Binary Shifts

Leading to Division & Multiplication

Examples 1& 2 -Right Shifts (Division)

| 128 | 64 | 32 | 16 | 8 | 4 | 2 | 1 | | | Shift | Denary | Effect |
|-----|--------------------------------------|------------|----|-----------------------|-----------------------|----------------|----|---|---|-------|--------|----------------------------|
| 27 | 2 ⁶ | 2 5 | 24 | 2 ³ | 2 ² | 2 ¹ | 20 | | | | | |
| 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | | | N/A | 144 | |
| | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | | 1 | 72 | Division by 21 |
| | 1 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 2 | 36 | Division by 2 ² |
| | 1 1 1 1 1 1 1 1 | | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 3 | 18 | Division by 2 ³ |

| 128 | 64 | 32 | 16 | 8 | 4 | 2 | 1 | | | | Shift - no of places | Denary | Effect |
|-----|----------------|-----------------------|----|-----------------------|-----------------------|----------------|------------|---|---|--------------------------------------|----------------------|--------|----------------------------|
| 27 | 2 ⁶ | 2 ⁵ | 24 | 2 ³ | 2 ² | 2 ¹ | 2 º | | | | | | |
| 0 | | 1 | | | | 0 | | | | | N/A | 40 | |
| | 0 | 0 | 1 | 0 | ! ! | 0 | | 0 | | 1 | 1 | 20 | Division by 21 |
| | | 0 | 0 | 1 | 0 | 1 | 0 | 0 | 0 | | 2 | | Division by 2 ² |
| | | | 0 | 0 | 1 | 0 | 1 | 0 | 0 | 1 1 1 1 1 1 1 1 | 3 | : | Division by 2 ³ |

Examples 3 & 4 - Right Shift with bits dropping off

| 128 | 64 | 32 | 16 | 8 | 4 | 2 | 1 | | Shift - no of | Denar | Effect |
|-----|------------|----|----|---|---|----------------|------------|----------|------------------|-------|--------|
| 27 | 2 6 | | 24 | | | 2 ¹ | 2 º | | | | |
| 1 | 0 | | 1 | 0 | 0 | 0 | 1 | | N/A | 145 | |
| | 1 | 0 | 0 | 1 | 0 | 0 | 0 | <u>1</u> | 1 | 72 | |

| 128 | 64 | 32 | 16 | 8 | 4 | 2 | 1 | | | Shift - no of places | Den | Effect |
|-----------------------|----|------------|----|-----------------------|-----------------------|----|----|----------|-----|----------------------|-----|--------|
| 2 ⁷ | 26 | 2 5 | 24 | 2 ³ | 2 ² | 21 | 20 | | | | | |
| 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | | | N/A | | |
| | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | | 1 | 6 | |
| | | | 0 | | 0 | | 1 | 0 | i i | 2 | 3 | |
| | | | 0 | 0 | 0 | 0 | 1 | <u>1</u> | 0 | 3 | 1 | |

Exercises on Right Shift (Division)

| 128 | 64 | 32 | 16 | 8 | 4 | 2 | 1 | Shift - no of places | Denary | Effect |
|-----|-----------------------|----|----|---|---|---|------------|----------------------|--------|--------|
| | 2 ⁶ | | | | | | 2 0 | | | |
| 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | N/A | | |
| | | | | | | | | 1 | | |
| | | | | | | | | 2 | | |
| | | | | | | | | 3 | | |

| 128 | 64 | 32 | 16 | 8 | 4 | 2 | 1 | | Shift - no of places | Denary | Effect |
|-----|------------|--------------|----|-----------------------|---|----------|----|---|----------------------|--------|--------|
| 27 | 2 6 | - | | 2 ³ | | - | 20 | | | | |
| 0 | 0 | i | 0 | | 1 | 1 | 0 | | N/A | | |
| | | | | | | | | | 1 | | |
| | | | | | | | | ; | 2 | | |
| | | | | | | | | | 3 | | |

Examples 5 & 6 -Left Shifts for Multiplication

| 128 | 64 | 32 | 16 | 8 | 4 | 2 | 1 | | Shift - no of places | Denary | Effect |
|-----|-----------------------|------------|----|-----------------------|-----------------------|----------------|----|--|----------------------|--------|----------------------|
| 27 | 2 ⁶ | 2 5 | 24 | 2 ³ | 2 ² | 2 ¹ | 20 | | | | |
| 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | | N/A | 6 | |
| 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | | 1 | 12 | Multiplication by 21 |
| 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | | | 24 | Multiplication by 22 |
| 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | | 3 | 48 | Multiplication by 23 |

| 128 | 64 | 32 | 16 | 8 | 4 | 2 | 1 | | Shift - no of places | Denary | Effect |
|-----|----|------------|----|------------|------------|----------------|----|--|----------------------|--------|----------------------|
| 27 | 26 | 2 5 | 24 | 2 ³ | 2 2 | 2 ¹ | 20 | | | | |
| 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | | N/A | 6 | |
| 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | | 1 | 12 | Multiplication by 21 |
| 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | | 2 | 24 | Multiplication by 22 |
| 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | | 3 | 48 | Multiplication by 23 |

Examples 7& 8- Left Shifts with Overflow

| | 128 | 64 | 32 | 16 | 8 | 4 | 2 | 1 | Shift - no of places | Denary | Effect |
|---|----------------|----------------|------------|-----------------------|-----------------------|-----------------------|----------------|----------------|----------------------|--------|--------|
| | 2 ⁷ | 2 ⁶ | 2 5 | 2 ⁴ | 2 ³ | 2 ² | 2 ¹ | 2 ⁰ | | | |
| | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | N/A | 134 | |
| 1 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 1 | 12 | |

| | 128 | 64 | 32 | 16 | 8 | 4 | 2 | 1 | Shift - no of places | Denary | Effect |
|---|-----|----|----|-------------|-----------------------|---|-------------|---|----------------------|--------|--------|
| | | | | | 2 ³ | | | | | | |
| | 1 | 1 | 0 | Ο | 0 | 1 | 1 | 0 | N/A | 198 | |
| 1 | | | | ! ! ! | 1 | | ! ! ! | 0 | 1 | 140 | |

Exercises for Left Shifts for Multiplication

| 128 | 64 | 32 | 16 | 8 | 4 | 2 | 1 | | Shift - no of places | Denary | Effect |
|-----|-----------------------|----|-------------|--------|--------|--------|--------|---------------------------------------|----------------------|--------|--------|
| | 2 ⁶ | | ! ! ! | ! ! | ! ! | ! ! | ! ! | 1 1 1 1 1 1 1 1 | | | |
| 0 | 0 | 0 | 0 | 1 | 1 | 1 | 0 | ; ; ; ; ; ; ; | N/A | 14 | |
| | | | | | | | | , , , , , , , , , , , , , , , , , , , | 1 | | |
| | | | | | | | | | 2 | | |
| | | | | | | | | | 3 | | |

| 128 | 64 | 32 | 16 | 8 | 4 | 2 | 1 | Shift - no of places | Denary | Effect |
|-----------------------|----|----|-------------|-------------|-----------------------|---|-------------|----------------------|--------|--------|
| 2 ⁷ | | | | | 2 ² | | | | | |
| 1 | | | ! ! ! | ! ! ! | 0 | | ! ! ! | N/A | 160 | |
| | | | | | | | | 1 | | |

Exercises and Answers on Right Shift (Division)

| 128 | 64 | 32 | 16 | 8 | 4 | 2 | 1 | | | Shift - no of places | Denary | Effect |
|-----|-----------------------|------------|----|-----------------------|-----------------------|----------------|----|--------------------------------------|--|----------------------|--------|----------------------------|
| 27 | 2 ⁶ | 2 5 | 24 | 2 ³ | 2 ² | 2 ¹ | 20 | | | | | |
| 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | | | N/A | 24 | |
| 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 1 1 1 1 1 1 1 1 | | 1 | 12 | Division by 21 |
| 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | | | 2 | 6 | Division by 2 ² |
| 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | | | 3 | 3 | Division by 2 ³ |

| 128 | 64 | 32 | 16 | 8 | 4 | 2 | 1 | | Shift - no of places | Denary | Effect |
|-----|------------|------------|----|-----------------------|-----------------------|----------------|------------|---|----------------------|--------|----------------------------|
| 27 | 2 6 | 2 5 | 24 | 2 ³ | 2 ² | 2 ¹ | 2 º | | | | |
| 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | | N/A | 12 | |
| 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | | 1 | 6 | Division by 21 |
| 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | | 2 | 3 | Division by 2 ² |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 3 | 1 | Losing a bit |

Exercises and Answers for Left Shifts for Multiplication

| 128 | 64 | 32 | 16 | 8 | 4 | 2 | 1 | | Shift | Denary | Effect |
|-----|------------|-----------------------|----|-----------------------|-----------------------|----------------|----|--|----------------------------|--------|----------------------------------|
| 27 | 2 6 | 2 ⁵ | 24 | 2 ³ | 2 ² | 2 ¹ | 20 | | ; ; ; ; ; ; | | |
| 0 | 0 | 0 | 0 | 1 | 1 | 1 | 0 | | N/A | 14 | |
| 0 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | | 1 | 28 | Multiplication by 21 |
| 0 | 0 | 1 | 1 | 1 | 0 | 0 | 0 | | 2 | 56 | Multiplication by 22 |
| 0 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | | 3 | 120 | Multiplication by 2 ³ |

| | 128 | 64 | 32 | 16 | 8 | 4 | 2 | 1 | | Shift - no of places | Denary | Effect |
|---|-----|----|------------|----|-----------------------|-----------------------|----------------|----|--|----------------------|--------|--------------|
| | 27 | 26 | 2 5 | 24 | 2 ³ | 2 ² | 2 ¹ | 20 | | | | |
| | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | | N/A | 160 | |
| 1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | | 1 | | Overflow bit |