frequency-domain (Cohen and Cavanagh, 2011) data and allow the simultaneous investigation of multiple independent variables while preserving the high temporal resolution of the EEG.”... See also (Hauk et al., 2006; Rousselet et al., 2008)... Example of two-stage regression analysis (i.e., individual-level then group-level, Dunagan et al., 2024)...

Generalised additive models

In generalised additive models (GAMs), the functional relationship between predictors and response variable is decomposed into a sum of low-dimensional non-parametric functions. A typical GAM has the following form:

$$y_i \sim \text{EF}(\mu_i, \phi)$$

$$g(\mu_i) = A_i + \mathbf{X}_i \gamma + \sum_{j=1}^J f_j(x_{ij})$$

where $y_i \sim \text{EF}(\mu_i, \phi)$ denotes that the observations y_i are distributed as some member of the exponential family of distributions (e.g., Gaussian, Gamma, Beta, Poisson) with mean μ_i and scale parameter ϕ ; $g(\cdot)$ is the link function, A is an offset, \mathbf{X}_i is the i th row of a parametric model matrix, γ is a vector of parameters for the parametric terms, f_j is a smooth function of covariate x_j . The smooth functions f_j are represented in the model via penalised splines basis expansions of the covariates, that are a weighted sum of basis functions:

$$f_j(x_{ij}) = \sum_{k=1}^K \beta_{jk} b_{jk}(x_{ij})$$

where β_{jk} is the weight (coefficient) associated with the k th basis function $b_{jk}()$ evaluated at the covariate value x_{ij} for the j th smooth function f_j . Splines' coefficients are penalised...

Objectives

...

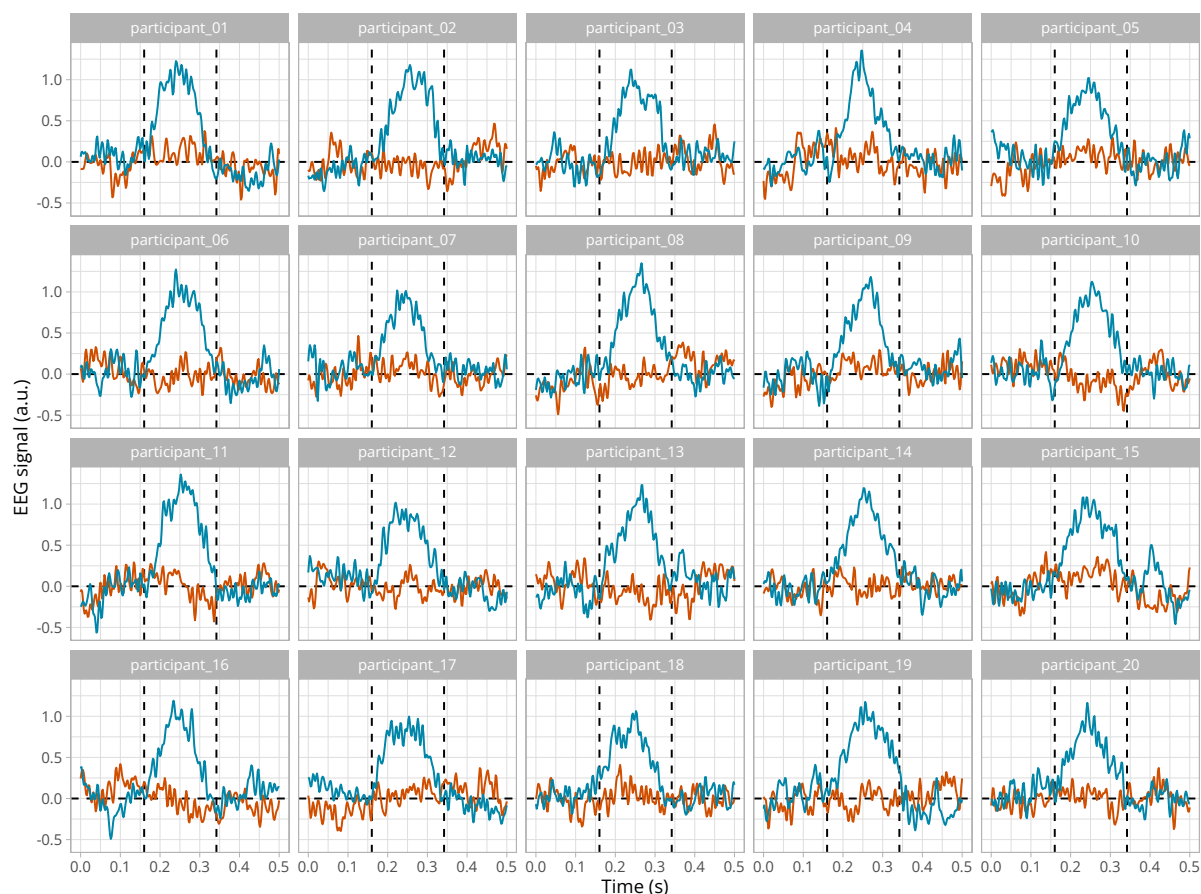
Methods

M/EEG data simulation

Following the approach used by Sassenhagen & Draschkow (2019) and Rousselet (2025), we simulated EEG data stemming from two conditions, one with noise only, and the other with noise + signal. As in previous studies, the noise was generated by superimposing 50 sinusoids at different frequencies, following an EEG-like spectrum (see details and code in Yeung et al., 2004). As in Rousselet (2025), the signal was generated from truncated Gaussian with an objective onset at 160 ms, a peak at 250 ms, and an offset at 342 ms. We simulated this signal for 250 timesteps between 0 and 0.5s, akin to a 500 Hz sampling rate. We simulated such data for a group of 20 participants with 50 trials per participant and condition (Figure 1).

Figure 1

Some ERPs in two conditions with 50 trials each, for a group of 20 participants.



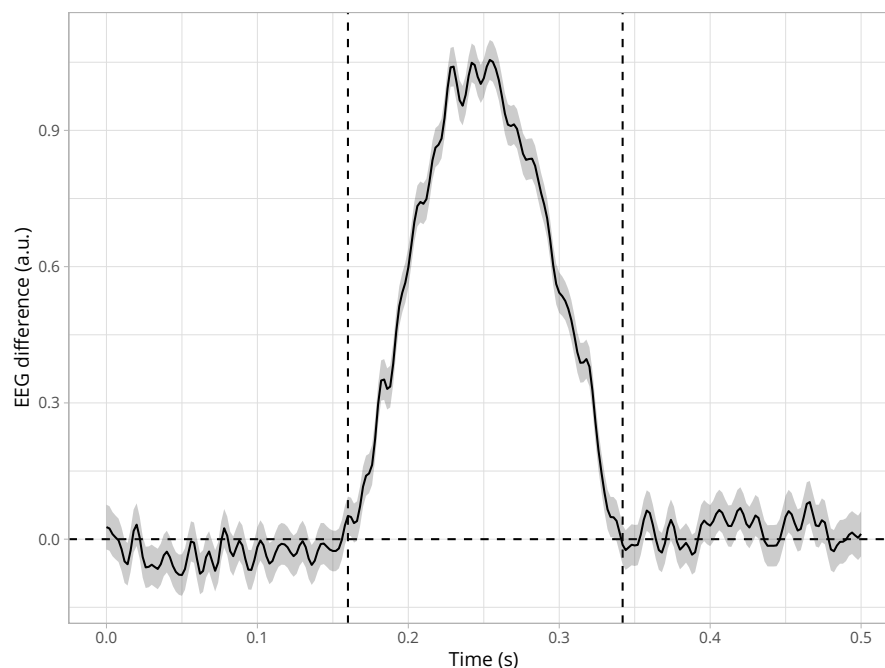
We computed the average of the ERP difference (Figure 2)...

Model fitting

We then fitted a GAM and GP regression model using the `brms` package (Bürkner, 2017, 2018; Nalborczyk et al., 2019). We used the default priors in `brms`, that is, weakly informative

Figure 2

Group-level average difference between conditions (mean \pm standard error of the mean). The ‘true’ onset and offset are indicated by the vertical dashed lines.



priors. Four Markov Chain Monte-Carlo (MCMC) were ran for each model to approximate the posterior distribution, including each 5000 iterations and a warmup of 2000 iterations. Posterior convergence was assessed examining trace plots as well as the Gelman–Rubin statisti \hat{R} .

```
# averaging across participants
ppt_df <- raw_df %>%
  group_by(participant, condition, time) %>%
  summarise(eeg = mean(eeg) ) %>%
  # mutate(eeg = as.numeric(scale(x = eeg, scale = FALSE) ) ) %>%
  ungroup()

# defining a contrast for condition
contrasts(ppt_df$condition) <- c(-0.5, 0.5)

# fitting the GAM
gam <- brm(
  # cubic regression splines with k-1 basis functions
  eeg ~ condition + s(time, bs = "cr", k = 10, by = condition),
  data = ppt_df,
  family = gaussian(),
  warmup = 2000,
  iter = 5000,
  chains = 4,
  cores = 4,
  file = "models/gam.rds"
)
```

```

# computing eeg_diff and averaging across participants
# group_df <- raw_df %>%
#   group_by(participant, time) %>%
#   pivot_wider(names_from = condition, values_from = eeg, values_fn = mean) %>%
#   mutate(eeg_diff = cond2 - cond1) %>%
#   summarise(eeg_diff = mean(eeg_diff) ) %>%
#   ungroup()

# see https://betanalpha.github.io/assets/case\_studies/gp\_part3/part3.html
# and https://betanalpha.github.io/assets/case\_studies/gaussian\_processes.html
gp_priors <- c(
  set_prior("normal(0, 1)", class = "Intercept"),
  set_prior("normal(0, 1)", class = "b"),
  set_prior("exponential(1)", class = "sigma"),
  set_prior("exponential(1)", class = "sdgp")
)

gp_model <- brm(
  # k refers to the number of basis functions for
  # computing Hilbert-space approximate GPs
  # if k = NA (default), exact GPs are computed
  # eeg ~ gp(time, by = condition),
  eeg ~ condition + gp(time, by = condition, k = 20, cov = "exp_quad"),
  data = ppt_df,
  family = gaussian(),
  # prior = gp_priors,
  control = list(adapt_delta = 0.99, max_treedepth = 15),
  backend = "cmdstanr",
  iter = 2000,
  chains = 4,
  cores = 4,
  file = "models/gp.rds"
)

```

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And we plot the posterior predictions...

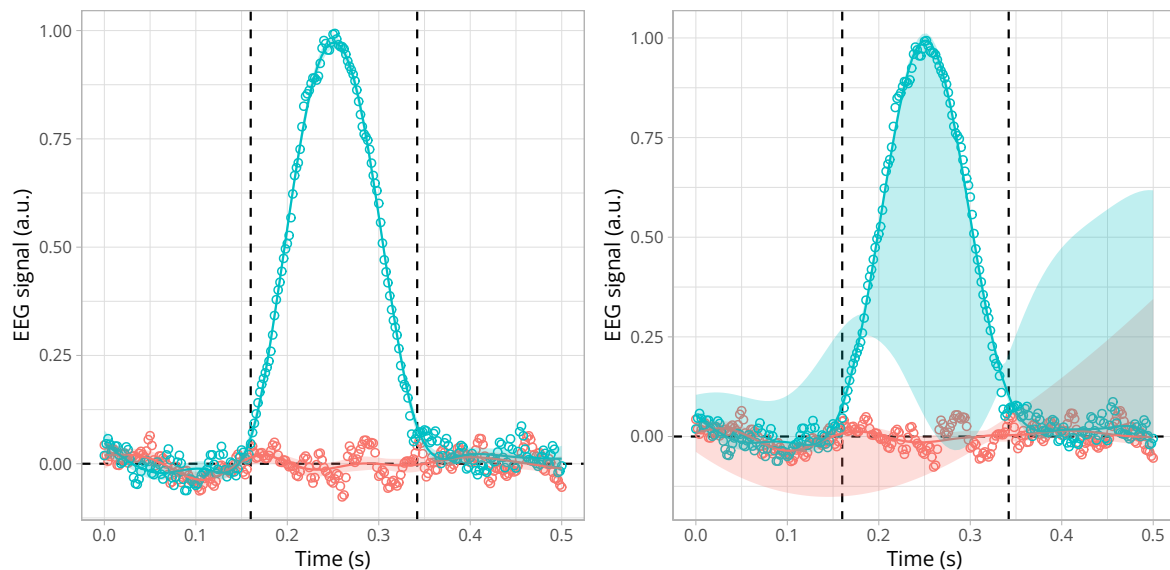
```

# plotting the posterior predictions
plot_post_preds(model = gam) + plot_post_preds(model = gp_model)

```

Figure 3

Posterior predictions of the GAM (left) and GP (right) models.

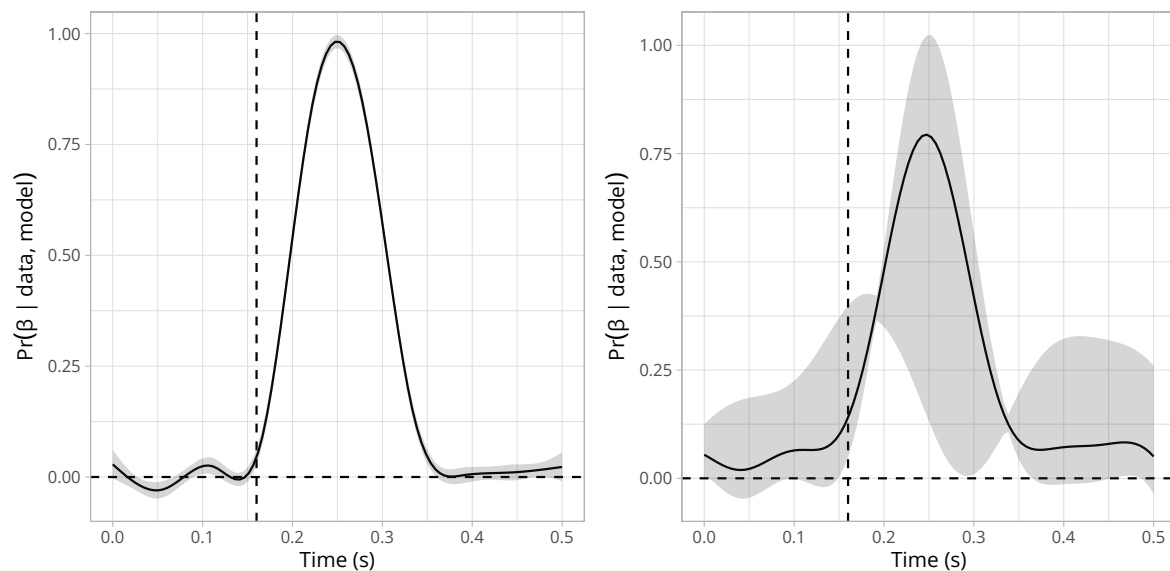


Posterior probability of difference above 0

We can retrieve the posterior probability of the slope for `condition` at each timestep (Figure 4).

Figure 4

Slope for the difference between conditions according to the GAM (left) or the GP (right).

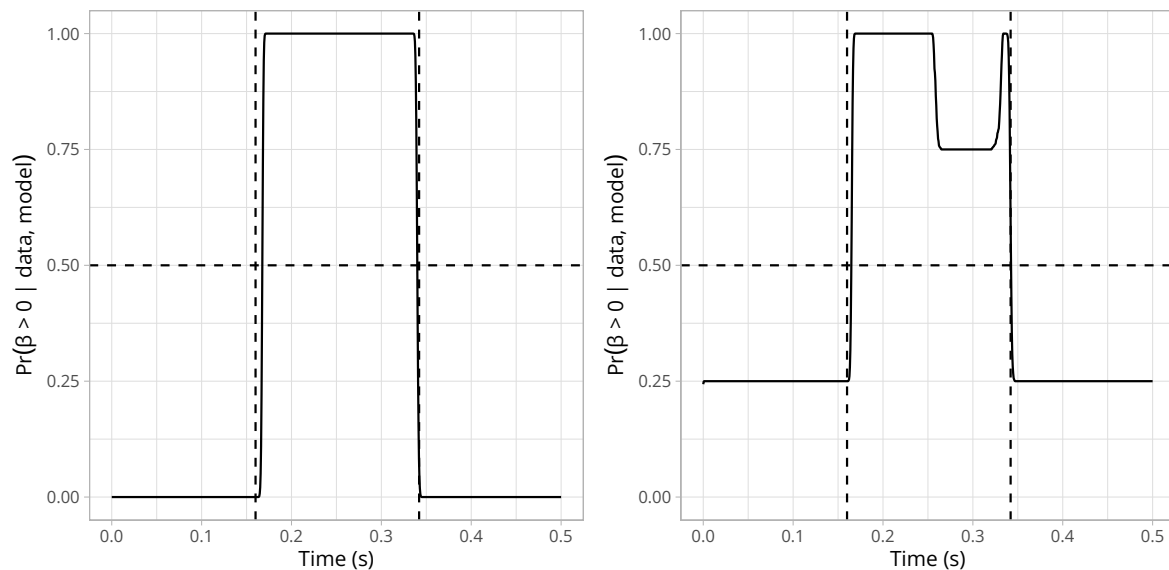


We can also compute the posterior probability of the slope for `condition` being above $0 + \epsilon$ (Figure 5), with ϵ defined as 10% of the standard deviation of the raw EEG signal.

We can also express this as the ratio of posterior probabilities (i.e., $p/(1-p)$) and visualise the timecourse of this ratio superimposed with the conventional thresholds on evidence ratios (Figure 6).

Figure 5

Posterior probability of the ERP difference (slope) being above 0 according to the GAM (left) and the GP (right).



70 Multilevel modelling using ERP summary statistics

71 Next we fit a hierarchical/multilevel GAM using summary statistics of ERPs (mean and
72 SD) at the participant level (similar to what is done in meta-analysis).

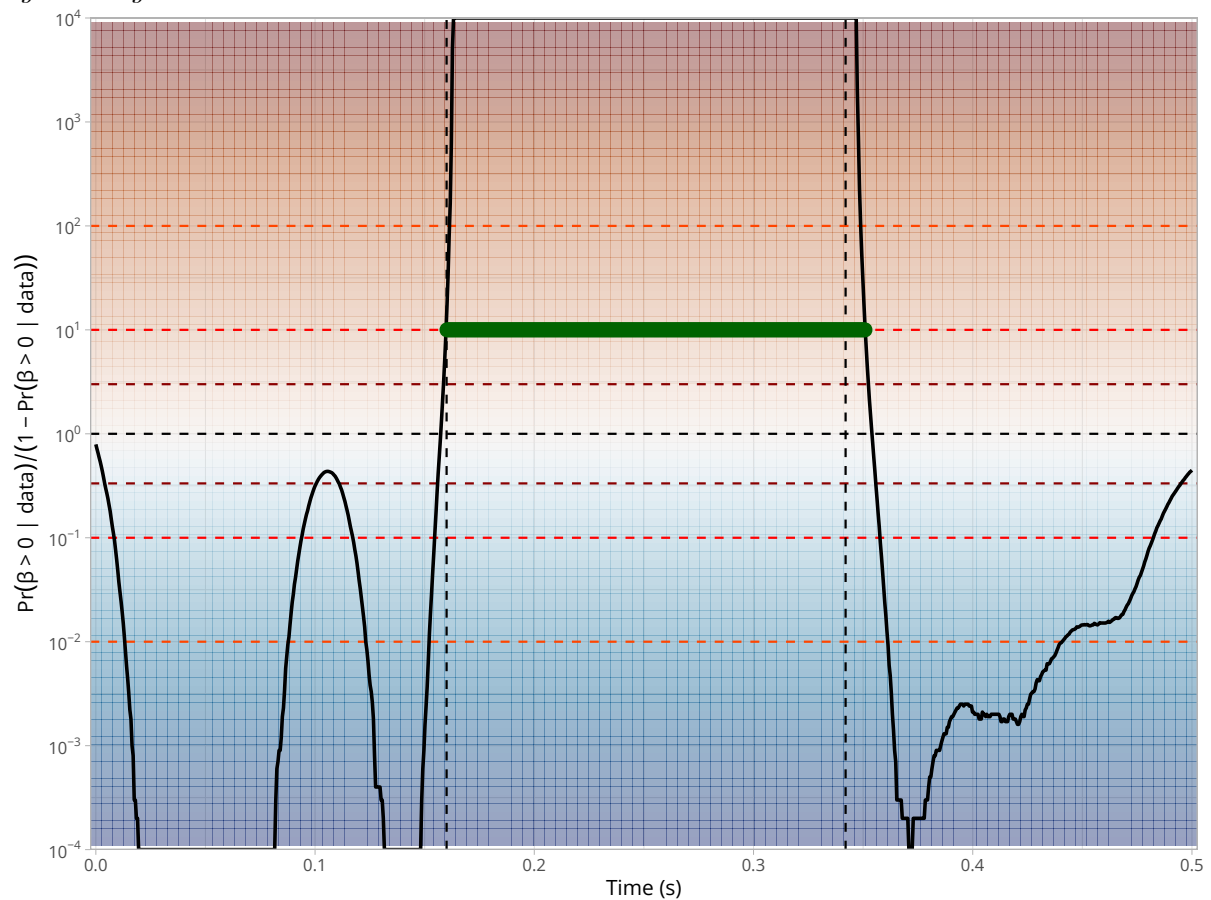
```
# averaging across participants
summary_df <- raw_df %>%
  summarise(
    eeg_mean = mean(eeg),
    eeg_sd = sd(eeg),
    .by = c(participant, condition, time)
  )

# defining a contrast for condition
contrasts(summary_df$condition) <- c(-0.5, 0.5)

# fitting the GAM
meta_gam <- brm(
  # using by-participant SD of ERPs across trials
  eeg_mean | se(eeg_sd) ~
    condition + s(time, bs = "cr", k = 10, by = condition) +
    (1 | participant),
  data = summary_df,
  family = gaussian(),
  warmup = 2000,
  iter = 5000,
  chains = 4,
  cores = 4,
  file = "models/meta_gam.rds"
)
```


Figure 6

Ratio of posterior probability according to the GAM. Timesteps above threshold (10) are highlighted in green.



```
# fitting the GP
meta_gp <- brm(
  # using by-participant SD of ERPs across trials
  eeg_mean | se(eeg_sd) ~
    condition + gp(time, k = 20, by = condition) +
    (1 | participant),
  data = summary_df,
  family = gaussian(),
  control = list(adapt_delta = 0.99),
  iter = 5000,
  chains = 4,
  cores = 4,
  file = "models/meta_gp.rds"
)
```

```
# plotting the posterior predictions
meta_gam_preds <- plot(
  conditional_effects(x = meta_gam, effect = "time:condition"),
  points = FALSE, theme = theme_light(), plot = FALSE
)[[1]] +
```

```

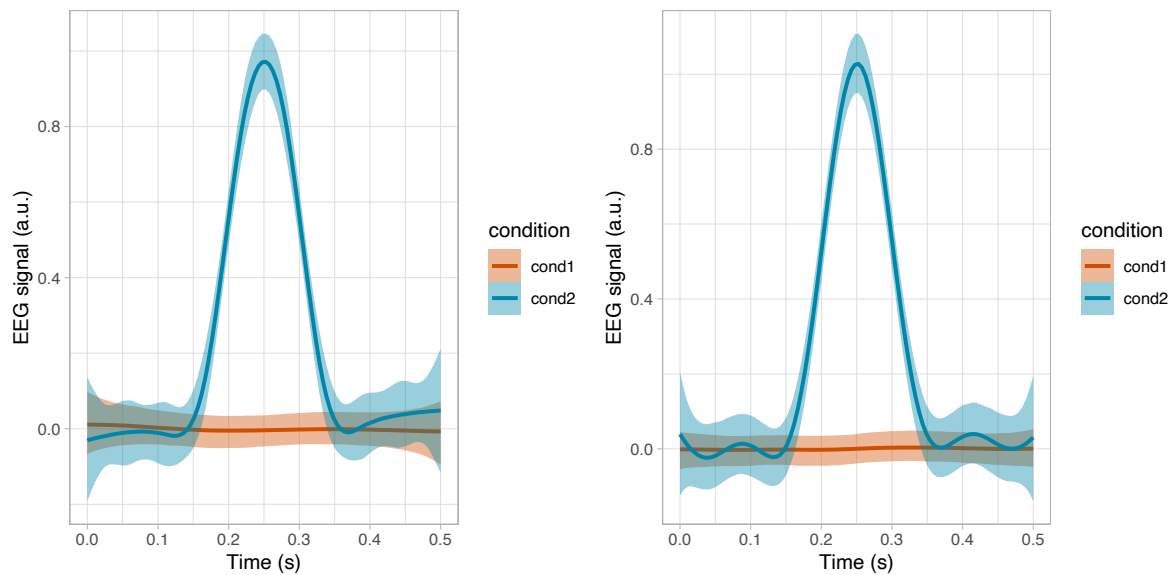
scale_colour_met_d(name = "Johnson") +
scale_fill_met_d(name = "Johnson") +
labs(x = "Time (s)", y = "EEG signal (a.u.)")
meta_gp_preds <- plot(
  conditional_effects(x = meta_gp, effect = "time:condition"),
  points = FALSE, theme = theme_light(), plot = FALSE
)[[1]] +
scale_colour_met_d(name = "Johnson") +
scale_fill_met_d(name = "Johnson") +
labs(x = "Time (s)", y = "EEG signal (a.u.)")

# combining the two plots
meta_gam_preds + meta_gp_preds

```

Figure 7

Posterior predictions for the hierarchical GAM and GP.



Error properties of the proposed approach

We then computed the difference between the true and estimated onset/offset of the ERP difference (error $:= |\hat{\theta} - \theta|$), according to various **eps** and **threshold** values. Remember that the signal is generated from a truncated Gaussian with an objective onset at 160 ms, a maximum at 250 ms, and an offset at 342 ms. Figure 8 shows that the hierarchical GAM can *exactly* recover the true onset and offset values, given some reasonable choice of **eps** and **threshold** values (e.g., a threshold of 20).

	eps	threshold	estimated_onset	estimated_offset	error_onset	error_offset
1	0.00	13	0.16	0.34	0	0.002
2	0.00	14	0.16	0.34	0	0.002
3	0.00	15	0.16	0.34	0	0.002
4	0.00	16	0.16	0.34	0	0.002
5	0.00	17	0.16	0.34	0	0.002
6	0.01	10	0.16	0.34	0	0.002

Figure 8

Error function of onset (left) and offset (right) estimation according to various **eps** and **threshold** values (according to the hierarchical GAM). Minimum error values are indicated by red crosses.



87 Application to actual M/EEG data

88 Assessing the reliability of the proposed approach (in comparison to other methods)
 89 using some sort of split-half reliability ([Rosenblatt et al., 2018](#))?

90 Comparing the identified onsets/offsets to other approaches

91 We considered five methods for multiplicity corrections: two FDR methods; two cluster-
 92 based methods; and the maximum statistics. The two FDR methods were BH95 (Benjamini &
 93 Hochberg, 1995; 10.1111/j.2517-6161.1995.tb02031.x) and BY01 (Benjamini & Yekutieli, 2001;
 94 10.1214/aos/1013699998), which were applied to the permutation p-values using the `p.adjust`
 95 function in R. The first cluster-based inference was implemented using a cluster-sum statistic of
 96 squared t-values...

97 We also compared the performance of the GAMM (in correctly identifying/estimating
 98 the onset and offset of ERP difference across conditions) to the performance of the binary
 99 segmentation method as implemented in the R package `changepoint` v 2.2.4 ([Killick et al., 2022a](#)),
 100 threshold-free cluster enhancement (TFCE, [Smith & Nichols, 2009](#)), as implemented
 101 in MNE-Python ([Gramfort, 2013](#)), and using the raw t-, p-, or s-values timecourse. S-values
 102 ([Greenland, 2019](#))...

Figure 9

Timecourse of squared t-values and s-values (continuous measure of evidence given by $-\log_2(p\text{-value})$) with true onset and onset identified using the raw (uncorrected) p-values or the corrected p-values (BH, BY, Holm).

True onset: 0.16s, Uncorrected onset: 0.172s, BH onset: 0.172s, BY onset: 0.176s, Holm onset: 0.18s

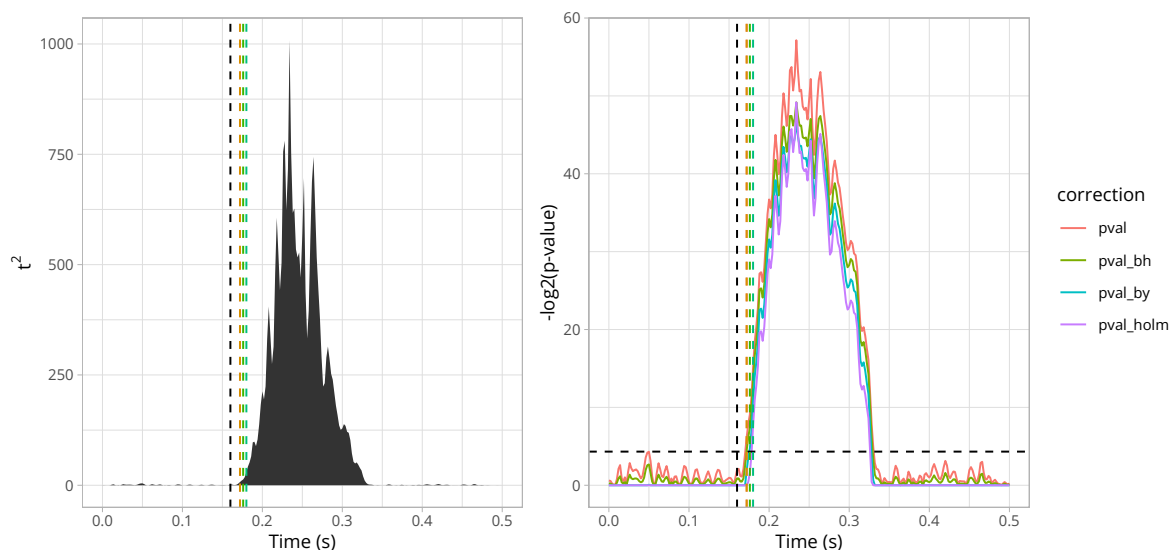
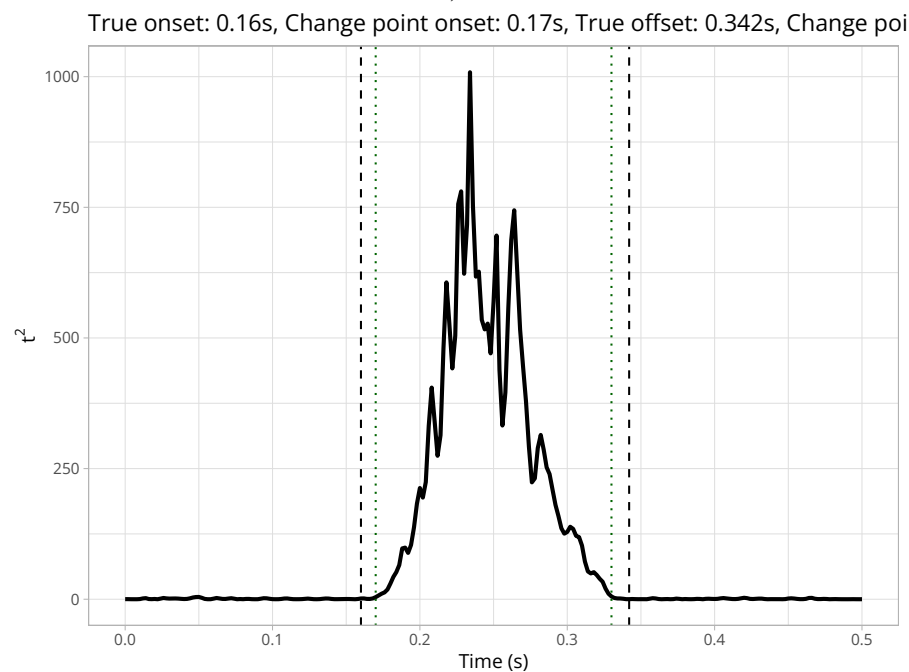


Figure 10

T-values timecourse with true onset/offset and onset/offset identified using the changepoint package (binary segmentation method, in green).



Now cluster-based permutations using MNE-Python ([Gramfort, 2013](#)) via the R package `reticulate` v 1.35.0 ([Ushey et al., 2024](#))...

```
# importing the decoding scores
p_values_df <- readRDS(file = "results/mne_permutation_decoding_scores.rds")

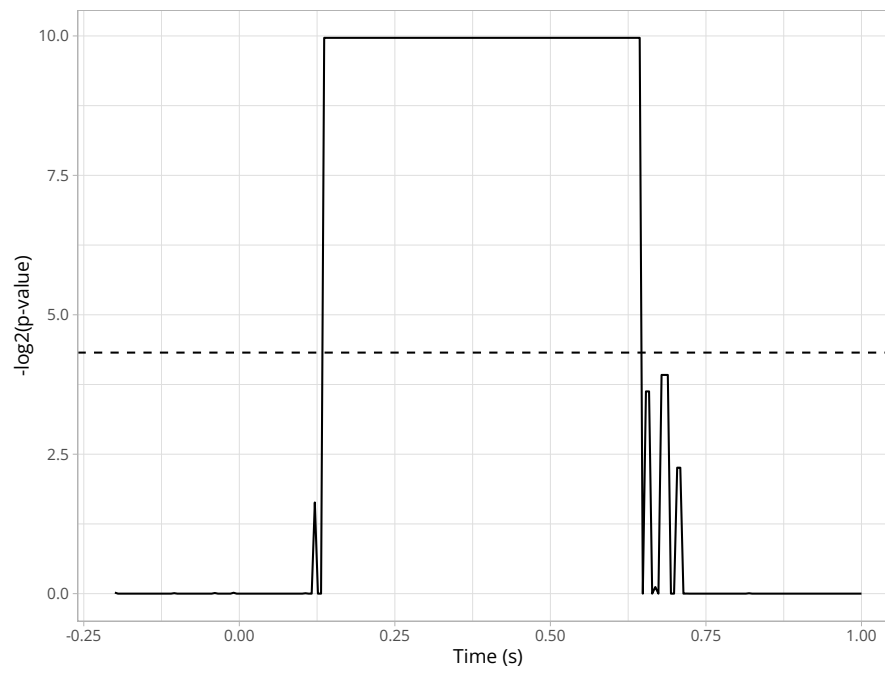
# plotting the s-values (-log2(p-values))
p_values_df %>%
  mutate(sval = -log2(pval) ) %>%
  ggplot(aes(x = time, y = sval) ) +
  geom_line(linewidth = 0.5) +
  geom_hline(yintercept = -log2(0.05), linetype = 2) +
  labs(
    x = "Time (s)",
    y = "-log2(p-value)"
  )
```

Simulation study

Onset/offset estimation methods were assessed using these summary statistics of the Monte Carlo sampling distributions of onsets: bias (median-based), mean absolute error (MAE) and variance, with 10.000 iterations (i.e., 10.000 simulated datasets)...

Figure 11

Cluster-based permutation tests via MNE-Python.



Results

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Discussion

Summary of the proposed approach

Increasing potential usage

Prepare a wrapper `R` package and show how to call it in `Python` and integrate it with `MNE-Python` ([Gramfort, 2013](#)) pipelines...

Limitations and future directions

Can be applied to any 1D timeseries (e.g., pupillometry, electromyography)... Extending the approach to spatiotemporal data (i.e., time + sensors)...

Conclusions

Packages

123

124 We used R version 4.2.3 ([R Core Team, 2023](#)) and the following R packages: brms v.
125 2.22.0 ([Bürkner, 2017, 2018, 2021](#)), changepoint v. 2.2.4 ([Killick et al., 2022b](#); [Killick & Eckley,](#)
126 [2014](#)), grateful v. 0.2.10 ([Rodriguez-Sanchez & Jackson, 2023](#)), knitr v. 1.45 ([Xie, 2014, 2015,](#)
127 [2023](#)), MetBrewer v. 0.2.0 ([Mills, 2022](#)), pakret v. 0.2.2 ([Gallou, 2024](#)), patchwork v. 1.2.0
128 ([T. L. Pedersen, 2024](#)), rmarkdown v. 2.29 ([Allaire et al., 2024](#); [Xie et al., 2018, 2020](#)), scales
129 v. 1.3.0 ([Wickham et al., 2023](#)), scico v. 1.5.0 ([T. L. Pedersen & Crameri, 2023](#)), tidybayes v.
130 3.0.6 ([Kay, 2023](#)), tidyverse v. 2.0.0 ([Wickham et al., 2019](#)).

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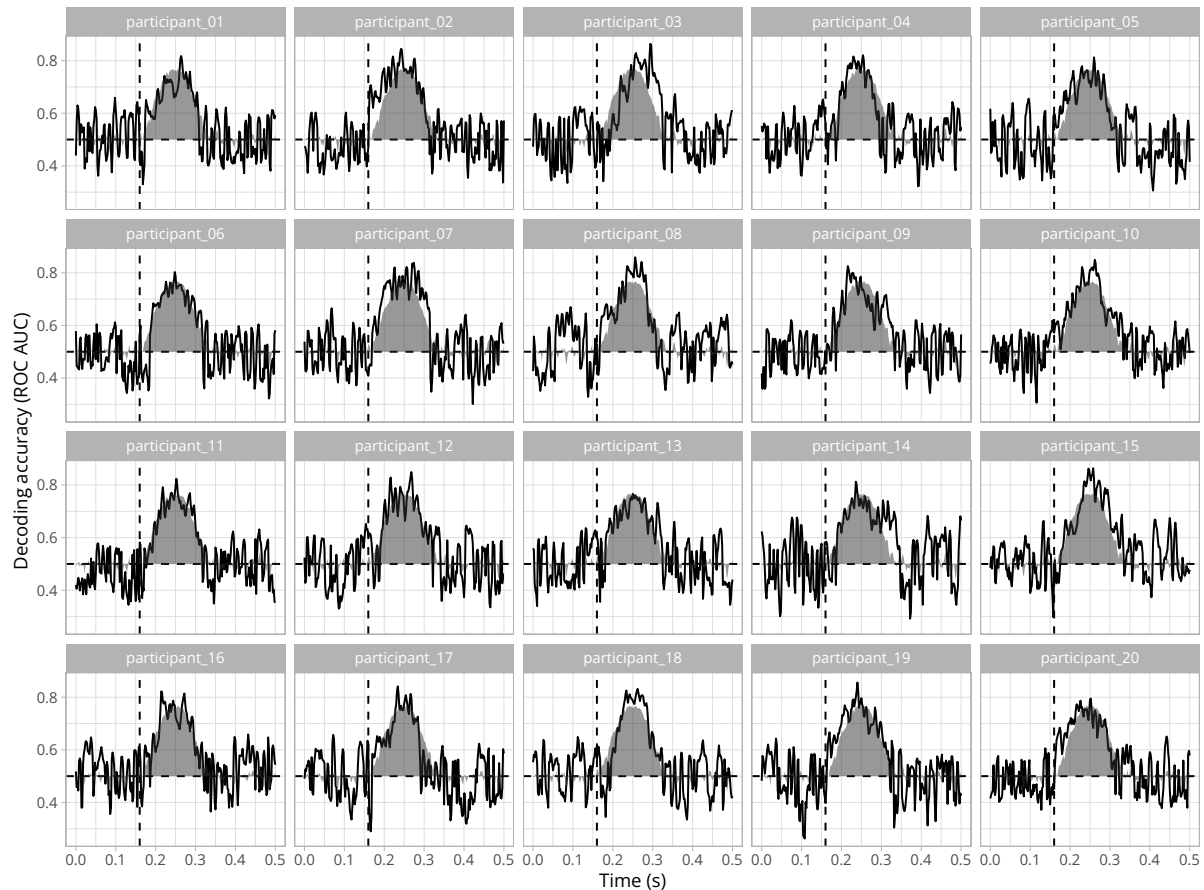
Appendix A

Application to time-resolved decoding results (accuracy over time)

We conducted time-resolved multivariate pattern analysis (MVPA), also known as decoding. As a result, we have a timecourse of decoding accuracies (e.g., ROC AUC), bounded between 0 and 1, per participant (Figure A1)...

Figure A1

Exemplary average timecourse of binary decoding accuracy (ROC AUC) for each participant. Group-level average decoding accuracy is depicted as a grey background density in each panel.



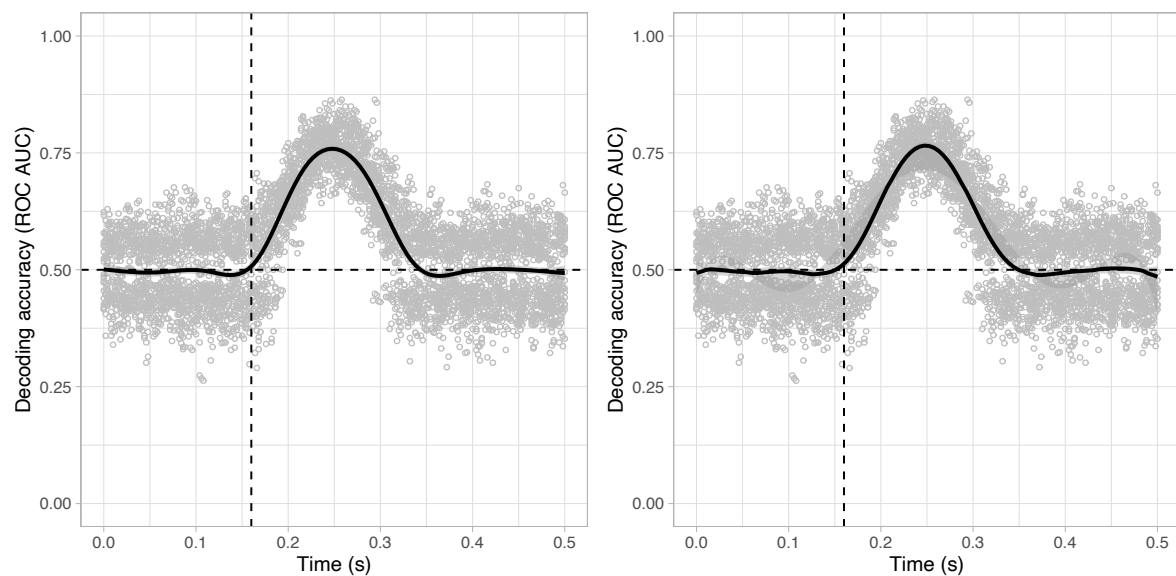
Now, we want to *test* whether the group-level average decoding accuracy is above chance (i.e., 0.5) at each timestep. We use a similar GAM/GP as previously, but we replace the Normal likelihood function by a Beta one to account for the bounded nature of AUC values (between 0 and 1).

```
# fitting the GAM
decoding_gam <- brm(
  auc ~ s(time, bs = "cr", k = 10),
  data = decoding_data,
  family = Beta(),
  iter = 5000,
  chains = 4,
  cores = 4,
  file = "models/decoding_gam.rds"
)
```

```
# fitting the GP
decoding_gp <- brm(
  auc ~ gp(time, k = 20),
  data = decoding_data,
  family = Beta(),
  control = list(adapt_delta = 0.99),
  iter = 5000,
  chains = 4,
  cores = 4,
  file = "models/decoding_gp.rds"
)
```

Figure A2

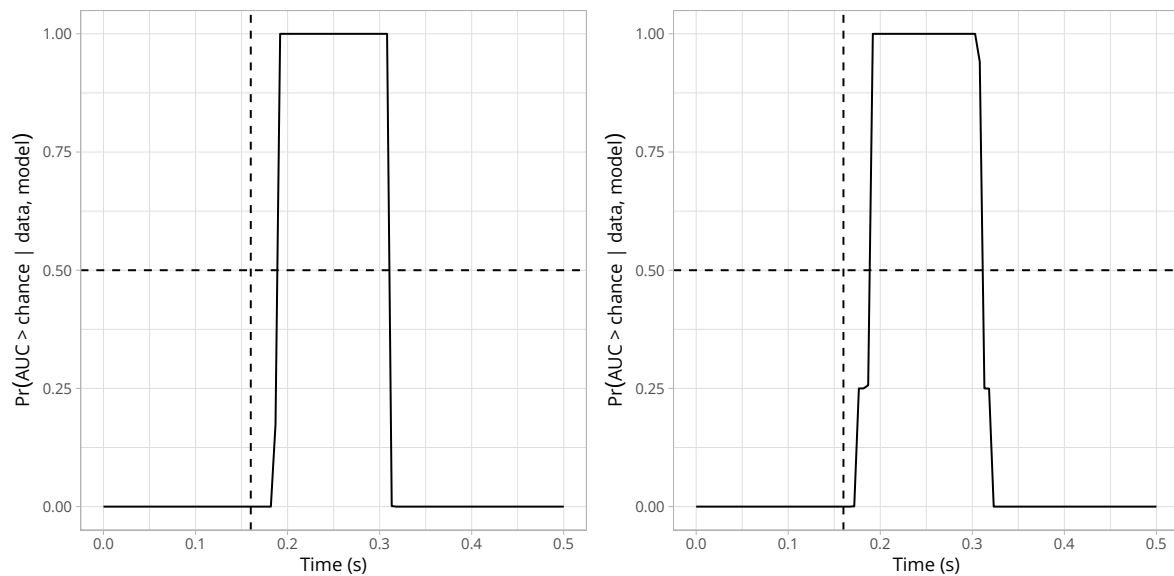
Posterior predictions of the GAM (left) and GP (right) fitted on decoding accuracy over time.



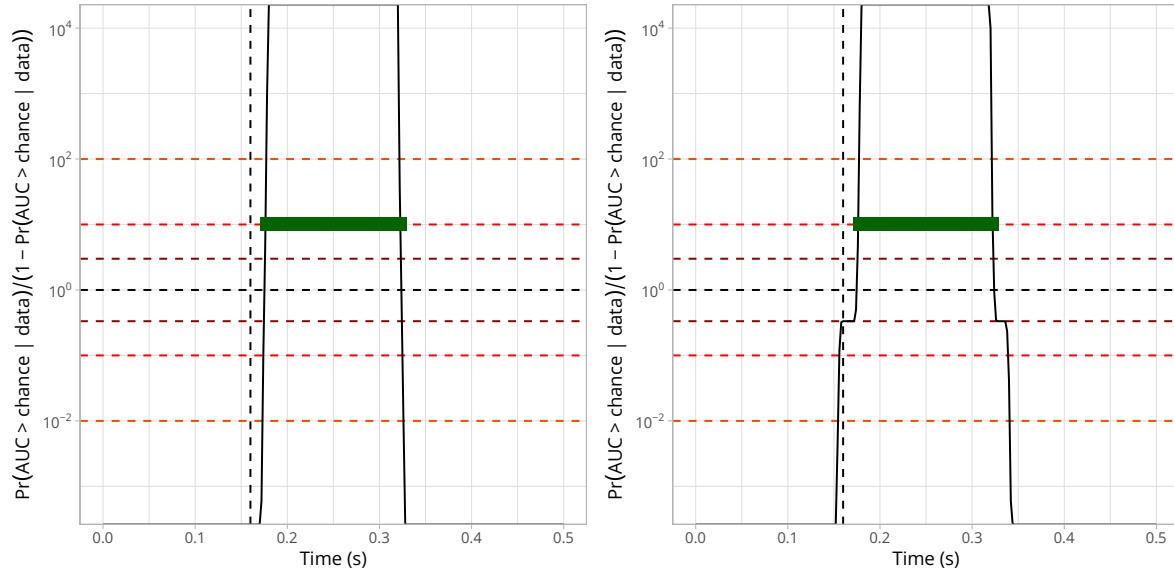
Next, we plot the posterior probability of decoding accuracy being above chance level (plus some epsilon) (Figure A3).

Figure A3

Posterior probability of decoding accuracy being above chance level according to the GAM (left) or the GP (right).

**Figure A4**

Ratio of posterior probabilities of decoding accuracy being above chance level according to the GAM (left) or the GP (right).



Appendix B

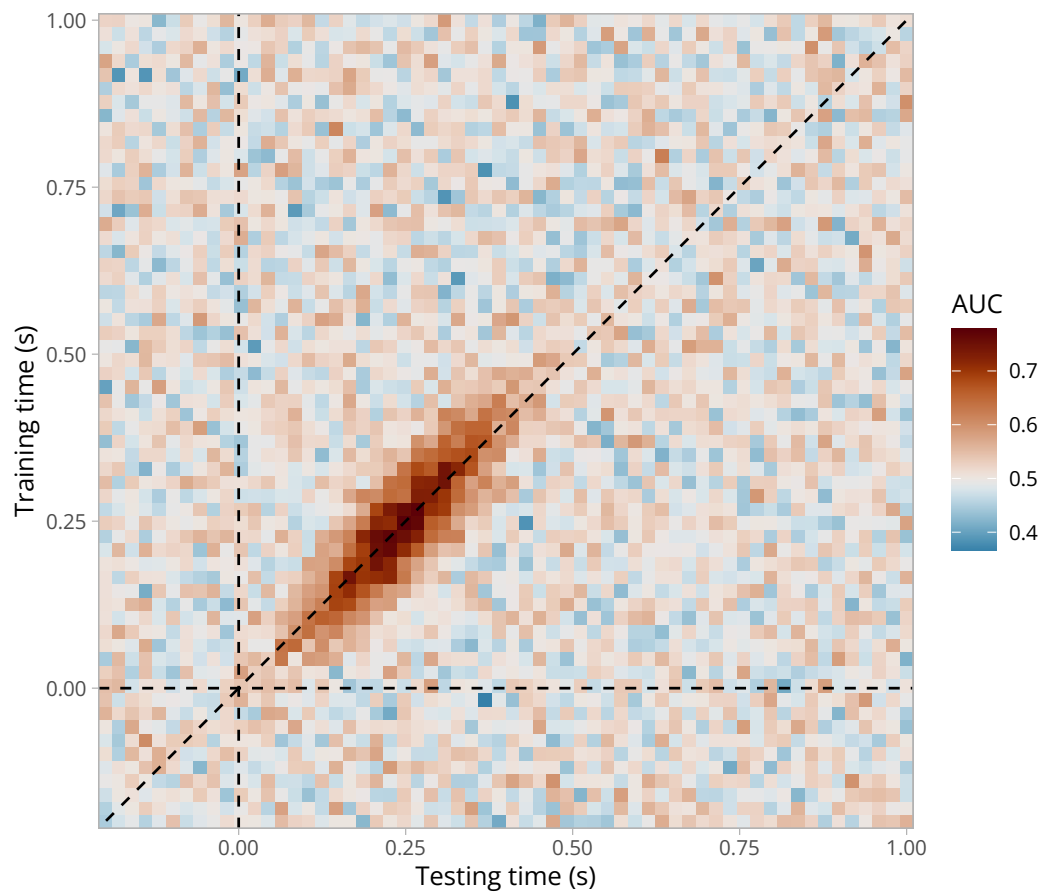
Application to 2D time-resolved decoding results (cross-temporal generalisation)

Assume we have M/EEG data and we have conducted cross-temporal generalisation analyses (King & Dehaene, 2014). As a result, we have a 2D matrix where each element contains the decoding accuracy (e.g., ROC AUC) of a classifier trained at timestep t_i and tested at timestep t_j (Figure B1).

Now, we want to test whether and when decoding performance is above chance level (0.5 for a binary decoding task). These two models are computationally heavier to fit (more

Figure B1

Exemplary (simulated) group-level average cross-temporal generalisation matrix of decoding performance (ROC AUC).



301 observations and 2D smooth functions)...

```
# fitting a GAM with two temporal dimensions
timegen_gam <- brm(
  # 2D thin-plate spline (tp)
  # auc ~ s(train_time, test_time, bs = "tp", k = 10),
  auc ~ t2(train_time, test_time, bs = "tp", k = 10),
  data = timegen_data,
  family = Beta(),
  iter = 5000,
  chains = 4,
  cores = 4,
  file = "models/timegen_gam_t2.rds"
)

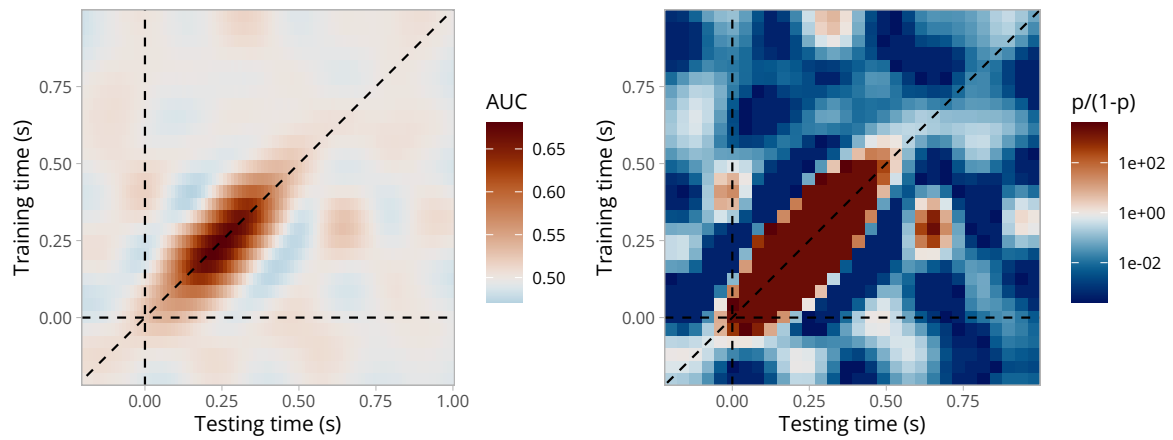
# fitting a GP with two temporal dimensions
# timegen_gp <- brm(
#   auc ~ gp(train_time, test_time, k = 20),
#   data = timegen_data,
#   family = Beta(),
#   control = list(adapt_delta = 0.95),
```



```
# iter = 2000,  
# chains = 4,  
# cores = 4,  
# file = "models/timegen_gp.rds"  
# )
```

Figure B2

Posterior probability of decoding accuracy being above chance level (2D GAM).



Appendix C

Mathematical formulation of the bivariate GAM

To model cross-temporal generalisation matrices of decoding performance (ROC AUC), we extended the initial (decoding) GAM to take into account the bivariate temporal distribution of AUC values, thus producing naturally smoothed estimates (timecourses) of AUC values and posterior probabilities. This model can be written as follows:

$$\begin{aligned} \text{AUC}_i &\sim \text{Beta}(\mu_i, \phi) \\ g(\mu_i) &= f(\text{train}_i, \text{test}_i) \end{aligned}$$

where we assume that AUC values come from a Beta distribution with two parameters μ and ϕ . We can think of $f(\text{train}_i, \text{test}_i)$ as a surface (a smooth function of two variables) that we can model using a 2-dimensional splines. Let $\mathbf{s}_i = (\text{train}_i, \text{test}_i)$ be some pair of training and testing samples, and let $\mathbf{k}_m = (\text{train}_m, \text{test}_m)$ denote the m^{th} knot in the domain of train_i and test_i . We can then express the smooth function as:

$$f(\text{train}_i, \text{test}_i) = \alpha + \sum_{m=1}^M \beta_m b_m(\tilde{s}_i, \tilde{k}_m)$$

Note that $b_m(\cdot)$ is a basis function that maps $R \times R \rightarrow R$. A popular bivariate basis function uses *thin-plate splines*, which extend to $\mathbf{s}_i \in \mathbb{R}^d$ and ∂l_g penalties. These splines are designed to interpolate and approximate smooth surfaces over two dimensions (hence the “bivariate” term). For $d = 2$ dimensions and $l = 2$ (smoothness penalty involving second order derivative):

$$f(\tilde{s}_i) = \alpha + \beta_1 x_i + \beta_2 z_i + \sum_{m=1}^M \beta_{2+m} b_m(\tilde{s}_i, \tilde{k}_m)$$

using the the radial basis function given by:

$$b_m(\tilde{s}_i, \tilde{k}_m) = \left\| \tilde{s}_i - \tilde{k}_m \right\|^2 \log \left\| \tilde{s}_i - \tilde{k}_m \right\|$$

where $\|\mathbf{s}_i - \mathbf{k}_m\|$ is the Euclidean distance between the covariate \mathbf{s}_i and the knot location \mathbf{k}_m .

Appendix D

Threshold-free cluster enhancement

Cluster-based permutation approaches require defining a cluster-forming threshold (e.g., a t - or f -value) as the initial step of the algorithm. As different cluster-forming thresholds lead to clusters with different spatial or temporal extent, this threshold modulates the sensitivity of the subsequent permutation test. The threshold-free cluster enhancement method (TFCE) was introduced by Smith & Nichols (2009) to overcome this arbitrary threshold.

In brief, the TFCE method works as follows. Instead of picking an arbitrary cluster-forming threshold (e.g., $t = 2$), we try all (or many) possible thresholds in a given range and check whether a given timestep/voxel belongs to a significant cluster under any of the set of thresholds... Then, instead of using cluster mass, we use a weighted average between the cluster extend (e , how broad is the cluster, that is, how many connected samples it contains) and the cluster height (h , how high is the cluster, that is, how large is the test statistic) according to the formula:

$$\text{TFCE} = \int_h e(h)^E h^H dh$$

Where... the parameters E and H are set a priori and control the influence of the extend and height on the TFCE. Then, p -value for timestep/voxel i is computed by comparing it TFCE with the null distribution of TFCE values. For each permuted signal, we keep the maximal value over the whole signal for the null distribution of the TFCE.... But see Sassenhagen & Draschkow (2019)...

Appendix E**Using the R package and integration with MNE-Python**

336 Explain how to use the R package and to integrate it with MNE epochs...

```
# to-do adding some code here...
```