Numerical Problem Solving using The NAG Library from Excel



Program

Overview of the NAG Library

Quick Demonstration

Some Worked Examples

Practical



The NAG Library

Can be thought of as:

- □ Single code base
- Multiple interfaces

Interfaces:

- Fortran
- □ .NET (C#)
- □ MATLAB®
- Statistical Add-ins for Excel

(NAG Fortran Library)

(NAG C Library)

(NAG .NET Library)

(NAG Toolbox for MATLAB)



Show Installation Directory



What Do You Get?

- Where is it?C:\Program Files (x86)\NAG\FL25\fldll254ml
- A number of DLLs and lots of Fortran stuff
- Some Excel examples samples\excel_examples\
- VB6 headers vb6_headers\
- Documentation (possibly)
- Full documentation and additional examples from:
 - □ www.nag.co.uk



What Can I Do With it? – A Demo

Fitting a Variance Gamma distribution to data

PDF has 4 parameters (c, σ , θ and ν) and is given by:

$$f(x) = \frac{2\exp(\theta(x-c)/\sigma^{2})}{v^{1/\nu}\Gamma(1/\nu)\sigma\sqrt{2\pi}} \left(\frac{|x-c|}{\sqrt{2\sigma^{2}/\nu + \theta^{2}}}\right)^{1/\nu - 1/2} K_{1/\nu + 1/2} \left(\frac{|x-c|\sqrt{2\sigma^{2}/\nu + \theta^{2}}}{\sigma^{2}}\right)$$

Moments:

$$E(X) = \mu = c + \theta$$

$$E((X - \mu)^{2}) = \sigma^{2} + \theta^{2} \nu$$

$$E((X - \mu)^{3}) = 2\theta^{3} \nu^{2} + 3\sigma^{2} \theta \nu$$

$$E((X - \mu)^{4}) = 3\sigma^{4} \nu + 12\sigma^{2} \theta^{2} \nu^{2} + 6\theta^{4} \nu^{3} + 3\sigma^{4} + 6\sigma^{2} \theta^{2} \nu + 3\theta^{4} \nu^{2}$$



Show Demo



NAG Library Contents

- C05: Root Finding
- C06: Summation of Series
- D01: Quadrature
- D02: ODEs
- D03: PDEs
- D04: Numerical Differentiation
- D05: Integral Equations
- E01: Interpolation
- E02: Curve and Surface Fitting
- **■** E04: Local Optimization
- E05: Global Optimization
- F: Linear Algebra

- G01: Statistical Functions
- G02: Correlation / Regression
- G03: Multivariate Methods
- G05: RNGs
- G07: Univariate Estimation
- G08: Nonparametric Statistics
- G10: Smoothing in Statistics
- G12: Survival Analysis
- G13: Time Series Analysis
- H: Operations Research
- S: Special Functions
 - Option pricing



Show Documentation



NAG Documentation

- Organised in chapters, by functionality
 - Strange, but structured, naming
- Each chapter has an introduction
 - Overview of the problems
 - Suggested routines, often with a flow chart
- Each routine has an individual document
 - □ Routine prototype
 - Description and references
 - Description of arguments
 - Description of possible error exits



Programming for Excel

VBA

- Visual Basic for Applications
- Comes as part of Excel
- No compiler is required
- □ Was going to become deprecated but maybe not now

COM

Usually C based, requires compiler

VSTO

- Relatively new
- □ .NET based, requires compiler



Show Example 1

log Gamma function $ln(\Gamma(x))$



Example 1: VBA – part 1

- VBA accessed via Developers Tab
 - □ Turned on in File -> Excel Options -> Customize Ribbon

- May need to alter security settings to allow macros to run
 - File -> Trust Center -> Trust Center Settings -> Macro Settings



Example 1: VBA – part 2

- Option Base 1
 - Not required
- Option Explicit
 - Doesn't always warn, especially if variable is an array
- Third party libraries accessed via Declare statement
 - □ Declare Function < name > lib < location > < prototype >
 - □ Declare Sub <name> lib <location> <prototype>
- Rename third party routines via "alias"
 - Declare Sub <new name> lib <location> alias <old name>



Example 1: NAG

- Declarations are supplied for all NAG routines
 - □ Use VB6 declarations
- Error handling via IFAIL
 - □ On entry: Three possible values, 0, -1 or 1.
 - ☐ IFAIL = 0 (noisy, hard return). **Don't use**, will close Excel.
 - □ IFAIL = -1 (noisy, soft return). Uses a (non-Excel) pop up window.
 - □ IFAIL = 1 (quiet, soft return). Recommended
 - □ On exit:
 - □ IFAIL = 0 means everything is OK
 - □ IFAIL <> 0 is either a warning or error
 - Returned value is a numeric code which can be looked up
 - □ Good practice to test for non-zero values



Show Example 2

Summary Statistics



Example 2: VBA

Array Functions

- Allow a function to return more than one value
- Dynamic
- Usually return a 2D variant array
 - □ Can return a 1D variant array, but will be a row vector
 - □ Can be an array of a different type (i.e. double), but then can't be used to return error messages etc
- Expanded using Shift+Ctrl and Return
- Extra space is filled with #N/A
- □ Access individual elements of array via functions like
 INDEX, i.e. "= index(myFun(),4,1)" returns element (4,1)
 - □ Note: Multiple uses of index causes myFun to run multiple times



Example 2: NAG

- All arguments are passed by reference
- Must supply the first element of an array, rather than the array itself, so:

```
call G01AAF(N, X(1), ...)
rather than
CALL G01AAF(N,X, ...)
```

Same applies to 2D arrays:

```
CALL G02AAF(G(1,1), ...)
```

2D arrays are stored in column major order



Show Example 3

Modified Bessel Function

$$K_{\nu}(x)$$



Example 3: VBA

Types can be defined using:

```
Type Complex

Real_Part as Double

Complex_Part as Double

End Type
```

Types can be accessed using:

```
Dim z as Complex
z.Real_Part = 0.0
z.Complex Part = 1.0
```



Example 3: NAG

 Any user defined types required by a NAG routine are supplied in the declaration file

- Routines with character (or string) arguments have a "hidden" argument:
 - corresponds to the length of the character argument
 - will not appear in the documentation
 - does appear in the VB declaration
 - string arguments and their lengths are one of the few passed by value



Show Example 4

System of Non-Linear Equations

$$(3-2x_1)x_1 - 2x_2 = -1$$

$$-x_{i-1} + (3-2x_i)x_i - 2x_{i+1} = -1 \quad i = 2,3,...,8$$

$$-x_8 + (3-2x_9)x_9 = -1$$



Example 4: VBA

- RtlMoveMemory can be used to copy memory
 - □ RtlMoveMemory(to,from,amount)
 - □ in kernel32 DLL
 - comes with windows
- AddressOf can be used to access the address of a function or subroutine
- Len function can be used to obtain the size of a type Dim y(10) as double, x(10) as double, size_double as long size_double = Len(x(1)) Call RtlMoveMemory(x(1), y(1), n*size_double)



Example 4: NAG

- User callable functions (or subroutines) must be passed to NAG routines using AddressOf
- IUSER and RUSER can be used to pass information
- In User callable routines:
 - Arrays in the routine argument list are pointers (long's)
 - Data must be copied out of and in to these arrays using RtlMoveMemory
 - Most NAG examples alias RtlMoveMemory to
 CopyMemFromPtr and CopyMemToPtr. Which have different ByVal / ByRef pattern.
- Declaration file has prototype for callable functions



Where Can I Get Additional Help?

Examples supplied with library

- NAG website
 - http://www.nag.co.uk/numeric/nagandexcel.asp
- Mail support
 - mailto:support@nag.co.uk



Practical

A copy of the course material is available at: https://github.com/nagdevelopment/ExcelTraining

